

# CS323: Compilers

Spring 2023

## Week 11: Instruction Scheduling (contd..), Control Flow Graphs

Acknowledgements: Milind Kulkarni

# List scheduling - Example

1. LD A, R1

2. LD B, R2

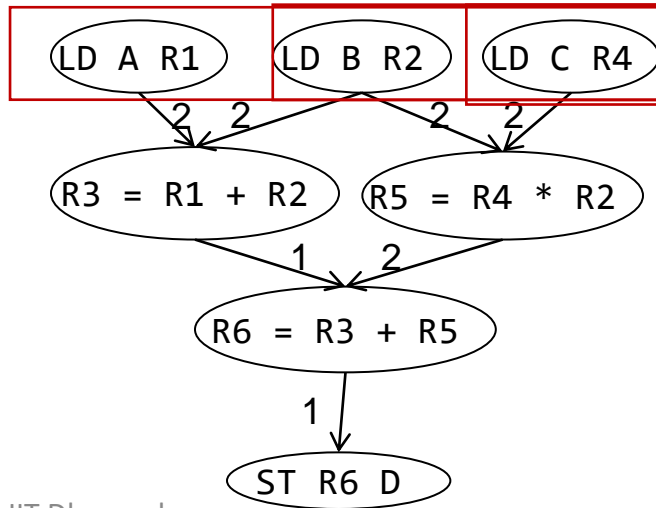
3. R3 = R1 + R2

4. LD C, R4

5. R5 = R4 \* R2

6. R6 = R3 + R5

7. ST R6, D



Cycle #      Available      Scheduled      Completed  
Instruction(s)    Instruction(s)    Instruction(s)

0	1, 2, 4	1*	
1	2, 4		
2	2, 4	2*	1
3	4		
4	3,4	3,4	2
5			3
6	5	5	4
7			
8	6	6	5
9	7	7	6
10			7

\*an instruction from the list of available instructions is picked at random and scheduled

# List scheduling

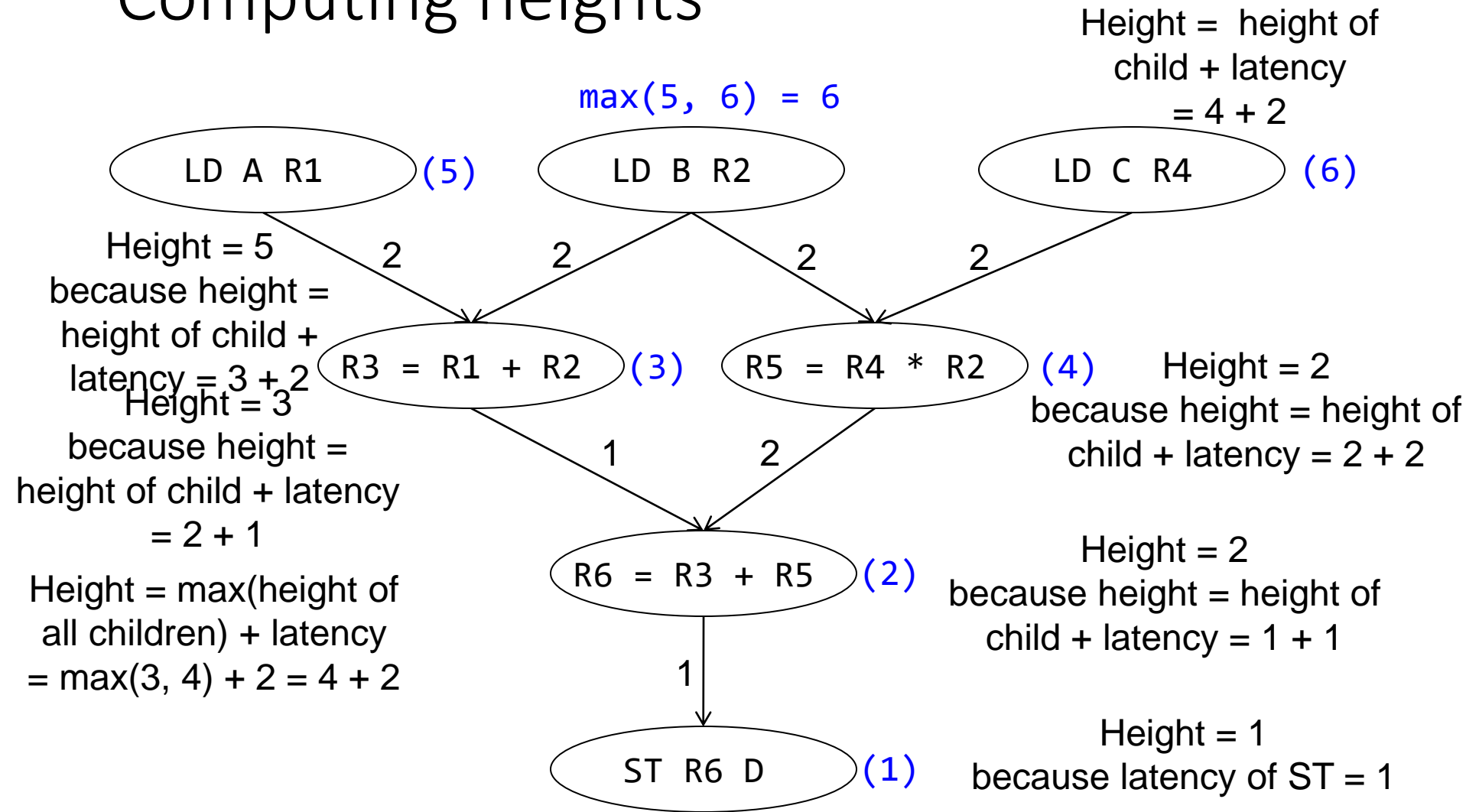
1. LD A, R1
2. LD B, R2
3.  $R3 = R1 + R2$
4. LD C, R4
5.  $R5 = R4 * R2$
6.  $R6 = R3 + R5$
7. ST R6, D

Cycle	ALU0	ALU1	LD/ST
0			1
1			1
2			2
3			2
4	3		4
5			4
6	5		
7			
8	6		
9			7
10			

# Height-based scheduling

- Important to prioritize instructions
  - Instructions that have a lot of downstream instructions dependent on them should be scheduled earlier
- Instruction scheduling NP-hard in general, but **height-based scheduling** is effective
- Instruction height = latency from instruction to farthest-away leaf
  - Leaf node height = instruction latency
  - Interior node height =  $\max(\text{heights of children} + \text{instruction latency})$
- Schedule instructions with highest height first

# Computing heights



# Height-based list scheduling

1. LD A, R1  
2. LD B, R2  
3.  $R3 = R1 + R2$   
4. LD C, R4  
5.  $R5 = R4 * R2$   
6.  $R6 = R3 + R5$   
7. ST R6, D

Cycle	ALU0	ALU1	LD/ST
0			2
1			2
2			4
3			4
4	5		1
5			1
6	3		
7	6		
8	7		
9			
10			

# Instruction Scheduling - Exercise

- 2 ALUs (fully pipelined) and one LD/ST unit (not pipelined) are available.
  - Either of the ALUs can execute ADD (1 cycle). Only one of the ALUs can execute MUL (2 cycles).
  - LDs take up an ALU for 1 cycle and LD/ST unit for two cycles.
  - STs take up an ALU for 1 cycle and LD/ST unit for one cycle.
- i) Draw reservation tables, ii) DAG for the code shown iii) schedule using height based list scheduling.*

