


```

80  MIR: 28
81  StrongCG: 18
82  GUB cover: 10
83  Zero half: 2
84  RLT: 17
85  Relax-and-lift: 54
86  BQP: 3
87
88  Explored 1 nodes (30905 simplex iterations) in 21.37 seconds (36.73 work units)
89  Thread count was 8 (of 8 available processors)
90
91  Solution count 6: 843 883 1323 ... 3883
92
93  Optimal solution found (tolerance 1.00e-10)
94  Best objective 8.430000000000e+02, best bound 8.430000000000e+02, gap 0.0000%
95  Set parameter MIPGap to value 1e-08
96  Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
97
98  CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
99  Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
100
101  Optimize a model with 1983204 rows, 1559473 columns and 13693357 nonzeros
102  Model fingerprint: 0xd0c8d0c8
103  Variable types: 766961 continuous, 792512 integer (787112 binary)
104  Coefficient statistics:
105  Matrix range    [1e-01, 1e+10]
106  Objective range [6e-05, 5e+01]
107  Bounds range    [1e+00, 8e+01]
108  RHS range       [8e-01, 1e+10]
109  Warning: Model contains large matrix coefficients
110  Warning: Model contains large rhs
111      Consider reformulating model or setting NumericFocus parameter
112      to avoid numerical issues.
113  Presolve removed 1978251 rows and 1557811 columns
114  Presolve time: 4.13s
115  Presolved: 4953 rows, 1662 columns, 13084 nonzeros
116  Variable types: 6 continuous, 1656 integer (953 binary)
117  Found heuristic solution: objective 3879.1111111
118  Found heuristic solution: objective 3899.1111111
119
120  Root simplex log...
121
122  Iteration  Objective    Primal Inf.  Dual Inf.  Time
123      0  1.1382000e+04  5.068677e+03  0.000000e+00  5s
124    1590  5.6051111e+03  0.000000e+00  0.000000e+00  5s
125
126  Root relaxation: objective 5.605111e+03, 1590 iterations, 0.02 seconds (0.02 work units)
127
128  Nodes | Current Node | Objective Bounds | Work
129  Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
130
131  H  0  0          5605.111111 15291.7778 173% - 5s
132    0  0  -  0  5605.1111 5605.1111 0.00% - 5s
133
134  Explored 1 nodes (2002 simplex iterations) in 5.43 seconds (5.92 work units)
135  Thread count was 8 (of 8 available processors)
136
137  Solution count 3: 5605.11 3899.11 3879.11
138
139  Optimal solution found (tolerance 1.00e-08)
140  Best objective 5.605111111111e+03, best bound 5.605111111111e+03, gap 0.0000%
141  SP is solved
142  SP's optimal solution is'□5605
143
144  Itr = 0
145  Collect_LB = [843.0]
146  Collect_UB = [12053.222222222226]
147  Collect_Hua = [0.0]
148  Collect_SPObjVal = [5605.111111111113]
149  Collect_MPObjValNHua = [843.0]
150
151
152  Set parameter MIPGap to value 0.05
153  Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
154
155  CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
156  Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
157
158  Optimize a model with 918834 rows, 246921 columns and 2721754 nonzeros
159  Model fingerprint: 0x49ec2d1c
160  Variable types: 1 continuous, 246920 integer (236784 binary)
161  Coefficient statistics:
162  Matrix range    [1e-01, 1e+10]
163  Objective range [1e+00, 2e+01]

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164 Bounds range [1e+00, 1e+00]
165 RHS range [1e+00, 2e+10]
166 Warning: Model contains large matrix coefficients
167 Warning: Model contains large rhs
168 Consider reformulating model or setting NumericFocus parameter
169 to avoid numerical issues.
