

# The Robotarium

## Python Guide

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# 1 The Robotarium

## 1.1 The Robotarium Project

The Robotarium project provides a remotely accessible swarm robotics research and education platform that remains freely accessible to anyone. Currently, robotics research and education requires significant investments in terms of manpower and resources to competitively participate. However, we believe that anyone with new, amazing ideas should be able to see their algorithms deployed on real robots, rather than purely simulated. In order to make this vision a reality, the Robotarium team has created a remote-access, robotics lab where anyone can upload and test their ideas on real robotic hardware.

## 1.2 How to Use the Robotarium Simulator

To execute your experiments on the Robotarium robots, download one of the simulators, prototype your code in simulation, and submit the exact same code for execution on actual robots through the [Robotarium's web](#) interface. You can get started right away using the Robotarium simulator provided [here](#). A set of well-documented examples (that are also part of the provided simulators) will help you get started immediately. In a nutshell, completing the following three steps is all that is required to run your experiment on the Robotarium:

1. Download the Robotarium's [MATLAB](#) or [Python](#) simulator. (For the Robotarium MATLAB's guide please click [here](#))
2. Write and verify your script functions correctly in the simulator.
3. Upload your scripts through your account on the Robotarium website.

## 1.3 How to use the Robotarium Hardware

Now that you tried your code in the simulator, if it does not output any potential errors, it is time to try to run your code on real robots!

1. Sign up for a Robotarium account and wait to get approved by one of the Robotarium's admins. This can take 1-2 business days!
2. Create your experiment in the web interface, upload your code, and submit it for execution.

### 1.3.1 Create a Robotarium Account

Creating a Robotarium account can be done in four (4) easy steps :

1. Go to the Robotarium website and navigate to the right corner, click in Sign Up



Figure 1: The landing page of the Robotarium website.

2. Complete the form with your email, password, and confirmation. Then, add your name, city, state, institute, and the reason you want to use the Robotarium. Please do not provide a fake e-mail as this is the way the Robotarium staff and system will contact you about your experiment status. We ask for your demographic information to keep track of *who* is using the Robotarium so it can be better developed to serve its user community. After creating your personal profile, you should see the message in Figure 2b, thanking you for signing up. If you do not receive a confirmation email within a few minutes, make sure to click on the "Resend Verification Link."

(a) Create your log in information by providing an e-mail and creating a password.

(b) Demographic information to complete.

Figure 2: Process to create a Robotarium user account.

3. In your inbox, you should receive a message asking you to verify your account. Click on the link to verify.



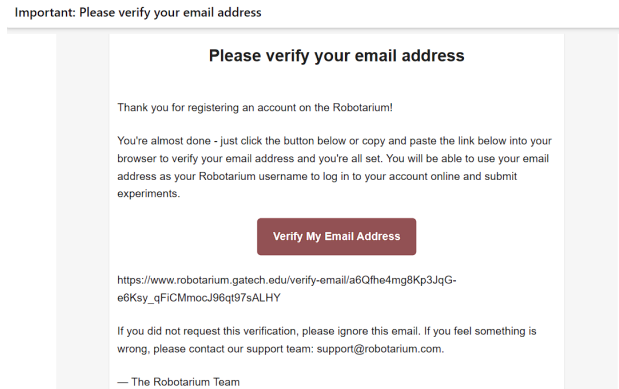


Figure 3: Verification Message

4. Wait for approval by the Robotarium admins (this should take about 1-2 business days) and then you will be able to submit code to the Robotarium using your personal user account!

### 1.3.2 Submit Code to Robotarium

After you have created a user account for the Robotarium and it has been approved, you can now submit code to the Robotarium whenever you want for it to be run on real robots. The submission steps are:

1. When you navigate to the dashboard, you will see the “Pending Experiments” and “Completed Experiments” tabs. If you have not run anything, it will look like [Figure 4](#)

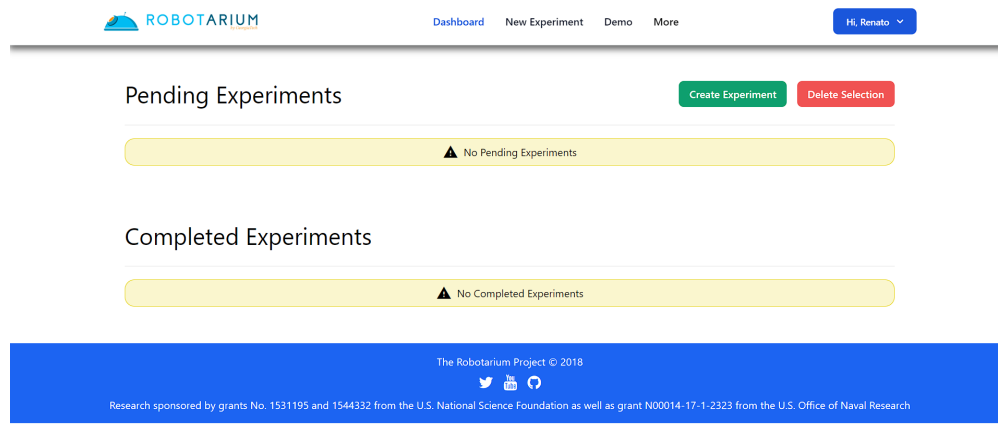


Figure 4: Dashboard

- Click on the “Create Experiment” button. We will be submitting a file called “experiment.py” as an experiment to run on the Robotarium. You should see the “Define Your Experiment!” (Figure 5) heading at the top of the page. On this page, you will provide an experiment title, experiment description, estimated experiment duration, and number of robots you will need. Again, this information is used to understand what our users are deploying on the Robotarium to inform its development directions. Note, if the submitted experiment takes longer than your estimated duration to execute, we will still generate the video and you can view if there were any issues that occurred.

**DEFINE YOUR EXPERIMENT!**

This page allows you to describe the parameters of your experiment. These parameters enable the automated execution and management of experiments on the Robotarium and will be used in the future to automatically generate scripts that can be used with the Robotarium Matlab simulator. Don't forget to save your experiment description for later use!

Load Experiment

**EXPERIMENT DESCRIPTION**

Title

Estimated Duration (seconds) (max: 900)

Figure 5: Define your Experiment

- After you have defined your experiment, upload the associated experiment file(s). Note, do not upload any of the Robotarium files you downloaded with the simulator, only custom ones you have created. If your program required more than one file, please make sure you include all necessary files. For a single file or multiple files, indicate which is the “main” file by clicking the box next to it as shown in Figure 6.
- Once you are satisfied with the files you have included and the experiment description, click the green “Submit Experiment” button to submit the experiment. You also have the option to save the experiment and submit it for later and to download the .json file of the simulator parameters based on your input. When you have submitted the experiment, the dashboard should show your experiment in the “Pending Experiments” section, with the “Status” as “submitted” (Figure 7)

**EXPERIMENT FILES**

Allowed File Extensions: .m, .jpg, .jpeg, .png, .gif, .tiff, .bmp, .py, .mat, .npy

Drop Files or Click to Browse Files

Main File	File Name	Status	View	Download	Remove
<input checked="" type="checkbox"/>	experiment.py	✓			

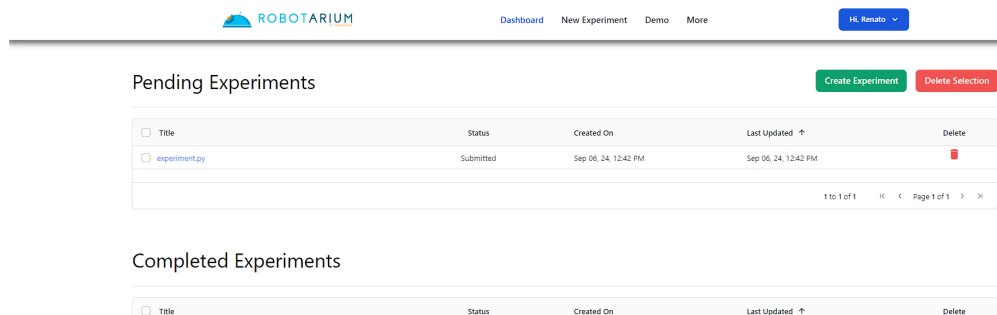
1 to 1 of 1 < > Page 1 of 1 >

Save Experiment Clear All Submit Experiment

The Robotarium Project © 2018

Figure 6: Submission of Experiment

- Experiments take between 10 minutes and 2 days to execute, depending on the use traffic of the Robotarium. During that time, your experiment will be in the "Pending Experiment" dashboard as shown in Figure 7. You will get an email when your experiment has completed or if any issues were detected with the submission.

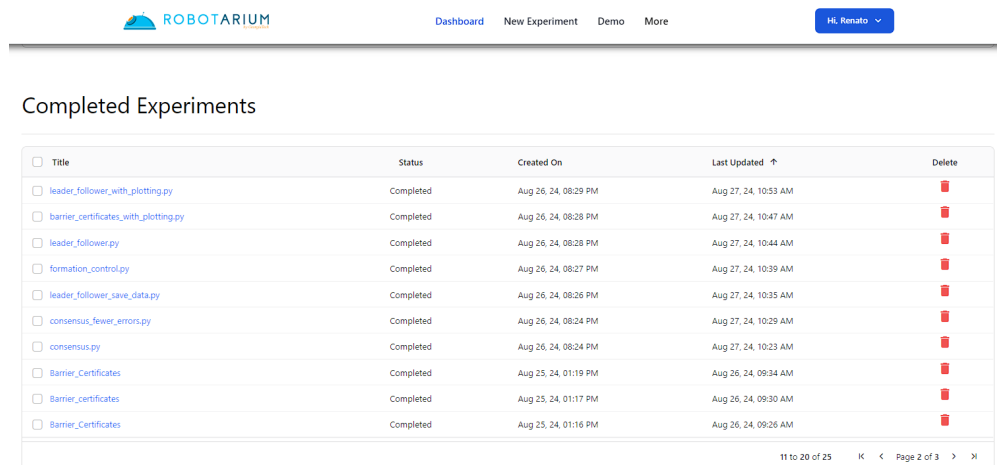


<input type="checkbox"/> Title	Status	Created On	Last Updated ↑	Delete
<a href="#">experiment.py</a>	Submitted	Sep 06, 24, 12:42 PM	Sep 06, 24, 12:42 PM	

1 to 1 of 1    <    >    Page 1 of 1    > >

Figure 7: Pending Experiment

- Once your experiment has been executed, you can view it in the "Completed Experiments" dashboard (Figure 8). By selecting the desired experiment, you will be taken to the results page, where you can find details such as the Experiment Settings, Experiment Video, Scripts, Return Messages, Data Files, and Log Files as shown in Figure 9.



<input type="checkbox"/> Title	Status	Created On	Last Updated ↑	Delete
<a href="#">leader_follower_with_plotting.py</a>	Completed	Aug 26, 24, 08:29 PM	Aug 27, 24, 10:53 AM	
<a href="#">barrier_certificates_with_plotting.py</a>	Completed	Aug 26, 24, 08:28 PM	Aug 27, 24, 10:47 AM	
<a href="#">leader_follower.py</a>	Completed	Aug 26, 24, 08:28 PM	Aug 27, 24, 10:44 AM	
<a href="#">formation_control.py</a>	Completed	Aug 26, 24, 08:27 PM	Aug 27, 24, 10:39 AM	
<a href="#">leader_follower_save_data.py</a>	Completed	Aug 26, 24, 08:26 PM	Aug 27, 24, 10:35 AM	
<a href="#">consensus_fewer_errors.py</a>	Completed	Aug 26, 24, 08:24 PM	Aug 27, 24, 10:29 AM	
<a href="#">consensus.py</a>	Completed	Aug 26, 24, 08:24 PM	Aug 27, 24, 10:23 AM	
<a href="#">Barrier_Certificates</a>	Completed	Aug 25, 24, 01:19 PM	Aug 26, 24, 09:34 AM	
<a href="#">Barrier_certificates</a>	Completed	Aug 25, 24, 01:17 PM	Aug 26, 24, 09:30 AM	
<a href="#">Barrier_Certificates</a>	Completed	Aug 25, 24, 01:16 PM	Aug 26, 24, 09:26 AM	

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Figure 8: Completed Experiment

## Experiment Setting

Created On	Tue, 27 Aug 2024 00:26:06 GMT
Last Updated	Tue, 27 Aug 2024 14:35:59 GMT
Completion Date	Tue, 27 Aug 2024 14:35:59 GMT
Estimated Duration	400
Status	completed
Number of Robots	4

(a) Experiment Setting.

## Experiment Video

[Click here to watch experiment](#)

(b) Experiment Video.

## Scripts

Main File	File Name	Upload Date	View	Download
	leader_follower_save_data.py	Aug 26, 24, 08:28 PM		
1 to 1 of 1   < > Page 1 of 1				

(c) Scripts.

## Return Messages

No return messages available yet

(d) Return Messages.

## Data Files

Main File	File Name	Upload Date	View	Download
	inter_robot_distance_data.txt	Aug 27, 24, 10:35 AM		
	goal_distance_data.txt	Aug 27, 24, 10:35 AM		
	goal_distance_data.npy	Aug 27, 24, 10:35 AM		
	inter_robot_distance_data.npy	Aug 27, 24, 10:35 AM		
1 to 4 of 4   < > Page 1 of 1				

(e) Data Files.

## Log Files

Main File	File Name	Upload Date	View	Download
	log.txt	Aug 27, 24, 10:35 AM		
1 to 1 of 1   < > Page 1 of 1				

(f) Log Files.

Figure 9: Experiment Outputs.

If you have any questions, feel free to contact [Sean Wilson](#).

## 1.4 Robotarium References for Citation

If you use the Robotarium for research purposes and want to mention it in one of your publications, please cite one of the following references. If your research included Robotarium experiments after January 2019, the publication titled *The Robotarium: Globally Impactful Opportunities, Challenges, and Lessons Learned in Remote-Access, Distributed Control of Multirobot Systems* is most appropriate. The other citations are included for your reference.

1. Sean Wilson, Paul Glotfelter, Li Wang, et al. (2020). “The Robotarium: Globally Impactful Opportunities, Challenges, and Lessons Learned in Remote-Access, Distributed Control of Multirobot Systems”. In: *IEEE Control Systems Magazine* 40.1, pp. 26–44. DOI: [10.1109/MCS.2019.2949973](https://doi.org/10.1109/MCS.2019.2949973)
2. Sean Wilson, Paul Glotfelter, Siddharth Mayya, et al. (2021). “The Robotarium: Automation of a Remotely Accessible, Multi-Robot Testbed”. In: *IEEE Robotics and Automation Letters* 6.2, pp. 2922–2929. DOI: [10.1109/LRA.2021.3062796](https://doi.org/10.1109/LRA.2021.3062796)
3. Sean Wilson and Magnus Egerstedt (2023). “The Robotarium: A Remotely-Accessible, Multi-Robot Testbed for Control Research and Education”. In: *IEEE Open Journal of Control Systems* 2, pp. 12–23. DOI: [10.1109/OJCSYS.2022.3231523](https://doi.org/10.1109/OJCSYS.2022.3231523)
4. Daniel Pickem et al. (2017). “The Robotarium: A remotely accessible swarm robotics research testbed”. In: *2017 IEEE International Conference on Robotics and Automation (ICRA)*, pp. 1699–1706. DOI: [10.1109/ICRA.2017.7989200](https://doi.org/10.1109/ICRA.2017.7989200).

For information about the current robotic platform on the Robotarium, please refer to the following publication and Github repository.

1. Soobum Kim et al. (2024b). “GTernal: A robot design for the autonomous operation of a multi-robot research testbed”. In: *International Symposium on Distributed Autonomous Robotic Systems*
2. Soobum Kim et al. (Sept. 2024a). *GTernal*. URL: <https://github.com/robotarium/GTernal>

## 2 Prerequisites

This section provides intuition and then covers the mathematical principles used in the Robotarium for modeling and control of the robots. While it provides valuable insights, it is not essential to read in detail to use the Robotarium unless you are interested in the mathematical underpinnings.

### 2.1 Differential-Drive Robots

The Robotarium allows for the simultaneous control of up to 20 differential-drive robots called GTernals. These robots are equipped with two parallel wheels that can be moved independently. This design allows the robots to perform a variety of maneuvers, such as moving forward, backward, and rotating in place.

The way to control the robots at the Robotarium is each robot used with a linear and angular velocity to execute.

#### 2.1.1 GTernals Linear Velocity

To move the robot straight, both wheels must move at the same speed in the same direction. When this occurs, the robot ideally drive perfectly straight. We call this a linear velocity,  $v$ , as shown in [Figure 10](#).

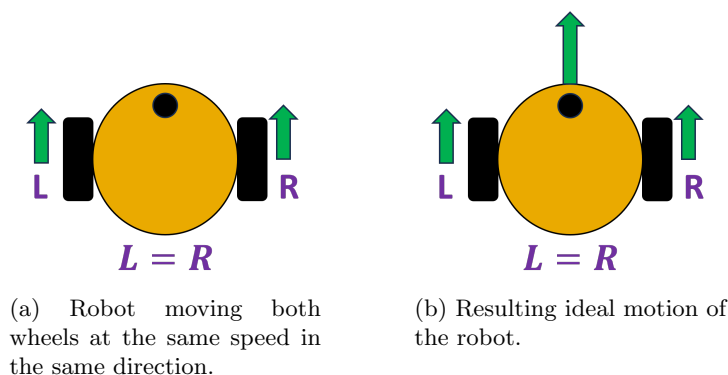


Figure 10: Linear velocity for differential drive robots.

#### 2.1.2 GTernals Angular Velocity

To change the robot's heading, the wheels need to rotate in opposite directions, with one wheel moving forward and the other backward. If we rotate the motors in opposite directions at the same rate, the robot will spin without translating at all. We call this pure rotation an angular velocity, as shown in [Figure 11](#).

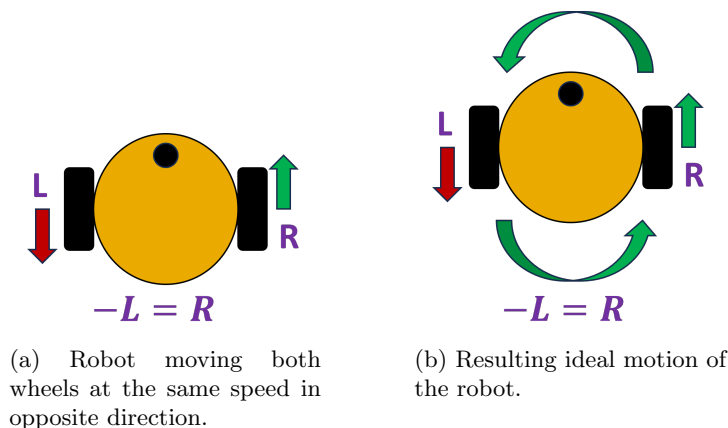


Figure 11: Angular velocity for differential drive robots.

### 2.1.3 GTernals Linear and Angular Velocity

When both linear and angular velocities are combined, the robot can perform more complex maneuvers, such as moving in curved trajectories. This is achieved by having the wheels rotate at different speeds, as demonstrated in Figure 12

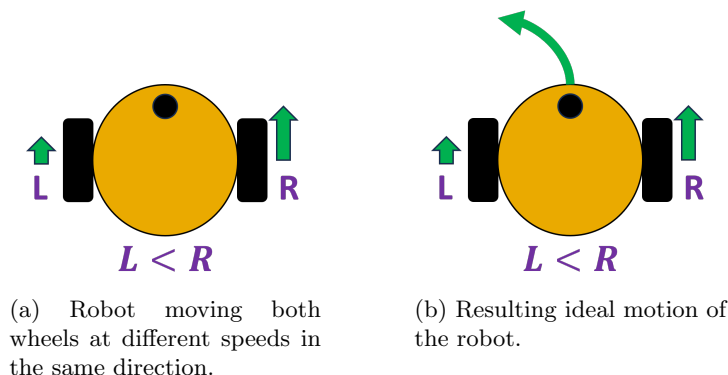


Figure 12: Linear and Angular Velocity for GTernals

## 2.2 Open Loop vs Close Loop

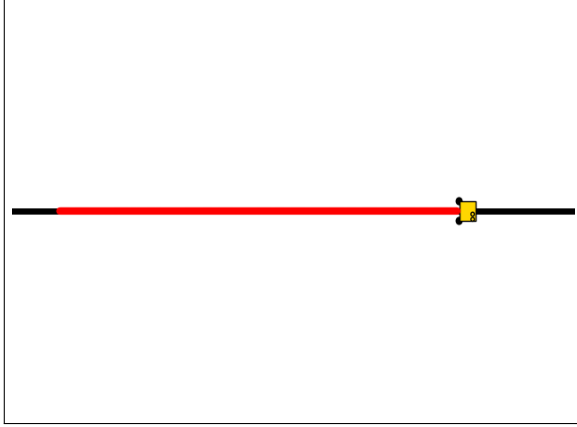
Let's imagine we have a trajectory (e.g. drive in a straight line) that enables a GTernal to reach its goal. To make the robot follow that trajectory, we can approach the problem in two ways:

- **Open-Loop Control:** In this method, the robot follows the path "blindly" by applying pre-computed control inputs and hoping nothing will go wrong. The robot executes predefined commands without considering any feedback from its environment. This approach assumes the robot will follow the path perfectly, without deviations.
- **Closed-Loop Control:** In closed-loop control, the robot follows the path for a short period, then "observes" whether it has deviated at all. Based on this feedback, the robot recomputes and adapts its control inputs to stay on track. This ensures that even if the robot experiences disturbances, it can adjust and stay on its desired trajectory.

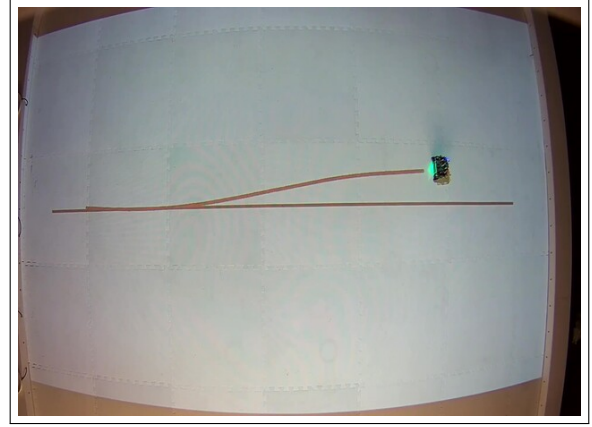
Let's explore an example of the implications of each approach. Imagine we have a robot, and we instruct it to follow a straight line by giving it a constant linear velocity in an open-loop control scenario. What do you think would happen?

With this open-loop command, the robot would initially follow the intended straight path. However, if any disturbances occur—such as uneven terrain, wheel slippage, or external forces—the robot will not be able to correct its course. Additionally, there may be effects like actuator dynamic or communication delays that can cause the robot to behave differently than expected. As a result, the robot's trajectory would gradually deviate from the straight line. This is because open-loop control assumes nothing will go wrong, so the robot blindly executes the pre-defined commands. This can be seen in Figure 13. Notice in the perfect simulation, everything works out and the robot drives along the straight line but in reality where there are unexpected complications, the constant linear velocity does not result in straight motion. This is one of the many reasons to use the Robotarium, robots are extremely complex consisting of many interacting systems that can be hard to model mathematically and in simulation. Using the Robotarium exposes your developed algorithms to those complexities and allows you to validate your ideas in hardware.

