### Sapienza University of Rome

### Master in Artificial Intelligence and Robotics Master in Engineering in Computer Science

## Machine Learning

A.Y. 2020/2021

Prof. L. locchi, F. Patrizi

L. locchi, F. Patrizi

11. Artificial Neural Networks

1/52

Sapienza University of Rome, Italy - Machine Learning (2020/2021)

### 11. Artificial Neural Networks

L. locchi, F. Patrizi

with contributions from Valsamis Ntouskos

L. locchi, F. Patrizi

11. Artificial Neural Networks

#### Overview

- Feedforward networks
- Architecture design
- Cost functions
- Activation functions
- Gradient computation (back-propagation)
- Learning (stochastic gradient descent)
- Regularization

#### References

Ian Goodfellow and Yoshua Bengio and Aaron Courville. Deep Learning - Chapters 6, 7, 8. http://www.deeplearningbook.org

L. locchi, F. Patrizi

11. Artificial Neural Networks

3/52

Sapienza University of Rome, Italy - Machine Learning (2020/2021)

# Artificial Neural Networks (ANN)

#### Alternative names:

- Neural Networks (NN)
- Feedforward Neural Networks (FNN)
- Multilayer Perceptrons (MLP)

Function approximator using a parametric model.

Suitable for tasks described as associating a vector to another vector.

L. locchi, F. Patrizi

11. Artificial Neural Networks

# Artificial Neural Networks (ANN)

#### Goal:

Estimate some function  $f: X \to Y$ , with  $Y = \{C_1, \dots, C_k\}$  or  $Y = \Re$ 

#### Data:

$$D = \{(\mathbf{x}_n, t_n)_{n=1}^N\}$$
 such that  $t_n \approx f(\mathbf{x}_n)$ 

#### Framework:

Define  $y = \hat{f}(\mathbf{x}; \boldsymbol{\theta})$  and learn parameters  $\boldsymbol{\theta}$  so that  $\hat{f}$  approximates f.

L. locchi, F. Patrizi

11. Artificial Neural Networks

5 / 52

Sapienza University of Rome, Italy - Machine Learning (2020/2021)

### Feedforward Networks

#### Draw inspiration from brain structures

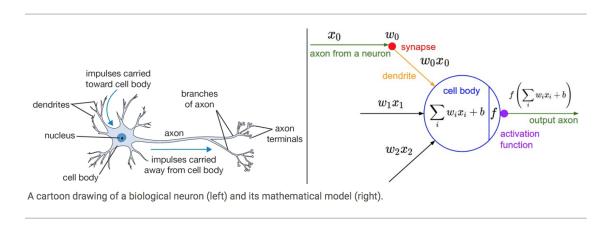


Image from Isaac Changhau https://isaacchanghau.github.io

Hidden layer output can be seen as an array of **unit** (neuron) activations based on the connections with the previous units

Note: Only use some insights, they are not a model of the brain!

L. locchi, F. Patrizi

11. Artificial Neural Networks

# Feedforward Networks - Terminology

Feedforward information flows from input to output without any loop Networks f is a composition of elementary functions in an acyclic graph

Example:

$$f(\mathbf{x}; \boldsymbol{\theta}) = f^{(3)}(f^{(2)}(f^{(1)}(\mathbf{x}; \boldsymbol{\theta}^{(1)}); \boldsymbol{\theta}^{(2)}); \boldsymbol{\theta}^{(3)})$$

where:

 $f^{(m)}$  the m-th layer of the network

and

 $oldsymbol{ heta}^{(m)}$  the corresponding parameters

L. locchi, F. Patrizi

11. Artificial Neural Networks

7 / 52

Sapienza University of Rome, Italy - Machine Learning (2020/2021)

# Feedforward Networks - Terminology

#### FNNs are chain structures

The length of the chain is the **depth** of the network

Final layer also called output layer

**Deep learning** follows from the use of networks with a large number of layers (large depth)

L. locchi, F. Patrizi

11. Artificial Neural Networks

### Feedforward Networks

#### Why FNNs?

Linear models cannot model interaction between input variables

Kernel methods require the choice of suitable kernels

- use generic kernels e.g. RBF, polynomial, etc. (convex problem)
- use hand-crafted kernels application specific (convex problem)

