

# CS601: Software Development for Scientific Computing

Autumn 2023

Week1: Overview

# Course Takeaways (intended)

- Non-CS majors:
  1. Write code (mostly in C/C++) and
  2. Develop software (not just write standalone code)
    - Numerical software
- CS-Majors:

In addition to the above two:

  3. Learn to face mathematical equations and implement them with confidence

# Why C++ ?

- C/C++/Fortran codes form the majority in scientific computing codes
- Catch a lot of errors early (e.g. at *compile-time* rather than at *run-time*)
- Has features for *object-oriented* software development
- Known to result in codes with better *performance*

# What is this course about?

Software Development

+

Scientific Computing

# Software Development

- *Software development is the process of **conceiving, specifying, designing, programming, documenting, testing,** and **bug fixing** involved in **creating and maintaining applications, frameworks, or other software components.***

*Software development is a process of writing and maintaining the source code, but in a broader sense, it includes all that is involved between the **conception** of the desired software through to the **final manifestation** of the software, ...*

- Wikipedia on "Software Development"

# Scientific Computing

- Also called computational science
  - *Development of models to understand systems (biological, physical, chemical, engineering, humanities)*

*Collection of tools, techniques, and theories required **to solve on a computer** mathematical models of problems in science and engineering*

# This course **NOT** about..

- Software Engineering
  - Systematic study of Techniques, Methodology, and Tools to build correct software within time and price budget (topics covered in CS305)
    - People, Software life cycle and management etc.
- Scientific Computing
  - Rigorous exploration of numerical methods, their analysis, and theories
  - Programming models (topics covered in CS410)

# Who this course is for?

- You are interested in scientific computing
- You are interested in high-performance computing
- You want to build / add to a large software system

