Table Driven Parsing algorithm

Lecture 8

Predictive Parsing

Assume that the grammar is LL(1)

Backtracking will never be needed

Always know which right hand side to choose (with one look-ahead)

- No Left Recursion
- Grammar is Left-Factored.

Step 1: From grammar, construct table.
Step 2: Use table to parse strings.

Predictive Parsing

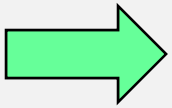
Assume that the grammar is LL(1)

Backtracking will never be needed

Always know which right hand side to choose (with one look-ahead)

- No Left Recursion
- Grammar is Left-Factored.

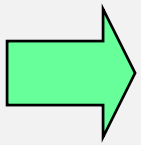
$$
\begin{aligned}
E &= E + T \mid T \\
T &= T * F \mid F \\
F &= (E) \mid \mathrm{id}
\end{aligned}
$$



$$
\begin{aligned}
E &\rightarrow T\ E' \\
E' &\rightarrow +\ T\ E' \mid \varepsilon. \\
T &\rightarrow F\ T' \\
T' &\rightarrow *\ F\ T' \mid \varepsilon. \\
F &\rightarrow (E) \mid \mathrm{id}
\end{aligned}
$$

Example of FIRST

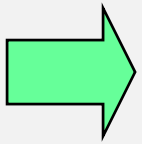
$E \rightarrow T\ E'$
$E' \rightarrow +\ T\ E' \mid \varepsilon$
$T \rightarrow F\ E'$
$T' \rightarrow *\ F\ T' \mid \varepsilon$
$F \rightarrow (\ E\ ) \mid id$



$A \rightarrow \alpha$	FIRST(α)
$E \rightarrow T\ E'$	(id
$E' \rightarrow +\ T\ E'$	+
$E_R \rightarrow \varepsilon$	ε
$T \rightarrow F\ T'$	(id
$T' \rightarrow *\ F\ T'$	*
$T' \rightarrow \varepsilon$	ε
$F \rightarrow (\ E\ )$	(
$F \rightarrow id$	id

Example of FOLLOW

$E \rightarrow T\ E'$
$E' \rightarrow +\ T\ E' \mid \varepsilon$
$T \rightarrow F\ E'$
$T' \rightarrow *\ F\ T' \mid \varepsilon$
$F \rightarrow (\ E\ ) \mid id$



$A \rightarrow \alpha$	FIRST(α)	FOLLOW(A)
$E \rightarrow T\ E'$	(id	$)
$E' \rightarrow +\ T\ E'$	+	$)
$E_R \rightarrow \varepsilon$	ε	
$T \rightarrow F\ T'$	(id	+ $)
$T' \rightarrow *\ F\ T'$	*	+ $)
$T' \rightarrow \varepsilon$	ε	
$F \rightarrow (\ E\ )$	(	* + $)
$F \rightarrow id$	id	

Pre-computed Parsing Table

For each production X → α
– for each terminal t in First(α): put α in Table[X,t]
– if ε is in First(α) then:
for each terminal t in Follow(X): put α in Table[X,t]

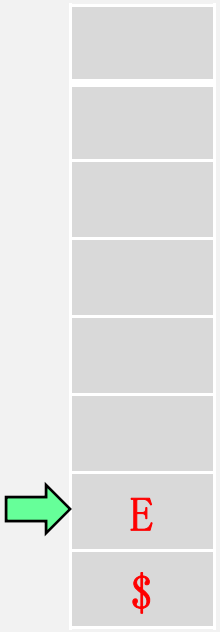
Non terminals	Input Symbols					
	id	+	*	(	)	$
E	$E \to TE'$			$E \to TE'$		
E'		$E' \to +TE'$			$E' \to \varepsilon$	$E' \to \varepsilon$
T	$T \to FT'$			$T \to FT'$		
T'		$T' \to \varepsilon$	$T' \to *FT'$		$T' \to \varepsilon$	$T' \to \varepsilon$
F	$F \to \mathrm{id}$			$F \to (E)$		

Predictive Parsing Program

(id*id)+id

Output

$$
\begin{aligned}
E &\rightarrow T\ E' \\
E' &\rightarrow +\ T\ E' \mid \varepsilon \\
T &\rightarrow F\ E' \\
T' &\rightarrow *\ F\ T' \mid \varepsilon \\
F &\rightarrow (\ E\ ) \mid \mathrm{id}
\end{aligned}
$$



(	id	*	id	)	+	id	$

Add $ to end of input
Push $
Push E

	id	+	*	(	)	$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \varepsilon$	$E' \rightarrow \varepsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \varepsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \varepsilon$	$T' \rightarrow \varepsilon$
F	$F \rightarrow \mathrm{id}$			$F \rightarrow (E)$		

Predictive Parsing Progra

(id*id)+id

Output

$$
\begin{aligned}
E &\rightarrow T\ E' \\
E' &\rightarrow +\ T\ E' \mid \varepsilon \\
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\end{aligned}
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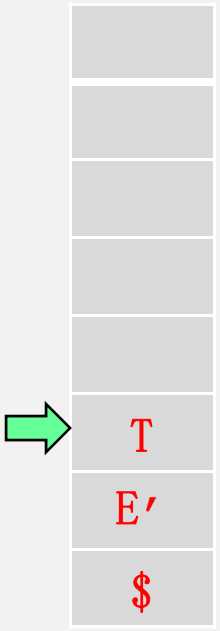


(	id	*	id	)	+	id	$

Look at Table [E, '(']
Use rule E→TE'
Pop E
Push E'
Push T
Print E→TE'

	id	+	*	(	)	$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \varepsilon$	$E' \rightarrow \varepsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \varepsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \varepsilon$	$T' \rightarrow \varepsilon$
F	$F \rightarrow \mathrm{id}$			$F \rightarrow (E)$		

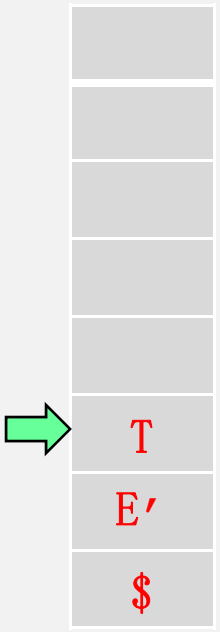
Predictive Parsing Progra

(id*id)+id

Output

E → T E′

E → T E′
E′ → + T E′ | ε
T → F E′
T′ → * F T′ | ε
F → (E) | id



(	id	*	id	)	+	id	$

Look at Table [E, '(']
Use rule E→TE'
Pop E
Push E'
Push T
Print E→TE'

	id	+	*	(	)	$
E	$E \to TE'$			$E \to TE'$		
E'		$E' \to +TE'$			$E' \to \varepsilon$	$E' \to \varepsilon$
T	$T \to FT'$			$T \to FT'$		
T'		$T' \to \varepsilon$	$T' \to *FT'$		$T' \to \varepsilon$	$T' \to \varepsilon$
F	$F \to$ id			$F \to (E)$		

Predictive Parsing Progra

(id*id)+id

Output

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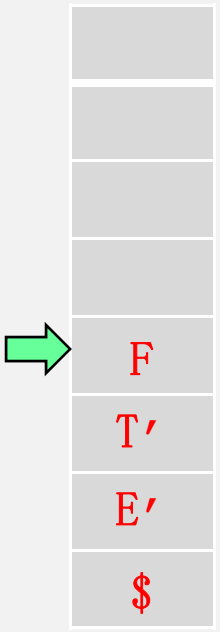
E → T E′
E′ → + T E′ | ε
T → F E′
T′ → * F T′ | ε
F → (E) | id



(	id	*	id	)	+	id	$

Table [T, '('] = T → FT'
Pop T
Push T'
Push F
Print T → FT'

	id	+	*	(	)	$
E	$E \to TE'$			$E \to TE'$		
E'		$E' \to +TE'$			$E' \to \varepsilon$	$E' \to \varepsilon$
T	$T \to FT'$			$T \to FT'$		
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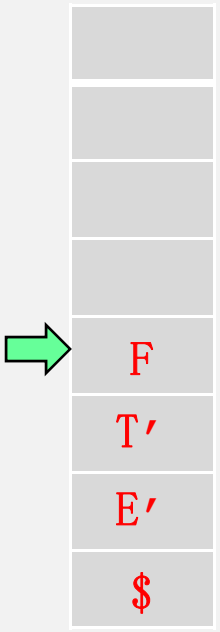
Predictive Parsing Progra

(id*id)+id

Output

E → T E′
T → FT'

E → T E′
E′ → + T E′ | ε
T → F E′
T′ → * F T′ | ε
F → (E) | id



(	id	*	id	)	+	id	$

Table [T, '('] = T → FT'
Pop T
Push T'
Push F
Print T → FT'

	id	+	*	(	)	$
E	$E \to TE'$			$E \to TE'$		
E'		$E' \to +TE'$			$E' \to \varepsilon$	$E' \to \varepsilon$
T	$T \to FT'$			$T \to FT'$		
T'		$T' \to \varepsilon$	$T' \to *FT'$		$T' \to \varepsilon$	$T' \to \varepsilon$
F	$F \to$ id			$F \to (E)$		

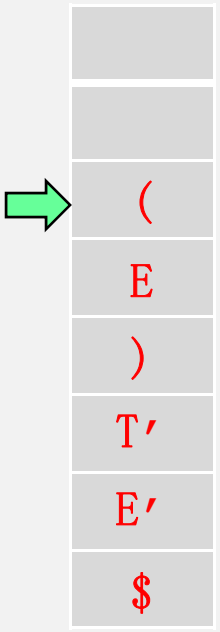
Predictive Parsing Progra

$E \rightarrow T\ E'$
$E' \rightarrow +\ T\ E' \mid \varepsilon$
$T \rightarrow F\ E'$
$T' \rightarrow *\ F\ T' \mid \varepsilon$
$F \rightarrow (\ E\ ) \mid id$

(id*id)+id

Output

E → T E′
T → F T'



(	id	*	id	)	+	id	$

Table [F, '('] = F →(E)
Pop F
Push (
Push E
Push)
Print F →(E)

	id	+	*	(	)	$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \varepsilon$	$E' \rightarrow \varepsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \varepsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \varepsilon$	$T' \rightarrow \varepsilon$
F	$F \rightarrow$ id			$F \rightarrow (E)$		

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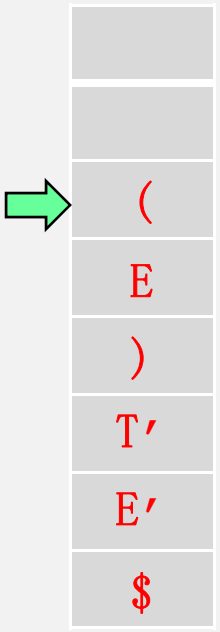
$E' \rightarrow +\ T\ E' \mid \varepsilon$
$T \rightarrow F\ E'$
$T' \rightarrow *\ F\ T' \mid \varepsilon$
$F \rightarrow (\ E\ ) \mid id$

(id*id)+id

Output

E → T E′
T → F T'
F →(E)



(	id	*	id	)	+	id	$

Table [F, '('] = F →(E)
Pop F
Push (
Push E
Push)
Print F →(E)

	id	+	*	(	)	$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \varepsilon$	$E' \rightarrow \varepsilon$
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F	$F \rightarrow$ id			$F \rightarrow (E)$		

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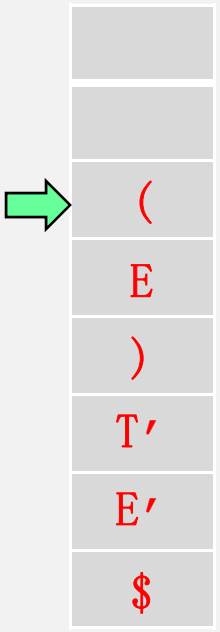
(id*id)+id

Output

E → T E′
T → F T'
F →(E)



(	id	*	id	)	+	id	$

Top of Stack matches next input
Pop and Scan

	id	+	*	(	)	$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \varepsilon$	$E' \rightarrow \varepsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \varepsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \varepsilon$	$T' \rightarrow \varepsilon$
F	$F \rightarrow$ id			$F \rightarrow (E)$		

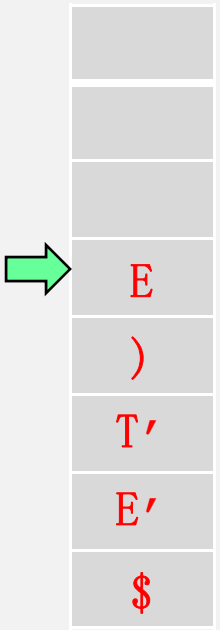
Predictive Parsing Progra

(id*id)+id

Output

E → T E′
T → F T'
F → (E)

E → T E′
E′ → + T E′ | ε
T → F E′
T′ → * F T′ | ε
F → (E) | id



(	id	*	id	)	+	id	$

Table [E, id] = E → TE'
Pop E
Push E'
Push T
Print E → TE'

	id	+	*	(	)	$
E	$E \to TE'$			$E \to TE'$		
E'		$E' \to +TE'$			$E' \to \varepsilon$	$E' \to \varepsilon$
T	$T \to FT'$			$T \to FT'$		
T'		$T' \to \varepsilon$	$T' \to *FT'$		$T' \to \varepsilon$	$T' \to \varepsilon$
F	$F \to$ id			$F \to (E)$		

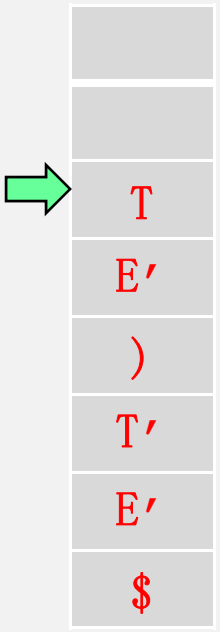
Predictive Parsing Progra

(id*id)+id

Output

E → T E′
T → F T'
F → (E)

