

Principles of Compiler Construction

Prof. Wen-jun LI

School of Computer Science and Engineering Inslwj@mail.sysu.edu.cn

Lecture 9. Semantic Analysis and Intermediate Code Generation

- 1. Introduction
- 2. Types and Declarations
- 3. Assignments and Expressions
- 4. Type Checking
- 5. Boolean Expressions
- Backpatching and Flow-of-Control Statements

1. Introduction

- Review
 - Front end vs. back end
 - o $m \times n$: m front ends and n back ends.
 - Interface between front ends and back ends
 - Intermediate representation
 - Why IR? Extendability and optimization.
 - Semantic (static) analysis
 - The most common analysis
 - Type checking
 - Other static checking
 - Unreachable code
 - Use of uninitialized variables
 - etc.

Static Checking

- Semantic analysis also focuses on the well-formness of source code
 - Due to the expressiveness power of Context-Free Grammars.
 - For example,
 - Number matching of actual parameters.
 - Context sensitive requirements cannot be specified using a context free grammar.
 - o break statement must be in a loop or switch.
 - Requires a complicated and unnatural context free grammar.

Intermediate Representation

- High level intermediate representations
 - AST and DAG
 - Suitable for tasks like static type checking
- Low level intermediate representations
 - 3-address code: x = y op z
 - Suitable for machine-dependent tasks, such as register allocation and instruction selection.
- IR choice/design are application specific
 - C language is commonly used (AT&T Bell Lab Advanced C++)

Three-Address Code

Compiler-generated temporary variables

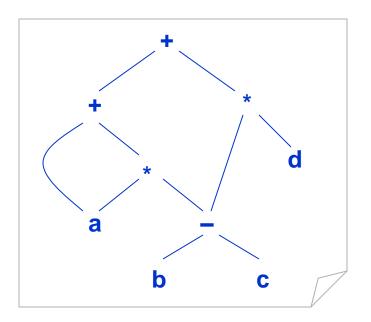
•
$$t_1 = y * z$$

 $t_2 = x + t_1$

An example

•
$$t_1 = b - c$$

 $t_2 = a * t_1$
 $t_3 = a + t_2$
 $t_4 = t_1 * d$
 $t_5 = t_3 + t_4$



Addresses

- Addresses in 3-address code
 - Name (variables in source code)
 - May be implemented as a pointer or reference to its entry in the symbol table.
 - Constant
 - Type conversions must be considered.
 - Compiler-generated temporary
 - Useful for optimization.
 - Register allocation.

Instructions

Common 3-address instructions

```
• x = y op z // arithmetic and logical
 x = op y // negation and conversion
                // copy
  x = y
goto L // unconditional jump
 if x goto L // conditional jump
  ifFalse x goto L // conditional jump
  if x op y goto L // relational operation

    param x<sub>1</sub> // parameter passing

  param X<sub>2</sub>
  param X<sub>n</sub>
          // procedure call
  call p, n
  y = call p, n // function call
  return y // return a value
```

Instructions (cont')

Common 3-address instructions

```
x = y[i] // indexed copy, i is the offset
x[i] = y
x = &y // address and pointer assignment
x = *y
*x = y
```

Three-Address Code: Example

Source code

```
• do i = i + 1;
while (a[i] < v);</pre>
```

Translation to 3-address code (symbolic labels)

```
• L: t_1 = i + 1

i = t_1

t_2 = i * 8

t_3 = a[t_2]

if t_3 < v goto L
```

Another translation form (position numbers)

```
• 100: t_1 = i + 1

101: i = t_1

102: t_2 = i * 8

103: t_3 = a[t_2]

104: if t_3 < v goto 100
```

Implementations of Three-Address Code

- Quadruples (quads)
 - Pros and cons?
- Triples
 - Pros and cons?
- Indirect triples
 - Pros and cons?

