

# Sorting Algorithms

## Heap Sort

# Time Complexity

**Best, Average and Worst Case:**

$$O(N * \text{Log}N)$$

# Space Complexity

**No additional space required  
(In-place algorithm)**

**$O(1)$**

# Original Array

0

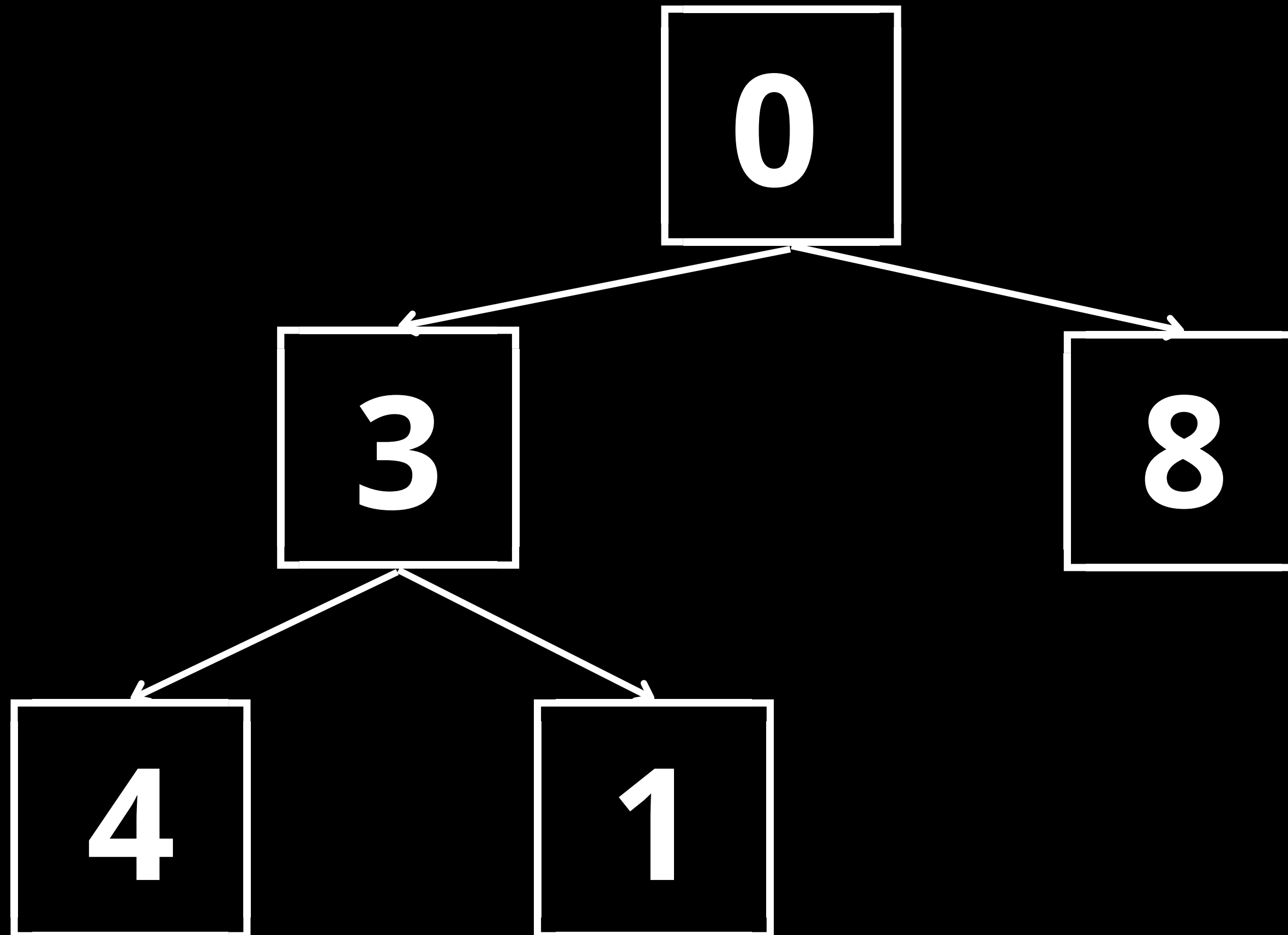
3

8

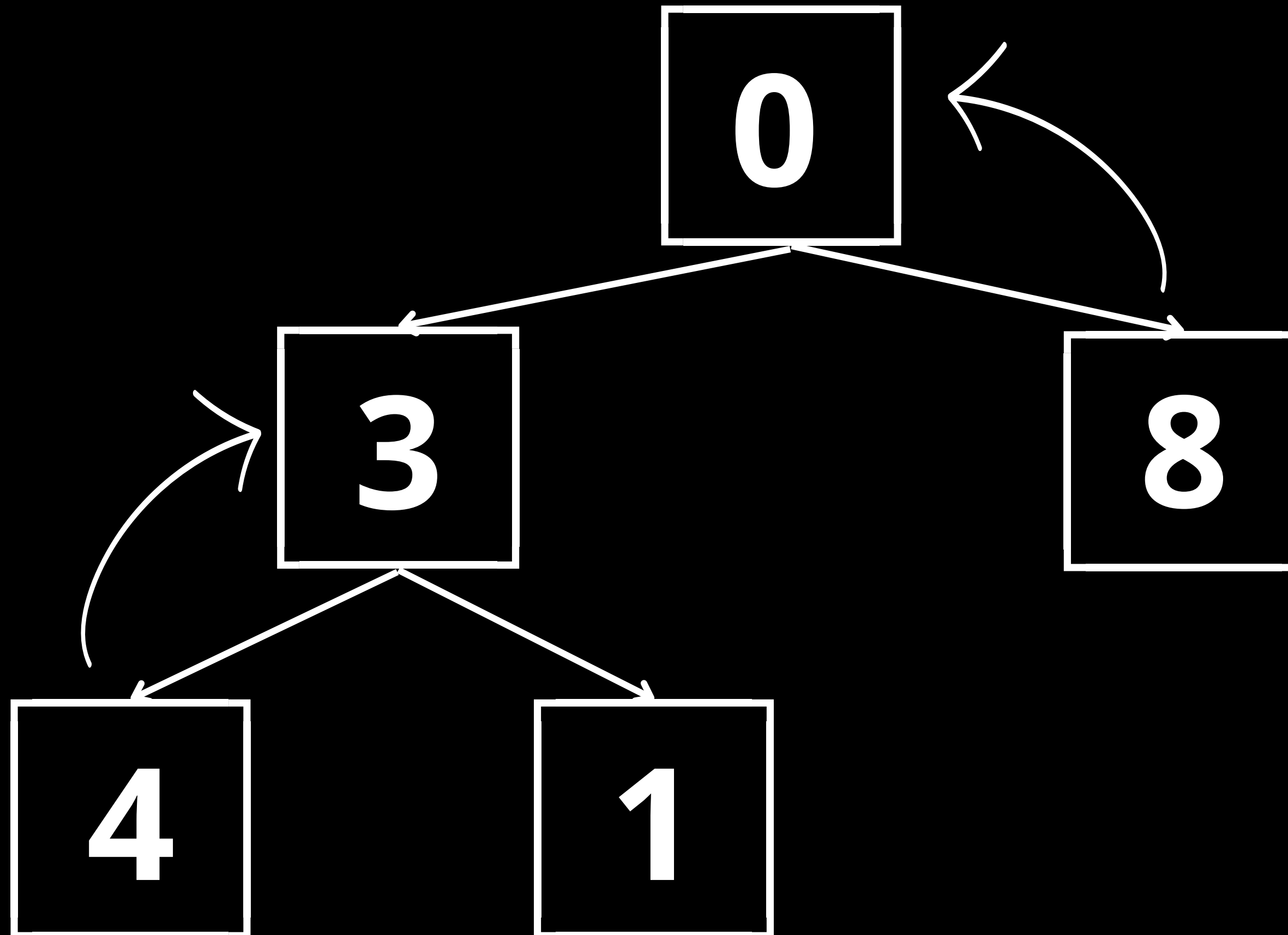
4

1

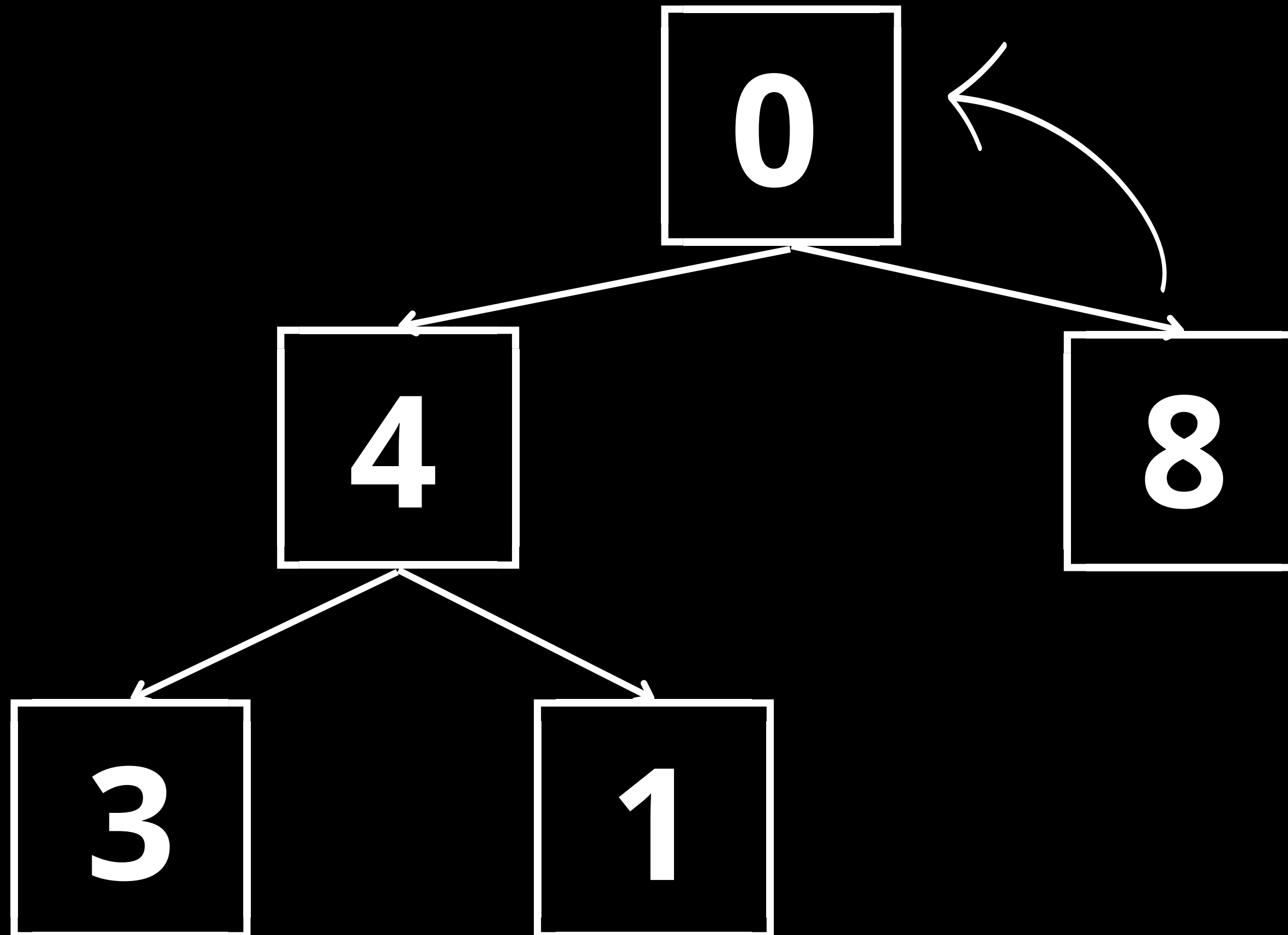
# Create a Complete Binary Tree with the Array