E → T E′
E′ → + T E′ | ε
T → F E′
T′ → * F T′ | ε
F → (E) | id



(	id	*	id	)	+	id	$

Table [E, id] = E → TE'
Pop E
Push E'
Push T
Print E → TE'

	id	+	*	(	)	$
E	$E \to TE'$			$E \to TE'$		
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F	$F \to$ id			$F \to (E)$		

Predictive Parsing Progra

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$T' \rightarrow *\ F\ T' \mid \varepsilon$
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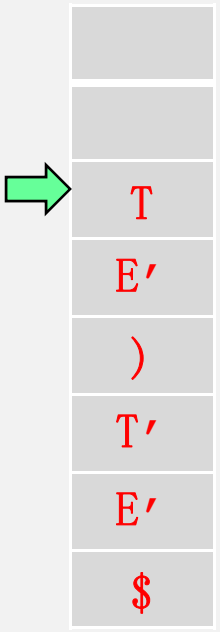
(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'



(	id	*	id	)	+	id	$

Table [T, id] = T → FT'
Pop T
Push T'
Push F
Print T → FT'

	id	+	*	(	)	$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
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(id*id)+id

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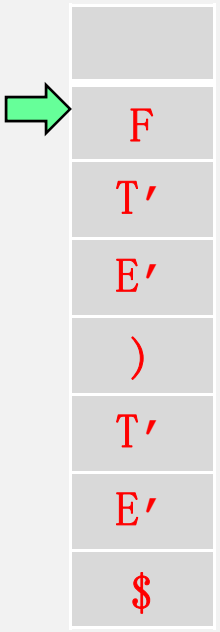
E → T E′
T → F T'
F → (E)
E → T E'



(	id	*	id	)	+	id	$

Table [T, id] = T → FT'
Pop T
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Push F
Print T → FT'

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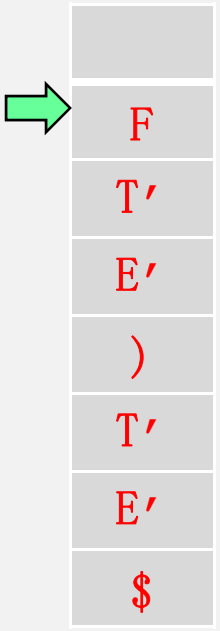
(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'



(	id	*	id	)	+	id	$

Table [T, id] = T → FT'
Pop T
Push T'
Push F
Print T → FT'

	id	+	*	(	)	$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
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(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'

F
T′
E′
)
T′
E′
$

(	id	*	id	)	+	id	$

Table [F, id] = F → id
Pop F
Push id
Print F → id

	id	+	*	(	)	$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
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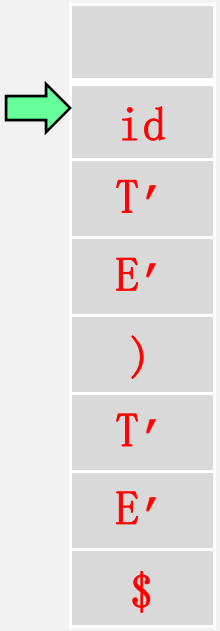
(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'



(	id	*	id	)	+	id	$

Table [F, id] = F → id
Pop F
Push id
Print F → id

	id	+	*	(	)	$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \varepsilon$	$E' \rightarrow \varepsilon$
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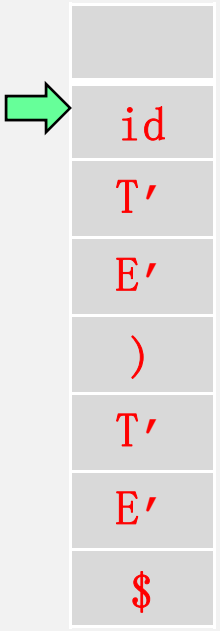
(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id



(	id	*	id	)	+	id	$

Table [F, id] = F → id
Pop F
Push id
Print F → id

	id	+	*	(	)	$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \varepsilon$	$E' \rightarrow \varepsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \varepsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \varepsilon$	$T' \rightarrow \varepsilon$
F	$F \rightarrow$ id			$F \rightarrow (E)$		

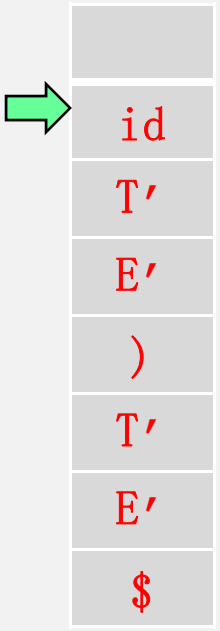
Predictive Parsing Progra

$E \rightarrow T\ E'$
$E' \rightarrow +\ T\ E' \mid \varepsilon$
$T \rightarrow F\ E'$
$T' \rightarrow *\ F\ T' \mid \varepsilon$
$F \rightarrow (\ E\ ) \mid id$

(id*id)+id

Output

$E \rightarrow T\ E'$
$T \rightarrow F\ T'$
$F \rightarrow (\ E\ )$
$E \rightarrow T\ E'$
$T \rightarrow FT'$
$F \rightarrow id$



(	id	*	id	)	+	id	$

Top of Stack matches next input
Pop and Scan

	id	+	*	(	)	$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \varepsilon$	$E' \rightarrow \varepsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \varepsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \varepsilon$	$T' \rightarrow \varepsilon$
F	$F \rightarrow$ id			$F \rightarrow (E)$		

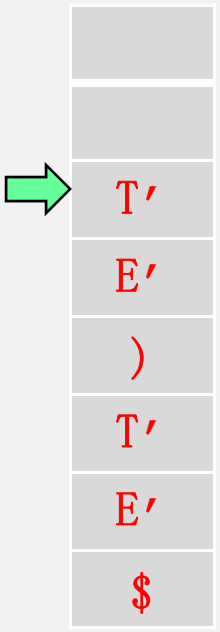
Predictive Parsing Progra

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id

E → T E′
E′ → + T E′ | ε
T → F E′
T′ → * F T′ | ε
F → (E) | id



(	id	*	id	)	+	id	$

Top of Stack matches next input
Pop and Scan

	id	+	*	(	)	$
E	$E \to TE'$			$E \to TE'$		
E'		$E' \to +TE'$			$E' \to \varepsilon$	$E' \to \varepsilon$
T	$T \to FT'$			$T \to FT'$		
T'		$T' \to \varepsilon$	$T' \to *FT'$		$T' \to \varepsilon$	$T' \to \varepsilon$
F	$F \to$ id			$F \to (E)$		

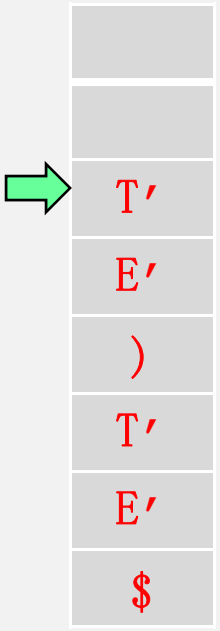
Predictive Parsing Progra

$E \rightarrow T\ E'$
$E' \rightarrow +\ T\ E' \mid \varepsilon$
$T \rightarrow F\ E'$
$T' \rightarrow *\ F\ T' \mid \varepsilon$
$F \rightarrow (\ E\ ) \mid id$

(id*id)+id

Output

$E \rightarrow T\ E'$
$T \rightarrow F\ T'$
$F \rightarrow (\ E\ )$
$E \rightarrow T\ E'$
$T \rightarrow FT'$
$F \rightarrow id$



(	id	*	id	)	+	id	$

Table [T', '*'] = T' → *FT'
Pop T'
Push T'
Push F
Push '*'
Print T' → *FT'

	id	+	*	(	)	$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \varepsilon$	$E' \rightarrow \varepsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \varepsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \varepsilon$	$T' \rightarrow \varepsilon$
F	$F \rightarrow$ id			$F \rightarrow (E)$		

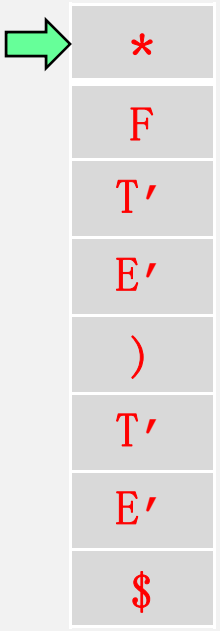
Predictive Parsing Progra

$E \rightarrow T\ E'$
$E' \rightarrow +\ T\ E' \mid \varepsilon$
$T \rightarrow F\ E'$
$T' \rightarrow *\ F\ T' \mid \varepsilon$
$F \rightarrow (\ E\ ) \mid id$

(id*id)+id

Output

$E \rightarrow T\ E'$
$T \rightarrow F\ T'$
$F \rightarrow (\ E\ )$
$E \rightarrow T\ E'$
$T \rightarrow FT'$
$F \rightarrow id$



(	id	*	id	)	+	id	$

Table [T', '*'] = T' → *FT'
Pop T'
Push T'
Push F
Push '*'
Print T' → *FT'

	id	+	*	(	)	$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \varepsilon$	$E' \rightarrow \varepsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \varepsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \varepsilon$	$T' \rightarrow \varepsilon$
F	$F \rightarrow$ id			$F \rightarrow (E)$		

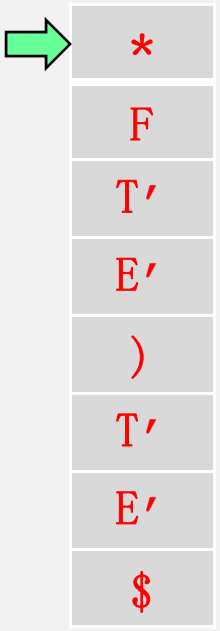
Predictive Parsing Progra

$E \rightarrow T\ E'$
$E' \rightarrow +\ T\ E' \mid \varepsilon$
$T \rightarrow F\ E'$
$T' \rightarrow *\ F\ T' \mid \varepsilon$
$F \rightarrow (\ E\ ) \mid id$

(id*id)+id

Output

$E \rightarrow T\ E'$
$T \rightarrow F\ T'$
$F \rightarrow (\ E\ )$
$E \rightarrow T\ E'$
$T \rightarrow FT'$
$F \rightarrow id$
$T' \rightarrow *FT'$



(	id	*	id	)	+	id	$

Table [T', '*'] = T' → *FT'
Pop T'
Push T'
Push F
Push '*'
Print T' → *FT'

	id	+	*	(	)	$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \varepsilon$	$E' \rightarrow \varepsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \varepsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \varepsilon$	$T' \rightarrow \varepsilon$
F	$F \rightarrow$ id			$F \rightarrow (E)$		

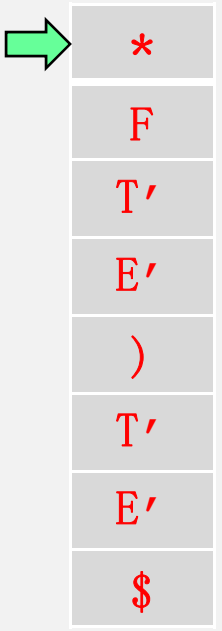
Predictive Parsing Progra

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT'

E → T E′
E′ → + T E′ | ε
T → F E′
T′ → * F T′ | ε
F → (E) | id



(	id	*	id	)	+	id	$

Top of Stack matches next input
Pop and Scan

	id	+	*	(	)	$
E	$E \to TE'$			$E \to TE'$		
E'		$E' \to +TE'$			$E' \to \varepsilon$	$E' \to \varepsilon$
T	$T \to FT'$			$T \to FT'$		
T'		$T' \to \varepsilon$	$T' \to *FT'$		$T' \to \varepsilon$	$T' \to \varepsilon$
F	$F \to$ id			$F \to (E)$		

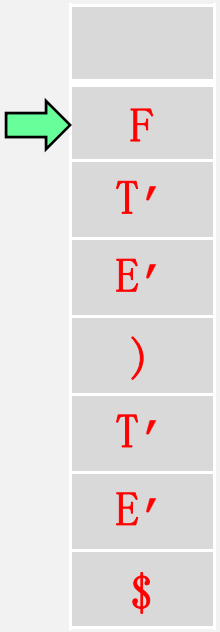
Predictive Parsing Progra

$E \rightarrow T\ E'$
$E' \rightarrow +\ T\ E' \mid \varepsilon$
$T \rightarrow F\ E'$
$T' \rightarrow *\ F\ T' \mid \varepsilon$
$F \rightarrow (\ E\ ) \mid id$

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT'



(	id	*	id	)	+	id	$

Top of Stack matches next input
Pop and Scan

	id	+	*	(	)	$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \varepsilon$	$E' \rightarrow \varepsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \varepsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \varepsilon$	$T' \rightarrow \varepsilon$
F	$F \rightarrow$ id			$F \rightarrow (E)$		

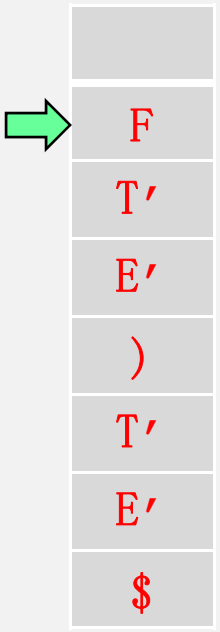
Predictive Parsing Progra

$E \rightarrow T\ E'$
$E' \rightarrow +\ T\ E' \mid \varepsilon$
$T \rightarrow F\ E'$
$T' \rightarrow *\ F\ T' \mid \varepsilon$
$F \rightarrow (\ E\ ) \mid id$

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT'



