



Standard Code Library

Part3 - String

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Section.5 字符串

后缀自动机

- 广义后缀自动机如果直接使用以下代码的话会产生一些冗余状态（置 last 为 1），所以要用拓扑排序。用 len 基数排序不能。
- 字符集大的话要使用 **map**。
- 树上 dp 时注意边界（root 和 null）。
- rsort 中的数组 a 是拓扑序 [1, sz)

```
1 struct SAM{
2     int ch[N << 1][26], fa[N << 1], len[N << 1], vis[N << 1];
3     int last, tot;
4     SAM(): last(1), tot(1) {}
5     inline void extend(int x){ /* 单字符扩展
6         int p = last, np = last = ++tot;
7         len[np] = len[p] + 1, vis[np] = 1;
8         for(; p && !ch[p][x]; p = fa[p]) ch[p][x] = np;
9         if(!p) fa[np] = 1;
10        else{
11            int q = ch[p][x];
12            if(len[q] == len[p] + 1) fa[np] = q;
13            else {
14                int nq = ++tot;
15                for(int i = 0; i < 26; i++) ch[nq][i] = ch[q][i]; //for(int i = 0; i < 26; i++) ch[nq][i] = ch[q][i];
16                fa[nq] = fa[q], fa[np] = fa[q] = nq, len[nq] = len[p] + 1;
17                for(; ch[p][x] == q; p = fa[p]) ch[p][x] = nq;
18            }
19        }
20    }
21 }sam;
```

- 最长公共子串

```
1 /* 最长公共子串
2 string lcs(const string &T) {
3     int v = 0, l = 0, best = 0, bestpos = 0;
4     for (int i = 0; i < T.size(); i++) {
5         while (v && !sam.ch[v][T[i] - 'a']) {
6             v = sam.fa[v];
7             l = sam.len[v];
8         }
9         if (sam.ch[v][T[i] - 'a']) {
10            v = sam.ch[v][T[i] - 'a'];
11            l++;
12        }
13        if (l > best) {
14            best = l;
15            bestpos = i;
16        }
17    }
18    return T.substr(bestpos - best + 1, best);
19 }
```

- 真·广义后缀自动机

```
1 int t[M][26], len[M] = {-1}, fa[M], sz = 2, last = 1;
2 LL cnt[M][2];
3 void ins(int ch, int id) {
4     int p = last, np = 0, nq = 0, q = -1;
5     if (!t[p][ch]) {
6         np = sz++;
7         len[np] = len[p] + 1;
8         for (; p && !t[p][ch]; p = fa[p]) t[p][ch] = np;
9     }
10    if (!p) fa[np] = 1;
11    else {
12        q = t[p][ch];
13        if (len[p] + 1 == len[q]) fa[np] = q;
14        else {
15            nq = sz++; len[nq] = len[p] + 1;
16            memcpy(t[nq], t[q], sizeof t[0]);
```

```

17         fa[nq] = fa[q];
18         fa[np] = fa[q] = nq;
19         for (; t[p][ch] == q; p = fa[p]) t[p][ch] = nq;
20     }
21 }
22 last = np ? np : nq ? nq : q;
23 cnt[last][id] = 1;
24 }

```

- 按字典序建立后缀树注意逆序插入
- rsort2 里的 a 不是拓扑序，需要拓扑序就去树上做

```

1 void ins(int ch, int pp) {
2     int p = last, np = last = sz++;
3     len[np] = len[p] + 1; one[np] = pos[np] = pp;
4     for (; p && !t[p][ch]; p = fa[p]) t[p][ch] = np;
5     if (!p) { fa[np] = 1; return; }
6     int q = t[p][ch];
7     if (len[q] == len[p] + 1) fa[np] = q;
8     else {
9         int nq = sz++; len[nq] = len[p] + 1; one[nq] = one[q];
10        memcpy(t[nq], t[q], sizeof t[0]);
11        fa[nq] = fa[q];
12        fa[q] = fa[np] = nq;
13        for (; p && t[p][ch] == q; p = fa[p]) t[p][ch] = nq;
14    }
15 }
16
17 int up[M], c[256] = {2}, a[M];
18 void rsort2() {
19     FOR (i, 1, 256) c[i] = 0;
20     FOR (i, 2, sz) up[i] = s[one[i] + len[fa[i]]];
21     FOR (i, 2, sz) c[up[i]]++;
22     FOR (i, 1, 256) c[i] += c[i - 1];
23     FOR (i, 2, sz) a[--c[up[i]]] = i;
24     FOR (i, 2, sz) G[fa[a[i]]].push_back(a[i]);
25 }