1: LD A R1	11: ST R10 E
2: LD B R2	12: ST R7 F
3: LD C R3	
4: LD D R4	
5: R5 = R1 + R2	
6: R6 = R5 * R3	
7: R7 = R1 + R6	
8: R8 = R6 + R5	
9: R9 = R4 + R7	
10: R10 = R9 + R8	

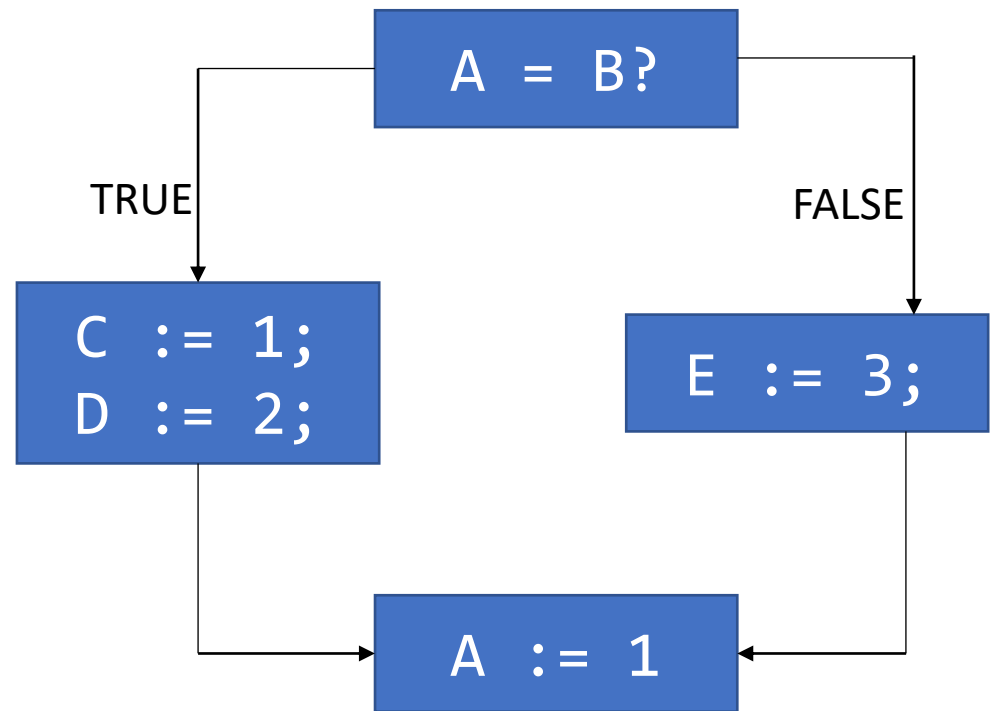
# Basic Blocks and Flow Graphs

- Basic Block
  - Maximal sequence of consecutive instructions with the following properties:
    - The first instruction of the basic block is the *only entry point*
    - The last instruction of the basic block is either the halt instruction or the *only exit point*
- Flow Graph
  - Nodes are the basic blocks
  - Directed edge indicates which block follows which block



# Basic Blocks and Flow Graphs - Example

```
if A = B then  
    C := 1;  
    D := 2;  
else  
    E := 3  
fi  
A := 1;
```



A data flow graph

# Flow Graphs

- Capture how control transfers between basic blocks due to:
  - Conditional constructs
  - Loops
- Are necessary when we want optimize considering larger parts of the program
  - Multiple procedures
  - Whole program

# Flow Graphs - Representation

- We need to label and track statements that are jump targets
  - **Explicit targets** – targets mentioned in jump statement
  - **Implicit targets** – targets that follow conditional jump statement
    - Statement that is executed if the branch is not taken
- Implementation
  - Linked lists for Basic Blocks
  - Graph data structures for flow graphs

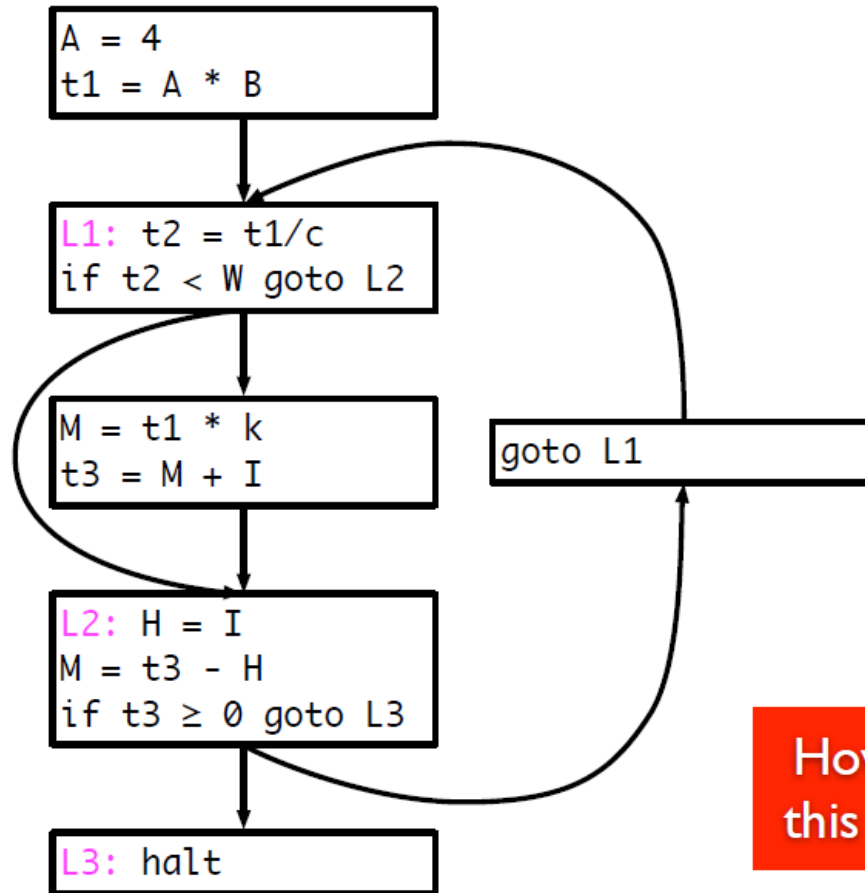
# Running example

```
A = 4
t1 = A * B
repeat {
  t2 = t1/C
  if (t2 ≥ W) {
    M = t1 * k
    t3 = M + I
  }
  H = I
  M = t3 - H
} until (T3 ≥ 0)
```

# Running example

```
1      A = 4
2      t1 = A * B
3  L1:  t2 = t1 / C
4      if t2 < W goto L2
5      M = t1 * k
6      t3 = M + I
7  L2:  H = I
8      M = t3 - H
9      if t3 ≥ 0 goto L3
10     goto L1
11  L3:  halt
```

# CFG for running example



How do we build  
this automatically?