(	id	*	id	)	+	id	$

Table [F, id] = F → id
Pop F
Push id
Print F → id

	id	+	*	(	)	$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \varepsilon$	$E' \rightarrow \varepsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \varepsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \varepsilon$	$T' \rightarrow \varepsilon$
F	$F \rightarrow$ id			$F \rightarrow (E)$		

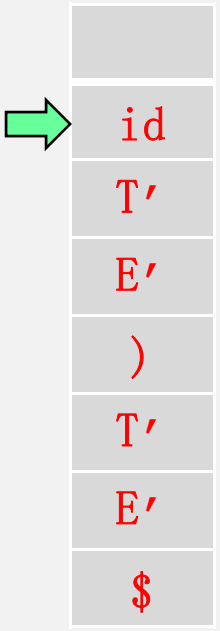
Predictive Parsing Progra

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT'

E → T E′
E′ → + T E′ | ε
T → F E′
T′ → * F T′ | ε
F → (E) | id



(	id	*	id	)	+	id	$

Table [F, id] = F → id
Pop F
Push id
Print F → id

	id	+	*	(	)	$
E	$E \to TE'$			$E \to TE'$		
E'		$E' \to +TE'$			$E' \to \varepsilon$	$E' \to \varepsilon$
T	$T \to FT'$			$T \to FT'$		
T'		$T' \to \varepsilon$	$T' \to *FT'$		$T' \to \varepsilon$	$T' \to \varepsilon$
F	$F \to$ id			$F \to (E)$		

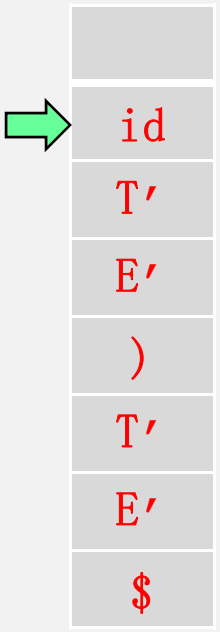
Predictive Parsing Progra

$E \rightarrow T\ E'$
$E' \rightarrow +\ T\ E' \mid \varepsilon$
$T \rightarrow F\ E'$
$T' \rightarrow *\ F\ T' \mid \varepsilon$
$F \rightarrow (\ E\ ) \mid id$

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT'
F → id



(	id	*	id	)	+	id	$

Table [F, id] = F → id
Pop F
Push id
Print F → id

	id	+	*	(	)	$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \varepsilon$	$E' \rightarrow \varepsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \varepsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \varepsilon$	$T' \rightarrow \varepsilon$
F	$F \rightarrow$ id			$F \rightarrow (E)$		

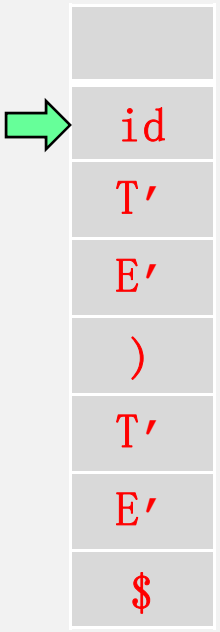
Predictive Parsing Progra

$E \rightarrow T\ E'$
$E' \rightarrow +\ T\ E' \mid \varepsilon$
$T \rightarrow F\ E'$
$T' \rightarrow *\ F\ T' \mid \varepsilon$
$F \rightarrow (\ E\ ) \mid id$

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT'
F → id



(	id	*	id	)	+	id	$

Top of Stack matches next input
Pop and Scan

	id	+	*	(	)	$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \varepsilon$	$E' \rightarrow \varepsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \varepsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \varepsilon$	$T' \rightarrow \varepsilon$
F	$F \rightarrow$ id			$F \rightarrow (E)$		

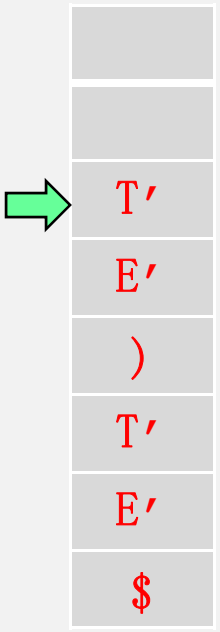
Predictive Parsing Progra

$E \rightarrow T\ E'$
$E' \rightarrow +\ T\ E' \mid \varepsilon$
$T \rightarrow F\ E'$
$T' \rightarrow *\ F\ T' \mid \varepsilon$
$F \rightarrow (\ E\ ) \mid id$

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT'
F → id



(	id	*	id	)	+	id	$

Top of Stack matches next input
Pop and Scan

	id	+	*	(	)	$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \varepsilon$	$E' \rightarrow \varepsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \varepsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \varepsilon$	$T' \rightarrow \varepsilon$
F	$F \rightarrow$ id			$F \rightarrow (E)$		

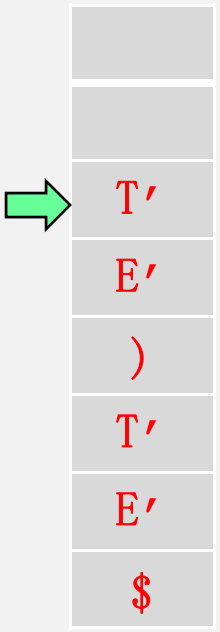
Predictive Parsing Progra

$E \rightarrow T\ E'$
$E' \rightarrow +\ T\ E' \mid \varepsilon$
$T \rightarrow F\ E'$
$T' \rightarrow *\ F\ T' \mid \varepsilon$
$F \rightarrow (\ E\ ) \mid id$

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT'
F → id



(	id	*	id	)	+	id	$

Table [T', ')'] = T' → ε
Pop T'
Push <nothing>
Print T' → ε

	id	+	*	(	)	$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \varepsilon$	$E' \rightarrow \varepsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \varepsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \varepsilon$	$T' \rightarrow \varepsilon$
F	$F \rightarrow$ id			$F \rightarrow (E)$		

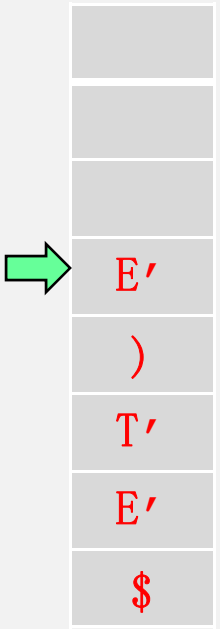
Predictive Parsing Progra

$E \rightarrow T\ E'$
$E' \rightarrow +\ T\ E' \mid \varepsilon$
$T \rightarrow F\ E'$
$T' \rightarrow *\ F\ T' \mid \varepsilon$
$F \rightarrow (\ E\ ) \mid id$

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT'
F → id
T'→ ε



(	id	*	id	)	+	id	$

Table [T', ')'] = T' → ε
Pop T'
Push <nothing>
Print T' → ε

	id	+	*	(	)	$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \varepsilon$	$E' \rightarrow \varepsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \varepsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \varepsilon$	$T' \rightarrow \varepsilon$
F	$F \rightarrow$ id			$F \rightarrow (E)$		

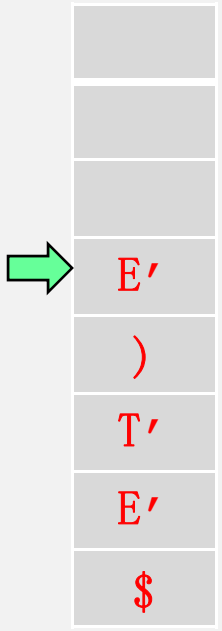
Predictive Parsing Progra

$E \rightarrow T\ E'$
$E' \rightarrow +\ T\ E' \mid \varepsilon$
$T \rightarrow F\ E'$
$T' \rightarrow *\ F\ T' \mid \varepsilon$
$F \rightarrow (\ E\ ) \mid id$

(id*id)+id

Output

$E \rightarrow T\ E'$
$T \rightarrow F\ T'$
$F \rightarrow (\ E\ )$
$E \rightarrow T\ E'$
$T \rightarrow FT'$
$F \rightarrow id$
$T' \rightarrow *FT'$
$F \rightarrow id$
$T' \rightarrow \varepsilon$



(	id	*	id	)	+	id	$

Table [E', ')'] = $E' \rightarrow \varepsilon$
Pop E'
Push <nothing>
Print $E' \rightarrow \varepsilon$

	id	+	*	(	)	$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \varepsilon$	$E' \rightarrow \varepsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \varepsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \varepsilon$	$T' \rightarrow \varepsilon$
F	$F \rightarrow$ id			$F \rightarrow (E)$		

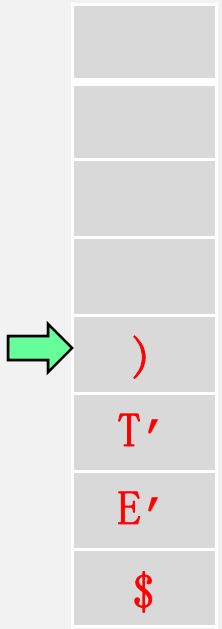
Predictive Parsing Progra

$E \rightarrow T\ E'$
$E' \rightarrow +\ T\ E' \mid \varepsilon$
$T \rightarrow F\ E'$
$T' \rightarrow *\ F\ T' \mid \varepsilon$
$F \rightarrow (\ E\ ) \mid id$

(id*id)+id

Output

$E \rightarrow T\ E'$
$T \rightarrow F\ T'$
$F \rightarrow (\ E\ )$
$E \rightarrow T\ E'$
$T \rightarrow FT'$
$F \rightarrow id$
$T' \rightarrow *FT'$
$F \rightarrow id$
$T' \rightarrow \varepsilon$



(	id	*	id	)	+	id	$

Table [E', ')'] = $E' \rightarrow \varepsilon$
Pop E'
Push <nothing>
Print $E' \rightarrow \varepsilon$

	id	+	*	(	)	$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \varepsilon$	$E' \rightarrow \varepsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \varepsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \varepsilon$	$T' \rightarrow \varepsilon$
F	$F \rightarrow$ id			$F \rightarrow (E)$		

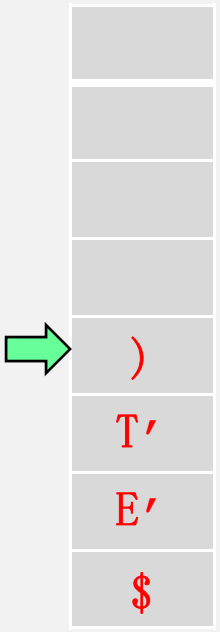
Predictive Parsing Progra

$E \rightarrow T\ E'$
$E' \rightarrow +\ T\ E' \mid \varepsilon$
$T \rightarrow F\ E'$
$T' \rightarrow *\ F\ T' \mid \varepsilon$
$F \rightarrow (\ E\ ) \mid id$

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT'
F → id
T'→ ε
E'→ ε



(	id	*	id	)	+	id	$

Table [E', ')'] = E' → ε
Pop E'
Push <nothing>
Print E' → ε

	id	+	*	(	)	$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \varepsilon$	$E' \rightarrow \varepsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \varepsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \varepsilon$	$T' \rightarrow \varepsilon$
F	$F \rightarrow$ id			$F \rightarrow (E)$		

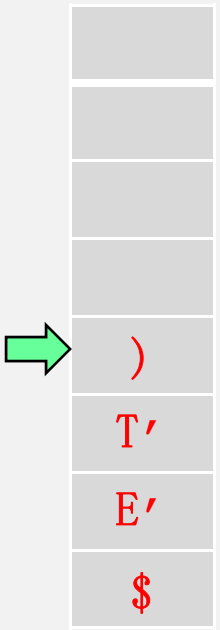
Predictive Parsing Progra

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT'
F → id
T'→ ε
E'→ ε

E → T E′
E′ → + T E′ | ε
T → F E′
T′ → * F T′ | ε
F → (E) | id



(	id	*	id	)	+	id	$

Top of Stack matches next input
Pop and Scan

	id	+	*	(	)	$
E	$E \to TE'$			$E \to TE'$		
E'		$E' \to +TE'$			$E' \to \varepsilon$	$E' \to \varepsilon$
T	$T \to FT'$			$T \to FT'$		
T'		$T' \to \varepsilon$	$T' \to *FT'$		$T' \to \varepsilon$	$T' \to \varepsilon$
F	$F \to$ id			$F \to (E)$		

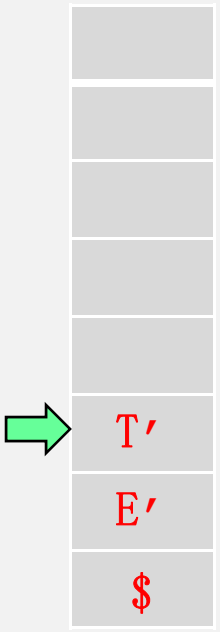
Predictive Parsing Progra

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT'
F → id
T'→ ε
E'→ ε

E → T E′
E′ → + T E′ | ε
T → F E′
T′ → * F T′ | ε
F → (E) | id



(	id	*	id	)	+	id	$

Top of Stack matches next input
Pop and Scan

	id	+	*	(	)	$
E	$E \to TE'$			$E \to TE'$		
E'		$E' \to +TE'$			$E' \to \varepsilon$	$E' \to \varepsilon$
T	$T \to FT'$			$T \to FT'$		
T'		$T' \to \varepsilon$	$T' \to *FT'$		$T' \to \varepsilon$	$T' \to \varepsilon$
F	$F \to$ id			$F \to (E)$		