Space consuming Flexibility to optimizations

1) Quadruples

- Source code
 - a = b * c + b * c
- Three-address code

•
$$t_1 = minus c$$

 $t_2 = b * t_1$
 $t_3 = minus c$
 $t_4 = b * t_3$
 $t_5 = t_2 + t_4$
 $a = t_5$

Quads

	ор	arg ₁	arg ₂	result
0	minus	С		t_1
1	*	b	t_1	t_2
2	minus	С		t_3
3	*	b	t_3	$t_{\scriptscriptstyle{4}}$
4	+	t_2	$t_{\scriptscriptstyle{4}}$	$t_{\scriptscriptstyle{5}}$
5		$t_{\scriptscriptstyle{5}}$		а
	•••			

2) Triples

Three-address code

•
$$t_1 = minus c$$

 $t_2 = b * t_1$
 $t_3 = minus c$
 $t_4 = b * t_3$
 $t_5 = t_2 + t_4$
 $a = t_5$

	ор	arg ₁	arg ₂
0	minus	С	
1	*	b	(0)
2	minus	С	
3	*	b	(2)
4	+	(1)	(3)
5	II	а	(4)
:			

3) Indirect Triples

Three-address code

•
$$t_1 = minus c$$

 $t_2 = b * t_1$
 $t_3 = minus c$
 $t_4 = b * t_3$
 $t_5 = t_2 + t_4$
 $a = t_5$

(0)
(1)
(2)
(3)
(4)
(5)

	ор	arg ₁	arg ₂
0	minus	С	
1	*	b	(0)
2	minus	С	
3	*	b	(2)
4	+	(1)	(3)
5	II	а	(4)

In Java, array of instruction objects

2. Types and Declarations

- Declaration
 - Literals: implicitly
 - Variables: explicitly
 - Other names: explicitly
- Type checking in strong-typing languages
 - Type compatibility
 - Type inference
 - Implicit type conversion
 - Resolving overloading operators

Simplified Grammar

Declare only one name at a time

```
D \rightarrow T id; D | \epsilon
T \rightarrow B C | record { D }
B \rightarrow int | double
C \rightarrow [ num ] C | \epsilon
```

Translation of Type Declarations

Computing types and their widths

```
T \rightarrow B { t = B.type; w = B.width }

C { T.type = C.type; T.width = C.width }

B \rightarrow int { B.type = INTEGER; B.width = 4 }

B \rightarrow double { B.type = DOUBLE; B.width = 8 }

C \rightarrow [ num ] C<sub>1</sub> { C.type = array(num.value, C<sub>1</sub>.type);

C.width = num.value \times C<sub>1</sub>.width }

C \rightarrow \varepsilon { C.type = t; C.width = w }
```

Just try it: int[2][3] What is T.type and T.width?

Type expression

Translation of Type Declarations (cont')

Computing relative addresses

```
\begin{array}{c} P \to \\ D \end{array} \hspace{0.5cm} \{ \hspace{0.5cm} \text{offset} = 0 \hspace{0.5cm} \} \hspace{0.5cm} \text{top denotes the } \\ \text{current symbol table} \end{array} D \to T \hspace{0.5cm} \text{id} \hspace{0.5cm} ; \hspace{0.5cm} \text{offset} \hspace{0.5cm} += T. \text{width} \hspace{0.5cm} \} D \to \epsilon D \to \epsilon Embedded \hspace{0.5cm} \text{actions can be } \\ \text{removed with markers} \end{array}
```

Another Example

Enter types and their widths

Just try it: **k: array [5] of ^real**What are the side effects?