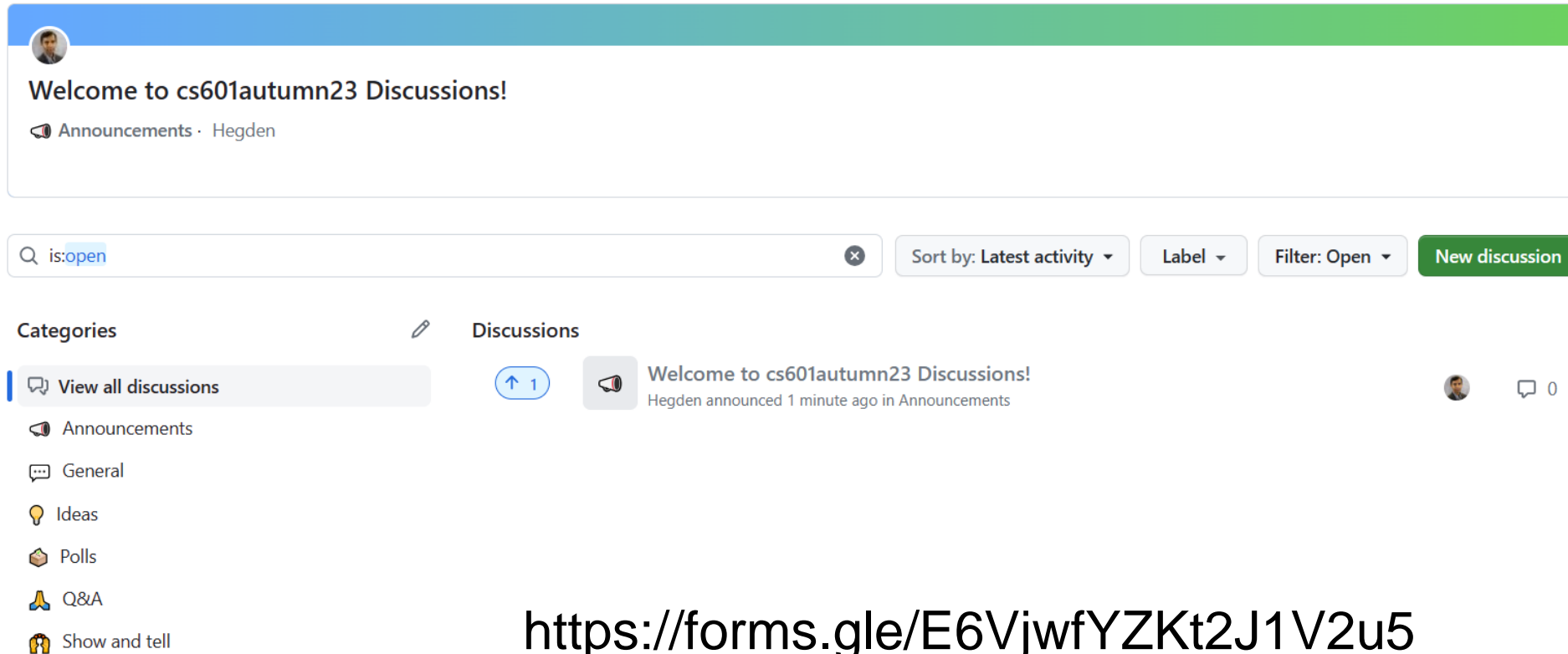


# Course Webpage

- <https://hegden.github.io/cs601>

# GitHub Discussions

- <https://github.com/IITDhCSE/cs601autumn23/discussions>



The screenshot shows the GitHub Discussions interface for the repository `cs601autumn23`. At the top, a welcome banner from user `Hegden` in the `Announcements` category is displayed. Below the banner is a search bar with the text `is:open`, a close button, and filters for `Sort by: Latest activity`, `Label`, and `Filter: Open`. A `New discussion` button is also present. On the left, the `Categories` sidebar lists `View all discussions` (selected), `Announcements`, `General`, `Ideas`, `Polls`, `Q&A`, and `Show and tell`. The main `Discussions` area shows a single announcement from `Hegden` titled `Welcome to cs601autumn23 Discussions!`, posted 1 minute ago. A small icon indicates 1 discussion is shown.

Welcome to cs601autumn23 Discussions!

Announcements · Hegden

Search: `is:open` [Close] [Sort by: Latest activity] [Label] [Filter: Open] [New discussion]

Categories

- View all discussions
- Announcements
- General
- Ideas
- Polls
- Q&A
- Show and tell

Discussions

1

Welcome to cs601autumn23 Discussions!  
Hegden announced 1 minute ago in Announcements

<https://forms.gle/E6VjwfYZKt2J1V2u5>

# Let us try an exam question (from this course) on ChatGPT

- Question:

Computing  $\sqrt{x^2 + y^2}$  is a common problem. A common implementation strategy is as follows:

```
double ComputeHypotenuse(double x, double y) {  
    return sqrt(x*x + y*y);  
}
```

However, the above strategy is not robust. How would you implement a robust code?

- <https://chat.openai.com/share/bcf4d871-21cf-4799-9275-1486345ce6dd>

## Takeaways:

- You still need to know the right questions to ask.
- Know if the answer provided makes sense.

*Develop intuition*

Let us dive into an example....

# Example - Factorial

- $$n! = n \times (n-1) \times (n-2) \times \dots \times 3 \times 2 \times 1$$
$$(n-1)! = (n-1) \times (n-2) \times \dots \times 3 \times 2 \times 1$$

therefore,

**Definition1:**  $n! = n \times (n-1)!$

*is this definition complete?*

- plug 0 to n and the equation breaks.

**Definition2:**

$$n! = \begin{cases} n \times (n-1)! & \text{when } n \geq 1 \\ 1 & \text{when } n = 0 \end{cases}$$

# Exercise 1

- Does this code implement the definition of factorial correctly?

```
int fact(int n){  
    if(n==0)  
        return 1;  
  
    return n*fact(n-1);  
  
}
```

# Example - Factorial

**Definition2:**

$$n! = \begin{cases} n \times (n-1)! & \text{when } n \geq 1 \\ 1 & \text{when } n = 0 \end{cases}$$

*is this definition complete?*

- $n!$  is not defined for negative  $n$

# Solution - Factorial

```
int fact(int n){  
    if(n<0)  
        return ERROR;  
    if(n==0)  
        return 1;  
  
    return n*fact(n-1);  
  
}
```



# Exercise 2

- In how many flops does the code execute?  
assume 1 flop = 1 step executing **any** arithmetic operation

```
int fact(int n){  
    if(n<0)  
        return ERROR;  
    if(n==0)  
        return 1;  
  
    return n*fact(n-1);  
  
}
```

# Exercise 3

- Does the code yield correct results for any  $n$ ?

```
int fact(int n){  
    if(n<0)  
        return ERROR;  
    if(n==0)  
        return 1;  
  
    return n*fact(n-1);  
  
}
```

# Who this course is for?

- Anybody who wishes to develop "computational thinking"
  - A skill necessary for everyone, not just computer programmers
  - An approach to problem solving, designing systems, and understanding human behavior that draws on concepts fundamental to computer science.