If you want to try this experiment, you can run the following code on the Robotarium. This script instructs a GTernal to follow a straight-line trajectory by setting a constant linear velocity. In the simulation, the robot will follow the path perfectly since the simulator does not consider real-world disturbances. However, when you execute this code in the Robotarium environment, you'll notice how perturbations, such as friction or slight imperfections in the motors, influence the robot's trajectory, preventing it from following a perfect straight line.



(a) Open-loop at the Simulator



(b) Open-loop at the Robotarium

Figure 13: Simulator vs Real Life Open-Loop Control. The black line is the path the robot should take and the red line is what the robot actually drove.

If the robot used closed-loop control, it would continuously monitor its position and correct its trajectory in response to any disturbances. For example, if the robot veers slightly off the straight path, it would detect the deviation and adjust its wheels' speeds to bring it back on track. This makes closed-loop control more robust in dynamic environments or when disturbances are likely. While we do not provide an example to do this in this part of the guide, you are welcome to try to develop your own or use one of the many controllers listed below.

```

1  import rps.robotarium as robotarium
2  from rps.utilities.transformations import *
3  from rps.utilities.barrier_certificates import *
4  from rps.utilities.misc import *
5  from rps.utilities.controllers import *
6  import numpy as np
7  import time
8
9  N = 1 # Number of Robots
10
11  init_pos = np.array([-1.3,0,0]).reshape(3,1) # Initial Positions
12
13  iterations = 450 # Run the simulation/experiment for 450 steps
14
15  r = robotarium.Robotarium(number_of_robots=N, show_figure=True, initial_conditions=init_pos, sim_in_real_time=True) #
    ↳ Instantiate the Robotarium
16
17  line_width = 5 # Big lines
18  position_history = np.empty((2,0)) # History to show what the robot does
19  r.axes.plot([-1.6,1.6],[0,0],linewidth=line_width,color='k',zorder=-1) # Plot reference line
20
21  for t in range(iterations):
22
23      x = r.get_poses() # Get the poses of robots
24
25      dxu = np.array([0.15,0]).reshape(2,1) # Define the Speed of the robot
26
27      r.set_velocities(np.arange(N), dxu) # Set the velocities using unicycle commands
28
29      # Plotting the robot's true trajectory.
30      position_history=np.append(position_history, x[:2],axis=1)
31      if(t == iterations-1):
32          r.axes.scatter(position_history[0,:],position_history[1,:], s=1, linewidth=line_width, color='r',
    ↳ linestyle='dashed')
33
34      r.step() # Iterate the simulation
35
36  time.sleep(5)
37
38  r.call_at_scripts_end() # Call at end of script to print debug information

```

Listing 1: Example code for a robot moving in a straight line.



## 2.3 Differential-Drive Kinematics

Kinematics is a branch of mechanics that deals with the motion of objects without considering the forces that cause the motion. There are two main problems Kinematics aims to solve *Forward Kinematics* and *Inverse Kinematics*.

- Forward kinematics answers the following question. Given the initial state of the system  $\mathbf{x}_0$  (e.g. robot pose  $\mathbf{x}_0 = [x(0), y(0), \theta(0)]^T$ ) and input controls to the system (e.g velocity), find the final state of the system  $\mathbf{x}_t$  (e.g. robot pose  $\mathbf{x}_t = [x(t), y(t), \theta(t)]^T$ ) reached by the robot.
- Inverse kinematics answers the following question. Given the initial state of the system  $\mathbf{x}_0$  (e.g. robot pose  $\mathbf{x}_0 = [x(0), y(0), \theta(0)]^T$ ) and a desired final state of the system  $\mathbf{x}_t$  (e.g. robot pose  $\mathbf{x}_t = [x(t), y(t), \theta(t)]^T$ ), find the input controls to the system (e.g velocity),

Note that in general, inverse kinematics is a much harder problem than forward kinematics.

### Forward Kinematics for Differential-Drive Robots

A differential-drive robot has two actuators (left wheel speed  $\dot{\phi}_l$  and right wheel speed  $\dot{\phi}_r$ ). Through the geometric relation of the wheel locations to the robot body and assuming there is no wheel slip and only motion in the direction the wheel spins, we can determine the entire robot's forward velocity and rotational velocity <sup>2</sup>.

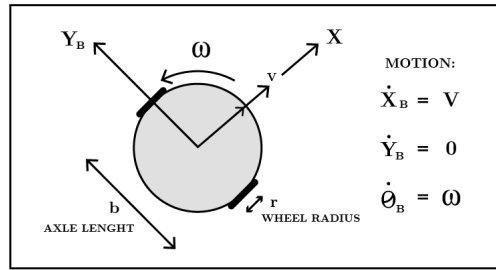


Figure 14: Body Frame Kinematics

### Forward Velocity

$$v = \frac{r\dot{\phi}_l}{2} + \frac{r\dot{\phi}_r}{2} \quad \text{where } r \text{ is the radius of the wheel}$$

### Rotational Velocity

$$w = \frac{r\dot{\phi}_r}{d} - \frac{r\dot{\phi}_l}{d} \quad \text{where } d \text{ is the axle length}$$

Then, the motion of the robot in a can be described as

$$\begin{pmatrix} \dot{x}_B \\ \dot{y}_B \\ \dot{\theta}_B \end{pmatrix} = \begin{pmatrix} v \\ 0 \\ w \end{pmatrix}$$

<sup>2</sup>Roland Siegwart, IllahR. Nourbakhsh, and DavideScaramuzza. Introduction to Autonomous Mobile Robots, 2nd ed., 2011.

This is a motion model that describe how the robot state change in its own local coordinate system. We can notice that  $y = 0$  since we have assumed the wheels cannot slip. Therefore, we have a motion constraint. This motion constraint is similar to cars and bicycles that cannot immediately drive left or right.

Now, we are going to use this motion model to create a system of equations that describes the robot's state change in a global coordinate (e.g. with respect to the coordinate system of the Robotarium). In other words, given a known control inputs, how does the robot move with respect to a **global coordinate system**?

In order to do that, we will use a rotational matrix  $R(\theta)$

$$\begin{aligned}\begin{pmatrix} \dot{x} \\ \dot{y} \\ \dot{\theta} \end{pmatrix} &= R(\theta) \begin{pmatrix} \dot{x}_B \\ \dot{y}_B \\ \dot{\theta}_B \end{pmatrix} \\ \begin{pmatrix} \dot{x} \\ \dot{y} \\ \dot{\theta} \end{pmatrix} &= \begin{pmatrix} \cos(\theta) & -\sin(\theta) & 0 \\ \sin(\theta) & \cos(\theta) & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} \dot{x}_B \\ \dot{y}_B \\ \dot{\theta}_B \end{pmatrix} \\ \begin{pmatrix} \dot{x} \\ \dot{y} \\ \dot{\theta} \end{pmatrix} &= \begin{pmatrix} \cos(\theta) & -\sin(\theta) & 0 \\ \sin(\theta) & \cos(\theta) & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} v \\ 0 \\ w \end{pmatrix} \\ \begin{pmatrix} \dot{x} \\ \dot{y} \\ \dot{\theta} \end{pmatrix} &= \begin{pmatrix} v \cos(\theta) \\ v \sin(\theta) \\ w \end{pmatrix}\end{aligned}$$

Now, giving inputs  $u$  and  $w$  and the orientation  $\theta$ , I can tell how the robot moves in the world frame.

## Inverse Kinematics

While forward kinematics are useful. Typically, we are more interested in answering the question, given a desired motion in the global coordinate system, what should the control inputs be to move in that direction?

Deriving the formula used previously, we can invert the previous equations to find the **control inputs**

$$\begin{aligned}\begin{pmatrix} v \\ 0 \\ w \end{pmatrix} &= R^{-1}(\theta) \begin{pmatrix} \dot{x} \\ \dot{y} \\ \dot{\theta} \end{pmatrix} \\ \begin{pmatrix} v \\ 0 \\ w \end{pmatrix} &= \begin{pmatrix} \cos(\theta) & \sin(\theta) & 0 \\ -\sin(\theta) & \cos(\theta) & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} \dot{x} \\ \dot{y} \\ \dot{\theta} \end{pmatrix} \\ \begin{pmatrix} v \\ 0 \\ w \end{pmatrix} &= \begin{pmatrix} \cos(\theta)\dot{x} + \sin(\theta)\dot{y} \\ \cos(\theta)\dot{x} - \sin(\theta)\dot{y} \\ \dot{\theta} \end{pmatrix}\end{aligned}$$

Then, we obtain that

$$\begin{aligned}v &= \cos(\theta)\dot{x} + \sin(\theta)\dot{y} \\ w &= \dot{\theta}\end{aligned}$$

and that

$$\begin{aligned}\dot{\phi}_l &= v - \frac{wd}{2r} = \cos(\theta)\dot{x} + \sin(\theta)\dot{y} - \frac{\dot{\theta}d}{2r} \\ \dot{\phi}_r &= v + \frac{wd}{2r} = \cos(\theta)\dot{x} + \sin(\theta)\dot{y} + \frac{\dot{\theta}d}{2r}\end{aligned}$$

So now we can control the wheel speeds! But, (since our robot is non-holonomic), we have to add a constraint

$$\dot{x}\cos(\theta) = \dot{y}\sin(\theta)$$

Being non-holonomic, implies that we cannot change the  $y_B$  in the robot's body-frame. If we want to change something in the  $y_B$ , we must change something in  $x_B$  in the robot body-frame. In order to do that, we must leverage a new trick, *feedback linearization*.

## 2.4 Dynamics in The Robotarium

The robots deployed on the Robotarium are differential drive robots. In simulation the motion of the robots in the global coordinate frame are modeled through the unicycle model.

### 2.4.1 Unicycle Dynamics

The unicycle model has two input quantities, the linear velocity ( $v$ ) and the angular velocity ( $\omega$ ). The linear velocity has units m/s and the angular velocity has units radians/s. The set of equations that fully describes the velocities of the global pose  $(x, y, \theta)$  are

$$\begin{pmatrix} \dot{x} \\ \dot{y} \\ \dot{\theta} \end{pmatrix} = \begin{pmatrix} v \cos(\theta) \\ v \sin(\theta) \\ \omega \end{pmatrix}$$

### 2.4.2 Single-Integrator Dynamics

Another model we can use is the single integrator model. This simple model treats the robot's state as a point,  $p = [x, y] \in \mathbb{R}^2$  which is the x-coordinate (x) and y-coordinate (y) and the input ( $u \in \mathbb{R}^2$ ) which is just the x-velocity ( $v_x$ ) and y-velocity ( $v_y$ ) or  $u = [v_x, v_y]$ . Because we give the full state information needed for the model, the output, is the state. The model that represents this can be described with the following equations

$$\begin{aligned}\dot{p} &= u \\ y &= p\end{aligned}$$

In the model, the input  $u$  is the derivative of the state ( $\dot{p}$  = derivative of  $p$ ) meaning if we were to integrate over that input we would get the state of the robot, hence the name single integrator. Programming algorithms with the single integrator model allows you to disregard dynamics and only consider how velocities affect the point-to-point motion over time. In the simulator, we provide code to transform between the two models of the GTernal, however, inputs to the GTernal must be in unicycle model form. In other words, GTernal only accept linear velocity and angular velocity inputs.

### 2.4.3 Transformation from Unicycle to Single-Integrator Dynamics

#### Single Integrator to Unicycle Transformation:

We are trying to answer the following question. Given desired velocities in the single integrator model, how do we convert these into control inputs for a unicycle robot?

To derive the unicycle control inputs from the single integrator commands, we use the following transformation:

$$\begin{aligned}\begin{pmatrix} v \\ w \end{pmatrix} &= \begin{pmatrix} 1 & 0 \\ 0 & \frac{1}{l} \end{pmatrix} R(-\theta) \begin{pmatrix} u_x \\ u_y \end{pmatrix} \\ \begin{pmatrix} v \\ w \end{pmatrix} &= \begin{pmatrix} 1 & 0 \\ 0 & \frac{1}{l} \end{pmatrix} \begin{pmatrix} \cos(\theta) & \sin(\theta) \\ -\sin(\theta) & \cos(\theta) \end{pmatrix} \begin{pmatrix} u_x \\ u_y \end{pmatrix} \\ \begin{pmatrix} v \\ w \end{pmatrix} &= \begin{pmatrix} \cos(\theta)u_x + \sin(\theta)u_y \\ \frac{-\sin(\theta)u_x + \cos(\theta)u_y}{l} \end{pmatrix}\end{aligned}$$

Thus, we obtain the unicycle control inputs as:

$$\begin{aligned}v &= \cos(\theta)u_x + \sin(\theta)u_y \\ w &= \frac{-\sin(\theta)u_x + \cos(\theta)u_y}{l}\end{aligned}$$

These equations allow us to convert the single integrator velocity commands  $(u_x, u_y)$  into the unicycle model's linear and angular velocities  $(v, w)$ .

## 2.5 Basic Code Structure

This section gives an example of the minimum code necessary for users to run their algorithms on the Robotarium. The code itself is non-operational (Eventually the robots will leave the test bed or crash between them), but it provides useful function calls and commands that users will need to call in order to run programs successfully. The code is discussed line-by-line below.

```

1  import rps.robotarium as robotarium
2  from rps.utilities.transformations import *
3  from rps.utilities.barrier_certificates import *
4  from rps.utilities.misc import *
5  from rps.utilities.controllers import *
6  import numpy as np
7  import time
8
9  N = 1 # Number of Robots
10
11 iterations = 450 # Run the simulation/experiment for 450 steps
12
13 r = robotarium.Robotarium(number_of_robots=N, show_figure=True, sim_in_real_time=True) # Instantiate the Robotarium
14
15 # Velocity parameters for the Robots
16 linear_velocity = 0.15 # Constant linear velocity (m/s)
17 angular_velocity = 0 # No angular velocity (to move straight)
18
19 for t in range(iterations):
20
21     x = r.get_poses() # Get the poses of robots
22
23     dxu = np.zeros((2, N)) # Array to hold the velocities for each robot
24     dxu[0, :] = linear_velocity # Set the linear velocity
25     dxu[1, :] = angular_velocity # No angular velocity (straight line)
26
27     r.set_velocities(np.arange(N), dxu) # Apply the velocities to the robots
28
29     r.step() # Step the simulation
30
31 r.call_at_scripts_end() # Call this function at the end of the script to properly close the simulation

```

Listing 2: Basic Implementation Code Structure. The functions called and variables declared in this file are meant to familiarize users with the tools available on the Robotarium

---

### Algorithm 1 Basic Implementation Code Structure

---

- |  |           |
|--|-----------|
| 1: Import necessary libraries                                      | ▷ [1-7]   |
| 2: Set the number of robots for the simulation                     | ▷ [9]     |
| 3: Determine the number of Iteration.                              | ▷ [11]    |
| 4: Instantiate the Robotarium object with the specified parameters | ▷ [13]    |
| 5: Define linear and angular velocities                            | ▷ [16,17] |
| 6: <b>for</b> t < iterations <b>do</b>                             | ▷ [19]    |
| 7:     Get the current pose of the robot                           | ▷ [21]    |
| 8:     Set the velocity of the robot                               | ▷ [27]    |
| 9:     Iterate the simulation                                      | ▷ [29]    |
| 10: <b>end for</b>   |           |
| 11: Call the script end function to finalize the simulation        | ▷ [31]    |
- 

Each step is explained below. If you need more information about a specific function, please click on ▷ [ · · · ] in the Pseudo-Code. Almost all instructions are linked to the function section, where we provide detailed explanations (We use this format through all the guide).

The basic skeleton code must have:

1. We first import all the libraries that we will use in our experiment. You can check the libraries available in [Appendix A](#)
2. Declare the number of robots you would like to use. In simulation, this number must be greater than zero and less than fifty. If submitting the code to be run on the Robotarium testbed, the number of robots must be greater than 0 and less than 20.
3. Indicate how many iterations you would like the algorithm to run. If this is replaced with a while loop, make sure the script terminates.
4. Initialize Robotarium object/environment. This allows users to use the functions within the class.
5. In this example, we create two variable for the linear and angular velocity, it is not necessary, and we can add the angular and linear speed directly in the velocity function.
6. Loop over the number of iterations you specify, for instance the expected run-time of your algorithm.
7. Retrieve pose information for all robots. This function returns a matrix of size  $3 \times N$ , where  $N$  is the number of robots and a 3 dimensional pose of the x-coordinate, y-coordinate, and orientation of a robot( $\theta$ ) in the global coordinate frame.
8. At each iteration, set the desired velocities of the robot. Note: Prior to this function call, your algorithm should have generated a matrix of input velocities of size  $2 \times N$ , where the velocities are desired linear velocities ( $v$ ) and angular velocities ( $\omega$ ) for each robot (We did this in line [23-25]).
9. The step function, sends the velocity inputs previously created to the robots. If you do not call this function, the robots will not move!
10. Remember, make sure the script terminates!
11. Lastly, the debug function is called to make sure that no errors have occurred in the script. It is strongly recommend to implement this function to notify you if any potential errors are found regarding potential robot collisions, actuator saturation, or failure to stay within the testing area. If you submit code that contains errors caught by this debugger, your submitted experiment may be rejected when submitting it to be run on the testbed. After you have run the experiment, you should see a message similar to [Figure 16](#).

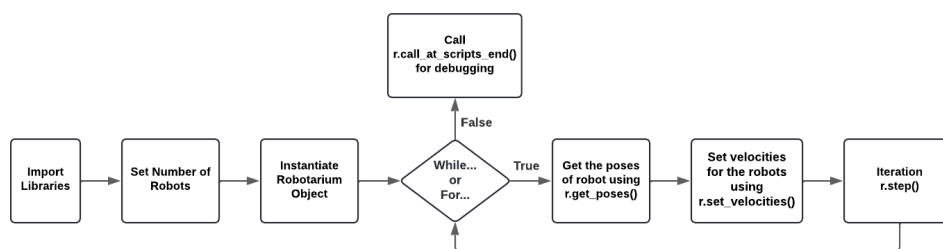


Figure 15: Basic Implementation Code Structure. The functions called and variables declared in this file are meant to familiarize users with the tools available on the Robotarium

```

##### DEBUG OUTPUT #####
Your simulation will take approximately 15 real seconds when deployed on the Robotarium.

Simulation had 450 iteration(s) where the actuator limits were exceeded.
  
```

Figure 16: This message will show if you run the debug command after your code has ran. If you receive the no errors message, it improves your chances that your code is within acceptance parameters!

## 2.6 Specification of the Robotarium

### 2.6.1 How fast do the robots move?

The robots in the Robotarium have a minimum linear speed of 0.03 cm/s, and a maximum linear speed of 20 cm/s and a maximum rotational speed of approximately 3.6 rad/s (which is roughly 1/2 rotation per second). However, to protect the motors from erratic behavior at high speeds, the motors are thresholded to rotate at a maximum speed of 12.5 rad/s. Consequently, any combination of high linear and rotational commands within these maximum bounds will be adjusted to ensure the rotational speed of the motors does not exceed this limit.

### 2.6.2 What is the dimension of the arena?

The robots operate within a 3.2m x 2m area, which corresponds to the coverage area of the projector used in the Robotarium. This space provides enough room for the robots to maneuver while still being constrained enough to observe interactions effectively.

### 2.6.3 How big are the robots?

Each robot in the Robotarium is 11 cm wide, 10 cm long, and 9.5 cm tall. However, when considering the antenna and tracking markers, the effective height of the robots is taller. These dimensions are crucial for ensuring that the robots can navigate the arena without colliding with each other or the boundaries.

### 2.6.4 What is the minimum distance allowed between robots to avoid collision?

The robots have a diameter of approximately 11 cm. However, to ensure that the robots do not collide, it is recommended to maintain a minimum distance of 15 cm between them. This spacing helps avoid accidental collisions, especially when the robots are in motion. To further reduce the risk of collisions, you can use barrier certificates, which are built-in functions designed to keep the robots from colliding during experiments. More information about barrier certificates and barrier certificate functions can be found in [subsection 4.5](#).

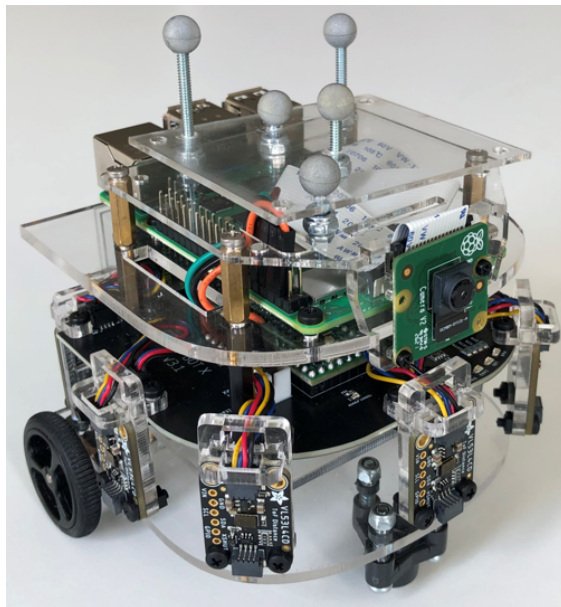


Figure 17: GTernal Robot

## 2.7 Communication Delays and Their Impact on Remote Robot Control

Imagine we are controlling a robot on the planet Jupiter from Earth. This robot is capable of perceiving its environment and sending the information back to Earth, where a group of scientists decides the next action based on the information received. There are two key pieces of information that we need to consider:

1. The distance between Earth and Jupiter (approximately 588 million kilometers at their closest point).
2. The speed at which information travels (In a vacuum, radio waves travel at the speed of light, approximate  $3 \cdot 10^8 \frac{m}{s}$ )

With this information, we can calculate the time it would take for the robot to receive instructions from Earth and send information back.

$$\frac{\text{Distance between the planets}}{\text{Velocity of the information}} = \frac{588,000,000 \text{ km} \cdot (\frac{1,000m}{1km})}{3 \cdot 10^8 \frac{m}{s}} \approx 1,960 \text{ s}$$

It would take approximately 1,960 second (a little more than 30 minutes) for a one way trip of communication. and more than an hour (3,920 second) for the round trip.

Let say the vehicle is continuously moving at  $1 \frac{m}{s}$ , the robot will be moving while waiting the next control command. Since the round trip is 3,920 seconds

$$1 \frac{m}{s} \cdot 3,920 \text{ s} \approx 3,920 \text{ m}$$

The robot would move 3,920 m between control command. And even more worrying, the robot is driving "blind" since is waiting instruction from earth.

If well this is an extreme example, it important to consider the speed of the information as well as computation time. The Robotarium is a little bit closer to its robots than Jupiter is to Earth, so we can obtain the position of the robot much faster. However, we also have to consider the time it takes for the central tracking server and robots on the Robotarium to process the information as well. The travel time of information and computation requirements for its baseline usage allows decisions to be made on the Robotarium approximately every 0.033 seconds. This is interpreted that each iteration in the Robotarium is equal to 0.033 s in the real world. For instance, if we have a simulation that has 1000 iteration, the time in real life would be approximately

$$0.033 \text{ s} \cdot 1000 \approx 33.00 \text{ seconds}$$

This 0.033 seconds is because of the time delay it takes on the real Robotarium to communicate and process data. It is important to note that if your submitted code takes longer than 0.033 seconds to execute a single loop this time delay will increase!



