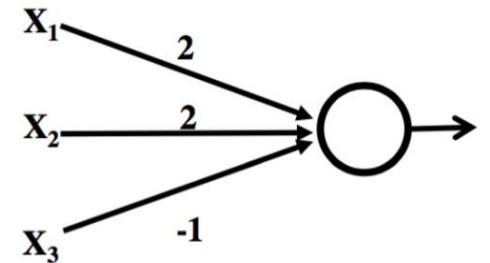


# **Neural Networks**

# **Fundamentals of AI (AE1FAI)**

Slides created by Dr Rong Qu & Dr John Drake  
Modified by Dr Huan Jin

# NEURAL NETWORKS



**McCulloch & Pitts** (1943) are generally recognised as the designers of the first neural network

- Many **simple units combine** to give an increased computational power
- The idea of a **threshold**
- Many of their ideas still used today

**Hebb** (1949) developed the **first learning rule**

- McCulloch & Pitts network has **fixed weights**
- If two neurons were active at the same time the strength between them should be increased

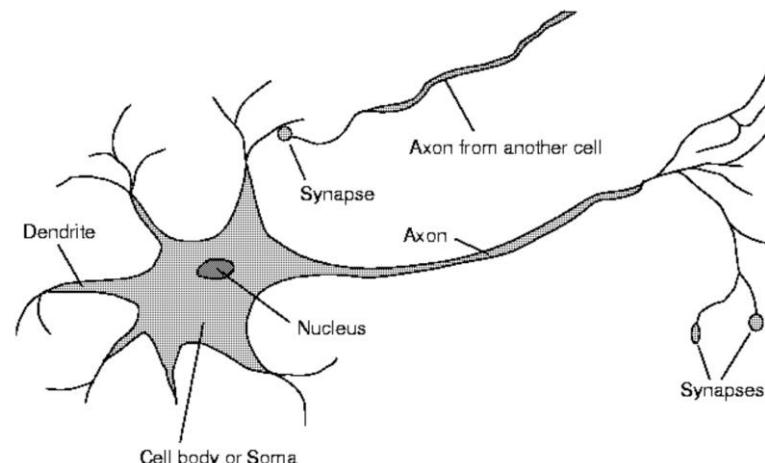
# NEURAL NETWORKS

During the 50's and 60's

- Many researchers worked on the **perceptron**, leading to great excitement
- This model can be proved to converge to the correct weights: learning → thinking
- More powerful learning algorithm than Hebb

1969 saw the death of neural network research

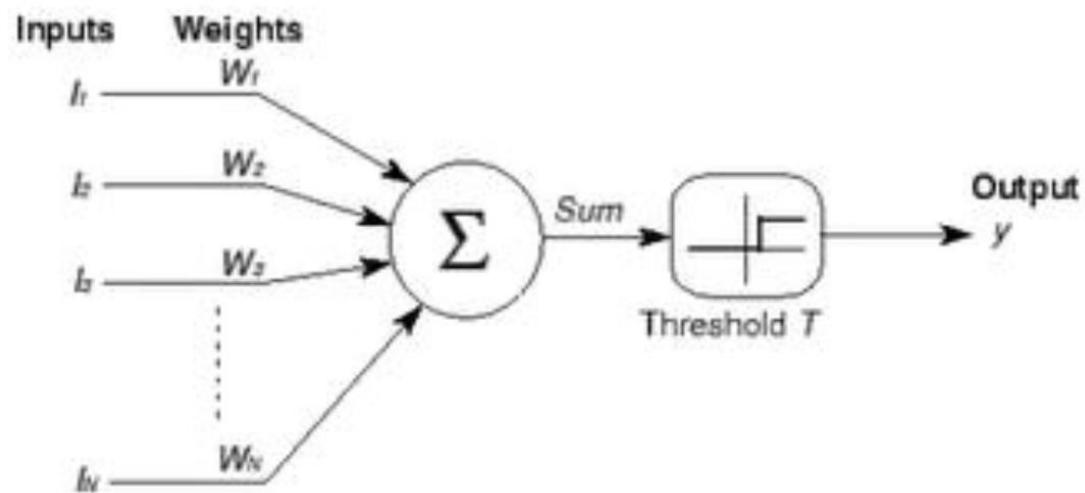
- **Minsky & Papert**
- Perceptron can't learn certain type of important functions
- Research of ANN went to decline for about 15 years



# THE FIRST NEURAL NETWORKS

McCulloch and Pitts produced the first neural network in 1943

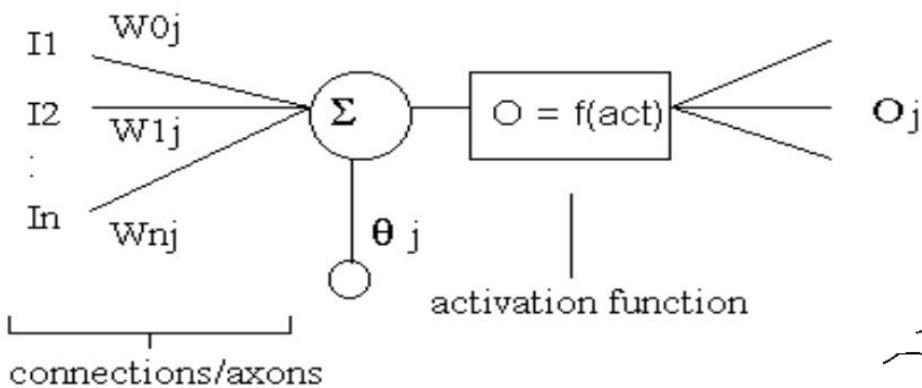
Many of the principles can still be seen in neural networks of today



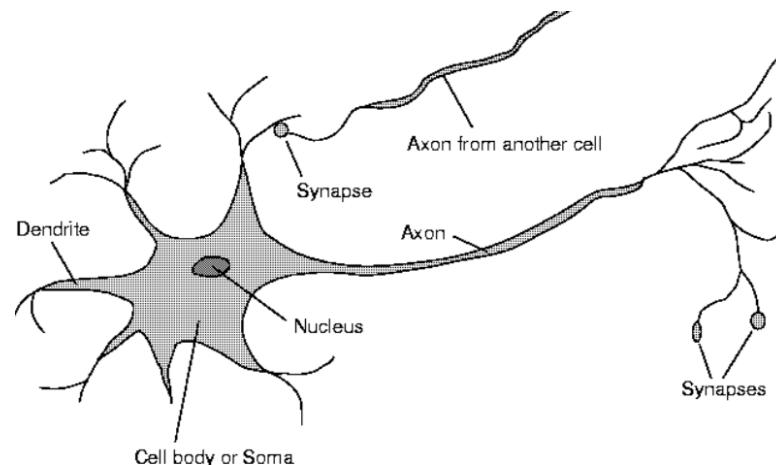
# THE FIRST NEURAL NETWORKS

Consists of:

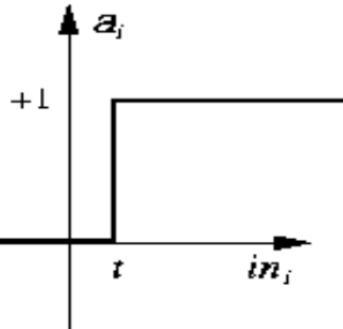
- A set of inputs - (**dendrites**)
- A set of resistances/weights – (**synapses**)
- A processing element - (**neuron**)
- A single output - (**axon**)



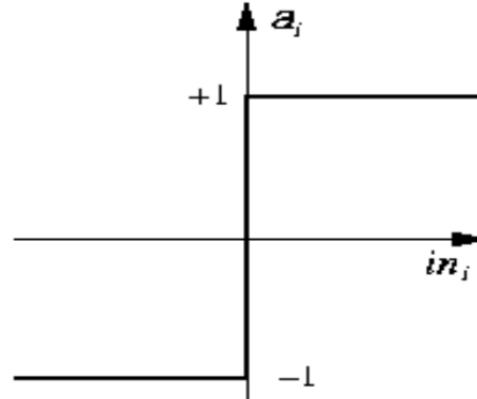
The activation of a neuron is **binary**. That is, the neuron either fires or does not fire (all or nothing)



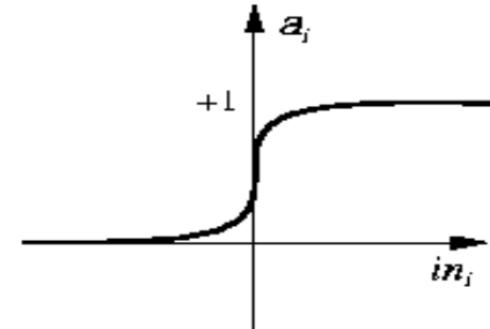
# ACTIVATION FUNCTIONS



(a) Step function



(b) Sign function



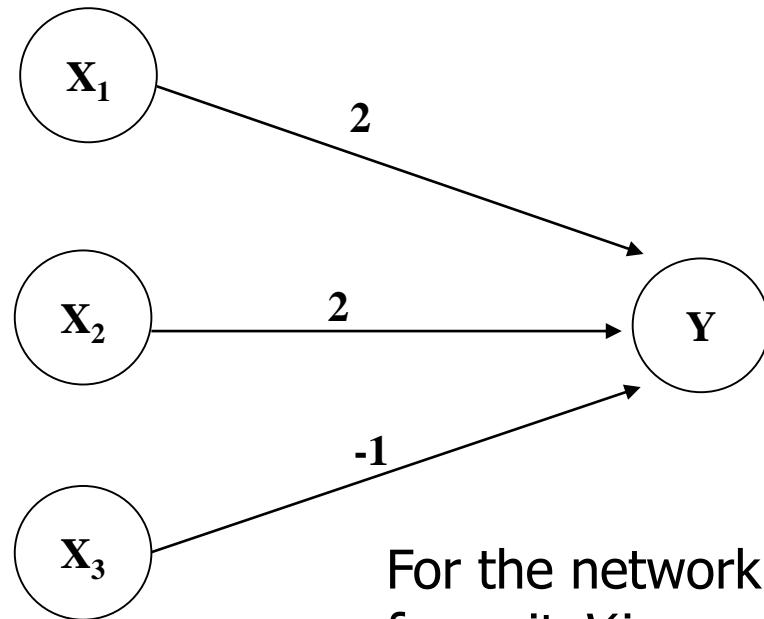
(c) Sigmoid function

$$\text{Step}_t(x) = 1 \text{ if } x \geq t, \text{ else } 0$$

$$\text{Sign}(x) = +1 \text{ if } x \geq 0, \text{ else } -1$$

$$\text{Sigmoid}(x) = \frac{1}{1+e^{-x}}$$

# THE FIRST NEURAL NETWORKS



$$y_{in} = x_1 * 2 + x_2 * 2 + x_3 * (-1)$$

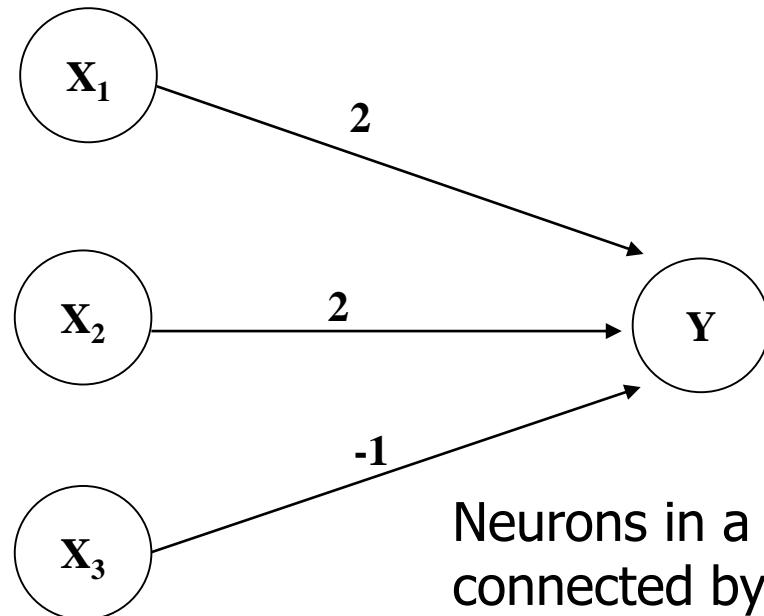
**Weighted Sum**

For the network shown here the activation function for unit  $Y$  is

$f(y_{in}) = 1$  (**fire**), if  $y_{in} \geq \theta$ ; else  $0$  (**not fire**)  
where  $y_{in}$  is the total input signal received  
(weighted sum);

$\theta$  is the **threshold** for  $Y$

# THE FIRST NEURAL NETWORKS

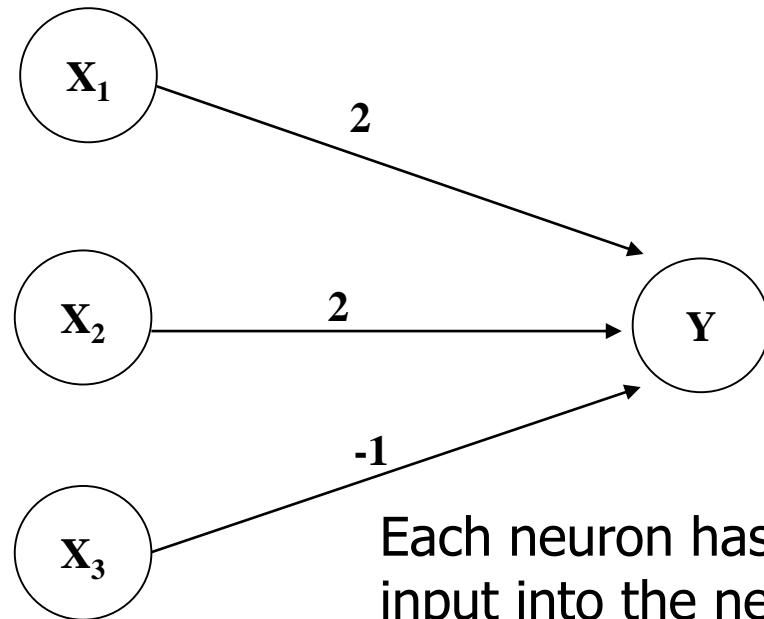


Neurons in a McCulloch-Pitts network are connected by **directed, weighted paths**

If the weight on a path is positive the path is **excitatory**, otherwise it is **inhibitory**

$x_1$  and  $x_2$  encourage the neuron to fire  
 $x_3$  prevents the neuron from firing

# THE FIRST NEURAL NETWORKS

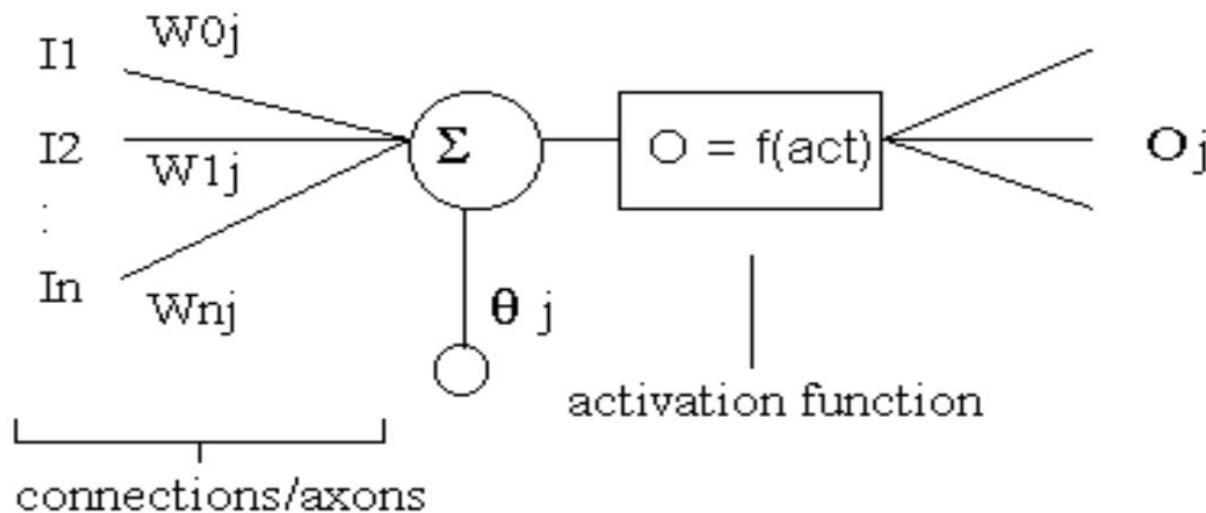


Each neuron has a fixed **threshold**. If the net input into the neuron is greater than or equal to the threshold, the neuron fires

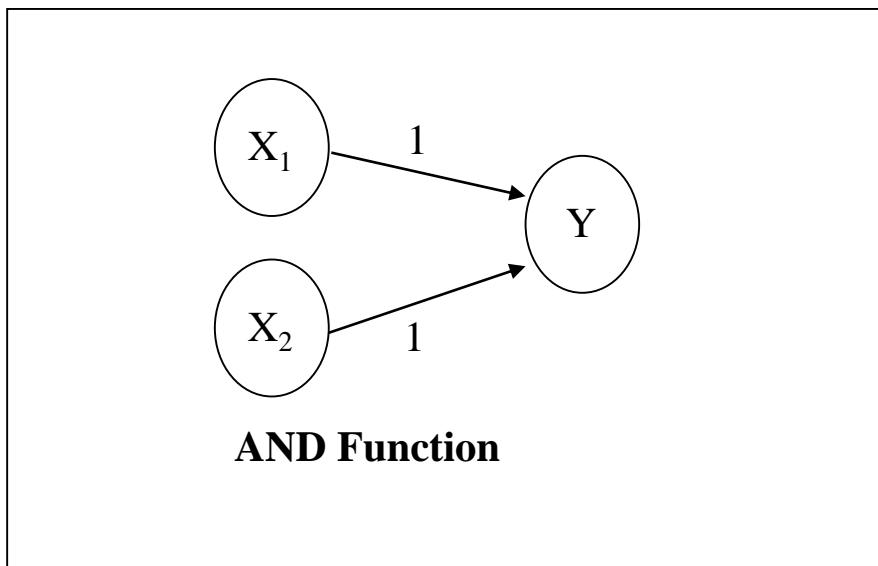
# THE FIRST NEURAL NETWORKS

Using McCulloch-Pitts model we can model logic functions

Let's look at 4 logic functions



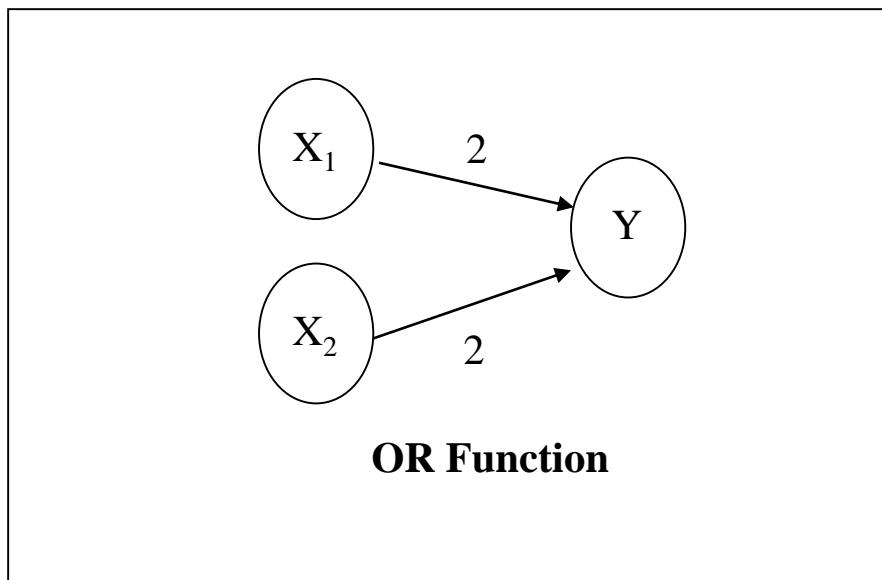
# THE FIRST NEURAL NETWORKS



AND		
X1	X2	Y
1	1	1
1	0	0
0	1	0
0	0	0

$$\text{Threshold}(Y) = 2$$

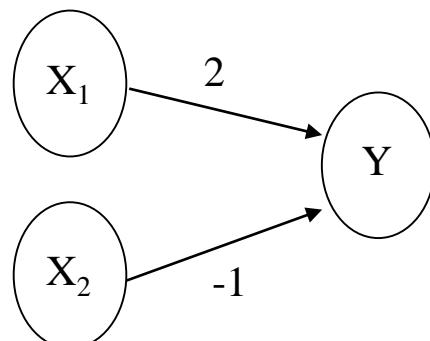
# THE FIRST NEURAL NETWORKS



$\text{Threshold}(Y) = 2$

OR		Y
X1	X2	
1	1	1
1	0	1
0	1	1
0	0	0

# THE FIRST NEURAL NETWORKS



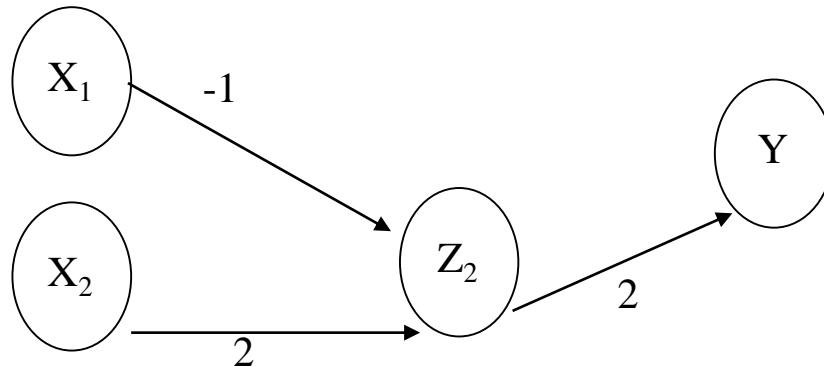
**AND NOT Function**

AND NOT		Y
X1	X2	
1	1	0
1	0	1
0	1	0
0	0	0

$$\text{Threshold}(Y) = 2$$

# THE FIRST NEURAL NETWORKS

$$X_1 \text{ XOR } X_2 = (X_1 \text{ AND NOT } X_2) \text{ OR } (X_2 \text{ AND NOT } X_1)$$

