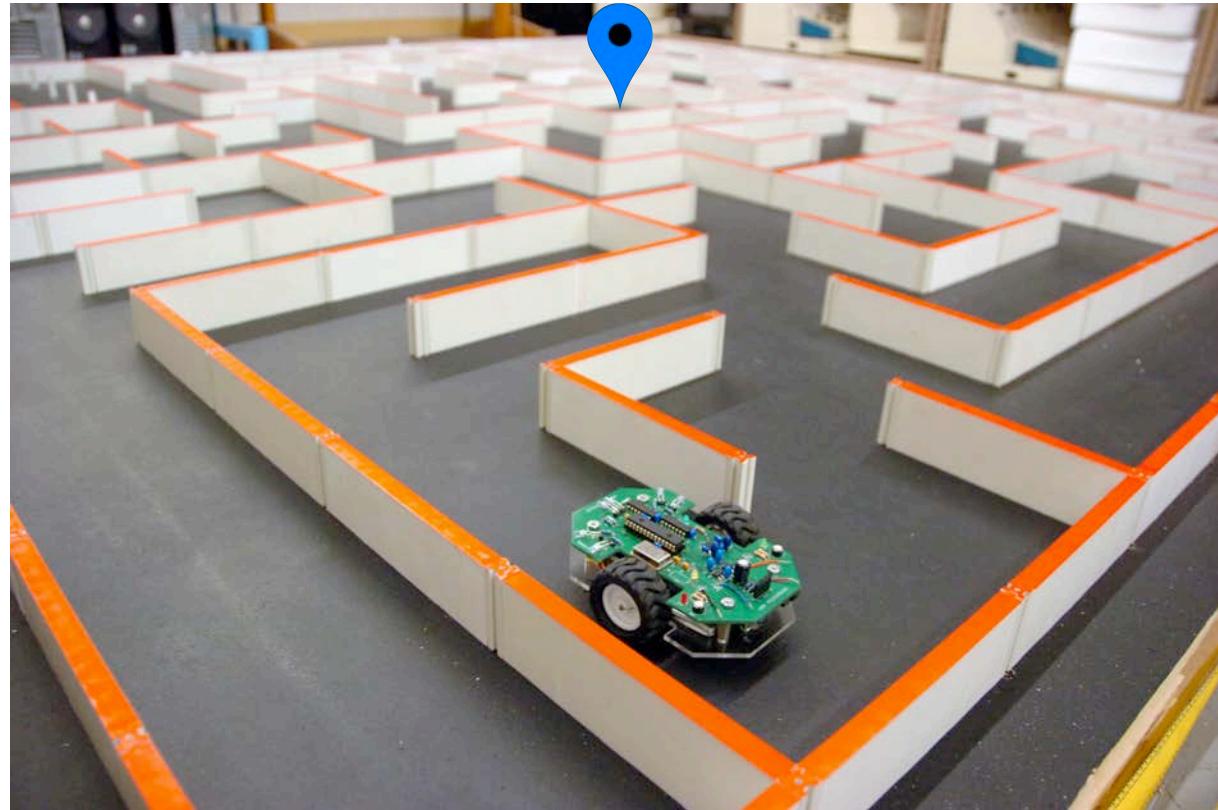


Autonomous Navigation: Global Search



Robotics 102
Introduction to AI and Programming
University of Michigan and Berea College
Fall 2021

<https://app.emaze.com/@AIRRTROT/idea-2-the-robot-maze#1>

Michigan Robotics 102 - robotics102.org



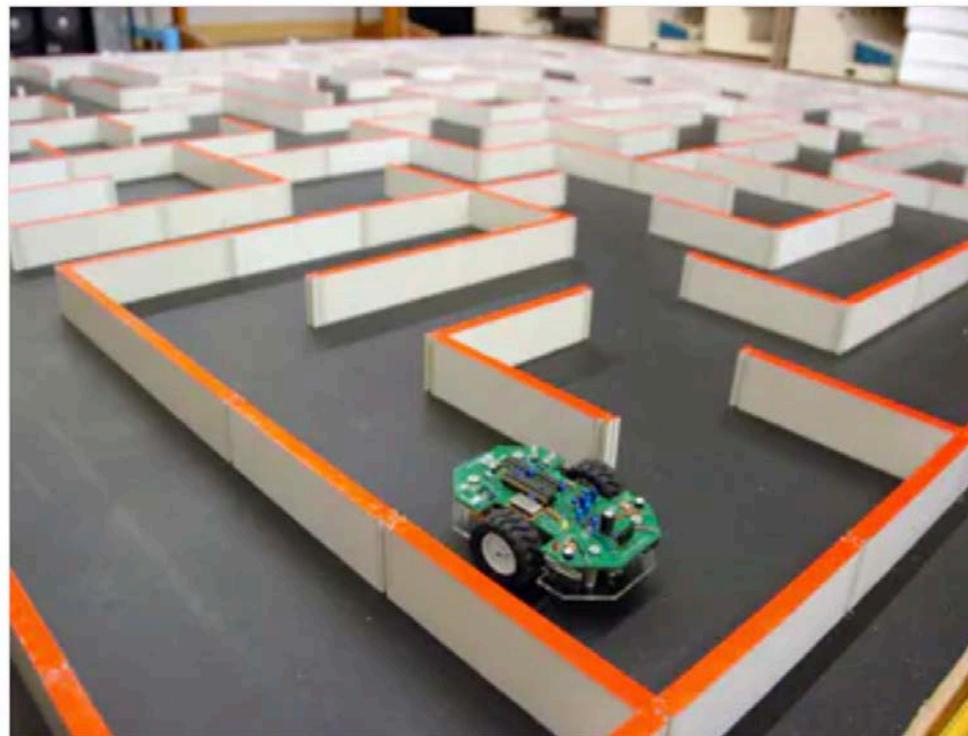
Jordan Wong

Published June 19, 2015

IEEE Micromouse

Autonomous mouse that can traverse any 16 by 16 maze.

⌚ Intermediate 📄 Full instructions provided ⚡ 1,762

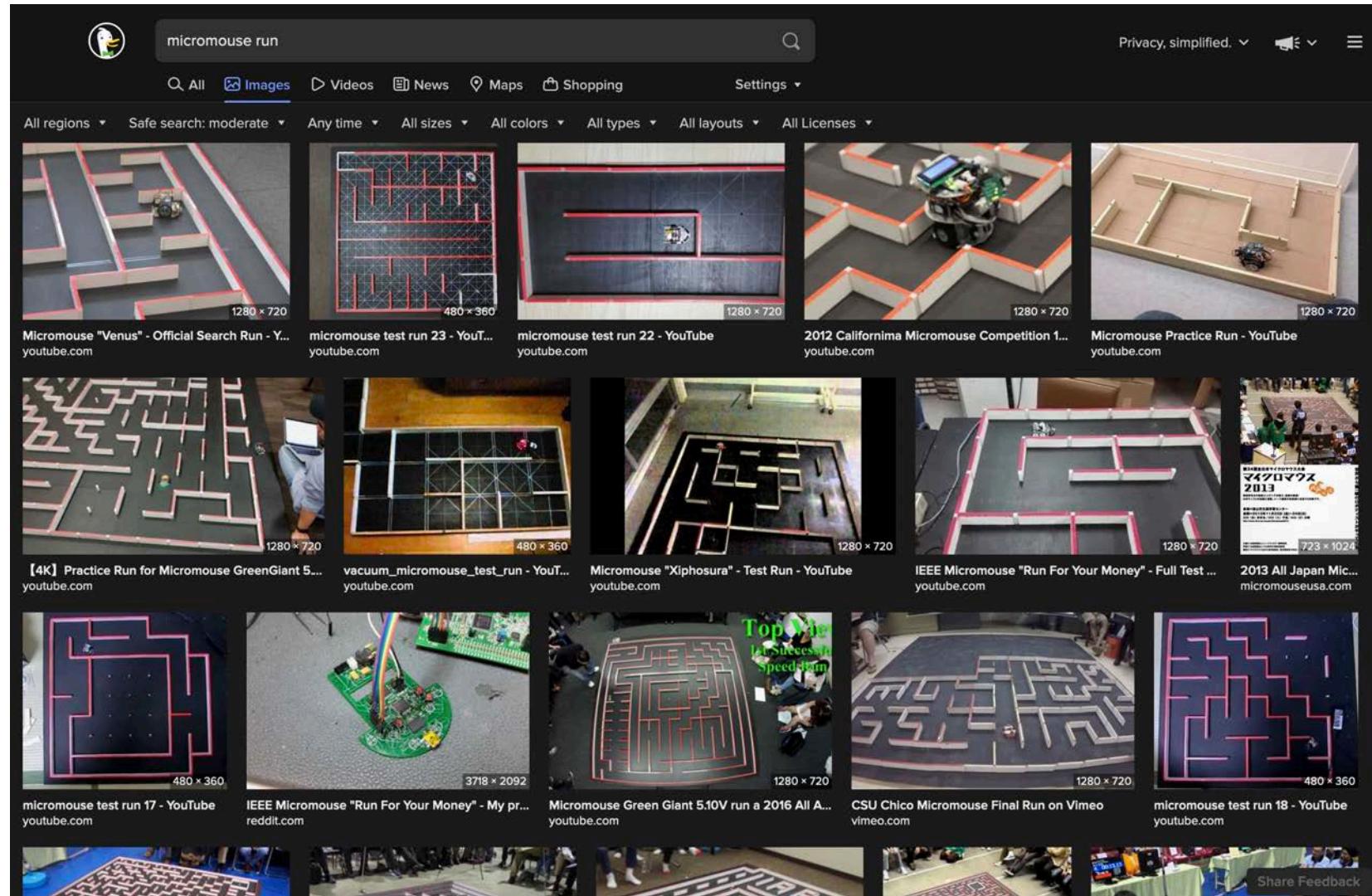


<https://www.hackster.io/jordanjameswong/micromouse-83dab7>

Michigan Robotics 102 - robotics102.org



2011 All Japan micromouse contest: Ng BengKiat 4th Fast RUN
<https://www.youtube.com/watch?v=CLwICJKV4dw>



Our goal

Our goal

Give you the power of autonomous navigation



Our goal

Give you the power of autonomous navigation



Our goal

Give you the power of autonomous navigation



Autonomous Navigation



Autonomous Navigation by global search



*Think of our robot's navigation
as solving a maze*



Autonomous Navigation by global search

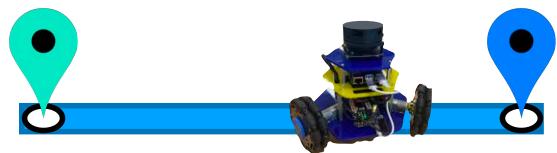
*Think of our robot's navigation
as solving a maze*



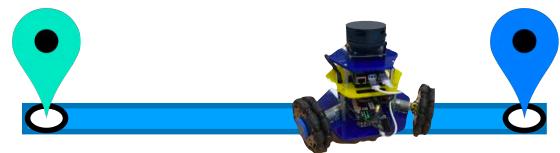
Autonomous Navigation by global search

*Think of our robot's navigation
as solving a maze*



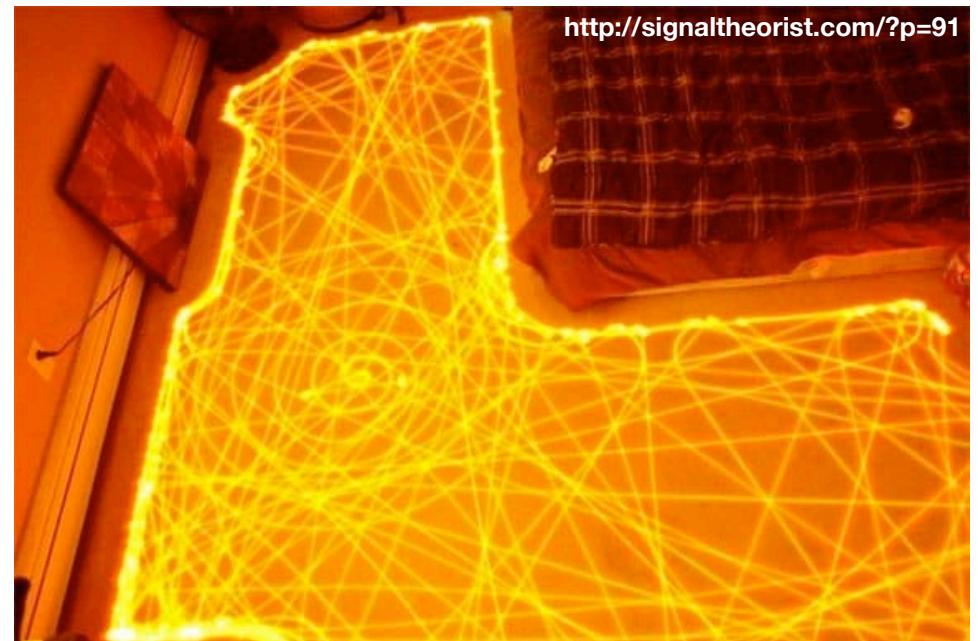
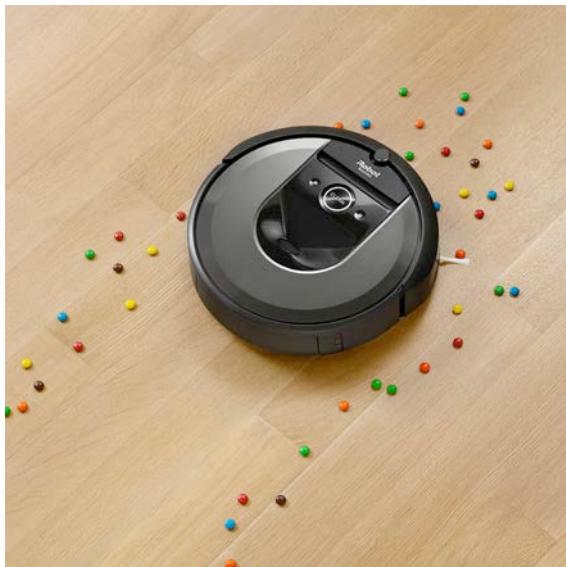


**What options do we have
for navigating our robot?**



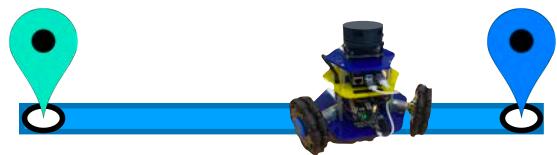
What options do we have for navigating our robot?

Just move randomly



Random walk algorithms

Michigan Robotics 102 - robotics102.org



What options do we have for navigating our robot?

Just move randomly

Follow wall to goal



Bug algorithms

Michigan Robotics 102 - robotics102.org



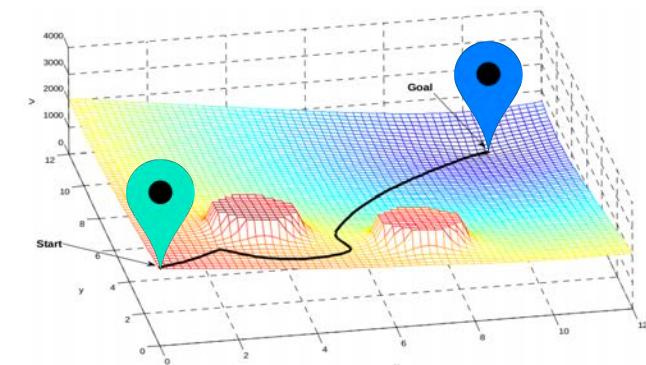
Just move randomly

Follow wall to goal

Build a map to guide us

Project 2: Potential Fields

Autonomous
navigation to a
goal location



Build a map to guide us

What path would a potential field produce?



Build a map to guide us

What path would a potential field produce?

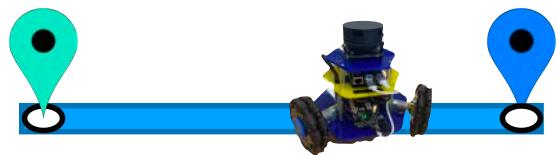


What path would a potential field produce?

**Local minimum
(or dead end)**

Start location



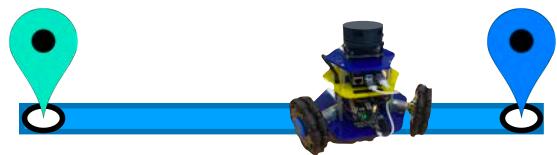


**What options do we have
for navigating our robot?**

Just move randomly

Follow wall to goal

Build a map to guide us



Just move randomly

Follow wall to goal

Build a map to guide us

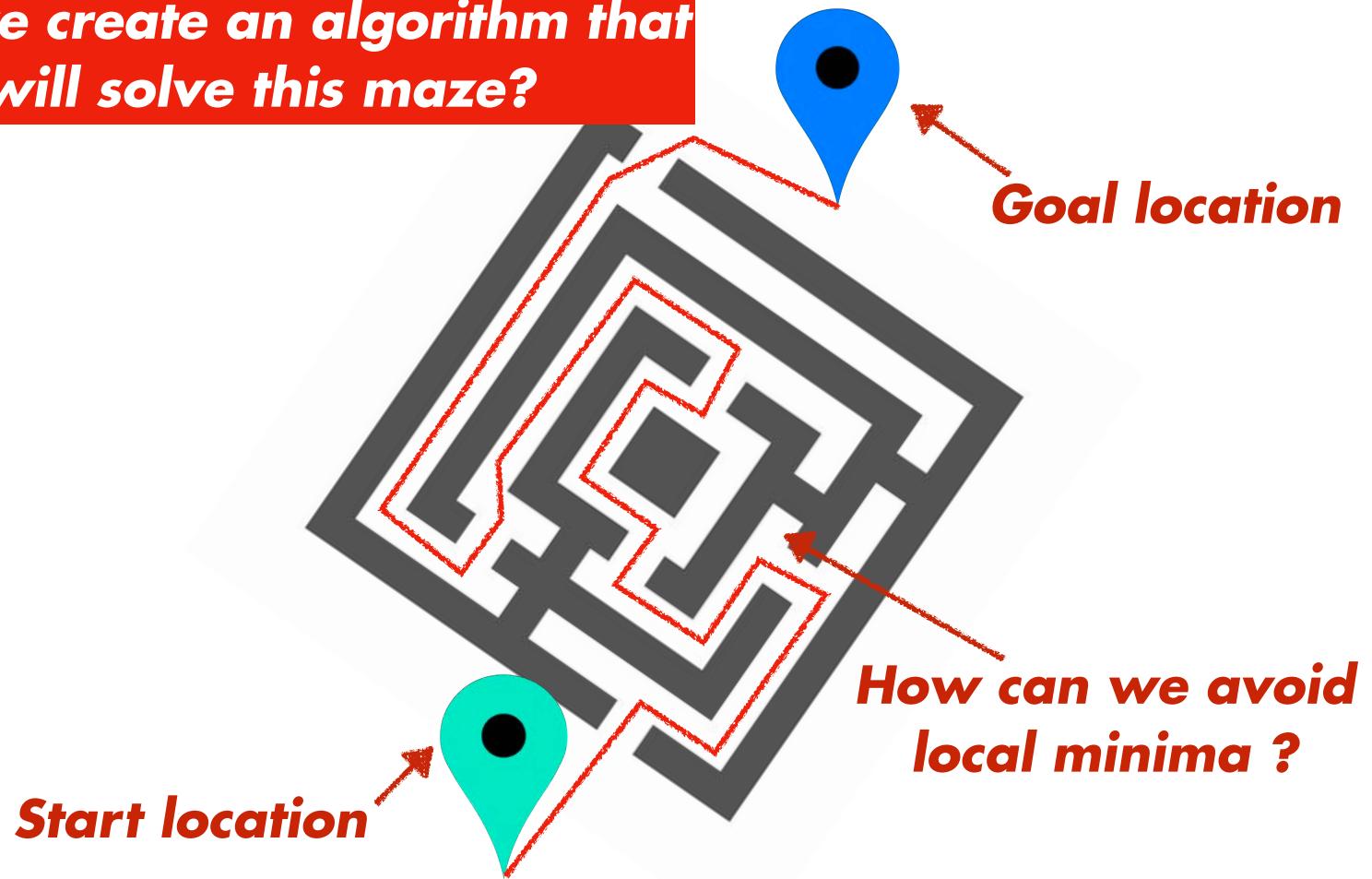
Consider all possible paths

Project 3: A* Pathfinding

Autonomous
navigation to a
goal location

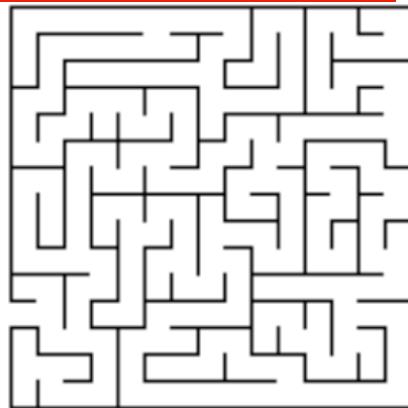


***Can we create an algorithm that
will solve this maze?***



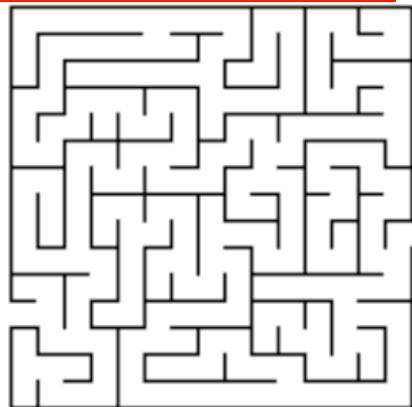
***Can we create an algorithm that
will solve this maze?***

and this one?



***Can we create an algorithm that
will solve this maze?***

and this one?



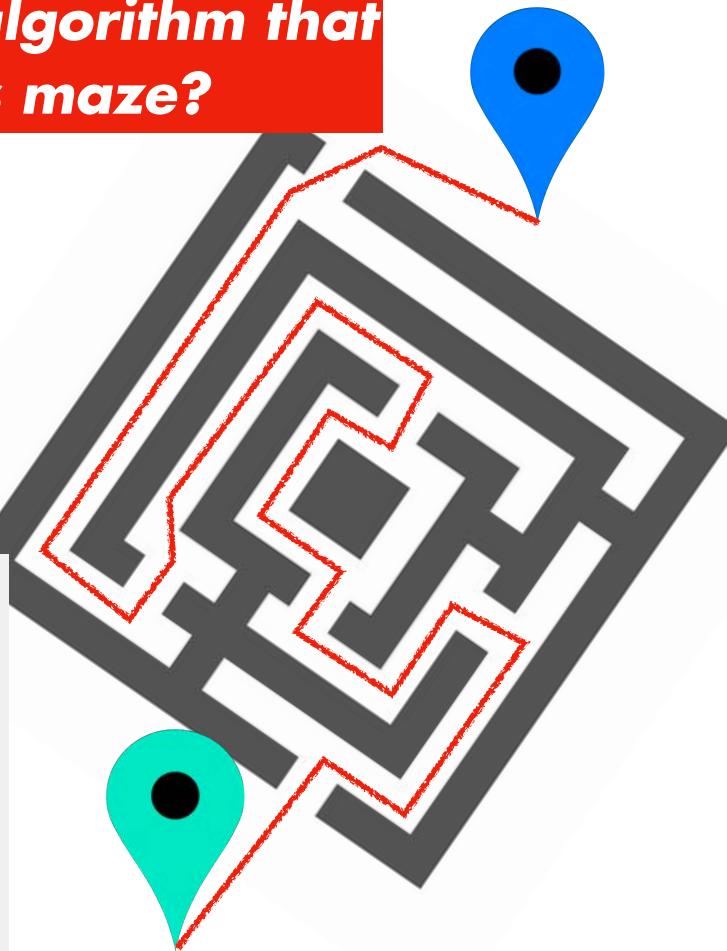
and this one?

xefer

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Maze Generator

Rows: 50 Maze Id: odijjhfmoljdjodgdg
Columns: 80 Anfractuosity: Low High
Cell Size: 8



xefer

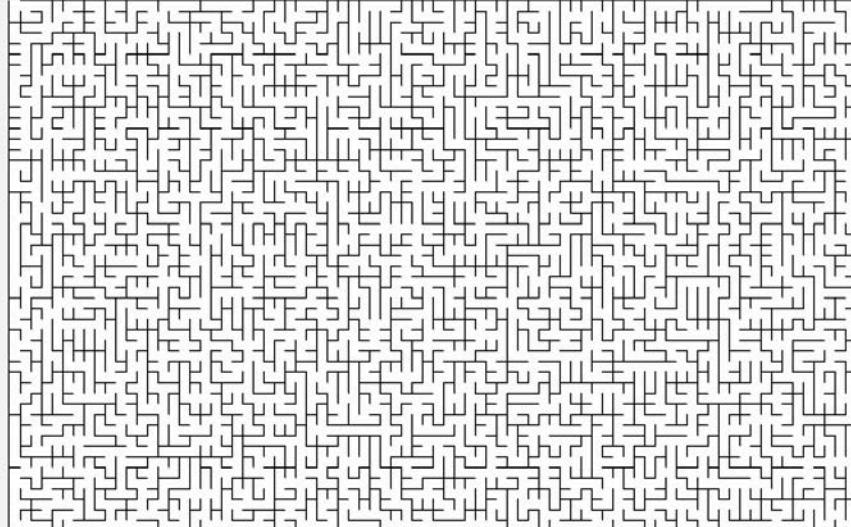
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Maze Generator

Rows: Maze Id: **odijjhfmoljdjodgodg**

Columns:

Cell Size: Anfractuosity: Low High



<https://www.xefer.com/maze-generator>

Michigan Robotics 102 - robotics102.org

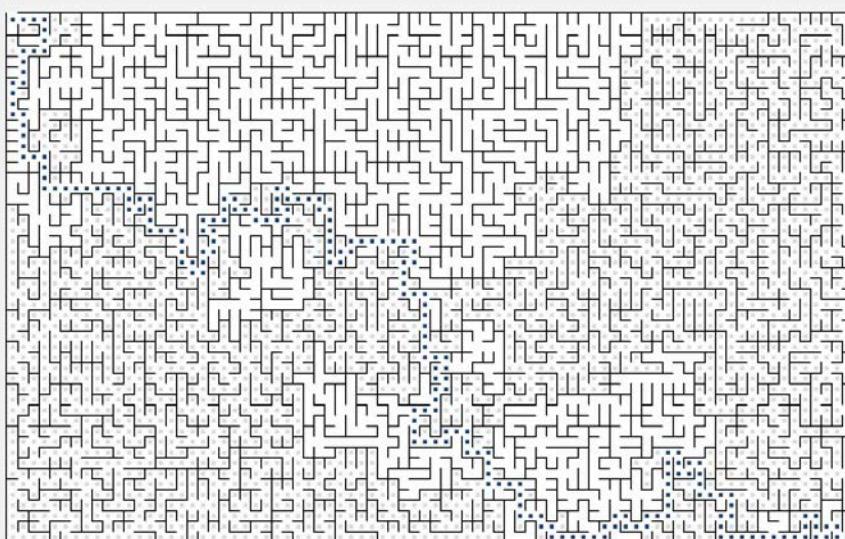
***How does this
algorithm work?***

xefer

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Maze Generator

Rows: 50 Maze Id: **odijjhfmoljdjodgodg**
Columns: 80
Cell Size: 8 Anfractuosity: Low High



<https://www.xefer.com/maze-generator>

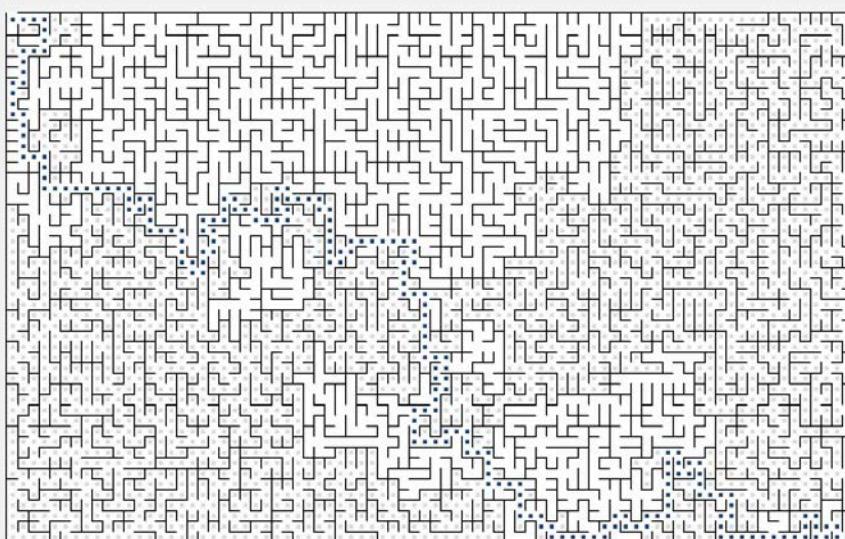
**How does this
algorithm work?**

xefer

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Maze Generator

Rows: 50 Maze Id: **odijjhfmoljodgodg**
Columns: 80
Cell Size: 8 Anfractuosity: Low High
Generate **Solve**



<https://www.xefer.com/maze-generator>

**Represent the
map as a graph**

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Maze Generator

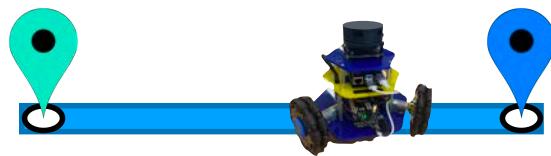
Rows: 50 Maze Id: **odijjhfmoljdjodgodg**
Columns: 80
Cell Size: 8 Anfractuosity: Low High

<https://www.xefer.com/maze-generator>

How does this algorithm work?

Represent the map as a graph

Search over all possible paths



Just move randomly

Follow wall to goal

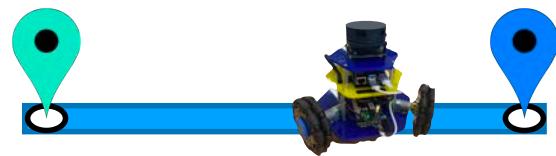
Build a map to guide us

Consider ***Search over all
possible paths***

Project 3: A* Pathfinding

Autonomous
navigation to a
goal location





Just move randomly

Follow wall to goal

Build a map to guide us

Search over all possible paths

Project 3: A^* Pathfinding

Autonomous
navigation to a
goal location



Project 3: A* Pathfinding

Autonomous
navigation to a
goal location



Search over all possible paths

Already done from Project 2

- Build map of environment
- Represent map as graph with a grid layout
- Store parent of each node
 - along route to start location
- Store path distance at each node
 - along route to start location
- Global search to find routing

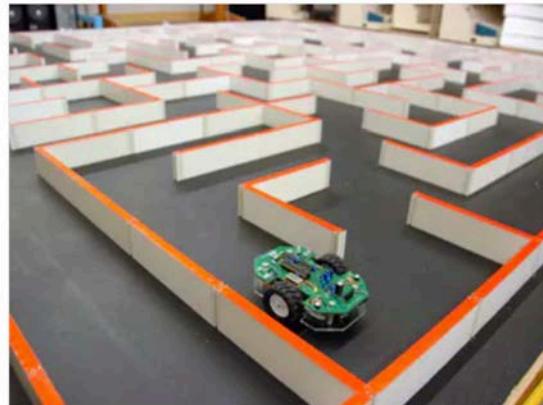
Micromouse represents maze as a grid graph then performs “Floodfill” to find path to goal

Jordan Wong
Published June 19, 2015

IEEE Micromouse

Autonomous mouse that can traverse any 16 by 16 maze.

Intermediate Full instructions provided 1,762

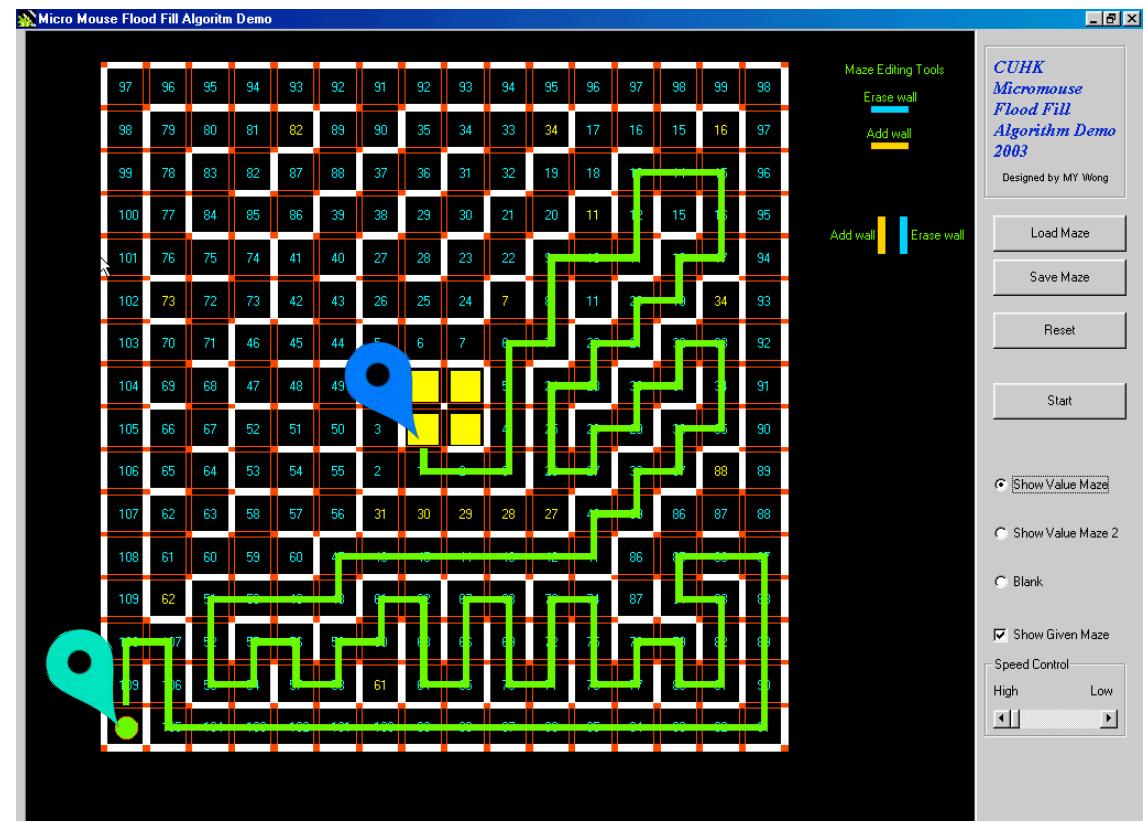


<https://medium.com/@austinxiao/ieee-micromouse-2016-software-design-496653ff104d>

Michigan Robotics 102 - robotics102.org

Micromouse represents maze as a grid graph then performs “Floodfill” to find path to goal

Result from pathfinding:



<https://medium.com/@austinxiao/ieee-micromouse-2016-software-design-496653ff104d>

Michigan Robotics 102 - robotics102.org

Micromouse represents maze as a grid graph then performs “Floodfill” to find path to goal

Result from pathfinding:

**Provides cell-to-cell
routing along found path**



<https://medium.com/@austinxiao/ieee-micromouse-2016-software-design-496653ff104d>

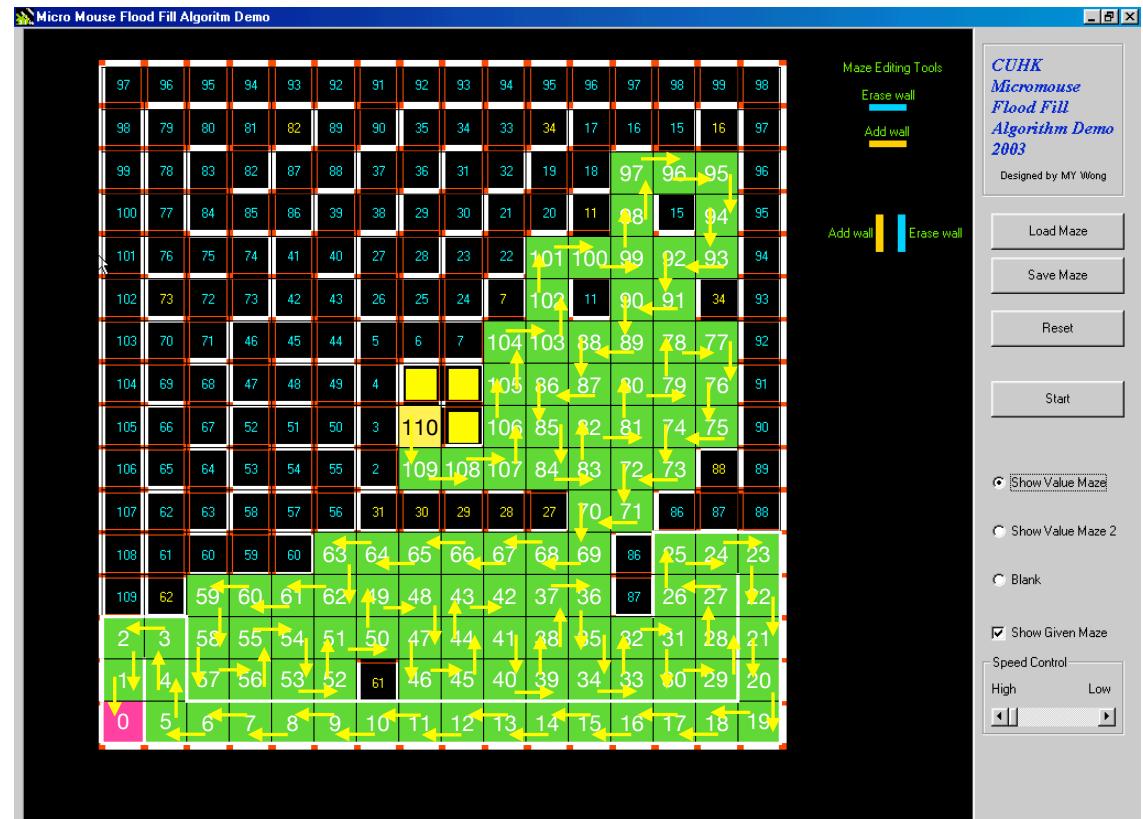
Michigan Robotics 102 - robotics102.org

Micromouse represents maze as a grid graph then performs “Floodfill” to find path to goal

Result from pathfinding:

Provides cell-to-cell routing along found path

Distance along path at each cell



<https://medium.com/@austinxiao/ieee-micromouse-2016-software-design-496653ff104d>

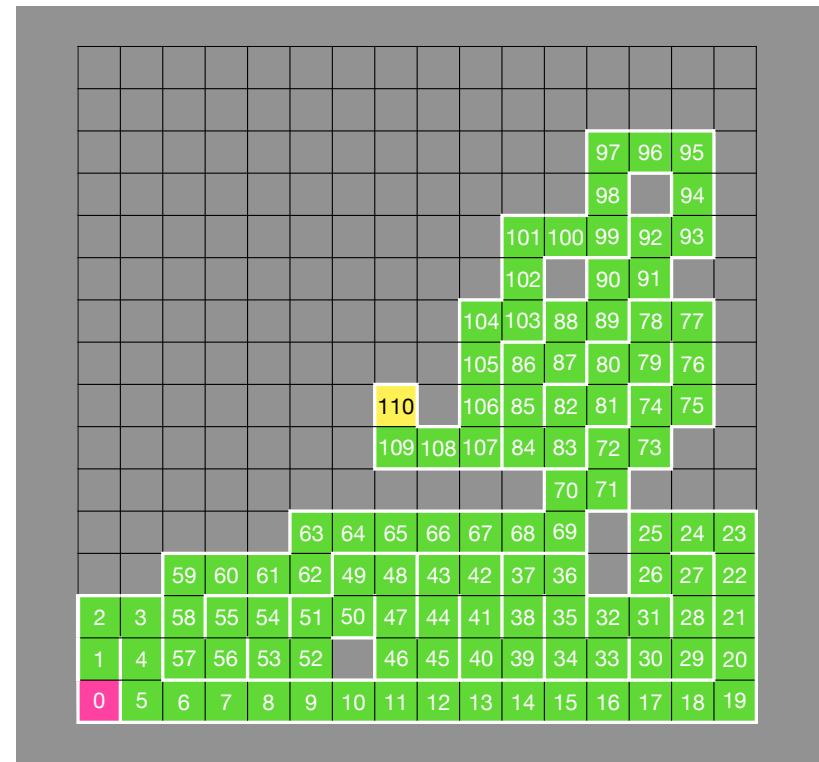
Michigan Robotics 102 - robotics102.org

Micromouse represents maze as a grid graph then performs “Floodfill” to find path to goal

Result from pathfinding:

***Provides cell-to-cell
routing along found path***

***Distance along path
at each cell***

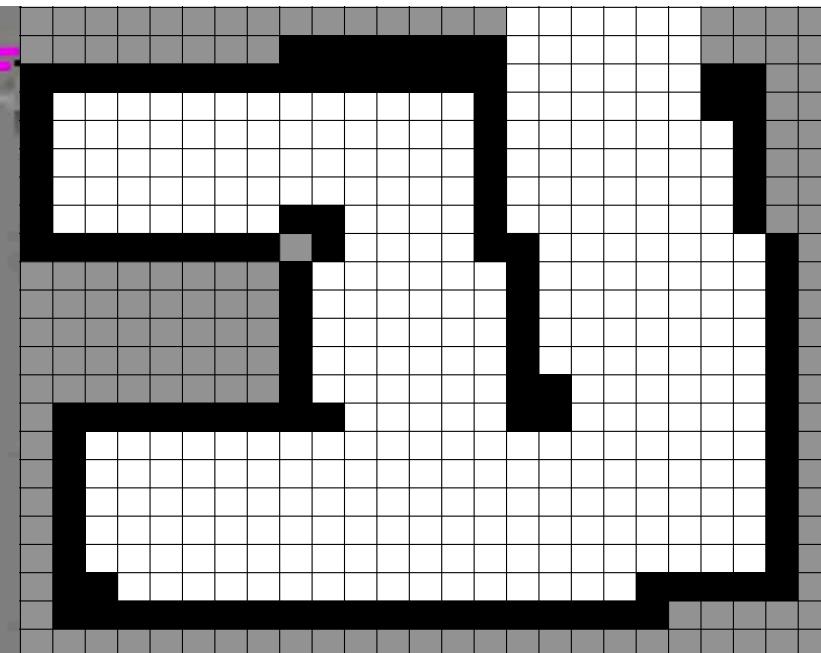


**Remember what this graph looks
like for our robot maps**

***Robot map is stored as an image
and represented as a graph***



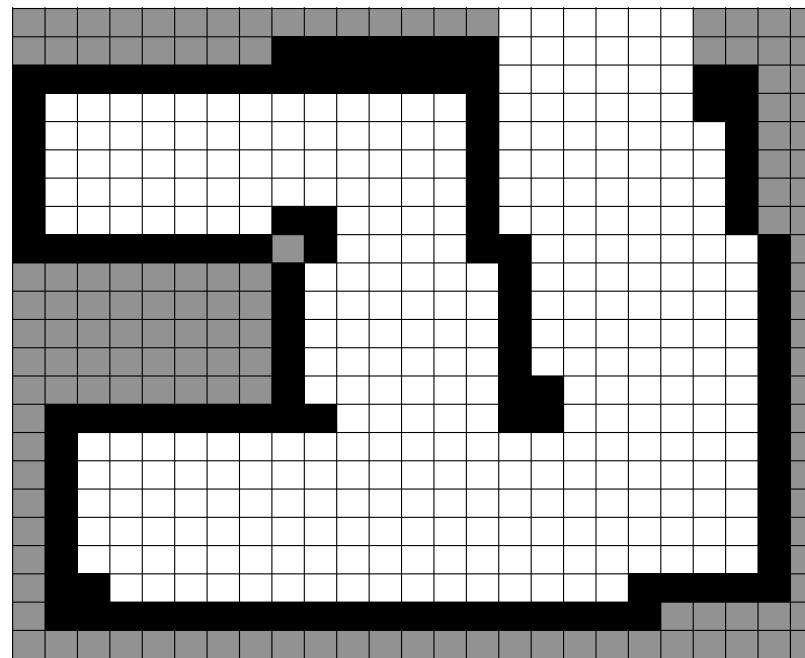
Real world



SLAM output

***Robot map is stored as an image
and represented as a graph***

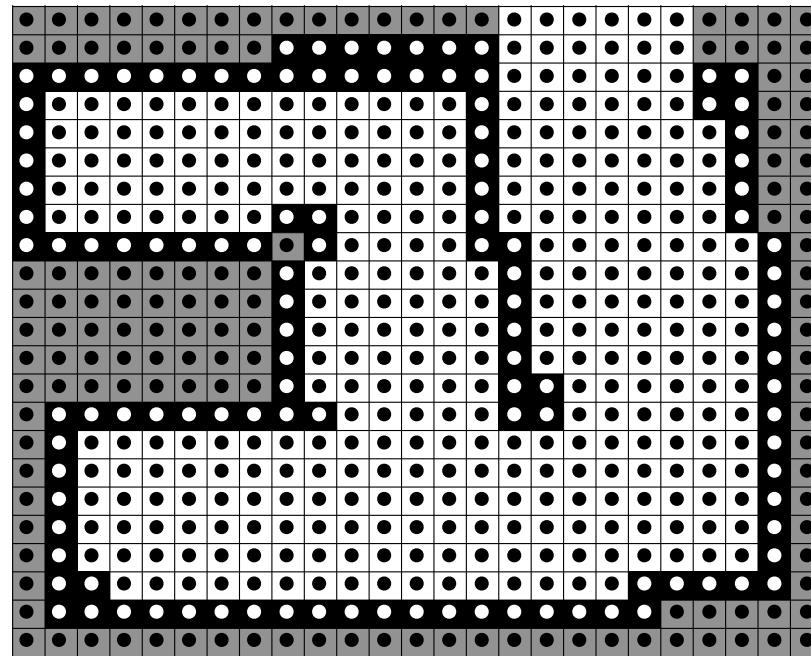
***A vector of cells over
robot locations***



***Robot map is stored as an image
and represented as a graph***

***A vector of cells over
robot locations***

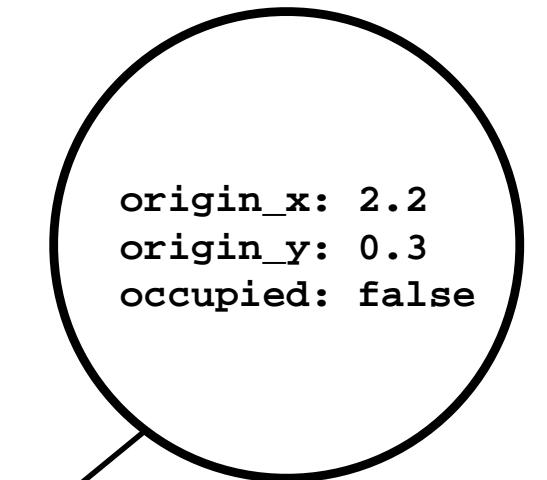
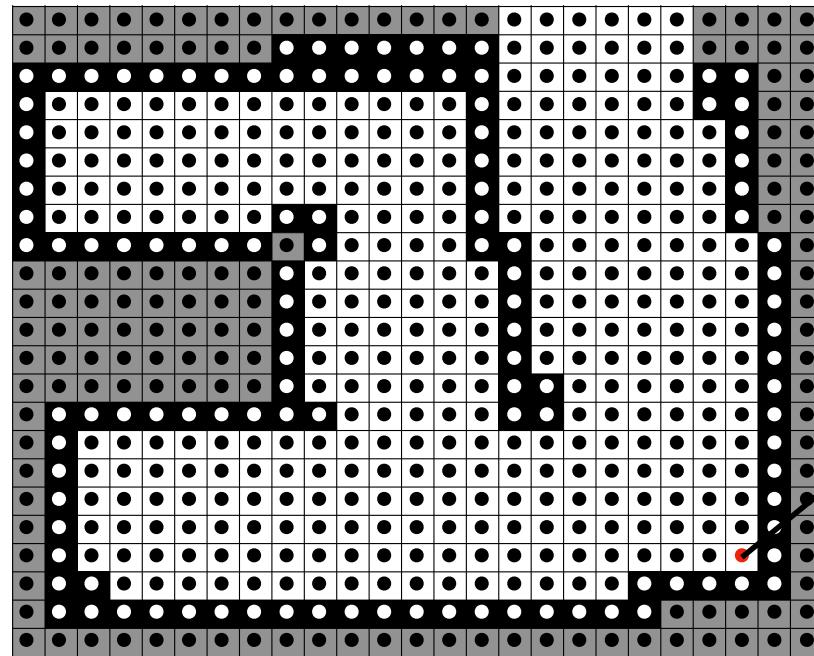
***Every cell has a
node in the graph***



***Robot map is stored as an image
and represented as a graph***

***A vector of cells over
robot locations***

***Every cell has a
node in the graph***



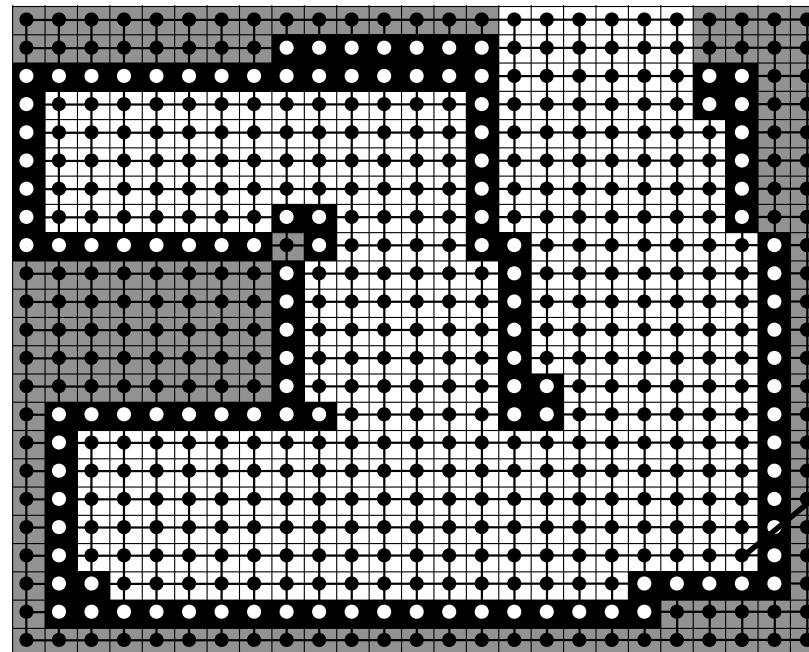
***A graph node
stores a struct of
information about
the cell***

***Robot map is stored as an image
and represented as a graph***

***A vector of cells over
robot locations***

***Every cell has a
node in the graph***

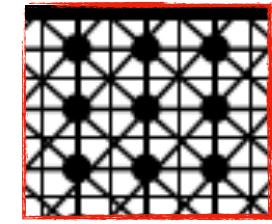
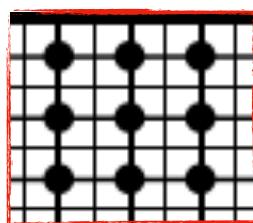
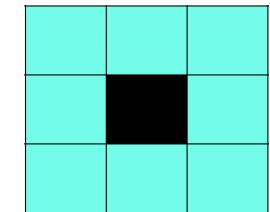
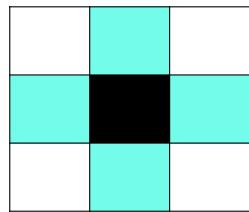
***Every pair of
neighboring cells
shares an edge in
the graph***



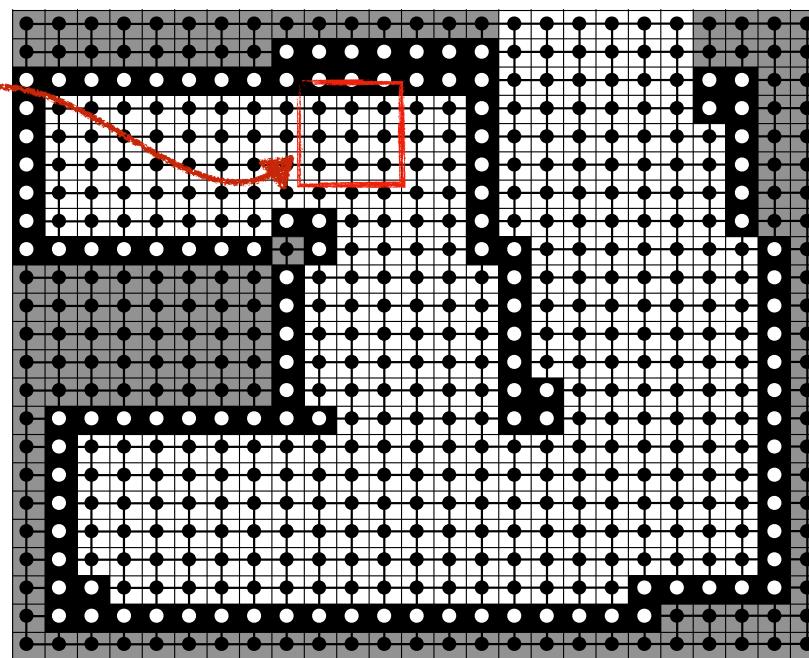
origin_x: 2.2
origin_y: 0.3
occupied: false

***A graph node
stores a struct of
information about
the cell***

**Grid graphs are typically either
4-connected or 8-connected**

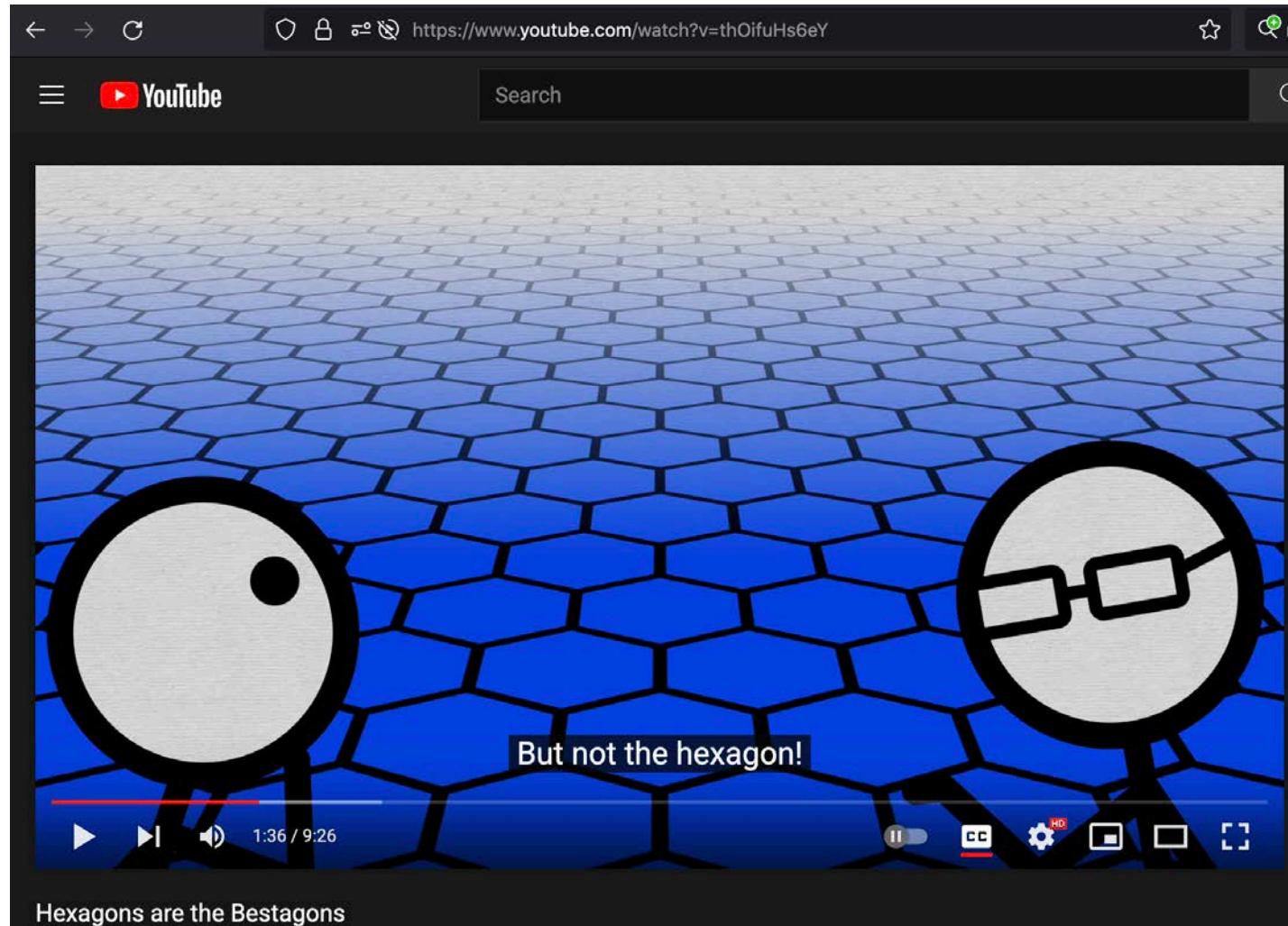


"NSEW"



Diagonals included

Quick tangent: Why are hexagons the bestagons ?



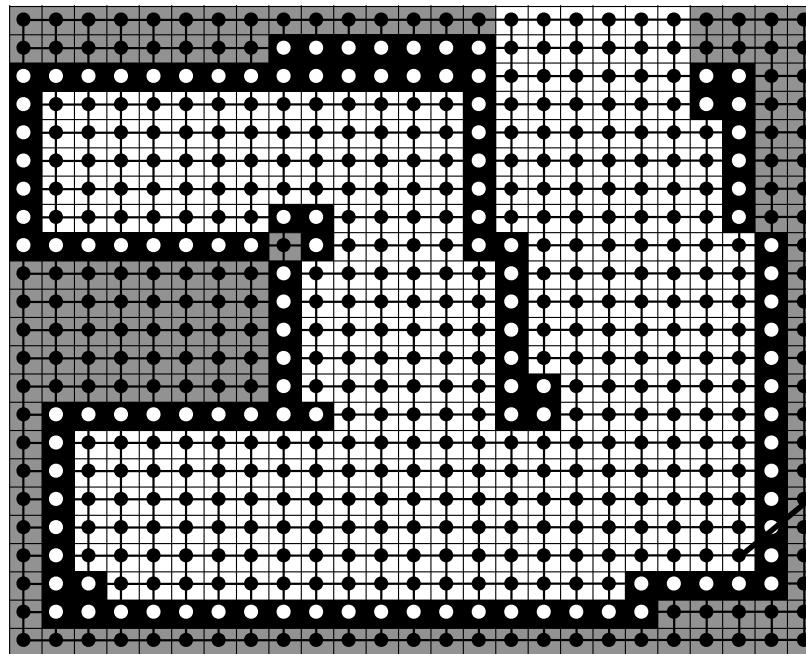
- Store parent of each node along route to start location
- Store path distance at each node along route to start location

Path expressed as the route to navigate at a node

A vector of cells over robot locations

Every cell has a node in the graph

Every pair of neighboring cells shares an edge in the graph

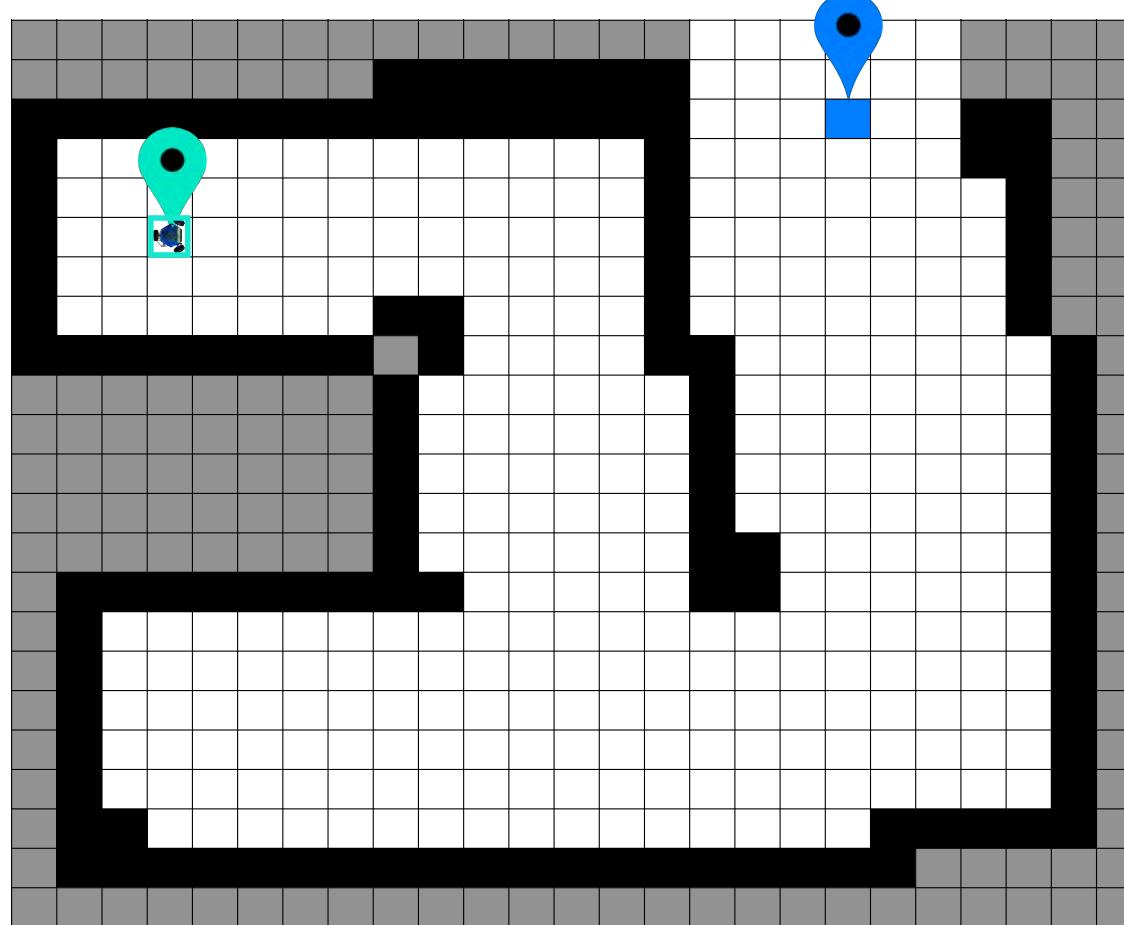


origin_x: 2.2
origin_y: 0.3
occupied: false
parent: ??
distance: ??

A graph node stores a struct of information about the cell

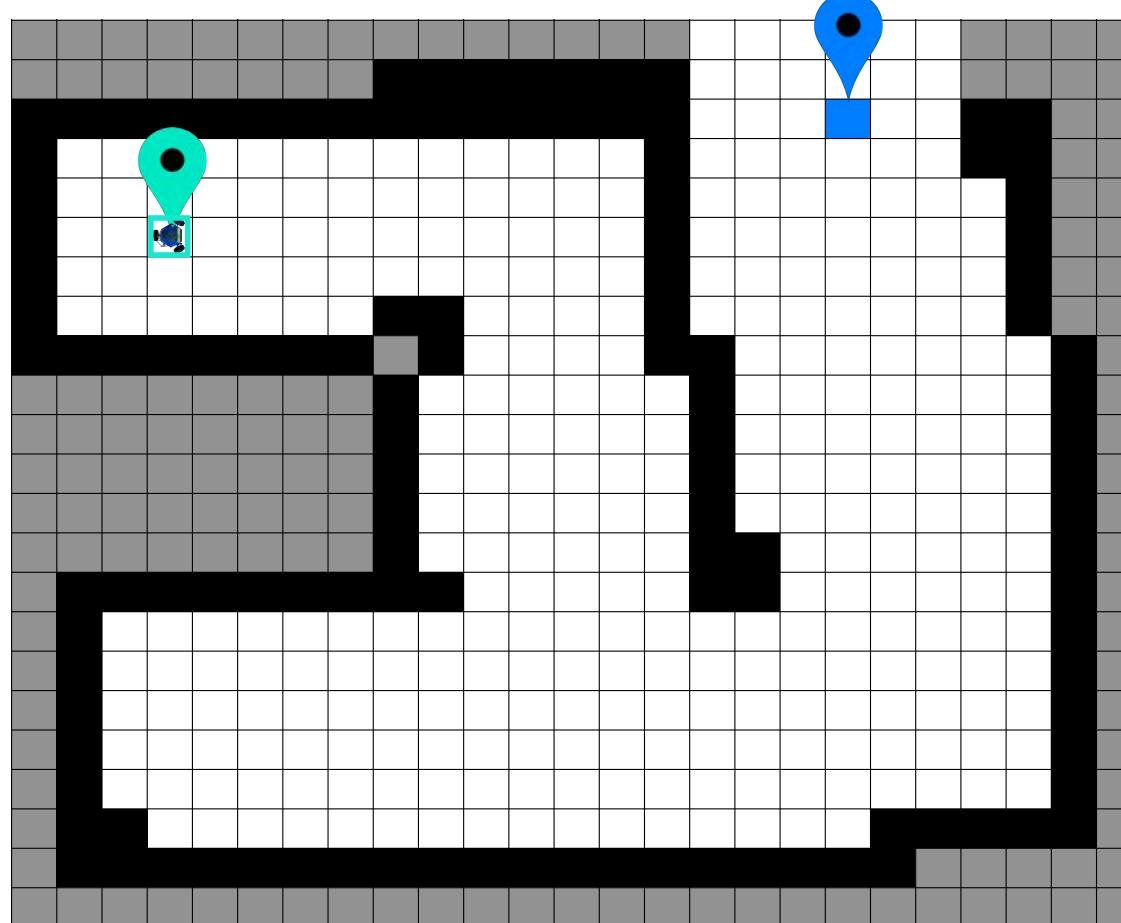
Assume robot planning a route from a given start location to a given goal location

How does Floodfill compute .parent and .distance for each node?



Assume robot planning a route from a given start location to a given goal location

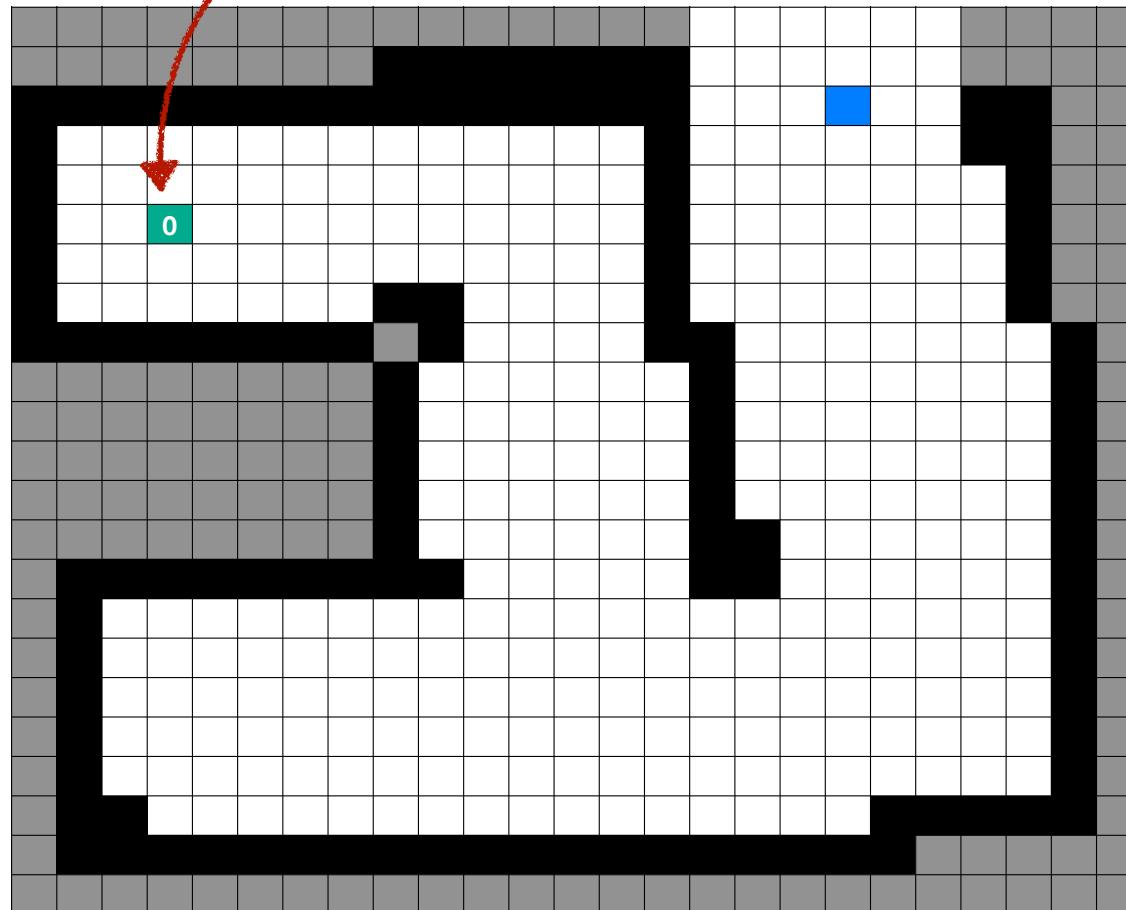
How does Floodfill compute .parent and .distance for each node?