Figure 18: Vicon System in the Robotarium



## 3 Code Examples (examples)

In this section you will find different examples that demonstrate how to interact with the Python Simulator. These examples showcase different scenarios that you can apply when working with the robots. All of these examples are available for download with the Python Simulator Package.

Each example was designed to help you understand and implement the essential feature and capabilities of the Robotarium, from basic movement commands to more complex behaviors such as formation control.

### 3.1 go\_to\_point

#### 3.1.1 Robots go to a point using Single Integrator

This code controls multiple robot that move towards a specified goal while avoiding collision with other robots or driving outside the testbed boundaries. The Single Integrator model was used for generating control inputs (dxi). The Unicycle Model was used for the actual control signal sent to the robots (dxu), this involved converting the single integrator control inputs to unicycle commands.

```
1  import rps.robotarium as robotarium
2  from rps.utilities.transformations import *
3  from rps.utilities.barrier_certificates import *
4  from rps.utilities.misc import *
5  from rps.utilities.controllers import *
6  import numpy as np
7  import time
8
9  N = 5 # Number of Robots
10
11  initial_conditions = np.array(np.mat('1 0.5 -0.5 0 0.28; 0.8 -0.3 -0.75 0.1 0.34; 0 0 0 0 0')) # Initial Positions
12
13  r = robotarium.Robotarium(number_of_robots=N, show_figure=True, initial_conditions=initial_conditions,
14  ↪  sim_in_real_time=False) # Instantiate Robotarium
15
16  goal_points = generate_initial_conditions(N) # Goal Points
17
18  single_integrator_position_controller = create_si_position_controller() # Single integrator position controller
19
20  si_barrier_cert = create_single_integrator_barrier_certificate_with_boundary() # Barrier certificates to avoid collision
21
22  _, uni_to_si_states = create_si_to_uni_mapping() # Unicycle to Single Integrator States Mapping
23
24  si_to_uni_dyn = create_si_to_uni_dynamics_with_backwards_motion() # Single Integrator to Unicycle Velocity Commands
25
26  x = r.get_poses() # Get poses of the Robots
27
28  x_si = uni_to_si_states(x) # Transform poses to Single Integrator
29
30  r.step() # Iterate the simulation
31
32  # While all Robots are not in the goal points...
33  while (np.size(at_pose(np.vstack((x_si,x[2,:])), goal_points, rotation_error=100)) != N):
34
35      x = r.get_poses() # Get the poses of robots
36
37      x_si = uni_to_si_states(x) # Transform poses to Single Integrator
38
39      dxi = single_integrator_position_controller(x_si, goal_points[2][:]) # Create single-integrator control inputs
40
41      dxi_safe = si_barrier_cert(dxi, x_si) # Create safe control inputs (i.e., no collisions)
42
43      dxu_safe = si_to_uni_dyn(dxi_safe, x) # Transform single integrator velocity commands to unicycle
44
45      r.set_velocities(np.arange(N), dxu_safe) # Set the velocities of agents 1,...,N to dxu_safe
46
47      r.step() # Iterate the simulation
48
49  r.call_at_scripts_end() # Call at end of script to print debug information
```

Listing 3: si\_go\_to\_point.py example

---

**Algorithm 2** Pseudo Code `si_go_to_point.py`

---

1: Import important libraries	▷ [1-7]
2: Set the number of robots you would like to use	▷ [9]
3: An array with the initial positions of the robots.	▷ [11]
4: Initialize the Robotarium object.	▷ [13]
5: Generates a random set of points spaced within a bounded rectangle (the testbed) as goal points	▷ [15]
6: Create single integrator position controller	▷ [17]
7: Create barrier certificates to avoid collision	▷ [19]
8: Create mapping from single integrator states to unicycle states	▷ [21]
9: Create mapping from single integrator velocity commands to unicycle velocity commands	▷ [23]
10: Get initial poses of the robots	▷ [25]
11: Convert unicycle states to single integrator states	▷ [27]
12: Step the simulation to update visualization. Iterate the experiment	▷ [29]
13: <b>while</b> the number of robots not at the goal poses < N <b>do</b>	
14:     Get current poses of the robots.	▷ [34]
15:     Convert unicycle states to single integrator states	▷ [36]
16:     Create single-integrator control inputs	▷ [38]
17:     Create safe control inputs in order to avoid collision.	▷ [40]
18:     Transform single integrator velocity commands to unicycle	▷ [42]
19:     Set the velocities by mapping the single-integrator inputs to unicycle inputs	▷ [44]
20:     Step the simulation to update visualization. Iterate the experiment	▷ [46]
21: <b>end while</b>	
22: Call this script to debug at the end of the experiment.	▷ [48]

---

### 3.1.2 Robots go to a point Unicycle

This code controls multiple robots that move towards a specified goal while avoiding collision with other robots or driving outside the testbed boundaries. The Unicycle Model is used for generating control inputs and for the control command sent to the robots (dxu). Barrier certificates ensure safe control inputs to avoid collisions.

```

1  import rps.robotarium as robotarium
2  from rps.utilities.transformations import *
3  from rps.utilities.barrier_certificates import *
4  from rps.utilities.misc import *
5  from rps.utilities.controllers import *
6  import numpy as np
7  import time
8
9  N = 5 # Number of Robots
10
11  initial_conditions = np.array(np.mat('1 0.5 -0.5 0 0.28; 0.8 -0.3 -0.75 0.1 0.34; 0 0 0 0 0')) # Initial Poses
12
13  r = robotarium.Robotarium(number_of_robots=N, show_figure=True,
14  ↪ initial_conditions=initial_conditions,sim_in_real_time=True) # Instantiate Robotarium object
15
16  goal_points = generate_initial_conditions(N) # Goal Points
17
18  unicycle_position_controller = create_clf_unicycle_position_controller() # Create unicycle position controller
19
20  uni_barrier_cert = create_unicycle_barrier_certificate() # Create barrier certificates to avoid collision
21
22  x = r.get_poses() # Get the poses of the Robots
23
24  r.step() # Iterate the simulation
25
26  # While all Robots are not in the goal points...
27  while (np.size(at_pose(x, goal_points, rotation_error=100)) != N):
28
29      x = r.get_poses() # Get the poses of Robots
30
31      dxu = unicycle_position_controller(x, goal_points[2][:]) # Create single-integrator control inputs
32
33      dxu_safe = uni_barrier_cert(dxu, x) # Create safe control inputs (i.e., no collisions)
34
35      r.set_velocities(np.arange(N), dxu_safe) # Set the velocities of agents 1,...,N to dxu_safe
36
37      r.step() # Iterate the simulation
38
39  r.call_at_scripts_end() # Call at end of script to print debug information

```

Listing 4: uni\_go\_to\_point.py example

---

#### Algorithm 3 Pseudo Code uni\_go\_to\_point.py

---

- |   |         |
|---|---------|
| 1: Import important libraries   | ▷ [1-7] |
| 2: Set the number of robots you would like to use   | ▷ [9]   |
| 3: Define an array with the initial positions of the robots                                       | ▷ [11]  |
| 4: Initialize the Robotarium object   | ▷ [13]  |
| 5: Generate a random set of points spaced within a bounded rectangle (the testbed) as goal points | ▷ [15]  |
| 6: Create unicycle position controller  | ▷ [17]  |
| 7: Create barrier certificates to avoid collision   | ▷ [19]  |
| 8: Get initial poses of the robots  | ▷ [21]  |
| 9: Step the simulation to update visualization  | ▷ [23]  |
| 10: <b>while</b> the number of robots not at the goal poses < N <b>do</b>                         |         |
| 11:     Get current poses of the robots   | ▷ [28]  |
| 12:     Create unicycle control inputs  | ▷ [30]  |
| 13:     Create safe control inputs in order to avoid collision                                    | ▷ [32]  |
| 14:     Set the velocities by mapping the single-integrator inputs to unicycle inputs             | ▷ [34]  |
| 15:     Step the simulation to update visualization   | ▷ [36]  |
| 16: <b>end while</b>  |         |
| 17: Call this script to debug at the end of the experiment  | ▷ [38]  |
-

## 3.2 go\_to\_pose

### 3.2.1 Robots go to a point using Unicycle Pose Controller

This code controls multiple robots that move towards a specified pose (i.e. a position and orientation) while avoiding collisions with other robots or driving outside the testbed boundaries. The Unicycle Pose Controller is used for generating control inputs that are sent directly to the robots (`dxu`). Barrier certificates ensure safe control inputs to avoid collisions.

```
1  import rps.robotarium as robotarium
2  from rps.utilities.transformations import *
3  from rps.utilities.barrier_certificates import *
4  from rps.utilities.misc import *
5  from rps.utilities.controllers import *
6  import numpy as np
7  import time
8
9  N = 5 # Number of Robots
10
11  initial_conditions = np.array(np.mat('1 0.5 -0.5 0 0.28; 0.8 -0.3 -0.75 0.1 0.34; 0 0 0 0 0')) # Initial Positions
12
13  r = robotarium.Robotarium(number_of_robots=N, show_figure=True, initial_conditions=initial_conditions,
14  ↪  sim_in_real_time=True) # Instantiate Robotarium object
15
16  goal_points = generate_initial_conditions(N) # Goal Points
17
18  unicycle_pose_controller = create_clf_unicycle_pose_controller() # Create unicycle pose controller
19
20  uni_barrier_cert = create_unicycle_barrier_certificate() # Create barrier certificates to avoid collision
21
22  x = r.get_poses() # Get the poses of Robots
23
24  r.step() # Iterate the simulation
25
26  # While the Robots are not in the goal points
27  while (np.size(at_pose(x, goal_points)) != N):
28      x = r.get_poses() # Get the poses of Robots
29
30      dxu = unicycle_pose_controller(x, goal_points) # Create unicycle control inputs
31
32      dxu_safe = uni_barrier_cert(dxu, x) # Create safe control inputs (i.e., no collisions)
33
34      r.set_velocities(np.arange(N), dxu_safe) # Set the velocities of agents 1,...,N to dxu_safe
35
36      r.step() # Iterate the simulation
37
38  r.call_at_scripts_end() # Call at end of script to print debug information
```

Listing 5: `uni_go_to_pose_clf.py` example

---

**Algorithm 4** Pseudo Code `uni_go_to_pose_clf.py`

---

```
1: Import important libraries ▷ [1-7]
2: Set the number of robots you would like to use ▷ [9]
3: Define an array with the initial positions of the robots ▷ [11]
4: Initialize the Robotarium object ▷ [13]
5: Generate a random set of points spaced within a bounded rectangle (the testbed) as goal points ▷ [15]
6: Create unicycle pose controller ▷ [17]
7: Create barrier certificates to avoid collision ▷ [19]
8: Get initial poses of the robots ▷ [21]
9: Step the simulation to update visualization ▷ [23]
10: while the number of robots not at the goal poses < N do
11:     Get current poses of the robots ▷ [28]
12:     Create unicycle control inputs ▷ [30]
13:     Create safe control inputs in order to avoid collision ▷ [32]
14:     Set the velocities by mapping the single-integrator inputs to unicycle inputs ▷ [34]
15:     Step the simulation to update visualization ▷ [36]
16: end while
17: Call this script to debug at the end of the experiment ▷ [38]
```

---

### 3.2.2 Robots go to a point using Unicycle Hybrid Pose Controller

This code controls multiple robots that move towards a specified goal while avoiding collisions with other robots or driving outside the testbed boundaries. The Unicycle Hybrid Pose Controller is used for generating control inputs that are directly sent to the robots (dxu). Barrier certificates ensure safe control inputs to avoid collisions.

```

1  import rps.robotarium as robotarium
2  from rps.utilities.transformations import *
3  from rps.utilities.barrier_certificates import *
4  from rps.utilities.misc import *
5  from rps.utilities.controllers import *
6  import numpy as np
7  import time
8
9  N = 5 # Number of Robots
10
11  initial_conditions = np.array(np.mat('1 0.5 -0.5 0 0.28; 0.8 -0.3 -0.75 0.1 0.34; 0 0 0 0 0')) #Goal Points
12
13  r = robotarium.Robotarium(number_of_robots=N, show_figure=True, initial_conditions=initial_conditions,
14  ↪  sim_in_real_time=True) # Instantiate Robotarium object
15
16  goal_points = generate_initial_conditions(N) # Goal Points
17
18  unicycle_pose_controller = create_hybrid_unicycle_pose_controller() # Create unicycle hybrid pose controller
19
20  uni_barrier_cert = create_unicycle_barrier_certificate() # Create barrier certificates to avoid collision
21
22  x = r.get_poses() # Get the poses of Robots
23
24  r.step() # Iterate the simulation
25
26  # While the robots are not in the goal points
27  while (np.size(at_pose(x, goal_points)) != N):
28
29      x = r.get_poses() # Get poses of Robots
30
31      dxu = unicycle_pose_controller(x, goal_points) # Create unicycle control inputs
32
33      dxu_safe = uni_barrier_cert(dxu, x) # Create safe control inputs (i.e., no collisions)
34
35      r.set_velocities(np.arange(N), dxu_safe) # Set the velocities of agents 1,...,N to dxu_safe
36
37      r.step() # Iterate the simulation
38
39  r.call_at_scripts_end() # Call at end of script to print debug information

```

Listing 6: uni\_go\_to\_pose\_hybrid.py example

---

#### Algorithm 5 Pseudo Code uni\_go\_to\_pose\_hybrid.py

---

- |   |         |
|---|---------|
| 1: Import important libraries   | ▷ [1-7] |
| 2: Set the number of robots you would like to use   | ▷ [9]   |
| 3: Define an array with the initial positions of the robots                                       | ▷ [11]  |
| 4: Initialize the Robotarium object   | ▷ [13]  |
| 5: Generate a random set of points spaced within a bounded rectangle (the testbed) as goal points | ▷ [15]  |
| 6: Create unicycle hybrid pose controller   | ▷ [17]  |
| 7: Create barrier certificates to avoid collision   | ▷ [19]  |
| 8: Get initial poses of the robots  | ▷ [21]  |
| 9: Step the simulation to update visualization  | ▷ [23]  |
| 10: <b>while</b> the number of robots not at the goal poses < N <b>do</b>                         |         |
| 11:     Get current poses of the robots   | ▷ [28]  |
| 12:     Create unicycle control inputs  | ▷ [30]  |
| 13:     Create safe control inputs in order to avoid collision                                    | ▷ [32]  |
| 14:     Set the velocities by mapping the single-integrator inputs to unicycle inputs             | ▷ [34]  |
| 15:     Step the simulation to update visualization   | ▷ [36]  |
| 16: <b>end while</b>  |         |
| 17: Call this script to debug at the end of the experiment  | ▷ [38]  |
-

### 3.3 leader\_follower\_static

#### 3.3.1 Leader-Follower Formation Control

This code controls multiple robots in a leader-follower formation. The leader moves towards specified waypoints, and the followers maintain a formation around the leader while avoiding collisions. The control inputs are generated using a Single Integrator model and are then converted to Unicycle commands that are sent to the robots.

```
1 import rps.robotarium as robotarium
2 from rps.utilities.transformations import *
3 from rps.utilities.graph import *
4 from rps.utilities.barrier_certificates import *
5 from rps.utilities.misc import *
6 from rps.utilities.controllers import *
7 import numpy as np
8
9 iterations = 5000 # Run the simulation/experiment for 5000 steps
10
11 N = 4 # Number of robots
12
13 waypoints = np.array([[ -1, 1, 1], [0.8, -0.8, -0.8, 0.8]]) # Waypoints the leader moves to.
14
15 close_enough = 0.03; # How close the leader must get to the waypoint to move to the next one.
16
17 # Create the desired Laplacian
18 followers = -completeGL(N-1)
19 L = np.zeros((N,N))
20 L[1:N,1:N] = followers
21 L[1,1] = L[1,1] + 1
22 L[1,0] = -1
23
24 # Find connections
25 [rows,cols] = np.where(L==1)
26
27 dxi = np.zeros((2,N)) # For computational/memory reasons, initialize the velocity vector
28
29 state = 0 # Initialize leader state
30
31 magnitude_limit = 0.15 # Limit maximum linear speed of any robot
32
33 formation_control_gain = 10 # Gains for the Formation Control
34
35 desired_distance = 0.3 # desired distance between the Robots
36
37 initial_conditions = np.array([[0, 0.5, 0.3, -0.1], [0.5, 0.5, 0.2, 0], [0, 0, 0, 0]]) # Initial Positions
38
39 r = robotarium.Robotarium(number_of_robots=N, show_figure=True, initial_conditions=initial_conditions,
40 ↪ sim_in_real_time=True) # Instantiate the Robotarium
41
42 _, uni_to_si_states = create_si_to_uni_mapping() # Unicycle to Single Integrator States Mapping
43
44 si_to_uni_dyn = create_si_to_uni_dynamics() # Single Integrator to Unicycle Velocity Commands
45
46 si_barrier_cert = create_single_integrator_barrier_certificate_with_boundary() # Single-integrator barrier certificates
47
48 leader_controller = create_si_position_controller(velocity_magnitude_limit=0.1) # Single-integrator position controller
49
50 for t in range(iterations):
51     x = r.get_poses() # Get the poses of robots
52
53     xi = uni_to_si_states(x) # Transform poses to Single Integrator
54
55     # Followers
56     for i in range(1,N):
57         dxi[:,[i]] = np.zeros((2,1)) # Zero velocities
58         neighbors = topological_neighbors(L,i) # Get the topological neighbors of agent i
59
60         for j in neighbors:
61             dxi[:,[i]] += formation_control_gain*(np.power(np.linalg.norm(x[:,2,[j]]-x[:,2,[i]]),
62 ↪ 2)-np.power(desired_distance, 2))*(x[:,2,[j]]-x[:,2,[i]])
63
64     # Leader
65     waypoint = waypoints[:,state].reshape((2,1))
66
67     dxi[:,[0]] = leader_controller(x[:,2,[0]], waypoint)
68     if np.linalg.norm(x[:,2,[0]] - waypoint) < close_enough: # Leader moves to the waypoint and updates to the next one if
69 ↪ close
```

```

68     state = (state + 1) % 4
69
70     # Keep single integrator control vectors under specified magnitude
71     norms = np.linalg.norm(dxi, 2, 0) # Threshold control inputs
72     idxs_to_normalize = (norms > magnitude_limit) # Threshold control inputs
73     dxi[:, idxs_to_normalize] *= magnitude_limit/norms[idxs_to_normalize] # Threshold control inputs
74
75     dxi_safe = si_barrier_cert(dxi, x[:2,:]) # Use Barrier to avoid collision
76
77     dxu_safe = si_to_uni_dyn(dxi_safe, x) # Convert single-integrator to unicycle commands
78
79     r.set_velocities(np.arange(N), dxu_safe) # Set the velocities using unicycle commands
80
81     r.step() # Iterate the simulation
82
83     r.call_at_scripts_end() # Call at end of script to print debug information

```

Listing 7: leader\_follower.py example

---

**Algorithm 6** Pseudo Code leader\_follower.py

---

1: Import important libraries	▷ [1-7]
2: Set the number of iterations and number of robots	▷ [9,11]
3: Define waypoints and the proximity threshold for the leader	▷ [13,15]
4: Create the desired Laplacian matrix for leader-follower formation	▷ [17-25]
5: Initialize the velocity vector for computational/memory reasons	▷ [27]
6: Initialize the leader state	▷ [29]
7: Set the maximum linear speed limit	▷ [31]
8: Define gains and desired distance for formation control	▷ [33-35]
9: Set initial conditions to avoid barrier use at the beginning	▷ [37]
10: Instantiate the Robotarium object with the specified parameters	▷ [39]
11: Create mapping from single integrator states to unicycle states and vice versa.	▷ [41]
12: Create mapping from single integrator velocity commands to unicycle velocity commands	▷ [43]
13: Create barrier certificates to avoid collision	▷ [45]
14: Create single integrator position controller for the leader	▷ [47]
15: <b>for</b> each iteration from 1 to <b>iterations</b> <b>do</b>	
16:     Get the most recent pose information from the Robotarium	▷ [51]
17:     Convert unicycle states to single integrator states	▷ [53]
18: <b>Followers:</b>	
19: <b>for</b> each follower robot $i$ from 1 to $N - 1$ <b>do</b>	
20:             Zero velocities and get the topological neighbors of robot $i$	▷ [57-58]
21: <b>for</b> each neighbor $j$ of robot $i$ <b>do</b>	
22:                 Update the velocity of robot $i$ based on the distance to neighbor $j$	▷ [61]
23: <b>end for</b>	
24: <b>end for</b>	
25: <b>Leader:</b>	
26:         Set the current waypoint for the leader	▷ [64]
27:         Update the velocity of the leader towards the waypoint	▷ [66]
28: <b>if</b> the leader is close enough to the waypoint <b>then</b>	▷ [67]
29:             Move to the next waypoint	▷ [68]
30: <b>end if</b>	
31:         Threshold the control inputs to maintain specified magnitude limit	▷ [71-73]
32:         Use barrier certificates to ensure safe control inputs	▷ [75]
33:         Convert single-integrator inputs to unicycle commands	▷ [77]
34:         Set the velocities of the robots	▷ [79]
35:         Iterate the simulation	▷ [81]
36: <b>end for</b>	
37: Call this script to debug at the end of the experiment	▷ [83]

---



### 3.4 formation\_control.py

#### 3.4.1 Formation Control to Hold the Vertices of a Rectangle

This code controls multiple robots to form a rectangular shape while avoiding collisions. The control inputs are generated using a Single Integrator model and are then converted to Unicycle commands that are sent to the robots. The inter-agent distances are controlled using a weight matrix.

```
1 import rps.robotarium as robotarium
2 from rps.utilities.transformations import *
3 from rps.utilities.graph import *
4 from rps.utilities.barrier_certificates import *
5 from rps.utilities.misc import *
6 from rps.utilities.controllers import *
7
8 # Array representing the geometric distances between the agents. In this case, the agents try to form a Rectangle
9 L = np.array([
10     [3, -1, 0, -1, 0, -1],
11     [-1, 3, -1, 0, -1, 0],
12     [0, -1, 3, -1, 0, -1],
13     [-1, 0, -1, 3, -1, 0],
14     [0, -1, 0, -1, 3, -1],
15     [-1, 0, -1, 0, -1, 3]
16 ])
17
18 d = 0.3 # Desired distance between agent
19 ddiag = np.sqrt(5)*d
20 formation_control_gain = 10 # Desired gain
21
22 # Weight matrix to control inter-agent distances
23 weights = np.array([
24     [0, d, 0, d, 0, ddiag],
25     [d, 0, d, 0, d, 0],
26     [0, d, 0, ddiag, 0, d],
27     [d, 0, ddiag, 0, d, 0],
28     [0, d, 0, d, 0, d],
29     [ddiag, 0, d, 0, d, 0]
30 ])
31
32 iterations = 2000 # Run the simulation/experiment for 2000 steps
33
34 N = 6 # Number of Robots
35
36 magnitude_limit = 0.15 # Limit maximum linear speed of any robot
37
38 r = robotarium.Robotarium(number_of_robots=N, show_figure=True, sim_in_real_time=True) # Instantiate Robotarium object
39
40 si_barrier_cert = create_single_integrator_barrier_certificate_with_boundary() # Barrier certificates to avoid collision
41
42 si_to_uni_dyn = create_si_to_uni_dynamics() # Single Integrator to Unicycle Velocity Commands
43
44 for k in range(iterations):
45
46     x = r.get_poses() # Get the poses of the robots
47
48     dxi = np.zeros((2, N)) # Initialize a velocity vector
49
50     for i in range(N):
51         for j in topological_neighbors(L, i):
52             error = x[:,2, j] - x[:,2, i] # Perform a weighted consensus to make the rectangular shape
53             dxi[:, i] += formation_control_gain*(np.power(np.linalg.norm(error), 2)- np.power(weights[i, j], 2)) * error
54
55     norms = np.linalg.norm(dxi, 2, 0)
56     idxs_to_normalize = (norms > magnitude_limit) # Threshold control inputs
57     dxi[:, idxs_to_normalize] *= magnitude_limit/norms[idxs_to_normalize] # Keep single integrator control vectors under
58     ↪ specified magnitude
59
60     dxi_safe = si_barrier_cert(dxi, x[:,2, :]) # Make sure that the robots don't collide
61
62     dxu_safe = si_to_uni_dyn(dxi_safe, x) # Transform the single-integrator dynamics to unicycle dynamics
63
64     r.set_velocities(np.arange(N), dxu_safe) # Set the velocities of the robots
65
66     r.step() # Iterate the simulation
67
68 r.call_at_scripts_end() # Call at end of script to print debug information
```

