

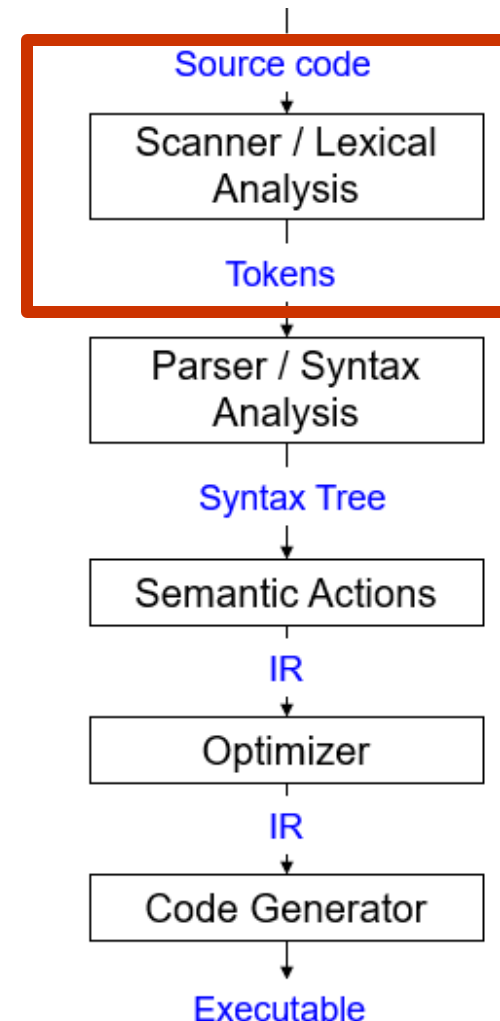
CS323: Compilers

Spring 2023

Week 3: Scanners (conclusion), Parsers

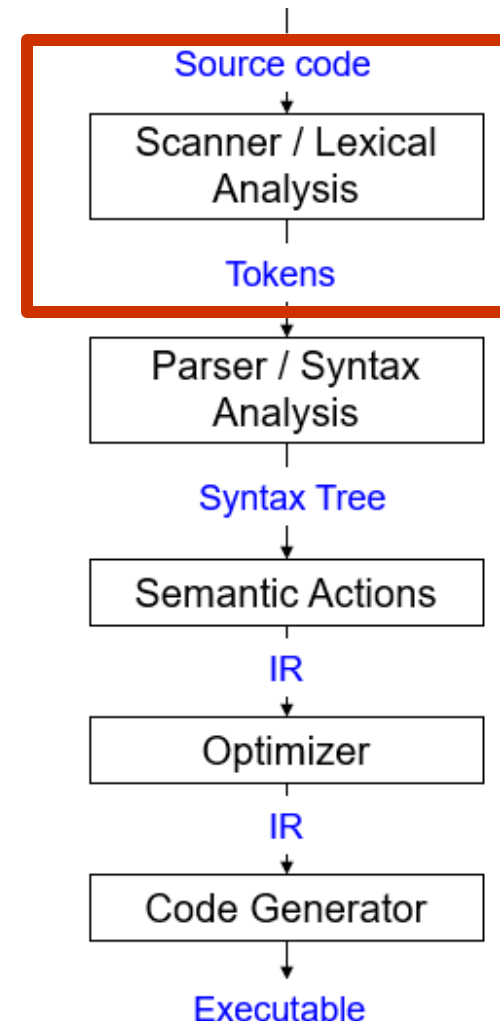
Scanners (Summary)

- Also called *Lexers / Lexical Analyzers*
- Input: stream of letters (program text / source code), Output: sequence / list of *tokens*
- Token: a pair <category/class, value>
 - Category defines a string *pattern*
 - Value also called *lexeme*
 - Value is a *prefix* (and hence, is a substring)
 - Value matches on of the patterns that category defines
- Scan *left-to-right* in program text, *look-ahead* to identify tokens.
 - Look-ahead buffer size determined by language design



Scanners (Summary)

- *Regular expressions* are used to formally define the patterns specified by token classes.
 - Some customization done while defining regular expressions: 1) Match the longest substring possible 2) Handle errors
- Tools such as Flex and ANTLR convert regular expressions to code. The code is your scanner implementation
 - The implementation typically converts regular expressions to *Finite Automata* (special kind of state diagram)
 - Automata are coded using efficient algorithms (E.g. Table-lookup method)
 - Efficient algorithms exist for substring matching (requiring single-pass over input program text)
 - Aho-Corasic, Knuth-Morris-Pratt (KMP)



Parsers - Overview

- Also called syntax analyzers
- Determine two things:
 1. Is a program syntactically valid?
(Analogy) is an English language sentence grammatically correct?
 2. What is the structure of programming language constructs? E.g. does the sequence*

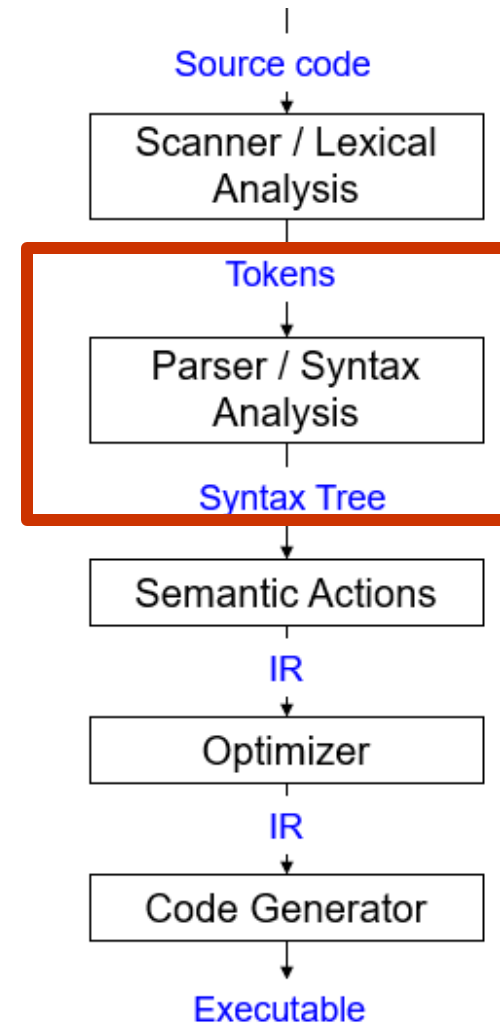
IF, ID(a), OP(<), ID(b), {, ID(a),
ASSIGN, LIT(5), }}

refer to an if statement?