#### FNN leaning:

complex combination of many parametric functions (non-convex problem)

L. locchi, F. Patrizi

11. Artificial Neural Networks

9 / 52

Sapienza University of Rome, Italy - Machine Learning (2020/2021)

## XOR Example - Linear model

Learning the XOR function - 2D input and 1D output

Dataset: 
$$D = \{((0,0)^T,0), ((0,1)^T,1), ((1,0)^T,1), ((1,1)^T,0)\}$$

Using linear regression with Mean Squared Error (MSE)

$$J(\boldsymbol{\theta}) = \frac{1}{N} \sum_{n=1}^{N} (t_n - y(\mathbf{x}_n))^2$$

with 
$$y(\mathbf{x}) = \mathbf{w}^T \mathbf{x} + w_0$$

Optimal solution:

$$\mathbf{w}=0$$
 and  $w_0=\frac{1}{2}$ , hence  $y=0.5$  everywhere!

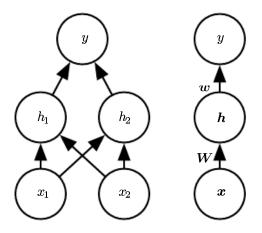
Reason: No linear separator can explain the non-linear XOR function

L. locchi, F. Patrizi

11. Artificial Neural Networks

# XOR Example - FNN

Specify a two layers network:



L. locchi, F. Patrizi

11. Artificial Neural Networks

11 / 52

Sapienza University of Rome, Italy - Machine Learning (2020/2021)

# XOR Example - FNN

Hidden units:

$$\mathbf{h} = g(\mathbf{W}^T \mathbf{x} + \mathbf{c})$$

with  $g(\alpha) = \max(0, \alpha)$ 

Output:

$$y = \mathbf{w}^T \mathbf{h} + b$$

Full model:

$$y(\mathbf{x}) = f(\mathbf{x}; \boldsymbol{\theta}) = \mathbf{w}^T \max(0, \mathbf{W}^T \mathbf{x} + \mathbf{c}) + b$$

with  $\boldsymbol{\theta} = \langle \mathbf{W}, \mathbf{c}, \mathbf{w}, b \rangle$ 

Note: non-linear model in heta

### XOR Example - FNN

Model:

$$y(\mathbf{x}) = f(\mathbf{x}; \boldsymbol{\theta}) = \mathbf{w}^T \max(0, \mathbf{W}^T \mathbf{x} + \mathbf{c}) + b$$

Mean Squared Error (MSE) loss function:

$$J(\boldsymbol{\theta}) = \frac{1}{N} \sum_{n=1}^{N} (t_n - y(\mathbf{x}_n))^2$$

Solution:

$$\mathbf{W} = \begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix}, \mathbf{c} = \begin{bmatrix} 0 \\ -1 \end{bmatrix}, \mathbf{w} = \begin{bmatrix} 1 \\ -2 \end{bmatrix}, b = 0$$

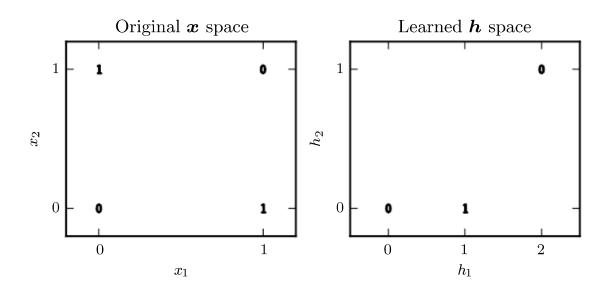
L. locchi, F. Patrizi

11. Artificial Neural Networks

13 / 52

Sapienza University of Rome, Italy - Machine Learning (2020/2021)

