CS406: Compilers Spring 2021

Week 5: Parsers

```
    S -> ABc$
    A -> xaA
    A -> yaA
    A -> c
    B -> b
    B -> λ
```

```
first (S) = { ? } Think of all possible strings derivable from S. Get the first terminal symbol in those strings or \lambda if S derives \lambda
```

```
1) S -> ABc$
2) A -> xaA
3) A -> yaA
4) A -> c
5) B -> b
6) B -> λ
first (S) = { x, y, c }
```

```
1) S -> ABc$
2) A -> xaA
3) A -> yaA
4) A -> c
5) B -> b
6) B -> λ

first (S) = { x, y, c }
first (A) = { ? }
```

```
1) S -> ABc$
2) A -> xaA
3) A -> yaA
4) A -> c
5) B -> b
6) B -> λ

first (S) = { x, y, c }
first (A) = { x, y, c }
```

```
1) S -> ABc$
2) A -> xaA
3) A -> yaA
4) A \rightarrow c
5) B -> b
6) B \rightarrow \lambda
first (S) = \{ x, y, c \}
first (A) = \{ x, y, c \}
first (B) = { ? }
```

```
1) S -> ABc$
2) A -> xaA
3) A -> yaA
4) A \rightarrow c
5) B -> b
6) B \rightarrow \lambda
first (S) = \{ x, y, c \}
first (A) = \{ x, y, c \}
first (B) = { b, \lambda }
```

```
    S -> ABc$
    A -> xaA
    A -> yaA
    A -> c
    B -> b
    B -> λ
```

```
follow (S) = \{?\}
```

Think of all strings **possible in the language** having the form ... Sa... Get the following terminal symbol a after S in those strings or \$ if you get a string ... \$\$

```
    S -> ABc$
    A -> xaA
    A -> yaA
    A -> c
    B -> b
    B -> λ
```

```
1) S -> ABc$
2) A -> xaA
3) A -> yaA
4) A -> c
5) B -> b
6) B -> λ

follow (S) = { }
follow (A) = { ? }
```

```
1) S -> ABc$
2) A -> xaA
3) A -> yaA
4) A -> c
5) B -> b
6) B -> λ

follow (S) = {
  follow (A) = { b, c }
    e.g. xaAbc$, xaAc$
```

```
1) S -> ABc$
2) A -> xaA
3) A -> yaA
4) A \rightarrow c
5) B -> b
6) B \rightarrow \lambda
follow(S) = { }
follow (A) = \{ b, c \}
                           e.g. xaAbc$, xaAc$
What happens when you consider. A -> xaA or A -> yaA ?
```

```
1) S -> ABc$
2) A -> xaA
3) A \rightarrow yaA
4) A -> c
5) B -> b
6) B \rightarrow \lambda
follow(S) = { }
follow (A) = \{ b, c \}
                              e.g. xaAbc$, xaAc$
What happens when you consider. A -> xaA or A -> yaA ?

    You will get string of the form A=>+ (xa)+A
```

But we need strings of the form: ..Aa.. or ..Ab. or ..Ac..

```
1) S -> ABc$
2) A -> xaA
3) A -> yaA
4) A \rightarrow c
5) B -> b
6) B \rightarrow \lambda
follow(S) = { }
follow (A) = \{ b, c \}
follow (B) = { ? }
```

```
1) S -> ABc$
2) A -> xaA
3) A -> yaA
4) A \rightarrow c
5) B -> b
6) B \rightarrow \lambda
follow(S) = { }
follow (A) = \{ b, c \}
follow (B) = \{c\}
```

```
1) S -> ABc$
2) A -> xaA
3) A -> yaA
4) A -> c
5) B -> b
6) B -> \lambda
\begin{cases} First(X_1...X_m) & \text{if } \lambda \notin First(X_1...X_m) \\ (First(X_1...X_m) - \lambda) \cup Follow(A) & \text{otherwise} \end{cases}

Predict (1) = { ? } = First(ABc$) if \lambda \notin First(ABc$)
```

```
1) S -> ABc$
2) A -> xaA
3) A -> yaA
```

4)	Α	->	C

6) B
$$\rightarrow$$
 λ

	X	у	а	b	С	\$
S	1	1			1	
Α						
В						

Predict
$$(1) = \{ x, y, c \}$$

```
    S -> ABc$
    A -> xaA
    A -> yaA
    A -> c
    B -> b
    B -> λ
```

	X	у	а	b	С	\$
S	1	1			1	
Α						
В						

```
Predict (1) = { x, y, c }

Predict (2) = { ? } = First(xaA) if \lambda \notin First(xaA)
```

```
    S -> ABc$
    A -> xaA
    A -> yaA
    A -> c
    B -> b
    B -> λ
```

	X	у	а	b	С	\$
S	1	1			1	
Α	2					
В						

```
Predict (1) = { x, y, c }
Predict (2) = { x }
```

```
    S -> ABc$
    A -> xaA
    A -> yaA
    A -> c
    B -> b
    B -> λ
```

	X	у	а	b	С	\$
S	1	1			1	
Α	2					
В						

```
Predict (1) = { x, y, c }

Predict (2) = { x }

Predict (3) = { ? } = First(yaA) if λ ∉ First(yaA)
```

```
    S -> ABc$
    A -> xaA
    A -> yaA
    A -> c
    B -> b
    B -> λ
```

	X	y	а	b	С	\$
S	1	1			1	
Α	2	3				
В						

```
Predict (1) = { x, y, c }
Predict (2) = { x }
Predict (3) = { y }
```

```
    S -> ABc$
    A -> xaA
    A -> yaA
    A -> c
    B -> b
    B -> λ
```

	Х	у	а	b	С	\$
S	1	1			1	
Α	2	3				
В						

```
Predict (1) = { x, y, c }

Predict (2) = { x }

Predict (3) = { y }

Predict (4) = { ? } = First(c) if λ ∉ First(c)
```

```
    S -> ABc$
    A -> xaA
    A -> yaA
```

6) B
$$\rightarrow$$
 λ

	X	у	а	b	С	\$
S	1	1			1	
Α	2	3			4	
В						

```
Predict (1) = { x, y, c }
Predict (2) = { x }
Predict (3) = { y }
Predict (4) = { c }
```

```
    S -> ABc$
    A -> xaA
    A -> yaA
    A -> c
    B -> b
    B -> λ
```

	X	у	а	b	С	\$
S	1	1			1	
Α	2	3			4	
В						

```
Predict (1) = { x, y, c }

Predict (2) = { x }

Predict (3) = { y }

Predict (4) = { c }

Predict (5) = { ? } = First(b) if λ ∉ First(b)
```

```
    S -> ABc$
    A -> xaA
    A -> yaA
    A -> c
    B -> b
    B -> λ
```

	X	у	а	b	С	\$
S	1	1			1	
Α	2	3			4	
В				5		

```
Predict (1) = { x, y, c }
Predict (2) = { x }
Predict (3) = { y }
Predict (4) = { c }
Predict (5) = { b }
```

```
    S -> ABc$
    A -> xaA
```

6) B
$$\rightarrow \lambda$$

	X	У	а	b	С	\$
S	1	1			1	
Α	2	3			4	
В				5		

```
Predict (1) = { x, y, c }

Predict (2) = { x }

Predict (3) = { y }

Predict (4) = { c }

Predict (5) = { b }

Predict (6) = { ? } = First(\lambda)?
```

```
1) S -> ABc$
```

6) B
$$\rightarrow \lambda$$

	X	У	а	b	С	\$
S	1	1			1	
Α	2	3			4	
В				5		

```
Predict (1) = { x, y, c }

Predict (2) = { x }

Predict (3) = { y }

Predict (4) = { c }

Predict (5) = { b }

Predict (6) = { ? } = First(\lambda) ? Follow(B)
```

```
    S -> ABc$
    A -> xaA
    A -> yaA
    A -> c
    B -> λ
```

	X	у	а	b	С	\$
S	1	1			1	
Α	2	3			4	
В				5	6	

```
Predict (1) = { x, y, c }
Predict (2) = { x }
Predict (3) = { y }
Predict (4) = { c }
Predict (5) = { b }
Predict (6) = { c }
```

Computing Parse-Table

3)
$$A \rightarrow yaA$$

4)
$$A \rightarrow c$$

6) B
$$\rightarrow$$
 λ

	X	у	а	b	С	\$
S	1	1			1	
Α	2	3			4	
В				5	6	

first (S) = {x, y, c} follow (S) = {} P(1) = {x,y,c} first (A) = {x, y, c} follow (A) = {b, c} P(2) = {x} first(B) = {b,
$$\lambda}$$
 follow(B) = {c} P(3) = {y} P(4) = {c}

Parsing using parse table and a stackbased model (non-recursive)

```
string: xacc$
```

Stack	Rem. Input	Action
?	xacc\$?

What do you put on the stack?

```
string: xacc$
```

```
Stack Rem. Input Action

> xacc$
```

What do you put on the stack? – strings that you derive

string: xacc\$

Stack* Rem. Input Action

sacc\$

Top-down parsing. So, start with S.

string: xacc\$



Top-down parsing. So, start with S.

What action do you take when stack-top has symbol S and the string to be matched has terminal x in front?

³⁴

string: xacc\$

Stack* Rem. Input Action

S xacc\$ Predict(1) S->ABc\$

Top-down parsing. So, start with S.

