

# CS241 Tutorial 7

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Topics:

- Top-Down Parsing

Definitions:

- LL(1): LEft to right scan of input Left canonical derivation 1 symbol of lookahead
- Top-down Parser: begins at start symbol and finds a derivation for the input string
- An LL(1) grammar is a grammar that can be parsed by an LL(1) Parser

## Predict Function

$\text{Predict}(A, a) = \{A \rightarrow \gamma \mid a \in \text{First}(\gamma) \vee (\gamma \Rightarrow * \epsilon \text{ and } a \in \text{Follow}(A))\}$

$\text{First}(\gamma) = \{b \mid \gamma \Rightarrow b\beta \text{ for some } \beta\}$

$\text{Follow}(A) = \{C \mid S' \Rightarrow * \alpha A c \beta \text{ for some } \alpha, \beta\}$

- A grammar is LL(1) if  $\forall A, a \mid |\text{Predict}(A, a)| \leq 1$

1.  $S' \rightarrow \vdash S \dashv$
2.  $S \rightarrow a X Y b$
3.  $S \rightarrow XY$
4.  $X \rightarrow pX$
5.  $X \rightarrow \epsilon$
6.  $Y \rightarrow q$
7.  $Y \rightarrow \epsilon$

## 1) Create Predict Table

$$\text{First}(\vdash S \neg) = \{\vdash\}$$

$$\text{First}(aXYb) = \{a\}$$

$$\text{First}(XY) = \{p, q\}$$

$$\text{First}(pX) = \{p\}$$

$$\text{First}(\epsilon) = \{\}$$

$$\text{First}(q) = \{q\}$$

$$\text{Follow}(S') = \{\}$$

$$\text{Follow}(S) = \{\neg\}$$

$$\text{Follow}(X) = \{b, \neg, q\}$$

$$\text{Follow}(Y) = \{b, \text{dashv}\}$$

	$\vdash$	a	b	p	q	$\neg$
S'	1					
S		2		3	3	3
X			5	4	5	5
Y			7		6	7

## 2) Parsing Example

Action	Consumed Input	$\cdot_{Top}Stack_{Bot}$	Remaining Input
Initialize	$\epsilon$	S'	$\vdash \text{appqb} \neg$
Expand 1	$\epsilon$	$\vdash S \neg$	$\vdash \text{appqb} \neg$
Match $\vdash$	$\vdash$	S $\neg$	$\text{appqb} \neg$
Expand 2	$\vdash$	aXYb $\neg$	$\text{appqb} \neg$
...			