CS406: Compilers
Spring 2022

Week 11: Loop Optimization, ..

#### Optimize Loops

Example - Code Motion
 Should be careful while doing optimization of loops

```
while J > I loop
    A(j) := 10/I;
    j := j + 2;
end loop;
```

#### Optimize Loops – Code Motion

 Should be careful while doing optimization of loops

```
while J > I loop
    A(j) := 10/I;
    j := j + 2;
end loop;
```

Optimization: can move 10/I out of loop.

#### Optimize Loops – Code Motion

 Should be careful while doing optimization of loops

```
while J > I loop
    A(j) := 10/I;
    j := j + 2;
end loop;
```

- Optimization: can move 10/I out of loop
- What if I = 0?

#### Optimize Loops – Code Motion

 Should be careful while doing optimization of loops

```
while J > I loop
    A(j) := 10/I;
    j := j + 2;
end loop;
```

- Optimization: can move 10/I out of loop
- What if I = 0?
- What if I != 0 but loop executes zero times?

# Optimization Criteria - Safety and Profitability

- Safety is the code produced after optimization producing same result?
- Profitability is the code produced after optimization running faster or uses less memory or triggers lesser number of page faults etc.

```
while J > I loop
    A(j) := 10/I;
    j := j + 2;
end loop;
```

- E.g. moving I out of the loop introduces exception (when I=0)
- E.g. if the loop is executed zero times, moving A(j) := 10/I out is not profitable

#### Optimize Loops – Code Generation

 The outline of code generation for 'for' loops looked like this:

```
for (<init_stmt>;<bool_expr>;<incr_stmt>)
                                            for (i=0; i<=255;i++) {
 <stmt_list>
                                                <stmt list>
end
                                                           Naïve code generation
                                             code for i=0;
                                             code for i<=255
                                    LOOP:
              <init_stmt>
                                             jump0 OUT
            LOOP:
                                             code for <stmt list>
              <bool_expr>
              j<!op> OUT
                                    INCR:
                                             code for i++
              <stmt_list>
                                             jump LOOP
            INCR:
                                    OUT:
              <incr_stmt>
              imp LOOP
                                     Question: why naïve is not good?
            OUT:
```

#### Optimize Loops – Code Generation

 What happens when ub is set to the maximum possible integer representable by the type of i?

CS406, IIT Dharwad

```
for (i=0; i<=255;i++) {
          <stmt list>
      }
                                                code for i=0;
                   Better code:
                                                compute 1b, ub
       code for i=0;
                                                code for lb<=ub
       code for lb=1, ub=255
                                                jump0 OUT
       code for 1b<=ub
                                                assign index=1b
       jump0 OUT
                                                assign limit=ub
LOOP: code for <stmt_list>
                                         LOOP:
                                                code for <stmt list>
       code for lb=ub
                                                code for index=limit
                              generalizing:
       jump1 OUT
                                                jump1 OUT
INCR:
       code for i++
                                        INCR:
                                                code for increment index
       jump LOOP
                                                jump LOOP
OUT:
                                        OUT:
```

8

- How do we identify expressions that can be moved out of the loop?
  - LoopDef = {} set of variables <u>defined</u> (i.e. whose values are overwritten) in the loop body
  - LoopUse = { } 'relevant' variables <u>used</u> in computing an expression

```
Mark_Invariants(Loop L) {
```

- 1. Compute LoopDef for L
- Mark as invariant all expressions, whose relevant variables don't belong to LoopDef

Example

LoopDef{}

```
for I = 1 to 100 \longrightarrow {A, J, K, I}

for J = 1 to 100 \longrightarrow {A, J, K}

for K = 1 to 100 \longrightarrow {A, K}

A[I][J][K] = (I*J)*K
```

Example

LoopUse{}

```
for I = 1 to 100 \longrightarrow {}

for J = 1 to 100 \longrightarrow {I}

for K = 1 to 100 \longrightarrow {I,J}

A[I][J][K] = (I*J)*K
```

• Example

Invariant Expressions

For an array access, A[m] => Addr(A) + m

```
For 3D array above*, Addr(A[I][J][K]) = Addr(A)+(I*10000)-10000+(J*100)-100+K-1
```

```
For an array access, A[m] => Addr(A) + m
For 3D array above*, Addr(A[I][J][K]) =
Addr(A)+(I*10000)-10000+(J*100)-100+K-1
```

Move the invariant expressions identified

Example

```
for I = 1 to 100
    temp3=A[I]
    for J = 1 to 100
        temp1=temp3[J]
        temp2=I*J
        for K = 1 to 100
        temp1[K] = temp2*K
```

Expressions cannot always be moved out!

