

# Wideband Planar Array With Integrated Feed and Matching Network for Wide-Angle Scanning

Justin A. Kasemodel, *Member, IEEE*, Chi-Chih Chen, *Senior Member, IEEE*, and John L. Volakis, *Fellow, IEEE*

**Abstract**—It is traditionally known that wideband apertures lose bandwidth when placed over a ground plane. To overcome this issue, this paper introduces a new non-symmetric tightly coupled dipole element for wideband phased arrays. The proposed array antenna incorporates additional degrees of freedom to control capacitance and cancel the ground plane inductance. Specifically, each arm on the dipole is different than the other (or non-symmetric). The arms are identical near the center feed section but dissimilar towards the ends, forming a ball-and-cup. It is demonstrated that the non-symmetric qualities achieve wideband performance. Concurrently, a design example for planar installation with balun and matching network is presented to cover X-band. The balun avoids extraneous radiation, maintains the array's low-profile height and is printed on top of the ground plane connecting to the array aperture with  $180^\circ$  out of phase vertical twin-wire transmission lines. To demonstrate the concept, a 64-element array with integrated feed and matching network is designed, fabricated and verified experimentally. The array aperture is placed  $\lambda/7$  (at 8 GHz) above the ground plane and shown to maintain a active VSWR less than 2 from 8–12.5 GHz while scanning up to  $70^\circ$  and  $60^\circ$  in E- and H-plane, respectively. The array's simulated diagonal plane cross-polarization is approximately 10 dB below the co-polarized component during  $60^\circ$  diagonal scan and follows the theoretical limit for an infinite current sheet.

**Index Terms**—Antenna feeds, broadband antennas, dipole antennas, phased arrays, planar arrays, scanning antennas, wide-angle scanning.

## I. INTRODUCTION

WITH space at a premium, there is strong interest to develop a single ultra wideband (UWB) phased array aperture, capable of concurrently supporting communications, electronic warfare and radar functions. Recent focus on conformal designs present new challenges for wideband apertures which commonly transform into narrowband or multiband configurations when placed on a ground plane. It is therefore not surprising that considerable attention has been given to electromagnetic bandgap (EBG) [1], [2] or frequency selective

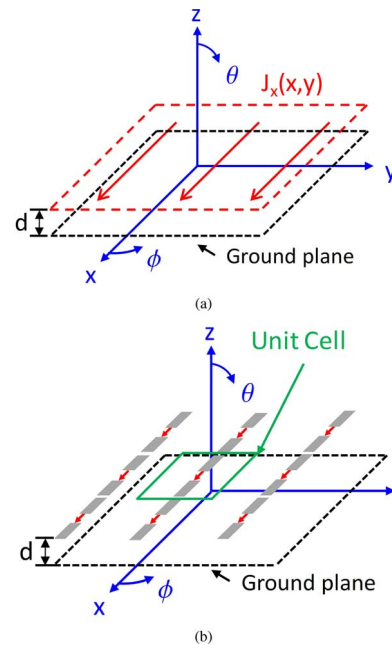


Fig. 1. (a) Infinite current sheet array over a ground plane and (b) tightly coupled dipole array implementation.

surfaces (FSS) [3] that mitigate the ground plane's destructive interference. However, EBGs, FSSs and other periodic ground planes are narrowband and not suited for wideband applications. Therefore, design of phased array apertures which are concurrently broadband and low-profile over a ground plane remains a challenge.

The infinite current sheet array (CSA) concept proposed by Wheeler [4] forms a theoretical basis for planar apertures. However, a broadband implementation was not realized in practice until Munk *et al.* [5], [6], emulated this concept using a tightly coupled dipole array (TCDA) as depicted in Fig. 1. An important aspect of TCDA is the capacitive coupling between elements that enables the following: 1) allows field propagation to neighboring elements; 2) reduces dipole resonant frequency; 3) cancels inductive ground plane loading as a result of the strong capacitive coupling among dipole elements, yielding a low-profile, ultrawideband phased array aperture. The latter is critical for retaining the aperture's wideband behavior when placed in close proximity to a ground plane.

Previous wideband phased array antennas such as TEM-horn [7], body-of-revolution [8], bunny-ear [9], tapered slot, or Vivaldi [10] relied upon the third dimension of the element (depth), to achieve large bandwidths. As a result, they do not allow for conformal installations. They are also costly and difficult to fabricate.

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It is well understood that mutual coupling in an array can cause detrimental changes in performance such as element impedance variations, polarization degradation, and undesirable radiation patterns. In fact, mutual coupling is responsible for one of the more challenging aspects of phased array design, that of retaining uniform scan impedance. A fundamentally different design approach was proposed by Munk [5], where mutual coupling is used to lower the operational frequency and increase bandwidth. This approach is similar to designing wideband wide-angle FSSs [11]. Likewise, mutual coupling was shown to lower the operational frequency of a spiral array in [12].

Building on Munk's concept, in this paper, we present a new conformal array design that has several advantages: 1) inherently low-profile with good diagonal plane cross-polarization performance; 2) allows for conformal mounting on platforms (where a metallic ground plane is used); 3) employs planar element geometry for fabrication ease; and 4) enables significant cost reduction using planar printed circuit board (PCB) fabrication technology. The design is based on an infinite periodic array of dipoles modified to provide an increase in their design degree of freedoms. Specifically, the proposed non-symmetric geometry can be exploited for UWB or improved performance over a specific bandwidth. For the latter, a design is developed to operate over the entire X-band (8–12.5 GHz). A unique feature of the proposed array is its planar layered PCB construction. A single microwave laminate is used for the array aperture and another underneath supports all associated baluns and matching networks. For example, a 2166 element X-band array with associated baluns can be printed on two sheets of standard (12 in  $\times$  18 in) PCB.

This paper is organized as follows. Section II introduces a novel non-symmetric element and provides a parametric study of its performance. A choice of parameters are then selected to achieve miniaturization and control input impedance. Section III presents a wideband feed providing impedance matching and balanced-to-unbalanced conversion (while maintaining the array's low-profile). The balun is printed on the array ground plane and connects to the array aperture using small twin-wire transmission lines. Section IV provides experimental demonstration using a 64 element (8  $\times$  8) X-band array prototype. Section V showcases the array's diagonal cross-polarization performance and develops a fundamental limit on the diagonal plane cross-polarization ratio of planar current sheet apertures.