170 Presolve removed 718229 rows and 223947 columns (presolve time = 5s) ...
171 Presolve removed 726369 rows and 224600 columns (presolve time = 10s) ...
172 Presolve removed 852160 rows and 234271 columns
173 Presolve time: 13.24s
174 Presolved: 66674 rows, 12650 columns, 250807 nonzeros
175 Variable types: 1 continuous, 12649 integer (10481 binary)
176
177 Deterministic concurrent LP optimizer: primal and dual simplex (primal and dual model)
178 Showing first log only...
179
180 Root relaxation presolved: 12650 rows, 79324 columns, 263457 nonzeros
181
182
183 Root simplex log...
184
185 Iteration Objective Primal Inf. Dual Inf. Time
186 0 6.4481111e+03 0.000000e+00 3.761177e+04 14s
187 Concurrent spin time: 0.17s
188
189 Solved with dual simplex (primal model)
190
191 Root relaxation: objective 6.448111e+03, 6967 iterations, 1.15 seconds (1.44 work units)
192 Total elapsed time = 15.80s
193
194 Nodes | Current Node | Objective Bounds | Work
195 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
196
197 0 0 6448.11111 0 276 -6448.11111 - - 16s
198 0 0 6448.11111 0 707 -6448.11111 - - 22s
199 0 0 6448.11111 0 690 -6448.11111 - - 22s
200 0 0 6448.11111 0 620 -6448.11111 - - 23s
201 0 0 6448.11111 0 295 -6448.11111 - - 40s
202 0 0 6448.11111 0 289 -6448.11111 - - 40s
203 0 0 6448.11111 0 255 -6448.11111 - - 43s
204 0 0 6448.11111 0 257 -6448.11111 - - 50s
205 0 0 6448.11111 0 321 -6448.11111 - - 51s
206 0 0 6448.11111 0 330 -6448.11111 - - 61s
207 0 0 6448.11111 0 310 -6448.11111 - - 63s
208 0 2 6448.11111 0 310 -6448.11111 - - 68s
209 1 4 6448.11111 1 402 -6448.11111 -11599 70s
210 7 12 6448.11111 3 873 -6448.11111 - 5074 75s
211 15 20 6448.11111 4 1283 -6448.11111 - 6630 85s
212 19 24 6448.11111 4 597 -6448.11111 - 6687 90s
213 32 37 6448.11111 6 560 -6448.11111 - 5545 97s
214 36 58 6448.11111 7 544 -6448.11111 - 5442 104s
215 62 93 6448.11111 11 773 -6448.11111 - 4650 113s
216 103 138 6468.56851 18 2017 -6448.11111 - 3842 125s
217 198 184 6448.11111 5 1439 -6448.11111 - 2733 132s
218 295 265 6448.11111 11 700 -6448.11111 - 2134 139s
219 401 387 6448.11111 16 900 -6448.11111 - 1700 144s
220 561 556 6448.11111 26 620 -6448.11111 - 1266 150s
221 789 793 6448.11111 36 621 -6448.11111 - 922 155s
222 1086 1032 6448.11111 51 461 -6448.11111 - 699 161s
223 1377 1132 6448.11111 61 489 -6448.11111 - 577 166s
224 1543 1158 6468.11111 70 1201 -6448.11111 - 549 172s
225 1602 1159 6688.11111 29 310 -6448.11111 - 560 198s
226 1604 1160 7588.11111 187 515 -6448.11111 - 559 208s
227 1605 1161 6448.11111 150 659 -6448.11111 - 559 223s
228 1606 1162 7468.11111 358 713 -6448.11111 - 558 229s
229 1607 1162 7528.11111 599 551 -6448.11111 - 558 243s
230 1608 1163 7548.11111 410 758 -6448.11111 - 557 249s
231 1609 1164 7668.11111 215 907 -6448.11111 - 557 267s
232 1610 1164 6448.11111 51 1076 -6448.11111 - 557 289s
233 1611 1165 7508.11111 293 1044 -6448.11111 - 556 323s
234 1612 1166 7548.11111 123 990 -6448.11111 - 556 329s
235 1613 1166 7548.11111 204 961 -6448.11111 - 556 361s
236 1614 1167 7468.11111 601 1353 -6448.11111 - 555 374s
237 1615 1168 7328.11111 33 674 -6448.11111 - 555 407s
238 1616 1168 7428.11111 571 538 -6448.11111 - 555 411s
239 H 1616 1109 6448.1111111 6448.11111 0.00% 555 426s
240
241 Cutting planes:
242 Learned: 2
243 Gomory: 1
244 Cover: 471
245 Implied bound: 820
246 Projected implied bound: 49
247 Clique: 785

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```
248 MIR: 114
249 StrongCG: 80
250 Flow cover: 392
251 GUB cover: 51
252 Zero half: 20
253 RLT: 52
254 Relax-and-lift: 121
255 BQP: 15
256
257 Explored 1616 nodes (1293220 simplex iterations) in 426.55 seconds (991.43 work units)
258 Thread count was 8 (of 8 available processors)
259
260 Solution count 1: 6448.11
261
262 Optimal solution found (tolerance 5.00e-02)
263 Best objective 6.448111111111e+03, best bound 6.448111111111e+03, gap 0.0000%
264 Set parameter MIPGap to value 1e-08
265 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
266
267 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
268 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
269
270 Optimize a model with 1983204 rows, 1559473 columns and 13693357 nonzeros
271 Model fingerprint: 0x628abfbb
272 Variable types: 766961 continuous, 792512 integer (787112 binary)
273 Coefficient statistics:
274   Matrix range    [1e-01, 1e+10]
275   Objective range [6e-05, 5e+01]
276   Bounds range    [1e+00, 8e+01]
277   RHS range       [8e-01, 1e+10]
278 Warning: Model contains large matrix coefficients
279 Warning: Model contains large rhs
280   Consider reformulating model or setting NumericFocus parameter
281   to avoid numerical issues.