# XOR Example - FNN



L. locchi, F. Patrizi

11. Artificial Neural Networks

## Architecture design

Overall structure of the network

How many hidden layers? **Depth** 

How many units in each layer? Width

Which kind of units? **Activation functions** 

Which kind of cost function? Loss function

L. locchi, F. Patrizi

11. Artificial Neural Networks

15 / 52

Sapienza University of Rome, Italy - Machine Learning (2020/2021)

### Architecture design

How many hidden layers? **Depth** 

**Universal approximation theorem**: a FFN with a linear output layer and at least one hidden layer with any "squashing" activation function (e.g., sigmoid) can approximate any Borel measurable function with any desired amount of error, provided that enough hidden units are used.

It works also for other activation functions (e.g., ReLU)

L. locchi, F. Patrizi

11. Artificial Neural Networks

### Architecture design

How many units in each layer? Width

Universal approximation theorem does not say how many units.

In general it is exponential in the size of the input.

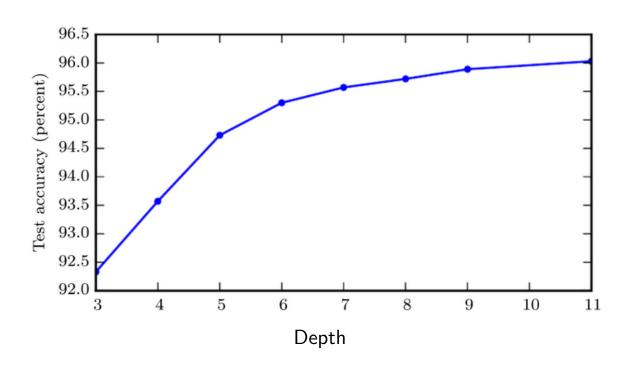
In theory, a short and very wide network can approximate any function.

In practice, a deep and narrow network is easier to train and provides better results in generalization.

L. locchi, F. Patrizi 11. Artificial Neural Networks 17 / 52

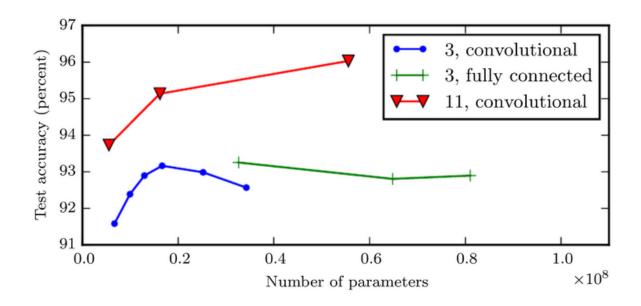
Sapienza University of Rome, Italy - Machine Learning (2020/2021)

## Architecture design



L. locchi, F. Patrizi

## Architecture design



L. locchi, F. Patrizi 11. Artificial Neural Networks 19 / 52
Sapienza University of Rome, Italy - Machine Learning (2020/2021)

## Architecture design

Which kind of units? Activation functions

Which kind of cost function? Loss function

Gradient-based learning remarks

- Unit saturation can hinder learning
- When units saturate gradient becomes very small
- Suitable cost functions and unit nonlinearities help to avoid saturation

L. locchi, F. Patrizi

11. Artificial Neural Networks

### Cost function

Model implicitly defines a conditional distribution  $p(\mathbf{t}|\mathbf{x}, \boldsymbol{\theta})$ 

Cost function: Maximum likelihood principle (cross-entropy)

$$J(\boldsymbol{\theta}) = E_{\mathbf{x}, \mathbf{t} \sim \mathcal{D}} \left[ -\ln(p(\mathbf{t}|\mathbf{x}, \boldsymbol{\theta})) \right]$$

Example:

Assuming additive Gaussian noise we have

$$p(\mathbf{t}|\mathbf{x}, \boldsymbol{\theta}) = \mathcal{N}(\mathbf{t}|f(\mathbf{x}; \boldsymbol{\theta}), \beta^{-1}I)$$

and hence

$$J(\boldsymbol{\theta}) = E_{\mathbf{x}, \mathbf{t} \sim \mathcal{D}} \left[ \frac{1}{2} ||\mathbf{t} - f(\mathbf{x}; \boldsymbol{\theta})||^2 \right]$$

Maximum likelihood estimation with Gaussian noise corresponds to mean squared error minimization.