Grow outward from the node at the start location

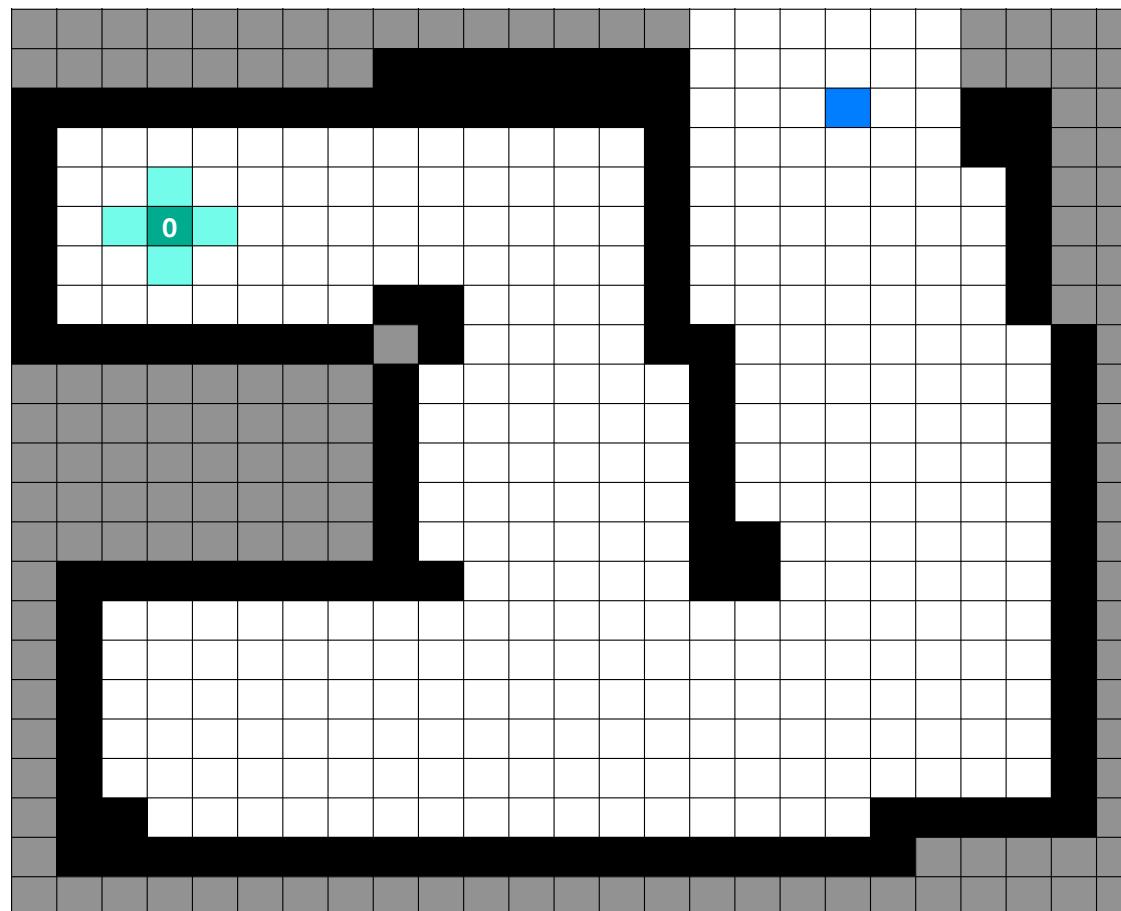
**Begin from
start node
with
no parent and
zero distance**

The start is the “root” of our search graph



***Begin from
start node
with
no parent and
zero distance***

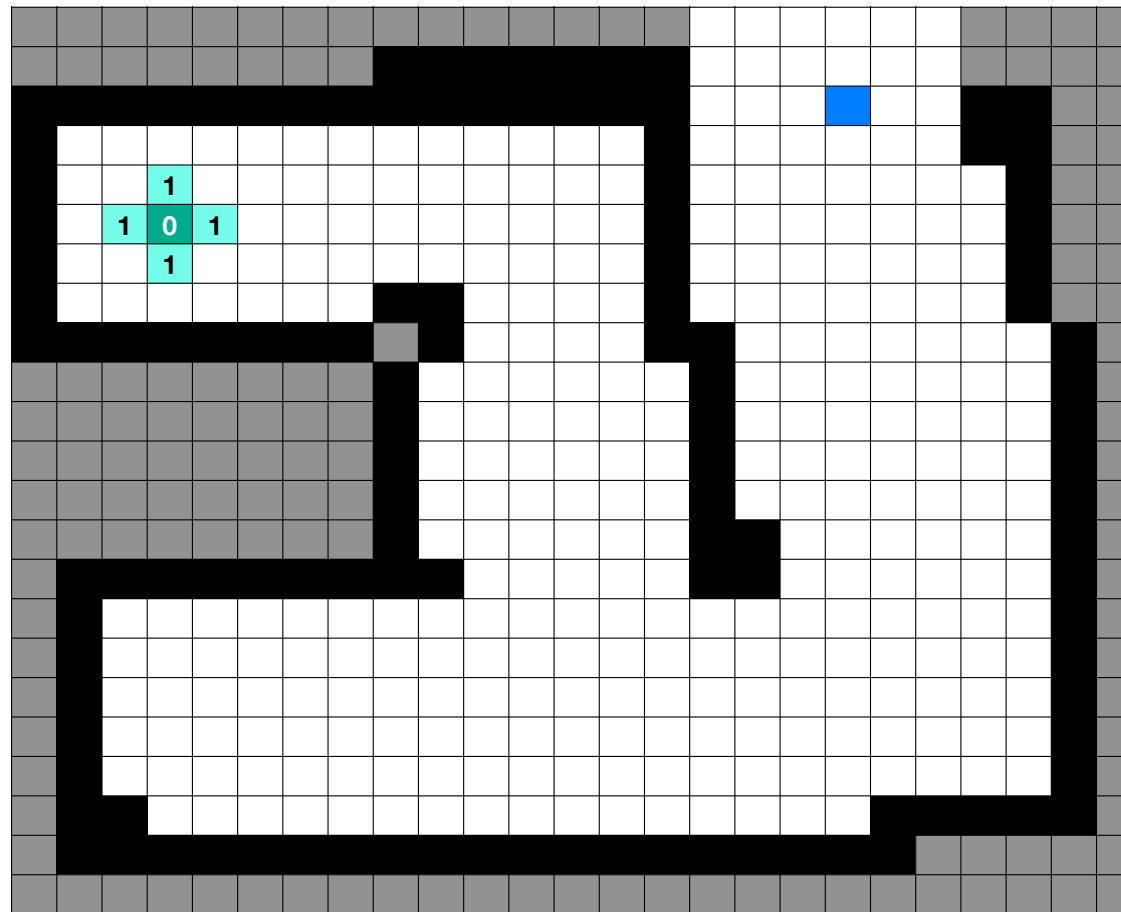
***All neighbors
of start are
“visited”***



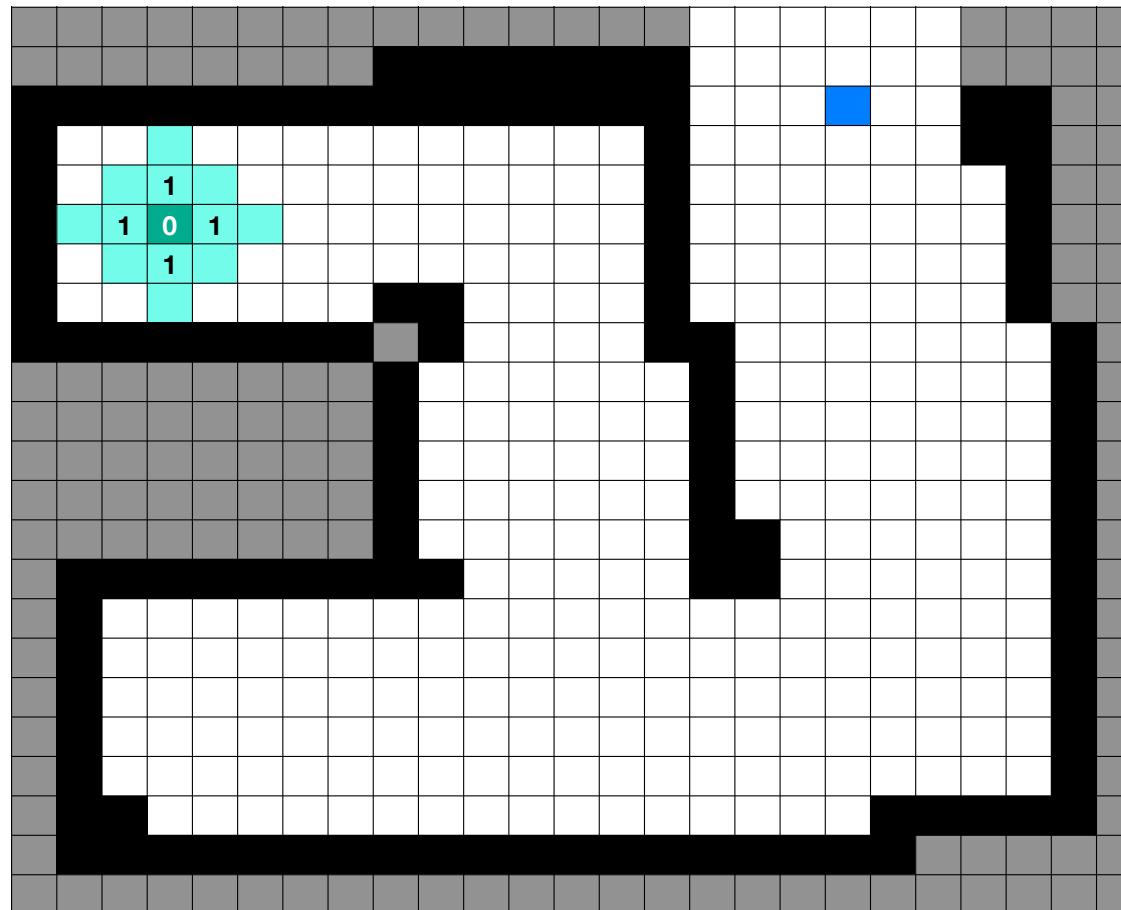
***Begin from
start node
with
no parent and
zero distance***

***All neighbors
of start are
“visited”***

***And assigned
one plus the
smallest
distance***

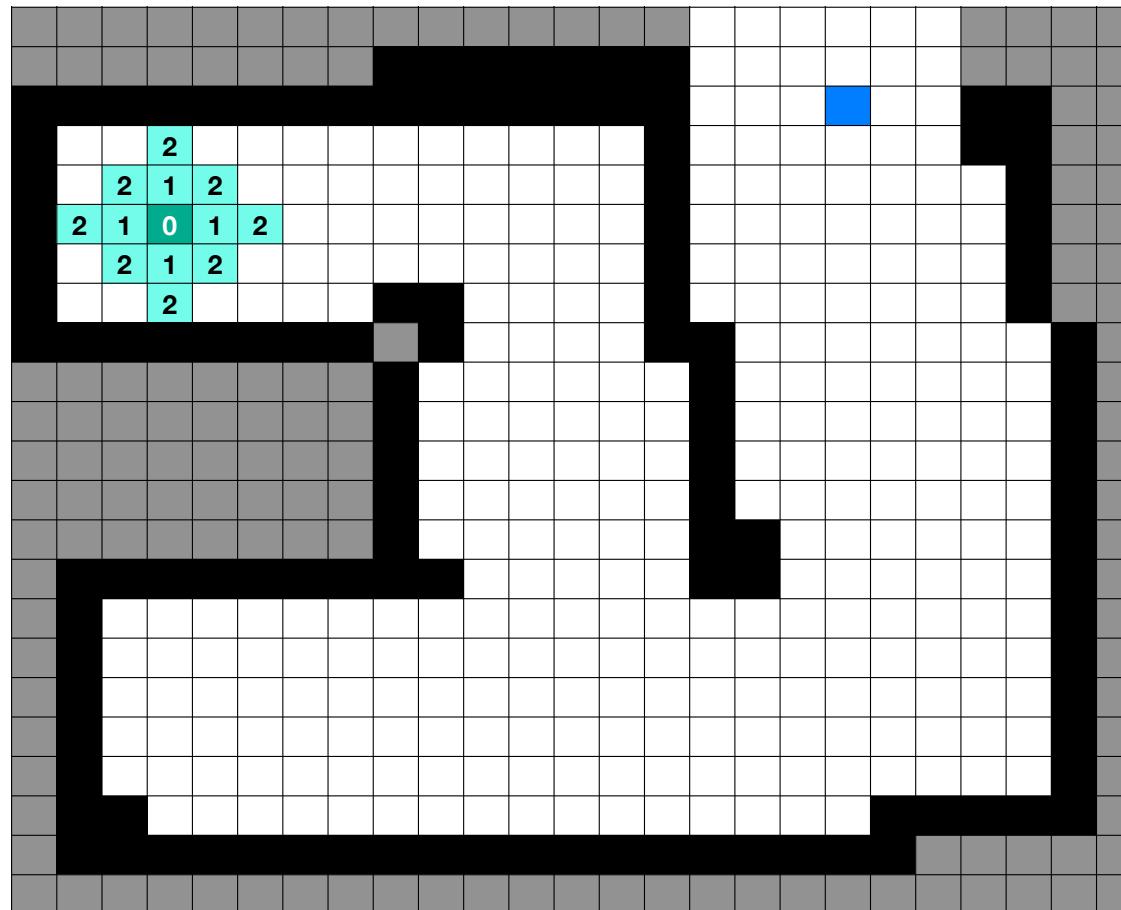


***Then, visit the
neighbors of
nodes just
visited***



***Then, visit the
neighbors of
nodes just
visited***

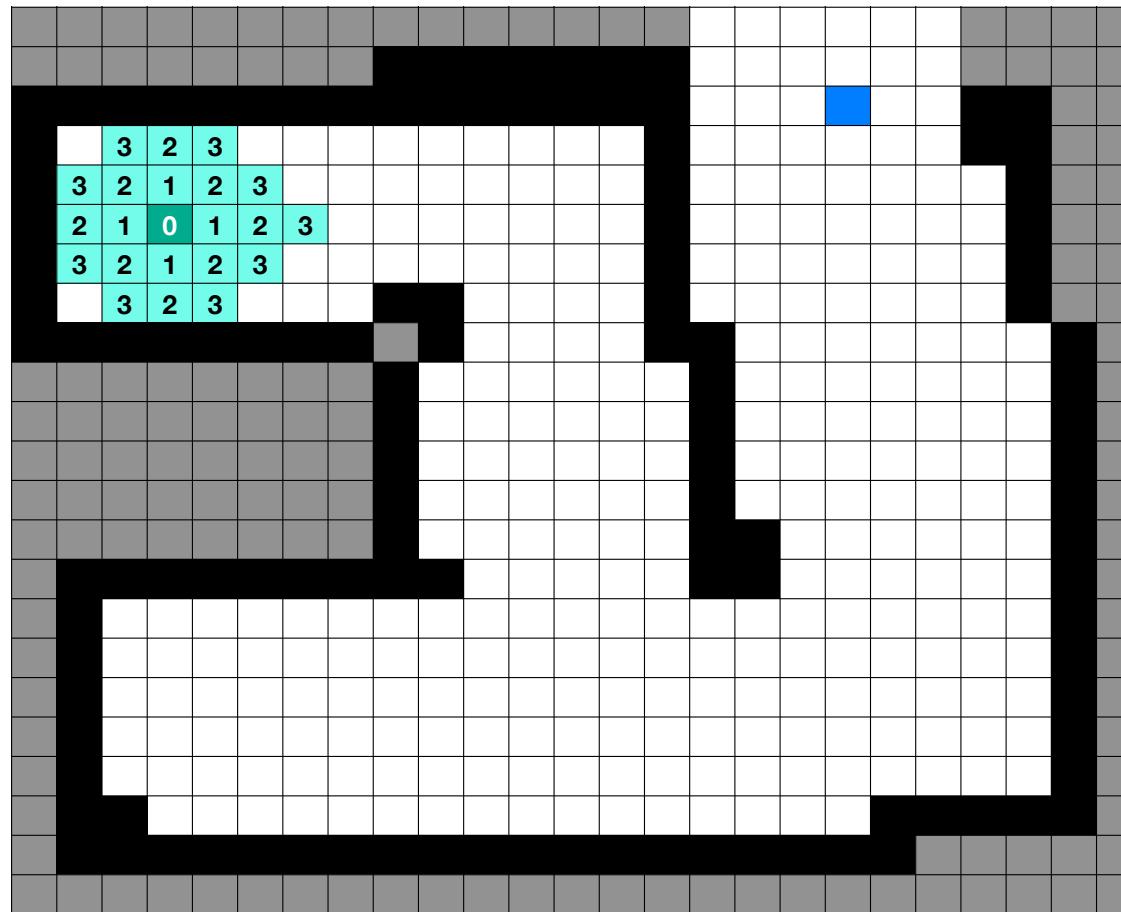
***Assign each
one plus the
smallest
distance***



**Then, visit the
neighbors of
nodes just
visited**

**Assign each
one plus the
smallest
distance**

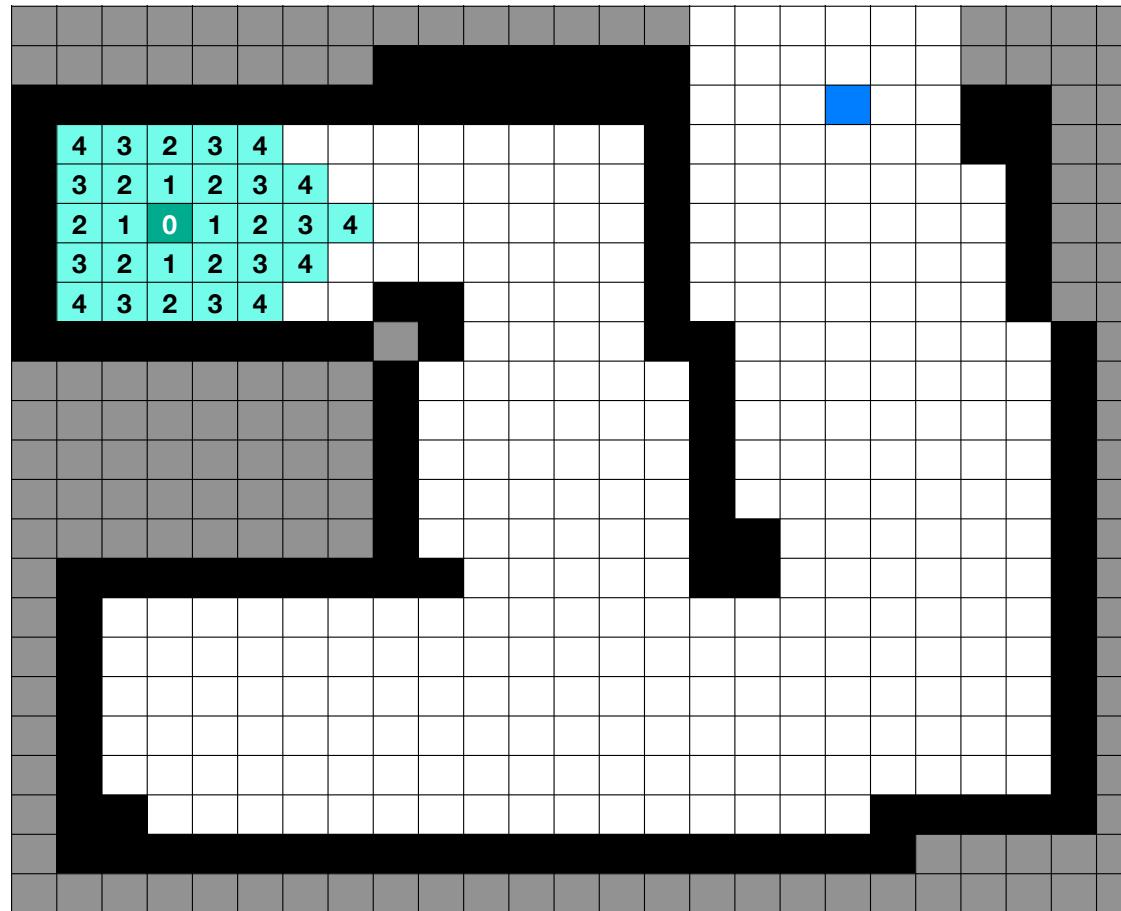
**Repeat for
next set of
neighbors**



**Then, visit the
neighbors of
nodes just
visited**

**Assign each
one plus the
smallest
distance**

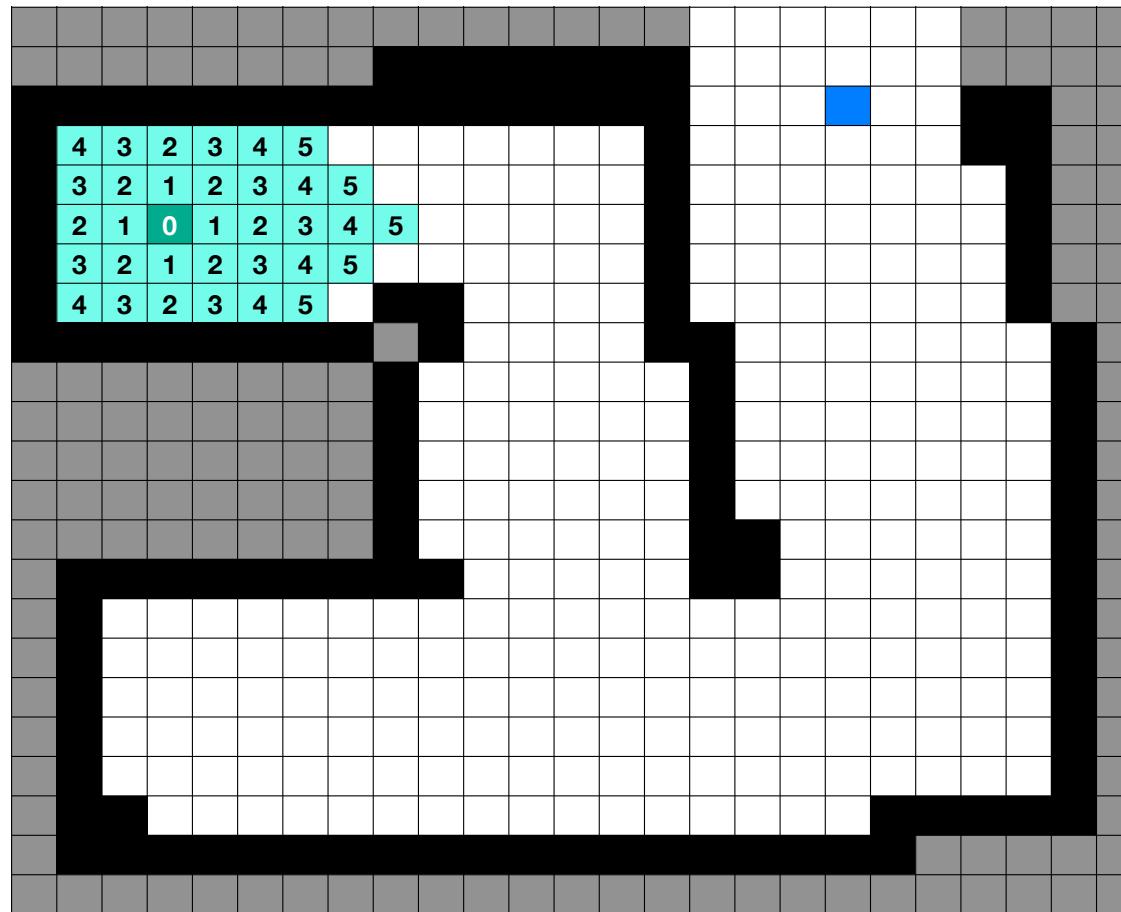
**Repeat for
next set of
neighbors**



**Then, visit the
neighbors of
nodes just
visited**

**Assign each
one plus the
smallest
distance**

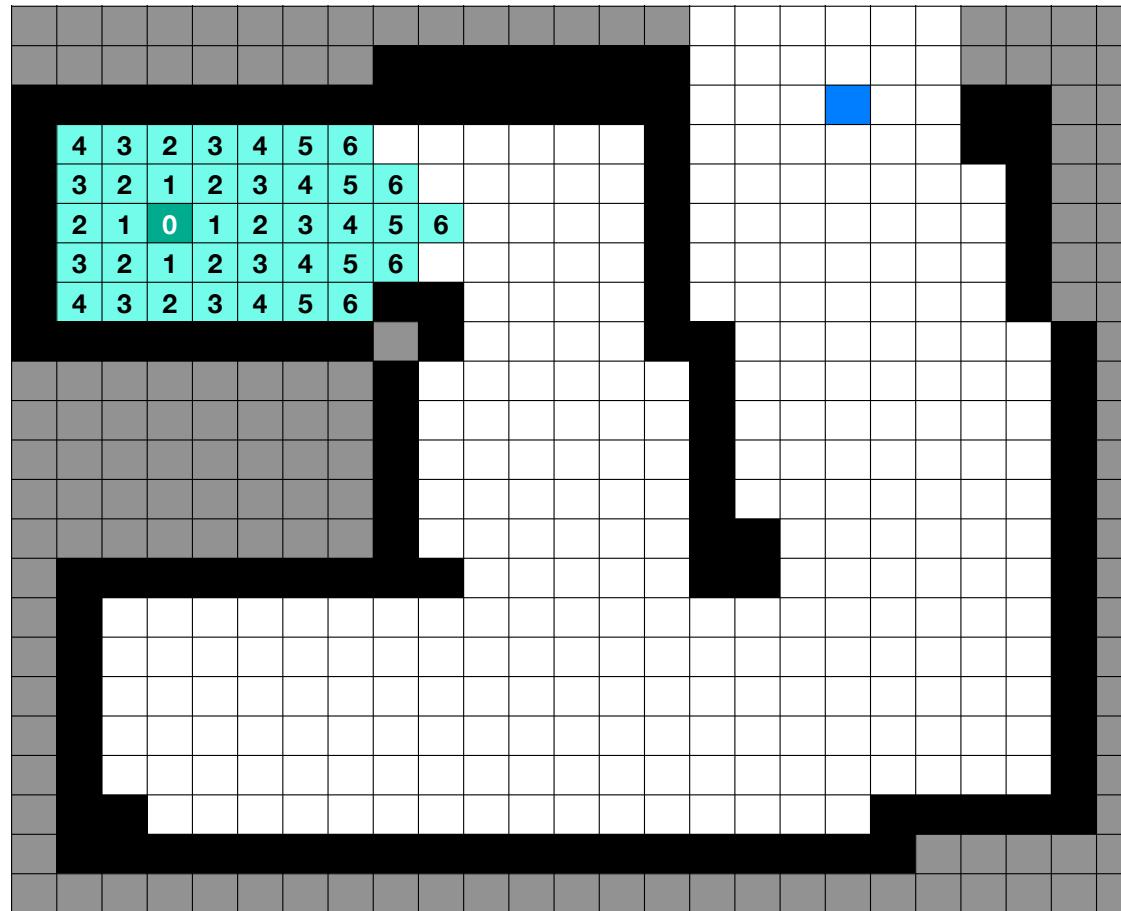
**Repeat for
next set of
neighbors**



**Then, visit the
neighbors of
nodes just
visited**

**Assign each
one plus the
smallest
distance**

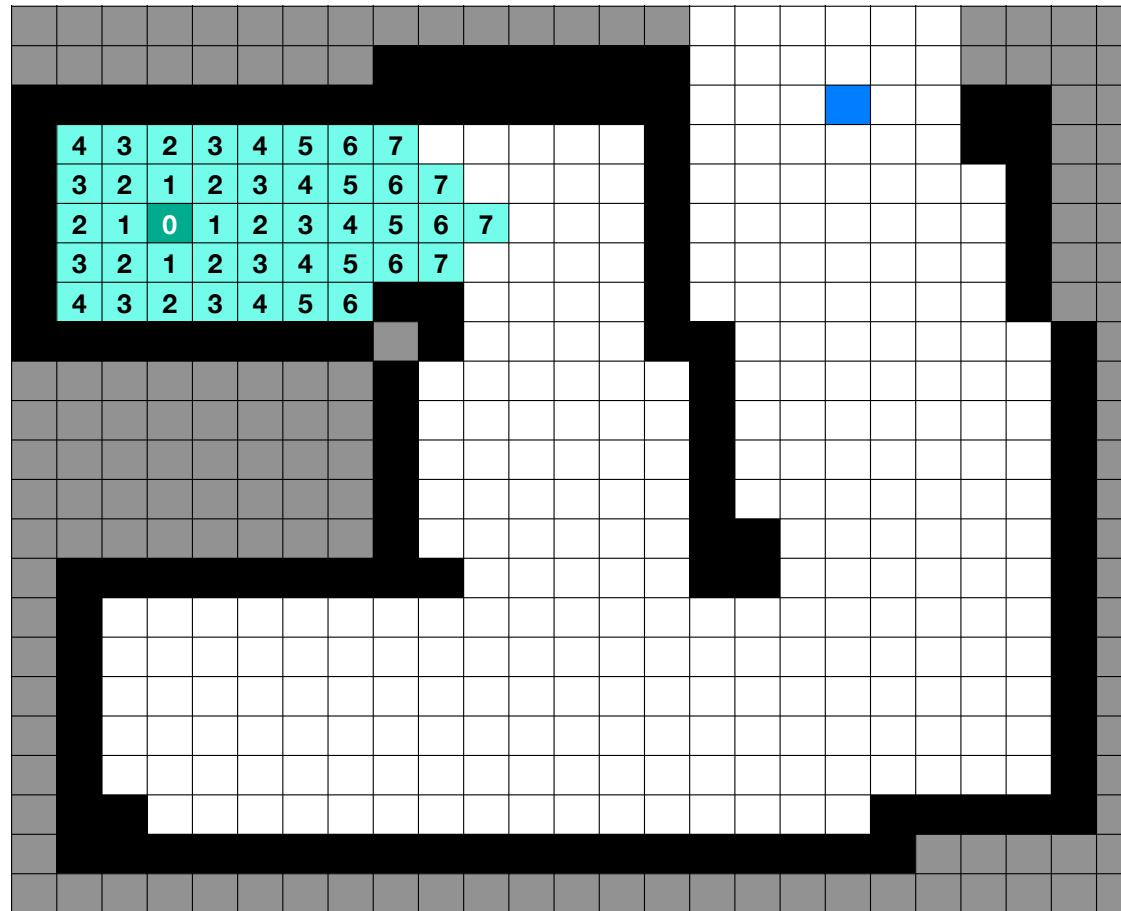
**Repeat for
next set of
neighbors**



**Then, visit the
neighbors of
nodes just
visited**

**Assign each
one plus the
smallest
distance**

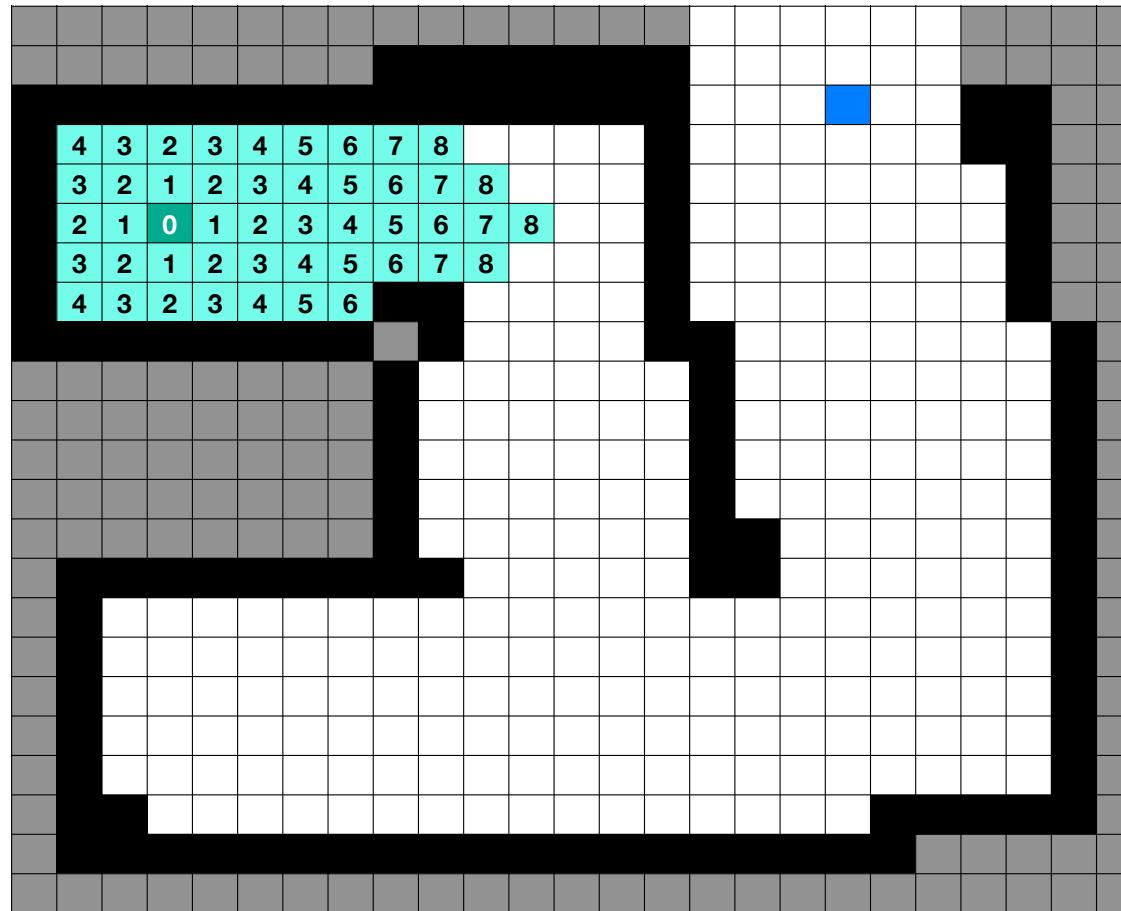
**Repeat for
next set of
neighbors**



**Then, visit the
neighbors of
nodes just
visited**

**Assign each
one plus the
smallest
distance**

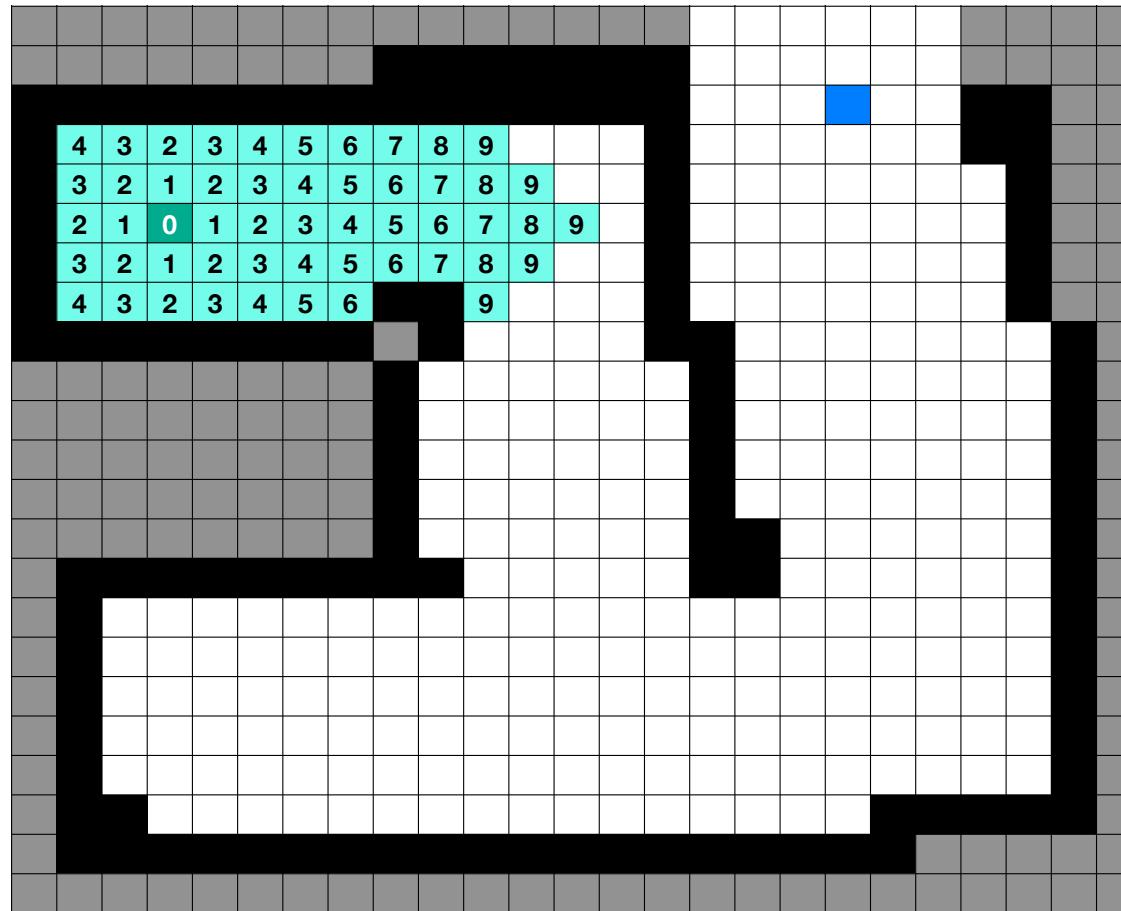
**Repeat for
next set of
neighbors**



***Then, visit the
neighbors of
nodes just
visited***

***Assign each
one plus the
smallest
distance***

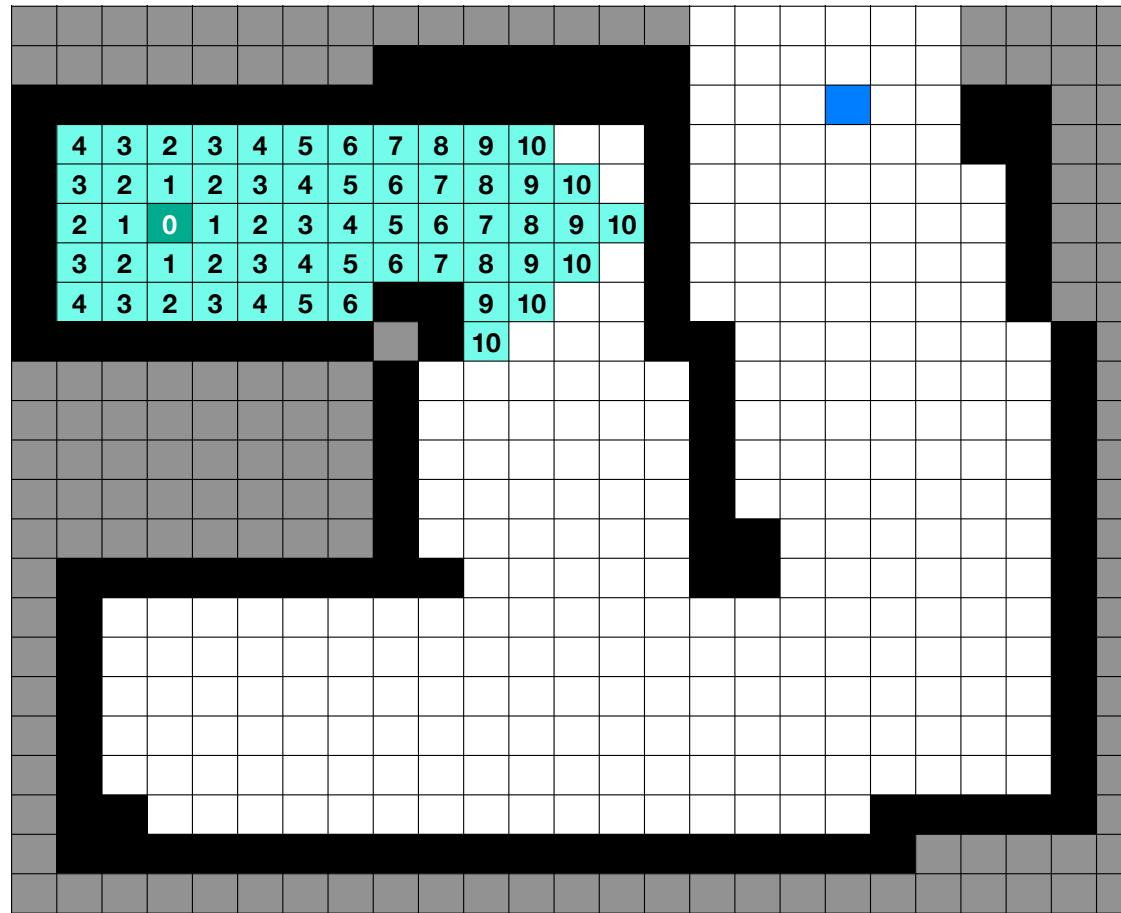
***Repeat for
next set of
neighbors***



**Then, visit the
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nodes just
visited**

**Assign each
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smallest
distance**

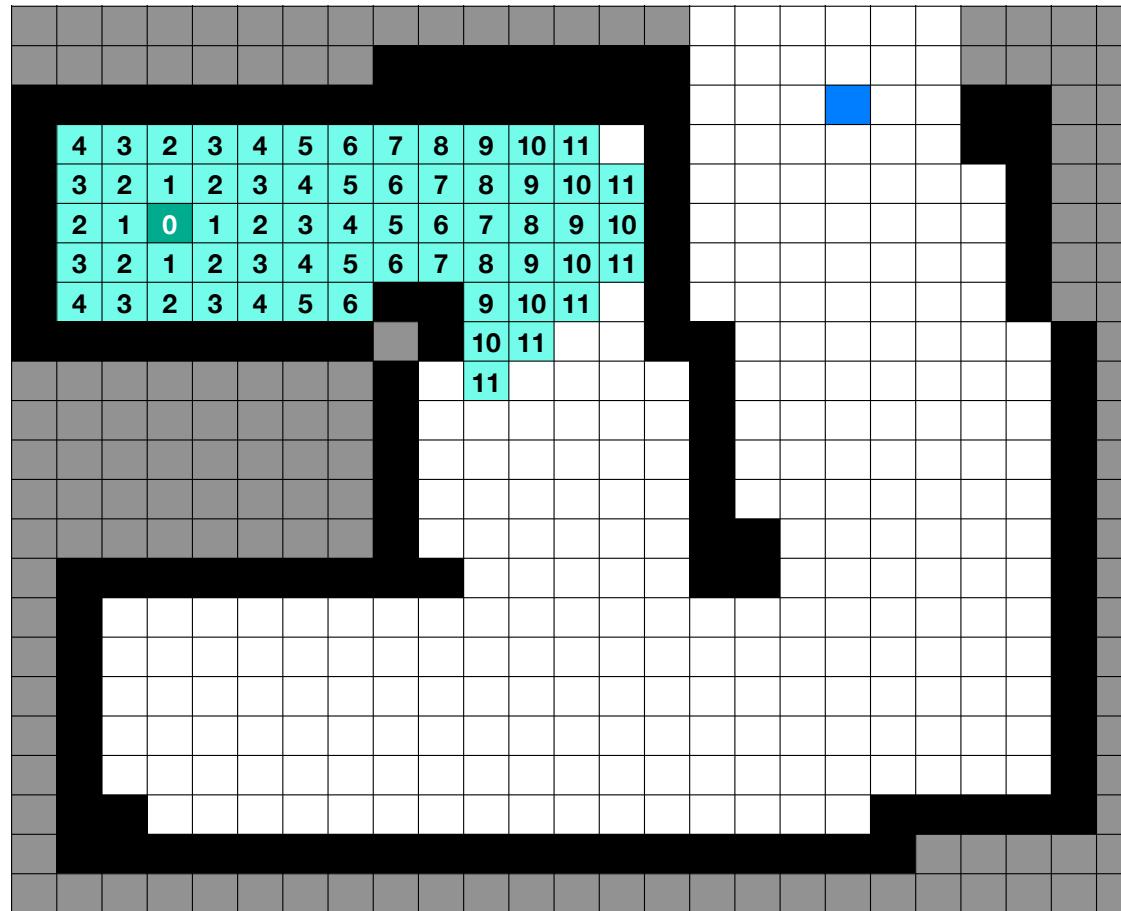
**Repeat for
next set of
neighbors**



**Then, visit the
neighbors of
nodes just
visited**

**Assign each
one plus the
smallest
distance**

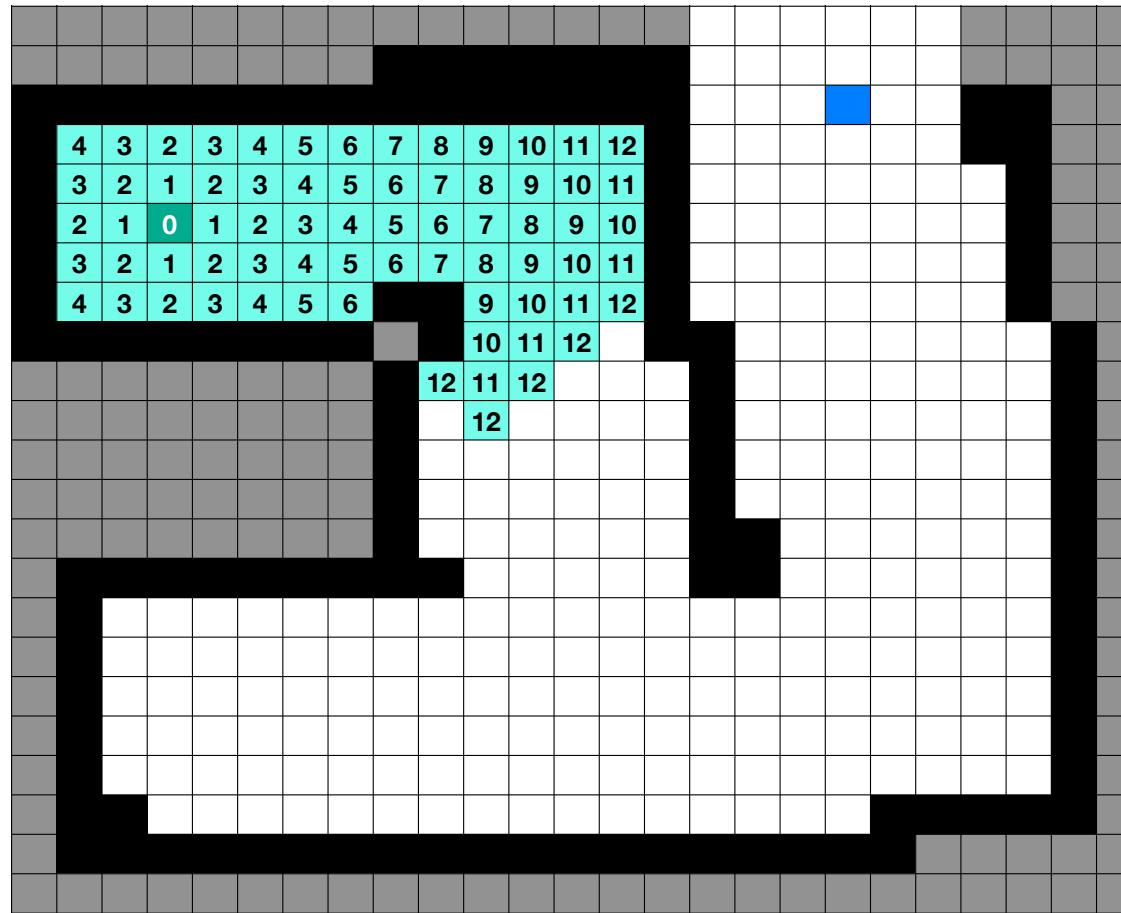
**Repeat for
next set of
neighbors**



**Then, visit the
neighbors of
nodes just
visited**

**Assign each
one plus the
smallest
distance**

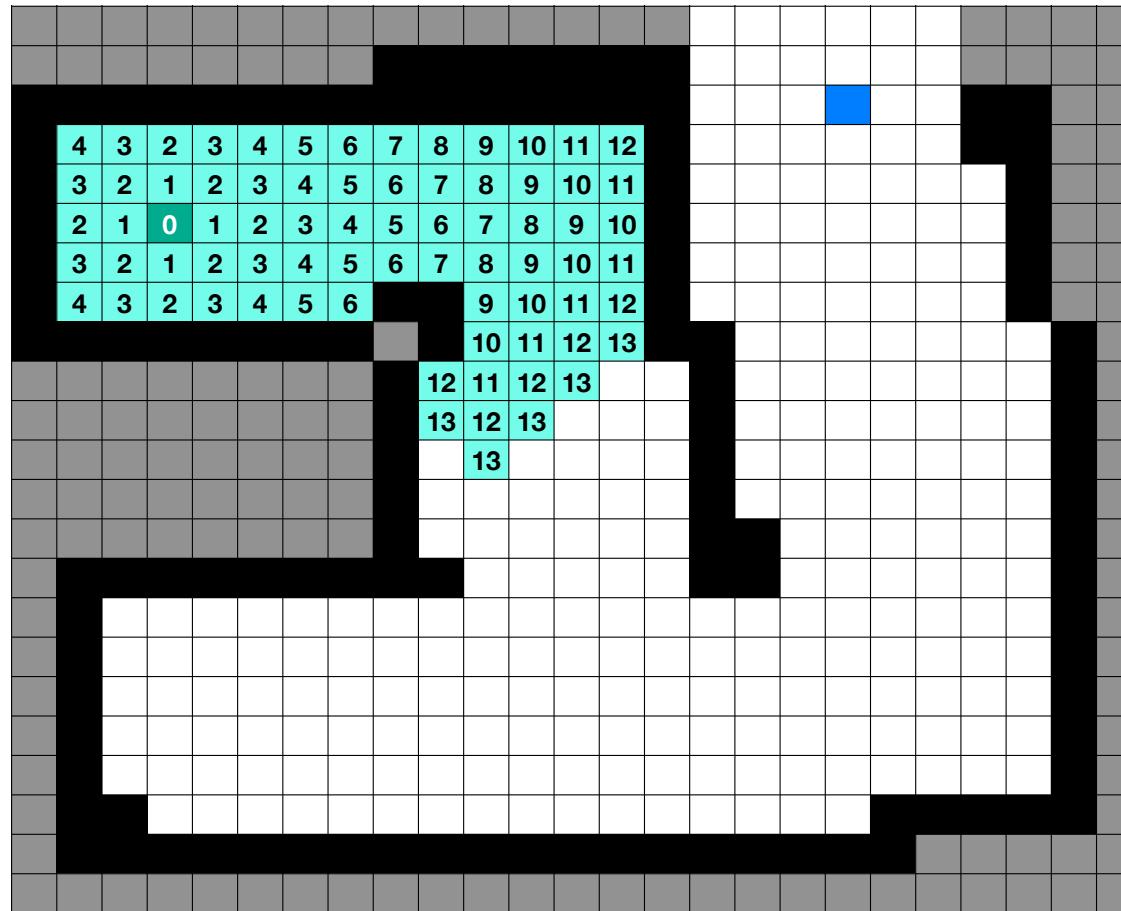
**Repeat for
next set of
neighbors**



**Then, visit the
neighbors of
nodes just
visited**

**Assign each
one plus the
smallest
distance**

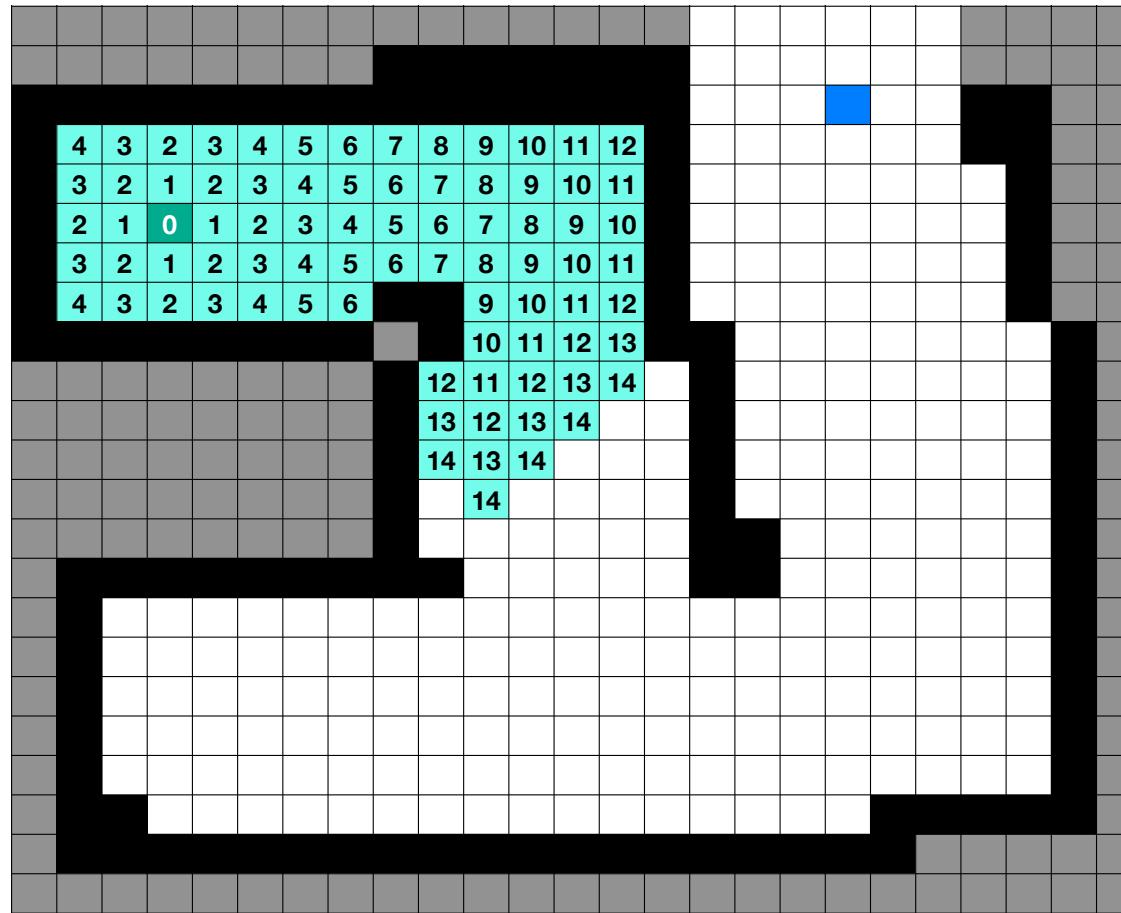
**Repeat for
next set of
neighbors**



**Then, visit the
neighbors of
nodes just
visited**

**Assign each
one plus the
smallest
distance**

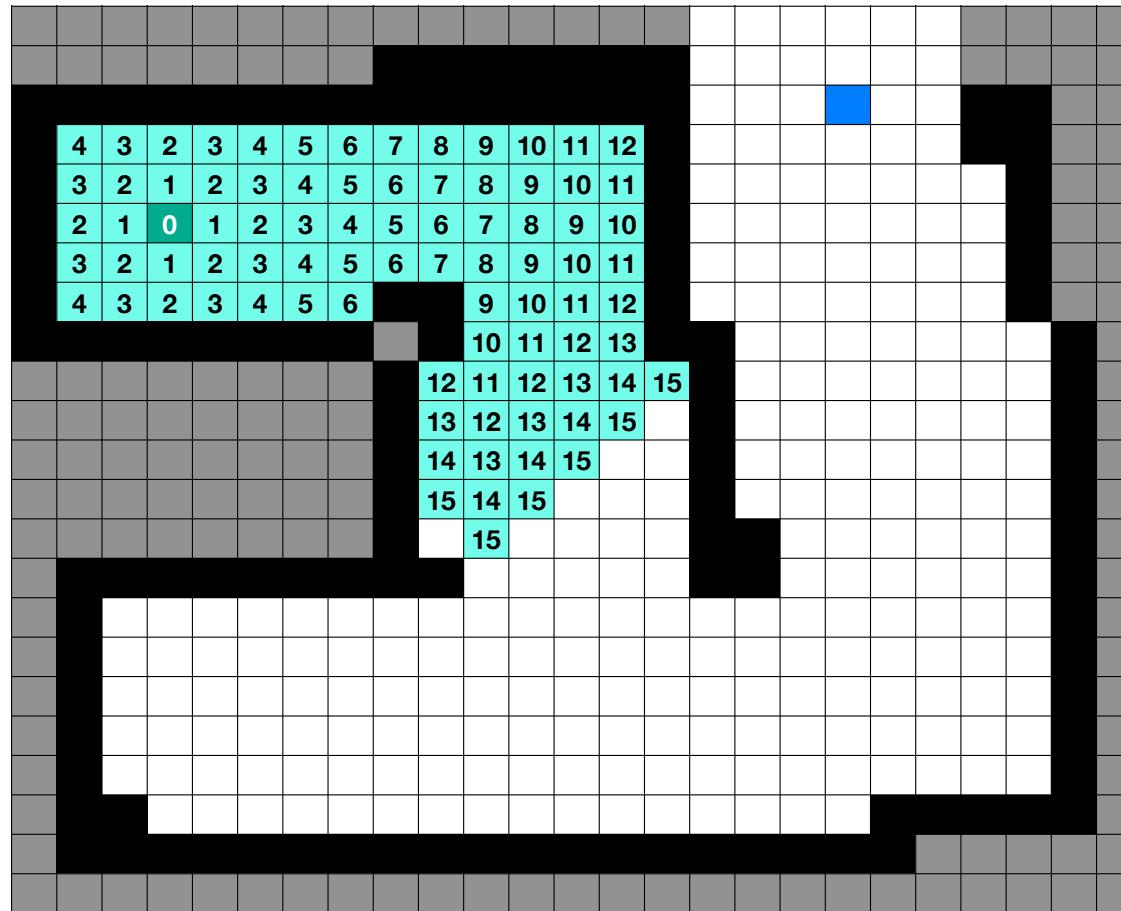
**Repeat for
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**Then, visit the
neighbors of
nodes just
visited**

