

tags: 影像處理

# Image Processing Homework 3

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## 1 Technical description

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### HSI

RGBHSI

基本上就按照講義的提供的公式寫出來

$$H = \begin{cases} \theta, & \text{if } B \leq G, \\ 360 - \theta, & \text{if } B > G, \end{cases}$$

$$\theta = \cos^{-1} \left\{ \frac{\frac{1}{2}[(R-G)+(R-B)]}{[(R-G)^2+(R-B)(G-B)]^{1/2}} \right\},$$

$$S = 1 - \frac{3}{(R+G+B)} [\min(R, G, B)],$$

$$I = \frac{1}{3}(R+G+B),$$

分母部分為了防止/0的發生所以有加一個不影響圖片的offset

$H = \text{acosd}(a./(b+0.0000001));$

挑整I，之後轉換回去

HSI2RGB部分則是參考此公式

■ *RG sector* ( $0^\circ \leq H < 120^\circ$ ):

$$B = I(1 - S), \quad (6.2-8)$$

$$R = I \left[ 1 + \frac{S \cos H}{\cos(60^\circ - H)} \right], \quad (6.2-9)$$

$$G = 3I - (R + B). \quad (6.2-10)$$

■ *GB sector* ( $120^\circ \leq H < 240^\circ$ ):

$$H = H - 120^\circ. \quad (6.2-11)$$

Then the RGB components are:

$$R = I(1 - S), \quad (6.2-12)$$

$$G = I \left[ 1 + \frac{S \cos H}{\cos(60^\circ - H)} \right], \quad (6.2-13)$$

$$B = 3I - (R + G). \quad (6.2-14)$$

■ *BR sector* ( $240^\circ \leq H \leq 360^\circ$ ):

$$H = H - 240^\circ. \quad (6.2-15)$$

Then the RGB components are:

$$G = I(1 - S), \quad (6.2-16)$$

$$B = I \left[ 1 + \frac{S \cos H}{\cos(60^\circ - H)} \right], \quad (6.2-17)$$

$$R = 3I - (G + B). \quad (6.2-18)$$

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## Lab

RGB沒辦法直接轉成Lab，因此使用(sRGB,D65) to XYZ的轉換公式轉成，之後照講義公式進行轉換。

0.4124564 0.3575761 0.1804375

0.2126729 0.7151522 0.0721750

0.0193339 0.1191920 0.9503041

% rgb2xyz(sRGB,D65)

X = 0.4124564 \* ImageR + 0.3575761 \* ImageG + 0.1804375 \* ImageB;

Y = 0.2126729 \* ImageR + 0.7151522 \* ImageG + 0.0721750 \* ImageB;

Z = 0.0193339 \* ImageR + 0.1191920 \* ImageG + 0.9503041 \* ImageB;

- The  $L^*a^*b^*$  color components are:

$$L^* = 116 \bullet h\left(\frac{Y}{Y_w}\right) - 16, \quad (6.5-9)$$

$$a^* = 500 \left[ h\left(\frac{X}{X_w}\right) - h\left(\frac{Y}{Y_w}\right) \right], \quad (6.5-10)$$

$$b^* = 200 \left[ h\left(\frac{Y}{Y_w}\right) - h\left(\frac{Z}{Z_w}\right) \right], \quad (6.5-11)$$

where

$$h(q) = \begin{cases} \sqrt[3]{q}, & q > 0.008856, \\ 7.787q + 16/116, & q \leq 0.008856, \end{cases} \quad (6.5-12)$$

```
% Xyz2Lab
```

```
for i = 1:m
```

```
    for j = 1:n
```

```
        % preProcess
```

```
        X(i,j) = X(i,j)/Xn;
```

```
        Y(i,j) = Y(i,j)/Yn;
```

```
        Z(i,j) = Z(i,j)/Zn;
```

```
        L(i,j) = 116.0 * HFunction(Y(i,j)) - 16;
```

```
        A(i,j) = 500.0 * ( HFunction( X(i,j) ) - HFunction( Y(i,j) ) );
```

```
        B(i,j) = 200.0 * ( HFunction( Y(i,j) ) - HFunction( Z(i,j) ) );
```

```
    end
```

```
end
```

```
function [result] = HFunction(x)
```

```
    Qn = 0.008856;
```

```
    if(x > Qn)
```

```
        result = x ^ (1.0/3.0);
```

```
    else
```

```
        result = 7.787 * x + (16.0/116.0);
```

```
    end
```

```
end
```

調整L之後，轉成 XYZ 再轉回rgb

參考這下列公式

LAB to XYZ

### From CIELAB to CIEXYZ [\[edit\]](#)

The reverse transformation is most easily expressed using the inverse of the function  $f$  above:

$$X = X_n f^{-1} \left( \frac{L^* + 16}{116} + \frac{a^*}{500} \right)$$

$$Y = Y_n f^{-1} \left( \frac{L^* + 16}{116} \right)$$

$$Z = Z_n f^{-1} \left( \frac{L^* + 16}{116} - \frac{b^*}{200} \right)$$

where

$$f^{-1}(t) = \begin{cases} t^3 & \text{if } t > \delta \\ 3\delta^2 \left( t - \frac{4}{29} \right) & \text{otherwise} \end{cases}$$

and where  $\delta = \frac{6}{29}$ .

