

Introduction to Deep Learning MIT 6.S191

Alexander Amini

January 28, 2019





'Deep Voice' Software Can Clone Anyone's Voice With Just 3.7 Seconds of Audio

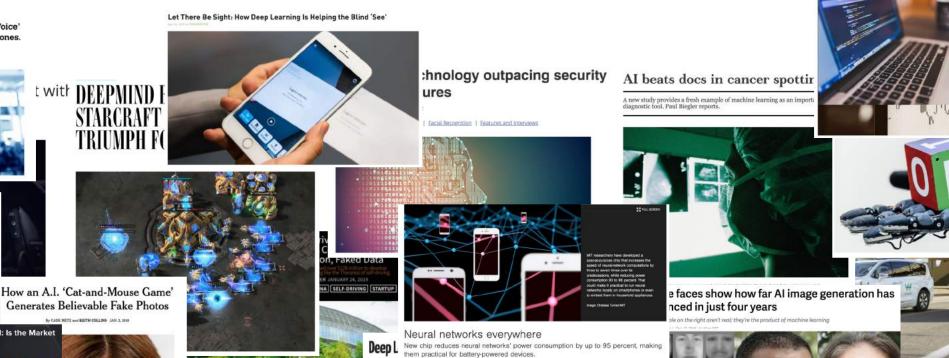
Using snippets of voices, Baidu's 'Deep Voice'

can generate new speech, accents, and tones. 'Creative' AlphaZero leads way for

chess computers and, maybe, science

Former chess world champion Garry Kasparov likes what he

The Rise of Deep Learning





To create the final image in this set, the system generated 10 million revisions over 1

After Millions of Trials, These Simulated Humans Learned to Do Perfect Backflips and Cartwheels

Researchers introduce a deep learning method that converts mono audio recordings into 3D sounds using video scenes

Automation And Algorithms: De-Risking Manufacturing With Artificial Intelligence

Al Can Help In Predicting Cryptocurrency

Value



The two key applications of AI in manufacturing are pricing and

By Robert F. Service | Dec. 6, 2018, 12:05 PM

Google's DeepMind aces protein folding

What is Deep Learning?

ARTIFICIAL INTELLIGENCE

Any technique that enables computers to mimic human behavior



MACHINE LEARNING

Ability to learn without explicitly being programmed



DEEP LEARNING

Extract patterns from data using neural networks

313472

Lecture Schedule

Part 1 Lab Session Part 2 Introduction to Deep Deep Sequence Modeling Intro to TensorFlow, Music Learning [Slides] [Video] Generation with RNNs [Slides] [Video] [Code] coming soon! coming soon! coming soon! Deep Computer Vision Deep Generative Models De-biasing Facial 2 [Slides] [Video] [Slides] [Video] Recognition Systems [Code] coming soon! comina soon! comina soon! Model-Free Reinforcement 3 Deep Reinforcement Limitations and New Frontiers Learning Learning [Slides] [Video] [Slides] [Video] [Code] coming soon! coming soon! coming soon! Work time for paper Data Visualization for Biologically Inspired reviews/project proposals Machine Learning Learning [Info][Slides] [Video] [Info][Slides] [Video] coming soon! coming soon! Learing and Perception Final Project Presentations Judging and Awards 5 [Info][Slides] [Video] Ceremony coming soon!



- Mon Jan 28 Fri Feb I
- 1:00 pm 4:00 pm
- Lecture + Lab Breakdown
- Graded P/D/F; 3 Units
- I Final Assignment

Final Class Project

Option I: Proposal Presentation

- Groups of 3 or 4
- Present a novel deep learning research idea or application
- 3 minutes (strict)
- List of example proposals on website: <u>introtodeeplearning.com</u>
- Presentations on Friday, Feb I
- Submit groups by Wednesday
 5pm to be eligible
- Submit slide by **Thursday 9pm** to be eligible

- Judged by a panel of industry judges
- Top winners are awarded:







4x Google Home MSRP: \$400



Final Class Project

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Option 2: Write a 1-page review of a deep learning paper

- Grade is based on clarity of writing and technical communication of main ideas
- Due **Friday I:00pm** (before lecture)

Class Support

- Piazza: http://piazza.com/mit/spring2019/6s191
 - Useful for discussing labs
- Course Website: http://introtodeeplearning.com
 - Lecture schedule
 - Slides and lecture recordings
 - Software labs
 - Grading policy
- Email us: introtodeeplearning-staff@mit.edu
- Office Hours by request

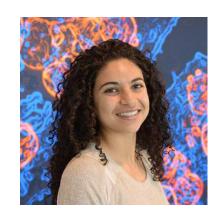


Course Staff

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Ava Soleimany Lead Organizer





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Julia



Felix



Jacob



Rohil



Gilbert

introtodeeplearning-staff@mit.edu

+ Ravi A.

Thanks to Sponsors!









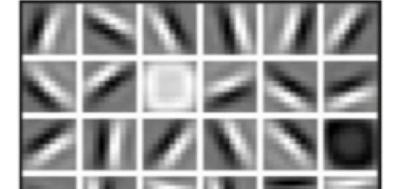
Why Deep Learning and Why Now?

Why Deep Learning?

Hand engineered features are time consuming, brittle and not scalable in practice

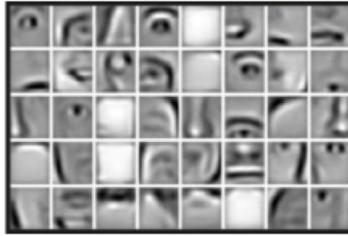
Can we learn the **underlying features** directly from data?

Low Level Features



Lines & Edges

Mid Level Features



Eyes & Nose & Ears

High Level Features



Facial Structure

Why Now?

Neural Networks date back decades, so why the resurgence?

Stochastic Gradient Descent

Perceptron

• Learnable Weights

Backpropagation

Multi-Layer Perceptron

Deep Convolutional NN

Digit Recognition

I. Big Data

- Larger Datasets
- Easier Collection& Storage







2. Hardware

- Graphics Processing Units (GPUs)
- Massively
 Parallelizable



3. Software

- Improved Techniques
- New Models
- Toolboxes





1958

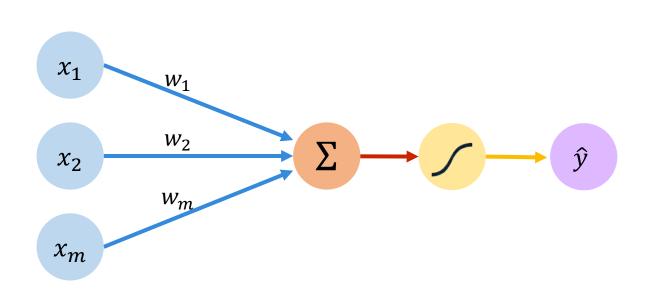
1986

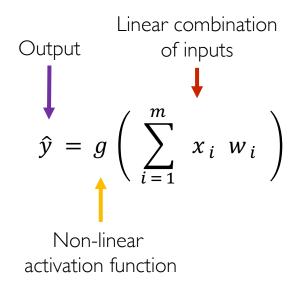
1995



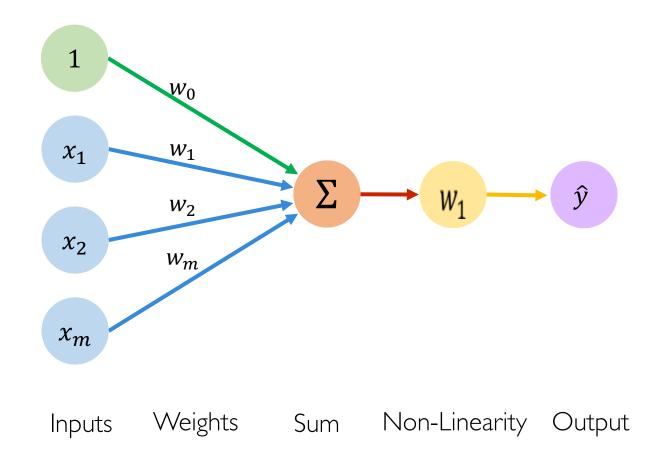
The Perceptron The structural building block of deep learning

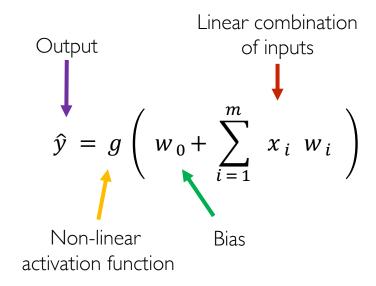
感知器:前向传播



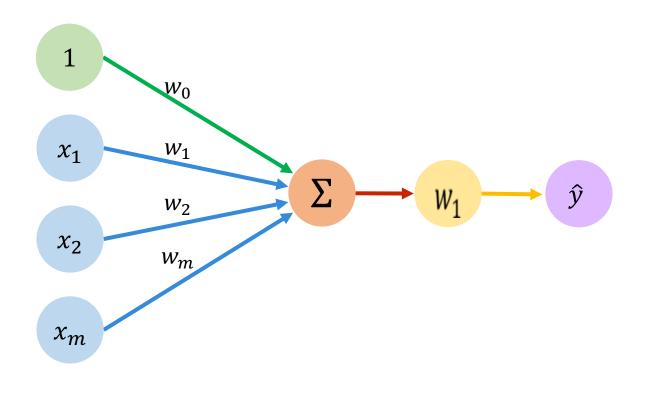


Inputs Weights Sum Non-Linearity Output









$$\hat{y} = g \left(w_0 + \sum_{i=1}^m x_i w_i \right)$$

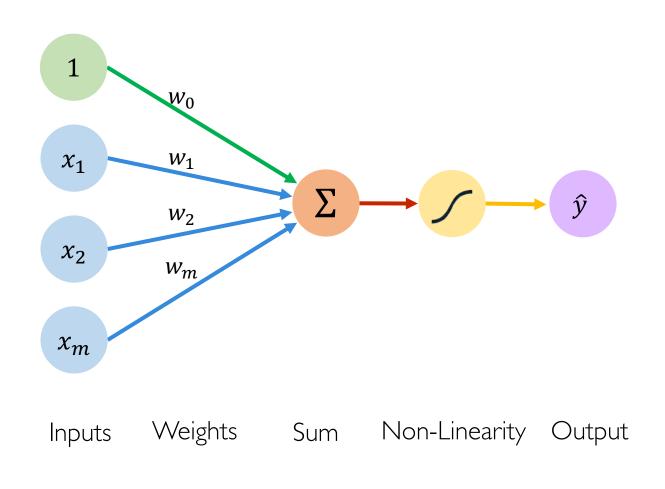
$$\hat{y} = g(w_0 + \boldsymbol{X}^T \boldsymbol{W})$$

where:
$$\boldsymbol{X} = \begin{bmatrix} x_1 \\ \vdots \\ x_m \end{bmatrix}$$
 and $\boldsymbol{W} = \begin{bmatrix} w_1 \\ \vdots \\ w_m \end{bmatrix}$