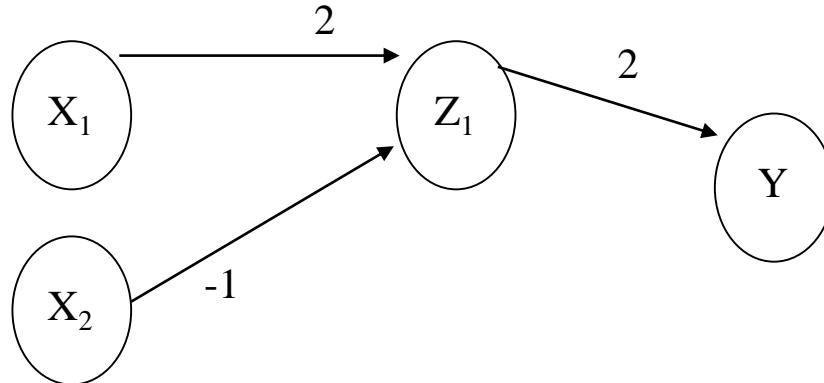


XOR		
X1	X2	Y
1	1	0
1	0	1
0	1	1
0	0	0

AND NOT		
X2	X1	Y
1	1	0
1	0	1
0	1	0
0	0	0

# THE FIRST NEURAL NETWORKS

$$X_1 \text{ XOR } X_2 = (X_1 \text{ AND NOT } X_2) \text{ OR } (X_2 \text{ AND NOT } X_1)$$

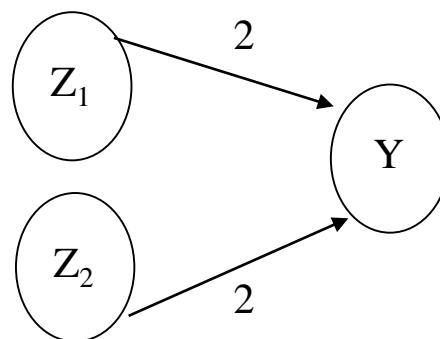


XOR		
X1	X2	Y
1	1	0
1	0	1
0	1	1
0	0	0

AND NOT		
X1	X2	Y
1	1	0
1	0	1
0	1	0
0	0	0

# THE FIRST NEURAL NETWORKS

$$X_1 \text{ XOR } X_2 = (X_1 \text{ AND NOT } X_2) \text{ OR } (X_2 \text{ AND NOT } X_1)$$

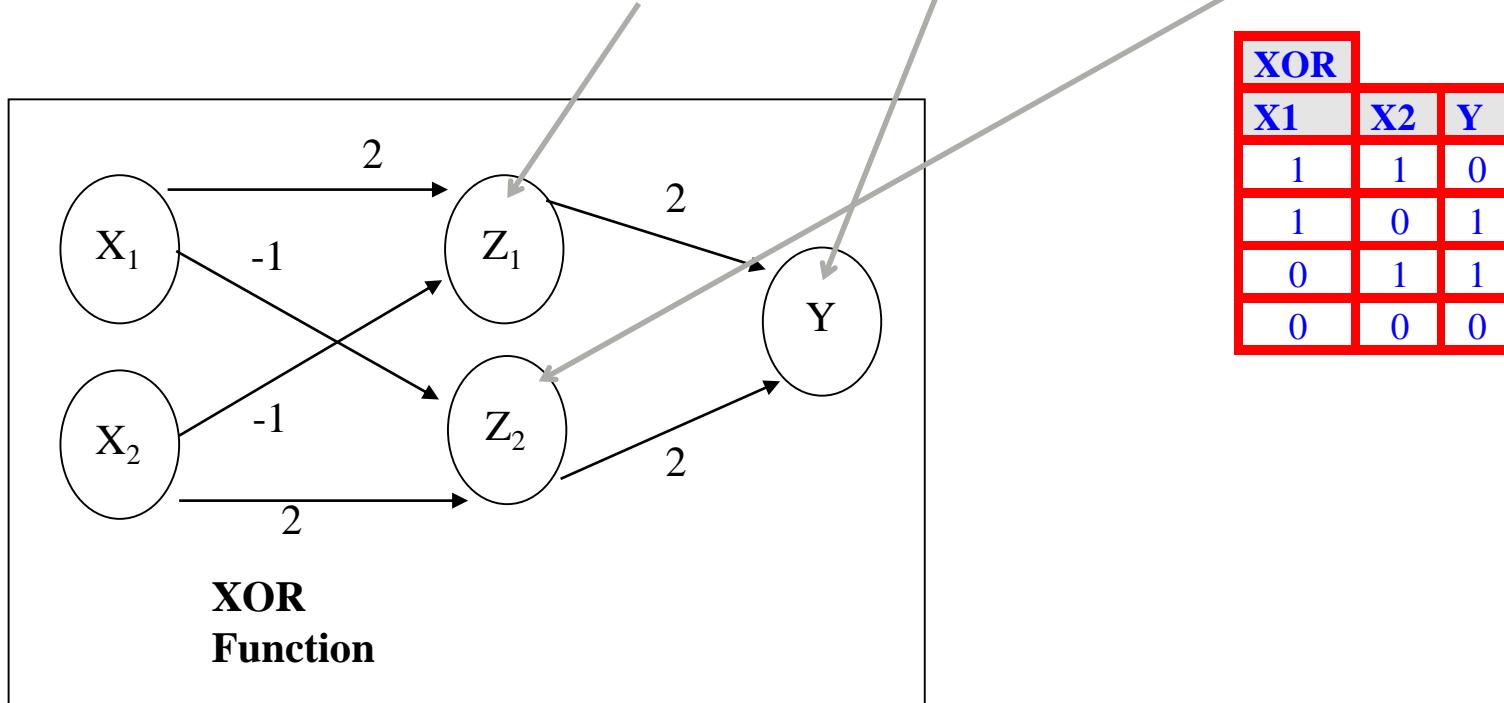


XOR		
X1	X2	Y
1	1	0
1	0	1
0	1	1
0	0	0

AND NOT		
X1	X2	Y
1	1	0
1	0	1
0	1	0
0	0	0

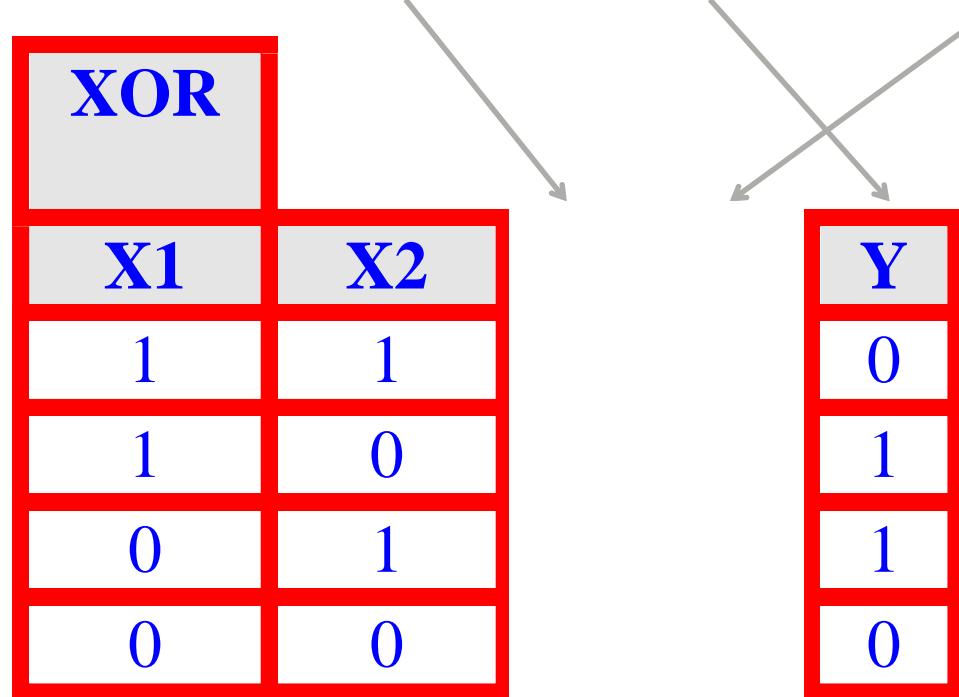
# THE FIRST NEURAL NETWORKS

$$X_1 \text{ XOR } X_2 = (X_1 \text{ AND NOT } X_2) \text{ OR } (X_2 \text{ AND NOT } X_1)$$



# THE FIRST NEURAL NETWORKS

$$X_1 \text{ XOR } X_2 = (X_1 \text{ AND NOT } X_2) \text{ OR } (X_2 \text{ AND NOT } X_1)$$

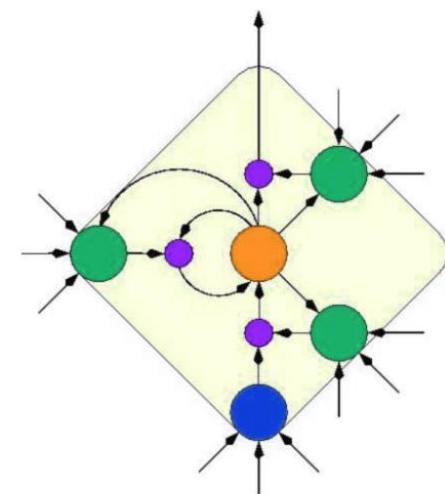
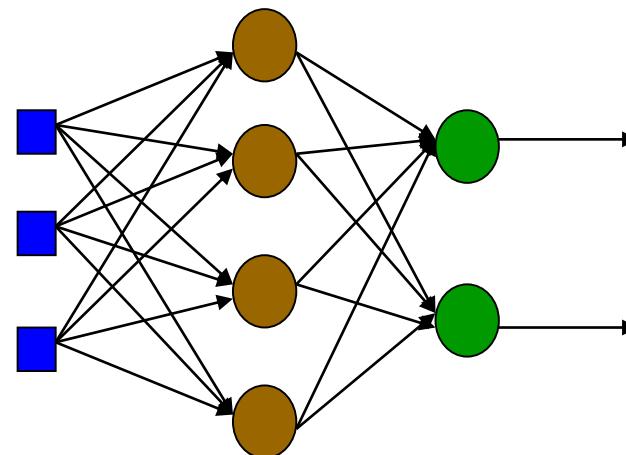
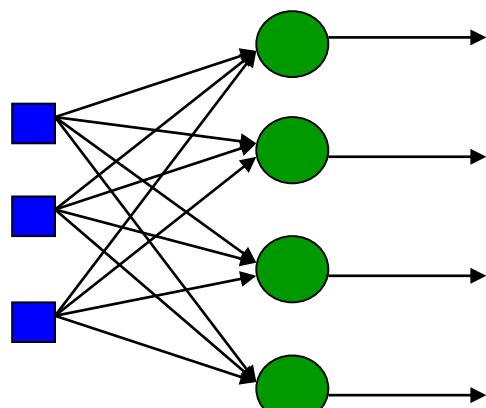


# NEURAL NETWORK ARCHITECTURES

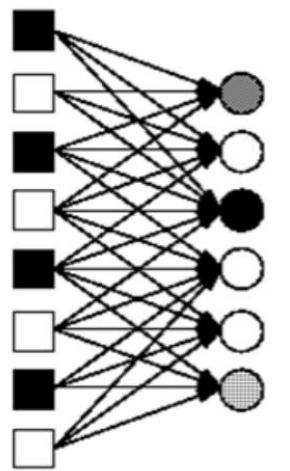
Three different classes of network architectures

- single-layer feed-forward
- multi-layer feed-forward
- recurrent

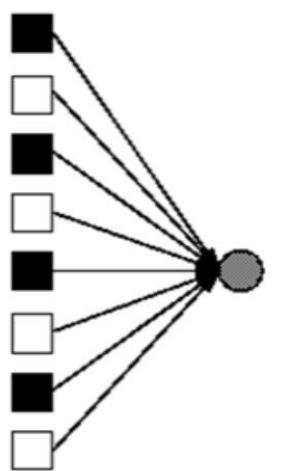
} neurons are organized  
in acyclic layers



# PERCEPTRON



$I_j$        $w_{j,i}$        $O_i$   
Input Units      Output Units  
**Perceptron Network**

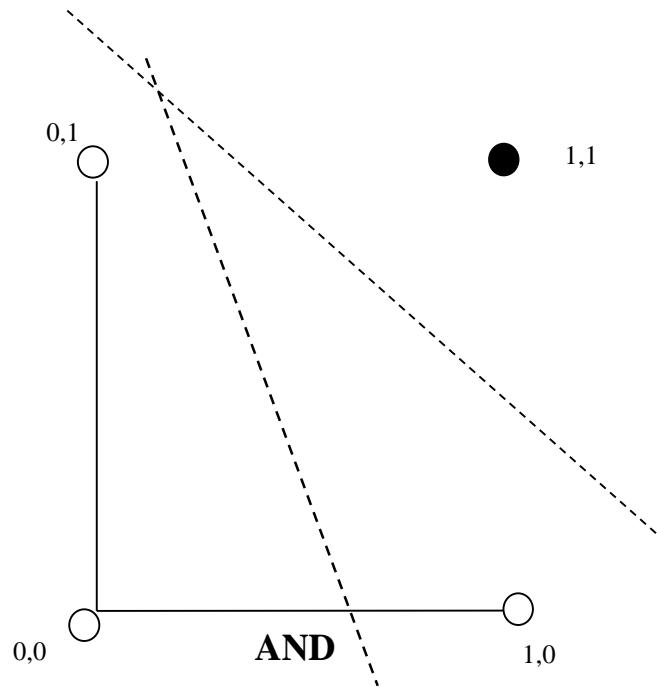


$I_j$        $w_j$        $O$   
Input Units      Output Unit  
**Single Perceptron**

Synonym for Single-Layer, Feed-Forward Network

- First Studied in the 1950's

# LINEAR SEPARABILITY



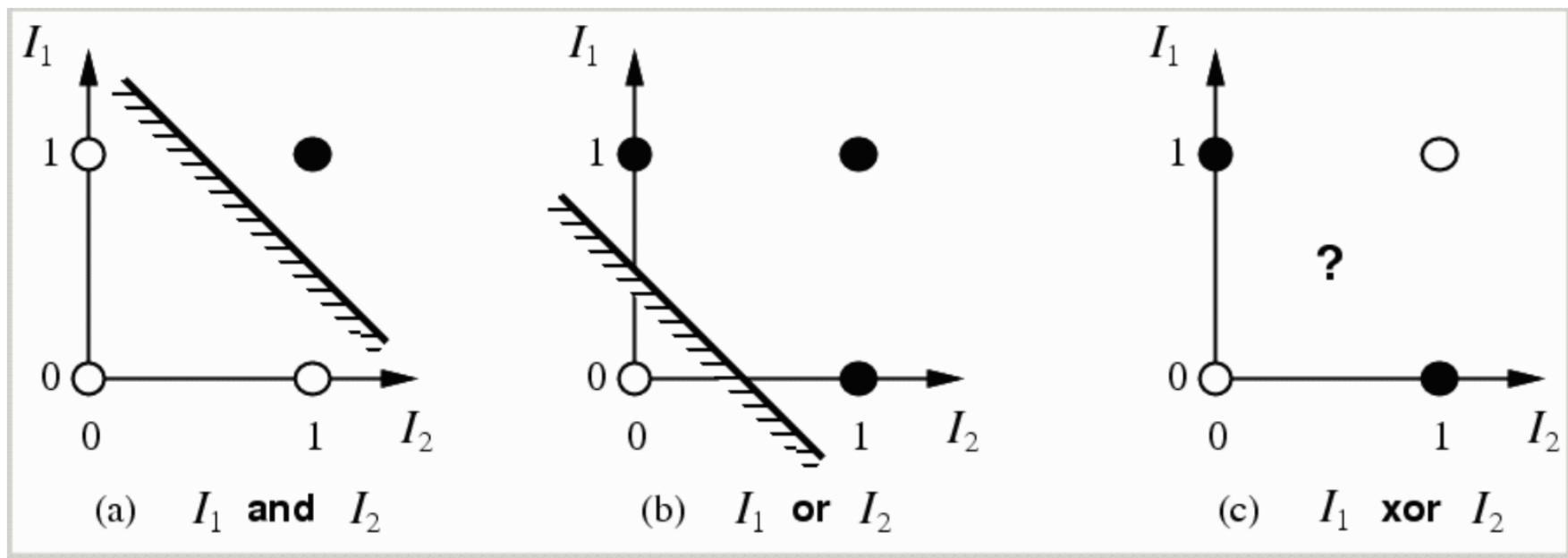
**Input 1**  
**Input 2**  
**Output**

AND			
Input 1	Input 2	Output	
0	0	0	1
0	1	0	1
1	0	0	1

- Functions which can be separated in this way are called **Linearly Separable**
- Only linearly Separable functions can be represented by a single layer NN (perceptron)

# LINEAR SEPARABILITY

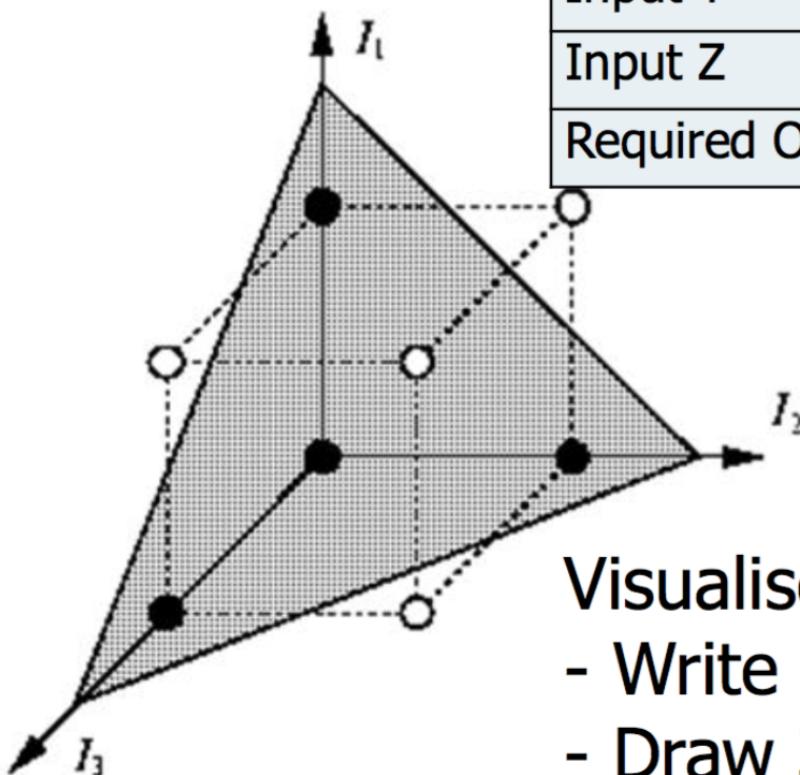
Minsky & Papert



Linear Separability is also possible in more than 3 dimensions  
– but it is harder to visualize

