



MAKE
SCHOOL

HASH TABLES

The Ultimate Data Structure

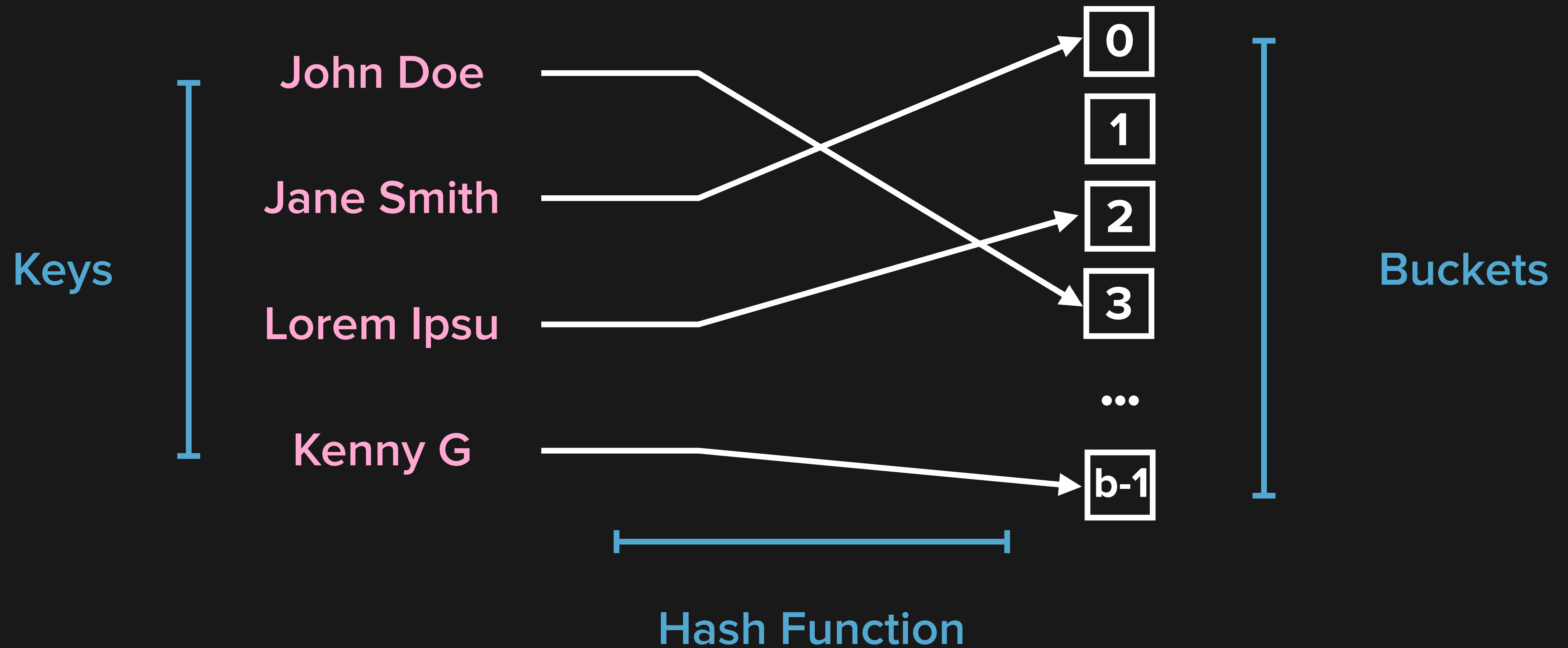
HASH TABLES

Maps keys → values (any objects)

Python's `dict()` / `{}` type is a hash table

Used because of strong average case performance (time complexity)

HASH TABLES



HASH FUNCTIONS

Converts a variable-size input (key) to a fixed-size integer output (hash code)