Another Example (cont')

Declarations in nested procedures

```
{ tableStack.push(new Table(null));
                  offsetStack.push(0) }
                 { addWidth(tableStack.top(), offsetStack.top());
      D
                  tableStack.pop();
                  offsetStack.pop() }
D \rightarrow D; D
D → proc id; { tableStack.push(new Table(tableStack.top()));
                  offsetStack.push(0) }
      D_1; S
                { addWidth(tableStack.top(), offsetStack.top());
                  tableStack.pop();
                  offsetStack.pop();
                  tableStack.top().enter(id.name, tableStack.top() }
D \rightarrow id : T
                 { tableStack.top().enter(id.name, T.type, offsetStack.top());
                  offsetStack.top() += T.width }
```

Another Example (cont')

Field names in records

3. Assignments and Expressions

- Intermediate code generation
 - Code concatenation

```
o gen(...)
```

- 0
- No side effects
- Incremental generation

```
DBv1: emit(...)
```

- DBv2: overloading gen(...)
- Side effects

Translation of Expressions

Code concatenation (syntax-directed definition)

	Productions	Semantic Rules
1	$S \rightarrow id = E;$	S.code = E.code gen(top.get(id .lexeme) '=' E.addr)
2	$E \to E_1 + E_2$	E.addr = new Temp(); E.code = E_1 .code E_2 .code gen(E.addr '=' E_1 .addr '+' E_2 .addr)
3	$E \rightarrow - E_1$	E.addr = new Temp(); E.code = E_1 .code gen(E.addr '=' ' minus ' E_1 .addr)
4	$E \to (E_1)$	$E.addr = E_1.addr;$ $E.code = E_1.code$
5	E → id	E.addr = top.get(id .lexeme); E.code = ' '

Translation of Expressions (cont')

Incremental translation (translation scheme)

Another Example

Declared variables

```
S \rightarrow id := E; { p = symbolTable.lookup(id.name);
                       if (p == null) throw new SomeException();
                       emit(p '=' E.place) }
E \rightarrow E_1 + E_2 { E.place = new Temp();
                       emit(E.place '=' E<sub>1</sub>.place '+' E<sub>2</sub>.place) }
\mathsf{E} \rightarrow -\mathsf{E}_1 { E.place = new Temp();
                       emit(E.place '=' 'minus' E<sub>1</sub>.place) }
E \rightarrow (E_1) { E.place = E_1.place }
\mathsf{E} \to \mathsf{id}
                     { p = symbolTable.lookup(id.name);
                       if (p == null) throw new SomeException();
                       E.place = p }
```

Addressing Array Elements

- 2-dimensional array layout
 - Row major vs. column major

		A[1, 1]
1st row	$\left\{ \right.$	A[1, 2]
		A[1, 3]
		A[2, 1]
2nd row	, {	A[2, 2]
		A[2, 3]

1st column {	A[1, 1]
	A[2, 1]
2nd column {	A[1, 2]
	A[2, 2]
3rd column {	A[1, 3]
	A[2, 3]

Addressing Array Elements

- Relative address of array elements
 - A[i]

```
    base + (i - low) × w
    i × w + (base - low × w)

Constant for optimization
```

A[i₁, i₂]

```
o base + ((i_1 - low_1) \times n_2 + i_2 - low_2) \times w
```

$$\circ ((i_1 \times n_2) + i_2) \times w + (base - (low_1 \times n_2 + low_2) \times w)$$

A[i₁, i₂, ..., i_k]

o
$$((...((i_1 \times n_2 + i_2) \times n_3 + i_3)...) \times n_k + i_k) \times w + base - ((...((low_1 \times n_2 + low_2) \times n_3 + low_3)...) \times n_k + low_k) \times w$$

Addressing Tips

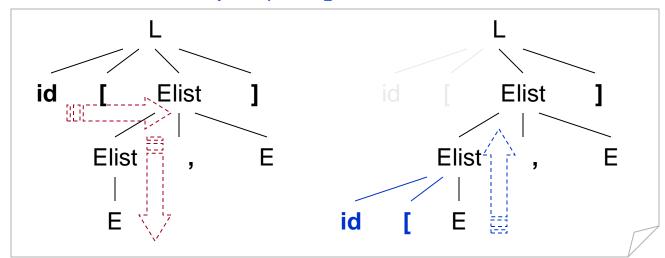
 For each increment of a new dimension, addressing is calculated recursively, e.g. from k to k + 1

```
• For variable part V: V \times n_{k+1} + i_{k+1}
```

