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80 Implied bound: 1
81 MIR: 7
82 StrongCG: 4
83 GUB cover: 26
84 RLT: 2
85 Relax-and-lift: 24
86 BQP: 1
87
88 Explored 1 nodes (25603 simplex iterations) in 24.04 seconds (46.24 work units)
89 Thread count was 8 (of 8 available processors)
90
91 Solution count 4: 803 1003 2123 3583
92
93 Optimal solution found (tolerance 1.00e-10)
94 Best objective 8.030000000000e+02, best bound 8.030000000000e+02, gap 0.0000%
95 Set parameter MIPGap to value 1e-08
96 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
97
98 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
99 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
100
101 Optimize a model with 536186 rows, 14427 columns and 1098485 nonzeros
102 Model fingerprint: 0xf8c80c4a
103 Variable types: 36 continuous, 14391 integer (8316 binary)
104 Coefficient statistics:
105 Matrix range [1e-01, 1e+10]
106 Objective range [6e-05, 5e+01]
107 Bounds range [1e+00, 1e+00]
108 RHS range [8e-01, 1e+10]
109 Warning: Model contains large matrix coefficients
110 Warning: Model contains large rhs
111 Consider reformulating model or setting NumericFocus parameter
112 to avoid numerical issues.
113 Presolve removed 533874 rows and 13592 columns
114 Presolve time: 0.38s
115 Presolved: 2312 rows, 835 columns, 6149 nonzeros
116 Variable types: 5 continuous, 830 integer (502 binary)
117 Found heuristic solution: objective 3536.0500186
118
119 Root relaxation: objective 4.329050e+03, 655 iterations, 0.00 seconds (0.01 work units)
120
121 Nodes | Current Node | Objective Bounds | Work
122 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
123
124 H 0 0 4329.0500186 8215.74099 89.8% - 0s
125 0 0 - 0 4329.05002 4329.05002 0.00% - 0s
126
127 Explored 1 nodes (967 simplex iterations) in 0.52 seconds (0.77 work units)
128 Thread count was 8 (of 8 available processors)
129
130 Solution count 2: 4329.05 3536.05
131
132 Optimal solution found (tolerance 1.00e-08)
133 Best objective 4.329050018628e+03, best bound 4.329050018628e+03, gap 0.0000%
134 SP is solved
135 SP's optimal solution is'□4329
136
137 Itr = 0
138 Collect_LB = [803.0]
139 Collect_UB = [9461.100037255623]
140 Collect_Hua = [0.0]
141 Collect_SPObjVal = [4329.050018627811]
142 Collect_MPObjValNHua = [803.0]
143
144
145 Set parameter MIPGap to value 1e-10
146 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
147
148 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
149 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
150
151 Optimize a model with 563247 rows, 283978 columns and 1563481 nonzeros
152 Model fingerprint: 0x92045efc
153 Variable types: 1 continuous, 283977 integer (283941 binary)
154 Coefficient statistics:
155 Matrix range [1e+00, 1e+10]
156 Objective range [1e+00, 2e+01]
157 Bounds range [1e+00, 1e+00]
158 RHS range [1e+00, 2e+10]
159 Warning: Model contains large matrix coefficients
160 Warning: Model contains large rhs
161 Consider reformulating model or setting NumericFocus parameter
162 to avoid numerical issues.
163 Presolve removed 404285 rows and 266303 columns (presolve time = 5s) ...

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164 Presolve removed 537986 rows and 276495 columns