Same input → same output

Input can be many types: number (int or float), string, or immutable collection

John Doe → **512340**

Jane Smith → **408749**

Lorem Ipsu → **943275**

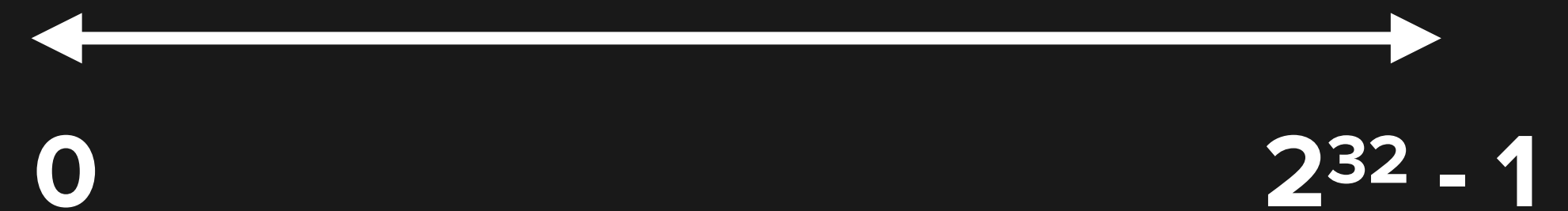
John Doe → **512340**

IDEAL HASH FUNCTION*

Repeatable

Fast

Output is unsigned integer



Arbitrarily distributes keys
among output space

Small differences in input result
in large differences in output

**Different for cryptographic hash functions*

STRING HASHING

Strings are sequences of characters

Characters have numerical values (ASCII codes)

Calculate a string's hash code by adding up all characters' ASCII codes ("Lose Lose" algorithm)

Note that `hash("dog") == hash("god")`

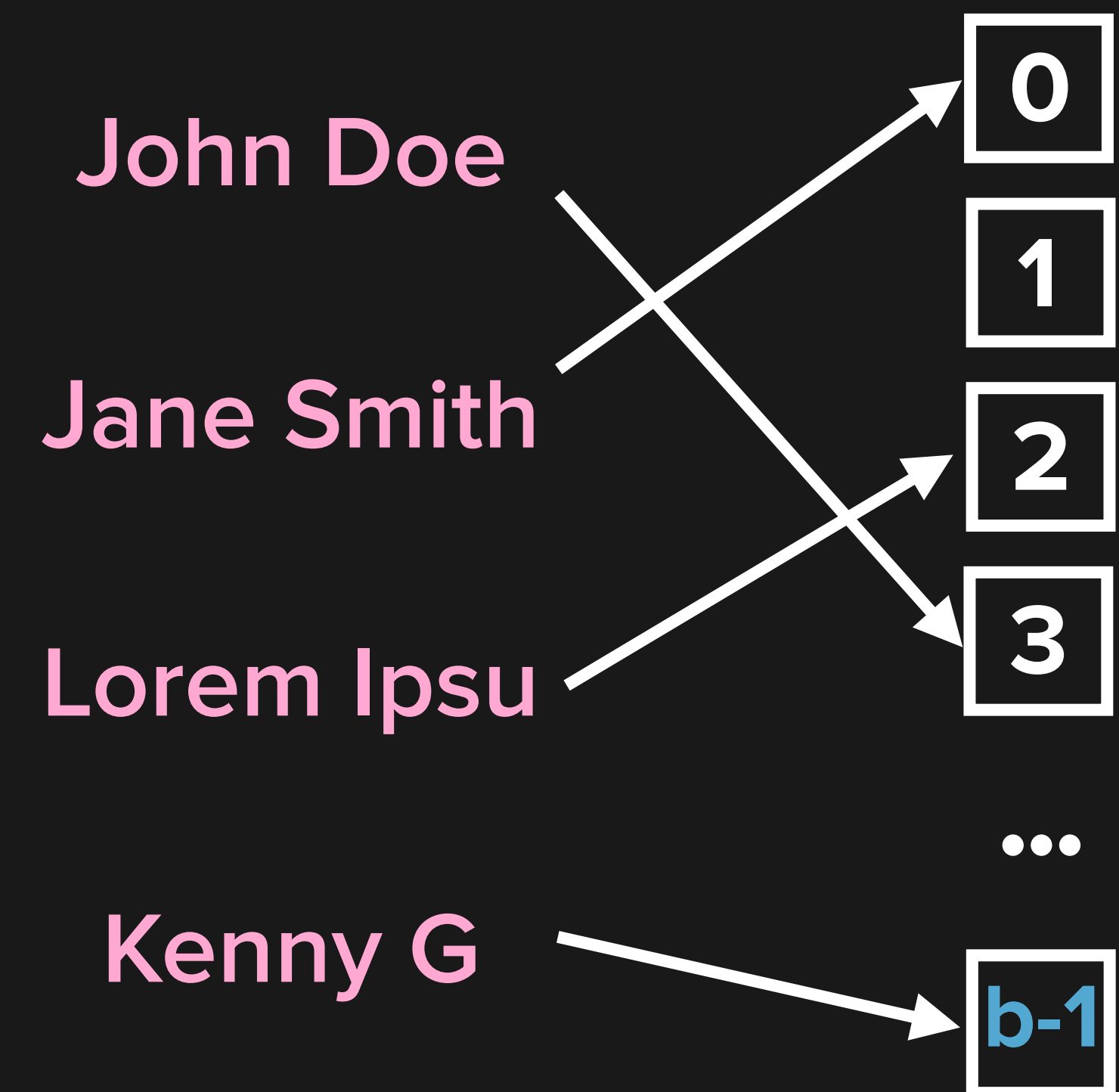
WHICH BUCKET?