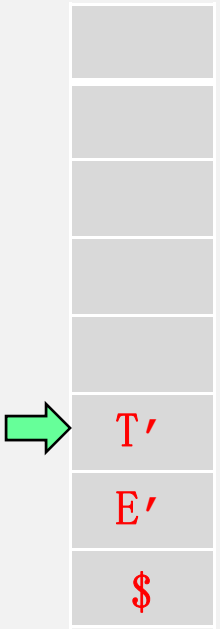
Predictive Parsing Progra

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT'
F → id
T'→ ε
E'→ ε

E → T E′
E′ → + T E′ | ε
T → F E′
T′ → * F T′ | ε
F → (E) | id



(	id	*	id	)	+	id	$

Table [T', '+'] = T' → ε
Pop T'
Push <nothing>
Print T' → ε

	id	+	*	(	)	$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \varepsilon$	$E' \rightarrow \varepsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \varepsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \varepsilon$	$T' \rightarrow \varepsilon$
F	$F \rightarrow$ id			$F \rightarrow (E)$		

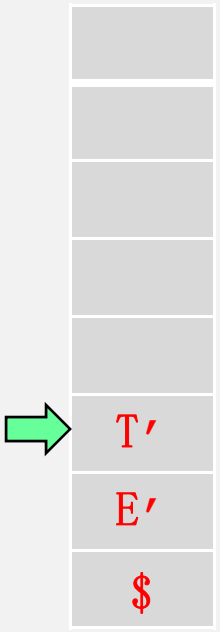
Predictive Parsing Progra

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT'
F → id
T'→ ε
E'→ ε
T'→ ε

E → T E′
E′ → + T E′ | ε
T → F E′
T′ → * F T′ | ε
F → (E) | id



(	id	*	id	)	+	id	$

Table [T', '+'] = T' → ε
Pop T'
Push <nothing>
Print T' → ε

	id	+	*	(	)	$
E	$E \to TE'$			$E \to TE'$		
E'		$E' \to +TE'$			$E' \to \varepsilon$	$E' \to \varepsilon$
T	$T \to FT'$			$T \to FT'$		
T'		$T' \to \varepsilon$	$T' \to *FT'$		$T' \to \varepsilon$	$T' \to \varepsilon$
F	$F \to$ id			$F \to (E)$		

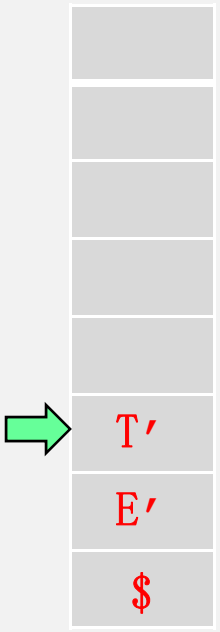
Predictive Parsing Progra

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT'
F → id
T'→ ε
E'→ ε
T'→ ε

E → T E′
E′ → + T E′ | ε
T → F E′
T′ → * F T′ | ε
F → (E) | id



(	id	*	id	)	+	id	$

Table [T', '+'] = T' → ε
Pop T'
Push <nothing>
Print T' → ε

	id	+	*	(	)	$
E	$E \to TE'$			$E \to TE'$		
E'		$E' \to +TE'$			$E' \to \varepsilon$	$E' \to \varepsilon$
T	$T \to FT'$			$T \to FT'$		
T'		$T' \to \varepsilon$	$T' \to *FT'$		$T' \to \varepsilon$	$T' \to \varepsilon$
F	$F \to$ id			$F \to (E)$		

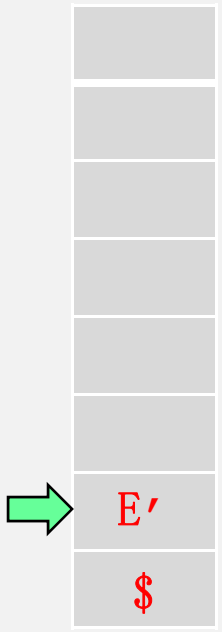
Predictive Parsing Progra

$E \rightarrow T\ E'$
$E' \rightarrow +\ T\ E' \mid \varepsilon$
$T \rightarrow F\ E'$
$T' \rightarrow *\ F\ T' \mid \varepsilon$
$F \rightarrow (\ E\ ) \mid id$

(id*id)+id

Output

$E \rightarrow T\ E'$
$T \rightarrow F\ T'$
$F \rightarrow (\ E\ )$
$E \rightarrow T\ E'$
$T \rightarrow FT'$
$F \rightarrow id$
$T' \rightarrow *FT'$
$F \rightarrow id$
$T' \rightarrow \varepsilon$
$E' \rightarrow \varepsilon$
$T' \rightarrow \varepsilon$



(	id	*	id	)	+	id	$

Table [T', '+'] = $T' \rightarrow \varepsilon$
Pop T'
Push <nothing>
Print $T' \rightarrow \varepsilon$

	id	+	*	(	)	$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \varepsilon$	$E' \rightarrow \varepsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \varepsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \varepsilon$	$T' \rightarrow \varepsilon$
F	$F \rightarrow$ id			$F \rightarrow (E)$		

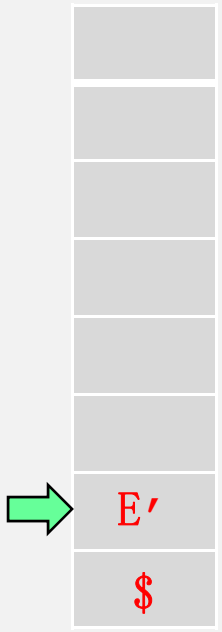
Predictive Parsing Progra

$E \rightarrow T\ E'$
$E' \rightarrow +\ T\ E' \mid \varepsilon$
$T \rightarrow F\ E'$
$T' \rightarrow *\ F\ T' \mid \varepsilon$
$F \rightarrow (\ E\ ) \mid id$

(id*id)+id

Output

$E \rightarrow T\ E'$
$T \rightarrow F\ T'$
$F \rightarrow (\ E\ )$
$E \rightarrow T\ E'$
$T \rightarrow FT'$
$F \rightarrow id$
$T' \rightarrow *FT'$
$F \rightarrow id$
$T' \rightarrow \varepsilon$
$E' \rightarrow \varepsilon$
$T' \rightarrow \varepsilon$



(	id	*	id	)	+	id	$

Table [E', '+'] = $E' \rightarrow +TE'$
Pop E'
Push E'
Push T
Push '+'
Print $E' \rightarrow +TE'$

	id	+	*	(	)	$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \varepsilon$	$E' \rightarrow \varepsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \varepsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \varepsilon$	$T' \rightarrow \varepsilon$
F	$F \rightarrow$ id			$F \rightarrow (E)$		

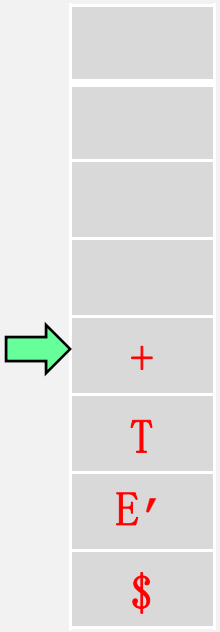
Predictive Parsing Progra

$E \rightarrow T\ E'$
$E' \rightarrow +\ T\ E' \mid \varepsilon$
$T \rightarrow F\ E'$
$T' \rightarrow *\ F\ T' \mid \varepsilon$
$F \rightarrow (\ E\ ) \mid id$

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT'
F → id
T'→ ε
E'→ ε
T'→ ε



(	id	*	id	)	+	id	$

Table [E', '+'] = E' → +TE'
Pop E'
Push E'
Push T
Push '+'
Print E' → +TE'

	id	+	*	(	)	$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \varepsilon$	$E' \rightarrow \varepsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \varepsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \varepsilon$	$T' \rightarrow \varepsilon$
F	$F \rightarrow$ id			$F \rightarrow (E)$		

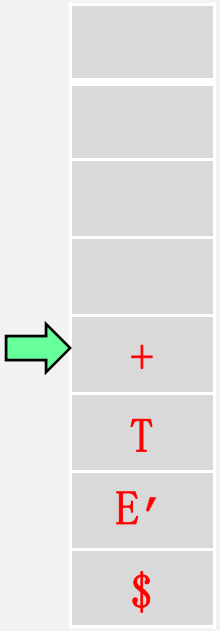
Predictive Parsing Progra

$E \rightarrow T\ E'$
$E' \rightarrow +\ T\ E' \mid \varepsilon$
$T \rightarrow F\ E'$
$T' \rightarrow *\ F\ T' \mid \varepsilon$
$F \rightarrow (\ E\ ) \mid id$

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT'
F → id
T'→ ε
E'→ ε
T'→ ε
E′→ +TE'



(	id	*	id	)	+	id	$

Table [E', '+'] = E' → +TE'
Pop E'
Push E'
Push T
Push '+'
Print E' → +TE'

	id	+	*	(	)	$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \varepsilon$	$E' \rightarrow \varepsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \varepsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \varepsilon$	$T' \rightarrow \varepsilon$
F	$F \rightarrow$ id			$F \rightarrow (E)$		

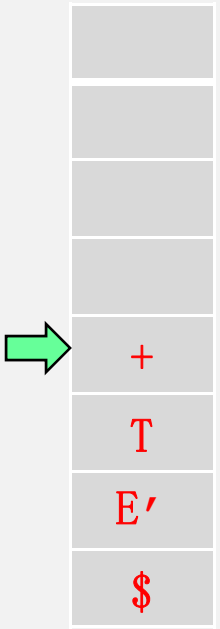
Predictive Parsing Progra

$E \rightarrow T\ E'$
$E' \rightarrow +\ T\ E' \mid \varepsilon$
$T \rightarrow F\ E'$
$T' \rightarrow *\ F\ T' \mid \varepsilon$
$F \rightarrow (\ E\ ) \mid id$

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT'
F → id
T'→ ε
E'→ ε
T'→ ε
E′→ +TE'



(	id	*	id	)	+	id	$

Top of Stack matches next input
Pop and Scan

	id	+	*	(	)	$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \varepsilon$	$E' \rightarrow \varepsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \varepsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \varepsilon$	$T' \rightarrow \varepsilon$
F	$F \rightarrow$ id			$F \rightarrow (E)$		

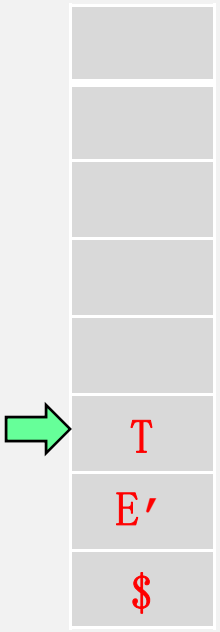
Predictive Parsing Progra

$E \rightarrow T\ E'$
$E' \rightarrow +\ T\ E' \mid \varepsilon$
$T \rightarrow F\ E'$
$T' \rightarrow *\ F\ T' \mid \varepsilon$
$F \rightarrow (\ E\ ) \mid id$

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT'
F → id
T'→ ε
E'→ ε
T'→ ε
E′→ +TE'



(	id	*	id	)	+	id	$

Top of Stack matches next input
Pop and Scan

	id	+	*	(	)	$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \varepsilon$	$E' \rightarrow \varepsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \varepsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \varepsilon$	$T' \rightarrow \varepsilon$
F	$F \rightarrow$ id			$F \rightarrow (E)$		

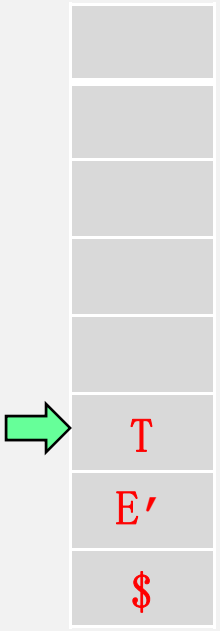
Predictive Parsing Progra

$E \rightarrow T\ E'$
$E' \rightarrow +\ T\ E' \mid \varepsilon$
$T \rightarrow F\ E'$
$T' \rightarrow *\ F\ T' \mid \varepsilon$
$F \rightarrow (\ E\ ) \mid id$

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT'
F → id
T'→ ε
E'→ ε
T'→ ε
E′→ +TE'



(	id	*	id	)	+	id	$

Table [T, id] = T → FT'
Pop T
Push T'
Push F
Print T → FT'

	id	+	*	(	)	$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \varepsilon$	$E' \rightarrow \varepsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \varepsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \varepsilon$	$T' \rightarrow \varepsilon$
F	$F \rightarrow$ id			$F \rightarrow (E)$		

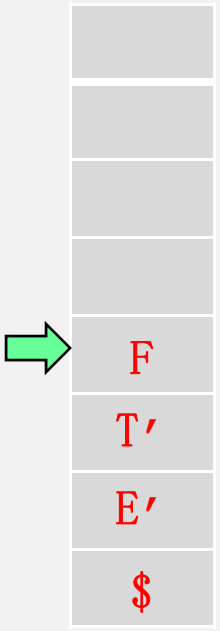
Predictive Parsing Progra

$E \rightarrow T\ E'$
$E' \rightarrow +\ T\ E' \mid \varepsilon$
$T \rightarrow F\ E'$
$T' \rightarrow *\ F\ T' \mid \varepsilon$
$F \rightarrow (\ E\ ) \mid id$

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT'
F → id
T'→ ε
E'→ ε
T'→ ε
E′→ +TE'



(	id	*	id	)	+	id	$

Table [T, id] = T → FT'
Pop T
Push T'
Push F
Print T → FT'

	id	+	*	(	)	$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \varepsilon$	$E' \rightarrow \varepsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \varepsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \varepsilon$	$T' \rightarrow \varepsilon$
F	$F \rightarrow$ id			$F \rightarrow (E)$		

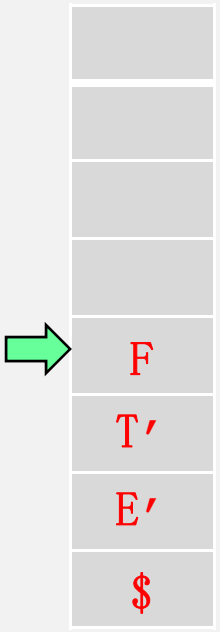
Predictive Parsing Progra

$E \rightarrow T\ E'$
$E' \rightarrow +\ T\ E' \mid \varepsilon$
$T \rightarrow F\ E'$
$T' \rightarrow *\ F\ T' \mid \varepsilon$
$F \rightarrow (\ E\ ) \mid id$