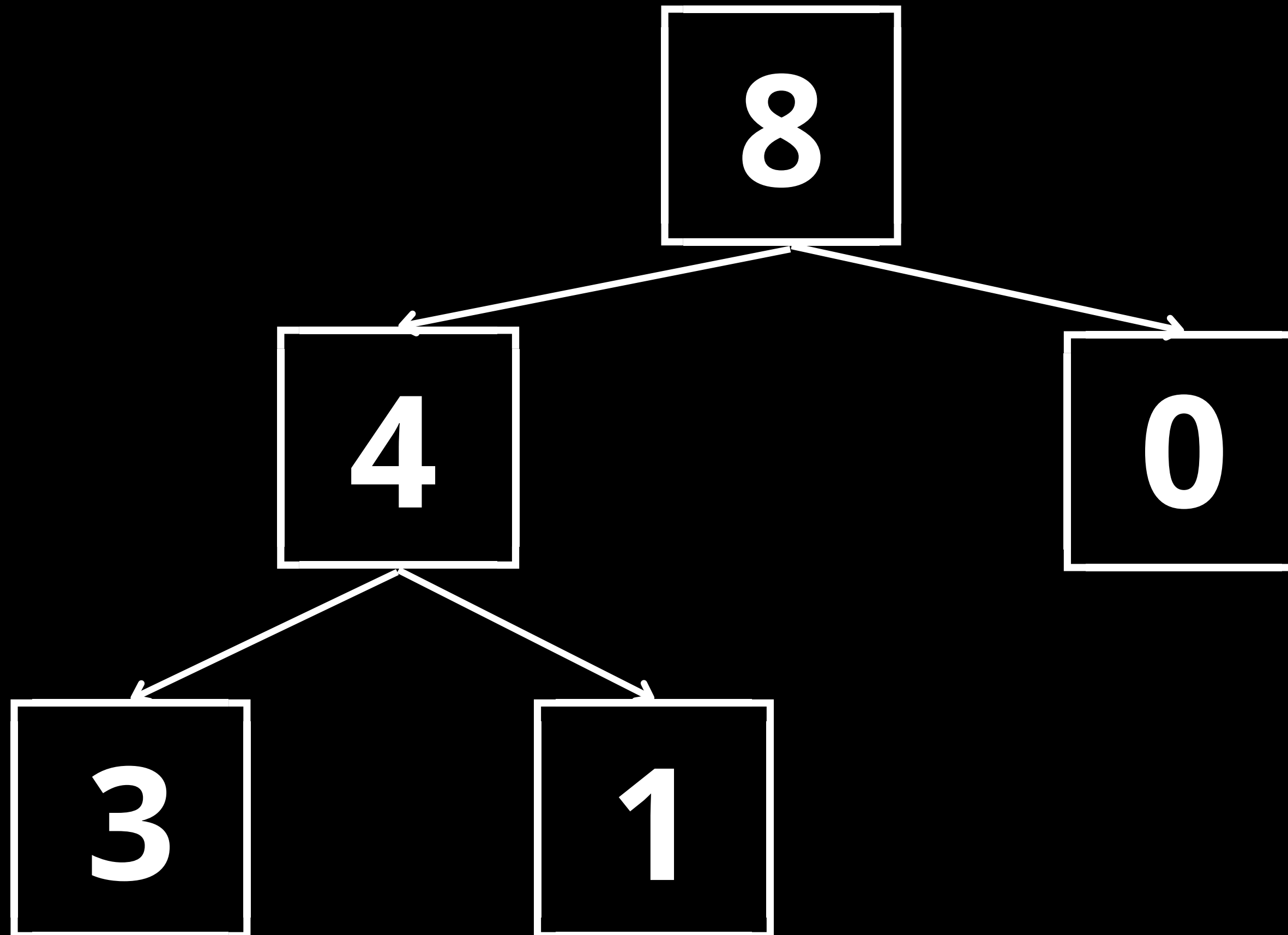
**Now transform it into a Max Heap**



**Now transform it into a Max Heap**



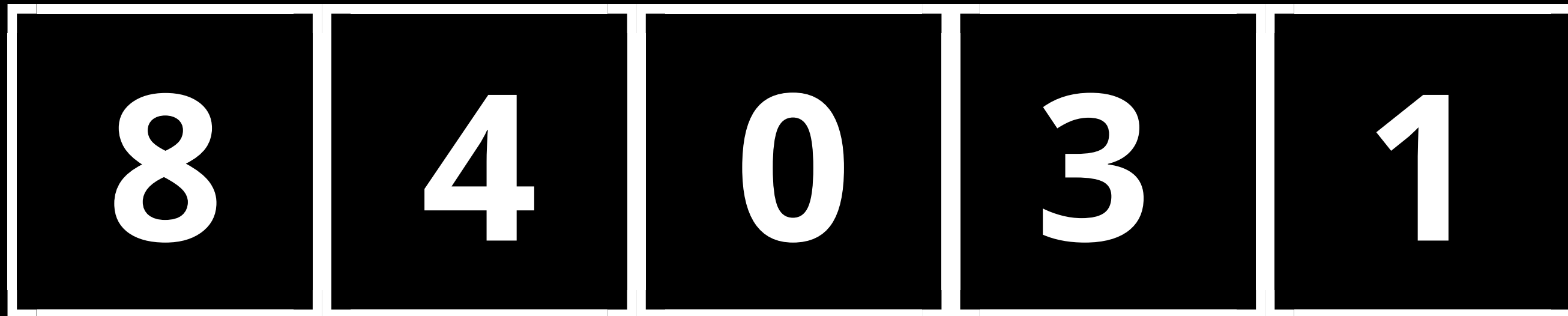
**This is our Max Heap**





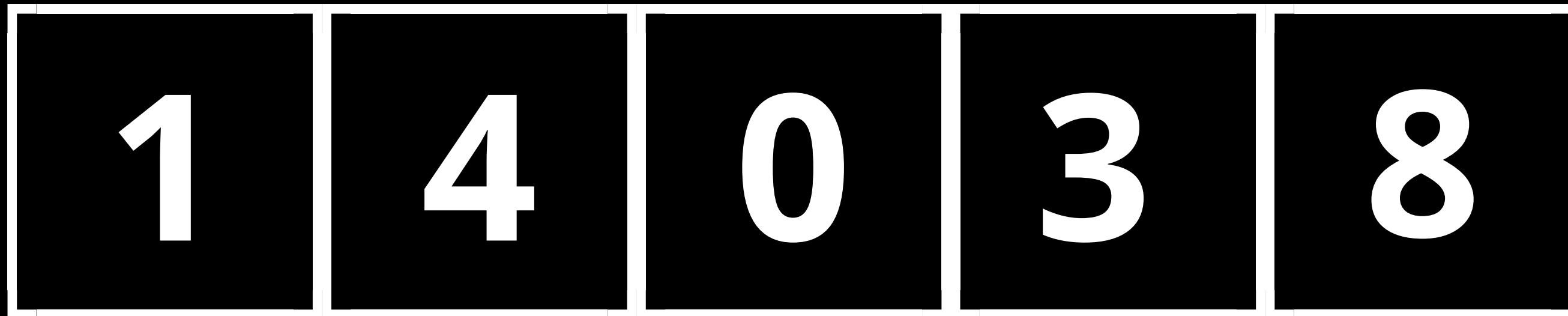
**Now that we have a Max Heap, we can remove the root. To do so, we can simply swap it with the last current element in the array, and re-generate a Max Heap from the remaining elements up to size-1;**

**Current Array:**



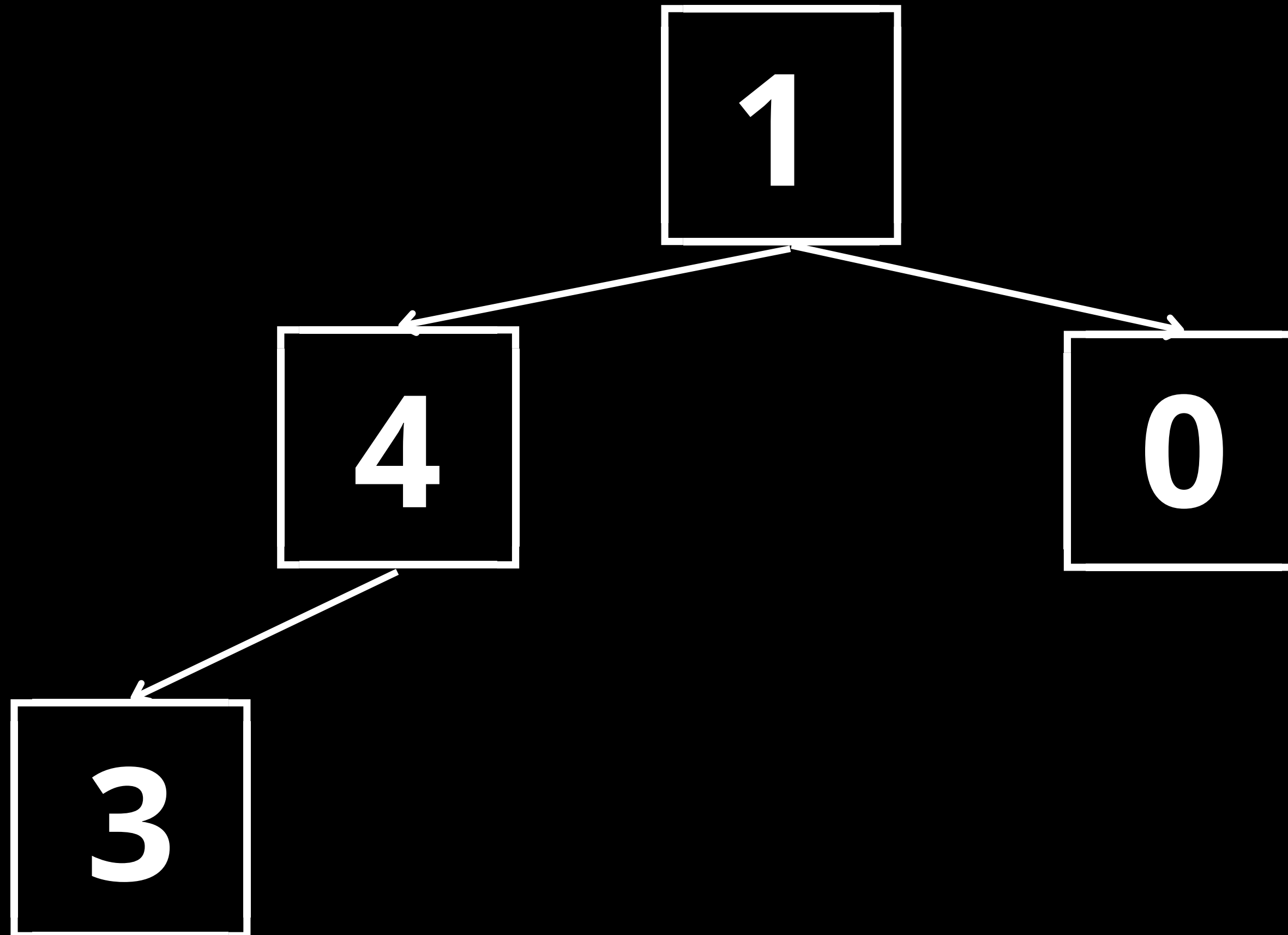
**Now that we have removed the root, we  
can regenerate our Max Heap from  
indexes 0 to size-1**