**Assign each
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smallest
distance**

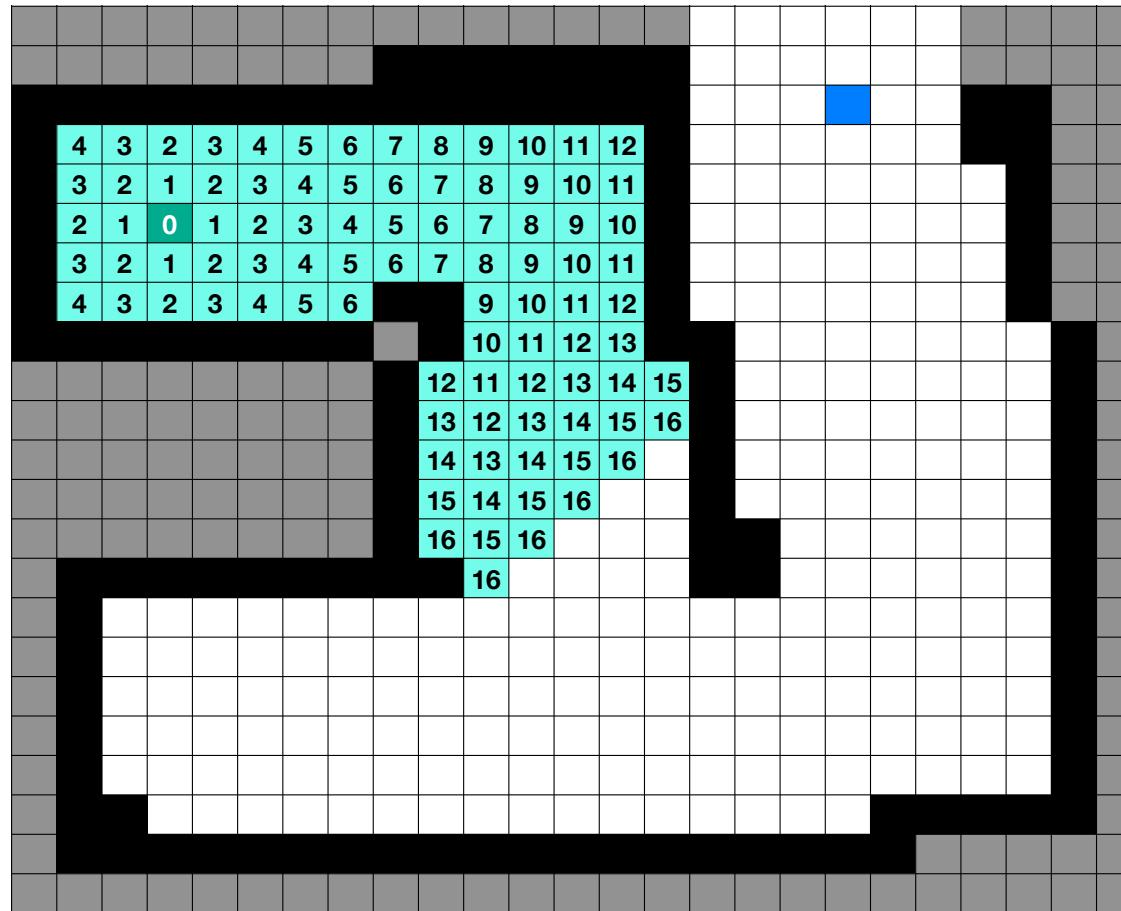
**Repeat for
next set of
neighbors**



**Then, visit the
neighbors of
nodes just
visited**

**Assign each
one plus the
smallest
distance**

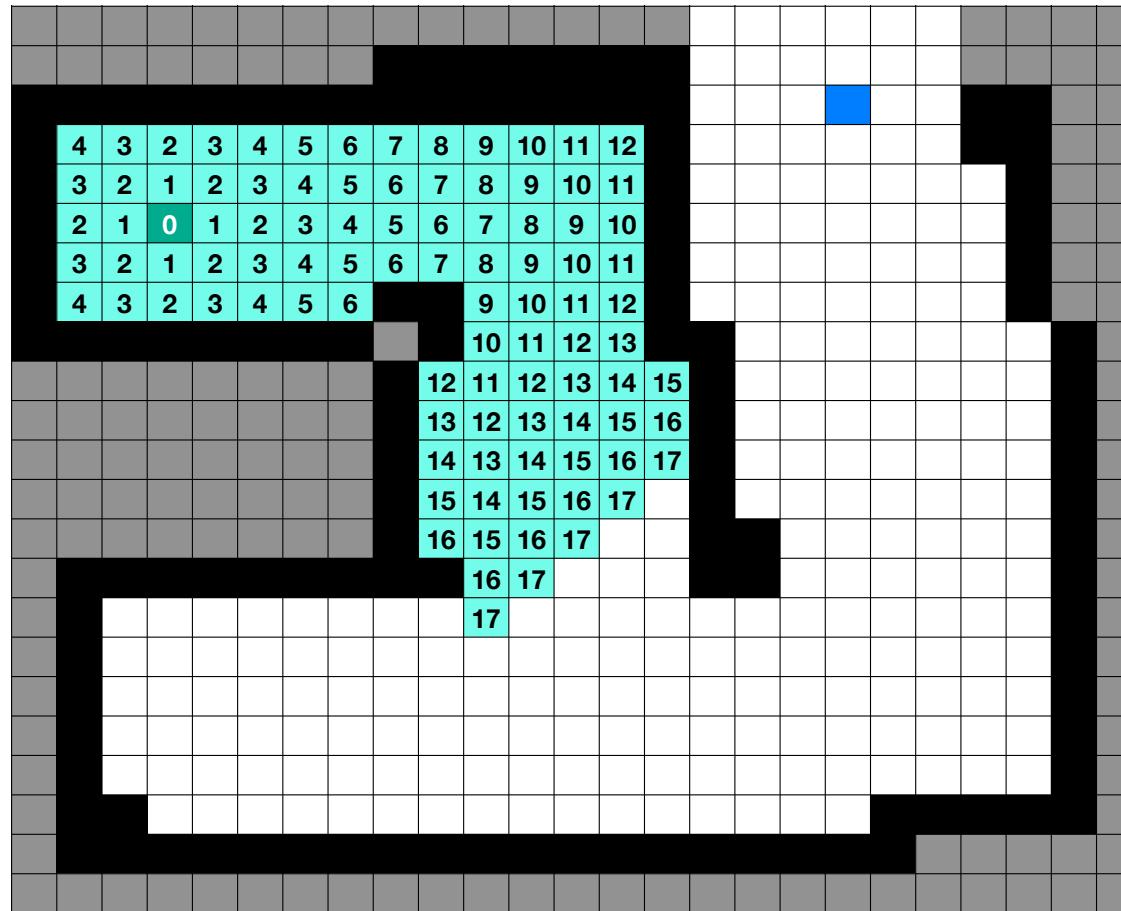
**Repeat for
next set of
neighbors**



**Then, visit the
neighbors of
nodes just
visited**

**Assign each
one plus the
smallest
distance**

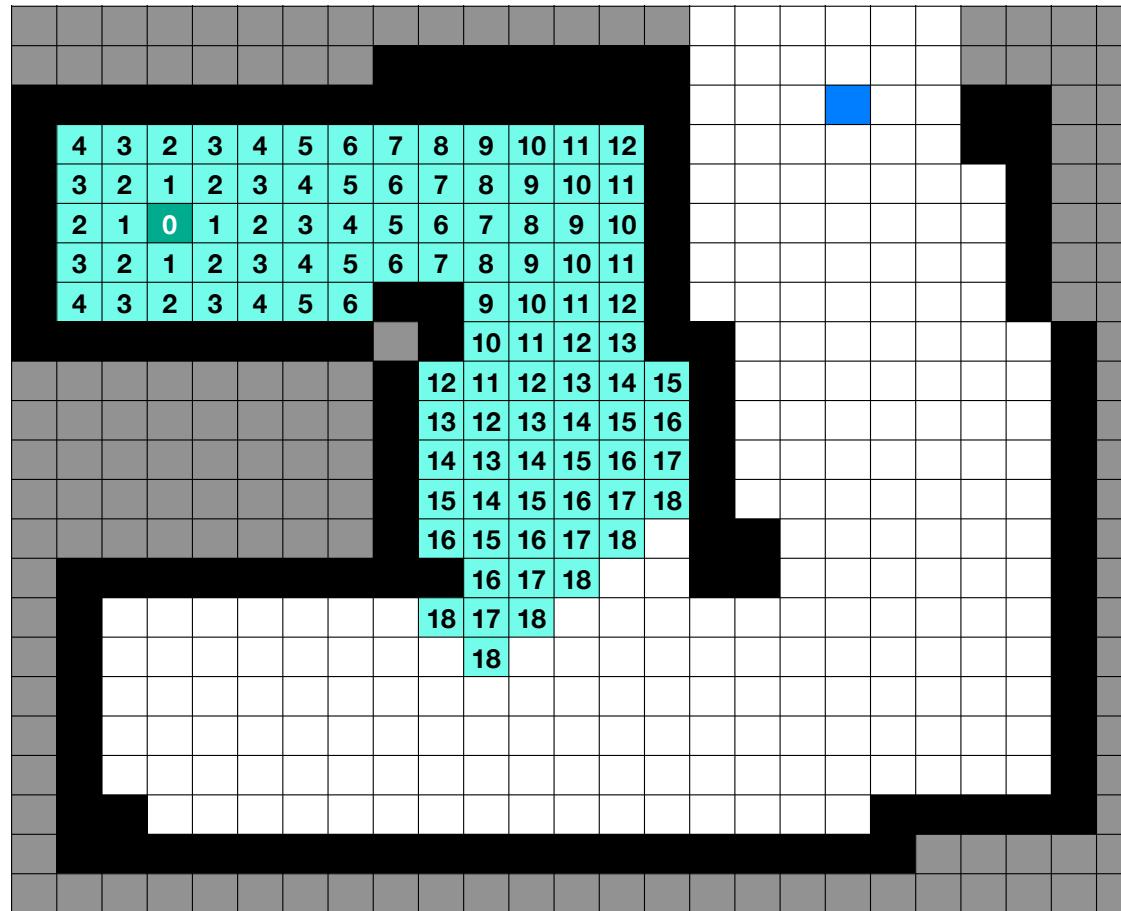
**Repeat for
next set of
neighbors**



**Then, visit the
neighbors of
nodes just
visited**

**Assign each
one plus the
smallest
distance**

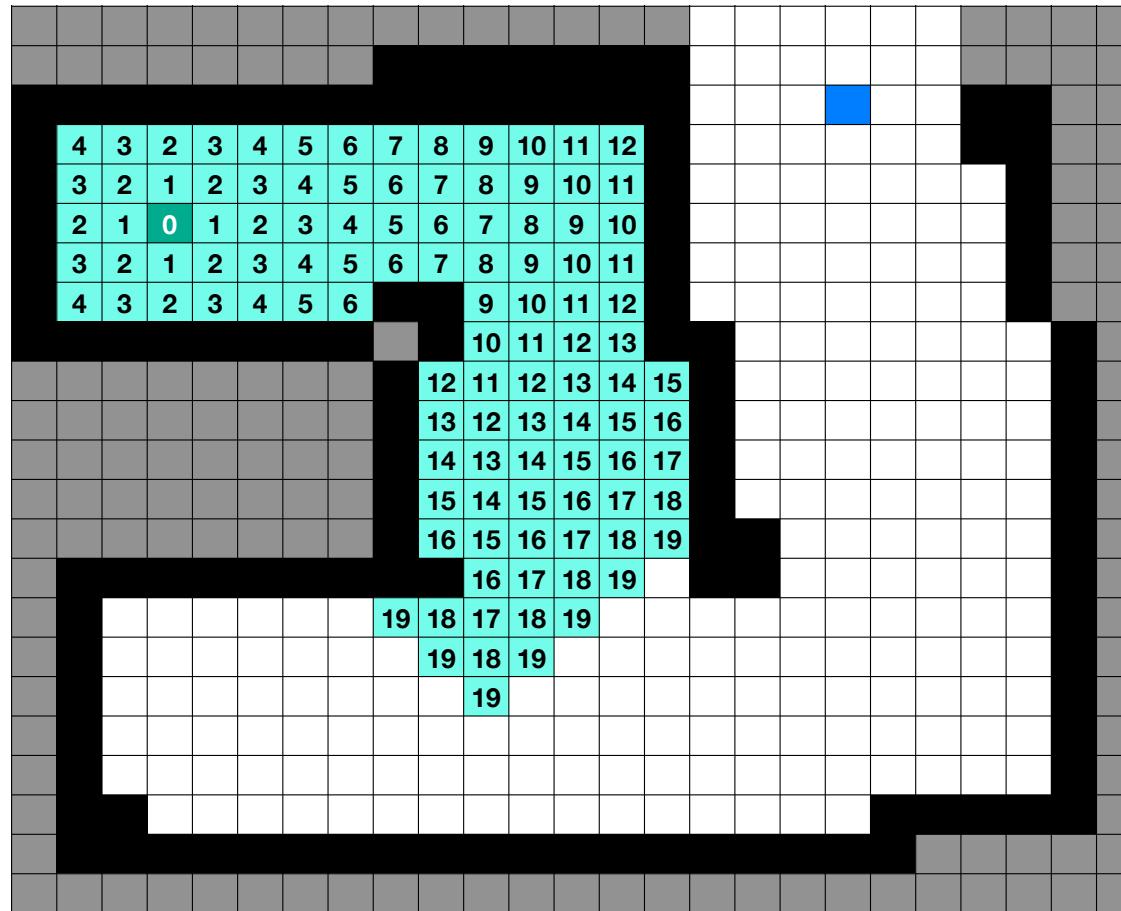
**Repeat for
next set of
neighbors**



**Then, visit the
neighbors of
nodes just
visited**

**Assign each
one plus the
smallest
distance**

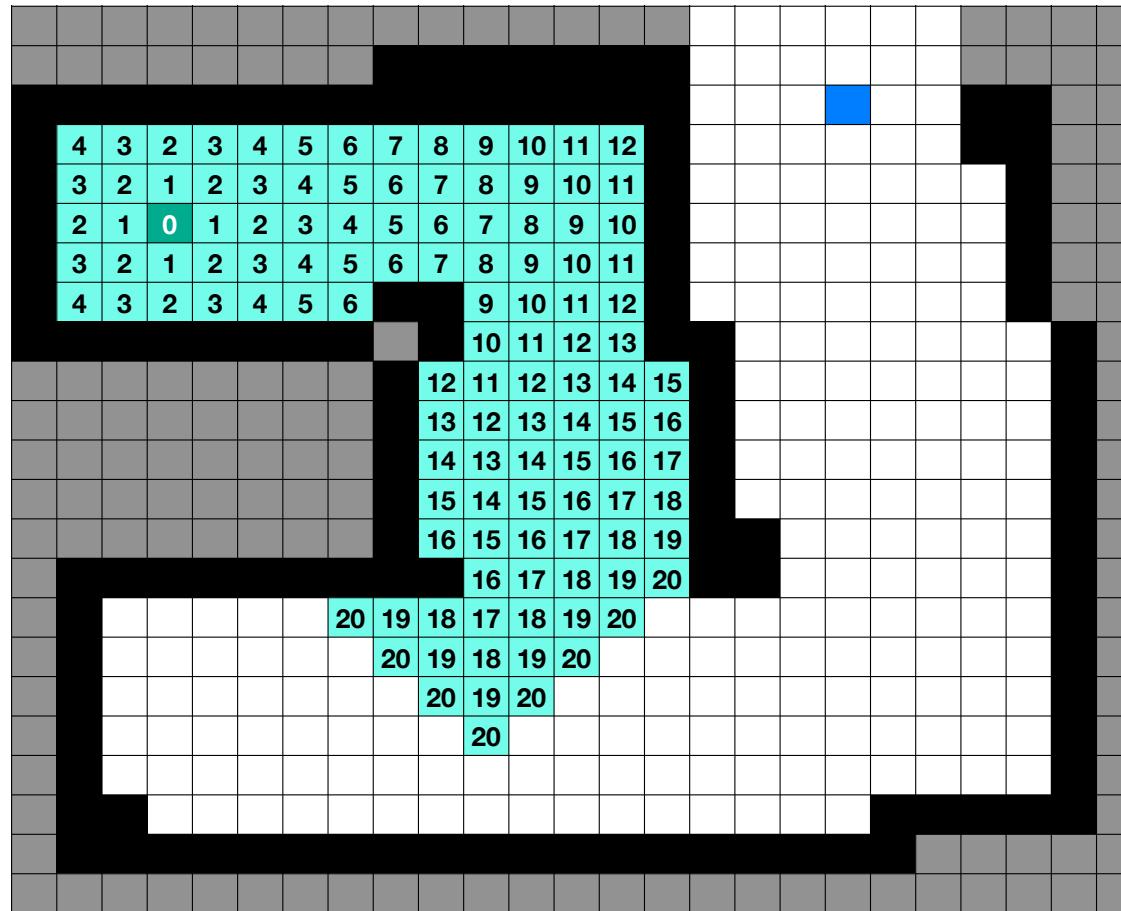
**Repeat for
next set of
neighbors**



**Then, visit the
neighbors of
nodes just
visited**

**Assign each
one plus the
smallest
distance**

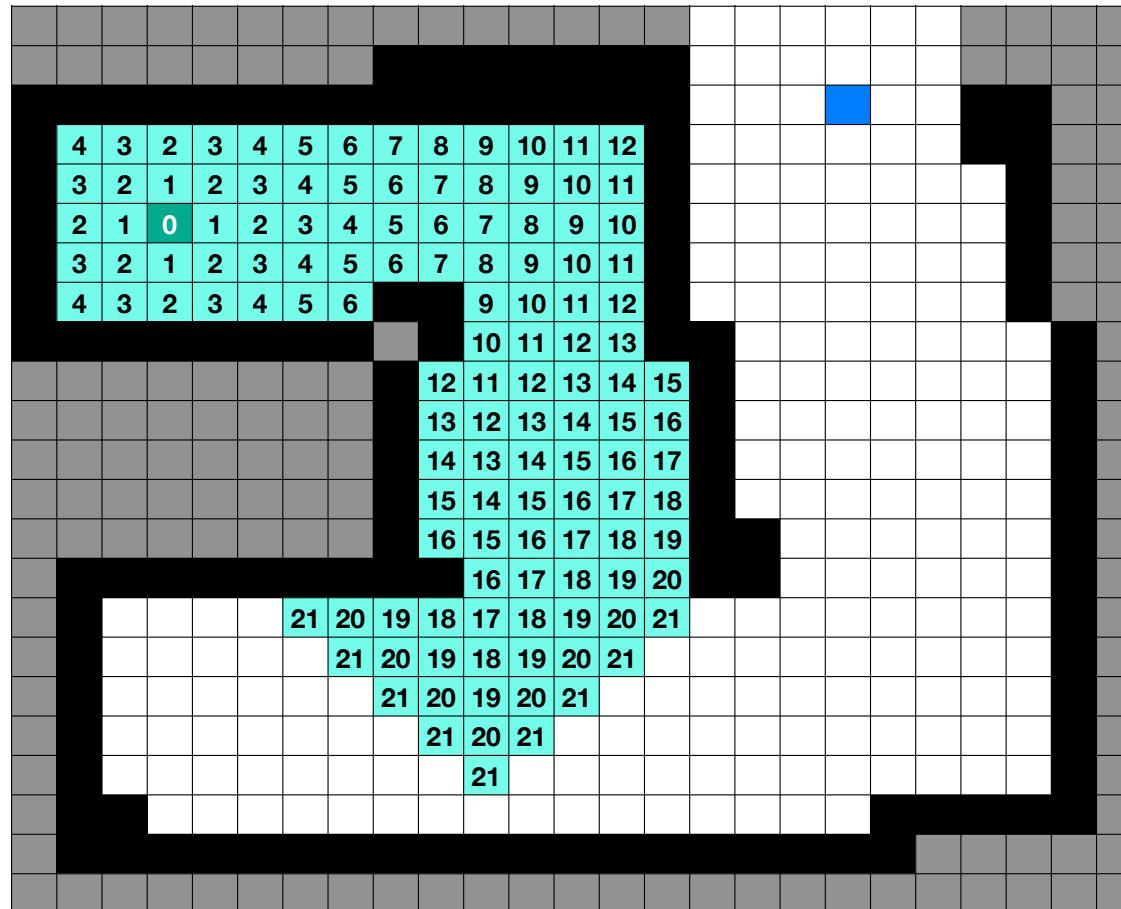
**Repeat for
next set of
neighbors**



**Then, visit the
neighbors of
nodes just
visited**

**Assign each
one plus the
smallest
distance**

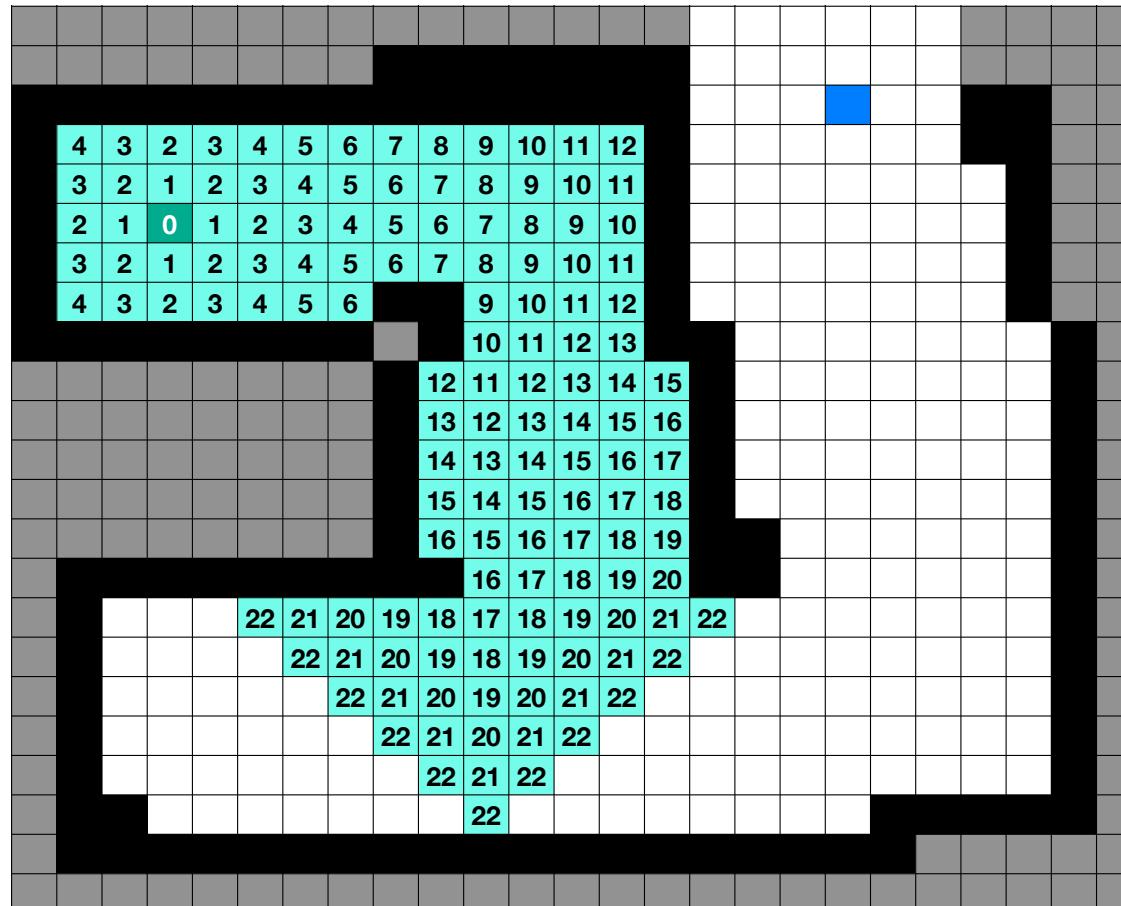
**Repeat for
next set of
neighbors**



**Then, visit the
neighbors of
nodes just
visited**

**Assign each
one plus the
smallest
distance**

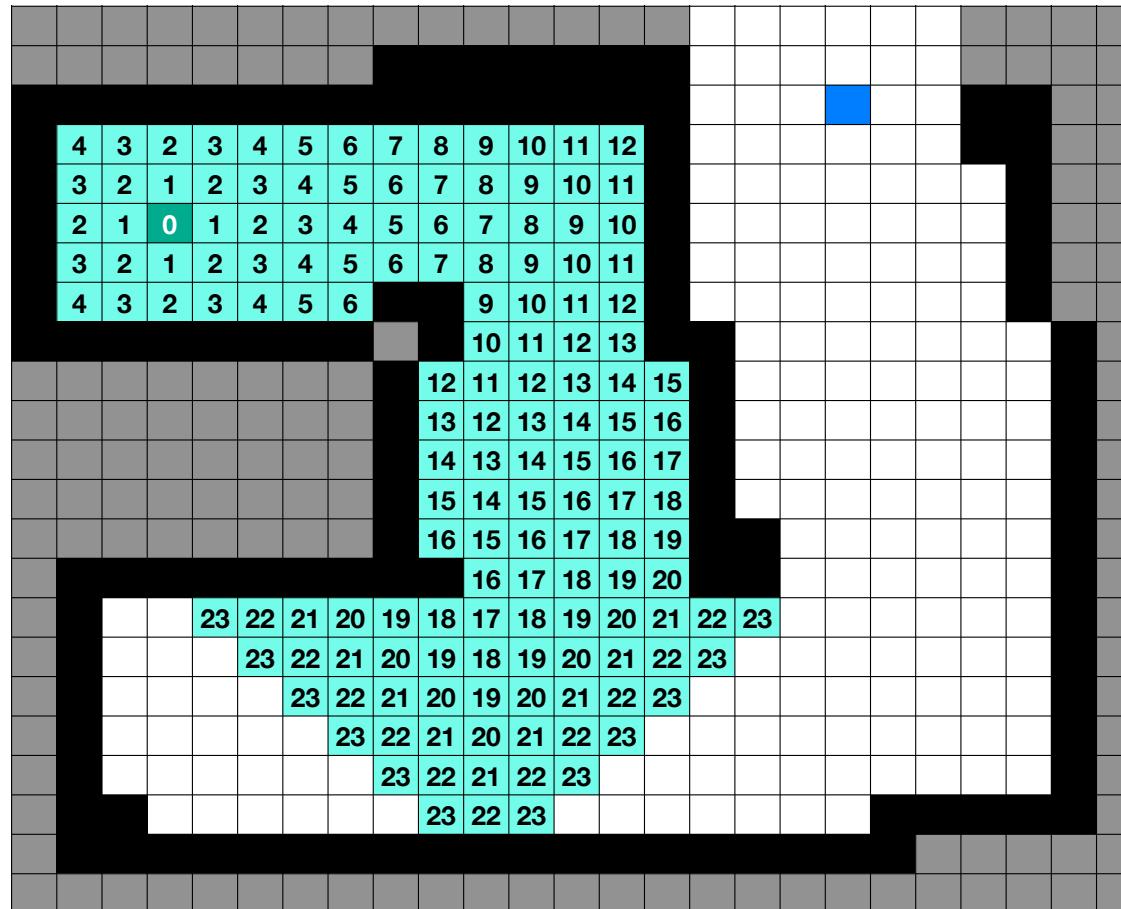
**Repeat for
next set of
neighbors**



**Then, visit the
neighbors of
nodes just
visited**

**Assign each
one plus the
smallest
distance**

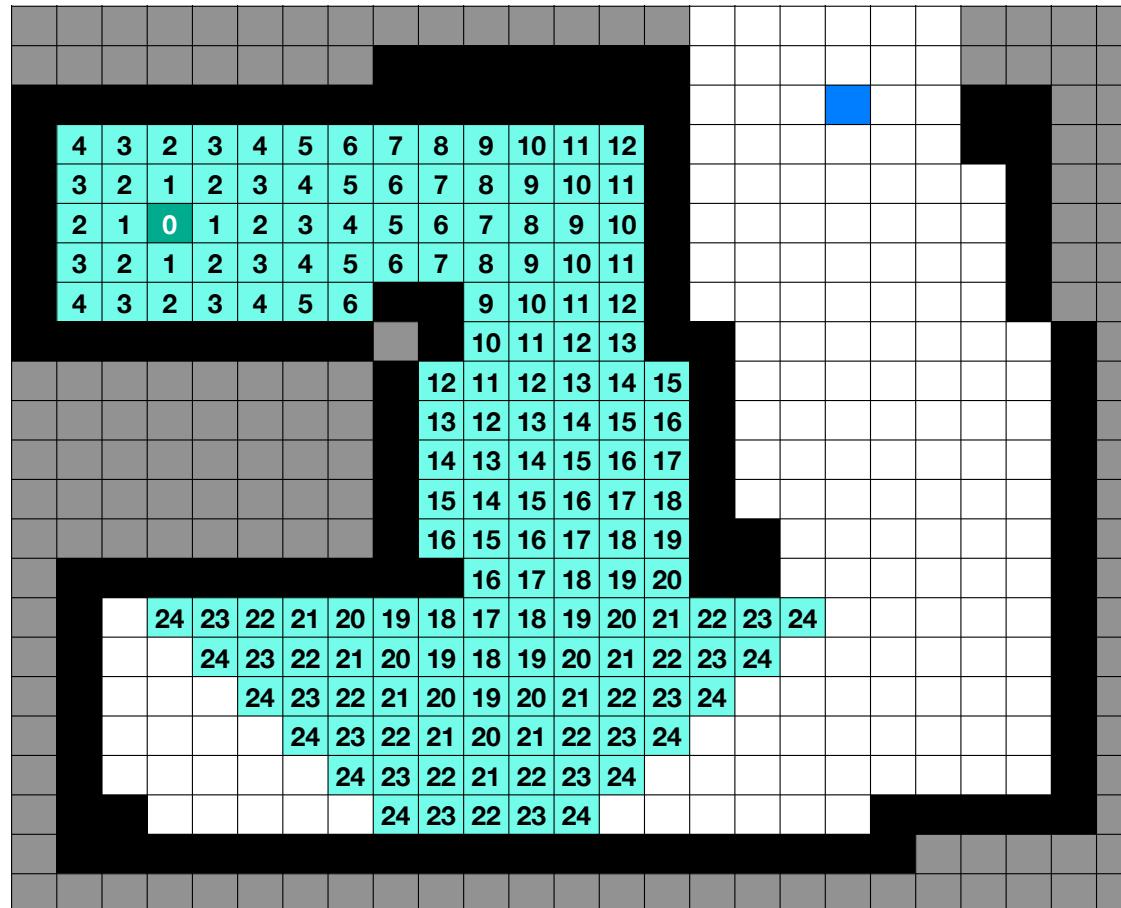
**Repeat for
next set of
neighbors**



**Then, visit the
neighbors of
nodes just
visited**

**Assign each
one plus the
smallest
distance**

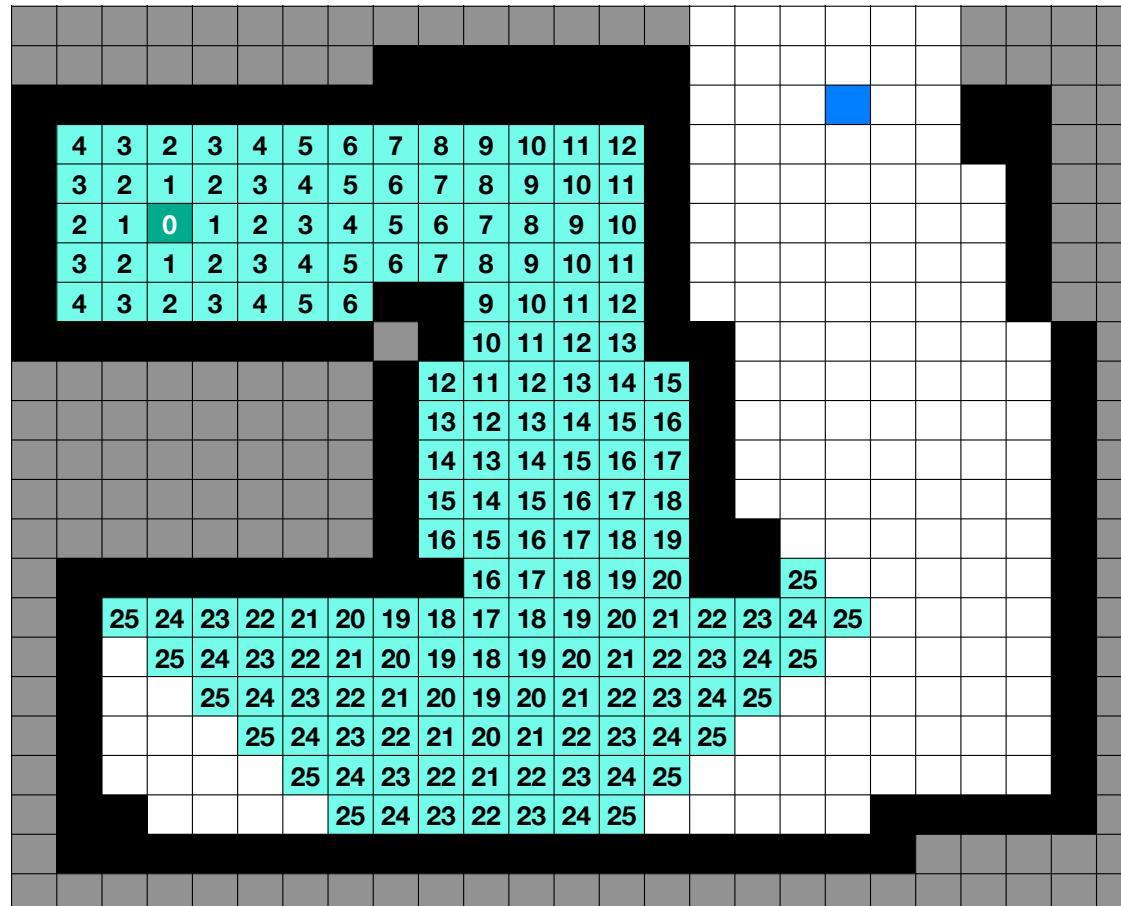
**Repeat for
next set of
neighbors**



**Then, visit the
neighbors of
nodes just
visited**

**Assign each
one plus the
smallest
distance**

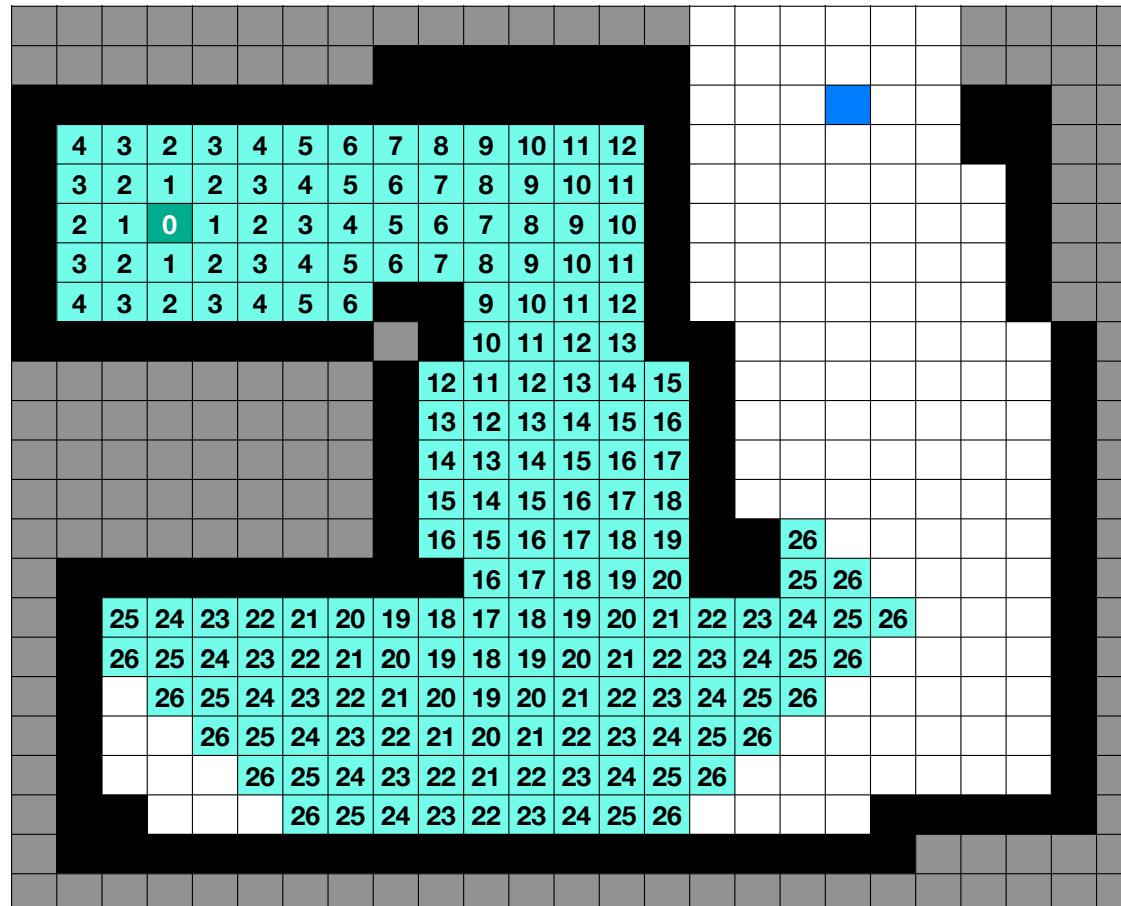
**Repeat for
next set of
neighbors**



**Then, visit the
neighbors of
nodes just
visited**

**Assign each
one plus the
smallest
distance**

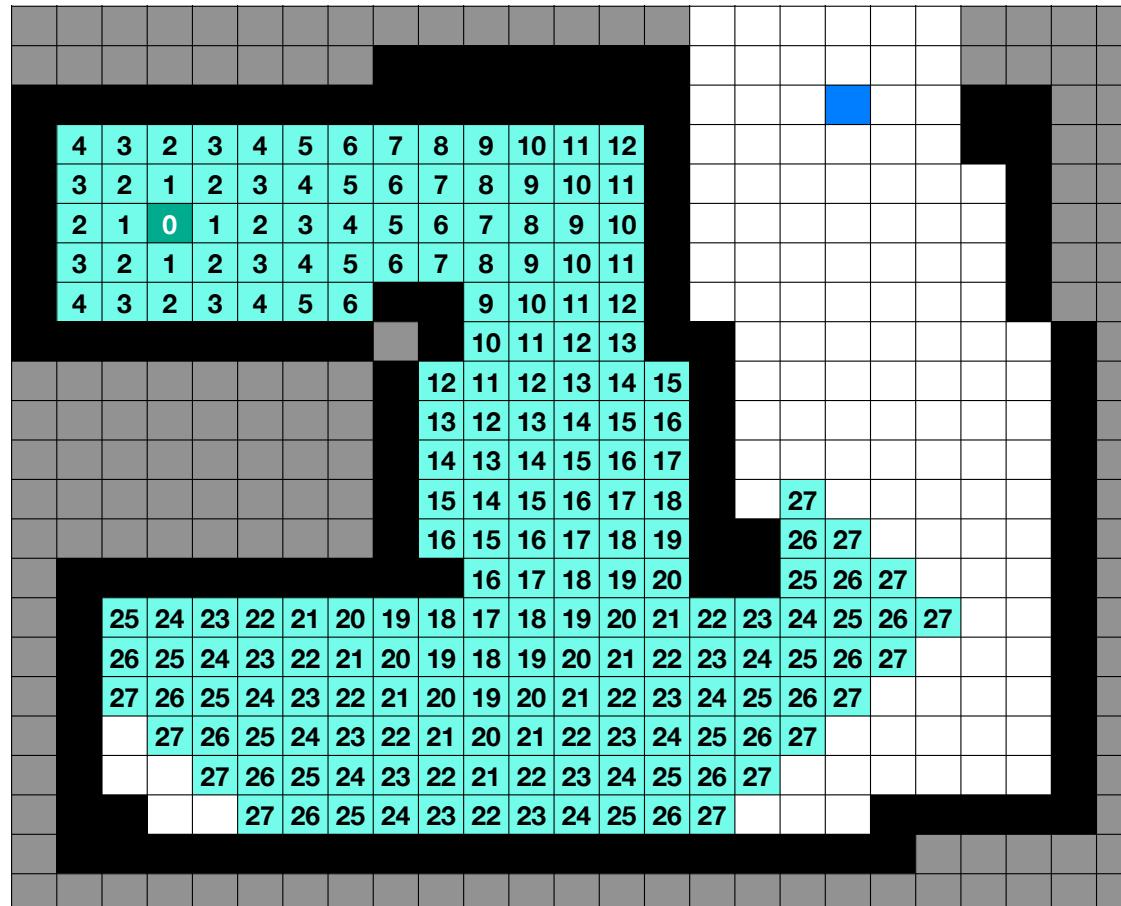
**Repeat for
next set of
neighbors**



**Then, visit the
neighbors of
nodes just
visited**

**Assign each
one plus the
smallest
distance**

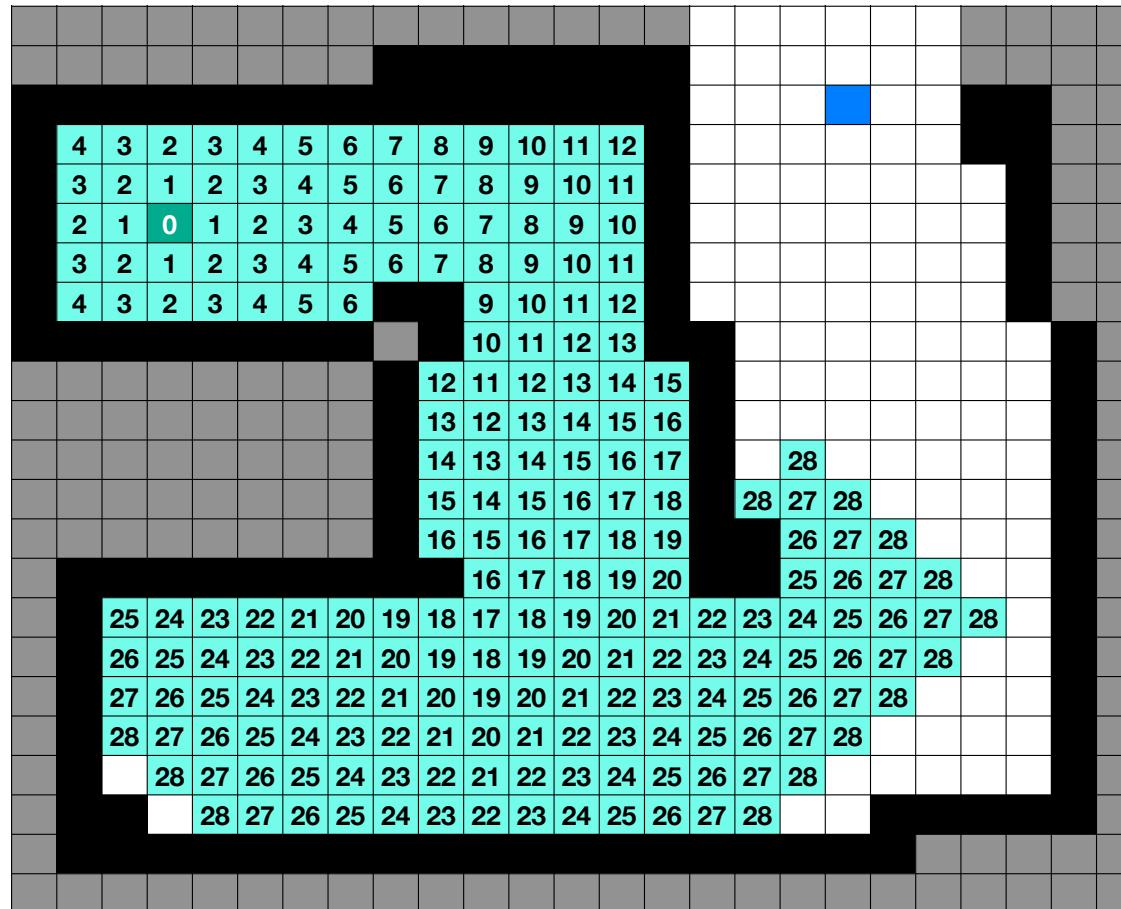
**Repeat for
next set of
neighbors**



**Then, visit the
neighbors of
nodes just
visited**

**Assign each
one plus the
smallest
distance**

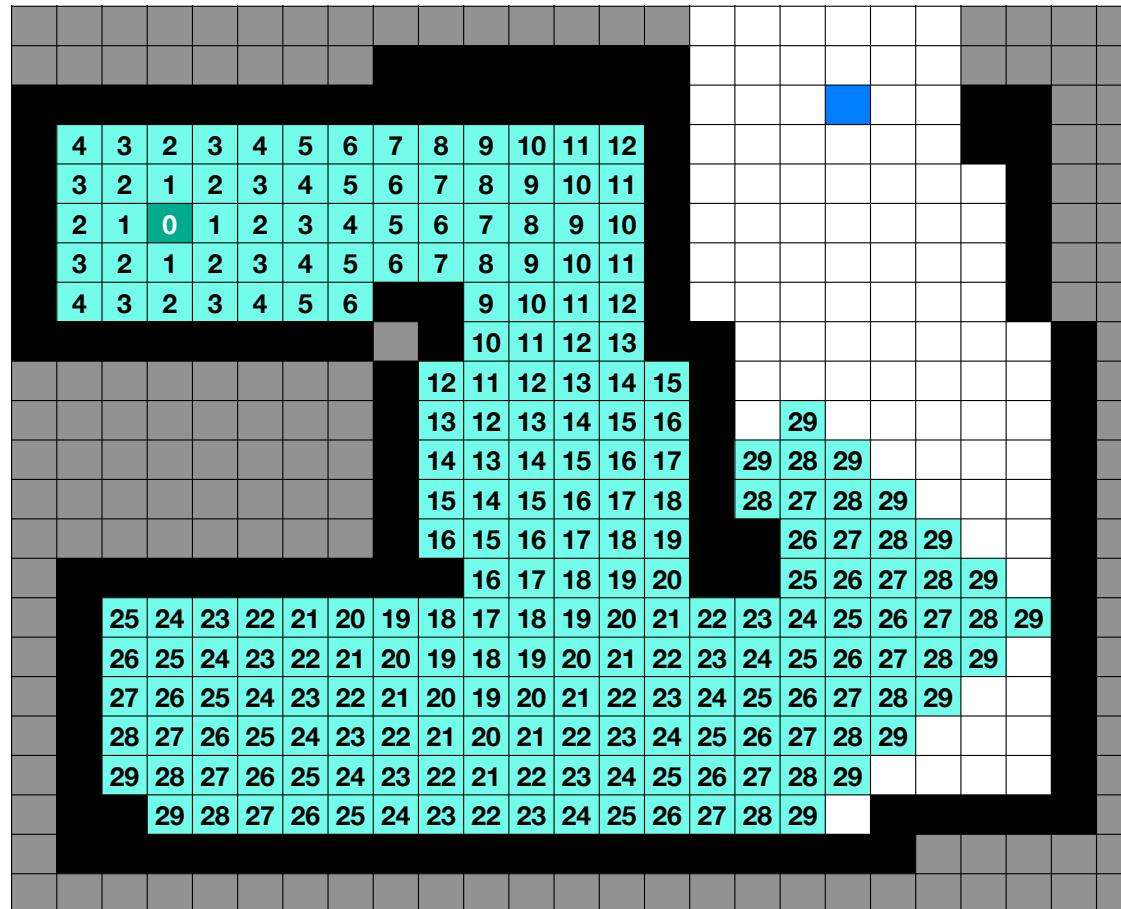
**Repeat for
next set of
neighbors**



**Then, visit the
neighbors of
nodes just
visited**

**Assign each
one plus the
smallest
distance**

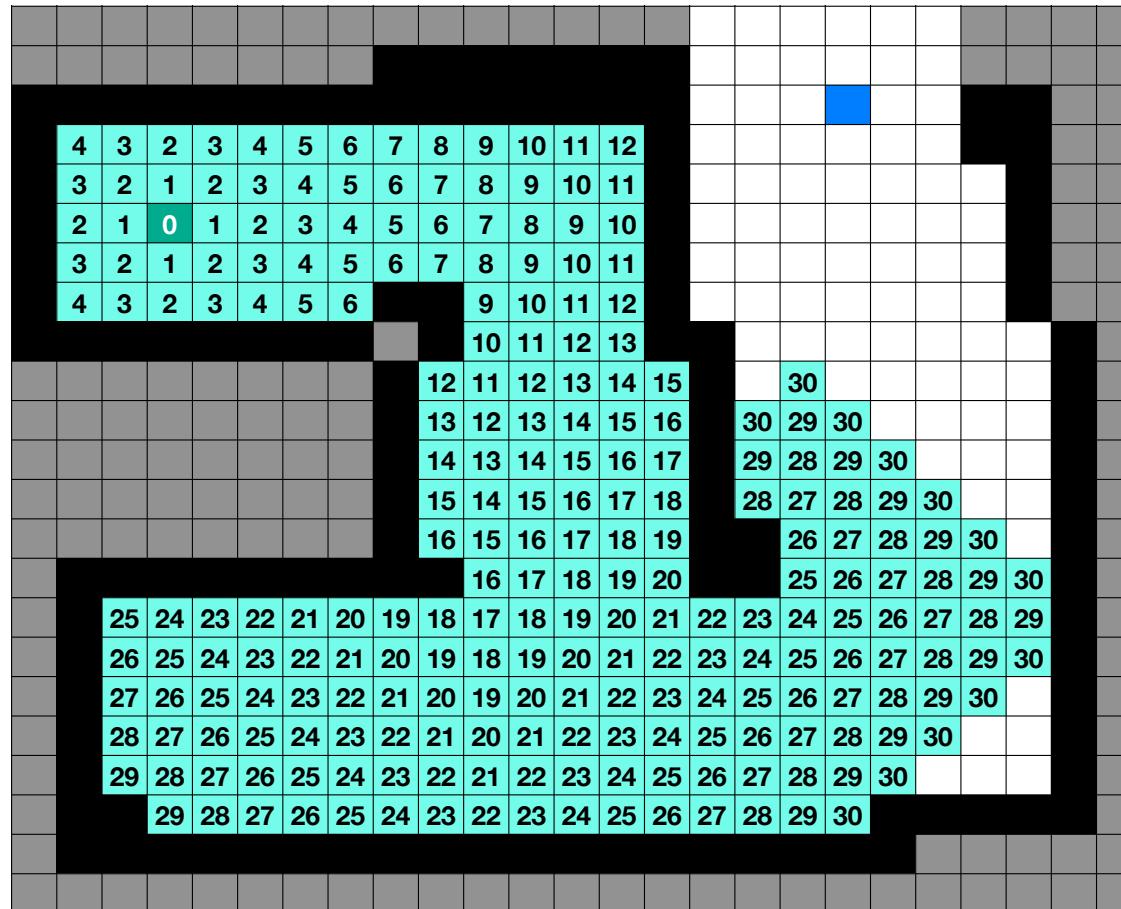
**Repeat for
next set of
neighbors**



**Then, visit the
neighbors of
nodes just
visited**

**Assign each
one plus the
smallest
distance**

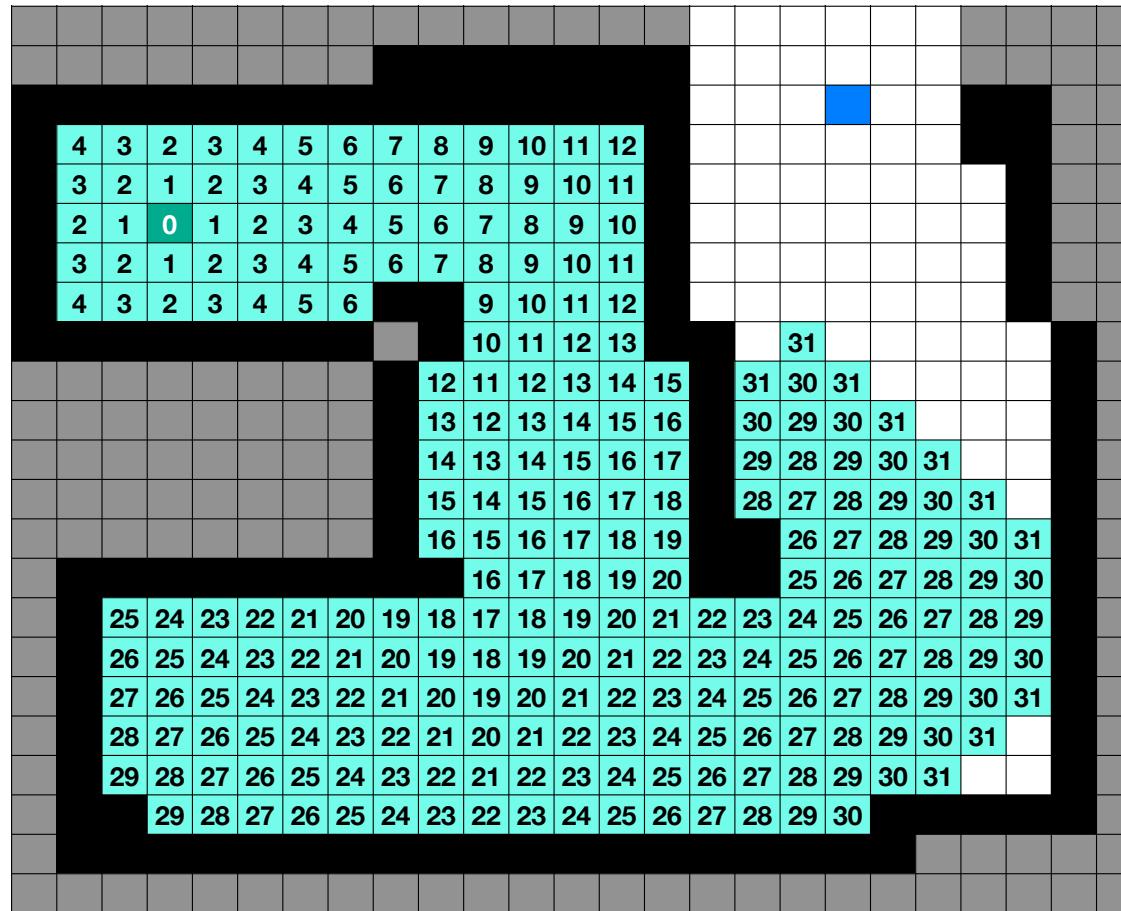
**Repeat for
next set of
neighbors**



**Then, visit the
neighbors of
nodes just
visited**

**Assign each
one plus the
smallest
distance**

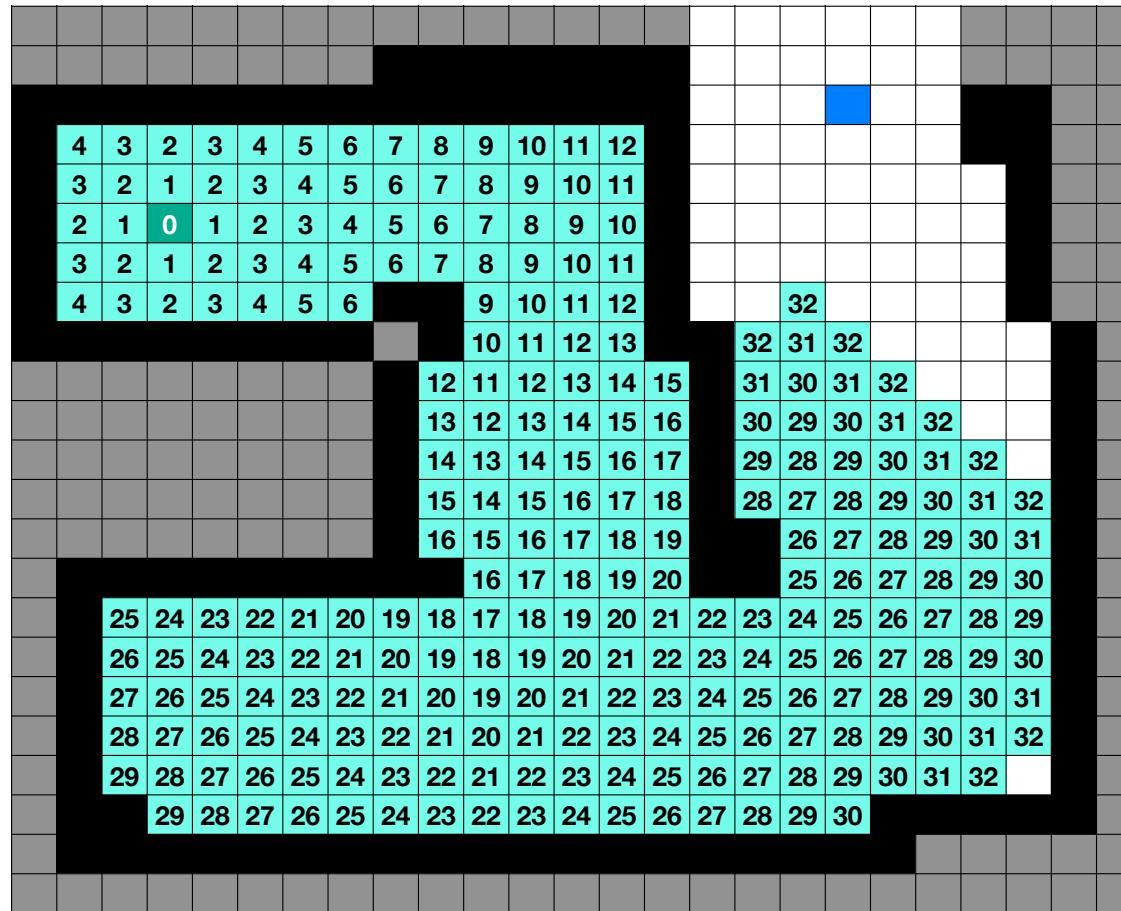
**Repeat for
next set of
neighbors**



**Then, visit the
neighbors of
nodes just
visited**

**Assign each
one plus the
smallest
distance**

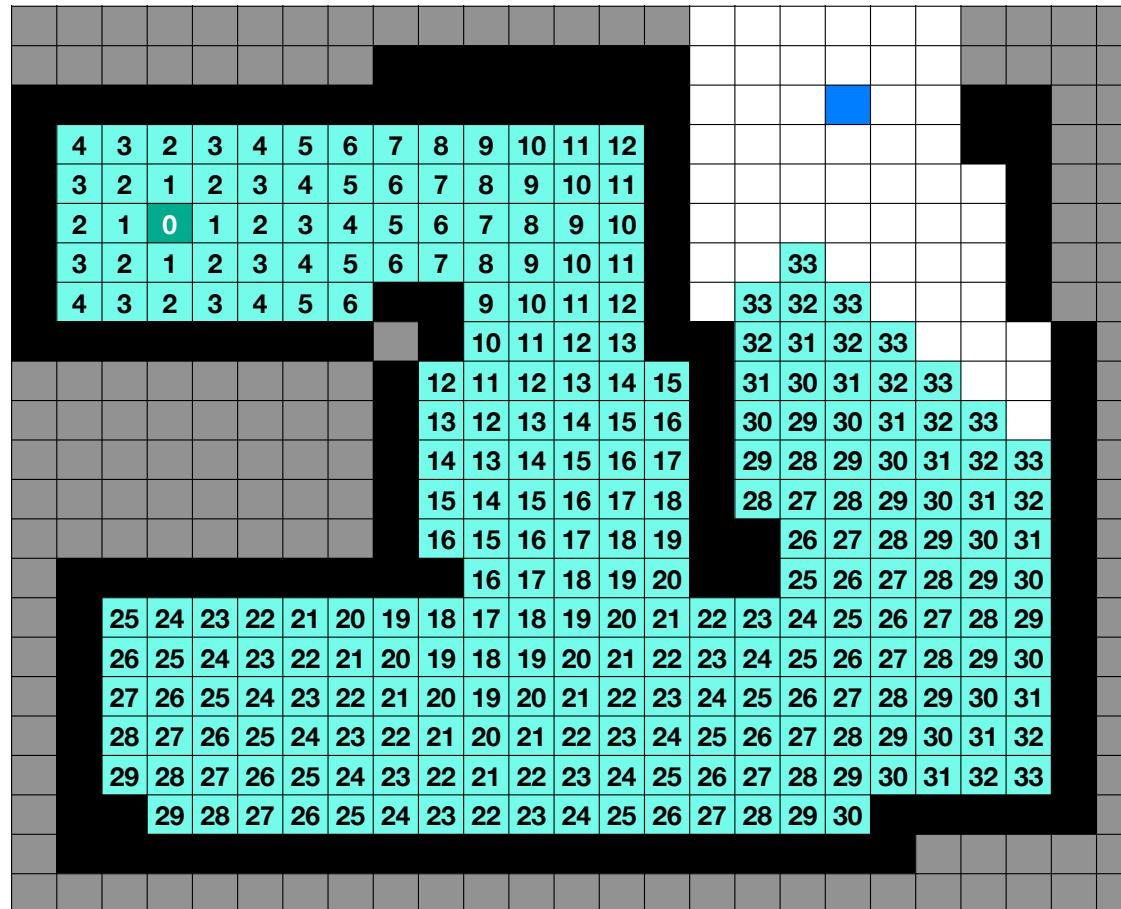
**Repeat for
next set of
neighbors**



**Then, visit the
neighbors of
nodes just
visited**

**Assign each
one plus the
smallest
distance**

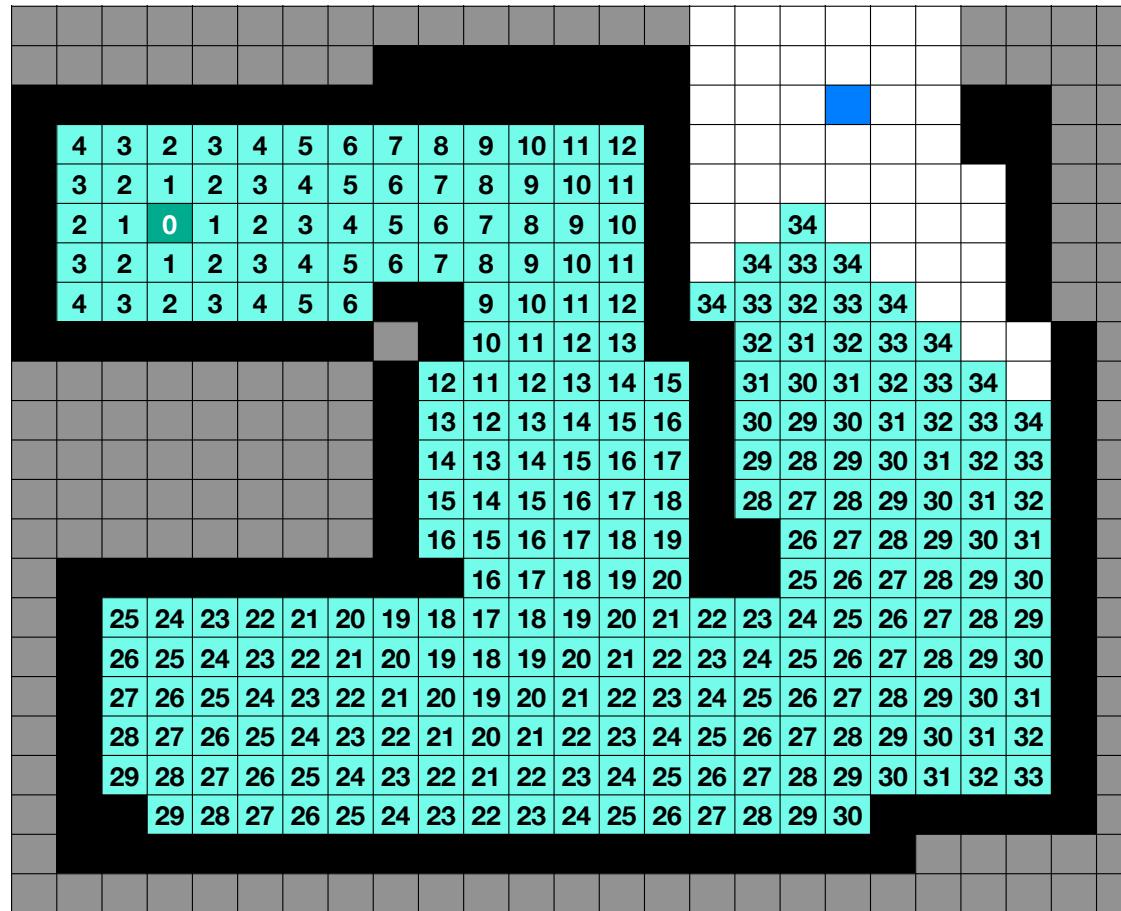
**Repeat for
next set of
neighbors**



**Then, visit the
neighbors of
nodes just
visited**

**Assign each
one plus the
smallest
distance**

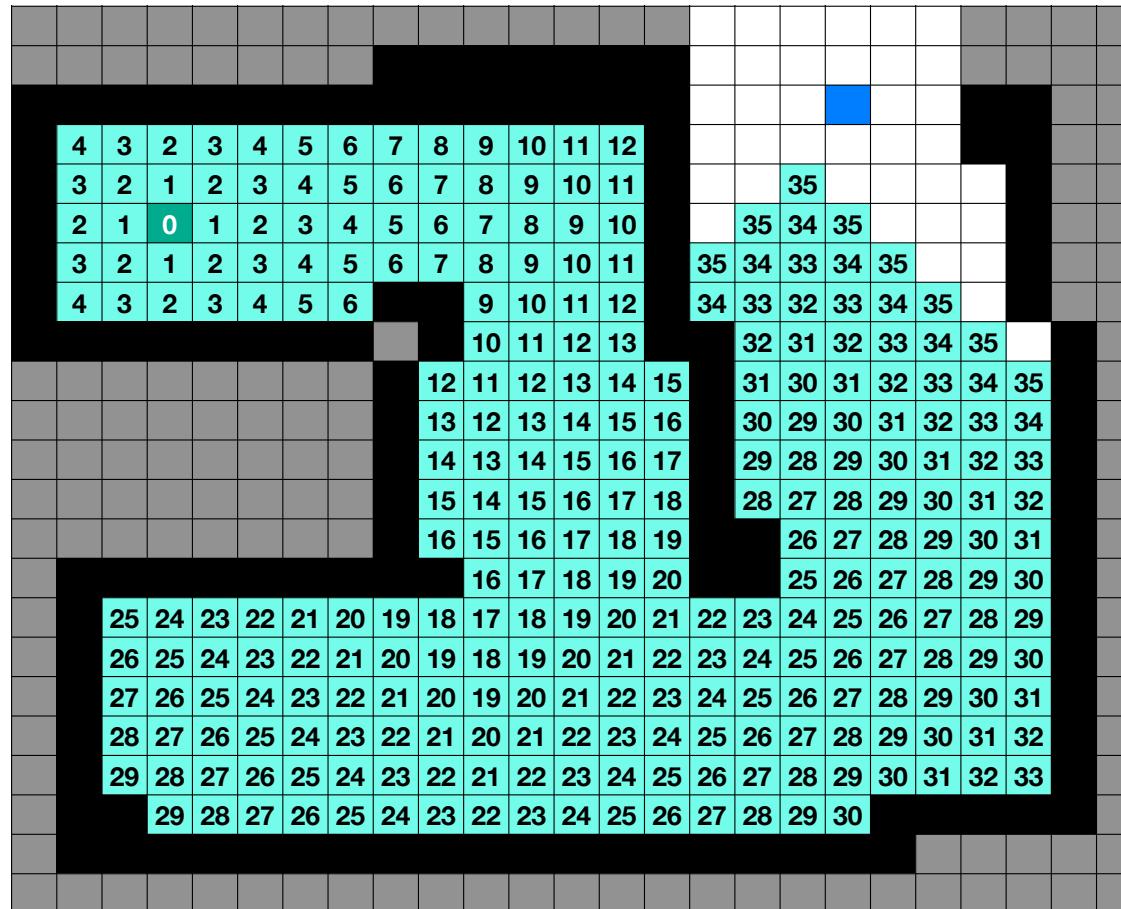
**Repeat for
next set of
neighbors**



**Then, visit the
neighbors of
nodes just
visited**

**Assign each
one plus the
smallest
distance**

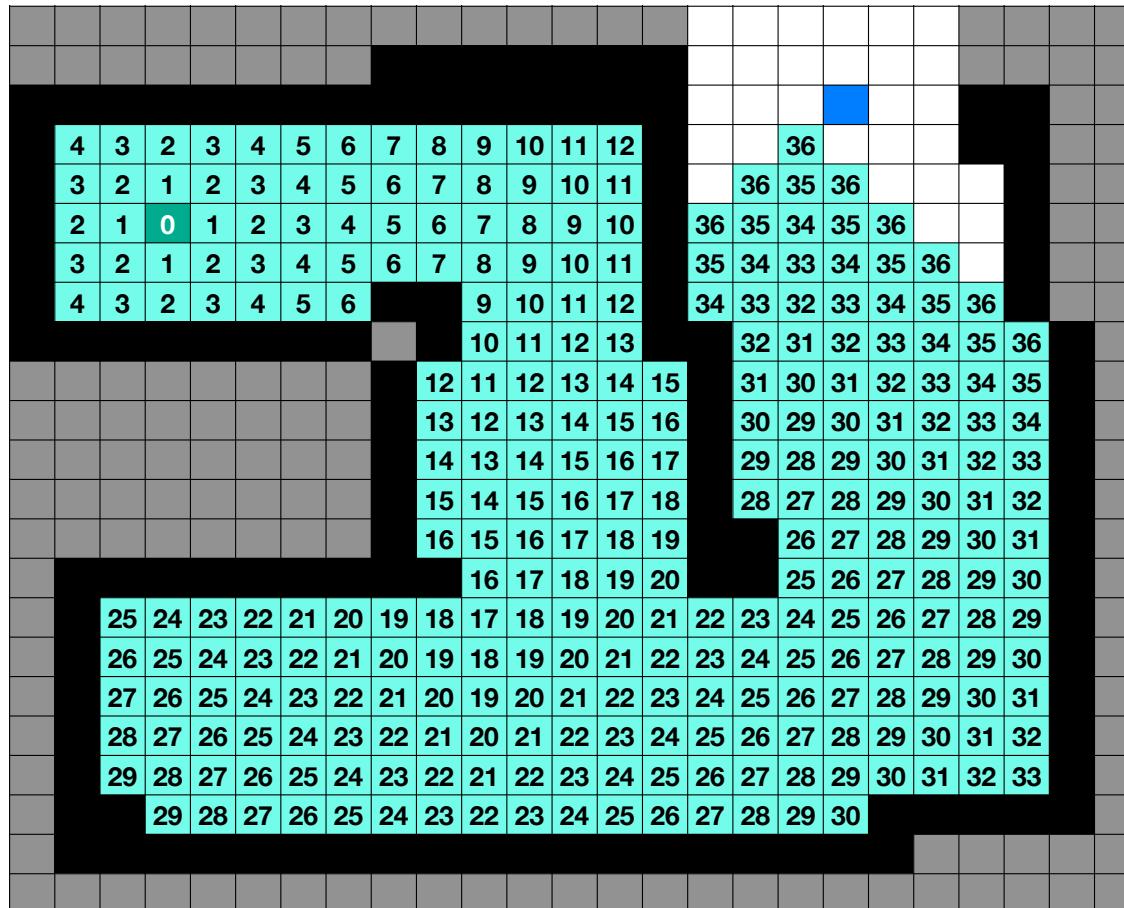
**Repeat for
next set of
neighbors**



**Then, visit the
neighbors of
nodes just
visited**

**Assign each
one plus the
smallest
distance**

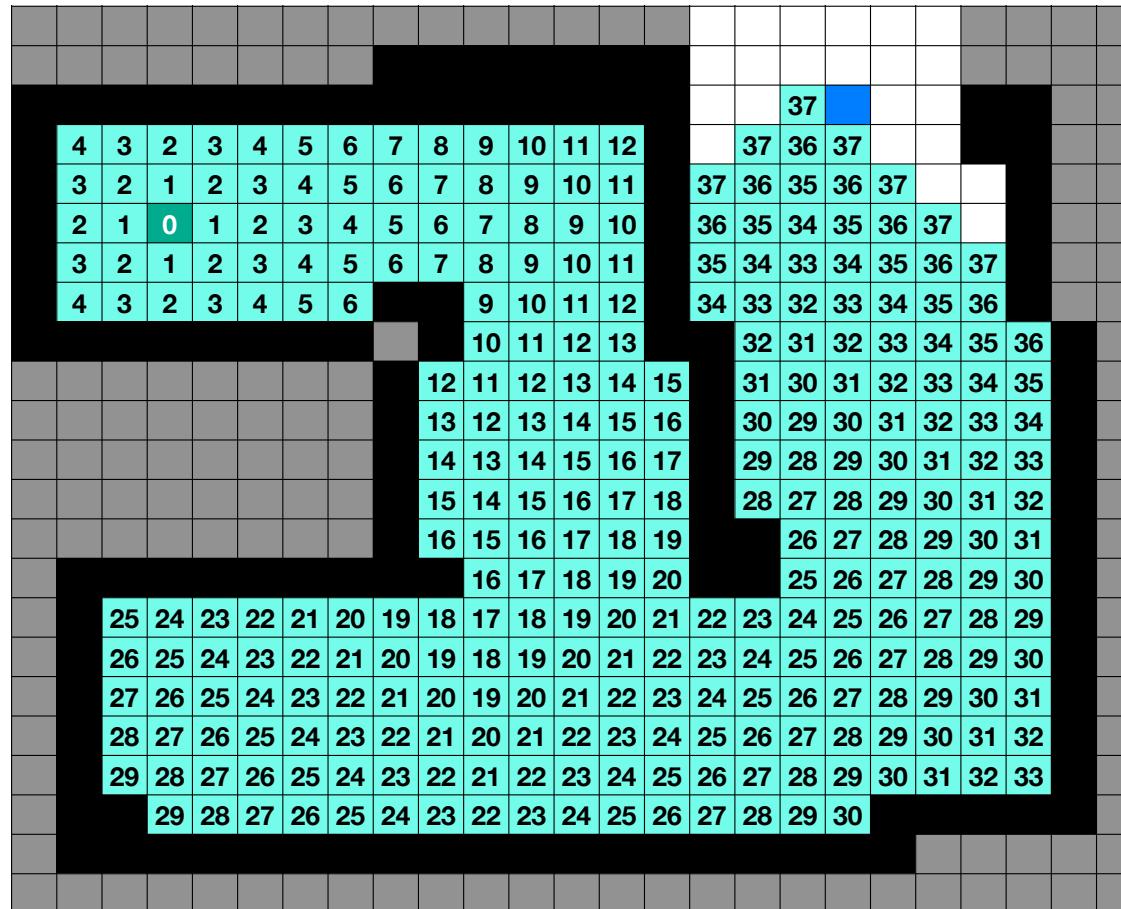
**Repeat for
next set of
neighbors**



**Then, visit the
neighbors of
nodes just
visited**

**Assign each
one plus the
smallest
distance**

**Repeat for
next set of
neighbors**

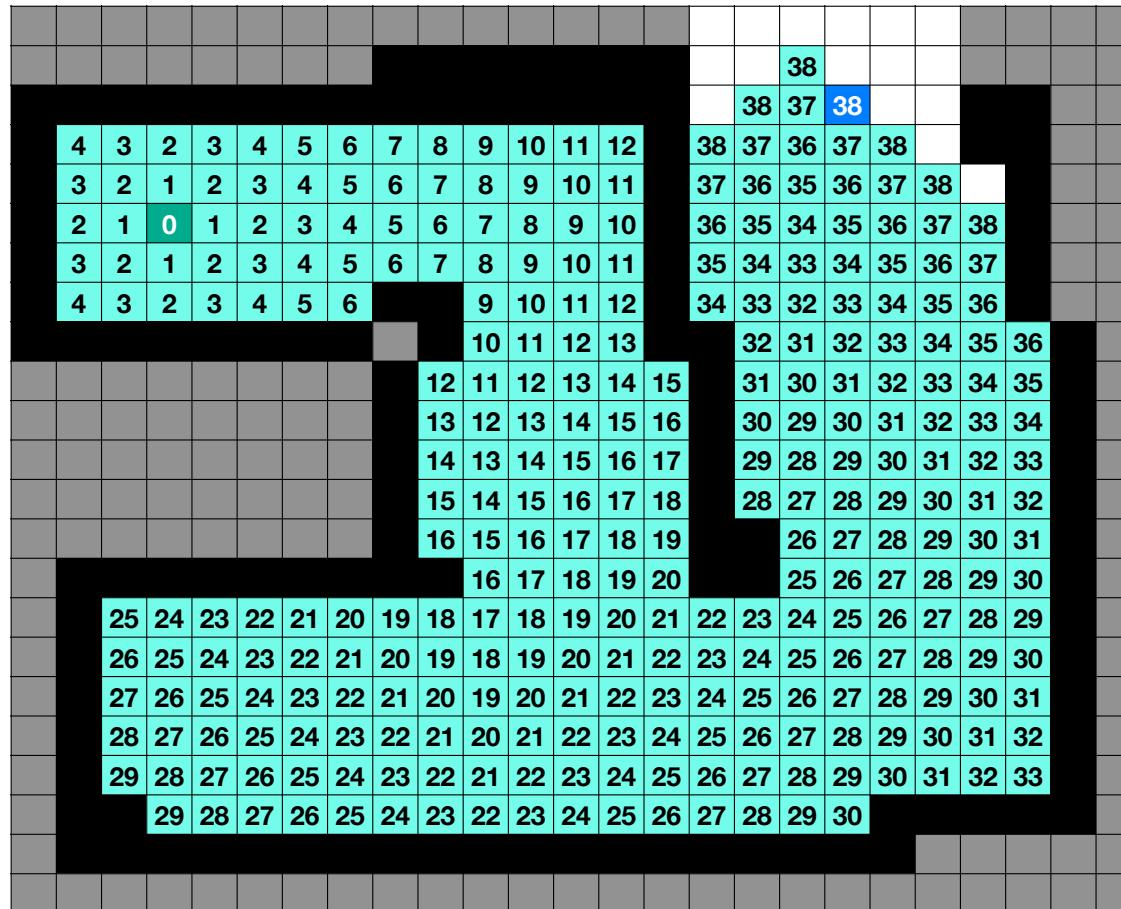


Then, visit the neighbors of nodes just visited

Assign each one plus the smallest distance

Repeat for next set of neighbors

Once goal node reached, perform local search back to start

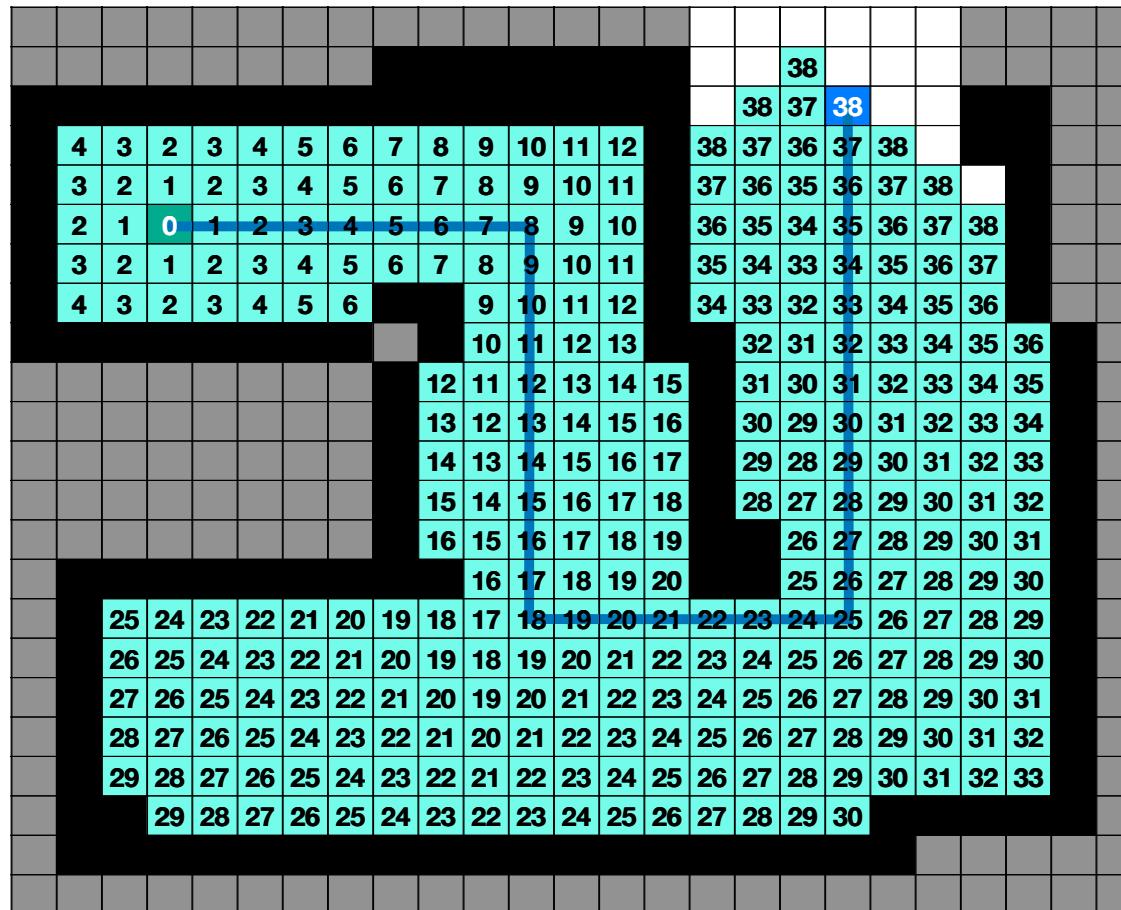


Then, visit the neighbors of nodes just visited

Assign each one plus the smallest distance

Repeat for next set of neighbors

Once goal node reached, perform local search back to start



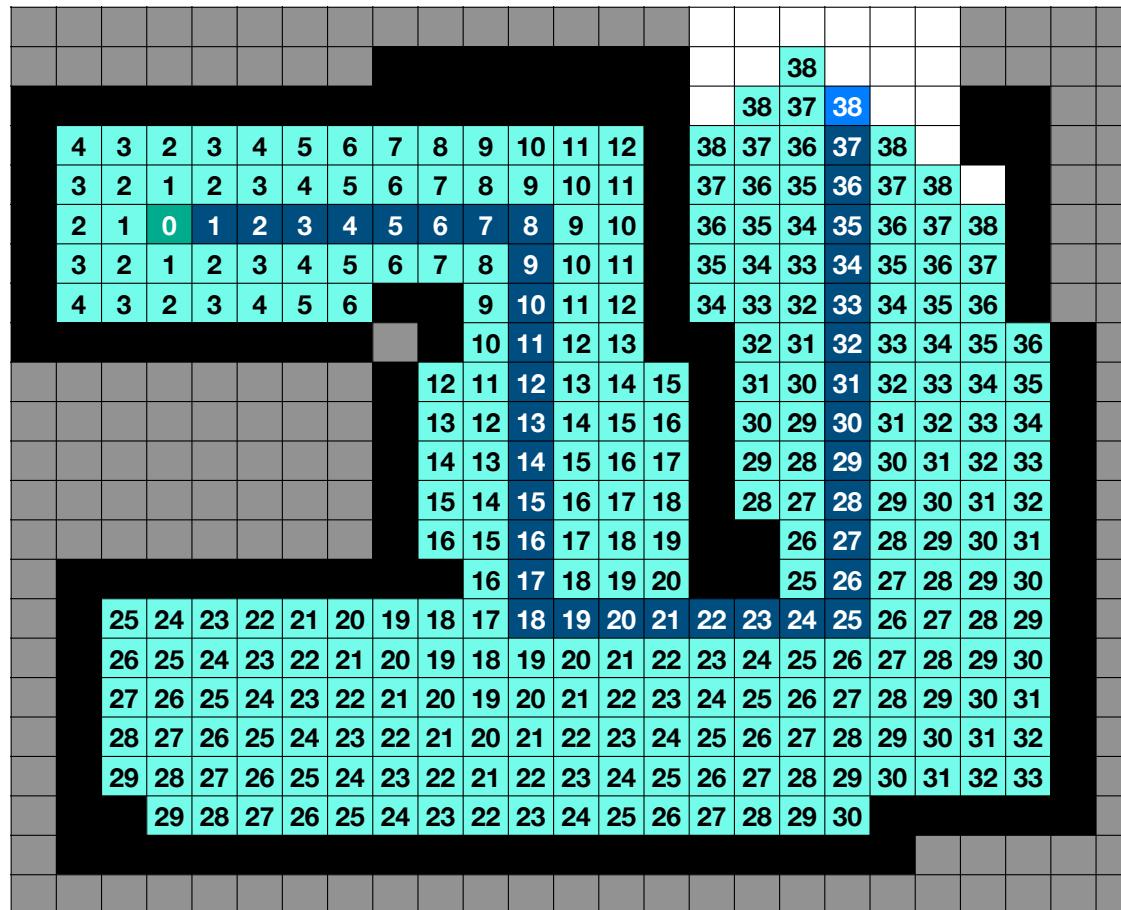
Then, visit the neighbors of nodes just visited