Case I: We can move t = a op b if the statement <u>dominates</u> all loop exits where t is live

A node bb1 dominates node bb2 if all paths to bb2 must go through bb1

```
for (...) {
    if(*)
    a = 100
}
c=a
```

Cannot move a=100 because it does not dominate c=a i.e. there is one path (when if condition is false) c=a can be executed /'reached' without going to a=100

Expressions cannot always be moved out!

Case II: We can move t = a op b if there is only one definition of t in the loop

```
for (...) {
   if(*)
    a = 100
   else
   a = 200
}
```

Multiple definition of a

Expressions cannot always be moved out!

**Case III:** We can move t = a op b if t is not defined before the loop, where the definition reaches t's use after the loop

```
a=5
for (...) {
    a = 4+b
}
c=a
```

Definition of a in a=5 reaches c=a, which is defined after the loop

- Like strength reduction in peephole optimization
  - E.g. replace a\*2 with a<<1</li>
- Applies to uses of induction variable in loops
  - Basic induction variable (I) only definition within the loop is of the form I = I ± S, (S is loop invariant)
    - I usually determines number of iterations
  - Mutual induction variable (J) defined within the loop, its value is linear function of other induction variable, I, such that

J = I \* C ± D (C, D are loop invariants)

```
strength_reduce(Loop L) {
  Mark Invariants(L);
   foreach expression E of the form I*C+D where I is
L's loop index and C and D are loop invariants
      1. Create a temporary T
      2. Replace each occurrence of E in L with T
      3. Insert T:=I_0*C+D, where I_0 is the initial value of the
         induction variable, immediately before L
      4. Insert T:=T+S*C, where S is the step size, at the end of
         L's body
```

- Suppose induction variable I takes on values  $I_{o,j}$   $I_{o}+S$ ,  $I_{o}+2S$ ,  $I_{o}+3S$ ... in iterations 1, 2, 3, 4, and so on...
- Then, in consecutive iterations, Expression
   I\*C+D takes on values

$$I_o*C+D$$
  
 $(I_o+S)*C+D = I_o*C+S*C+D$   
 $(I_o+2S)*C+D = I_o*C+2S*C+D$ 

- The expression changes by a constant S\*C
- Therefore, we have replaced a \* and + with a +

Example (Applying to innermost loop)

```
for I = 1 to 100
                              for I=1 to 100
  for J = 1 to 100
                                 temp3=Addr(A[i])
     for K = 1 to 100
                                 for J=1 to 100
        A[I][J][K] = (I*J)*K
                                    temp1=Addr(temp3(J))
                                    temp2=I*J
                                    for K=1 to 100
                                       temp1[K]=temp2*K
                   temp2=I*J
                   temp4=temp2
                   for K=1 to 100
      //S=1
                      temp1[K]=temp4
      //C=temp2
                      temp4=temp4+temp2
    CS406, IIT Dharwad
                                                     22
```

Exercise (Apply to intermediate loop)

```
for I=1 to 100
                            temp2=I*J
  temp3=Addr(A[i])
                            temp4=temp2
  for J=1 to 100
                            for K=1 to 100
     temp1=Addr(temp3(J))
                               temp1[K]=temp4
     temp2=I*J
                               temp4=temp4+temp2
     for K=1 to 100
        temp1[K]=temp2*K
               // Induction var = J
               // S = 1
               // Expression = I * J
```

Exercise (Apply to intermediate loop)

```
temp5=I
for J=1 to 100
     temp1=Addr(temp3(J))
     temp2=temp5
     temp4=temp2
     for K=1 to 100
        temp1[K]=temp4
        temp4=temp4+temp2
     temp5=temp5+I
```

CS406, IIT Dharwad

24

Further strength reduction possible?

```
for I=1 to 100
  temp3=Addr(A[i])
  temp5=I
  for J=1 to 100
     temp1=Addr(temp3(J))
     temp2=temp5
     temp4=temp2
     for K=1 to 100
        temp1[K]=temp4
        temp4=temp4+temp2
     temp5=temp5+I
```