**Current Array:**

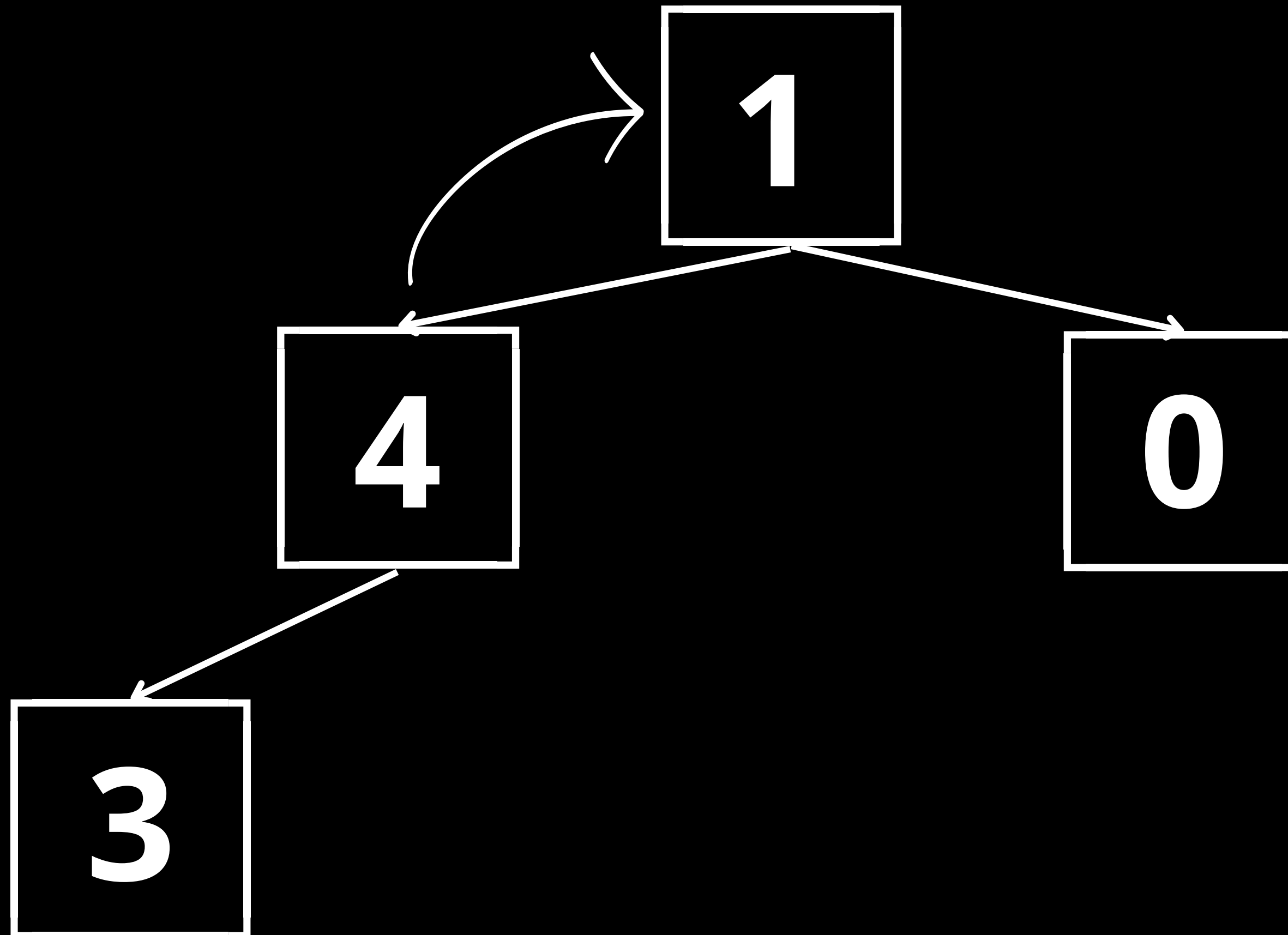


**Ignore this last index on  
next Max Heap iteration**

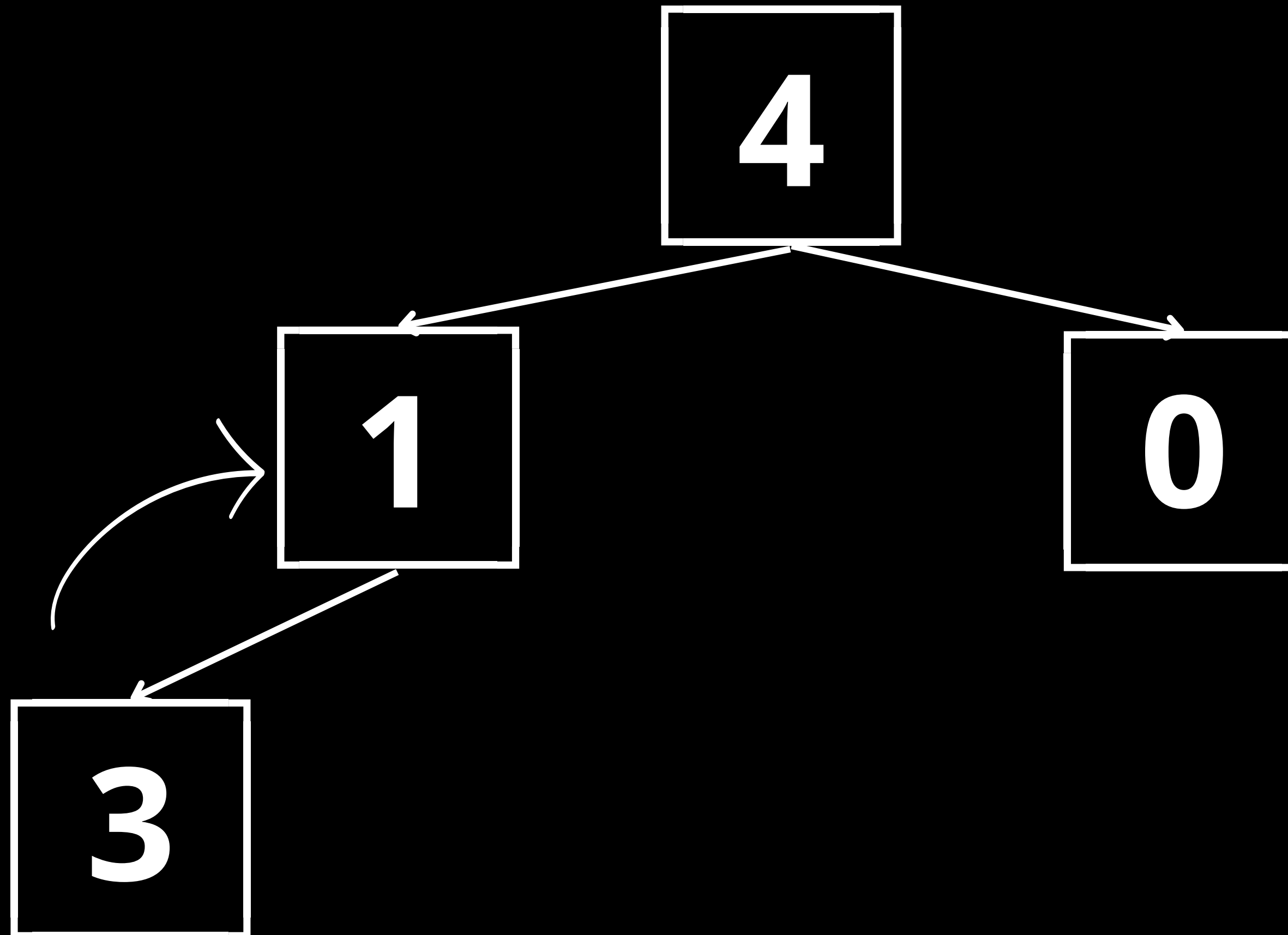
**Next Binary Tree is:**



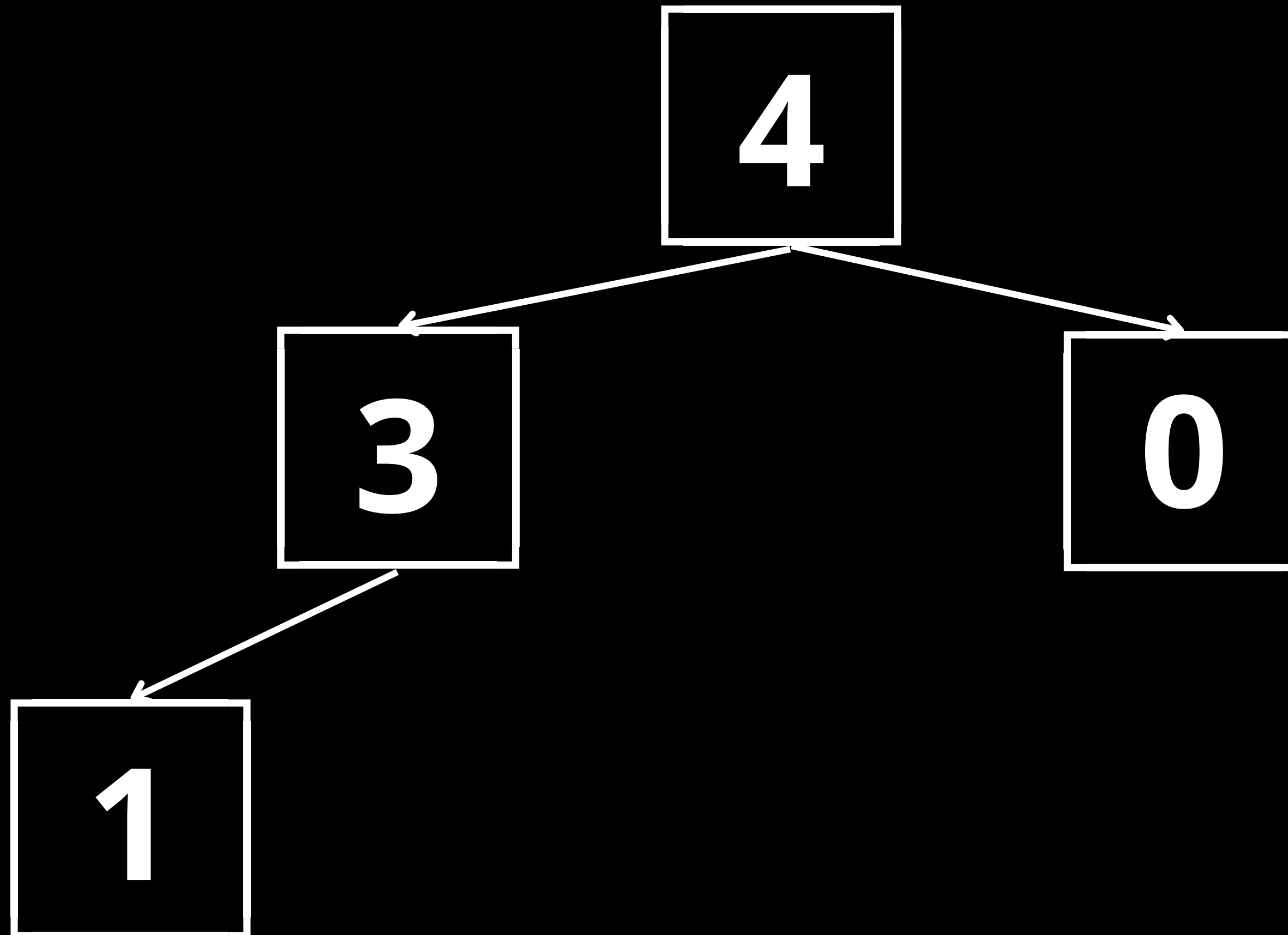
**Now transform it into a Max Heap**



**Now transform it into a Max Heap**

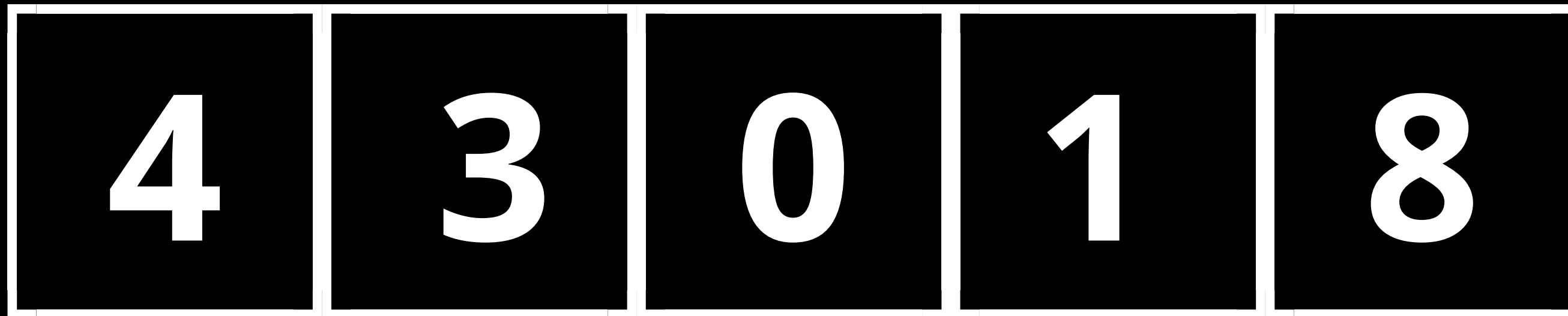