165 Presolve time: 7.49s
166 Presolved: 25261 rows, 7483 columns, 100784 nonzeros
167 Variable types: 0 continuous, 7483 integer (7461 binary)
168
169 Root simplex log...
170
171 Iteration   Objective    Primal Inf.   Dual Inf.    Time
172      0  5.1320500e+03  8.8900000e+02  0.0000000e+00  8s
173    4703  5.1320500e+03  0.0000000e+00  0.0000000e+00  8s
174
175 Root relaxation: objective 5.132050e+03, 4703 iterations, 0.17 seconds (0.23 work units)
176
177   Nodes | Current Node | Objective Bounds | Work
178 Expl Unexpl | Obj Depth IntInf | Incumbent  BestBd  Gap | It/Node Time
179
180  0  0 5132.05002  0  36    -5132.05002  -  -  8s
181  0  0 5132.05002  0 134    -5132.05002  -  -  8s
182  0  0 5132.05002  0 132    -5132.05002  -  -  9s
183  0  0 5132.05002  0 448    -5132.05002  -  -  9s
184  0  0 5132.05002  0 418    -5132.05002  -  -  9s
185  0  0 5132.05002  0 454    -5132.05002  -  - 10s
186  0  0 5132.05002  0 156    -5132.05002  -  - 12s
187  0  0 5132.05002  0 565    -5132.05002  -  - 13s
188  0  0 5132.05002  0 507    -5132.05002  -  - 13s
189  0  0 5132.05002  0 303    -5132.05002  -  - 17s
190  0  0 5132.05002  0 297    -5132.05002  -  - 17s
191  0  0 5132.05002  0 514    -5132.05002  -  - 19s
192  0  0 5132.05002  0 340    -5132.05002  -  - 24s
193 H  0  0          7652.0500186 5132.05002 32.9%  - 25s
194  0  0 5132.05002  0 303 7652.05002 5132.05002 32.9%  - 26s
195 H  0  0          7052.0500186 5132.05002 27.2%  - 27s
196 H  0  0          6972.0500186 5132.05002 26.4%  - 27s
197 H  0  0          6572.0500186 5132.05002 21.9%  - 27s
198  0  2 5132.05002  0 303 6572.05002 5132.05002 21.9%  - 28s
199  3  8 5132.05002  2 493 6572.05002 5132.05002 21.9% 7035 31s
200 15 20 5134.13314  4 1219 6572.05002 5132.05002 21.9% 5430 35s
201 28 34 5132.05002  6 663 6572.05002 5132.05002 21.9% 4266 40s
202 63 52 5133.55107  9 1138 6572.05002 5132.05002 21.9% 2841 45s
203 130 129 5251.57943 16 874 6572.05002 5132.05002 21.9% 2108 50s
204 H 225 234          5932.0500186 5132.05002 13.5% 1272 52s
205 H 391 264          5852.0500186 5132.05002 12.3% 758 53s
206 445 332 5612.05002 112 151 5852.05002 5132.05002 12.3% 679 55s
207 H 592 228          5412.0500186 5132.05002 5.17% 584 58s
208 599 240 5141.30069 12 753 5412.05002 5132.05002 5.17% 609 60s
209 763 215 5152.05002 44 610 5412.05002 5132.05002 5.17% 563 65s
210 H 807 229          5332.0500186 5132.05002 3.75% 591 67s
211 821 238 5152.05002 52 608 5332.05002 5132.05002 3.75% 609 70s
212 888 154 5152.05002 55 303 5332.05002 5132.05002 3.75% 624 81s
213 894 158 5302.05002  5 646 5332.05002 5175.18834 2.94% 620 85s
214 900 162 5192.05002  6 471 5332.05002 5192.05002 2.63% 616 90s
215 H 905 156          5232.0500186 5192.05002 0.76% 612 94s
216
217 Cutting planes:
218   Learned: 1
219   Gomory: 27
220   Cover: 426
221   Implied bound: 40
222   Projected implied bound: 43
223   Clique: 68
224   MIR: 98
225   StrongCG: 34
226   Flow cover: 231
227   GUB cover: 53
228   Zero half: 92
229   RLT: 13
230   Relax-and-lift: 115
231   BQP: 2
232
233 Explored 906 nodes (712058 simplex iterations) in 95.05 seconds (234.58 work units)
234 Thread count was 8 (of 8 available processors)
235
236 Solution count 9: 5232.05 5332.05 5412.05 ... 7652.05
237
238 Optimal solution found (tolerance 1.00e-10)
239 Best objective 5.232050018628e+03, best bound 5.232050018628e+03, gap 0.0000%
240 Set parameter MIPGap to value 1e-08
241 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
242
243 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
244 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
245
246 Optimize a model with 536186 rows, 14427 columns and 1098485 nonzeros
247 Model fingerprint: 0xc35efe82

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248 Variable types: 36 continuous, 14391 integer (8316 binary)
249 Coefficient statistics:
250   Matrix range   [1e-01, 1e+10]
251   Objective range [6e-05, 5e+01]
252   Bounds range   [1e+00, 1e+00]
253   RHS range      [8e-01, 1e+10]
254 Warning: Model contains large matrix coefficients
255 Warning: Model contains large rhs
256   Consider reformulating model or setting NumericFocus parameter
257   to avoid numerical issues.