(Analogy) diagramming English sentences

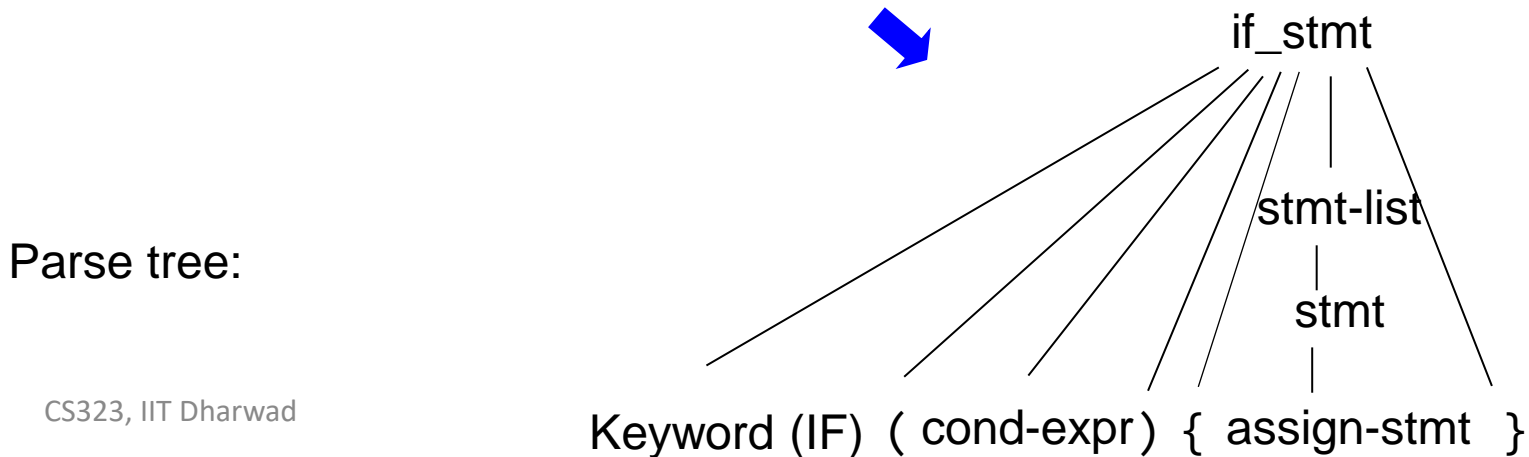
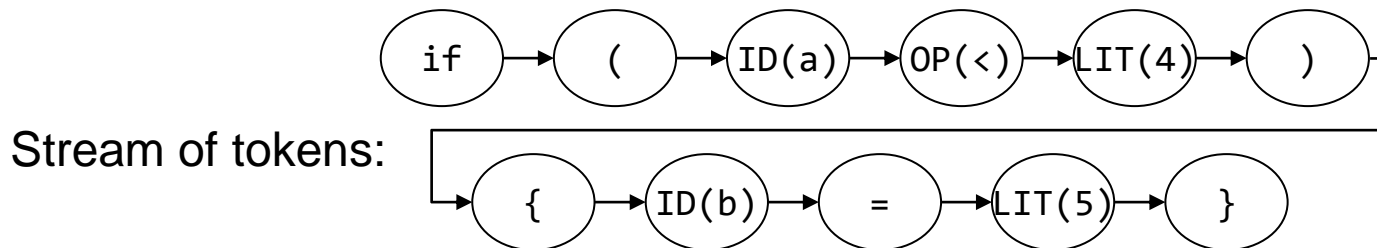
* Corresponding program text:

```
if (a < 4) {  
    b = 5  
}
```



Parsers - Overview

- Input: stream of tokens
- Output: Parse tree
 - sometimes implicit



Parsers – what do we need to know?

1. How do we define language constructs?
 - Context-free grammars
2. How do we determine: 1) valid strings in the language? 2) structure of program?
 - LL Parsers, LR Parsers
3. How do we write Parsers?
 - E.g. use a parser generator tool such as Bison

Languages

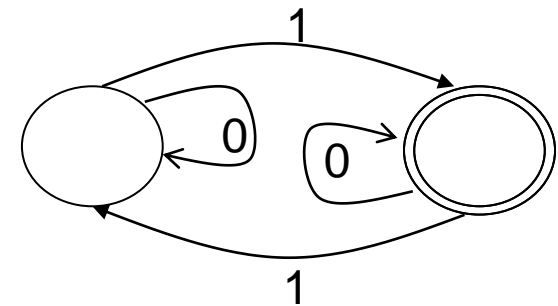
- A language is (possibly infinite) set of strings
- Regular expressions specify *regular languages*. However, regular languages are *weak formal languages* to describe the features of a practical programming language.

What set of strings does this FA accept?

The FA shown accepts all string with *odd number of 1s*.

What is the regular expression for the FA?