• For constant part C: $C \times n_{k+1} + low_{k+1}$

Grammar for Array References

- Array references in Pascal: a[2, 3]
 - L \rightarrow id [Elist] | id
 - Elist \rightarrow Elist, E | E
- Grammar transformation (why?)
 - L \rightarrow Elist] | id
 - Elist → Elist, E | id [E



Translation Scheme

Addressing array elements in Pascal

```
(1) S \rightarrow L := E { if (L.offset == null) emit(L.place '=' E.place)
                       else emit(L.place '[' L.offset ']' '=' E.place) }
(2) E \rightarrow E_1 + E_2 { E.place = new Temp();
                       emit(E.place '=' E_1.place '+' E_2.place) }
(3) E \rightarrow (E_1) { E.place = E_1.place }
(4) E \rightarrow L
                    { if (L.offset == null) E.place = L.place
                       else {
                           E.place = new Temp();
                           emit(E.place '=' L.place '[' L.offset ']')
                       } }
(5) L \rightarrow Elist
                     { L.place = new Temp();
                       emit(L.place '=' constant(Elist.array));
                       L.offset = new Temp();
                       emit(L.offset '=' Elist.place '*' width(Elist.array) }
(6) L \rightarrow id
                     { L.place = id.place;
                       L.offset = null }
                                                         L.place = base - C * w
                                                            L.offset = \vee * w
```

L is a simple id (if L.offset is null) or an array reference

Translation Scheme (cont')

Addressing array elements in Pascal (cont')

```
(7) Elist \rightarrow Elist<sub>1</sub>, E { t = new Temp();
                               m = Elist_1.ndim + 1;
                               emit(t '=' Elist<sub>1</sub>.place '*' limit(Elist<sub>1</sub>.array, m));
                               emit(t '+=' E.place);
                               Elist.array = Elist<sub>1</sub>.array;
                               Elist.place = t;
                               Elist.ndim = m }
(8) Elist \rightarrow id [ E { Elist.array = id.place;
                               Elist.place = E.place;
                               Elist.ndim = 1 }
                                                                   Elist.array = base
```

Elist.place = V **Elist.ndim** = dimensions

Another Translation Scheme

- Array references in C/C++: a[2][3]
 - For all n, $low_n = 0$
 - Addressing formula
 - A[i]
 - base + i × w
 - A[i₁][i₂]
 - base + $i_1 \times w_1 + i_2 \times w_2$
 - w₁ is the width of a row
 - w₂ is the width of an element in a row
 - A[i₁][i₂]...[i_k]
 - base + $i_1 \times w_1 + i_2 \times w_2 + ... + i_k \times w_k$

Java does NOT use row-major storage for arrays

Another Translation Scheme (cont')

Translation scheme

```
S \rightarrow id = E; { gen(top.get(id.lexeme) '=' E.addr) }
               S \rightarrow L = E; { gen(L.array.base '[' L.addr ']' '=' E.addr) }
               E \rightarrow E_1 + E_2 { E.addr = new Temp();
                                       gen(E.addr '=' E_1.addr '+' E_2.addr) }
              \mathsf{E} \rightarrow \mathsf{id} { E.addr = top.get(\mathsf{id}.lexeme) }
               \mathsf{E} \to \mathsf{L}
                                   { E.addr = new Temp();
                                       gen(E.addr '=' L.array.base '[' L.addr ']') }
               L \rightarrow id [E] { L.array = top.get(id.lexeme);
                                       L.type = L.array.type.element;
                                       L.addr = new Temp();
                                       gen(L.addr '=' E.addr '*' L.type.width) }
               L \rightarrow L_1 [ E ] { L.array = L_1.array;
                                       L.type = L_1.type.element;
                                       t = new Temp();
L only for array reference
                                       L.addr = new Temp();
   E.addr = E.place
 L.array.base = L.place
                                       gen(t '=' E.addr '*' L.type.width);
    L.addr = L.offset
                                       gen(L.addr '=' L_1.addr '+' t) }
```