Weights

Sum

Non-Linearity Output

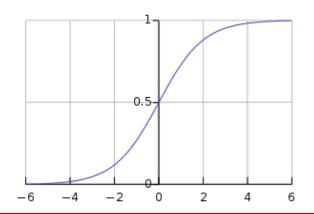


Activation Functions

$$\hat{y} = g(w_0 + X^T W)$$

• Example: sigmoid function

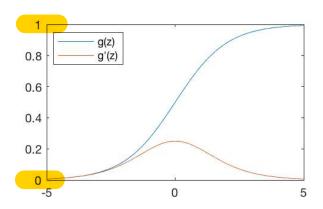
$$g(z) = \sigma(z) = \frac{1}{1 + e^{-z}}$$



 \boldsymbol{Z}

Common Activation Functions

Sigmoid Function

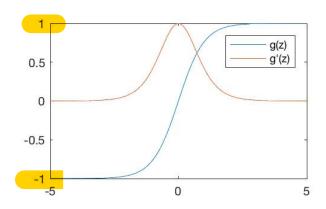


$$g(z) = \frac{1}{1 + e^{-z}}$$

$$g'(z) = g(z)(1 - g(z))$$



Hyperbolic Tangent (tanh)

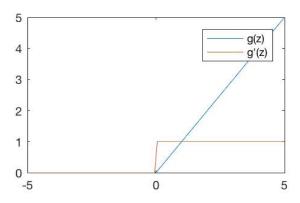


$$g(z) = \frac{e^{z} - e^{-z}}{e^{z} + e^{-z}}$$

$$g'(z) = 1 - g(z)^2$$



Rectified Linear Unit (ReLU)



$$g(z) = \max(0, z)$$

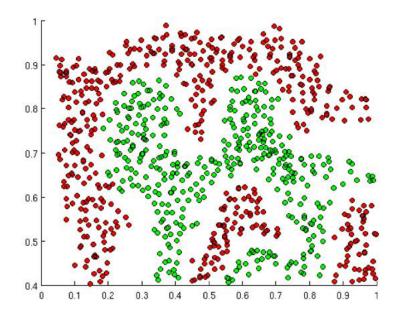
$$g'(z) = \begin{cases} 1, & z > 0 \\ 0, & \text{otherwise} \end{cases}$$



NOTE: All activation functions are non-linear

Importance of Activation Functions

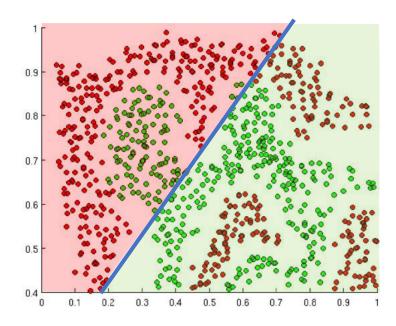
The purpose of activation functions is to **introduce non-linearities** into the network 向神经网络引入非线性化



What if we wanted to build a Neural Network to distinguish green vs red points?

Importance of Activation Functions

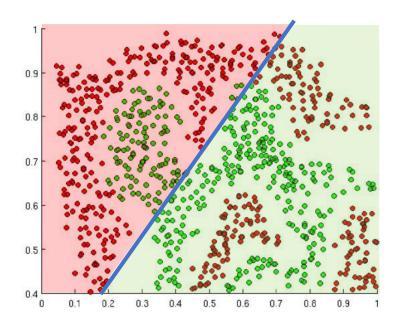
The purpose of activation functions is to **introduce non-linearities** into the network



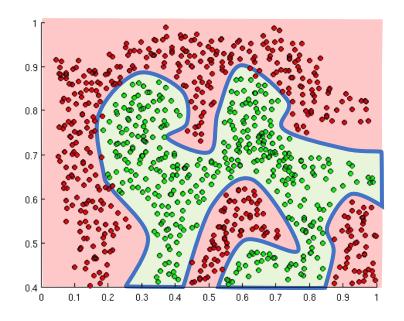
Linear Activation functions produce linear decisions no matter the network size

Importance of Activation Functions

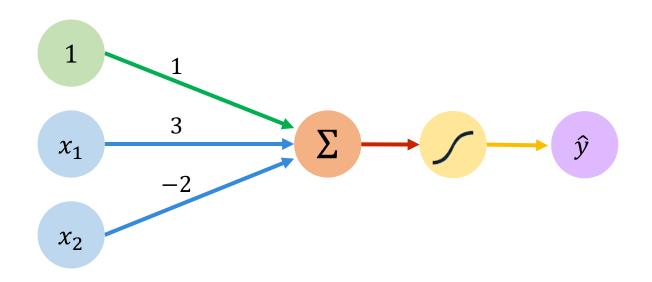
The purpose of activation functions is to **introduce non-linearities** into the network



Linear Activation functions produce linear decisions no matter the network size



Non-linearities allow us to approximate arbitrarily complex functions



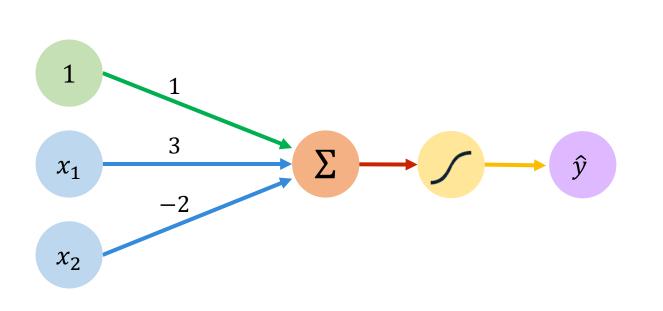
We have:
$$w_0 = 1$$
 and $\boldsymbol{W} = \begin{bmatrix} 3 \\ -2 \end{bmatrix}$

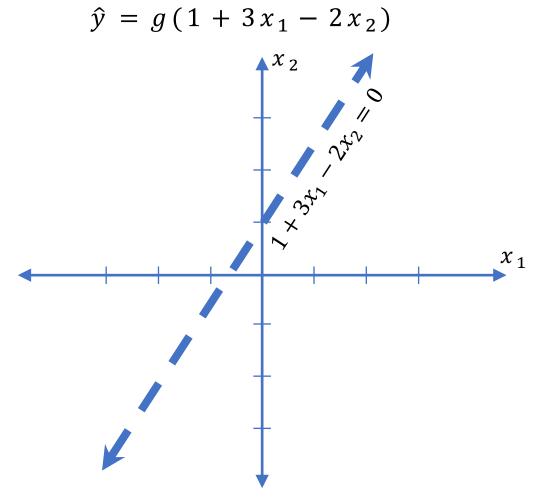
$$\hat{y} = g(w_0 + X^T W)$$

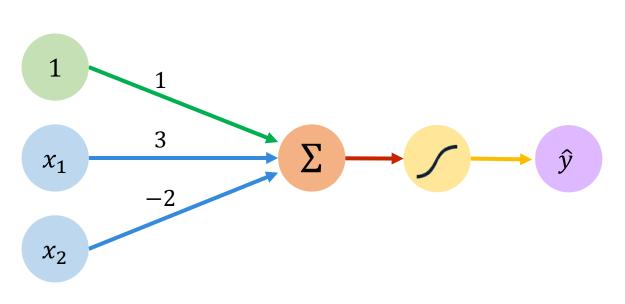
$$= g\left(1 + \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}^T \begin{bmatrix} 3 \\ -2 \end{bmatrix}\right)$$

$$\hat{y} = g(1 + 3x_1 - 2x_2)$$

This is just a line in 2D!