# LINEAR SEPARABILITY

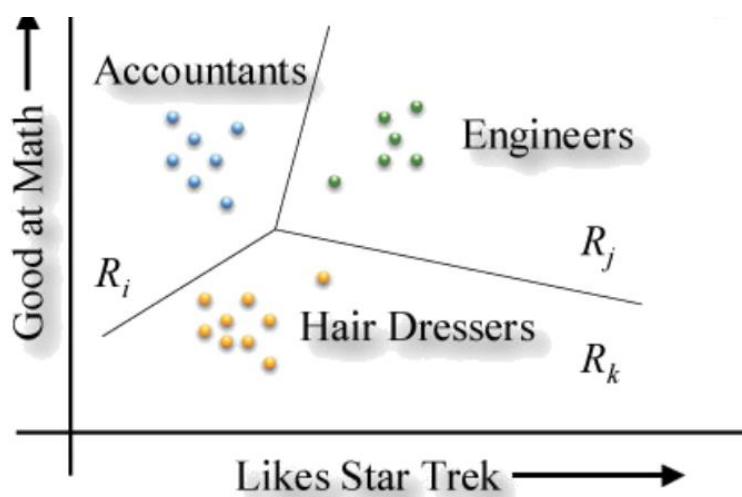
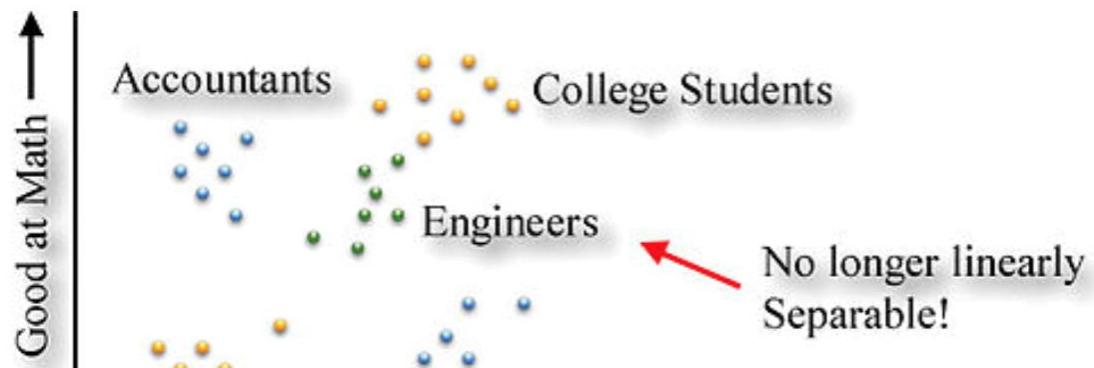
Input X	0	0	1	1	0	0	1	1
Input Y	0	1	0	1	0	1	0	1
Input Z	0	0	0	0	1	1	1	1
Required Output	<b>1</b>	<b>1</b>	<b>1</b>	<b>0</b>	<b>1</b>	<b>0</b>	<b>0</b>	<b>0</b>



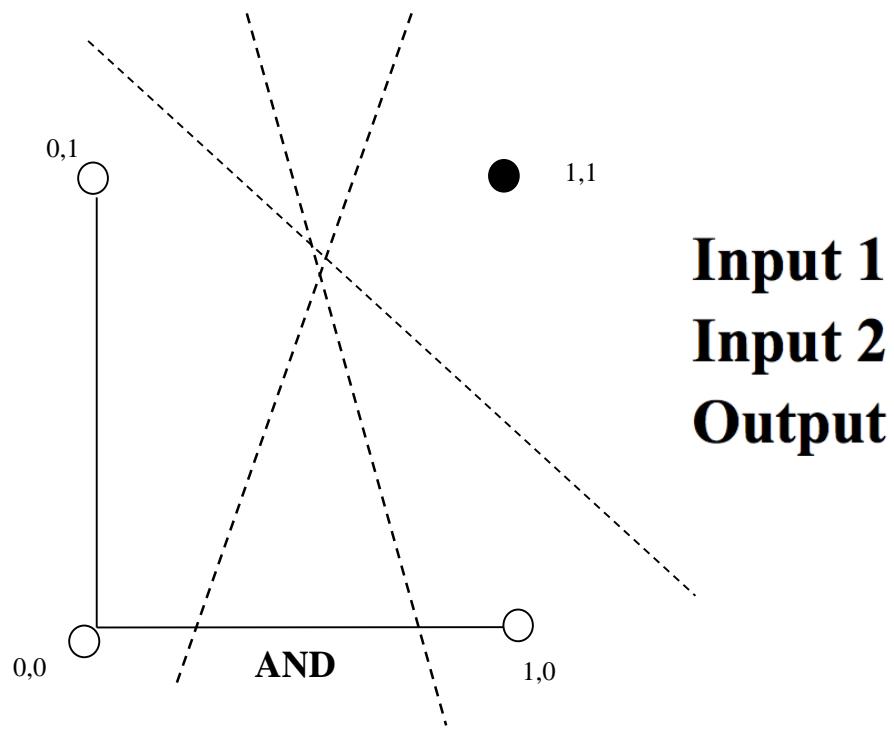
Visualise ANN with 3 inputs

- Write the truth table
- Draw 3D graphical representation

# LINEAR SEPARABILITY



# TRAINING A NN



AND			
0	0	1	1
0	1	0	1
0	0	0	1

A Neural Network Playground

Outlook Web App

excitatory\_百度搜索

百度翻译

playground.tensorflow.org

Epoch 000,091

Learning rate 0.03

Activation Tanh

Regularization None

Regularization rate 0

Problem type Classification

**DATA**

Which dataset do you want to use?

Ratio of training to test data: 50%

Noise: 0

Batch size: 10

**FEATURES**

Which properties do you want to feed in?

**2 HIDDEN LAYERS**

+ -

$X_1$   $X_2$   $X_1^2$   $X_2^2$   $X_1 X_2$   $\sin(X_1)$   $\sin(X_2)$

2 neurons

This is the output from one neuron. Hover to see it larger.

The outputs are mixed with varying weights, shown by the thickness of the lines.

**OUTPUT**

Test loss 0.011  
Training loss 0.012

-6 -5 -4 -3 -2 -1 0 1 2 3 4 5 6

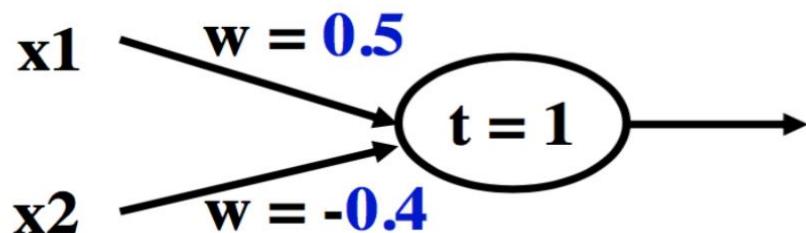
6 5 4 3 2 1 0 -1 -2 -3 -4 -5 -6

Colors shows data, neuron and weight values.

Show test data  Discretize output

**REGENERATE**

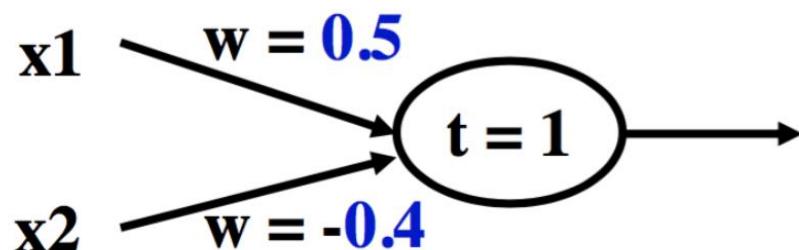
# Training a NN



AND		
<b>X1</b>	<b>X2</b>	<b>T</b>
0	0	0
0	1	0
1	0	0
1	1	1

<b>X1</b>	<b>X2</b>	<b>Summation</b>	<b>Output</b>
0	0	$(0 * 0.5) + (0 * -0.4) = 0$	0
0	1		
1	0		
1	1		

# Training a NN



AND		<b>X1</b>	<b>X2</b>	<b>T</b>	<b>O</b>
0	0	0	0	0	0
0	1	0	1	0	0
1	0	1	0	0	0
1	1	1	1	1	0

<b>X1</b>	<b>X2</b>	<b>Summation</b>	<b>Output</b>
0	0	$(0 * 0.5) + (0 * -0.4) = 0$	0
0	1	$(0 * 0.5) + (1 * -0.4) = -0.4$	0
1	0	$(1 * 0.5) + (0 * -0.4) = 0.5$	0
1	1	$(1 * 0.5) + (1 * -0.4) = 0.1$	0

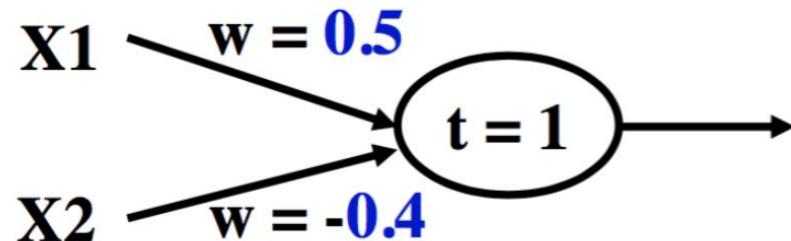
# Training a NN

AND			
X1	X2	T	O
0	0	0	0
0	1	0	0
1	0	0	0
1	1	1	0

While epoch produces an error

Check next inputs (pattern) from epoch

End While



Epoch: The entire training set feed into the neural network.

The AND function: an epoch consists of four sets of inputs (patterns) feed into the network ([0,0], [0,1], [1,0], [1,1])

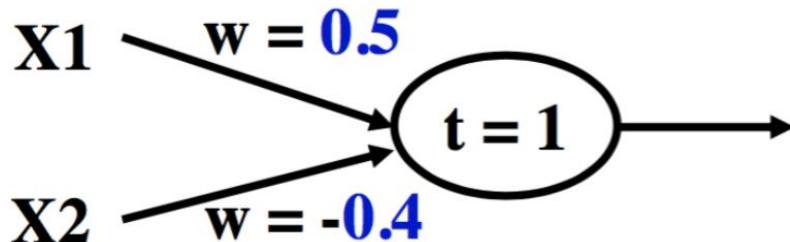
# Training a NN

While epoch produces an error

Check next inputs (pattern) from epoch

$$\text{Err} = T - O$$

AND			
X1	X2	T	O
0	0	0	0
0	1	0	0
1	0	0	0
1	1	1	0



End While

Training Value, T : The value that we require the network to produce. For example, with [0,0] for the AND function the training value will be 0.

# Training a NN

While epoch produces an error

Check next inputs (pattern) from epoch

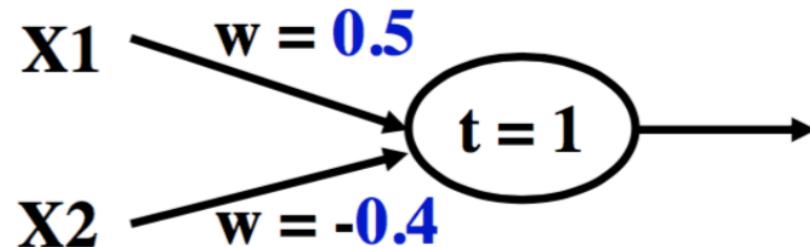
$$\text{Err} = T - O$$

If Err  $\neq 0$  then

End If

End While

AND			
X1	X2	T	O
0	0	0	0
0	1	0	0
1	0	0	0
1	1	1	0



Error, Err : The amount the output by the network O differs from the training value T.

# Training a NN

What is the problem if the learning rate is set too high, or too low?

While epoch produces an error

Check next inputs (pattern) from epoch

$$\text{Err} = T - O$$

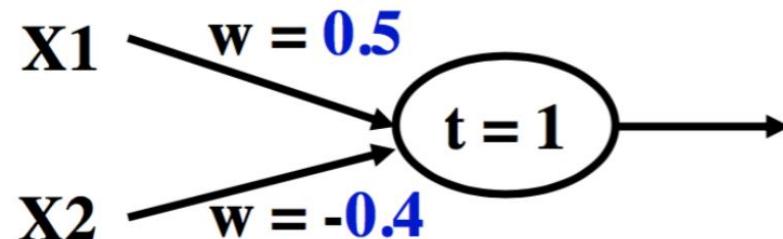
If Err  $\neq 0$  then

$$w_i = w_i + LR * X_i * \text{Err}$$

End If

End While

AND		T	O
X1	X2		
0	0	0	0
0	1	0	0
1	0	0	0
1	1	1	0



**X<sub>i</sub>:** Inputs to the neuron

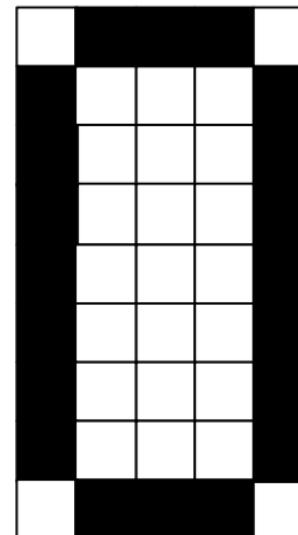
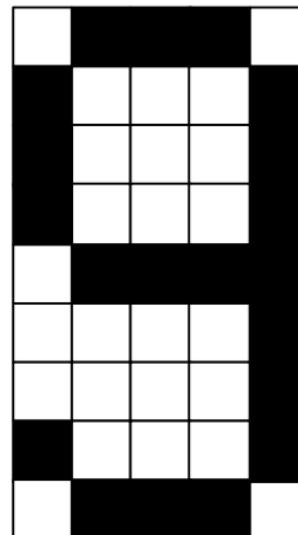
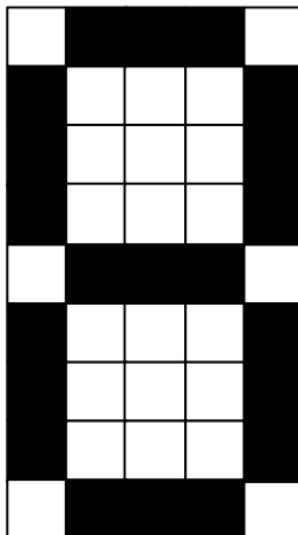
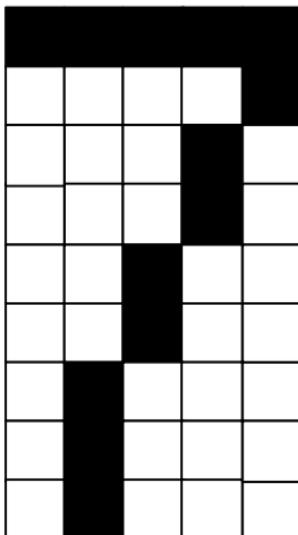
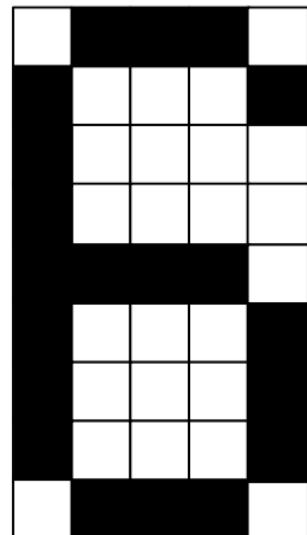
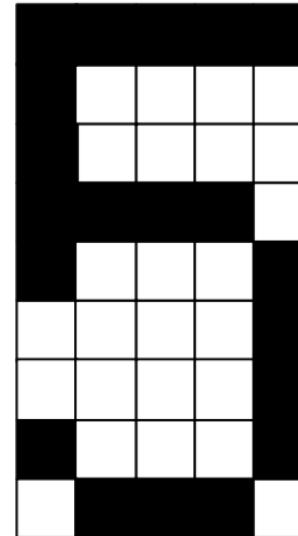
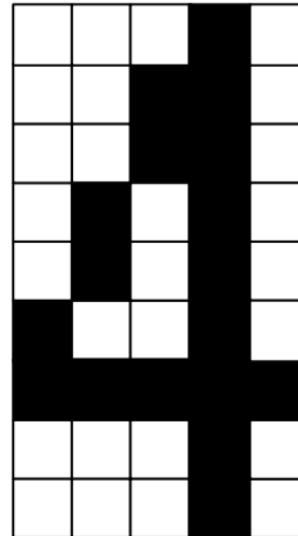
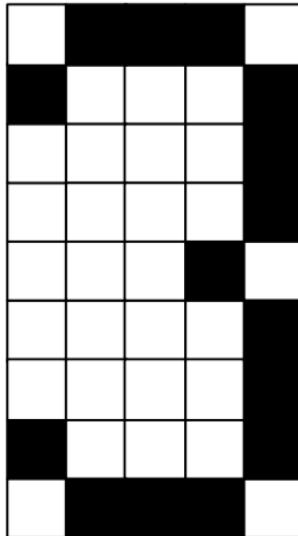
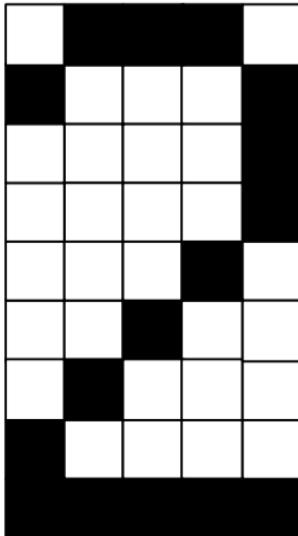
**w<sub>i</sub>:** Weight from input X<sub>i</sub> to the output

**LR:** The learning rate: how quickly the network converges.

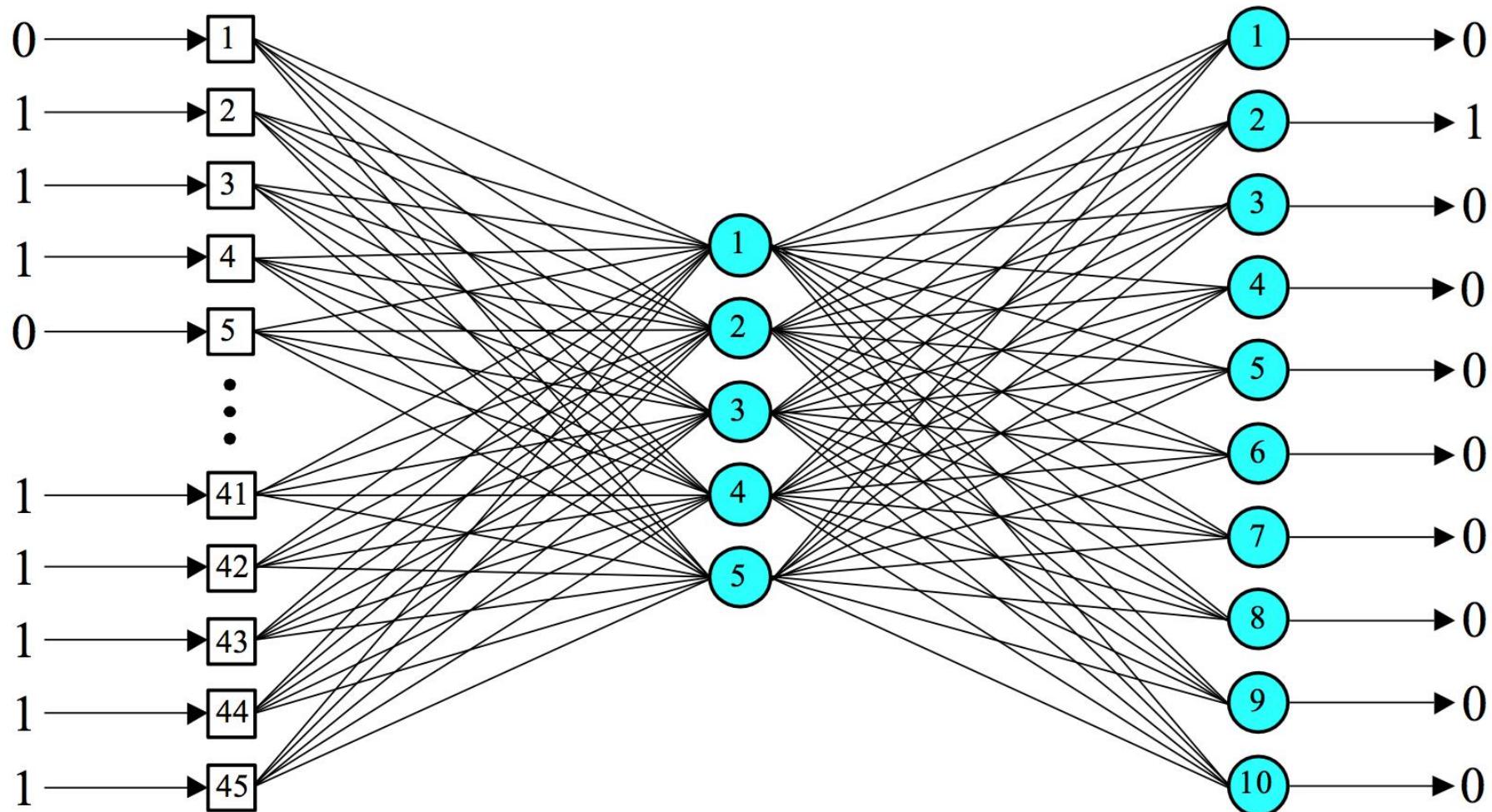
It is set by experimentation, typically 0.1