```

- 广义后缀自动机建后缀树，必须反向插入

```

1 int t[M][26], len[M] = {0}, fa[M], sz = 2, last = 1;
2 char* one[M];
3 void ins(int ch, char* pp) {
4     int p = last, np = 0, nq = 0, q = -1;
5     if (!t[p][ch]) {
6         np = sz++; one[np] = pp;
7         len[np] = len[p] + 1;
8         for (; p && !t[p][ch]; p = fa[p]) t[p][ch] = np;
9     }
10    if (!p) fa[np] = 1;
11    else {
12        q = t[p][ch];
13        if (len[p] + 1 == len[q]) fa[np] = q;
14        else {
15            nq = sz++; len[nq] = len[p] + 1; one[nq] = one[q];
16            memcpy(t[nq], t[q], sizeof t[0]);
17            fa[nq] = fa[q];
18            fa[np] = fa[q] = nq;
19            for (; t[p][ch] == q; p = fa[p]) t[p][ch] = nq;
20        }
21    }
22    last = np ? np : nq ? nq : q;
23 }
24 int up[M], c[256] = {2}, aa[M];
25 vector<int> G[M];
26 void rsort() {
27     FOR (i, 1, 256) c[i] = 0;
28     FOR (i, 2, sz) up[i] = *(one[i] + len[fa[i]]);
29     FOR (i, 2, sz) c[up[i]]++;
30     FOR (i, 1, 256) c[i] += c[i - 1];
31     FOR (i, 2, sz) aa[--c[up[i]]] = i;
32     FOR (i, 2, sz) G[fa[aa[i]]].push_back(aa[i]);

```

```
33 }
```

- 匹配

```
1 int u = 1, l = 0;
2 FOR (i, 0, strlen(s)) {
3     int ch = s[i] - 'a';
4     while (u && !t[u][ch]) { u = fa[u]; l = len[u]; }
5     ++l; u = t[u][ch];
6     if (!u) u = 1;
7     if (l) // do something...
8 }
```

- 获取子串状态

```
1 int get_state(int l, int r) {
2     int u = rpos[r], s = r - l + 1;
3     FOR (i, SP - 1, -1) if (len[pa[u][i]] >= s) u = pa[u][i];
4     return u;
5 }
```

- 配合 LCT

```
1 namespace lct_sam {
2     extern struct P *const null;
3     const int M = N;
4     struct P {
5         P *fa, *ls, *rs;
6         int last;
7
8         bool has_fa() { return fa->ls == this || fa->rs == this; }
9         bool d() { return fa->ls == this; }
10        P*& c(bool x) { return x ? ls : rs; }
11        P* up() { return this; }
12        void down() {
13            if (ls != null) ls->last = last;
14            if (rs != null) rs->last = last;
15        }
16        void all_down() { if (has_fa()) fa->all_down(); down(); }
17    } *const null = new P{0, 0, 0, 0}, pool[M], *pit = pool;
18    P* G[N];
19    int t[M][26], len[M] = {-1}, fa[M], sz = 2, last = 1;
20
21    void rot(P* o) {
22        bool dd = o->d();
23        P *f = o->fa, *t = o->c(!dd);
24        if (f->has_fa()) f->fa->c(f->d()) = o; o->fa = f->fa;
25        if (t != null) t->fa = f; f->c(dd) = t;
26        o->c(!dd) = f->up(); f->fa = o;
27    }
28    void splay(P* o) {
29        o->all_down();
30        while (o->has_fa()) {
31            if (o->fa->has_fa())
32                rot(o->d() ^ o->fa->d() ? o : o->fa);
33            rot(o);
34        }
35        o->up();
36    }
37    void access(int last, P* u, P* v = null) {
38        if (u == null) { v->last = last; return; }
39        splay(u);
40        P *t = u;
41        while (t->ls != null) t = t->ls;
42        int L = len[fa[t - pool]] + 1, R = len[u - pool];
43
44        if (u->last) bit::add(u->last - R + 2, u->last - L + 2, 1);
45        else bit::add(1, 1, R - L + 1);
46        bit::add(last - R + 2, last - L + 2, -1);
47
48        u->rs = v;
49        access(last, u->up()->fa, u);
50    }
51 }
```

```

51 void insert(P* u, P* v, P* t) {
52     if (v != null) { splay(v); v->rs = null; }
53     splay(u);
54     u->fa = t; t->fa = v;
55 }
56
57 void ins(int ch, int pp) {
58     int p = last, np = last = sz++;
59     len[np] = len[p] + 1;
60     for (; p && !t[p][ch]; p = fa[p]) t[p][ch] = np;
61     if (!p) fa[np] = 1;
62     else {
63         int q = t[p][ch];
64         if (len[p] + 1 == len[q]) { fa[np] = q; G[np]->fa = G[q]; }
65         else {
66             int nq = sz++; len[nq] = len[p] + 1;
67             memcpy(t[nq], t[q], sizeof t[0]);
68             insert(G[q], G[fa[q]], G[nq]);
69             G[nq]->last = G[q]->last;
70             fa[nq] = fa[q];
71             fa[np] = fa[q] = nq;
72             G[np]->fa = G[nq];
73             for (; t[p][ch] == q; p = fa[p]) t[p][ch] = nq;
74         }
75     }
76     access(pp + 1, G[np]);
77 }
78
79 void init() {
80     ++pit;
81     FOR (i, 1, N) {
82         G[i] = pit++;
83         G[i]->ls = G[i]->rs = G[i]->fa = null;
84     }
85     G[1] = null;
86 }
87 }