# Constructing a CFG

- To construct a CFG where each node is a basic block
  - Identify *leaders*: first statement of a basic block
  - In program order, construct a block by appending subsequent statements up to, but not including, the next leader
- Identifying leaders
  - First statement in the program
  - Explicit target of any conditional or unconditional branch
  - Implicit target of any branch

# Partitioning algorithm

- Input: set of statements,  $stat(i)$  =  $i^{th}$  statement in input
- Output: set of *leaders*, set of basic blocks where  $block(x)$  is the set of statements in the block with leader  $x$
- Algorithm

```
leaders = {1}           //Leaders always includes first statement
for i = 1 to |n|       //|n| = number of statements
    if  $stat(i)$  is a branch, then
        leaders = leaders  $\cup$  all potential targets
    end for
worklist = leaders
while worklist not empty do
    x = remove earliest statement in worklist
    block(x) = {x}
    for (i = x + 1; i  $\leq$  |n| and i  $\notin$  leaders; i++)
        block(x) = block(x)  $\cup$  {i}
    end for
end while
```



# Running example

```
1      A = 4
2      t1 = A * B
3  L1:  t2 = t1 / C
4      if t2 < W goto L2
5      M = t1 * k
6      t3 = M + I
7  L2:  H = I
8      M = t3 - H
9      if t3 ≥ 0 goto L3
10     goto L1
11  L3:  halt
```

Leaders = ?

Basic blocks = ?

```
leaders = {1}           //Leaders always includes first statement
for i = 1 to |n|        //|n| = number of statements
    if stat(i) is a branch, then
        leaders = leaders ∪ all potential targets
end for
worklist = leaders
```

# Running example

1	A = 4
---	-------

```
2      t1 = A * B
3  L1:  t2 = t1 / C
4      if t2 < W goto L2
5      M = t1 * k
6      t3 = M + I
7  L2:  H = I
8      M = t3 - H
9      if t3 ≥ 0 goto L3
10     goto L1
11  L3:  halt
```

Leaders = {1}

Basic blocks =

# Running example

```
1      A = 4
2      t1 = A * B
3  L1:  t2 = t1 / C
4      if t2 < W goto L2
5      M = t1 * k
6      t3 = M + I
7  L2:  H = I
8      M = t3 - H
9      if t3 ≥ 0 goto L3
10     goto L1
11  L3:  halt
```

Leaders = {1}

Basic blocks =

# Running example

```
1      A = 4
2      t1 = A * B
3  L1:  t2 = t1 / C
4      if t2 < W goto L2
5      M = t1 * k
6      t3 = M + I
7  L2:  H = I
8      M = t3 - H
9      if t3 ≥ 0 goto L3
10     goto L1
11  L3:  halt
```

Leaders = {1, 3}

Basic blocks =

# Running example

```
1      A = 4
2      t1 = A * B
3  L1:  t2 = t1 / C
4      if t2 < W goto L2
5      M = t1 * k
6      t3 = M + I
7  L2:  H = I
8      M = t3 - H
9      if t3 ≥ 0 goto L3
10     goto L1
11  L3:  halt
```

Leaders = {1, 3}

Basic blocks =

# Running example

```
1      A = 4
2      t1 = A * B
3  L1:  t2 = t1 / C
4      if t2 < W goto L2
5      M = t1 * k
6      t3 = M + I
7  L2:  H = I
8      M = t3 - H
9      if t3 ≥ 0 goto L3
10     goto L1
11  L3:  halt
```

Leaders = {1, 3, 5}

Basic blocks =

# Running example

```
1      A = 4
2      t1 = A * B
3  L1:  t2 = t1 / C
4      if t2 < W goto L2
5      M = t1 * k
6      t3 = M + I
7  L2:  H = I
8      M = t3 - H
9      if t3 ≥ 0 goto L3
10     goto L1
11  L3:  halt
```

Leaders = {1, 3, 5}

Basic blocks =

# Running example

```
1      A = 4
2      t1 = A * B
3  L1:  t2 = t1 / C
4      if t2 < W goto L2
5      M = t1 * k
6      t3 = M + I
7  L2:  H = I
8      M = t3 - H
9      if t3 ≥ 0 goto L3
10     goto L1
11  L3:  halt
```

Leaders = {1, 3, 5, 7}

Basic blocks =



# Running example

```
1      A = 4
2      t1 = A * B
3  L1:  t2 = t1 / C
4      if t2 < W goto L2
5      M = t1 * k
6      t3 = M + I
7  L2:  H = I
8      M = t3 - H
9      if t3 ≥ 0 goto L3
10     goto L1
11  L3:  halt
```

Leaders = {1, 3, 5, 7}

Basic blocks =

# Running example

```
1      A = 4
2      t1 = A * B
3  L1:  t2 = t1 / C
4      if t2 < W goto L2
5      M = t1 * k
6      t3 = M + I
7  L2:  H = I
8      M = t3 - H
9      if t3 ≥ 0 goto L3
10     goto L1
11  L3:  halt
```

Leaders = {1, 3, 5, 7}

Basic blocks =

# Running example

```
1      A = 4
2      t1 = A * B
3  L1:  t2 = t1 / C
4      if t2 < W goto L2
5      M = t1 * k
6      t3 = M + I
7  L2:  H = I
8      M = t3 - H
9      if t3 ≥ 0 goto L3
10     goto L1
11  L3:  halt
```

Leaders = {1, 3, 5, 7, 10}

Basic blocks =

# Running example

```
1      A = 4
2      t1 = A * B
3  L1:  t2 = t1 / C
4      if t2 < W goto L2
5      M = t1 * k
6      t3 = M + I
7  L2:  H = I
8      M = t3 - H
9      if t3 ≥ 0 goto L3
10     goto L1
11  L3:  halt
```

Leaders = {1, 3, 5, 7, 10, 11}  
Basic blocks = ?

*worklist = leaders*

**while** *worklist* not empty **do**

*x* = remove earliest statement in *worklist*

*block(x)* = {*x*}

**for** (*i* = *x* + 1; *i* ≤ |*n*| and *i* ∉ *leaders*; *i*++)

*block(x)* = *block(x)* ∪ {*i*}

**end for**

**end while**

# Running example

```
1      A = 4
2      t1 = A * B
3  L1:  t2 = t1 / C
4      if t2 < W goto L2
5      M = t1 * k
6      t3 = M + I
7  L2:  H = I
8      M = t3 - H
9      if t3 ≥ 0 goto L3
10     goto L1
11  L3:  halt
```

Leaders = {1, 3, 5, 7, 10, 11}  
Basic blocks =

Block(1) = ?

# Running example

```
1      A = 4
2      t1 = A * B
3  L1:  t2 = t1 / C
4      if t2 < W goto L2
5      M = t1 * k
6      t3 = M + I
7  L2:  H = I
8      M = t3 - H
9      if t3 ≥ 0 goto L3
10     goto L1
11  L3:  halt
```

Leaders = {1, 3, 5, 7, 10, 11}

Basic blocks =

Block(1) = ?