# Bit Maps for Digit Recognition

1	2	3	4	5
6	7	8	9	10
11	12	13	14	15
16	17	18	19	20
21	22	23	24	25
26	27	28	29	30
31	32	33	34	35
36	37	38	39	40
41	42	43	44	45

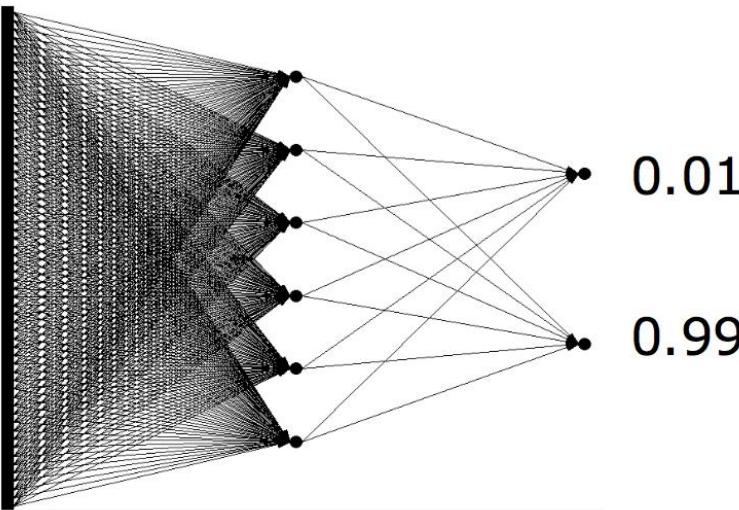
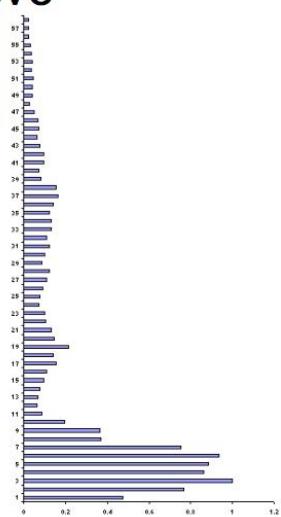


# Neural Network for Printed Digit Recognition



# Voice Recognition

Steve



Network  
Architecture

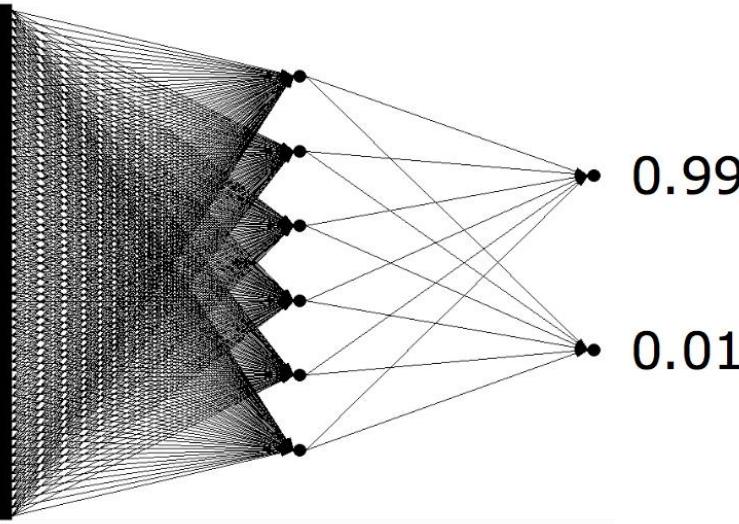
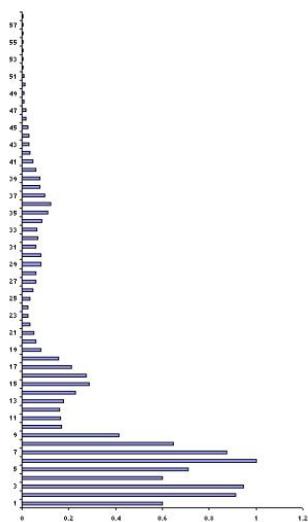
Feedforward Network

60 inputs (one for  
each frequency bin);

6 hidden;

2 output (0-1 for  
"Steve", 1-0 for  
"David")

David



# SUMMARY

First neural networks (McCulloch-Pitts)

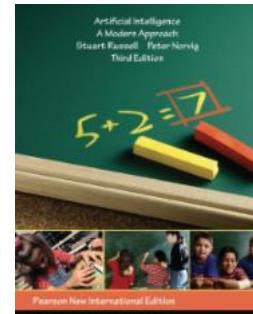
Simple networks

Perceptron (single layer NN)

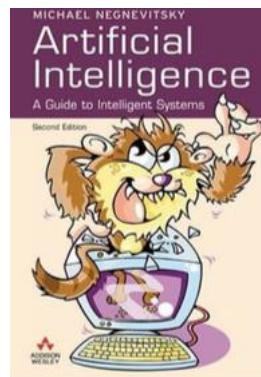
- Representation
- Limitations (linearly separable)
- Learning

# FURTHER READING

AIMA Chapter 1.2.4, 18.7



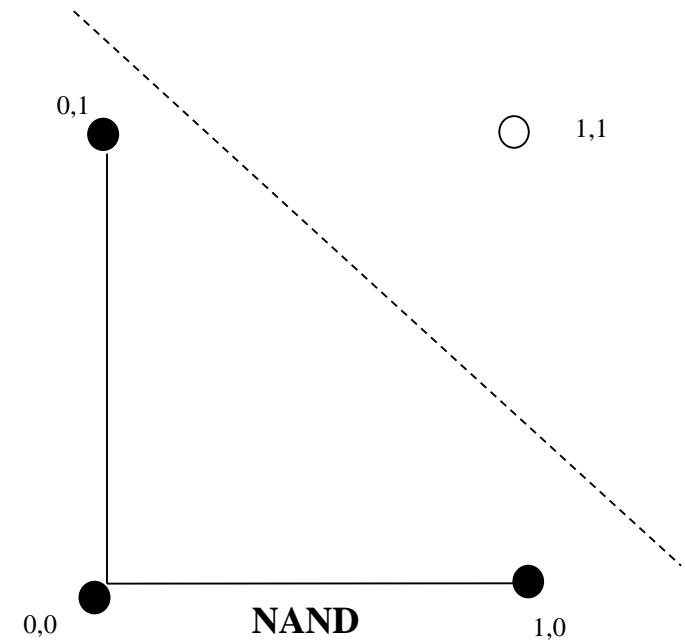
AIIS Chapter 6



# TRAINING A PERCEPTRON

Can we train a perceptron to learn logical NAND?

NAND				
Input 1	0	0	1	1
Input 2	0	1	0	1
Output	1	1	1	0



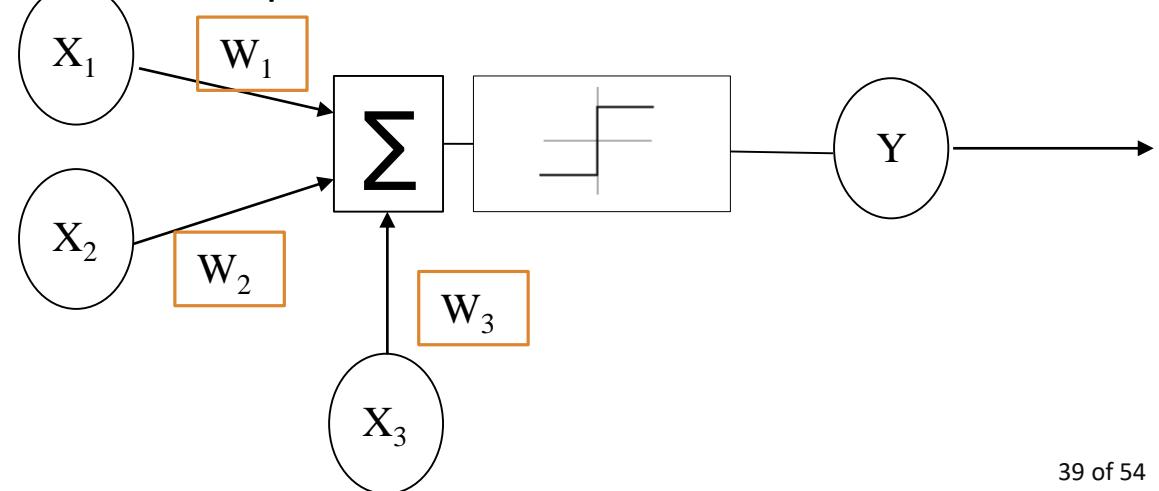
# THE LEARNING PROCESS

Randomly assign initial weights

Do:

- Present the network with input
- Calculate the error value in the output
- Adjust the weightings of the inputs according to the error

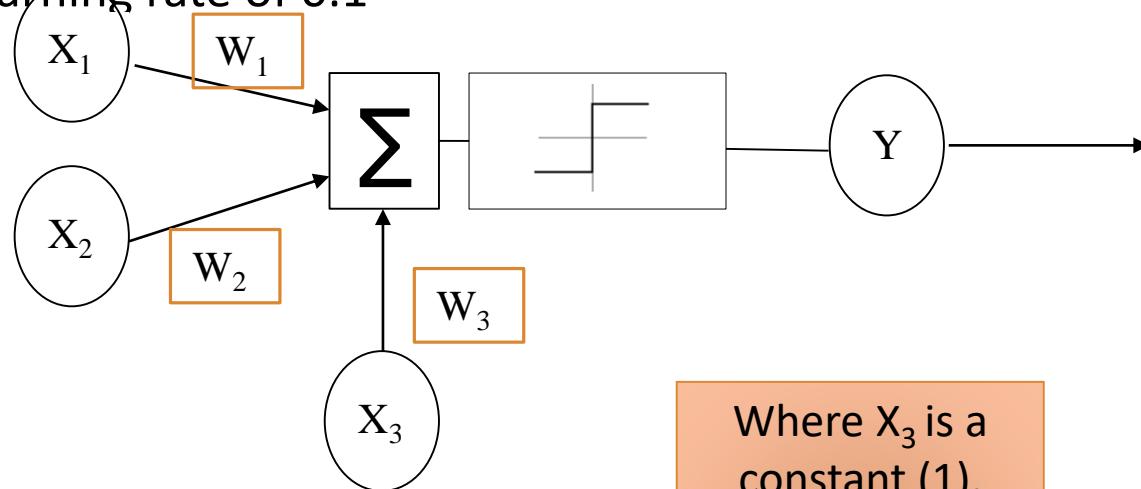
Until no error value exists for all inputs



# TRAINING A PERCEPTRON

Given a threshold value of 0.6

And a learning rate of 0.1



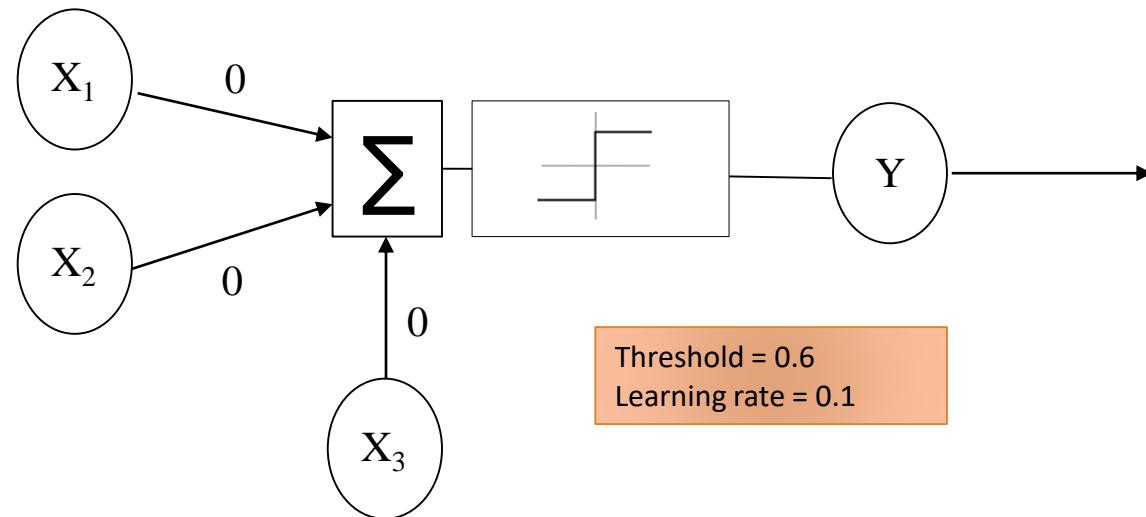
Where  $X_3$  is a constant (1), weighting the perceptron within the network

Input 1	Input 2	Desired Output
0	0	1
0	1	1
1	0	1
1	1	0

Input 1	Input 2	Desired Output
0	0	1
0	1	1
1	0	1
1	1	0

# TRAINING A PERCEPTRON

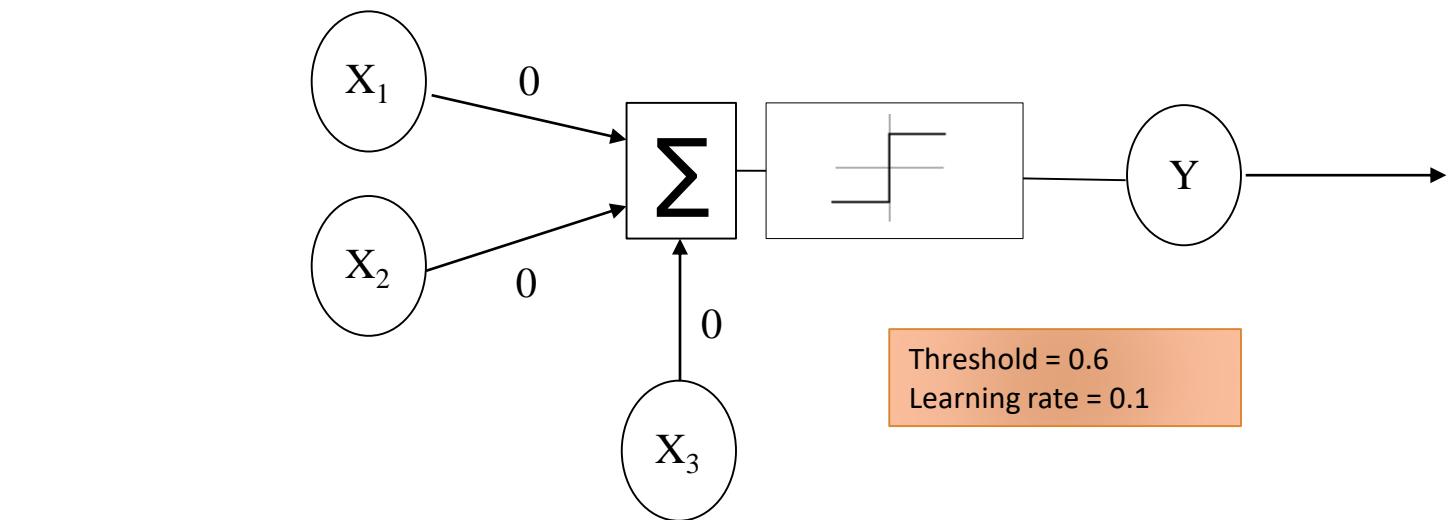
X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	Sum	Output	Error	Correction
0	0	1	0.0	0.0	0.0	0.0			
0	1	1							
1	0	1							
1	1	1							



Input 1	Input 2	Desired Output
0	0	1
0	1	1
1	0	1
1	1	0

# TRAINING A PERCEPTRON

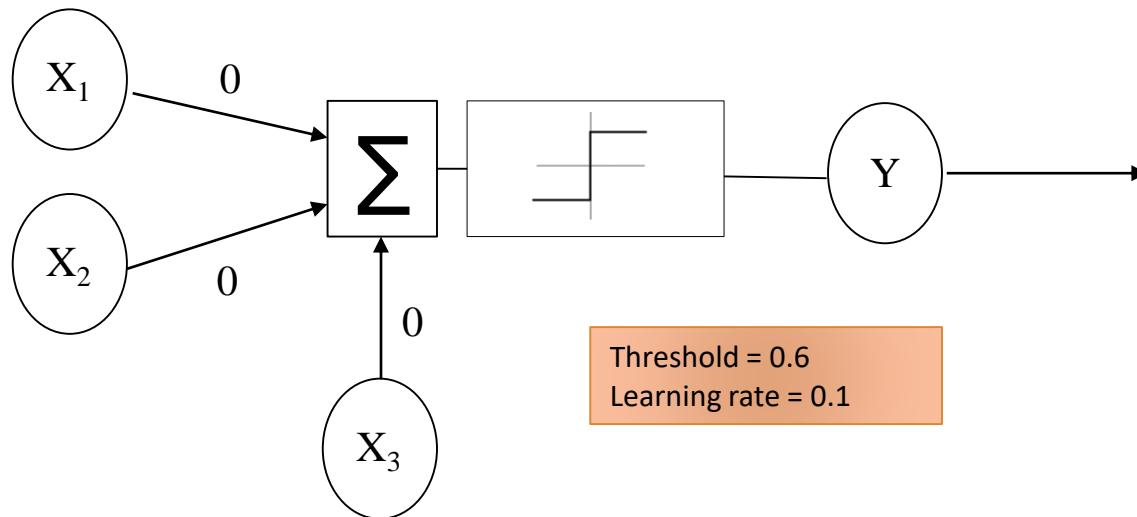
X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	Sum	Output	Error	Correction
0	0	1	0.0	0.0	0.0	0.0	0	1	+0.1
0	1	1							
1	0	1							
1	1	1							



Input 1	Input 2	Desired Output
0	0	1
0	1	1
1	0	1
1	1	0

# TRAINING A PERCEPTRON

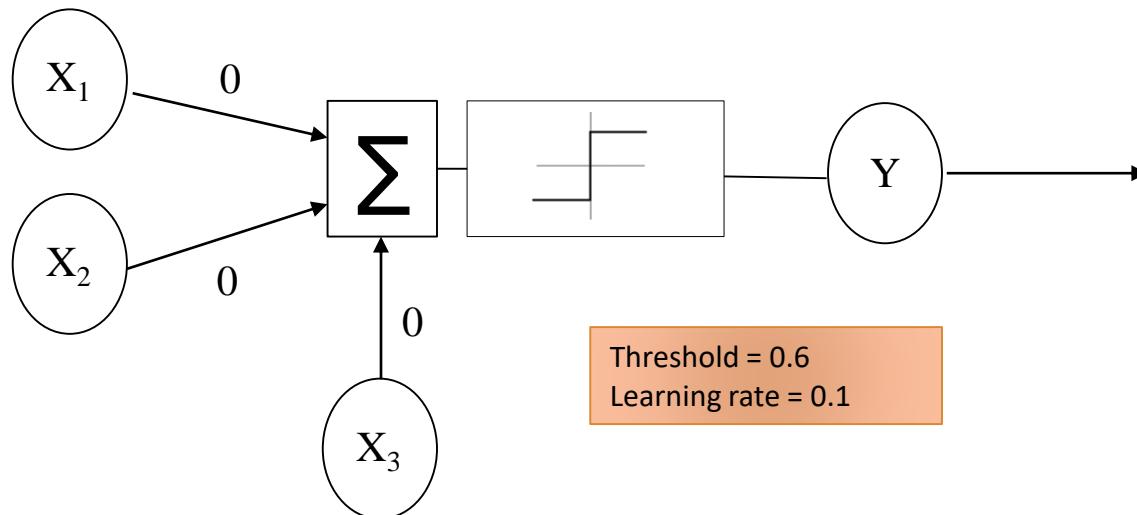
X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	Sum	Output	Error	Correction
0	0	1	0.0	0.0	0.0	0.0	0	1	+0.1
0	1	1	0.0	0.0	0.1	0.1			
1	0	1							
1	1	1							



