

THE RATIO CAN BE WRITTEN IN THE FOLLOWING FORMATS:

2 TO 3 2 : 3 2 / 3



BLUE
2 LITRES

RED
3 LITRES

RATIOS
3:4

$$x : 6 = 15 : 18$$

$$\frac{1}{2} = \frac{x}{8}$$

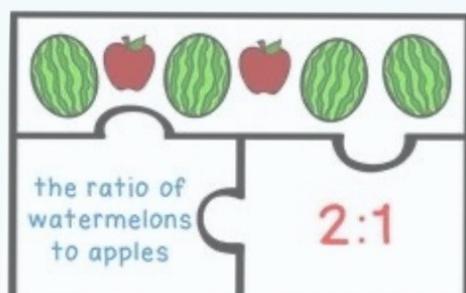
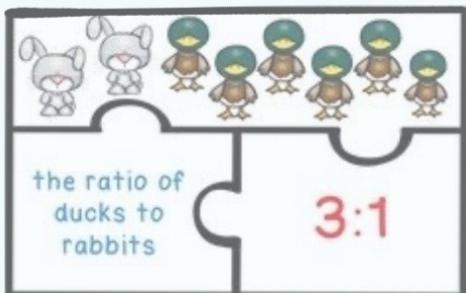
RATIOS

$$3 : 5 = x : 15$$

$$\frac{x}{3} = \frac{5}{2}$$

$$x : 3 = 16 : 24$$

$$\frac{6}{3} = \frac{x}{10}$$



Question 1

Ralf and Susie share \$57 in the ratio 2 : 1.

- (a) Calculate the amount Ralf receives.

[2]

$$3 \text{ units} = 57$$

$$1 \text{ unit} = 19$$

$$2 \text{ units} = \$38$$

- (b) Ralf gives \$2 to Susie.

[2]

Calculate the new ratio Ralf's money : Susie's money.

Give your answer in its simplest form.

$$36 : 21$$

$$12 : 7$$

Question 2

Pip and Ali share \$785 in the ratio

$$\text{Pip : Ali} = 4 : 1$$

[2]

Work out Pip's share.

$$5 \text{ units} = 785$$

$$1 \text{ unit} = 157$$

$$4 \text{ units} = \$628$$

Question 3

Ahmed and Babar share 240 g of sweets in the ratio 7:3.

Calculate the amount Ahmed receives.

[2]

$$10 \text{ units} = 240 \text{ g}$$

$$1 \text{ unit} = 24 \text{ g}$$

$$\begin{aligned}\text{Ahmed} &= 7 \text{ units} \\ &= 168 \text{ g}\end{aligned}$$

Question 4

Ahmed, Batuk and Chand share \$1000 in the ratio 8:7:5.

[3]

Calculate the amount each receives.

$$20 \text{ units} = \$1000$$

$$1 \text{ unit} = \$50$$

$$\text{Ahmed} = 400 \text{ \$}$$

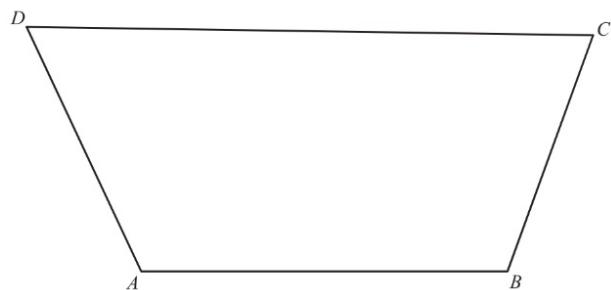
$$\text{Batuk} = 350 \text{ \$}$$

$$\text{Chand} = 250 \text{ \$}$$

The Maths Society

Question 5

The diagram shows the plan, $ABCD$, of a park.
The scale is 1 centimetre represents 20 metres.



Scale: 1 cm to 20 m

- (a) Find the actual distance BC .

[2]

Question 6

Hans draws a plan of a field using a scale of 1 centimetre to represent 15 metres.
The actual area of the field is 10800 m^2 .

Calculate the area of the field on the plan.