Start from statement 2 and add  
till either the end or a leader is  
reached

# Running example

```
1      A = 4
2      t1 = A * B
3  L1:  t2 = t1 / C
4      if t2 < W goto L2
5      M = t1 * k
6      t3 = M + I
7  L2:  H = I
8      M = t3 - H
9      if t3 ≥ 0 goto L3
10     goto L1
11  L3:  halt
```

Leaders = {1, 3, 5, 7, 10, 11}      Block(1) = {1, 2}  
Basic blocks =

# Running example

```
1      A = 4
2      t1 = A * B
3  L1:  t2 = t1 / C
4      if t2 < W goto L2
5      M = t1 * k
6      t3 = M + I
7  L2:  H = I
8      M = t3 - H
9      if t3 ≥ 0 goto L3
10     goto L1
11  L3:  halt
```

Leaders = {1, 3, 5, 7, 10, 11}      Block(3) = ?  
Basic blocks =



# Running example

```
1      A = 4
2      t1 = A * B
3  L1:  t2 = t1 / C
4      if t2 < W goto L2
5      M = t1 * k
6      t3 = M + I
7  L2:  H = I
8      M = t3 - H
9      if t3 ≥ 0 goto L3
10     goto L1
11  L3:  halt
```

Leaders = {1, 3, 5, 7, 10, 11}      Block(3) = {3, 4}  
Basic blocks =

# Running example

```
1      A = 4
2      t1 = A * B
3  L1:  t2 = t1 / C
4      if t2 < W goto L2
5      M = t1 * k
6      t3 = M + I
7  L2:  H = I
8      M = t3 - H
9      if t3 ≥ 0 goto L3
10     goto L1
11  L3:  halt
```

Leaders = {1, 3, 5, 7, 10, 11}      Block(5) = ?  
Basic blocks =

# Running example

```
1      A = 4
2      t1 = A * B
3  L1:  t2 = t1 / C
4      if t2 < W goto L2
5      M = t1 * k
6      t3 = M + I
7  L2:  H = I
8      M = t3 - H
9      if t3 ≥ 0 goto L3
10     goto L1
11  L3:  halt
```

Leaders = {1, 3, 5, 7, 10, 11}      Block(5) = {5, 6}  
Basic blocks =

# Running example

```
1      A = 4
2      t1 = A * B
3  L1:  t2 = t1 / C
4      if t2 < W goto L2
5      M = t1 * k
6      t3 = M + I
7  L2:  H = I
8      M = t3 - H
9      if t3 ≥ 0 goto L3
10     goto L1
11  L3:  halt
```

Leaders = {1, 3, 5, 7, 10, 11}      Block(7) = ?  
Basic blocks =

# Running example

```
1      A = 4
2      t1 = A * B
3  L1:  t2 = t1 / C
4      if t2 < W goto L2
5      M = t1 * k
6      t3 = M + I
7  L2:  H = I
8      M = t3 - H
9      if t3 ≥ 0 goto L3
10     goto L1
11  L3:  halt
```

Leaders = {1, 3, 5, 7, 10, 11}      Block(7) = {7, 8, 9}  
Basic blocks =

# Running example

```
1      A = 4
2      t1 = A * B
3  L1:  t2 = t1 / C
4      if t2 < W goto L2
5      M = t1 * k
6      t3 = M + I
7  L2:  H = I
8      M = t3 - H
9      if t3 ≥ 0 goto L3
10     goto L1
11  L3:  halt
```

Leaders = {1, 3, 5, 7, 10, 11}      Block(10) = ?  
Basic blocks =

# Running example

```
1      A = 4
2      t1 = A * B
3  L1:  t2 = t1 / C
4      if t2 < W goto L2
5      M = t1 * k
6      t3 = M + I
7  L2:  H = I
8      M = t3 - H
9      if t3 ≥ 0 goto L3
10     goto L1
11  L3:  halt
```

Leaders = {1, 3, 5, 7, 10, 11}      Block(10) = {10}  
Basic blocks =

# Running example

```
1      A = 4
2      t1 = A * B
3  L1:  t2 = t1 / C
4      if t2 < W goto L2
5      M = t1 * k
6      t3 = M + I
7  L2:  H = I
8      M = t3 - H
9      if t3 ≥ 0 goto L3
10     goto L1
11  L3:  halt
```

Leaders = {1, 3, 5, 7, 10, 11}      Block(11) = {11}  
Basic blocks =



# Running example

1		A = 4
2		t1 = A * B
<hr/>		
3	L1:	t2 = t1 / C
4		if t2 < W goto L2
<hr/>		
5		M = t1 * k
6		t3 = M + I
<hr/>		
7	L2:	H = I
8		M = t3 - H
9		if t3 ≥ 0 goto L3
<hr/>		
10		goto L1
<hr/>		
11	L3:	halt

Leaders = {1, 3, 5, 7, 10, 11}

Basic blocks = { {1, 2}, {3, 4}, {5, 6}, {7, 8, 9}, {10}, {11} }

# Putting edges in CFG

- There is a directed edge from  $B_1$  to  $B_2$  if
  - There is a branch from the last statement of  $B_1$  to the first statement (leader) of  $B_2$
  - $B_2$  immediately follows  $B_1$  in program order and  $B_1$  does not end with an unconditional branch
- Input: *block*, a sequence of basic blocks
- Output: The CFG

```
for  $i = 1$  to  $|block|$      $\{\{1,2\}, \{3,4\}, \{5,6\}, \{7,8,9\}, \{10\}, \{11\}\}$   
     $x =$  last statement of  $block(i)$   
    if  $stat(x)$  is a branch, then  
        for each explicit target  $y$  of  $stat(x)$   
            create edge from block  $i$  to block  $y$   
        end for  
    if  $stat(x)$  is not unconditional then  
        create edge from block  $i$  to block  $i+1$   
    end for
```

# Putting edges in CFG

- There is a directed edge from  $B_1$  to  $B_2$  if
  - There is a branch from the last statement of  $B_1$  to the first statement (leader) of  $B_2$
  - $B_2$  immediately follows  $B_1$  in program order and  $B_1$  does not end with an unconditional branch
- Input: *block*, a sequence of basic blocks
- Output: The CFG

```

for  $i = 1$  to  $|block|$ 
     $\{ \{1, 2\}, \{3, 4\}, \{5, 6\}, \{7, 8, 9\}, \{10\}, \{11\} \}$ 
     $x = \text{last statement of block}(i)$ 
    2:  $t1 = A * B$ 
    if  $\text{stat}(x)$  is a branch, then
        for each explicit target  $y$  of  $\text{stat}(x)$ 
            create edge from block  $i$  to block  $y$ 
        end for
    if  $\text{stat}(x)$  is not unconditional then
        create edge from block  $i$  to block  $i+1$ 
    end for
    
```

Edge from block 1 to block 2

# Putting edges in CFG

- There is a directed edge from  $B_1$  to  $B_2$  if
  - There is a branch from the last statement of  $B_1$  to the first statement (leader) of  $B_2$
  - $B_2$  immediately follows  $B_1$  in program order and  $B_1$  does not end with an unconditional branch
- Input: *block*, a sequence of basic blocks
- Output: The CFG

```

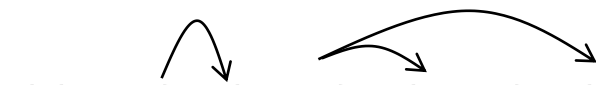
for  $i = 1$  to  $|block|$      $\{\{1, 2\}, \{3, 4\}, \{5, 6\}, \{7, 8, 9\}, \{10\}, \{11\}\}$ 
     $x = \text{last statement of } block(i)$     4:  $\text{if } t2 < W \text{ goto } L2$ 
    if  $stat(x)$  is a branch, then
        for each explicit target  $y$  of  $stat(x)$ 
            create edge from block  $i$  to block  $y$ 
        end for
    if  $stat(x)$  is not unconditional then
        create edge from block  $i$  to block  $i+1$ 
    end for
    
```

Edge from block 2 to block 4

# Putting edges in CFG

- There is a directed edge from  $B_1$  to  $B_2$  if
  - There is a branch from the last statement of  $B_1$  to the first statement (leader) of  $B_2$
  - $B_2$  immediately follows  $B_1$  in program order and  $B_1$  does not end with an unconditional branch
- Input: *block*, a sequence of basic blocks
- Output: The CFG