Input 1	Input 2	Desired Output
0	0	1
0	1	1
1	0	1
1	1	0

# TRAINING A PERCEPTRON

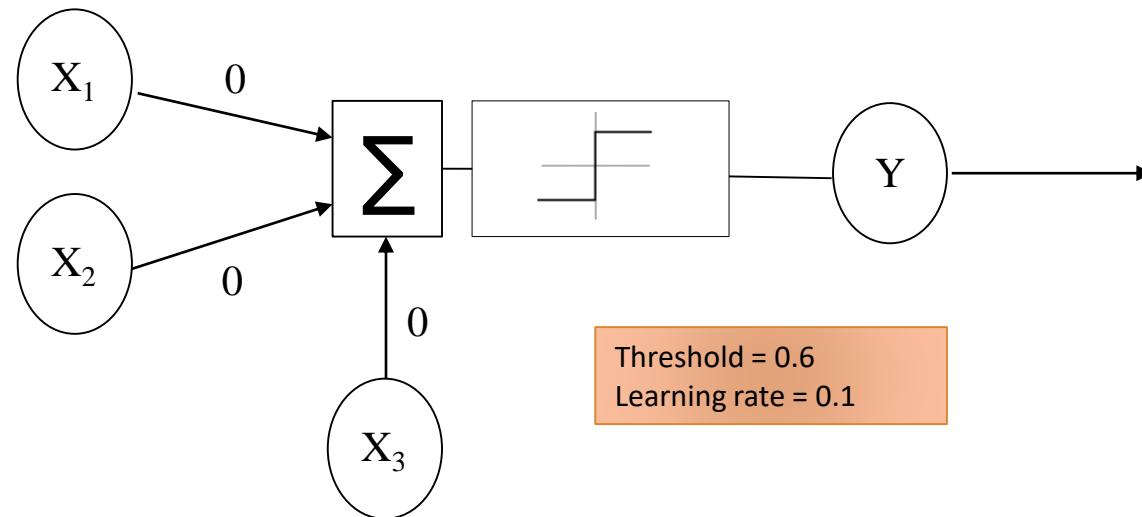
X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	Sum	Output	Error	Correction
0	0	1	0.0	0.0	0.0	0.0	0	1	+0.1
0	1	1	0.0	0.0	0.1	0.1	0	1	+0.1
1	0	1							
1	1	1							



Input 1	Input 2	Desired Output
0	0	1
0	1	1
1	0	1
1	1	0

# TRAINING A PERCEPTRON

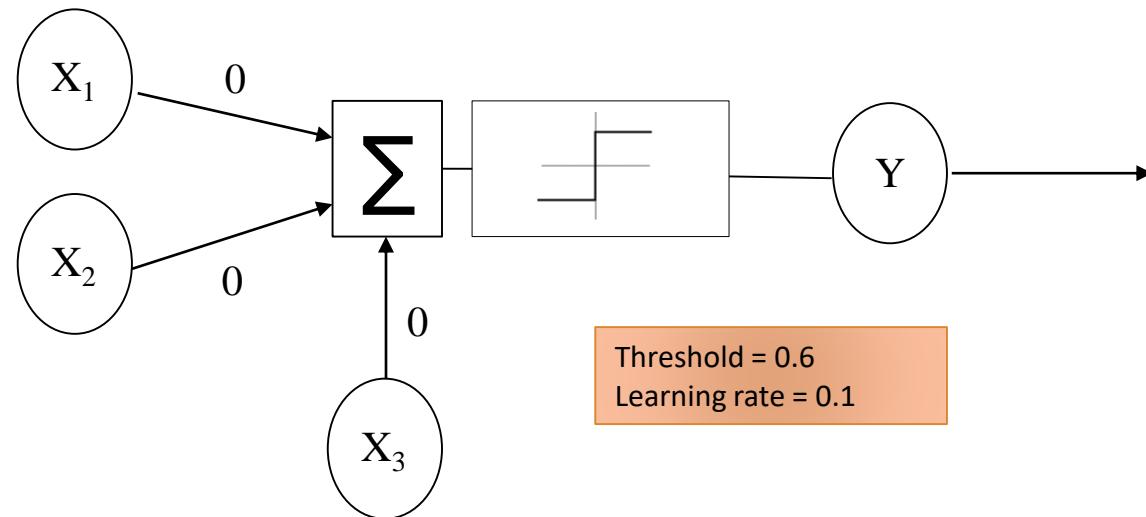
X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	Sum	Output	Error	Correction
0	0	1	0.0	0.0	0.0	0.0	0	1	+0.1
0	1	1	0.0	0.0	0.1	0.1	0	1	+0.1
1	0	1	0.0	0.1	0.2				
1	1	1							



Input 1	Input 2	Desired Output
0	0	1
0	1	1
1	0	1
1	1	0

# TRAINING A PERCEPTRON

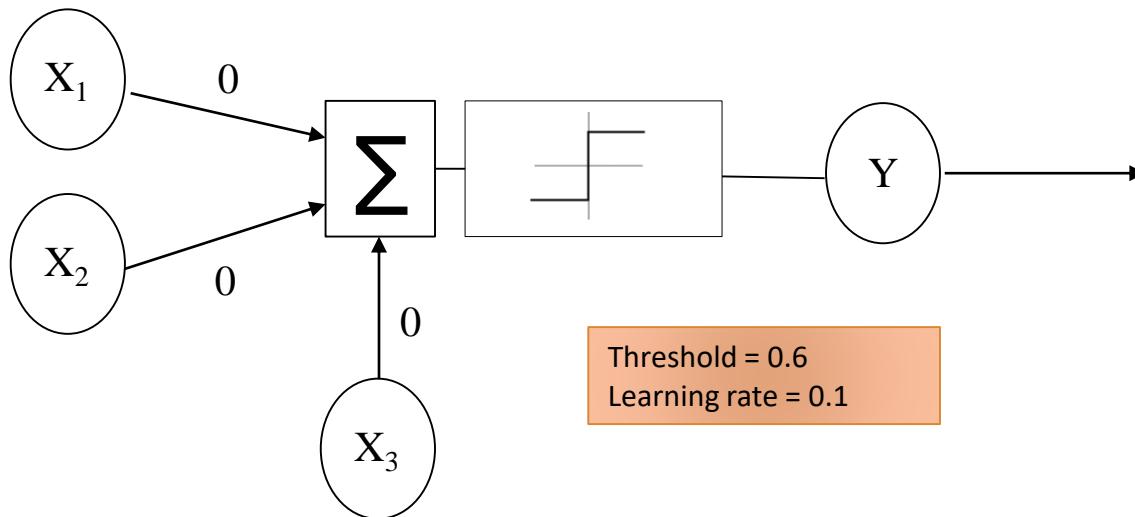
X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	Sum	Output	Error	Correction
0	0	1	0.0	0.0	0.0	0.0	0	1	+0.1
0	1	1	0.0	0.0	0.1	0.1	0	1	+0.1
1	0	1	0.0	0.1	0.2	0.2	0	1	+0.1
1	1	1							



Input 1	Input 2	Desired Output
0	0	1
0	1	1
1	0	1
1	1	0

# TRAINING A PERCEPTRON

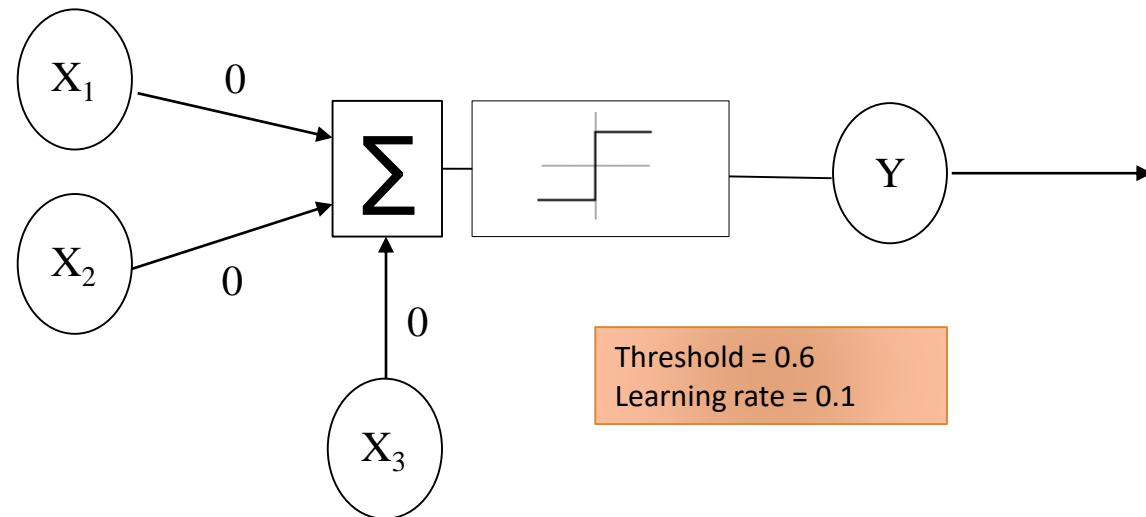
X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	Sum	Output	Error	Correction
0	0	1	0.0	0.0	0.0	0.0	0	1	+0.1
0	1	1	0.0	0.0	0.1	0.1	0	1	+0.1
1	0	1	0.0	0.1	0.2	0.2	0	1	+0.1
1	1	1	0.1	0.1	0.3	0.5			



Input 1	Input 2	Desired Output
0	0	1
0	1	1
1	0	1
1	1	0

# TRAINING A PERCEPTRON

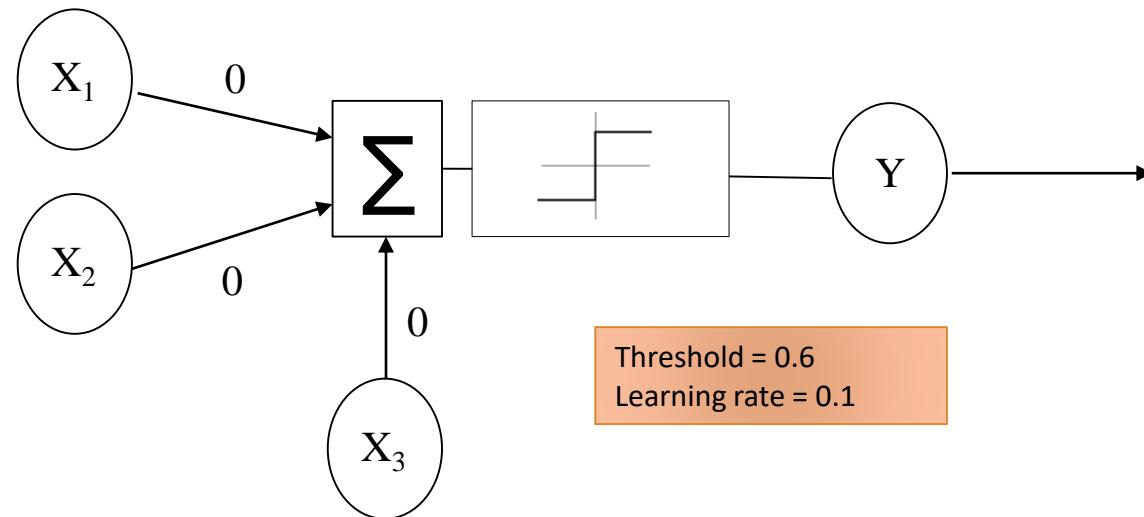
X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	Sum	Output	Error	Correction
0	0	1	0.0	0.0	0.0	0.0	0	1	+0.1
0	1	1	0.0	0.0	0.1	0.1	0	1	+0.1
1	0	1	0.0	0.1	0.2	0.2	0	1	+0.1
1	1	1	0.1	0.1	0.3	0.5	0	0	±0.0



Input 1	Input 2	Desired Output
0	0	1
0	1	1
1	0	1
1	1	0

# TRAINING A PERCEPTRON

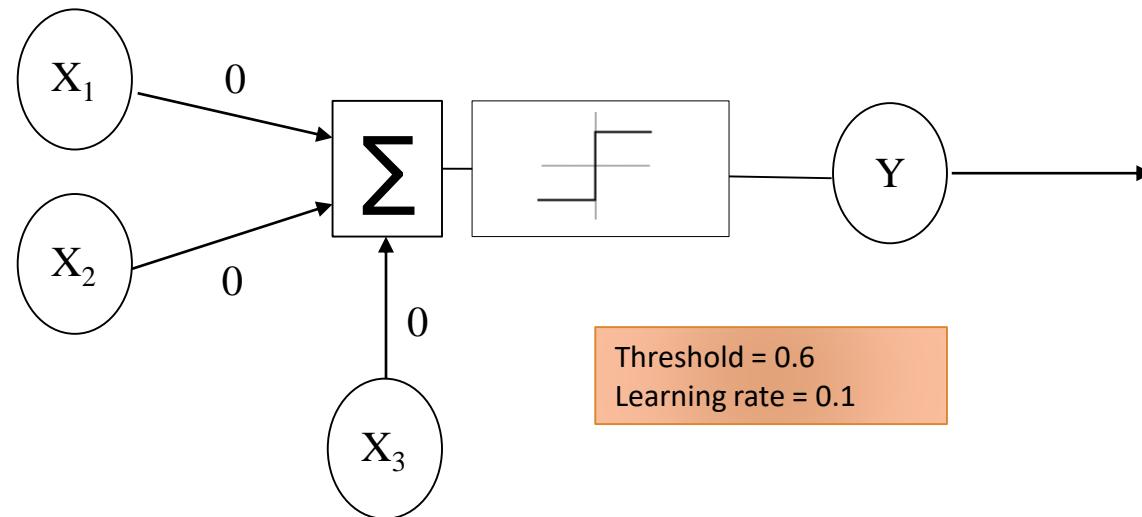
X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	Sum	Output	Error	Correction
0	0	1	0.1	0.1	0.3	0.3			
0	1	1							
1	0	1							
1	1	1							



Input 1	Input 2	Desired Output
0	0	1
0	1	1
1	0	1
1	1	0

# TRAINING A PERCEPTRON

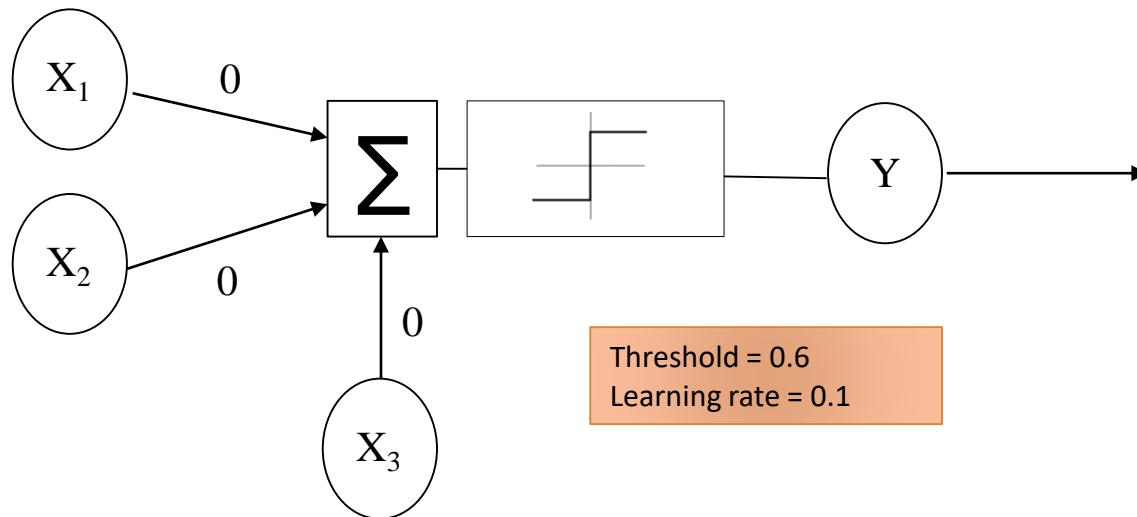
X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	Sum	Output	Error	Correction
0	0	1	0.1	0.1	0.3	0.3	0	1	+0.1
0	1	1							
1	0	1							
1	1	1							



Input 1	Input 2	Desired Output
0	0	1
0	1	1
1	0	1
1	1	0

# TRAINING A PERCEPTRON

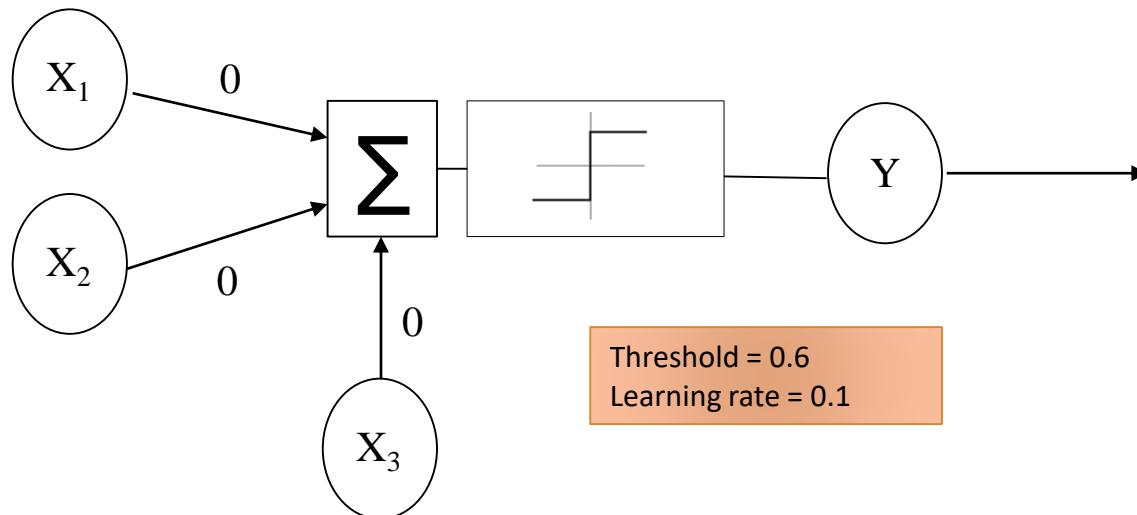
X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	Sum	Output	Error	Correction
0	0	1	0.1	0.1	0.3	0.3	0	1	+0.1
0	1	1	0.1	0.1	0.4	0.5			
1	0	1							
1	1	1							



Input 1	Input 2	Desired Output
0	0	1
0	1	1
1	0	1
1	1	0

# TRAINING A PERCEPTRON

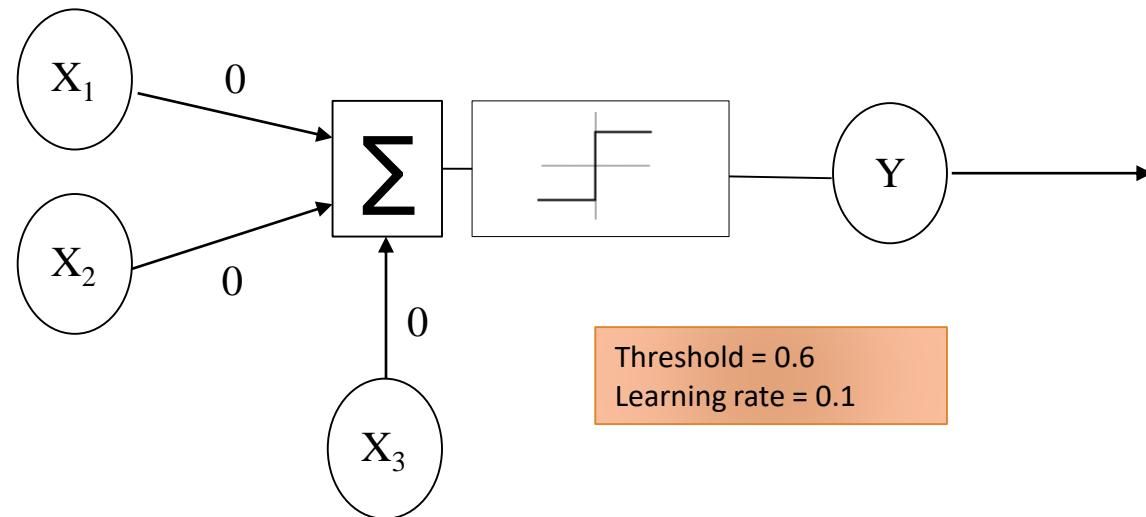
X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	Sum	Output	Error	Correction
0	0	1	0.1	0.1	0.3	0.3	0	1	+0.1
0	1	1	0.1	0.1	0.4	0.5	0	1	+0.1
1	0	1							
1	1	1							