## II. NON-SYMMETRIC ARRAY ELEMENT

The proposed non-symmetric dipole element unit cell is depicted in Fig. 2(a). Each arm is different than the other for better control of its self inductance and mutual capacitance with neighboring elements. The non-symmetric TCDA element is characterized by five variables;  $t_1$  (cup width),  $t_2$  (ball width),  $t_3$  (arm width),  $g$  (element separation gap), and  $\alpha$  (cup opening angle). Below, we pursue a parametric study of these five geometric values with the TCDA unit cell width and distance ( $d$ ) above the ground plane constant at 11.5 mm ( $.5\lambda_H$ ) and 8 mm

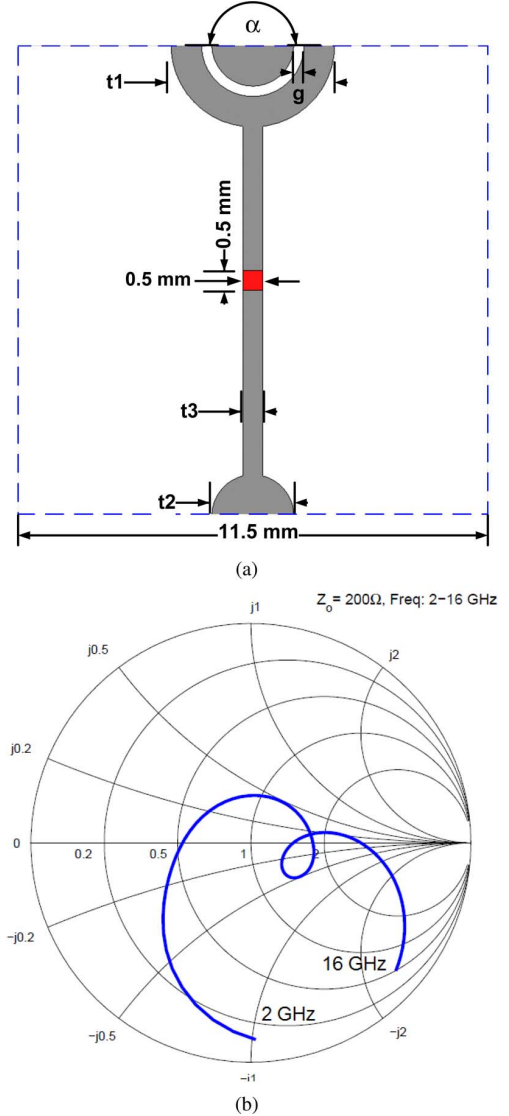


Fig. 2. Nonsymmetric element for TCDAs with  $t_1 = 2$  mm,  $t_2 = 1$  mm,  $t_3 = 0.5$  mm,  $g = 0.254$  mm,  $\alpha = 180^\circ$  placed 8 mm above a ground plane. (a) Top view of the unit-cell geometry and (b) input impedance for broadside radiation normalized to  $Z_0 = 200 \Omega$ .

( $0.35\lambda_H$ ), respectively, where  $\lambda_H$  is the free space wavelength at the highest design frequency of 13 GHz.

As a starting point, we chose the following parameters:  $t_1 = 2$  mm,  $t_2 = 1$  mm,  $t_3 = 0.5$  mm,  $g = 0.254$  mm,  $\alpha = 180^\circ$ . For this case the active input impedance is depicted in Fig. 2(b) as computed with infinite array analysis (periodic boundary conditions) using Ansoft's HFSS v12. Similar to [5] a nonsymmetric TCDA has a capacitive reactance at low frequencies which then passes through two resonances and two anti-resonances at higher frequencies forming a loop on the Smith chart. We note that a nonsymmetric TCDA has a broadside bandwidth of approximately 4.5:1 (active VSWR less than 2) which is similar to symmetric TCDAs found in the literature. The corresponding E- and H-plane scan element pattern (SEP), formally called the active element pattern [13], are shown in Fig. 3. This SEP includes the element pattern with all mutual coupling accounted for. Thus, the overall array pattern (ignoring edge effects) can be computed using the scan

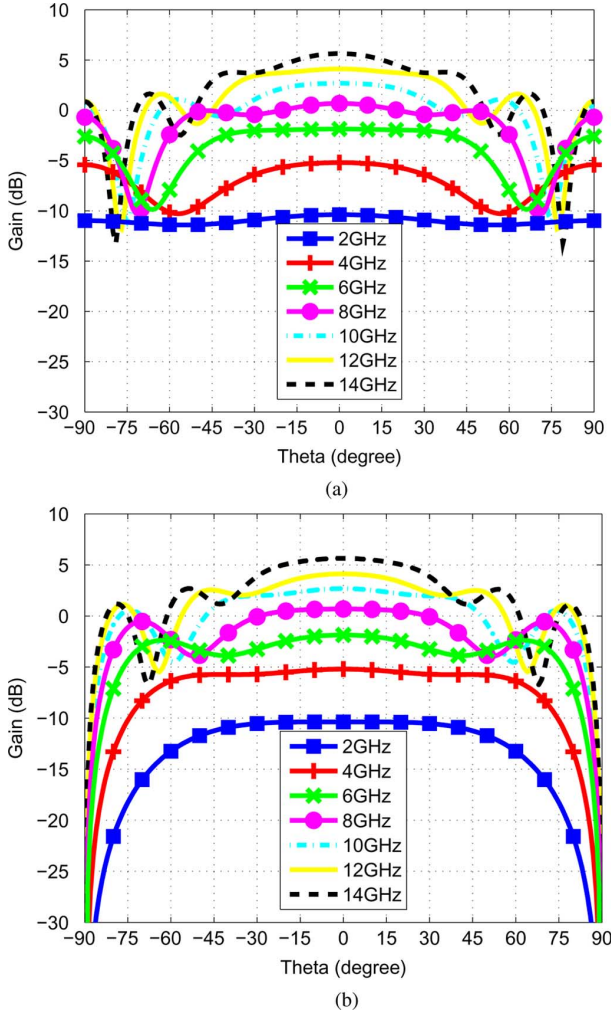


Fig. 3. Scan element pattern of the non-symmetric TCDA geometry in Fig. 2(a). (a) E-plane. (b) H-plane.

element pattern and array factor for a given finite array size and lattice [14].