Assign each one plus the smallest distance

Repeat for next set of neighbors

Once goal node reached, perform local search back to start

Assign parents along path in decreasing order



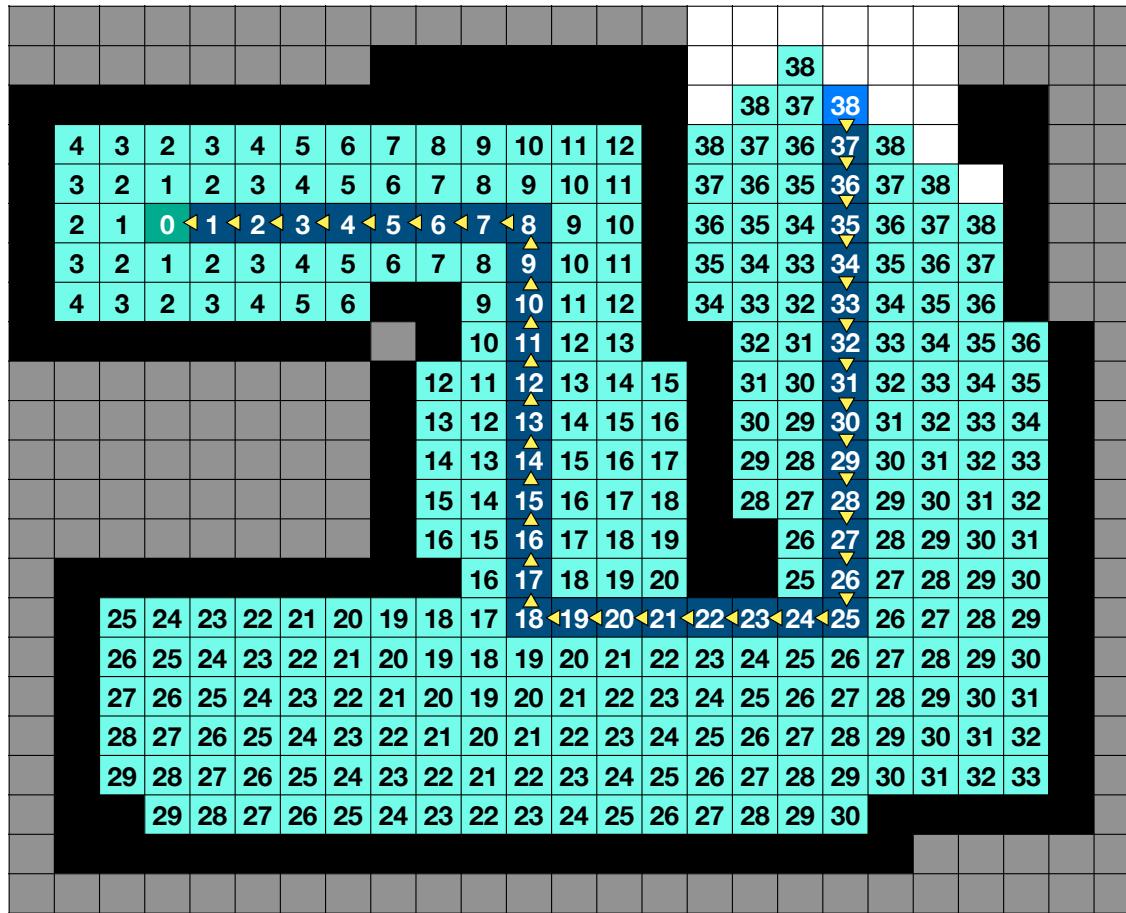
Then, visit the neighbors of nodes just visited

Assign each one plus the smallest distance

Repeat for next set of neighbors

Once goal node reached, perform local search back to start

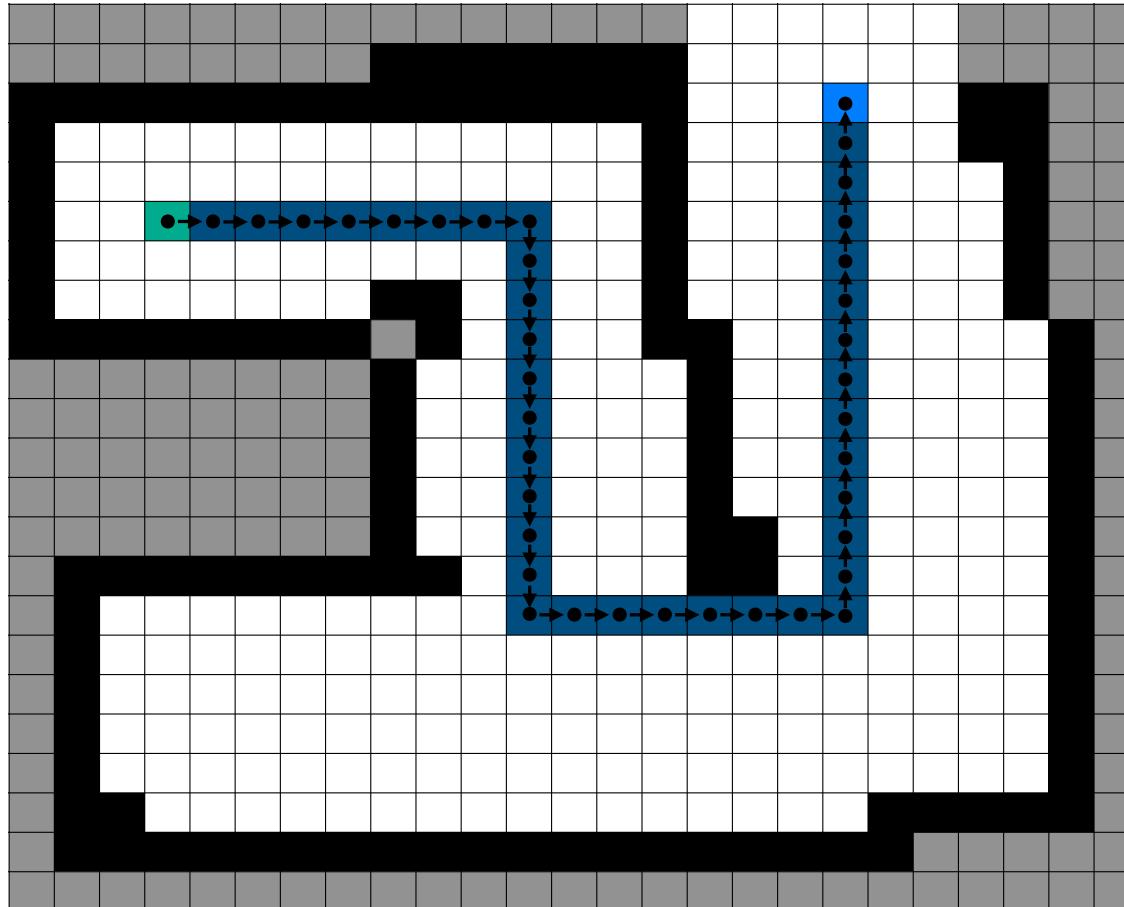
Assign parents along path in decreasing order



Then, visit the neighbors of nodes just visited

Assign each one plus the smallest distance

Repeat for next set of neighbors



Once goal node reached, perform local search back to start

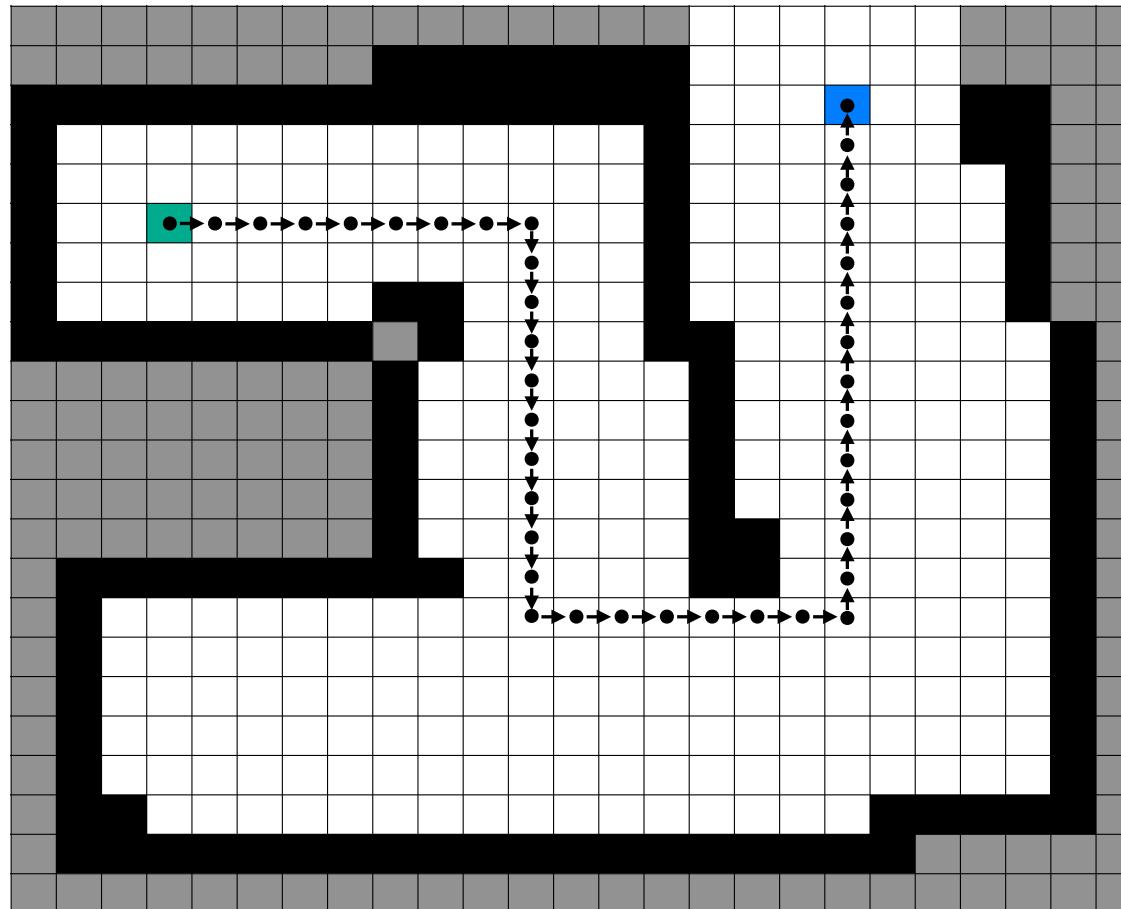
Assign parents along path in decreasing order

Form list of navigation waypoints

Then, visit the neighbors of nodes just visited

Assign each one plus the smallest distance

Repeat for next set of neighbors



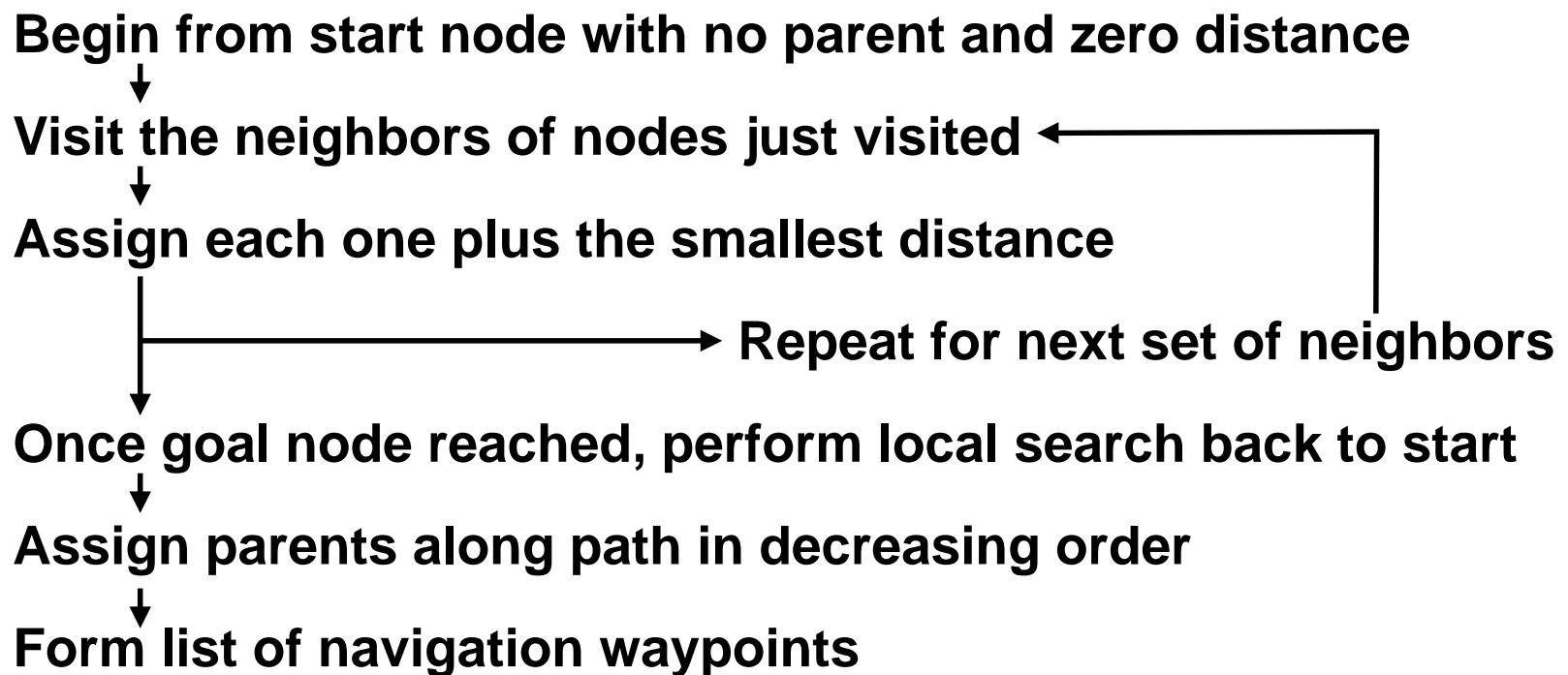
Once goal node reached, perform local search back to start

Assign parents along path in decreasing order

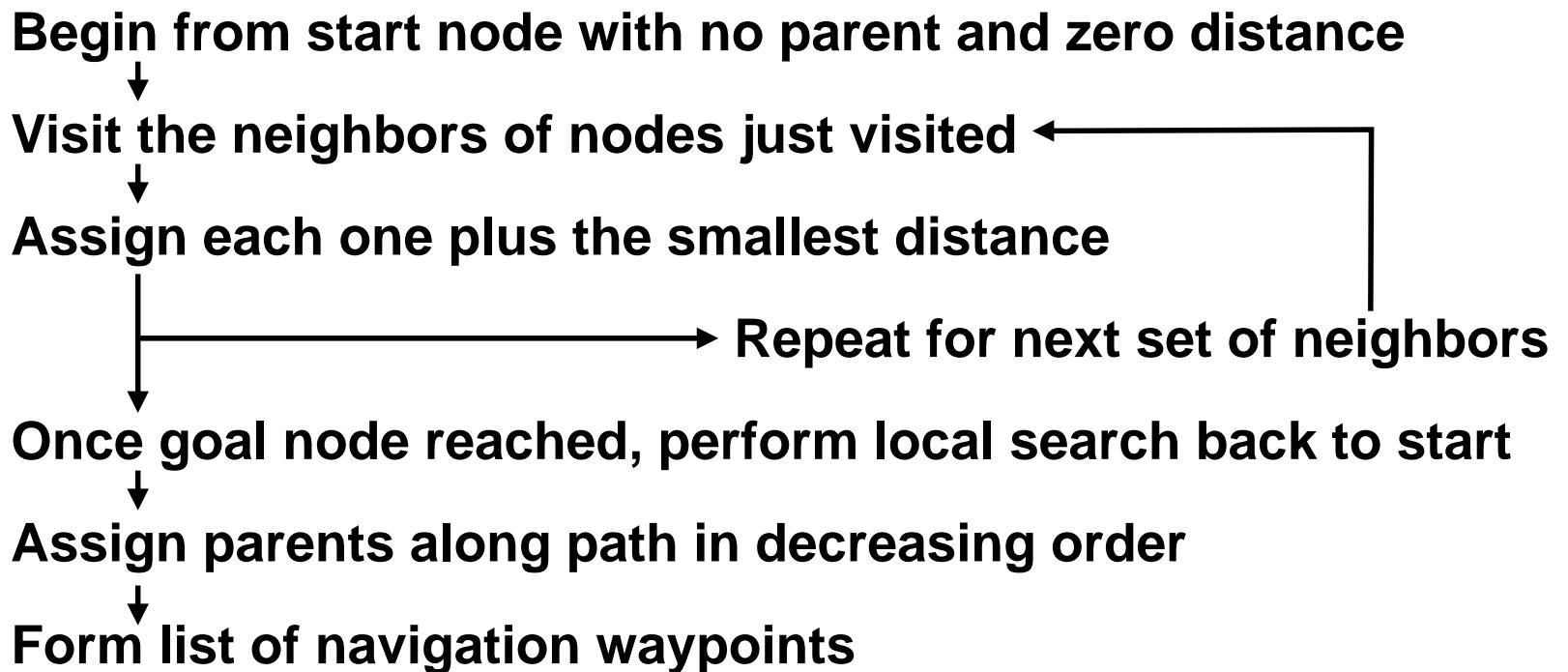
Form list of navigation waypoints

Global search to find routing

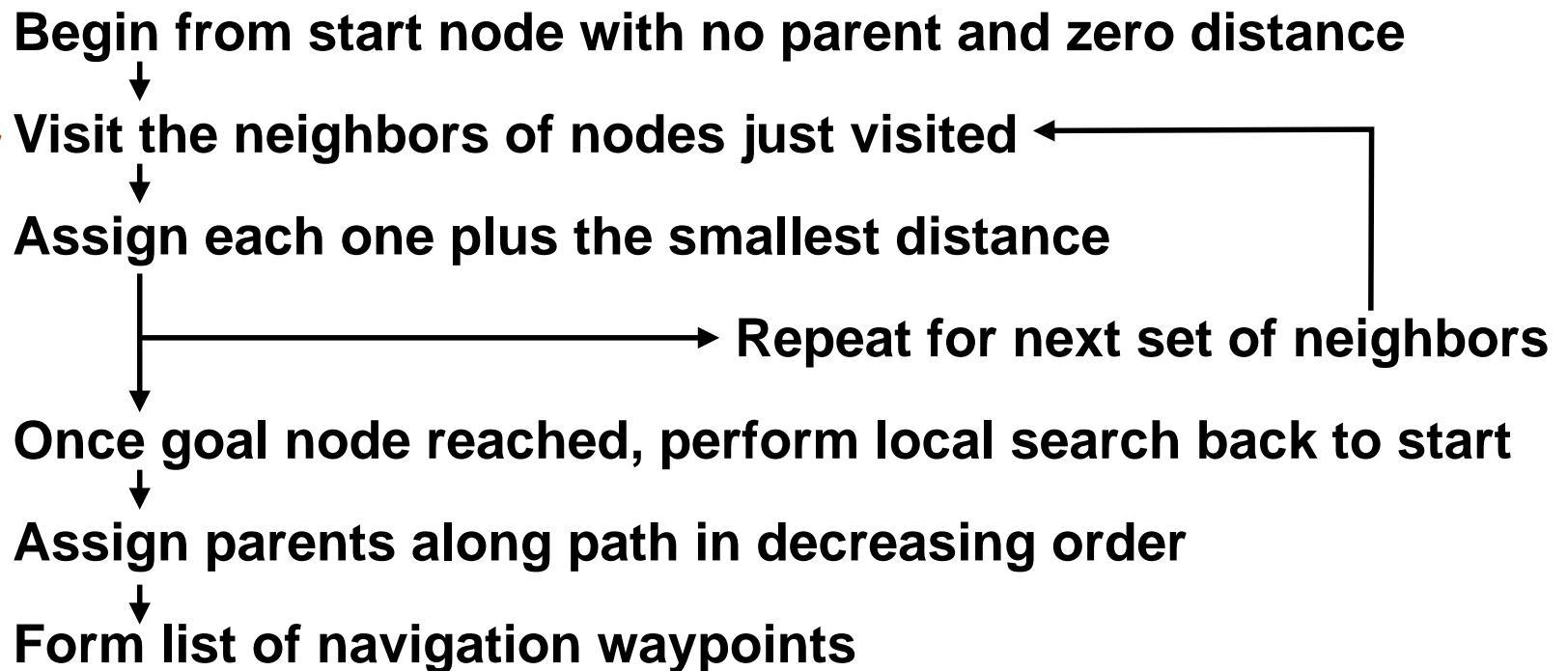
Does this search algorithm have a name ?



Brushfire Algorithm

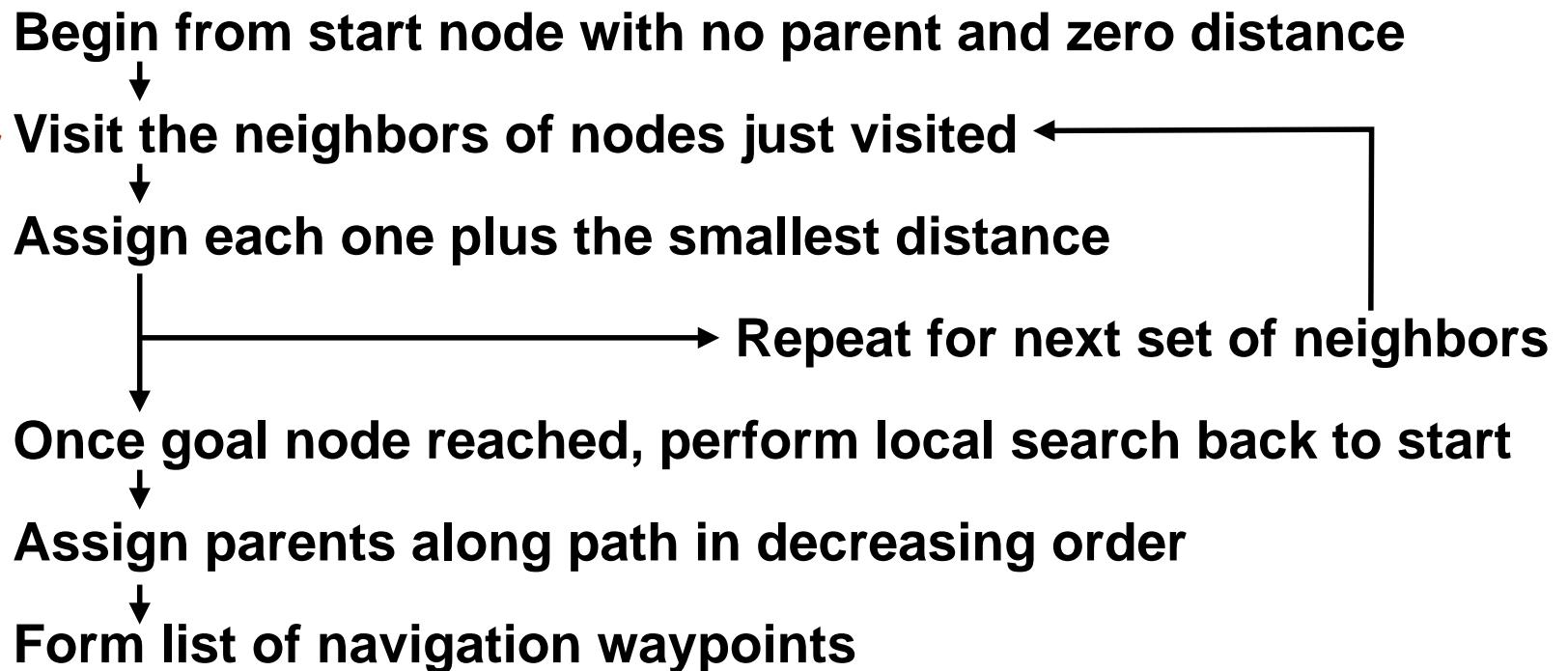


Brushfire Algorithm



How to keep track of visited nodes?

Brushfire Algorithm

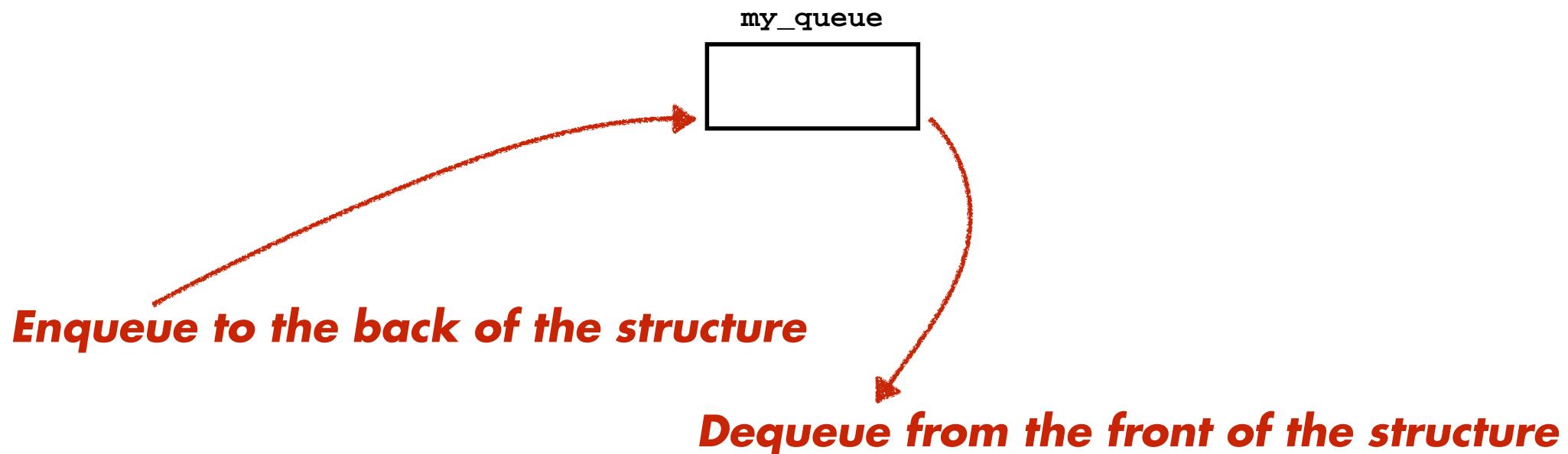


How to keep track of visited nodes?