Input 1	Input 2	Desired Output
0	0	1
0	1	1
1	0	1
1	1	0

# TRAINING A PERCEPTRON

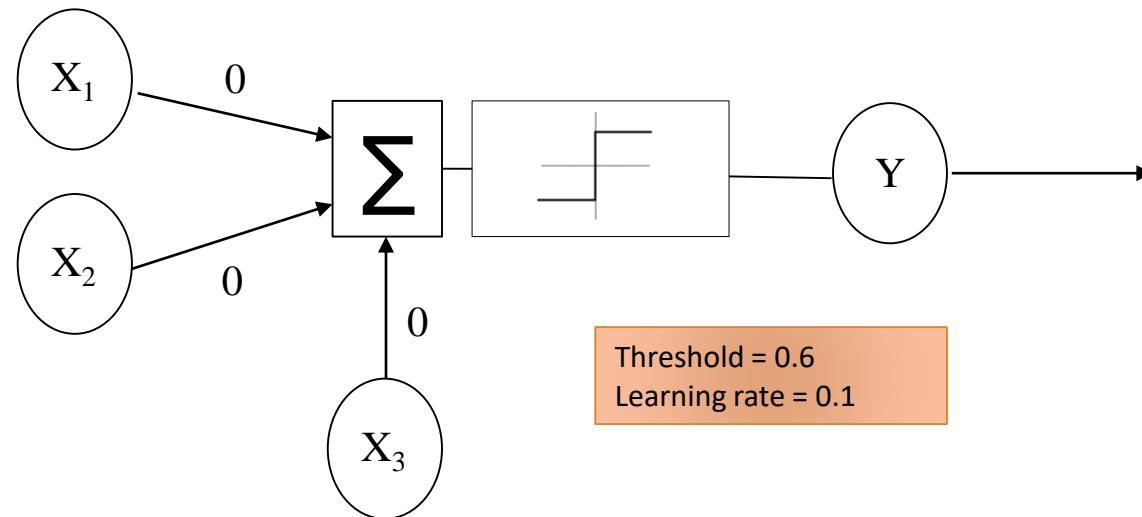
X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	Sum	Output	Error	Correction
0	0	1	0.1	0.1	0.3	0.3	0	1	+0.1
0	1	1	0.1	0.1	0.4	0.5	0	1	+0.1
1	0	1	0.1	0.2	0.5	0.6			
1	1	1							



Input 1	Input 2	Desired Output
0	0	1
0	1	1
1	0	1
1	1	0

# TRAINING A PERCEPTRON

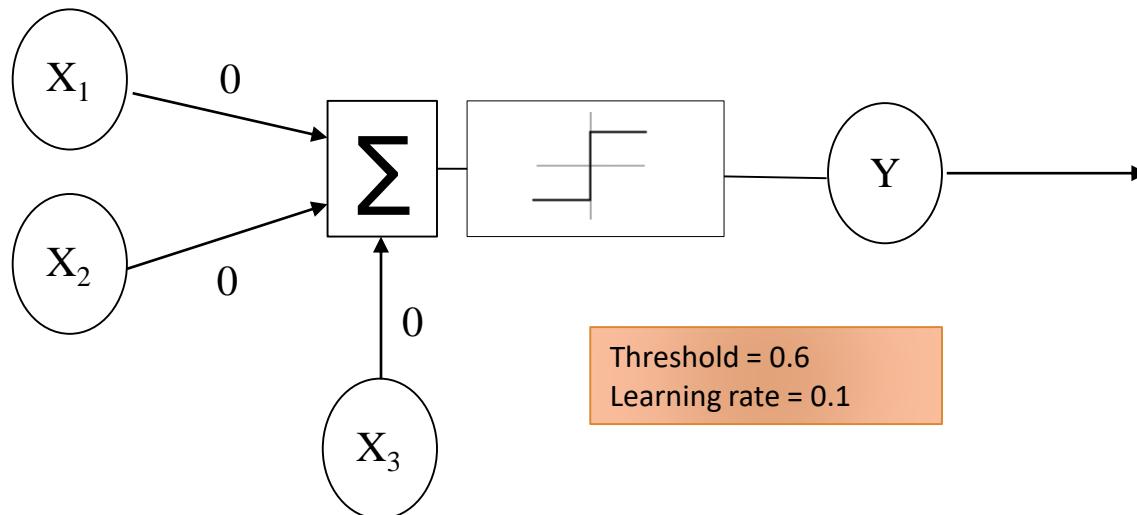
X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	Sum	Output	Error	Correction
0	0	1	0.1	0.1	0.3	0.3	0	1	+0.1
0	1	1	0.1	0.1	0.4	0.5	0	1	+0.1
1	0	1	0.1	0.2	0.5	0.6	1	0	±0.0
1	1	1							



Input 1	Input 2	Desired Output
0	0	1
0	1	1
1	0	1
1	1	0

# TRAINING A PERCEPTRON

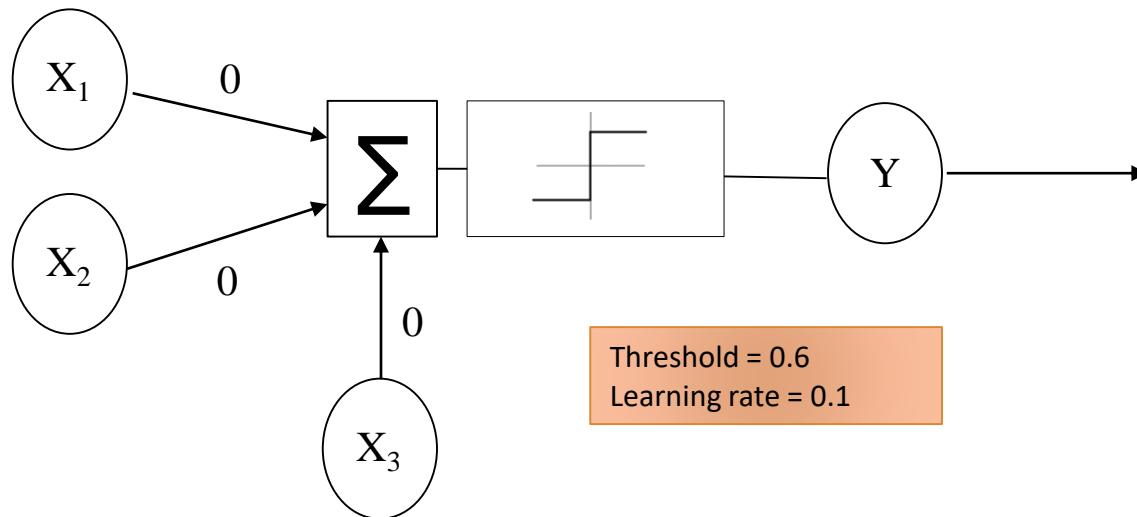
X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	Sum	Output	Error	Correction
0	0	1	0.1	0.1	0.3	0.3	0	1	+0.1
0	1	1	0.1	0.1	0.4	0.5	0	1	+0.1
1	0	1	0.1	0.2	0.5	0.6	1	0	±0.0
1	1	1	0.1	0.2	0.5	0.8			



Input 1	Input 2	Desired Output
0	0	1
0	1	1
1	0	1
1	1	0

# TRAINING A PERCEPTRON

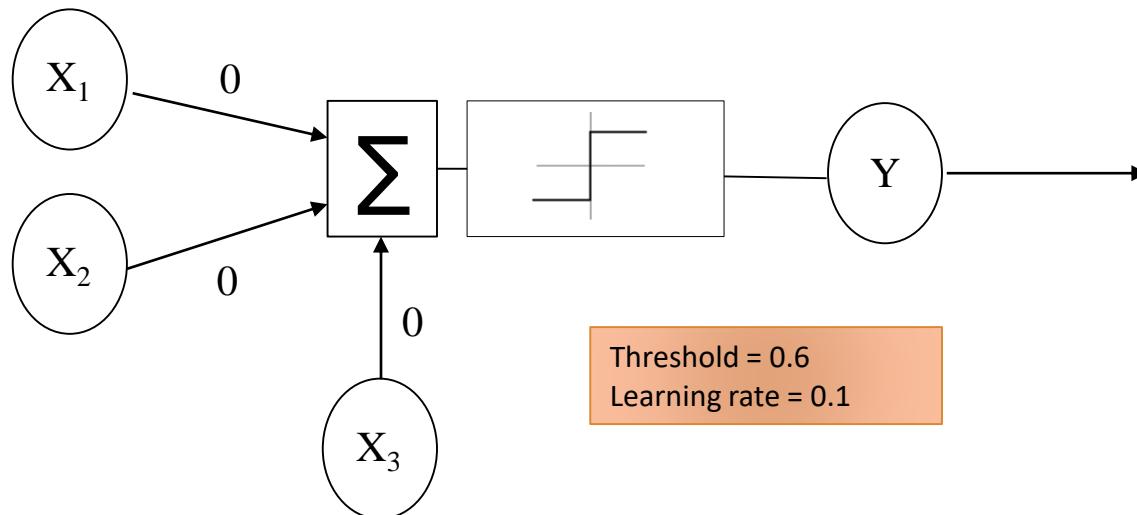
X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	Sum	Output	Error	Correction
0	0	1	0.1	0.1	0.3	0.3	0	1	+0.1
0	1	1	0.1	0.1	0.4	0.5	0	1	+0.1
1	0	1	0.1	0.2	0.5	0.6	1	0	-0.1
1	1	1	0.1	0.2	0.5	0.8	1	-1	-0.1



Input 1	Input 2	Desired Output
0	0	1
0	1	1
1	0	1
1	1	0

# TRAINING A PERCEPTRON

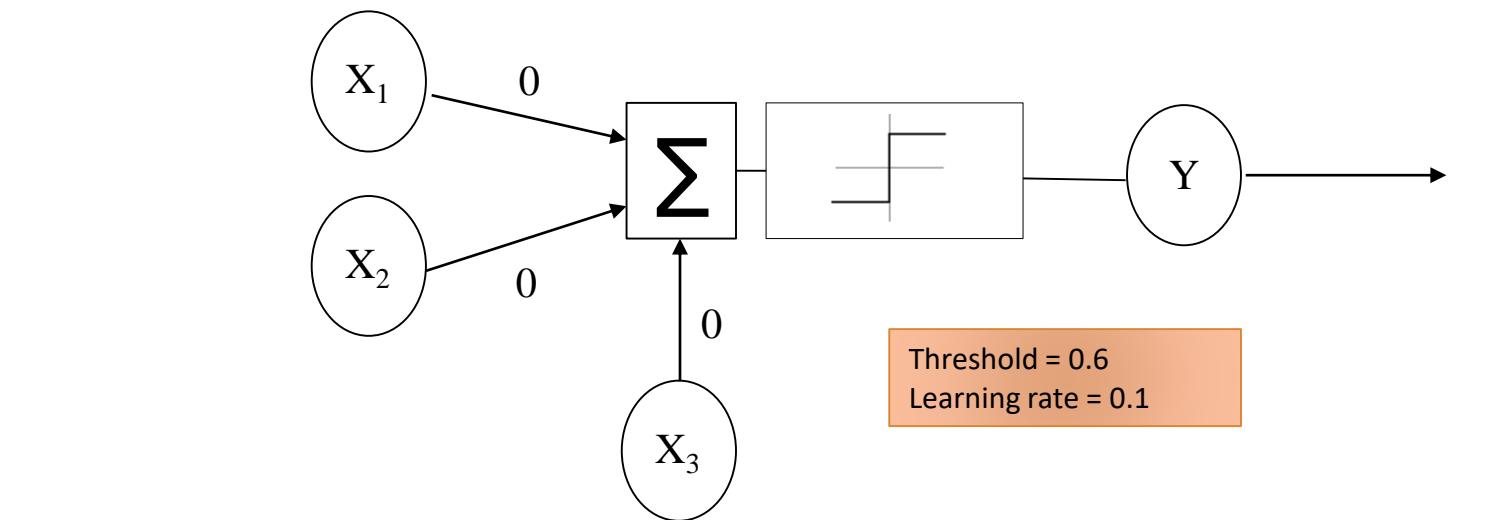
X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	Sum	Output	Error	Correction
0	0	1	0.0	0.1	0.4				
0	1	1							
1	0	1							
1	1	1							



Input 1	Input 2	Desired Output
0	0	1
0	1	1
1	0	1
1	1	0

# TRAINING A PERCEPTRON

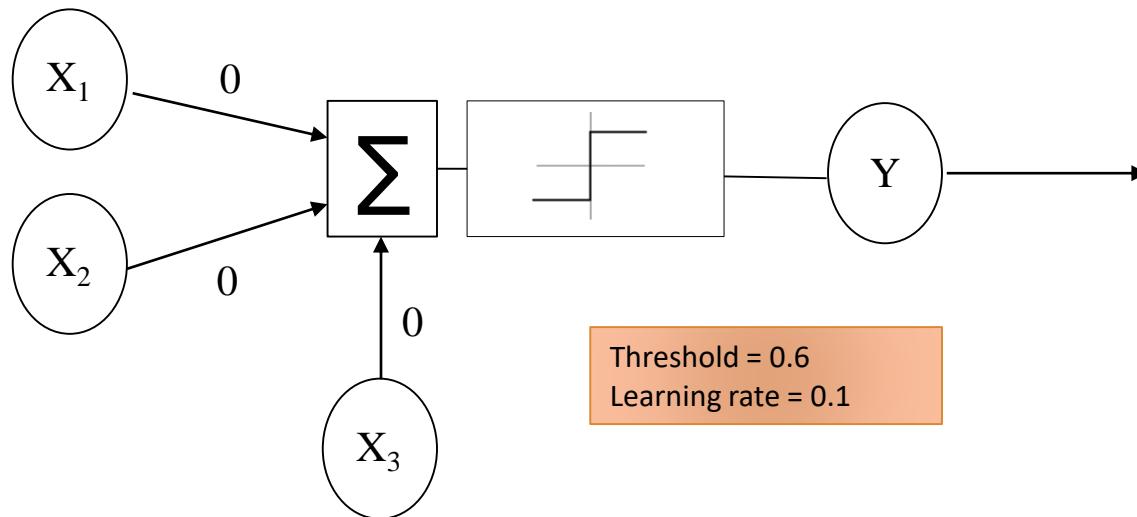
X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	Sum	Output	Error	Correction
0	0	1	0.0	0.1	0.4	0.4	0	1	+0.1
0	1	1							
1	0	1							
1	1	1							



Input 1	Input 2	Desired Output
0	0	1
0	1	1
1	0	1
1	1	0

# TRAINING A PERCEPTRON

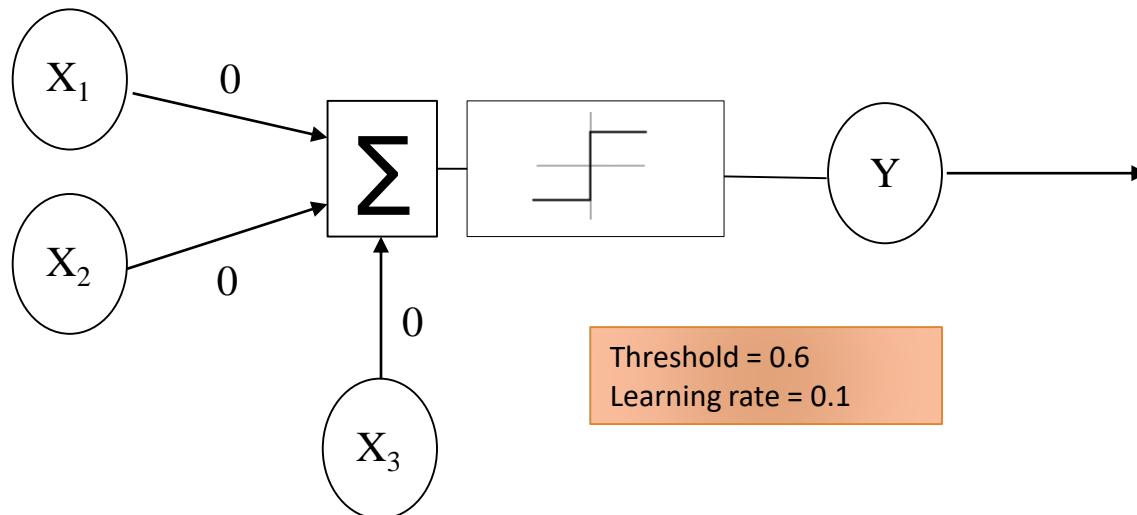
X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	Sum	Output	Error	Correction
0	0	1	0.0	0.1	0.4	0.4	0	1	+0.1
0	1	1	0.0	0.1	0.5				
1	0	1							
1	1	1							



Input 1	Input 2	Desired Output
0	0	1
0	1	1
1	0	1
1	1	0

# TRAINING A PERCEPTRON

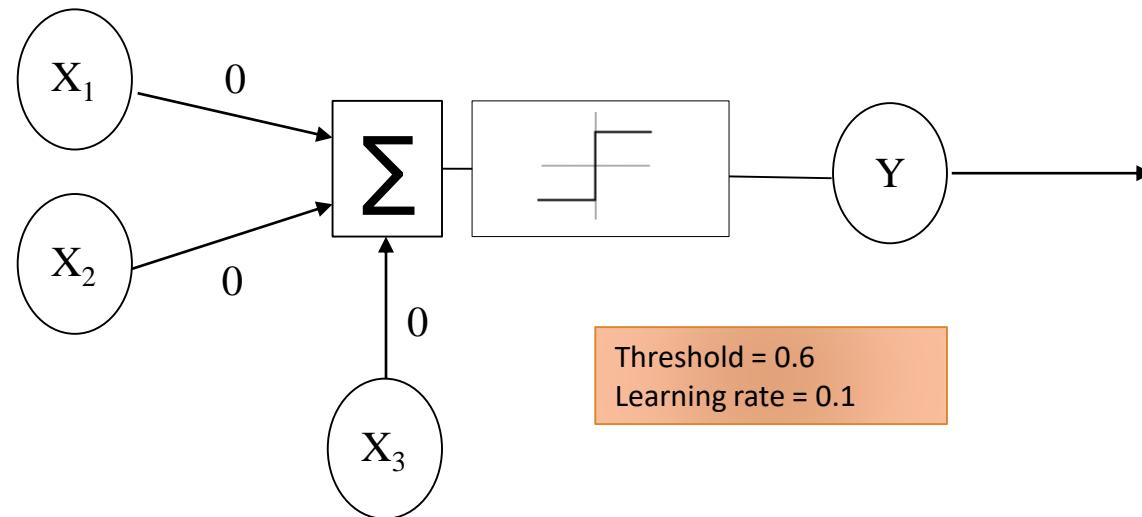
X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	Sum	Output	Error	Correction
0	0	1	0.0	0.1	0.4	0.4	0	1	+0.1
0	1	1	0.0	0.1	0.5	0.6	1	0	-0.0
1	0	1							
1	1	1							



Input 1	Input 2	Desired Output
0	0	1
0	1	1
1	0	1
1	1	0

# TRAINING A PERCEPTRON

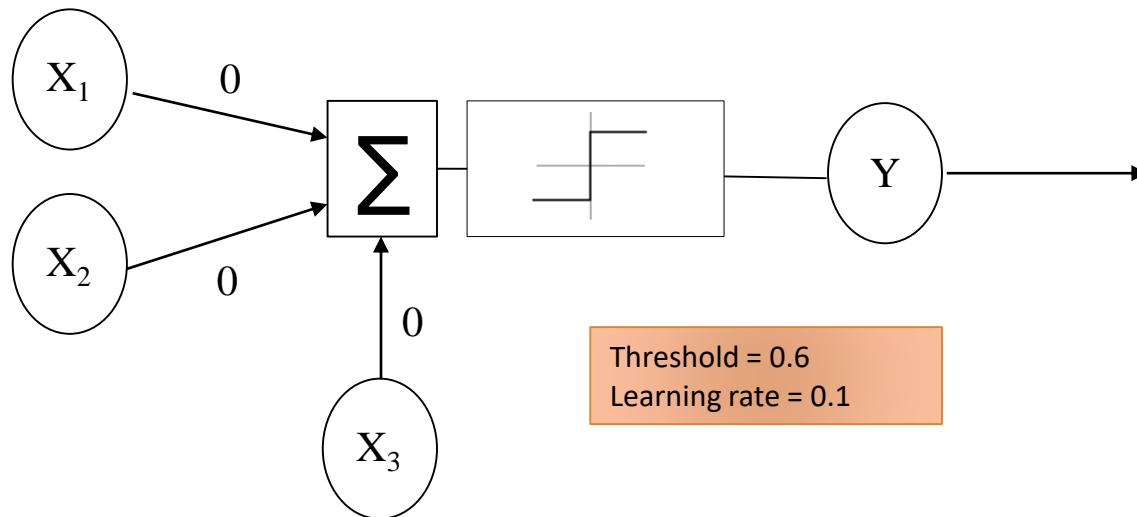
X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	Sum	Output	Error	Correction
0	0	1	0.0	0.1	0.4	0.4	0	1	+0.1
0	1	1	0.0	0.1	0.5	0.6	1	0	-0.0
1	0	1	0.0	0.1	0.5	0.5	0	1	+0.1
1	1	1							