From Fig. 3 we observe the E-plane SEP is similar to the H-plane pattern for  $-45^\circ \leq \theta \leq 45^\circ$  and fairly constant over a broad range of frequencies. However, at low elevation angles (towards grazing) the E and H-plane patterns deviate substantially. Specifically, the E-plane pattern has sharper nulls, while the H-plane pattern vanishes at  $\theta = \pm 90^\circ$ . The latter is associated with cancellation of radiated fields along the horizon due to the ground plane image current. As expected, the boresight SEP ( $\theta = 0^\circ$ ) is equal to the maximum unit cell directivity calculated by

$$D = \frac{4\pi A}{\lambda^2} \quad (1)$$

where  $A$  is the unit cell area. We remark that the SEP is typically stable with moderate geometry variations. Thus, we primarily focus on the scan impedance when designing the proposed broadband planar TCDA.

The first non-symmetric TCDA parameter to study is  $t_1$  (cup width). We found as  $t_1$  increases the low frequency reactance is reduced (a desirable effect). However, the resistance above

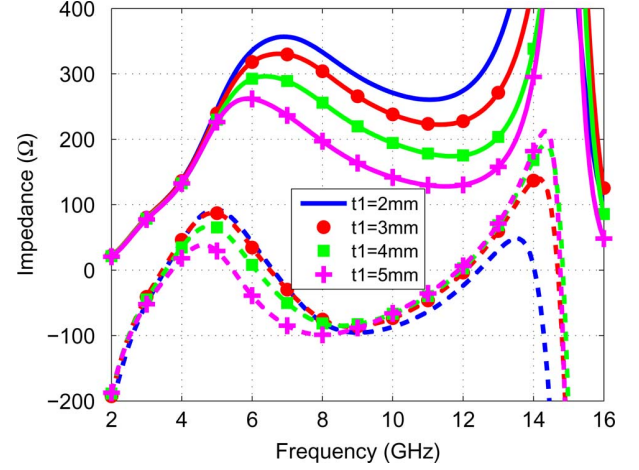


Fig. 4. Active resistance (solid) and reactance (dash) of the TCDA in Fig. 2(a) at broadside with  $t_1$  varied. All other parameters are kept constant:  $t_2 = 1$  mm,  $t_3 = 0.5$  mm,  $g = 0.254$  mm,  $\alpha = 180^\circ$ .

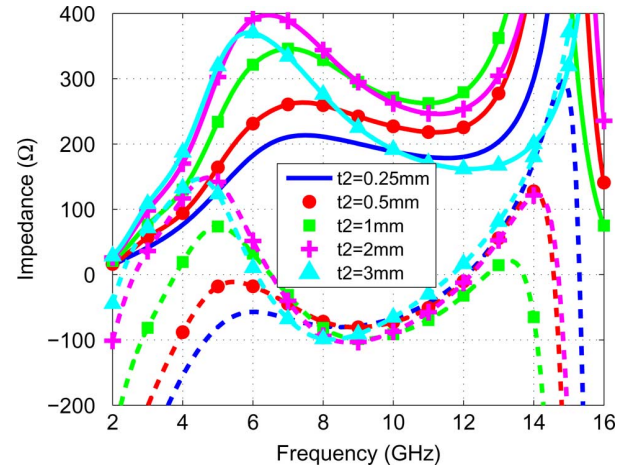


Fig. 5. Active resistance (solid) and reactance (dash) of the TCDA in Fig. 2(a) at broadside with the inner ball diameter ( $t_2$ ) varied and  $t_1 = t_2 + g + 0.25$  mm. All other parameters are kept constant:  $t_3 = 0.5$  mm,  $g = 0.254$  mm,  $\alpha = 180^\circ$ .

6 GHz is reduced as depicted in Fig. 4. Frequencies below 5 GHz are minimally effected.

To facilitate the study of  $t_2$  (the inner ball diameter), and not short the element to its neighbor,  $t_1$  had to also vary. Specifically, we set  $t_1 = t_2 + g + 0.25$  mm, implying a constant 0.25-mm cup rim width. Fig. 5 shows the impedance of the TCDA as  $t_2$  was varied from 0.25 mm to 3 mm. We observe that  $t_2$  needs to be larger to lower the first resonance peak from 12 GHz down to 2.2 GHz when  $t_2 = 3$  mm. This is because as  $t_2$  increases, the capacitive junction area also increases, resulting in a larger mutual capacitance. As such, significant miniaturization is achieved (the lowest operational frequency is reduced).

The next parameter considered was the arm width or  $t_3$ . As  $t_3$  increases, we observe a reduction of resistance and a larger reactance variation over the band (see Fig. 6). Below 5 GHz, the resistance is constant but for higher frequencies the resistance increases fourfold when decreasing the arm width to 3 mm from 0.5 mm. The larger resistance is attributed to a increased wire (self) inductance, also evident from the increased inductive reactance over the entire frequency range. As such, dipole arm



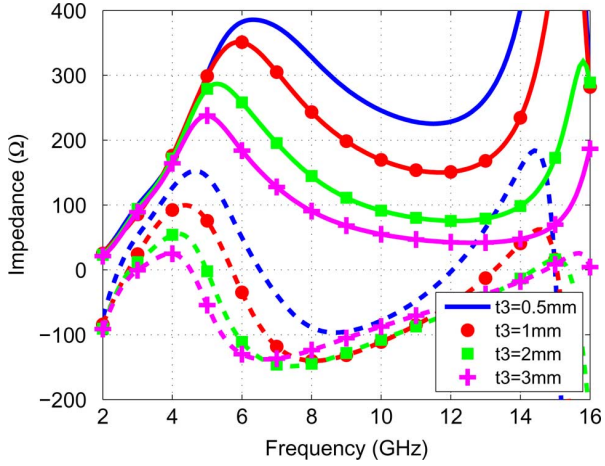


Fig. 6. Active resistance (solid) and reactance (dash) of the TCDA in Fig. 2(a) at broadside when  $t_3$  is varied. All other parameters are kept constant:  $t_1 = 2$  mm,  $t_2 = 1$  mm,  $g = 0.254$  mm,  $\alpha = 180^\circ$ .