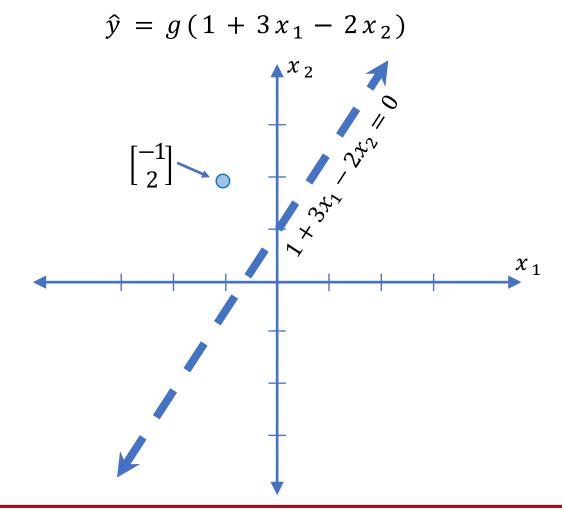


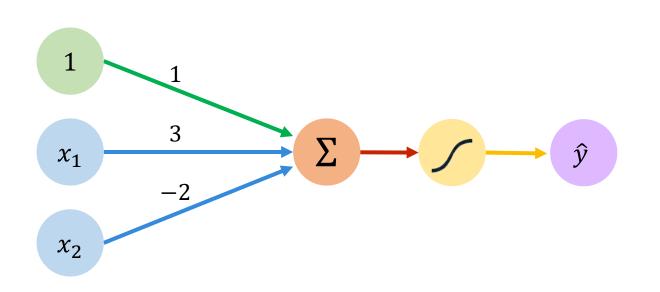


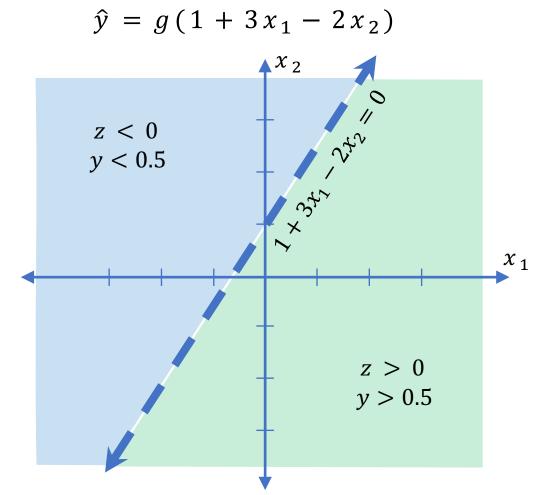
Assume we have input: $X = \begin{bmatrix} -1 \\ 2 \end{bmatrix}$

$$\hat{y} = g (1 + (3*-1) - (2*2))$$

= $g (-6) \approx 0.002$

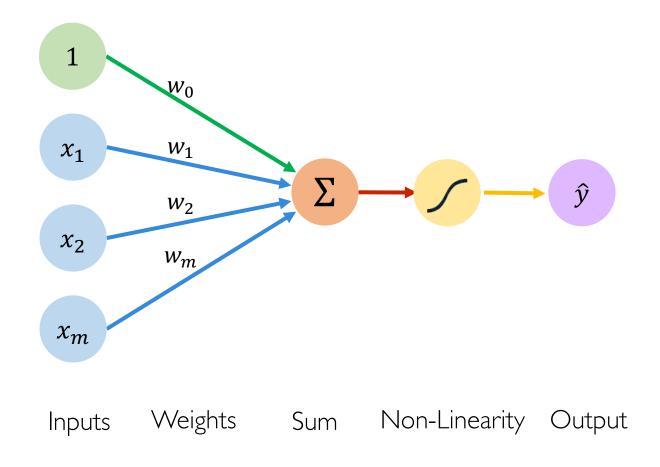




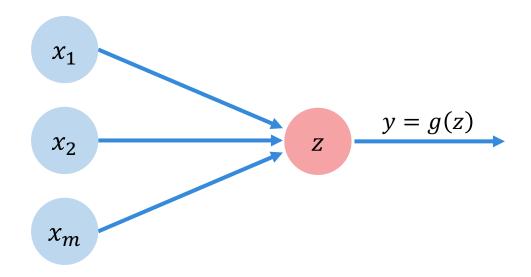


Building Neural Networks with Perceptrons

The Perceptron: Simplified

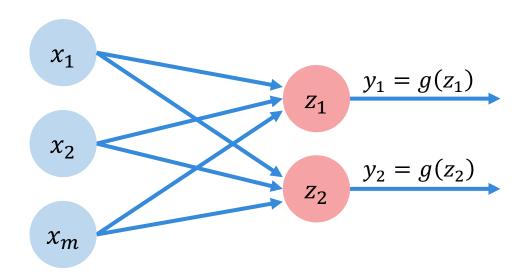


The Perceptron: Simplified



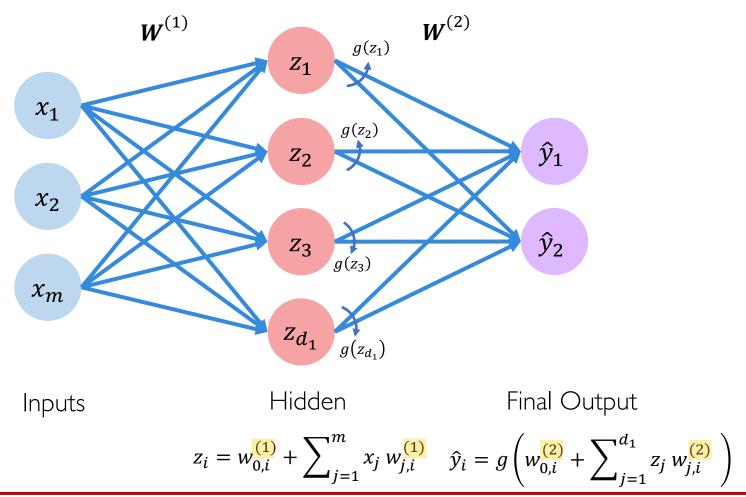
$$z = w_0 + \sum_{j=1}^m x_j w_j$$

Multi Output Perceptron



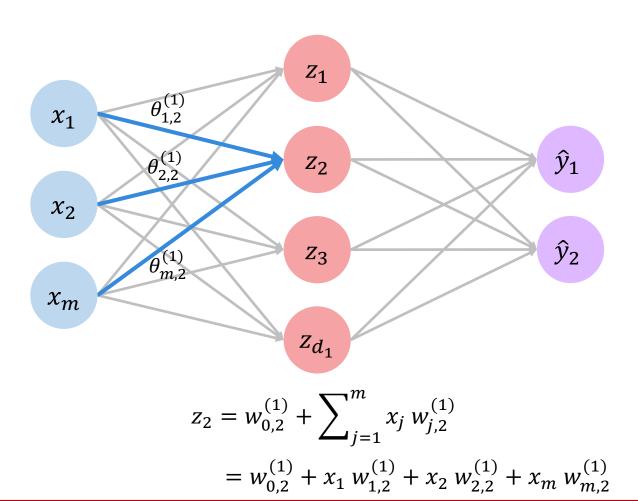
$$z_{\underline{i}} = w_{0,\underline{i}} + \sum_{j=1}^{m} x_j w_{j,\underline{i}}$$

Single Layer Neural Network



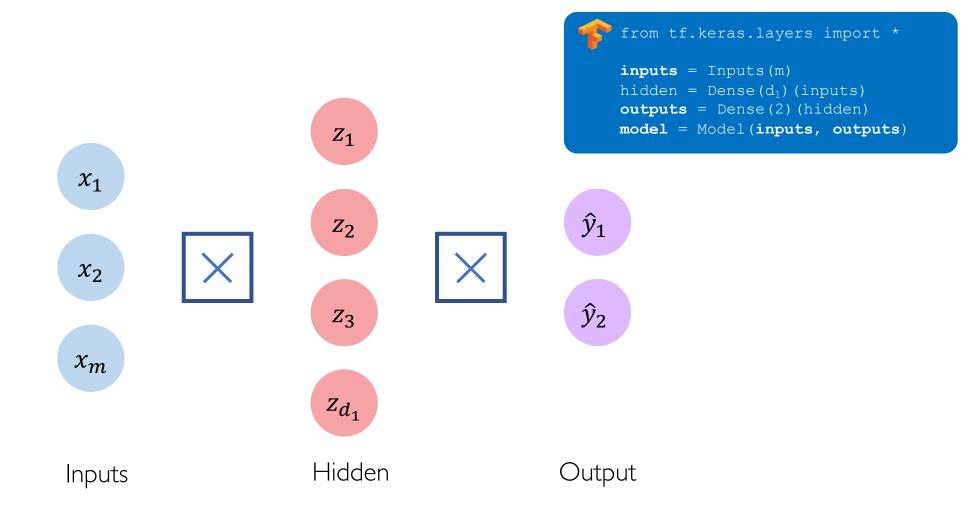


Single Layer Neural Network

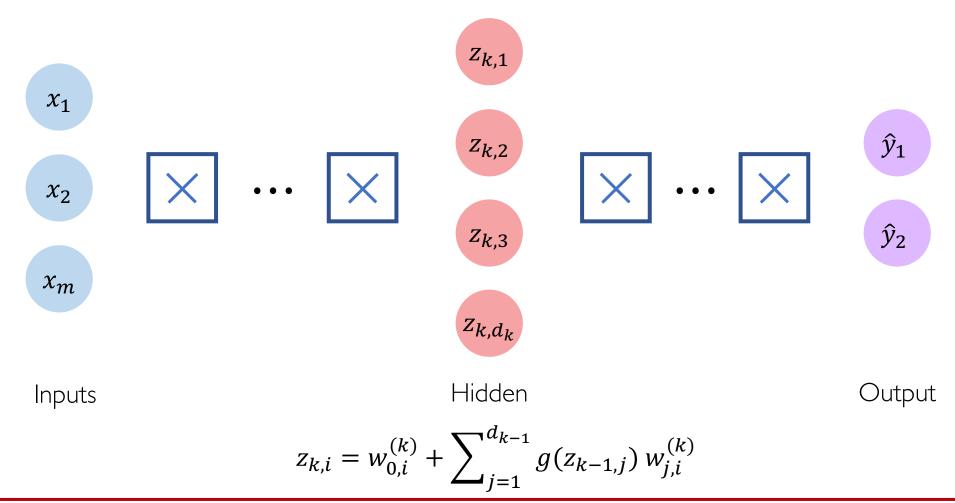




Multi Output Perceptron



Deep Neural Network



Applying Neural Networks

Example Problem

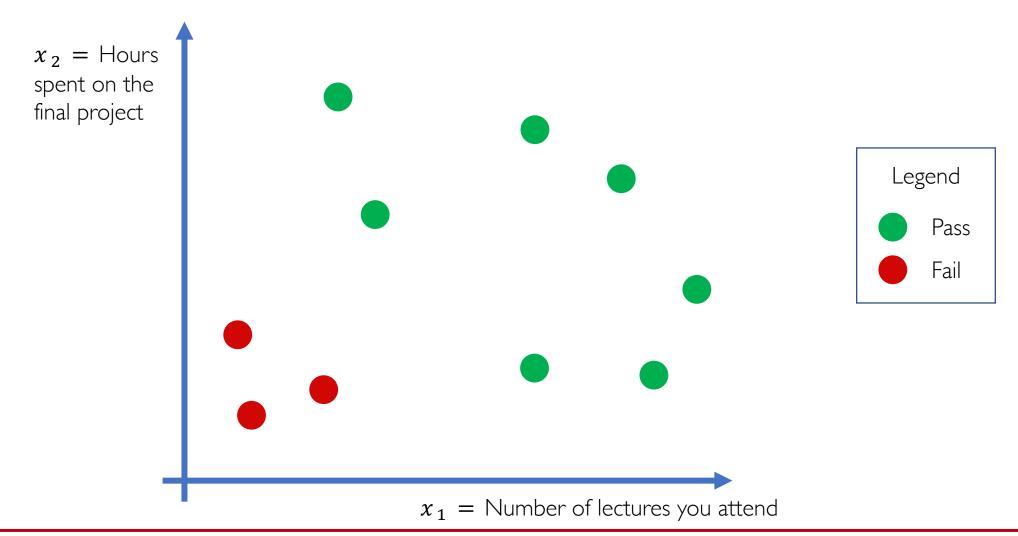
Will I pass this class?