**This is our new Max Heap**



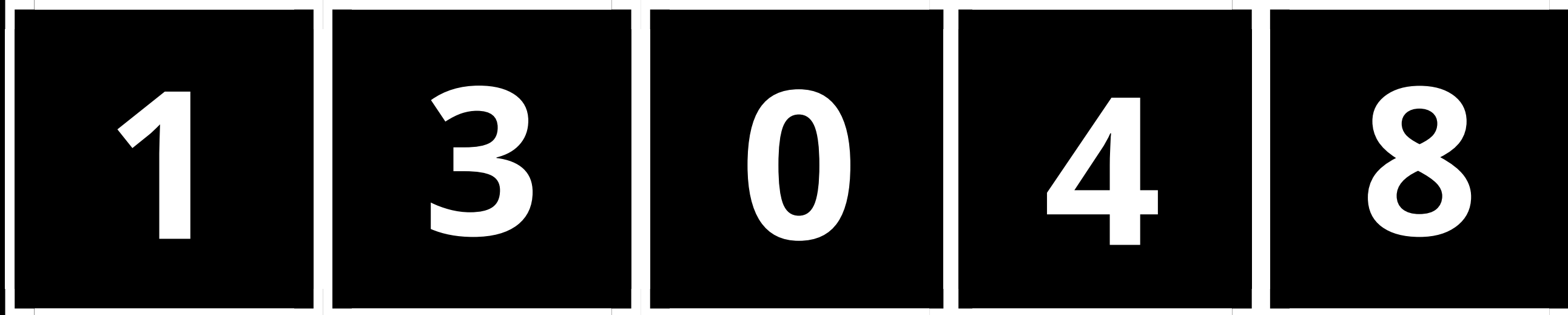
**Now that we have a Max Heap, we can remove the root. To do so, we can simply swap it with the last current element in the array, and re-generate a Max Heap from the remaining elements up to size-2;**