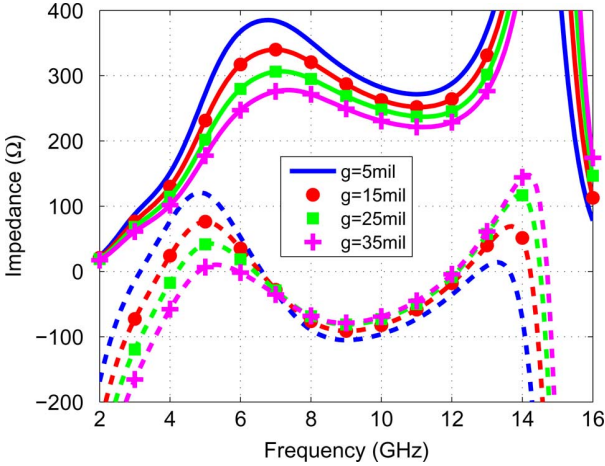


Fig. 7. Active resistance (solid) and reactance (dash) of the TCDA in Fig. 2(a) at broadside with the ball-and-cup gap ( $g$ ) varied. All other parameters are kept constant:  $t_1 = 2$  mm,  $t_2 = 1$  mm,  $t_3 = 0.5$  mm,  $\alpha = 180^\circ$ .

width is an important parameter used to match the TCDA's radiation resistance to a specific system impedance.

Another important design parameter is the gap separating the ball and cup,  $g$ . When  $g$  is small, we expect a significant increase in mutual coupling (effectively miniaturizing the antenna). This also translates to a larger resistance at all frequencies. Concurrently, the operational bandwidth is shifted to lower frequencies. Fig. 7 does indeed show these effects. Therefore, we want to keep the gap separation as small as possible (i.e., within manufacturing tolerances) for broadband operation.

The final parameter considered is the cup opening angle  $\alpha$  depicted in Fig. 8(a). Fig. 8(b) shows the impedance curves versus frequency for  $\alpha = 45^\circ, 105^\circ, 165^\circ, 225^\circ$ , and  $275^\circ$ . We observe that as  $\alpha$  is reduced, coupling increases due to the larger capacitive area. This, of course, leads to the desired effect of lowering the frequency of operation. However, the resistance increases rapidly at 6 GHz making the array difficult to match over a broad frequency range given a constant system impedance, for example  $200 \Omega$ . Using the aforementioned impedance tuning results, the following parameters were selected for our X-band demonstration array:  $t_1 = 1.75$  mm,  $t_2 = 0.75$  mm,  $t_3 = 1$  mm,  $g = 0.1778$  mm, and  $\alpha = 85^\circ$ . This provides a fairly

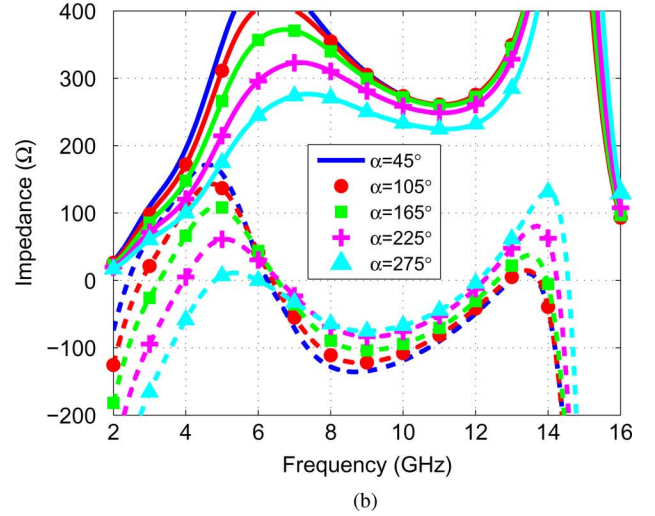
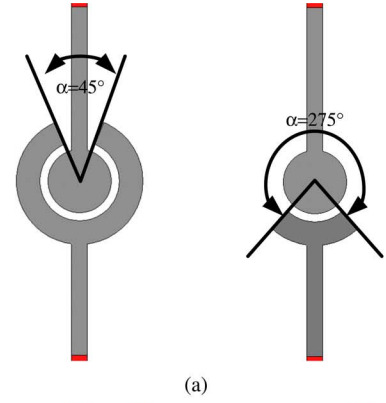


Fig. 8. Active impedance of the TCDA in Fig. 2(a) at broadside for varying  $\alpha$  values. All other parameters are kept constant:  $t_1 = 2$  mm,  $t_2 = 1$  mm,  $t_3 = 0.5$  mm, and  $g = 0.254$  mm. (a) Ball-and-cup geometry showing different  $\alpha$  values. (b) Resistance (solid) and reactance (dash).

constant input impedance of  $\approx 200 \Omega$  with a small reactive component.

### III. TCDA WITH WIDEBAND BALUN FEED

A wideband TCDA requires a wideband balanced feed for each element. As such, in [15] we designed, fabricated, and experimentally verified a small X-band prototype array with a wideband microstrip ring hybrid. The array had a single active element with remaining 63 elements terminated in  $100\text{-}\Omega$  resistors at the array aperture. The prototype array was used to examine some of the fabrication challenges and to validate numerical calculations. The hybrid employed coupled microstrip lines for bandwidth improvement [16]. However, further studies showed that the microstrip probe in [15] led to an increased cross-polarized field (only 10 dB below the copolarized component). We remark the array aperture without feed maintains a cross-polarized level 50 dB below copolarized gain in the principal planes. We therefore proceeded to minimize probe-ring coupling by relocating the probe location. The developed ring hybrid is shown in Fig. 9 and supports a  $50\text{-}\Omega$  coaxial input (GPO connector). The hybrid has two output ports extending inside the ring,  $180^\circ$  out of phase from each other producing the desired balanced feed. As a result, the fields add in series forming a  $100 \Omega$  balanced line. Unlike the design in [16], the

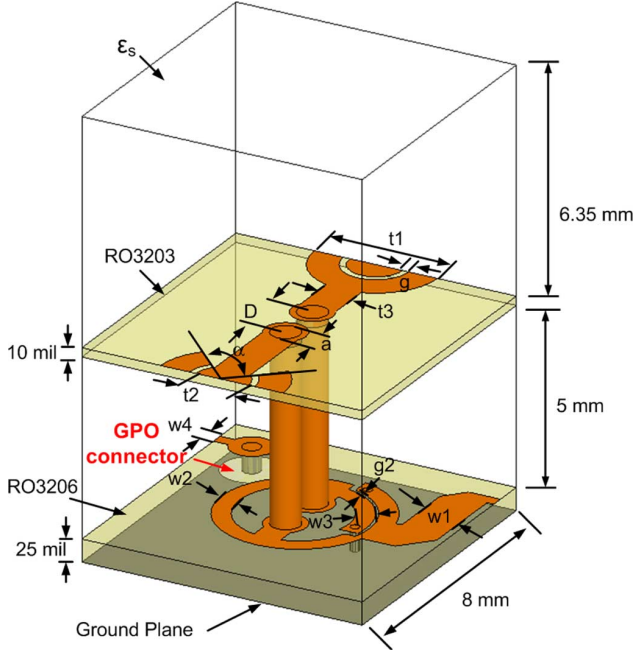


Fig. 9. Nonsymmetric TCDA unit cell geometry including the WAIM superstrate, integrated microstrip balun and twin wire matching network interconnects. The array parameters are given by:  $t_1 = 1.75$  mm,  $t_2 = 0.75$  mm,  $t_3 = 1$  mm,  $g = 0.1778$  mm,  $\alpha = 85^\circ$ ,  $a = 0.8128$  mm,  $D = 1.4$  mm,  $w_1 = 1.2192$  mm,  $w_2 = 0.508$  mm,  $w_3 = 0.4318$  mm,  $w_4 = 0.3556$  mm,  $g_2 = 0.0762$  mm, and  $\epsilon_s = 1.7$ .

unused terminated sum or in-phase port was removed, reducing insertion loss by approximately 0.25 dB.