$(0^*10^*)(0^*10^*)^*$



Regular expressions can describe strings specifying *parity*:

$\{ \text{ mod } k \mid k = \# \text{ states in FA} \}$

weakness: regular expressions can't describe a string of the form: $\{ (\text{ }^i \text{ })^i \mid i \geq 1 \}$

Regular Languages

- Regular expressions can't describe a string of the form:

$$\{ ({}^i)^i \mid i \geq 1 \}$$

E.g. Parenthesized expressions

`((2+3)*5)`

Programming language syntax is i.e. recursive

`(((int x;)))`

Nested structures:

IF
 IF
 IF
 FI
 FI
 FI
FI

Context Free Grammar (CFG)

- Natural notation for describing recursive structure definitions. Hence, suitable for specifying language constructs.
- Consist of:
 - A set of *Terminals* (T)
 - A set of *Non-terminals* (N)
 - A *Start Symbol* ($S \in N$)
 - A set of *Productions* ($X \rightarrow Y_1 \dots Y_N$) (aka. rules)

$$P: X \longrightarrow Y_1 Y_2 Y_3 \dots Y_N \quad X \in N, \quad Y_i \in N \cup T \cup \epsilon/\lambda$$

Context Free Grammar (CFG)

- Grammar $G = (T, N, S, P)$

E.g. $G = (\{a, b\}, \{S, A, B\}, S, \{S \rightarrow AB, A \rightarrow Aa, A \rightarrow a, B \rightarrow Bb, B \rightarrow b\})$

- Implicit meanings
 - First rule listed in the set of productions contains start symbol (on the left-hand side)
 - In the set of productions, you can replace the symbol X (appearing on the right-hand side only) with the string of symbols that are on the right-hand side of a rule, which has X (on the left-hand side)

Context Free Grammar (CFG)

1. Begin with only S as the initial string

2. Replace S

- S replaced with AB

3. Repeat 2 until the string contains only terminals

i. AB replaced with aB

ii. aB replaced with ab

$G = (T, N, S, P)$
 $P: \{ S \rightarrow AB, \\ A \rightarrow Aa, \\ A \rightarrow a, \\ B \rightarrow Bb, \\ B \rightarrow b \}$

Summary: we move from S to a string of terminals through a series of transformations:

$\alpha_0 \rightarrow \dots \rightarrow \alpha_n$ where $\alpha_1 \dots \alpha_n$ are strings

Shorthand notation: $\alpha_0 \xrightarrow{*} \alpha_n$

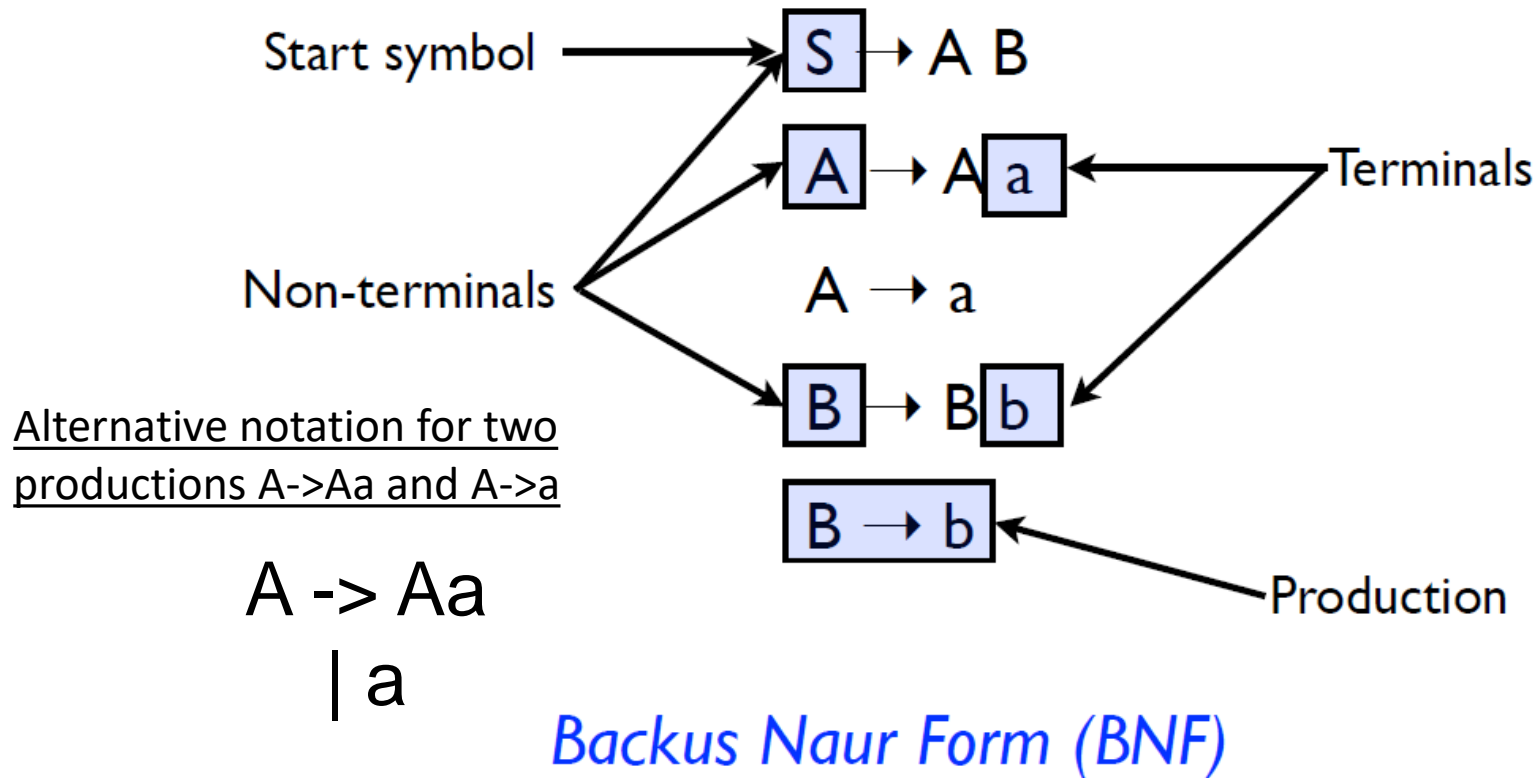
Detour: Context-Sensitive Grammar

- Can have context-sensitive grammar and languages (think: $aB \rightarrow ab$)
 - Cannot replace right-hand side with left-hand side irrespective of the context.
 - E.g. $aB \rightarrow ab$ lays down a context: 'a' must be a prefix in order to transform the string "aB" to a string of terminals "ab"
 - ccaBb can be replaced by ccabb

Is grammar G context-free?