Hash codes are very large integers,
but we want the index of a bucket

We can use the modulus operator %

$\text{index} = \text{hash}(\text{key}) \% \text{buckets}$

index ranges from 0 to $\text{buckets}-1$



HASH COLLISIONS

It is impossible to map all possible inputs to a fixed output space without some inputs generating the same output (hash code)

Different inputs (keys) generating the same output (hash code) is called a *hash collision*

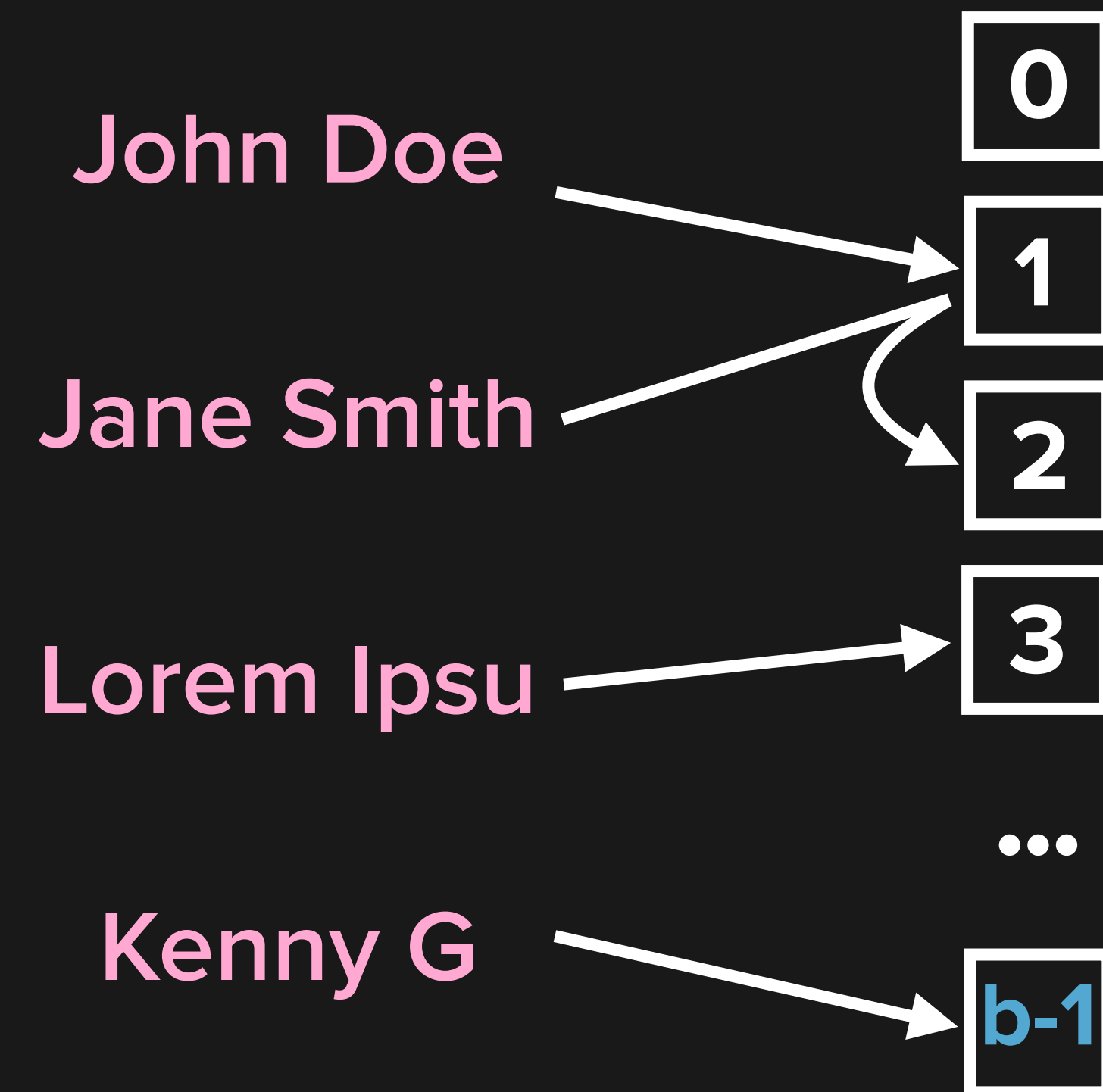
LINEAR PROBING

Each bucket contains at most one entry

On collision - find next open bucket, add entry there

To retrieve - find bucket, if that's not entry, try next bucket until you find entry or empty bucket