Due to the large array input resistance ( $R_a \approx 200$  to  $300 \Omega$  for typical nonsymmetric TCDA), the element cannot be directly connected to the  $100\text{-}\Omega$  ring output. Instead, a small twin-wire transmission line was used to connect and impedance match the array to the balun. Specifically, a twin-wire diameter and spacing of  $0.8128$  mm (20 gauge) and  $1.4$  mm, was used respectively. This yielded a characteristic impedance of  $136 \Omega$ , sufficient for our design while remaining easy to fabricate.

To avoid common-mode excitation typically found in tightly coupled arrays, the unit cell width and ground plane spacing was reduced to  $8$  mm and  $5$  mm, respectively. Reducing these dimensions shifts the common-mode above band. The common mode occurs when the antenna length and vertical feed lines are  $1\lambda$  long. For more information on tightly coupled aperture common modes, the reader is referred to [17], [18]. In addition, a  $6.35$ -mm-thick wide-angle impedance matching (WAIM) superstrate [19] having a dielectric constant ( $\epsilon_s$ ) of  $1.7$  was added to facilitate a wider scanning range. The non-symmetric element with integrated feed, microstrip hybrid and radome is shown in Fig. 9. Of importance is that the balun feed and array is printed using standard low-cost COTS PCB (Rogers 3203 for the array aperture and Rogers 3206 for the balun).

The boresight directivity and realized gain is shown in Fig. 10. We observe that the realized gain approaches the directivity from  $8$ – $12.5$  GHz and cross polarization is less than  $-20$  dB. Furthermore, the realized gain is within  $0.3$  dB of the maximum aperture directivity and the radiation efficiency is greater than  $93\%$  including dielectric and copper conductor losses. Of importance is the remarkable scanning performance

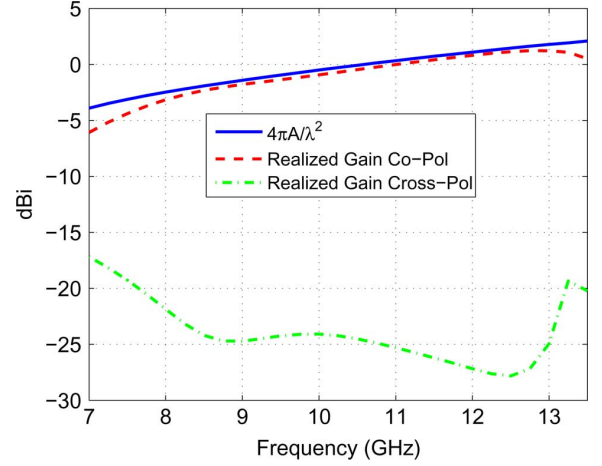


Fig. 10. Broadside realized gain of the non-symmetric TCDA unit cell with balun feed and WAIM radome.

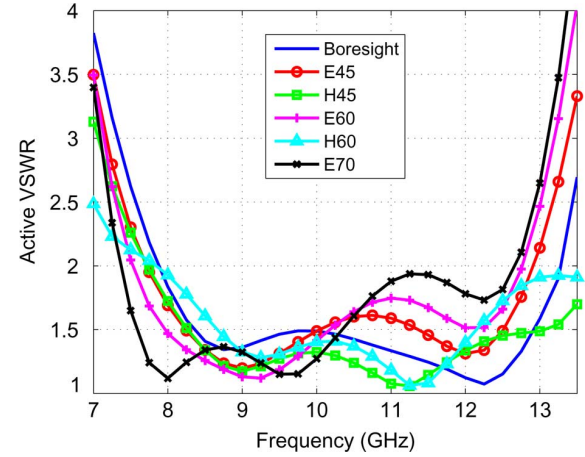


Fig. 11. Non-symmetric TCDA unit cell with feed active VSWR over multiple scan angles.

of this array. As depicted in Fig. 11, the array maintains an active VSWR less than 2 from  $8$ – $12.5$  GHz while scanning up to  $70^\circ$  in the E-plane and  $60^\circ$  in the H-plane.

#### IV. $8 \times 8$ FINITE ARRAY EXPERIMENTAL RESULTS

An  $8 \times 8$  array was fabricated for measurements as depicted in Fig. 12. To realize this array, a solder mask was employed on the array and balun PCBs for soldering ease as shown in Fig. 12(b). In addition, each board was extended  $12.7$  mm around the array aperture to facilitate four nylon bolt holes. We also carried out finite array simulations using HFSS to serve as reference for the fabricated finite array prototype. We note that the only differences between fabricated and simulated geometries are the solder mask.

The array was mounted on a low permittivity dielectric pylon in the Electrosience Laboratory compact range. Fig. 13 displays the measured and simulated realized gain versus frequency for a single element (number 29) excited with all others terminated using  $50\text{-}\Omega$  GPO loads. The measured and simulated results are in good agreement, given the finite array simulation size with multiple dielectrics and detailed feed geometries. The simulation uses  $1.83$  million tetrahedra and memory usage of  $61.1$  GB.