```

- 维护区间本质不同字符串数目
- 给你一个长度为 n 的字符串 s , m 次询问, 第 i 次询问 s 上的一个区间 $[l_i, r_i]$ 上有多少个本质不同的子串

```

1  #include<bits/stdc++.h>
2  using namespace std;
3  #define Re register int
4  typedef long long ll;
5
6  const int N = 200005;
7  struct info
8  {
9      int id, t;
10 };
11 int n, m, lst, num, res, g[N], ls[N], len[N], lk[N], ch[N][28], lt[N], son[N][2];
12 char s[N];
13 bool lz[N];
14 ll sum[N << 2], ad[N << 2], ans[N];
15 vector<info> q[N];
16
17 inline int read()
18 {
19     char c = getchar();
20     int ans = 0;
21     while (c < 48 || c > 57) c = getchar();
22     while (c >= 48 && c <= 57) ans = (ans << 3) + (ans << 1) + (c ^ 48), c = getchar();
23     return ans;
24 }
25
26 inline void write(ll x)
27 {
28     int num = 0;
29     char sc[25];
30     if (!x) sc[num = 1] = 48;

```

```

31     while (x) sc[++num] = x % 10 + 48, x /= 10;
32     while (num) putchar(sc[num--]);
33     putchar('\n');
34 }
35
36 inline void push_down(int id, int l, int mid, int r)
37 {
38     sum[id << 1] += ad[id] * (mid - l + 1), sum[id << 1 | 1] += ad[id] * (r - mid);
39     ad[id << 1] += ad[id], ad[id << 1 | 1] += ad[id];
40     ad[id] = 0;
41 }
42
43 inline void modify(int id, int l, int r, int x, int y, int z)
44 {
45     if (x <= l && r <= y)
46     {
47         sum[id] += 1ll * z * (r - l + 1), ad[id] += z;
48         return;
49     }
50     int mid = l + r >> 1;
51     if (ad[id]) push_down(id, l, mid, r);
52     if (x <= mid) modify(id << 1, l, mid, x, y, z);
53     if (y > mid) modify(id << 1 | 1, mid + 1, r, x, y, z);
54     sum[id] = sum[id << 1] + sum[id << 1 | 1];
55 }
56
57 inline ll que(int id, int l, int r, int x, int y)
58 {
59     if (x <= l && r <= y) return sum[id];
60     int mid = l + r >> 1;
61     ll ans = 0;
62     if (ad[id]) push_down(id, l, mid, r);
63     if (x <= mid) ans = que(id << 1, l, mid, x, y);
64     if (y > mid) ans += que(id << 1 | 1, mid + 1, r, x, y);
65     return ans;
66 }
67
68 inline bool check(int x)
69 {
70     return son[lk[x]][0] == x || son[lk[x]][1] == x;
71 }
72
73 inline void pushdown(int x)
74 {
75     if (son[x][0]) lt[son[x][0]] = lt[x], lz[son[x][0]] = 1;
76     if (son[x][1]) lt[son[x][1]] = lt[x], lz[son[x][1]] = 1;
77     lz[x] = 0;
78 }
79
80 inline void rotate(int x)
81 {
82     int y = lk[x], z = lk[y];
83     bool t = son[y][1] ^ x;
84     if (check(y)) son[z][son[z][1] == y] = x;
85     lk[x] = z, lk[y] = x;
86     if (son[x][t]) lk[son[x][t]] = y;
87     son[y][t ^ 1] = son[x][t], son[x][t] = y;
88 }
89
90 inline void splay(int x)
91 {
92     g[res = 1] = x;
93     while (check(g[res])) g[res + 1] = lk[g[res]], ++res;
94     while (res)
95     {
96         if (lz[g[res]]) pushdown(g[res]);
97         --res;
98     }
99     while (check(x))
100     {
101         int y = lk[x];