L. locchi, F. Patrizi

11. Artificial Neural Networks

21 / 52

Sapienza University of Rome, Italy - Machine Learning (2020/2021)

## Output units activation functions

Let  $\mathbf{h}=f(\mathbf{x};\boldsymbol{\theta}^{(n-1)})$  the output of the hidden layers, which output model  $y=f^{(n)}(\mathbf{h};\boldsymbol{\theta}^{(n)})$  ? which cost function  $J(\boldsymbol{\theta})$  ?

Choice of network output units and cost function are related.

- Regression
- Binary classification
- Multi-classes classification

L. locchi, F. Patrizi

11. Artificial Neural Networks

## Output units activation functions

#### Regression

**Linear units**: Identity activation function

$$y = \mathbf{W}^T \mathbf{h} + \mathbf{b}$$

Use a Gaussian distribution noise model

$$p(t|\mathbf{x}) = \mathcal{N}(t|y, \beta^{-1})$$

<u>Cost function:</u> maximum likelihood (cross-entropy) that is equivalent to minimizing **mean squared error**.

Note: linear units do not saturate

L. locchi, F. Patrizi

11. Artificial Neural Networks

23 / 52

Sapienza University of Rome, Italy - Machine Learning (2020/2021)

## Output units activation functions

#### **Binary classification**

**Sigmoid units**: Sigmoid activation function  $y = \sigma(\mathbf{w}^T \mathbf{h} + b)$ 

The likelihood corresponds to a Bernoulli distribution

$$J(\boldsymbol{\theta}) = E_{\mathbf{x},t \sim \mathcal{D}} \left[ -\ln p(t|\mathbf{x}) \right]$$
$$-\ln p(t|\mathbf{x}) = -\ln \sigma(\alpha)^t (1 - \sigma(\alpha))^{1-t}$$
$$= -\ln \sigma((2t - 1)\alpha)$$
$$= \text{softplus}((1 - 2t)\alpha)$$

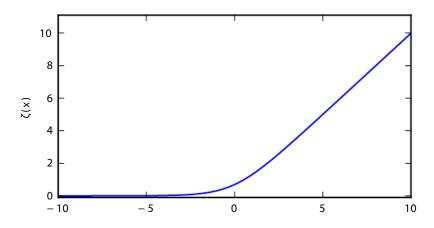
with  $\alpha = \mathbf{w}^T \mathbf{h} + b$ .

Note: Unit saturates only when it gives the correct answer.

L. locchi, F. Patrizi

11. Artificial Neural Networks

## Output units activation functions



The softplus function

L. locchi, F. Patrizi

11. Artificial Neural Networks

25 / 52

Sapienza University of Rome, Italy - Machine Learning (2020/2021)

## Output units activation functions

#### Multi-class classification

Softmax units: Softmax activation function

$$y_i = \mathtt{softmax}(\alpha_i) = \frac{\exp(\alpha_i)}{\sum_j \exp(\alpha_j)}$$

Likelihood corresponds to a Multinomial distribution

$$J_i(\boldsymbol{\theta}) = E_{\mathbf{x}, \mathbf{t} \sim \mathcal{D}} \left[ -\ln \mathtt{softmax}(\alpha_i) \right]$$

with  $\alpha_i = \mathbf{w}_i^T \mathbf{h} + b_i$ .

Note: Unit saturates only when there are minimal errors.

L. locchi, F. Patrizi

11. Artificial Neural Networks

## Output units activation functions

#### Summary

Regression: linear output unit, mean squared error loss function

Binary classification: sigmoid output unit, binary cross-entropy

Multi-class classification: softmax output unit, categorical cross-entropy

Note: on-going research on different loss functions.