### Optimize Loops – Loop Unrolling

- Modifying induction variable in each iteration can be expensive
- Can instead unroll loops and perform multiple iterations for each increment of the induction variable
- What are the advantages and disadvantages?

```
for (i = 0; i < N; i++)
A[i] = ...
```

Unroll by factor of 4

```
for (i = 0; i < N; i += 4)

A[i] = ...

A[i+1] = ...

A[i+2] = ...

A[i+3] = ...
```

#### Optimize Loops - Summary

- Low level optimization
  - Moving code around in a single loop
  - Examples: loop invariant code motion, strength reduction, loop unrolling
- High level optimization
  - Restructuring loops, often affects multiple loops
  - Examples: loop fusion, loop interchange, loop tiling

### Useful optimizations

- Common subexpression elimination (global)
  - Need to know which expressions are available at a point
- Dead code elimination
  - Need to know if the effects of a piece of code are never needed, or if code cannot be reached
- Constant folding
  - Need to know if variable has a constant value
- So how do we get this information?

### Dataflow analysis

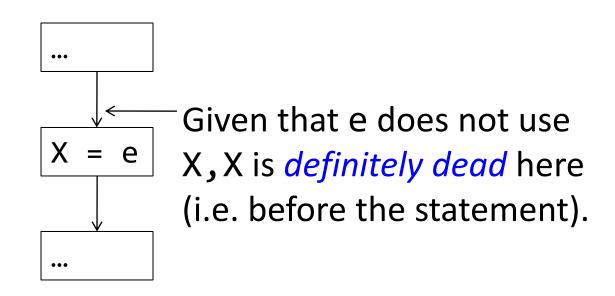
- Framework for doing compiler analyses to drive optimization
- Works across basic blocks
- Examples
  - Constant propagation: determine which variables are constant
  - Liveness analysis: determine which variables are live
  - Available expressions: determine which expressions are have valid computed values
  - Reaching definitions: determine which definitions could "reach" a use

#### Liveness – Recap...

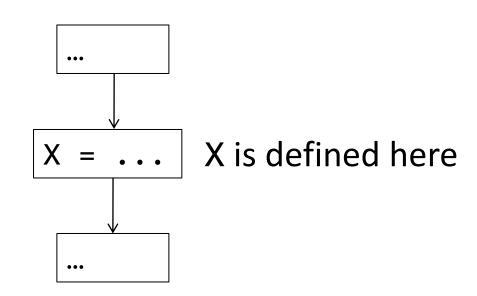
- A variable X is live at statement S if:
  - There is a statement S' that uses X
  - There is a path from S to S'
  - There are no intervening definitions of X

#### Liveness – Recap...

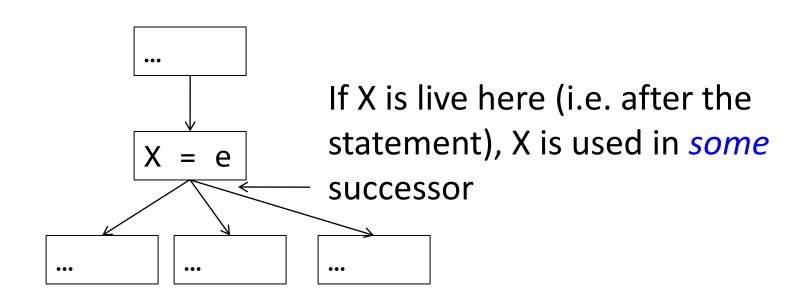
- A variable X is dead at statement S if it is not live at S
  - What about  $\dots$ ; X = X + 1?



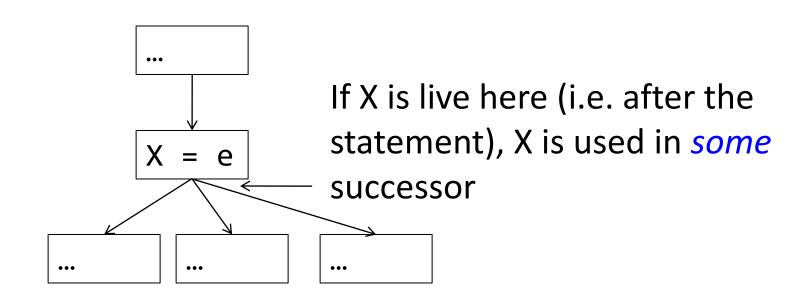
• Define a set LiveIn(b), where b is a basic block, as: the set of all variables live at the entrance of a basic block