```



```

102         if (check(y)) rotate(((son[y][1] == x) ^ (son[lk[y]][1] == y)) ? x : y);
103         rotate(x);
104     }
105 }
106
107 inline int find(int x)
108 {
109     if (!x) return 0;
110     splay(x);
111     while (son[x][1]) x = son[x][1];
112     return len[x];
113 }
114
115 inline void access(int x, int y)
116 {
117     for (Re i = 0; x; x = lk[i = x])
118     {
119         splay(x);
120         if (lz[x]) pushdown(x);
121         if (lt[x]) modify(1, 1, n, lt[x] - len[x] + 1, lt[x] - len[lk[x]], -1);
122         son[x][1] = i;
123     }
124     splay(1), lt[1] = y, lz[1] = 1;
125 }
126
127 inline void ins(int x)
128 {
129     int y = ++num;
130     len[y] = len[lst] + 1;
131     while (lst && !ch[lst][x]) ch[lst][x] = y, lst = lk[lst];
132     if (lst)
133     {
134         int q = ch[lst][x];
135         if (len[q] == len[lst] + 1) lk[y] = q;
136         else
137         {
138             len[++num] = len[lst] + 1, lk[num] = lk[q], lk[q] = lk[y] = num;
139             memcpy(ch[num], ch[q], sizeof ch[num]);
140             while (lst && ch[lst][x] == q) ch[lst][x] = num, lst = lk[lst];
141         }
142     }
143     else lk[y] = 1;
144     lst = y;
145 }
146
147 int main()
148 {
149     scanf("%s", s + 1);
150     n = strlen(s + 1), m = read();
151     for (Re i = 0; i < m; ++i)
152     {
153         int u = read(), v = read();
154         q[v].push_back(info{i, u});
155     }
156     lst = num = 1;
157     for (Re i = 1; i <= n; ++i) ins(s[i] - 97), ls[i] = lst;
158     for (Re i = 1; i <= n; ++i)
159     {
160         access(ls[i], i), modify(1, 1, n, 1, i, 1);
161         int u = q[i].size();
162         for (Re j = 0; j < u; ++j) ans[q[i][j].id] = que(1, 1, n, q[i][j].t, i);
163     }
164     for (Re i = 0; i < m; ++i) write(ans[i]);
165     return 0;
166 }
167

```

回文自动机

- num 是该结点表示的前缀的回文后缀个数

- cnt 是该结点表示的回文串在原串中的出现次数（使用前需要向父亲更新）

```

1 namespace pam {
2     int t[N][26], fa[N], len[N], rs[N], cnt[N], num[N];
3     int sz, n, last;
4     int _new(int l) {
5         len[sz] = l; cnt[sz] = num[sz] = 0;
6         return sz++;
7     }
8     void init() {
9         memset(t, 0, sz * sizeof t[0]);
10        rs[n = sz = 0] = -1;
11        last = _new(0);
12        fa[last] = _new(-1);
13    }
14    int get_fa(int x) {
15        while (rs[n - 1 - len[x]] != rs[n]) x = fa[x];
16        return x;
17    }
18    void ins(int ch) {
19        rs[++n] = ch;
20        int p = get_fa(last);
21        if (!t[p][ch]) {
22            int np = _new(len[p] + 2);
23            num[np] = num[fa[np]] = t[get_fa(fa[p])][ch] + 1;
24            t[p][ch] = np;
25        }
26        ++cnt[last = t[p][ch]];
27    }
28 }

```

manacher

```

1 int RL[N];
2 void manacher(int* a, int n) { // "abc" => "#a#b#a#"
3     int r = 0, p = 0;
4     FOR (i, 0, n) {
5         if (i < r) RL[i] = min(RL[2 * p - i], r - i);
6         else RL[i] = 1;
7         while (i - RL[i] >= 0 && i + RL[i] < n && a[i - RL[i]] == a[i + RL[i]])
8             RL[i]++;
9         if (RL[i] + i - 1 > r) { r = RL[i] + i - 1; p = i; }
10    }
11    FOR (i, 0, n) --RL[i];
12 }
13