$G = (T, N, S, P)$
 $P: \{$
 $S \rightarrow AB,$
 $A \rightarrow Aa,$
 $A \rightarrow a,$
 $B \rightarrow Bb,$
 $B \rightarrow b \}$

Simple grammar (Summary)



Programming language syntax

- Programming language syntax is defined with CFGs
- Constructs in language become non-terminals
- May use auxiliary non-terminals to make it easier to define constructs

`if_stmt` → if (`cond_expr`) then `statement` `else_part`

`else_part` → else `statement`

`else_part` → λ

- Tokens in language become terminals

Language of the Grammar

- Language $L(G)$ of the context-free grammar G
 - Set of strings that can be derived from S
 - $\{a_1a_2a_3 \dots a_N \mid a_i \in T \ \forall i \text{ and } S \xrightarrow{*} a_1a_2a_3 \dots a_N\}$
 - Is called context-free language
 - All regular languages are context-free but not vice-versa.
 - Can have many grammars generating same language.

String Derivations: Does a string belong to the Language?

- How do we apply the grammar rules to determine the acceptability of a string? (i.e. the string belongs to the language, $L(G)$, specified by the CFG G)
 - Begin with S
 - Replace S
 - Repeat till string contains terminals only. Why terminals only?
 $L(G)$ must contain strings of terminals only
- Notation:
 - We will use Greek letters to denote strings containing non-terminals and terminals
- Derivations: sequence of rules applied to produce the string of terminals

Generating strings (Example)

$S \rightarrow A B$

$A \rightarrow A a$

$A \rightarrow a$

$B \rightarrow B b$

$B \rightarrow b$

- Given a start rule, productions tell us how to rewrite a non-terminal into a different set of symbols
- Some productions may rewrite to λ . That just removes the non-terminal

To derive the string “a a b b b” we can do the following rewrites:

$S \Rightarrow A B \Rightarrow A a B \Rightarrow a a B \Rightarrow a a B b \Rightarrow$
 $a a B b b \Rightarrow a a b b b$

CFG and Parsers

- Is it enough if parsers answer “yes” or “no” to check if a string belongs to context-free language?
 - Also need a parse tree
- What if the answer is a “no”?
 - Handle errors
- How do we implement CFGs?
 - E.g. Bison

Exercise

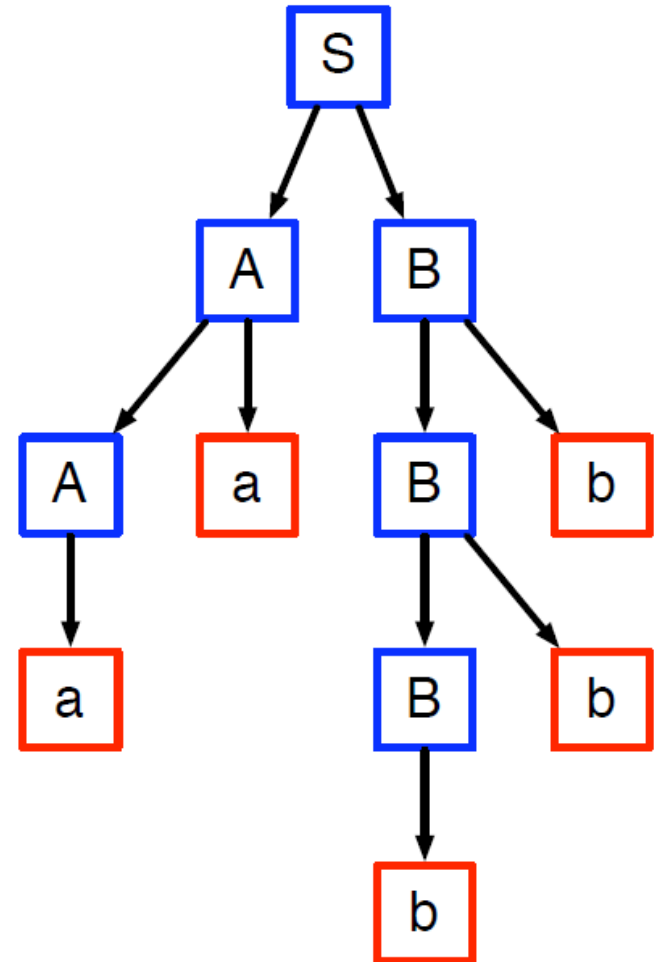
Which of the below strings are accepted by the grammar:

- 1: $A \rightarrow aAa$
- 2: $A \rightarrow bBb$
- 3: $A \rightarrow \lambda$
- 4: $B \rightarrow cA$
- 5: $B \rightarrow \lambda$

- 1. abcba 1- \rightarrow 2- \rightarrow 4- \rightarrow 3
- 2. abcbca
- 3. abba 1- \rightarrow 2- \rightarrow 5
- 4. abca

Parse trees

- Tree which shows how a string was produced by a language
- Interior nodes of tree: non-terminals
 - Children: the terminals and non-terminals generated by applying a production rule
- Leaf nodes: terminals



Derivations and Parse Trees

- Recall: Derivation is a sequence of rules applied to produce a string
 - $S \rightarrow \alpha_0 \rightarrow \alpha_1 \rightarrow \alpha_2 \rightarrow \dots \rightarrow \alpha_n$
- A derivation defines a parse tree
 - Parse tree is an alternative way to gather information on how the string was derived
 - A parse tree may have many derivations (think: different permutations of α)

Derivations and Parse Trees

- Consider the grammar with the following rules:

1: $E \rightarrow E + E$

2: $E \rightarrow E * E$

3: $E \rightarrow id$

- Produce derivations for the string: **$id*id+id$**

Derivations and Parse Trees

- Consider the grammar with the following rules:

1: $E \rightarrow E + E$

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- Produce derivations for the string: **id*id+id**

Apply 1: **Start with E**, the start symbol Parse Tree

E



Derivations and Parse Trees

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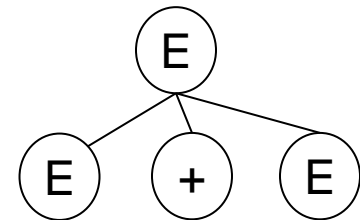
- Produce derivations for the string: **id*id+id**