**Current Array:**



**Now that we have removed the root, we  
can regenerate our Max Heap from  
indexes 0 to size-2**

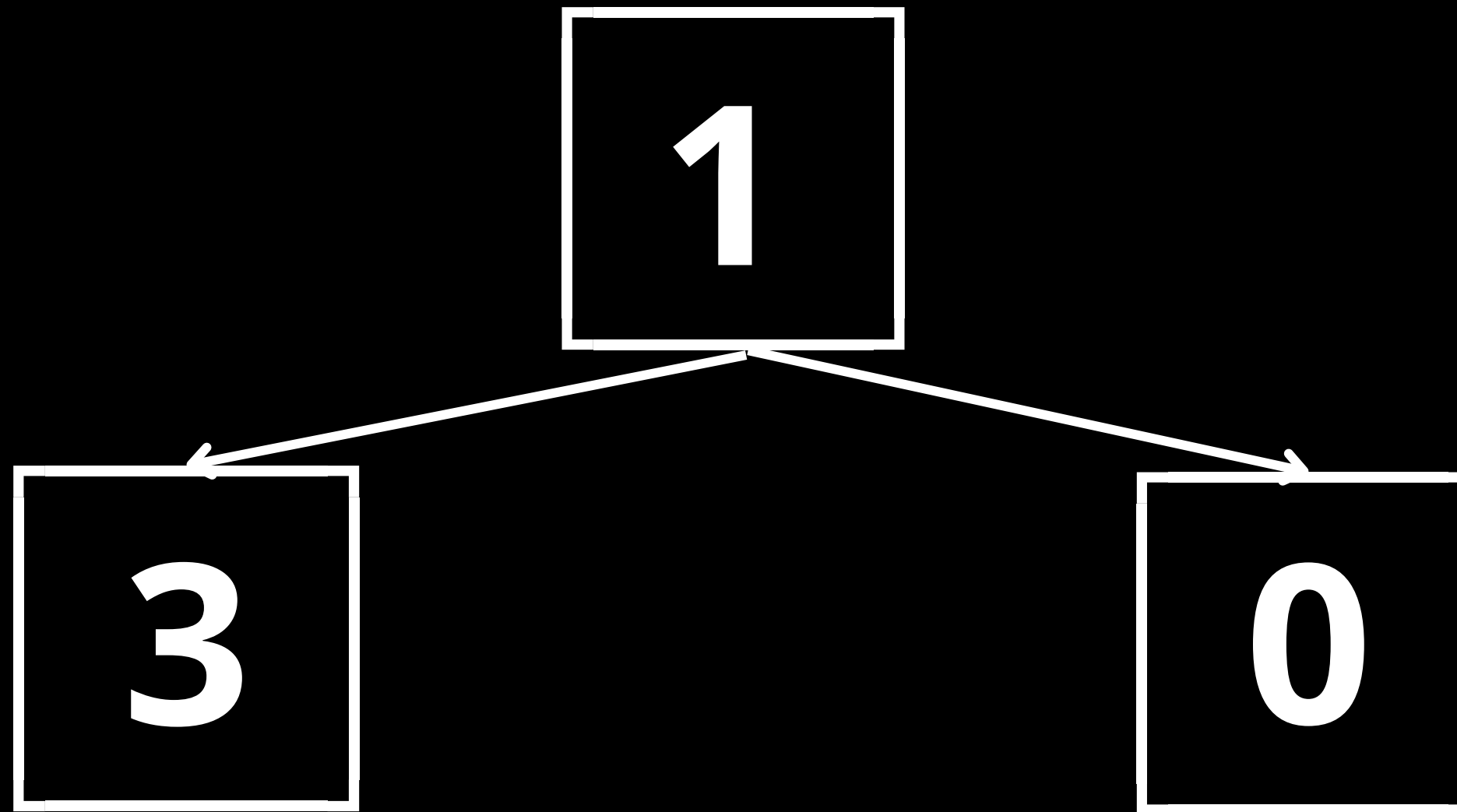
**Current Array:**



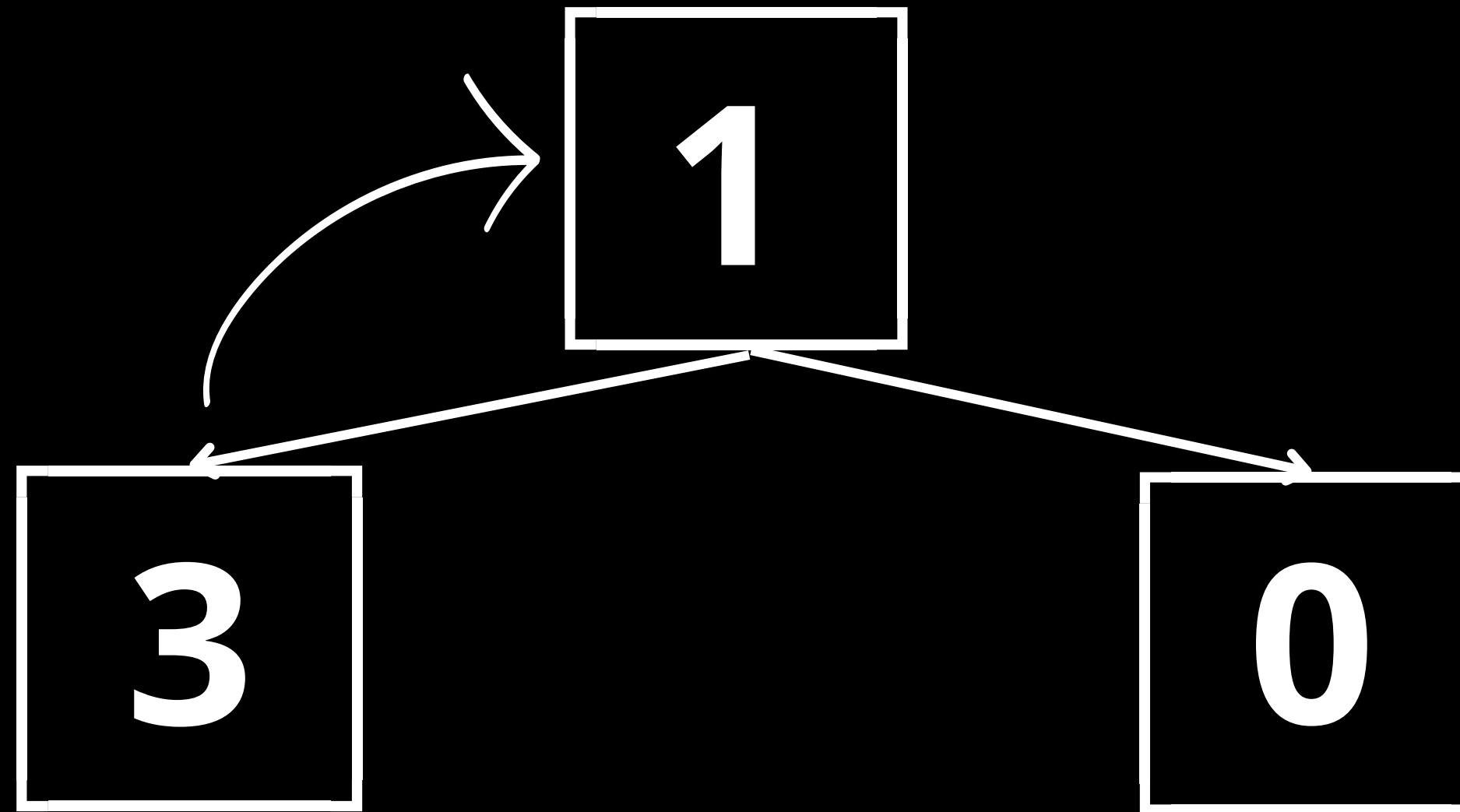
**Ignore up to this index on  
next Max Heap iteration**



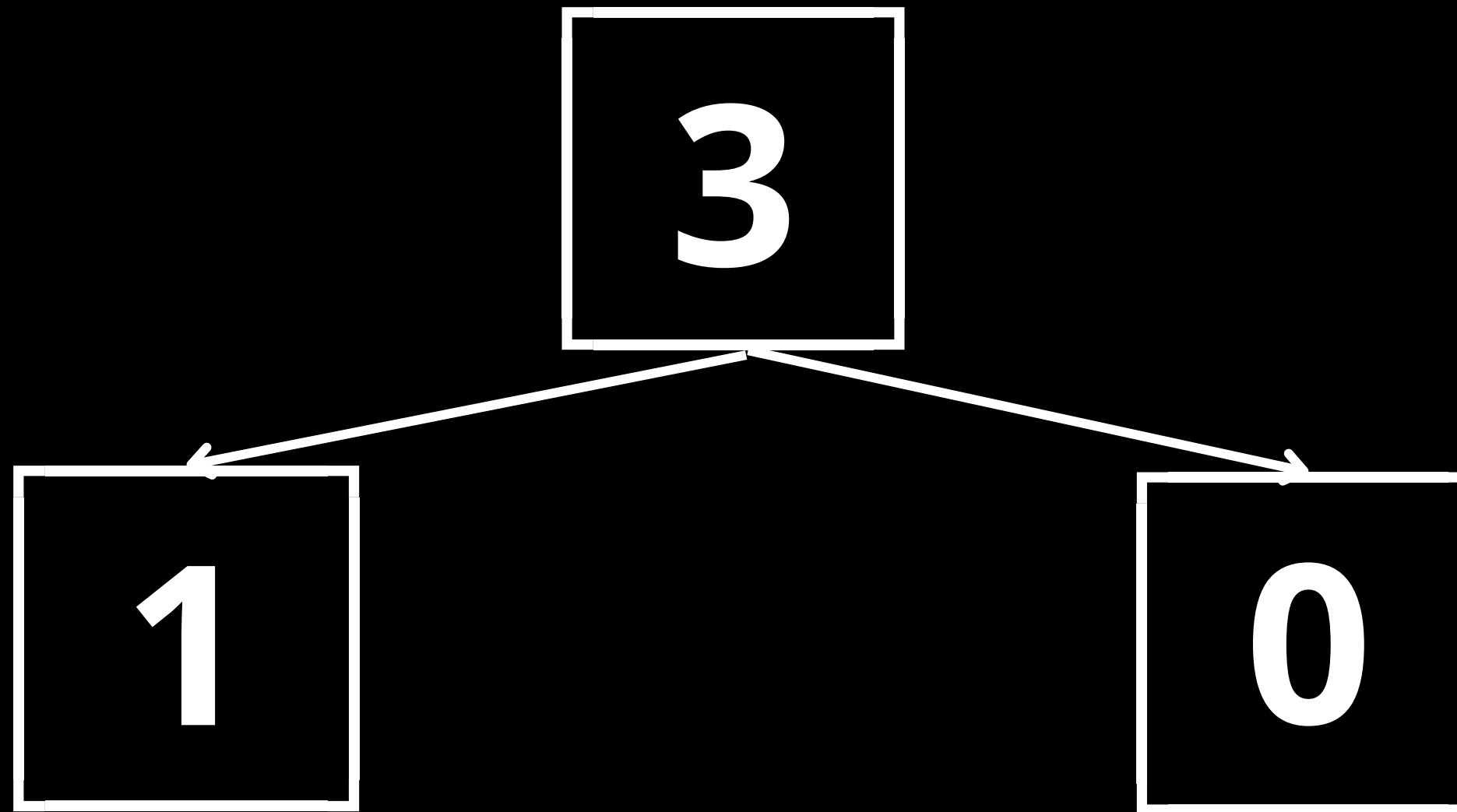