[2]

$$\begin{aligned}1 \text{ cm} &= 15 \text{ m} \\1 \text{ cm}^2 &= 225 \text{ m}^2 \\? &= 10800 \text{ m}^2 \\&= \frac{10800}{225} = 48 \text{ cm}^2\end{aligned}$$

Question 7

Pedro and Eva do their homework.
Pedro takes 84 minutes to do his homework.

The ratio Pedro's time : Eva's time = 7 : 6.

[2]

Work out the number of minutes Eva takes to do her homework.

$$\begin{aligned}7 \text{ units} &= 84 \\1 \text{ unit} &= 12 \text{ min} \\Eva &= 6 \text{ unit} = 72 \text{ mins}\end{aligned}$$

Question 8

Jamie needs 300 g of flour to make 20 cakes.

[2]

How much flour does he need to make 12 cakes?

$$\begin{aligned}20 \text{ cakes} &= 300 \text{ g} \\12 &= ? \\&= \frac{12}{20} \times 300 \\&= 180 \text{ g}\end{aligned}$$

The Maths Society

Question 9

Martha divides \$240 between spending and saving in the ratio

$$\text{spending : saving} = 7 : 8.$$

[2]

Calculate the amount Martha has for spending.

$$15 \text{ units} = 240\$\text{}$$

$$7 \text{ unit} = 112\$$$

Question 10

The scale on a map is 1: 20 000.

- (a) Calculate the actual distance between two points which are 2.7 cm apart on the map.
Give your answer in kilometres.

[2]

$$\begin{aligned}1 \text{ cm} &= 20000 \text{ cm} \\2.7 \text{ cm} &= 54000 \text{ cm} \\&= 0.54 \text{ km}\end{aligned}$$

- (b) A field has an area of 64400 m^2 .
Calculate the area of the field on the map in cm^2 .

[2]

$$\begin{aligned}1 \text{ cm} &= 2 \times 10^4 \text{ cm} \\1 \text{ cm}^2 &= 4 \times 10^8 \text{ cm}^2 \\? &= 644 \times 10^6 \text{ cm}^2\end{aligned}\quad \left| \begin{aligned}&= \frac{6.44 \times 10^8}{4 \times 10^8} \\&= 1.61 \text{ cm}^2\end{aligned}\right.$$

Question 11

The scale of a map is 1: 250 000.

- (a) The actual distance between two cities is 80 km.

$$8000000 \text{ cm}$$

[2]

Calculate this distance on the map. Give your answer in centimetres.

$$\begin{aligned}1 \text{ cm} &= 25 \times 10^4 \text{ cm} \\? &= 8 \times 10^6 \text{ cm} \\&= \frac{8 \times 10^6}{25 \times 10^4} = 32 \text{ cm}\end{aligned}$$

- (b) On the map a large forest has an area of 6 cm^2 .

[2]

Calculate the actual area of the forest. Give your answer in square kilometres.

$$\begin{aligned}1 \text{ cm}^2 &= 625 \times 10^8 \text{ cm}^2 & \text{km} &\xrightarrow{10^3} \text{m} &\xrightarrow{10^2} \text{cm} \\6 &= ? \\&= 3750 \times 10^8 \text{ cm}^2 \\&= 37.5 \text{ km}^2\end{aligned}$$

Question 1

A map is drawn to a scale of 1 : 1000 000.
A forest on the map has an area of 4.6 cm².

[2]

Calculate the actual area of the forest in square kilometres.

$$\begin{aligned}1 \text{ cm} &= 10^6 \text{ cm} \\1 \text{ cm}^2 &= 10^{12} \text{ cm}^2 \\4.6 \text{ cm}^2 &= ? \\&= 4.6 \times 10^{12} \text{ cm}^2 \\&= 4.6 \times 10^2 \text{ km}^2 \\&= 460 \text{ km}^2\end{aligned}$$

Question 2

The scale on a map is 1 : 50 000.
The area of a field on the map is 1.2 square centimetres.