```

哈希

内置了自动双哈希开关（小心 TLE）。

```

1 #include <bits/stdc++.h>
2 using namespace std;
3
4 #define ENABLE_DOUBLE_HASH
5
6 typedef long long LL;
7 typedef unsigned long long ULL;
8
9 const int x = 135;
10 const int N = 4e5 + 10;
11 const int p1 = 1e9 + 7, p2 = 1e9 + 9;
12 ULL xp1[N], xp2[N], xp[N];
13
14 void init_xp() {
15     xp1[0] = xp2[0] = xp[0] = 1;
16     for (int i = 1; i < N; ++i) {
17         xp1[i] = xp1[i - 1] * x % p1;
18         xp2[i] = xp2[i - 1] * x % p2;
19         xp[i] = xp[i - 1] * x;
20     }
21 }

```

```

20     }
21 }
22
23 struct String {
24     char s[N];
25     int length, subsize;
26     bool sorted;
27     ULL h[N], hl[N];
28
29     ULL hash() {
30         length = strlen(s);
31         ULL res1 = 0, res2 = 0;
32         h[length] = 0; // ATTENTION!
33         for (int j = length - 1; j >= 0; --j) {
34             #ifdef ENABLE_DOUBLE_HASH
35                 res1 = (res1 * x + s[j]) % p1;
36                 res2 = (res2 * x + s[j]) % p2;
37                 h[j] = (res1 << 32) | res2;
38             #else
39                 res1 = res1 * x + s[j];
40                 h[j] = res1;
41             #endif
42             // printf("%llu\n", h[j]);
43         }
44         return h[0];
45     }
46
47     // 获取子串哈希, 左闭右开区间
48     ULL get_substring_hash(int left, int right) const {
49         int len = right - left;
50         #ifdef ENABLE_DOUBLE_HASH
51             // get hash of s[left...right-1]
52             unsigned int mask32 = ~(0u);
53             ULL left1 = h[left] >> 32, right1 = h[right] >> 32;
54             ULL left2 = h[left] & mask32, right2 = h[right] & mask32;
55             return (((left1 - right1 * xp1[len] % p1 + p1) % p1) << 32) |
56                 (((left2 - right2 * xp2[len] % p2 + p2) % p2));
57         #else
58             return h[left] - h[right] * xp[len];
59         #endif
60     }
61
62     void get_all_subs_hash(int sublen) {
63         subsize = length - sublen + 1;
64         for (int i = 0; i < subsize; ++i)
65             hl[i] = get_substring_hash(i, i + sublen);
66         sorted = 0;
67     }
68
69     void sort_substring_hash() {
70         sort(hl, hl + subsize);
71         sorted = 1;
72     }
73
74     bool match(ULL key) const {
75         if (!sorted) assert (0);
76         if (!subsize) return false;
77         return binary_search(hl, hl + subsize, key);
78     }
79
80     void init(const char *t) {
81         length = strlen(t);
82         strcpy(s, t);
83     }
84 };
85
86 int LCP(const String &a, const String &b, int ai, int bi) {
87     // Find LCP of a[ai...] and b[bi...]
88     int l = 0, r = min(a.length - ai, b.length - bi);
89     while (l < r) {
90         int mid = (l + r + 1) / 2;

```

```

91         if (a.get_substring_hash(ai, ai + mid) == b.get_substring_hash(bi, bi + mid))
92             l = mid;
93         else r = mid - 1;
94     }
95     return l;
96 }
97
98 int check(int ans) {
99     if (T.length < ans) return 1;
100    T.get_all_subs_hash(ans); T.sort_substring_hash();
101    for (int i = 0; i < S.length - ans + 1; ++i)
102        if (!T.match(S.get_substring_hash(i, i + ans)))
103            return 1;
104    return 0;
105 }
106
107 int main() {
108     init_xp(); // DON'T FORGET TO DO THIS!
109
110     for (int tt = 1; tt <= kases; ++tt) {
111         scanf("%d", &n); scanf("%s", str);
112         S.init(str);
113         S.hash(); T.hash();
114     }
115 }

```

二维哈希

```

1 struct Hash2D { // 1-index
2     static const LL px = 131, py = 233, MOD = 998244353;
3     static LL pwx[N], pwy[N];
4     int a[N][N];
5     LL hv[N][N];
6     static void init_xp() {
7         pwx[0] = pwy[0] = 1;
8         FOR (i, 1, N) {
9             pwx[i] = pwx[i - 1] * px % MOD;
10            pwy[i] = pwy[i - 1] * py % MOD;
11        }
12    }
13    void init_hash(int n, int m) {
14        FOR (i, 1, n + 1) {
15            LL s = 0;
16            FOR (j, 1, m + 1) {
17                s = (s * py + a[i][j]) % MOD;
18                hv[i][j] = (hv[i - 1][j] * px + s) % MOD;
19            }
20        }
21    }
22    LL h(int x, int y, int dx, int dy) {
23        --x; --y;
24        LL ret = hv[x + dx][y + dy] + hv[x][y] * pwx[dx] % MOD * pwy[dy]
25            - hv[x][y + dy] * pwx[dx] - hv[x + dx][y] * pwy[dy];
26        return (ret % MOD + MOD) % MOD;
27    }
28 } ha, hb;
29 LL Hash2D::pwx[N], Hash2D::pwy[N];