Apply 1: Replace E with E + E

E

E+E

Parse Tree



Derivations and Parse Trees

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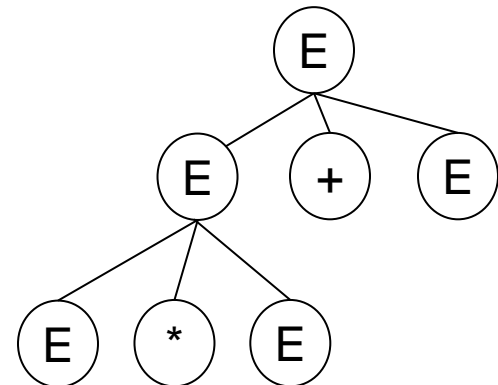
Apply 2: **Replace E with $E * E$**

E

$E + E$

$E * E + E$

Parse Tree



Derivations and Parse Trees

- Consider the grammar with the following rules:

1: $E \rightarrow E + E$

2: $E \rightarrow E * E$

3: $E \rightarrow id$

- Produce derivations for the string: **$id*id+id$**

Apply 3: Replace E with id

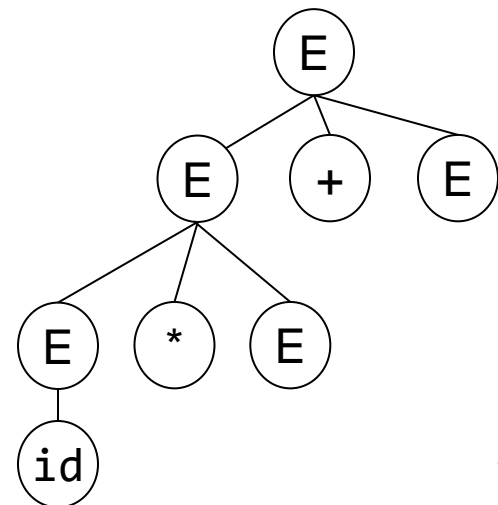
E

E+E

E*E+E

id*E+E

Parse Tree



Derivations and Parse Trees

- Consider the grammar with the following rules:

1: $E \rightarrow E + E$

2: $E \rightarrow E * E$

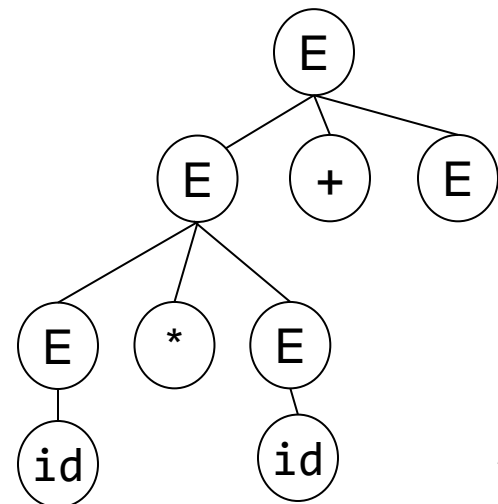
3: $E \rightarrow id$

- Produce derivations for the string: **$id*id+id$**

Apply 3: Replace E with id

E
E+E
E*E+E
id*E+E
id*id+E

Parse Tree



Derivations and Parse Trees

- Consider the grammar with the following rules:

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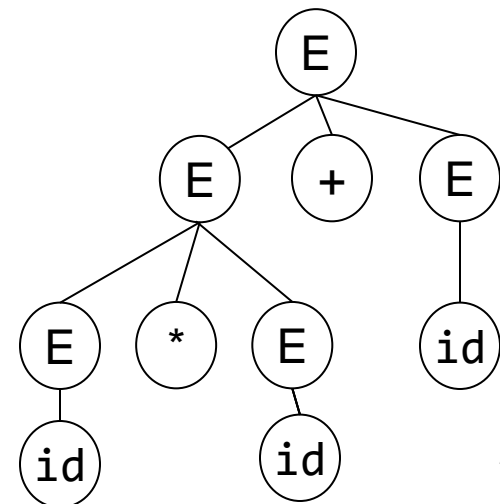
3: $E \rightarrow id$

- Produce derivations for the string: **$id * id + id$**

Apply 3: Replace E with id

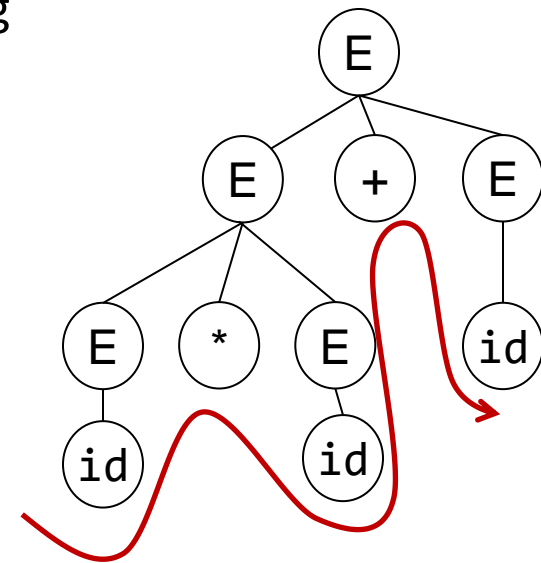
E
E+E
E*E+E
id*E+E
id*id+E
id*id+id

Parse Tree



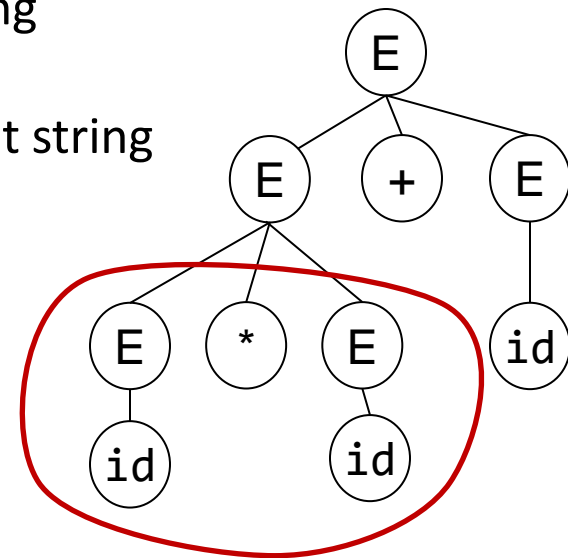
Derivations and Parse Trees

- Note in previous slides:
 - Replacement done on left-most non-terminal in the string - **called left-most derivation**
 - Terminals at leaves and non-terminal as interior nodes
 - Inorder traversal of leaves produces input string `id*id+id`