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT'
F → id
T'→ ε
E'→ ε
T'→ ε
E′→ +TE'
T → FT'



(	id	*	id	)	+	id	$

Table [T, id] = T → FT'
Pop T
Push T'
Push F
Print T → FT'

	id	+	*	(	)	$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \varepsilon$	$E' \rightarrow \varepsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \varepsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \varepsilon$	$T' \rightarrow \varepsilon$
F	$F \rightarrow$ id			$F \rightarrow (E)$		

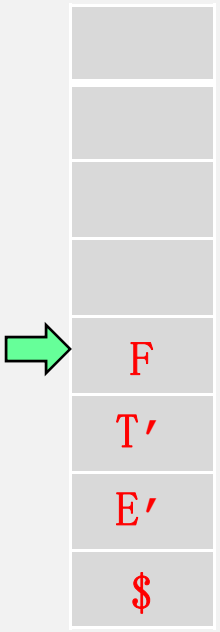
Predictive Parsing Progra

$E \rightarrow T\ E'$
$E' \rightarrow +\ T\ E' \mid \varepsilon$
$T \rightarrow F\ E'$
$T' \rightarrow *\ F\ T' \mid \varepsilon$
$F \rightarrow (\ E\ ) \mid id$

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT'
F → id
T'→ ε
E'→ ε
T'→ ε
E′→ +TE'
T → FT'



(	id	*	id	)	+	id	$

Table [F, id] = F → id
Pop F
Push id
Print F → id

	id	+	*	(	)	$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \varepsilon$	$E' \rightarrow \varepsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \varepsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \varepsilon$	$T' \rightarrow \varepsilon$
F	$F \rightarrow$ id			$F \rightarrow (E)$		

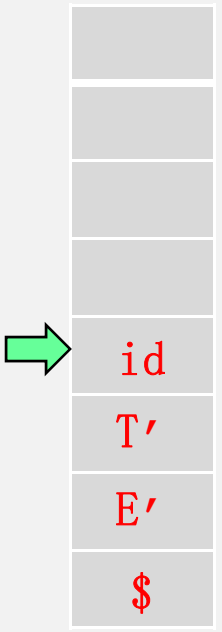
Predictive Parsing Progra

$E \rightarrow T\ E'$
$E' \rightarrow +\ T\ E' \mid \varepsilon$
$T \rightarrow F\ E'$
$T' \rightarrow *\ F\ T' \mid \varepsilon$
$F \rightarrow (\ E\ ) \mid id$

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT'
F → id
T'→ ε
E'→ ε
T'→ ε
E′→ +TE'
T → FT'



(	id	*	id	)	+	id	$

Table [F, id] = F → id
Pop F
Push id
Print F → id

	id	+	*	(	)	$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \varepsilon$	$E' \rightarrow \varepsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \varepsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \varepsilon$	$T' \rightarrow \varepsilon$
F	$F \rightarrow$ id			$F \rightarrow (E)$		

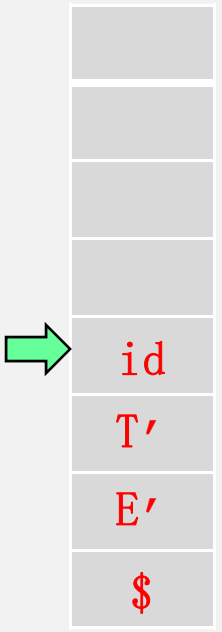
Predictive Parsing Progra

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT‘
F → id
T'→ ε
E'→ ε
T'→ ε
E′→ +TE‘
T → FT‘
F → id

E → T E′
E′ → + T E′ | ε
T → F E′
T′ → * F T′ | ε
F → (E) | id



(	id	*	id	)	+	id	$

Table [F, id] = F → id
Pop F
Push id
Print F → id

	id	+	*	(	)	$
E	$E \to TE'$			$E \to TE'$		
E'		$E' \to +TE'$			$E' \to \varepsilon$	$E' \to \varepsilon$
T	$T \to FT'$			$T \to FT'$		
T'		$T' \to \varepsilon$	$T' \to *FT'$		$T' \to \varepsilon$	$T' \to \varepsilon$
F	$F \to$ id			$F \to (E)$		

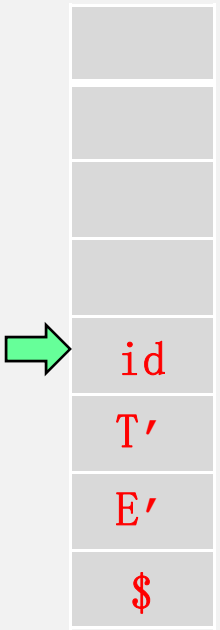
Predictive Parsing Progra

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT'
F → id
T'→ ε
E'→ ε
T'→ ε
E′→ +TE'
T → FT'
F → id

E → T E′
E′ → + T E′ | ε
T → F E′
T′ → * F T′ | ε
F → (E) | id



(	id	*	id	)	+	id	$

Top of Stack matches next input
Pop and Scan

	id	+	*	(	)	$
E	$E \to TE'$			$E \to TE'$		
E'		$E' \to +TE'$			$E' \to \varepsilon$	$E' \to \varepsilon$
T	$T \to FT'$			$T \to FT'$		
T'		$T' \to \varepsilon$	$T' \to *FT'$		$T' \to \varepsilon$	$T' \to \varepsilon$
F	$F \to$ id			$F \to (E)$		

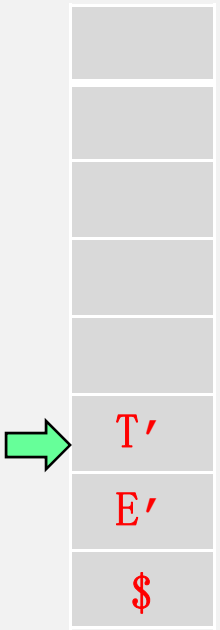
Predictive Parsing Progra

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT'
F → id
T'→ ε
E'→ ε
T'→ ε
E′→ +TE'
T → FT'
F → id

E → T E′
E′ → + T E′ | ε
T → F E′
T′ → * F T′ | ε
F → (E) | id



(	id	*	id	)	+	id	$

Top of Stack matches next input
Pop and Scan

	id	+	*	(	)	$
E	$E \to TE'$			$E \to TE'$		
E'		$E' \to +TE'$			$E' \to \varepsilon$	$E' \to \varepsilon$
T	$T \to FT'$			$T \to FT'$		
T'		$T' \to \varepsilon$	$T' \to *FT'$		$T' \to \varepsilon$	$T' \to \varepsilon$
F	$F \to$ id			$F \to (E)$		

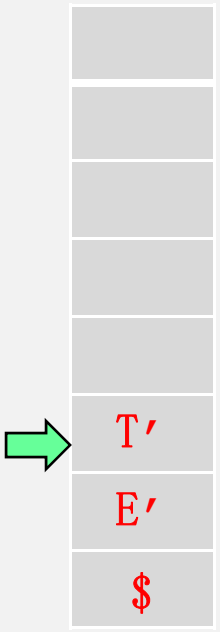
Predictive Parsing Progra

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT‘
F → id
T'→ ε
E'→ ε
T'→ ε
E′→ +TE‘
T → FT‘
F → id
T'→ ε

E → T E′
E′ → + T E′ | ε
T → F E′
T′ → * F T′ | ε
F → (E) | id



(	id	*	id	)	+	id	$

Table [T', $] = T' → ε
Pop T'
Push <nothing>
Print T' → ε

	id	+	*	(	)	$
E	$E \to TE'$			$E \to TE'$		
E'		$E' \to +TE'$			$E' \to \varepsilon$	$E' \to \varepsilon$
T	$T \to FT'$			$T \to FT'$		
T'		$T' \to \varepsilon$	$T' \to *FT'$		$T' \to \varepsilon$	$T' \to \varepsilon$
F	$F \to$ id			$F \to (E)$		

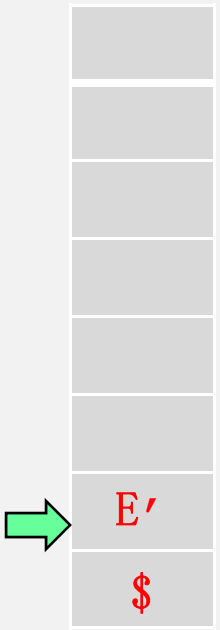
Predictive Parsing Progra

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT'
F → id
T'→ ε
E'→ ε
T'→ ε
E′→ +TE'
T → FT'
F → id
T'→ ε

E → T E′
E′ → + T E′ | ε
T → F E′
T′ → * F T′ | ε
F → (E) | id



(	id	*	id	)	+	id	$

Table [T', $] = T' → ε
Pop T'
Push <nothing>
Print T' → ε

	id	+	*	(	)	$
E	$E \to TE'$			$E \to TE'$		
E'		$E' \to +TE'$			$E' \to \varepsilon$	$E' \to \varepsilon$
T	$T \to FT'$			$T \to FT'$		
T'		$T' \to \varepsilon$	$T' \to *FT'$		$T' \to \varepsilon$	$T' \to \varepsilon$
F	$F \to$ id			$F \to (E)$		

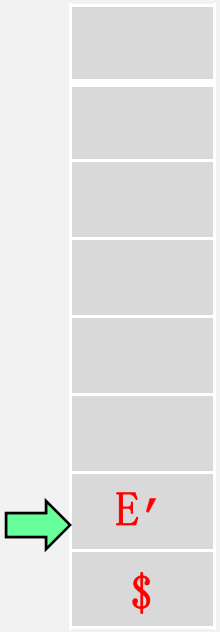
Predictive Parsing Progra

$E \rightarrow T\ E'$
$E' \rightarrow +\ T\ E' \mid \varepsilon$
$T \rightarrow F\ E'$
$T' \rightarrow *\ F\ T' \mid \varepsilon$
$F \rightarrow (\ E\ ) \mid id$

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT'
F → id
T'→ ε
E'→ ε
T'→ ε
E′→ +TE'
T → FT'
F → id
T'→ ε



(	id	*	id	)	+	id	$

Table [E', ε] = E' → ε
Pop E'
Push <nothing>
Print E' → ε

	id	+	*	(	)	$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \varepsilon$	$E' \rightarrow \varepsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \varepsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \varepsilon$	$T' \rightarrow \varepsilon$
F	$F \rightarrow$ id			$F \rightarrow (E)$		

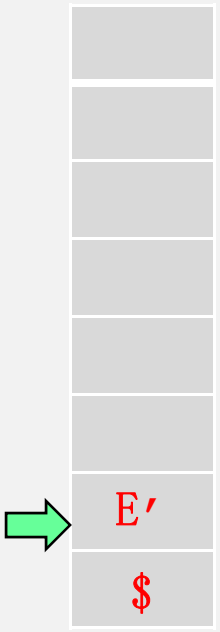
Predictive Parsing Progra

$E \rightarrow T\ E'$
$E' \rightarrow +\ T\ E' \mid \varepsilon$
$T \rightarrow F\ E'$
$T' \rightarrow *\ F\ T' \mid \varepsilon$
$F \rightarrow (\ E\ ) \mid id$

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT'
F → id
T'→ ε
E'→ ε
T'→ ε
E′→ +TE'
T → FT'
F → id
T'→ ε



(	id	*	id	)	+	id	$

Table [E', ε] = E' → ε
Pop E'
Push <nothing>
Print E' → ε

	id	+	*	(	)	$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \varepsilon$	$E' \rightarrow \varepsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \varepsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \varepsilon$	$T' \rightarrow \varepsilon$
F	$F \rightarrow$ id			$F \rightarrow (E)$		

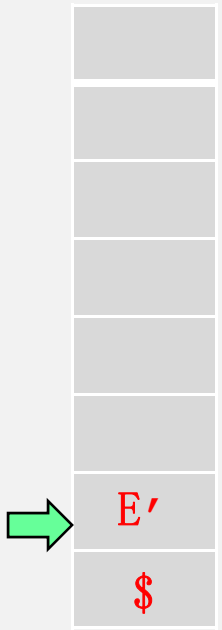
Predictive Parsing Progra

$E \rightarrow T\ E'$
$E' \rightarrow +\ T\ E' \mid \varepsilon$
$T \rightarrow F\ E'$
$T' \rightarrow *\ F\ T' \mid \varepsilon$
$F \rightarrow (\ E\ ) \mid id$

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT‘
F → id
T'→ ε
E'→ ε
T'→ ε
E′→ +TE‘
T → FT‘
F → id
T'→ ε
E'→ ε



(	id	*	id	)	+	id	$

Table [E', ε] = E' → ε
Pop E'
Push <nothing>
Print E' → ε

	id	+	*	(	)	$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \varepsilon$	$E' \rightarrow \varepsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \varepsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \varepsilon$	$T' \rightarrow \varepsilon$
F	$F \rightarrow$ id			$F \rightarrow (E)$		

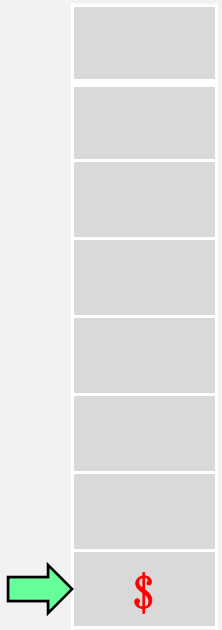
Predictive Parsing Progra

$E \rightarrow T\ E'$
$E' \rightarrow +\ T\ E' \mid \varepsilon$
$T \rightarrow F\ E'$
$T' \rightarrow *\ F\ T' \mid \varepsilon$
$F \rightarrow (\ E\ ) \mid id$