258 Presolve removed 531398 rows and 12899 columns
259 Presolve time: 0.38s
260 Presolved: 4788 rows, 1528 columns, 12871 nonzeros
261 Variable types: 8 continuous, 1520 integer (882 binary)
262 Found heuristic solution: objective 3697.0500186
263
264 Root relaxation: objective 5.285581e+03, 1398 iterations, 0.01 seconds (0.02 work units)
265
266   Nodes | Current Node | Objective Bounds | Work
267 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
268
269   0   0 5285.58074   0 11 3697.05002 5285.58074 43.0% - 0s
270 H   0   0           4376.5807430 5285.58074 20.8% - 0s
271 H   0   0           5285.5807430 5285.58074 0.00% - 0s
272   0   0 5285.58074   0 11 5285.58074 5285.58074 0.00% - 0s
273
274 Explored 1 nodes (1896 simplex iterations) in 0.58 seconds (0.80 work units)
275 Thread count was 8 (of 8 available processors)
276
277 Solution count 3: 5285.58 4376.58 3697.05
278
279 Optimal solution found (tolerance 1.00e-08)
280 Best objective 5.285580742960e+03, best bound 5.285580742960e+03, gap 0.0000%
281 SP is solved
282 SP's optimal solution is'□5285
283
284 Itr = 1
285 Collect_LB = [803.0, 5232.050018627811]
286 Collect_UB = [9461.100037255623, 6188.580742959544]
287 Collect_Hua = [0.0, 4329.050018627811]
288 Collect_SPObjVal = [4329.050018627811, 5285.580742959544]
289 Collect_MPObjValNHua = [803.0, 903.0]
290
291
292 Set parameter MIPGap to value 1e-10
293 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
294
295 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
296 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
297
298 Optimize a model with 563247 rows, 283978 columns and 1563481 nonzeros
299 Model fingerprint: 0xfa7b8115
300 Variable types: 1 continuous, 283977 integer (283941 binary)
301 Coefficient statistics:
302   Matrix range   [1e+00, 1e+10]
303   Objective range [1e+00, 2e+01]
304   Bounds range   [1e+00, 1e+00]
305   RHS range      [1e+00, 2e+10]
306 Warning: Model contains large matrix coefficients
307 Warning: Model contains large rhs
308   Consider reformulating model or setting NumericFocus parameter
309   to avoid numerical issues.