Derivations and Parse Trees

- Note in previous slides:
 - Replacement done on left-most non-terminal in the string - **called left-most derivation**
 - Terminals at leaves and non-terminal as interior nodes
 - Inorder traversal of leaves produces input string $id*id+id$
 - Parse tree shows association of operations. Input string doesn't
 - * associated with identifiers in the subtree $(id * id)+id$



Derivations and Parse Trees

- Consider the same grammar (having the following rules):

1: $E \rightarrow E + E$

2: $E \rightarrow E * E$

3: $E \rightarrow id$

- Produce derivations for the string: **id*id+id**
 - Using **right-most derivations**
i.e. replace the right-most non-terminal

Derivations and Parse Trees

- Consider the grammar with the following rules:

1: $E \rightarrow E + E$

2: $E \rightarrow E * E$

3: $E \rightarrow id$

- Produce derivations for the string: **id*id+id**

Start with E, the start symbol



Parse Tree

E

Derivations and Parse Trees

- Consider the grammar with the following rules:

1: $E \rightarrow E + E$

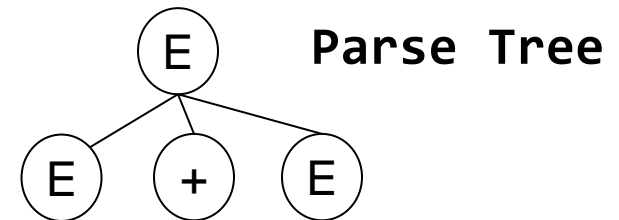
2: $E \rightarrow E * E$

3: $E \rightarrow id$

- Produce derivations for the string: **$id*id+id$**

Apply 2: Replace E with E+E

E
E+E



Derivations and Parse Trees

- Consider the grammar with the following rules:

1: $E \rightarrow E + E$

2: $E \rightarrow E * E$

3: $E \rightarrow id$

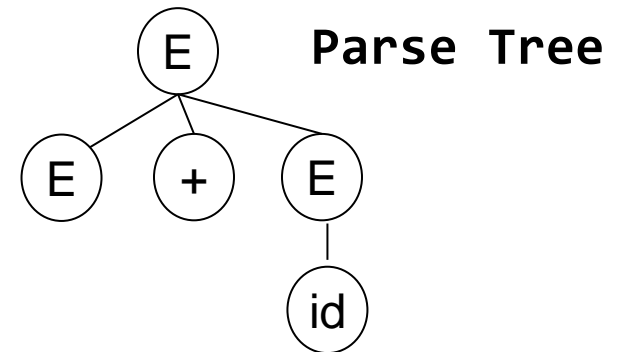
- Produce derivations for the string: **$id*id+id$**

Apply 1: Replace E with id

E

E+E

E+id



Derivations and Parse Trees

- Consider the grammar with the following rules:

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3: $E \rightarrow id$

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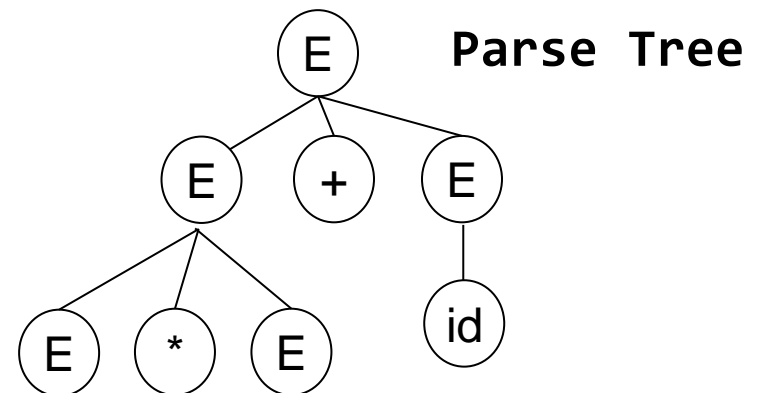
Apply 3: Replace E with $E * E$

E

$E + E$

$E + id$

$E * E + id$



Derivations and Parse Trees

- Consider the grammar with the following rules:

1: $E \rightarrow E + E$

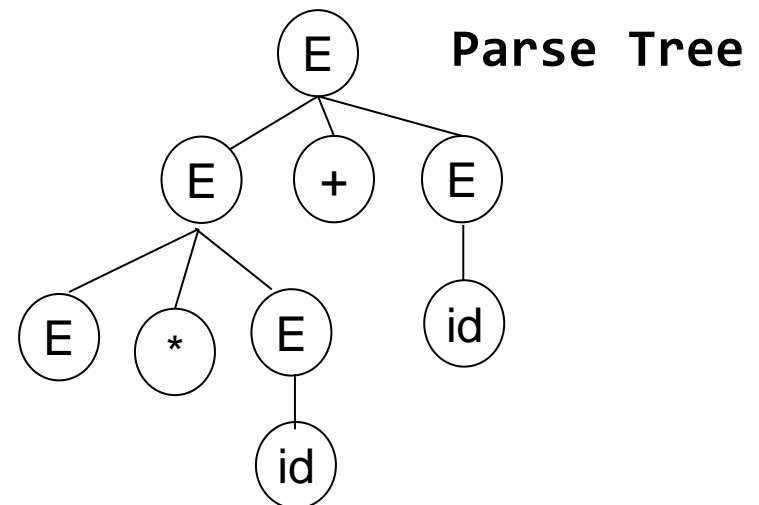
2: $E \rightarrow E * E$

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- Produce derivations for the string: **$id*id+id$**