Listing 8: formation\_control.py example

---

**Algorithm 7** Pseudo Code `formation_control.py`

---

```
1: Import important libraries ▷ [1-6]
2: Define the Laplacian matrix representing the geometric distances between the agents ▷ [9]
3: Define the gains for the experiment and the desired distances ▷ [18-21]
4: Define the weight matrix to control inter-agent distances ▷ [23]
5: Set the number of iterations and number of robots ▷ [32,34]
6: Set the maximum linear speed limit ▷ [36]
7: Instantiate the Robotarium object with the specified parameters ▷ [38]
8: Create barrier certificates to avoid collision ▷ [40]
9: Create mapping from single integrator velocity commands to unicycle velocity commands ▷ [42]
10: for each iteration from 1 to iterations do
11:     Get the poses of the robots ▷ [46]
12:     Initialize a velocity vector ▷ [49]
13:     for each robot  $i$  from 1 to  $N$  do
14:         for each neighbor  $j$  of robot  $i$  do ▷ [56]
15:             Perform a weighted consensus to make the rectangular shape ▷ [52-53]
16:         end for
17:     end for
18:     Threshold the control inputs to maintain specified magnitude limit ▷ [55-57]
19:     Use barrier certificates to ensure safe control inputs ▷ [59]
20:     Convert single-integrator inputs to unicycle commands ▷ [61]
21:     Set the velocities of the robots ▷ [63]
22:     Iterate the simulation ▷ [65]
23: end for
24: Call this script to debug at the end of the experiment ▷ [67]
```

---

## 3.5 barrier\_certificate

### 3.5.1 Single Integrator Barrier Certificate

This code controls multiple robots to form a circle, switching their positions on the circle a specified number of times. The control inputs are generated using a Single Integrator model and are then converted to Unicycle commands that are sent to the actual robots. Barrier certificates applied to the single integrator control commands ensure safe control inputs to avoid collisions. Note that the safe single integrator control commands (*dxi\_safe*) are transformed to unicycle control commands. Do not use single integrator barrier certificates with unicycle control commands.

```
1 import rps.robotarium as robotarium
2 from rps.utilities.transformations import *
3 from rps.utilities.barrier_certificates import *
4 from rps.utilities.misc import *
5 from rps.utilities.controllers import *
6 import numpy as np
7
8 N = 10 # Number of Robots
9
10 r = robotarium.Robotarium(number_of_robots=N, show_figure=True, sim_in_real_time=True) # Instantiate the Robotarium object
11
12 num_cycles = 2 # Number times Robots form circle
13
14 count = -1 # Number times they have formed the circle (starts at -1 since initial formation will increment the count)
15
16 si_barrier_cert = create_single_integrator_barrier_certificate() # Create barrier certificates to avoid collision
17
18 si_position_controller = create_si_position_controller() # Create single integrator position controller
19
20 si_to_uni_dyn, uni_to_si_states = create_si_to_uni_mapping() # Create SI to UNI dynamics transformation
21
22 # Generates points on a circle inscribed in a 6x6 square centered at the origin. Robots swap positions on the circle.
23 radius = 1
24 xybound = radius * np.array([-1, 1, -1, 1])
25 p_theta = 2 * np.pi * (np.arange(0, 2 * N, 2) / (2 * N))
26 p_circ = np.vstack([
27     np.hstack([xybound[1] * np.cos(p_theta), xybound[1] * np.cos(p_theta + np.pi)]),
28     np.hstack([xybound[3] * np.sin(p_theta), xybound[3] * np.sin(p_theta + np.pi)])
29 ])
30
31 flag = 0 # These variables are so we can tell when the robots should switch positions on the circle.
32 x_goal = p_circ[:, :N]
33
34 while(1): # While True
35
36     x = r.get_poses() # Get the poses of robots
37
38     x_si = uni_to_si_states(x) # Transform unicycle state to Single Integrator state.
39
40     si_velocities = np.zeros((2, N)) # Initialize a velocities variable
41
42     if(np.linalg.norm(x_goal - x_si) < 0.05): # If all the agent are close enough to the goals
43         flag = 1 - flag # Change
44         count += 1 # Increase the counter
45
46     if count == num_cycles: # if the robots did the circle twice
47         break # End the Experiment
48
49     if(flag == 0): # If 0, we change the goal to the other side of the circle
50         x_goal = p_circ[:, :N]
51     else:
52         x_goal = p_circ[:, N:] # If 1, we change the goal to the other side of the circle
53
54     dxi = si_position_controller(x_si, x_goal) # Use a position controller to drive to the goal position
55
56     dxi_safe = si_barrier_cert(dxi, x_si) # Use the barrier certificates to make sure that the agents don't collide
57
58     dxu_safe = si_to_uni_dyn(dxi_safe, x) # Use the second single-integrator-to-unicycle mapping to map to unicycle
59     ↪ dynamics
60
61     r.set_velocities(np.arange(N), dxu_safe) # Set the velocities of agents 1,...,N to dxu_safe
62
63     r.step() # Iterate the simulation
64
65 r.call_at_scripts_end() # Call at end of script to print debug information
```

Listing 9: `barrier_certificate.py` example

---

**Algorithm 8** Pseudo Code `barrier_certificate.py`

---

1: Import important libraries	▷ [1-6]
2: Set the number of robots for the simulation	▷ [8]
3: Instantiate the Robotarium object with the specified parameters	▷ [10]
4: Define the number of cycles for the circle formation and initialize the count	▷ [12,14]
5: Create single integrator barrier certificates	▷ [16]
6: Create single integrator position controller	▷ [18]
7: Create mapping from single integrator states to unicycle states and vice versa.	▷ [20]
8: Generate points on a circle inscribed in a 6x6 square centered on the origin	▷ [22-29]
9: Initialize variables to manage goal switching	▷ [31-33]
10: <b>while</b> True <b>do</b>	
11:     Get the poses of the agents	▷ [37]
12:     Convert unicycle states to single integrator states	▷ [39]
13:     Initialize a velocities variable	▷ [41]
14: <b>if</b> all agents are close enough to the goals <b>then</b>	
15:         Switch the goal flag and increment the count	▷ [44-45]
16: <b>end if</b>	
17: <b>if</b> count equals the number of cycles <b>then</b>	
18:         Break the loop	▷ [48]
19: <b>end if</b>	
20:     Switch goals based on the flag state	▷ [50-53]
21:     Use the position controller to drive to the goal position	▷ [55]
22:     Use the barrier certificates to avoid collisions	▷ [57]
23:     Map single-integrator inputs to unicycle dynamics	▷ [59]
24:     Set the velocities of the robots	▷ [61]
25:     Iterate the simulation	▷ [63]
26: <b>end while</b>	
27: Call this script to debug at the end of the experiment	▷ [65]

---

### 3.5.2 Robots Moving Towards Unreachable Goals with Single-Integrator Model

This code controls multiple robots to move towards goal points that are outside the arena. The robots will never reach these goal points, and the simulation will run for a specified number of iterations. The control inputs are generated using a Single Integrator model and are then converted to Unicycle commands for actual movement. Barrier certificates applied to the single integrator control commands ensure safe control inputs to avoid collisions. Note that the safe single integrator control commands ( $dx_{i\_safe}$ ) are transformed to unicycle control commands. Do not use single integrator barrier certificates with unicycle control commands.

```
1 import rps.robotarium as robotarium
2 from rps.utilities.transformations import *
3 from rps.utilities.barrier_certificates import *
4 from rps.utilities.misc import *
5 from rps.utilities.controllers import *
6 import numpy as np
7
8 N = 5 # Number of Robots
9
10 initial_conditions = np.array(np.mat('1 0.5 -0.5 0 0.28; 0.8 -0.3 -0.75 0.1 0.34; 0 0 0 0 0')) # Initial positions
11
12 r = robotarium.Robotarium(number_of_robots=N, show_figure=True, initial_conditions=initial_conditions,
13 ↪ sim_in_real_time=True) # Instantiate Robotarium object
14
15 iterations = 3000 # Run the simulation/experiment for 3000 steps
16
17 goal_points = np.array(np.mat('5 -5 5 -5 5; 5 5 -5 -5 5; 0 0 0 0 0')) # Goal points
18
19 si_position_controller = create_si_position_controller() # Create single integrator position controller
20
21 si_to_uni_dyn, uni_to_si_states = create_si_to_uni_mapping() # Create SI to UNI dynamics transformation
22
23 si_barrier_cert = create_single_integrator_barrier_certificate_with_boundary() # Create barrier certificates to avoid
24 ↪ collision
25
26 x = r.get_poses() # Get the poses of robots
27
28 r.step() # Iterate the simulation
29
30 # While the Robots are not in the goal points
31 for i in range(iterations):
32
33     x = r.get_poses() # Get the poses of robots
34
35     xi = uni_to_si_states(x) # Transform unicycle states to single integrator
36
37     dxi = si_position_controller(xi, goal_points[:2, :]) # Create single-integrator control inputs
38
39     dxi_safe = si_barrier_cert(dxi, xi) # Create safe control inputs (i.e., no collisions)
40
41     dxu_safe = si_to_uni_dyn(dxi_safe, x) # Map the single integrator back to unicycle dynamics
42
43     r.set_velocities(np.arange(N), dxu_safe) # Set the velocities of agents 1,...,N to dxu_safe
44
45     r.step() # Iterate the simulation
46
47 r.call_at_scripts_end() # Call at end of script to print debug information
```

Listing 10: si\_barriers\_with\_boundary.py example

---

**Algorithm 9** Pseudo Code `si_barriers_with_boundary.py`

---

1: Import important libraries	▷ [1-6]
2: Set the number of robots for the simulation	▷ [8]
3: Define the initial positions of the robots	▷ [10]
4: Instantiate the Robotarium object with the specified parameters	▷ [12]
5: Set the number of iterations for the simulation	▷ [14]
6: Define goal points outside of the arena	▷ [16]
7: Create single integrator position controller	▷ [18]
8: Create SI to UNI dynamics transformation	▷ [20]
9: Create barrier certificates to avoid collision	▷ [22]
10: Get initial poses of the robots	▷ [24]
11: Step the simulation to update visualization	▷ [26]
12: <b>for</b> each iteration from 1 to <b>iterations</b> <b>do</b>	
13:     Get the current poses of the robots	▷ [31]
14:     Convert unicycle states to single integrator states	▷ [33]
15:     Create single-integrator control inputs	▷ [35]
16:     Use barrier certificates to ensure safe control inputs	▷ [37]
17:     Map single-integrator inputs to unicycle dynamics	▷ [39]
18:     Set the velocities of the robots	▷ [41]
19:     Iterate the simulation	▷ [43]
20: <b>end for</b>	
21: Call this script to debug at the end of the experiment	▷ [45]

---

### 3.5.3 Robots Moving Towards Unreachable Goals with Unicycle Model

This code controls multiple robots to move towards goal points that are outside the arena using a unicycle model. The robots will never reach these goal points, and the simulation will run for a specified number of iterations. The control inputs are generated using a Unicycle model. Barrier certificates ensure safe control inputs to avoid collisions. Since we did not specify the initial position, the robots start in random positions. Barrier certificates applied to the single integrator control commands ensure safe control inputs to avoid collisions. Do not use unicycle model barrier certificates with single integrator control commands.

```
1 import rps.robotarium as robotarium
2 from rps.utilities.transformations import *
3 from rps.utilities.barrier_certificates import *
4 from rps.utilities.misc import *
5 from rps.utilities.controllers import *
6 import numpy as np
7
8 N = 5 # Number of Robots
9
10 r = robotarium.Robotarium(number_of_robots=N, show_figure=True, sim_in_real_time=True) # Instantiate Robotarium object
11
12 iterations = 3000 # Run the simulation/experiment for 3000 steps
13
14 goal_points = np.array(np.mat('5 5 5 5 5; 5 5 5 5 5; 0 0 0 0 0')) # Goal points
15
16 unicycle_position_controller = create_clf_unicycle_position_controller() # Create unicycle position controller
17
18 uni_barrier_cert = create_unicycle_barrier_certificate_with_boundary() # Create barrier certificates to avoid collision
19
20 x = r.get_poses() # Get the poses of robots
21
22 r.step() # Iterate the simulation
23
24 for i in range(iterations):
25
26     x = r.get_poses() # Get the poses of robots
27
28     dxu = unicycle_position_controller(x, goal_points[:2][:]) # Create unicycle control inputs
29
30     dxu_safe = uni_barrier_cert(dxu, x) # Create safe control inputs (i.e., no collisions)
31
32     r.set_velocities(np.arange(N), dxu_safe) # Set the velocities of agents 1,...,N to dxu_safe
33
34     r.step() # Iterate the simulation
35
36 r.call_at_scripts_end() # Call at end of script to print debug information
```

Listing 11: uni\_barriers\_with\_boundary.py example



---

**Algorithm 10** Pseudo Code `uni_barriers_with_boundary.py`

---

1: Import important libraries	▷ [1-6]
2: Set the number of robots for the simulation	▷ [8]
3: Instantiate the Robotarium object with the specified parameters	▷ [10]
4: Set the number of iterations for the simulation	▷ [12]
5: Define goal points outside of the arena	▷ [14]
6: Create unicycle position controller	▷ [16]
7: Create barrier certificates to avoid collision	▷ [18]
8: Get initial poses of the robots	▷ [20]
9: Step the simulation to update visualization	▷ [22]
10: <b>for</b> each iteration from 1 to <b>iterations</b> <b>do</b>	
11:     Get the current poses of the robots	▷ [26]
12:     Create unicycle control inputs	▷ [28]
13:     Use barrier certificates to ensure safe control inputs	▷ [30]
14:     Set the velocities by mapping the single-integrator inputs to unicycle inputs	▷ [32]
15:     Iterate the simulation	▷ [34]
16: <b>end for</b>	
17: Call this script to debug at the end of the experiment	▷ [36]

---

### 3.5.4 Robots Moving Towards Unreachable Goals with Unicycle Differential Drive Model

This code controls multiple robots to move towards goal points that are outside the arena using a unicycle model and a unicycle model barrier certificate that is mapped to the wheel velocities of the differential drive robot. These barriers are more conservative than the single integrator or unicycle barrier certificates previously as they account for noise in the motors. The robots will never reach these goal points, and the simulation will run for a specified number of iterations. The control inputs are generated using a Unicycle model. Barrier certificates ensure safe control inputs to avoid collisions.

```

1  import rps.robotarium as robotarium
2  from rps.utilities.transformations import *
3  from rps.utilities.barrier_certificates import *
4  from rps.utilities.misc import *
5  from rps.utilities.controllers import *
6  import numpy as np
7
8  N = 5 # Number of Robots
9
10 r = robotarium.Robotarium(number_of_robots=N, show_figure=True, sim_in_real_time=True) # Instantiate Robotarium object
11
12 iterations = 3000 # Run the simulation/experiment for 3000 steps
13
14 goal_points = np.array(np.mat('5 5 5 5 5; 5 5 5 5 5; 0 0 0 0 0')) # Goal Points
15
16 unicycle_position_controller = create_clf_unicycle_position_controller() # Create unicycle position controller
17
18 uni_barrier_cert = create_unicycle_differential_drive_barrier_certificate_with_boundary() # Create barrier certificates to
    ↪ avoid collision
19
20 x = r.get_poses() # Get the poses of robots
21
22 r.step() # Iterate the simulation
23
24 for i in range(iterations):
25
26     x = r.get_poses() # Get the poses of robots
27
28     dxu = unicycle_position_controller(x, goal_points[:2][:]) # Create unicycle control inputs
29
30     dxu_safe = uni_barrier_cert(dxu, x) # Create safe control inputs (i.e., no collisions)
31
32     r.set_velocities(np.arange(N), dxu_safe) # Set the velocities of agents 1,...,N to dxu_safe
33
34     r.step() # Iterate the simulation
35
36 r.call_at_scripts_end() # Call at end of script to print debug information

```

Listing 12: uni\_dd\_barriers\_with\_boundary.py example

---

#### Algorithm 11 Pseudo Code uni\_dd\_barriers\_with\_boundary.py

---

- |   |         |
|---|---------|
| 1: Import important libraries   | ▷ [1-6] |
| 2: Set the number of robots for the simulation  | ▷ [8]   |
| 3: Instantiate the Robotarium object with the specified parameters                    | ▷ [10]  |
| 4: Set the number of iterations for the simulation                                    | ▷ [12]  |
| 5: Define goal points outside of the arena  | ▷ [14]  |
| 6: Create unicycle position controller  | ▷ [16]  |
| 7: Create barrier certificates to avoid collision                                     | ▷ [18]  |
| 8: Get initial poses of the robots  | ▷ [20]  |
| 9: Step the simulation to update visualization  | ▷ [22]  |
| 10: <b>for</b> each iteration from 1 to <b>iterations</b> <b>do</b>                   |         |
| 11:     Get the current poses of the robots   | ▷ [26]  |
| 12:     Create unicycle control inputs  | ▷ [28]  |
| 13:     Use barrier certificates to ensure safe control inputs                        | ▷ [30]  |
| 14:     Set the velocities by mapping the single-integrator inputs to unicycle inputs | ▷ [32]  |
| 15:     Iterate the simulation  | ▷ [34]  |
| 16: <b>end for</b>  |         |
-

## 3.6 data\_saving

### 3.6.1 Leader-Follower Formation with Data Saving

This code controls multiple robots in a leader-follower formation. The leader moves towards specified waypoints, and the followers maintain a formation. The control inputs are generated using a Single Integrator model and are then converted to Unicycle commands that are sent to the robots. Barrier certificates ensure safe control inputs to avoid collisions. Additionally, the code saves data on the distance between connected robots and the distance between the leader and the goal location when the goal is reached. Two data sets will be saved, one saving the distance between connected robots through time, and another with the distance between the leader and goal location when the goal is "reached". They will each be saved as .npz files and human readable csv .txt files.

```
1  import rps.robotarium as robotarium
2  from rps.utilities.transformations import *
3  from rps.utilities.graph import *
4  from rps.utilities.barrier_certificates import *
5  from rps.utilities.misc import *
6  from rps.utilities.controllers import *
7  import numpy as np
8  import time
9
10 iterations = 5000 # Run the simulation/experiment for 5000 steps
11
12 N = 4 # Number of robots
13
14 waypoints = np.array([[ -1, -1, 1, 1],[0.8, -0.8, -0.8, 0.8]]) # Waypoints the leader moves to.
15
16 close_enough = 0.03; # How close the leader must get to the waypoint to move to the next one.
17
18 # Preallocate data saving
19 robot_distance = np.zeros((5,iterations)) # Saving 4 inter-robot distances and time
20 goal_distance = np.empty((0,2))
21 start_time = time.time()
22
23 # Create the desired Laplacian
24 followers = -completeGL(N-1)
25 L = np.zeros((N,N))
26 L[1:N,1:N] = followers
27 L[1,1] = L[1,1] + 1
28 L[1,0] = -1
29
30 # Find connections
31 [rows,cols] = np.where(L==1)
32
33 dxi = np.zeros((2,N)) # For computational/memory reasons, initialize the velocity vector
34
35 state = 0 # Initialize leader state
36
37 magnitude_limit = 0.15 # Limit maximum linear speed of any robot
38
39 formation_control_gain = 10 # Gains for the Formation Control
40
41 desired_distance = 0.3 # Desired distance between the Robots
42
43 initial_conditions = np.array([[0, 0.5, 0.3, -0.1],[0.5, 0.5, 0.2, 0],[0, 0, 0, 0]]) # Initial Positions
44
45 r = robotarium.Robotarium(number_of_robots=N, show_figure=True, initial_conditions=initial_conditions,
46 ↪  sim_in_real_time=True) # Instantiate the Robotarium
47
48 _, uni_to_si_states = create_si_to_uni_mapping() # Unicycle to Single Integrator States Mapping
49
50 si_to_uni_dyn = create_si_to_uni_dynamics() # Single Integrator to Unicycle Velocity Commands
51
52 si_barrier_cert = create_single_integrator_barrier_certificate_with_boundary() # Single-integrator barrier certificates
53
54 leader_controller = create_si_position_controller(velocity_magnitude_limit=0.1) # Single-integrator position controller
55
56 for t in range(iterations):
57     x = r.get_poses() # Get the pose of robots
58
59     xi = uni_to_si_states(x) # Transform poses to Single Integrator
60
61     # Followers
62     for i in range(1, N):
```

```

63     dxi[:, [i]] = np.zeros((2, 1)) # Zero velocities
64     neighbors = topological_neighbors(L, i) # Get the topological neighbors of agent i
65
66     for j in neighbors:
67         dxi[:, [i]] += formation_control_gain * (np.power(np.linalg.norm(x[:2, [j]] - x[:2, [i]]), 2) -
68             ↪ np.power(desired_distance, 2)) * (x[:2, [j]] - x[:2, [i]])
69
70     # Leader
71     waypoint = waypoints[:, state].reshape((2, 1))
72
73     dxi[:, [0]] = leader_controller(x[:2, [0]], waypoint)
74     if np.linalg.norm(x[:2, [0]] - waypoint) < close_enough: # Leader moves to the waypoint and updates to the next one if
75         ↪ close
76         state = (state + 1) % 4
77         goal_distance = np.append(goal_distance, np.array([[np.linalg.norm(xi[:, [0]] - waypoint)], [time.time() -
78             ↪ start_time]]))
79
80     # Keep single integrator control vectors under specified magnitude
81     norms = np.linalg.norm(dxi, 2, 0) # Threshold control inputs
82     idxs_to_normalize = (norms > magnitude_limit) # Threshold control inputs
83     dxi[:, idxs_to_normalize] *= magnitude_limit / norms[idxs_to_normalize] # Threshold control inputs
84
85     dxi_safe = si_barrier_cert(dxi, x[:2, :]) # Use Barrier to avoid collision
86
87     dxu_safe = si_to_uni_dyn(dxi_safe, x) # Convert single-integrator to unicycle commands
88
89     r.set_velocities(np.arange(N), dxu_safe) # Set the velocities using unicycle commands
90
91     # Compute data to be saved and stored in matrix (Distance between connected robots)
92     robot_distance[0, t] = np.linalg.norm(xi[:, [0]] - xi[:, [1]])
93     robot_distance[4, t] = time.time() - start_time
94     for j in range(1, int(len(rows) / 2) + 1):
95         robot_distance[j, t] = np.linalg.norm(xi[:, [rows[j]]] - xi[:, [cols[j]]])
96
97     r.step() # Iterate the simulation
98
99     # Save Data Locally as Numpy
100     np.save('goal_distance_data', goal_distance)
101     np.save('inter_robot_distance_data', robot_distance)
102
103     # Save Data Locally as CSV Text File
104     np.savetxt('goal_distance_data.txt', goal_distance, delimiter=',')
105     np.savetxt('inter_robot_distance_data.txt', robot_distance.T, delimiter=',')
106
107     # Call at end of script to print debug information
108     r.call_at_scripts_end()