What action do you take when stack-top has symbol S and the string to be

matched has terminal x in front? - consult parse table

	X	У	а	b	С	\$
S	1	1			1	
Α	2	3			4	
В				5	6	

³⁵

string: xacc\$

ABc\$

Stack* Rem. Input Action

xacc\$ Predict(1) S->ABc\$

 x
 y
 a
 b
 c
 \$

 S
 1
 1
 1
 1

 A
 2
 3
 4
 4

 B
 5
 6
 6

³⁶

string: xacc\$

Stack*	Rem. Input	Action	
S	xacc\$	Predict(1)	S->ABc\$
<mark>A</mark> Bc\$	<mark>x</mark> acc\$		

What action do you take when stack-top has symbol A and the string to be matched has terminal x in front? - consult parse table

	X	У	а	b	С	\$
S	~	~			1	
Α	2	3			4	
В				5	6	

³⁷

string: xacc\$

Stack*	Rem. Input	Action
S	xacc\$	Predict(1) S->ABc\$
ABc\$	xacc\$	<pre>Predict(2) A->xaA</pre>

What action do you take when stack-top has symbol A and the string to be matched has terminal x in front? - consult parse table

	X	У	а	b	С	\$
S	1	1			1	
Α	2	3			4	
В				5	6	

³⁸

Stack*	Rem. Input	Action		
S	xacc\$	Predict(1) S->A	=	
ABc\$	xacc\$	<pre>Predict(2) A->x</pre>	aA	
VANDCU				

	X	У	а	Ь	С	\$
S	1	1			1	
Α	2	3			4	
В				5	6	

Stack*	Rem. Input	Action	
S	xacc\$	Predict(1)	S->ABc\$
ABc\$	xacc\$	Predict(2)	A->xaA
<mark>x</mark> aABc\$	<mark>x</mark> acc\$?	

	X	У	а	Ь	С	\$
S	1	1			1	
Α	2	3			4	
В				5	6	

Stack*	Rem. Input	Action	
S	xacc\$	Predict(1)	S->ABc\$
ABc\$	xacc\$	Predict(2)	A->xaA
<mark>x</mark> aABc\$	<mark>x</mark> acc\$	<pre>match(x)</pre>	

	X	У	а	b	С	\$
S	1	1			1	
Α	2	3			4	
В		·		5	6	

Stack*	Rem. Input	Action	
S	xacc\$	Predict(1)	S->ABc\$
ABc\$	xacc\$	Predict(2)	A->xaA
xaABc\$	xacc\$	match(x)	
<mark>a</mark> ABc\$	<mark>a</mark> cc\$	<pre>match(a)</pre>	

	X	У	а	b	С	\$
S	1	1			1	
Α	2	3			4	
В				5	6	

Stack*	Rem. Input	Action
S	xacc\$	Predict(1) S->ABc\$
ABc\$	xacc\$	Predict(2) A->xaA
xaABc\$	xacc\$	<pre>match(x)</pre>
aABc\$	acc\$	match(a)
<mark>A</mark> Bc\$	<mark>c</mark> c\$? x y a b

x
 y
 a
 b
 c
 \$

 S
 1
 1
 1

 A
 2
 3
 4

 B
 5
 6

⁴³

Rem Innut

string: xacc\$

Stack*

	X	У	а	b	С	\$
S	1	1			1	
Α	2	3			4	
В				5	6	

Action

Stack	Kem. mpat	Action			<u> </u>
S	xacc\$	Predict(1)	S->/	ЧВс	\$
ABc\$	xacc\$	Predict(2)	A->>	каА	ı
xaABc\$	xacc\$	match(x)			
aABc\$	acc\$	<pre>match(a)</pre>			
<mark>A</mark> Bc\$	<mark>c</mark> c\$	Predict(4)	A->0		

⁴⁴

Dam Innut

string: xacc\$

Stack*

	X	У	a	b	С	\$
S	1	1			1	
Α	2	3			4	
В				5	6	

Slack	Keni. Input	Action				J
S	xacc\$	Predict(1)	S-:	>AE	3 c	:\$
ABc\$	xacc\$	Predict(2)	A- 2	×X	aΔ	1
xaABc\$	xacc\$	match(x)				
aABc\$	acc\$	<pre>match(a)</pre>				
<mark>A</mark> Bc\$	cc\$	Predict(4)	A- 2	> C		
<mark>c</mark> Bc\$						

⁴⁵

Dom Innut

string: xacc\$

Ctack*

	X	У	а	b	C	\$
S	1	1			1	
Α	2	3			4	
В				5	6	

Action

Slack	Kem. Input	Action	
S	xacc\$	Predict(1)	S->ABc\$
ABc\$	xacc\$	Predict(2)	A->xaA
xaABc\$	xacc\$	match(x)	
aABc\$	acc\$	<pre>match(a)</pre>	
ABc\$	cc\$	Predict(4)	A->c
<mark>c</mark> Bc\$	<mark>c</mark> c\$?	

⁴⁶

string: xacc\$

Stack*

	X	У	а	b	С	\$
S	1	1			1	
Α	2	3			4	
В				5	6	

Action

Otaon	itemi mpat	Action	
S	xacc\$	Predict(1)	S->ABc
ABc\$	xacc\$	Predict(2)	A->xaA
xaABc\$	xacc\$	match(x)	
aABc\$	acc\$	match(a)	
ABc\$	cc\$	Predict(4)	A->c
<mark>c</mark> Bc\$	<mark>c</mark> c\$	<pre>match(c)</pre>	

Rem Innut

⁴⁷

	X	У	а	b	С	\$
S	1	1			1	
Α	2	3			4	
В				5	6	

Stac	:k*	
Stac	K*	

Action	

	-		
S	xacc\$	Predict(1)	S->ABc\$
ABc\$	xacc\$	Predict(2)	A->xaA
xaABc\$	xacc\$	match(x)	
aABc\$	acc\$	match(a)	
ABc\$	cc\$	Predict(4)	A->c
cBc\$	cc\$	<pre>match(c)</pre>	
<mark>B</mark> c\$	<mark>c</mark> \$?	

⁴⁸

string: xacc\$

Stack*

	X	У	а	b	С	\$
S	1	1			1	
Α	2	3			4	
В				5	6	

S->ABc\$

A->xaA

 $A \rightarrow c$

 $B - > \lambda$

Action

	•	L
S	xacc\$	Predict(1)
ABc\$	xacc\$	Predict(2)
xaABc\$	xacc\$	match(x)
aABc\$	acc\$	<pre>match(a)</pre>
ABc\$	cc\$	Predict(4)
cBc\$	cc\$	<pre>match(c)</pre>
Bc\$	c\$	Predict(6)

Rem. Input

⁴⁹

string: xacc\$

	X	У	а	b	С	\$
S	1	1			1	
Α	2	3			4	
В				5	6	

Stack*	Rem. Input
--------	------------

S
ABc\$
xaABc\$
aABc\$
ABc\$
cBc\$
<mark>B</mark> c\$
_ c\$

```
xacc$ Predict(1) S->ABc$
xacc$ Predict(2) A->xaA
xacc$ match(x)
acc$ match(a)
cc$ Predict(4) A->c
cc$ match(c)
c$ Predict(6) B->λ
```

Action

⁵⁰

string: xacc\$

	X	У	а	b	C	\$
S	1	1			1	
Α	2	3			4	
В				5	6	

S->ABc\$

A->xaA

A - > c

 $B - > \lambda$

Action

Stack*	Rem.	Inpu
Stack	Rem.	mp

S	xacc\$	Predict(1)
ABc\$	xacc\$	Predict(2)
xaABc\$	xacc\$	match(x)
aABc\$	acc\$	match(a)
ABc\$	cc\$	Predict(4)
cBc\$	cc\$	<pre>match(c)</pre>
Bc\$	c \$	Predict(6)
<mark>c</mark> \$	<mark>c</mark> \$?

⁵¹

string: xacc\$

Stack*

	X	У	a	b	C	\$
S	1	1			1	
Α	2	3			4	
В				5	6	

Action

Otaon	rtom mpat	71011011
S	xacc\$	Predict(1) S->ABc\$
ABc\$	xacc\$	Predict(2) A->xaA
xaABc\$	xacc\$	match(x)
aABc\$	acc\$	match(a)
ABc\$	cc\$	Predict(4) A->c
cBc\$	cc\$	match(c)
Bc\$	<u>c</u> \$	Predict(6) B->λ
<mark>c</mark> \$	<mark>c</mark> \$	<pre>match(c)</pre>

Rem. Input

⁵²

Rem. Input

string: xacc\$

Stack*

	X	У	а	b	С	\$
S	1	1			1	
Α	2	3			4	
В				5	6	

Action

O 001011			
S	xacc\$	Predict(1)	S->ABc\$
ABc\$	xacc\$	Predict(2)	A->xaA
xaABc\$	xacc\$	match(x)	
aABc\$	acc\$	match(a)	
ABc\$	cc\$	Predict(4)	A->c
cBc\$	cc\$	<pre>match(c)</pre>	
Bc\$	c \$	Predict(6)	B->λ
c \$	c \$	<pre>match(c)</pre>	
\$	\$	Done!	