Let's start with a simple two feature model

 x_1 = Number of lectures you attend

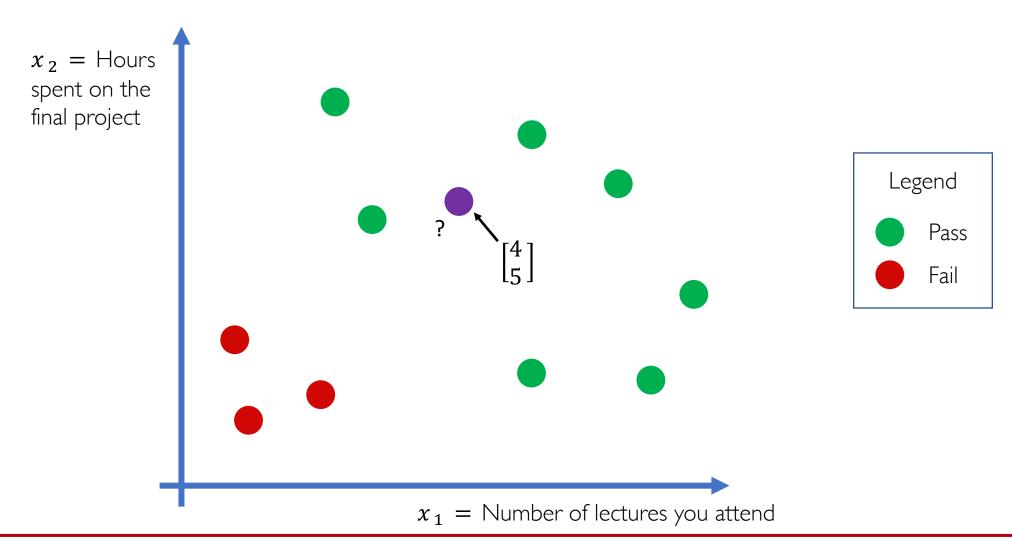
 x_2 = Hours spent on the final project

Example Problem: Will I pass this class?



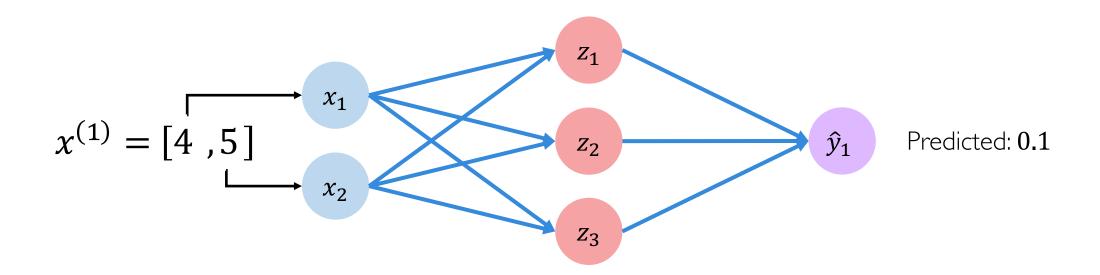


Example Problem: Will I pass this class?

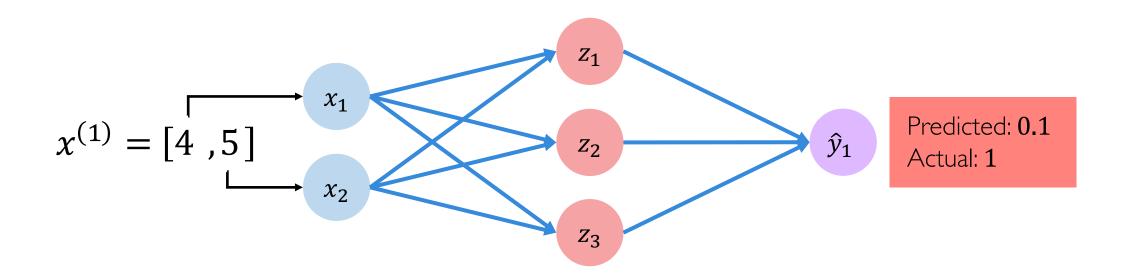




Example Problem: Will I pass this class?



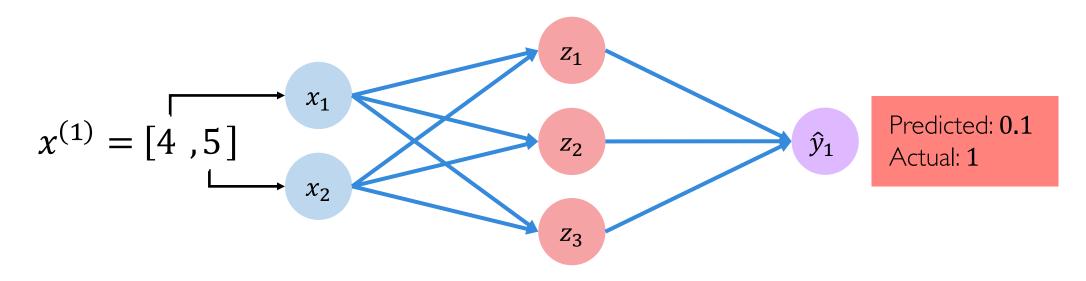
Example Problem: Will I pass this class?



Quantifying Loss

量化损失

The **loss** of our network measures the cost incurred from incorrect predictions



$$\mathcal{L}\left(f\left(x^{(i)};W\right),y^{(i)}\right)$$
Predicted Actual

Empirical Loss

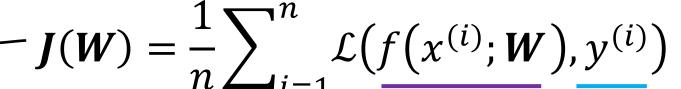
经验损失

The **empirical loss** measures the total loss over our entire dataset

$$\mathbf{X} = \begin{bmatrix} 4 & 5 \\ 2 & 1 \\ 5 & 8 \\ \vdots & \vdots \end{bmatrix} \qquad \begin{array}{c} x_1 \\ x_2 \\ x_3 \end{array} \qquad \begin{array}{c} f(x) & y \\ 0.1 \\ 0.8 \\ 0.6 \\ \vdots \end{array} \qquad \begin{bmatrix} 0 & 1 \\ 0 & 0 \\ 0 & 1 \\ \vdots \end{bmatrix}$$

Also known as:

- Objective function
- Cost function
- Empirical Risk



Predicted

Actual



Binary Cross Entropy Loss

二元交叉熵损失——输出为概率

Cross entropy loss can be used with models that output a probability between 0 and 1

$$X = \begin{bmatrix} 4, & 5 \\ 2, & 1 \\ 5, & 8 \\ \vdots & \vdots \end{bmatrix} \qquad \begin{array}{c} x_1 \\ x_2 \\ \hline \end{array}$$

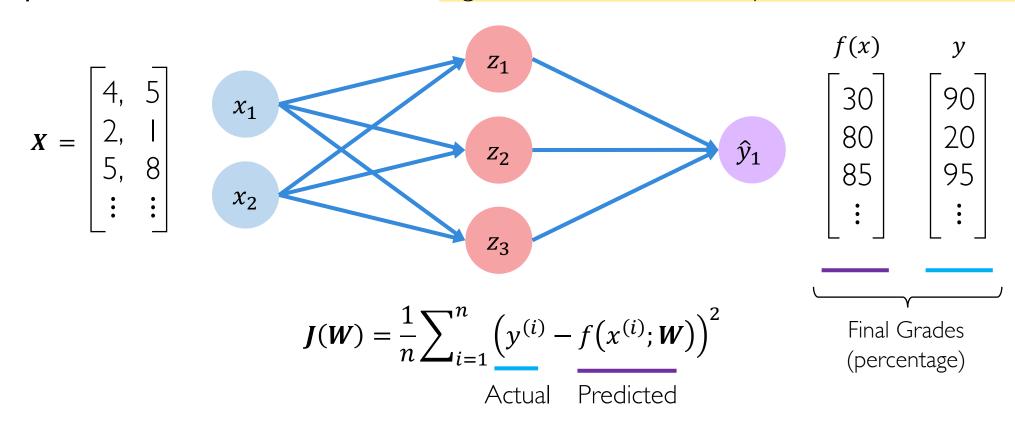
$$\begin{array}{c} f(x) & y \\ \hline 0.1 \\ 0.8 \\ 0.6 \\ \vdots \end{array} \qquad \begin{bmatrix} 0 & 1 \\ 0 & 0 \\ 0 & 1 \\ \vdots \end{bmatrix}$$

$$J(\mathbf{W}) = \frac{1}{n} \sum_{i=1}^{n} y^{(i)} \log \left(f(x^{(i)}; \mathbf{W}) \right) + (1 - y^{(i)}) \log \left(1 - f(x^{(i)}; \mathbf{W}) \right)$$
Actual Predicted Actual Predicted