282 Presolve removed 1977412 rows and 1557598 columns
283 Presolve time: 4.00s
284 Presolved: 5792 rows, 1875 columns, 15428 nonzeros
285 Variable types: 6 continuous, 1869 integer (1078 binary)
286 Found heuristic solution: objective 4013.111111
287
288 Root simplex log...
289
290 Iteration   Objective    Primal Inf.   Dual Inf.    Time
291      0    1.1588000e+04  7.539023e+03  0.000000e+00  5s
292    1710    5.7831111e+03  0.000000e+00  0.000000e+00  5s
293
294 Root relaxation: objective 5.783111e+03, 1710 iterations, 0.02 seconds (0.02 work units)
295
296   Nodes | Current Node | Objective Bounds | Work
297 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
298
299 * 0 0 0 0 5783.111111 5783.1111 0.00% - 5s
300
301 Explored 1 nodes (2218 simplex iterations) in 5.33 seconds (5.70 work units)
302 Thread count was 8 (of 8 available processors)
303
304 Solution count 2: 5783.11 4013.11
305
306 Optimal solution found (tolerance 1.00e-08)
307 Best objective 5.783111111111e+03, best bound 5.783111111111e+03, gap 0.0000%
308 SP is solved
309 SP's optimal solution is'□5783
310
311 Itr = 1
312 Collect_LB = [843.0, 6448.111111111113]
313 Collect_UB = [12053.222222222226, 6626.111111111113]
314 Collect_Hua = [0.0, 5605.111111111113]
315 Collect_SPObjVal = [5605.111111111113, 5783.111111111113]
316 Collect_MPObjValNHua = [843.0, 843.0]
317
318
319 Set parameter MIPGap to value 0.05
320 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
321
322 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
323 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
324
325 Optimize a model with 1348788 rows, 264417 columns and 4091262 nonzeros
326 Model fingerprint: 0xc30003d2
327 Variable types: 1 continuous, 264416 integer (244176 binary)
328 Coefficient statistics:
329   Matrix range    [1e-01, 1e+10]
330   Objective range [1e+00, 2e+01]
331   Bounds range    [1e+00, 1e+00]
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332 RHS range      [1e+00, 2e+10]
333 Warning: Model contains large matrix coefficients
334 Warning: Model contains large rhs
335     Consider reformulating model or setting NumericFocus parameter
336     to avoid numerical issues.
337 Presolve removed 1099815 rows and 236086 columns (presolve time = 5s) ...
338 Presolve removed 1123080 rows and 237835 columns (presolve time = 10s) ...
339 Presolve removed 1123080 rows and 237835 columns (presolve time = 15s) ...
340 Presolve removed 1238220 rows and 246750 columns
341 Presolve time: 19.43s
342 Presolved: 110568 rows, 17667 columns, 406401 nonzeros
343 Variable types: 1 continuous, 17666 integer (13354 binary)
344
345 Deterministic concurrent LP optimizer: primal and dual simplex (primal and dual model)
346 Showing first log only...
347
348 Root relaxation presolved: 17667 rows, 128235 columns, 424068 nonzeros
349
350
351 Root simplex log...
352
353 Iteration  Objective    Primal Inf.   Dual Inf.   Time
354      0  6.6261111e+03  0.000000e+00  7.289923e+04  21s
355 19633  6.6261111e+03  0.000000e+00  0.000000e+00  23s
356 19633  6.6261111e+03  0.000000e+00  0.000000e+00  23s
357 Concurrent spin time: 0.35s
358
359 Solved with primal simplex
360
361 Root relaxation: objective 6.626111e+03, 19633 iterations, 3.18 seconds (4.37 work units)
362 Total elapsed time = 26.05s
363
364 Nodes | Current Node | Objective Bounds | Work
365 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
366
367 0 0 6626.11111 0 751 -6626.11111 - - 29s
368 0 0 6626.11111 0 988 -6626.11111 - - 36s
369 0 0 6626.11111 0 994 -6626.11111 - - 37s
370 0 0 6626.11111 0 955 -6626.11111 - - 37s
371 0 0 6626.11111 0 900 -6626.11111 - - 39s
372 0 0 6626.11111 0 897 -6626.11111 - - 39s
373 0 0 6626.11111 0 512 -6626.11111 - - 49s
374 0 0 6626.11111 0 517 -6626.11111 - - 51s
375 0 0 6626.11111 0 497 -6626.11111 - - 60s
376 0 0 6626.11111 0 600 -6626.11111 - - 62s