Queue data structure

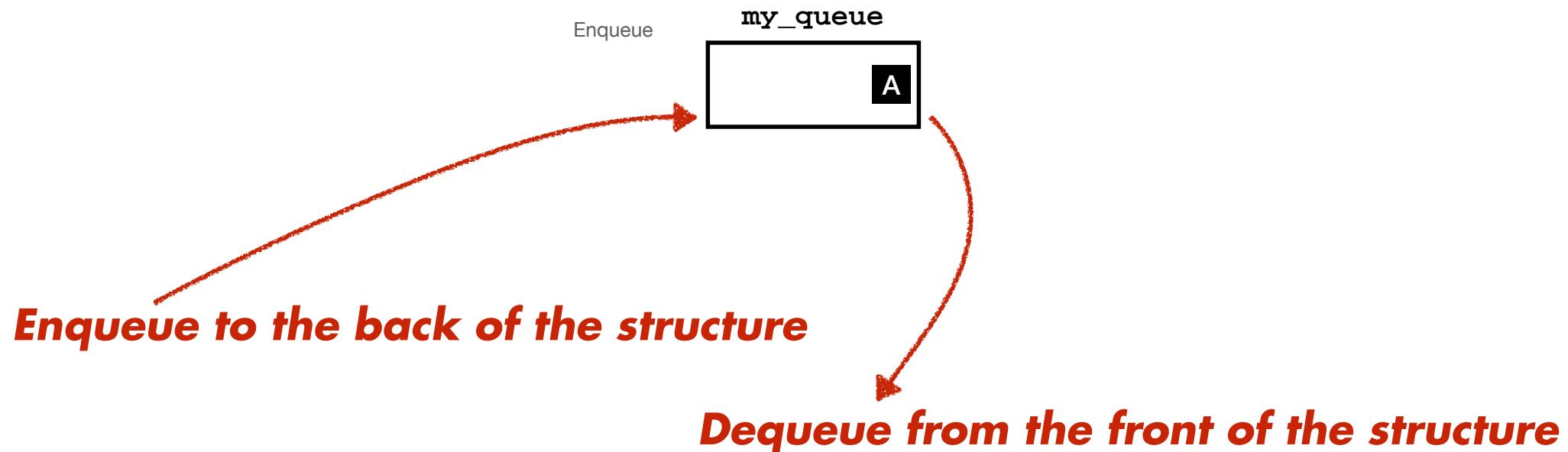
Queue data structure

"First in, first out" (FIFO) data structure



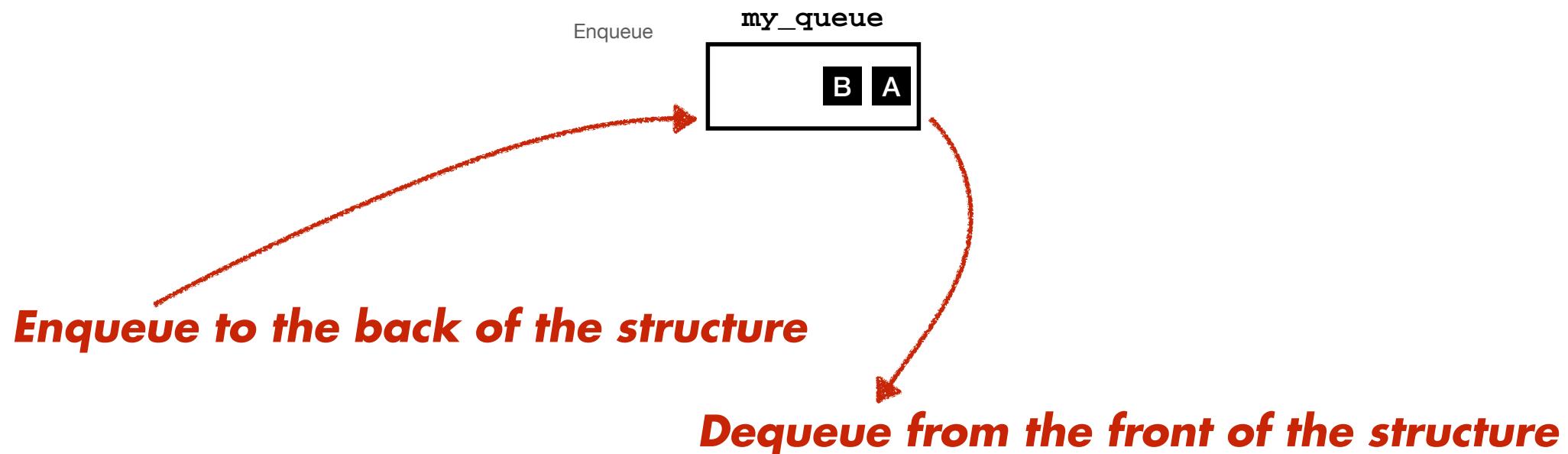
Queue data structure

"First in, first out" (FIFO) data structure



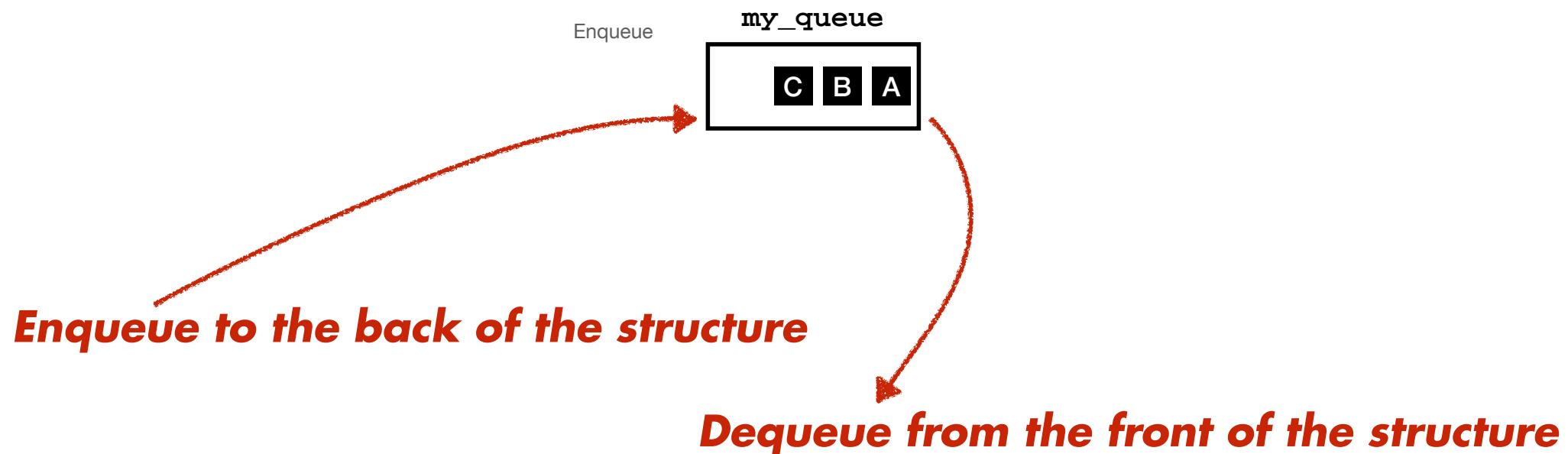
Queue data structure

"First in, first out" (FIFO) data structure



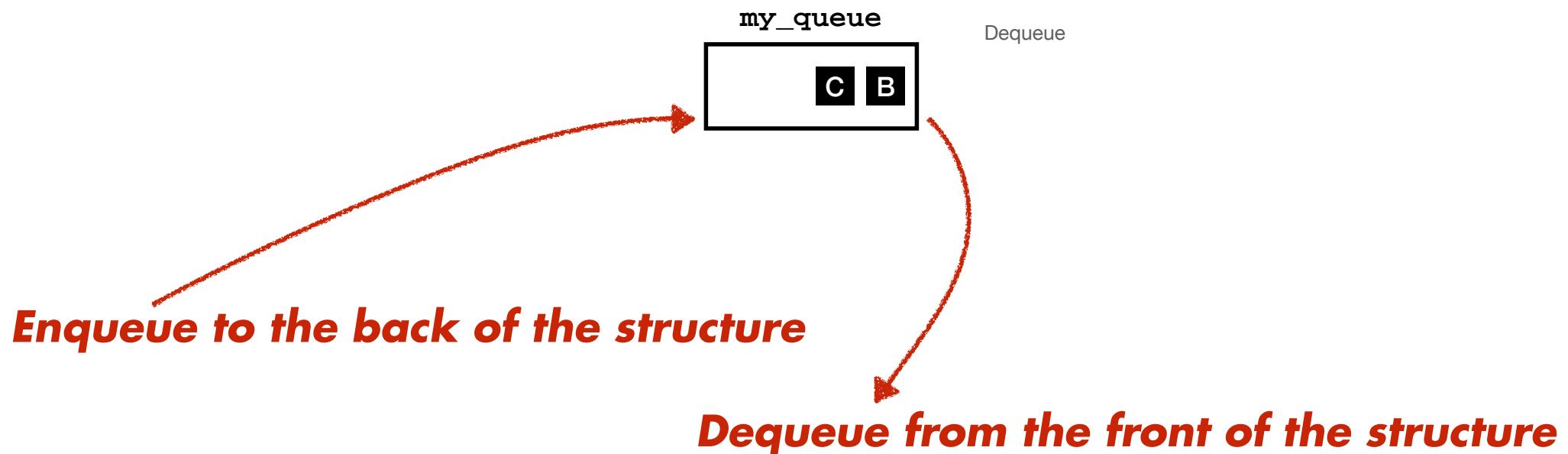
Queue data structure

"First in, first out" (FIFO) data structure



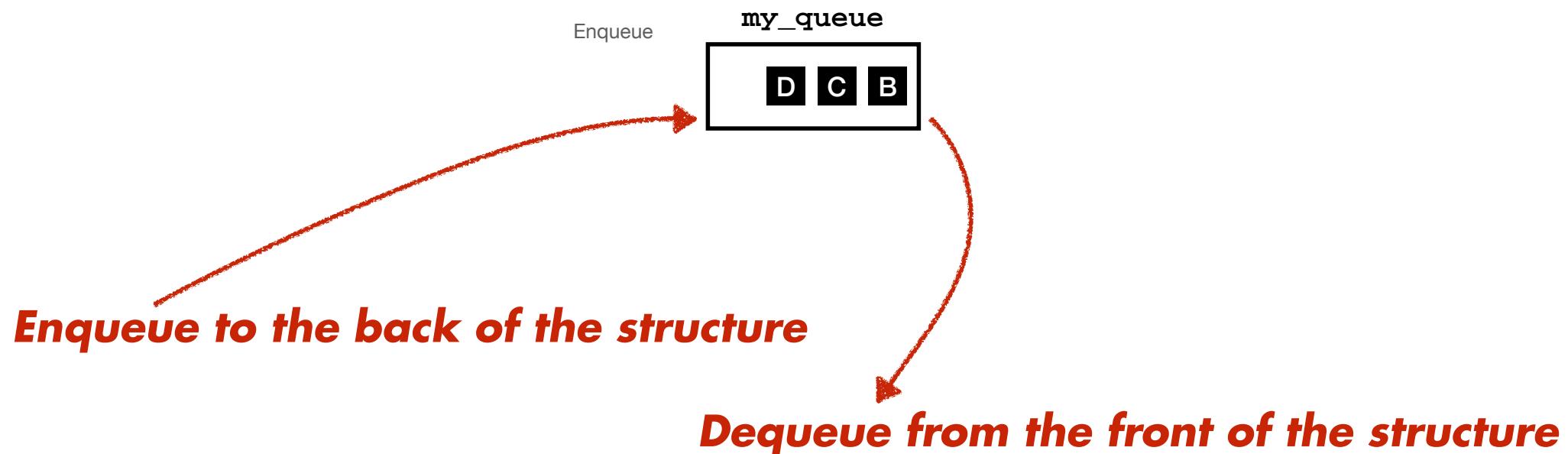
Queue data structure

"First in, first out" (FIFO) data structure



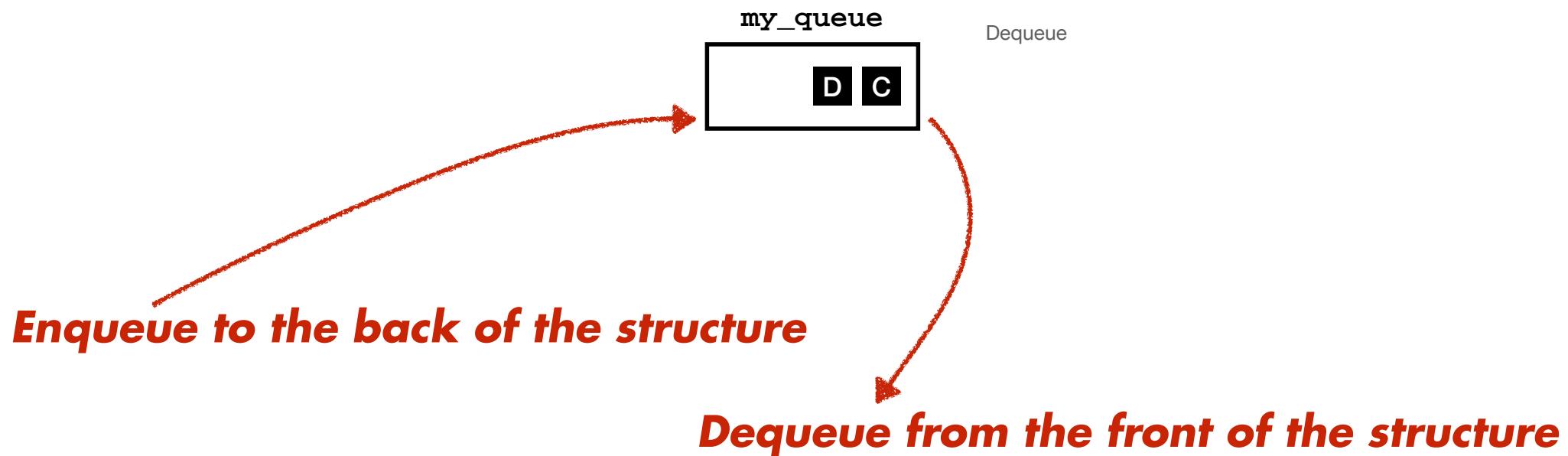
Queue data structure

"First in, first out" (FIFO) data structure



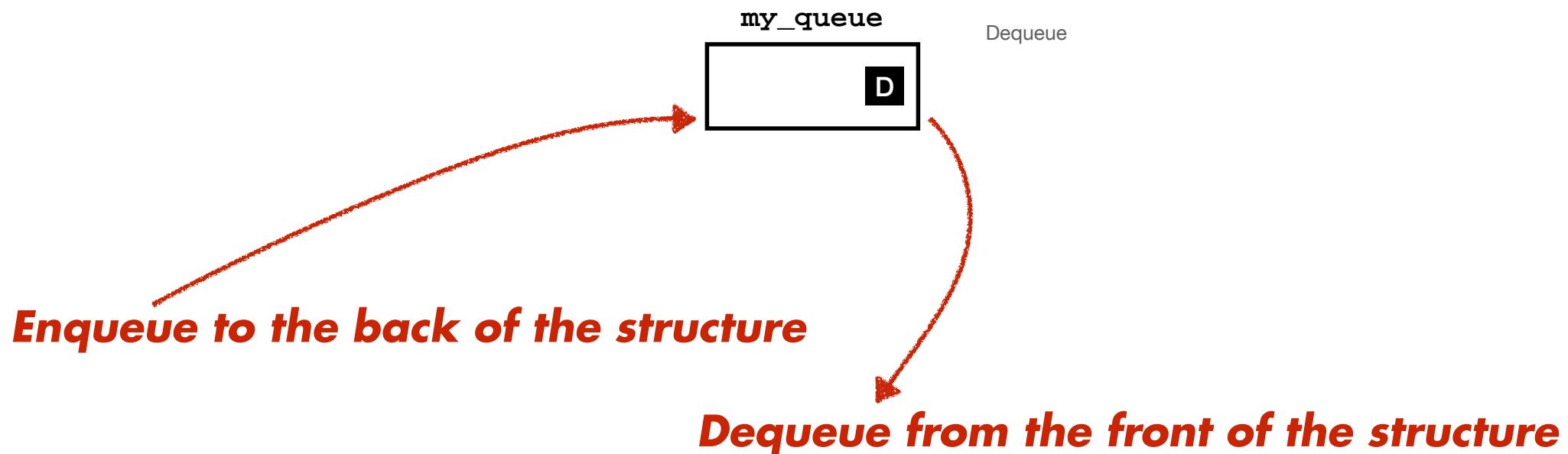
Queue data structure

"First in, first out" (FIFO) data structure



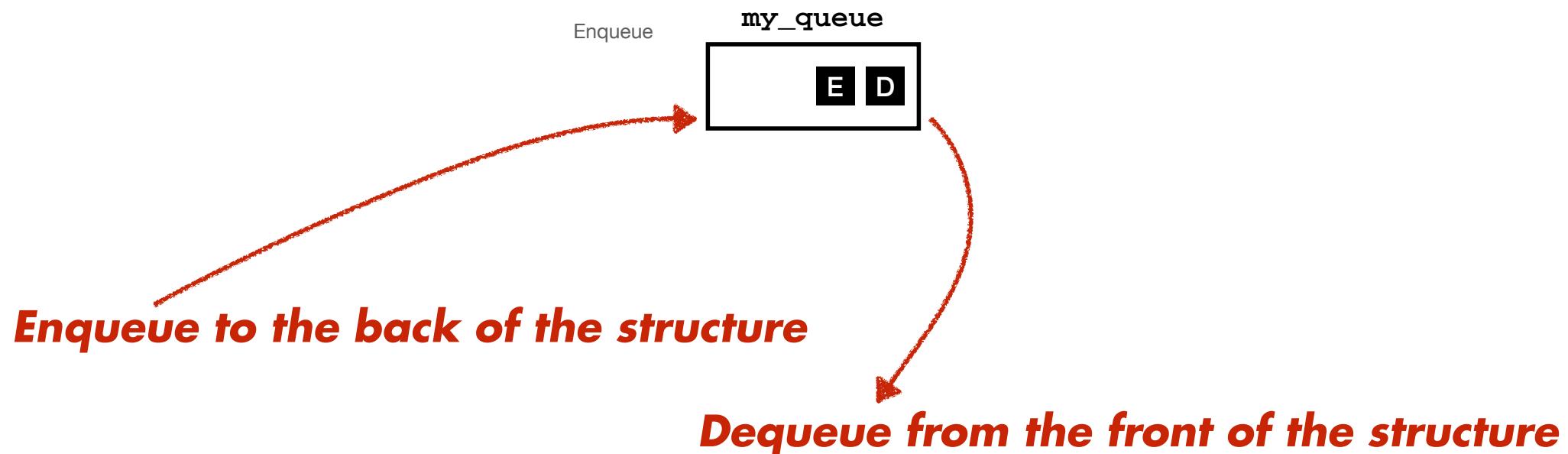
Queue data structure

“First in, first out” (FIFO) data structure



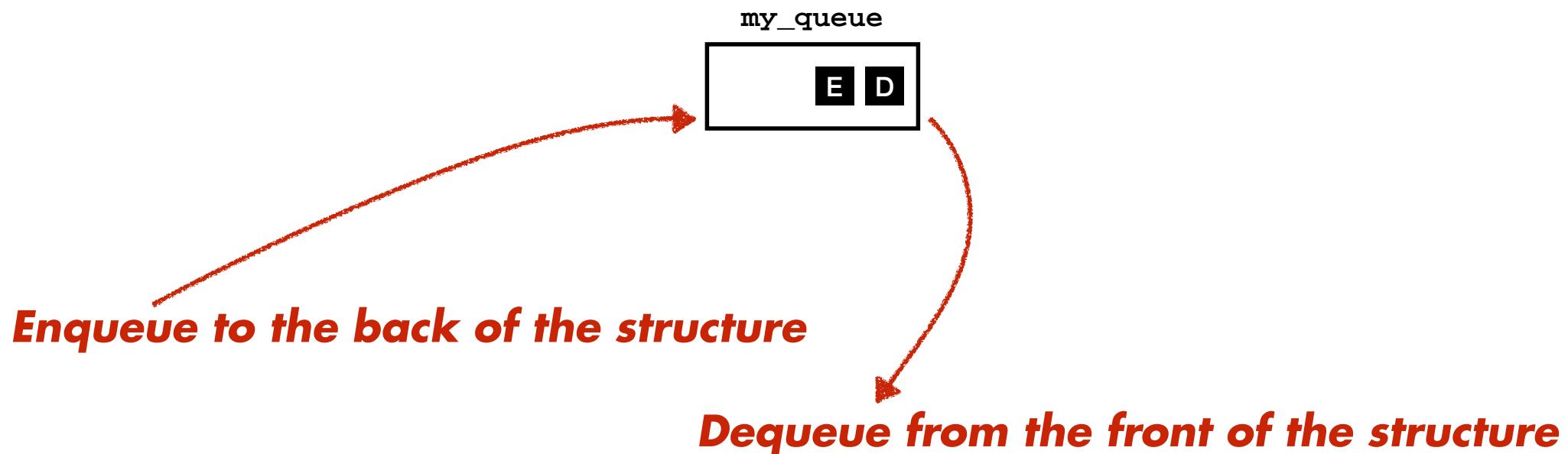
Queue data structure

"First in, first out" (FIFO) data structure



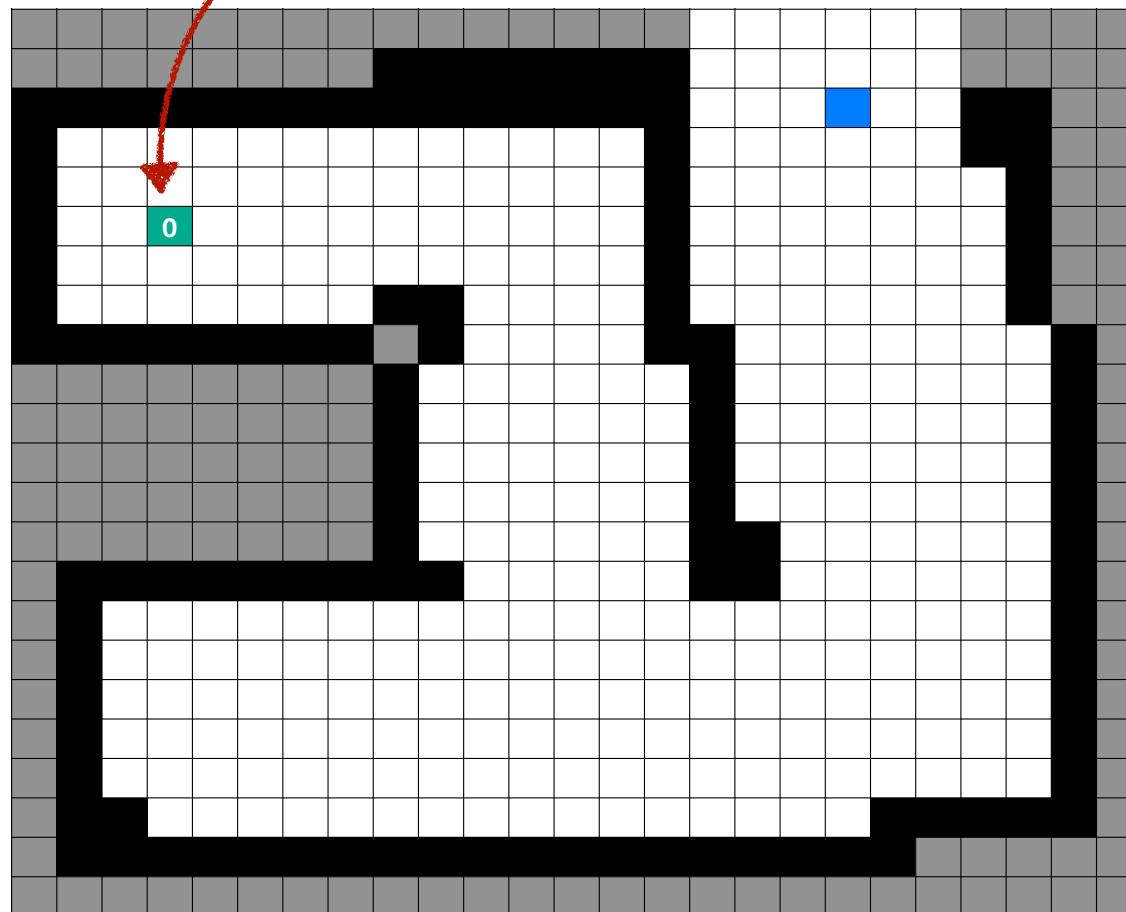
Queue data structure

"First in, first out" (FIFO) data structure



***Begin from
start node
with
no parent and
zero distance***

Going back to our example from the root node

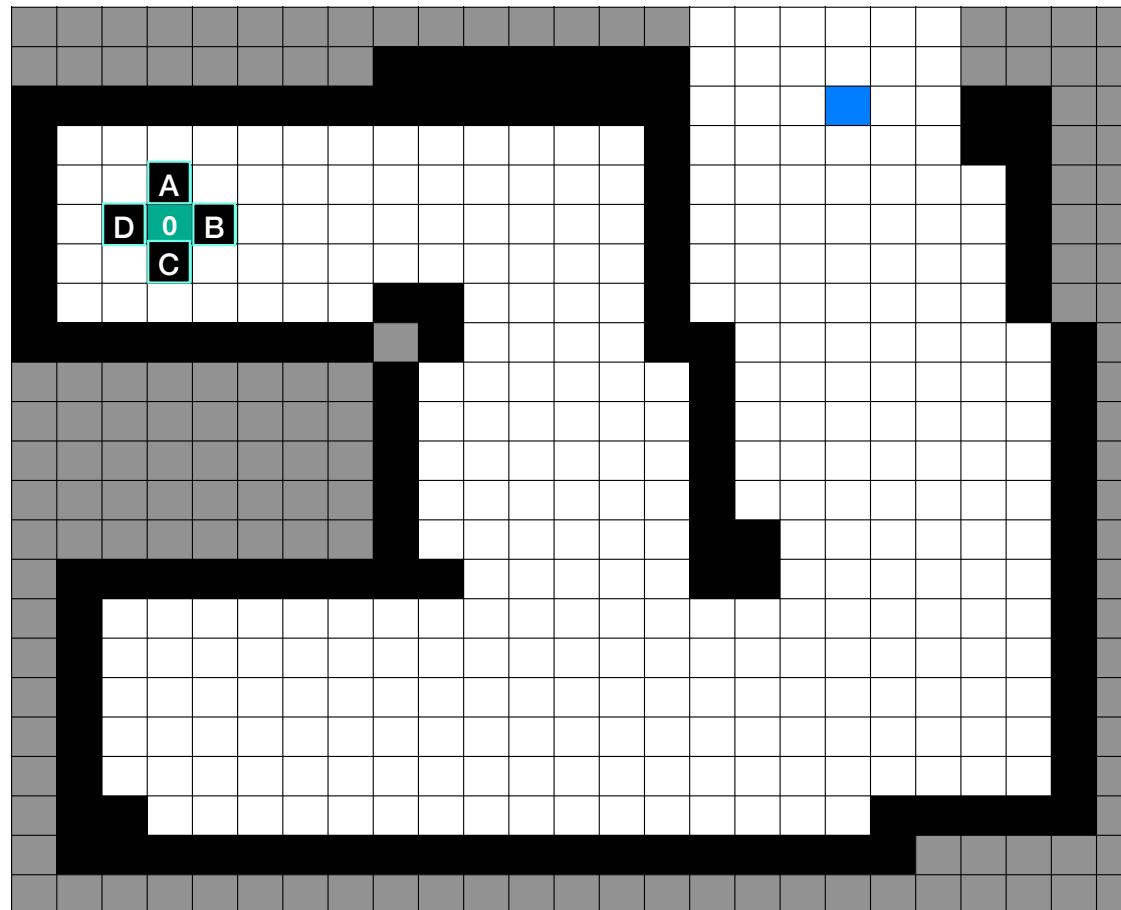


visit_queue



*Begin from
start node
with
no parent and
zero distance*

**All neighbors
of start are
“queued”**

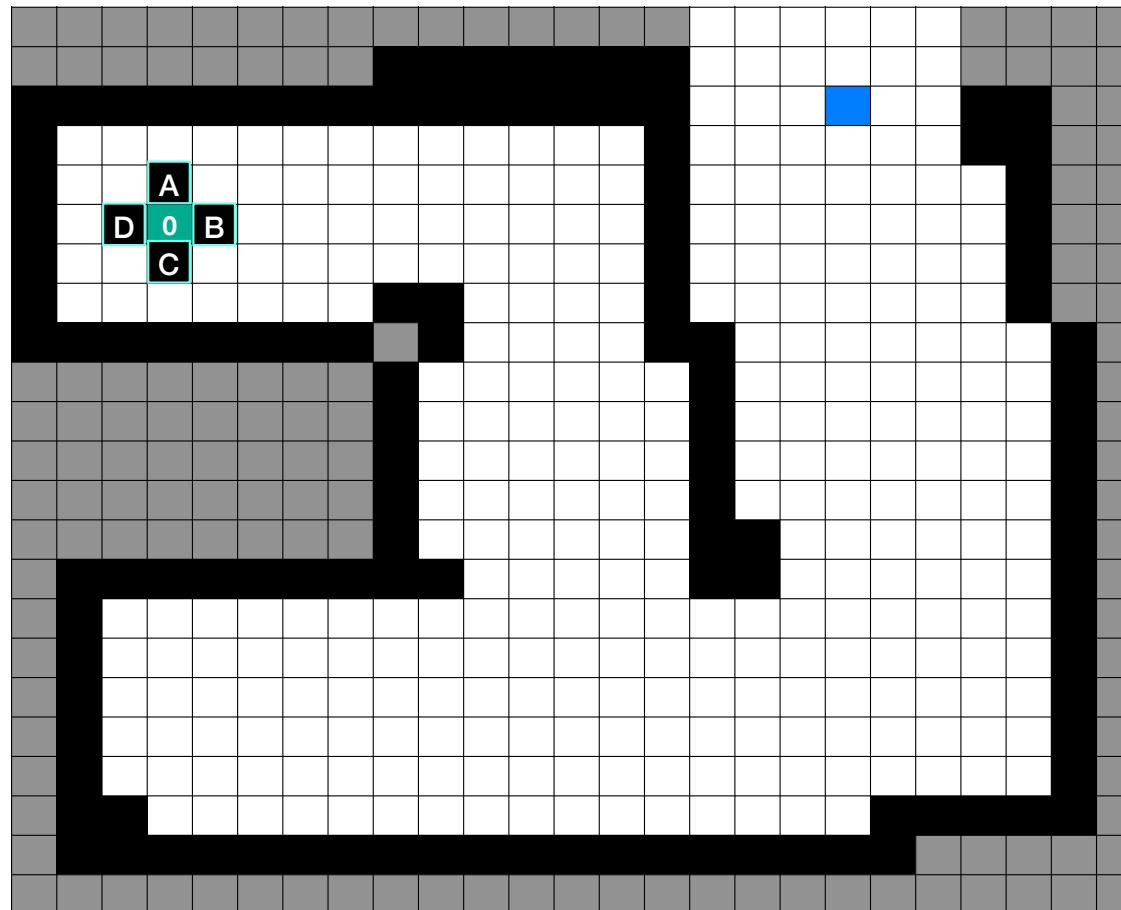


visit_queue



*Begin from
start node
with
no parent and
zero distance*

**All neighbors
of start are
“queued”**

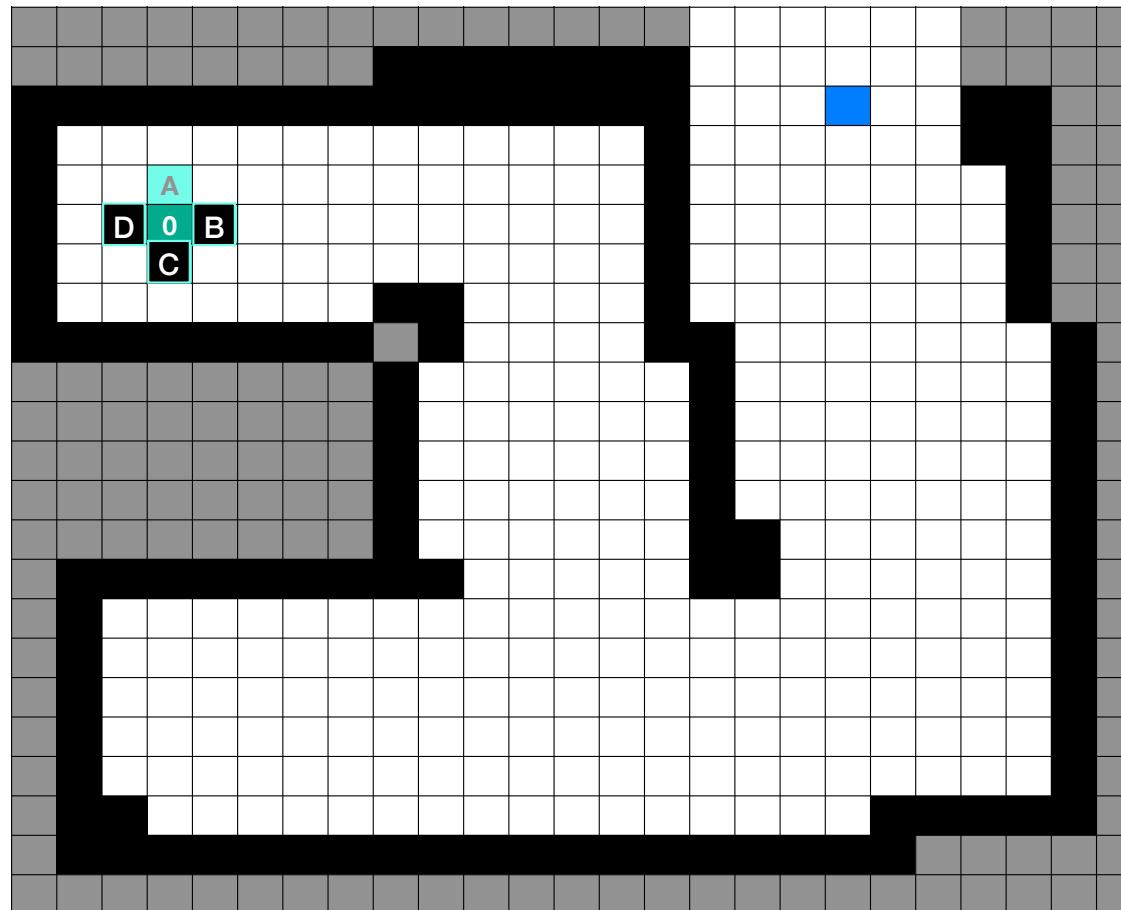


visit_queue



*Begin from
start node
with
no parent and
zero distance*

**All neighbors
of start are
“queued”**



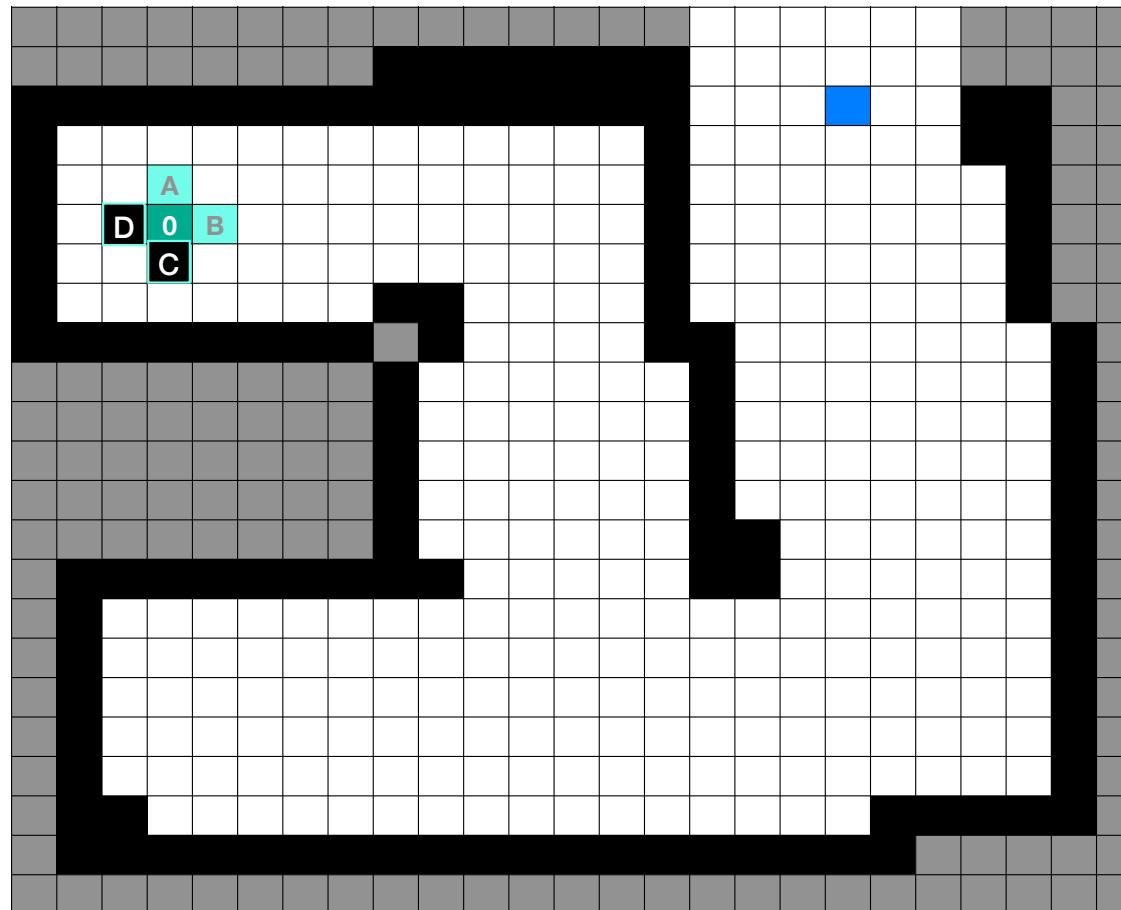
visit_queue



Enqueue

*Begin from
start node
with
no parent and
zero distance*

**All neighbors
of start are
“queued”**



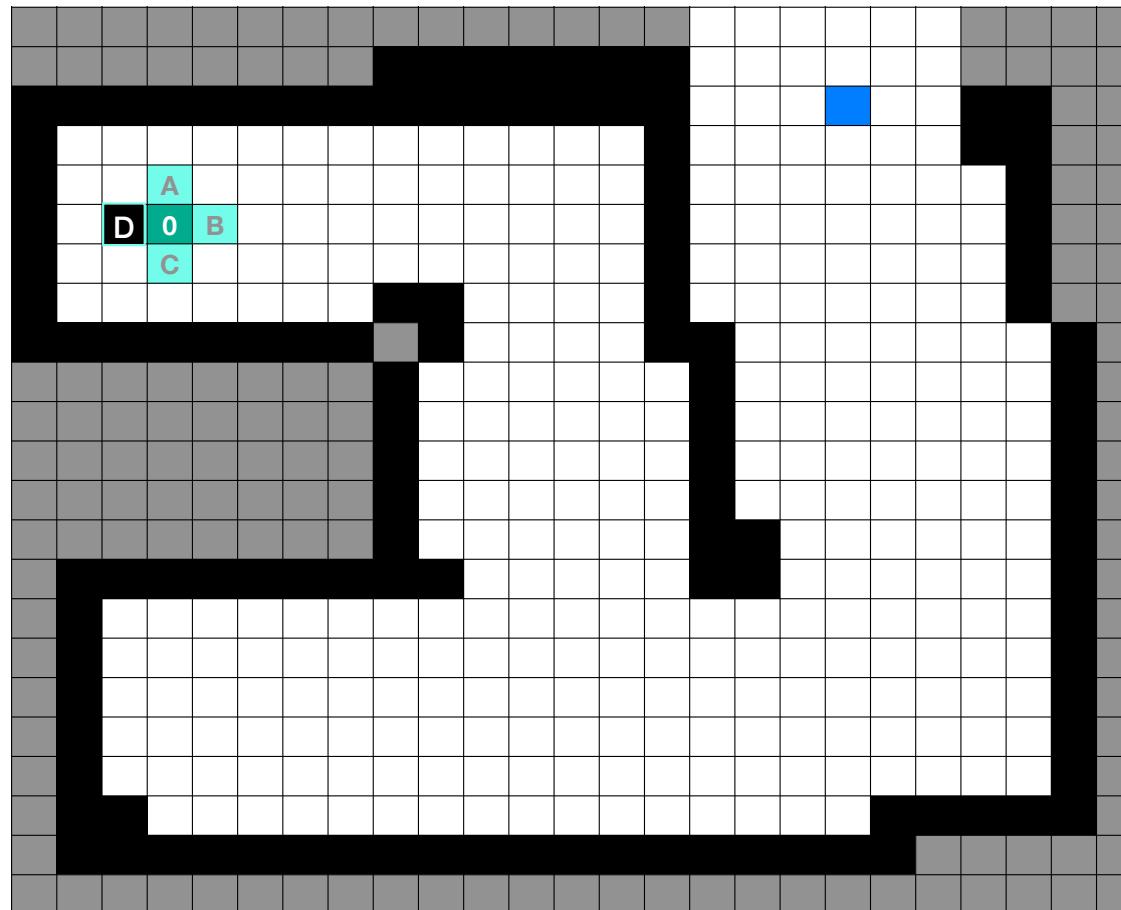
visit_queue

B A

Enqueue

*Begin from
start node
with
no parent and
zero distance*

**All neighbors
of start are
“queued”**



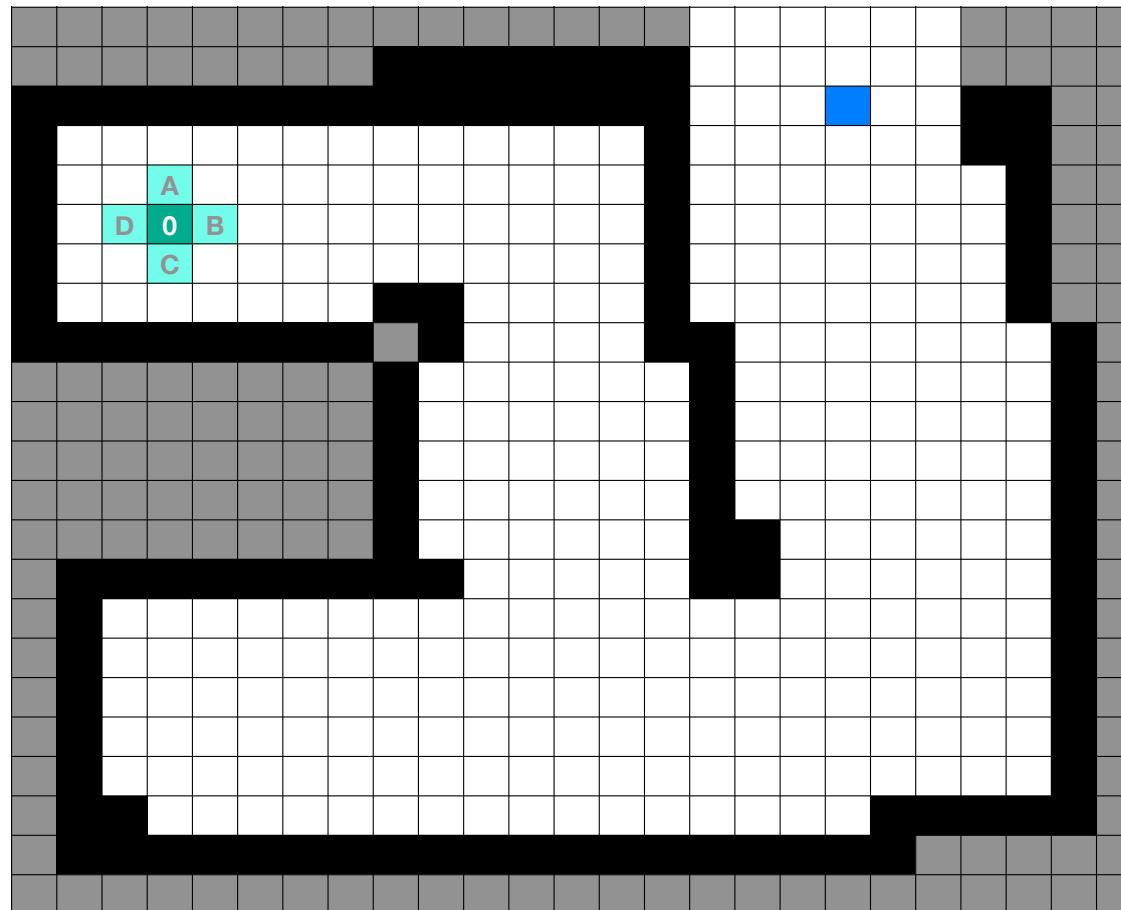
visit_queue

C B A

Enqueue

*Begin from
start node
with
no parent and
zero distance*

**All neighbors
of start are
“queued”**



visit_queue

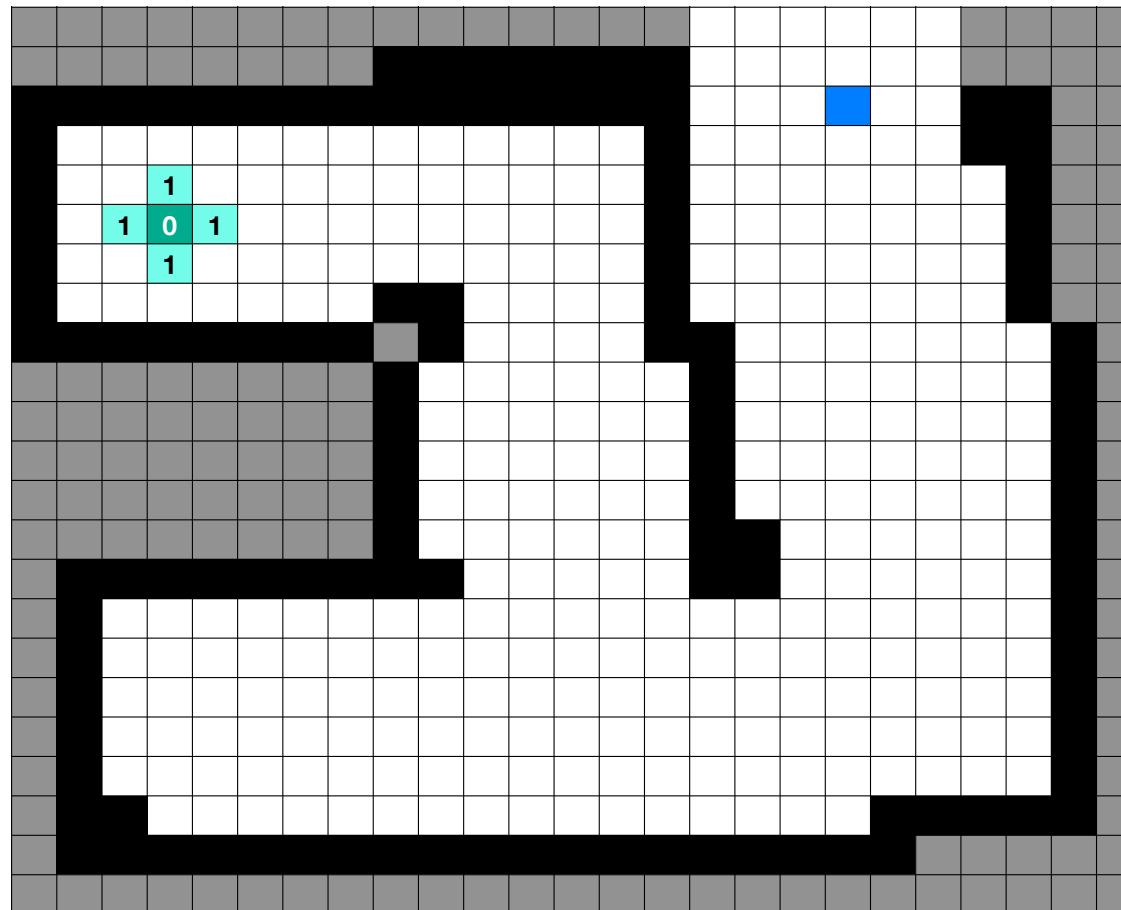
D C B A

Enqueue

*Begin from
start node
with
no parent and
zero distance*

*All neighbors
of start are
“queued”*

*and assigned
distance as
one plus start
node distance*



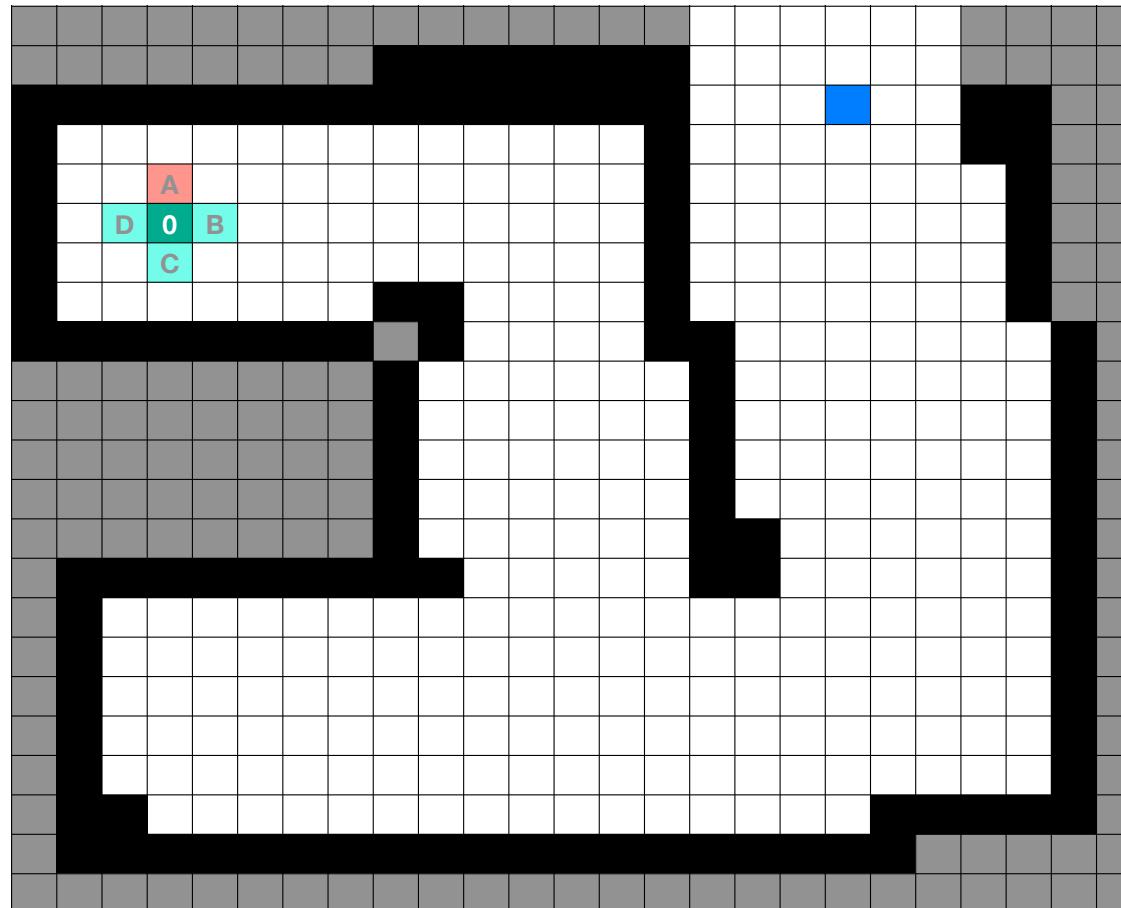
visit_queue

D C B A

**Repeat for
next node in
the queue**

*All neighbors
of current node
are “queued”*

*and assigned
distance as one
plus current
node distance*



visit_queue

D C B

Dequeue

A

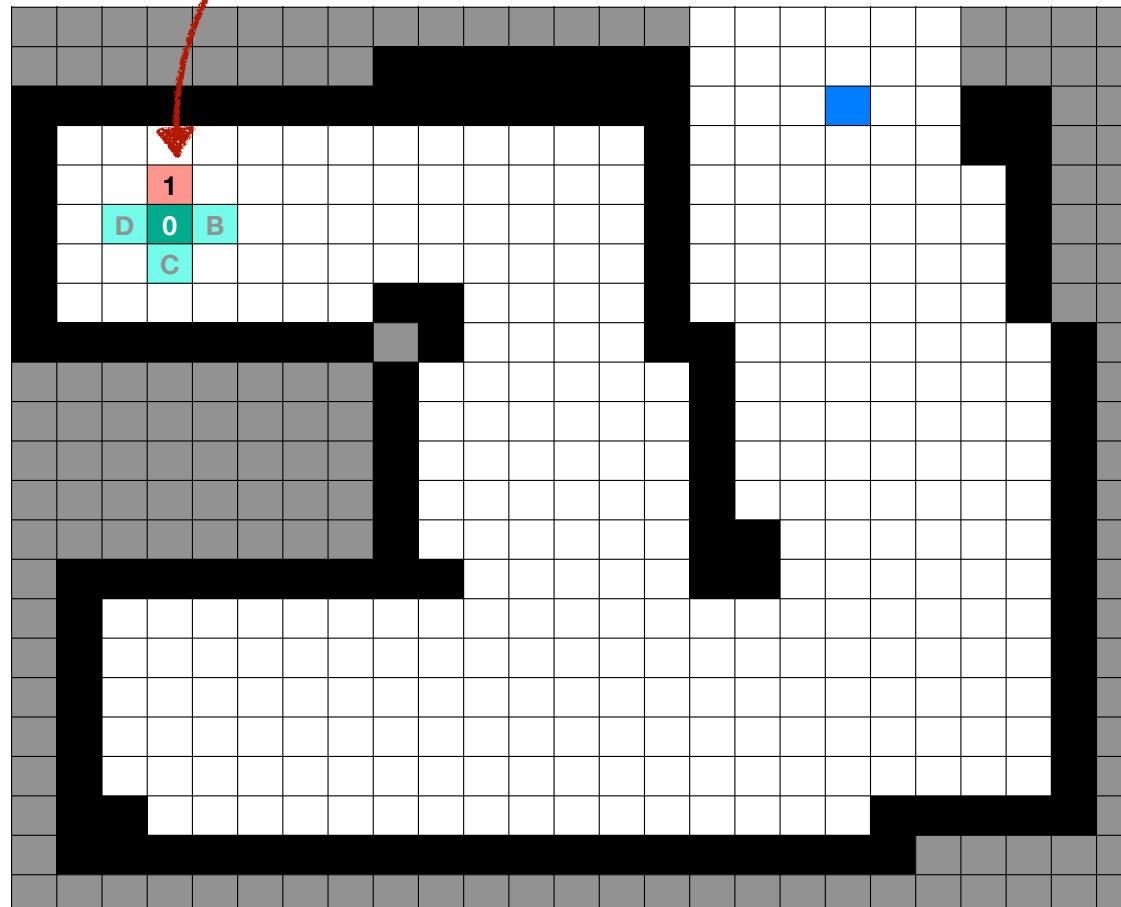
current_node

**Repeat for
next node in
the queue**

**All neighbors
of current node
are “queued”**

**and assigned
distance as one
plus current
node distance**

**Path distance at current node was already
assigned in previous iteration**



visit_queue

D C B

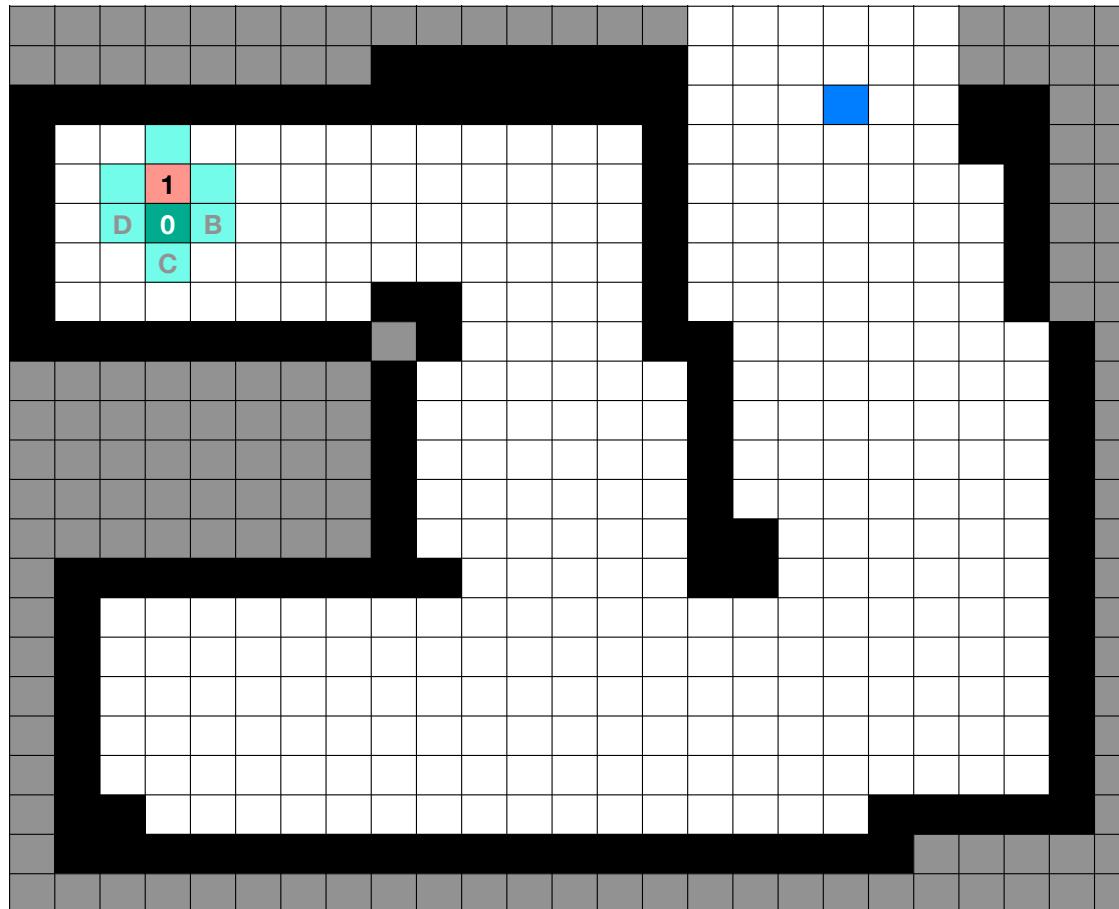
A

current_node

*Repeat for
next node in
the queue*

**All neighbors
of current node
are “queued”**

*and assigned
distance as one
plus current
node distance*



visit_queue

D C B

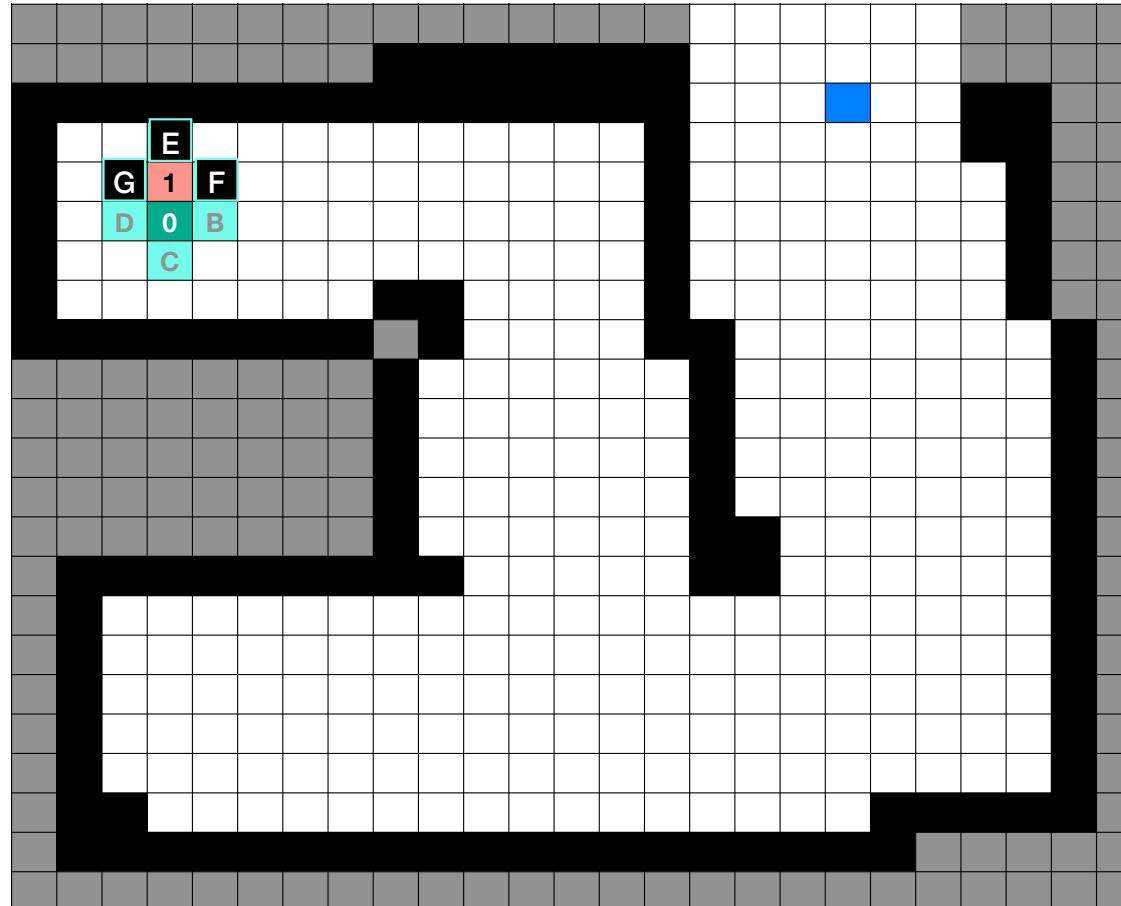
A

current_node

*Repeat for
next node in
the queue*

**All neighbors
of current node
are “queued”**

*and assigned
distance as one
plus current
node distance*



visit_queue

D C B

A

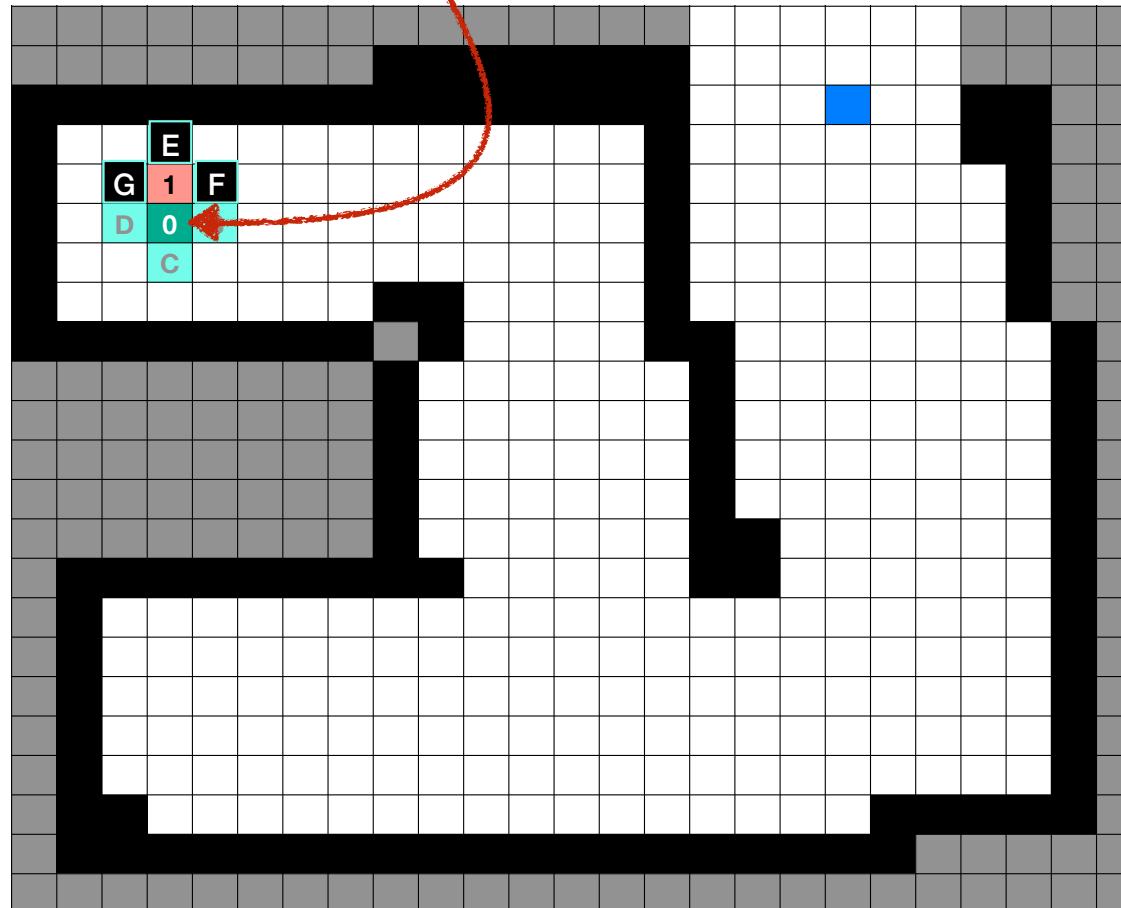
current_node

*Repeat for
next node in
the queue*

**All neighbors
of current node
are “queued”**

*and assigned
distance as one
plus current
node distance*

Do not revisit or re-enqueue nodes



`visit_queue`

`D C B`

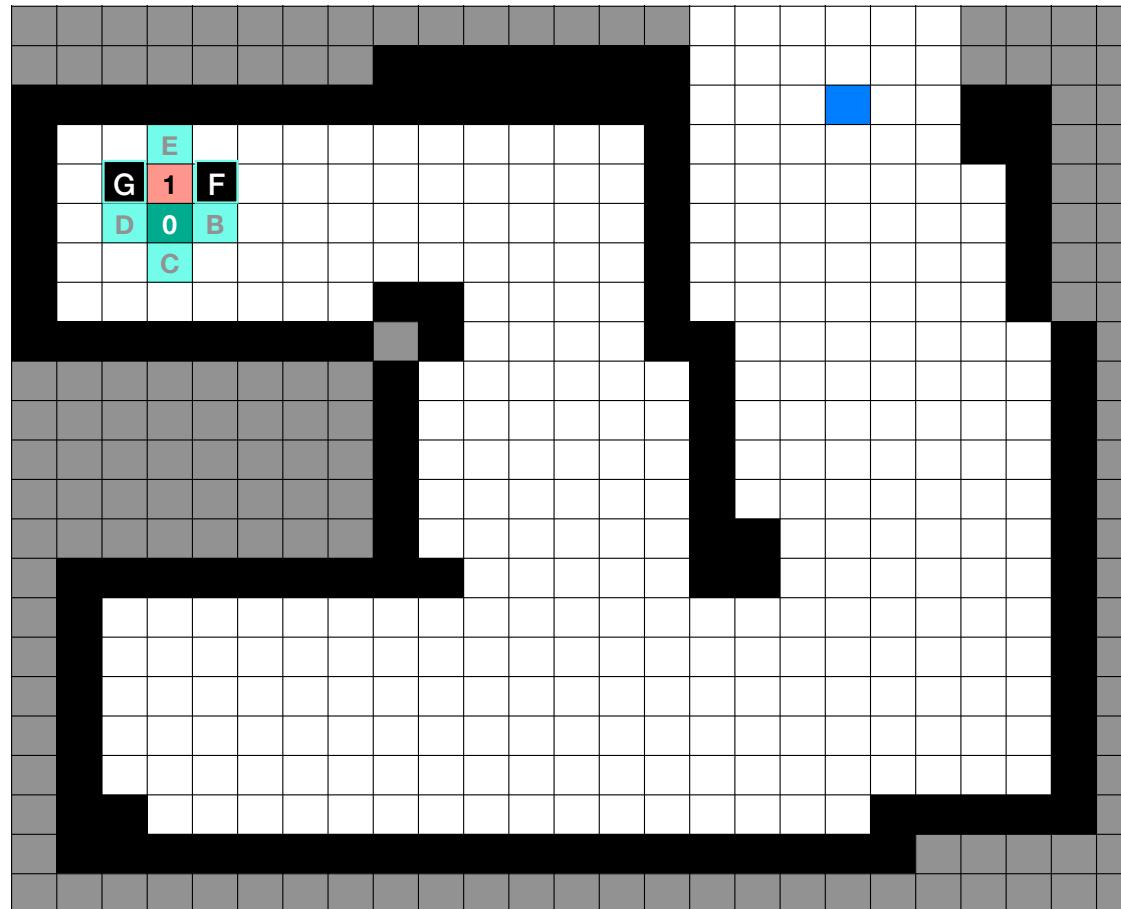
`A`

`current_node`

*Repeat for
next node in
the queue*

**All neighbors
of current node
are “queued”**

*and assigned
distance as one
plus current
node distance*



visit_queue

E D C B

Enqueue

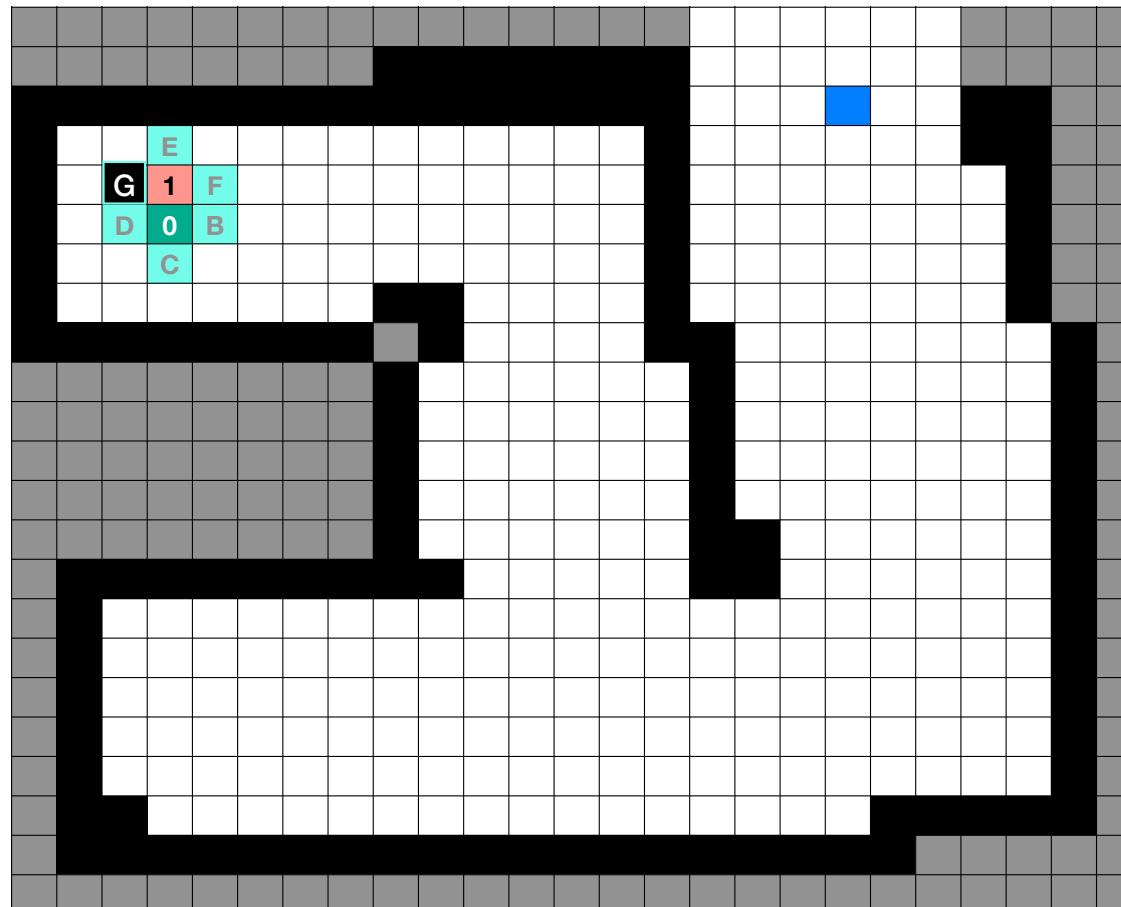
A

current_node

*Repeat for
next node in
the queue*

**All neighbors
of current node
are “queued”**

*and assigned
distance as one
plus current
node distance*



visit_queue

F E D C B

Enqueue

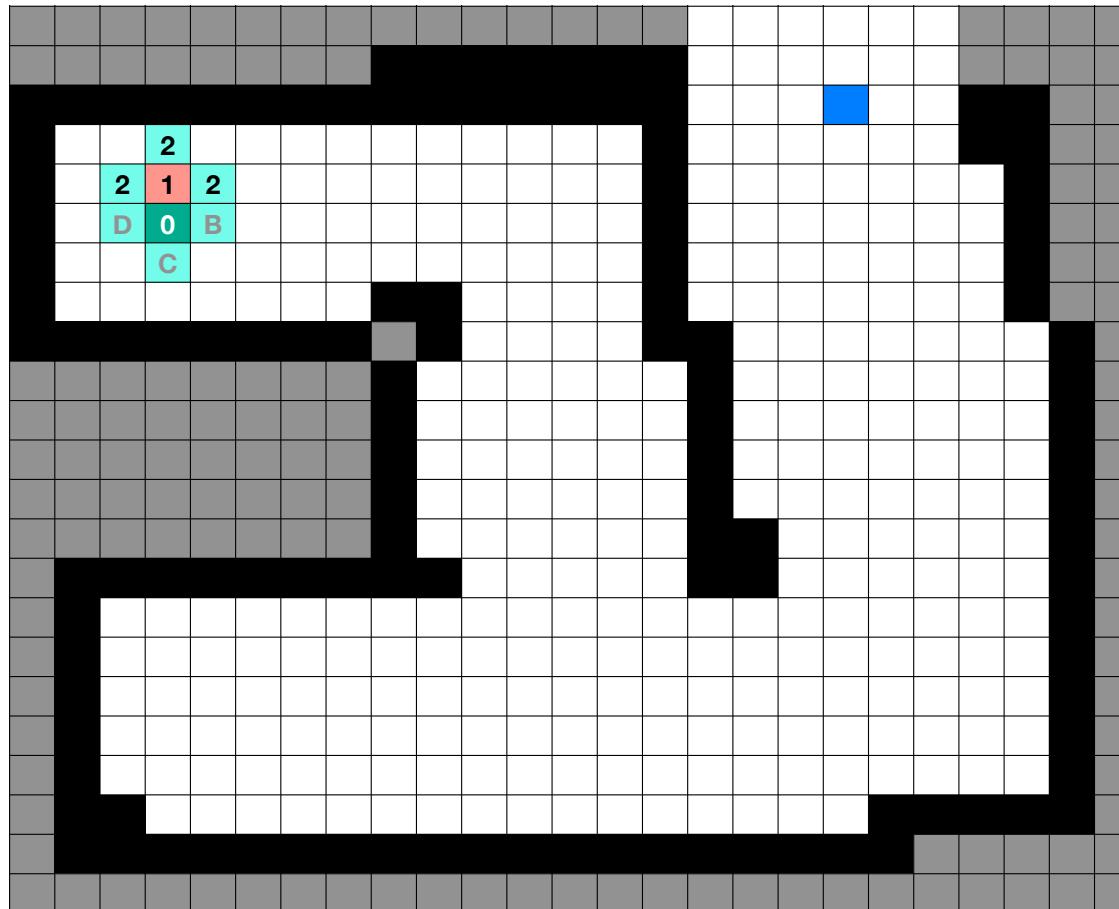
A

current_node

*Repeat for
next node in
the queue*

*All neighbors
of current node
are "queued"*

*and assigned
distance as one
plus current
node distance*



visit_queue

G F E D C B

Enqueue

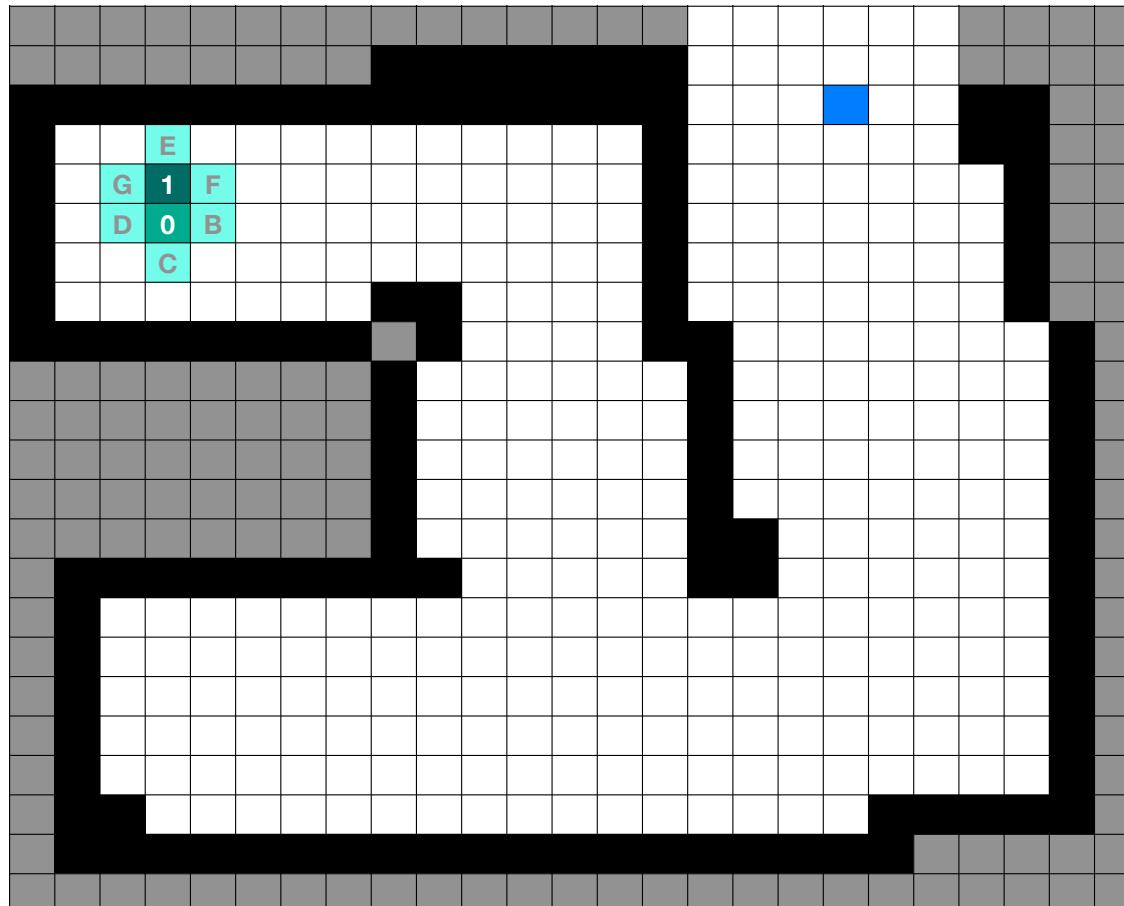
A

current_node

*Repeat for
next node in
the queue*

*All neighbors
of current node
are "queued"*

*and assigned
distance as one
plus current
node distance*



visit_queue

G F E D C B

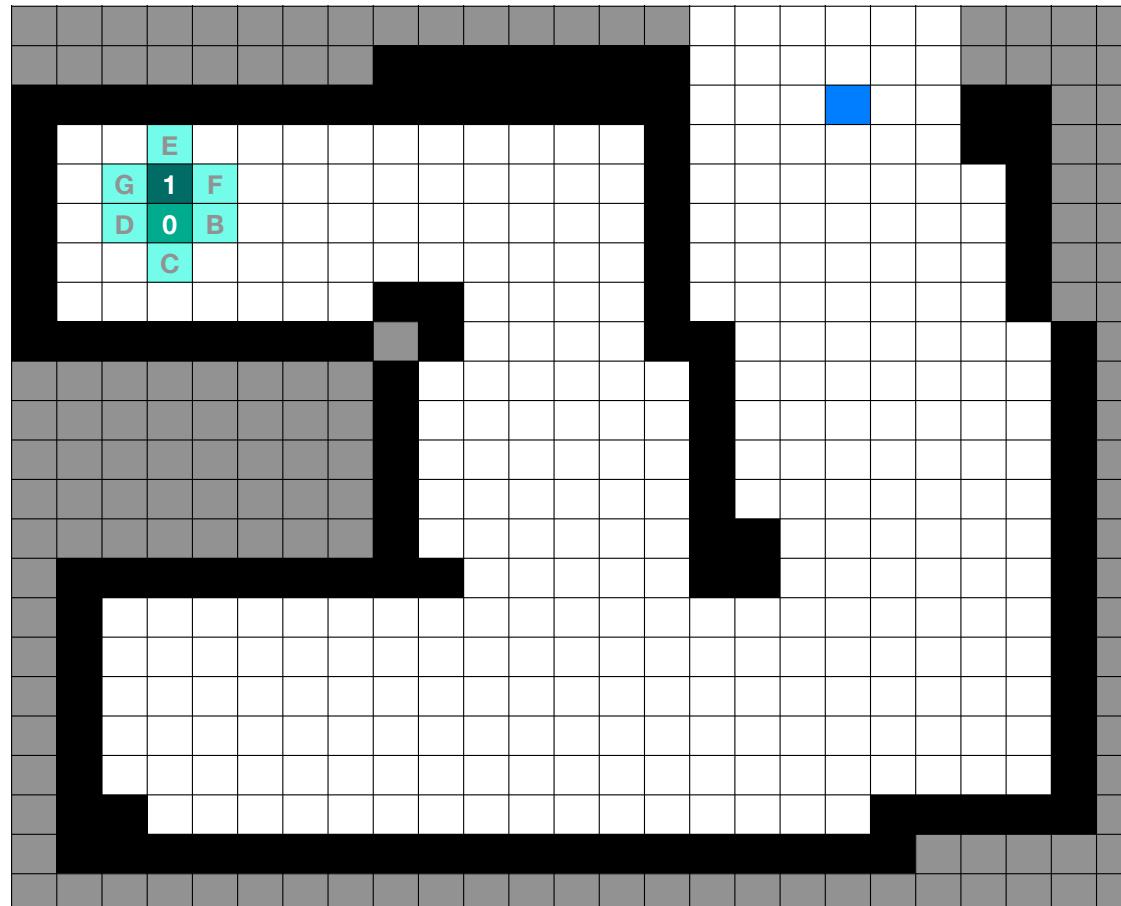
current_node

Node A
**done being
processed**

**Repeat for
next node in
the queue**

*All neighbors
of current node
are “queued”*

*and assigned
distance as one
plus current
node distance*



visit_queue

G F E D C B

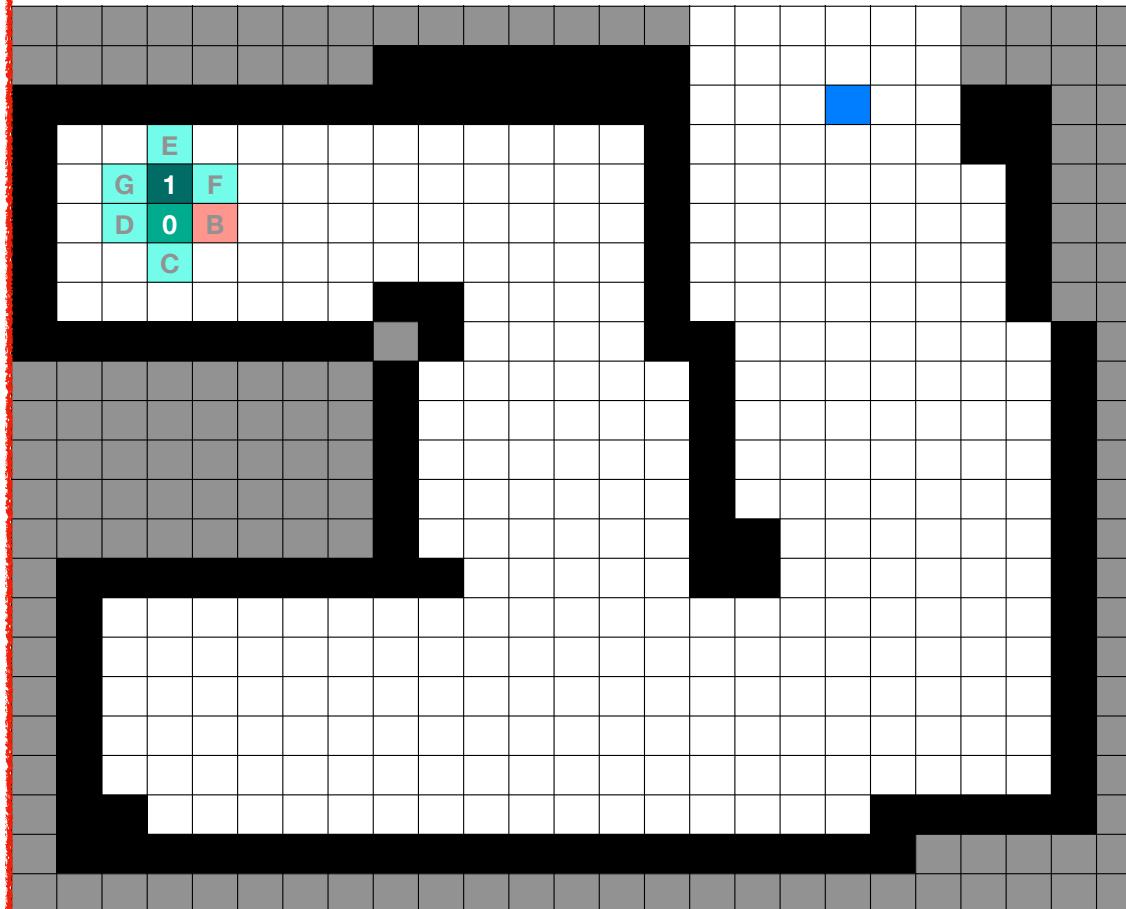
current_node

**Repeat for
next node in
the queue**

**All neighbors
of current node
are “queued”**

**and assigned
distance as one
plus current
node distance**

Continue until goal reached or queue is empty



visit_queue

G F E D C

Dequeue

B

current_node

How to keep track of visited nodes?

Queue data structure

Begin from start node with no parent and zero distance

Visit the neighbors of nodes just visited

Assign each one plus the smallest distance

Repeat for next set of neighbors

Once goal node reached, perform local search back to start

Assign parents along path in decreasing order

Form list of navigation waypoints



Global search to find routing

Begin from start node with no parent and zero distance

Visit the neighbors of nodes just visited

Assign each one plus the smallest distance

Repeat for next set of neighbors

Once goal node reached, perform local search back to start

Assign parents along path in decreasing order

Form list of navigation waypoints

Global search to find routing

Begin from start node with no parent and zero distance

↓
Visit the neighbors of nodes just visited

↓
Assign each one plus the smallest distance

→ Repeat for next set of neighbors

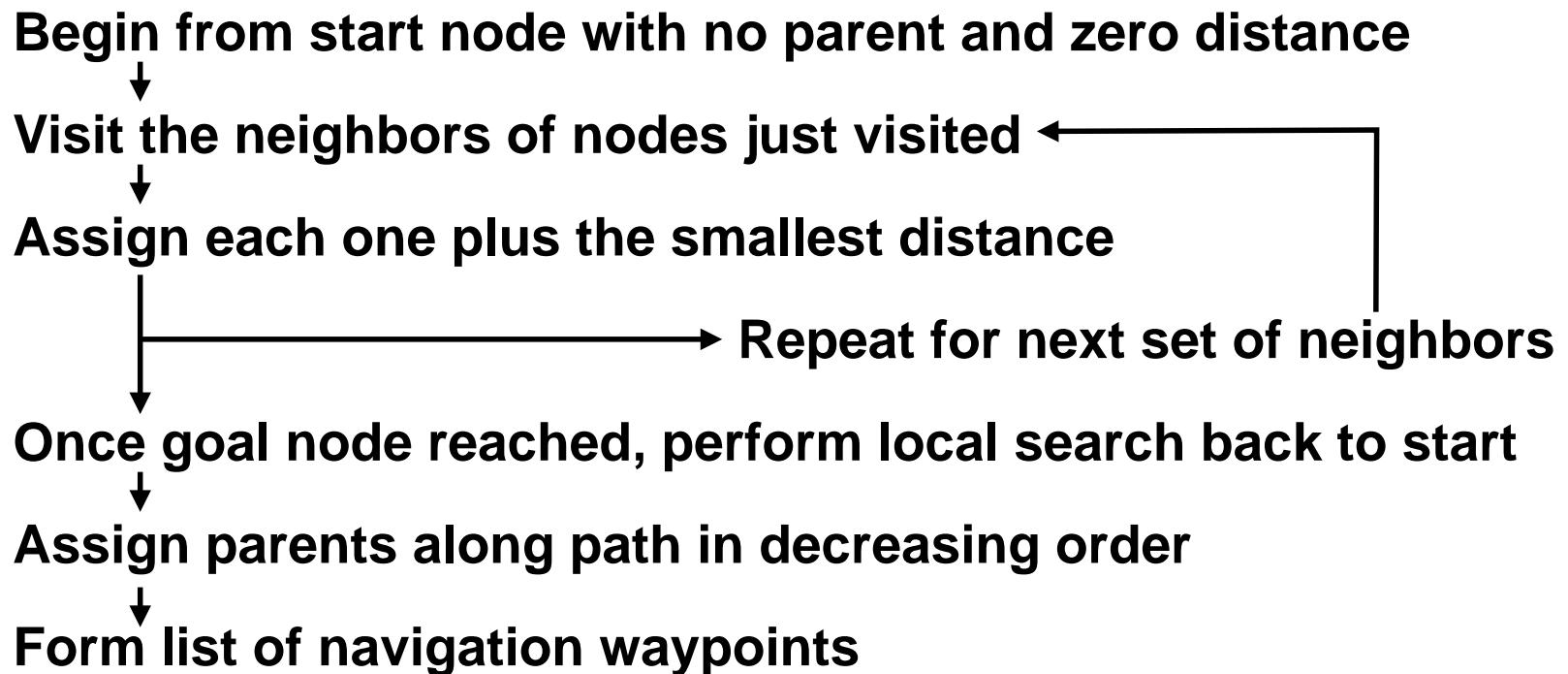
Once goal node reached, perform local search back to start

↓
Assign parents along path in decreasing order

↓
Form list of navigation waypoints

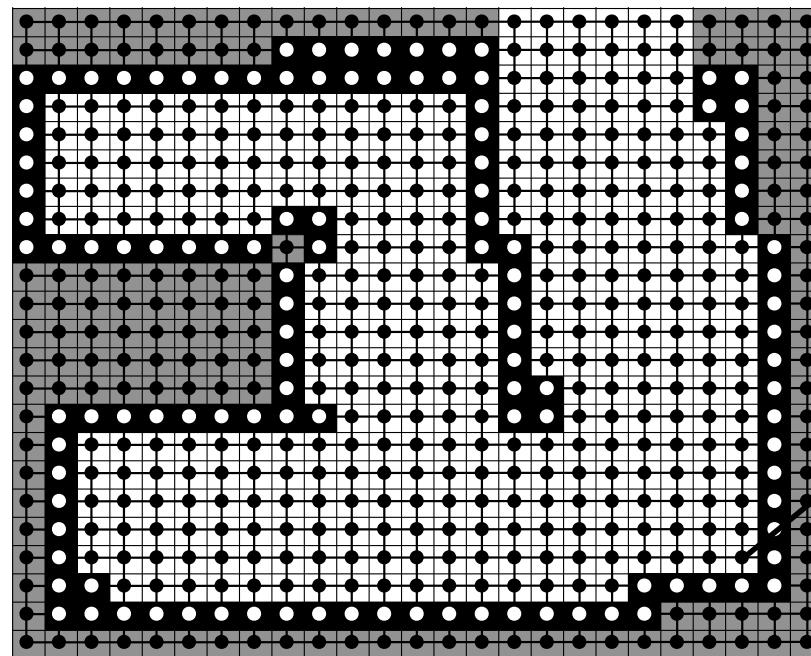
Is this local search necessary?

Brushfire is one of several algorithms that perform a “floodfill”



Breadth-first Search

For Breadth-first Search, each cell needs to keep track of whether it has been visited and queued



origin_x: 2.2
origin_y: 0.3
occupied: false
parent: ??
distance: ??
visited: false
queued: false

A graph node stores a struct of information about the cell

Breadth-first Search

Initialize :

All nodes to have no parent, max distance, and as unvisited

Start node to have no parent and zero distance

Visit queue with start node as its only enqueued element

Iterate : While visit list not empty and currently visited node is not the goal

Dequeue new current node to visit and mark it as visited

For each neighbor :

Add to visit queue, if not previously visited or queued

If Distance of neighbor > Distance of current node + ...

Cost to move from current node to neighbor

Then Update neighbor's parent to be current node and ...

distance to be distance of current node + cost to move

Breadth-first Search

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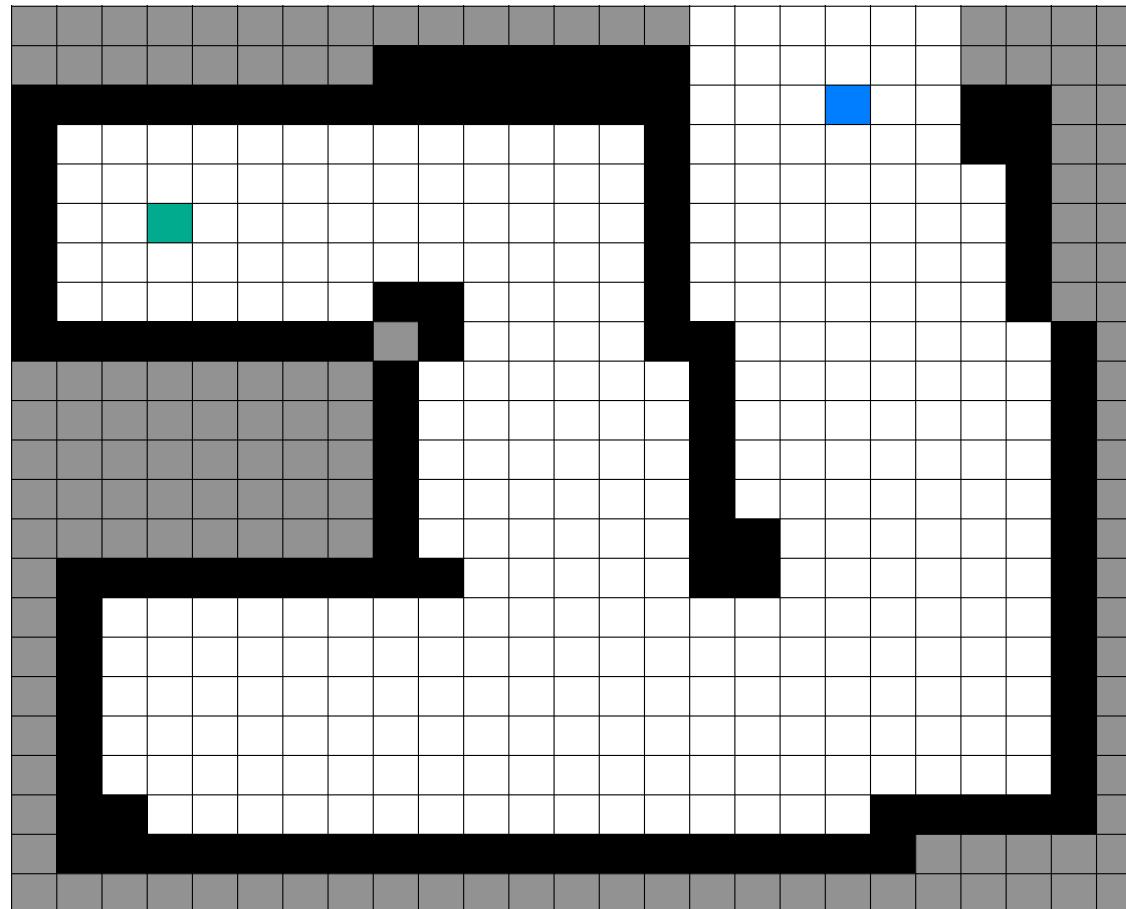
If Distance of neighbor > Distance of current node + ...

Cost to move from current node to neighbor

Then Update neighbor's parent to be current node and ...

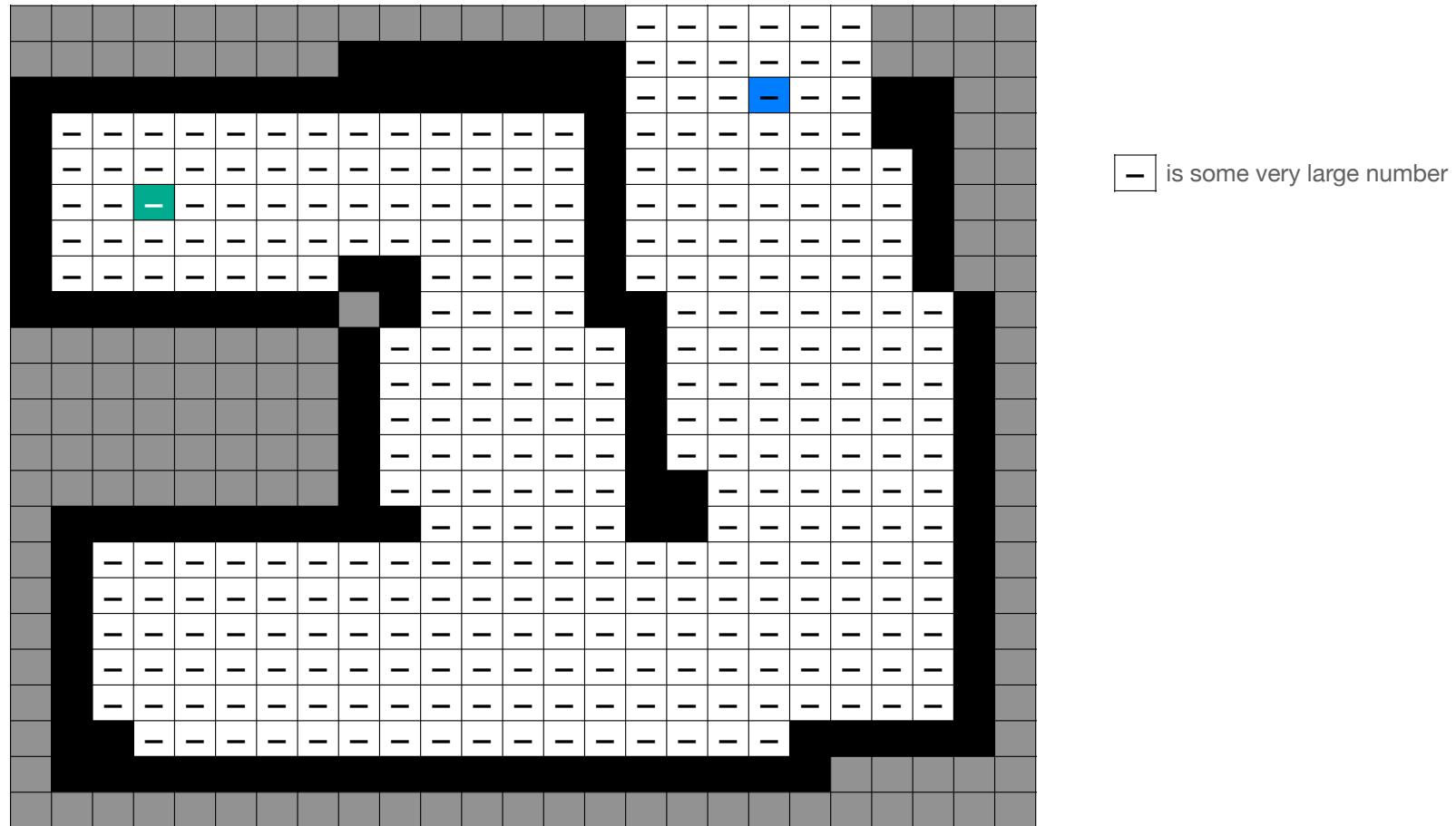
distance to be distance of current node + cost to move

All nodes to have no parent, max distance, and as unvisited

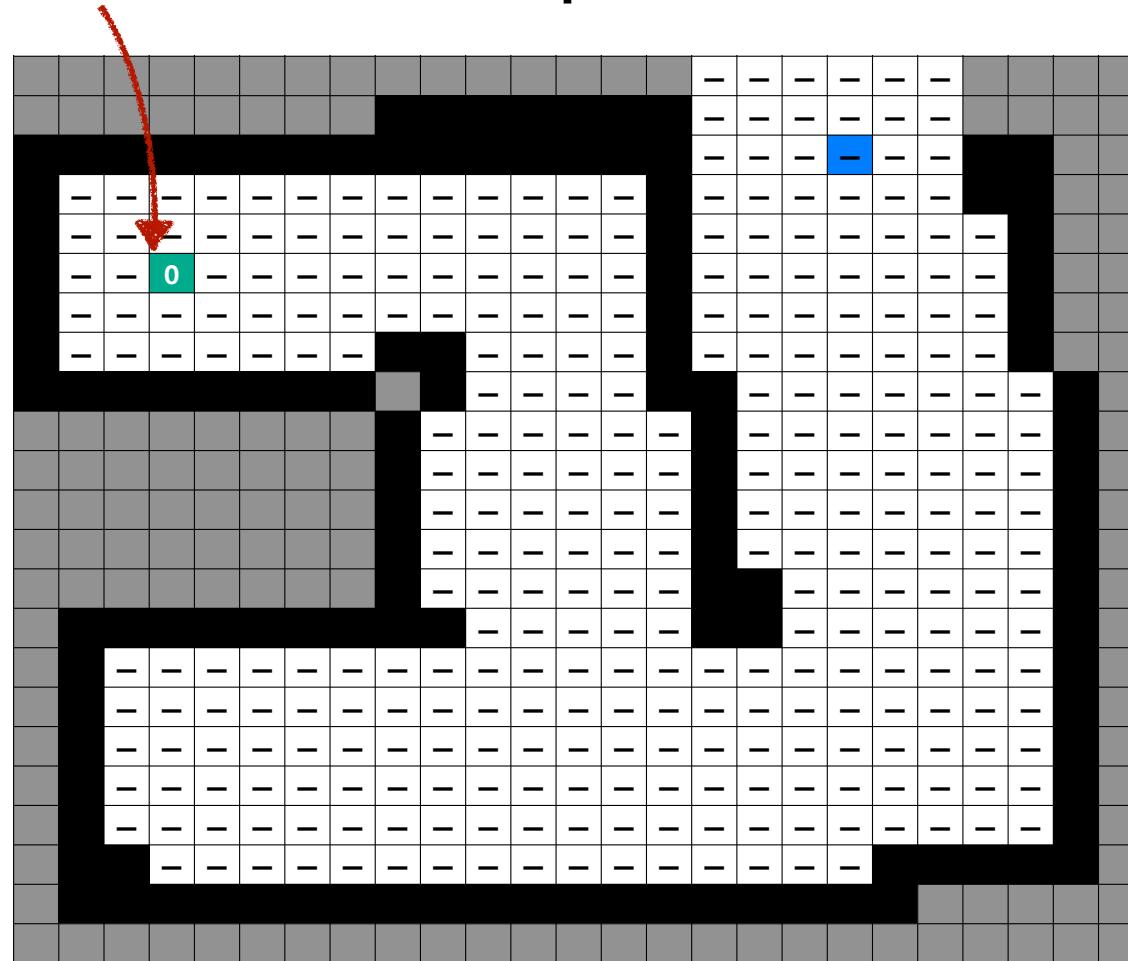


— is some very large number

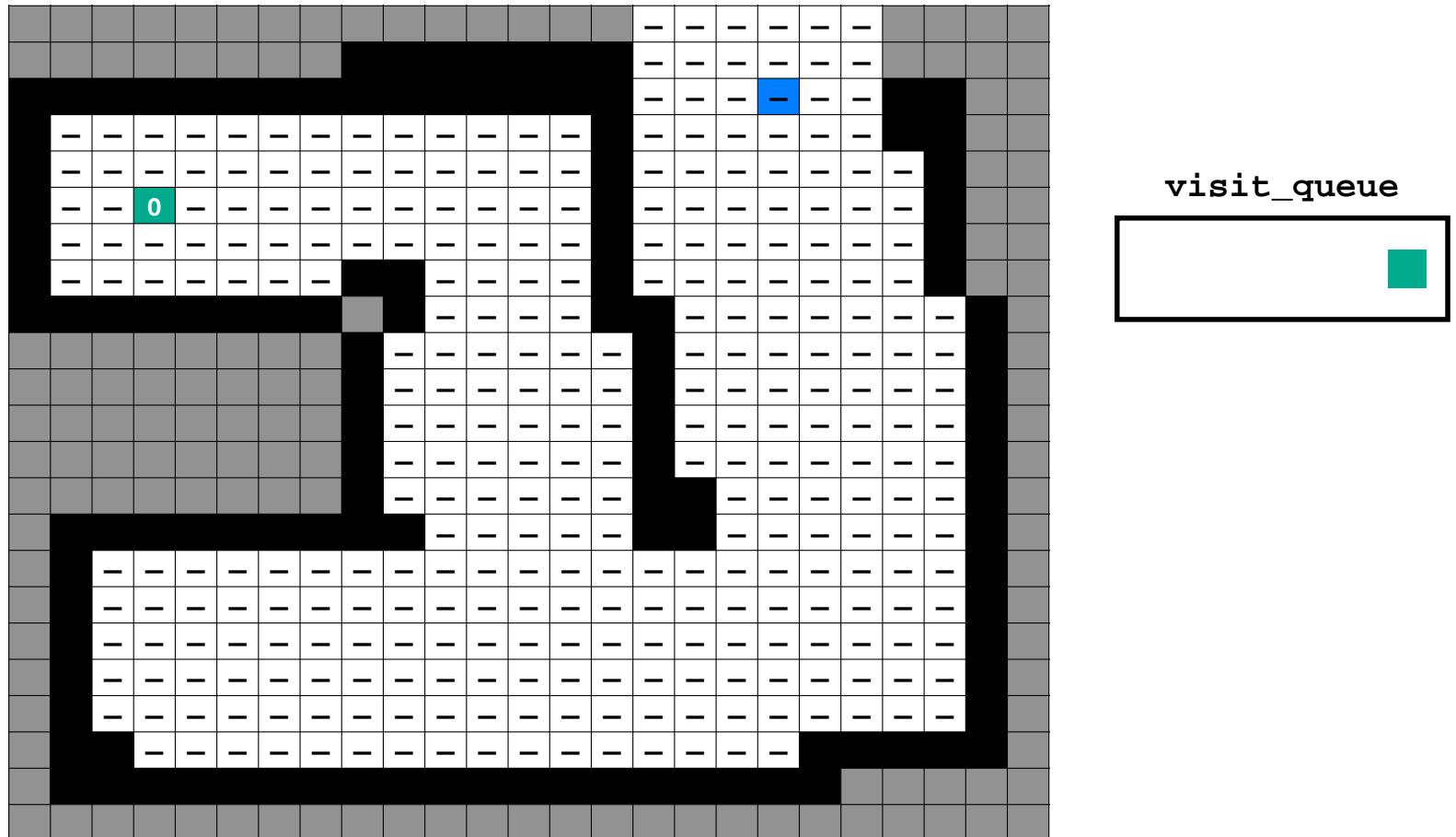
All nodes to have no parent, max distance, and as unvisited



Start node to have no parent and zero distance



Visit queue with start node as its only enqueued element



Initialize :

All nodes to have no parent, max distance, and as unvisited

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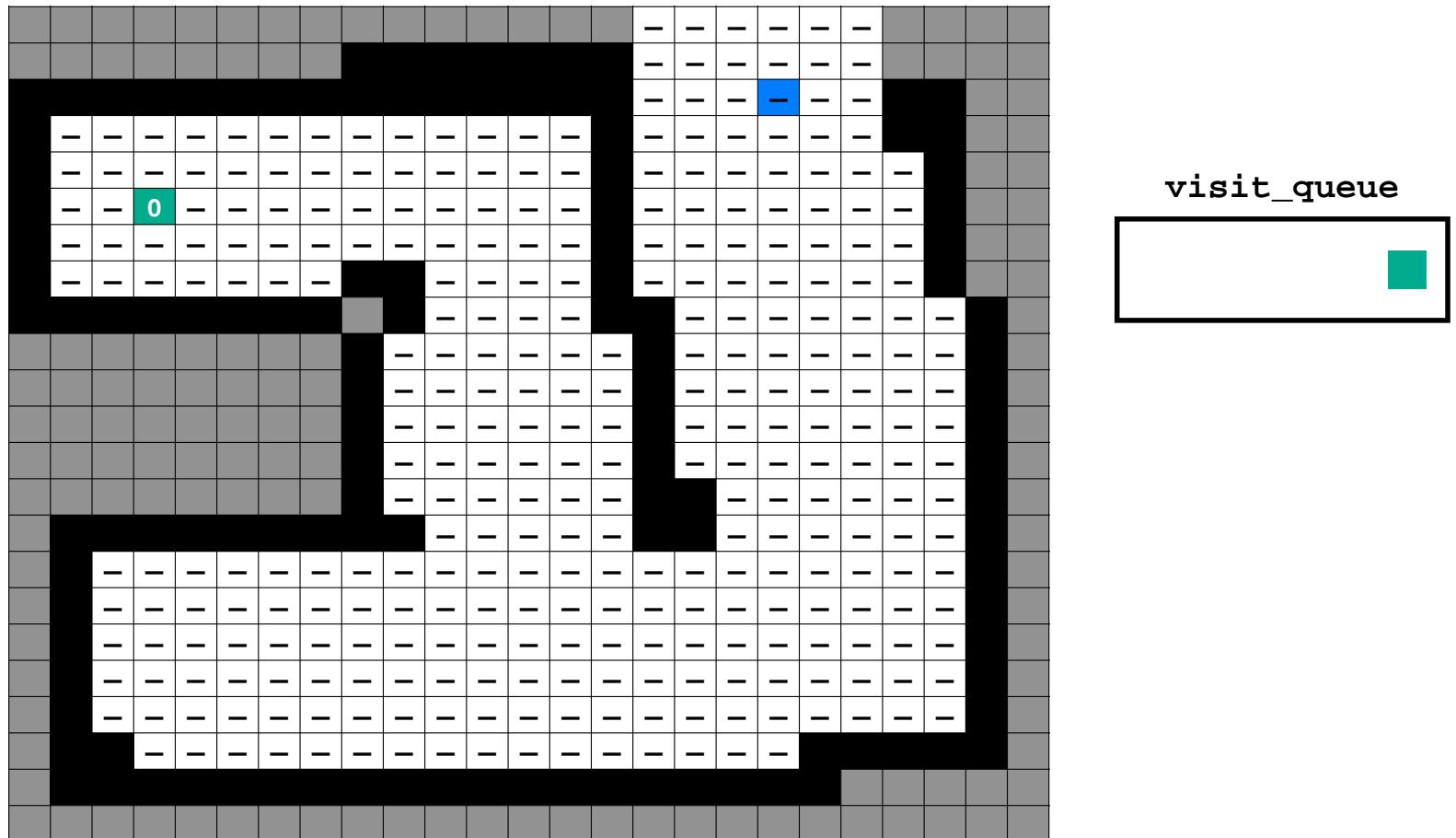
If Distance of neighbor > Distance of current node + ...