310 Presolve removed 413428 rows and 267080 columns (presolve time = 5s) ...
311 Presolve removed 539039 rows and 276661 columns
312 Presolve time: 7.74s
313 Presolved: 24208 rows, 7317 columns, 96550 nonzeros
314 Variable types: 0 continuous, 7317 integer (7295 binary)
315
316 Root simplex log...
317
318 Iteration Objective Primal Inf. Dual Inf. Time
319   0 6.1071522e+03 8.840000e+02 0.000000e+00 8s
320 3521 6.1071522e+03 0.000000e+00 0.000000e+00 8s
321
322 Root relaxation: objective 6.107152e+03, 3521 iterations, 0.08 seconds (0.10 work units)
323
324   Nodes | Current Node | Objective Bounds | Work
325 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
326
327   0   0 6107.15217   0 34 -6107.15217 - - 8s
328   0   0 6107.15217   0 136 -6107.15217 - - 9s
329   0   0 6107.15217   0 147 -6107.15217 - - 9s
330   0   0 6107.15217   0 127 -6107.15217 - - 9s
331   0   0 6107.15217   0 264 -6107.15217 - - 9s

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332 0 0 6107.15217 0 258 -6107.15217 - - 9s
333 0 0 6107.15217 0 226 -6107.15217 - - 11s
334 0 0 6107.15217 0 224 -6107.15217 - - 11s
335 0 0 6107.15217 0 427 -6107.15217 - - 11s
336 0 0 6107.15217 0 458 -6107.15217 - - 11s
337 0 0 6107.15217 0 198 -6107.15217 - - 15s
338 0 0 6107.15217 0 244 -6107.15217 - - 15s
339 0 0 6107.15217 0 220 -6107.15217 - - 15s
340 0 0 6107.15217 0 284 -6107.15217 - - 16s
341 0 0 6107.15217 0 264 -6107.15217 - - 16s
342 0 0 6107.15217 0 113 -6107.15217 - - 18s
343 H 0 0 8827.1521715 6107.15217 30.8% - 18s
344 0 0 6107.15217 0 67 8827.15217 6107.15217 30.8% - 18s
345 H 0 0 7087.1521715 6107.15217 13.8% - 19s
346 H 0 0 6707.1521715 6107.15217 8.95% - 20s
347 0 2 6107.15217 0 67 6707.15217 6107.15217 8.95% - 20s
348 36 34 6107.15217 9 234 6707.15217 6107.15217 8.95% 1604 25s
349 H 69 65 6567.1521715 6107.15217 7.00% 1251 28s
350 H 117 100 6367.1521715 6107.15217 4.08% 930 29s
351 131 105 6107.15217 27 309 6367.15217 6107.15217 4.08% 885 30s
352 H 368 214 6307.1521715 6107.15217 3.17% 523 34s
353 388 236 6107.15217 51 450 6307.15217 6107.15217 3.17% 543 35s
354 H 529 255 6267.1521715 6107.15217 2.55% 439 36s
355 H 557 264 6247.1521715 6107.15217 2.24% 420 36s
356 H 562 264 6207.1521715 6107.15217 1.61% 417 36s
357 H 642 275 6167.1521715 6107.15217 0.97% 372 37s
358 959 3 6107.15217 9 187 6167.15217 6107.15217 0.97% 278 40s
359 H 1016 75 6127.1521715 6107.15217 0.33% 285 41s
360
361 Explored 1120 nodes (365288 simplex iterations) in 43.22 seconds (85.45 work units)
362 Thread count was 8 (of 8 available processors)
363
364 Solution count 10: 6127.15 6167.15 6207.15 ... 7087.15
365
366 Optimal solution found (tolerance 1.00e-10)
367 Best objective 6.127152171531e+03, best bound 6.127152171531e+03, gap 0.0000%
368 Set parameter MIPGap to value 1e-08
369 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
370
371 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
372 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
373
374 Optimize a model with 536186 rows, 14427 columns and 1098485 nonzeros
375 Model fingerprint: 0xb8512909
376 Variable types: 36 continuous, 14391 integer (8316 binary)
377 Coefficient statistics:
378 Matrix range [1e-01, 1e+10]
379 Objective range [6e-05, 5e+01]
380 Bounds range [1e+00, 1e+00]
381 RHS range [8e-01, 1e+10]
382 Warning: Model contains large matrix coefficients
383 Warning: Model contains large rhs
384 Consider reformulating model or setting NumericFocus parameter
385 to avoid numerical issues.