# Computational Thinking - Examples

- How difficult is the problem to solve? And what is the best way to solve?
- Modularizing something in anticipation of multiple users
- Prefetching and caching in anticipation of future use
- Thinking recursively
- Reformulating a seemingly difficult problem into one which we know how to solve by reduction, embedding, transformation, simulation
  - Are approximate solutions accepted?
  - False positives and False negatives allowed? etc.
- Using abstraction and decomposition in tackling large problem
- ...

# Computational Thinking – 2 As

- Abstractions
  - Our “mental” tools
  - Includes: choosing right abstractions, operating at multiple layers of abstractions, and defining relationships among layers
- Automation
  - Our “metal” tools that amplify the power of “mental” tools
  - Is mechanizing our abstractions, layers, and relationships
    - Need precise and exact notations / models for the “computer” below (“computer” can be human or machine)

# Computing - 2 As Combined

- Computing is the **automation** of our **abstractions**
- Provides us the ability to scale
  - Make infeasible problems feasible
    - E.g. SHA-1 not safe anymore
  - Improve the answer's precision
    - E.g. capture the image of a black-hole

**Summary:** choose the right abstraction and computer

# Computational Thinking – applied to the factorial exercise

- Need to be precise (formulating)
  - recall:  $n! = 1$  for  $n=0$ , not defined for negative  $n$
- Choosing right abstractions
  - recall: use of recursion, correct data type
- Ability to define the complexity
  - recall: flop calculation
- What else?

# Computational Thinking – applied to the factorial exercise

- Need to be precise (formulating)
  - recall:  $n! = 1$  for  $n=0$ , not defined for negative  $n$
- Choosing right abstractions
  - recall: use of recursion, correct data type
- Ability to define the complexity
  - recall: flop calculation
- Choose the right “computer” for mechanizing the abstractions chosen



# General Approach to Solving a Computational Problem

1. **Problem statement:** more precise this is, the easier it is to design and implement
2. **Solution Algorithm:** exactly how is the problem going to be solved
3. **Implementation:** breaking the algorithm into manageable pieces and putting it all together to solve the problem using a language of choice.
4. **Verification:** checking that the implementation solves the original problem.
  - For numerical software this is often most difficult step, because you don't know the correct answer.

# Scientific Software - Characteristics

- The answer is not a typical yes/no, red/blue/green
- The answer varies continuously. Think of computing the value of  $\pi = 3.141592\dots$
- Uses approximations. Think of *discretization*
- Employs efficient *kernels*
  - Kernels are core operations that are executed very frequently
- Should be able to adapt to change.
  - Writing everything from scratch is not an option
- Deals with large-scale problems
  - Lot of input/output data or both
  - Computationally hard

# Toward Scientific Software

- Necessary Skills:
  - Understanding the mathematical problem
  - Understanding numerics
  - Designing algorithms and data structures
  - Selecting language and using libraries and tools
  - Verify the correctness of the results
  - Quick learning of new programming languages

# Exercise

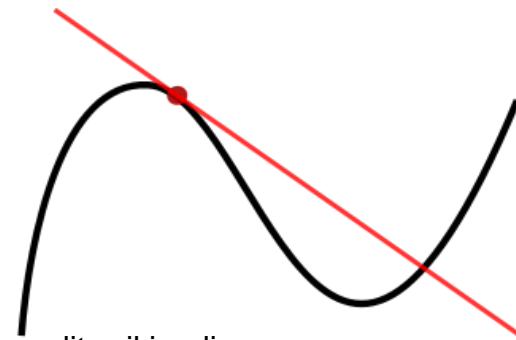
Compute root(s) of:

$$x = \cos x; \quad x \in \mathbb{R}$$

roots, also called zeros, is the value of the argument/input to the function when the function output vanishes i.e. becomes zero

# Mathematical Problem

- let  $y = f(x)$   
 $f(x) = \cos(x) - x$
- At  $x = x_n$ , the value of  $y$  is  $f(x_n)$ . The coordinates of the point are  $(x_n, f(x_n)) = \text{known point}$ .
- From calculus: **derivative** of a function of single variable at a chosen input value, when it exists, is the **slope of the tangent** to the graph at that input value.
  - $f'(x_n)$  is the slope of the line that is tangent to  $f(x)$  at  $x_n$