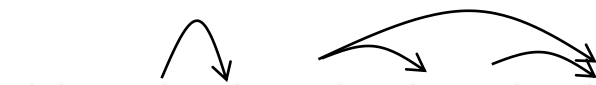
```
for i = 1 to |block|    {{1,2}}, {{3,4}}, {{5,6}}, {{7,8,9}}, {{10}}, {{11}}
    x = last statement of block(i)
    if stat(x) is a branch, then
        for each explicit target y of stat(x)
            create edge from block i to block y
        end for
    if stat(x) is not unconditional then
        create edge from block i to block i+1
    end for
```



Edge from block 2 to block 3

# Putting edges in CFG

- There is a directed edge from  $B_1$  to  $B_2$  if
  - There is a branch from the last statement of  $B_1$  to the first statement (leader) of  $B_2$
  - $B_2$  immediately follows  $B_1$  in program order and  $B_1$  does not end with an unconditional branch
- Input: *block*, a sequence of basic blocks
- Output: The CFG



```

for  $i = 1$  to  $|block|$ 
     $x = \text{last statement of } block(i)$ 
    6:  $t3 = M + I$ 
    if  $stat(x)$  is a branch, then
        for each explicit target  $y$  of  $stat(x)$ 
            create edge from block  $i$  to block  $y$ 
        end for
    if  $stat(x)$  is not unconditional then
        create edge from block  $i$  to block  $i+1$ 
    end for
    
```

Edge from block 3 to block 4

# Putting edges in CFG

- There is a directed edge from  $B_1$  to  $B_2$  if
  - There is a branch from the last statement of  $B_1$  to the first statement (leader) of  $B_2$
  - $B_2$  immediately follows  $B_1$  in program order and  $B_1$  does not end with an unconditional branch
- Input: *block*, a sequence of basic blocks
- Output: The CFG

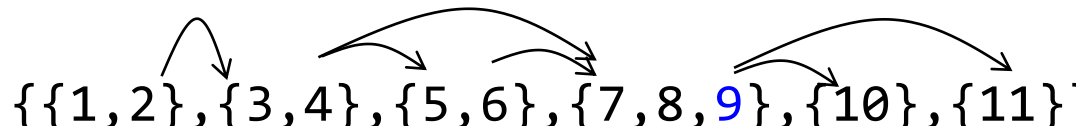
```

for  $i = 1$  to  $|block|$ 
     $x =$  last statement of  $block(i)$ 
    if  $stat(x)$  is a branch, then
        for each explicit target  $y$  of  $stat(x)$ 
            create edge from block  $i$  to block  $y$ 
        end for
    if  $stat(x)$  is not unconditional then
        create edge from block  $i$  to block  $i+1$ 
    end for
    
```

Edge from block 4 to block 6

# Putting edges in CFG

- There is a directed edge from  $B_1$  to  $B_2$  if
  - There is a branch from the last statement of  $B_1$  to the first statement (leader) of  $B_2$
  - $B_2$  immediately follows  $B_1$  in program order and  $B_1$  does not end with an unconditional branch
- Input: *block*, a sequence of basic blocks
- Output: The CFG