```

Listing 13: leader\_follower\_data\_saving.py example

---

**Algorithm 12** Pseudo Code `leader_follower_data_saving.py`

---

1: Import important libraries	▷ [1-8]
2: Set experiment constants, including the number of iterations and robots	▷ [10, 12]
3: Define waypoints for the leader and the distance threshold to switch waypoints	▷ [14,16]
4: Preallocate data arrays for saving distances	▷ [19-21]
5: Create the desired Laplacian for the formation	▷ [24-28]
6: Find connections between robots	▷ [31]
7: Initialize the velocity vector for computational efficiency	▷ [33]
8: Initialize leader state and set maximum linear speed	▷ [35,37]
9: Create gains for the formation control algorithm and set desired distances	▷ [39,41]
10: Define initial conditions to avoid barrier use at the beginning	▷ [43]
11: Instantiate the Robotarium object with the specified parameters	▷ [45]
12: Create mapping from single integrator states to unicycle states and vice versa.	▷ [47]
13: Single Integrator to Unicycle Velocity Commands	▷ [49]
14: Create barrier certificates to avoid collision	▷ [51]
15: Create single integrator position controller	▷ [53]
16: <b>for</b> each iteration from 1 to <b>iterations</b> <b>do</b>	
17:     Get the most recent pose information from the Robotarium	▷ [57]
18:     Convert unicycle poses to single-integrator poses	▷ [59]
19: <b>for</b> each follower robot $i$ from 1 to $N - 1$ <b>do</b>	
20:         Initialize the velocity vector for robot $i$	▷ [63]
21:         Get the topological neighbors of robot $i$	▷ [64]
22: <b>for</b> each neighbor $j$ of robot $i$ <b>do</b>	
23:             Perform formation control to maintain desired distances	▷ [67]
24: <b>end for</b>	
25: <b>end for</b>	
26:     Set the waypoint for the leader	▷ [70]
27:     Use the position controller to drive the leader to the waypoint	▷ [72]
28: <b>if</b> leader is close enough to the waypoint <b>then</b>	
29:         Update the state and save goal distance data	▷ [73-75]
30: <b>end if</b>	
31:     Threshold control inputs to maintain specified magnitude limit	▷ [78-80]
32:     Use barrier certificates to ensure safe control inputs	▷ [82]
33:     Convert single-integrator inputs to unicycle commands	▷ [84]
34:     Set the velocities of the robots	▷ [86]
35:     Save inter-robot distance data	▷ [89-92]
36:     Iterate the simulation	▷ [94]
37: <b>end for</b>	
38: Save data locally as Numpy and CSV text files	▷ [97-102]
39: Call this script to debug at the end of the experiment	▷ [105]

---

## 3.7 consensus

### 3.7.1 Consensus Algorithm for Multiple Robots

This code controls multiple robots to achieve consensus on their positions using a cycle graph Laplacian. The robots use Single Integrator dynamics for control inputs and Unicycle dynamics for actual movement. Barrier certificates ensure safe control inputs to avoid collisions and prevent robots from driving off the testbed.

```
1  import rps.robotarium as robotarium
2  from rps.utilities.graph import *
3  from rps.utilities.transformations import *
4  from rps.utilities.barrier_certificates import *
5  from rps.utilities.misc import *
6  from rps.utilities.controllers import *
7  import numpy as np
8
9  N = 12 # Number of robots
10
11  r = robotarium.Robotarium(number_of_robots=N, show_figure=True, sim_in_real_time=True) # Instantiate Robotarium object
12
13  iterations = 1000 # Run the simulation/experiment for 1000 steps
14
15  si_barrier_cert = create_single_integrator_barrier_certificate_with_boundary() # Single-integrator barrier certificates
16
17  si_to_uni_dyn, uni_to_si_states = create_si_to_uni_mapping() # Create SI to UNI dynamics transformation
18
19  L = cycle_GL(N) # Generated a connected graph Laplacian (for a cycle graph).
20
21  for k in range(iterations):
22
23      x = r.get_poses() # Get the poses of the robots
24
25      x_si = uni_to_si_states(x) # Convert to single-integrator poses
26
27      si_velocities = np.zeros((2, N)) # Initialize the single-integrator control inputs
28
29      for i in range(N): # For each robot...
30
31          j = topological_neighbors(L, i) # Get the neighbors of robot 'i' (encoded in the graph Laplacian)
32
33          si_velocities[:, i] = np.sum(x_si[:, j] - x_si[:, i, None], 1) # Compute the consensus algorithm
34
35      si_velocities_safe = si_barrier_cert(si_velocities, x_si) # Use the barrier certificate to avoid collisions
36
37      dxu_safe = si_to_uni_dyn(si_velocities_safe, x) # Transform single integrator to unicycle
38
39      r.set_velocities(np.arange(N), dxu_safe) # Set the velocities of agents 1,...,N to dxu_safe
40
41      r.step() # Iterate the simulation
42
43  r.call_at_scripts_end() # Call at end of script to print debug information
```

Listing 14: consensus.py example

---

**Algorithm 13** Pseudo Code `consensus.py`

---

1: Import important libraries	▷ [1-7]
2: Set the number of robots for the simulation	▷ [9]
3: Instantiate the Robotarium object with the specified parameters	▷ [11]
4: Set the number of iterations for the simulation	▷ [13]
5: Create barrier certificates to avoid collisions	▷ [15]
6: Create mapping from single integrator states to unicycle states and vice versa	▷ [17]
7: Generate a connected graph Laplacian for a cycle graph	▷ [19]
8: <b>for</b> each iteration from 1 to <b>iterations</b> <b>do</b>	
9:     Get the current poses of the robots	▷ [23]
10:     Convert unicycle states to single integrator states	▷ [25]
11:     Initialize the single-integrator control inputs	▷ [27]
12: <b>for</b> each robot $i$ from 1 to $N$ <b>do</b>	
13:         Get the neighbors of robot $i$ (encoded in the graph Laplacian)	▷ [31]
14:         Compute the consensus algorithm	▷ [33]
15: <b>end for</b>	
16:     Use the barrier certificate to avoid collisions	▷ [35]
17:     Transform single-integrator control inputs to unicycle commands	▷ [37]
18:     Set the velocities of the robots	▷ [39]
19:     Iterate the simulation	▷ [41]
20: <b>end for</b>	
21: Call this script to print debug information and for your script to run on the Robotarium	▷ [43]

---

### 3.7.2 Consensus Algorithm for Multiple Robots with Magnitude Limit

This code controls multiple robots to achieve consensus on their positions using a cycle graph Laplacian. The robots use Single Integrator dynamics for control inputs and Unicycle dynamics for actual movement. Barrier certificates ensure safe control inputs to avoid collisions and prevent robots from driving off the testbed. Additionally, control inputs are kept within a specified magnitude limit.

```
1  import rps.robotarium as robotarium
2  from rps.utilities.graph import *
3  from rps.utilities.transformations import *
4  from rps.utilities.barrier_certificates import *
5  from rps.utilities.misc import *
6  from rps.utilities.controllers import *
7  import numpy as np
8
9  N = 12 # Number of robots
10
11  r = robotarium.Robotarium(number_of_robots=N, show_figure=True, sim_in_real_time=True) # Instantiate Robotarium object
12
13  iterations = 1000 # Run the simulation/experiment for 1000 steps
14
15  magnitude_limit = 0.15 # Maximum linear speed of robot specified by motos
16
17  si_barrier_cert = create_single_integrator_barrier_certificate_with_boundary() # Single-integrator barrier certificates
18
19  si_to_uni_dyn, uni_to_si_states = create_si_to_uni_mapping() # Create SI to UNI dynamics transformation
20
21  L = cycle_GL(N) # Generated a connected graph Laplacian (for a cycle graph).
22
23  for k in range(iterations):
24
25      x = r.get_poses() # Get the poses of robots
26
27      x_si = uni_to_si_states(x) # Convert to single-integrator poses
28
29      si_velocities = np.zeros((2, N)) # Initialize the single-integrator control inputs
30
31      for i in range(N): # For each robot...
32
33          j = topological_neighbors(L, i) # Get the neighbors of robot 'i' (encoded in the graph Laplacian)
34
35          si_velocities[:, i] = np.sum(x_si[:, j] - x_si[:, i, None], 1) # Compute the consensus algorithm
36
37          dxi = si_velocities[:, i]
38
39          # Keep single integrator control vectors under specified magnitude
40          norms = np.linalg.norm(dxi, 2, 0)
41          idxs_to_normalize = (norms > magnitude_limit) # Threshold control inputs
42          dxi[:, idxs_to_normalize] *= magnitude_limit/norms[idxs_to_normalize]
43
44          si_velocities_safe = si_barrier_cert(si_velocities, x_si) # Use the barrier certificate to avoid collisions
45
46          dxu_safe = si_to_uni_dyn(si_velocities_safe, x) # Transform single integrator to unicycle
47
48          r.set_velocities(np.arange(N), dxu_safe) # Set the velocities of agents 1,...,N to dxu_safe
49
50          r.step() # Iterate the simulation
51
52  r.call_at_scripts_end() # Call at end of script to print debug information
```

Listing 15: consensus\_fewer\_errors.py example



---

**Algorithm 14** Pseudo Code `consensus_fewer_errors.py`

---

1: Import important libraries	▷ [1-7]
2: Set the number of robots for the simulation	▷ [9]
3: Instantiate the Robotarium object with the specified parameters	▷ [11]
4: Set the number of iterations for the simulation	▷ [13]
5: Define the maximum linear speed of the robots	▷ [15]
6: Create barrier certificates to avoid collisions	▷ [17]
7: Create mapping from single integrator states to unicycle states and vice versa	▷ [19]
8: Generate a connected graph Laplacian for a cycle graph	▷ [21]
9: <b>for</b> each iteration from 1 to <b>iterations</b> <b>do</b>	
10:     Get the current poses of the robots	▷ [25]
11:     Convert unicycle states to single integrator states	▷ [27]
12:     Initialize the single-integrator control inputs	▷ [29]
13: <b>for</b> each robot $i$ from 1 to $N$ <b>do</b>	
14:         Get the neighbors of robot $i$ (encoded in the graph Laplacian)	▷ [33]
15:         Compute the consensus algorithm	▷ [35]
16:         Get the velocity vector of Robots	▷ [37]
17: <b>end for</b>	
18:     Keep single-integrator control vectors under specified magnitude limit	▷ [40-42]
19:     Use the barrier certificate to avoid collisions	▷ [44]
20:     Transform single-integrator control inputs to unicycle commands	▷ [46]
21:     Set the velocities of the robots	▷ [48]
22:     Iterate the simulation	▷ [50]
23: <b>end for</b>	
24: Call this script to print debug information and for your script to run on the Robotarium	▷ [52]

---

## 3.8 plotting

### 3.8.1 Robots Form a Circle and Switch Positions with Plotting

This code controls multiple robots to form a circle and switch positions while avoiding collisions using Single Integrator dynamics for control inputs and Unicycle dynamics for actual movement. Barrier certificates ensure safe control inputs, and plotting parameters are used for visualization.

```
1  import rps.robotarium as robotarium
2  from rps.utilities.transformations import *
3  from rps.utilities.barrier_certificates import *
4  from rps.utilities.misc import *
5  from rps.utilities.controllers import *
6  import numpy as np
7  import time
8
9  N = 10 # Number of robots
10
11  r = robotarium.Robotarium(number_of_robots=N, show_figure=True, sim_in_real_time=True) # Instantiate the Robotarium object
12  ↪ with these parameters
13
14  num_cycles=2 # How many times should the robots form the circle?
15
16  count = -1 # How many times have they formed the circle? (starts at -1 since initial formation will increment the count)
17
18  safety_radius = 0.17 # Default Barrier Parameters
19
20  # Plotting Parameters
21  CM = np.random.rand(N,3) # Random Colors array for plotting
22  safety_radius_marker_size = determine_marker_size(r,safety_radius) # Will scale the plotted markers to be the diameter of
23  ↪ provided argument (in meters)
24  font_height_meters = 0.1
25  font_height_points = determine_font_size(r,font_height_meters) # Will scale the plotted font height to that of the provided
26  ↪ argument (in meters)
27
28  x=r.get_poses() # Get the poses of robots
29
30  g = r.axes.scatter(x[0,:], x[1,:], s=np.pi/4*safety_radius_marker_size, marker='o',
31  ↪ facecolors='none',edgecolors=CM,linewidth=7) # Initial plots
32
33  #g = r.axes.plot(x[0,:], x[1:], markersize=safety_radius_marker_size, linestyle='none', marker='o', markerfacecolor='none',
34  ↪ markeredgecolor=CM,linewidth=7)
35
36  r.step() # Iterate the Simulation
37
38  si_barrier_cert = create_single_integrator_barrier_certificate() # Single-integrator barrier certificates
39
40  si_position_controller = create_si_position_controller() # Create single integrator position controller
41
42  si_to_uni_dyn, uni_to_si_states = create_si_to_uni_mapping() # Create SI to UNI dynamics tranformation
43
44  # This portion of the code generates points on a circle enscribed in a 6x6 square that's centered on the origin. The robots
45  ↪ switch positions on the circle.
46  xybound = np.array([-1.2, 1.2, -1, 1])
47  p_theta = 2*np.pi*(np.arange(0, 2*N, 2)/(2*N))
48  p_circ = np.vstack([
49  ↪ np.hstack([xybound[1]*np.cos(p_theta), xybound[1]*np.cos(p_theta+np.pi)]),
50  ↪ np.hstack([xybound[3]*np.sin(p_theta), xybound[3]*np.sin(p_theta+np.pi)])
51  ↪ ])
52
53  # These variables are so we can tell when the robots should switch positions on the circle.
54  flag = 0
55  x_goal = p_circ[:, :N]
56
57  while(1): # While True
58
59  ↪ x = r.get_poses() # Get the poses of the robots
60
61  ↪ # Update Plotted Visualization
62  ↪ g.set_offsets(x[:,2:].T)
63  ↪ # This updates the marker sizes if the figure window size is changed. This should be removed when submitting to the
64  ↪ Robotarium.
65  ↪ g.set_sizes([determine_marker_size(r,safety_radius)])
66
67  ↪ x_si = uni_to_si_states(x) # Single-integrator to unicycle mapping
68
69  ↪ si_velocities = np.zeros((2, N)) # Initialize a velocities variable
```

```

64     if(np.linalg.norm(x_goal - x_si) < 0.05): # Check if all the agents are close enough to the goals
65         flag = 1-flag
66         count += 1
67
68     if count == num_cycles: # If True, end simulation
69         break
70
71     # Switch goals depending on the state of flag (goals switch to opposite sides of the circle)
72     if(flag == 0):
73         x_goal = p_circ[:, :N]
74     else:
75         x_goal = p_circ[:, N:]
76
77     dxi = si_position_controller(x_si,x_goal) # Use a position controller to drive to the goal position
78
79     dxi_safe = si_barrier_cert(dxi, x_si) # Use the barrier certificates to make sure that the agents don't collide
80
81     dxu_safe = si_to_uni_dyn(dxi_safe, x) # Single-integrator-to-unicycle mapping
82
83     r.set_velocities(np.arange(N), dxu_safe) # Set the velocities of agents 1,...,N to dxu_safe
84
85     r.step() # Iterate the simulation
86
87     # Caption before finishing the simulation
88     finished_caption = "All robots safely reached \n their destination"
89     finished_label = r.axes.text(0,0,finished_caption,fontsize=font_height_points,
90     ↪ color='k',fontweight='bold',horizontalalignment='center',verticalalignment='center',zorder=20)
91     r.step()
92     time.sleep(5)
93     r.call_at_scripts_end() # Call at end of script to print debug information

```

Listing 16: barrier\_certificates\_with\_plotting.py example

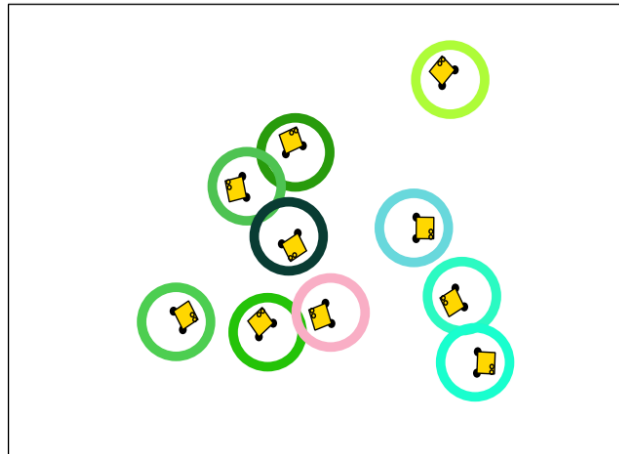


Figure 19: Barrier Certificates with Plotting

---

**Algorithm 15** Pseudo Code `barrier_certificates_with_plotting.py`

---

1: Import important libraries	▷ [1-7]
2: Set the number of robots for the simulation	▷ [9]
3: Instantiate the Robotarium object with the specified parameters	▷ [11]
4: Set the number of cycles the robots should form the circle	▷ [13,15]
5: Define default barrier parameters	▷ [17]
6: Create array with different colors	▷ [20]
7: Create the appropriate Marker Size	▷ [21]
8: Create the appropriate Font Size	▷ [23]
9: Get the current pose of the robots	▷ [25]
10: Initialize plots for robot positions	▷ [27]
11: Iterate the simulation	▷ [31]
12: Create barrier certificates to avoid collisions	▷ [33]
13: Create single integrator position controller	▷ [35]
14: Create mapping from single integrator states to unicycle states and vice versa	▷ [37]
15: Generate points on a circle inscribed in a 6x6 square	▷ [40-45]
16: Set initial goals and flags for switching positions	▷ [48-49]
17: <b>while</b> True <b>do</b>	
18:     Get the current poses of the robots	▷ [53]
19:     Update plotted visualization	▷ [56-58]
20:     Convert unicycle states to single integrator states	▷ [60]
21:     Initialize the single-integrator control inputs	▷ [62]
22: <b>if</b> all agents are close enough to the goals <b>then</b>	
23:         Switch the flag and increment the count	▷ [65-66]
24: <b>end if</b>	
25: <b>if</b> count equals the number of cycles <b>then</b>	
26:         Break the loop	▷ [69]
27: <b>end if</b>	
28: <b>if</b> flag is 0 <b>then</b>	
29:         Set goals to one side of the circle	▷ [72]
30: <b>else</b>	
31:         Set goals to the opposite side of the circle	▷ [75]
32: <b>end if</b>	
33:     Use the position controller to drive to the goal position	▷ [77]
34:     Use the barrier certificates to avoid collisions	▷ [79]
35:     Convert single-integrator control inputs to unicycle commands	▷ [81]
36:     Set the velocities of the robots	▷ [83]
37:     Iterate the simulation	▷ [85]
38: <b>end while</b>	
39: Display a finished caption and wait for a few seconds	▷ [87-89]
40: Iterate the simulation	▷ [90]
41: Call this script to print debug information and for your script to run on the Robotarium	▷ [93]

---

### 3.8.2 Leader-Follower Formation Control with Plotting

This code controls a leader-follower formation of robots. The leader robot moves towards predefined waypoints, while follower robots maintain a desired distance from each other. The code uses Single Integrator dynamics for generating control inputs and Unicycle dynamics for actual robot movement. Barrier certificates ensure safe control inputs, and various plotting parameters are used for visualization.

```

1  import rps.robotarium as robotarium
2  from rps.utilities.transformations import *
3  from rps.utilities.graph import *
4  from rps.utilities.barrier_certificates import *
5  from rps.utilities.misc import *
6  from rps.utilities.controllers import *
7  import numpy as np
8
9  iterations = 5000 # Run the simulation/experiment for 5000 steps
10
11  N = 4 # Number of robots
12
13  waypoints = np.array([[ -1, -1, 1, 1],[0.8, -0.8, -0.8, 0.8]]) # Waypoints the leader moves to.
14
15  close_enough = 0.03; # How close the leader must get to the waypoint to move to the next one.
16
17  # Create the desired Laplacian
18  followers = -completeGL(N-1)
19  L = np.zeros((N,N))
20  L[1:N,1:N] = followers
21  L[1,1] = L[1,1] + 1
22  L[1,0] = -1
23
24  # Find connections
25  [rows,cols] = np.where(L==1)
26
27  dxi = np.zeros((2,N)) # For computational/memory reasons, initialize the velocity vector
28
29  state = 0 # Initialize leader state
30
31  magnitude_limit = 0.15 # Limit maximum linear speed of any robot
32
33  formation_control_gain = 10 # Gains for the Formation Control
34
35  desired_distance = 0.3 # Desired distance between the Robots
36
37  initial_conditions = np.array([[0, 0.5, 0.3, -0.1],[0.5, 0.5, 0.2, 0],[0, 0, 0, 0]]) # Initial Positions
38
39  r = robotarium.Robotarium(number_of_robots=N, show_figure=True, initial_conditions=initial_conditions,
40  ↪  sim_in_real_time=True) # Instantiate the Robotarium
41
42  _, uni_to_si_states = create_si_to_uni_mapping() # Unicycle to Single Integrator States Mapping
43
44  si_to_uni_dyn = create_si_to_uni_dynamics() # Single Integrator to Unicycle Velocity Commands
45
46  si_barrier_cert = create_single_integrator_barrier_certificate_with_boundary() # Single-integrator barrier certificates
47
48  leader_controller = create_si_position_controller(velocity_magnitude_limit=0.1) # Single-integrator position controller
49
50  # Plotting Parameters
51  CM = np.random.rand(N,3) # Random Colors array for plotting
52  marker_size_goal = determine_marker_size(r,0.2) # Will scale the plotted markers to be the diameter of provided argument
53  ↪  (in meters)
54  font_size_m = 0.1
55  font_size = determine_font_size(r,font_size_m) # Will scale the plotted font height to that of the provided argument (in
56  ↪  meters)
57  line_width = 5
58
59  # Create goal text and markers
60
61  # Text with goal identification
62  goal_caption = ['G{0}'.format(ii) for ii in range(waypoints.shape[1])]
63  # Plot text for caption
64  waypoint_text = [r.axes.text(waypoints[0,ii], waypoints[1,ii], goal_caption[ii], fontsize=font_size,
65  ↪  color='k',fontweight='bold',horizontalalignment='center',verticalalignment='center',zorder=-2)
66  for ii in range(waypoints.shape[1])]
67  g = [r.axes.scatter(waypoints[0,ii], waypoints[1,ii], s=marker_size_goal, marker='s',
68  ↪  facecolors='none',edgecolors=CM[ii,:],linewidth=line_width,zorder=-2)
69  for ii in range(waypoints.shape[1])]
70
71  # Plot Graph Connections