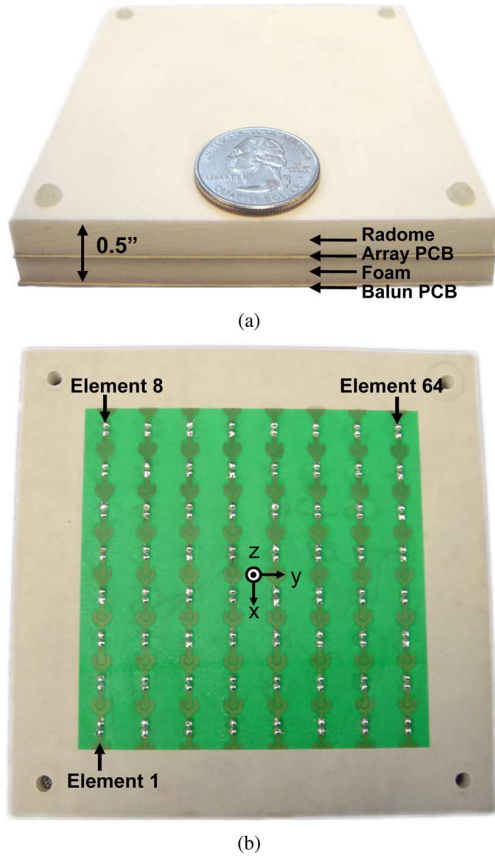


Fig. 12. X-band 64-element linear polarized array prototype. (a) With radome. (b) Radome removed.

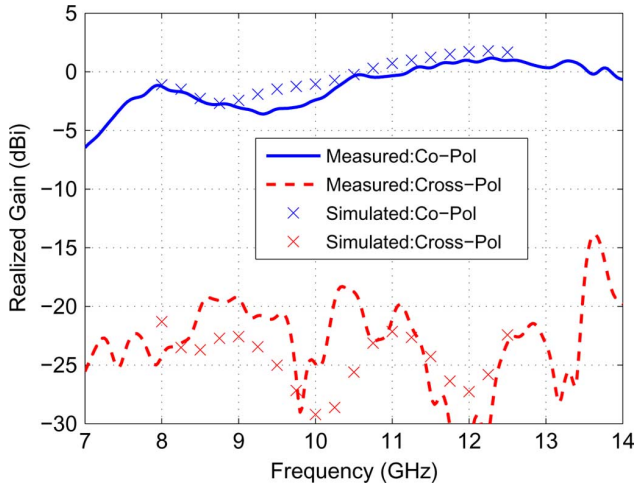


Fig. 13. Finite array broadside realized gain for a central element excited and remaining elements terminated in  $50\ \Omega$  loads.

The E- and H-plane SEP for element 29 (near the array center) at 10 GHz (center frequency of the operating band) is shown in Figs. 14 and 15, respectively. The Ludwig third definition of cross-polarization is used [20], and found to be approximately  $-20$  dB or lower over most of the principal plane scanning range. Due to the relative small size of the test array, edge effects dominate, therefore the SEP and active impedance of each element varies considerably [21]. As such, the increased level of cross-polarization near  $\theta = 20^\circ$  is not representative of the cross-polarization level while scanning. For more details on the

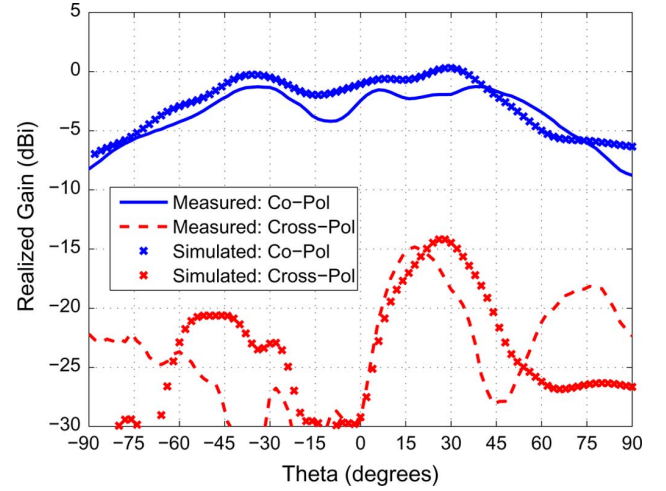


Fig. 14. Finite array E-plane SEP for a central element excited and remaining elements terminated in  $50\ \Omega$  loads.

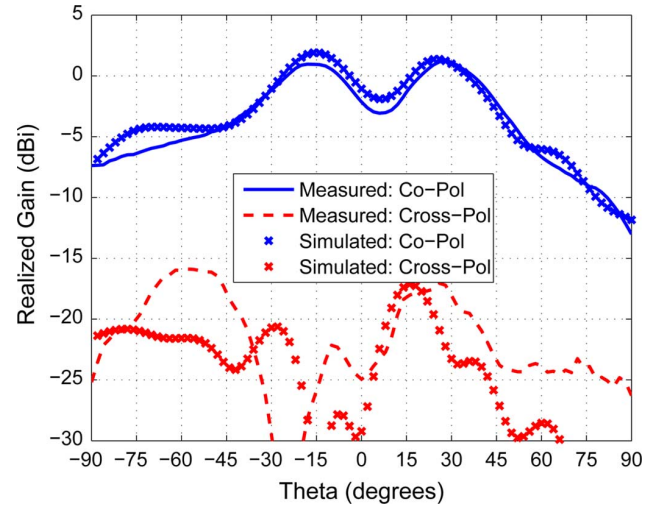


Fig. 15. Finite array H-plane SEP for a central element excited and remaining elements terminated in  $50\ \Omega$  loads.

measured SEP variation and S-parameters across the aperture the reader is referred to [22]. The radiation patterns from 8 to 12.5 GHz show similar agreement and were omitted for brevity.

Of particular interest is the fully excited array gain and polarization level while scanning. To demonstrate the wide-angle scanning performance of the non-symmetric TCDA prototype, the radiation pattern of each element was measured and combined with uniform weighting using MATLAB. In addition, the array element excitations were progressively phased in simulation to steer the beam for numerical predictions.