⁵³

Identifying LL(1) Grammar

- What we saw was an example of LL(1) Grammar
 - Scan input Left-to-right, produce Left-most derivation with 1 symbol look-ahead

Identifying LL(1) Grammar

- What we saw was an example of LL(1) Grammar
 - Scan input Left-to-right, produce Left-most derivation with 1 symbol look-ahead
- Not all Grammars are LL(1)
 - A Grammar is LL(1) iff for a production A -> α | β , where α and β are distinct:
 - 1. For no terminal a do both α and β derive strings beginning with a (i.e. no common prefix)
 - 2. At most one of α and β can derive an empty string
 - 3. If $\beta \stackrel{*}{\Rightarrow} \epsilon$, then α does not derive any string beginning with a terminal in Follow(A). If $\alpha \stackrel{*}{\Rightarrow} \epsilon$, then β does not derive any string beginning with a terminal in Follow(A)

Example (Left Factoring)

Consider

```
<stmt> → if <expr> then <stmt list> endif
<stmt> → if <expr> then <stmt list> else <stmt list> endif
```

- This is not LL(I) (why?)
- We can turn this in to

```
<stmt> → if <expr> then <stmt list> <if suffix> <if suffix> → endif <if suffix> → else <stmt list> endif
```

Example (Left Factoring)

Consider

```
<stmt> → if <expr> then <stmt list> endif
<stmt> → if <expr> then <stmt list> else <stmt list> endif
```

- This is not LL(1) (why?)
- We can turn this in to

```
<stmt> → if <expr> then <stmt list> <if suffix> <if suffix> → endif <if suffix> → else <stmt list> endif
```

Left Factoring

$$A \rightarrow \alpha \beta \mid \alpha \mu$$



 $A \rightarrow \alpha N$

 $N \rightarrow \beta$ $N \rightarrow \mu$

Left recursion

- Left recursion is a problem for LL(I) parsers
 - LHS is also the first symbol of the RHS
- Consider:

$$E \rightarrow E + T$$

• What would happen with the stack-based algorithm?

Left recursion

- Left recursion is a problem for LL(I) parsers
 - LHS is also the first symbol of the RHS
- Consider:

$$E \rightarrow E + T$$

• What would happen with the stack-based algorithm?

```
E
E + T
E + T + T
E + T + T + T
```

Eliminating Left Recursion

$$A \rightarrow A \alpha \mid \beta$$



A -> NT

 $N \rightarrow \beta$

 $T \rightarrow \alpha T$

 $T \rightarrow \lambda$

Eliminating Left Recursion

$$E \rightarrow E + T$$



E -> E1 Etail

E1 -> T

Etail -> + T Etail

Etail -> λ

LL(k) parsers

- Can look ahead more than one symbol at a time
 - k-symbol lookahead requires extending first and follow sets
 - 2-symbol lookahead can distinguish between more rules:

$$A \rightarrow ax \mid ay$$

- More lookahead leads to more powerful parsers
- What are the downsides?

Are all grammars LL(k)?

No! Consider the following grammar:

$$S \rightarrow E$$

 $E \rightarrow (E + E)$
 $E \rightarrow (E - E)$
 $E \rightarrow x$

- When parsing E, how do we know whether to use rule 2 or 3?
 - Potentially unbounded number of characters before the distinguishing '+' or '-' is found
 - No amount of lookahead will help!

LL(k)? - Example

```
string: ((x+x))$
Stack* Rem. Input
                                Action
          ((x+x))$
                         Predict(1) S->E
                         Predict(2) or Predict(3)?
                              X
           LL(1)
                 S
                              1
                   2,3
                              4
                 ((
                              )$
                                 (X
                     +(
             S
     LL(2)
             Ε
                 2,3
                                 4
```

1) $S \rightarrow E$

4) $E \rightarrow x$

2) E -> (E+E)

3) $E \rightarrow (E-E)$

In real languages?

- Consider the if-then-else problem
- if x then y else z
- Problem: else is optional
- if a then if b then c else d
 - Which if does the else belong to?
- This is analogous to a "bracket language": $[i]^j$ ($i \ge j$)

```
S \rightarrow [S C \\ S \rightarrow \lambda  [[] can be parsed: SS\(\lambda C \) or SSC\(\lambda \)
C \rightarrow \lambda (it's ambiguous!)
```

Solving the if-then-else problem

- The ambiguity exists at the language level. To fix, we need to define the semantics properly
 - "] matches nearest unmatched ["
 - This is the rule C uses for if-then-else
 - What if we try this?

```
S \rightarrow [S \\ S \rightarrow SI \\ SI \rightarrow [SI]
```

This grammar is still not LL(I) (or LL(k) for any k!)

Two possible fixes

- If there is an ambiguity, prioritize one production over another
 - e.g., if C is on the stack, always match "]" before matching "λ"

$$\begin{array}{ccc} S & \rightarrow [SC \\ S & \rightarrow \lambda \\ C & \rightarrow] \\ C & \rightarrow \lambda \end{array}$$

- Another option: change the language!
 - e.g., all if-statements need to be closed with an endif

```
S \rightarrow if S E

S \rightarrow other

E \rightarrow else S endif

E \rightarrow endif
```

Parsing if-then-else

- What if we don't want to change the language?
 - C does not require { } to delimit single-statement blocks
- To parse if-then-else, we need to be able to look ahead at the entire rhs of a production before deciding which production to use
 - In other words, we need to determine how many "]" to match before we start matching "["s
- LR parsers can do this!

Bottom-up Parsing

- More general than top-down parsing
- Used in most parser-generator tools
- Need not have left-factored grammars (i.e. can have left recursion)
- E.g. can work with the bracket language

Bottom-up Parsing

 Reduce a string to start symbol by reverse 'inverting' productions

Bottom-up Parsing

 Reduce a string to start symbol by reverse 'inverting' productions

```
id * id + id
```

```
E -> T + E
E -> T
T -> id * T
T -> id
```

```
id * <mark>id</mark> + id
id * <mark>T</mark> + id
```

```
id * id + id
id * T + id
T + id
```

```
id * id + id
id * T + id
T + id
T + T
```

```
id * id + id
id * T + id
T + id
T + T
T + E
```

```
id * id + id
id * T + id
T + id
T + T
T + E
E
```

```
E -> T + E
E -> T
T -> id * T
T -> id
```

```
id * id + id
id * T + id
T + id
T + T
T + E
```

```
E -> T + E
E -> T
T -> id * T
T -> id
```

 Reduce a string to start symbol by reverse 'inverting' productions

```
id * id + id
id * T + id
T + id
T + T
T + E
E
```

E -> T + E

E -> T

T -> id * T

T -> id

Right-most derivation

 Scan the input left-to-right and shift tokens – put them on the stack.

```
| id * id + id
id | * id + id
id * id + id
id * | id + id
id * id | + id
```

 Replace a set of symbols at the top of the stack that are RHS of a production. Put the LHS of the production on stack – Reduce

```
| id * id + id
id | * id + id
id * | id + id
id * | id + id
id * id | + id
```

Did not discuss when and why a particular production was chosen

```
id * id + id
id * T + id
```

i.e. why replace the id highlighted in input string?

LR Parsers

- Parser which does a Left-to-right, Right-most derivation
 - Rather than parse top-down, like LL parsers do, parse bottom-up, starting from leaves
- Basic idea: put tokens on a stack until an entire production is found
- Issues:
 - Recognizing the endpoint of a production
 - Finding the length of a production (RHS)
 - Finding the corresponding nonterminal (the LHS of the production)

Data structures

- At each state, given the next token,
 - A goto table defines the successor state
 - An action table defines whether to
 - shift put the next state and token on the stack
 - reduce an RHS is found; process the production
 - terminate parsing is complete

Simple example

I.
$$P \rightarrow S$$

2.
$$S \rightarrow x; S$$

3.
$$S \rightarrow e$$

			5	Symbo	ol		
		Х	;	е	Р	S	Action
	0	_		3		5	Shift
	_		2				Shift
State	2	_		3		4	Shift
State	3						Reduce 3
	4						Reduce 2
	5						Accept

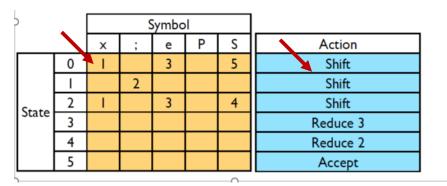
Parsing using an LR(0) parser

- Basic idea: parser keeps track, simultaneously, of all possible productions that could be matched given what it's seen so far.
 When it sees a full production, match it.
- Maintain a parse stack that tells you what state you're in
 - Start in state 0
- In each state, look up in action table whether to:
 - shift: consume a token off the input; look for next state in goto table; push next state onto stack
 - reduce: match a production; pop off as many symbols from state stack as seen in production; look up where to go according to non-terminal we just matched; push next state onto stack
 - accept: terminate parse

>	Symbol						
		Х	;	е	Р	S	Action
	0	\perp		3		5	Shift
[_		2				Shift
State	2	_		3		4	Shift
State	3						Reduce 3
	4						Reduce 2
	5						Accept

Step	Parse Stack	Rem. Input	Parser Action
1	0	x;x;e	?

Start with state 0



Step	Parse Stack	Rem. Input	Parser Action
1	0	<mark>x</mark> ;x;e	Shift(1)

Symbol					ol		
		х	;	е	Р	S	Action
	0			3		5	Shift
	_		2				Shift
State	2	_		3		4	Shift
State	3						Reduce 3
	4						Reduce 2
	5						Accept

Step	Parse Stack	Rem. Input	Parser Action
1	0	x;x;e	Shift(1)
2	0 1	<mark>;</mark> x;e	?

Symbol							
		Х	;	е	Р	S	Action
	0	6		3		5	Shift
[_		2				Shift
State	2	_		3		4	Shift
State	3						Reduce 3
[4						Reduce 2
	5						Accept

Step	Parse Stack	Rem. Input	Parser Action
1	0	x;x;e	Shift(1)
2	0 1	<mark>;</mark> x;e	Shift(2)

>			5				
			;	е	Р	S	Action
	0	_		3		5	Shift
	_		2				Shift
State	2	_		3		4	Shift
State	3						Reduce 3
	4						Reduce 2
	5						Accept

Step	Parse Stack	Rem. Input	Parser Action
1	0	x;x;e	Shift(1)
2	0 1	;x;e	Shift(2)
3	0 1 <mark>2</mark>	<mark>x</mark> ;e	?