Mean Squared Error Loss

均方误差损失——回归模型、输出为连续数字

Mean squared error loss can be used with regression models that output continuous real numbers



Training Neural Networks

We want to find the network weights that achieve the lowest loss

$$W^* = \underset{W}{\operatorname{argmin}} \frac{1}{n} \sum_{i=1}^{n} \mathcal{L}(f(x^{(i)}; W), y^{(i)})$$
$$W^* = \underset{W}{\operatorname{argmin}} J(W)$$

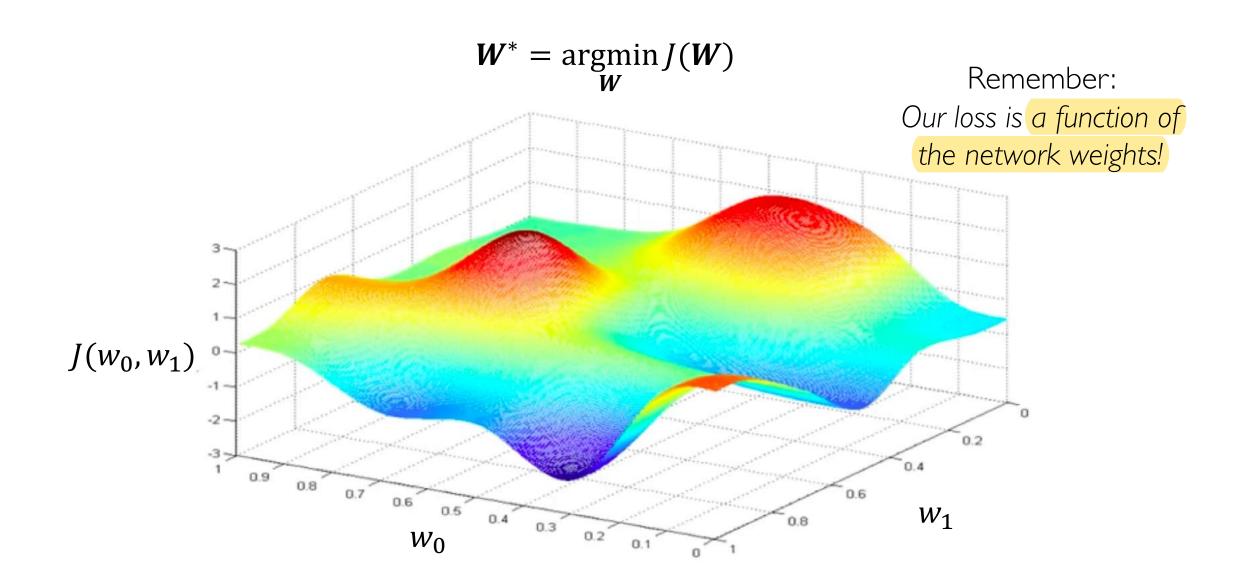
We want to find the network weights that achieve the lowest loss

$$\boldsymbol{W}^* = \underset{\boldsymbol{W}}{\operatorname{argmin}} \frac{1}{n} \sum_{i=1}^{n} \mathcal{L}(f(\boldsymbol{x}^{(i)}; \boldsymbol{W}), \boldsymbol{y}^{(i)})$$

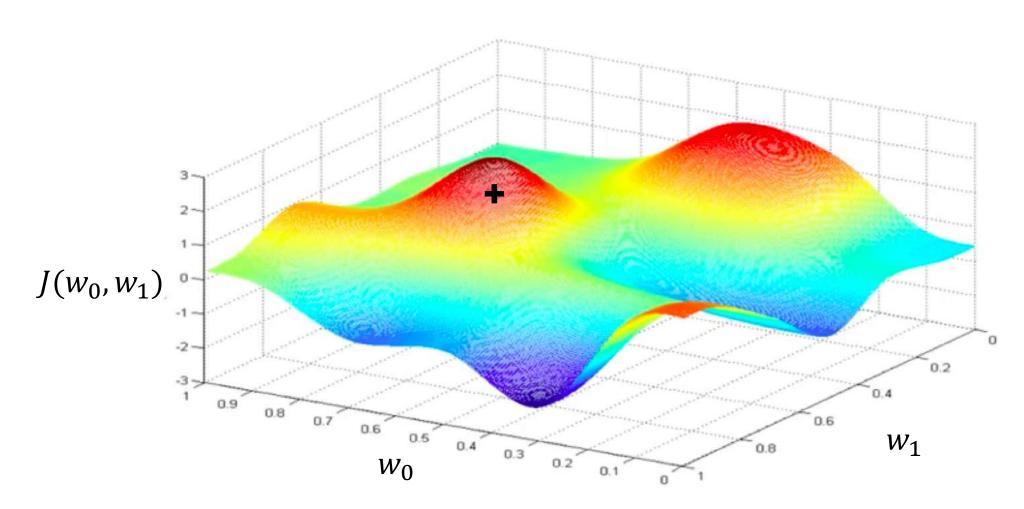
$$\boldsymbol{W}^* = \underset{\boldsymbol{W}}{\operatorname{argmin}} J(\boldsymbol{W})$$

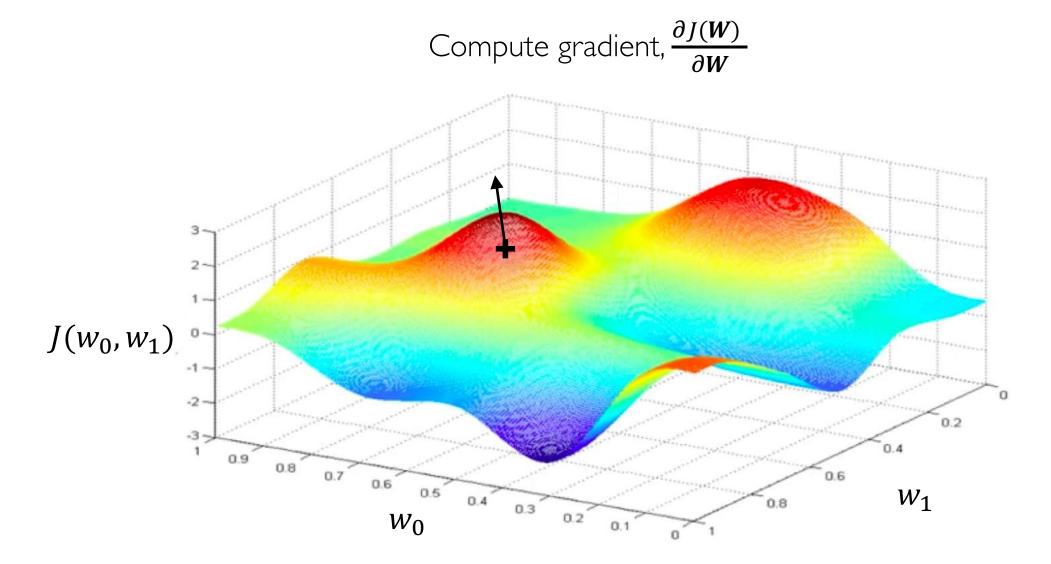
$$\overset{\text{Remember:}}{\boldsymbol{W}}$$

$$\boldsymbol{W} = \{\boldsymbol{W}^{(0)}, \boldsymbol{W}^{(1)}, \dots\}$$

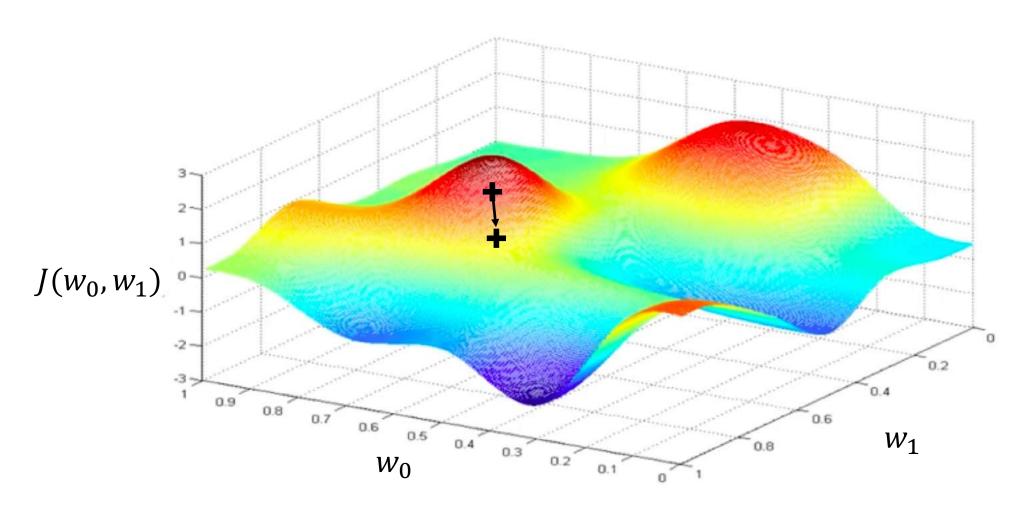


Randomly pick an initial (w_0, w_1)