**for**  $i = 1$  to  $|block|$      $\{\{1, 2\}, \{3, 4\}, \{5, 6\}, \{7, 8, 9\}, \{10\}, \{11\}\}$ 


$x = \text{last statement of } block(i)$

**if**  $stat(x)$  is a branch, **then**

**for** each explicit target  $y$  of  $stat(x)$

        create edge from block  $i$  to block  $y$

**end for**

$\text{Edge from block 4 to block 5}$

$\text{if } stat(x) \text{ is not unconditional then}$

    create edge from block  $i$  to block  $i+1$

**end for**



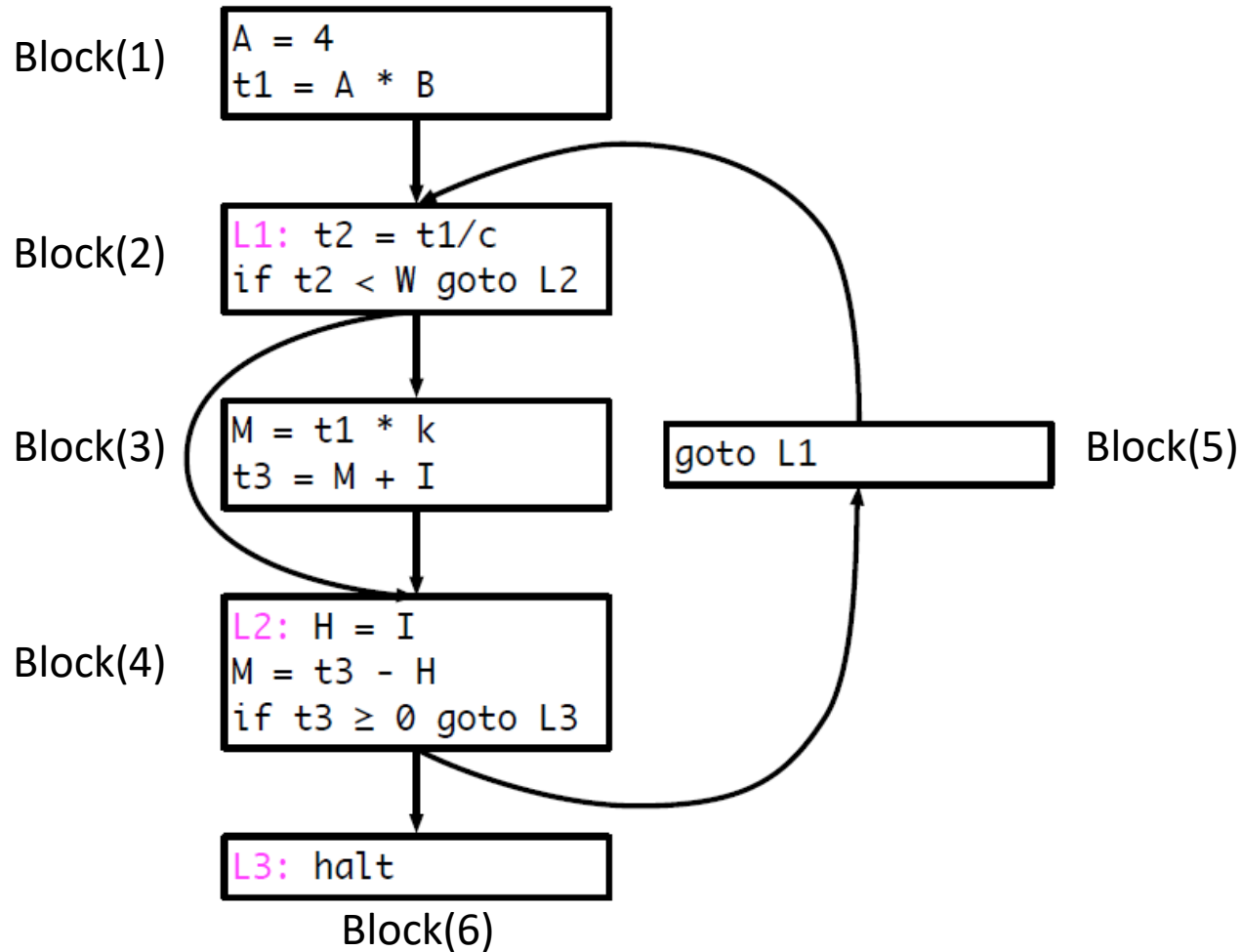
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    end for
```

Edge from block 5 to block 2

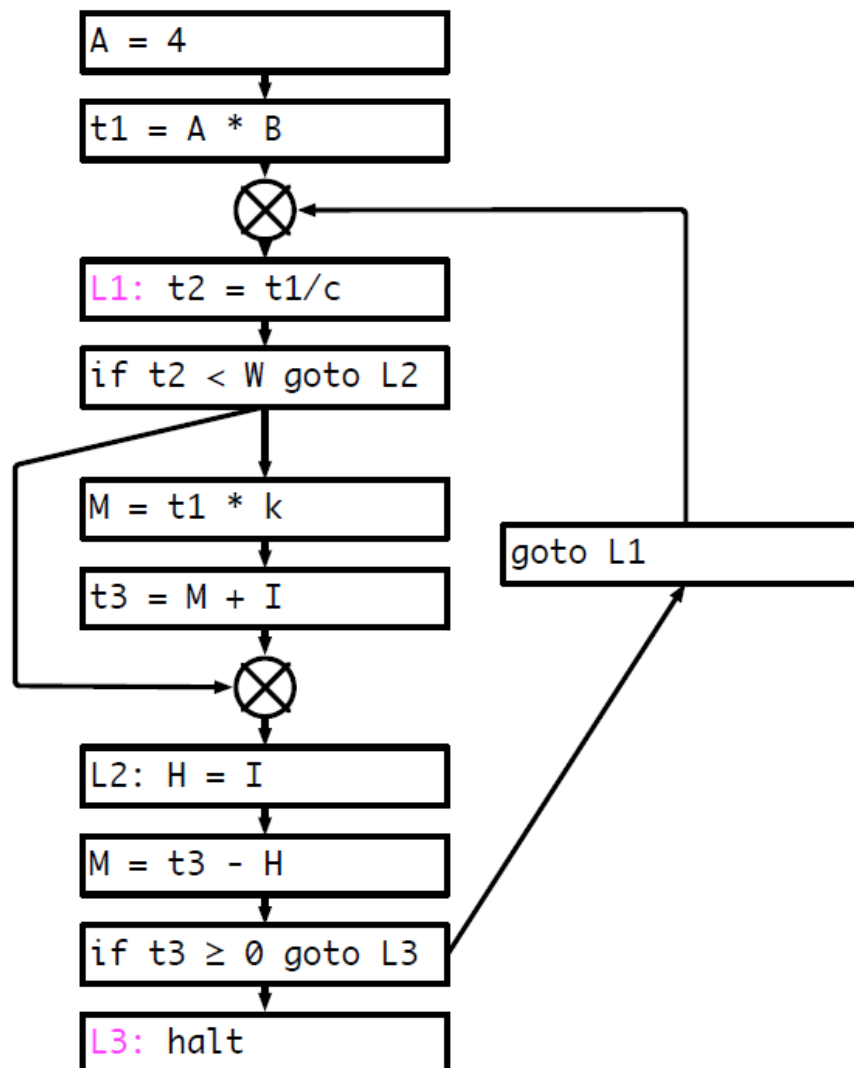
# Result



# Discussion

- Some times we will also consider the *statement-level* CFG, where each node is a statement rather than a basic block
- Either kind of graph is referred to as a CFG
- In statement-level CFG, we often use a node to explicitly represent *merging* of control
- Control merges when two different CFG nodes point to the same node
- Note: if input language is *structured*, front-end can generate basic block directly
- “GOTO considered harmful”

# Statement level CFG



# Control Flow Graphs - Use

- Why do we need CFGs? - Global Optimization
  - Optimizing compilers do global optimization ( i.e. optimize beyond basic blocks)
    - Differentiating aspect of normal and optimizing compilers
  - E.g. loops are the most frequent targets of global optimization (because they are often the “hot-spots” during program execution)

**how do we identify loops in CFGs?**

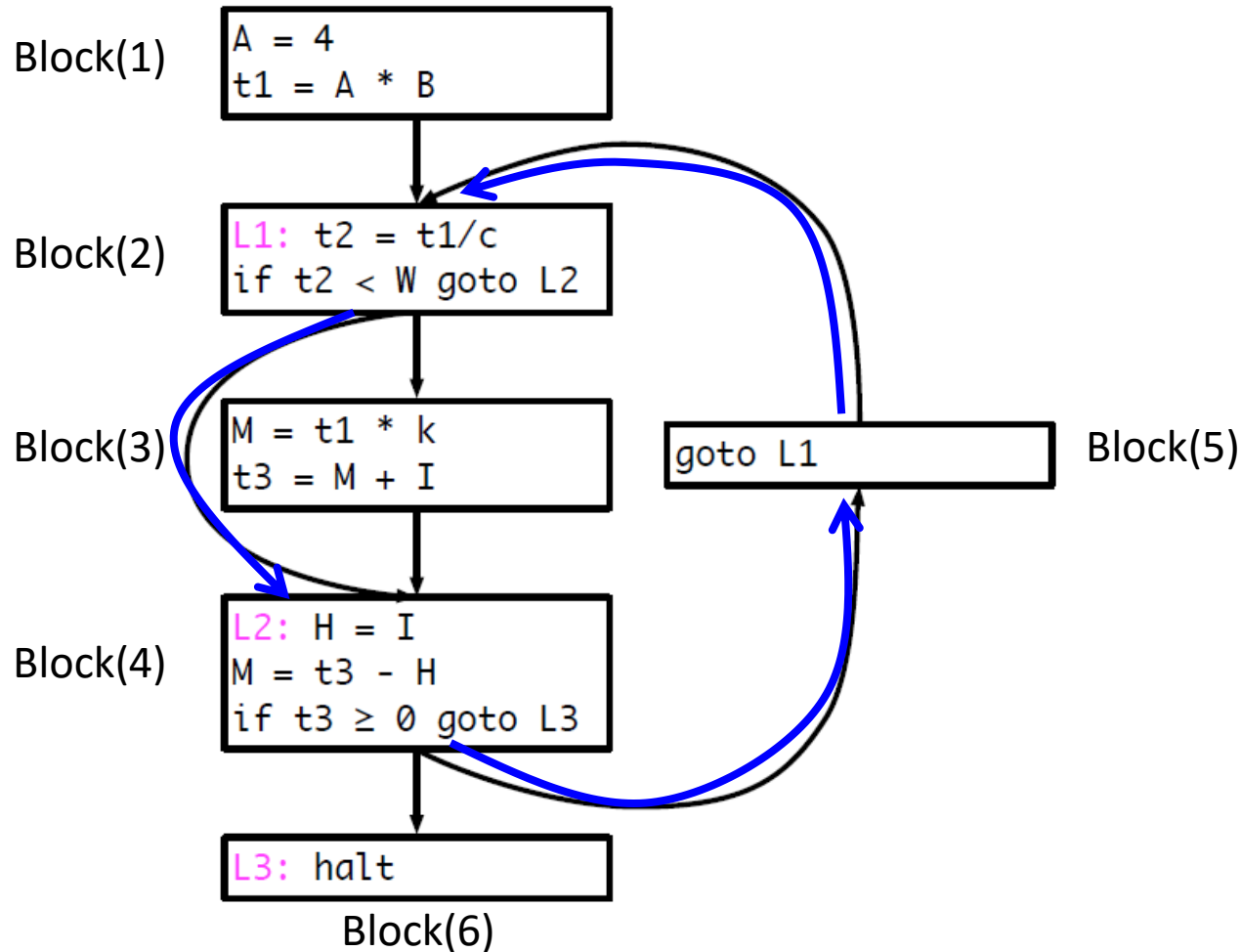
# Identify Loops in CFGs

- Loops – **how do we identify loops in CFGs?**