Cost to move from current node to neighbor

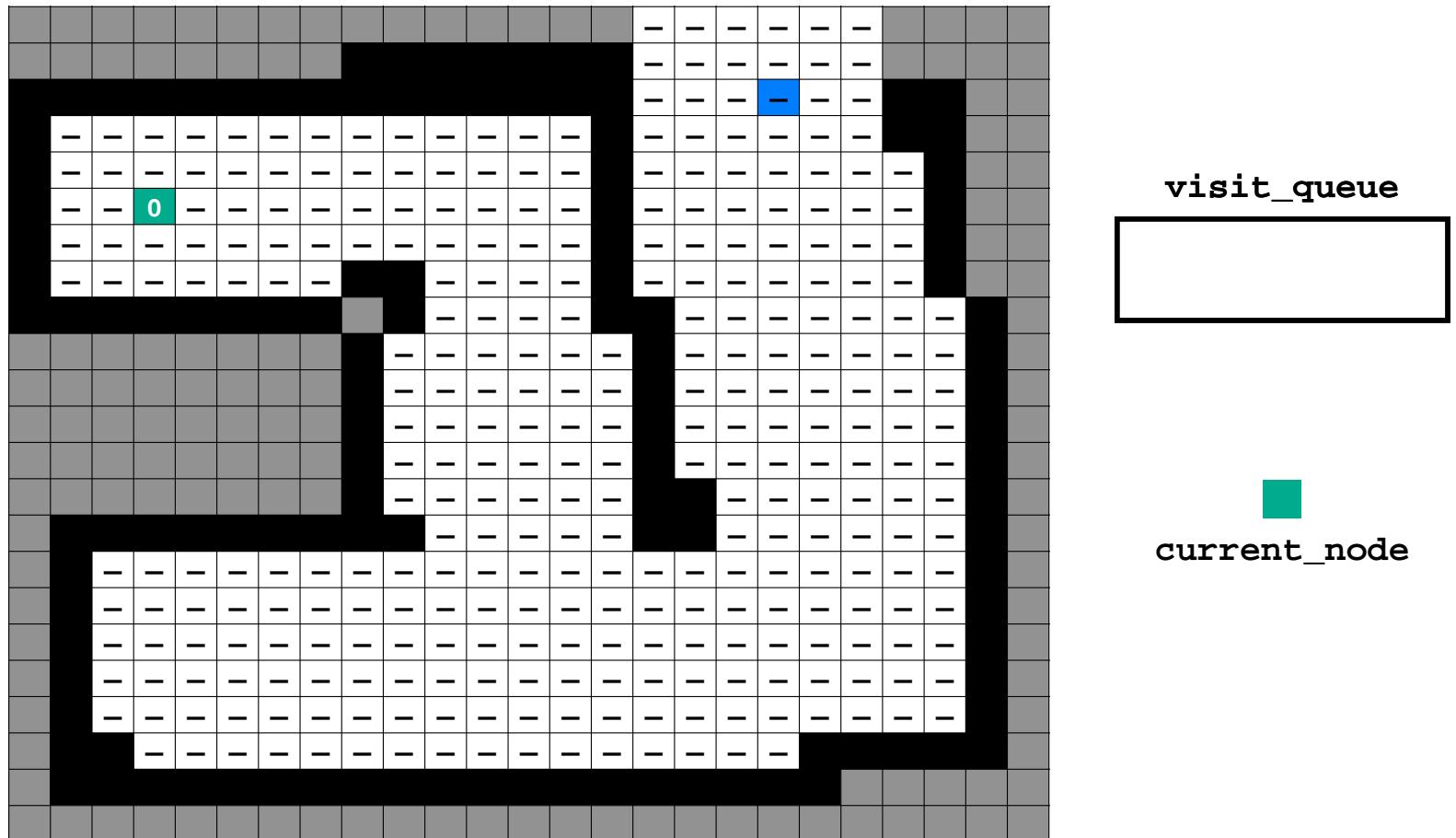
Then Update neighbor's parent to be current node and ...

distance to be distance of current node + cost to move

Dequeue new current node to visit and mark it as visited



Dequeue new current node to visit and mark it as visited



Initialize :

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For each neighbor :

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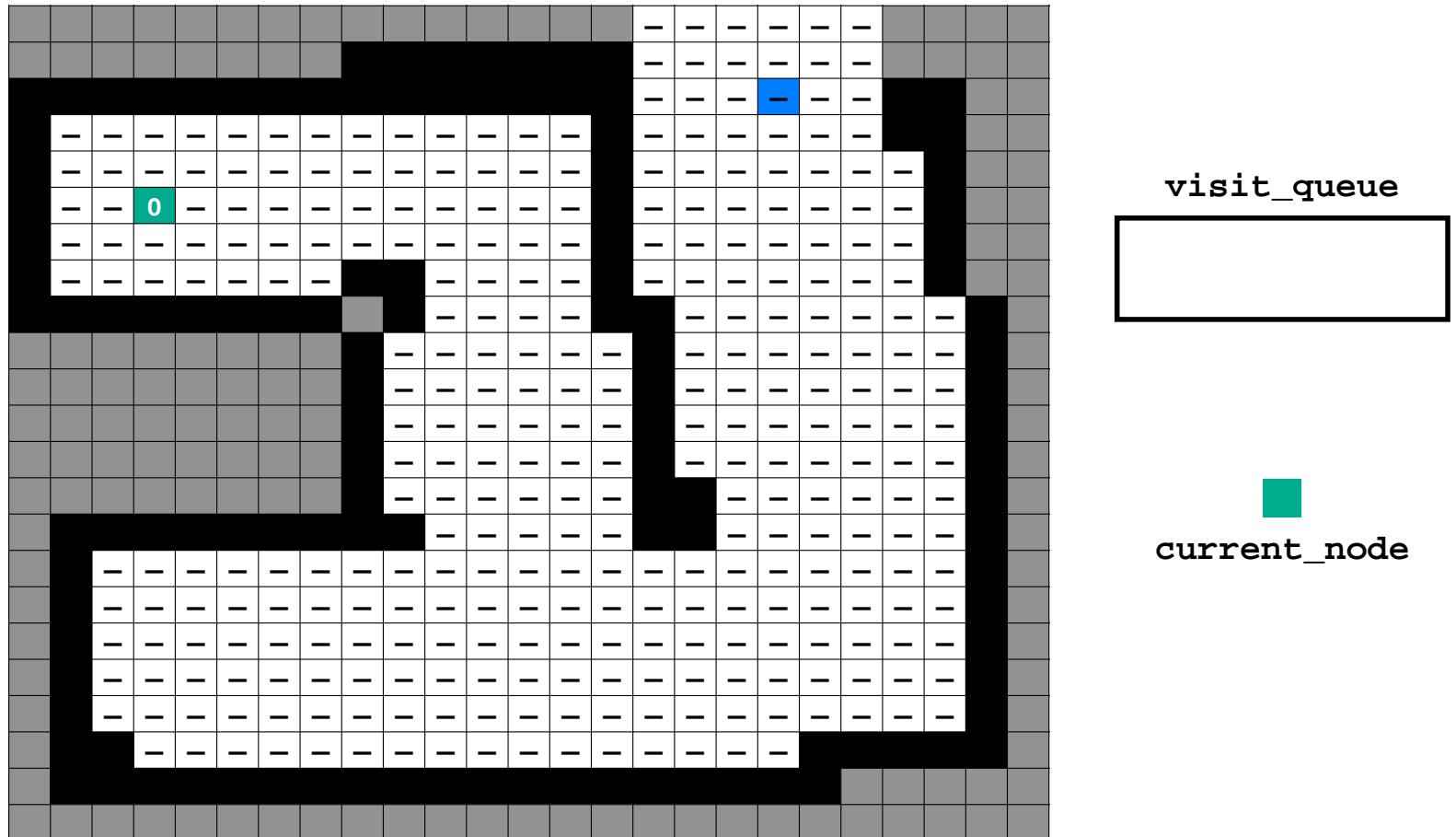
If Distance of neighbor > Distance of current node + ...

Cost to move from current node to neighbor

Then Update neighbor's parent to be current node and ...

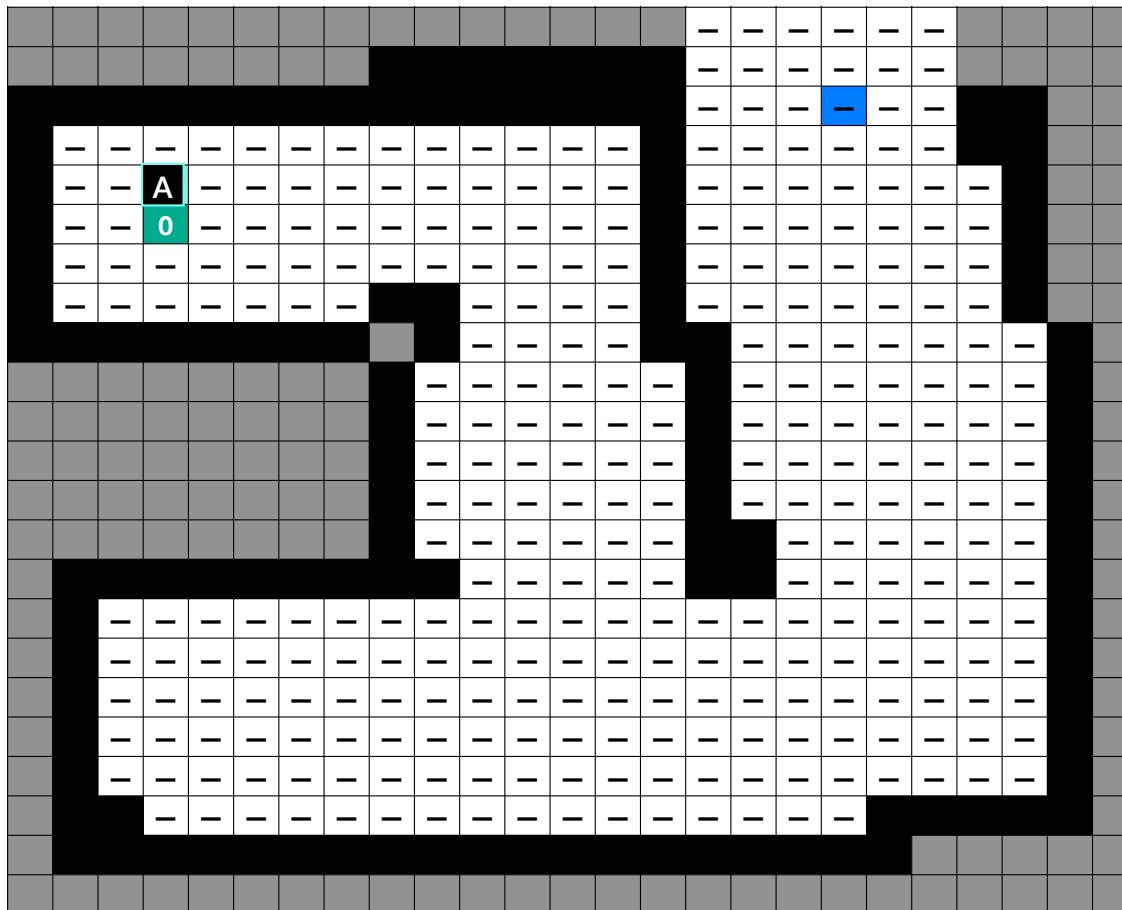
distance to be distance of current node + cost to move

Add to visit queue, if not previously visited or queued



Add to visit queue, if not previously visited or queued

**Queue first
neighbor**



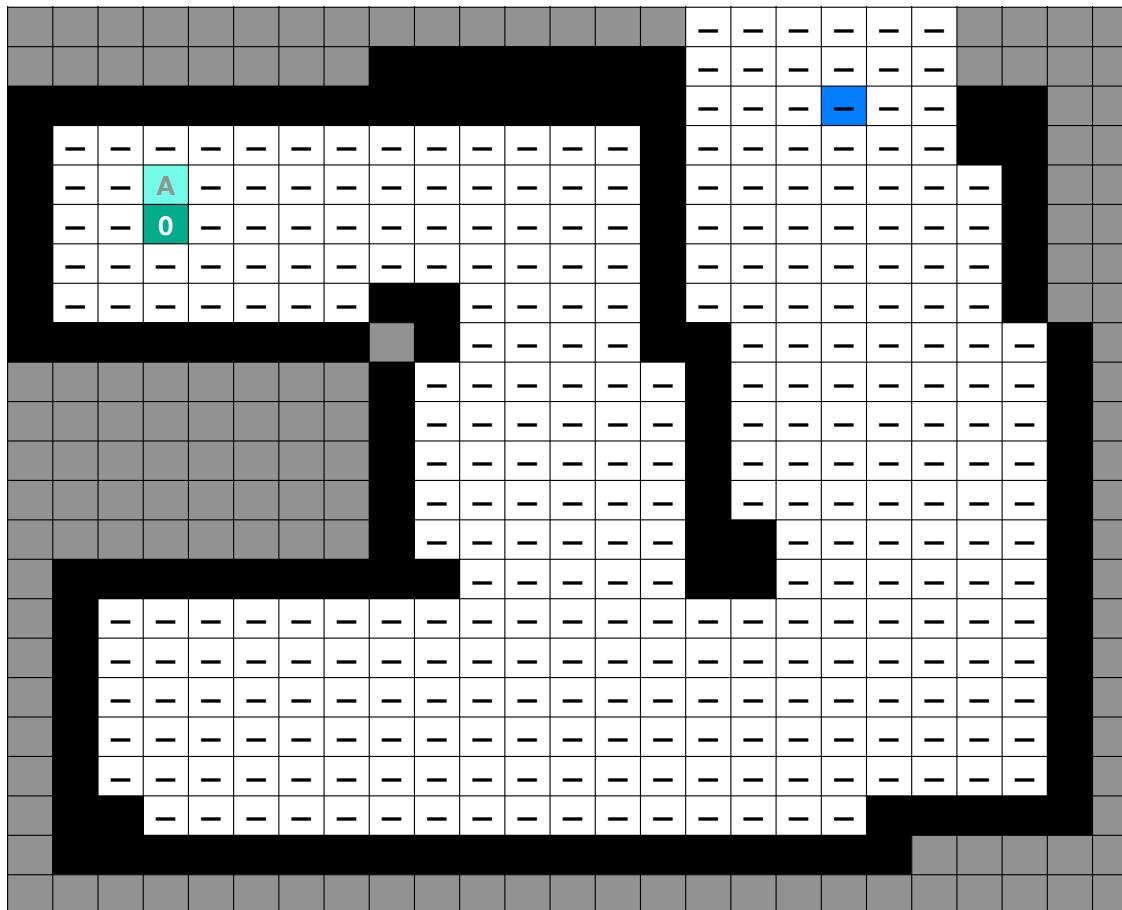
visit_queue



current_node

Add to visit queue, if not previously visited or queued

**Queue first
neighbor**



visit_queue



current_node

Initialize :

All nodes to have no parent, max distance, and as unvisited

Start node to have no parent and zero distance

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If Distance of neighbor > Distance of current node + ...

Cost to move from current node to neighbor

Then Update neighbor's parent to be current node and ...

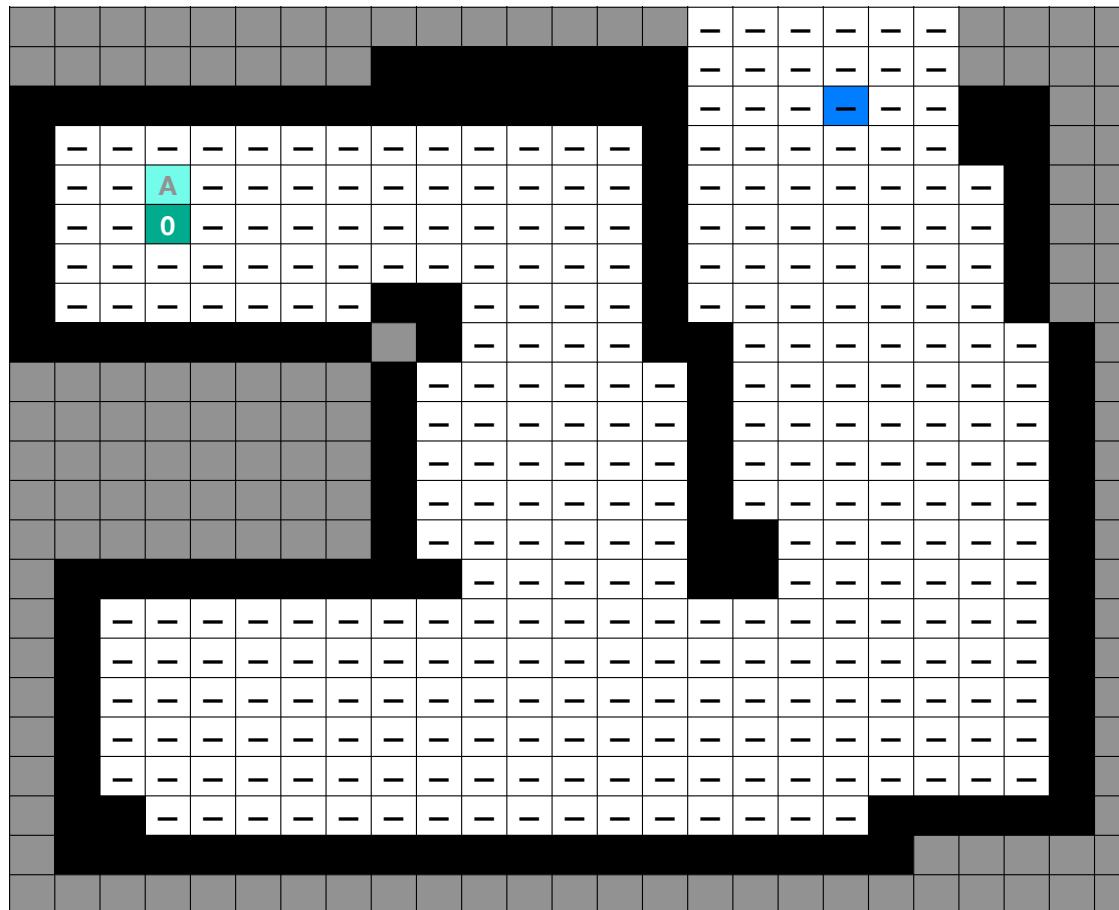
distance to be distance of current node + cost to move

If Distance of neighbor > Distance of current node + ...

-

0

Cost to move from current node to neighbor



1

visit_queue



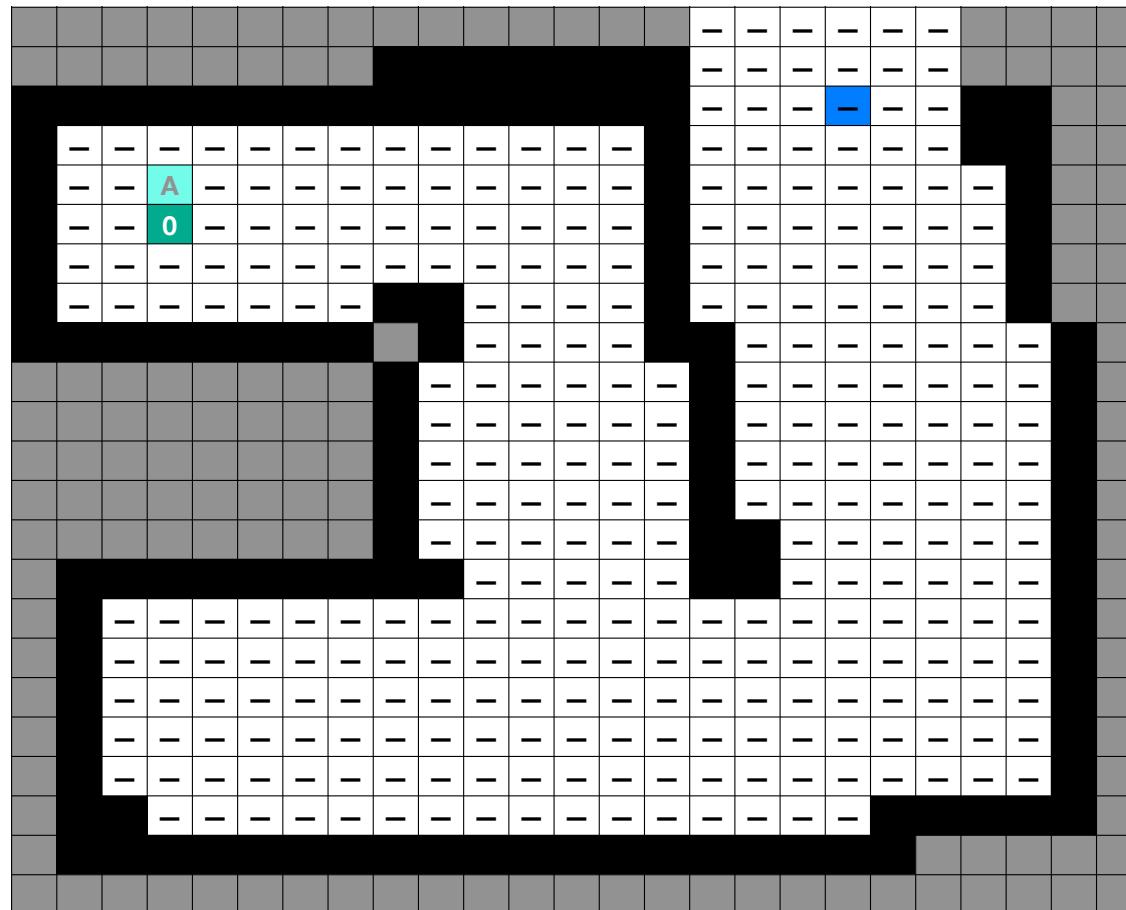
A

■

current_node

`- > 0 + 1`

`true`

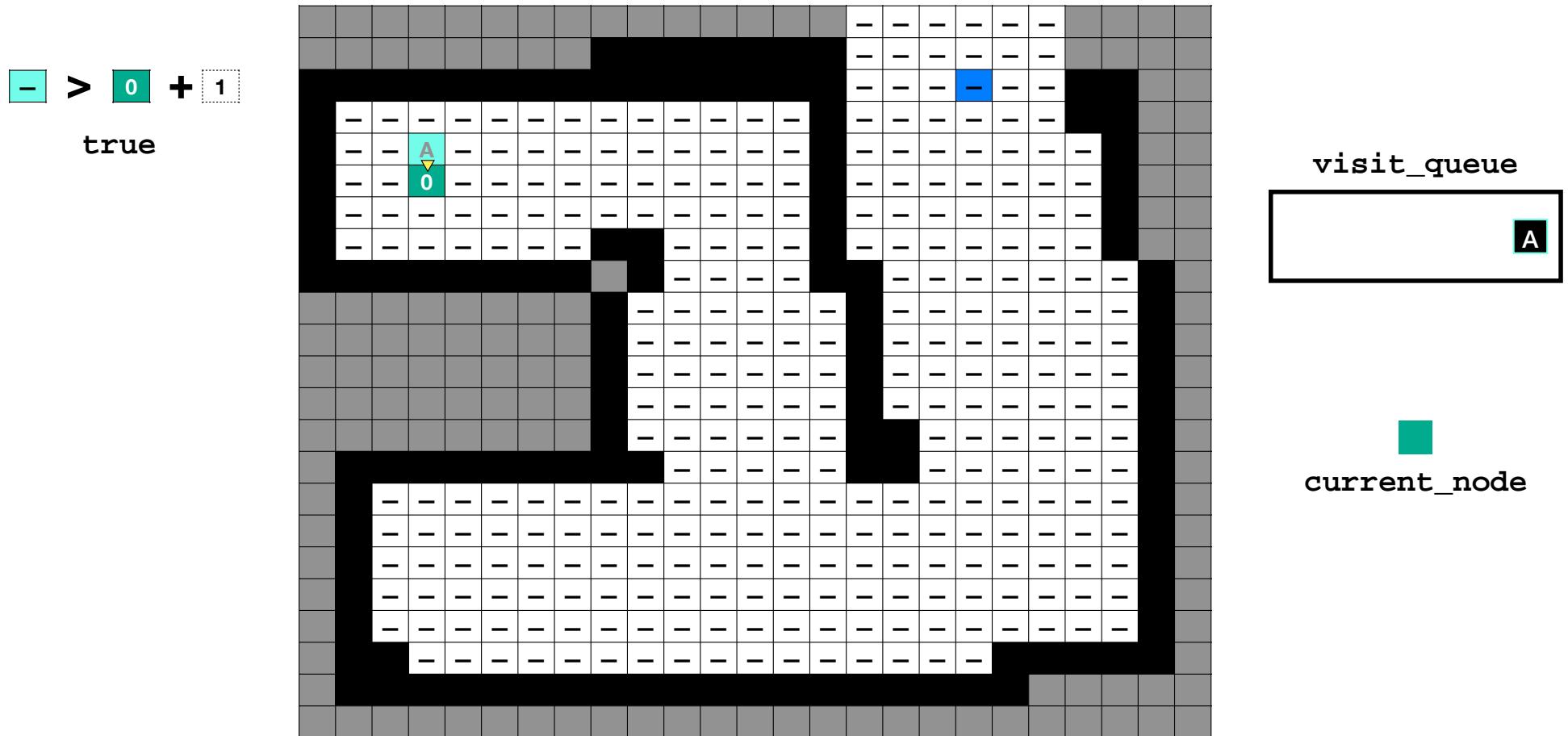


`visit_queue`



`current_node`

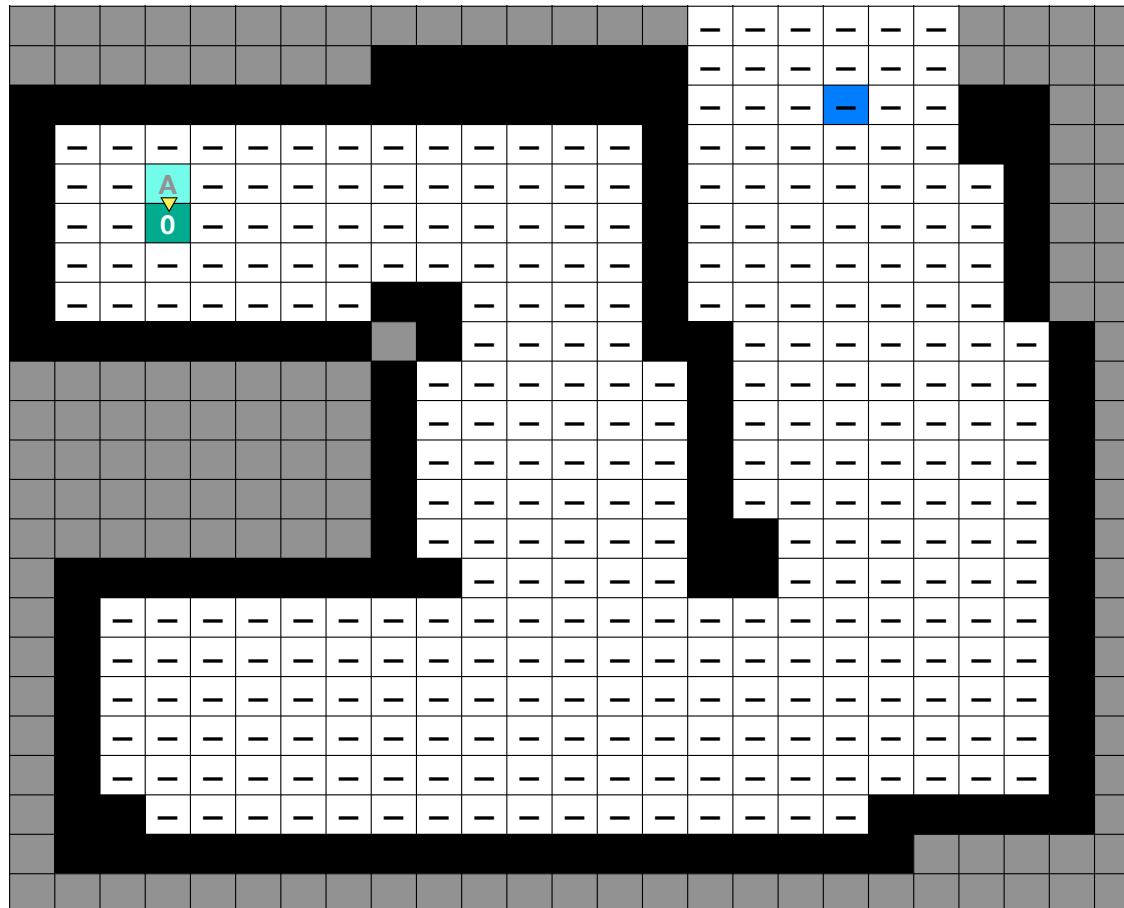
Then Update neighbor's parent to be current node and ...



update neighbor's distance to be distance of current node + cost to move

- > 0 + 1

true



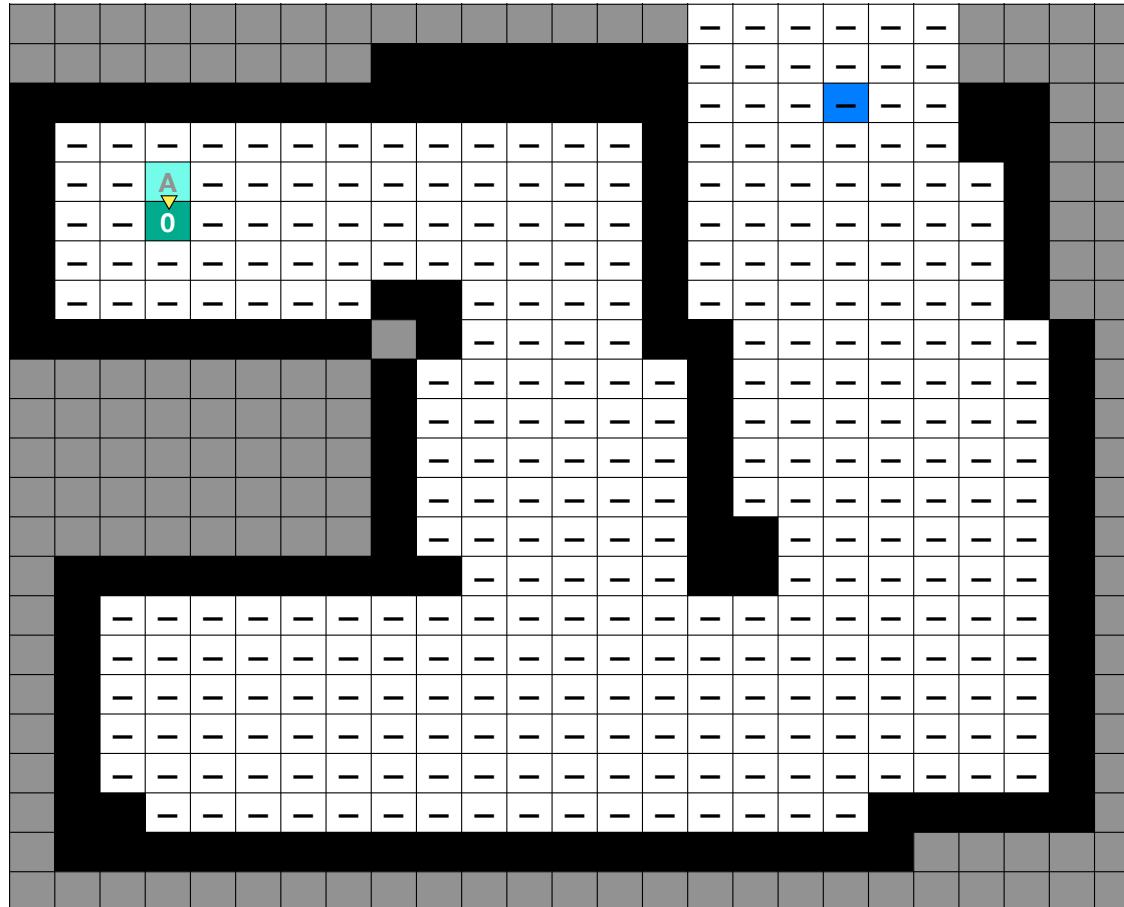
visit_queue



current_node

update neighbor's distance to be distance of current node + cost to move

$$0 + 1$$



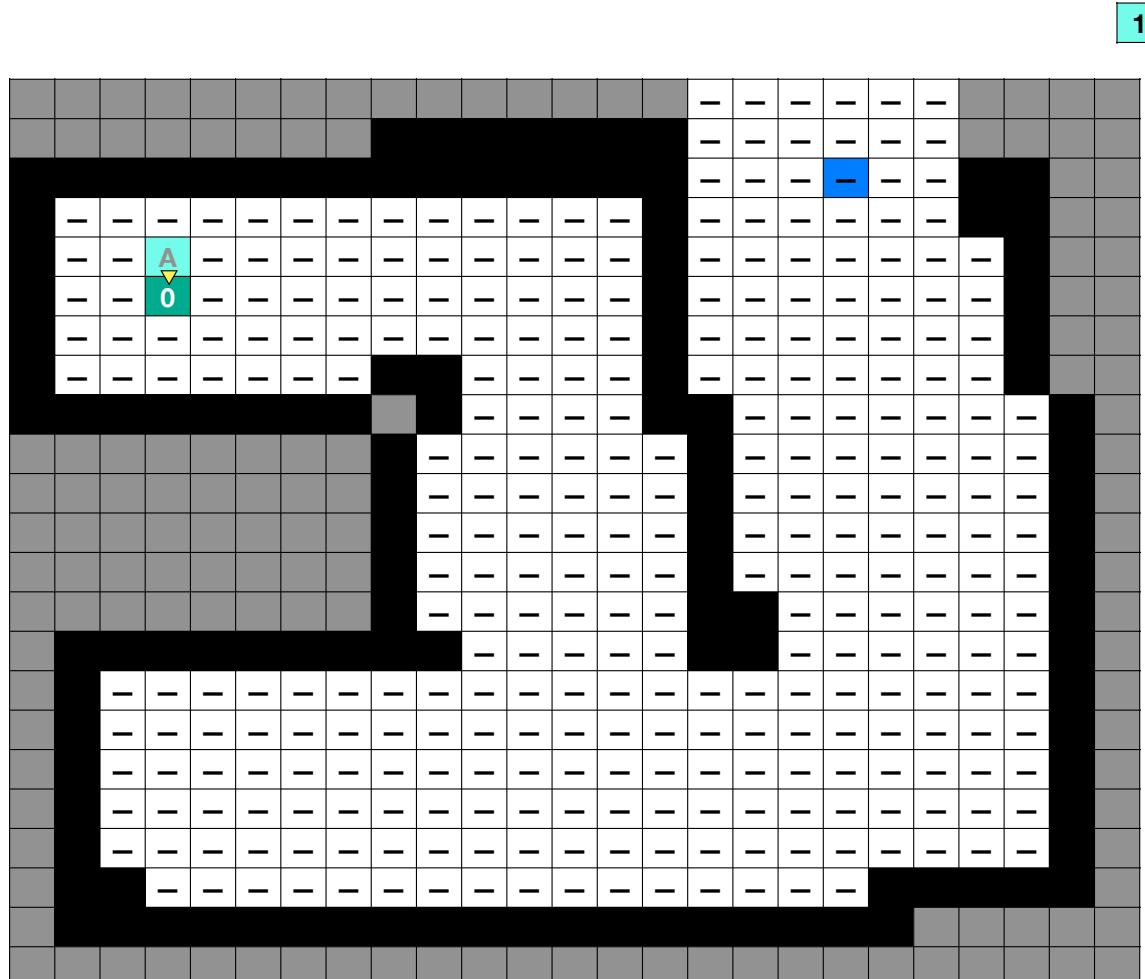
visit_queue

A



current_node

update neighbor's distance to be distance of current node + cost to move

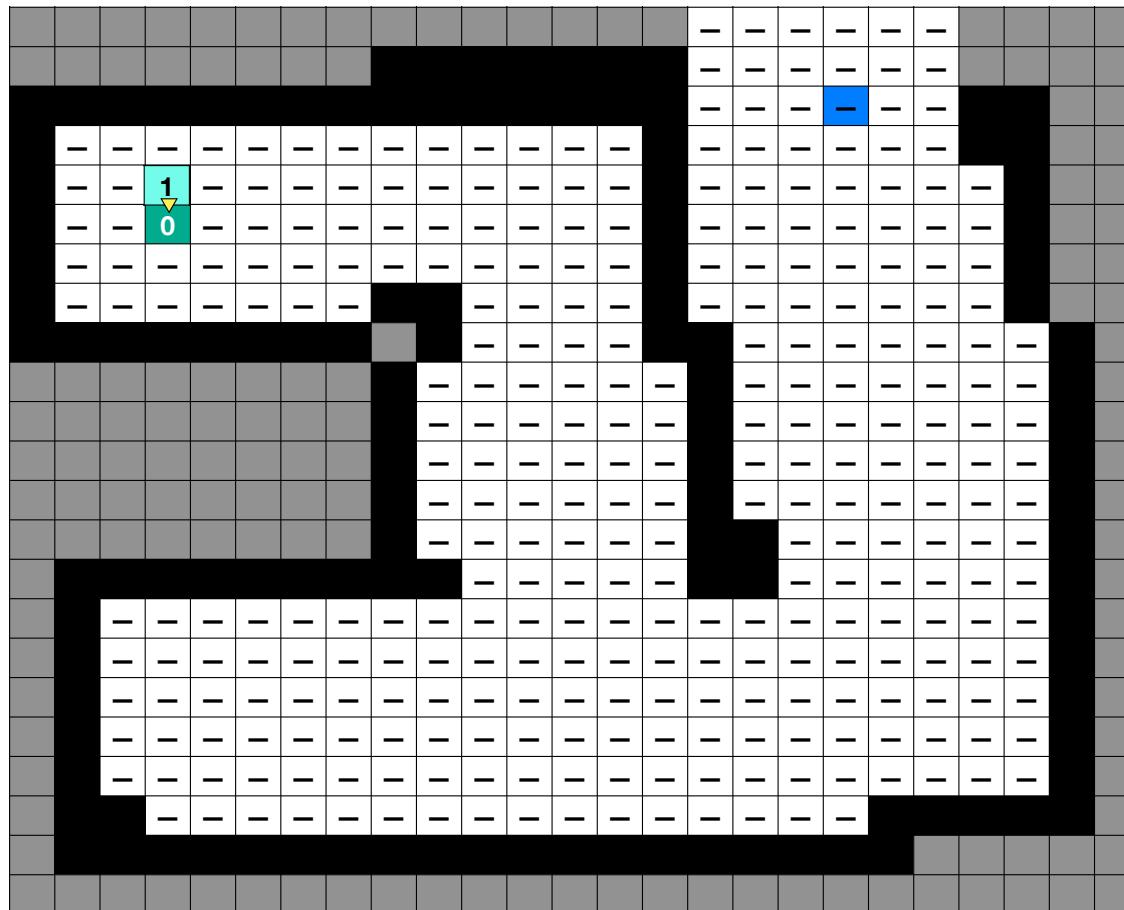


visit_queue

A

current_node

update neighbor's distance to be distance of current node + cost to move



visit_queue



current_node

Initialize :

All nodes to have no parent, max distance, and as unvisited

Start node to have no parent and zero distance

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Iterate : While visit list not empty and currently visited node is not the goal

Dequeue new current node to visit and mark it as visited

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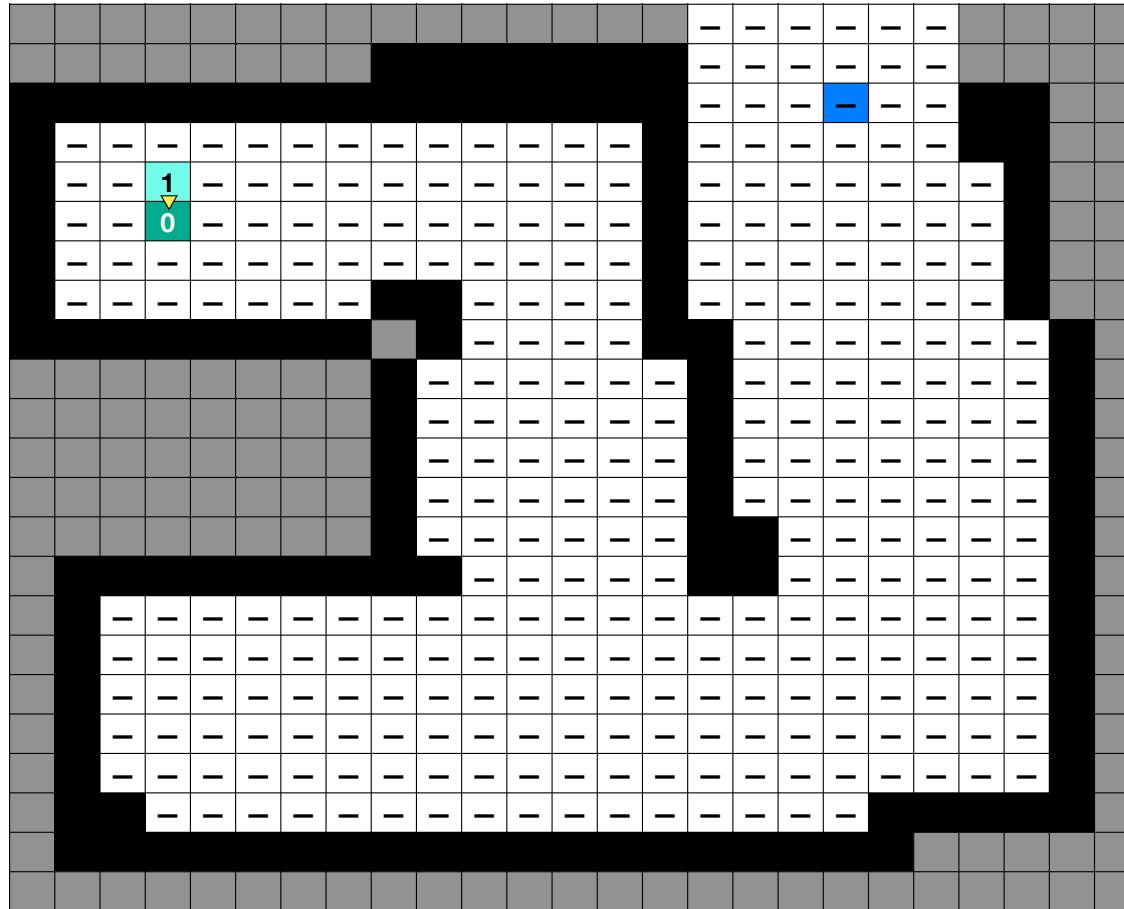
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Cost to move from current node to neighbor

Then Update neighbor's parent to be current node and ...