>			5				
		Х	;	е	Р	S	Action
	0	_		3		5	Shift
	H		2				Shift
State	2	_		3		4	Shift
State	3						Reduce 3
	4						Reduce 2
	5						Accept

Step	Parse Stack	Rem. Input	Parser Action
1	0	x;x;e	Shift(1)
2	0 1	;x;e	Shift(2)
3	0 1 <mark>2</mark>	<mark>x</mark> ;e	Shift(1)

5			5				
		Х	;	е	Р	S	Action
	0	_		3		5	Shift
			2				Shift
State	2	_		3		4	Shift
State	3						Reduce 3
	4						Reduce 2
	5						Accept

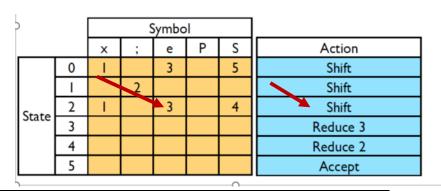
Step	Parse Stack	Rem. Input	Parser Action
1	0	x;x;e	Shift(1)
2	0 1	;x;e	Shift(2)
3	012	x;e	Shift(1)
4	0 1 2 <mark>1</mark>	<mark>;</mark> e	?

			5	Symbo	ı		
		Х	;	е	Р	S	Action
	0	6		3		5	Shift
	_		2				Shift
State	2	_		3		4	Shift
State	3						Reduce 3
[4						Reduce 2
	5						Accept

Step	Parse Stack	Rem. Input	Parser Action
1	0	x;x;e	Shift(1)
2	0 1	;x;e	Shift(2)
3	0 1 2	x;e	Shift(1)
4	0 1 2 <mark>1</mark>	<mark>;</mark> e	Shift(2)

>			5				
		х	;	е	Р	S	Action
	0			3		5	Shift
	_		2				Shift
State	2	_		3		4	Shift
State	3						Reduce 3
	4						Reduce 2
	5						Accept

Step	Parse Stack	Rem. Input	Parser Action
1	0	x;x;e	Shift(1)
2	0 1	;x;e	Shift(2)
3	0 1 2	x;e	Shift(1)
4	0121	;e	Shift(2)
5	0 1 2 1 <mark>2</mark>	e	?



Step	Parse Stack	Rem. Input	Parser Action
1	0	x;x;e	Shift(1)
2	0 1	;x;e	Shift(2)
3	0 1 2	x;e	Shift(1)
4	0 1 2 1	;e	Shift(2)
5	0 1 2 1 <mark>2</mark>	e	Shift(3)

5			5				
		Х	;	е	Р	S	Action
	0	_		3		5	Shift
			2				Shift
State	2	_		3		4	Shift
State	3						Reduce 3
	4						Reduce 2
	5						Accept

Step	Parse Stack	Rem. Input	Parser Action
1	0	x;x;e	Shift(1)
2	0 1	;x;e	Shift(2)
3	0 1 2	x;e	Shift(1)
4	0 1 2 1	;e	Shift(2)
5	01212	е	Shift(3)
6	01212 <mark>3</mark>		?

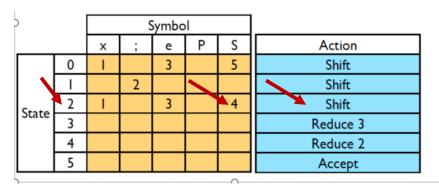
>			5	Symbo	ı		
		Х	;	е	Р	S	Action
	0	_		3		5	Shift
	-		2				Shift
State	2	_		3		4	Shift
State	3						Reduce 3
	4						Reduce 2
	5						Accept

Step	Parse Stack	Rem. Input	Parser Action
1	0	x;x;e	Shift(1)
2	0 1	;x;e	Shift(2)
3	012	x;e	Shift(1)
4	0121	;e	Shift(2)
5	01212	е	Shift(3)
6	0 1 2 1 2 <mark>3</mark>		Reduce 3

}			5	Symbo	ol		
		Х	;	е	Р	S	Action
	0	_		3		5	Shift
	Ι		2				Shift
State	2	_		3		4	Shift
State	3						Reduce 3
	4						Reduce 2
	5						Accept

Step	Parse Stack	Rem. Input	Parser Action
1	0	x;x;e	Shift(1)
2	0 1	;x;e	Shift(2)
3	012	x;e	Shift(1)
4	0121	;e	Shift(2)
5	01212	е	Shift(3)
6	012123		Reduce 3
7	0 1 2 1 <mark>2</mark>		

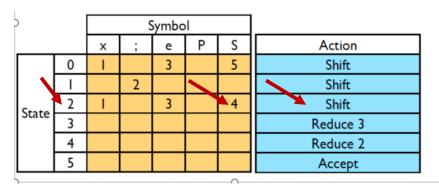
Look at rule III and pop 1 symbol of the stack because RHS of rule III has just 1 symbol



100

Step	Parse Stack	Rem. Input	Parser Action
1	0	x;x;e	Shift(1)
2	0 1	;x;e	Shift(2)
3	012	x;e	Shift(1)
4	0121	;e	Shift(2)
5	01212	е	Shift(3)
6	012123		Reduce 3
7	0 1 2 1 <mark>2</mark>		

Now stack top has symbol 2 and LHS of rule III has S (imagine you saw S at input).
 Consult goto and action table.



101

Step	Parse Stack	Rem. Input	Parser Action
1	0	x;x;e	Shift(1)
2	0 1	;x;e	Shift(2)
3	012	x;e	Shift(1)
4	0121	;e	Shift(2)
5	01212	е	Shift(3)
6	012123		Reduce 3 (shift(4))
7	012124		

Now stack top has symbol 2 and LHS of rule III has S (imagine you saw S at input).
 Consult goto and action table. Shift(4)

Symbol						
	Х	;	е	Р	S	Action
0	\perp		3		5	Shift
Ι		2				Shift
2	\perp		3		4	Shift
3						Reduce 3
4						Reduce 2
5						Accept
	0 1 2 3 4 5				,	, , , ,

Step	Parse Stack	Rem. Input	Parser Action
1	0	x;x;e	Shift(1)
2	0 1	;x;e	Shift(2)
3	012	x;e	Shift(1)
4	0121	;e	Shift(2)
5	01212	е	Shift(3)
6	012123		Reduce 3 (shift(4))
7	01212 <mark>4</mark>		?

Now stack top has symbol 2 and LHS of rule III has S (imagine you saw S at input).
 Consult goto and action table. Shift(4)

>	Symbol						
		Х	;	е	Р	S	Action
	0	_		3		5	Shift
	-		2				Shift
State	2	_		3		4	Shift
	3						Reduce 3
	4						Reduce 2
	5						Accept

Step	Parse Stack	Rem. Input	Parser Action
1	0	x;x;e	Shift(1)
2	0 1	;x;e	Shift(2)
3	0 1 2	x;e	Shift(1)
4	0 1 2 1	;e	Shift(2)
5	01212	е	Shift(3)
6	012123		Reduce 3 (shift(4))
7	012124		Reduce 2

Symbol						
	Х	;	е	Р	S	Action
0	_		3		5	Shift
_		2				Shift
2	_		3		4	Shift
3						Reduce 3
4						Reduce 2
5						Accept
	0 1 2 3 4 5		x ;	x ; e 0 1 3 1 2	x ; e P 0 I 3 1 2	x ; e P S 0 1 3 5 1 2

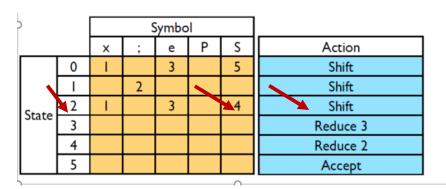
Step	Parse Stack	Rem. Input	Parser Action
1	0	x;x;e	Shift(1)
2	0 1	;x;e	Shift(2)
3	0 1 2	x;e	Shift(1)
4	0 1 2 1	;e	Shift(2)
5	01212	е	Shift(3)
6	012123		Reduce 3 (shift(4))
7	012124		Reduce 2
8	012		

Look at rule II and pop 3 symbols of the stack because RHS of rule II has 3 symbols

>			5	Symbo	ol		
		х	;	е	Р	S	Action
	0			3		5	Shift
	_		2		1		Shift
State	2	_		3		1 4	Shift
State	3						Reduce 3
	4						Reduce 2
	5						Accept

Step	Parse Stack	Rem. Input	Parser Action
1	0	x;x;e	Shift(1)
2	0 1	;x;e	Shift(2)
3	0 1 2	x;e	Shift(1)
4	0121	;e	Shift(2)
5	01212	е	Shift(3)
6	012123		Reduce 3 (shift(4))
7	012124		Reduce 2
8	0 1 <mark>2</mark>		

Now stack top has symbol 2 and LHS of rule II has S (imagine you saw S at input). Consult
goto and action table.