% LAB to XYZ

```
for i = 1:m
    for j = 1:n
        % prepare fx,fy,fz
        fy = (ImageL(i,j) + 16.0)/116.0;
        fz = fy - ImageB(i,j)/200.0;
        fx = ImageA(i,j)/500 + fy;
        % Y transformation
        if(fy ^3.0 > En)
            Y(i,j) = (fy^3);
        else
            Y(i,j) = (fy - (16.0/116.0))/7.787;
        end
    end
end
```

XYZ to rgb(sRGB,D65)

3.2404542 -1.5371385 -0.4985314

-0.9692660 1.8760108 0.0415560

0.0556434 -0.2040259 1.0572252

% xyz2rgb(sRGB,D65)

R = 3.2404542 \* X - 1.5371385 \* Y - 0.4985314 \* Z;

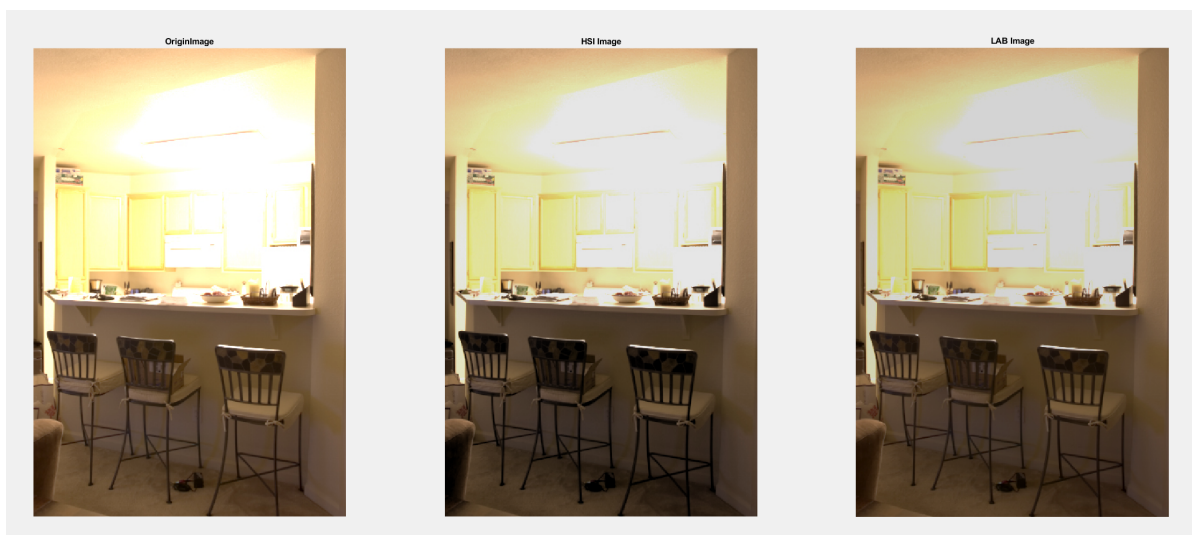
G = -0.9692660 \* X + 1.8760108 \* Y + 0.0415560 \* Z;

B = 0.0556434 \* X - 0.2040259 \* Y + 1.0572252 \* Z;