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT‘
F → id
T'→ ε
E'→ ε
T'→ ε
E′→ +TE‘
T → FT‘
F → id
T'→ ε
E'→ ε



(	id	*	id	)	+	id	$

Table [E', ε] = E' → ε
Pop E'
Push <nothing>
Print E' → ε

	id	+	*	(	)	$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \varepsilon$	$E' \rightarrow \varepsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \varepsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \varepsilon$	$T' \rightarrow \varepsilon$
F	$F \rightarrow$ id			$F \rightarrow (E)$		

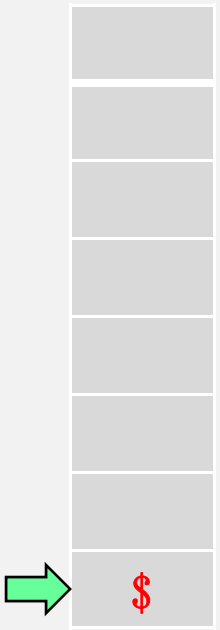
Predictive Parsing Progra

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT‘
F → id
T'→ ε
E'→ ε
T'→ ε
E′→ +TE‘
T → FT‘
F → id
T'→ ε
E'→ ε

E → T E′
E′ → + T E′ | ε
T → F E′
T′ → * F T′ | ε
F → (E) | id



(	id	*	id	)	+	id	$

Input symbol == $
Top of stack == $
Loop terminates with success

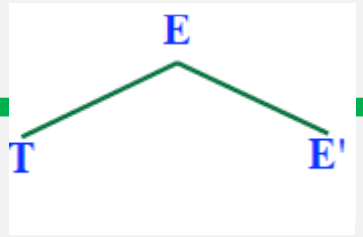
	id	+	*	(	)	$
E	$E \rightarrow TE'$			$E \rightarrow TE'$		
E'		$E' \rightarrow +TE'$			$E' \rightarrow \varepsilon$	$E' \rightarrow \varepsilon$
T	$T \rightarrow FT'$			$T \rightarrow FT'$		
T'		$T' \rightarrow \varepsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \varepsilon$	$T' \rightarrow \varepsilon$
F	$F \rightarrow$ id			$F \rightarrow (E)$		

Predictive Parsing Progra

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT'
F → id
T'→ ε
E'→ ε
T'→ ε
E′→ +TE'
T → FT'
F → id
T'→ ε
E'→ ε



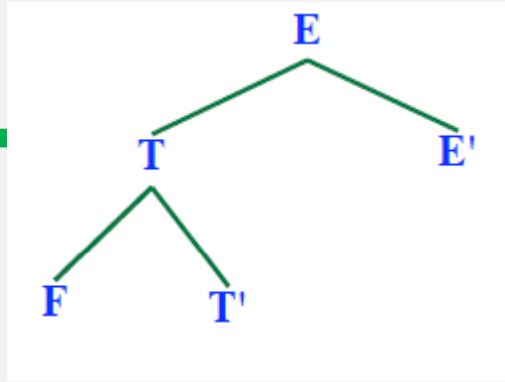
E → T E′
E′ → + T E′ | ε
T → F E′
T′ → * F T′ | ε
F → (E) | id

Predictive Parsing Progra

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT‘
F → id
T'→ ε
E'→ ε
T'→ ε
E′→ +TE‘
T → FT‘
F → id
T'→ ε
E'→ ε



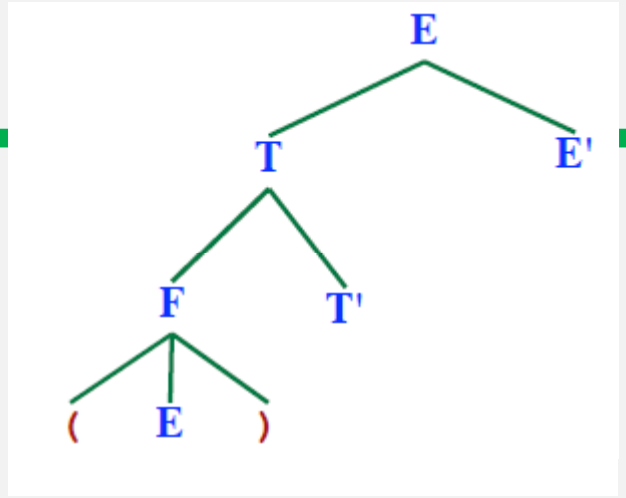
E → T E′
E′ → + T E′ | ε
T → F E′
T′ → * F T′ | ε
F → (E) | id

Predictive Parsing Progra

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT‘
F → id
T'→ ε
E'→ ε
T'→ ε
E′→ +TE‘
T → FT‘
F → id
T'→ ε
E'→ ε



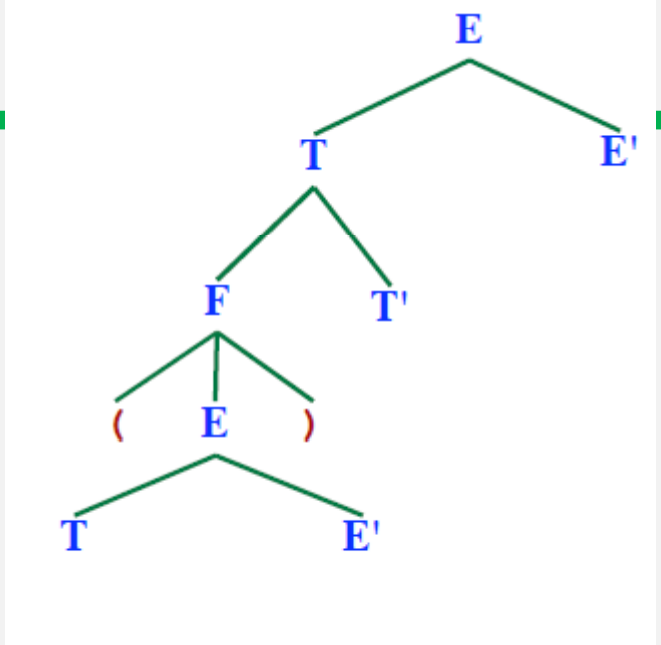
E → T E′
E′ → + T E′ | ε
T → F E′
T′ → * F T′ | ε
F → (E) | id

Predictive Parsing Progra

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT'
F → id
T'→ ε
E'→ ε
T'→ ε
E′→ +TE'
T → FT'
F → id
T'→ ε
E'→ ε



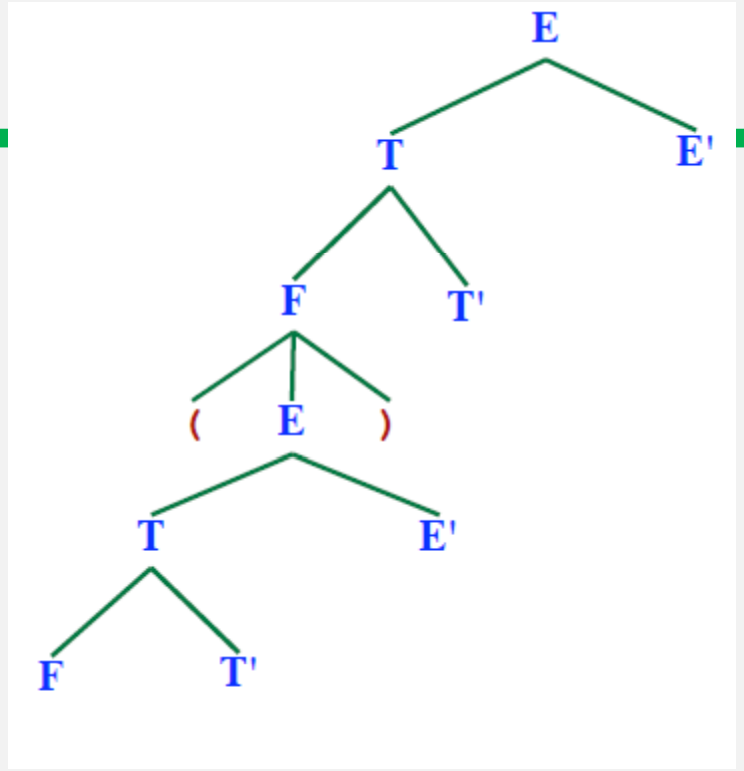
E → T E′
E′ → + T E′ | ε
T → F E′
T′ → * F T′ | ε
F → (E) | id

Predictive Parsing Progra

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT'
F → id
T'→ ε
E'→ ε
T'→ ε
E′→ +TE'
T → FT'
F → id
T'→ ε
E'→ ε



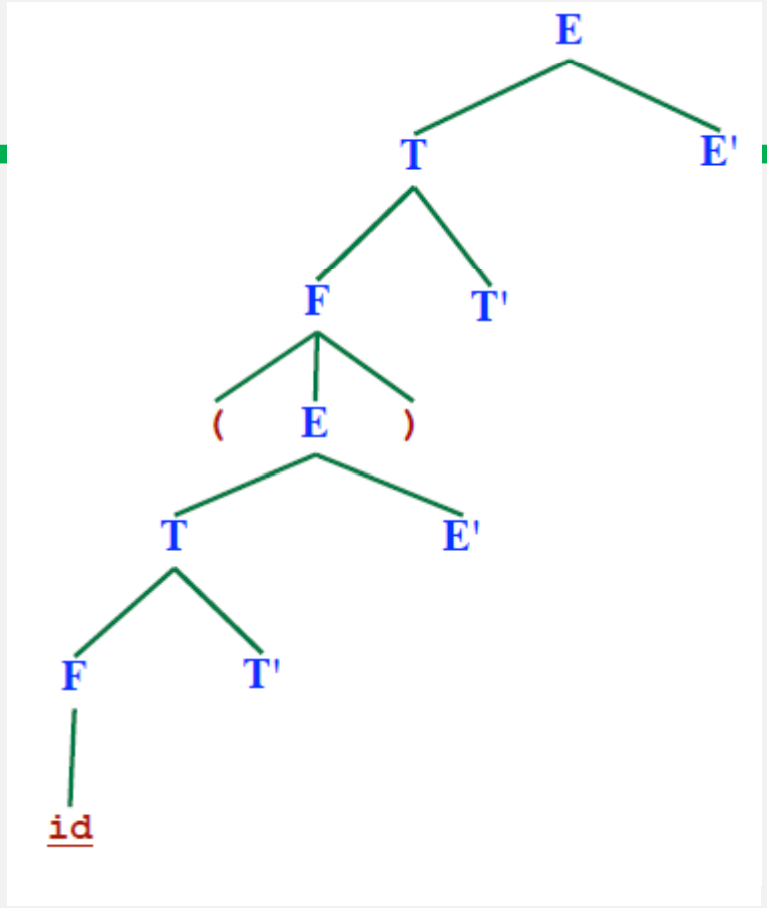
E → T E′
E′ → + T E′ | ε
T → F E′
T′ → * F T′ | ε
F → (E) | id

Predictive Parsing Progra

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT‘
F → id
T'→ ε
E'→ ε
T'→ ε
E′→ +TE‘
T → FT‘
F → id
T'→ ε
E'→ ε



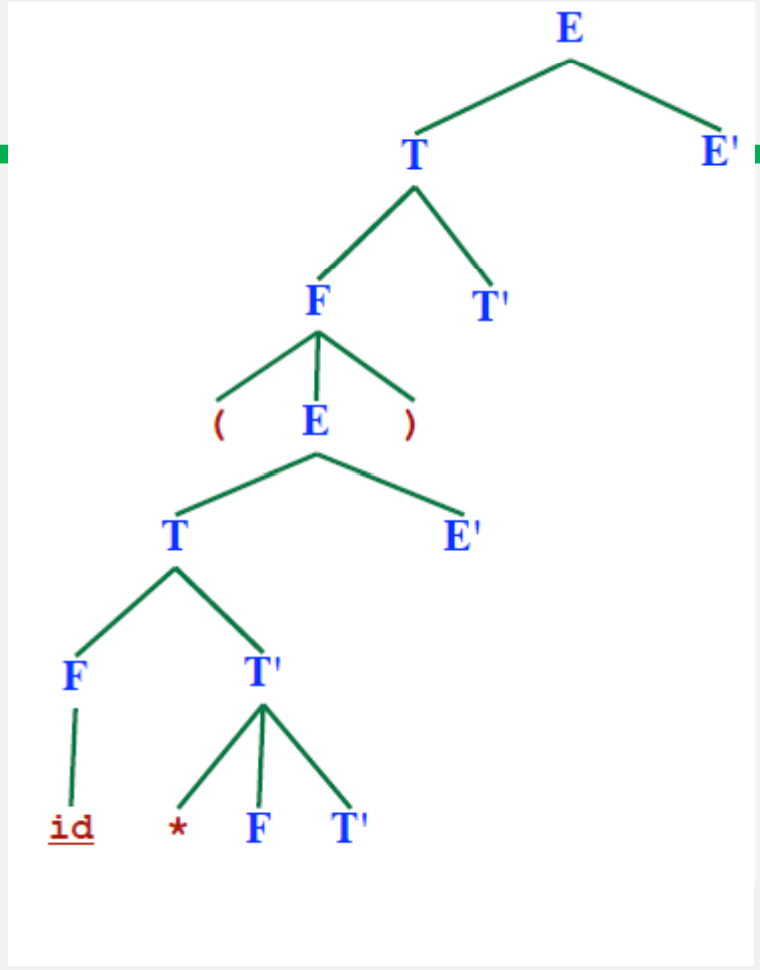
E → T E′
E′ → + T E′ | ε
T → F E′
T′ → * F T′ | ε
F → (E) | id

Predictive Parsing Progra

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT'
F → id
T'→ ε
E'→ ε
T'→ ε
E′→ +TE'
T → FT'
F → id
T'→ ε
E'→ ε