L. locchi, F. Patrizi

11. Artificial Neural Networks

27 / 52

Sapienza University of Rome, Italy - Machine Learning (2020/2021)

### Hidden units activation functions

Many choices, some intuitions, no theoretical principles.

Predicting which activation function will work best is usually impossible.

### **Rectified Linear Units** (ReLU):

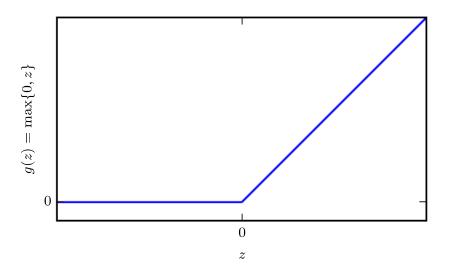
$$g(\alpha) = \max(0, \alpha).$$

- Easy to optimize similar to linear units
- Not differentiable at 0 does not cause problems in practice

L. locchi, F. Patrizi

11. Artificial Neural Networks

### Hidden unit activation functions



L. locchi, F. Patrizi

11. Artificial Neural Networks

29 / 52

Sapienza University of Rome, Italy - Machine Learning (2020/2021)

### Hidden unit activation functions

#### Sigmod and hyperbolic tangent:

$$g(\alpha) = \sigma(\alpha)$$

and

$$g(\alpha) = \tanh(\alpha)$$

Closely related as  $tanh(\alpha) = 2\sigma(2\alpha) - 1$ .

#### Remarks:

- No logarithm at the output, the units saturate easily.
- Gradient based learning is very slow.
- Hyperbolic tangent gives larger gradients with respect to the sigmoid.
- Useful in other contexts (e.g., recurrent networks, autoencoders).

### Activation functions overview

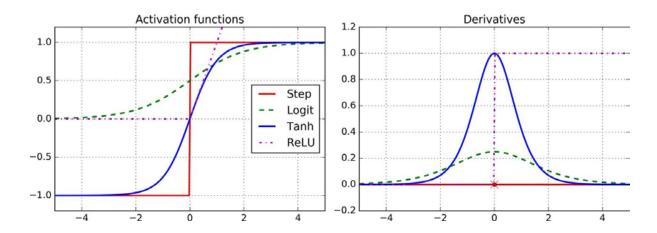


Image from Geron A. "Hands-On Machine Learning with Scikit-Learn and TensorFlow", O'Reilly 2017

L. locchi, F. Patrizi

11. Artificial Neural Networks

31 / 52

Sapienza University of Rome, Italy - Machine Learning (2020/2021)

## **Gradient Computation**

Information flows forward through the network when computing network output y from input x

To train the network we need to compute the gradients with respect to the network parameters  $\boldsymbol{\theta}$ 

The **back-propagation** or **backprop** algorithm is used to propagate gradient computation from the cost through the whole network

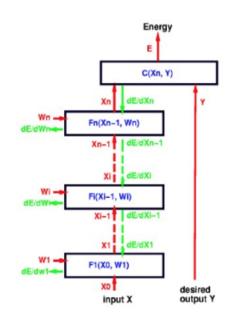


Image by Y. LeCun

## **Gradient Computation**

Goal: Compute the gradient of the cost function w.r.t. the parameters

$$\nabla_{\boldsymbol{\theta}} J(\boldsymbol{\theta})$$

Analytic computation of the gradient is straightforward

- simple application of the chain rule
- numerical evaluation can be expensive

Back-propagation is simple and efficient.