4. Type Checking

- Strong typing vs. weak typing
 - Strongness is relative
- Type definitions
 - Primitive types: enumeration of constant
 - Composite types: type expressions
 - Type of functions: signatures
 - if f has type s → t and x has type s
 then expression f(x) has type t

Translation Scheme: An Example

Type checking, inference and implicit casting

```
E \rightarrow E_1 * E_2  { E.place := new Temp();
                  if (E_1.type == TK_INT \&\& E_2.type == TK_INT) {
                     emit(E.place '=' E_1.place '*<sub>int</sub>' E_2.place);
                     E.type = TK_INT;
                  } elsif (E_1.type == TK_REAL && E_2.type == TK_REAL) {
                     emit(E.place '=' E_1.place '*<sub>real</sub>' E_2.place);
                     E.type = TK REAL;
                  } elsif (E_1.type == TK_INT && E_2.type == TK_REAL) {
                     t := new Temp();
                     emit(t '=' 'int2real' E<sub>1</sub>.place);
                     emit(E.place '=' t '*<sub>real</sub>' E<sub>2</sub>.place);
                     E.type = TK REAL;
                  } elsif (...) { ... }
```

5. Boolean Expressions

- Boolean expressions are used in
 - Flows of control
 - Computing logical values

Computing Logical Values

a < b equals to if (a < b) then 1 else 0

```
E \rightarrow E_1 \text{ or } E_2 { E.place = new Temp();
                            emit(E.place '=' E_1.place 'or' E_2.place) }
E \rightarrow E_1 and E_2 { E.place = new Temp();
                            emit(E.place '=' E_1.place 'and' E_2.place) }
E \rightarrow not E_1 { E.place = new Temp();
                            emit(E.place '=' 'not' E<sub>1</sub>.place) }
E \rightarrow (E_1) { E.place = E_1.place }
E \rightarrow id_1 relop id_2  { E.place = new Temp();
                            emit('if' id<sub>1</sub>.place relop.op id<sub>2</sub>.place 'goto' currentStmt+3);
                            emit(E.place '=' '0');
                            emit('goto' currentStmt+2);
                            emit(E.place '=' '1') }
\mathsf{E} \rightarrow \mathsf{true}
                         { E.place = new Temp();
                            emit(E.place '=' '1') }
\mathsf{E} \to \mathsf{false}
                         { E.place = new Temp();
                            emit(E.place '=' '0') }
```

Computing Logical Values: An Example

- Source code
 - a < b or c < d and e < f
- Intermediate code

```
100: if a < b goto 103
                               108: if e < f goto 111
                                    t_3 = 0
101: t_1 = 0
                               109:
                               110: goto 112
102: goto 104
103: t_1 = 1
                               111: t_3 = 1
                               112: t_4 = t_2 and t_3
104: if c < d goto 107
                               113: t_5 = t_1 \text{ or } t_4
105: t_2 = 0
                               114: ...
106: goto 108
107: t_2 = 1
```