Apply 3: Replace E with id

E
E+E
E+id
E*E+id
E*id+id



Derivations and Parse Trees

- Consider the grammar with the following rules:

1: $E \rightarrow E + E$

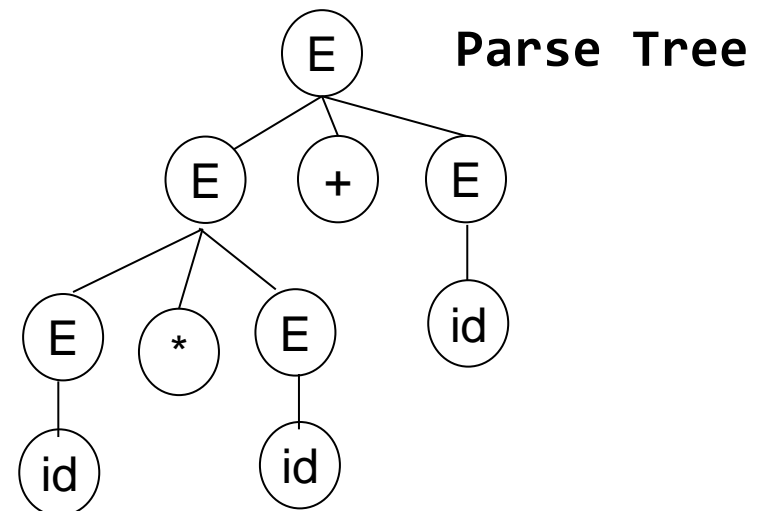
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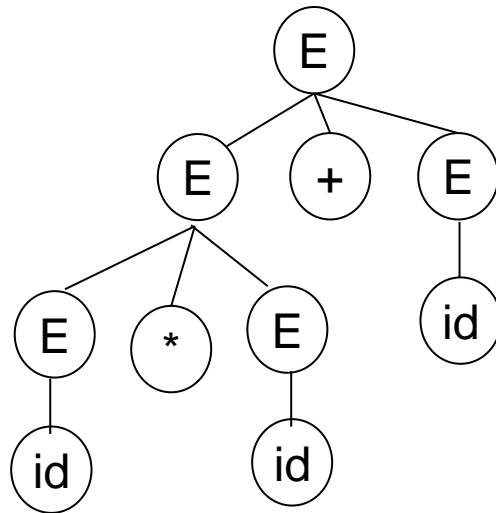
Apply 3: Replace E with id

E
E+E
E+id
E*E+id
E*id+id
id*id+id



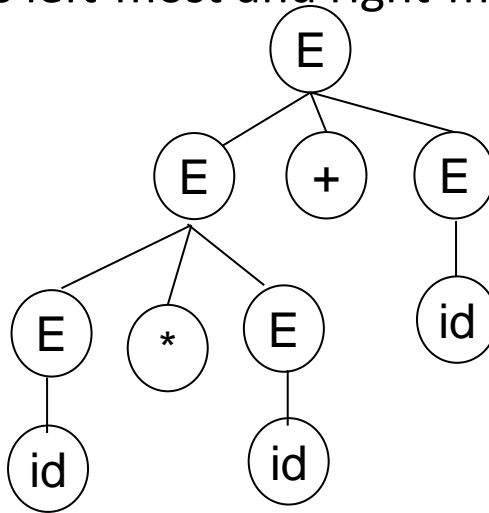
Derivations and Parse Trees

- We get the **same parse tree** using left-most and right-most derivations.
 - Every parse tree has left-most and right-most (and any random order) derivations.



Derivations and Parse Trees

- We get the **same parse tree** using left-most and right-most derivations.
 - Every parse tree has left-most and right-most (and any random order) derivations.



- But there could be a string (or more than one strings) for which there exists derivations that would get different parse trees

Derivations and Parse Trees

- Consider the grammar with the following rules:

1: $E \rightarrow E + E$

2: $E \rightarrow E * E$

3: $E \rightarrow id$

- Produce derivations for the string: **id*id+id**

Start with E, the start symbol



Parse Tree

E

Derivations and Parse Trees

- Consider the grammar with the following rules:

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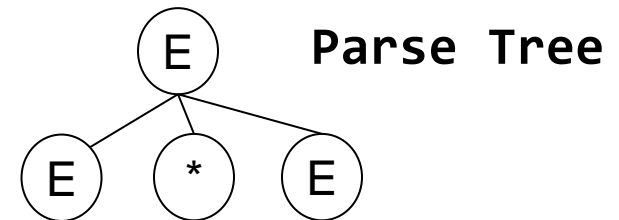
2: $E \rightarrow E * E$

3: $E \rightarrow id$

- Produce derivations for the string: **id*id+id**

Apply 2: **Replace E with E*E** *Earlier it was replace E with E+E*

E
E*E



Derivations and Parse Trees

- Consider the grammar with the following rules:

1: $E \rightarrow E + E$

2: $E \rightarrow E * E$

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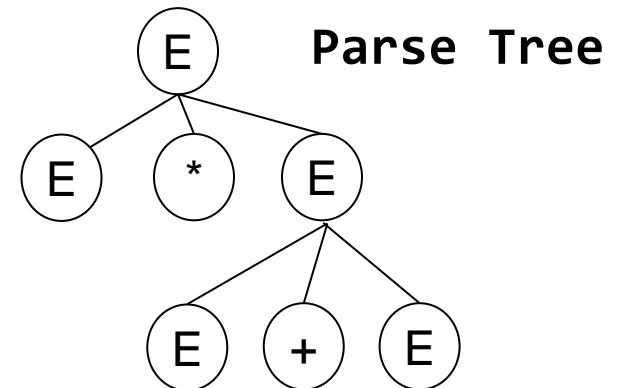
- Produce derivations for the string: **$id*id+id$**

