EE-559 – Deep learning1b. PyTorch Tensors

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PyTorch's tensors

A tensor is a generalized matrix, a finite table of numerical values indexed along several discrete dimensions.

- A 1d tensor is a vector (e.g. a sound sample),
- A 2d tensor is a matrix (e.g. a grayscale image),
- A 3d tensor is a vector of identically sized matrices (e.g. a multi-channel image),
- A 4d tensor is a matrix of identically sized matrices (e.g. a sequence of multi-channel images),
- etc.

Tensors are used to encode the signal to process, but also the internal states and parameters of the "neural networks".

Manipulating data through this constrained structure allows to use CPUs and GPUs at peak performance.

Compounded data structures can represent more diverse data types.

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PyTorch is a Python library built on top of torch's THNN computational backend.

Its main features are:

- Efficient tensor operations on CPU/GPU,
- automatic on-the-fly differentiation (autograd),
- · optimizers,
- data I/O.

"Efficient tensor operations" encompass both standard linear algebra and, as we will see later, deep-learning specific operations (convolution, pooling, etc.)

A key specificity of PyTorch is the central role of autograd: tensor operations are specified dynamically as python operations. We will come back to this.

```
>>> from torch import Tensor
>>> x = Tensor(5)
>>> x.size()
torch.Size([5])
>>> x.fill_(1.125)
1.1250
1.1250
1.1250
1.1250
1.1250
[torch.FloatTensor of size 5]
>>> x.sum()
5.625
>>> x.mean()
1.125
>>> x.std()
0.0
```

The default tensor type torch. Tensor is an alias for torch. FloatTensor, but there are others with greater/lesser precision and on CPU/GPU.

It can be set to a different type with torch.set_default_tensor_type

In-place operations are suffixed with an underscore.

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torch. Tensor.narrow creates a new tensor which is a sub-part of an existing tensor, by constraining one of the indexes.

```
>>> a = Tensor(4, 5).zero_()
>>> a

0 0 0 0 0 0
0 0 0 0 0
0 0 0 0 0
0 0 0 0 0
[torch.FloatTensor of size 4x5]
>>> a.narrow(1, 2, 2).fill_(1.0)

1 1
1 1
1 1
1 1
[torch.FloatTensor of size 4x2]
>>> a

0 0 1 1 0
0 0 1 1 0
0 0 1 1 0
[torch.FloatTensor of size 4x5]
```

PyTorch provides interfacing to standard linear operations, such as linear system solving or Eigen-decomposition.

```
>>> y = Tensor(3).normal_()
>>> y
-1.6978
-0.6911
-1.1713
[torch.FloatTensor of size 3]
>>> m = Tensor(3, 3).normal_()
>>> q, _ = torch.gels(y, m)
>>> torch.mm(m, q)
-1.6978
-0.6911
-1.1713
[torch.FloatTensor of size 3x1]
```

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Example: linear regression

Given a list of points

$$(x_n, y_n) \in \mathbb{R} \times \mathbb{R}, \ n = 1, \dots, N,$$

can we find the "best line"

$$f(x; a, b) = ax + b$$

going "through the points", e.g. minimizing the mean square error

$$\underset{a,b}{\operatorname{argmin}} \frac{1}{N} \sum_{n=1}^{N} \left(\underbrace{ax_n + b}_{f(x_n;a,b)} - y_n \right)^2.$$

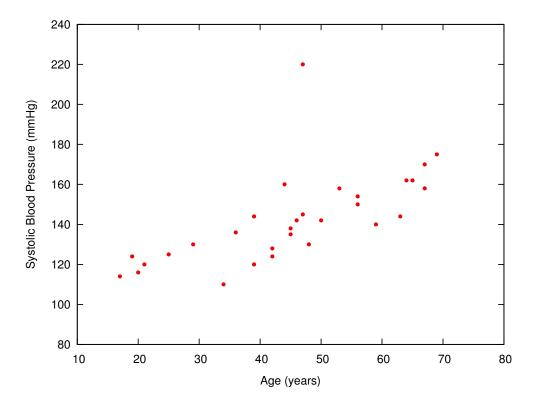
Such a model would allow to predict the y associated to a new x, simply by calculating f(x; a, b).