```

后缀数组

构造时间: $O(L \log L)$; 查询时间 $O(\log L)$ 。**suffix** 数组是排好序的后缀下标, **suffix** 的反数组是后缀数组。

```

1 #include <bits/stdc++.h>
2 using namespace std;
3
4 const int N = 2e5 + 10;
5 const int Nlog = 18;
6
7 struct SuffixArray {
8     const int L;
9     vector<vector<int>> > P;

```

```

10 vector<pair<pair<int, int>, int> > M;
11 int s[N], sa[N], rank[N], height[N];
12 // s: raw string
13 // sa[i]=k: s[k...L-1] ranks i (0 based)
14 // rank[i]=k: the rank of s[i...L-1] is k (0 based)
15 // height[i] = lcp(sa[i-1], sa[i])
16
17 SuffixArray(const string &raw_s) : L(raw_s.length()), P(1, vector<int>(L, 0)), M(L) {
18     for (int i = 0; i < L; i++)
19         P[0][i] = this->s[i] = int(raw_s[i]);
20     for (int skip = 1, level = 1; skip < L; skip *= 2, level++) {
21         P.push_back(vector<int>(L, 0));
22         for (int i = 0; i < L; i++)
23             M[i] = make_pair(make_pair(P[level - 1][i], i + skip < L ? P[level - 1][i + skip] : -1000), i);
24         sort(M.begin(), M.end());
25         for (int i = 0; i < L; i++)
26             P[level][M[i].second] = (i > 0 && M[i].first == M[i - 1].first) ? P[level][M[i - 1].second] : i;
27     }
28     for (unsigned i = 0; i < P.back().size(); ++i) {
29         rank[i] = P.back()[i];
30         sa[rank[i]] = i;
31     }
32 }
33
34 // This is a traditional way to calculate LCP
35 void getHeight() {
36     memset(height, 0, sizeof height);
37     int k = 0;
38     for (int i = 0; i < L; ++i) {
39         if (rank[i] == 0) continue;
40         if (k) k--;
41         int j = sa[rank[i] - 1];
42         while (i + k < L && j + k < L && s[i + k] == s[j + k]) ++k;
43         height[rank[i]] = k;
44     }
45     rmq_init(height, L);
46 }
47
48 int f[N][Nlog];
49 inline int highbit(int x) {
50     return 31 - __builtin_clz(x);
51 }
52
53 int rmq_query(int x, int y) {
54     int p = highbit(y - x + 1);
55     return min(f[x][p], f[y - (1 << p) + 1][p]);
56 }
57
58 // arr has to be 0 based
59 void rmq_init(int *arr, int length) {
60     for (int x = 0; x <= highbit(length); ++x)
61         for (int i = 0; i <= length - (1 << x); ++i) {
62             if (!x) f[i][x] = arr[i];
63             else f[i][x] = min(f[i][x - 1], f[i + (1 << (x - 1))][x - 1]);
64         }
65 }
66
67 #ifdef NEW
68 // returns the length of the longest common prefix of s[i...L-1] and s[j...L-1]
69 int LongestCommonPrefix(int i, int j) {
70     int len = 0;
71     if (i == j) return L - i;
72     for (int k = (int) P.size() - 1; k >= 0 && i < L && j < L; k--) {
73         if (P[k][i] == P[k][j]) {
74             i += 1 << k;
75             j += 1 << k;
76             len += 1 << k;
77         }
78     }
79     return len;
80 }