**Next Binary Tree is:**



**Now transform it into a Max Heap**

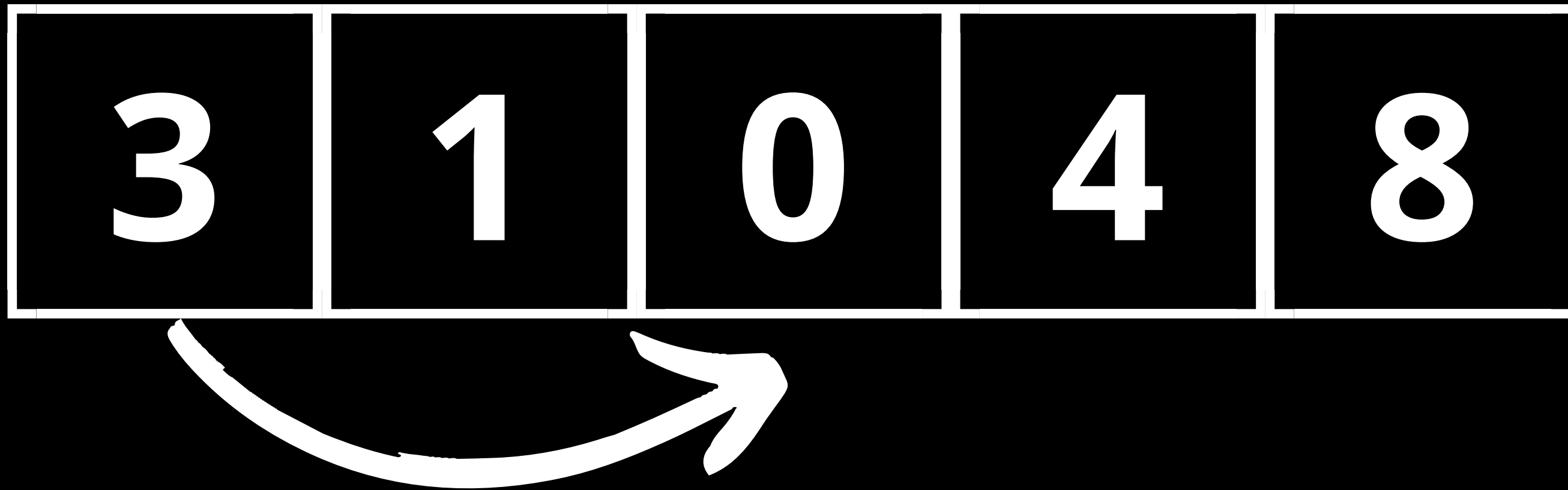


**This is our new Max Heap**



**Now that we have a Max Heap, we can remove the root. To do so, we can simply swap it with the last current element in the array, and re-generate a Max Heap from the remaining elements up to size-3;**