```

```

67
68 x = r.get_poses() # Get the pose of robots
69
70 linked_follower_index = np.empty((2,3))
71 follower_text = np.empty((3,0))
72 for jj in range(1,int(len(rows)/2)+1):
73     linked_follower_index[:,[jj-1]] = np.array([[rows[jj]], [cols[jj]]])
74     follower_text = np.append(follower_text, '{0}'.format(jj))
75
76 line_follower = [r.axes.plot([x[0,rows[kk]], x[0,cols[kk]]], [x[1,rows[kk]],
77 ↪ x[1,cols[kk]]], linewidth=line_width, color='b', zorder=-1)
78     for kk in range(1,N)]
79 line_leader = r.axes.plot([x[0,0], x[0,1]], [x[1,0], x[1,1]], linewidth=line_width, color='r', zorder = -1)
80 follower_labels = [r.axes.text(x[0,kk], x[1,kk]+0.15, follower_text[kk-1], fontsize=font_size,
81 ↪ color='b', fontweight='bold', horizontalalignment='center', verticalalignment='center', zorder=0)
82     for kk in range(1,N)]
83 leader_label = r.axes.text(x[0,0], x[1,0]+0.15, "Leader", fontsize=font_size,
84 ↪ color='r', fontweight='bold', horizontalalignment='center', verticalalignment='center', zorder=0)
85
86 r.step() # Iterate the simulation
87
88 for t in range(iterations):
89
90     x = r.get_poses() # Get the pose of robots
91
92     xi = uni_to_si_states(x) # Transform poses to Single Integrator
93
94     for q in range(N-1):
95         follower_labels[q].set_position([xi[0,q+1], xi[1,q+1]+0.15])
96         follower_labels[q].set_fontsize(determine_font_size(r, font_size_m))
97         line_follower[q][0].set_data([x[0, rows[q+1]], x[0, cols[q+1]], [x[1, rows[q+1]], x[1, cols[q+1]]])
98
99         leader_label.set_position([xi[0,0], xi[1,0]+0.15])
100         leader_label.set_fontsize(determine_font_size(r, font_size_m))
101         line_leader[0].set_data([x[0,0], x[0,1]], [x[1,0], x[1,1]])
102
103     # This updates the marker sizes if the figure window size is changed. This should be removed when submitting to the
104     ↪ Robotarium.
105     for q in range(waypoints.shape[1]):
106         waypoint_text[q].set_fontsize(determine_font_size(r, font_size_m))
107         g[q].set_sizes([determine_marker_size(r, 0.2)])
108
109     # Followers
110     for i in range(1, N):
111         dxi[:, [i]] = np.zeros((2, 1)) # Zero velocities
112         neighbors = topological_neighbors(L, i) # Get the topological neighbors of agent i
113
114         for j in neighbors:
115             dxi[:, [i]] += formation_control_gain * (np.power(np.linalg.norm(x[:2, [j]] - x[:2, [i]]), 2) -
116             ↪ np.power(desired_distance, 2)) * (x[:2, [j]] - x[:2, [i]])
117
118     # Leader
119     waypoint = waypoints[:, state].reshape((2, 1))
120
121     dxi[:, [0]] = leader_controller(x[:2, [0]], waypoint)
122     if np.linalg.norm(x[:2, [0]] - waypoint) < close_enough: # Leader moves to the waypoint and updates to the next one if
123     ↪ close
124         state = (state + 1) % 4
125
126     # Keep single integrator control vectors under specified magnitude
127     norms = np.linalg.norm(dxi, 2, 0) # Threshold control inputs
128     idxs_to_normalize = (norms > magnitude_limit) # Threshold control inputs
129     dxi[:, idxs_to_normalize] *= magnitude_limit / norms[idxs_to_normalize] # Threshold control inputs
130
131     dxi_safe = si_barrier_cert(dxi, x[:2, :]) # Use Barrier to avoid collision
132
133     dxu_safe = si_to_uni_dyn(dxi_safe, x) # Convert single-integrator to unicycle commands
134
135     r.set_velocities(np.arange(N), dxu_safe) # Set the velocities of agents 1,...,N to dxu_safe
136
137     r.step() # Iterate the simulation
138
139 r.call_at_scripts_end() # Call at end of script to print debug information

```

Listing 17: leader\_follower\_with\_plotting.py example

---

**Algorithm 16** Pseudo Code `leader_follower_with_plotting.py`

---

1: Import important libraries	▷ [1-7]
2: Set number of iterations and number of robots	▷ [9,11]
3: Define waypoints for the leader and the distance threshold to switch waypoints	▷ [13,15]
4: Create the desired Laplacian and find connections	▷ [18-25]
5: Initialize the velocity vector	▷ [27]
6: Initialize leader state and set magnitude limit	▷ [29,31]
7: Create gains for the formation control algorithm and desired distance	▷ [33,35]
8: Set initial conditions to avoid barrier use at the beginning	▷ [37]
9: Instantiate the Robotarium object with specified parameters	▷ [39]
10: Create mapping from single integrator states to unicycle states and vice versa.	▷ [41]
11: Create Single Integrator to unicycle dynamic mapping	▷ [43]
12: Create barrier certificates to avoid collision	▷ [45]
13: Create single integrator position controller for leader	▷ [47]
14: Create array with different colors	▷ [50]
15: Create the appropriate Marker Size	▷ [51]
16: font size	▷ [52]
17: Create the appropriate Font Size	▷ [53]
18: Desired line width	▷ [54]
19: Create goal text and markers	▷ [59-64]
20: Plot graph connections	▷ [68-81]
21: Step the simulation to update visualization	▷ [83]
22: <b>for</b> each iteration (1 to iterations) <b>do</b>	
23:     Get the most recent pose information from the Robotarium	▷ [87]
24:     Convert unicycle poses to single-integrator poses	▷ [89]
25:     Update plot handles for followers and leader	▷ [91-98]
26:     Update marker sizes if the figure window size changes	▷ [101-103]
27: <b>Followers:</b>	
28: <b>for</b> each follower robot (1 to N-1) <b>do</b>	
29:         Zero velocities and get topological neighbors	▷ [108-109]
30: <b>for</b> each neighbor <b>do</b>	
31:             Compute formation control inputs	▷ [112]
32: <b>end for</b>	
33: <b>end for</b>	
34: <b>Leader:</b>	
35:     Set goal waypoint and compute control inputs	▷ [115, 117]
36: <b>if</b> leader is close enough to the waypoint <b>then</b>	
37:         Update the waypoint state	▷ [119]
38: <b>end if</b>	
39:     Threshold control inputs to keep them under the magnitude limit	▷ [122-124]
40:     Use barriers certification	▷ [126]
41:     Convert single-integrator to unicycle commands	▷ [128]
42:     Set the velocities of the robots	▷ [130]
43:     Iterate the simulation	▷ [132]
44: <b>end for</b>	
45: Call this script to print debug information and for your script to run on the Robotarium	▷ [134]

---

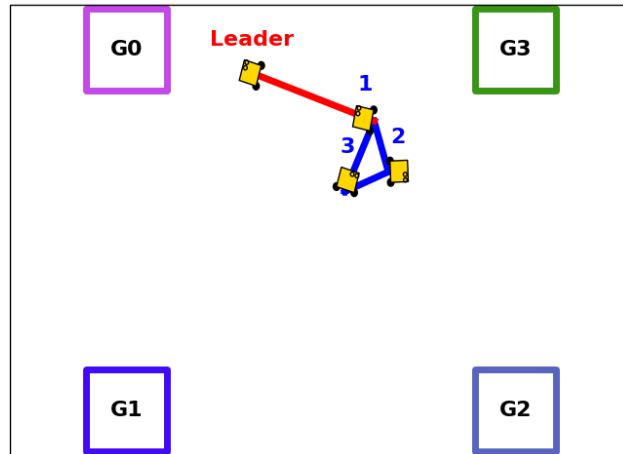


Figure 20: Leader Follower with Plotting



### 3.8.3 Robots go to a point using Single Integrator and Unicycle Dynamics with background

This code controls multiple robots that move towards specified goal points while avoiding collisions with other robots and boundaries. The Single Integrator model is used for generating control inputs ( $dx_i$ ), and the Unicycle model is used for actual robot movement ( $dx_u$ ). The control inputs are converted from Single Integrator to Unicycle commands using a specified transformation. Additionally, the background of the testbed can be changed.

```
1 import rps.robotarium as robotarium
2 from rps.utilities.transformations import *
3 from rps.utilities.barrier_certificates import *
4 from rps.utilities.misc import *
5 from rps.utilities.controllers import *
6 import numpy as np
7 import time
8
9 N = 4 # Number of Robots
10
11 initial_conditions = np.array(np.mat('1 0.5 -0.5 0; 0.8 -0.3 -0.75 0.1; 0 0 0 0'))
12
13 r = robotarium.Robotarium(number_of_robots=N, show_figure=True, initial_conditions=initial_conditions,
14 ↪ sim_in_real_time=False) # Instantiate Robotarium
15
16 goal_points = 0.9*np.array([[ -1, 1, -1, 1], [-1, -1, 1, 1], [0,0,0,0]]) # Goal Points
17
18 single_integrator_position_controller = create_si_position_controller() # Single integrator position controller
19
20 si_barrier_cert = create_single_integrator_barrier_certificate_with_boundary() # Barrier certificates to avoid collision
21
22 _, uni_to_si_states = create_si_to_uni_mapping() # Unicycle to Single Integrator States Mapping
23
24 si_to_uni_dyn = create_si_to_uni_dynamics_with_backwards_motion() # Single Integrator to Unicycle Velocity Commands
25
26 # Read in and scale image
27 gt_img = plt.imread('GTLogo.png')
28 x_img = np.linspace(-1.0, 1.0, gt_img.shape[1])
29 y_img = np.linspace(-1.0, 1.0, gt_img.shape[0])
30
31 gt_img_handle = r.axes.imshow(gt_img, extent=(-1, 1, -1, 1))
32
33 x = r.get_poses() # Get poses of the Robots
34
35 x_si = uni_to_si_states(x) # Transform poses to Single Integrator
36
37 r.step() # Iterate the simulation
38
39 # While all Robots are not in the goal points...
40 while (np.size(at_pose(np.vstack((x_si,x[2,:])), goal_points, rotation_error=100)) != N):
41     x = r.get_poses() # Get the poses of robots
42
43     x_si = uni_to_si_states(x) # Transform poses to Single Integrator
44
45     dxi = single_integrator_position_controller(x_si, goal_points[2:][:]) # Create single-integrator control inputs
46
47     dxi_safe = si_barrier_cert(dxi, x_si) # Create safe control inputs (i.e., no collisions)
48
49     dxu_safe = si_to_uni_dyn(dxi_safe, x) # Transform single integrator velocity commands to unicycle
50
51     r.set_velocities(np.arange(N), dxu_safe) # Set the velocities using the Unicycle Commands
52
53     r.step() # Iterate the simulation
54
55 r.call_at_scripts_end() # Call at end of script to print debug information
```

Listing 18: si\_go\_to\_point\_gt.py example

---

**Algorithm 17** Pseudo Code `si_go_to_point_gt.py`

---

1: Import important libraries	▷ [1-7]
2: Set the number of robots and initial conditions	▷ [9-11]
3: Initialize the Robotarium object	▷ [13]
4: Define goal points for the robots	▷ [15]
5: Create single integrator position controller	▷ [17]
6: Create barrier certificates to avoid collisions	▷ [19]
7: Create mapping from unicycle states to single integrator states	▷ [21]
8: Create mapping from single integrator velocity commands to unicycle velocity commands	▷ [23]
9: Read in and scale image for visualization	▷ [26-30]
10: Define initial robot poses	▷ [32]
11: Convert unicycle states to single integrator states	▷ [34]
12: Iterate the simulation	▷ [36]
13: <b>while</b> number of robots at the required poses is less than N <b>do</b>	
14:     Get current poses of the robots	▷ [41]
15:     Convert unicycle states to single integrator states	▷ [43]
16:     Create single-integrator control inputs	▷ [45]
17:     Create safe control inputs to avoid collisions	▷ [47]
18:     Transform single integrator velocity commands to unicycle	▷ [49]
19:     Set the velocities of the robots	▷ [51]
20:     Iterate the simulation	▷ [53]
21: <b>end while</b>	
22: Call this script to print debug information and for your script to run on the Robotarium	▷ [55]

---



Figure 21: Si go to point with GT logo at the Background

### 3.8.4 Robots go to a point using Single Integrator with Plotting

This code controls multiple robots that move towards specified goal points while avoiding collisions with other robots and boundaries. The Single Integrator model is used for generating control inputs ( $dx_i$ ), and the Unicycle model is used for actual robot movement ( $dx_u$ ). The control inputs are converted from Single Integrator to Unicycle commands using a specified transformation. Additionally, the safety radius of robots and goal points are visualized in real-time.

```
1 import rps.robotarium as robotarium
2 from rps.utilities.transformations import *
3 from rps.utilities.barrier_certificates import *
4 from rps.utilities.misc import *
5 from rps.utilities.controllers import *
6 import numpy as np
7 import time
8
9 N = 5 # Number of Robots
10
11 initial_conditions = np.array(np.mat('1 0.5 -0.5 0 0.28; 0.8 -0.3 -0.75 0.1 0.34; 0 0 0 0 0')) # Initial Positions
12
13 r = robotarium.Robotarium(number_of_robots=N, show_figure=True, initial_conditions=initial_conditions,
14   ↪ sim_in_real_time=False) # Instantiate Robotarium
15
16 goal_points = generate_initial_conditions(N, width=r.boundaries[2]-2*r.robot_diameter, height =
17   ↪ r.boundaries[3]-2*r.robot_diameter, spacing=0.5) # Define goal points by removing orientation from poses
18
19 single_integrator_position_controller = create_si_position_controller() # Single integrator position controller
20
21 si_barrier_cert = create_single_integrator_barrier_certificate_with_boundary() # Barrier certificates to avoid collision
22
23 _, uni_to_si_states = create_si_to_uni_mapping() # Unicycle to Single Integrator States Mapping
24
25 si_to_uni_dyn = create_si_to_uni_dynamics_with_backwards_motion() # Single Integrator to Unicycle Velocity Commands
26
27 x = r.get_poses() # Get poses of the Robots
28
29 x_si = uni_to_si_states(x) # Transform poses to Single Integrator
30
31 # Plotting Parameters
32 CM = np.random.rand(N,3) # Random Colors array for plotting
33 robot_marker_size_m = 0.15
34 marker_size_goal = determine_marker_size(r,goal_marker_size_m) # Will scale the plotted markers to be the diameter of
35   ↪ provided argument (in meters)
36 marker_size_robot = determine_marker_size(r, robot_marker_size_m) # Will scale the plotted markers to be the diameter of
37   ↪ provided argument (in meters)
38 font_size = determine_font_size(r,0.1) # Will scale the plotted font height to that of the provided argument (in meters)
39 line_width = 5
40
41 # Create Goal Point Markers
42 # Text with goal identification
43 goal_caption = ['G{0}'.format(ii) for ii in range(goal_points.shape[1])]
44 #Plot text for caption
45 goal_points.text = [r.axes.text(goal_points[0,ii], goal_points[1,ii], goal_caption[ii], fontsize=font_size,
46   ↪ color='k',fontweight='bold',horizontalalignment='center',verticalalignment='center',zorder=-2)
47 for ii in range(goal_points.shape[1])]
48 goal_markers = [r.axes.scatter(goal_points[0,ii], goal_points[1,ii], s=marker_size_goal, marker='s',
49   ↪ facecolors='none',edgecolors=CM[ii,:],linewidth=line_width,zorder=-2)
50 for ii in range(goal_points.shape[1])]
51 robot_markers = [r.axes.scatter(x[0,ii], x[1,ii], s=marker_size_robot, marker='o',
52   ↪ facecolors='none',edgecolors=CM[ii,:],linewidth=line_width)
53 for ii in range(goal_points.shape[1])]
54
55 r.step() # Iterate the simulation
56
57 # While all Robots are not in the goal points...
58 while (np.size(at_pose(np.vstack((x_si,x[2,:])), goal_points, rotation_error=100)) != N):
59
60     x = r.get_poses() # Get poses of Robots
61
62     x_si = uni_to_si_states(x) # Transform poses to Single Integrator
63
64     # Update Plot
65     # Update Robot Marker Plotted Visualization
66     for i in range(x.shape[1]):
67         robot_markers[i].set_offsets(x[:,2,i].T)
68         # This updates the marker sizes if the figure window size is changed.
69         # This should be removed when submitting to the Robotarium.
70         robot_markers[i].set_sizes([determine_marker_size(r, robot_marker_size_m)])
```

```

64
65     for j in range(goal_points.shape[1]):
66         goal_markers[j].set_sizes([determine_marker_size(r, goal_marker_size_m)])
67
68     dxi = single_integrator_position_controller(x_si, goal_points[:2][:]) # Create single-integrator control inputs
69
70     dxi_safe = si_barrier_cert(dxi, x_si) # Create safe control inputs (i.e., no collisions)
71
72     dxu_safe = si_to_uni_dyn(dxi_safe, x) # Transform single integrator velocity commands to unicycle
73
74     r.set_velocities(np.arange(N), dxu_safe) # Set the velocities using the Unicycle Commands
75
76     r.step() # Iterate the simulation
77
78 r.call_at_scripts_end() # Call at end of script to print debug information

```

Listing 19: si\_go\_to\_point\_with\_plotting.py example

---

**Algorithm 18** Pseudo Code si\_go\_to\_point\_with\_plotting.py

---

- |  |           |
|--|-----------|
| 1: Import important libraries  | ▷ [1-7]   |
| 2: Set the number of robots and initial conditions   | ▷ [9-11]  |
| 3: Initialize the Robotarium object  | ▷ [13]    |
| 4: Define goal points for the robots   | ▷ [15]    |
| 5: Create single integrator position controller  | ▷ [17]    |
| 6: Create barrier certificates to avoid collisions   | ▷ [19]    |
| 7: Create mapping from unicycle states to single integrator states                           | ▷ [21]    |
| 8: Create mapping from single integrator velocity commands to unicycle velocity commands     | ▷ [23]    |
| 9: Define initial robot poses  | ▷ [25]    |
| 10: Convert unicycle states to single integrator states                                      | ▷ [27]    |
| 11: Create array with different colors   | ▷ [30]    |
| 12: Goal Marker Size   | ▷ [31]    |
| 13: Appropriate Marker Size Goal   | ▷ [33]    |
| 14: Robot Marker Size  | ▷ [32]    |
| 15: Appropriate Marker Size Robot  | ▷ [33]    |
| 16: Create the appropriate Font Size   | ▷ [34]    |
| 17: Line width   | ▷ [35]    |
| 18: Create the text with Goal Identification   | ▷ [39]    |
| 19: Create Plot for Caption  | ▷ [41-46] |
| 20: Iterate the simulation   | ▷ [48]    |
| 21: <b>while</b> number of robots at the required poses is less than N <b>do</b>             |           |
| 22:     Get current poses of the robots  | ▷ [53]    |
| 23:     Convert unicycle states to single integrator states                                  | ▷ [55]    |
| 24:     Update robot marker plotted visualization  | ▷ [59-66] |
| 25:     Create single-integrator control inputs  | ▷ [68]    |
| 26:     Create safe control inputs to avoid collisions                                       | ▷ [70]    |
| 27:     Transform single integrator velocity commands to unicycle                            | ▷ [72]    |
| 28:     Set the velocities of the robots   | ▷ [74]    |
| 29:     Iterate the simulation   | ▷ [76]    |
| 30: <b>end while</b>   |           |
| 31: Call this script to print debug information and for your script to run on the Robotarium | ▷ [78]    |
-

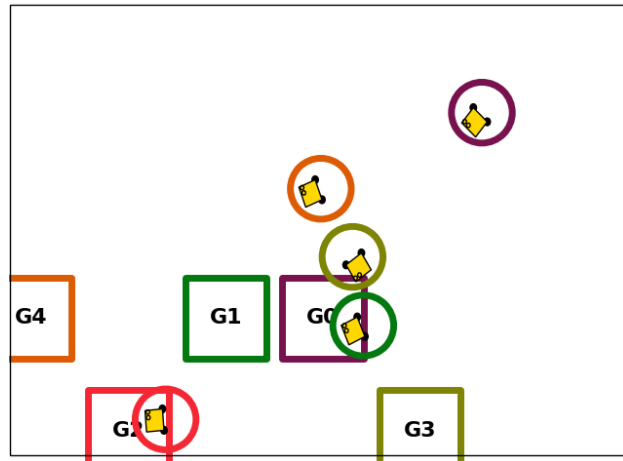


Figure 22: si go to point with plotting

### 3.8.5 Robots go to a point using Unicycle Pose Controller with Plotting

This code controls multiple robots that move towards specified goal points while avoiding collisions with other robots and boundaries. The Unicycle model is used for generating control inputs ( $dxu$ ). Additionally, the positions and orientations of robots and goal points are visualized in real-time.

```
1 import rps.robotarium as robotarium
2 from rps.utilities.transformations import *
3 from rps.utilities.barrier_certificates import *
4 from rps.utilities.misc import *
5 from rps.utilities.controllers import *
6 import numpy as np
7 import time
8
9 N = 5 # Number of Robots
10
11 initial_conditions = np.array(np.mat('1 0.5 -0.5 0 0.28; 0.8 -0.3 -0.75 0.1 0.34; 0 0 0 0 0')) # Initial position
12
13 r = robotarium.Robotarium(number_of_robots=N, show_figure=True,
14 ↪ initial_conditions=initial_conditions,sim_in_real_time=True) # Instantiate Robotarium object
15
16 goal_points = generate_initial_conditions(N, width=r.boundaries[2]-2*r.robot_diameter, height =
17 ↪ r.boundaries[3]-2*r.robot_diameter, spacing=0.5) # Define goal points by removing orientation from poses
18
19 unicycle_pose_controller = create_hybrid_unicycle_pose_controller() # Create unicycle hybrid pose controller
20
21 uni_barrier_cert = create_unicycle_barrier_certificate() # Create barrier certificates to avoid collision
22
23 x = r.get_poses() # Get the poses of the robots
24
25 # Plotting Parameters
26 CM = np.random.rand(N,3) # Random Colors array for plotting
27 goal_marker_size_m = 0.2
28 robot_marker_size_m = 0.15
29 marker_size_goal = determine_marker_size(r,goal_marker_size_m) # Will scale the plotted markers to be the diameter of
30 ↪ provided argument (in meters)
31 marker_size_robot = determine_marker_size(r, robot_marker_size_m) # Will scale the plotted markers to be the diameter of
32 ↪ provided argument (in meters)
33 font_size = determine_font_size(r,0.1) # Will scale the plotted font height to that of the provided argument (in meters)
34 line_width = 5
35
36 # Create Goal Point Markers
37 # Test with goal identification
38 goal_caption = ['G{0}'.format(ii) for ii in range(goal_points.shape[1])]
39 # Arrow for desired orientation
40 goal_orientation_arrows = [r.axes.arrow(goal_points[0,ii], goal_points[1,ii],
41 ↪ goal_marker_size_m*np.cos(goal_points[2,ii]), goal_marker_size_m*np.sin(goal_points[2,ii]), width = 0.02,
42 ↪ length_includes_head=True, color = CM[ii,:], zorder=-2)
43 for ii in range(goal_points.shape[1])]
44 # Plot text for caption
45 goal_points.text = [r.axes.text(goal_points[0,ii], goal_points[1,ii], goal_caption[ii], fontsize=font_size,
46 ↪ color='k',fontweight='bold',horizontalalignment='center',verticalalignment='center',zorder=-3)
47 for ii in range(goal_points.shape[1])]
48 goal_markers = [r.axes.scatter(goal_points[0,ii], goal_points[1,ii], s=marker_size_goal, marker='s',
49 ↪ facecolors='none',edgecolors=CM[ii,:],linewidth=line_width,zorder=-3)
50 for ii in range(goal_points.shape[1])]
51 robot_markers = [r.axes.scatter(x[0,ii], x[1,ii], s=marker_size_robot, marker='o',
52 ↪ facecolors='none',edgecolors=CM[ii,:],linewidth=line_width)
53 for ii in range(goal_points.shape[1])]
54
55 r.step() # Iterate the simulation
56
57 # While all Robots are not in the goal points...
58 while (np.size(at_pose(x, goal_points)) != N):
59
60     x = r.get_poses() # Get poses of agents
61
62     # Update Plot
63     # Update Robot Marker Plotted Visualization
64     for i in range(x.shape[1]):
65         robot_markers[i].set_offsets(x[:,2,i].T)
66         # This updates the marker sizes if the figure window size is changed.
67         # This should be removed when submitting to the Robotarium.
68         robot_markers[i].set_sizes([determine_marker_size(r, robot_marker_size_m)])
69
70     for j in range(goal_points.shape[1]):
71         goal_markers[j].set_sizes([determine_marker_size(r, goal_marker_size_m)])
72
73     dxu = unicycle_pose_controller(x, goal_points) # Create unicycle control inputs
```

```

65     dxu_safe = uni_barrier_cert(dxu, x) # Create safe control inputs (i.e., no collisions)
66
67     r.set_velocities(np.arange(N), dxu_safe) # Set the velocities of agents 1,...,N to dxu_safe
68
69     r.step() # Iterate the simulation
70
71     r.call_at_scripts_end() # Call at end of script to print debug information
72