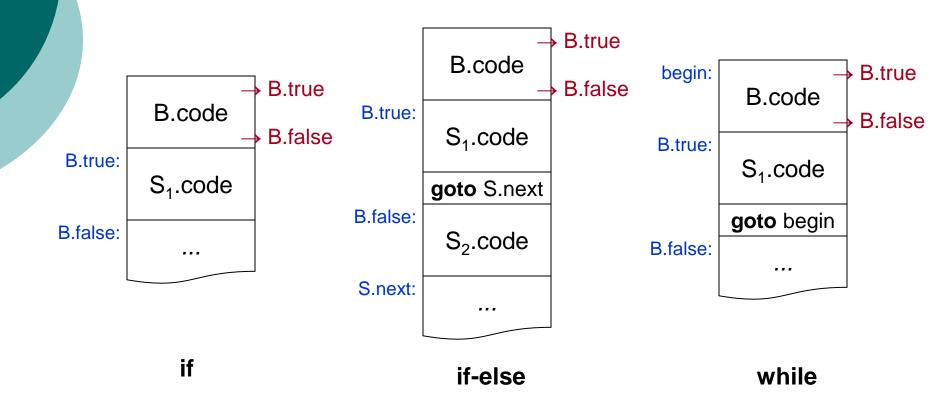
Short-Circuit Evaluation

Flow-of-Control Statements

```
• S \rightarrow if ( B ) S<sub>1</sub>
• S \rightarrow if ( B ) S<sub>1</sub> else S<sub>2</sub>
• S \rightarrow while ( B ) S<sub>1</sub>
```

- Short-circuit evaluation for && and | |
 - For higher evaluation efficiency
 - And ...

Generated Code Illustration



Syntax-Directed Definition for Flow-of-Control Statements

Productions	Semantic Rules	S.next come from?	
$P \rightarrow S$	S.next = new Label();		
	P.code = S.code label(S.next)		
S → assign	S.code = assign .code		
$S \rightarrow S_1$	$S_1.next = new Label();$		
S_2	S_2 .next = S.next;		
	$S.code = S_1.code \mid \mid label(S_1.next) \mid \mid S_2.code$		
$S \rightarrow \mathbf{if} (B) S_1$	B.true = new Label();		
	B.false = S_1 .next = S.next;		
	S.code = B.code label(B.true) S1.code		
$S \rightarrow if(B)S_1$	B.true = new Label();		
else S ₂	B.false = new Label();		
	$S_1.next = S_2.next = S.next;$		
	S.code = B.code label(B.true) S_1 .code gen(' goto ' S.next) label(B.false) S_1	S ₂ .code	
$S \rightarrow $ while (B)	begin = new Label();	A	
S_1	B.true = new Label();	Avoid redundant goto s	
	B.false = S.next;	gotos	
	$S_1.next = begin;$		
	S.code = label(begin) B.code label(B.true) S_1 .code gen('goto' begin)		

Where does

Syntax-Directed Definition for Booleans

Productions	Semantic Rules	
$B \rightarrow B_1 \mid \mid B_2$	B_1 .true = B.true; B_1 .false = new Label();	Short-Circuit Evaluation
	B_2 .true = B.true; B_2 .false = B.false; $B.code = B_1.code label(B_1.false) B_2.code$	
$B \rightarrow B_1 \&\& B_2$	B ₁ .true = new Label(); B ₁ .false = B.false; B ₂ .true = B.true; B ₂ .false = B.false; B.code = B ₁ .code label(B ₁ .true) B ₂ .code	
$B \to ! \; B_1$	B_1 .true = B.false; B_1 .false = B.true; B .code = B_1 .code	
$B \rightarrow E_1 \text{ relop } E_2$	B.code = E_1 .code E_2 .code gen(' if ' E_1 .addr relop .op E_2 .addr gen(' goto ' B.false)	' goto ' B.true)
B → true	B.code = gen('goto' B.true)	
B → false	B.code = gen('goto' B.false)	

Syntax-Directed Translation: An Example

- Source code
 - if $(x < 100 \mid | x > 200 \&\& x != y) x = 0$
- Intermediate code

6. Backpatching and Flow-of-Control Statements

- In SDD for Flow-of-Control Statements
 - Where does S.next come from?
 - Only after all intermediate code are generated, can S.next be computed.
- In SDD for Booleans
 - Where do B.true and B.false come from?
 - Must be provided by the context of the boolean expressions.
 - The context depends on the result of S.next.