Remarks:

- back-propagation is only used to compute the gradients
- back-propagation is not a training algorithm
- back-propagation is not specific to FNNs

L. locchi, F. Patrizi

11. Artificial Neural Networks

33 / 52

Sapienza University of Rome, Italy - Machine Learning (2020/2021)

### Chain rule

Let: y = g(x) and z = f(g(x)) = f(y)

Applying the chain rule we have:

$$\frac{dz}{dx} = \frac{dz}{dy}\frac{dy}{dx}$$

For vector functions,  $g:\mathbb{R}^m\mapsto\mathbb{R}^n$  and  $f:\mathbb{R}^n\mapsto\mathbb{R}$  we have:

$$\frac{\partial z}{\partial x_i} = \sum_{j} \frac{\partial z}{\partial y_j} \frac{\partial y_j}{\partial x_i},$$

equivalently in vector notation:

$$\nabla_{\mathbf{x}} z = \left(\frac{\partial \mathbf{y}}{\partial \mathbf{x}}\right)^T \nabla_{\mathbf{y}} z,$$

with  $\frac{\partial \mathbf{y}}{\partial \mathbf{x}}$  the  $n \times m$  Jacobian matrix of g.

L. locchi, F. Patrizi

11. Artificial Neural Networks

## Back-propagation algorithm

#### Forward step

```
Require: Network depth l
Require: W^{(i)}, i \in \{1, \dots, l\} weight matrices Require: \mathbf{b}^{(i)}, i \in \{1, \dots, l\} bias parameters Require: \mathbf{x} input value Require: \mathbf{t} target value h^{(0)} = \mathbf{x} for k = 1, \dots, l do \boldsymbol{\alpha}^{(k)} = \mathbf{b}^{(k)} + W^{(k)} \mathbf{h}^{(k-1)} \mathbf{h}^{(k)} = f(\boldsymbol{\alpha}^{(k)}) end for \mathbf{v} = \mathbf{h}^{(l)}
```

L. locchi, F. Patrizi

 $J = L(\mathbf{t}, \mathbf{y})$ 

11. Artificial Neural Networks

35 / 52

Sapienza University of Rome, Italy - Machine Learning (2020/2021)

# Back-propagation algorithm

#### Backward step

$$\mathbf{g} \leftarrow 
abla_{\mathbf{y}} J = 
abla_{\mathbf{y}} L(\mathbf{t}, \mathbf{y})$$
 for  $k = l, l - 1, \dots, 1$  do Propagate gradients to

Propagate gradients to the pre-nonlinearity activations:

$$\mathbf{g} \leftarrow \nabla_{\boldsymbol{\alpha}^{(k)}} J = \mathbf{g} \odot f'(\boldsymbol{\alpha}^{(k)}) \ \{\odot \text{ denotes elementwise product}\}\ \nabla_{\mathbf{b}^{(k)}} J = \mathbf{g}$$

$$\nabla_{W^{(k)}} J = \mathbf{g}(\mathbf{h}^{(k-1)})^T$$

Propagate gradients to the next lower-level hidden layer:

$$\mathbf{g} \leftarrow \nabla_{\mathbf{h}^{(k-1)}} J = (W^{(k)})^T \mathbf{g}$$

end for

L. locchi, F. Patrizi

11. Artificial Neural Networks

## Back-propagation algorithm

#### Remarks:

- The previous version of backprop is specific for fully connected MLPs
- More general versions for acyclic graphs exist
- Dynamic programming is used to avoid doing the same computations multiple times
- Gradients can be computed either in symbolic or numerical form

L. locchi, F. Patrizi

11. Artificial Neural Networks

37 / 52

Sapienza University of Rome, Italy - Machine Learning (2020/2021)

## Learning algorithms

- Stochastic Gradient Descent (SGD)
- SGD with momentum
- Algorithms with adaptive learning rates

L. locchi, F. Patrizi

11. Artificial Neural Networks

### Stochastic Gradient Descent

**Require:** Learning rate  $\eta \ge 0$ **Require:** Initial values of  $\theta^{(1)}$ 

 $k \leftarrow 1$ 

while stopping criterion not met do

Sample a subset (minibatch)  $\{\mathbf{x}^{(1)},\ldots,\mathbf{x}^{(m)}\}$  of m examples from the dataset  $\mathcal{D}$ 