```

Listing 20: uni\_go\_to\_pose\_hybrid\_with\_plotting.py example

---

**Algorithm 19** Pseudo Code uni\_go\_to\_pose\_hybrid\_with\_plotting.py

---

- |  |           |
|--|-----------|
| 1: Import important libraries  | ▷ [1-7]   |
| 2: Set the number of robots and initial conditions   | ▷ [9-11]  |
| 3: Initialize the Robotarium object  | ▷ [13]    |
| 4: Define goal points for the robots   | ▷ [15]    |
| 5: Create unicycle pose controller   | ▷ [17]    |
| 6: Create barrier certificates to avoid collisions   | ▷ [19]    |
| 7: Define initial robot poses  | ▷ [21]    |
| 8: Create array with different colors  | ▷ [24]    |
| 9: Goal Marker Size  | ▷ [25]    |
| 10: Robot Marker Size  | ▷ [36]    |
| 11: Appropriate Marker Size Goal   | ▷ [27]    |
| 12: Appropriate Marker Size Goal   | ▷ [28]    |
| 13: Create the appropriate Font Size   | ▷ [29]    |
| 14: Line width   | ▷ [30]    |
| 15: Create the text with Goal Identification   | ▷ [34]    |
| 16: Create arrow for the desired orientation   | ▷ [36]    |
| 17: Create Plot for Caption  | ▷ [38-44] |
| 18: Iteration the simulation   | ▷ [46]    |
| 19: <b>while</b> number of robots at the required poses is less than N <b>do</b>             |           |
| 20:     Get current poses of the robots  | ▷ [51]    |
| 21:     Update robot marker plotted visualization  | ▷ [53-62] |
| 22:     Create unicycle control inputs   | ▷ [64]    |
| 23:     Create safe control inputs to avoid collisions                                       | ▷ [66]    |
| 24:     Set the velocities of the robots   | ▷ [68]    |
| 25:     Iterate the simulation   | ▷ [70]    |
| 26: <b>end while</b>   |           |
| 27: Call this script to print debug information and for your script to run on the Robotarium | ▷ [72]    |
-

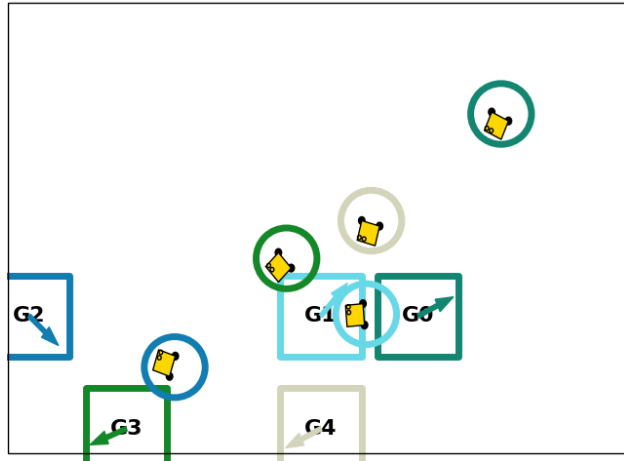


Figure 23: `uni_go_to_pose_hybrid` with plotting



## 4 Functions

This section describes a variety of functions that are essential for controlling robots in the Robotarium. These functions facilitate different aspects of robot control, such as state transformations, collision avoidance, and movement controllers. Below is a brief introduction to the key functions available in the `rps.utilities` module.

### 4.1 Libraries

In order to have all the utilities that the Robotarium offers you need to import the functions. Do not forget to include this line at the beginning of your code. You can check the other libraries available in [Appendix A](#)

```
import rps.robotarium as robotarium
from rps.utilities.transformations import *
from rps.utilities.graph import *
from rps.utilities.barrier_certificates import *
from rps.utilities.misc import *
from rps.utilities.controllers import *
import numpy as np
import time
```

Listing 21: Robotarium Libraries

In case you do not want to use everything, you can always just import the function that you know you will use.

### 4.2 Class Robotarium

This section provides an overview of the key functions in the Robotarium API. These functions allow you to control the robots, retrieve their states, and manage the simulation environment.

#### 4.2.1 Initialization

```
r = robotarium.Robotarium(number_of_robots=N, show_figure=True, initial_conditions=
initial_conditions, sim_in_real_time=False)
```

Listing 22: Initialization

This function initializes the Robotarium class, setting up parameters such as the number of robots, initial conditions, and visualization settings. It takes for inputs:

- **Number of Robots (N):** The number of Robots. This parameter is used for almost all the functions. Currently the Robotarium accepts up to 20 robots for the experiments.
- **Show Figure:** If True, you can see the simulation. Else, you cannot.
- **Initial Conditions:** Initial conditions are the initial positions that we want for our robots. The initial positions are given in a  $\mathbb{R}^{3 \times N}$  numpy array that specify the pose and orientation of each robot
- **Simulation in Real Time:** If true, the simulation will take exactly 0.033 s. If false, the simulation will run as fast as it can depending the power of your computer.

This function will be always in your code.

#### 4.2.2 Set velocity of Robots

```
r.set_velocities(ids, velocities)
```

Listing 23: Set velocity of Robot function

The `set_velocities` function allows you to set the linear and angular velocities of the robots. It is important to highlight that to set the velocity of the robots, we always use **unicycle control inputs**. It takes for input:

- **ids**: The ID's of each robot, usually we use a  $\mathbb{R}^{1 \times N}$  numpy array
- **dxu**: A  $\mathbb{R}^{2 \times N}$  numpy array with the unicycle control inputs.

#### 4.2.3 Retrieving Poses

```
r.get_poses()
```

Listing 24: Get poses function

This function returns a  $\mathbb{R}^{3 \times N}$  numpy array with the current states (positions and orientations) of the robots. Every angle is interpreted as a radian on the Robotarium.

#### 4.2.4 Step in the Simulation

```
r.step()
```

Listing 25: Iteration in the Robotarium

The `step` function advances the simulation by one time step, updating the dynamics of the robots and visualization (if enabled). A time step in the Robotarium is 0.033 seconds. This is important to consider since there is a maximum time per experiment in the Robotarium, so be sure that your experiment can run within the limit.

#### 4.2.5 End of Experiment

```
r.call_at_scripts_end()
```

Listing 26: Function to end experiments

Every-time we finish our simulation we need to include this function in order to print out any errors that might cause our experiment to fail or to be rejected by the Robotarium

## 4.3 Transformations

Transformations between the unicycle model and the single integrator model are essential for simplifying control design, decoupling control inputs, easing the implementation of algorithms, and facilitating path planning and tracking.

### 4.3.1 Single Integrator to Unicycle Dynamics

This function returns a function that maps from single-integrator to unicycle dynamics with angular velocity magnitude restrictions.

```
def create_si_to_uni_dynamics(linear_velocity_gain=1, angular_velocity_limit=np.pi):
```

Listing 27: Single Integrator to Unicycle Dynamics Main Function

This function has two parameters that can be adjusted based on the user's requirements

- **Linear Velocity Gain** ( $v_g$ ): Gain for the unicycle's linear velocity. This parameter must be  $v_g > 0$ . Different gain values alter the robots' responses.
- **Angular Velocity Limit** ( $w$ ): Limit for the angular velocity. This parameter must be  $|w| \geq 0$ .

The function returns a mapping function from single-integrator to unicycle dynamics with angular velocity magnitude restrictions.

```
def si_to_uni_dyn(dxi, poses):
```

Listing 28: Single Integrator to Unicycle Dynamics Returned Function

This function maps single-integrator dynamics to unicycle dynamics. It takes the following inputs:

- **dxi**: A  $\mathbb{R}^{2 \times N}$  numpy array with single-integrator control inputs.
- **poses**: A  $\mathbb{R}^{2 \times N}$  numpy array with single-integrator poses.

It returns a  $\mathbb{R}^{2 \times N}$  numpy array of unicycle control inputs (linear velocity  $v$  and angular velocity  $w$ ).

### 4.3.2 Single-Integrator to Unicycle Dynamics with Backwards Motion

```
def create_si_to_uni_dynamics_with_backwards_motion(linear_velocity_gain=1,
angular_velocity_limit=np.pi):
```

Listing 29: Function to Create a Mapping from Single-Integrator to Unicycle Dynamics

This function has two parameters that can be adjusted based on the user's requirements:

- **Linear Velocity Gain** ( $v_g$ ): Gain for the unicycle's linear velocity. This parameter must be  $v_g > 0$ . Different gain values alter the robots' responses.
- **Angular Velocity Limit** ( $w$ ): Limit for the angular velocity. This parameter must be  $|w| \geq 0$ .

The function returns a mapping function from single-integrator to unicycle dynamics with angular velocity magnitude restrictions.

```
def si_to_uni_dyn(dxi, poses):
```

Listing 30: Single Integrator to Unicycle Dynamics Returned Function

This function maps single-integrator dynamics to unicycle dynamics. It takes the following inputs:

- **dxi:** A  $\mathbb{R}^{2 \times N}$  numpy array with single-integrator control inputs.
- **poses:** A  $\mathbb{R}^{2 \times N}$  numpy array with single-integrator poses.

It returns a  $\mathbb{R}^{2 \times N}$  numpy array of unicycle control inputs (linear velocity  $v$  and angular velocity  $w$ ).

The key difference with the previous function is that this function allows the robots to drive backwards if that direction of linear velocity requires less rotation. In simple terms, this allows the robots to drive in reverse. This can be useful in situations where turning around to face forward would require a large angular change, but simply moving backward would be more efficient and quicker. Imagine the following scenario: a robot needs to move to a target behind it. There are two options:

- The robot can turn around (rotate 180 degrees) and then move forward.
- The robot can move backward directly, requiring minimal or no rotation.

In many cases, moving backward directly can be more efficient because it avoids the need for large rotational movements.

#### 4.3.3 Mapping from Single Integrator to Unicycle Dynamics

```
def create_si_to_uni_mapping(projection_distance=0.05, angular_velocity_limit=np.pi):
```

Listing 31: Function to Create Single Integrator to Unicycle Dynamics Mapping

This function creates two functions: one for mapping single-integrator dynamics to unicycle dynamics (`si_to_uni_dyn`) and one for mapping unicycle states to single-integrator states (`uni_to_si_states`). This mapping is done by placing a virtual control "point" in front of the unicycle, which helps in simplifying the control of unicycle robots.

This function has two parameters that can be adjusted based on the user's requirements:

- **Projection Distance:** How far ahead to place the virtual control point. This parameter must be positive (*ProjectionDistance*  $> 0$ ).
- **Angular Velocity Limit:** The maximum angular velocity that can be provided. This parameter must be  $|w| \geq 0$ . (Between lines 117 and 121, there is an error; it should be `angular_velocity_limit`).

The first function it returns is the same as before:

```
def si_to_uni_dyn(dxi, poses):
```

Listing 32: Single Integrator to Unicycle Dynamics Returned Function

This function maps single-integrator dynamics to unicycle dynamics. It takes the following inputs:

- **dxi:** A  $\mathbb{R}^{2 \times N}$  numpy array with single-integrator control inputs.
- **poses:** A  $\mathbb{R}^{2 \times N}$  numpy array with single-integrator poses.

It returns a  $\mathbb{R}^{2 \times N}$  numpy array of unicycle control inputs (linear velocity  $v$  and angular velocity  $w$ ).  
The second function is:

```
def uni_to_si_states(poses):
```

Listing 33: Unicycle to Single Integrator States Mapping Function

This function maps unicycle states to single-integrator states by placing a virtual control point ahead of the unicycle. It takes the following input:

- **poses:** A  $\mathbb{R}^{3 \times N}$  numpy array of unicycle states, where each column represents the x position, y position, and orientation  $\theta$ .

It returns a  $\mathbb{R}^{2 \times N}$  numpy array of single-integrator states, where each column represents the x and y positions of the virtual control point.

#### 4.3.4 Mapping from Unicycle Dynamics to Single Integrator Using Projection Distance

```
def create_uni_to_si_dynamics(projection_distance=0.05):
```

Listing 34: Function for Mapping from Unicycle Dynamics to Single Integrator Using Projection Distance

This function creates a mapping function from unicycle dynamics to single-integrator dynamics.

```
def uni_to_si_dyn(dxu, poses):
```

Listing 35: Unicycle Dynamics to Single Integrator Returned Function

This function maps unicycle dynamics to single-integrator dynamics. It takes the following inputs:

- **dxu:** A  $\mathbb{R}^{2 \times N}$  numpy array of unicycle control inputs.
- **poses:** A  $\mathbb{R}^{3 \times N}$  numpy array of unicycle poses.
- **Projection Distance:** How far ahead of the unicycle model to place the control point.

It returns a  $\mathbb{R}^{2 \times N}$  numpy array of single-integrator control inputs.

## 4.4 Controllers

Controllers are necessary to ensure that robots and control systems behave as desired, maintain stability, and handle disturbances and uncertainties.

### 4.4.1 Position Controller for Single Integrator

```
def create_si_position_controller(x_velocity_gain=1, y_velocity_gain=1,
velocity_magnitude_limit=0.15):
```

Listing 36: Position Controller for Single Integrator Function

This function creates a position controller for a single integrator. It drives a single integrator to a user-defined point using a proportional controller. The inputs of this function are:

- **X Velocity Gain** ( $v_{x_g}$ ): Gain for the x-direction velocity. This parameter must be  $v_{x_g} > 0$ . Different gain values alter the robots' responses.
- **Y Velocity Gain** ( $v_{y_g}$ ): Gain for the y-direction velocity. This parameter must be  $v_{y_g} > 0$ . Different gain values alter the robots' responses.
- **Velocity Magnitude Limit** ( $|v|$ ): The maximum magnitude of the velocity vector (should be less than the max linear speed of the platform). This parameter must be  $0 \leq |v| \leq V_{max}(0.2 \frac{m}{s})$ .

The function returns another function that creates a position controller for a single integrator.

```
def si_position_controller(xi, positions):
```

Listing 37: Position Controller for Single Integrator Function

This returned function takes the following inputs:

- $x_i$ : A  $\mathbb{R}^{2 \times N}$  numpy array of the single-integrator states of the robots.
- **positions**: A  $\mathbb{R}^{2 \times N}$  numpy array with the desired points each robot should achieve.

It returns a  $\mathbb{R}^{2 \times N}$  numpy array of single-integrator control inputs.

### 4.4.2 Unicycle Model Pose Controller Based on Control Lyapunov Function

```
def create_clf_unicycle_position_controller(linear_velocity_gain=0.8, angular_velocity_gain=3):
```

Listing 38: Unicycle Model Pose Controller Function

This function returns a unicycle model pose controller function that allows robots to drive the unicycle model to a given position and orientation. It takes the following parameters:

- **Linear Velocity Gain** ( $v_g$ ): The gain impacting the produced unicycle linear velocity. This parameter must be  $v_g \geq 0$ . Different gain values alter the robots' responses.
- **Angular Velocity Gain** ( $\omega_g$ ): The gain impacting the produced unicycle angular velocity. This parameter must be  $\omega_g \geq 0$ .

The returned function utilizes a Control Lyapunov Function (CLF) to drive a unicycle system to a desired position. This function operates on unicycle states and desired positions to return a unicycle velocity command vector.

```
def position_uni_clf_controller(states, positions):
```

Listing 39: Unicycle Model Pose Controller Returned Function

The inputs required by this function are:

- **states:** A  $\mathbb{R}^{3 \times N}$  numpy array of unicycle states  $(x, y, \theta)$ .
- **positions:** A  $\mathbb{R}^{3 \times N}$  numpy array of the desired positions  $(x_{goal}, y_{goal})$ .

It returns a  $\mathbb{R}^{2 \times N}$  numpy array of unicycle control inputs (linear velocity  $v$  and angular velocity  $\omega$ ).

#### 4.4.3 Unicycle Model Position Controller Based on Control Lyapunov Function

```
def create_clf_unicycle_pose_controller(approach_angle_gain=1, desired_angle_gain=2.7,
rotation_error_gain=1):
```

Listing 40: Unicycle Model Position Controller

This function returns a controller that will drive a unicycle-modeled agent to a desired pose (position and orientation). The inputs of this function are:

- **Approach Angle Gain:** Affects how the unicycle approaches the desired position.
- **Desired Angle Gain:** Affects how the unicycle approaches the desired angle.
- **Rotation Error Gain:** Affects how quickly the unicycle corrects rotation errors.

The returned function is:

```
def pose_uni_clf_controller(states, poses):
```

Listing 41: Unicycle Model Position Controller Returned Function

The inputs required by this function are:

- **states:** A  $\mathbb{R}^{3 \times N}$  numpy array of unicycle states  $(x, y, \theta)$ .
- **poses:** A  $\mathbb{R}^{3 \times N}$  numpy array of the desired positions  $(x_{goal}, y_{goal}, \theta_{goal})$ .

It returns a  $\mathbb{R}^{2 \times N}$  numpy array of unicycle control inputs (linear velocity  $v$  and angular velocity  $\omega$ ).

#### 4.4.4 Unicycle Model Position Controller Based on Hybrid Controller

```
def create_hybrid_unicycle_pose_controller(linear_velocity_gain=1, angular_velocity_gain=2,
velocity_magnitude_limit=0.15, angular_velocity_limit=np.pi, position_error=0.05,
position_epsilon=0.03, rotation_error=0.05):
```

Listing 42: Unicycle Model Position Controller Based on Hybrid Controller Function

This function returns a controller that drives a unicycle-modeled agent to a pose  $(x, y, \theta)$ . This controller is based on a hybrid approach that drives the robot in a straight line to the desired position and then rotates to the desired orientation. The inputs for this function are:

- **Linear Velocity Gain:** Affects how much the linear velocity is scaled based on the position error.
- **Angular Velocity Gain:** Affects how much the angular velocity is scaled based on the heading error.
- **Velocity Magnitude Limit:** Threshold for the maximum linear velocity that the robot can achieve.
- **Angular Velocity Limit:** Threshold for the maximum rotational velocity that the robot can achieve.
- **Position Error:** The error tolerance for the final position of the robot.
- **Position Epsilon:** The amount of translational distance allowed during rotation before correcting the position again.
- **Rotation Error:** The error tolerance for the final orientation of the robot.

The returned function is:

```
def pose_uni_hybrid_controller(states, poses, input_approach_state=np.empty([0, 0])):
```

Listing 43: Unicycle Model Position Controller Based on Hybrid Controller Returned Function

The inputs required by this function are:

- **states:** A  $\mathbb{R}^{3 \times N}$  numpy array of unicycle states  $(x, y, \theta)$ .
- **poses:** A  $\mathbb{R}^{3 \times N}$  numpy array of the desired positions  $(x_{goal}, y_{goal}, \theta_{goal})$ .
- **input\_approach\_state:** Optional input representing the approach state; it can be an empty array if not used.

It returns a  $\mathbb{R}^{2 \times N}$  numpy array of unicycle control inputs (linear velocity  $v$  and angular velocity  $\omega$ ).



## 4.5 Barrier Certificates

Barrier certificates are used in the Robotarium to ensure that robots avoid collisions while executing user-defined control inputs. Essentially, these certificates enforce a "do not collide" constraint, which is expressed as a differential constraint in terms of the control signal.

Here's how they work:

1. **User-Defined Control Input:** At any given moment, a user generates a control input that defines how they want the robot to move. This input is typically based on the robot's current task or objective, such as following a path or reaching a target point.
2. **Collision Avoidance Constraint:** The barrier certificate imposes a constraint that prevents collisions. This constraint is mathematically expressed in a way that considers the control signal and ensures that the robot's trajectory stays clear of obstacles and other robots.
3. **Minimally Invasive Adjustments:** The key feature of barrier certificates is that they are minimally invasive. This means that they make the smallest possible changes to the user-defined control input to satisfy the "do not collide" constraint. In other words, the barrier certificate adjusts the robot's movement just enough to avoid a collision, while preserving as much of the original control intent as possible.

Barrier certificates are functions that guarantee collision free behavior for robots once provided the control input (velocities) and the states of all the robots considered. Unless you have implemented your own obstacle avoidance program to ensure collisions are avoided, we strongly recommend implementing our provided barrier certificates to ensure your programs are accepted!