```

```

81  #else
82  int LongestCommonPrefix(int i, int j) {
83      // getHeight() must be called first
84      if (i == j) return L - i;
85      if (i > j) swap(i, j);
86      return rmq_query(i + 1, j);
87  }
88  #endif
89
90  int checkNonOverlappingSubstring(int K) {
91      // check if there is two non-overlapping identical substring of length K
92      int minsa = 0, maxsa = 0;
93      for (int i = 0; i < L; ++i) {
94          if (height[i] < K) {
95              minsa = sa[i]; maxsa = sa[i];
96          } else {
97              minsa = min(minsa, sa[i]);
98              maxsa = max(maxsa, sa[i]);
99              if (maxsa - minsa >= K) return 1;
100          }
101      }
102      return 0;
103  }
104
105  int checkBelongToDifferentSubstring(int K, int split) {
106      int minsa = 0, maxsa = 0;
107      for (int i = 0; i < L; ++i) {
108          if (height[i] < K) {
109              minsa = sa[i]; maxsa = sa[i];
110          } else {
111              minsa = min(minsa, sa[i]);
112              maxsa = max(maxsa, sa[i]);
113              if (maxsa > split && minsa < split) return 1;
114          }
115      }
116      return 0;
117  }
118
119  } *S;
120
121  int main() {
122      string s, t;
123      cin >> s >> t;
124      int sp = s.length();
125      s += "*" + t;
126      S = new SuffixArray(s);
127      S->getHeight();
128      int left = 0, right = sp;
129      while (left < right) {
130          int mid = (left + right + 1) / 2;
131          if (S->checkBelongToDifferentSubstring(mid, sp))
132              left = mid;
133          else right = mid - 1;
134      }
135      printf("%d\n", left);
136  }

```

- SA-IS
- 仅在后缀自动机被卡内存或者卡常且需要 $O(1)$ LCA 的情况下使用（比赛中敲这个我觉得不行）
- UOJ 35

```

1  // rk [0..n-1] -> [1..n], sa/ht [1..n]
2  // s[i] > 0 && s[n] = 0
3  // b: normally as bucket
4  // c: normally as bucket1
5  // d: normally as bucket2
6  // f: normally as cntbuf
7
8  template<size_t size>
9  struct SuffixArray {
10      bool t[size << 1];

```

```

11 int b[size], c[size];
12 int sa[size], rk[size], ht[size];
13 inline bool isLMS(const int i, const bool *t) { return i > 0 && t[i] && !t[i - 1]; }
14 template<class T>
15 inline void inducedSort(T s, int *sa, const int n, const int M, const int bs,
16                         bool *t, int *b, int *f, int *p) {
17     fill(b, b + M, 0); fill(sa, sa + n, -1);
18     FOR (i, 0, n) b[s[i]]++;
19     f[0] = b[0];
20     FOR (i, 1, M) f[i] = f[i - 1] + b[i];
21     FORD (i, bs - 1, -1) sa[--f[s[p[i]]]] = p[i];
22     FOR (i, 1, M) f[i] = f[i - 1] + b[i - 1];
23     FOR (i, 0, n) if (sa[i] > 0 && !t[sa[i] - 1]) sa[f[s[sa[i] - 1]]++] = sa[i] - 1;
24     f[0] = b[0];
25     FOR (i, 1, M) f[i] = f[i - 1] + b[i];
26     FORD (i, n - 1, -1) if (sa[i] > 0 && t[sa[i] - 1]) sa[--f[s[sa[i] - 1]]] = sa[i] - 1;
27 }
28 template<class T>
29 inline void sais(T s, int *sa, int n, bool *t, int *b, int *c, int M) {
30     int i, j, bs = 0, cnt = 0, p = -1, x, *r = b + M;
31     t[n - 1] = 1;
32     FORD (i, n - 2, -1) t[i] = s[i] < s[i + 1] || (s[i] == s[i + 1] && t[i + 1]);
33     FOR (i, 1, n) if (t[i] && !t[i - 1]) c[bs++] = i;
34     inducedSort(s, sa, n, M, bs, t, b, r, c);
35     for (i = bs = 0; i < n; i++) if (isLMS(sa[i], t)) sa[bs++] = sa[i];
36     FOR (i, bs, n) sa[i] = -1;
37     FOR (i, 0, bs) {
38         x = sa[i];
39         for (j = 0; j < n; j++) {
40             if (p == -1 || s[x + j] != s[p + j] || t[x + j] != t[p + j]) { cnt++, p = x; break; }
41             else if (j > 0 && (isLMS(x + j, t) || isLMS(p + j, t))) break;
42         }
43         x = (~x & 1 ? x >> 1 : x - 1 >> 1), sa[bs + x] = cnt - 1;
44     }
45     for (i = j = n - 1; i >= bs; i--) if (sa[i] >= 0) sa[j--] = sa[i];
46     int *s1 = sa + n - bs, *d = c + bs;
47     if (cnt < bs) sais(s1, sa, bs, t + n, b, c + bs, cnt);
48     else FOR (i, 0, bs) sa[s1[i]] = i;
49     FOR (i, 0, bs) d[i] = c[sa[i]];
50     inducedSort(s, sa, n, M, bs, t, b, r, d);
51 }
52 template<typename T>
53 inline void getHeight(T s, const int n, const int *sa) {
54     for (int i = 0, k = 0; i < n; i++) {
55         if (rk[i] == 0) k = 0;
56         else {
57             if (k > 0) k--;
58             int j = sa[rk[i] - 1];
59             while (i + k < n && j + k < n && s[i + k] == s[j + k]) k++;
60         }
61         ht[rk[i]] = k;
62     }
63 }
64 template<class T>
65 inline void init(T s, int n, int M) {
66     sais(s, sa, ++n, t, b, c, M);
67     for (int i = 1; i < n; i++) rk[sa[i]] = i;
68     getHeight(s, n, sa);
69 }
70 };
71
72 const int N = 2E5 + 100;
73 SuffixArray<N> sa;
74
75 int main() {
76     string s; cin >> s; int n = s.length();
77     sa.init(s, n, 128);
78     FOR (i, 1, n + 1) printf("%d%c", sa.sa[i] + 1, i == _i - 1 ? '\n' : ' ');
79     FOR (i, 2, n + 1) printf("%d%c", sa.ht[i], i == _i - 1 ? '\n' : ' ');
80 }