Step	Parse Stack	Rem. Input	Parser Action
1	0	x;x;e	Shift(1)
2	0 1	;x;e	Shift(2)
3	0 1 2	x;e	Shift(1)
4	0 1 2 1	;e	Shift(2)
5	01212	е	Shift(3)
6	012123		Reduce 3 (shift(4))
7	012124		Reduce 2 (shift(4))
8	0 1 2 <mark>4</mark>		

• Now stack top has symbol 2 and LHS of rule II has S (imagine you saw S at input). Consult goto and action table. Shift(4)

5		Symbol					
		Х	;	е	Р	S	Action
	0	_		3		5	Shift
State	-		2				Shift
	2	_		3		4	Shift
	3						Reduce 3
	4						Reduce 2
	5						Accept

Step	Parse Stack	Rem. Input	Parser Action
1	0	x;x;e	Shift(1)
2	0 1	;x;e	Shift(2)
3	012	x;e	Shift(1)
4	0121	;e	Shift(2)
5	01212	е	Shift(3)
6	012123		Reduce 3 (shift(4))
7	012124		Reduce 2 (shift(4))
8	0124		?

x;x;e

7		Symbol					l
		х	;	е	Р	S	Action
	0	_		3		5	Shift
	_		2				Shift
State	2	1		3		4	Shift
State	3						Reduce 3
	4						Reduce 2
	5						Accept

Step	Parse Stack	Rem. Input	Parser Action
1	0	x;x;e	Shift(1)
2	0 1	;x;e	Shift(2)
3	0 1 2	x;e	Shift(1)
4	0121	;e	Shift(2)
5	01212	е	Shift(3)
6	012123		Reduce 3 (shift(4))
7	012124		Reduce 2 (shift(4))
8	0124		Reduce 2

}	Symbol						
		х	;	е	Р	S	Action
	0	_		3		5	Shift
	Ι		2				Shift
Stata	2	_		3		4	Shift
State	3						Reduce 3
	4						Reduce 2
	5						Accept

Step	Parse Stack	Rem. Input	Parser Action
1	0	x;x;e	Shift(1)
2	0 1	;x;e	Shift(2)
3	0 1 2	x;e	Shift(1)
4	0121	;e	Shift(2)
5	01212	е	Shift(3)
6	012123		Reduce 3 (shift(4))
7	012124		Reduce 2 (shift(4))
8	0124		Reduce 2
9	0		

-	Symbol						
		Х	;	е	Р	S	Action
	0			3		1 5	Shift
			2				Shift
State	2	_		3		4	Shift
State	3						Reduce 3
	4						Reduce 2
	5						Accept

Step	Parse Stack	Rem. Input	Parser Action
1	0	x;x;e	Shift(1)
2	0 1	;x;e	Shift(2)
3	0 1 2	x;e	Shift(1)
4	0 1 2 1	;e	Shift(2)
5	01212	е	Shift(3)
6	012123		Reduce 3 (shift(4))
7	012124		Reduce 2 (shift(4))
8	0 1 2 4		Reduce 2 (shift(5))
9	0 <mark>5</mark>		

>			Symbol				
		Х	;	е	Р	S	Action
	0	_		3		5	Shift
			2				Shift
State	2	_		3		4	Shift
State	3						Reduce 3
	4						Reduce 2
	5						Accept

Step	Parse Stack	Rem. Input	Parser Action
1	0	x;x;e	Shift(1)
2	0 1	;x;e	Shift(2)
3	0 1 2	x;e	Shift(1)
4	0121	;e	Shift(2)
5	01212	е	Shift(3)
6	012123		Reduce 3 (shift(4))
7	012124		Reduce 2 (shift(4))
8	0124		Reduce 2 (shift(5))
9	0 <mark>5</mark>		?

Input string
x;x;e

5	Symbol						
		х	;	е	Р	S	Action
	0	_		3		5	Shift
	П		2				Shift
State	2	_		3		4	Shift
State	3						Reduce 3
	4						Reduce 2
	5						Accept

Step	Parse Stack	Rem. Input	Parser Action
1	0	x;x;e	Shift(1)
2	0 1	;x;e	Shift(2)
3	0 1 2	x;e	Shift(1)
4	0 1 2 1	;e	Shift(2)
5	01212	е	Shift(3)
6	012123		Reduce 3 (shift(4))
7	012124		Reduce 2 (shift(4))
8	0 1 2 4		Reduce 2 (shift(5))
9	0 <mark>5</mark>		Accept

Step	Parser Action
1	Shift(1)
2	Shift(2)
3	Shift(1)
4	Shift(2)
5	Shift(3)
6	Reduce 3 (shift(4))
7	Reduce 2 (shift(4))
8	Reduce 2 (shift(5))
9	Accept

Step	Parser Action
1	Shift(1)
2	Shift(2)
3	Shift(1)
4	Shift(2)
5	Shift(3)
6	Reduce 3 (shift(4))
7	Reduce 2 (shift(4))
8	Reduce 2 (shift(5))
9	Accept

Step	Parser Action
1	Shift(1)
2	Shift(2)
3	Shift(1)
4	Shift(2)
5	Shift(3)
6	Reduce 3 (shift(4))
7	Reduce 2 (shift(4))
8	Reduce 2 (shift(5))
9	Accept

x ; x ; e

Step	Parser Action
1	Shift(1)
2	Shift(2)
3	Shift(1)
4	Shift(2)
5	Shift(3)
6	Reduce 3 (shift(4))
7	Reduce 2 (shift(4))
8	Reduce 2 (shift(5))
9	Accept

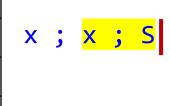
Step	Parser Action
1	Shift(1)
2	Shift(2)
3	Shift(1)
4	Shift(2)
5	Shift(3)
6	Reduce 3 (shift(4))
7	Reduce 2 (shift(4))
8	Reduce 2 (shift(5))
9	Accept

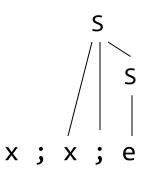
Step	Parser Action
1	Shift(1)
2	Shift(2)
3	Shift(1)
4	Shift(2)
5	Shift(3)
6	Reduce 3 (shift(4))
7	Reduce 2 (shift(4))
8	Reduce 2 (shift(5))
9	Accept

x ; x ; e

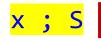
Step	Parser Action
1	Shift(1)
2	Shift(2)
3	Shift(1)
4	Shift(2)
5	Shift(3)
6	Reduce 3 (shift(4))
7	Reduce 2 (shift(4))
8	Reduce 2 (shift(5))
9	Accept

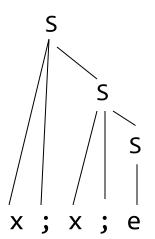
Step	Parser Action
1	Shift(1)
2	Shift(2)
3	Shift(1)
4	Shift(2)
5	Shift(3)
6	Reduce 3 (shift(4))
7	Reduce 2 (shift(4))
8	Reduce 2 (shift(5))
9	Accept



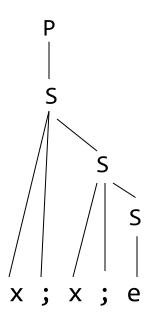


Step	Parser Action
1	Shift(1)
2	Shift(2)
3	Shift(1)
4	Shift(2)
5	Shift(3)
6	Reduce 3 (shift(4))
7	Reduce 2 (shift(4))
8	Reduce 2 (shift(5))
9	Accept





Step	Parser Action
1	Shift(1)
2	Shift(2)
3	Shift(1)
4	Shift(2)
5	Shift(3)
6	Reduce 3 (shift(4))
7	Reduce 2 (shift(4))
8	Reduce 2 (shift(5))
9	Accept



Shift-Reduce Parsing

The LR parsing seen previously is an example of shift-reduce parsing

- When do we shift and when do we reduce?
 - How do we construct goto and action tables?

Concept: configuration / item

Configuration or item has a form:

$$A \rightarrow X_1 \dots X_i \bullet X_{i+1} \dots X_j$$

- Dot can appear anywhere
- Represents a production part of which has been matched (what is to the left of Dot)
- ➤ LR parsers keep track of multiple (all) productions that can be potentially matched
 - ➤ We need a configuration set

Concept: configuration / item

> E.g. configuration set

```
stmt -> ID • := expr
stmt -> ID • : stmt
stmt -> ID •
```

Corresponding to productions:

```
stmt -> ID := expr
stmt -> ID : stmt
stmt -> ID
```

- Dot at the extreme left of RHS of a production denotes that production is predicted
- Dot at the extreme right of RHS of a production denotes that production is recognized
- ➤ if <u>Dot precedes a Non-Terminal</u> in a configuration set, more configurations need to be added to the set

- > For each configuration in the configuration set,
 - A -> $\alpha \cdot B\gamma$, where B is a non-terminal,
- 1 add configurations of the form:
 - $B \rightarrow \delta$
- if the addition introduces a configuration with Dot behind a new non-Terminal N, add all configurations having the form N -> ϵ

Repeat 2 when another new non-terminal is introduced and so on..

```
➤ E.g. closure {S ->• E$}

Non-terminal
S ->• E$
```

Grammar S -> E\$ E -> E+T | T T -> ID | (E)

```
➤ E.g. closure {S ->• E$}

Non-terminal

S ->• E$

E ->• E+T
```

```
➤ E.g. closure {S ->• E$}

Non-terminal
S ->• E$
E ->• E+T
E ->• T
```

```
Fig. closure \{S \rightarrow E\}
S \rightarrow E
E \rightarrow E+T \mid T
T \rightarrow ID \mid (E)
S \rightarrow E+T
E \rightarrow E+T
New Non-terminal
```

```
F.g. closure {S → E$}

S → E$

E → E+T | T

T → ID | (E)

S → E$

E → E+T

T → ID
```

```
Grammar

E.g. closure {S ->• E$}

S -> E$

E -> E+T | T

T -> ID | (E)

S ->• E$

E ->• E+T

T ->• ID

T ->• (E)
```

➤ E.g. closure {S ->• E\$}

Grammar

Concept: successor

E.g. successor ({S -> E\$}, E)

$$\begin{cases}
S \rightarrow \bullet E \\
E \rightarrow \bullet E + T \\
E \rightarrow \bullet T \\
T \rightarrow \bullet ID \\
T \rightarrow \bullet (E)
\end{cases}$$

$$E \begin{cases}
S \rightarrow E \bullet S \\
E \rightarrow E \bullet + T
\end{cases}$$