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```
bash> cat systolic-blood-pressure-vs-age.dat
39 144
47 220
45 138
    145
65 162
46 142
67 170
42 124
67
    158
56
    154
64
    162
56 150
    140
34
    110
42
    128
48
    130
45
    135
17
    114
20 116
    124
    142
39 120
21 120
44 160
53 158
63 144
29
    130
25
    125
```



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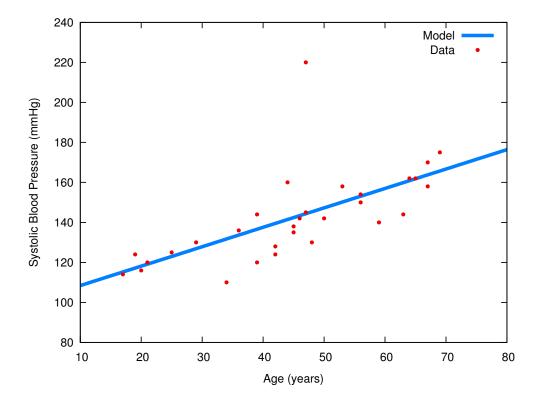
$$\begin{pmatrix}
x_1 & y_1 \\
x_2 & y_2 \\
\vdots & \vdots \\
x_N & y_N
\end{pmatrix}$$

$$\frac{\begin{pmatrix}
x_1 & 1.0 \\
x_2 & 1.0 \\
\vdots & \vdots \\
x_N & 1.0
\end{pmatrix}}{\sum_{\alpha \in \mathbb{R}^{2 \times 1}}} \simeq \begin{pmatrix}
y_1 \\
y_2 \\
\vdots \\
y_N
\end{pmatrix}$$

$$\frac{d}{data \in \mathbb{R}^{N \times 2}} \simeq \underbrace{\begin{pmatrix}
y_1 \\
y_2 \\
\vdots \\
y_N
\end{pmatrix}}_{y \in \mathbb{R}^{N \times 1}}$$

```
import torch, numpy
data = torch.from_numpy(numpy.loadtxt('systolic-blood-pressure-vs-age.dat')).float()
nb = data.size(0)

x, y = torch.Tensor(nb, 2), torch.Tensor(nb, 1)
x[:,0] = data[:,0]
x[:,1] = 1
y[:,0] = data[:,1]
alpha, _ = torch.gels(y, x)
a, b = alpha[0,0], alpha[1, 0]
```



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Manipulating high-dimension signals

Data type	CPU tensor	GPU tensor
32-bit float	torch.FloatTensor	torch.cuda.FloatTensor
64-bit float	torch.DoubleTensor	torch.cuda.DoubleTensor
8-bit int (unsigned)	torch.ByteTensor	${\tt torch.cuda.ByteTensor}$
64-bit int (signed)	torch.LongTensor	torch.cuda.LongTensor

```
>>> x = torch.LongTensor(12)
>>> type(x)
<class 'torch.LongTensor'>
>>> x = x.float()
>>> type(x)
<class 'torch.FloatTensor'>
>>> x = x.cuda()
>>> type(x)
<class 'torch.cuda.FloatTensor'>
```

Tensors of the torch.cuda types are physically in the GPU memory, and operations on them are done by the GPU. We will come back to that later.

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The default tensor type can be set with torch.set_default_tensor_type and used through torch.Tensor

```
>>> x = torch.Tensor()
>>> x
[torch.FloatTensor with no dimension]
>>> torch.set_default_tensor_type('torch.LongTensor')
>>> x = torch.Tensor()
>>> x
[torch.LongTensor with no dimension]
```

For concision we often start our code with from torch import Tensor and use Tensor in place of torch. Tensor.

Also, the new operator of a tensor allows to create one of same type

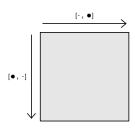
```
>>> y = torch.ByteTensor(10)
>>> u = y.new(3).fill_(123)
>>> u