### 4.5.1 Create a Barrier Certificate for a Single-Integrator System

```
def create_single_integrator_barrier_certificate(barrier_gain=100, safety_radius=0.17,
magnititude_limit=0.2):
```

Listing 44: Barrier Certificate for a Single-Integrator System

This function creates a barrier certificate for a single-integrator system. It returns another function for optimization reasons. The inputs for this function are:

- **Barrier Gain ( $B_g$ ):** Controls how quickly agents can approach each other. A lower value implies a slower approach. This parameter is strictly positive ( $B_g > 0$ ).
- **Safety Radius ( $S_r$ ):** Determines how far apart the robots will stay. This parameter must be greater than or equal to 0.12 m ( $S_r \geq 0.12$ ).
- **Magnitude Limit ( $|v|$ ):** Limits the linear speed of the robot. This parameter must be  $0 < |v| \leq 0.2$ .

The returned function is:

```
def f(dxi, x):
```

Listing 45: Barrier Certificate Returned Function

The inputs required by this function are:

- **dxi:** A  $\mathbb{R}^{2 \times N}$  numpy array of the single-integrator robot velocity commands.
- **x:** A  $\mathbb{R}^{2 \times N}$  numpy array of the robot states.

It returns a  $\mathbb{R}^{2 \times N}$  numpy array of modified velocity commands that ensure safety.

#### 4.5.2 Create a Barrier Certificate for a Single Integrator with Boundary

```
def create_single_integrator_barrier_certificate_with_boundary(barrier_gain=100,
safety_radius=0.17, magnitude_limit=0.2, boundary_points=np.array([-1.6, 1.6, -1.0, 1.0])):
```

Listing 46: Barrier Certificate for a Single-Integrator System with Boundary

This function creates a barrier certificate for a single-integrator system with a rectangular boundary included, ensuring that the robots do not leave the arena. It returns another function for optimization reasons. The inputs for this function are:

- **Barrier Gain** ( $B_g$ ): Controls how quickly agents can approach each other. A lower value implies a slower approach. This parameter is strictly positive ( $B_g > 0$ ).
- **Safety Radius** ( $S_r$ ): Determines how far apart the robots will stay. This parameter must be greater than or equal to 0.12 m ( $S_r \geq 0.12$ ).
- **Magnitude Limit** ( $|v|$ ): Limits the linear speed of the robot. This parameter must be  $0 < |v| \leq 0.2$ .
- **Boundary Points**: This array corresponds to the arena's dimensions. It should not be edited.

The returned function is:

```
def f(dxi, x):
```

Listing 47: Barrier Certificate Returned Function

The inputs required by this function are:

- **dxi**: A  $\mathbb{R}^{2 \times N}$  numpy array of the single-integrator robot velocity commands.
- **x**: A  $\mathbb{R}^{2 \times N}$  numpy array of the robot states.

It returns a  $\mathbb{R}^{2 \times N}$  numpy array of modified velocity commands that ensure safety and boundary compliance.

#### 4.5.3 Create a Barrier Certificate for a Single Integrator with Dynamic Gains

```
def create_single_integrator_barrier_certificate2(barrier_gain=100, unsafe_barrier_gain=1e6,
safety_radius=0.17, magnitude_limit=0.2):
```

Listing 48: Barrier Certificate for a Single Integrator with Dynamic Gains Function

This function creates a barrier certificate for a single-integrator system. It returns another function for optimization reasons. This function is different from `create_single_integrator_barrier_certificate()` as it dynamically changes the barrier gain to a large number if the single integrator point  $(\dot{x}, \dot{y})$  enters an unsafe region. The inputs for this function are:

- **Barrier Gain** ( $B_g$ ): Controls how quickly agents can approach each other. A lower value implies a slower approach. This parameter is strictly positive ( $B_g > 0$ ).
- **Unsafe Barrier Gain** ( $B_{unsafe}$ ): Controls how quickly the Barrier Gain changes when entering an unsafe region. This parameter must be positive ( $B_{unsafe} > 0$ ).
- **Safety Radius** ( $S_r$ ): Determines how far apart the robots will stay. This parameter must be greater than or equal to 0.12 m ( $S_r \geq 0.12$ ).

- **Magnitude Limit** ( $|v|$ ): Limits the linear speed of the robot. This parameter must be  $0 < |v| \leq 0.2$ .

The returned function is:

```
def f(dxi, x):
```

Listing 49: Barrier Certificate for a Single Integrator with Dynamic Gains Returned Function

The inputs required by this function are:

- **dxi**: A  $\mathbb{R}^{2 \times N}$  numpy array of the single-integrator robot velocity commands.
- **x**: A  $\mathbb{R}^{2 \times N}$  numpy array of the robot states.

It returns a  $\mathbb{R}^{2 \times N}$  numpy array of modified velocity commands that ensure safety.

#### 4.5.4 Create a Barrier Certificate for a Unicycle Model

```
def create_unicycle_barrier_certificate(barrier_gain=100, safety_radius=0.12,
projection_distance=0.05, magnitude_limit=0.2):
```

Listing 50: Barrier Certificate for a Unicycle Model Function

This function creates a barrier certificate for a unicycle model to avoid collisions. It uses diffeomorphism mapping and single integrator implementation. For optimization purposes, this function returns a unicycle barrier certificate function. The inputs for this function are:

- **Barrier Gain** ( $B_g$ ): Controls how quickly agents can approach each other. A lower value implies a slower approach. This parameter is strictly positive ( $B_g > 0$ ).
- **Safety Radius** ( $S_r$ ): Determines how far apart the robots will stay. This parameter must be greater than or equal to 0.12 m ( $S_r \geq 0.12$ ).
- **Projection Distance**: Determines how far ahead of the unicycle model to place the safety "bubble".
- **Magnitude Limit** ( $|v|$ ): Limits the linear speed of the robot. This parameter must be  $0 < |v| \leq 0.2$ .

The returned function is:

```
def f(dxu, x):
```

Listing 51: Barrier Certificate for a Unicycle Model Returned Function

The inputs required by this function are:

- **dxu**: A  $\mathbb{R}^{2 \times N}$  numpy array of the unicycle robot velocity commands.
- **x**: A  $\mathbb{R}^{2 \times N}$  numpy array of the robot states.

It returns a  $\mathbb{R}^{2 \times N}$  numpy array of modified velocity commands that ensure safety.

#### 4.5.5 Create a Barrier Certificate for a Unicycle Model with Boundary

```
def create_unicycle_barrier_certificate_with_boundary(barrier_gain=100, safety_radius=0.12,
projection_distance=0.05, magnitude_limit=0.2, boundary_points=np.array([-1.6, 1.6, -1.0, 1.0])):
```

Listing 52: Barrier Certificate for a Unicycle Model with Boundary Function

This function creates a barrier certificate for a unicycle system with a rectangular boundary included, ensuring that the robots do not leave the arena. It returns another function for optimization reasons. The inputs for this function are:

- **Barrier Gain** ( $B_g$ ): Controls how quickly agents can approach each other. A lower value implies a slower approach. This parameter is strictly positive ( $B_g > 0$ ).
- **Safety Radius** ( $S_r$ ): Determines how far apart the robots will stay. This parameter must be greater than or equal to 0.12 m ( $S_r \geq 0.12$ ).
- **Projection Distance**: Determines how far ahead of the unicycle model to place the safety "bubble".
- **Magnitude Limit** ( $|v|$ ): Limits the linear speed of the robot. This parameter must be  $0 < |v| \leq 0.2$ .

- **Boundary Points:** This array corresponds to the arena’s dimensions and should not be edited.

The returned function is:

```
def f(dxu, x):
```

Listing 53: Barrier Certificate for a Unicycle Model with Boundary Returned Function

The inputs required by this function are:

- **dxu:** A  $\mathbb{R}^{2 \times N}$  numpy array of the unicycle robot velocity commands.
- **x:** A  $\mathbb{R}^{2 \times N}$  numpy array of the robot states.

It returns a  $\mathbb{R}^{2 \times N}$  numpy array of modified velocity commands that ensure safety and boundary compliance.

#### 4.5.6 Create a Barrier Certificate for a Unicycle Model with Dynamic Gains

```
def create_unicycle_barrier_certificate2(barrier_gain=500, unsafe_barrier_gain=1e6,
safety_radius=0.12, projection_distance=0.05, magnitude_limit=0.2):
```

Listing 54: Barrier Certificate for a Unicycle Model with Dynamic Gains Function

This function creates a barrier certificate for a unicycle system. It returns another function for optimization reasons. This function is different from `create_unicycle_barrier_certificate` as it dynamically changes the barrier gain to a large number if the vehicle enters an unsafe region. The inputs for this function are:

- **Barrier Gain ( $B_g$ ):** Controls how quickly agents can approach each other. A lower value implies a slower approach. This parameter is strictly positive ( $B_g > 0$ ).
- **Unsafe Barrier Gain ( $B_{unsafe}$ ):** Controls how quickly the barrier gain changes when entering an unsafe region. This parameter must be positive ( $B_{unsafe} > 0$ ).
- **Safety Radius ( $S_r$ ):** Determines how far apart the robots will stay. This parameter must be greater than or equal to 0.12 m ( $S_r \geq 0.12$ ).
- **Projection Distance:** Determines how far ahead of the unicycle model to place the safety "bubble".
- **Magnitude Limit ( $|v|$ ):** Limits the linear speed of the robot. This parameter must be  $0 < |v| \leq 0.2$ .

The returned function is:

```
def f(dxu, x):
```

Listing 55: Barrier Certificate for a Unicycle Model with Dynamic Gains Returned Function

The inputs required by this function are:

- **dxu:** A  $\mathbb{R}^{2 \times N}$  numpy array of the unicycle robot velocity commands.
- **x:** A  $\mathbb{R}^{2 \times N}$  numpy array of the robot states.

It returns a  $\mathbb{R}^{2 \times N}$  numpy array of modified velocity commands that ensure safety by dynamically adjusting the barrier gain if needed.

#### 4.5.7 Create Unicycle Differential Drive Barrier Certificate

```
def create_unicycle_differential_drive_barrier_certificate(max_num_obstacle_points=100,
max_num_robots=30, disturbance=5, wheel_vel_limit=12.5, base_length=0.105,
wheel_radius=0.016, projection_distance=0.05, barrier_gain=150, safety_radius=0.17):
```

Listing 56: Unicycle Differential Drive Barrier Certificate Function

This function creates a barrier certificate for a unicycle differential drive system that considers errors in the motor dynamics. More information about this barrier certificate function can be found in Emam et al. 2022. It ensures that robots avoid collisions and operate within safe boundaries. The inputs for this function are:

- **Max Number of Obstacle Points:** Maximum number of obstacle points considered in the environment.
- **Max Number of Robots:** Maximum number of robots in the environment.
- **Disturbance:** A disturbance factor affecting the system.
- **Wheel Velocity Limit:** Maximum wheel velocity limit for the differential drive.
- **Base Length:** Distance between the wheels of the differential drive robot.
- **Wheel Radius:** Radius of the wheels.
- **Projection Distance:** Determines how far ahead of the unicycle model to place the safety "bubble".
- **Barrier Gain ( $B_g$ ):** Controls how quickly agents can approach each other. A lower value implies a slower approach. This parameter is strictly positive ( $B_g > 0$ ).
- **Safety Radius ( $S_r$ ):** Determines how far apart the robots will stay. This parameter must be greater than or equal to 0.17 m ( $S_r \geq 0.17$ ).

The returned function is:

```
def f(dxu, x):
```

Listing 57: Barrier Certificate for a Unicycle Differential Drive Returned Function

The inputs required by this function are:

- **dxu:** A  $\mathbb{R}^{2 \times N}$  numpy array of the unicycle robot velocity commands.
- **x:** A  $\mathbb{R}^{2 \times N}$  numpy array of the robot states.

It returns a  $\mathbb{R}^{2 \times N}$  numpy array of modified velocity commands that ensure safety.

#### 4.5.8 Create Unicycle Differential Drive Barrier Certificate with Boundary

```
def create_unicycle_differential_drive_barrier_certificate_with_boundary(
max_num_obstacle_points=100, max_num_robots=30, disturbance=5, wheel_vel_limit=12.5,
base_length=0.105, wheel_radius=0.016, projection_distance=0.05, barrier_gain=150,
safety_radius=0.17, boundary_points=np.array([-1.6, 1.6, -1.0, 1.0])):
```

Listing 58: Unicycle Differential Drive Barrier Certificate with Boundary Function

This function creates a barrier certificate for a unicycle differential drive system with a rectangular boundary included, ensuring that robots avoid collisions and stay within the defined operational area. More information about this barrier certificate function can be found in Emam et al. 2022. The inputs for this function are:

- **Max Number of Obstacle Points:** Maximum number of obstacle points considered in the environment.
- **Max Number of Robots:** Maximum number of robots in the environment.
- **Disturbance:** A disturbance factor affecting the system.
- **Wheel Velocity Limit:** Maximum wheel velocity limit for the differential drive.
- **Base Length:** Distance between the wheels of the differential drive robot.
- **Wheel Radius:** Radius of the wheels.
- **Projection Distance:** Determines how far ahead of the unicycle model to place the safety "bubble".
- **Barrier Gain ( $B_g$ ):** Controls how quickly agents can approach each other. A lower value implies a slower approach. This parameter is strictly positive ( $B_g > 0$ ).
- **Safety Radius ( $S_r$ ):** Determines how far apart the robots will stay. This parameter must be greater than or equal to 0.17 m ( $S_r \geq 0.17$ ).
- **Boundary Points:** This array corresponds to the arena's dimensions and should not be edited.

The returned function is:

```
def f(dxu, x):
```

Listing 59: Barrier Certificate for a Unicycle Differential Drive with Boundary Returned Function

The inputs required by this function are:

- **dxu:** A  $\mathbb{R}^{2 \times N}$  numpy array of the unicycle robot velocity commands.
- **x:** A  $\mathbb{R}^{2 \times N}$  numpy array of the robot states.

It returns a  $\mathbb{R}^{2 \times N}$  numpy array of modified velocity commands that ensure safety and boundary compliance.

## 4.6 Barrier Certificates 2

### 4.6.1 Create Robust Barriers for Unicycle Differential Drive with Dynamic Gains

```
def create_robust_barriers(max_num_obstacles=100, max_num_robots=30, d=5, wheel_vel_limit=12.5,
base_length=0.105, wheel_radius=0.016, projection_distance=0.05, gamma=150,
safety_radius=0.12):
```

Listing 60: Robust Barriers for Unicycle Differential Drive with Dynamic Gains Function

This function creates robust barriers for a unicycle differential drive system, ensuring that robots avoid collisions and operate within safe boundaries. It dynamically adjusts barrier gains if the vehicle enters an unsafe region. The inputs for this function are:

- **Max Number of Obstacles:** Maximum number of obstacle points considered in the environment.
- **Max Number of Robots:** Maximum number of robots in the environment.
- **Disturbance ( $d$ ):** A disturbance factor affecting the system.
- **Wheel Velocity Limit:** Maximum wheel velocity limit for the differential drive.
- **Base Length:** Distance between the wheels of the differential drive robot.
- **Wheel Radius:** Radius of the wheels.
- **Projection Distance:** Determines how far ahead of the unicycle model to place the safety "bubble".
- **Barrier Gain ( $\gamma$ ):** Controls how quickly agents can approach each other. A lower value implies a slower approach. This parameter is strictly positive ( $\gamma > 0$ ).
- **Safety Radius ( $S_r$ ):** Determines how far apart the robots will stay. This parameter must be greater than or equal to 0.12 m ( $S_r \geq 0.12$ ).

The returned function is:

```
def robust_barriers(dxu, x, obstacles):
```

Listing 61: Robust Barriers for Unicycle Differential Drive with Dynamic Gains Returned Function

The inputs required by this function are:

- **dxu:** A  $\mathbb{R}^{2 \times N}$  numpy array of the unicycle robot velocity commands.
- **x:** A  $\mathbb{R}^{2 \times N}$  numpy array of the robot states.
- **obstacles:** A  $\mathbb{R}^{2 \times M}$  numpy array of the positions of obstacles.

It returns a  $\mathbb{R}^{2 \times N}$  numpy array of modified velocity commands that ensure safety by dynamically adjusting the barrier gain if needed.



## 4.7 Miscellaneous

This section provides a set of utility functions designed to support the initialization and validation of robot positions and orientations.

### 4.7.1 Generate Random Initial Positions for the Robots

```
def generate_initial_conditions(N, spacing=0.3, width=3, height=1.8):
```

Listing 62: Initial Position Function

This function generates random initial conditions in an area of the specified width and height at the required spacing. The inputs for this function are:

- **N**: Number of robots used in the experiment. This parameter must be positive. Specifically,  $N = 1, \dots, 20$
- **Spacing**: How far apart positions can be. This parameter must be positive.
- **Width**: Width of the area. This parameter must be positive.
- **Height**: Height of the area. This parameter must be positive.

It returns a  $\mathbb{R}^{3 \times N}$  numpy array of the robot states.

### 4.7.2 Evaluate Whether the Robots are "Close Enough" to Poses

```
def at_pose(states, poses, position_error=0.05, rotation_error=0.2):
```

Listing 63: Evaluate Whether Robots are "Close Enough" to Poses Function

In some cases, it is not necessary for robots to reach the exact position commanded. A small margin of error is acceptable, such as 1%. This function checks whether robots are "close enough" to the desired positions and orientations. The inputs for this function are:

- **States**: A  $\mathbb{R}^{3 \times N}$  numpy array of the unicycle states.
- **Poses**: A  $\mathbb{R}^{3 \times N}$  numpy array of the desired states.
- **Position Error**: The tolerable error in the position.
- **Rotation Error**: The tolerable error in the heading.

It returns a  $\mathbb{R}^{1 \times N}$  index array of the agents that are close enough.

### 4.7.3 Evaluate Whether Robots are "Close Enough" to Desired Position

```
def at_position(states, points, position_error=0.02):
```

Listing 64: Evaluate Whether Robots are "Close Enough" to the Desired Position Function

As before, in some cases, it is not necessary for robots to reach the exact desired position. A small margin of error is acceptable. This is useful when robots are moving through waypoints; if they are close enough, they can proceed to the next waypoint. The inputs for this function are:

- **States:** A  $\mathbb{R}^{3 \times N}$  numpy array of the unicycle states.
- **Points:** A  $\mathbb{R}^{2 \times N}$  numpy array of the desired positions.
- **Position Error:** The tolerable error in the position.

It returns a  $\mathbb{R}^{1 \times N}$  index array of the agents that are close enough.

#### 4.7.4 Marker Size

```
def determine_marker_size(robotarium_instance, marker_size_meters):
```

Listing 65: Marker Size Function

This function determines the appropriate marker size in points so it fits the Robotarium listing window. It calculates the ratio of the robot size to the x-axis and adjusts the marker size accordingly. The inputs for this function are:

- **Robotarium Instance:** The Robotarium object.
- **Marker Size Meters:** The desired size in meters.

It returns the appropriate marker size in points.

#### 4.7.5 Determine Font Size

```
def determine_font_size(robotarium_instance, font_height_meters):
```

Listing 66: Determine Font Size Function

This function determines the appropriate font size in points so that it fits the Robotarium figure window. It calculates the ratio of the desired font height to the y-axis of the figure window and adjusts the font size accordingly. The inputs for this function are:

- **Robotarium Instance:** The Robotarium object.
- **Font Height Meters:** The desired font height in meters.

It returns the appropriate font size in points.

## 4.8 Graph

This section provides a set of utility functions for generating graph Laplacians for different types of graphs and determining neighbors based on the graph Laplacian or distance.

### 4.8.1 Generate a Graph Laplacian for a Cycle Graph

```
def cycle_GL(N):
```

Listing 67: Generate a Graph Laplacian for a Cycle Graph

This function generates a graph Laplacian for a cycle graph. A cycle graph is a graph that consists of a single cycle, meaning each node is connected in a closed loop. The function ensures the resulting Laplacian matrix correctly represents the cycle graph structure. The inputs for this function are:

- **N**: Integer, the number of agents in the cycle graph. Must be positive.

It returns an  $N \times N$  numpy array representing the graph Laplacian.

### 4.8.2 Generate a Graph Laplacian for a Line Graph

```
def lineGL(N):
```

Listing 68: Generate a Graph Laplacian for a Line Graph

This function generates a graph Laplacian for a line graph. A line graph is a graph where each node is connected to its predecessor and successor nodes, forming a straight line. The inputs for this function are:

- **N**: Integer, the number of agents in the line graph. Must be positive.

It returns an  $N \times N$  numpy array representing the graph Laplacian.

### 4.8.3 Generate a Graph Laplacian for a Complete Graph

```
def completeGL(N):
```

Listing 69: Generate a Graph Laplacian for a Complete Graph

This function generates a graph Laplacian for a complete graph. A complete graph is a graph where each node is connected to every other node. The inputs for this function are:

- **N**: Integer, the number of agents in the complete graph. Must be positive.

It returns an  $N \times N$  numpy array representing the graph Laplacian.

### 4.8.4 Generate a Laplacian for a Random, Connected Graph

```
def random_connectedGL(v, e):
```

Listing 70: Generate a Laplacian for a Random, Connected Graph

This function generates a Laplacian for a random, connected graph with a specified number of vertices and additional edges. It ensures the graph remains connected. The inputs for this function are:

- **v**: Integer, the number of vertices (nodes) in the graph. Must be positive.
- **e**: Integer, the number of additional edges to add to the graph. Must be non-negative.

It returns a  $v \times v$  numpy array representing the graph Laplacian.

#### 4.8.5 Generate a Laplacian for a Random Graph

```
def randomGL(v, e):
```

Listing 71: Generate a Laplacian for a Random Graph

This function generates a Laplacian for a random graph with a specified number of vertices and edges. The inputs for this function are:

- **v**: Integer, the number of vertices (nodes) in the graph. Must be positive.
- **e**: Integer, the number of edges to add to the graph. Must be non-negative.

It returns a  $v \times v$  numpy array representing the graph Laplacian.

#### 4.8.6 Determine Topological Neighbors

```
def topological_neighbors(L, agent):
```

Listing 72: Determine Topological Neighbors

This function returns the neighbors of a particular agent using the graph Laplacian. Neighbors are defined as nodes directly connected to the agent. The inputs for this function are:

- **L**: An  $N \times N$  numpy array representing the graph Laplacian.
- **agent**: Integer, the agent number (0 to N-1).

It returns a 1xM numpy array with M neighbors.

#### 4.8.7 Determine Delta-Disk Neighbors

```
def delta_disk_neighbors(poses, agent, delta):
```

Listing 73: Determine Delta-Disk Neighbors

This function returns the agents within a specified distance (delta) from a given agent, excluding the agent itself. It uses the 2-norm to determine the distance. The inputs for this function are:

- **poses**: A  $3 \times N$  numpy array representing the unicycle states of the robots.
- **agent**: Integer, the agent whose neighbors within a radius will be returned.
- **delta**: Float, the radius of the delta disk considered.

It returns a 1xM numpy array with M neighbors.

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## 6 Conclusion

Congrats! You have successfully completed this guide and should now be closer to running your own full scripts/algorithms on the Robotarium. We are always improving the simulator and Robotarium so feel free to check this guide or the [website](#) for any updates! If you have any questions please contact Sean Wilson ([Sean.Wilson@gtri.gatech.edu](mailto:Sean.Wilson@gtri.gatech.edu))

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<sup>3</sup>The names above are listed in alphabetical order and not according to the level of contribution.

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## A Libraries Available in the Robotarium

Below is a list of the current libraries that are available in the Robotarium environment:

- `RobotariumAPI`
- `numpy`
- `scipy`
- `matplotlib`
- `cvxpy`