**Current Array:**



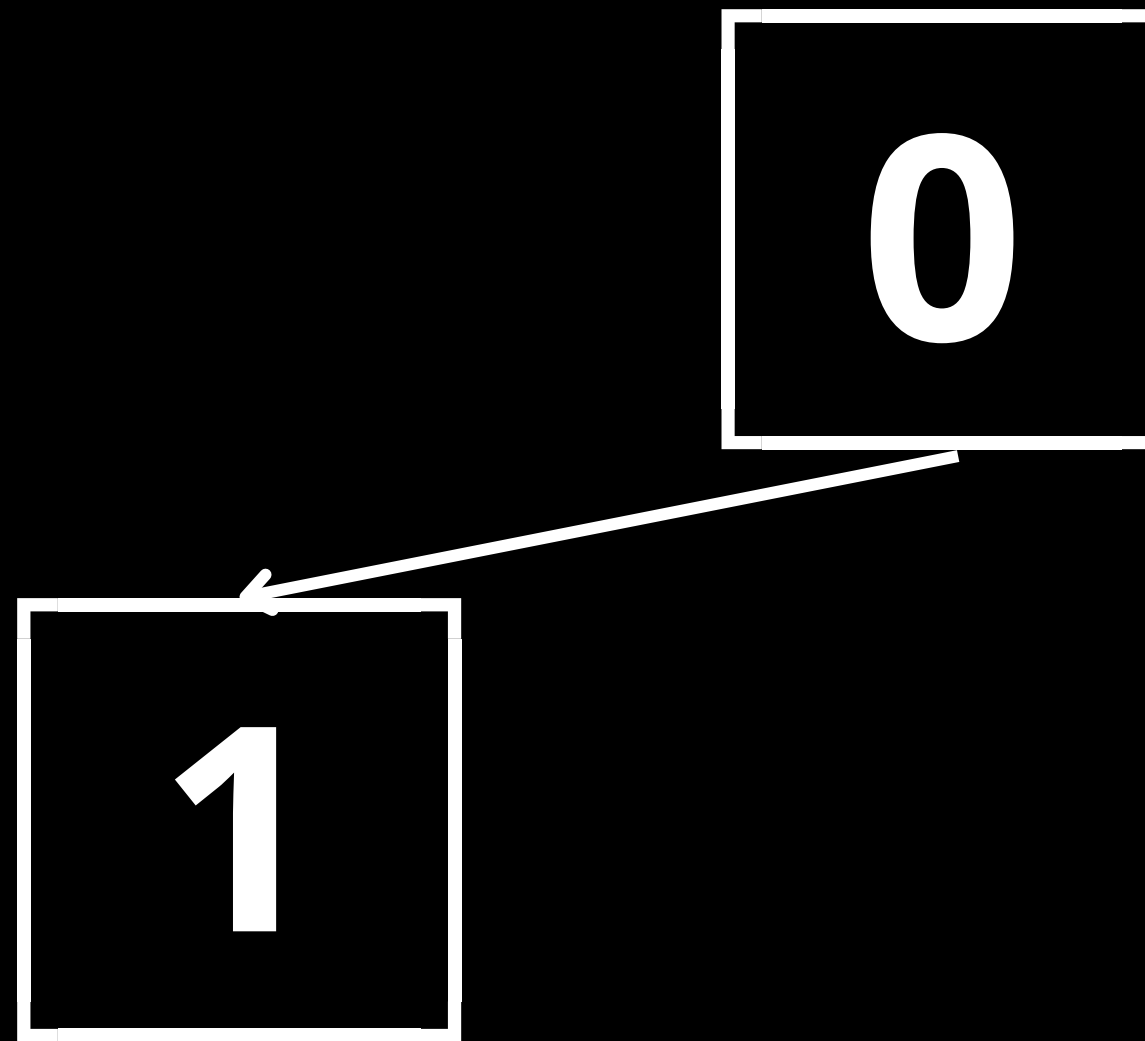
**Now that we have removed the root, we  
can regenerate our Max Heap from  
indexes 0 to size-3**