The E-plane measured and simulated radiation pattern while scanning to broadside,  $30^\circ$  and  $60^\circ$  is shown in Fig. 16. Similarly, the H-plane beam steering performance is displayed in Fig. 17. We note that the simulated realized gain pattern incorporates the active (or scan) reflection coefficient mismatch for each element where the measured patterns (and subsequently post-processed combined pattern) uses the element's self reflection coefficient ( $S_{11}$ ,  $S_{22}$ , etc.). Indeed, good agreement between simulated and measured scanning patterns in the principal planes are observed. The measured cross-polarized component is stronger than simulation predicted (not shown for clarity), but



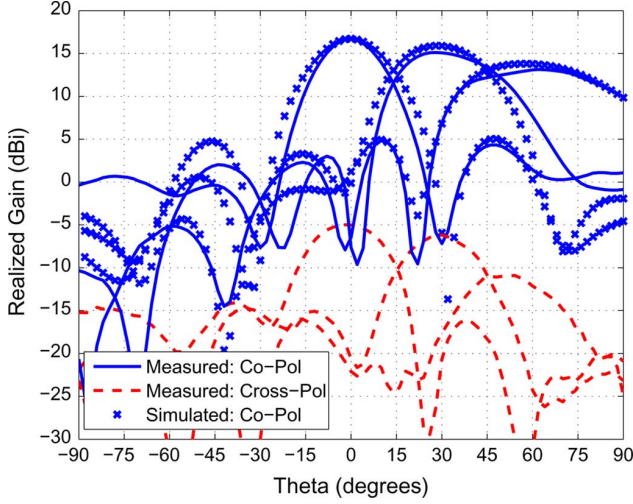


Fig. 16. Finite array E-plane radiation pattern at 10 GHz scanned to  $\theta_o = 0^\circ, 30^\circ, 60^\circ$ ,  $\phi_o = 0^\circ$ .

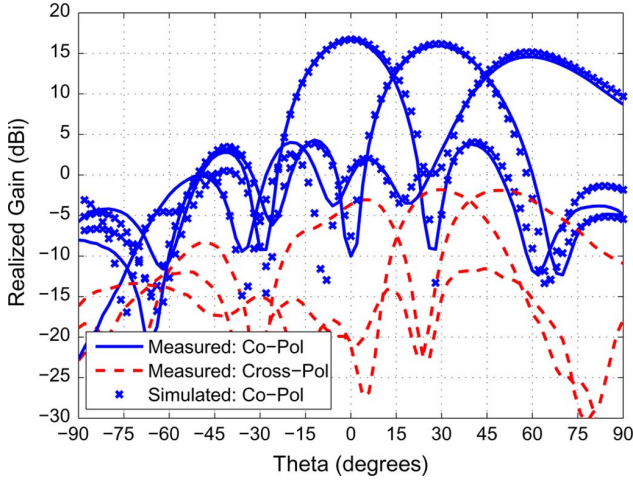


Fig. 17. Finite array H-plane radiation pattern at 10 GHz scanned to  $\theta_o = 0^\circ, 30^\circ, 60^\circ$ ,  $\phi_o = 0^\circ$ .

remains 18 dB below the copolarized component when scanned to  $60^\circ$  in the H-plane. It is believed that scattering from the array mounting fixture (as it is held by fiberglass attachments on the array's H-plane) contributes to the higher measured H-plane cross-polarized gain.

The measured and simulated broadside array gain is compared to the maximum theoretical directivity in Fig. 18. The simulated realized gain is higher than the theoretical limit above 11 GHz due to the finite ground plane diffraction adding in phase. Similarly, below 11 GHz the gain is slightly lower than the limit because the diffraction combines destructively. Further, we remark the area used in calculation was determined using the TCDA elements physical aperture area and not the PCB or ground plane area which extends past the aperture to accommodate mechanical mounting.

## V. DIAGONAL PLANE CROSS-POLARIZATION PERFORMANCE

It is of interest to compare the developed non-symmetric TCDA to other wideband array technologies. A key feature of low-profile phased array antennas is the improved cross polarization ratio in the diagonal plane compared to traditional

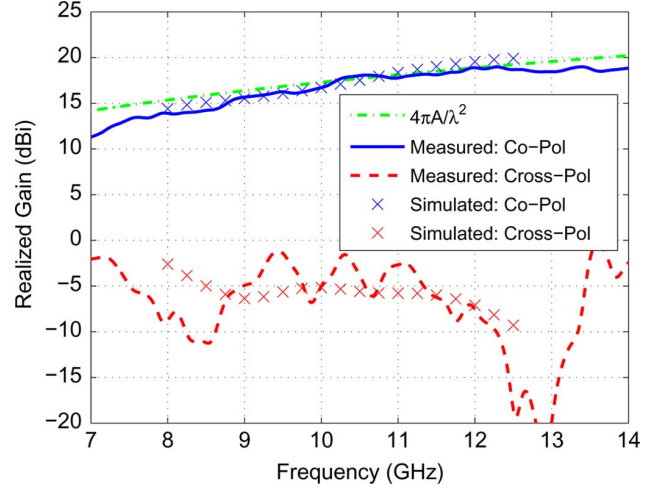


Fig. 18. Finite array broadside realized gain as a function of frequency with all elements excited.

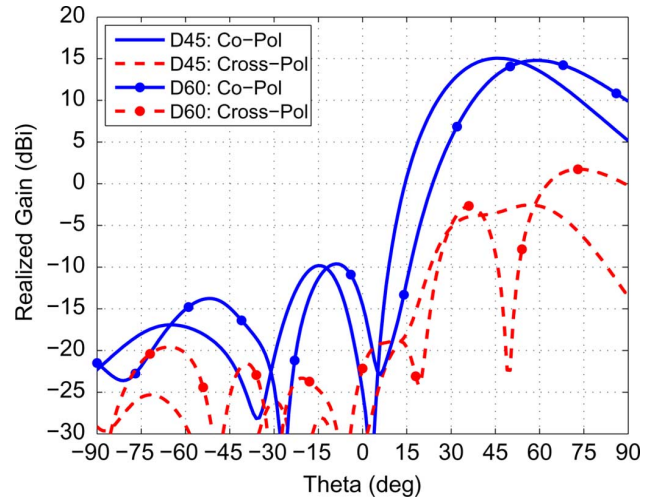


Fig. 19. Simulated finite array D-plane radiation pattern at 10 GHz scanned to  $\theta_o = 45^\circ, 60^\circ$ ,  $\phi_o = 45^\circ$ .

long UWB flared notch antenna designs [23], whose cross-polarization ratio can be positive (cross-polarization is stronger than the copolarized field) at wide scan angles.

First, we examined the D-plane cross-polarization ratio ( $E_x/E_y$ ) using the  $8 \times 8$  element finite array HFSS simulation model. The D-plane is defined as the diagonal plane ( $\phi = 45^\circ$ ) and again the Ludwig third definition of polarization was used. The simulation model was scanned with uniform amplitude to  $45^\circ$  and  $60^\circ$ . As shown in Fig. 19, the diagonal plane cross-polarization level is approximately 15 dB below the copolarized component. The cross-polarization maximum at  $60^\circ$  scan is  $12^\circ$  further in angle than the co-polarized main beam. With this mind, the cross-polarization ratio was calculated using the maximum level of cross-polarization.