Define a set Def(b), where b is a basic block,
 as: the set of all variables that are defined within block b

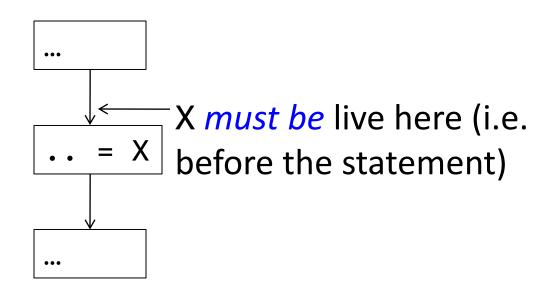


• Define a set LiveOut(b), where b is a basic block, as: the set of all variables live at the exit of a basic block



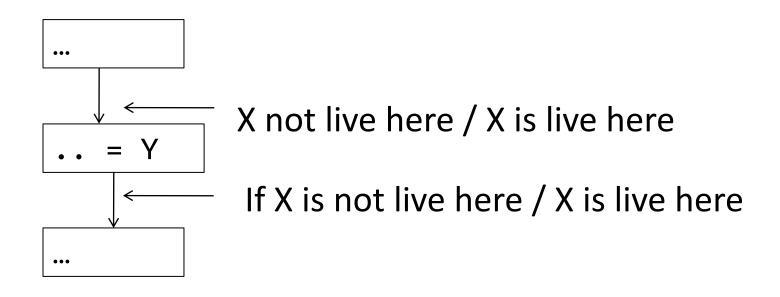
• If S(b) is the set of all successors of b, then

LiveOut(b) = 
$$\bigcup_{i \in S(b)}$$
 LiveIn(i)



 Define a set LiveUse(b), where b is a basic block, as: the set of all variables that are used within block b. LiveIn(b) ⊇ LiveUse(b)

#### Liveness in a CFG - Observation



•If a node neither uses nor defines X, the liveness property remains the same before and after executing the node

• If a variable is live on exit from b, it is either defined in b or live on entrance to b

•Under what scenarios can a variable be live at the entrance of a basic block?

• If a variable is live on exit from b, it is either defined in b or live on entrance to b

LiveIn(b) ⊇ LiveOut(b) - Def(b)

- •Under what scenarios can a variable be live at the entrance of a basic block?
  - •Either the variable is used in the basic block

• If a variable is live on exit from b, it is either defined in b or live on entrance to b

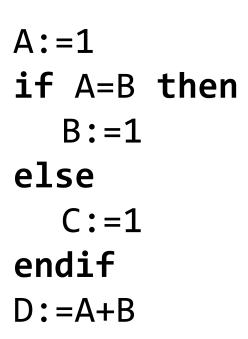
LiveIn(b) ⊇ LiveOut(b) - Def(b)

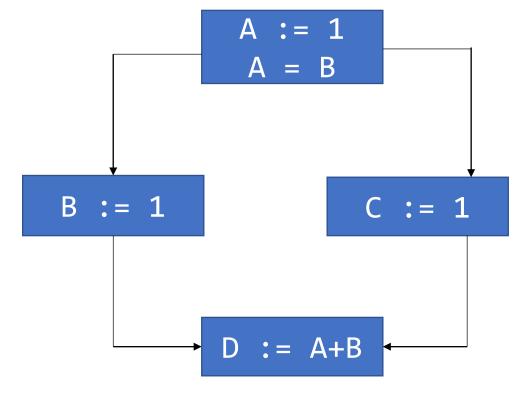
- •Under what scenarios can a variable be live at the entrance of a basic block?
  - •Either the variable is used in the basic block
  - •OR the variable is live at exit and not defined within the block

- •Under what scenarios can a variable be live at the entrance of a basic block?
  - Either the variable is used in the basic block
  - •OR the variable is live at exit and not defined within the block

```
LiveIn(b) = LiveUse(b) U (LiveOut(b) -
Def(b))
```