credit: wikipedia

# Mathematical Problem

- From high-school math: point-slope formula for equation of a line

$$y - y_1 = m(x - x_1),$$

given the slope  $m$  and any known point  $(x_1, y_1)$

- Substituting with:
  - $(x_n, f(x_n))$  = known point
  - $f'(x_n)$  = slope

**Equation of the tangent line to graph of  $f(x)$  at  $x_n$  :**

$$y - f(x_n) = f'(x_n)(x - x_n)$$

# Mathematical Problem

- Interested in finding roots i.e. value of  $x$  at  $y=0$  i.e. at point  $(x_{np1}, 0)$ .
- Substituting in the equation of the tangent line,

$$y - f(x_n) = f'(x_n)(x - x_n)$$

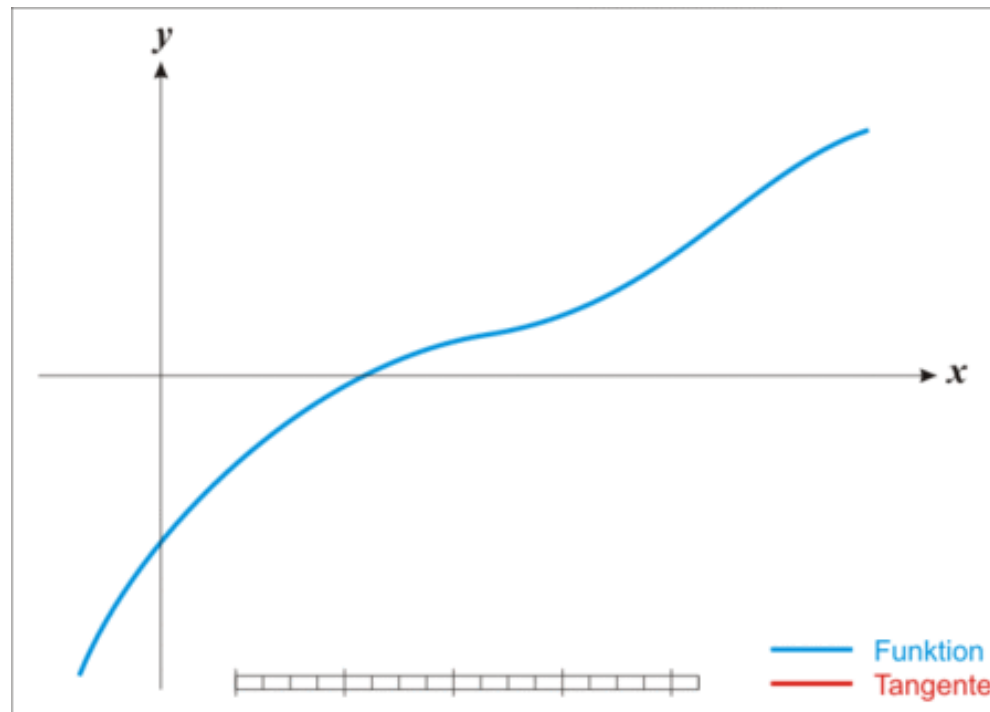
$$= -f(x_n) = f'(x_n)(x_{np1} - x_n)$$

$$= x_{np1} = x_n - f(x_n) / f'(x_n)$$

# Mathematical Problem

- Visualizing

(source: [https://en.wikipedia.org/wiki/Newton's\\_method](https://en.wikipedia.org/wiki/Newton's_method)) :



The function  $f$  is shown in blue and the tangent line is in red. We see that  $x_{n+1}$  is a better approximation than  $x_n$  for the root  $x$  of the function  $f$ .



# Mathematical Problem

$$x_2 = x_1 - f(x_1) / f'(x_1)$$

$$x_3 = x_2 - f(x_2) / f'(x_2)$$

$$x_4 = x_3 - f(x_3) / f'(x_3)$$

...

# Numerical Analysis

Talk to domain experts

- Choosing the initial value of  $x$
- Does the method converge ?
- What is an acceptable approximation?
- etc.

# Designing Algorithms and Data Structures

- Start with  $x_1$

$$x_2 = x_1 - f(x_1) / f'(x_1)$$

$$x_3 = x_2 - f(x_2) / f'(x_2)$$

$$x_4 = x_3 - f(x_3) / f'(x_3)$$

...