Grammar S -> E\$ E -> E+T | T

 $T \rightarrow ID \mid (E)$

- Consider all symbols that are to the <u>immediate right of Dot</u> and compute respective successors
 - You must compute closure of successor before finalizing items in successor

Concept: CFSM

- > Each configuration set becomes a state
- ➤ The symbol used as input for computing the successor becomes the transition
- Configuration-set finite state machine (CFSM)
 - The state diagram obtained after computing the chain of all successors (for all symbols) starting from the configuration involving the first production

Start with a configuration for the first production

<u>Grammar</u>

$$S->x;S$$

Compute closure

<u>Grammar</u>

$$S \rightarrow x;S$$

Add item

P->• S

 $S \rightarrow x;S$

Grammar

P->S

S->x;S

S->e

Add item

P->• S

 $S \rightarrow x;S$

S->• e

Grammar

P->S

S->x;S

S->e

No new non-terminal before Dot. This becomes a state in CFSM

P->• S

state 0

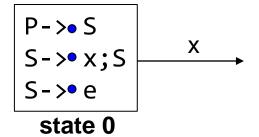
<u>Grammar</u>

P->S

S->x;S

S->e

Compute successor (of state 0) under symbol x



Grammar

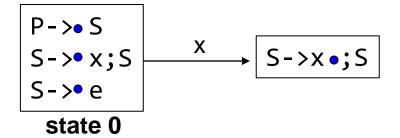
P->S

S->x;S

S->e

Consider items (in state 0), where x is to the immediate right of Dot. Advance Dot by one symbol.

Compute successor (of state 0) under symbol x



Grammar

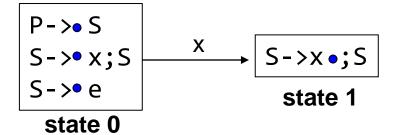
P->S

 $S \rightarrow x;S$

S->e

Consider items (in state 0), where x is to the immediate right of Dot. Advance Dot by one symbol.

Compute successor (of state 0) under symbol x



<u>Grammar</u>

P->S

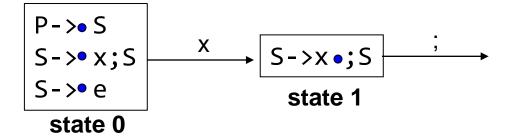
 $S \rightarrow x; S$

S->e

Consider items (in state 0), where x is to the immediate right of Dot. Advance Dot by one symbol.

No non-terminals immediately after Dot in the successor. So, no configurations get added. Successor becomes another state in CFSM.

Compute successor (of state 1) under symbol;



<u>Grammar</u>

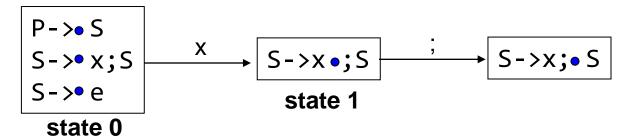
P->S

 $S \rightarrow x;S$

S->e

Consider items (in state 1), where ; is to the immediate right of Dot. Advance Dot by one symbol.

Compute successor (of state 1) under symbol;



Grammar

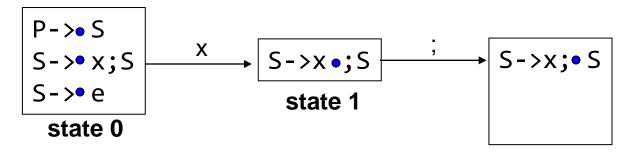
P->S

 $S \rightarrow x; S$

S->e

Consider items (in state 1), where ; is to the immediate right of Dot. Advance Dot by one symbol.

Compute successor (of state 1) under symbol;



<u>Grammar</u>

P->S

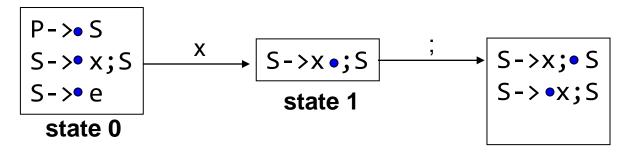
 $S \rightarrow x;S$

S->e

Consider items (in state 1), where ; is to the immediate right of Dot. Advance Dot by one symbol.

There is a non-terminal immediately after Dot in the successor of state 1. So, add configurations.

Compute successor (of state 1) under symbol;



Grammar

P->S

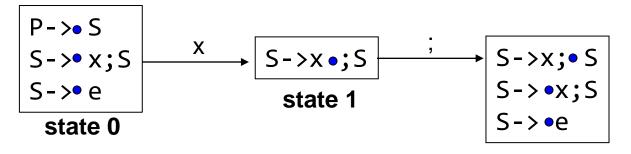
S->x;S

S->e

Consider items (in state 1), where ; is to the immediate right of Dot. Advance Dot by one symbol.

There is a non-terminal immediately after Dot in the successor of state 1. So, add configurations.

Compute successor (of state 1) under symbol;



<u>Grammar</u>

P->S

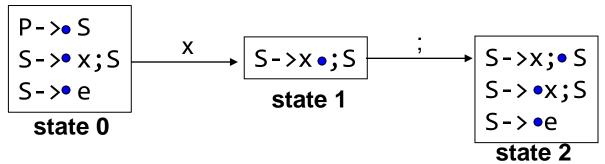
 $S \rightarrow x; S$

S->e

Consider items (in state 1), where ; is to the immediate right of Dot. Advance Dot by one symbol.

There is a non-terminal immediately after Dot in the successor of state 1. So, add configurations.

Compute successor (of state 1) under symbol;



<u>Grammar</u>

P->S

S->x;S

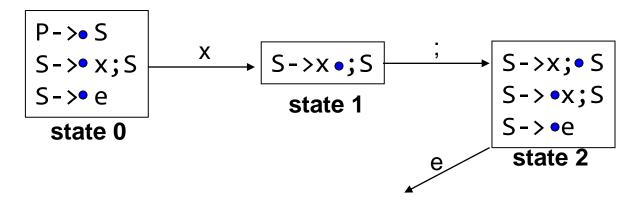
S->e

Consider items (in state 1), where ; is to the immediate right of Dot. Advance Dot by one symbol.

There is a non-terminal immediately after Dot in the successor of state 1. So, add configurations. No more items to be added.

Becomes another state in CFSM.

Compute successor (of state 2) under symbol e



<u>Grammar</u>

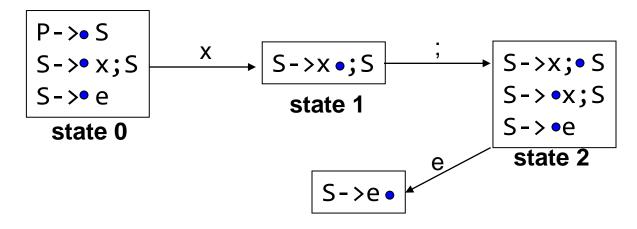
P->S

 $S \rightarrow x;S$

S->e

Consider items (in state 2), where e is to the immediate right of Dot. Advance Dot by one symbol.

Compute successor (of state 2) under symbol e



<u>Grammar</u>

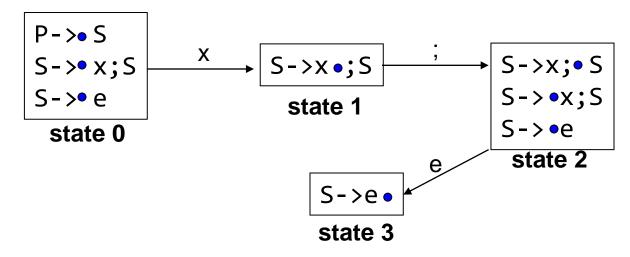
P->S

 $S \rightarrow x;S$

S->e

Consider items (in state 2), where e is to the immediate right of Dot. Advance Dot by one symbol.

Compute successor (of state 2) under symbol e



<u>Grammar</u>

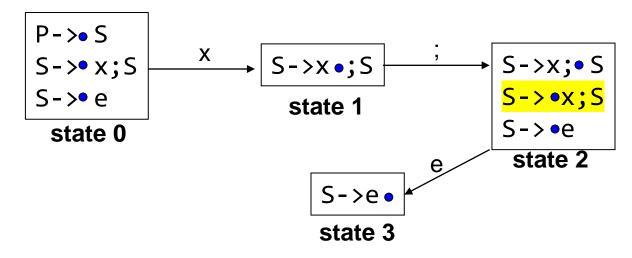
P->S

S->x;S

S->e

Consider items (in state 2), where e is to the immediate right of Dot. Advance Dot by one symbol. No more items to be added. Becomes another state in CFSM.

Compute successor (of state 2) under symbol x



<u>Grammar</u>

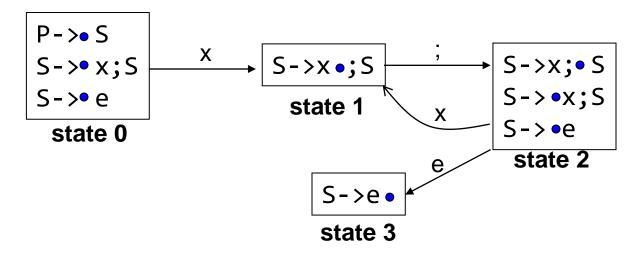
P->S

 $S \rightarrow x; S$

S->e

Consider items (in state 2), where x is to the immediate right of Dot. Advance Dot by one symbol.