Input 1	Input 2	Desired Output
0	0	1
0	1	1
1	0	1
1	1	0

# TRAINING A PERCEPTRON

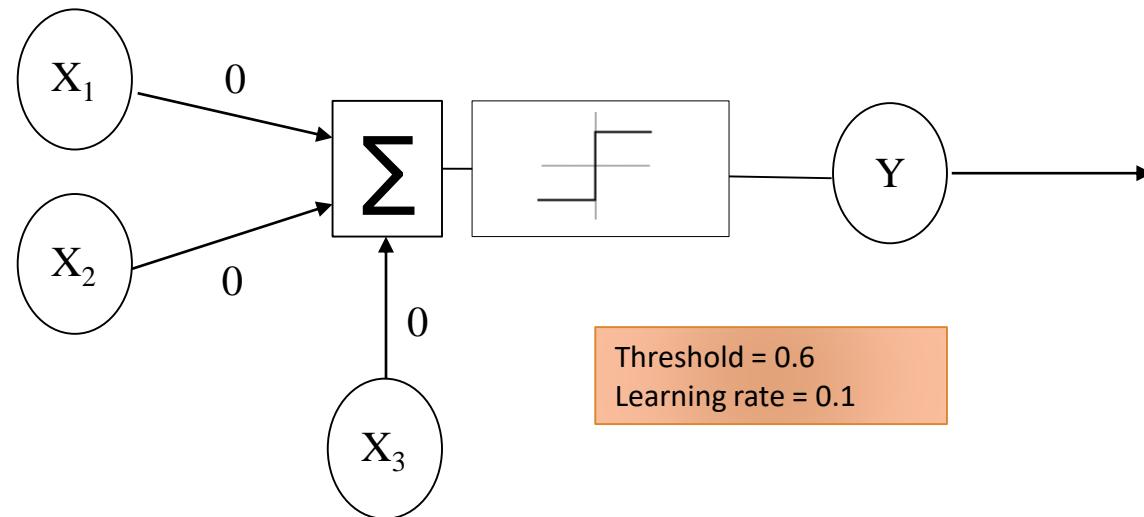
X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	Sum	Output	Error	Correction
0	0	1	0.0	0.1	0.4	0.4	0	1	+0.1
0	1	1	0.0	0.1	0.5	0.6	1	0	-0.0
1	0	1	0.0	0.1	0.5	0.5	0	1	+0.1
1	1	1	0.1	0.1	0.6	0.8	1	-1	-0.1



Input 1	Input 2	Desired Output
0	0	1
0	1	1
1	0	1
1	1	0

# TRAINING A PERCEPTRON

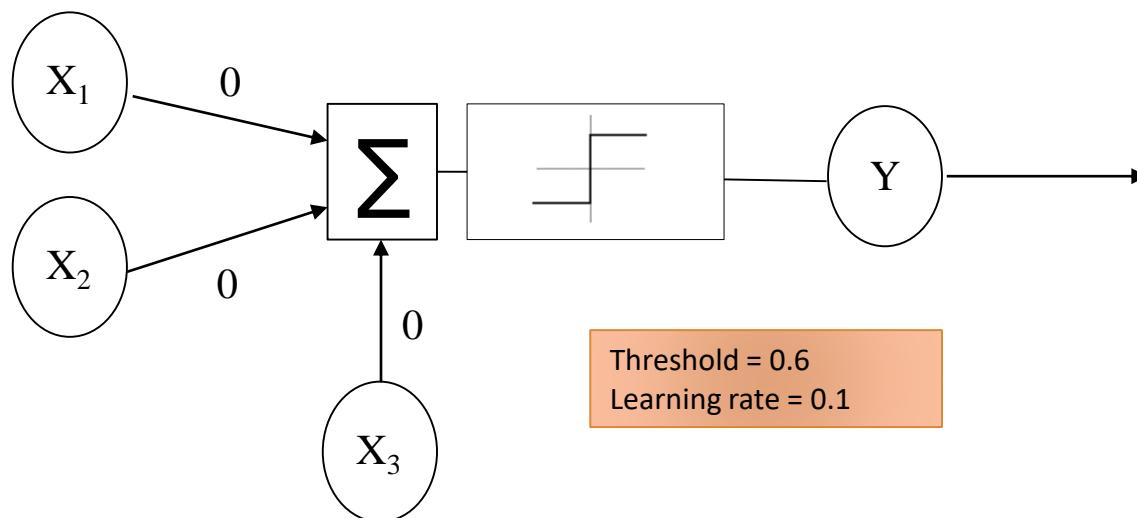
X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	Sum	Output	Error	Correction
0	0	1	0.0	0.0	0.5	0.5	0	1	+0.1
0	1	1							
1	0	1							
1	1	1							



Input 1	Input 2	Desired Output
0	0	1
0	1	1
1	0	1
1	1	0

# TRAINING A PERCEPTRON

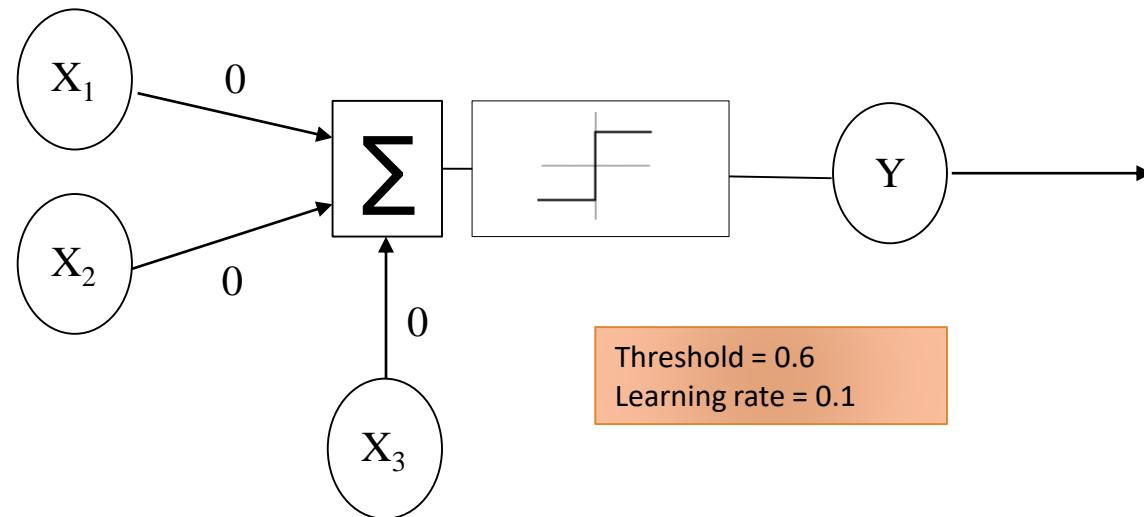
X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	Sum	Output	Error	Correction
0	0	1	0.0	0.0	0.5	0.5	0	1	+0.1
0	1	1	0.0	0.0	0.6	0.6	1	0	-0.0
1	0	1							
1	1	1							



Input 1	Input 2	Desired Output
0	0	1
0	1	1
1	0	1
1	1	0

# TRAINING A PERCEPTRON

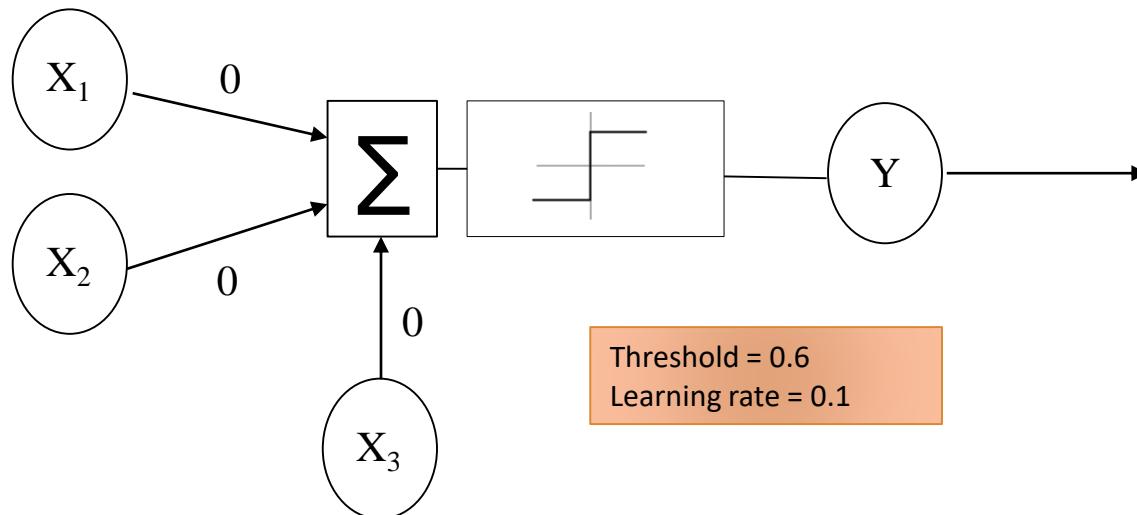
X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	Sum	Output	Error	Correction
0	0	1	0.0	0.0	0.5	0.5	0	1	+0.1
0	1	1	0.0	0.0	0.6	0.6	1	0	±0.0
1	0	1	0.0	0.0	0.6	0.6	1	0	±0.0
1	1	1							



Input 1	Input 2	Desired Output
0	0	1
0	1	1
1	0	1
1	1	0

# TRAINING A PERCEPTRON

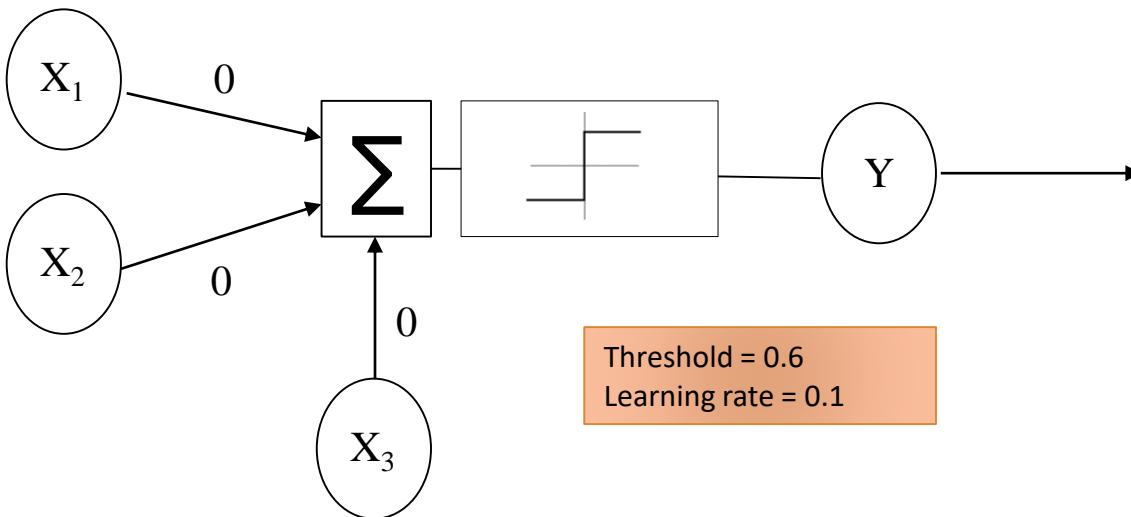
X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	Sum	Output	Error	Correction
0	0	1	0.0	0.0	0.5	0.5	0	1	+0.1
0	1	1	0.0	0.0	0.6	0.6	1	0	±0.0
1	0	1	0.0	0.0	0.6	0.6	1	0	±0.0
1	1	1	0.0	0.0	0.6	0.6	1	-1	-0.1



Input 1	Input 2	Desired Output
0	0	1
0	1	1
1	0	1
1	1	0

# TRAINING A PERCEPTRON

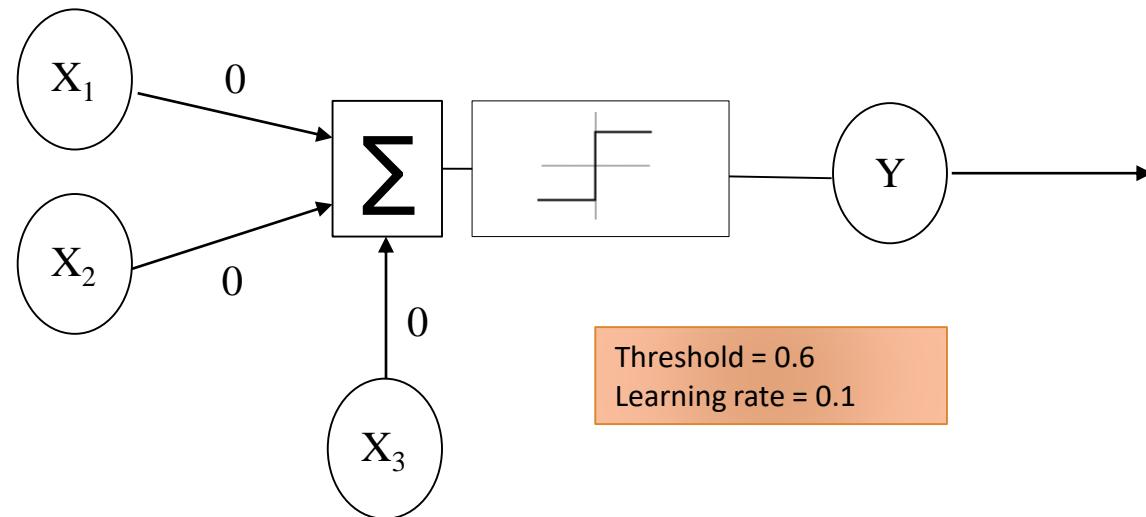
X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	Sum	Output	Error	Correction
0	0	1	-0.1	-0.1	0.5	0.5	0	1	+0.1
0	1	1							
1	0	1							
1	1	1							



Input 1	Input 2	Desired Output
0	0	1
0	1	1
1	0	1
1	1	0

# TRAINING A PERCEPTRON

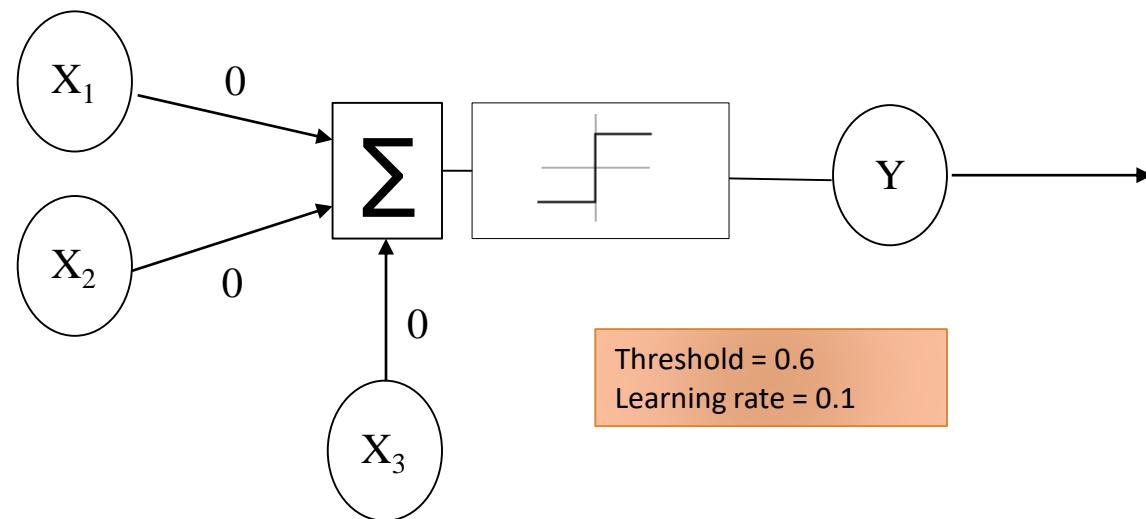
X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	Sum	Output	Error	Correction
0	0	1	-0.1	-0.1	0.5	0.5	0	1	+0.1
0	1	1	-0.1	-0.1	0.6	0.5	0	1	+0.1
1	0	1							
1	1	1							



Input 1	Input 2	Desired Output
0	0	1
0	1	1
1	0	1
1	1	0

# TRAINING A PERCEPTRON

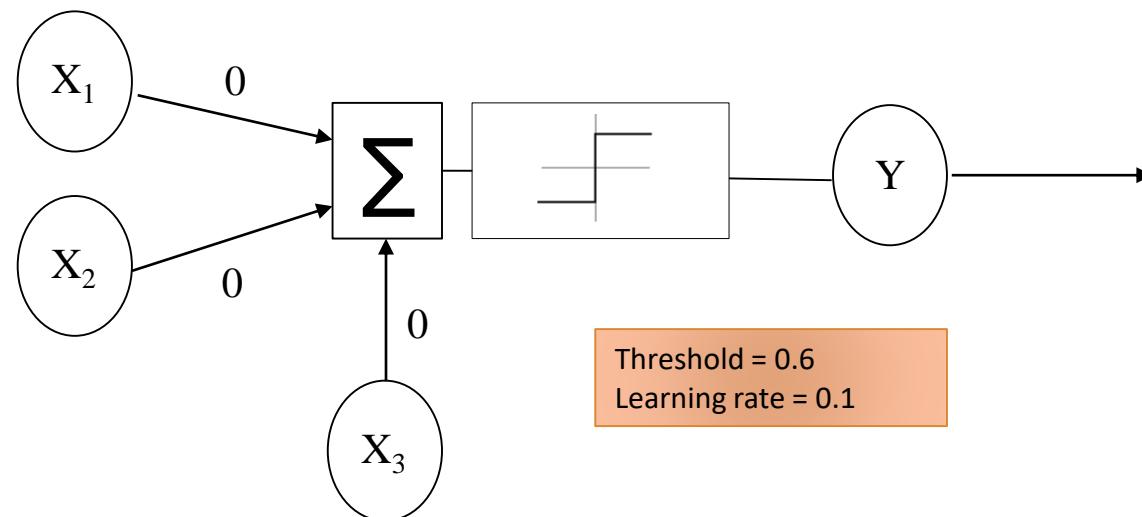
X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	Sum	Output	Error	Correction
0	0	1	-0.1	-0.1	0.5	0.5	0	1	+0.1
0	1	1	-0.1	-0.1	0.6	0.5	0	1	+0.1
1	0	1	-0.1	0.0	0.7	0.6	1	0	±0.0
1	1	1							



Input 1	Input 2	Desired Output
0	0	1
0	1	1
1	0	1
1	1	0

# TRAINING A PERCEPTRON

X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	Sum	Output	Error	Correction
0	0	1	-0.1	-0.1	0.5	0.5	0	1	+0.1
0	1	1	-0.1	-0.1	0.6	0.5	0	1	+0.1
1	0	1	-0.1	0.0	0.7	0.6	1	0	±0.0
1	1	1	-0.1	0.0	0.7	0.6	1	-1	-0.1