```

KMP

- 前缀函数（每一个前缀的最长 border）

```
1 void get_pi(int a[], char s[], int n) {
2     int j = a[0] = 0;
3     FOR (i, 1, n) {
4         while (j && s[i] != s[j]) j = a[j - 1];
5         a[i] = j += s[i] == s[j];
6     }
7 }
```

- Z 函数（每一个后缀和该字符串的 LCP 长度）

```
1 void get_z(int a[], char s[], int n) {
2     int l = 0, r = 0; a[0] = n;
3     FOR (i, 1, n) {
4         a[i] = i > r ? 0 : min(r - i + 1, a[i - l]);
5         while (i + a[i] < n && s[a[i]] == s[i + a[i]]) ++a[i];
6         if (i + a[i] - 1 > r) { l = i; r = i + a[i] - 1; }
7     }
8 }
```

Trie

```
1 namespace trie {
2     int t[N][26], sz, ed[N];
3     void init() { sz = 2; memset(ed, 0, sizeof ed); }
4     int _new() { memset(t[sz], 0, sizeof t[sz]); return sz++; }
5     void ins(char* s, int p) {
6         int u = 1;
7         FOR (i, 0, strlen(s)) {
8             int c = s[i] - 'a';
9             if (!t[u][c]) t[u][c] = _new();
10            u = t[u][c];
11        }
12        ed[u] = p;
13    }
14 }
```

AC 自动机

```
1 const int N = 1e6 + 100, M = 26;
2
3 int mp(char ch) { return ch - 'a'; }
4
5 struct ACA {
6     int ch[N][M], danger[N], fail[N];
7     int sz;
8     void init() {
9         sz = 1;
10        memset(ch[0], 0, sizeof ch[0]);
11        memset(danger, 0, sizeof danger);
12    }
13    void insert(const string &s, int m) {
14        int n = s.size(); int u = 0, c;
15        FOR (i, 0, n) {
16            c = mp(s[i]);
17            if (!ch[u][c]) {
18                memset(ch[sz], 0, sizeof ch[sz]);
19                danger[sz] = 0; ch[u][c] = sz++;
20            }
21            u = ch[u][c];
22        }
23        danger[u] |= 1 << m;
24    }
25    void build() {
26        queue<int> Q;
27        fail[0] = 0;
28        for (int c = 0, u; c < M; c++) {
29            u = ch[0][c];
```



```

30         if (u) { Q.push(u); fail[u] = 0; }
31     }
32     while (!Q.empty()) {
33         int r = Q.front(); Q.pop();
34         danger[r] |= danger[fail[r]];
35         for (int c = 0, u; c < M; c++) {
36             u = ch[r][c];
37             if (!u) {
38                 ch[r][c] = ch[fail[r]][c];
39                 continue;
40             }
41             fail[u] = ch[fail[r]][c];
42             Q.push(u);
43         }
44     }
45 }
46 } ac;
47
48 char s[N];
49
50 int main() {
51     int n; scanf("%d", &n);
52     ac.init();
53     while (n--) {
54         scanf("%s", s);
55         ac.insert(s, 0);
56     }
57     ac.build();
58
59     scanf("%s", s);
60     int u = 0; n = strlen(s);
61     FOR (i, 0, n) {
62         u = ac.ch[u][mp(s[i])];
63         if (ac.danger[u]) {
64             puts("YES");
65             return 0;
66         }
67     }
68     puts("NO");
69     return 0;
70 }

```