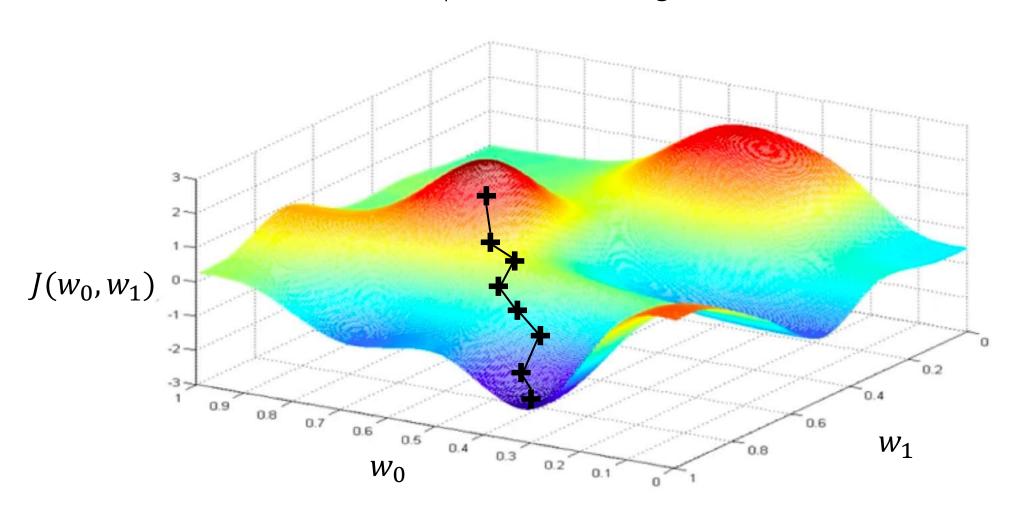




Take small step in opposite direction of gradient



Repeat until convergence



Algorithm

Initialize weights randomly $\sim \mathcal{N}(0, \sigma^2)$



- Loop until convergence:
- Compute gradient, $\frac{\partial J(W)}{\partial W}$ 3.
- Update weights, $W \leftarrow W \eta \frac{\partial J(W)}{\partial W}$
- grads = tf.gradients(ys=loss, xs=weights)
- weights_new = weights.assign(weights lr * grads)

5. Return weights

Algorithm

Initialize weights randomly $\sim \mathcal{N}(0, \sigma^2)$

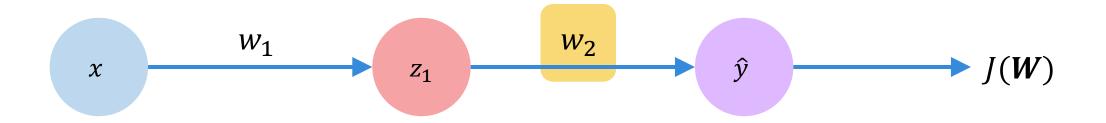


- Loop until convergence:
- 3.
- Compute gradient, $\frac{\partial J(W)}{\partial W}$ Update weights, $W \leftarrow W \eta \frac{\partial J(W)}{\partial W}$
- weights_new = weights.assign(weights lr * grads)

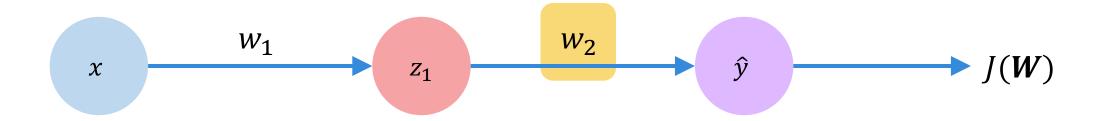
grads = tf.gradients(ys=loss, xs=weights)

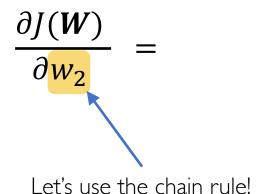
5. Return weights

反向传播

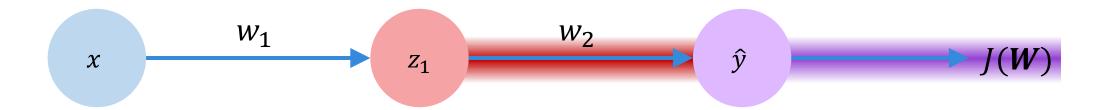


How does a small change in one weight (ex. w_2) affect the final loss J(W)?

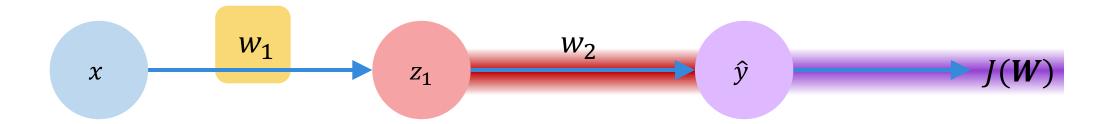


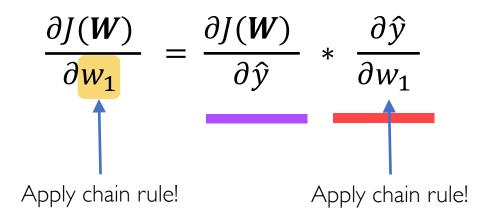




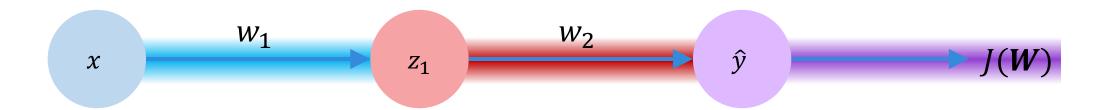


$$\frac{\partial J(\mathbf{W})}{\partial w_2} = \frac{\partial J(\mathbf{W})}{\partial \hat{y}} * \frac{\partial \hat{y}}{\partial w_2}$$

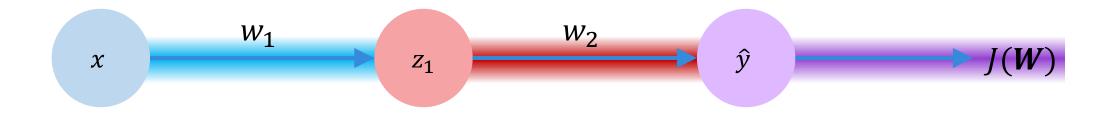








$$\frac{\partial J(\mathbf{W})}{\partial w_1} = \frac{\partial J(\mathbf{W})}{\partial \hat{y}} * \frac{\partial \hat{y}}{\partial z_1} * \frac{\partial z_1}{\partial w_1}$$

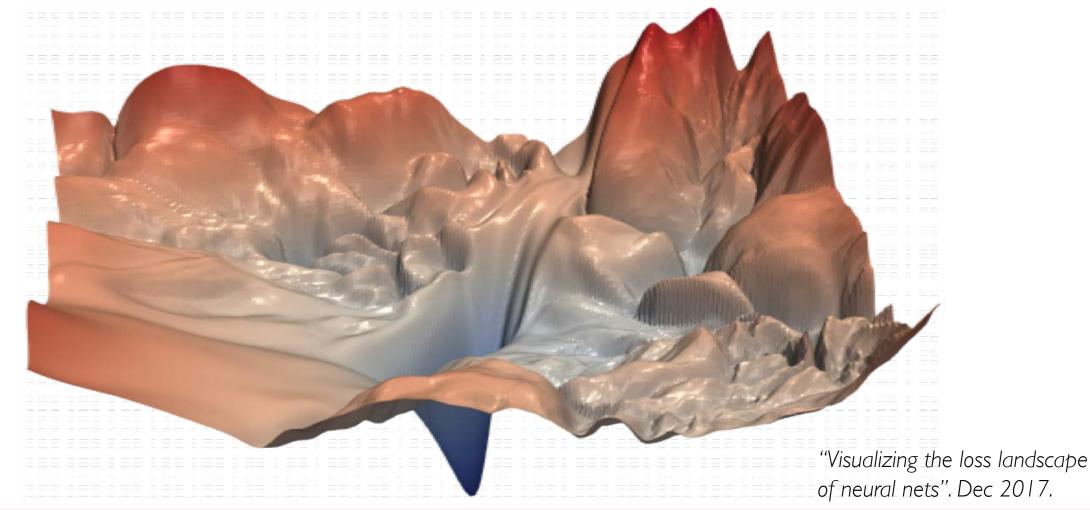


$$\frac{\partial J(\mathbf{W})}{\partial w_1} = \frac{\partial J(\mathbf{W})}{\partial \hat{y}} * \frac{\partial \hat{y}}{\partial z_1} * \frac{\partial z_1}{\partial w_1}$$

Repeat this for every weight in the network using gradients from later layers

Neural Networks in Practice: Optimization

Training Neural Networks is Difficult



Loss Functions Can Be Difficult to Optimize

Remember:

Optimization through gradient descent

$$\boldsymbol{W} \leftarrow \boldsymbol{W} - \eta \, \frac{\partial J(\boldsymbol{W})}{\partial \boldsymbol{W}}$$

Loss Functions Can Be Difficult to Optimize

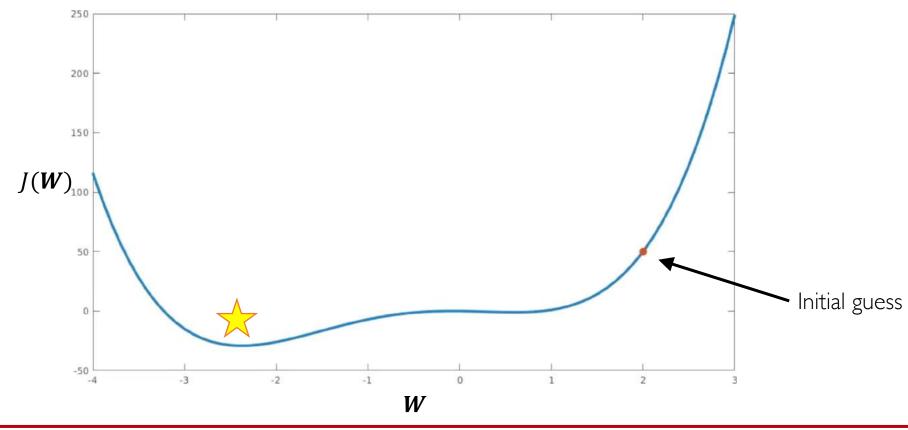
Remember:

Optimization through gradient descent

$$W \leftarrow W - \frac{\partial J(W)}{\partial W}$$
How can we set the learning rate?