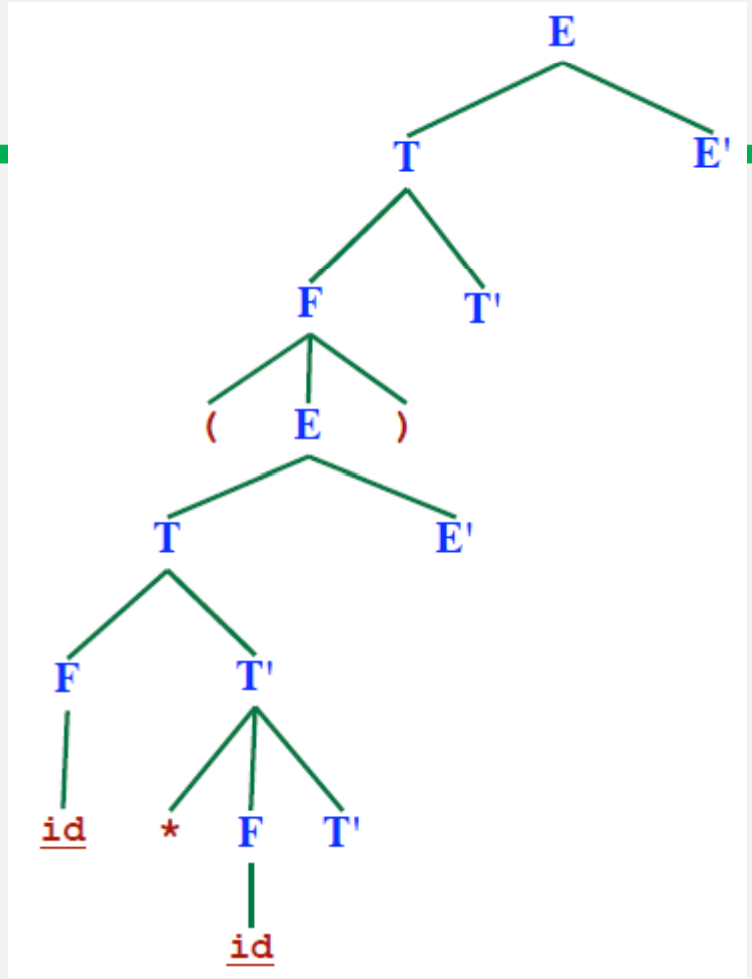
E → T E′
E′ → + T E′ | ε
T → F E′
T′ → * F T′ | ε
F → (E) | id

Predictive Parsing Progra

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT‘
F → id
T'→ ε
E'→ ε
T'→ ε
E′→ +TE‘
T → FT‘
F → id
T'→ ε
E'→ ε



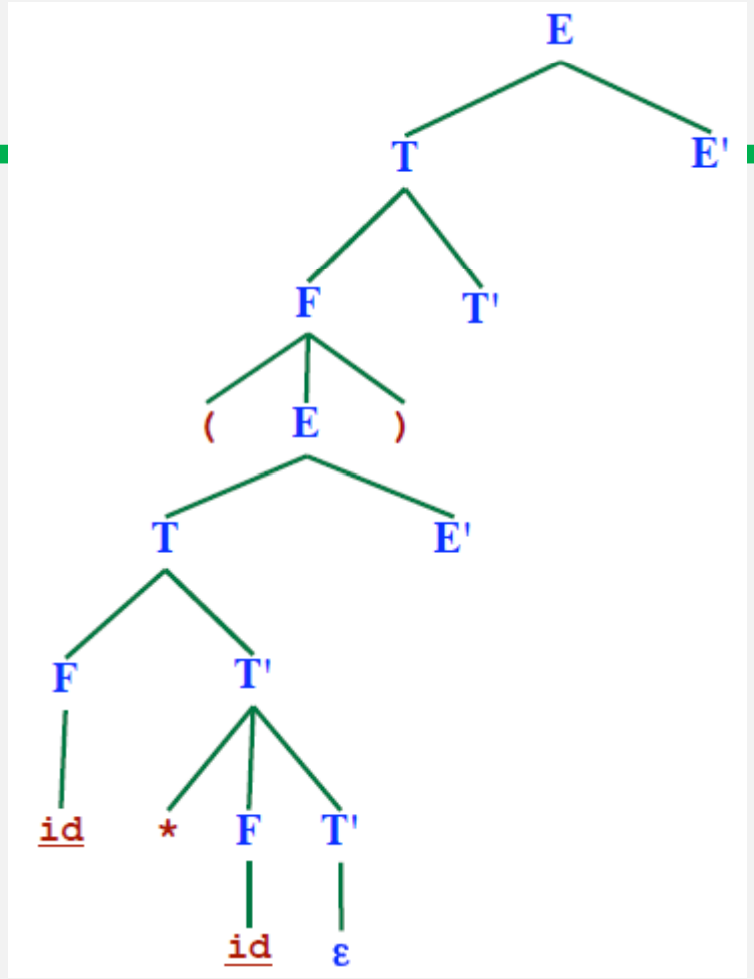
E → T E′
E′ → + T E′ | ε
T → F E′
T′ → * F T′ | ε
F → (E) | id

Predictive Parsing Progra

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT‘
F → id
T'→ ε
E'→ ε
T'→ ε
E′→ +TE‘
T → FT‘
F → id
T'→ ε
E'→ ε



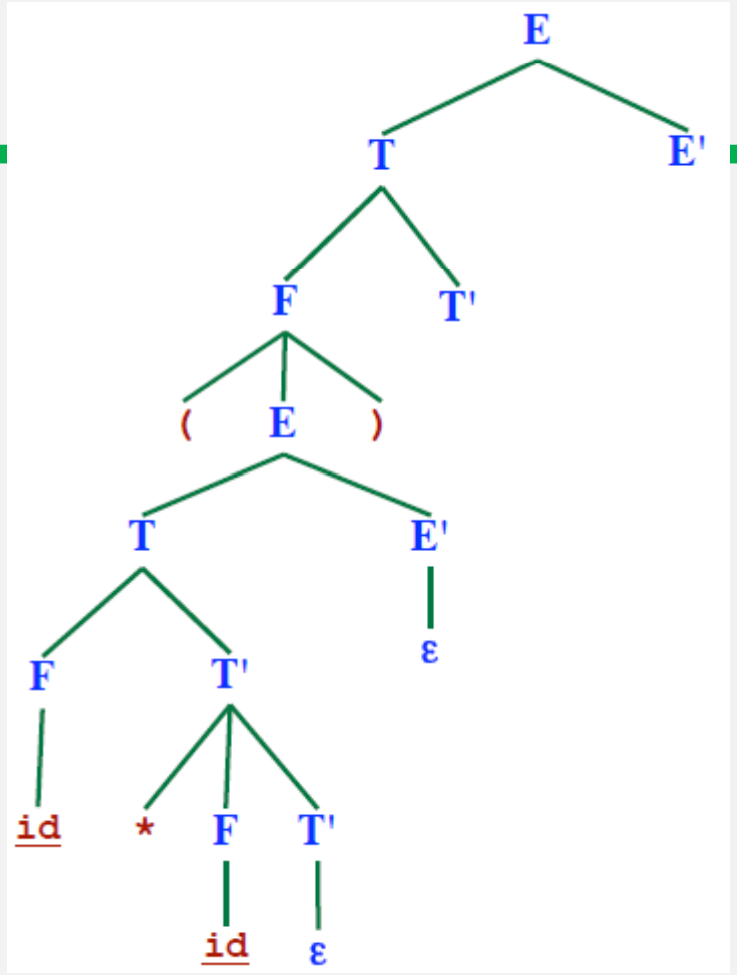
E → T E′
E′ → + T E′ | ε
T → F E′
T′ → * F T′ | ε
F → (E) | id

Predictive Parsing Progra

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT‘
F → id
T'→ ε
E'→ ε
T'→ ε
E′→ +TE‘
T → FT‘
F → id
T'→ ε
E'→ ε



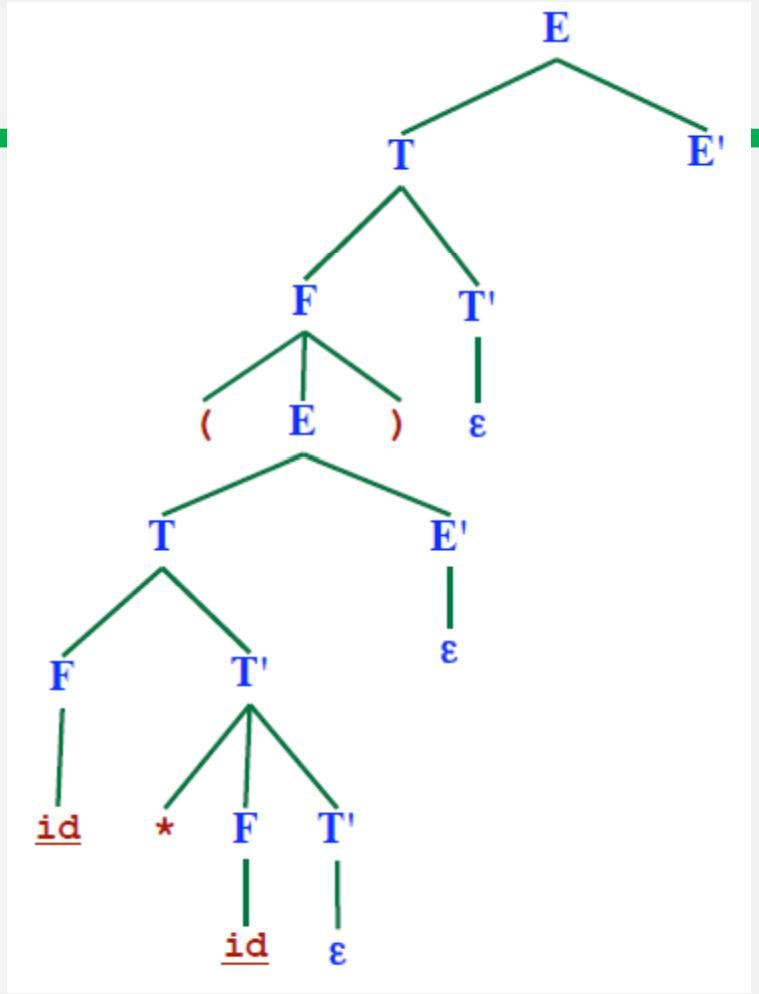
E → T E′
E′ → + T E′ | ε
T → F E′
T′ → * F T′ | ε
F → (E) | id

Predictive Parsing Progra

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT‘
F → id
T'→ ε
E'→ ε
T'→ ε
E′→ +TE‘
T → FT‘
F → id
T'→ ε
E'→ ε



E → T E′
E′ → + T E′ | ε
T → F E′
T′ → * F T′ | ε
F → (E) | id

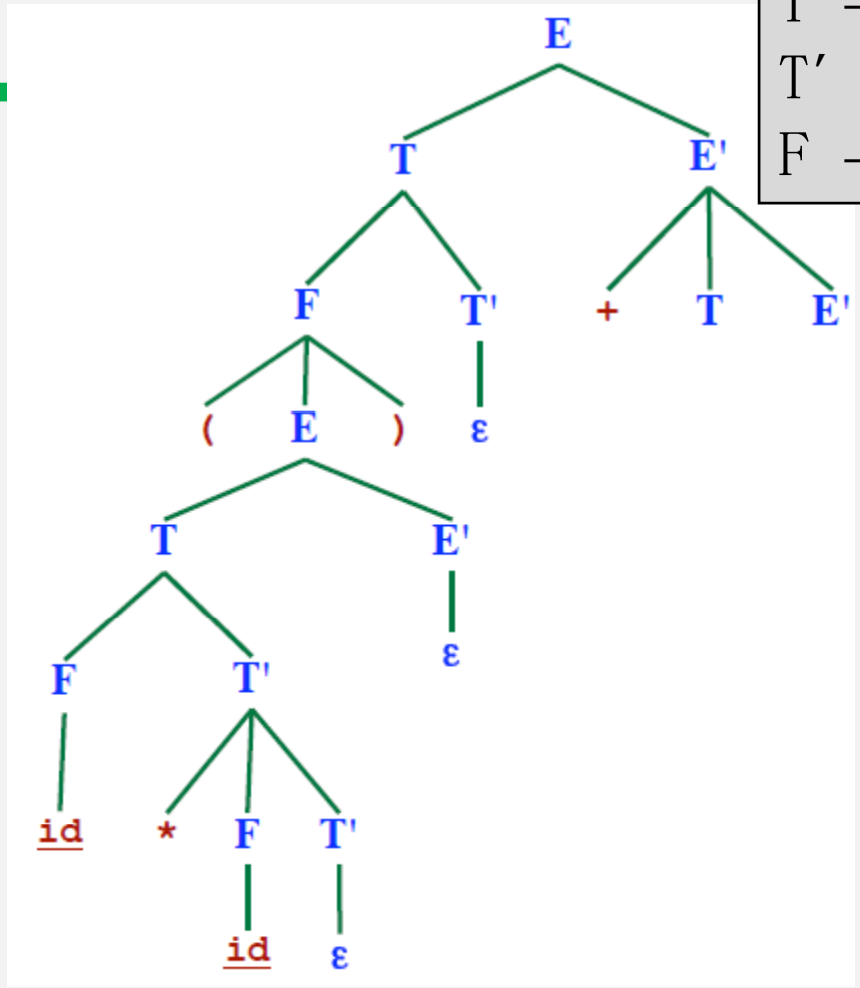
Predictive Parsing Progra

$E \rightarrow T\ E'$
$E' \rightarrow +\ T\ E' \mid \varepsilon$
$T \rightarrow F\ E'$
$T' \rightarrow *\ F\ T' \mid \varepsilon$
$F \rightarrow (\ E\ ) \mid id$