Python's **dict** uses probing



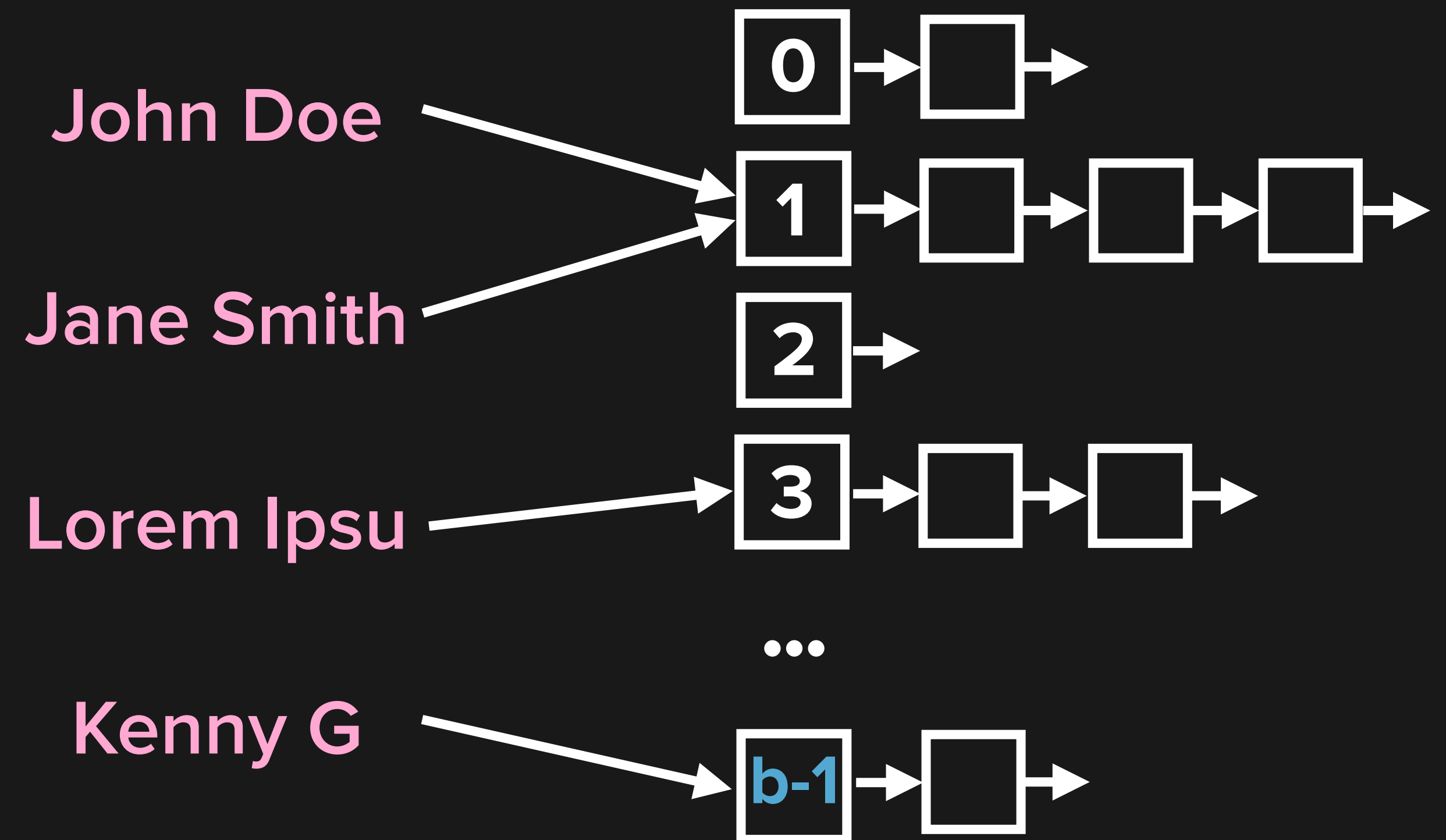
CHAINING

Each bucket contains a linked list of entries

On collision - add to the bucket's linked list

To retrieve - find bucket, find entry in linked list

We will use chaining to implement our hash table



LOAD FACTOR

Load Factor = $\text{entries} / \text{buckets}$

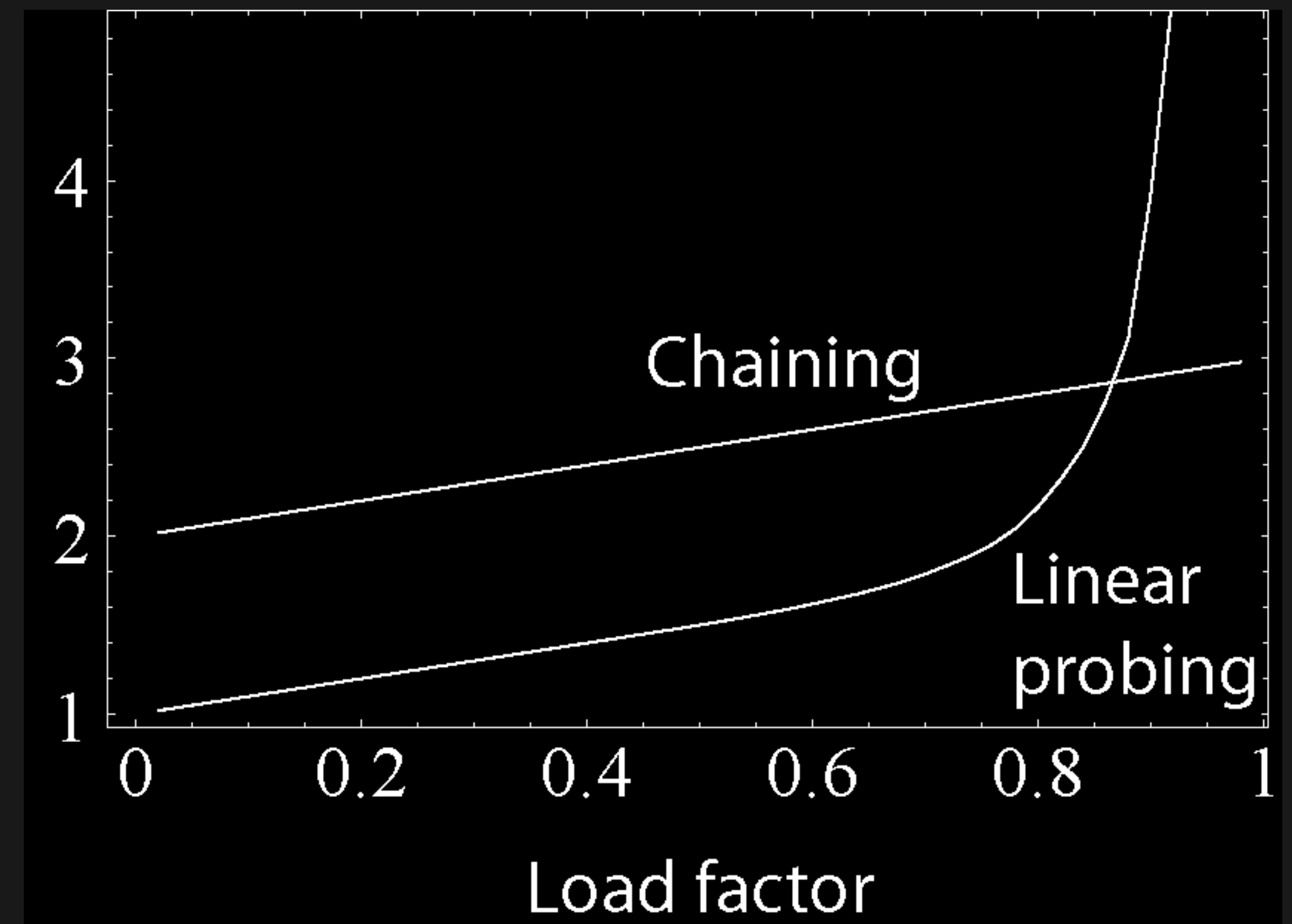
A hash table with 3 key-value entries in 8 buckets has a load factor of $3 / 8 = 0.375$

A hash table with 76 key-value entries in 128 buckets has a load factor of $76 / 128 = 0.59375$

LOAD FACTOR

Load factor affects performance

Collision resolution affects performance



COMPLEXITY ANALYSIS

	Average Case	Worst Case
Space	$O(n)$	$O(n)$
Search	$O(1)$	$O(n)$
Insert	$O(1)$	$O(n)$
Delete	$O(1)$	$O(n)$