

Search Algorithms

Binary Search

Time Complexity

Best Case:

$O(1)$

Average and Worst Case:

$O(\text{Log}N)$

Space Complexity

Iterative Approach:

**No additional space required
(In-place algorithm)**

$O(1)$

Recursive Approach:

$O(N)$

Array

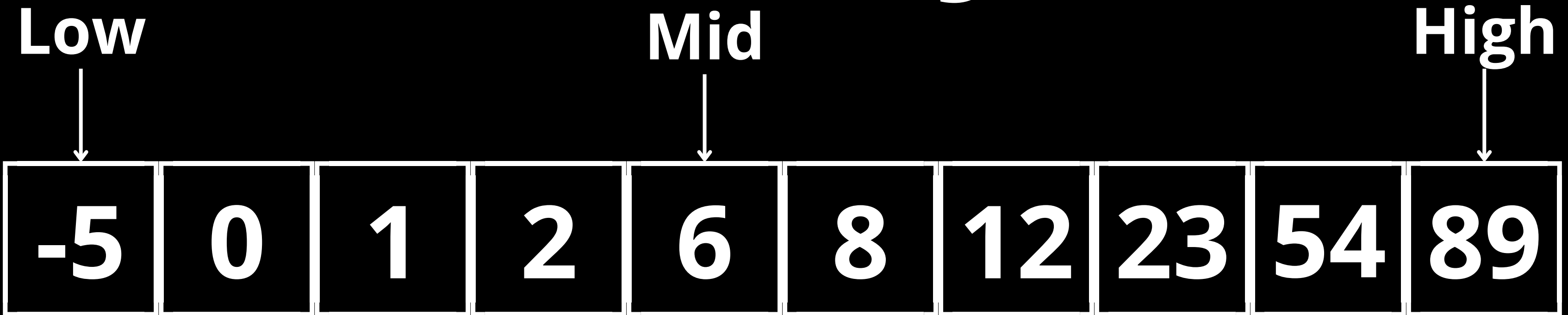
-5	0	1	2	6	8	12	23	54	89
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Value to look for: 54

Steps to find the value:

- Find the lowest and highest index of the array
- Find the middle index of the array: $(\text{low} + \text{high}) / 2$
- Check if the middle index element is the searched one
- If so, return the index, if not, check if its smaller or greater than the searched element
- If smaller, do a binary search on the upper half, if greater, do a binary search on the lower half

Array



Lowest index: 0


Biggest index: 9

Middle index: $(0+9)/2 = \text{floor}(4.5) = 4$

Array

Index 4

-5	0	1	2	6	8	12	23	54	89
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Is 6 equal to 54? No!

Is 6 smaller than 54? Yes!

Search on the upper half

Array

Low

Mid

High



-5	0	1	2	6	8	12	23	54	89
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Lowest index: $\text{mid}+1 = 5$


Biggest index: 9

Middle index: $(5+9)/2 = \text{floor}(7) = 7$

Array

Index 7

-5	0	1	2	6	8	12	23	54	89
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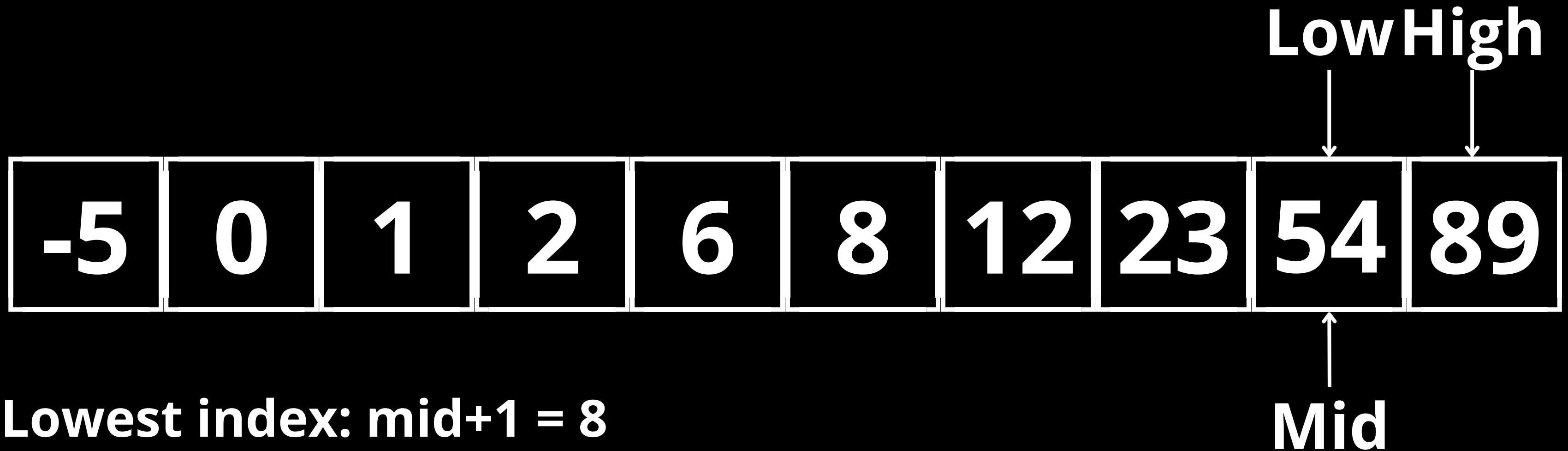


Is 23 equal to 54? No!

Is 23 smaller than 54? Yes!

Search on the upper half

Array



Lowest index: $\text{mid} + 1 = 8$

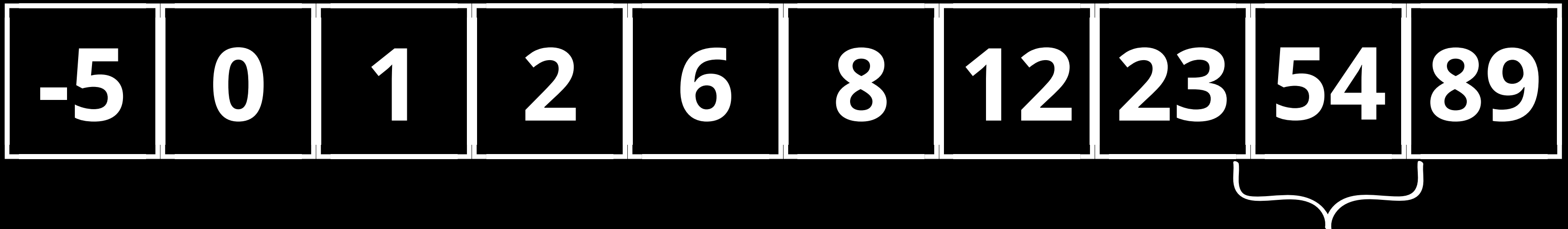
Biggest index: 9

Middle index: $(8 + 9) / 2 = \text{floor}(8.5) = 8$

Array

Index 4

-5	0	1	2	6	8	12	23	54	89
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Is 54 equal to 54? Yes!

Return index 8

Done!