distance to be distance of current node + cost to move

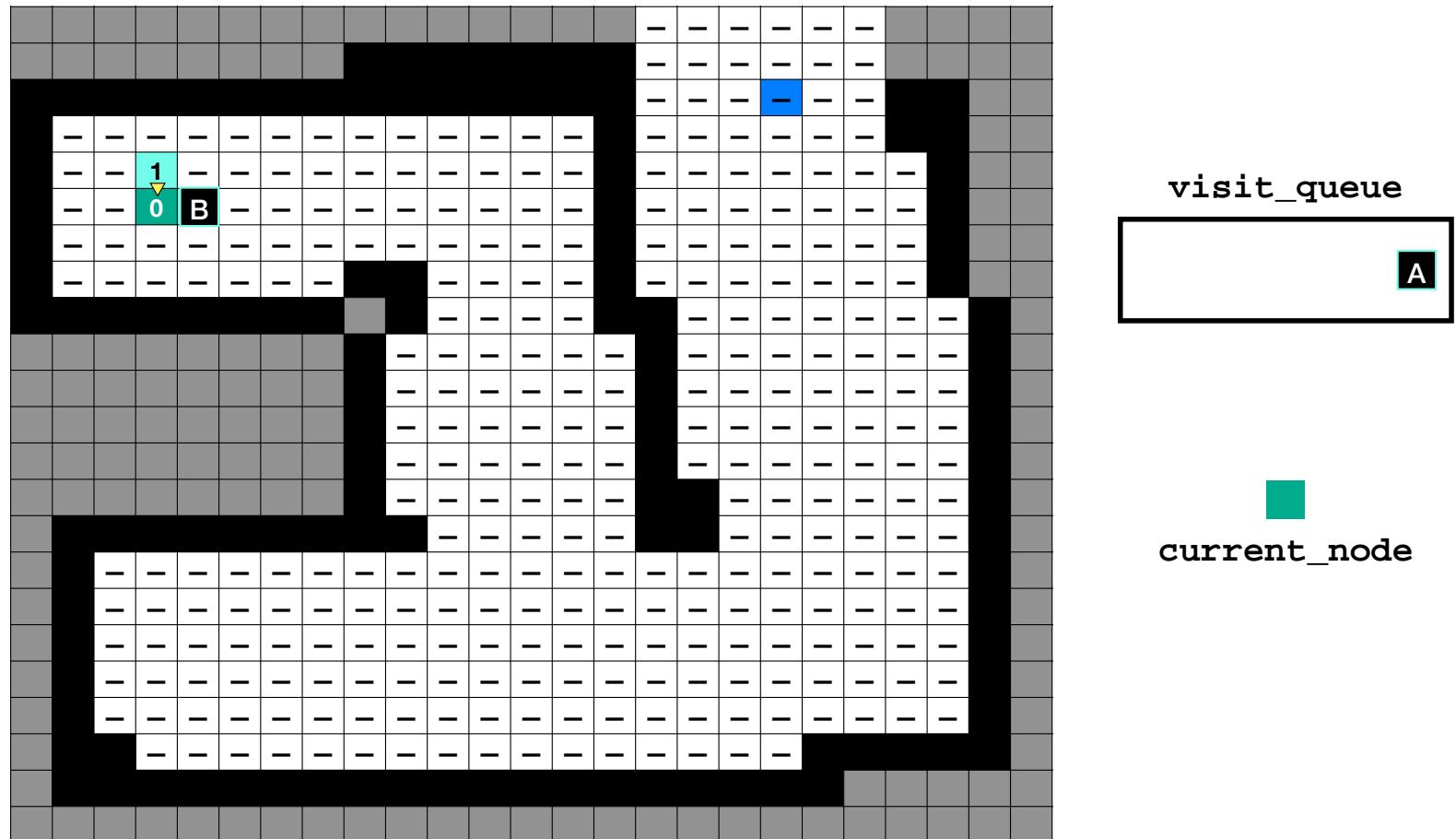


`visit_queue`

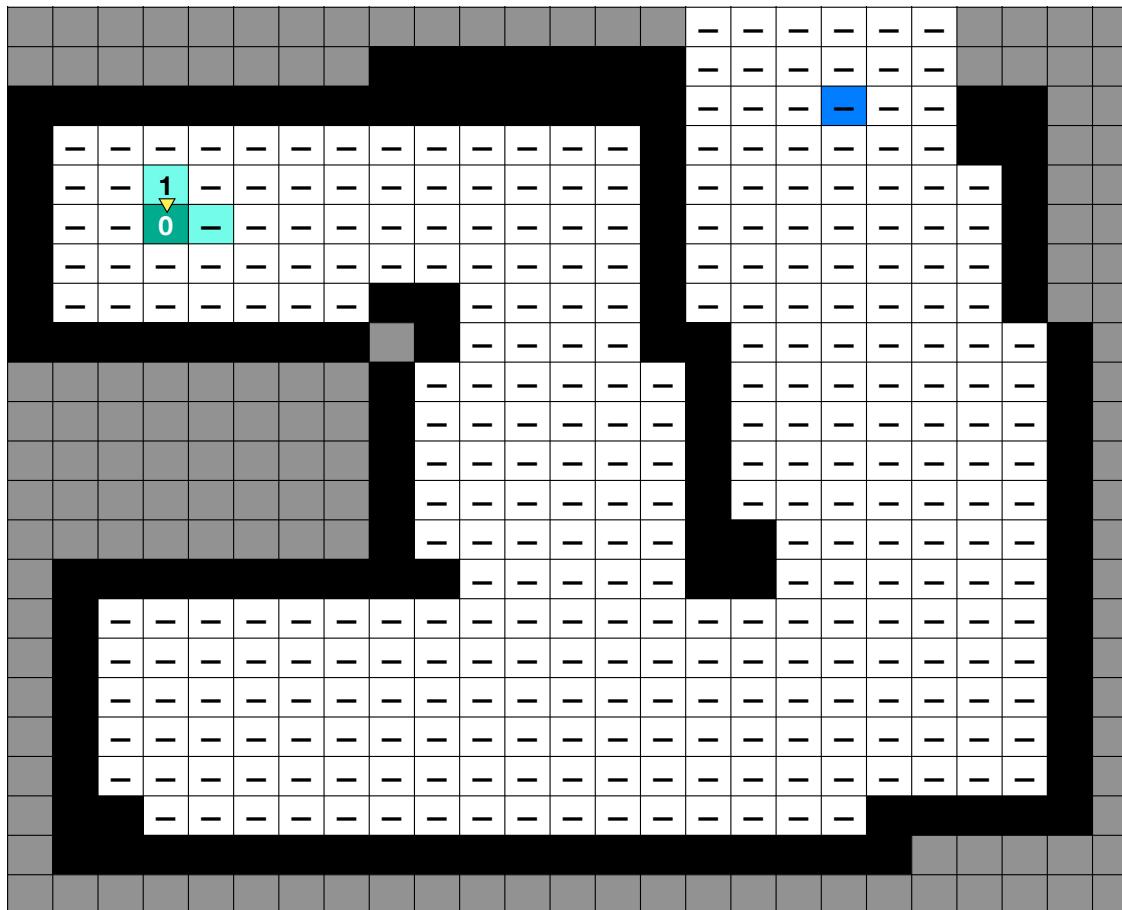


`current_node`

**Queue second
neighbor**



**Queue second
neighbor**

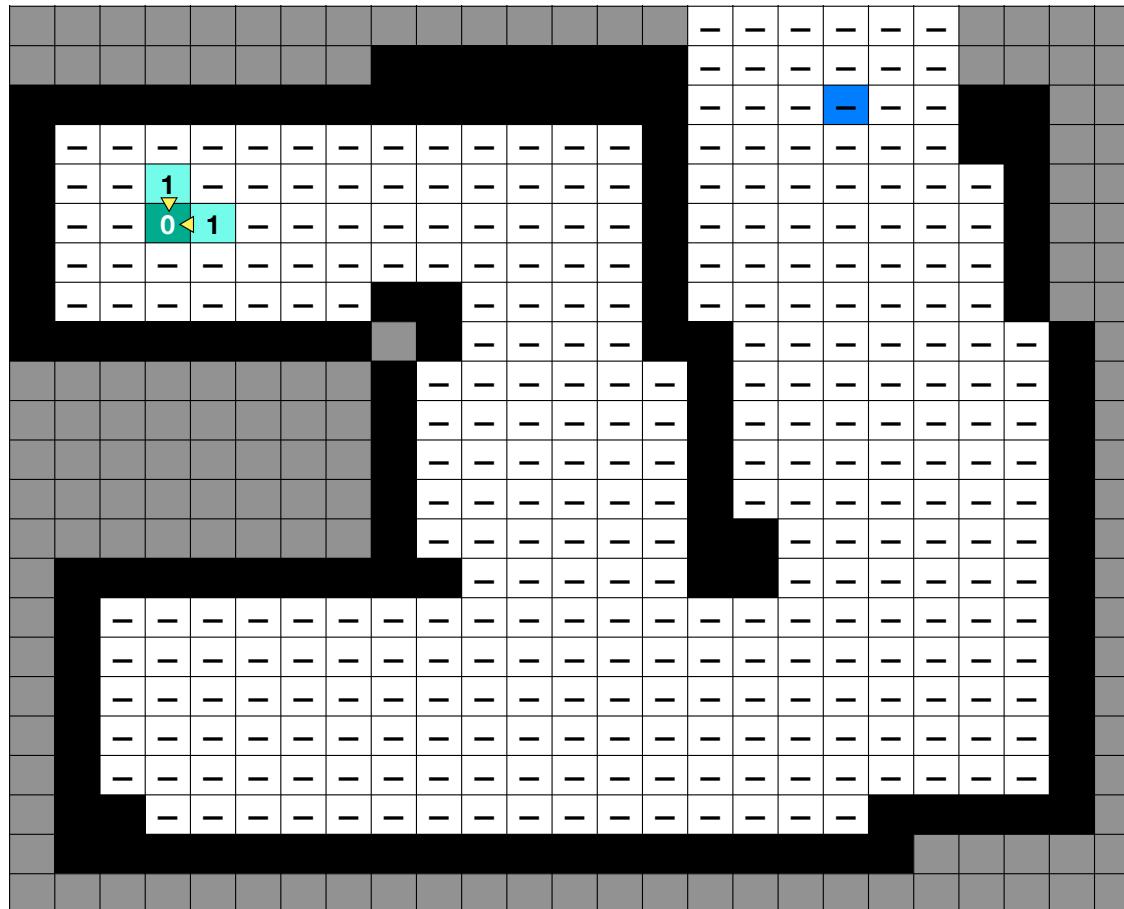


visit_queue



current_node

**Assign
distance and
parent**

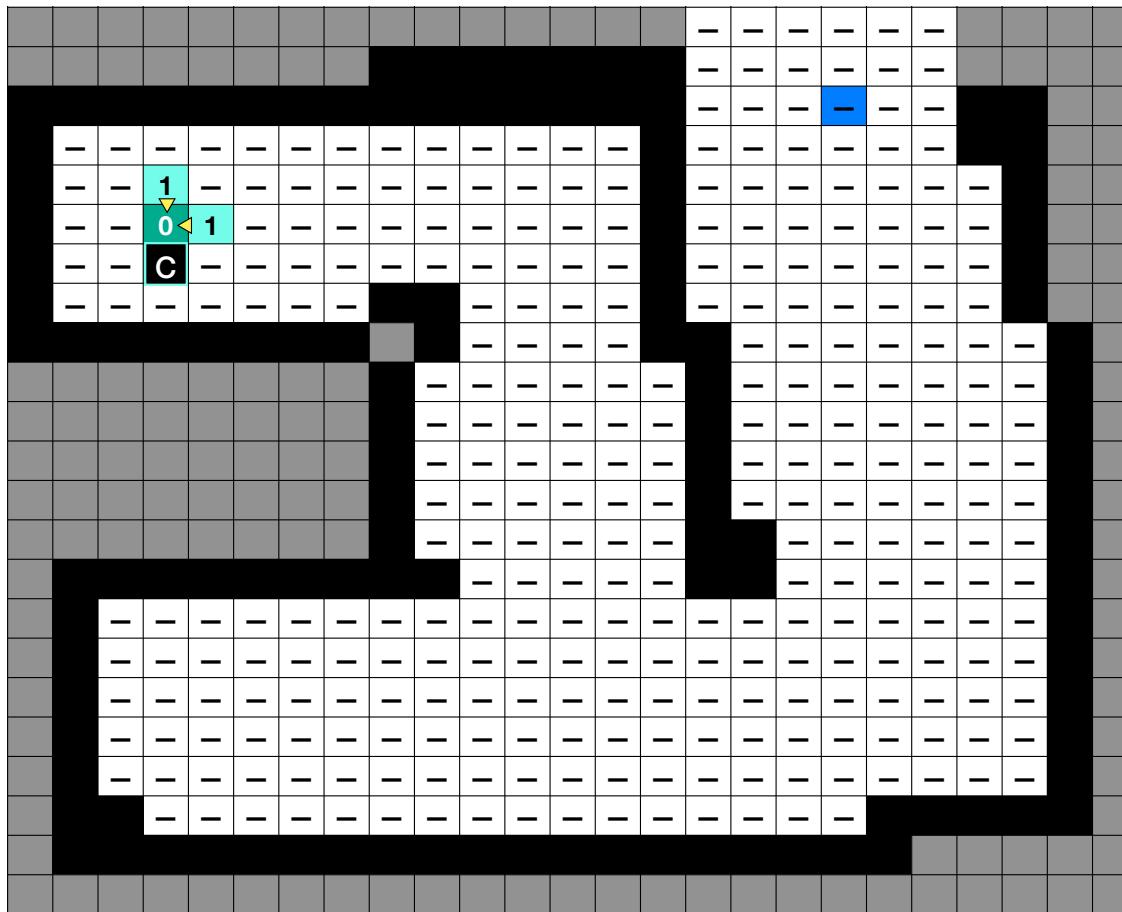


visit_queue



current_node

**Queue third
neighbor**

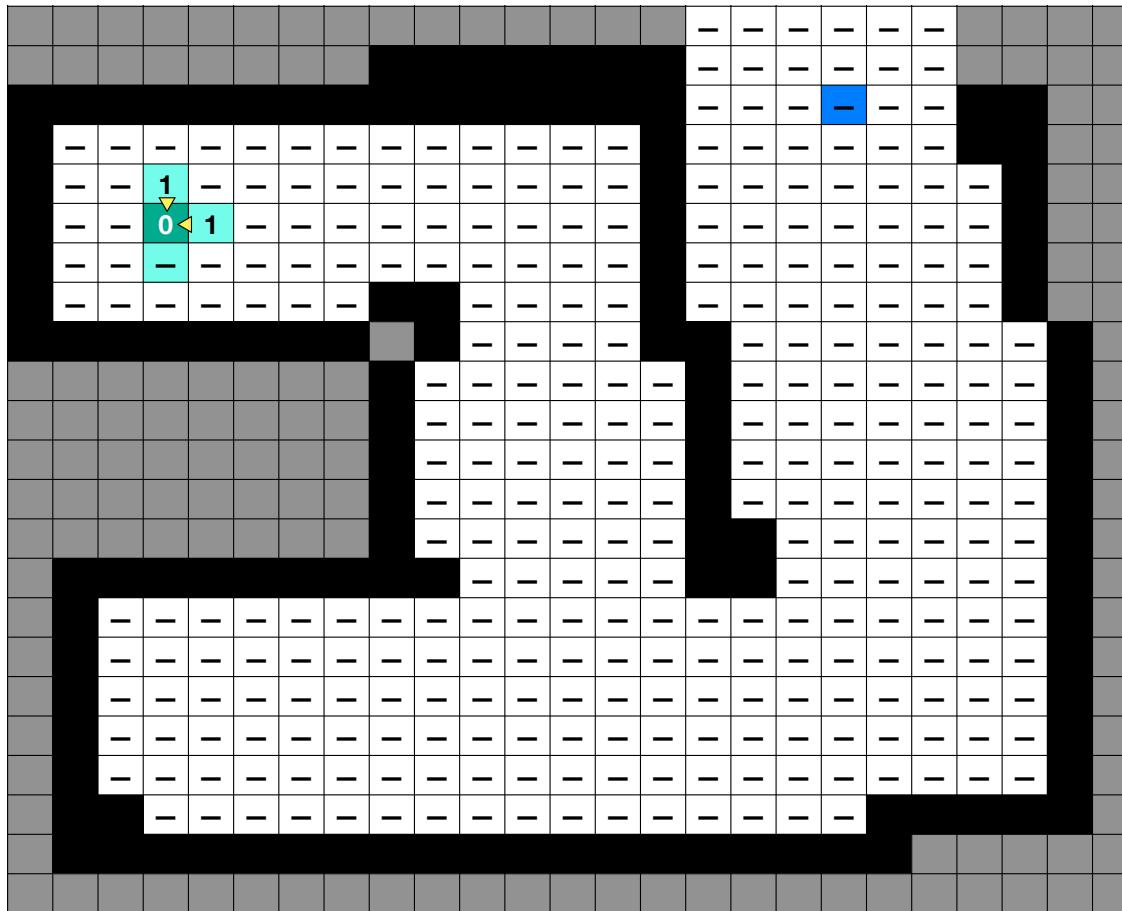


visit_queue



current_node

**Queue third
neighbor**



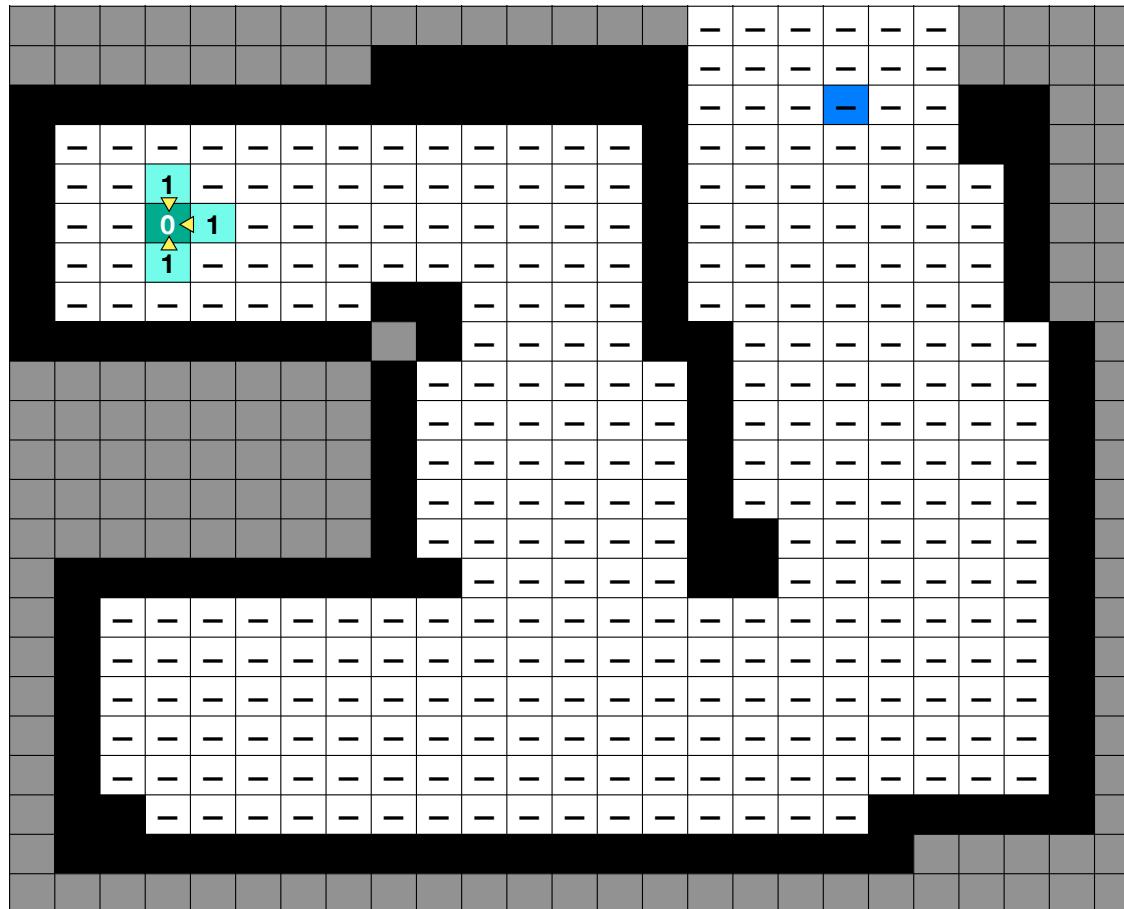
visit_queue

C B A



current_node

**Assign
distance and
parent**



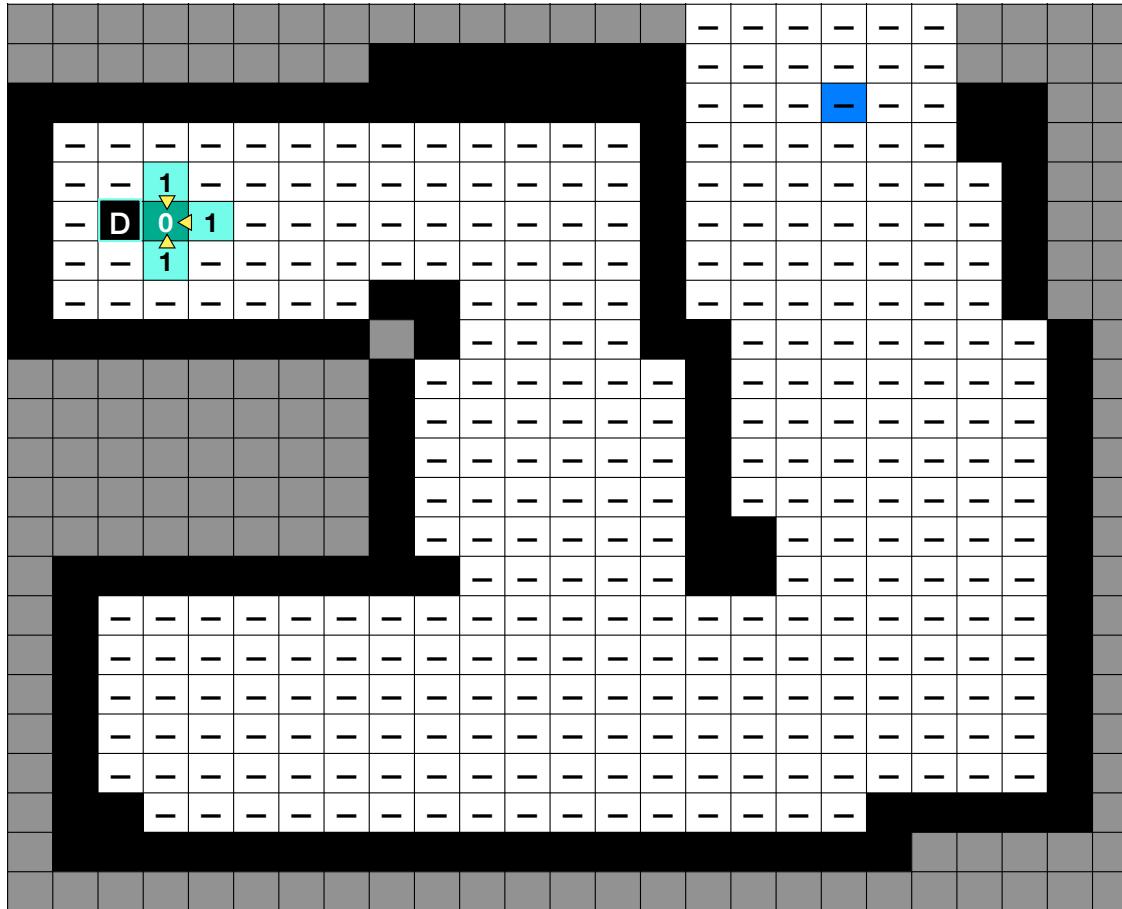
visit_queue

C B A



current_node

**Queue last
neighbor**



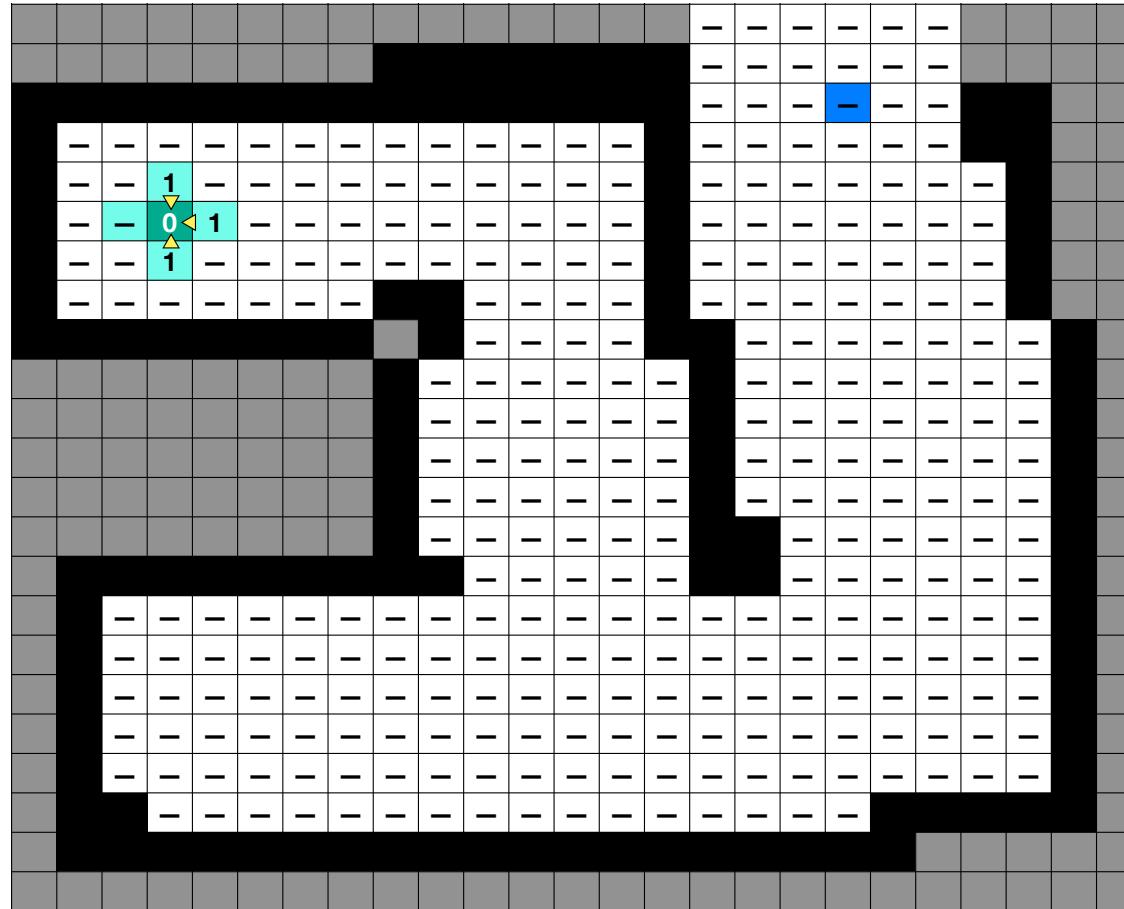
visit_queue

C B A



current_node

**Queue last
neighbor**



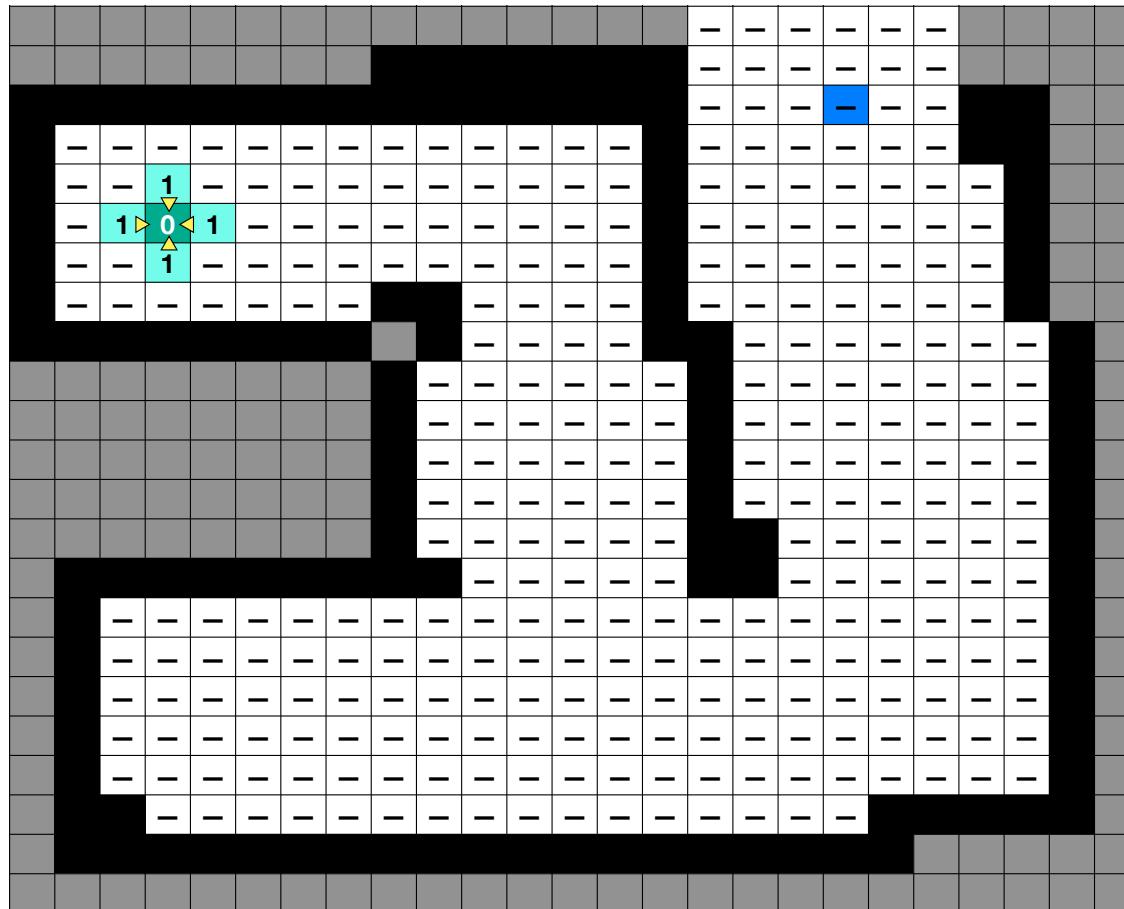
visit_queue

D C B A



current_node

**Assign
distance and
parent**

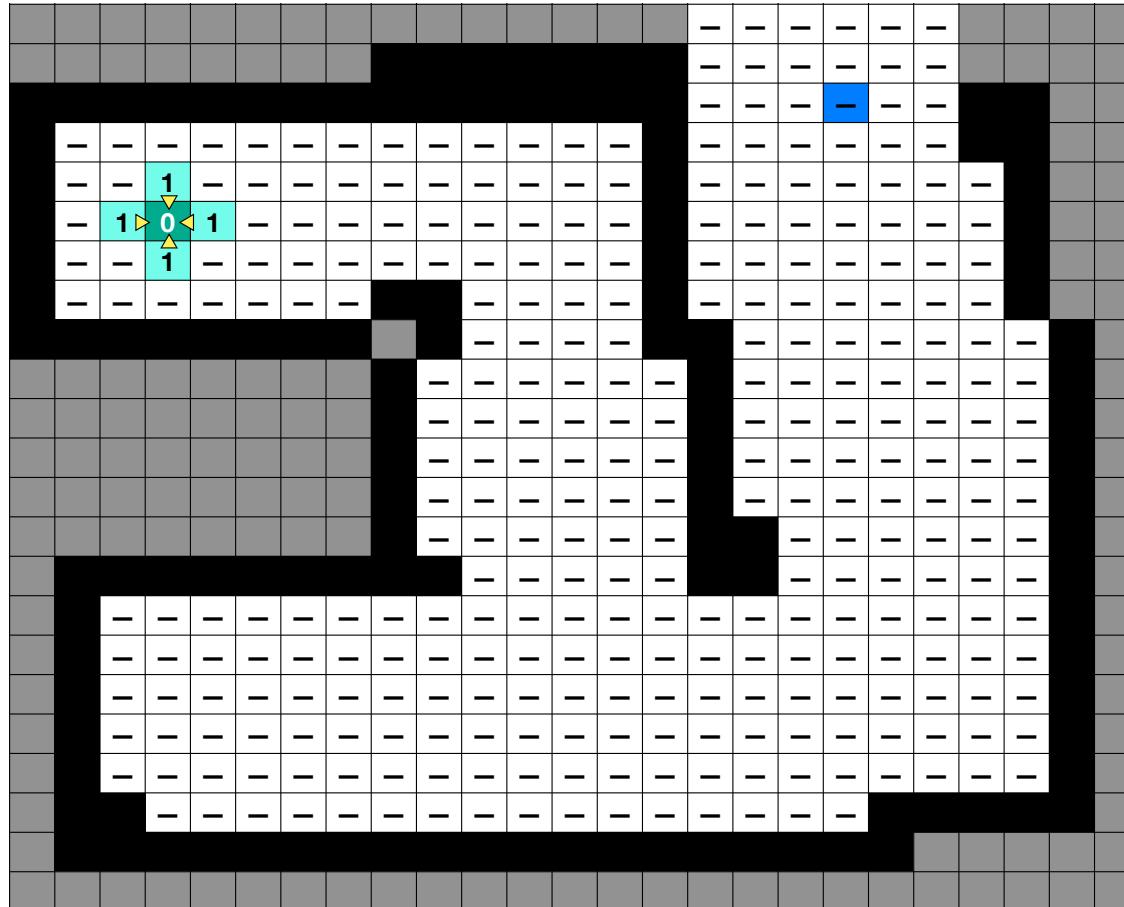


visit_queue

D C B A



current_node



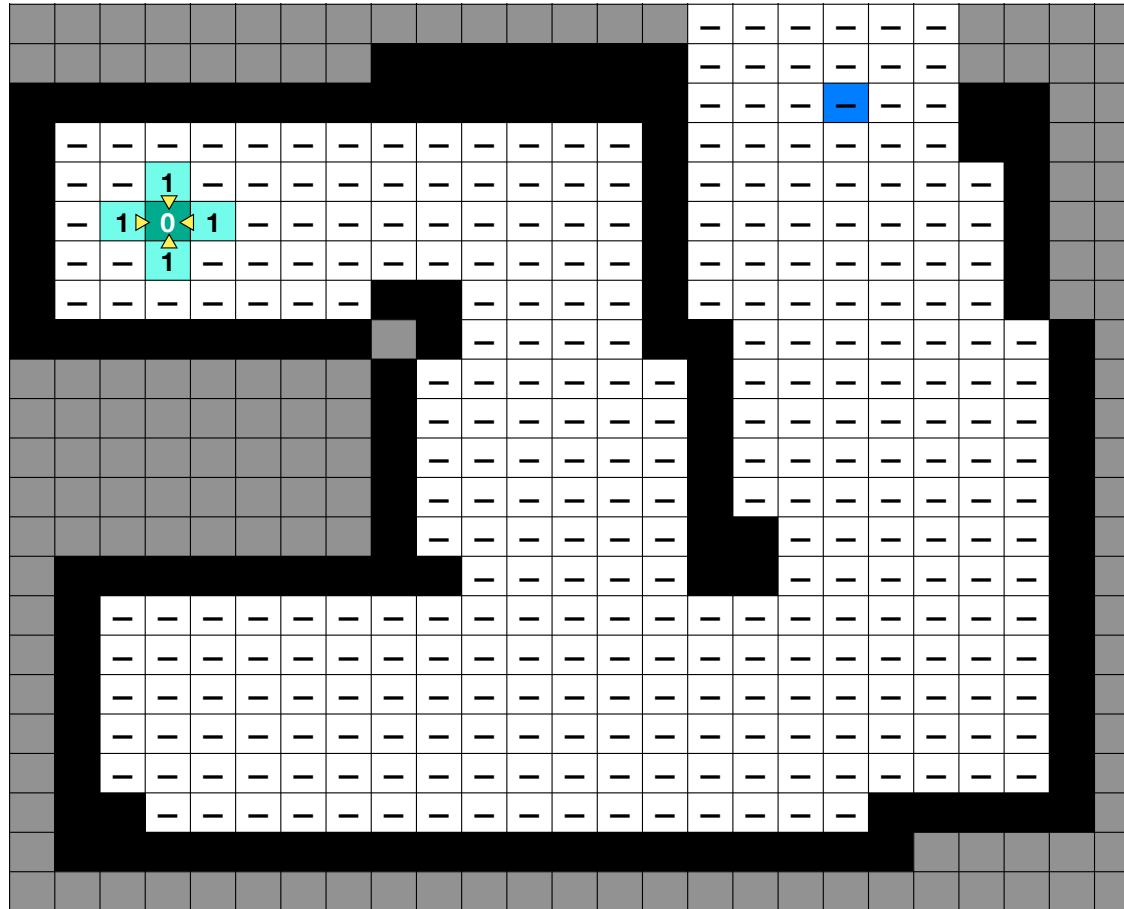
visit_queue

D C B A



current_node

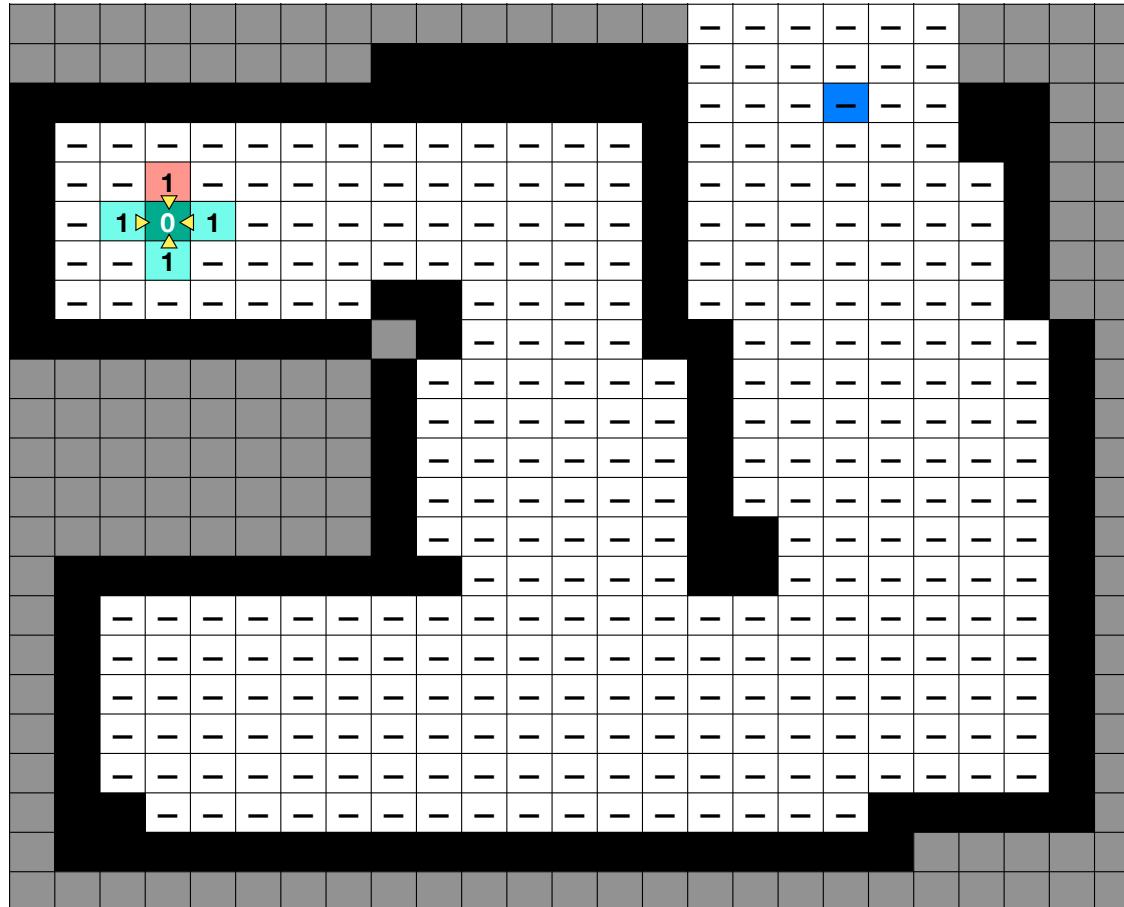
**Current node
fully processed**



`visit_queue`

D C B A

`current_node`



visit_queue

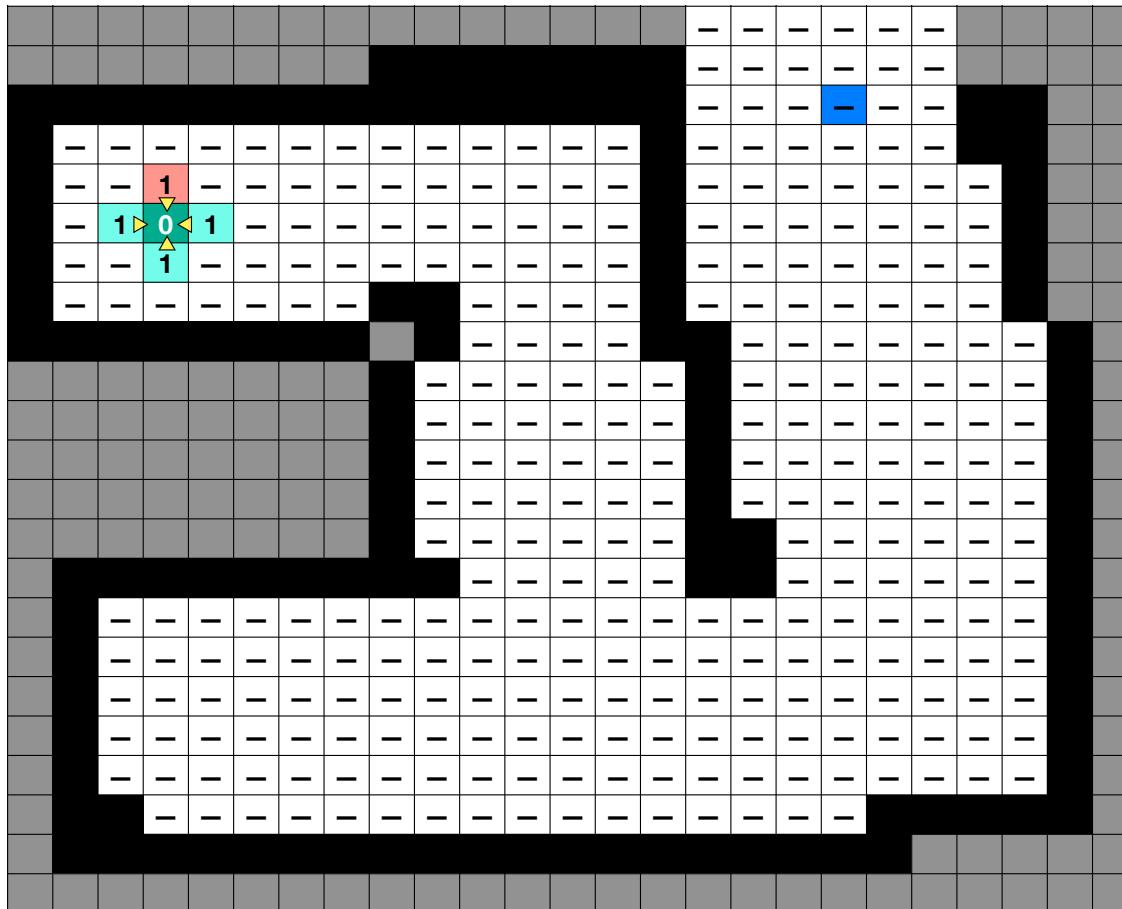
D C B

A

current_node

***Dequeue from
visit queue***

**Process
current node**



visit_queue

D C B

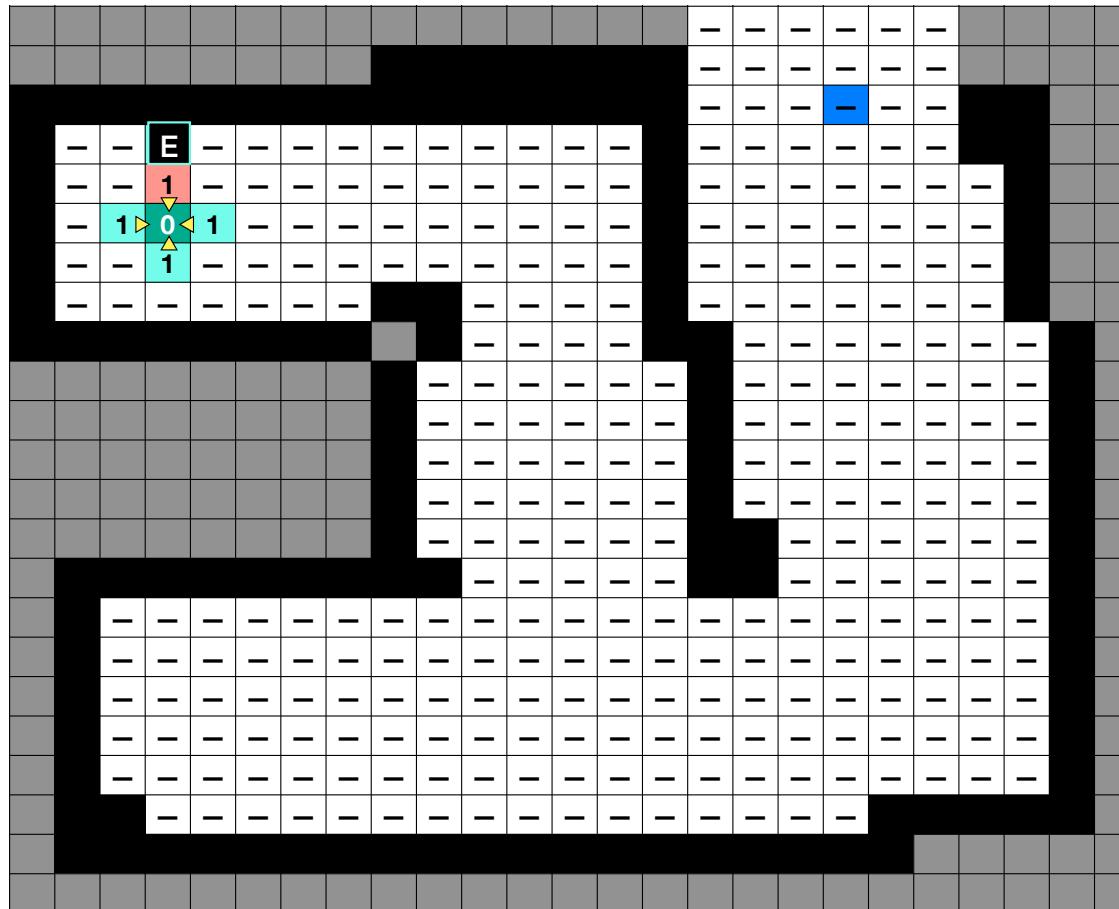
A

current_node

**Dequeue from
visit queue**

**Process
current node**

**Queue first
neighbor**



visit_queue

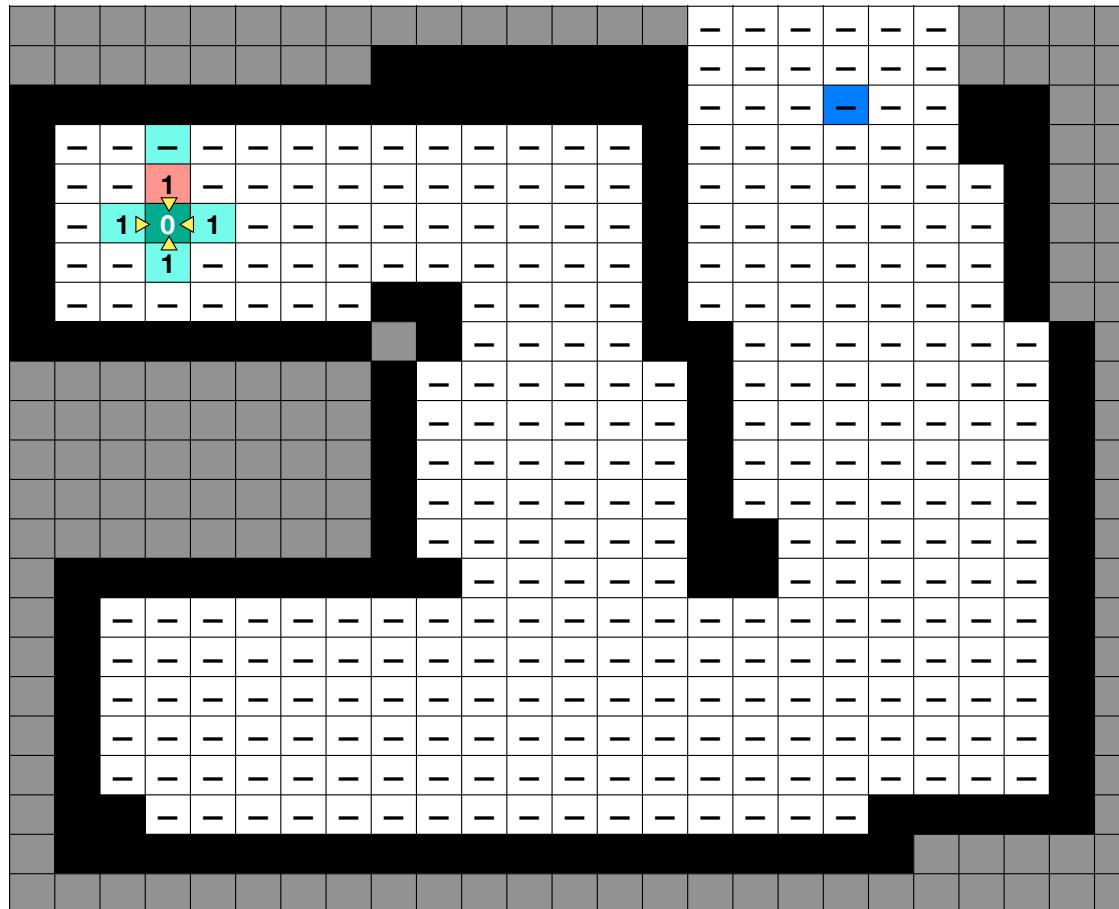
D C B

A

current_node

**Process
current node**

**Queue first
neighbor**



visit_queue

E D C B

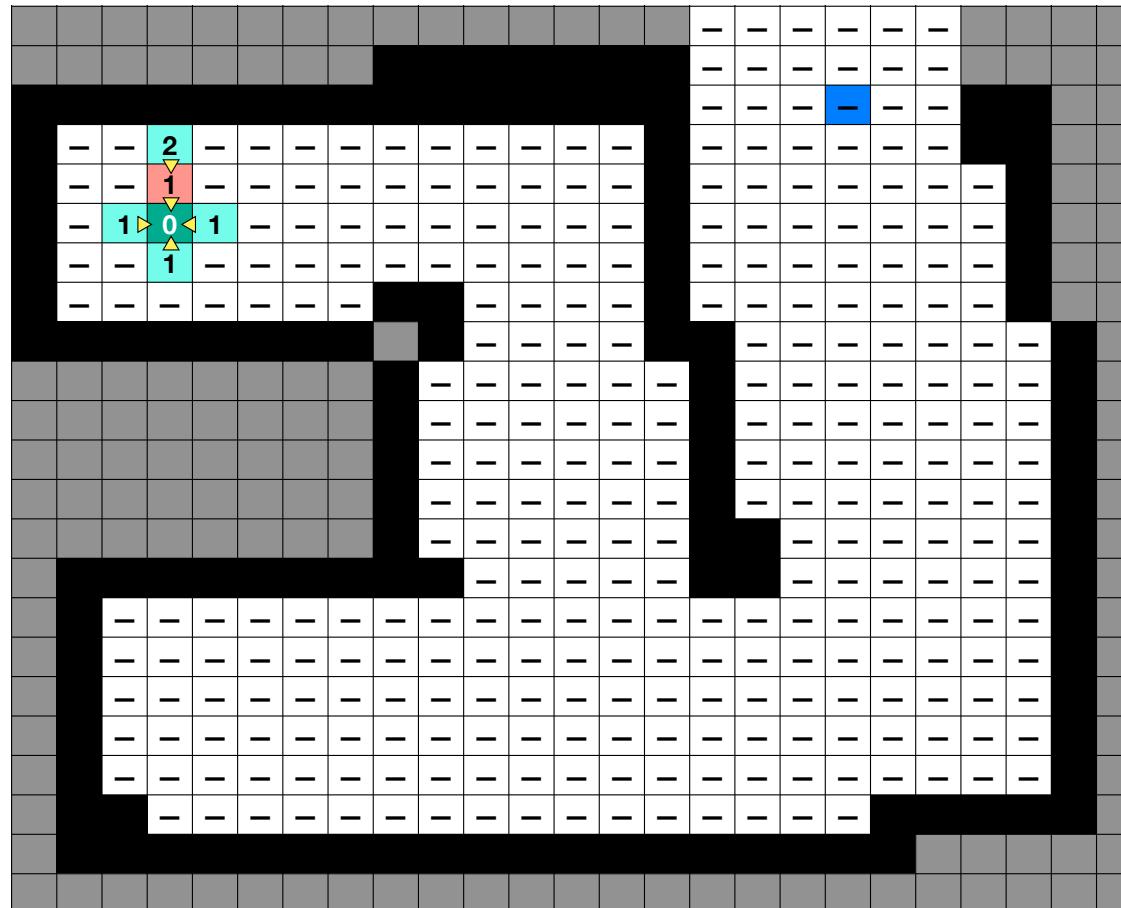
A

current_node

**Process
current node**

**Queue first
neighbor**

**Assign
distance and
parent**



visit_queue

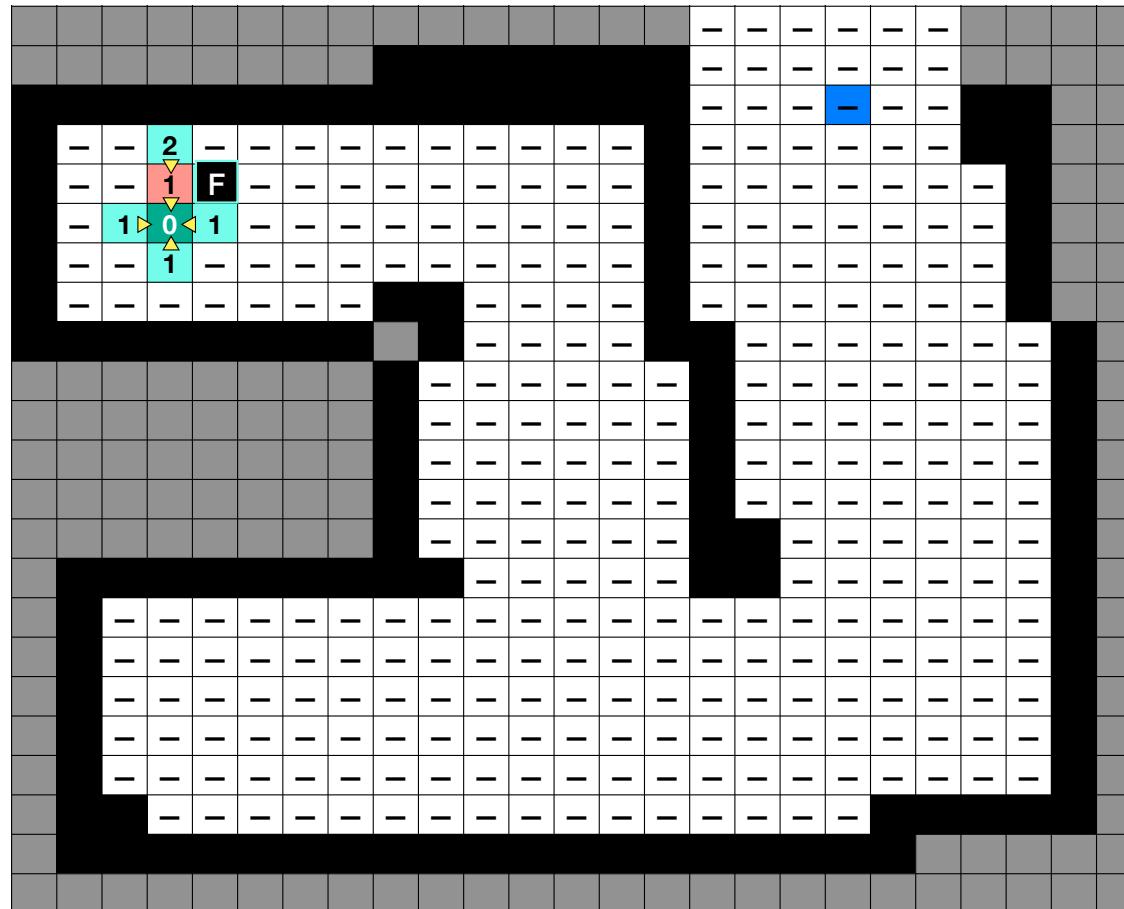
E D C B

A

current_node

**Process
current node**

**Queue second
neighbor**



visit_queue

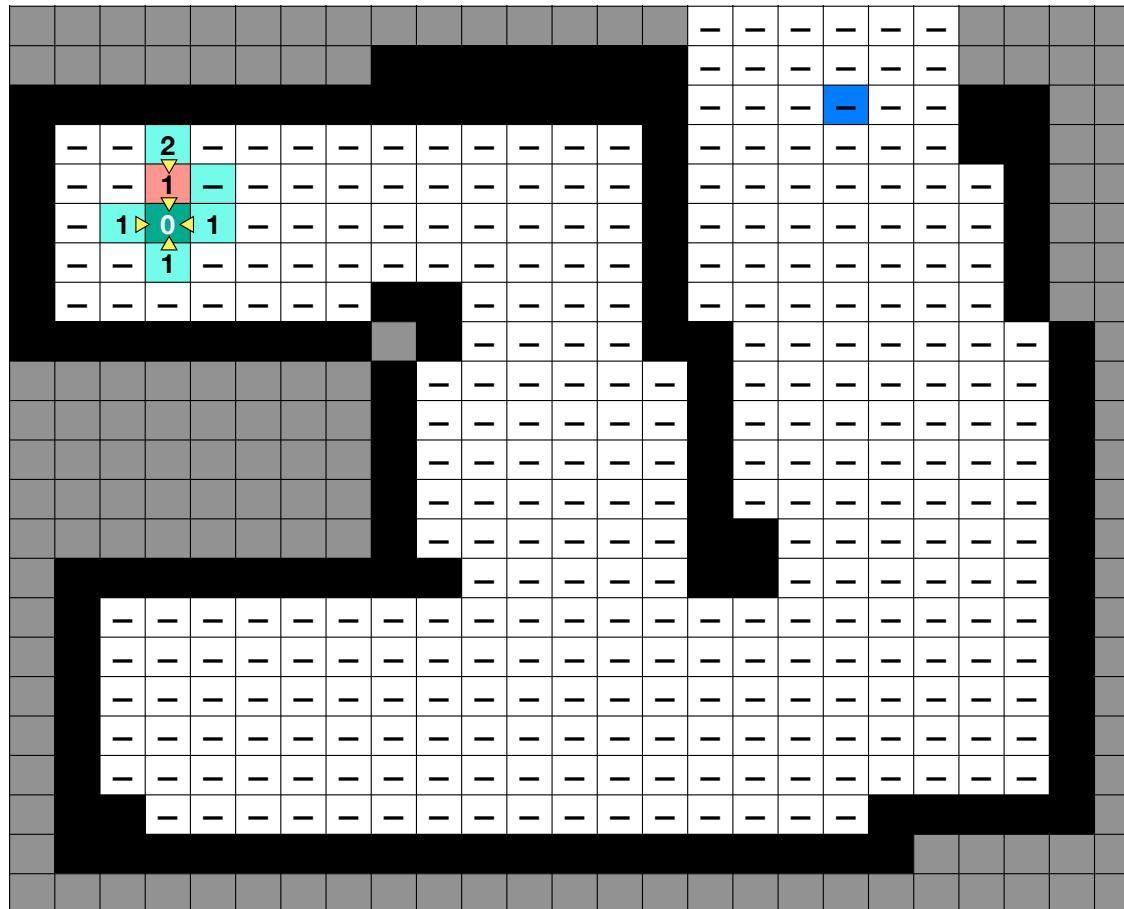
E D C B

A

current_node

**Process
current node**

**Queue second
neighbor**



visit_queue

F E D C B

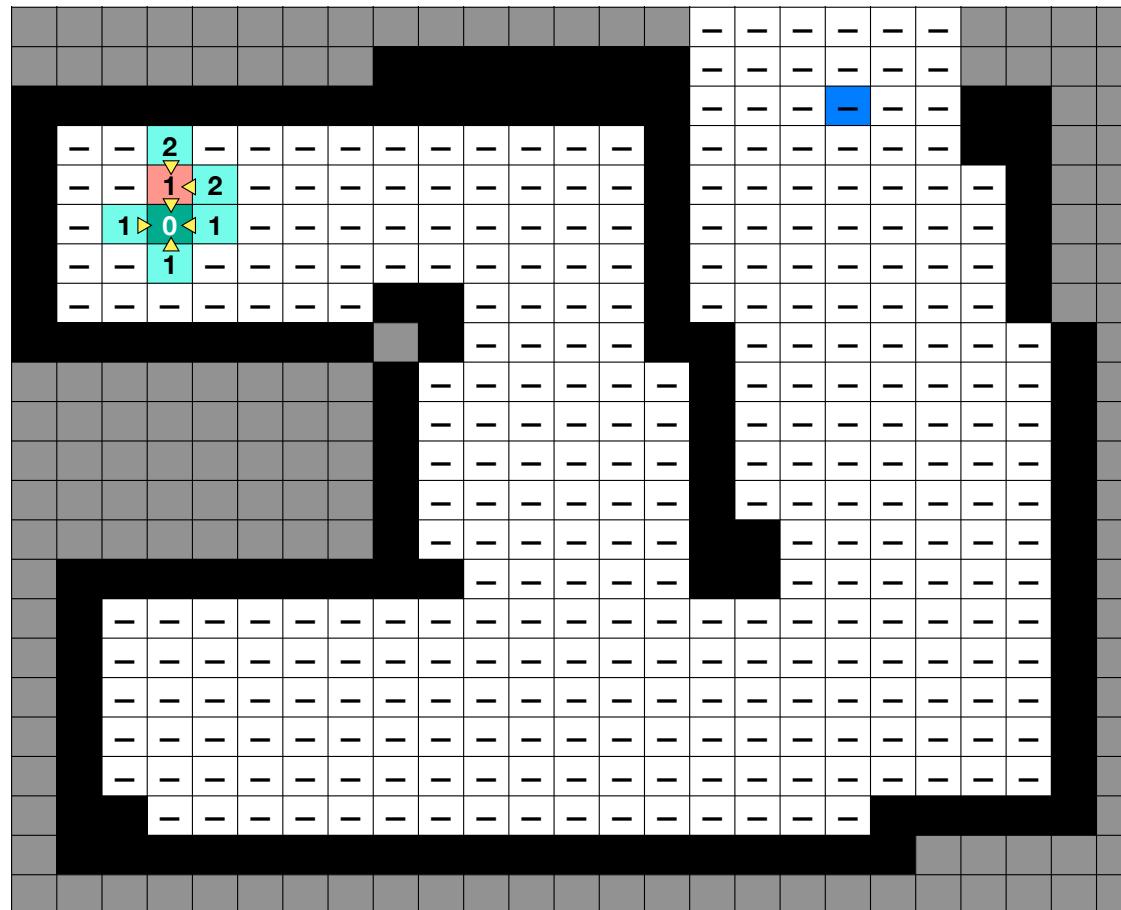
A

current_node

Process current node

Queue second neighbor

Assign distance and parent



visit_queue

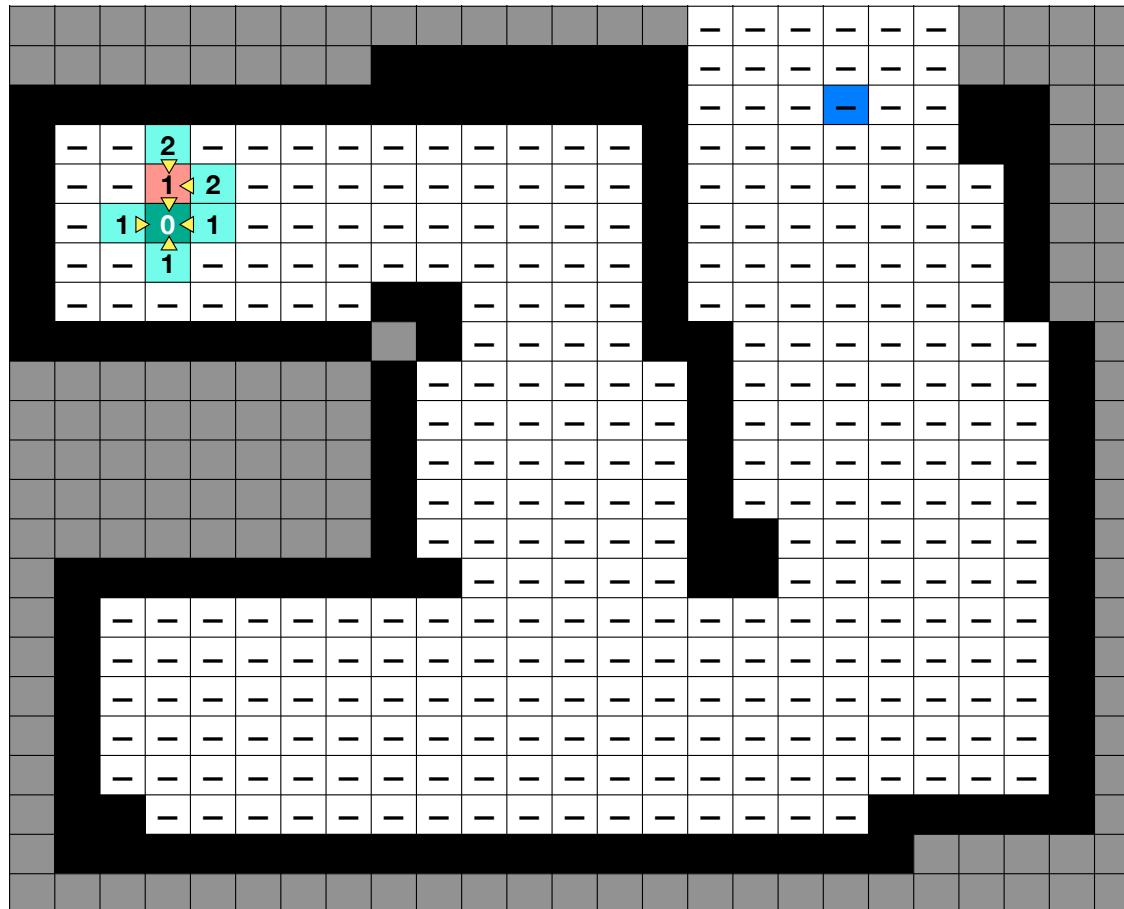
F E D C B

A

current_node

**Process
current node**

**Do not queue
third neighbor
(already
visited)**



visit_queue

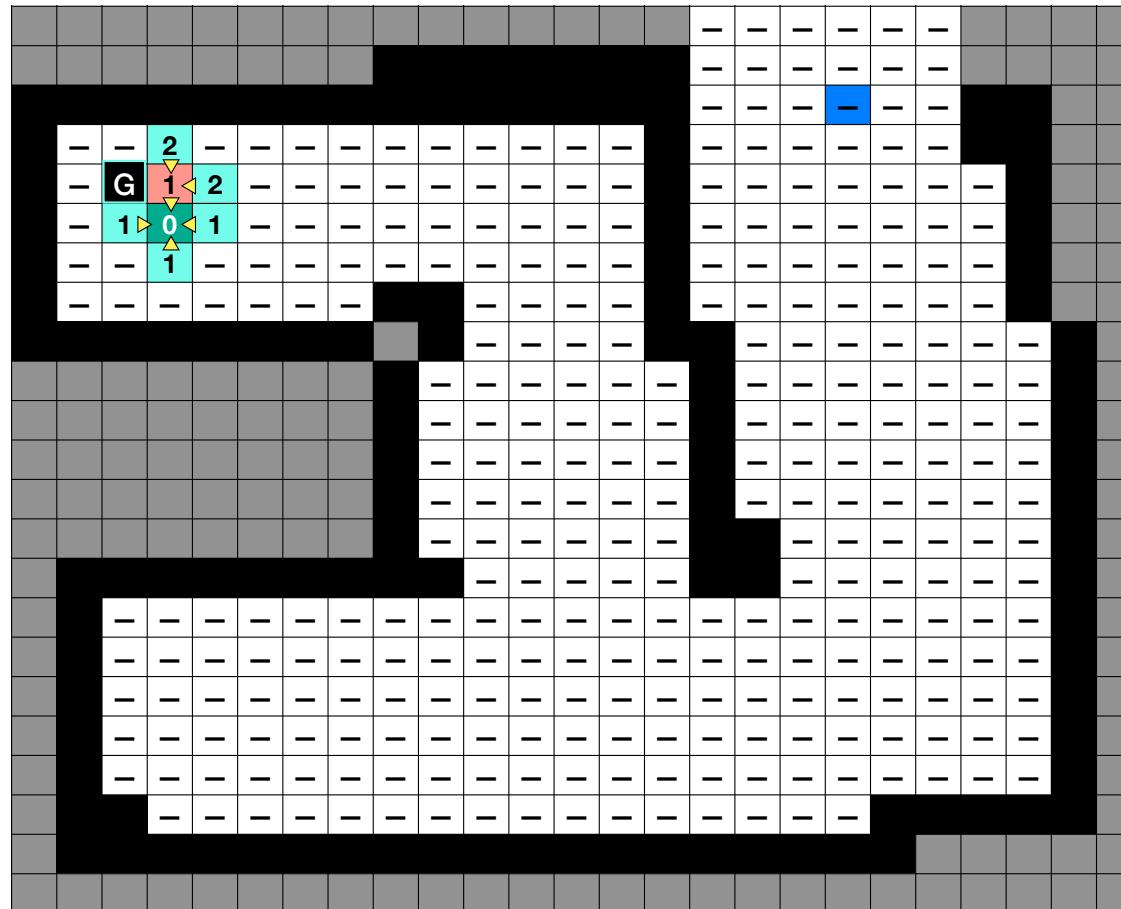
F E D C B

A

current_node

**Process
current node**

**Queue last
neighbor**



visit_queue

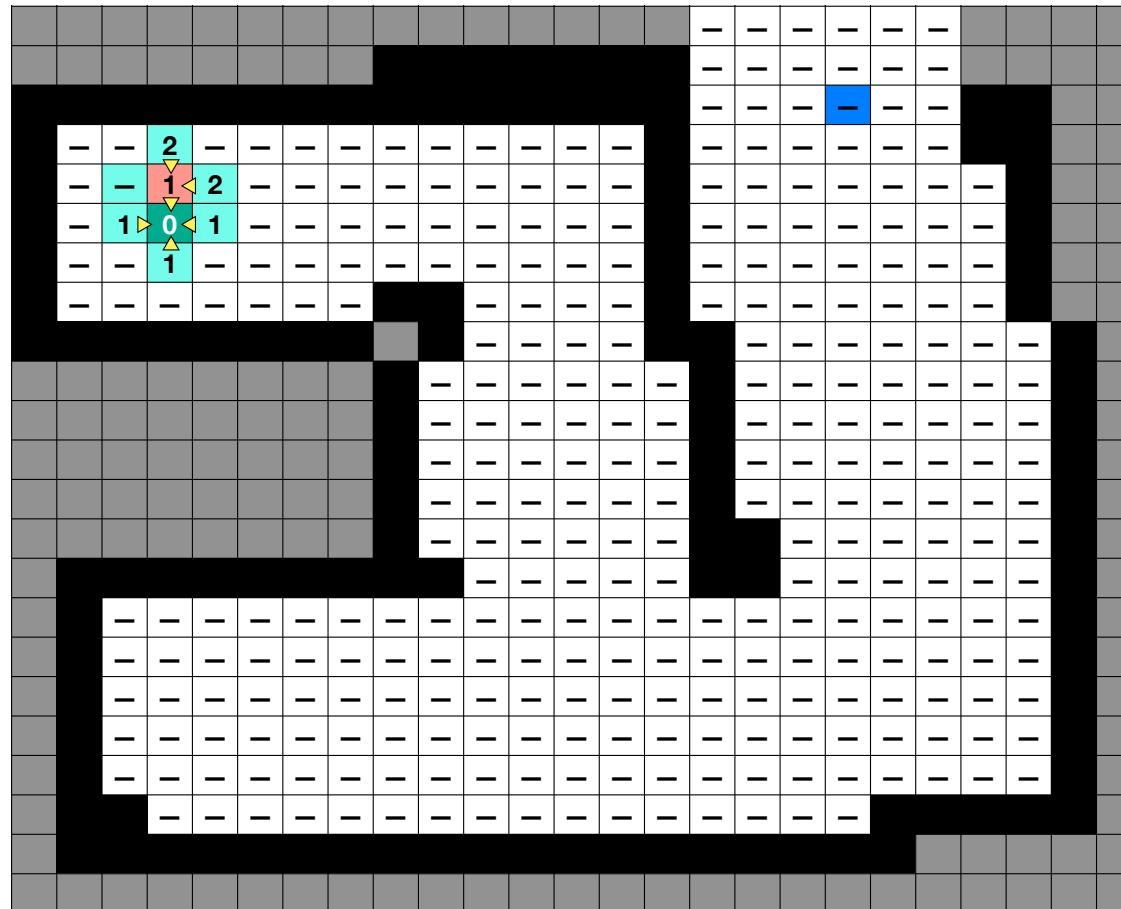
F E D C B

A

current_node

**Process
current node**

**Queue last
neighbor**



visit_queue

G F E D C B

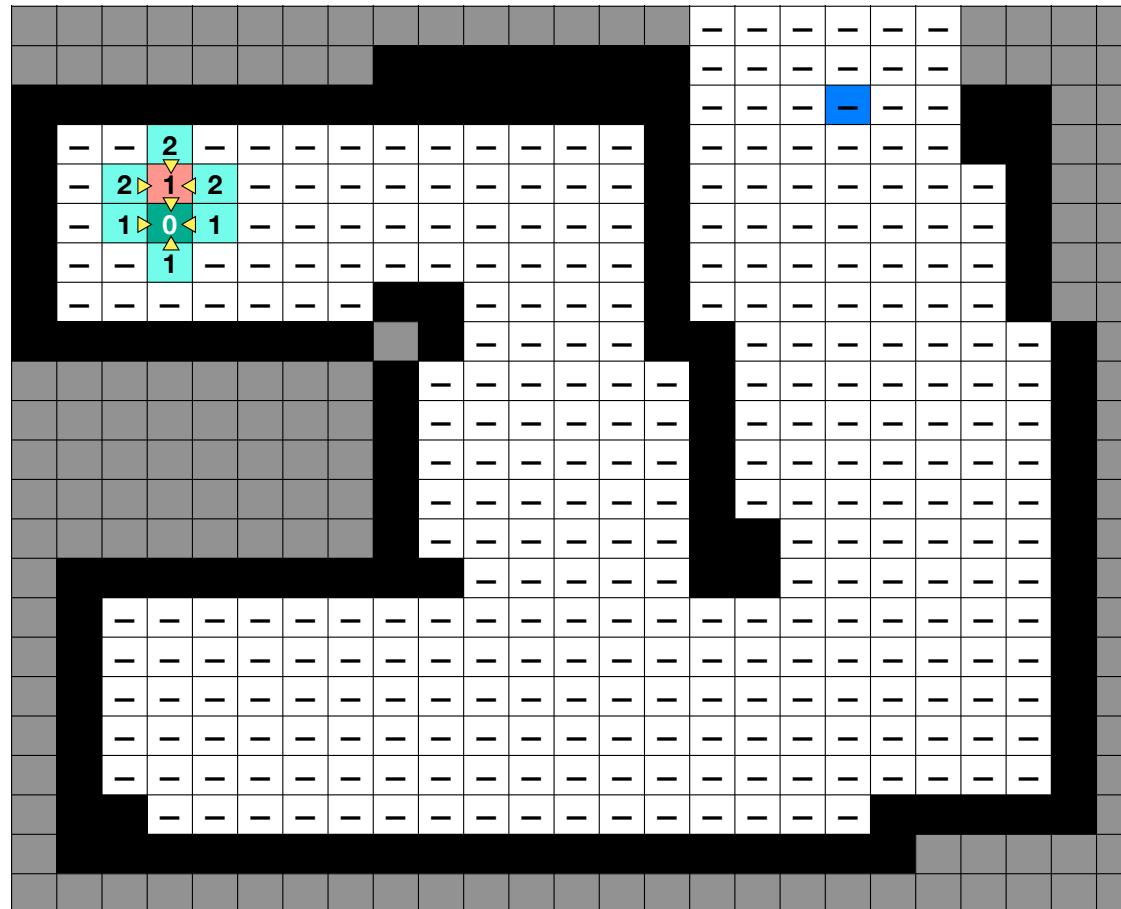
A

current_node

**Process
current node**

**Queue last
neighbor**

**Assign
distance and
parent**

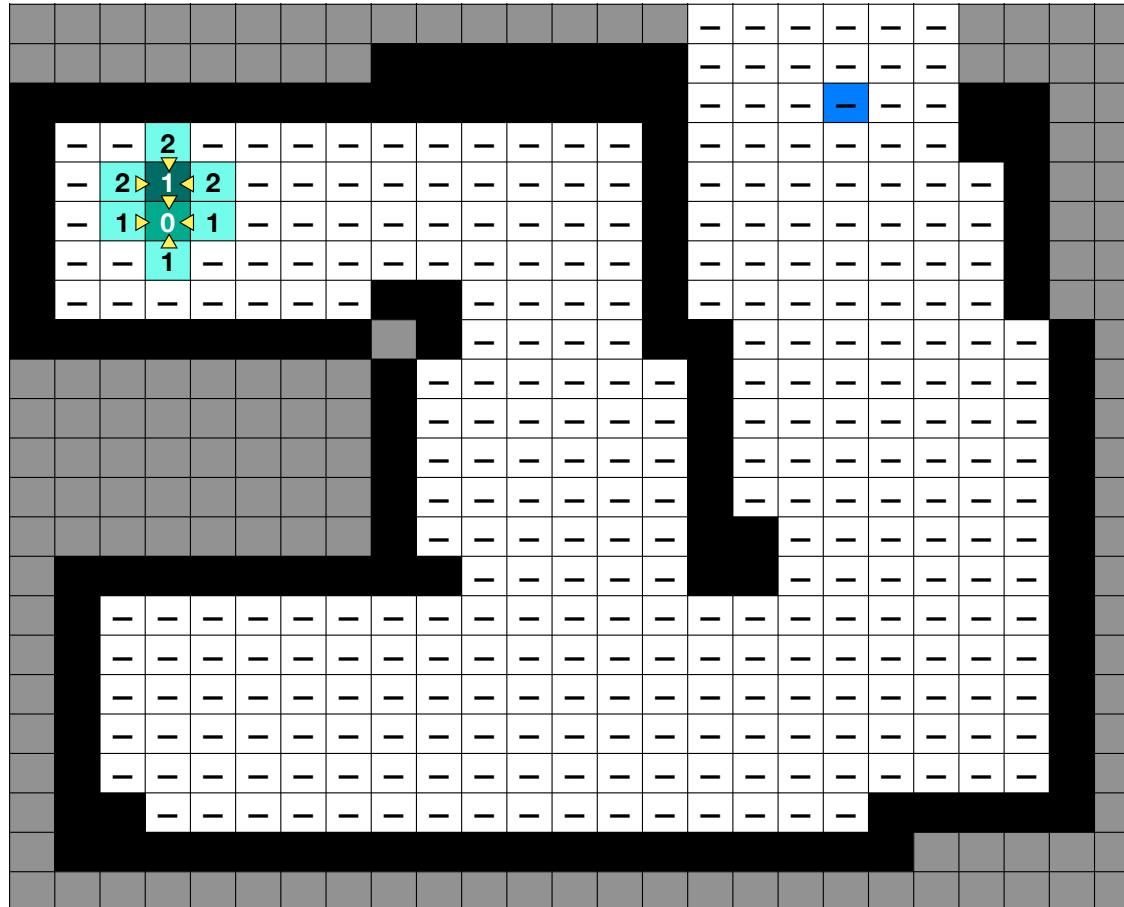


visit_queue

G F E D C B

A

current_node



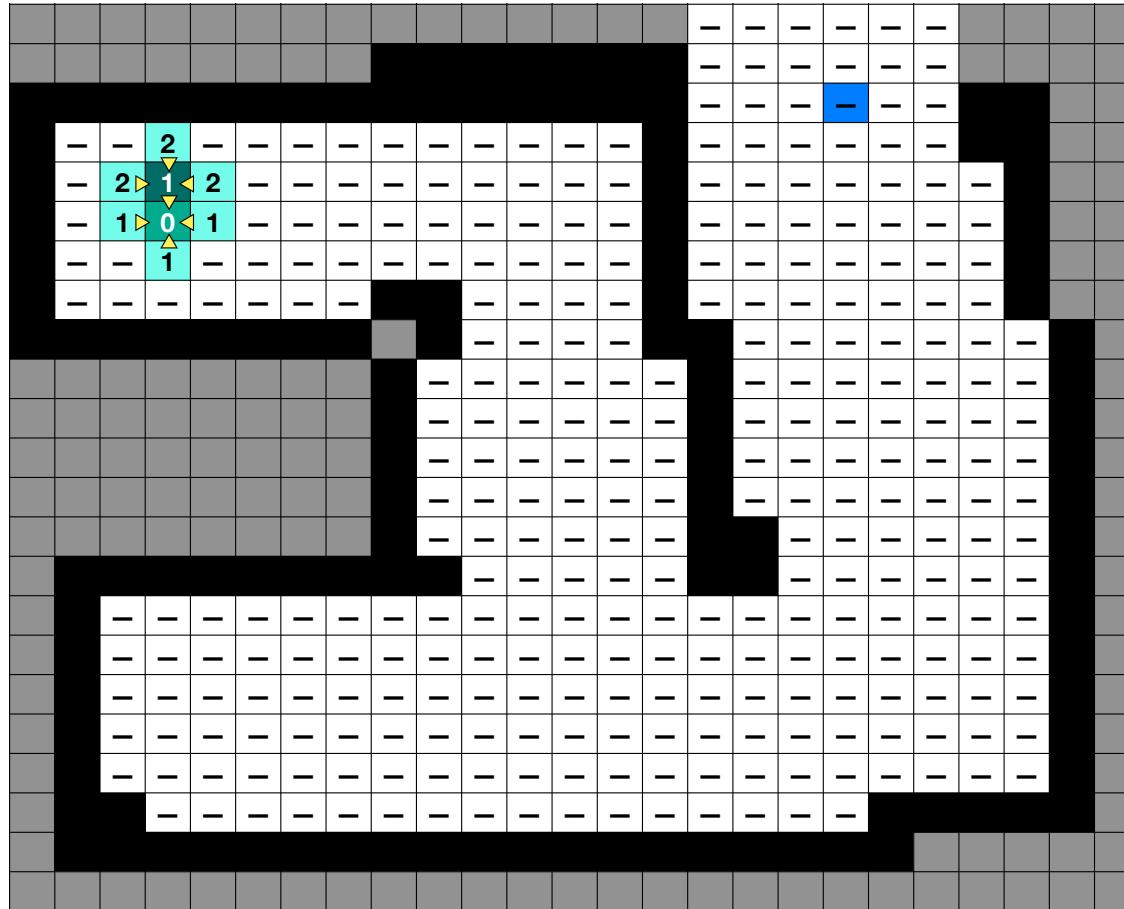
visit_queue

G F E D C B

A

current_node

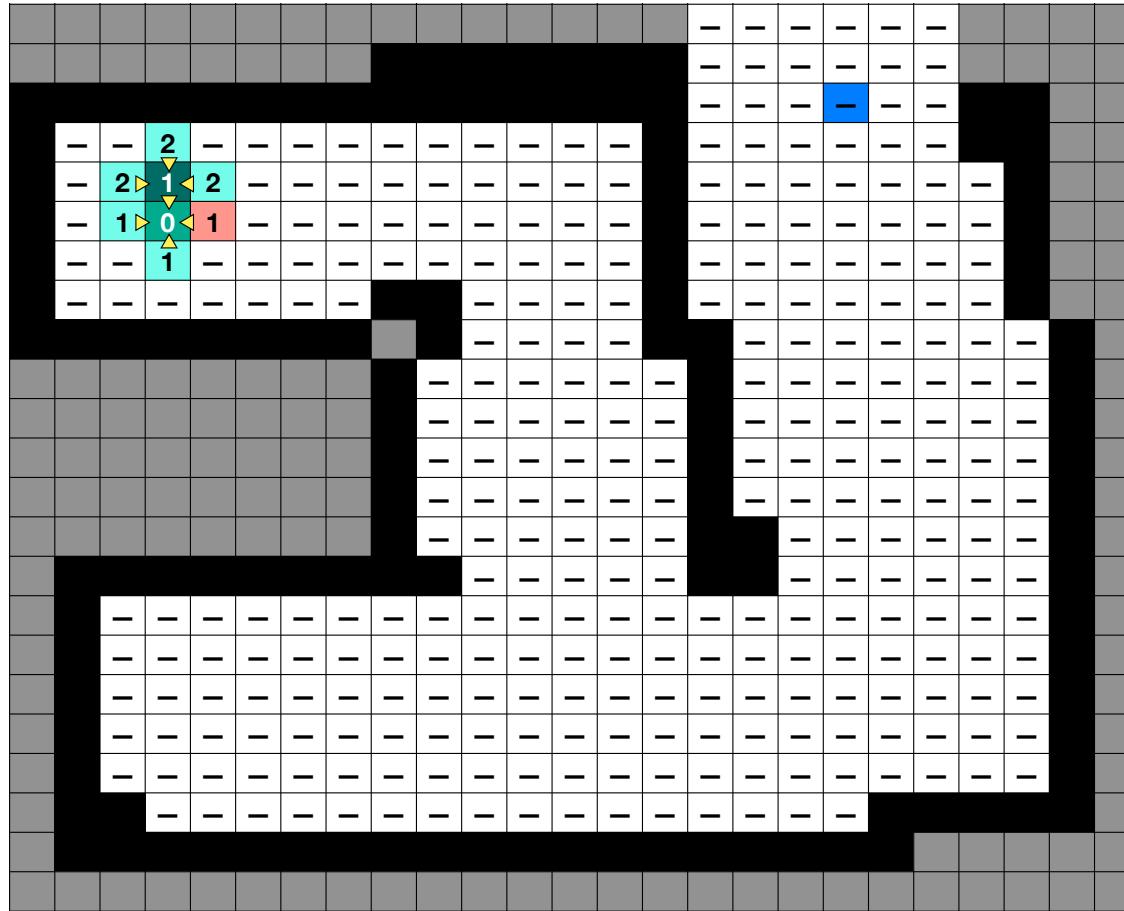
**Current node
fully processed**



visit_queue

G F E D C B

current_node



visit_queue

G F E D C

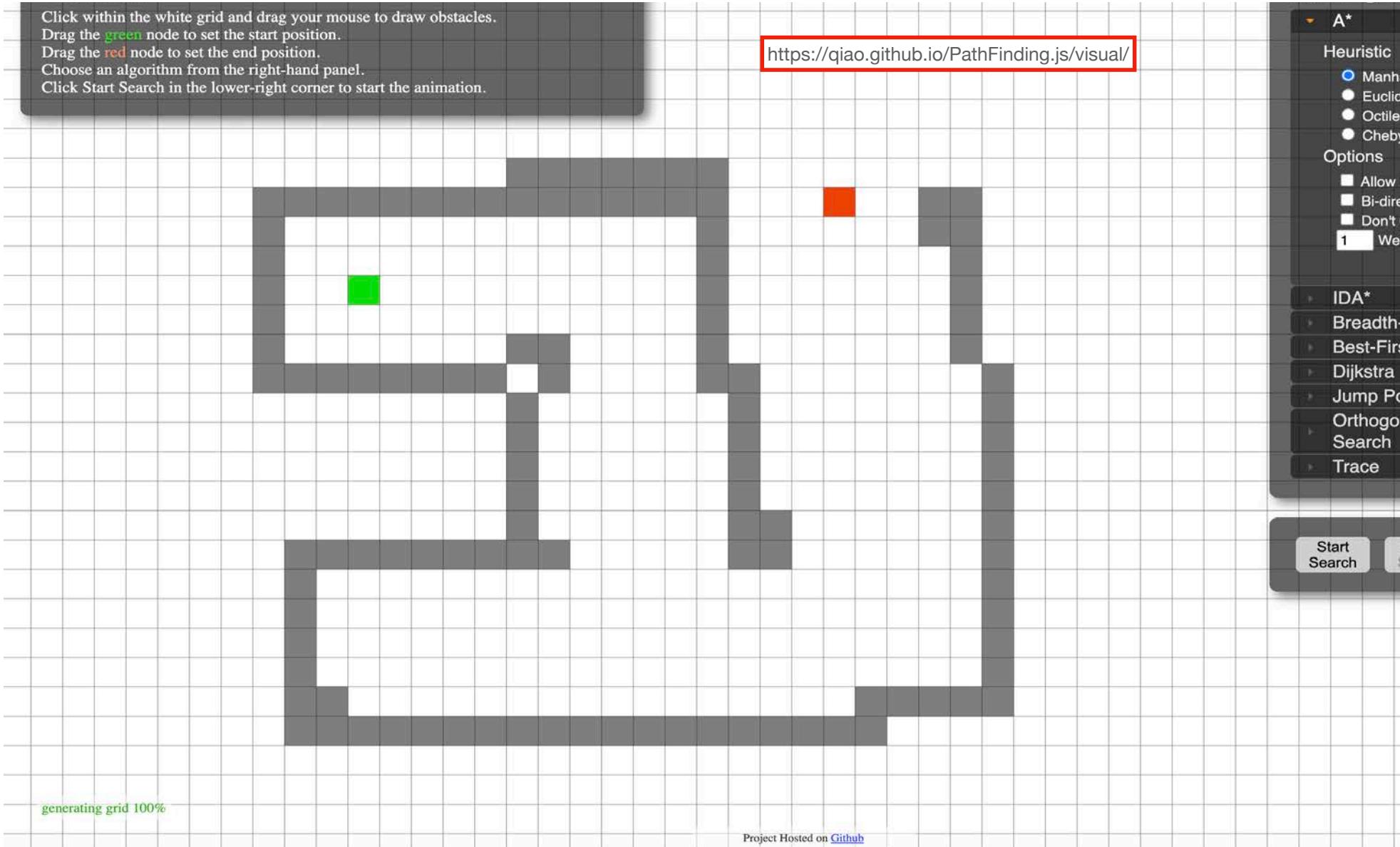
B

current_node

***Dequeue from
visit queue ...
process
continues***

Click within the white grid and drag your mouse to draw obstacles.
Drag the green node to set the start position.
Drag the red node to set the end position.
Choose an algorithm from the right-hand panel.
Click Start Search in the lower-right corner to start the animation.