Compute successor (of state 2) under symbol x



<u>Grammar</u>

P->S

 $S \rightarrow x;S$

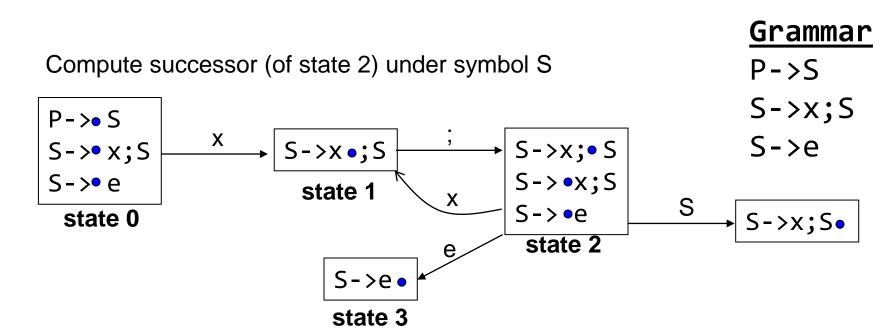
S->e

Consider items (in state 2), where x is to the immediate right of Dot. Advance Dot by one symbol.

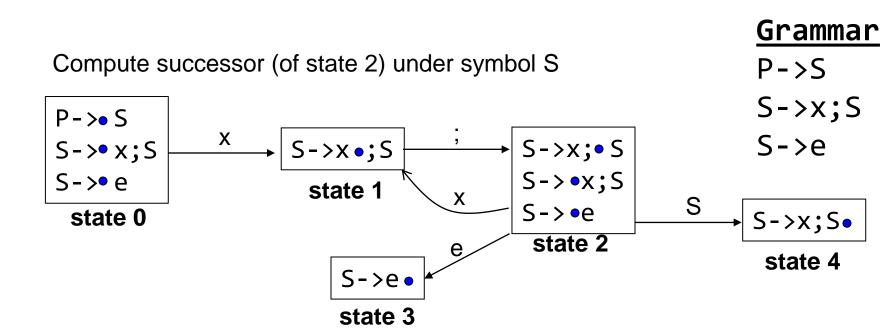
Compute successor (of state 2) under symbol S $P \rightarrow S$ $S \rightarrow x; S$

Consider items (in state 2), where S is to the immediate right of Dot. Advance Dot by one symbol.

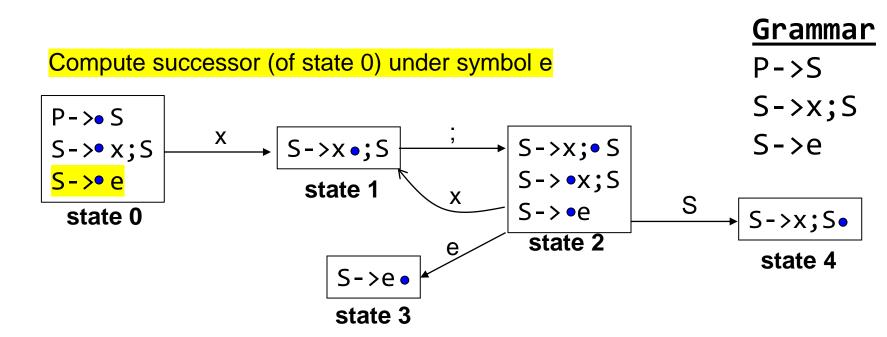
state 3



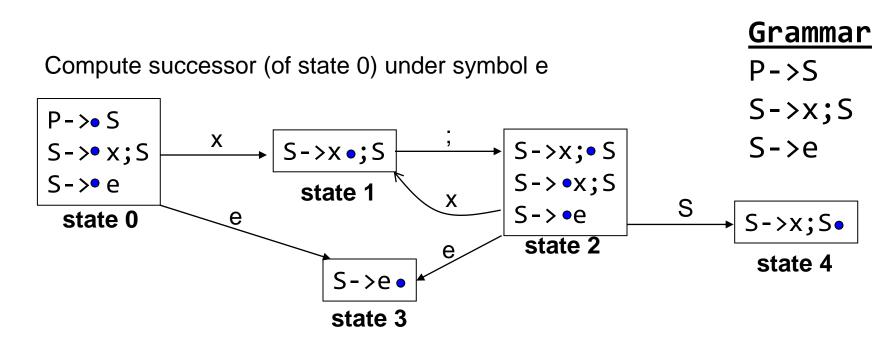
Consider items (in state 2), where S is to the immediate right of Dot. Advance Dot by one symbol.



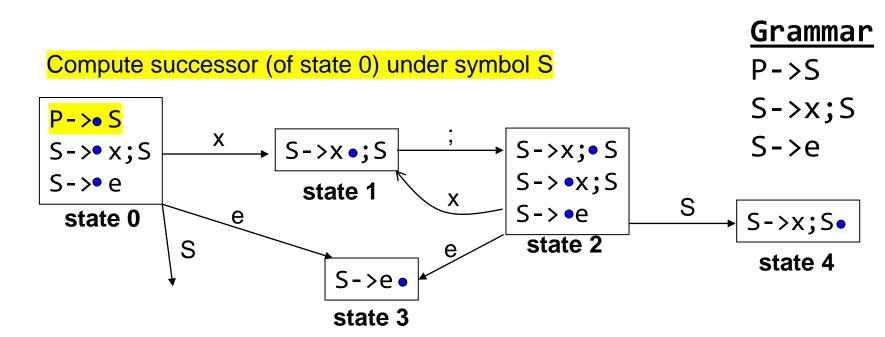
Consider items (in state 2), where S is to the immediate right of Dot. Advance Dot by one symbol. No more items to be added. Becomes another state in CFSM.



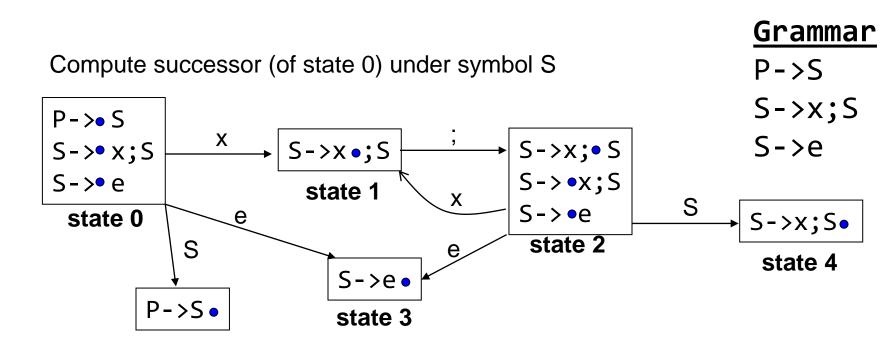
Consider items (in state 0), where e is to the immediate right of Dot. Advance Dot by one symbol.



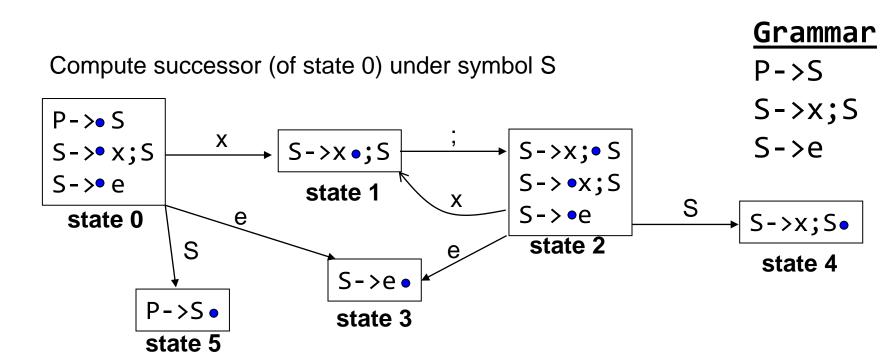
Consider items (in state 0), where e is to the immediate right of Dot. Advance Dot by one symbol.



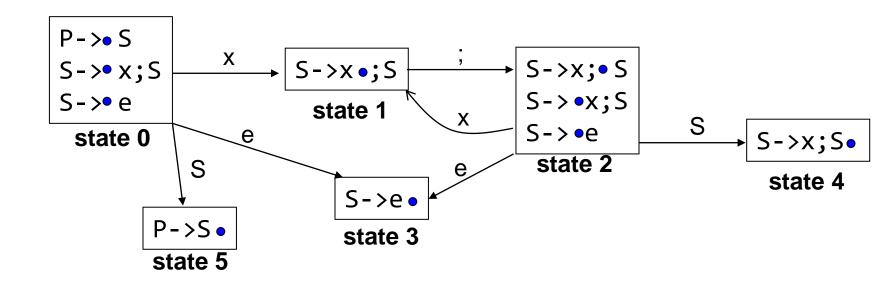
Consider items (in state 0), where S is to the immediate right of Dot. Advance Dot by one symbol.