Design Motivation and Solution

- Motivation
 - One-pass code generation
- Solution
 - Using backpatching
- It is a general approach to dealing with initial values which must be computed at the end.

Backpatching for Boolean Expressions

Translation scheme

```
B \rightarrow B_1 \mid M \mid B_2
                              { backpatch(B<sub>1</sub>.falseList, M.instruction);
                                B.trueList = merge(B_1.trueList, B_2.trueList);
                                B.falseList = B_2.falseList; }
                              { backpatch(B<sub>1</sub>.trueList, M.instruction);
B \rightarrow B_1 && M B_2
                                B.trueList = B_2.trueList;
                                B.falseList = merge(B_1.falseList, B_2.falseList); 
B \rightarrow ! B_1
                              { B.trueList = B₁.falseList;
                                B.falseList = B_1.trueList; 
B \rightarrow (B_1)
                              { B.trueList = B₁.trueList;
                                B.falseList = B_1.falseList; }
B \rightarrow E_1 \text{ relop } E_2
                              { B.trueList = new List(nextInstruction);
                                B.falseList = new List(nextInstruction + 1);
                                emit('if' E<sub>1</sub>.addr relop.op E<sub>2</sub>.addr 'goto __');
                                emit('goto ___'); }
                              { B.trueList = new List(nextInstruction);
B \rightarrow true
                                emit('goto '); }
B \rightarrow false
                              { B.falseList = new List(nextInstruction);
                                emit('goto '); }
                              { M.instruction = nextInstruction; }
M \rightarrow \epsilon
```

Backpatching for Flow-of-Control Statements

Translation scheme

```
S \rightarrow if (B) M S_1 \{ backpatch(B.trueList, M.instruction); \}
                          S.nextList = merge(B.falseList, S_1.nextList); 
S \rightarrow if (B) M_1 S_1 N else M_2 S_2
                       { backpatch(B.trueList, M<sub>1</sub>.instruction);
                          backpatch(B.falseList, M<sub>2</sub>.instruction);
                          S.nextList = merge(S_1.nextList, N.nextList, S_2.nextList); }
S \rightarrow  while M_1 (B) M_2 S_1
                       { backpatch(B.trueList, M<sub>2</sub>.instruction);
                          backpatch(S<sub>1</sub>.nextList, M<sub>1</sub>.instruction);
                          S.nextList = B.falseList;
                          emit('goto' M<sub>1</sub>.instruction); }
S \rightarrow \{L\} { S.nextList = L.nextList; }
S \rightarrow A; { S.nextList = new List(); // Assignment or Atom }
M \rightarrow \epsilon
                      { M.instruction = nextInstruction; }
N \rightarrow \epsilon
                       { N.nextList = new List(nextInstruction);
                          emit('goto '); }
L \rightarrow L_1 M S
                       { backpatch(L<sub>1</sub>.nextList, M.instruction);
                          L.nextList = S.nextList; }
L \rightarrow S
                       { L.nextList = S.nextList; }
```

Exercise 9.1

- What is the translation result of input token string: x := A[y, z]?
 - Tips: use the translation scheme for Pascal.

DBv1, pp.486

Exercise 9.2

- What is the translation result of input token string: c + a[i][j]?
 - Tips: use the translation scheme for C/C++.

DBv2, pp.385

Exercise 9.3

- What is the translation result of input token string: x < 100 || x > 200 && x != y?
 - Tips: use the translation scheme for boolean expressions with backpatching.
 - Suppose that the start position of the generated code is 100.

DBv2, pp.412-414

Further Reading

- Dragon Book, 2nd Edition (DBv2)
 - Comprehensive Reading:
 - Section 6.2 on introduction to intermediate representations.
 - Section 6.5 on type checking.
 - Section 6.3, 6.4, 6.6 and 6.7 on translations of various program constructs.
 - Skip Reading:
 - Section 6.1 on AST and DAG.
 - Section 6.8 and 6.9 on translations of switches and procedures.

Enjoy the Course!