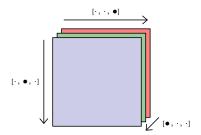
123
123
123
[torch.ByteTensor of size 3]
```

This is key to writing functions able to handle all the tensor types.

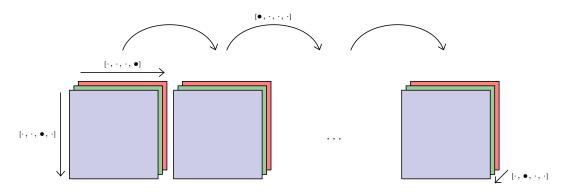
2d tensor (e.g. grayscale image)

3d tensor (e.g. rgb image)





4d tensor (e.g. sequence of rgb images)



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Here are some examples from the vast library of tensor operations:

Creation

- torch.Tensor()
- torch.Tensor(size)
- torch.Tensor(sequence)
- torch.eye(n)
- torch.from_numpy(ndarray)

Indexing, Slicing, Joining, Mutating

- torch.Tensor.view(*args)
- torch.Tensor.expand(*sizes)
- torch.cat(inputs, dimension=0)
- torch.chunk(tensor, chunks, dim=0)[source]
- torch.index_select(input, dim, index, out=None)
- torch.t(input, out=None)
- torch.transpose(input, dim0, dim1, out=None)

Filling

- Tensor.fill_(value)
- torch.bernoulli(input, out=None)
- torch.normal()

Pointwise math

- torch.abs(input, out=None)
- torch.add()
- torch.cos(input, out=None)
- torch.sigmoid(input, out=None)
- (+ many operators)

Math reduction

- torch.dist(input, other, p=2, out=None)
- torch.mean()
- torch.norm()
- torch.std()
- torch.sum()

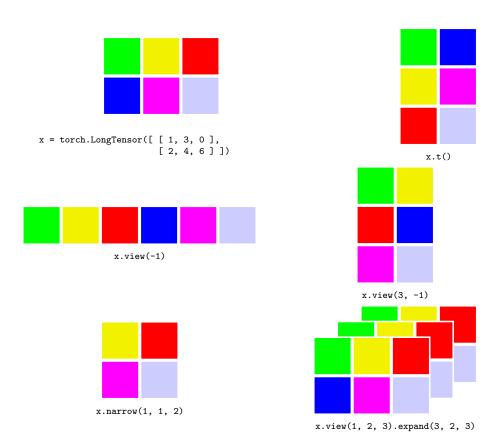
BLAS and LAPACK Operations

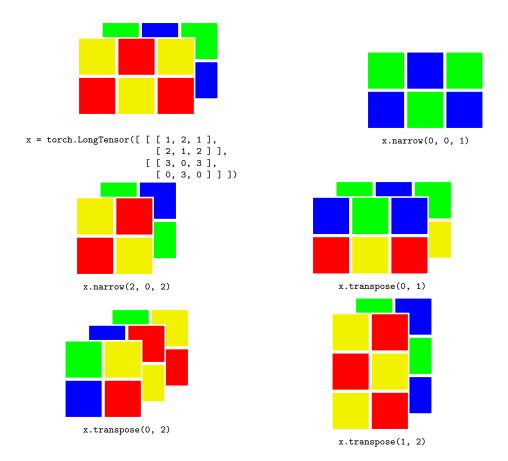
- torch.eig(a, eigenvectors=False, out=None)
- torch.gels(B, A, out=None)
- torch.inverse(input, out=None)
- torch.mm(mat1, mat2, out=None)
- torch.mv(mat, vec, out=None)

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PyTorch offers simple interfaces to standard image data-bases.

```
import torch
import torchvision

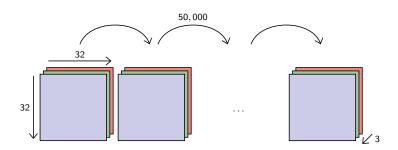
# Get the CIFAR10 train images, download if necessary
cifar = torchvision.datasets.CIFAR10('./data/cifar10/', train=True, download=True)

# Converts the numpy tensor into a PyTorch one
x = torch.from_numpy(cifar.train_data).transpose(1, 3).transpose(2, 3)

# Prints out some info
print(str(type(x)), x.size(), x.min(), x.max())
```

prints

Files already downloaded and verified <class 'torch.ByteTensor'> torch.Size([50000, 3, 32, 32]) 0 255



- # Narrow to the first images, make the tensor Float, and move the # values in [-1, 1] x = x.narrow(0, 0, 48).float().div(255)
- # Save these samples as a single image
 torchvision.utils.save_image(x, 'images-cifar-4x12.png', nrow = 12)



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Switch the row and column indexes
x.transpose_(2, 3)

torchvision.utils.save_image(x, 'images-cifar-4x12-rotated.png', nrow = 12)



Kill the green (1) and blue (2) channels
x.narrow(1, 1, 2).fill_(-1)

torchvision.utils.save_image(x, 'images-cifar-4x12-rotated-and-red.png', nrow = 12)



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Broadcasting

Broadcasting automagically expands dimensions of size 1 by replicating coefficients, when it is necessary to perform operations.

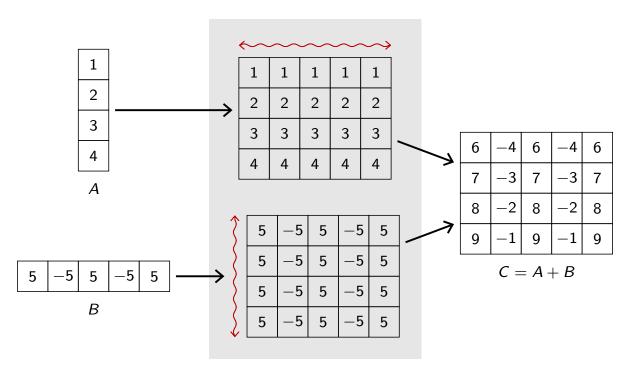
```
>>> A = Tensor([[1], [2], [3], [4]])
>>> A
1
2
3
[torch.FloatTensor of size 4x1]
>>> B = Tensor([[5, -5, 5, -5, 5]])
>>> B
5 -5 5 -5 5
[torch.FloatTensor of size 1x5]
>>> C = A + B
>>> C
6 -4 6 -4 6
7 -3 7 -3 7
8 -2 8 -2 8
9 -1 9 -1 9
[torch.FloatTensor of size 4x5]
```

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```
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```