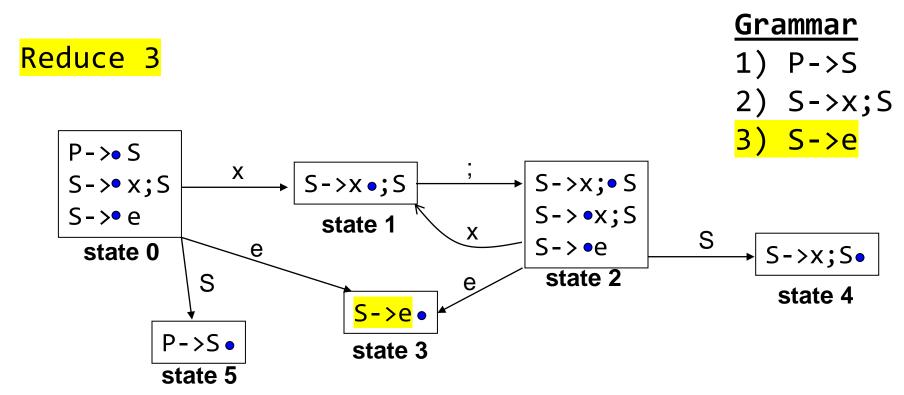


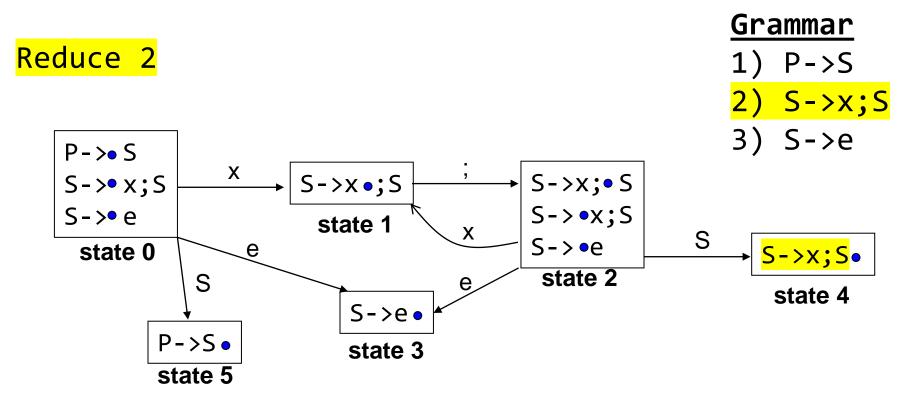
Consider items (in state 0), where S is to the immediate right of Dot. Advance Dot by one symbol.

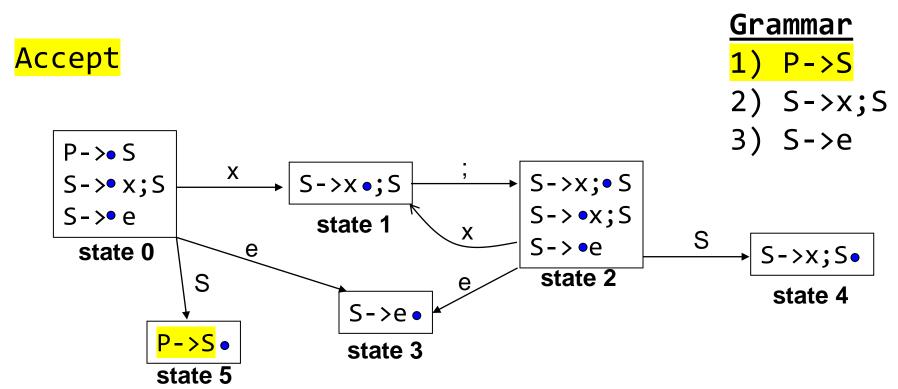


Consider items (in state 0), where S is to the immediate right of Dot. Advance Dot by one symbol. Cannot expand CFSM anymore.

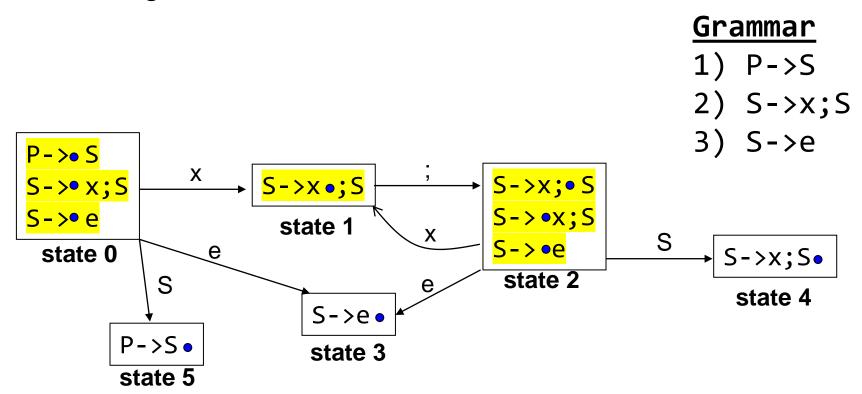








Remaining states become shift states



Conflicts

 What happens when a state has Dot at the extreme right for one item and in the middle for other items?

Shift-reduce conflict

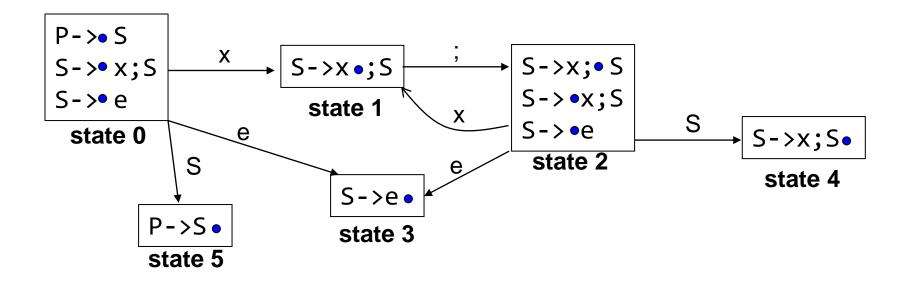
Parser is unable to decide between shifting and reducing

When Dot is at the extreme right for more than one items?

Reduce-Reduce conflict

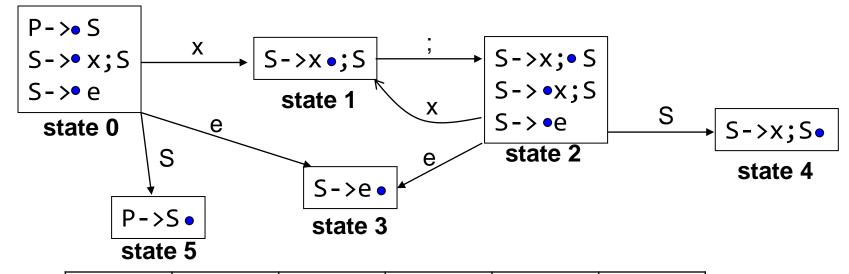
Parser is unable to decide between which productions to choose for reducing

Example: goto table



- construct transition table from CFSM.
 - Number of rows = number of states
 - Number of columns = number of symbols

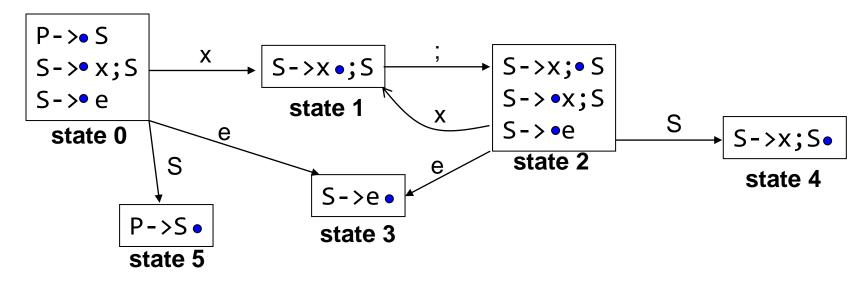
Example: goto table



state	x	;	е	Р	S
0	1		3		5
1		2			
2	1		3		4
3					
4					
5					

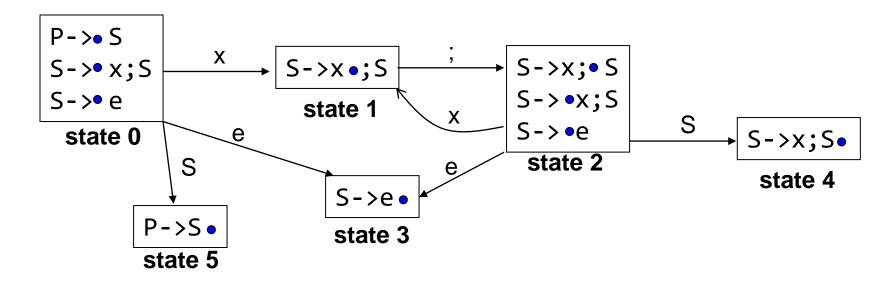
170

Example: action table



state	X	
0	Shift	
1	Shift	
2	Shift	
3	Reduce 3	
4	Reduce 2	
5	Accept	

Example: action table



		Symbol					
		х	;	е	Р	S	Action
	0	_		3		5	Shift
[_		2				Shift
State	2	_		3		4	Shift
State	3						Reduce 3
	4						Reduce 2
	5						Accept

Example

- Example of LR(0) parsing
 - No lookahead involved
 - Operate based on the parse stack state and with goto and action tables

LR(k) parsers

- LR(0) parsers
 - No lookahead
 - Predict which action to take by looking only at the symbols currently on the stack
- LR(k) parsers
 - Can look ahead k symbols
 - Most powerful class of deterministic bottom-up parsers
 - LR(I) and variants are the most common parsers

Top-down vs. Bottom-up parsers

- Top-down parsers expand the parse tree in pre-order
 - Identify parent nodes before the children
- Bottom-up parsers expand the parse tree in post-order
 - Identify children before the parents
- Notation:
 - LL(I):Top-down derivation with I symbol lookahead
 - LL(k):Top-down derivation with k symbols lookahead
 - LR(I): Bottom-up derivation with I symbol lookahead

Suggested Reading

- Alfred V. Aho, Monica S. Lam, Ravi Sethi and Jeffrey D.Ullman: Compilers: Principles, Techniques, and Tools, 2/E, AddisonWesley 2007
 - Chapter 2 (2.4), Chapter 4
- Fisher and LeBlanc: Crafting a Compiler with C
 - Chapter 4, Chapter 5, and Chapter 6