- Repeat for up to maxIterations
- Check for  $x_{n+1} - x_n$  to be “sufficiently small”
- Choose appropriate data types for  $x$

# Selecting libraries and tools

- E.g. use the math library in C++ (cmath)

# Verify the correctness of results

- Compare with 'gold' code / benchmark
- Compare with empirical data

# Scientific Software - Examples

## Entertainment

- Toy Story, Shrek rendered using data-center nodes

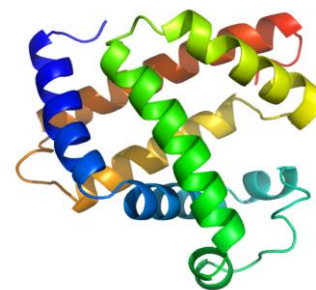
## Economics

- ad-placement

# Scientific Software - Examples

## Biology

- Shotgun algorithm expedites sequencing of human genome



Credit: Wikipedia

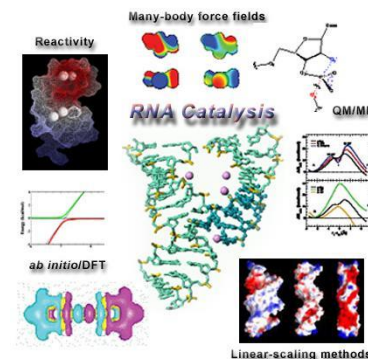
- Analyzing fMRI data



Credit: Wikipedia

## Chemistry

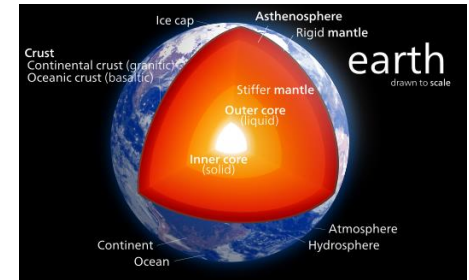
- optimization and search algorithms to identify best chemicals for improving reaction conditions to improve yields



# Scientific Software - Examples

## Geology

- Modeling the Earth's surface to the core



Credit: Wikipedia

## Astronomy

- kd-trees help analyze very large multi-dimensional data sets



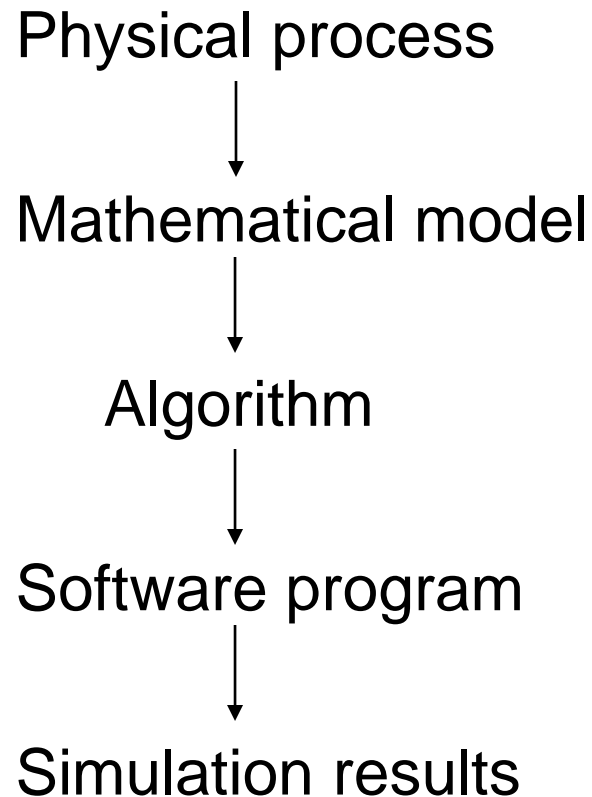
Credit: Kaggle.com

## Engineering

- Boeing 777 tested via computer simulation (not via wind tunnel)



# Recap: Toward Scientific Software



# Scientific Software - Motifs

noun

1. a decorative image or design, especially a repeated one forming a pattern.  
"the colourful hand-painted motifs which adorn narrowboats"

Similar:

design

pattern

decoration

figure

shape

logo

monogram



2. a dominant or recurring idea in an artistic work.  
"superstition is a recurring motif in the book"

- |                           |                                |
|---------------------------|--------------------------------|
| 1. Finite State Machines  | 8. Dynamic Programming         |
| 2. Combinatorial          | 9. <u>N-Body ( / particle)</u> |
| 3. Graph Traversal        | 10. MapReduce                  |
| 4. <u>Structured Grid</u> | 11. Backtrack / B&B            |
| 5. <u>Dense Matrix</u>    | 12. Graphical Models           |
| 6. <u>Sparse Matrix</u>   | 13. <u>Unstructured Grid</u>   |
| 7. <u>FFT</u>             |                                |