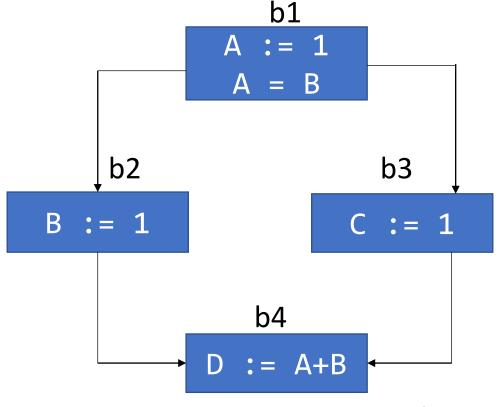
#### Draw CFG for the code:





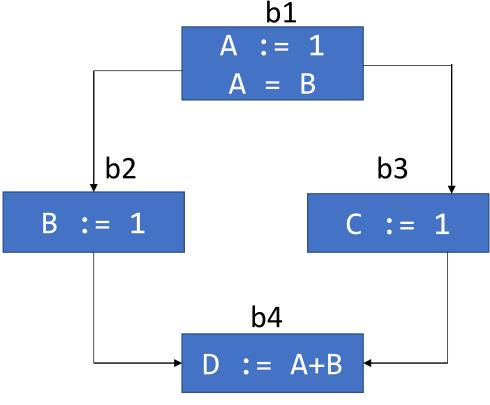
Compute Def(b) and LiveUse(b) sets

Block	Def	LiveUse
b1		
b2		
b3		
b4		



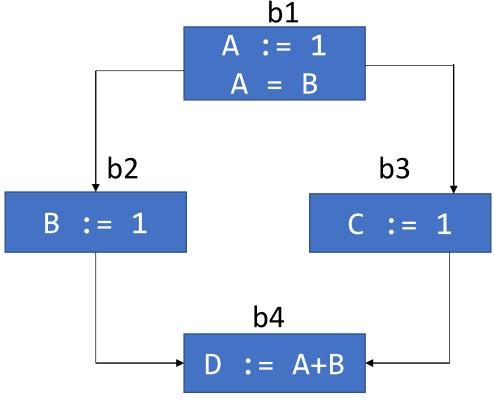
Compute Def(b) and LiveUse(b) sets

Block	Def	LiveUse
b1	{A}	{B}
b2		
b3		
b4		



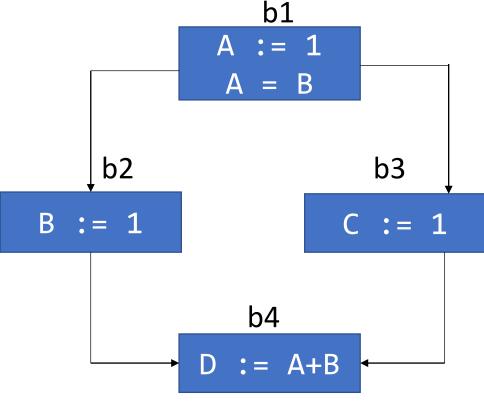
Compute Def(b) and LiveUse(b) sets

Block	Def	LiveUse
b1	{A}	{B}
b2	{B}	{}
b3		
b4		



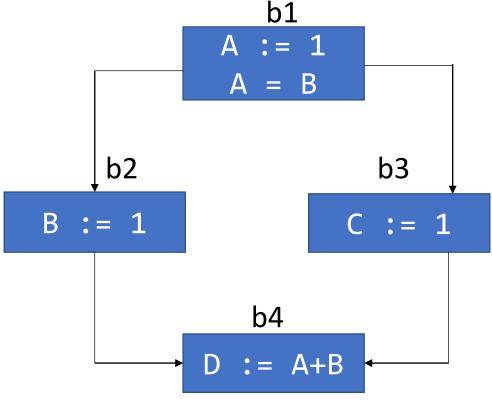
Compute Def(b) and LiveUse(b) sets

Block	Def	LiveUse
b1	{A}	{B}
b2	{B}	{}
b3	{C}	{}
b4		



Compute Def(b) and LiveUse(b) sets

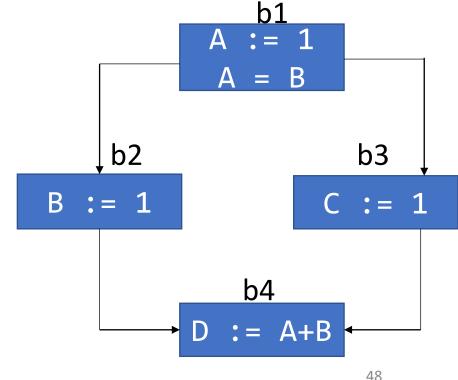
Block	Def	LiveUse
b1	{A}	{B}
b2	{B}	{}
b3	{C}	{}
b4	{D}	{A,B}



start from use of a variable to its definition.