```
A = Tensor([[1], [2], [3], [4]])
B = Tensor([[5, -5, 5, -5, 5]])
C = A + B
```



Broadcasted

Precisely, broadcasting proceeds as follows:

- 1. If one of the tensors has fewer dimensions than the other, it is reshaped by adding as many dimensions of size 1 as necessary in the front; then
- 2. for every mismatch if one of the two sizes is one, the tensor is expanded along this axis by replicating coefficients.

If there is a tensor size mismatch for one of the dimension and neither of them is one, the operation fails.

```
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```

```
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```

Tensor internals

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A tensor is a view of a storage, which is a low-level 1d vector.

```
>>> q = Tensor(2, 4).zero_()
>>> q.storage()
0.0
 0.0
 0.0
 0.0
 0.0
 0.0
 0.0
0.0
[torch.FloatStorage of size 8]
>>> s = q.storage()
>>> s[4] = 1.0
>>> s
0.0
 0.0
 0.0
 0.0
 1.0
 0.0
0.0
0.0
[torch.FloatStorage of size 8]
>>> q
0 0 0 0
1 0 0 0
[torch.FloatTensor of size 2x4]
```

Multiple tensors can share the same storage. It happens when using operations such as view(), expand() or transpose().

```
>>> r = q.view(2, 2, 2)
>>> r
(0,.,.) =
 0 0
(1 ,.,.) =
 1 0
0 0
[{\tt torch.FloatTensor\ of\ size\ 2x2x2}]
>>> r[1, 1, 0] = 1.0
>>> q
0 0 0 0
 1 0 1 0
[torch.FloatTensor of size 2x4]
>>> r.narrow(0, 1, 1).fill_(3.0)
(0 ,.,.) = 3 3 3 3
[torch.FloatTensor of size 1x2x2]
>>> q
 0 0 0 0
 3 3 3 3
[torch.FloatTensor of size 2x4]
```

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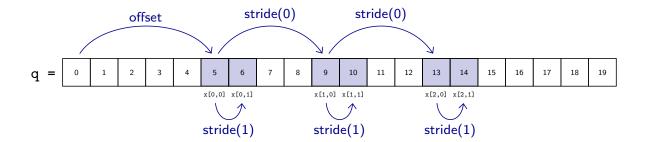
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The first coefficient of a tensor is the one at storage_offset() in storage(). To increment index k by 1, you have to move by stride(k) elements in the storage.

```
>>> q = torch.arange(0, 20).storage()
>>> x = torch.Tensor().set_(q, storage_offset = 5, size = (3, 2), stride = (4, 1))
>>> x

5     6
9     10
13     14
[torch.FloatTensor of size 3x2]
```



We can explicitly create different "views" of the same storage

```
>>> n = torch.linspace(1, 4, 4)
>>> n

1
2
3
4
[torch.FloatTensor of size 4]
>>> Tensor().set_(n.storage(), 1, (3, 3), (0, 1))

2  3  4
2  3  4
2  3  4
[torch.FloatTensor of size 3x3]
>>> Tensor().set_(n.storage(), 1, (2, 4), (1, 0))

2  2  2  2
3  3  3  3
[torch.FloatTensor of size 2x4]
```

This is in particular how transpositions and broadcasting are implemented.

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This organization explains the following (maybe surprising) error

t() creates a tensor that shares the storage with the original tensor. It cannot be "flattened" into a 1d contiguous view without a memory copy.

Practical session:

https://fleuret.org/dlc/dlc-practical-1.pdf

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