<https://qiao.github.io/PathFinding.js/visual/>



qiao.github.io/PathFinding.js/visual/

Instructions

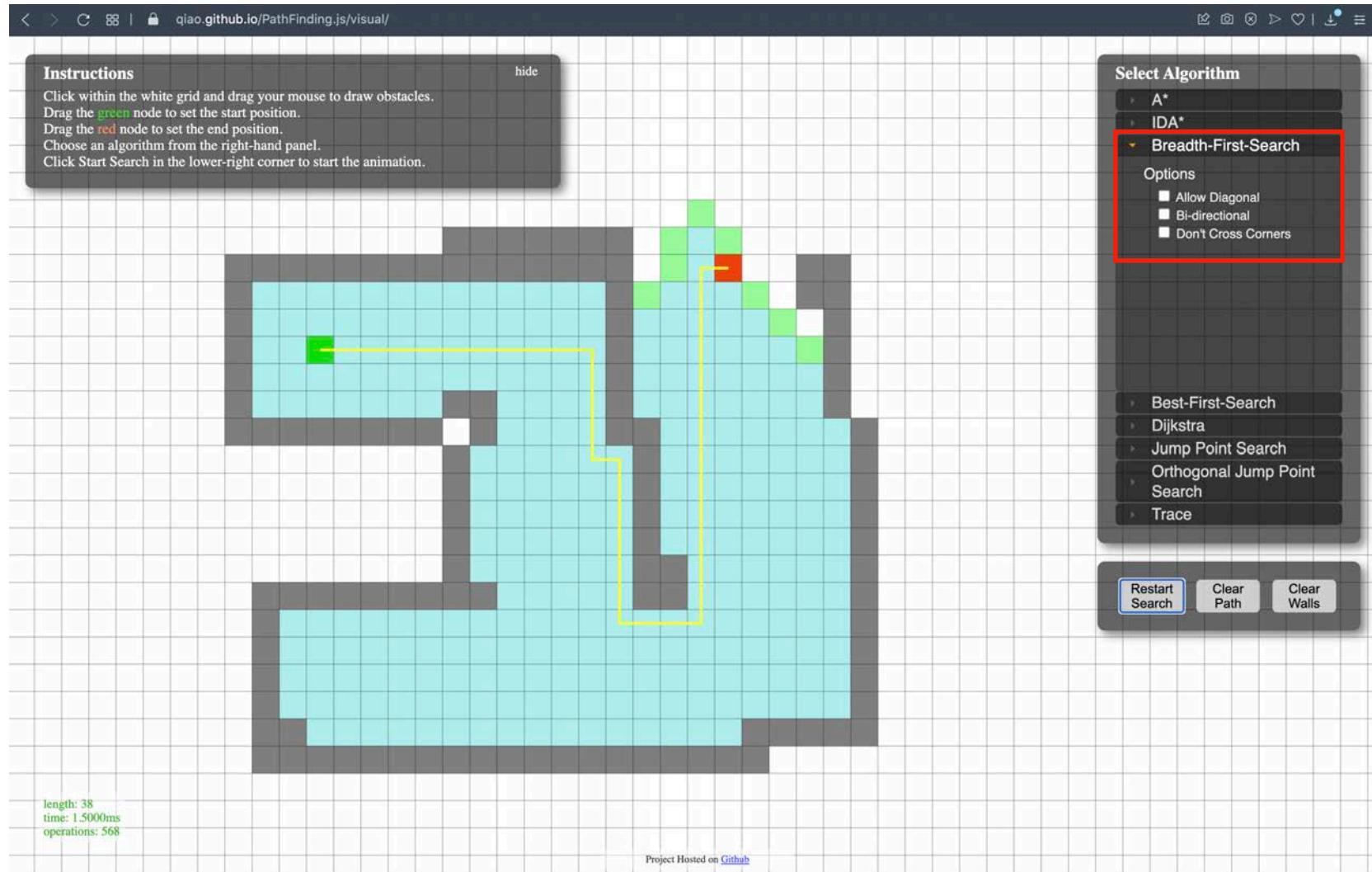
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Drag the green node to set the start position.
Drag the red node to set the end position.
Choose an algorithm from the right-hand panel.
Click Start Search in the lower-right corner to start the animation.

hide

Select Algorithm

- A*
- Heuristic
 - Manhattan
 - Euclidean
 - Octile
 - Chebyshev
- Options
 - Allow Diagonal
 - Bi-directional
 - Don't Cross Corners
 - Weight
- IDA*
- Breadth-First-Search
- Best-First-Search
- Dijkstra
- Jump Point Search
- Orthogonal Jump Point Search
- Trace

Start Search Pause Search Clear Walls



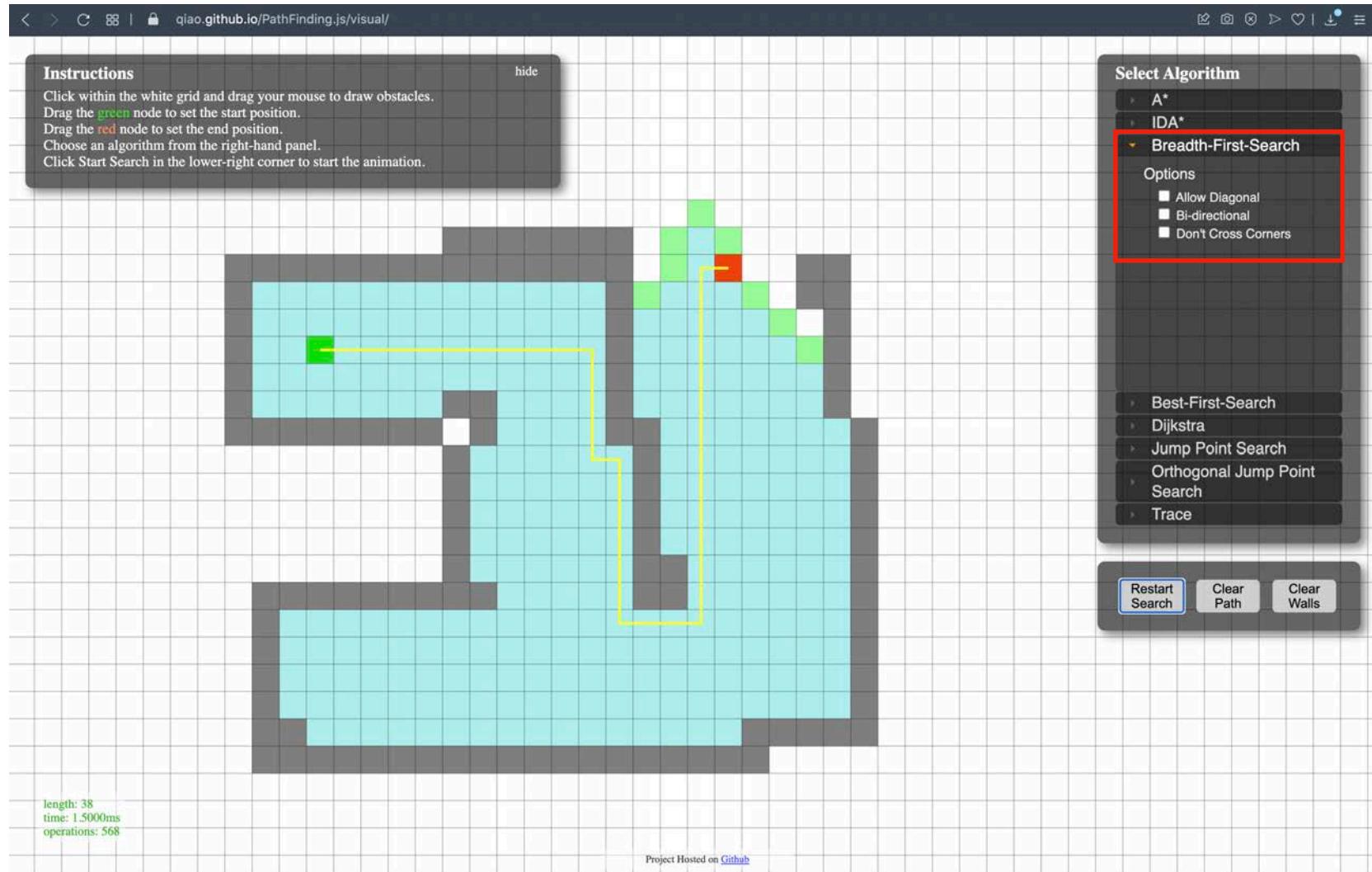
Michigan Robotics 102 - robotics102.org

Considerations for BFS

Is any path that reaches the goal a good path?

How many cells do we need to visit?

Could we use another visit strategy?



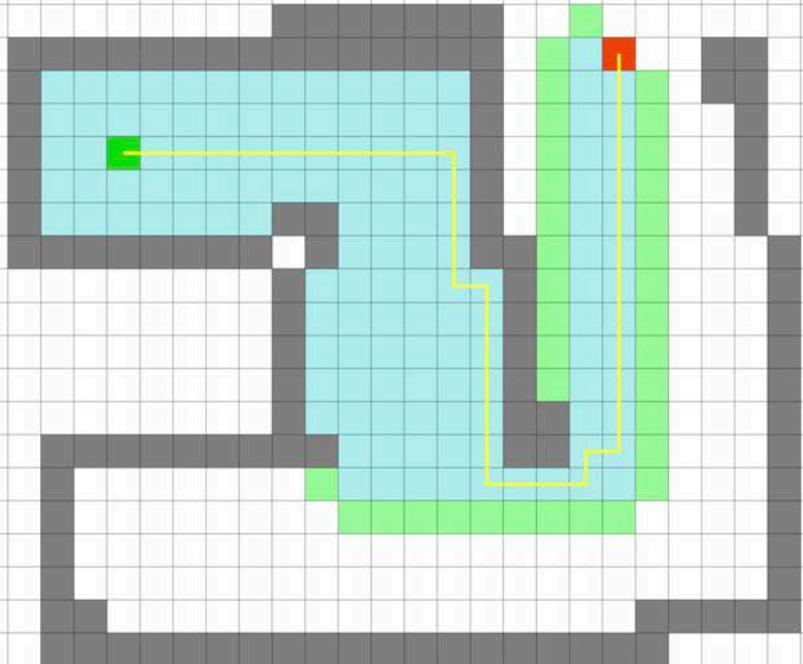
Michigan Robotics 102 - robotics102.org

qiao.github.io/PathFinding.js/visual/

Instructions

Click within the white grid and drag your mouse to draw obstacles.
 Drag the green node to set the start position.
 Drag the red node to set the end position.
 Choose an algorithm from the right-hand panel.
 Click Start Search in the lower-right corner to start the animation.

hide



length: 38
time: 2.5000ms
operations: 309

Select Algorithm

A*

- Heuristic
 - Manhattan
 - Euclidean
 - Octile
 - Chebyshev

Options

- Allow Diagonal
- Bi-directional
- Don't Cross Corners
- Weight

IDA*

Breadth-First-Search

Best-First-Search

Dijkstra

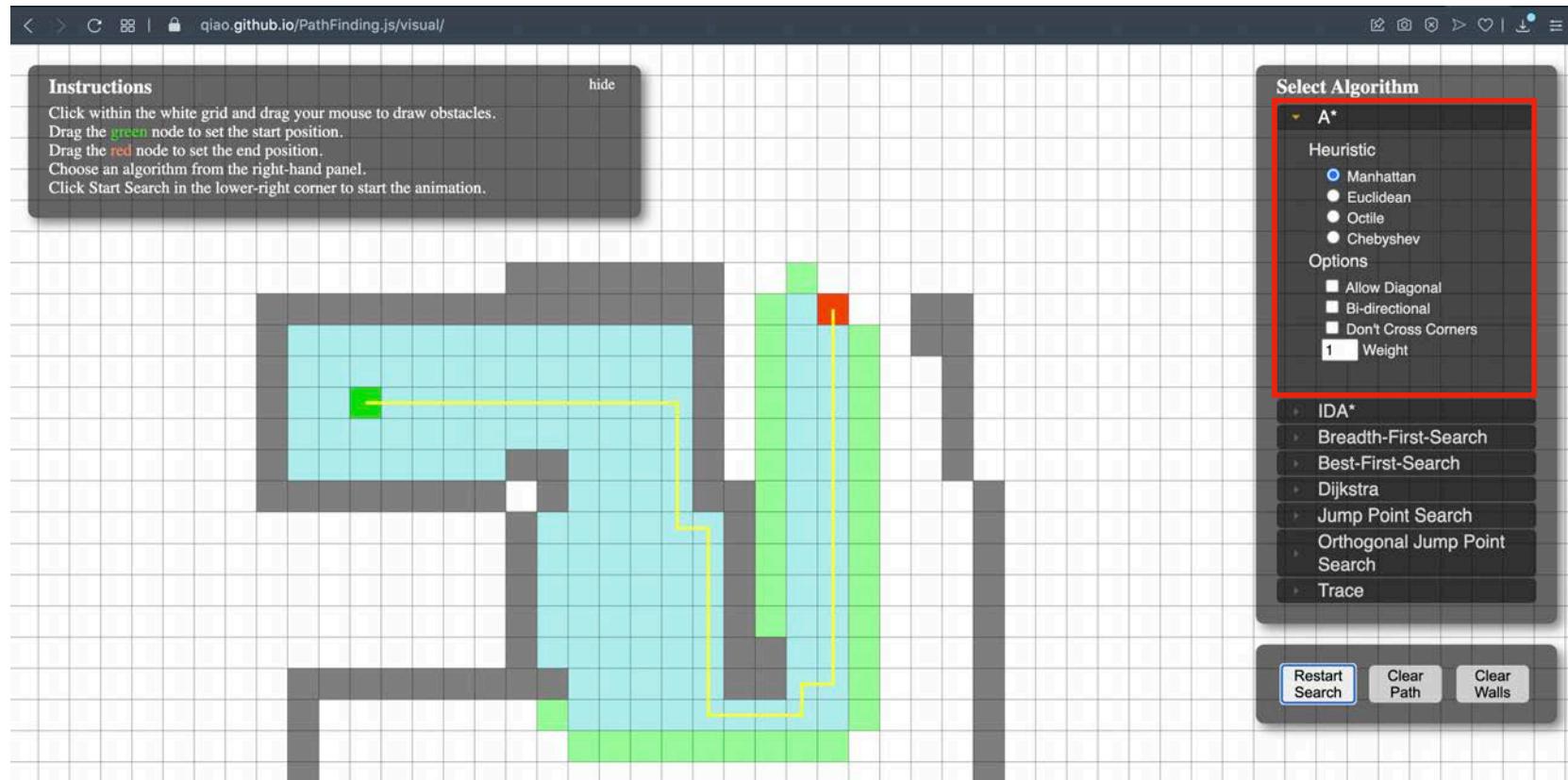
Jump Point Search

Orthogonal Jump Point Search

Trace

Restart Search Clear Path Clear Walls

Project Hosted on [Github](#)



How does A-Star generate a *shortest path* while visiting fewer nodes ?

length: 38
time: 2.5000ms
operations: 309

Breadth-first Search

Initialize :

All nodes to have no parent, max distance, and as unvisited

Start node to have no parent and zero distance

Visit queue with start node as its only enqueued element

Iterate : While visit list not empty and currently visited node is not the goal

Dequeue new current node to visit and mark it as visited

For each neighbor :

Add to visit queue, if not previously visited or queued

If Distance of neighbor > Distance of current node + ...

Cost to move from current node to neighbor

Then Update neighbor's parent to be current node and ...

distance to be distance of current node + cost to move

A-Star Search

Initialize :

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Start node to have no parent and zero distance

Visit queue with start node as its only enqueued element

Iterate : While visit list not empty and currently visited node is not the goal

Dequeue new current node to visit and mark it as visited

For each neighbor :

Add to visit **priority queue**, if not previously visited or queued

If Distance of neighbor > Distance of current node + ...

Cost to move from current node to neighbor

Then Update neighbor's parent to be current node and ...

distance to be distance of current node + cost to move

A-Star Search

Initialize :

All nodes to have no parent, max distance, and as unvisited

Start node to have no parent and zero distance

Visit queue with start node as its only enqueued element

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Dequeue new current node to visit and mark it as visited

For each neighbor :

Add to visit priority queue, if not previously visited or queued

If Distance of neighbor > Distance of current node + ...

How do we implement a priority queue?

Then Upd

What is a node's priority for A-Star?

distance to be distance of current node + cost to move

How do we implement a priority queue?

Topic for later courses in data structures (e.g., Michigan EECS 280)

Foreshadowing: use a binary heap

Considered an advanced extension for Project 3

What is a node's priority for A-Star?

How do we implement a priority queue?

Topic for later courses in data structures (e.g., Michigan EECS 280)

Foreshadowing: use a binary heap

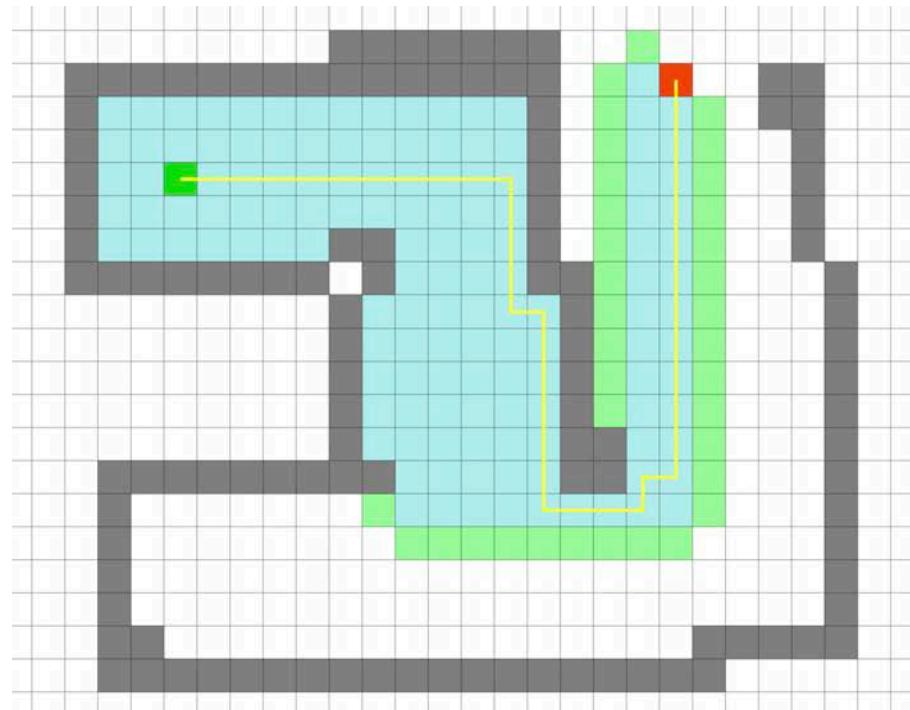
Considered an advanced extension for Project 3

What is a node's priority for A-Star?

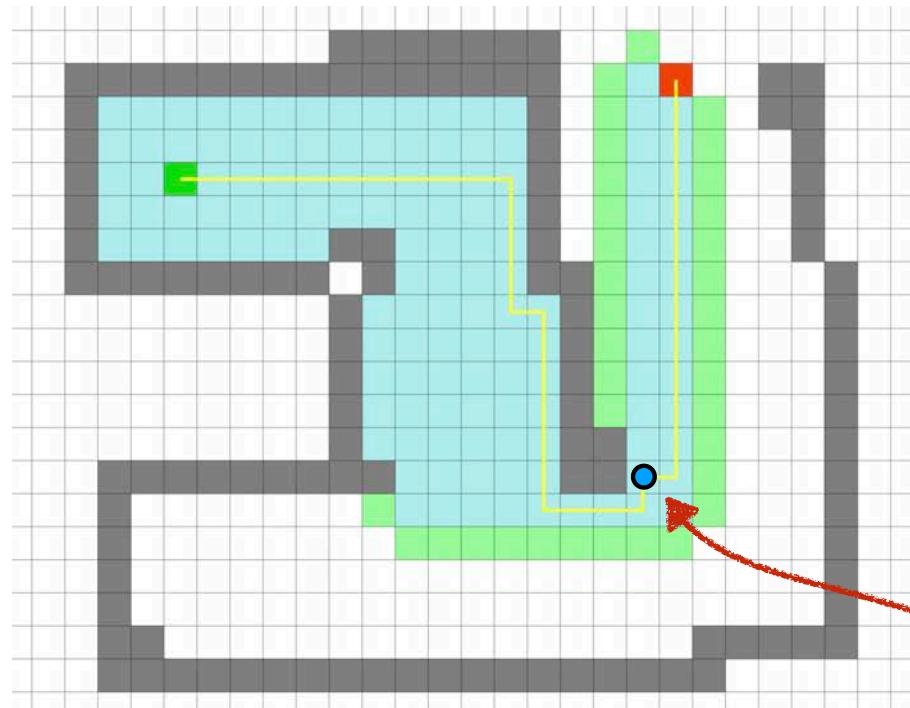
Use an optimistic heuristic for the best possible outcome

**Each node's priority is distance along path route to start +
best possible distance to goal**

**Each node's priority is distance along path route to start +
best possible distance to goal**

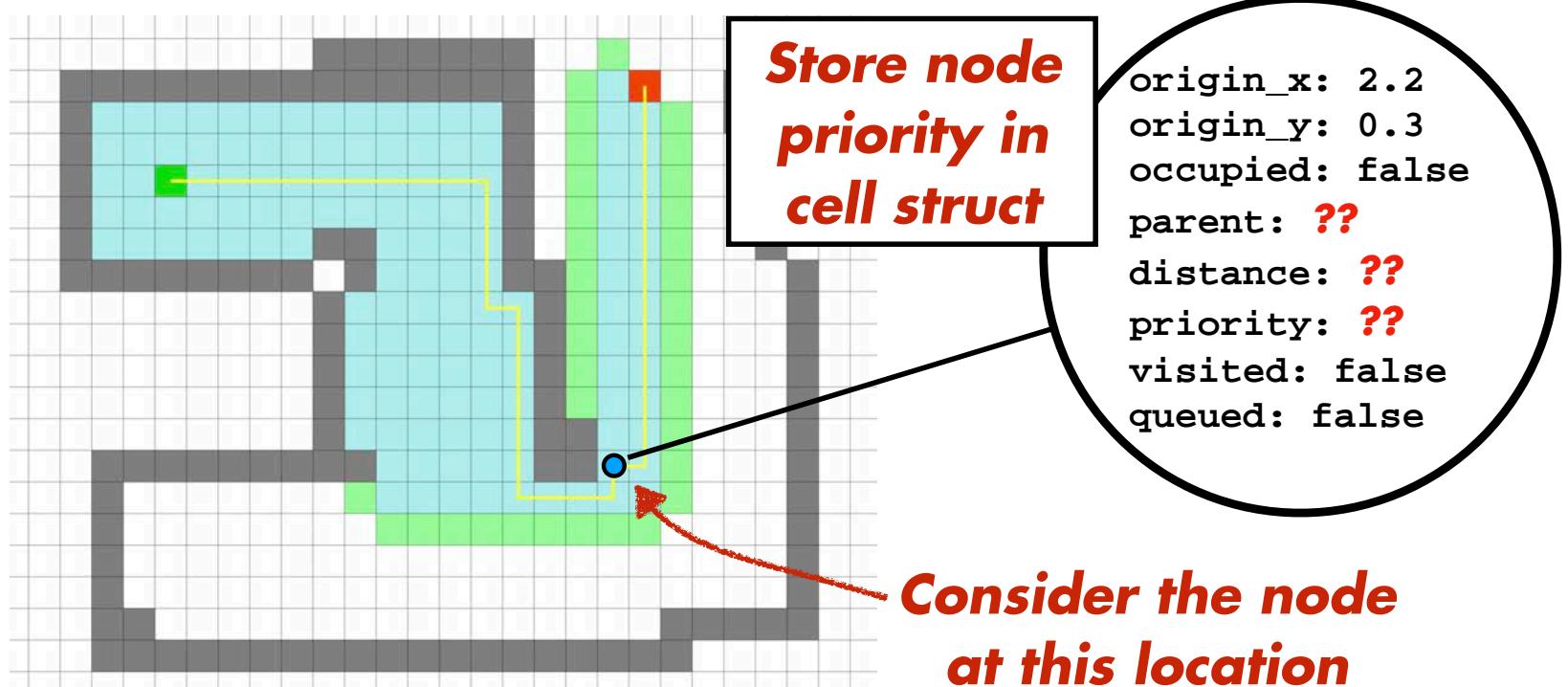


**Each node's priority is distance along path route to start +
best possible distance to goal**

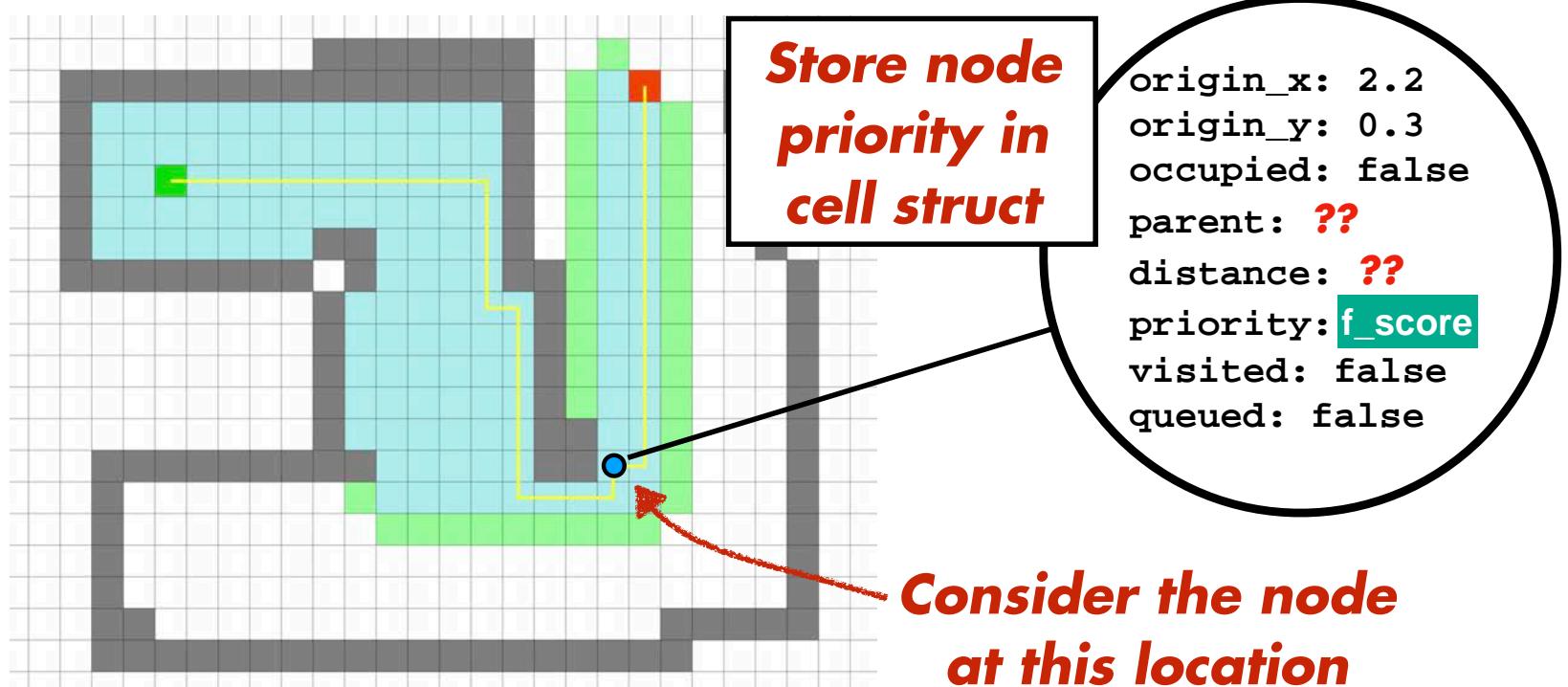


***Consider the node
at this location***

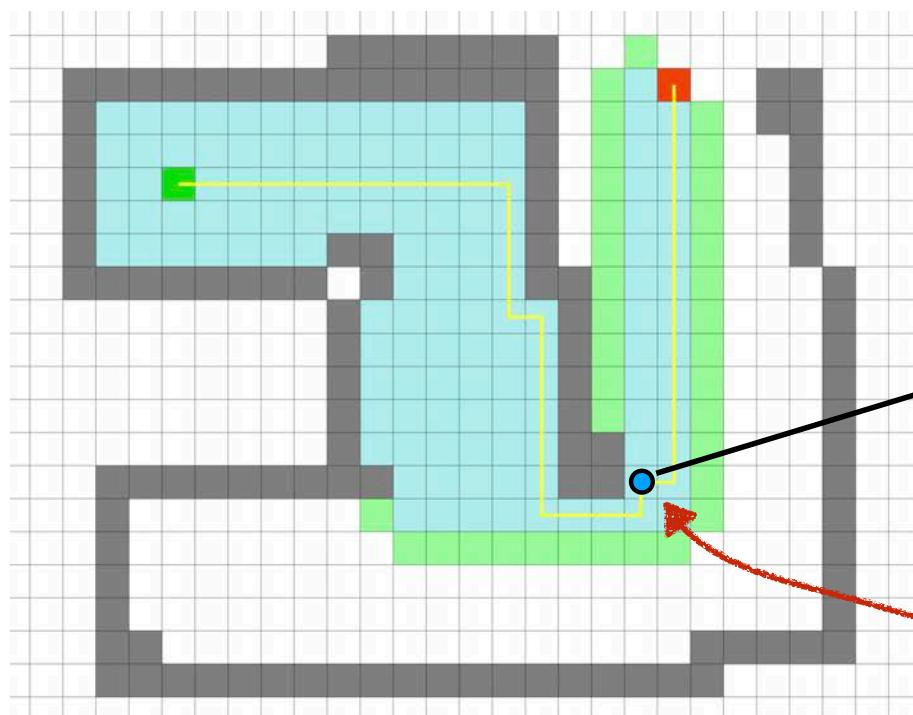
Each node's priority is distance along path route to start +
best possible distance to goal



Each node's priority is distance along path route to start +
best possible distance to goal



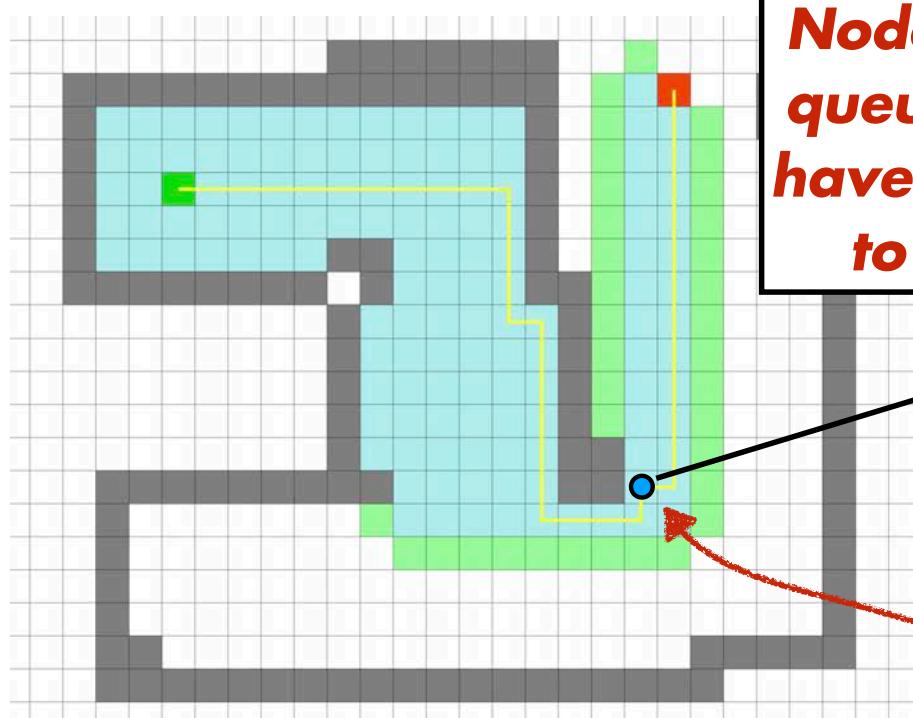
Each node's priority is distance along path route to start +
f_score best possible distance to goal



origin_x: 2.2
origin_y: 0.3
occupied: false
parent: ??
distance: ??
priority: **f_score**
visited: false
queued: false

***Consider the node
at this location***

Each node's priority is distance along path route to start +
f_score best possible distance to goal



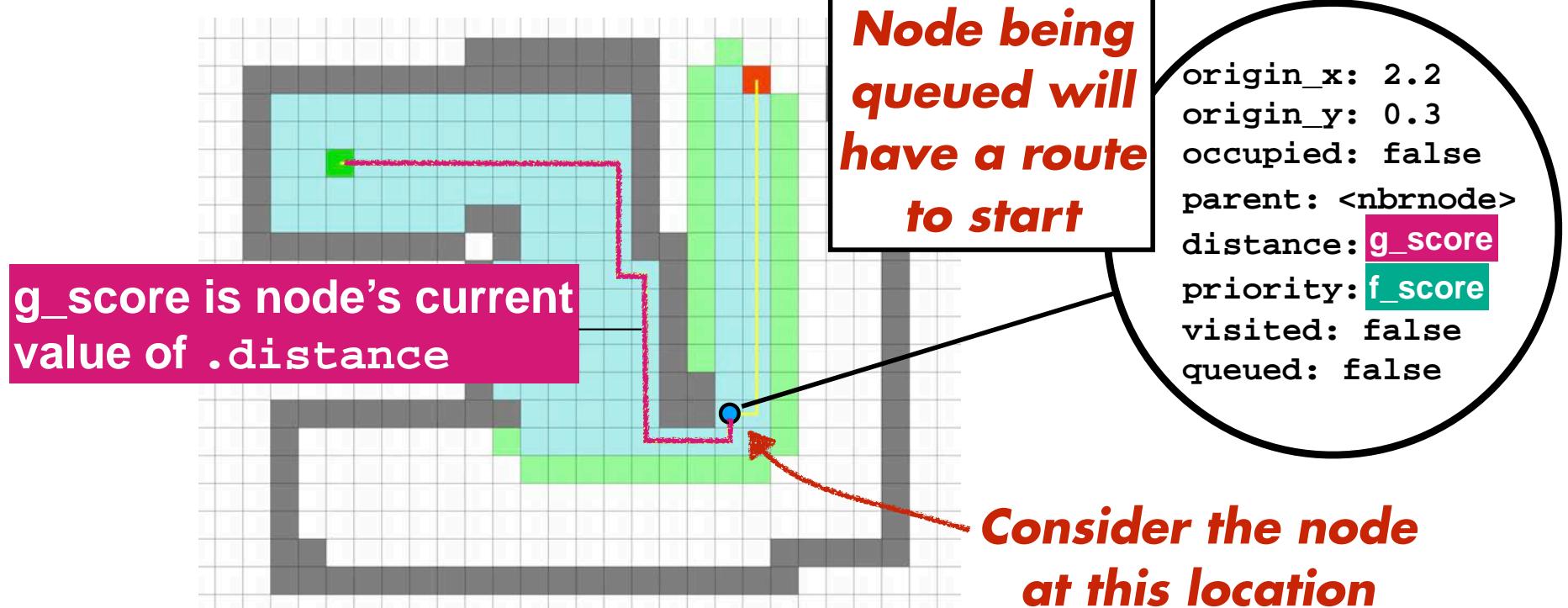
Node being queued will have a route to start

origin_x: 2.2
origin_y: 0.3
occupied: false
parent: <nbrnode>
distance: **g_score**
priority: **f_score**
visited: false
queued: false

Consider the node at this location

g_score

Each node's priority is distance along path route to start +
f_score best possible distance to goal

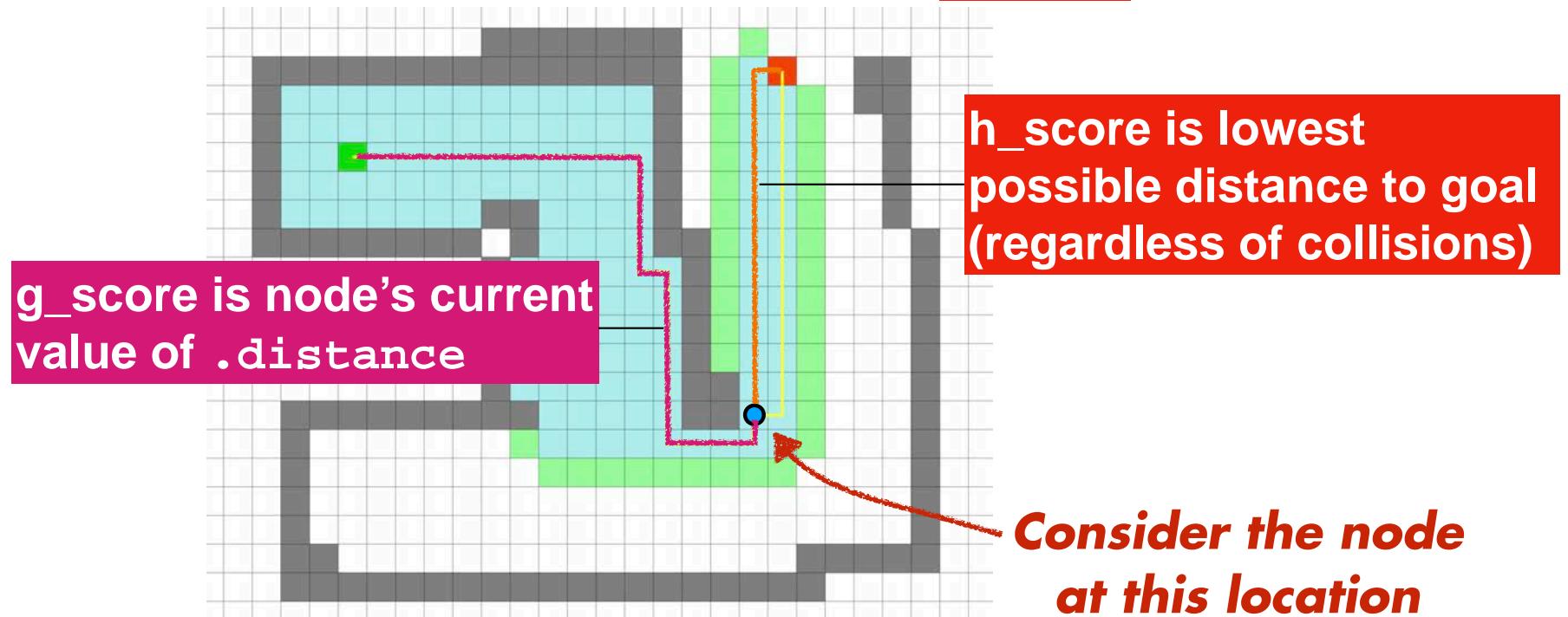


Each node's priority is distance along path route to start +

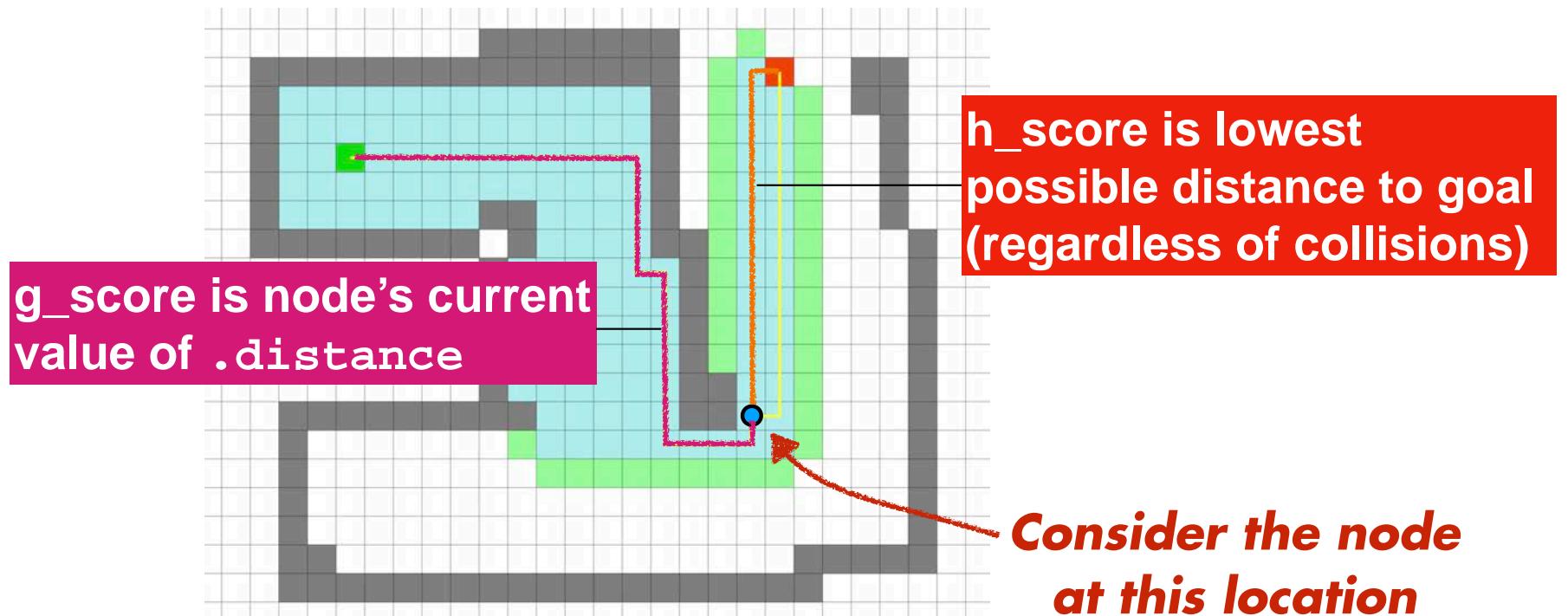
f_score

best possible distance to goal

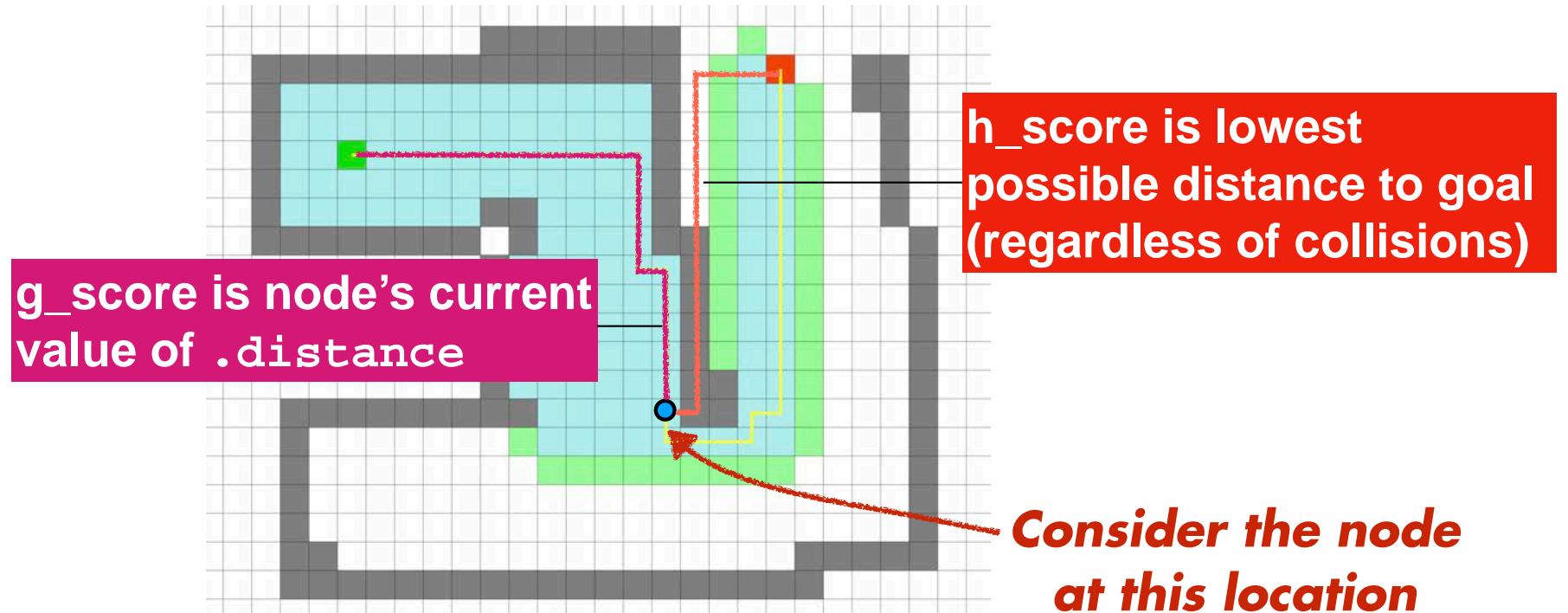
h_score



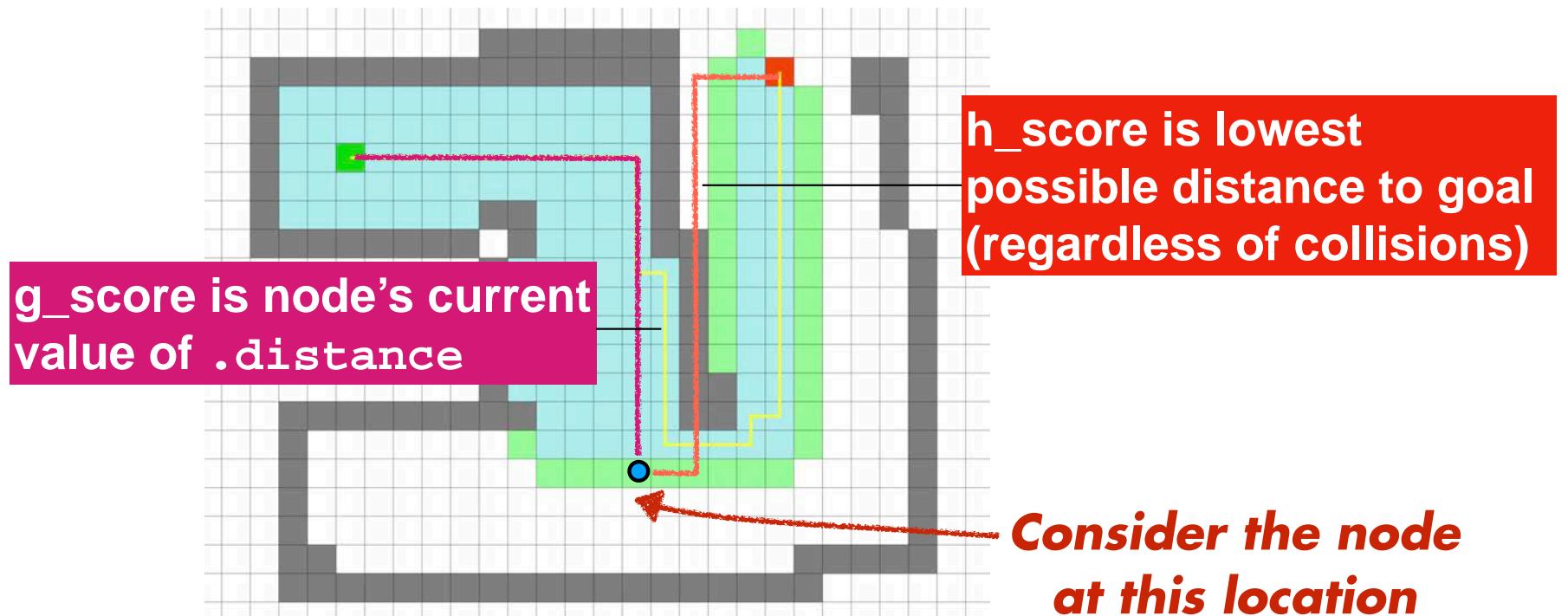
$$\text{.priority} \quad \quad \quad \text{.distance} \\ \text{f_score} = \text{g_score} + \text{h_score}$$



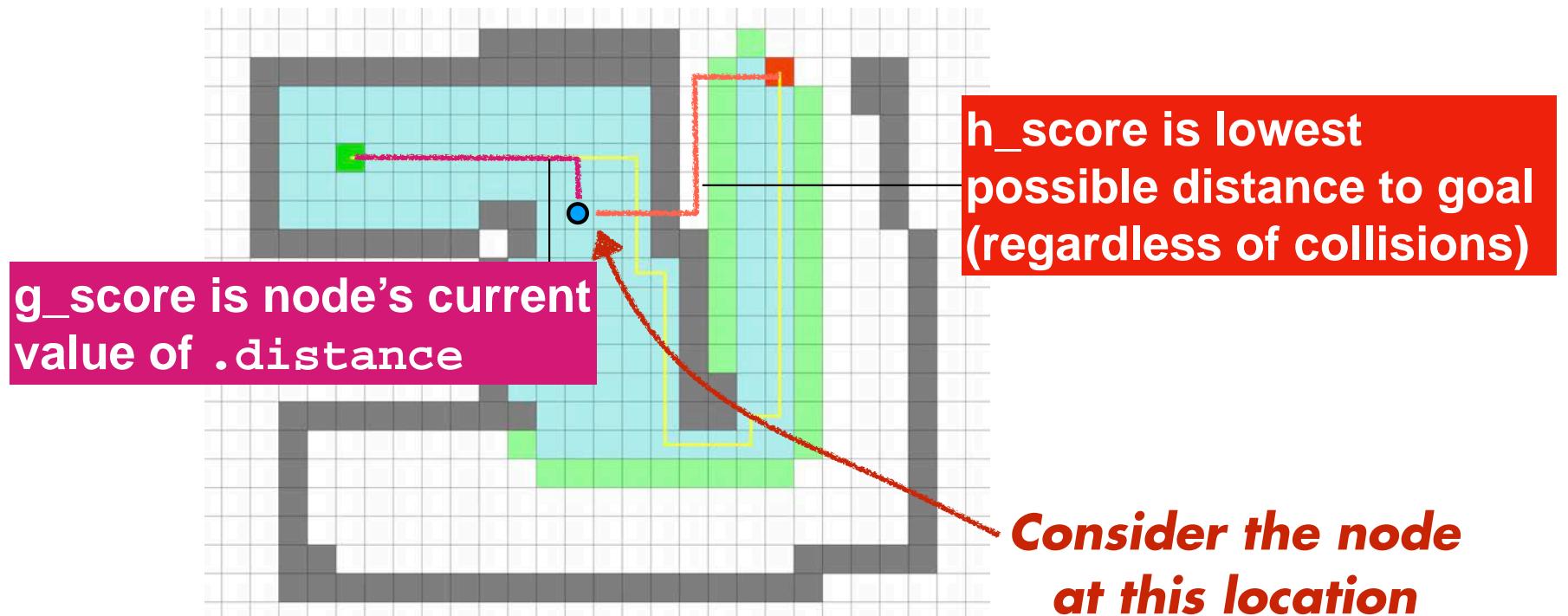
$$\text{.priority} \quad \quad \quad \text{.distance}$$
$$\text{f_score} = \text{g_score} + \text{h_score}$$



$$\text{.priority} \quad \quad \quad \text{.distance} \\ \text{f_score} \quad = \quad \text{g_score} + \text{h_score}$$



$$\text{.priority} \quad \quad \quad \text{.distance} \\ \text{f_score} \quad = \quad \text{g_score} + \text{h_score}$$





What options do we have
for navigating our robot?

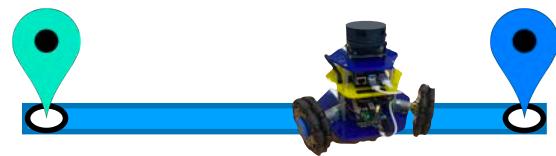
Just move randomly

Follow wall to goal

Build a map to guide us

Search over all possible paths

*Robot that plans paths
using global search ?*



What options do we have for navigating our robot?

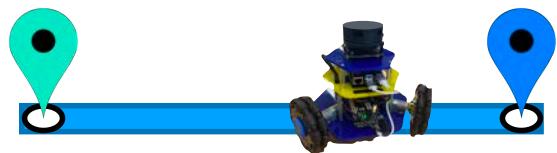
Just move randomly

Follow wall to goal

Build a map to guide us

Search over all possible paths





What options do we have for navigating our robot?

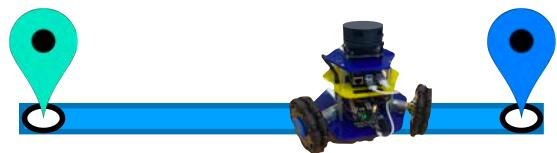
Just move randomly

Follow wall to goal

Build a map to guide us

Search over all possible paths

- + Complete algorithm
(guarantees correct answer)
- + Optimal path
- Expensive
- Responsiveness



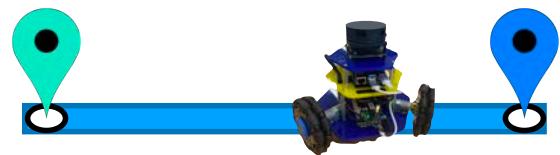
**What options do we have
for navigating our robot?**

Just move randomly

Follow wall to goal

Build a map to guide us

Search over all possible paths



**What options do we have
for navigating our robot?**

Random Walk

Bug Algorithm

Local Search

Global Search

Reaction

Deliberation



Random Walk

Bug Algorithm

Local Search

Global Search

Reaction

Deliberation



Random Walk

Bug Algorithm

Local Search

Global Search

Reaction

Deliberation



Random Walk

- + Cheap
- + Simple
- + Robust
- Slow

Bug Algorithm

- + Simple
- + Reliable
- Known goal location
- Forgetful

Local Search

- + Adaptable
- Requires SLAM
- Gets stuck

- + Complete
- + Optimal
- Expensive
- Responsive

Global Search

Reaction

Deliberation



Inexpensive

Overhead vs. Optimality

Complete

Simple

Speed vs. Guarantees

Thorough

Dynamic

Responsiveness to environment

Adaptable

There is no one right algorithm.

There is a larger world of possibilities.



Inexpensive

Overhead vs. Optimality

Complete

Simple

Speed vs. Guarantees

Thorough

Dynamic

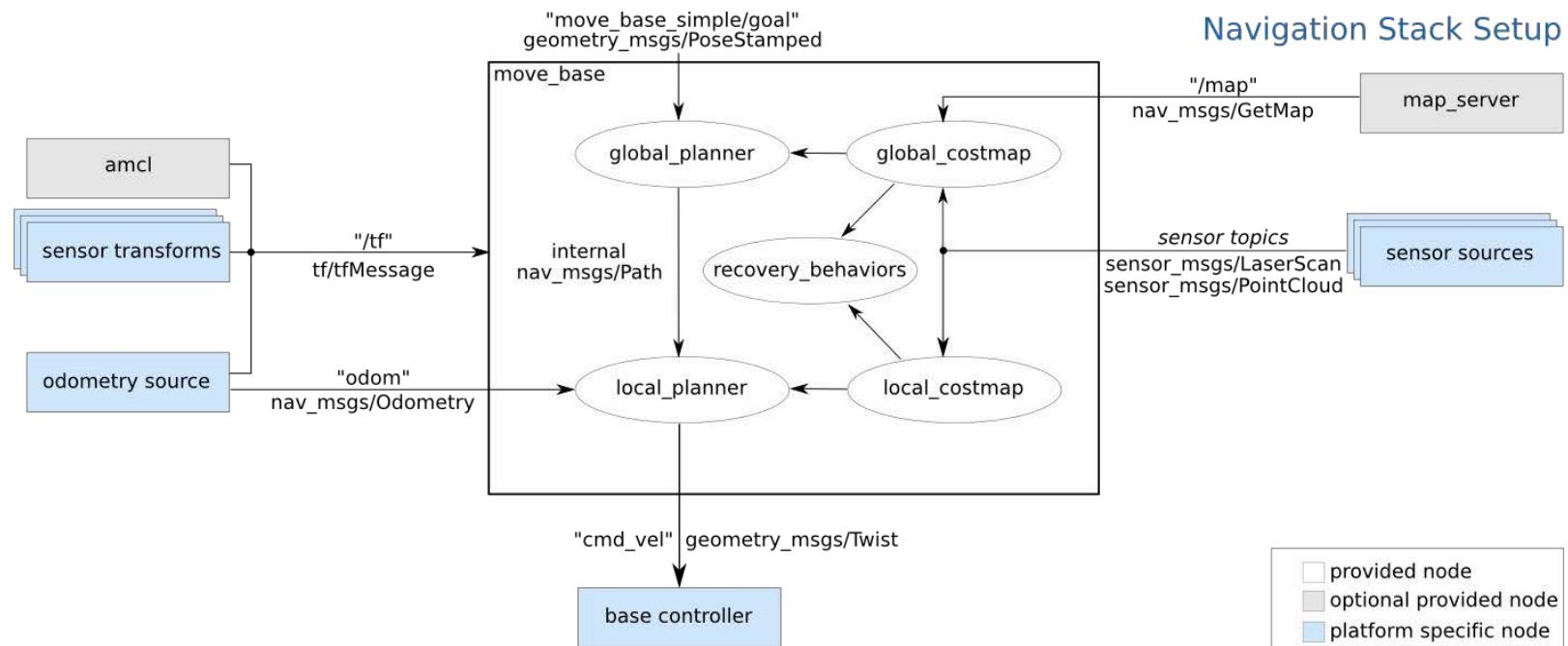
Responsiveness to environment

Adaptable

Reaction

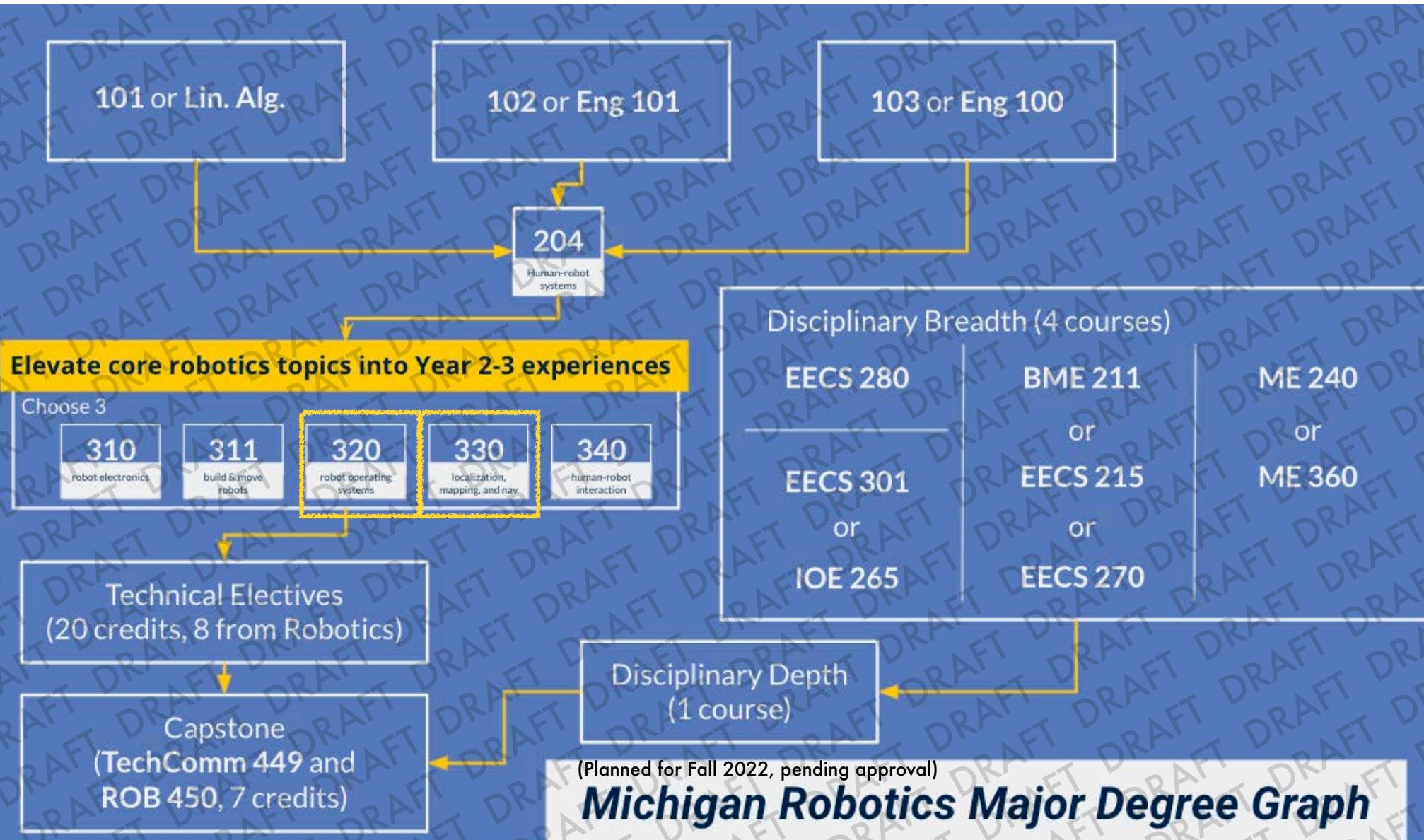
Deliberation

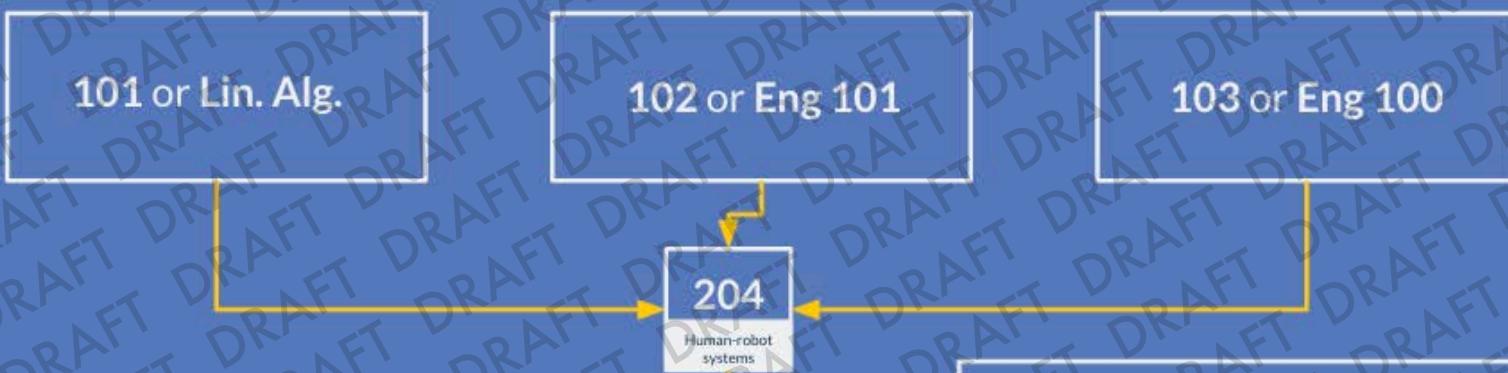
[navigation/ Tutorials/ RobotSetup](#)



Navigation in Robot Operating Systems

[Michigan Robotics 102 - robotics102.org](#)





Robotics 320: Planning for mobile manipulation robots



Technical Electives
(20 credits, 8 from Robotics)

Capstone
(TechComm 449 and
ROB 450, 7 credits)

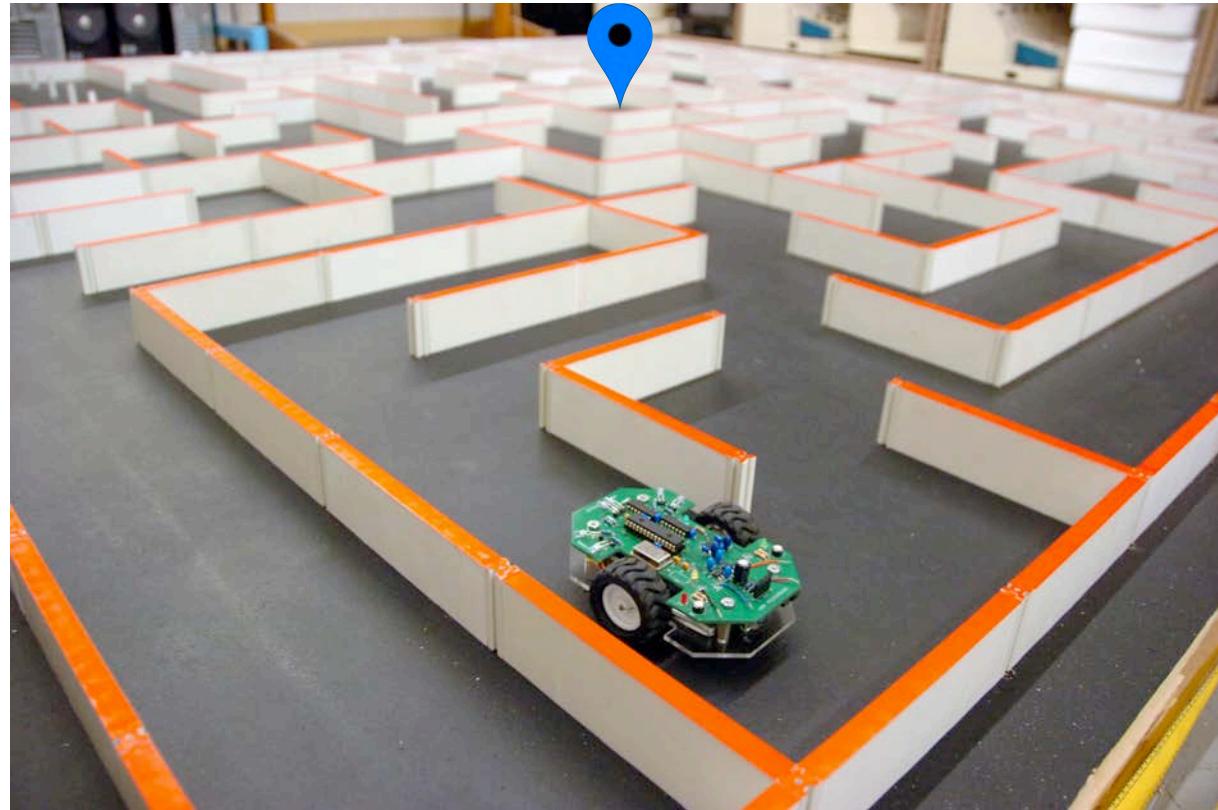
Robotics 330: Build SLAM system of your own

Disciplinary Depth
(1 course)

(Planned for Fall 2022, pending approval)

Michigan Robotics Major Degree Graph

Autonomous Navigation: Global Search



Robotics 102
Introduction to AI and Programming
University of Michigan and Berea College
Fall 2021

<https://app.emaze.com/@AIRRTROT/idea-2-the-robot-maze#1>

Michigan Robotics 102 - robotics102.org