Is this analysis going backward or forward w.r.t. control flow?

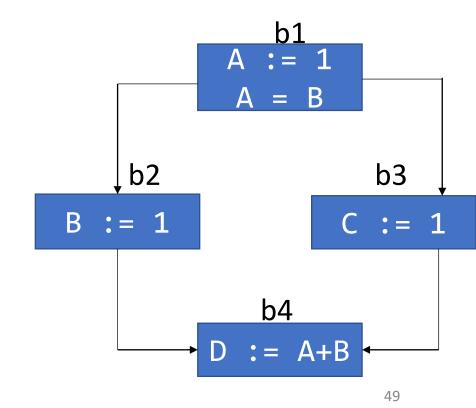
Block	Def	LiveUse
b1	{A}	{B}
b2	{B}	{}
b3	{C}	{}
b4 CS406, IIT Dharv	{D}	{A,B}



start from use of a variable to its definition.

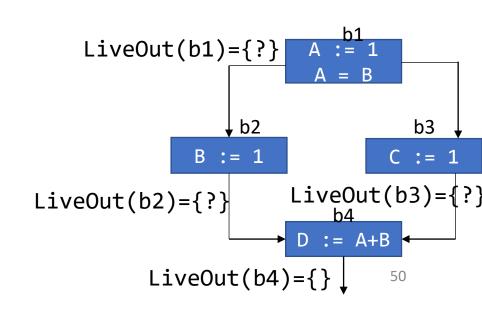
Backward-flow problem

Block	Def	LiveUse
b1	{A}	{B}
b2	{B}	{}
b3	{C}	{}
b4 CS406, IIT Dharw	{D}	{A,B}



- Start from use of a variable to its definition.
- •Compute:

Block	Def	LiveUse
b1	{A}	{B}
b2	{B}	{}
b3	{C}	{}
b4	{D}	{A,B}

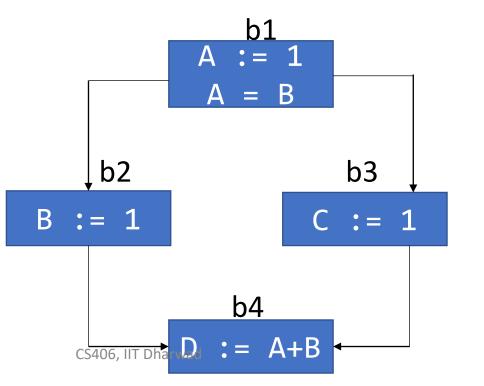


- Start from use of a variable to its definition.
- •Compute:

Block	Def	LiveUse
b1	{A}	{B}
b2	{B}	{}
b3	{C}	{}
b4	{D}	{A,B}

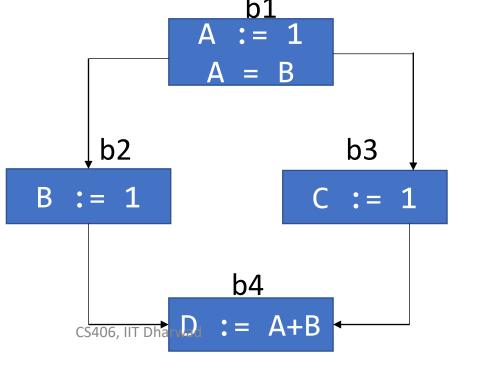
Block	Liveln	LiveOut
b1	{B}	{A,B}
b2	{A}	{A,B}
b3	{A,B}	{A,B}
b4	{A,B}	{}

- Assume that the CFG below represents your entire program
  - •What can you infer from the table?



Block	Liveln	LiveOut
b1	{B}	{A,B}
b2	{A}	{A,B}
b3	{A,B}	{A,B}
b4	{A,B}	{}

- Assume that the CFG below represents your entire program
  - •Variable B is live in b1, the entry basic block of CFG. This implies that B is used before it is defined. An error!



Block	Liveln	LiveOut
b1	{B}	{A,B}
b2	{A}	{A,B}
b3	{A,B}	{A,B}
b4	{A,B}	{}