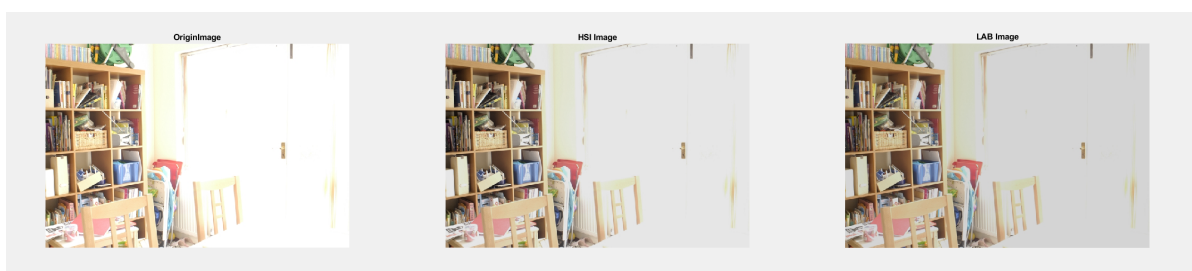
## 2 Experimental results

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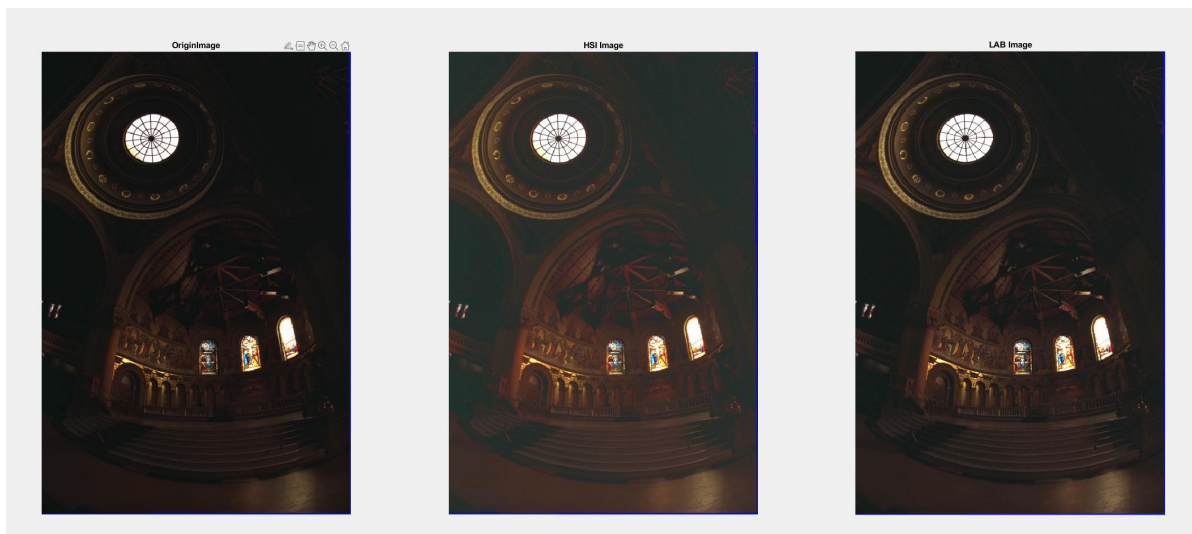
kitchen.jpg



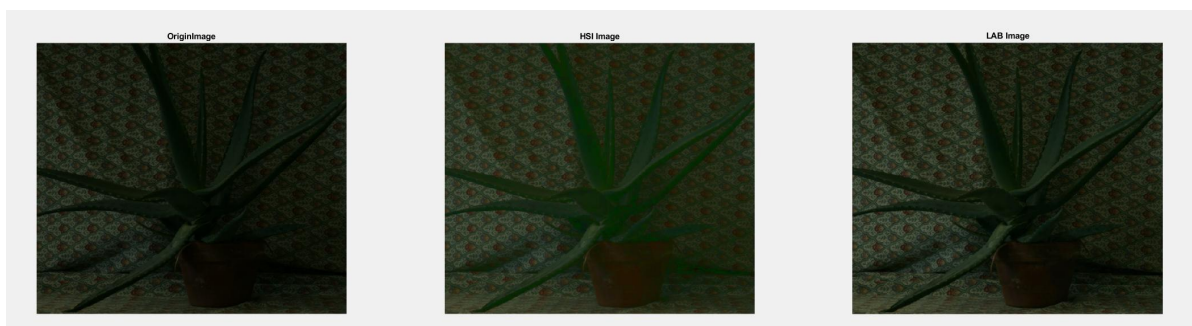
house.jpg



church.jpg



aloe.jpg



## 3 Discussions

在kitchen這張圖來說LAB的部分比較好一些，像是色彩部分就沒甚麼跑掉，修正後後方的櫃子也看得到了。

house部分，因為白色面積太大了修正的效果不是很好。

church和aloe對亮度作正修正，效果都不錯，細節也有展現出來，但是經實驗如果再修正多一點的話，可以更多細節，不過有噪點增加跟明亮處會有過曝的感覺。LAB的效果比HSI更好，色彩的感覺都沒有跑掉，而HSI部分則有點跑掉。

## 4 References and Appendix

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powerpoint on ecourse2

<https://en.wikipedia.org/wiki/SRGB>

[https://en.wikipedia.org/wiki/CIELAB\\_color\\_space](https://en.wikipedia.org/wiki/CIELAB_color_space)

[http://www.brucelindbloom.com/index.html?Eqn\\_Lab\\_to\\_XYZ.html](http://www.brucelindbloom.com/index.html?Eqn_Lab_to_XYZ.html)

[https://www.mathworks.com/matlabcentral/mlc-downloads/downloads/submissions/55098/versions/2/previews/Plant%20Disease\\_MutiSVM/Leaf\\_Disease\\_Detection\\_code/rgb2hsi.m/index.html](https://www.mathworks.com/matlabcentral/mlc-downloads/downloads/submissions/55098/versions/2/previews/Plant%20Disease_MutiSVM/Leaf_Disease_Detection_code/rgb2hsi.m/index.html)