The theoretically achievable cross-polarization ratio of a uniform current sheet was calculated using (2) and (3) and serves as a reference level for the proposed non-symmetric dipole array:

$$E_x = E_\theta \cos \phi - E_\phi \sin \phi \quad (2)$$

$$E_y = E_\theta \sin \phi + E_\phi \cos \phi. \quad (3)$$

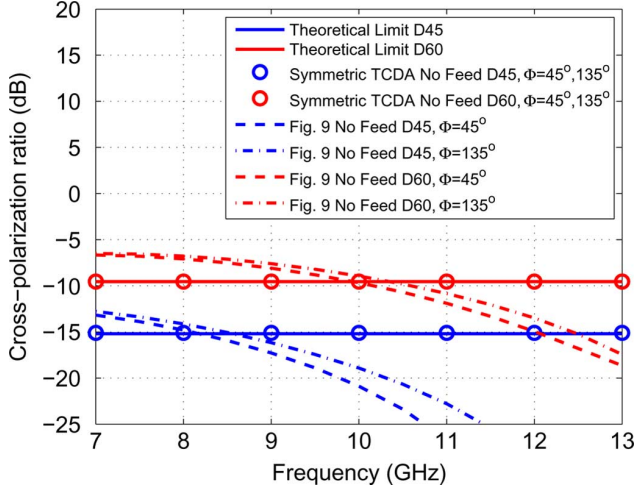


Fig. 20. Diagonal plane simulated infinite symmetric and non-symmetric TCDA without feed cross-polarization ratio scanned to  $\theta_o = 45^\circ, 60^\circ$ ,  $\phi_o = 45^\circ$  and  $135^\circ$ .

An infinite uniform  $x$ -directed electric current sheet's radiated field components,  $E_\theta$  and  $E_\phi$ , are given by [24] and shown in (4) and (5). Note the factor  $j\eta_o \exp\{-jk_o \cos \theta |z|\}$  was omitted where  $\eta_o$  is the intrinsic free-space wave impedance:

$$E_\theta = \cos \phi \quad (4)$$

$$E_\phi = \frac{-\sin \phi}{\cos \theta}. \quad (5)$$

Examining (2)–(5) it is clear the infinite current sheet polarization performance is not a function of frequency. To validate the formulation, a symmetric TCDA and the non-symmetric antenna in Fig. 9 was simulated without vertical twin-wire interconnects. A comparison between the theoretical cross-polarization limit is shown in Fig. 20. As expected, the symmetric element without feed is in perfect agreement with the limit and the nonsymmetric element is close. Due to the nonsymmetric structure, both  $\phi_o = 45^\circ$  and  $\phi_o = 135^\circ$  diagonal planes are shown. The element is symmetric with respect to the  $x$ -axis, therefore  $\phi_o = 225^\circ$  and  $\phi_o = 315^\circ$  is repetitive and omitted. The theoretical cross-polarization ratio of  $-15$  dB at  $45^\circ$  D-plane scan is in agreement with [25] where a Greens function formulation was used. Further, the theoretical limit also agrees with other wideband planar phased array author's observations [26], [27]. Fig. 20 demonstrates that symmetric TCDAs and nonsymmetric TCDAs emulate an infinite current sheet.

The cross-polarization ratio for the design in Fig. 9 with feed is shown in Fig. 21. The element's cross-polarization level is above the theoretical curve at the band limits and below at the center portion of the band. This is a result of small feed radiation constructively and destructively canceling with the unwanted cross-polarized radiated field. For completeness, the simulated finite array cross-polarization ratio at  $\phi_o = 45^\circ$  and  $\theta_o = 60^\circ$  is plotted at the operational band's low, mid and high frequencies. The finite array diffraction also interferes with the antenna radiation and tracks the unit cell predicted response fairly well until 8 GHz when array truncation effects dominate.

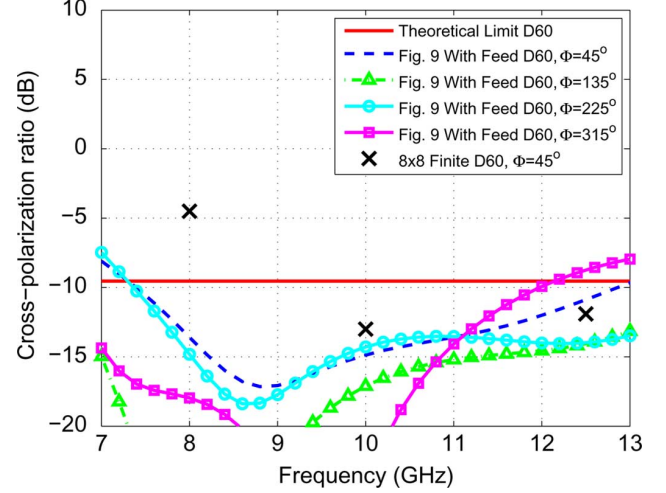


Fig. 21. Diagonal plane simulated infinite non-symmetric TCDA with feed and simulated  $8 \times 8$  finite array cross-polarization ratio scanned to  $\theta_o = 60^\circ$ .

## VI. CONCLUSION

A novel nonsymmetric tightly coupled dipole array with integrated balun and matching network was presented. The array is placed  $\lambda/7$  over a ground plane at the lowest frequency of operation (8 GHz). The array relied on a new non-symmetric dipole element offering several degrees of freedom to allow cancellation of the inductance caused by the ground plane. Multiple parametric sweeps were presented to control the array impedance and lower the frequency of operation. A wideband ring hybrid was proposed for unbalanced-to-balanced conversion. The feed is printed directly on the ground plane, maintaining the array's low-profile height and simple layered planar PCB construction. A  $136\text{-}\Omega$  twin wire transmission line connects the feed and aperture while providing impedance matching. We remark that the actual array bandwidth is much larger, and at this time is limited by the feed design. Future efforts will therefore focus on increasing feed bandwidth, to fully exploit the wide bandwidth enabled by this array concept. The developed ground plane backed array is capable of scanning up to  $75^\circ$  in E-plane and  $60^\circ$  in H-plane with an active VSWR less than 2 from 8–12.5 GHz (1.6:1). In the diagonal plane, the array's cross-polarization ratio agrees with a newly developed planar aperture theoretical limit of  $-15$  dB and  $-9.5$  dB at  $45^\circ$  and  $60^\circ$  scan, respectively. A small finite  $8 \times 8$  array was fabricated and verified experimentally. Good agreement between simulation and measurement was confirmed over multiple scan angles.

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