**Current Array:**

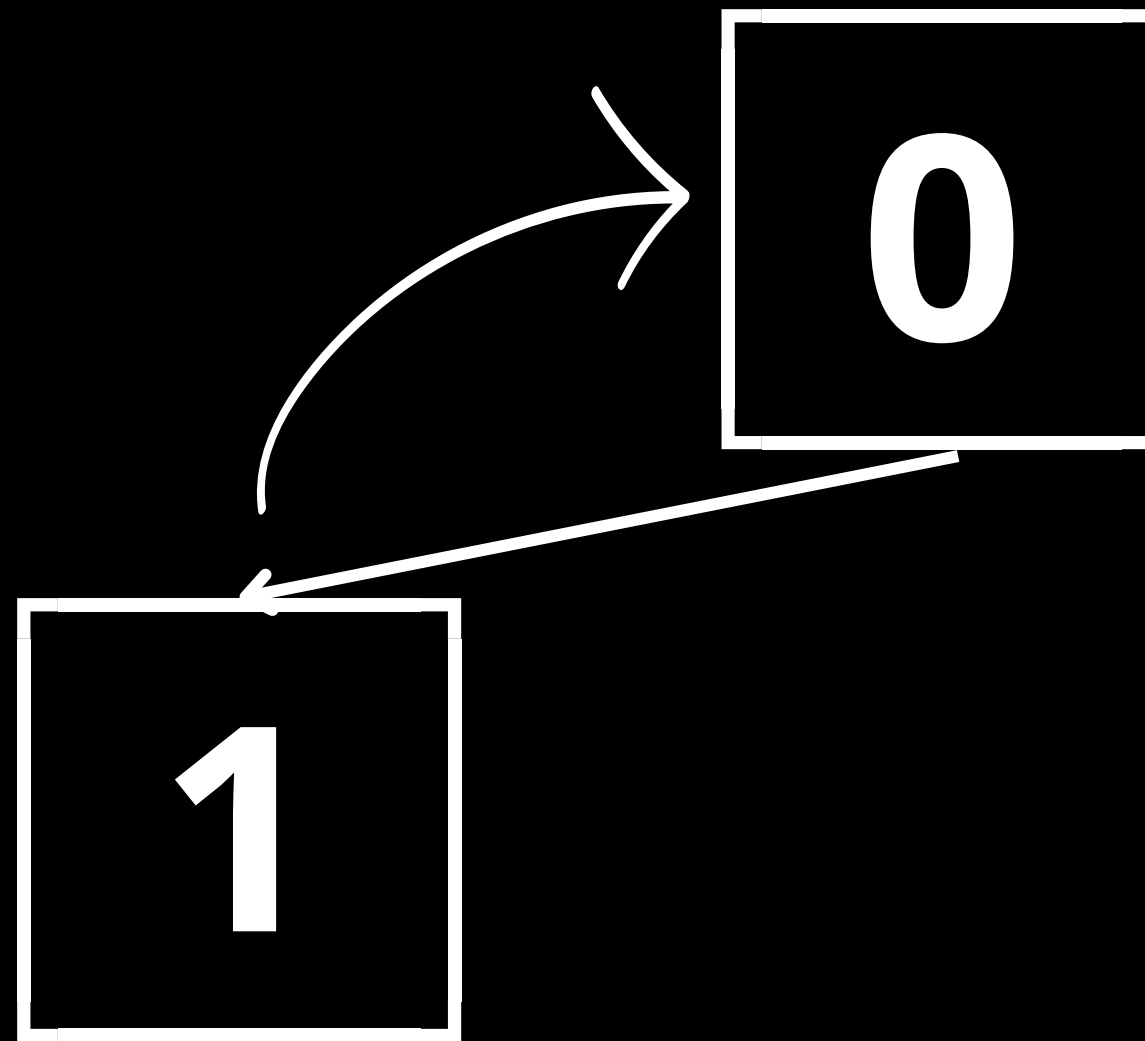


**Ignore up to this index on  
next Max Heap iteration**

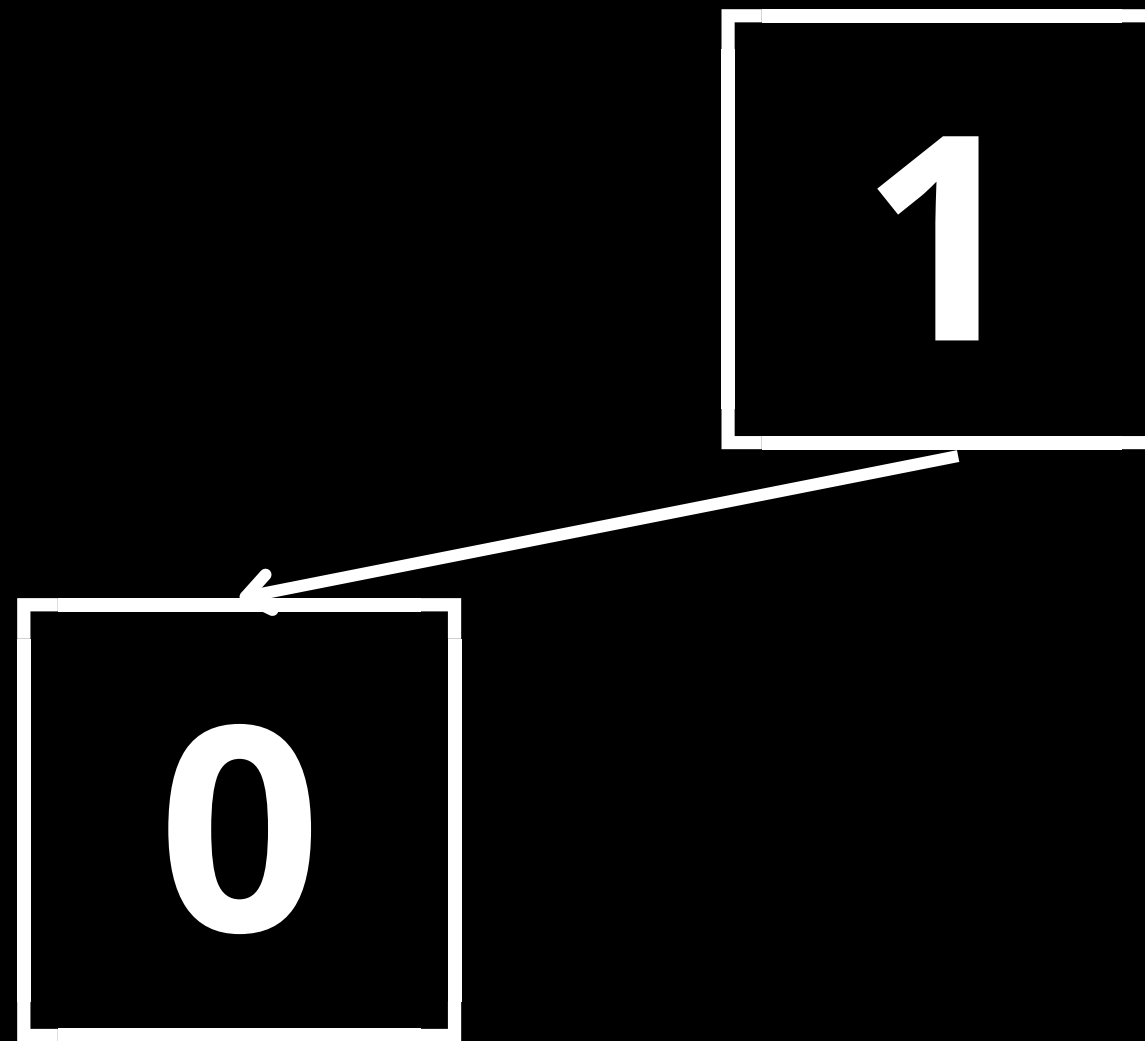
**Next Binary Tree is:**



**Now transform it into a Max Heap**



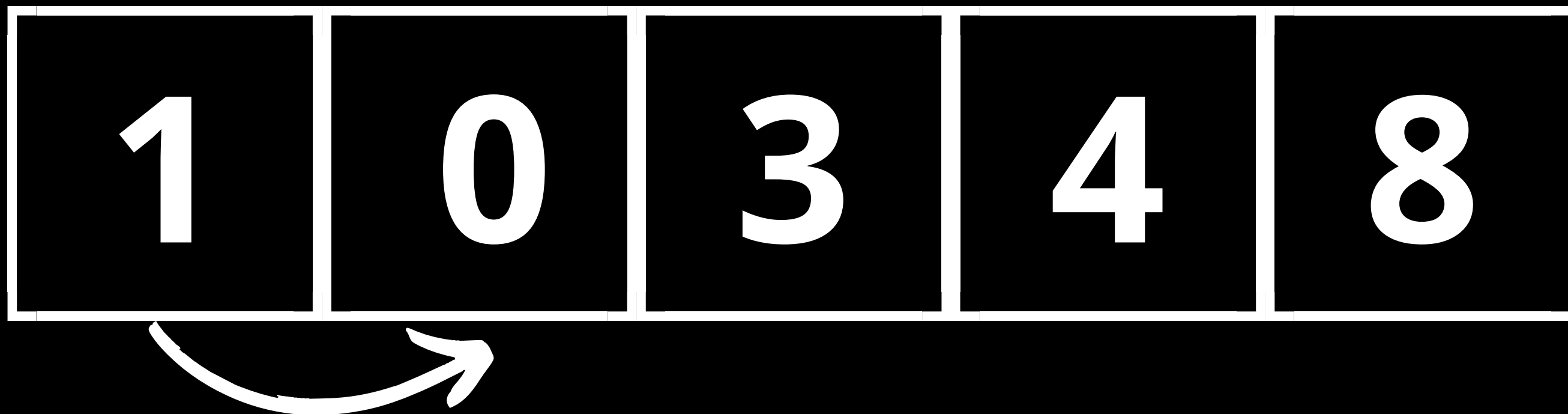
**This is our new Max Heap**





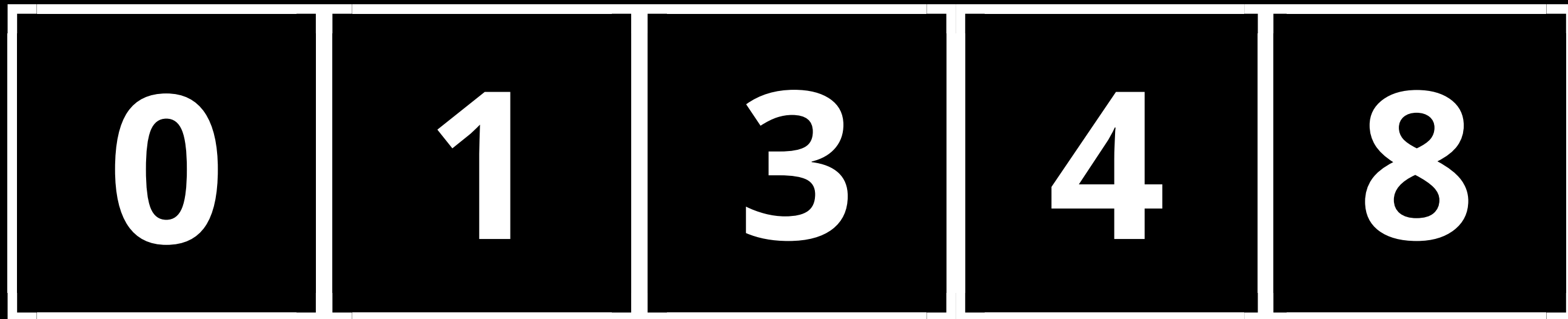
**Now that we have a Max Heap, we can remove the root. To do so, we can simply swap it with the last current element in the array, and re-generate a Max Heap from the remaining elements up to size-4;**

**Current Array:**



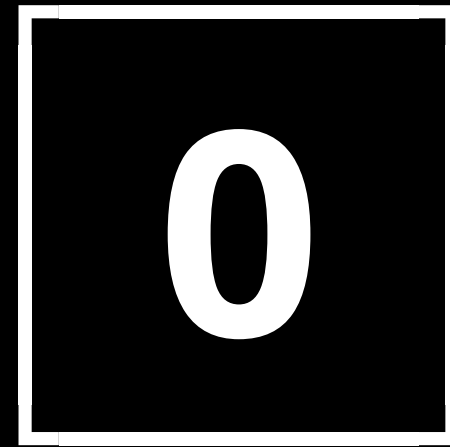
**Now that we have removed the root, we  
can regenerate our Max Heap from  
indexes 0 to size-4**

**Current Array:**



**Ignore up to this index on  
next Max Heap iteration**

**Next Binary Tree is:**



**As there is only one element left  
on the tree, it's already a Max  
Heap and it's already in it's  
correct position**

# Sorted Array

0

1

3

4

8