For a set of nodes,  $L$ , that belong to loop:

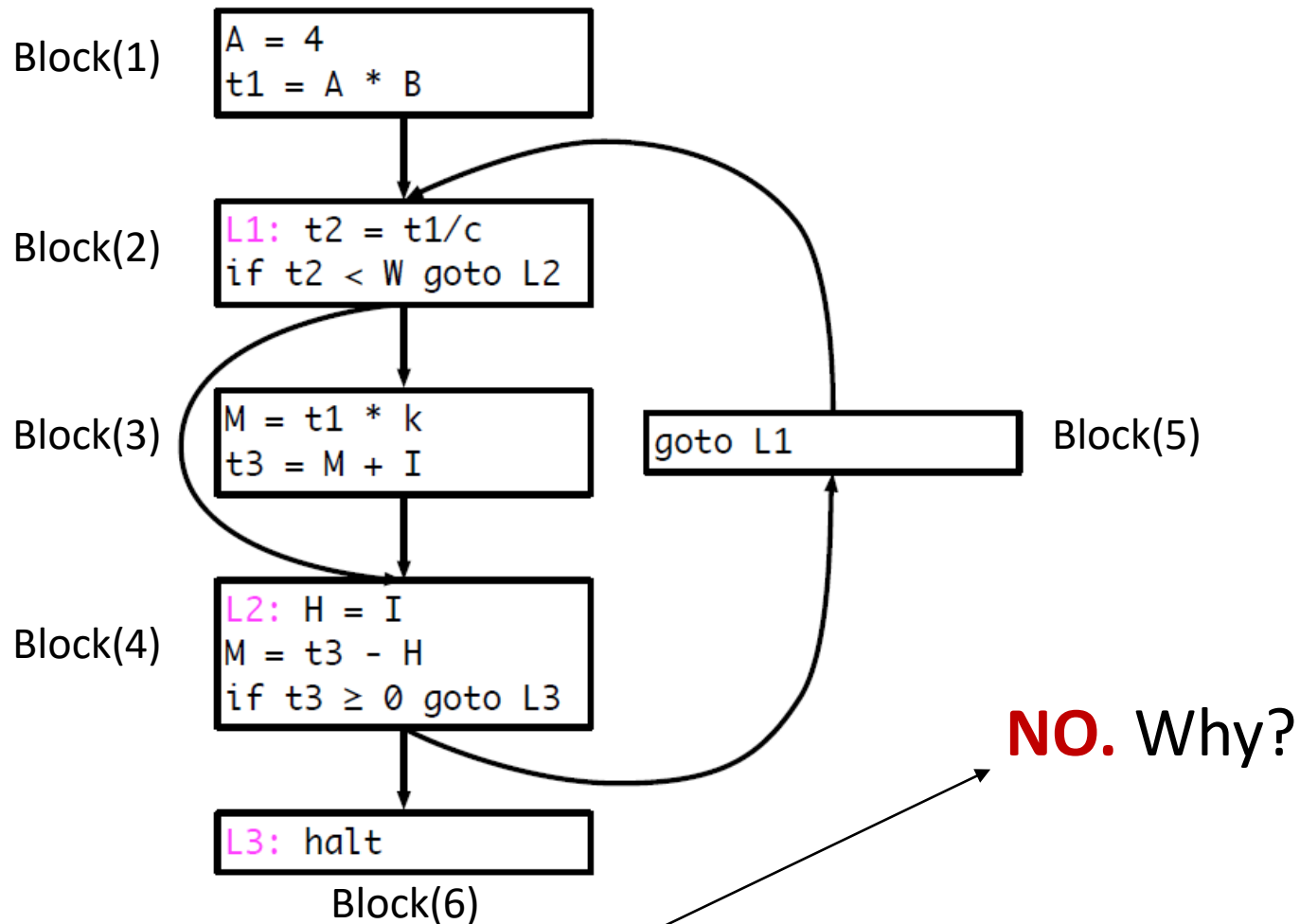
- 1) There is a *loop entry node* with the property that no other node in  $L$  has a predecessor outside  $L$ . That is, every path from entry of the entire flow graph (*graph entry node*) to any node in  $L$  goes through the loop entry node.
- 2) *Every node in  $L$*  has a non-empty path, completely within  $L$ , to the entry of  $L$ .

# Identify Loops in CFGs



Consider: {B2, B4, B5}. Is this a loop?, Are there other loops?

# Identify Loops in CFGs



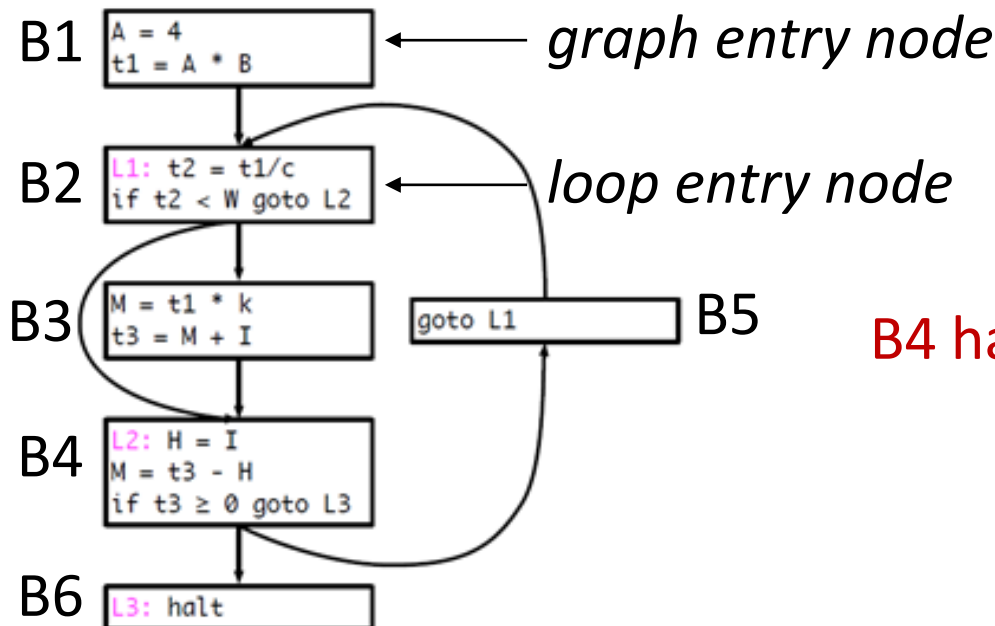
Consider: {B2, B4, B5}. Is this a loop?, Are there other loops?



# Identify Loops in CFGs

1) Is  $L = \{B2, B4, B5\}$  a loop?. **No.** Consider:

- 1) There is a *loop entry node* with the property that no other node in  $L$  has a predecessor outside  $L$ . That is, every path from entry of the entire flow graph (*graph entry node*) to any node in  $L$  goes through the loop entry node.

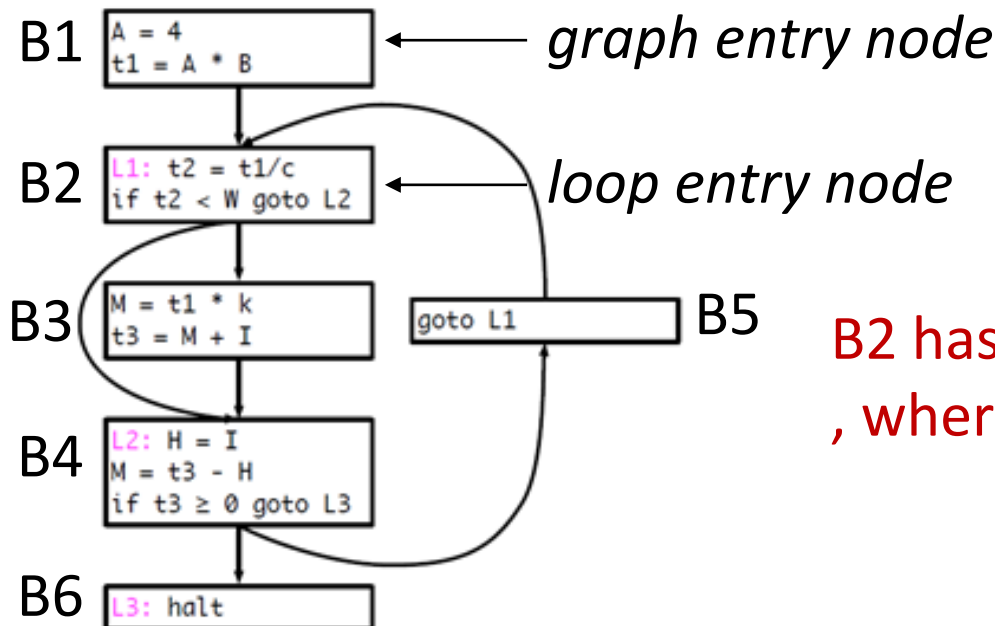


**B4 has a predecessor B3 not in L**

# Identify Loops in CFGs

1) Is  $L = \{B2, B4, B5\}$  a loop?. **No.** Consider:

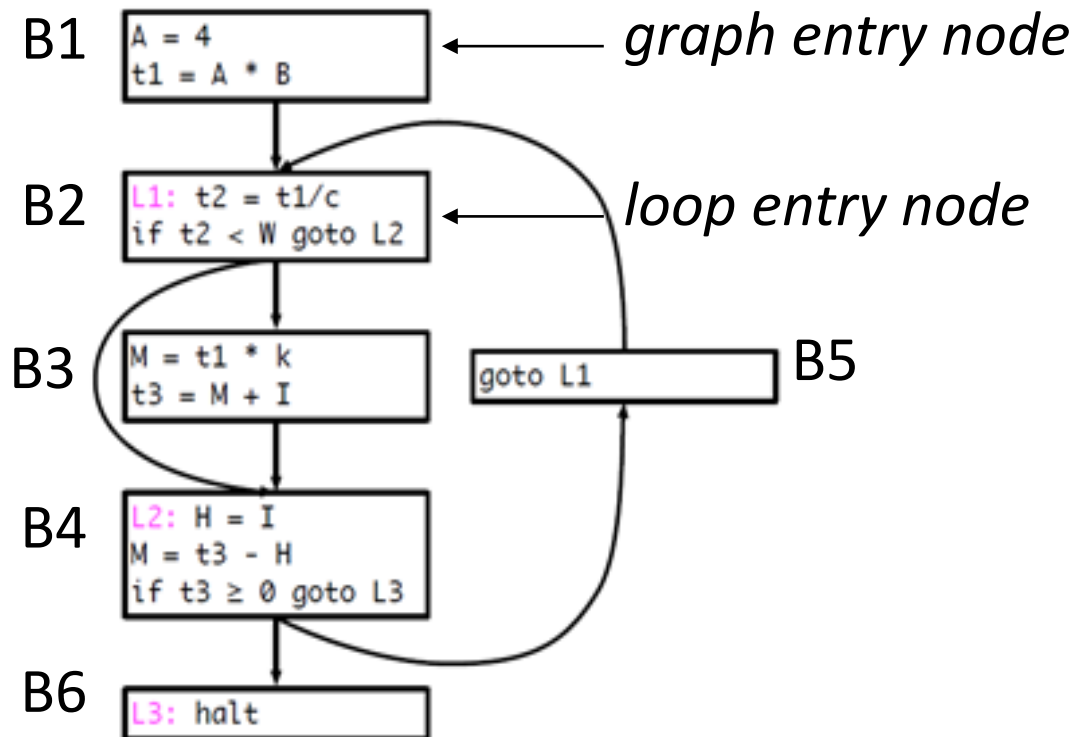
- *Every node in  $L$  has a non-empty path, completely within  $L$ , to the entry of  $L$ .*



**B2 has a path  $B2 \rightarrow B3 \rightarrow B4 \rightarrow B5 \rightarrow B2$ , where B3 is not in  $L$**

# Identify Loops in CFGs

1) Is  $L=\{B2, B3, B4, B5\}$  a loop?.



# Optimizing Loops

# Optimize Loops

- Example - Code Motion

Should be careful while doing optimization of loops