Setting the Learning Rate

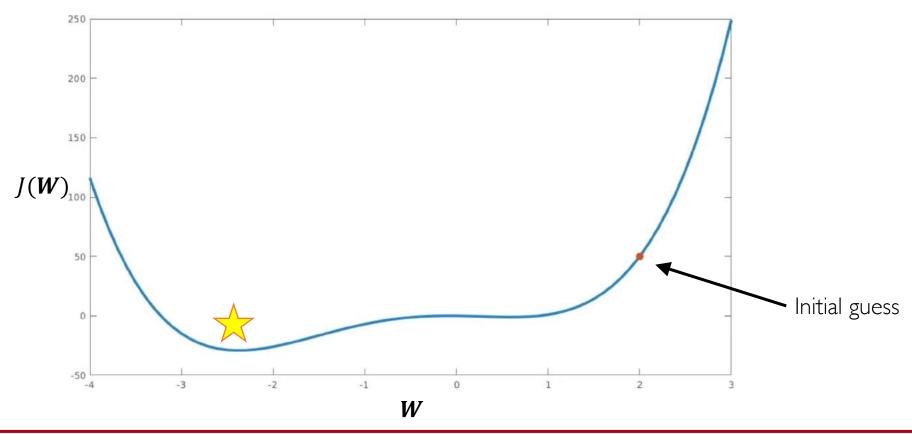
Small learning rate converges slowly and gets stuck in false local minima





Setting the Learning Rate

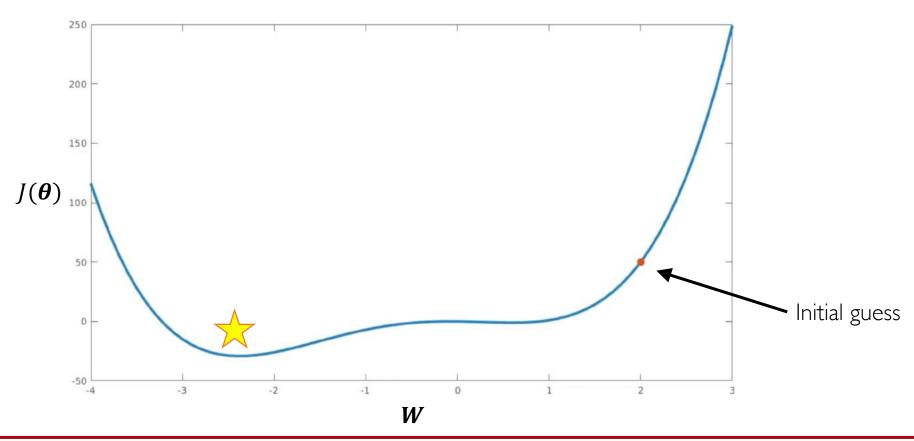
Large learning rates overshoot, become unstable and diverge





Setting the Learning Rate

Stable learning rates converge smoothly and avoid local minima



How to deal with this?

Idea I:

Try lots of different learning rates and see what works "just right"

How to deal with this?

Idea I:

Try lots of different learning rates and see what works "just right"

Idea 2:

Do something smarter!

Design an adaptive learning rate that "adapts" to the landscape



Adaptive Learning Rates

- Learning rates are no longer fixed
- Can be made larger or smaller depending on:
 - how large gradient is
 - how fast learning is happening
 - size of particular weights
 - etc...

Adaptive Learning Rate Algorithms

- Momentum
- Adagrad
- Adadelta
- Adam
- RMSProp









tf.train.RMSPropOptimizer

Qian et al. "On the momentum term in gradient descent learning algorithms." 1999.

Duchi et al. "Adaptive Subgradient Methods for Online Learning and Stochastic Optimization." 2011.

Zeiler et al. "ADADELTA: An Adaptive Learning Rate Method." 2012.

Kingma et al. "Adam: A Method for Stochastic Optimization." 2014.

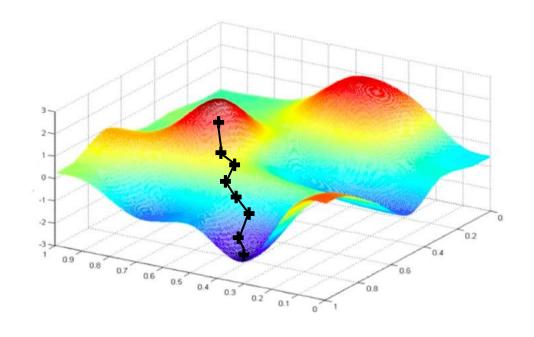
Additional details: http://ruder.io/optimizing-gradient-descent/



Neural Networks in Practice: Mini-batches

Algorithm

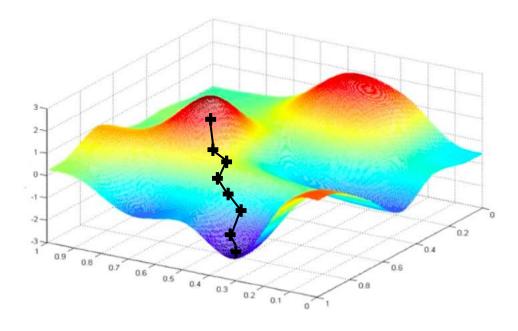
- I. Initialize weights randomly $\sim \mathcal{N}(0, \sigma^2)$
- 2. Loop until convergence:
- 3. Compute gradient, $\frac{\partial J(W)}{\partial W}$
- 4. Update weights, $\mathbf{W} \leftarrow \mathbf{W} \eta \frac{\partial J(\mathbf{W})}{\partial \mathbf{W}}$
- 5. Return weights



Gradient Descent

Algorithm

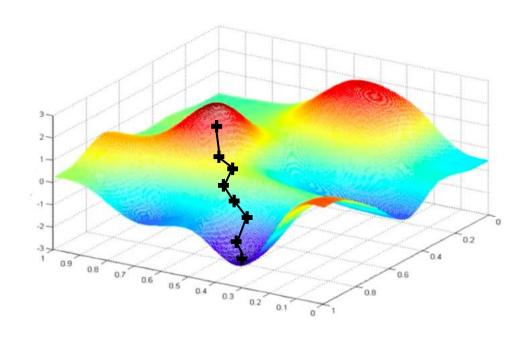
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Can be very computational to compute!

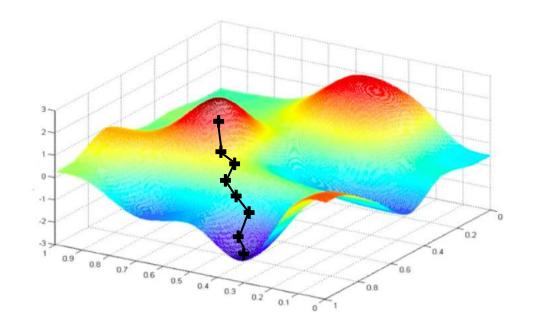
Algorithm

- 1. Initialize weights randomly $\sim \mathcal{N}(0, \sigma^2)$
- 2. Loop until convergence:
- 3. Pick single data point i
- 4. Compute gradient, $\frac{\partial J_i(W)}{\partial W}$
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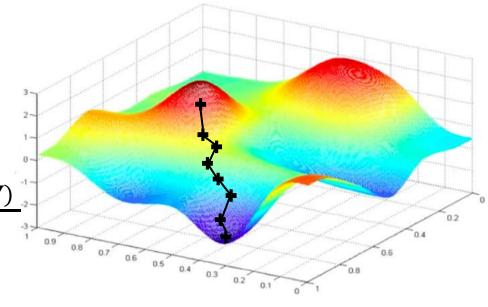
Easy to compute but very noisy (stochastic)!

Algorithm

- I. Initialize weights randomly $\sim \mathcal{N}(0, \sigma^2)$
- 2. Loop until convergence:
- 3. Pick batch of B data points

4. Compute gradient,
$$\frac{\partial J(W)}{\partial W} = \frac{1}{B} \sum_{k=1}^{B} \frac{\partial J_k(W)}{\partial W}$$

- 5. Update weights, $\mathbf{W} \leftarrow \mathbf{W} \eta \frac{\partial J(\mathbf{W})}{\partial \mathbf{W}}$
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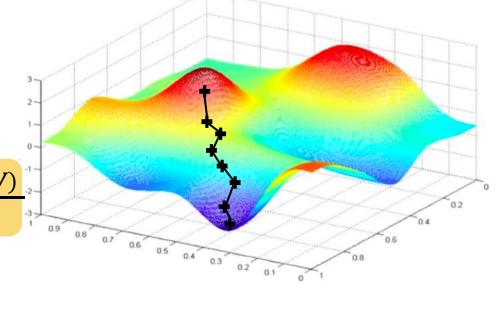
当每次是对整个训练集进行梯度下降的时候,就是 batch 梯度下降,当每次只对一个样本进行梯度下降的时候,是 stochastic 梯度下降,当每次处理样本的个数在上面二者之间,就是 mini batch 梯度下降。

Algorithm

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Fast to compute and a much better estimate of the true gradient!

Mini-batches while training

More accurate estimation of gradient

Smoother convergence Allows for larger learning rates

Mini-batches while training

More accurate estimation of gradient

Smoother convergence
Allows for larger learning rates

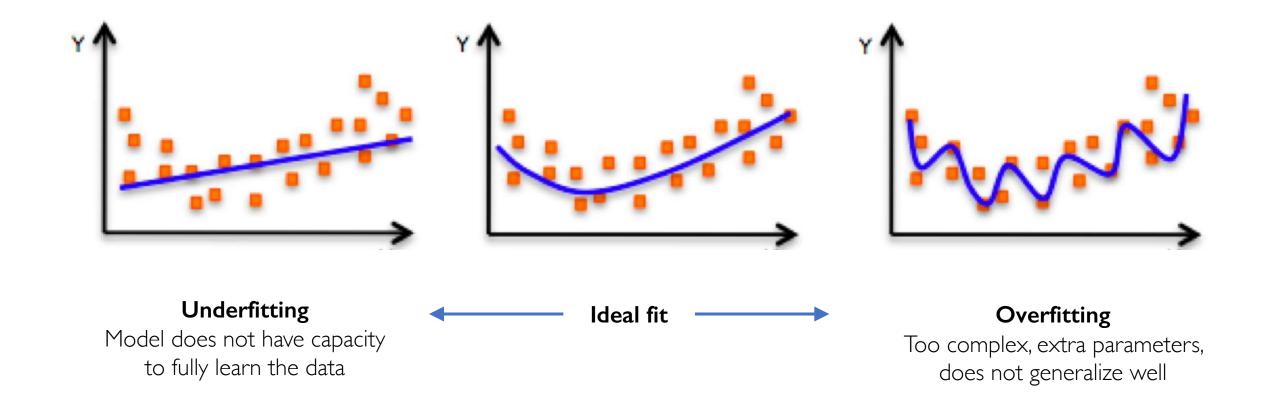
Mini-batches lead to fast training!