386 Presolve removed 531386 rows and 12898 columns
387 Presolve time: 0.38s
388 Presolved: 4800 rows, 1529 columns, 12833 nonzeros
389 Variable types: 8 continuous, 1521 integer (884 binary)
390 Found heuristic solution: objective 3487.2950287
391
392 Root relaxation: objective 5.058224e+03, 1535 iterations, 0.03 seconds (0.02 work units)
393
394 Nodes | Current Node | Objective Bounds | Work
395 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
396
397 0 0 5058.22411 0 10 3487.29503 5058.22411 45.0% - 0s
398 H 0 0 5057.8528892 5058.22411 0.01% - 0s
399
400 Cutting planes:
401 MIR: 1
402
403 Explored 1 nodes (2120 simplex iterations) in 0.58 seconds (0.84 work units)
404 Thread count was 8 (of 8 available processors)
405
406 Solution count 2: 5057.85 3487.3
407
408 Optimal solution found (tolerance 1.00e-08)
409 Best objective 5.057852889165e+03, best bound 5.057852889165e+03, gap 0.0000%
410 SP is solved
411 SP's optimal solution is'□5057
412
413 Itr = 2
414 Collect_LB = [803.0, 5232.050018627811, 6127.152171530973]
415 Collect_UB = [9461.100037255623, 6188.580742959544, 5899.424317736783]

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416 Collect_Hua = [0.0, 4329.050018627811, 5285.580742959544]
417 Collect_SPObjVal = [4329.050018627811, 5285.580742959544, 5057.852889165355]
418 Collect_MPObjValNHua = [803.0, 903.0, 841.5714285714284]
419
420
421 Ops, stop iteration
422 Values adopted from the Itr' th iteration, and Itr = {2}, judgeCount = {2}
423
424 ~~~~~judge = 2, SPObj_SPF = 5057.852889165355
425 Vessel i: 0: pi: 0-6, ai-di: 70-81, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 70-81, taoi-deltai: 70-81, taoPi_SP-deltaPi_SP: 70-75, betaNi:
11, bi: 11
426 Vessel i: 1: pi: 0-6, ai-di: 13-31, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 13-31, taoi-deltai: 13-31, taoPi_SP-deltaPi_SP: 13-31, betaNi:
18, bi: 18
427 Vessel i: 2: pi: 6-13, ai-di: 27-50, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 27-50, taoi-deltai: 27-50, taoPi_SP-deltaPi_SP: 27-50, betaNi:
23, bi: 23
428 Vessel i: 3: pi: 13-20, ai-di: 25-49, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 25-49, taoi-deltai: 25-49, taoPi_SP-deltaPi_SP: 25-49,
betaNi: 24, bi: 24
429 Vessel i: 4: pi: 21-27, ai-di: 31-37, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 31-37, taoi-deltai: 31-37, taoPi_SP-deltaPi_SP: 31-37,
betaNi: 6, bi: 6
430 Vessel i: 5: pi: 20-26, ai-di: 16-38, gi_SP-gpi_SP: 0.000000-0.800000, ai_SP-di: 16-38, taoi-deltai: 18-29, taoPi_SP-deltaPi_SP: 18-29,
betaNi: 11, bi: 11
431 Vessel i: 6: pi: 14-19, ai-di: 6-24, gi_SP-gpi_SP: 1.000000-0.000000, ai_SP-di: 14-24, taoi-deltai: 14-20, taoPi_SP-deltaPi_SP: 14-20, betaNi:
6, bi: 6
432 Vessel i: 7: pi: 27-34, ai-di: 30-49, gi_SP-gpi_SP: 1.000000-0.600000, ai_SP-di: 40-49, taoi-deltai: 39-44, taoPi_SP-deltaPi_SP: 40-44,
betaNi: 5, bi: 5
433 Vessel i: 8: pi: 20-27, ai-di: 40-73, gi_SP-gpi_SP: 0.400000-1.000000, ai_SP-di: 42-73, taoi-deltai: 43-62, taoPi_SP-deltaPi_SP: 43-62,
betaNi: 19, bi: 19
434
435 round LB = [803, 5232, 6127]
436 round UB = [9461, 6189, 5899]
437 round Hua = [0, 4329, 5286]
438 round SPObjVal = [4329, 5286, 5058]
439 round MPObjValNHua = [803, 903, 842]
440
441 OptimalObj = 6127.152171530973
442 Time: 230.000000
443
444
445
446

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