```
while J > I loop  
    A(j) := 10/I;  
    j := j + 2;  
end loop;
```

# Optimize Loops – Code Motion

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- What if  $I = 0$ ?

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    A(j) := 10/I;  
    j := j + 2;  
end loop;
```

- Optimization: can move  $10/I$  out of loop
- What if  $I = 0$ ?
- What if  $I \neq 0$  but loop executes zero times?



# Optimization Criteria - Safety and Profitability

- **Safety** - is the code produced after optimization producing same result?
- **Profitability** - is the code produced after optimization running faster or uses less memory or triggers lesser number of page faults etc.

```
while J > I loop  
    A(j) := 10/I;  
    j := j + 2;  
end loop;
```

- E.g. moving I out of the loop introduces exception (when I=0)
- E.g. if the loop is executed zero times, moving  $A(j) := 10/I$  out is not profitable

# Optimize Loops – Code Generation

- The outline of code generation for 'for' loops looked like this:

```
for (<init_stmt>;<bool_expr>;<incr_stmt>)  
  <stmt_list>  
end
```

↓

```
<init_stmt>  
LOOP:  
  <bool_expr>  
  j<!op> OUT  
  <stmt_list>  
INCR:  
  <incr_stmt>  
  jmp LOOP  
OUT:
```

```
for (i=0; i<=255;i++) {  
  <stmt_list>  
}
```

↓ **Naïve code generation**

```
code for i=0;  
LOOP: code for i<=255  
      jump0 OUT  
      code for <stmt_list>  
INCR:  code for i++  
      jump LOOP  
OUT:
```

*Question: why naïve is not good?*

# Optimize Loops – Code Generation

- What happens when ub is set to the maximum possible integer representable by the type of i?

```
for (i=0; i<=255;i++) {  
    <stmt_list>  
}
```

**Better code:**

```
code for i=0;  
code for lb=0, ub=255  
code for lb<=ub  
jump0 OUT  
LOOP:  code for <stmt_list>  
        code for i=ub  
        jump1 OUT  
INCR:  code for i++  
        jump LOOP  
OUT:
```

→  
**generalizing:**

```
code for i=0;  
compute lb, ub  
code for lb<=ub  
jump0 OUT  
assign index=lb  
assign limit=ub  
LOOP:  code for <stmt_list>  
        code for index=limit  
        jump1 OUT  
INCR:  code for increment index  
        jump LOOP  
OUT:
```