Can parallelize computation + achieve significant speed increases on GPU's



Neural Networks in Practice: Overfitting

The Problem of Overfitting



Regularization

What is it?

Technique that constrains our optimization problem to discourage complex models

Regularization

正则化,用于防止模型出现过拟合的现象。

方法有: Dropout和Early Stopping

What is it?

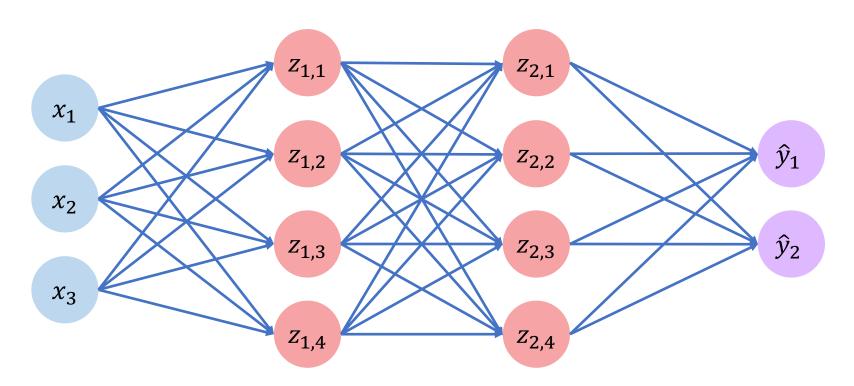
Technique that constrains our optimization problem to discourage complex models

Why do we need it?

Improve generalization of our model on unseen data

Regularization 1: Dropout

During training, randomly set some activations to 0

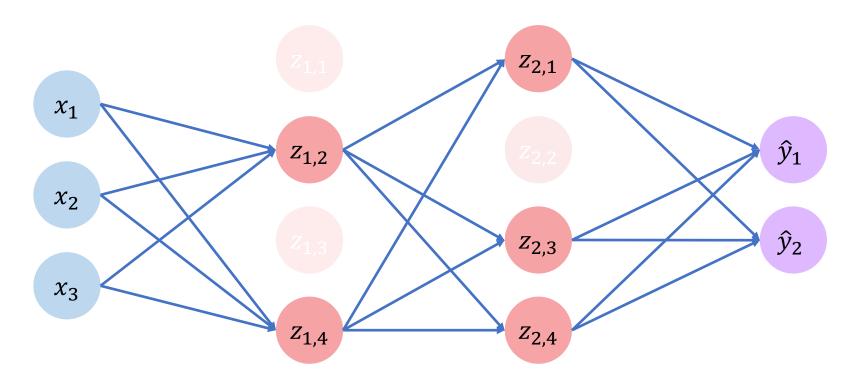




Regularization 1: Dropout

- During training, randomly set some activations to 0
 - Typically 'drop' 50% of activations in layer
 - Forces network to not rely on any I node



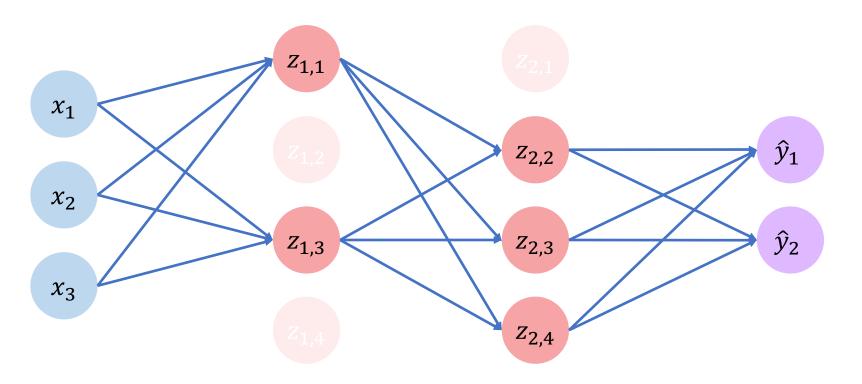




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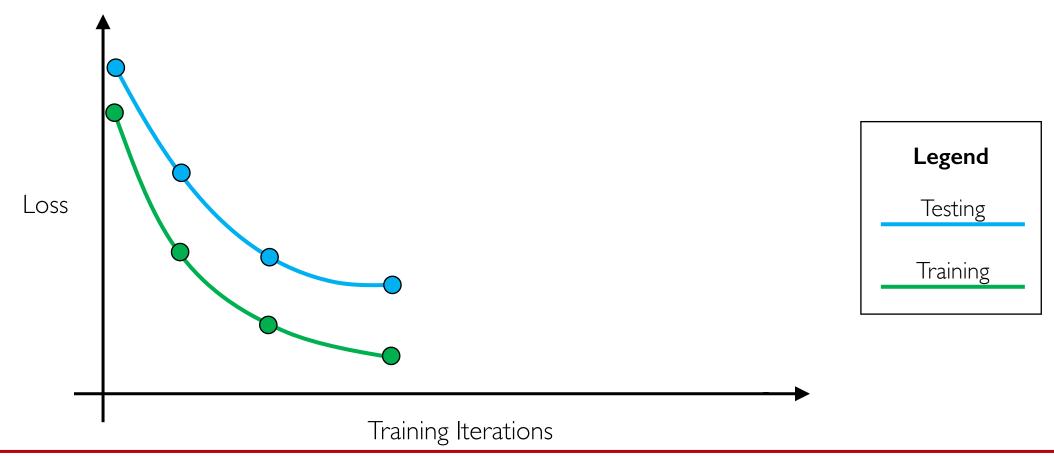


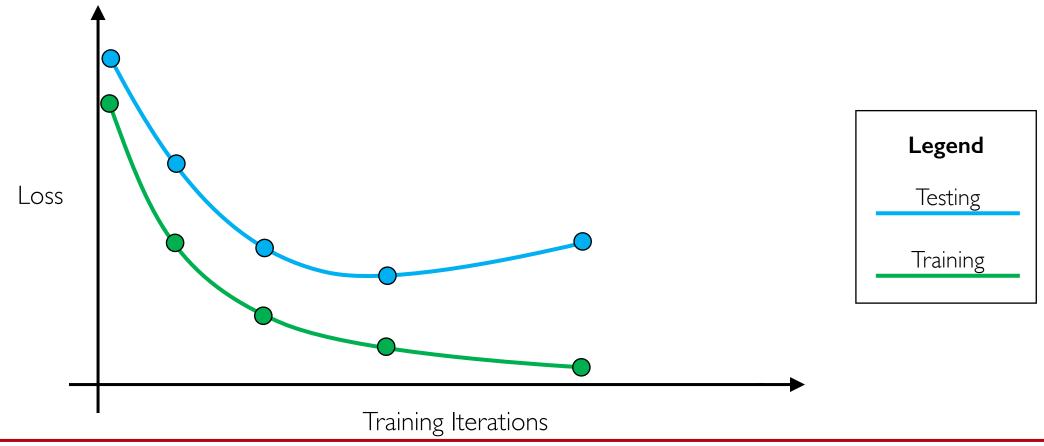




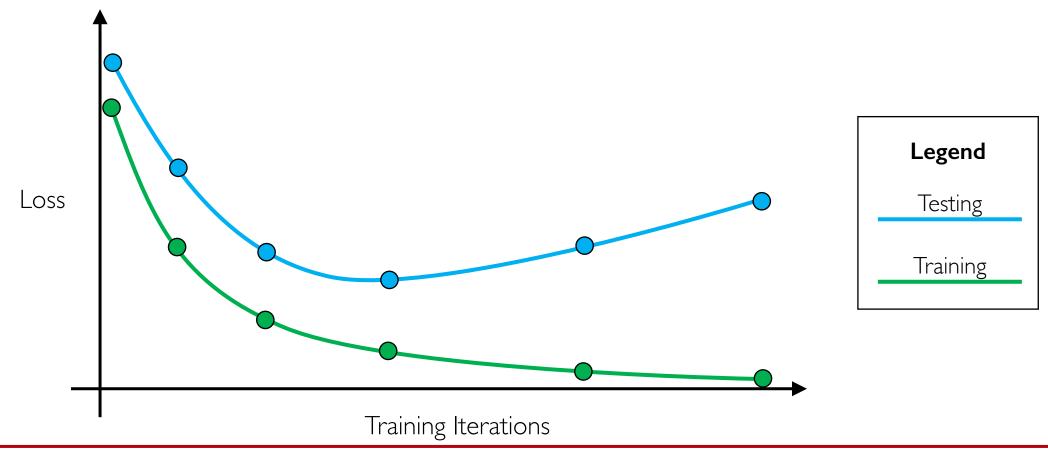


















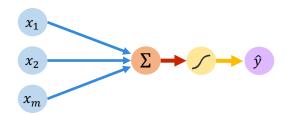




Core Foundation Review

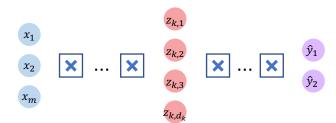
The Perceptron

- Structural building blocks
- Nonlinear activation functions



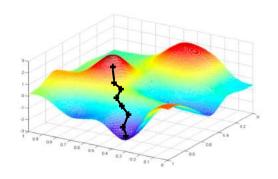
Neural Networks

- Stacking Perceptrons to form neural networks
- Optimization through backpropagation



Training in Practice

- Adaptive learning
- Batching
- Regularization



Questions?