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT'
F → id
T'→ ε
E'→ ε
T'→ ε
E′→ +TE'
T → FT'
F → id
T'→ ε
E'→ ε



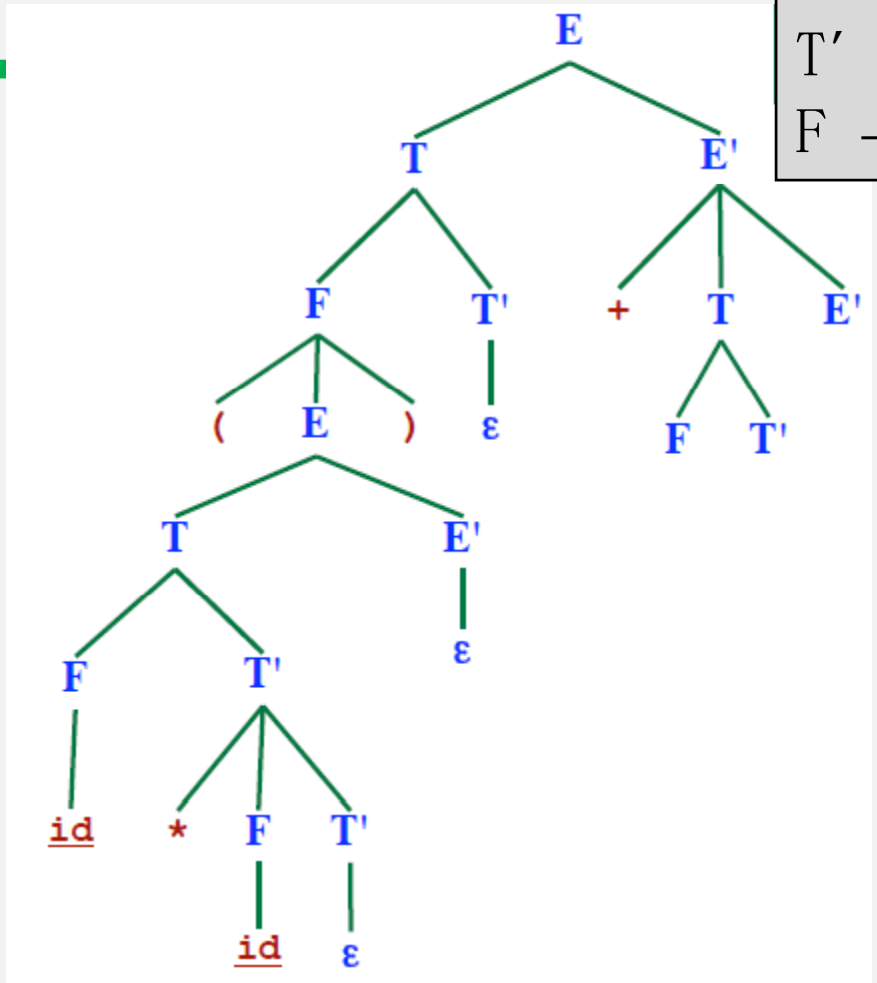
Predictive Parsing Progra

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT‘
F → id
T'→ ε
E'→ ε
T'→ ε
E′→ +TE‘
T → FT‘
F → id
T'→ ε
E'→ ε

E → T E′
E′ → + T E′ | ε
T → F E′
T′ → * F T′ | ε
F → (E) | id



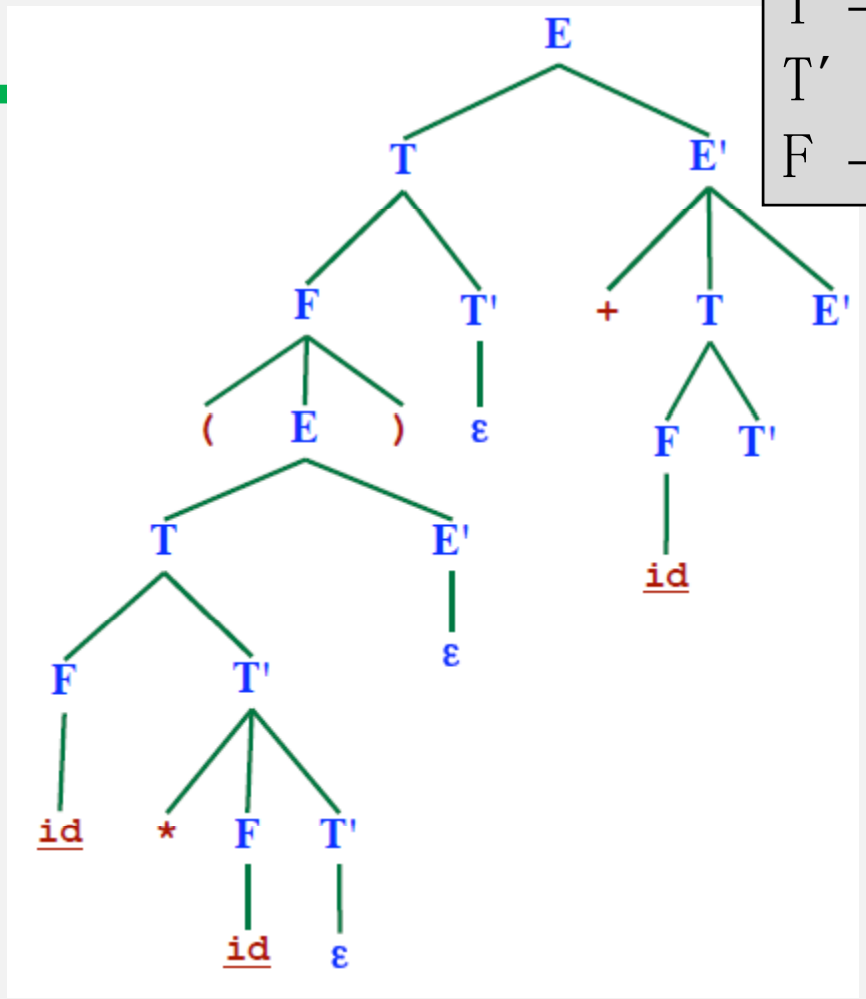
Predictive Parsing Progra

$E \rightarrow T\ E'$
$E' \rightarrow +\ T\ E' \mid \varepsilon$
$T \rightarrow F\ E'$
$T' \rightarrow *\ F\ T' \mid \varepsilon$
$F \rightarrow (\ E\ ) \mid id$

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT'
F → id
T'→ ε
E'→ ε
T'→ ε
E′→ +TE'
T → FT'
F → id
T'→ ε
E'→ ε



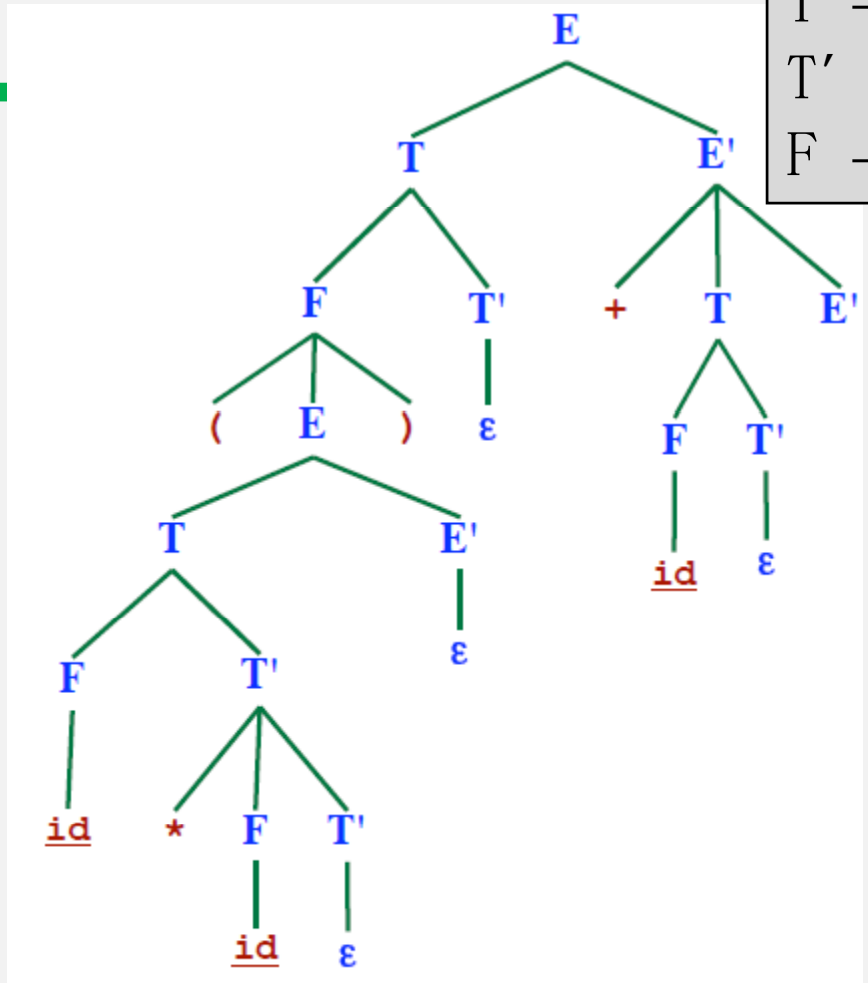
Predictive Parsing Progra

$E \rightarrow T\ E'$
$E' \rightarrow +\ T\ E' \mid \varepsilon$
$T \rightarrow F\ E'$
$T' \rightarrow *\ F\ T' \mid \varepsilon$
$F \rightarrow (\ E\ ) \mid id$

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT'
F → id
T'→ ε
E'→ ε
T'→ ε
E′→ +TE'
T → FT'
F → id
T'→ ε
E'→ ε



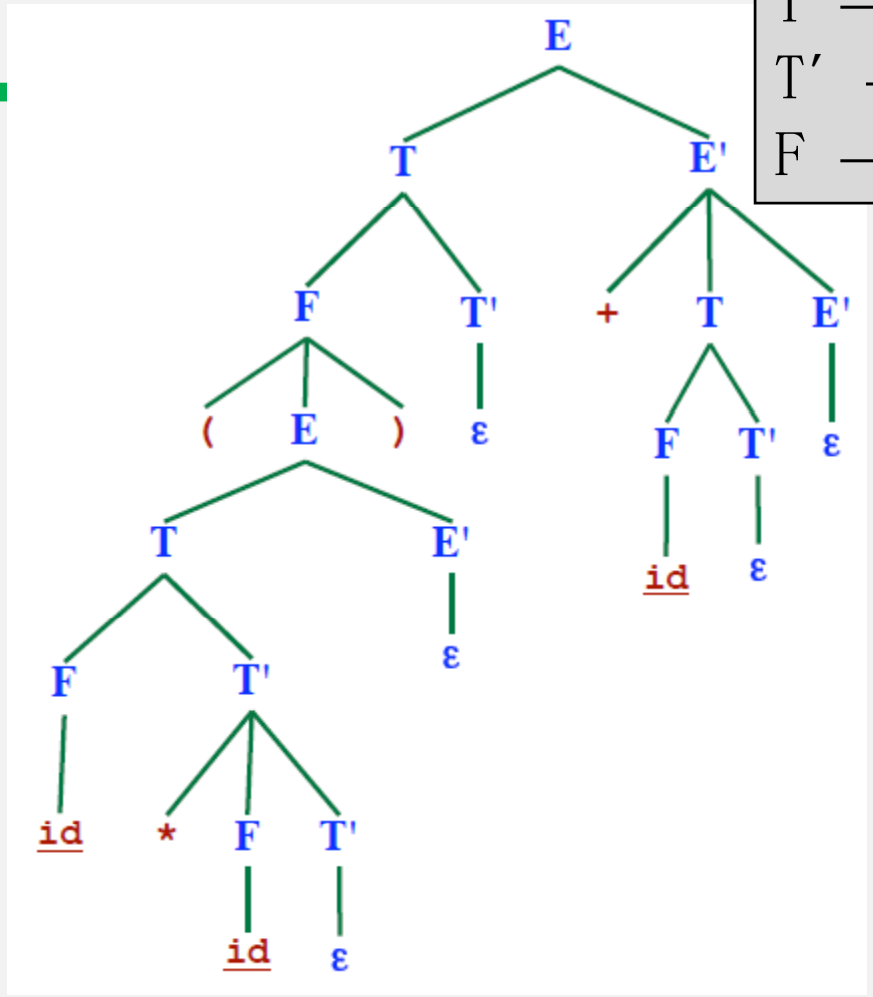
Predictive Parsing Progra

$E \rightarrow T\ E'$
$E' \rightarrow +\ T\ E' \mid \varepsilon$
$T \rightarrow F\ E'$
$T' \rightarrow *\ F\ T' \mid \varepsilon$
$F \rightarrow (\ E\ ) \mid id$

(id*id)+id

Output

E → T E′
T → F T'
F → (E)
E → T E'
T → FT'
F → id
T' → *FT'
F → id
T'→ ε
E'→ ε
T'→ ε
E′→ +TE'
T → FT'
F → id
T'→ ε
E'→ ε



Predictive Parsing Program

Output		Leftmost Derivation
E → T E’		E
T → F T'		T E'
F → (E)		F T' E'
E → T E'		(E) T' E'
T → FT'		(T E') T' E'
F → id		(F T' E') T' E'
T' → *FT‘		(id T' E') T' E'
F → id		(id * F T' E') T' E'
T'→ ε		(id * id T' E') T' E'
E'→ ε		(id * id E') T' E'
T'→ ε		(id * id) T' E'
E’→ +TE‘		(id * id) E'
T → FT‘		(id * id) + T E'
F → id		(id * id) + F T' E'
T'→ ε		(id * id) + id T' E'
E'→ ε		(id * id) + id E'
		(id * id) + id

Thank You