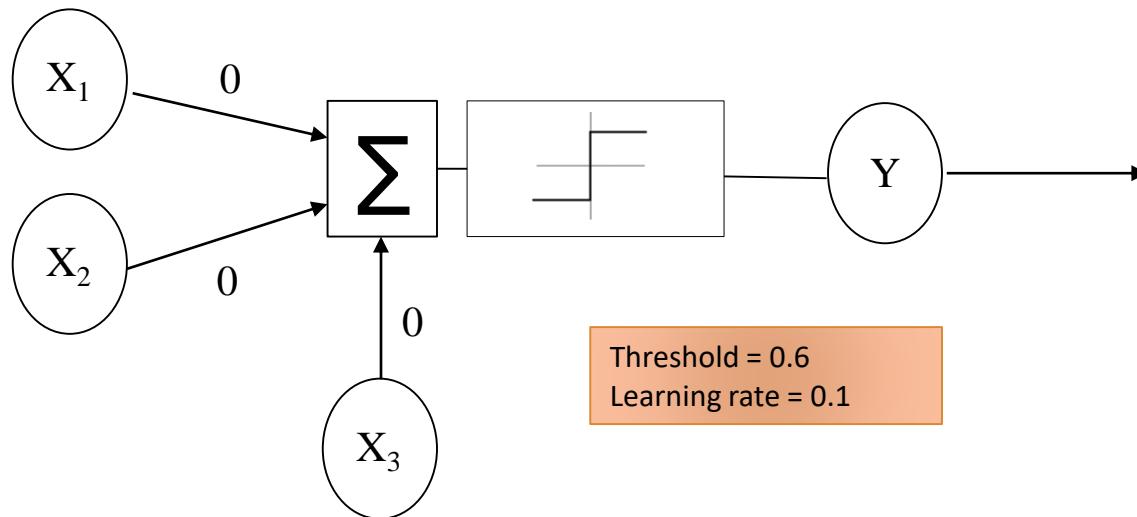




Input 1	Input 2	Desired Output
0	0	1
0	1	1
1	0	1
1	1	0

# TRAINING A PERCEPTRON

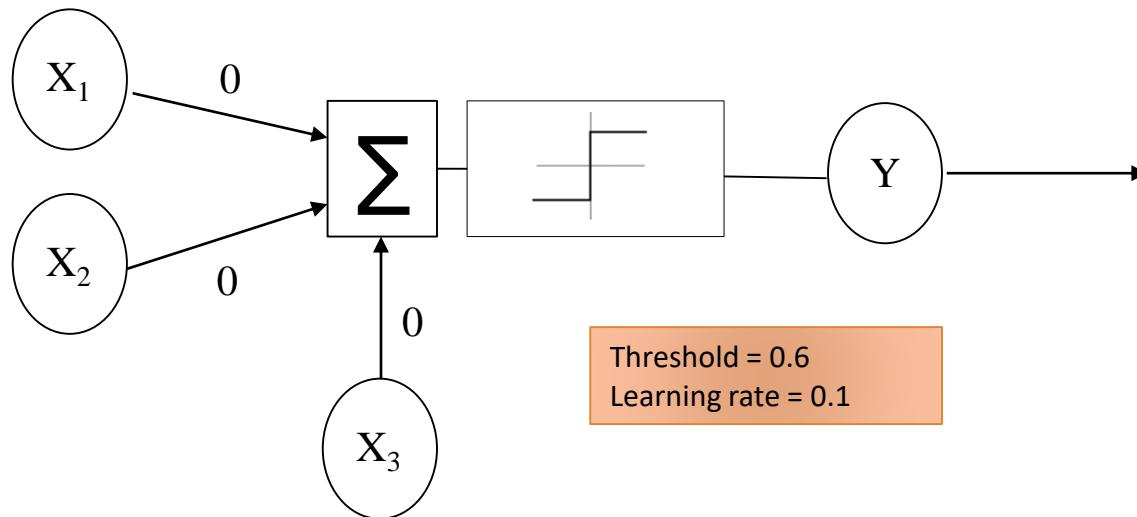
X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	Sum	Output	Error	Correction
0	0	1	-0.2	-0.1	0.6	0.6	1	0	±0.0
0	1	1	-0.2	-0.1	0.6	0.5	0	1	+0.1
1	0	1	-0.2	0.0	0.7	0.5	0	1	+0.1
1	1	1	-0.1	0.0	0.8	0.7	1	-1	-0.1



Input 1	Input 2	Desired Output
0	0	1
0	1	1
1	0	1
1	1	0

# TRAINING A PERCEPTRON

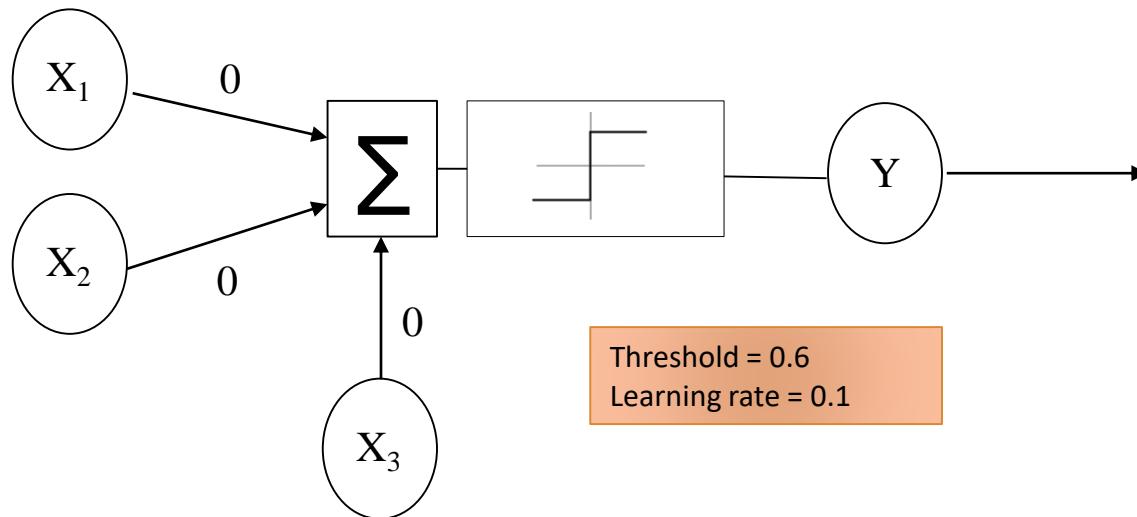
X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	Sum	Output	Error	Correction
0	0	1	-0.2	-0.1	0.7				
0	1	1							
1	0	1							
1	1	1							



Input 1	Input 2	Desired Output
0	0	1
0	1	1
1	0	1
1	1	0

# TRAINING A PERCEPTRON

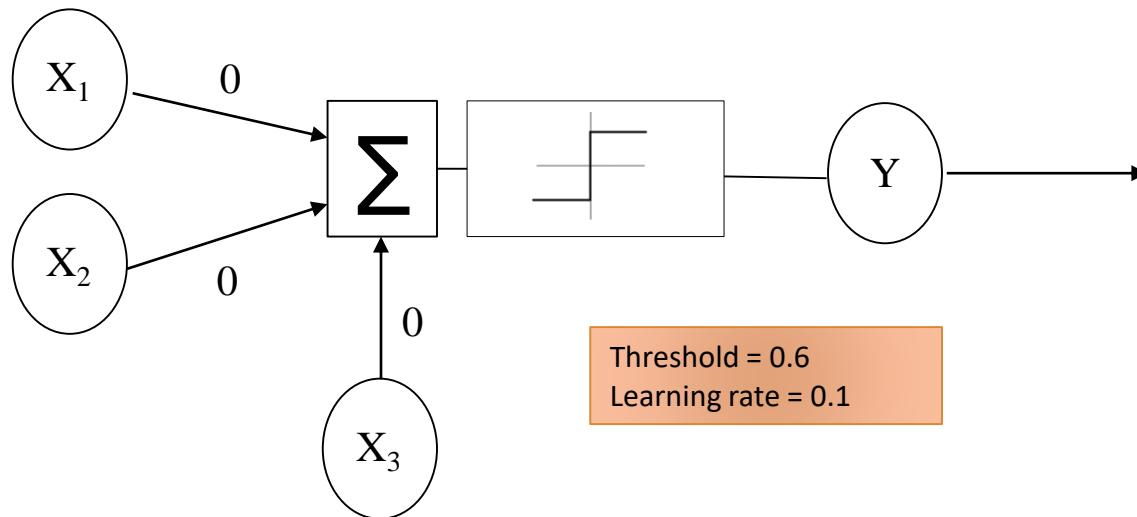
X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	Sum	Output	Error	Correction
0	0	1	-0.2	-0.1	0.7	0.7	1	0	±0.0
0	1	1	-0.2	-0.1	0.7	0.6	1	0	±0.0
1	0	1							
1	1	1							



Input 1	Input 2	Desired Output
0	0	1
0	1	1
1	0	1
1	1	0

# TRAINING A PERCEPTRON

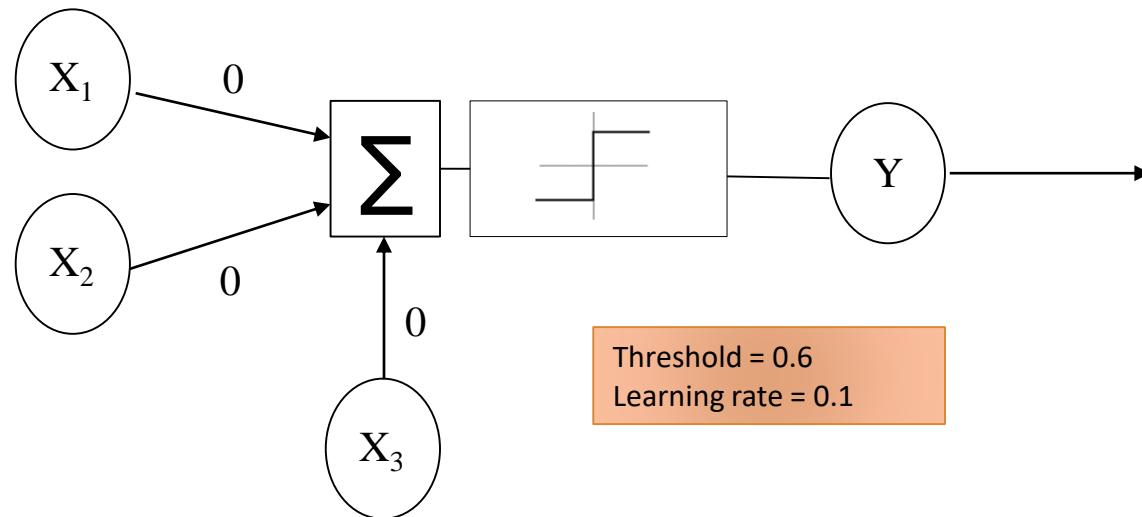
X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	Sum	Output	Error	Correction
0	0	1	-0.2	-0.1	0.7	0.7	1	0	±0.0
0	1	1	-0.2	-0.1	0.7	0.6	1	0	±0.0
1	0	1	-0.2	-0.1	0.7	0.5	0	1	+0.1
1	1	1	-0.1	-0.1	0.8	0.6	1	-1	-0.1



Input 1	Input 2	Desired Output
0	0	1
0	1	1
1	0	1
1	1	0

# TRAINING A PERCEPTRON

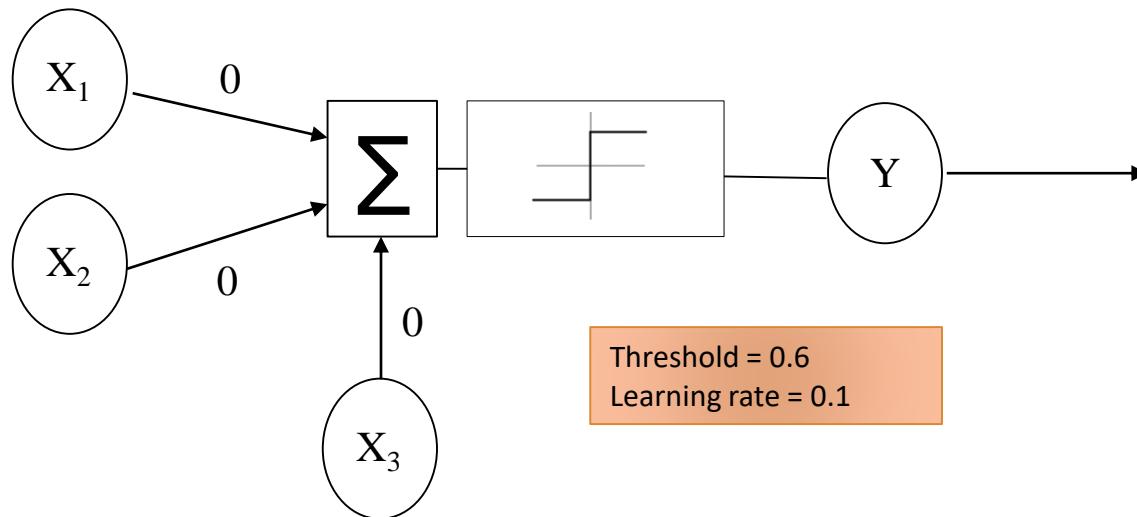
X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	Sum	Output	Error	Correction
0	0	1	-0.2	-0.2	0.7	0.7	1	0	±0.0
0	1	1	-0.2	-0.2	0.7	0.5	0	1	+0.1
1	0	1							
1	1	1							



Input 1	Input 2	Desired Output
0	0	1
0	1	1
1	0	1
1	1	0

# TRAINING A PERCEPTRON

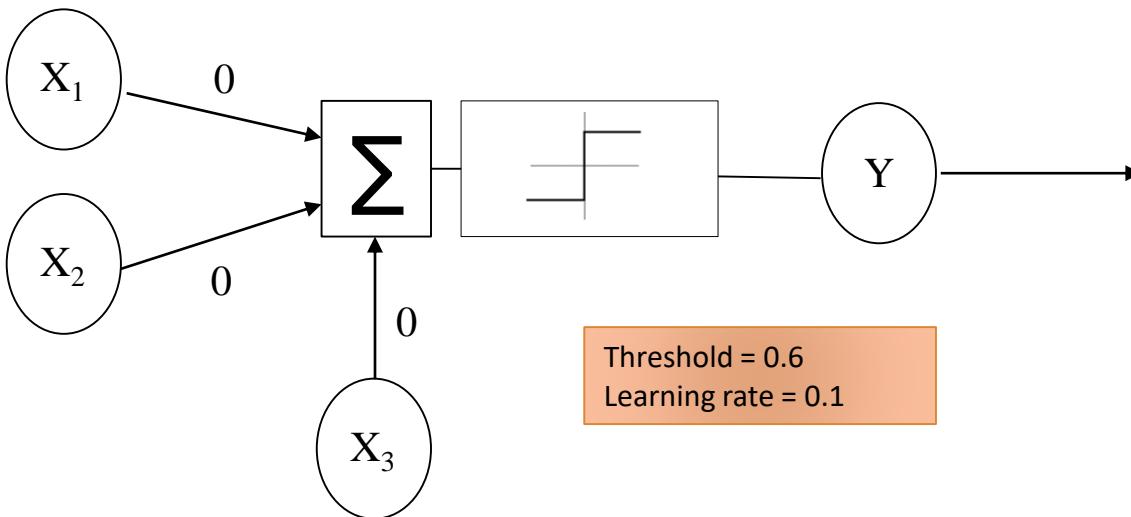
X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	Sum	Output	Error	Correction
0	0	1	-0.2	-0.2	0.7	0.7	1	0	±0.0
0	1	1	-0.2	-0.2	0.7	0.5	0	1	+0.1
1	0	1	-0.2	-0.1	0.8	0.6	1	0	±0.0
1	1	1	-0.2	-0.1	0.8	0.5	0	0	±0.0



Input 1	Input 2	Desired Output
0	0	1
0	1	1
1	0	1
1	1	0

# TRAINING A PERCEPTRON

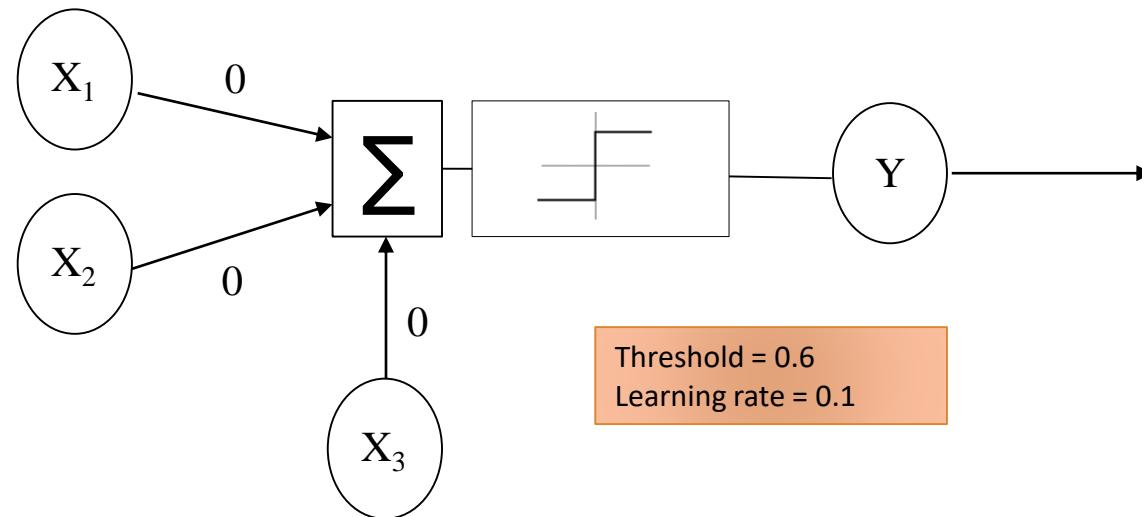
X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	Sum	Output	Error	Correction
0	0	1	-0.2	-0.1	0.8	0.8	1	0	±0.0
0	1	1							
1	0	1							
1	1	1							



Input 1	Input 2	Desired Output
0	0	1
0	1	1
1	0	1
1	1	0

# TRAINING A PERCEPTRON

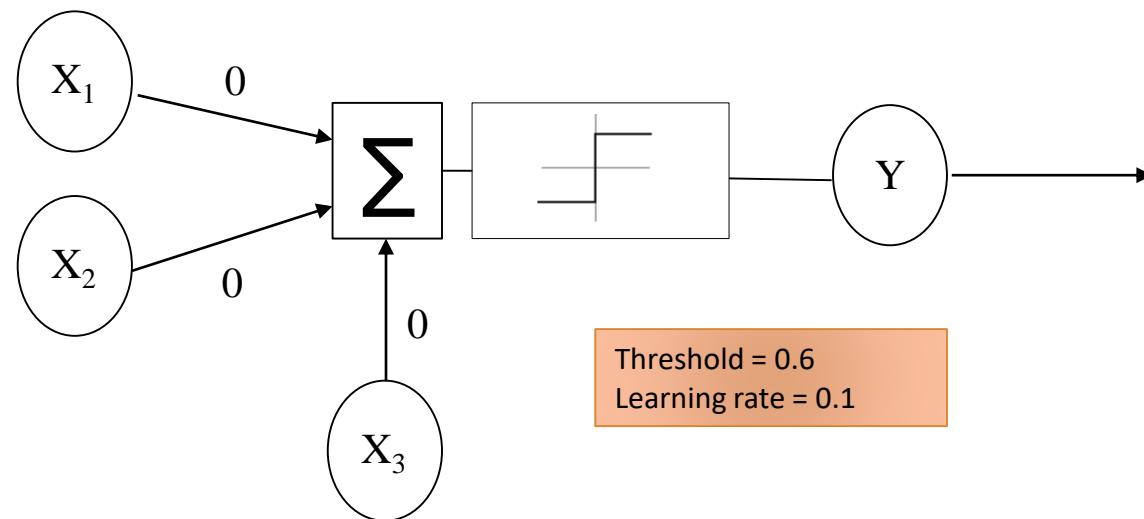
X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	Sum	Output	Error	Correction
0	0	1	-0.2	-0.1	0.8	0.8	1	0	±0.0
0	1	1	-0.2	-0.1	0.8	0.7	1	0	±0.0
1	0	1							
1	1	1							



Input 1	Input 2	Desired Output
0	0	1
0	1	1
1	0	1
1	1	0

# TRAINING A PERCEPTRON

X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	Sum	Output	Error	Correction
0	0	1	-0.2	-0.1	0.8	0.7	1	0	±0.0
0	1	1	-0.2	-0.1	0.8	0.7	1	0	±0.0
1	0	1	-0.2	-0.1	0.8	0.6	1	0	±0.0
1	1	1							



Input 1	Input 2	Desired Output
0	0	1
0	1	1
1	0	1
1	1	0

# TRAINING A PERCEPTRON

X <sub>1</sub>	X <sub>2</sub>	X <sub>3</sub>	W <sub>1</sub>	W <sub>2</sub>	W <sub>3</sub>	Sum	Output	Error	Correction
0	0	1	-0.2	-0.1	0.8	0.7	1	0	±0.0
0	1	1	-0.2	-0.1	0.8	0.7	1	0	±0.0
1	0	1	-0.2	-0.1	0.8	0.6	1	0	±0.0
1	1	1	-0.2	-0.1	0.8	0.5	0	0	±0.0