[2]

Calculate the actual area of the field in square kilometres.

$$\begin{aligned}1 \text{ cm} &= 50 000 \text{ cm} \\1 \text{ cm}^2 &= 25 \times 10^8 \text{ cm}^2 \\1.2 \text{ cm}^2 &= ? \\&= 30 \times 10^8 \text{ cm}^2 \\&= 0.3 \text{ km}^2\end{aligned}$$

Question 3

The volume of a child's model plane is 1200 cm³.
The volume of the full size plane is 4050 m³.

[3]

Find the scale of the model in the form 1 : n.

$$\begin{aligned}1200 \text{ cm}^3 &: 4050 \text{ m}^3 \\1200 \text{ cm}^3 &: 4050 \times 100 \times 100 \times 100 \text{ cm}^3 \\&: 40500000 \\12 &: 40500000 \\1 &: 3375000\end{aligned}$$

Question 4

A model of a ship is made to a scale of 1 : 200.
The surface area of the model is 7500 cm².

[3]

Calculate the surface area of the ship, giving your answer in square metres.

$$\begin{aligned}1 \text{ cm} &= 200 \text{ cm} \\1 \text{ cm}^2 &= 40000 \text{ cm}^2 \\7500 \text{ cm}^2 &= 4 \times 10^4 \times 75 \times 10^2 \quad \begin{array}{l}100 \\ \text{cm} - \text{m}\end{array} \\&= 150 \times 10^6 \text{ cm}^2 \\&= 15 \times 10^7 \text{ cm}^2 = 15 \times 10^3 \text{ m}^2\end{aligned}$$

Question 5

The scale of a map is 1 : 500 000.

- (a) The actual distance between two towns is 172 km. — **17200000**
Calculate the distance, in centimetres, between the towns on the map.

[2]

$$\begin{aligned}1 \text{ cm} &= 500000 \text{ cm} \\? &= 172 \times 10^5 \text{ cm} \\172 \times 10^5 &= 34.4 \text{ cm} \\5 \times 10^5 &\end{aligned}$$

- (b) The area of a lake on the map is 12 cm².
Calculate the actual area of the lake in km².

[2]

$$\begin{aligned}1 \text{ cm}^2 &= 25 \times 10^5 \text{ cm}^2 \\12 \text{ cm}^2 &= 3 \times 10^7 \text{ cm}^2 \\&= 0.003 \text{ km}^2\end{aligned}$$

Question 6

A car company sells a scale model $\frac{1}{10}$ of the size of one of its cars.

Complete the following table.

1 : 10

	Scale Model	Real Car
Area of windscreen (cm ²)	135	13500
Volume of storage space (cm ³)	408	408000

[3]

Question 7

A model of a car is made to a scale of 1 : 40.

The volume of the model is 45 cm³.

Calculate the volume of the car.

Give your answer in m³.

[3]

$$\begin{aligned}1\text{cm} &= 40\text{cm} \\1\text{cm}^3 &= 64000\text{cm}^3 \\45\text{cm}^3 &= 2880000\text{cm}^3 \\&= 2.88\text{m}^3\end{aligned}$$

Question 8

A company makes two models of television.

Model A has a rectangular screen that measures 44 cm by 32 cm.

Model B has a larger screen with these measurements increased in the ratio 5:4.

[2]

(a) Work out the measurements of the larger screen.

$$\begin{array}{l|l} \text{New : Original} & = 5:4 \\ x : 44 & = 5 : 4 \\ x = 55 & \quad | \quad y : 32 = 5 : 4 \\ & \quad | \quad \times 8 \\ & \quad y = 40 \end{array}$$

(b) Find the fraction $\frac{\text{model } A \text{ screen area}}{\text{model } B \text{ screen area}}$ in its simplest form.

[1]

$$\frac{1408}{2200} = \frac{16}{25}$$

Question 9

The ratios of teachers : male students : female students in a school are 2 : 17 : 18. The total number of students is 665.

Find the number of teachers.

[2]

$$35 \text{ units} = 665$$

$$1 \text{ unit} = 19$$

$$\text{teachers} = 2 \text{units} = 38$$