Compute gradient estimate:  $\mathbf{g} = \frac{1}{m} \nabla_{\boldsymbol{\theta}} \sum_{i} L(f(\mathbf{x}^{(i)}; \boldsymbol{\theta}^{(k)}), \mathbf{t}^{(i)})$ 

Apply update:  $oldsymbol{ heta}^{(k+1)} \leftarrow oldsymbol{ heta}^{(k)} - \eta \mathbf{g}$ 

 $k \leftarrow k + 1$ 

end while

L. locchi, F. Patrizi

11. Artificial Neural Networks

39 / 52

Sapienza University of Rome, Italy - Machine Learning (2020/2021)

### Stochastic Gradient Descent

 $\eta$  usually changes according to some rule through the iterations

Until iteration  $\tau$   $(k \leq \tau)$ :

$$\eta^{(k)} = \left(1 - \frac{k}{\tau}\right)\eta^{(k)} + \frac{k}{\tau}\eta^{(\tau)}$$

After iteration  $\tau$   $(k > \tau)$ :

$$\eta^{(k)} = \eta^{(\tau)}$$

### SGD with momentum

Momentum can accelerate learning

Motivation: Stochastic gradient can largely vary through the iterations

**Require:** Learning rate  $\eta \geq 0$ **Require:** Momentum  $\mu \geq 0$ **Require:** Initial values of  $\theta^{(1)}$  $k \leftarrow 1$ 

 $\mathbf{v}^{(1)} \leftarrow 0$ 

while stopping criterion not met do

Sample a subset (minibatch)  $\{\mathbf{x}^{(1)},\ldots,\mathbf{x}^{(m)}\}$  of m examples from the dataset  $\mathcal{D}$ 

Compute gradient estimate:  $\mathbf{g} = \frac{1}{m} \nabla_{\theta} \sum_{i} L(f(\mathbf{x}^{(i)}; \boldsymbol{\theta}^{(k)}), \mathbf{t}^{(i)})$ 

Compute velocity:  $\mathbf{v}^{(k+1)} \leftarrow \mu \mathbf{v}^{(k)} - \eta \mathbf{g}$ , with  $\mu \in [0,1)$ 

Apply update:  $\boldsymbol{\theta}^{(k+1)} \leftarrow \boldsymbol{\theta}^{(k)} + \mathbf{v}^{(k+1)}$ 

 $k \leftarrow k + 1$ 

end while

L. locchi, F. Patrizi

11. Artificial Neural Networks

41 / 52

Sapienza University of Rome, Italy - Machine Learning (2020/2021)

### SGD with momentum

Momentum  $\mu$  might also increase according to some rule through the iterations.

L. locchi, F. Patrizi

11. Artificial Neural Networks

### SGD with Nesterov momentum

#### **Nesterov momentum**

Momentum is applied before computing the gradient

$$\tilde{\boldsymbol{\theta}} = \boldsymbol{\theta}^{(k)} + \mu \mathbf{v}^{(k)}$$

$$\mathbf{g} = \frac{1}{m} \nabla_{\tilde{\boldsymbol{\theta}}} \sum_{i} L(f(\mathbf{x}^{(i)}; \tilde{\boldsymbol{\theta}}), \mathbf{t}^{(i)})$$

Sometimes it improves convergence rate.

L. locchi, F. Patrizi

11. Artificial Neural Networks

43 / 52

Sapienza University of Rome, Italy - Machine Learning (2020/2021)

# Algorithms with adaptive learning rates

Based on analysis of the gradient of the loss function it is possible to determine, at any step of the algorithm, whether the learning rate should be increased or decreased.

Some examples:

- AdaGrad
- RMSProp
- Adam

(see Deep Learning Book, Section 8.5 for details)

Which optimization algorithm should I choose?

Empirical approach.

L. locchi, F. Patrizi

11. Artificial Neural Networks

## Regularization

As with other ML approaches, regularization is an important feature to reduce overfitting (generalization error).