Apply 1: Replace E with $E+E$

E

$E * E$

$E * E + E$



Derivations and Parse Trees

- Consider the grammar with the following rules:

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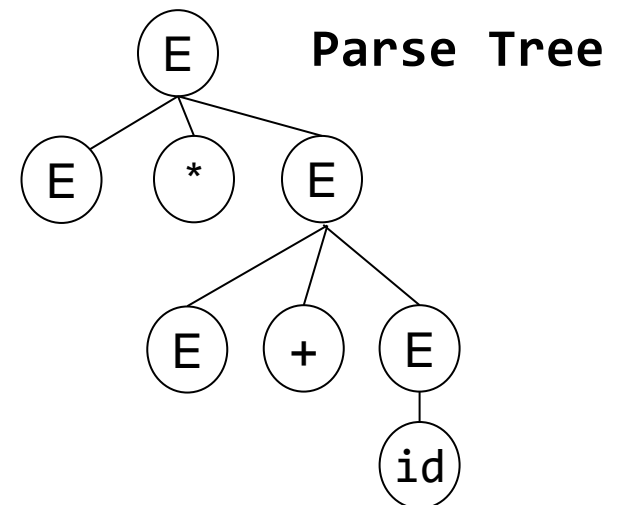
2: $E \rightarrow E * E$

3: $E \rightarrow id$

- Produce derivations for the string: **$id*id+id$**

Apply 3: Replace E with id

E
E * E
E * E + E
E * E + id



Derivations and Parse Trees

- Consider the grammar with the following rules:

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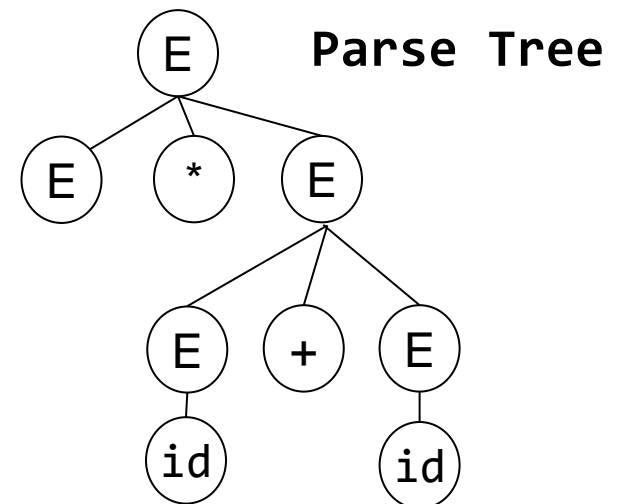
2: $E \rightarrow E * E$

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- Produce derivations for the string: **id*id+id**

Apply 3: Replace E with id

E
E * E
E * E + E
E * E + id
E * id + id



Derivations and Parse Trees

- Consider the grammar with the following rules:

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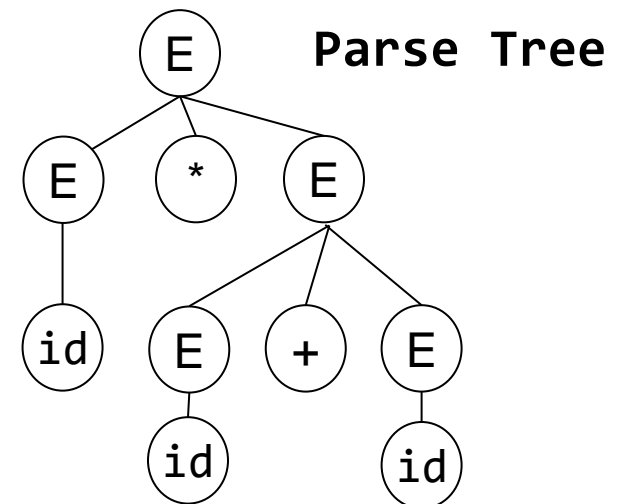
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- Produce derivations for the string: **id*id+id**

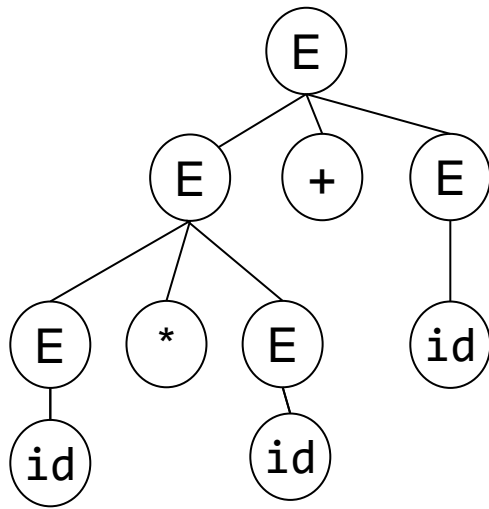
Apply 3: Replace E with id

E
E * E
E * E + E
E * E + id
E * id + id
id * id + id

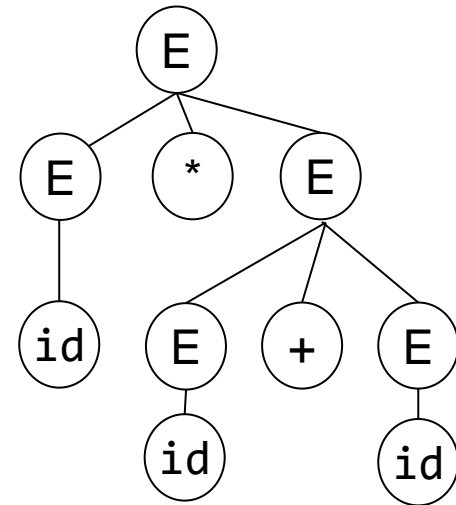


Derivations and Parse Trees

- Input string: $\text{id} * \text{id} + \text{id}$



earlier



now

- Inorder traversal of leaves in both trees produces the same input string

Ambiguous Grammar

- Grammar that produces more than one parse tree for some string

```
1: E -> E + E
2:   | E * E
3:   | id
```