For FNN, we have several options (can be applied at together):

- Parameter norm penalties
- Dataset augmentation
- Early stopping
- Parameter sharing
- Dropout

L. locchi, F. Patrizi

11. Artificial Neural Networks

45 / 52

Sapienza University of Rome, Italy - Machine Learning (2020/2021)

## Parameter norm penalties

Add a regularization term  $E_{\rm reg}$  to the cost function

$$E_{\text{reg}}(\boldsymbol{\theta}) = \sum_{j} |\theta_{j}|^{q}.$$

Resulting cost function:

$$\bar{J}(\boldsymbol{\theta}) = J(\boldsymbol{\theta}) + \lambda E_{\text{reg}}(\boldsymbol{\theta}).$$

L. locchi, F. Patrizi

11. Artificial Neural Networks

### Dataset augmentation

Generate additional data and include them in the dataset.

- Data transformations (e.g., image rotation, scaling, varying illumination conditions, ...)
- Adding noise

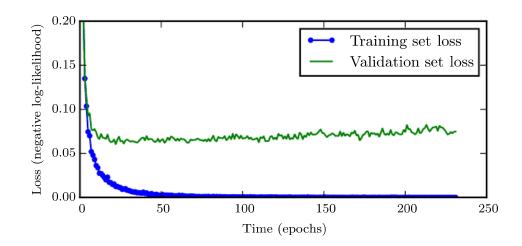
In Exercise 7, noisy XOR converges faster than XOR.

L. locchi, F. Patrizi
Sapienza University of Rome, Italy - Machine Learning (2020/2021)

Early stopping

### **Early stopping:**

Stop iterations early to avoid overfitting to the training set of data



When to stop? Use cross-validation to determine best values.

L. locchi, F. Patrizi

## Parameter sharing

**Parameter sharing**: constraint on having subsets of model parameters to be equal.

Advantages also in memory storage (only the unique subset of parameters need to be stored).

In Convolutional Neural Networks (CNNs) parameter sharing allows for invariance to translation.

L. locchi, F. Patrizi

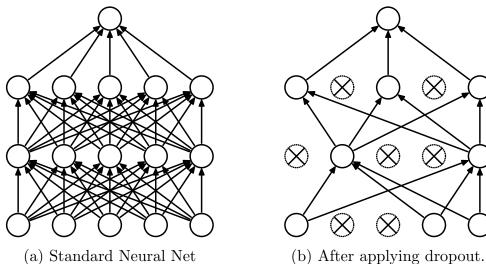
11. Artificial Neural Networks

49 / 52

Sapienza University of Rome, Italy - Machine Learning (2020/2021)

# Dropout

Dropout : Randomly remove network units with some probability  $\alpha$ 



(a) Standard Hearth Her (b) Theor applying dropout.

Image from Srivastava et al.. "Dropout: A Simple Way to Prevent Neural Networks from Overfitting"

L. locchi, F. Patrizi

11. Artificial Neural Networks

### Dropout

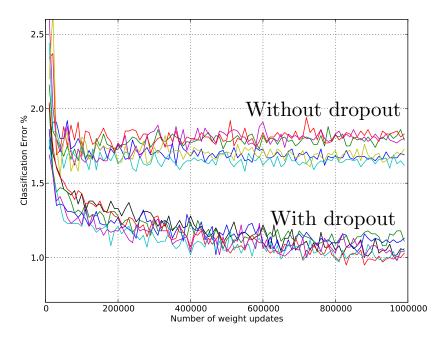


Image from Srivastava et al.. "Dropout: A Simple Way to Prevent Neural Networks from Overfitting"

L. Iocchi, F. Patrizi

11. Artificial Neural Networks

51 / 52

Sapienza University of Rome, Italy - Machine Learning (2020/2021)

# Summary

### Feedforward neural networks (FNNs)

- parametric models with many combination of simple functions
- can effectively approximate any function (no need to guess kernel models)
- must be carefully designed (empirically)
- efficient ways to optimize the loss function
- deep architectures perform better
- optimization performance can be improved with momentum and adaptive learning rate
- generalization error can be reduced with regularization

L. locchi, F. Patrizi