377 0 0 6626.11111 0 720 -6626.11111 - - 72s
378 0 0 6626.11111 0 718 -6626.11111 - - 72s
379 0 0 6626.11111 0 677 -6626.11111 - - 75s
380 0 0 6626.11111 0 680 -6626.11111 - - 75s
381 0 0 6626.11111 0 555 -6626.11111 - - 82s
382 0 0 6626.11111 0 555 -6626.11111 - - 86s
383 0 2 6626.11111 0 555 -6626.11111 - - 101s
384 3 8 6626.11111 2 978 -6626.11111 - 9383 109s
385 7 12 6626.11111 3 1059 -6626.11111 - 7745 113s
386 11 16 6626.11111 4 1105 -6626.11111 - 7385 118s
387 15 20 6626.11111 4 1531 -6626.11111 - 7568 125s
388 19 24 6626.11111 5 1169 -6626.11111 - 6464 133s
389 23 29 6626.11111 5 1394 -6626.11111 - 6065 136s
390 32 48 6626.11111 7 1340 -6626.11111 - 5331 145s
391 49 78 6626.11111 8 1322 -6626.11111 - 4285 162s
392 92 139 6626.11111 11 582 -6626.11111 - 3784 180s
393 196 182 6626.11111 7 1254 -6626.11111 - 2627 193s
394 294 227 6626.11111 9 1193 -6626.11111 - 2000 205s
395 418 270 6626.11111 17 507 -6626.11111 - 1562 215s
396 509 307 6626.11111 36 977 -6626.11111 - 1382 226s
397 548 354 6626.11111 46 946 -6626.11111 - 1454 239s
398 608 443 6626.11111 63 952 -6626.11111 - 1442 257s
399 723 686 6626.11111 104 781 -6626.11111 - 1340 284s
400 1012 1428 6626.11111 181 783 -6626.11111 - 1044 324s
401 1256 1428 7026.11111 184 1492 -6626.11111 - 860 325s
402 1824 1981 6646.11111 423 679 -6626.11111 - 625 348s
403 2477 2434 infeasible 624 -6626.11111 - 504 368s
404 3085 3287 7246.11111 427 732 -6626.11111 - 443 383s
405 4024 3288 6766.11111 420 555 -6626.11111 - 358 439s
406 4026 3289 6906.11111 708 770 -6626.11111 - 358 475s
407 4027 3290 7246.11111 401 888 -6626.11111 - 358 514s
408 4028 3291 6846.11111 31 1293 -6626.11111 - 358 538s
409 4029 3291 7326.11111 134 733 -6626.11111 - 358 563s
410 4030 3292 7086.11111 489 1049 -6626.11111 - 358 587s
411 4031 3293 7146.11111 392 1565 -6626.11111 - 358 634s
412 4032 3293 7126.11111 535 1486 -6626.11111 - 358 646s
413 4033 3294 6846.11111 676 1254 -6626.11111 - 357 695s
414 4034 3295 7246.11111 398 1564 -6626.11111 - 357 754s
415 4035 3295 6626.11111 19 1403 -6626.11111 - 357 838s

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416 H 4035 3130          6926.111111 6626.11111 4.33% 357 860s
417
418 Cutting planes:
419   Learned: 3
420   Gomory: 7
421   Lift-and-project: 2
422   Cover: 555
423   Implied bound: 648
424   Projected implied bound: 43
425   Clique: 1294
426   MIR: 161
427   StrongCG: 62
428   Flow cover: 723
429   GUB cover: 460
430   Zero half: 36
431   RLT: 62
432   Relax-and-lift: 328
433   BQP: 19
434   PSD: 3
435
436 Explored 4035 nodes (1958117 simplex iterations) in 861.03 seconds (2094.78 work units)
437 Thread count was 8 (of 8 available processors)
438
439 Solution count 1: 6926.11
440
441 Optimal solution found (tolerance 5.00e-02)
442 Best objective 6.926111111111e+03, best bound 6.626111111111e+03, gap 4.3314%
443 Warning: linear constraint 488881 and linear constraint 918835 have the same name "ConSP25_1[0,0]"
444 Set parameter MIPGap to value 1e-08
445 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
446
447 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
448 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
449
450 Optimize a model with 1983204 rows, 1559473 columns and 13693357 nonzeros
451 Model fingerprint: 0x6e000478
452 Variable types: 766961 continuous, 792512 integer (787112 binary)
453 Coefficient statistics:
454   Matrix range    [1e-01, 1e+10]
455   Objective range [6e-05, 5e+01]
456   Bounds range    [1e+00, 8e+01]
457   RHS range       [8e-01, 1e+10]
458 Warning: Model contains large matrix coefficients
459 Warning: Model contains large rhs
460   Consider reformulating model or setting NumericFocus parameter
461   to avoid numerical issues.
462 Presolve removed 1977003 rows and 1557513 columns
463 Presolve time: 3.81s
464 Presolved: 6201 rows, 1960 columns, 16532 nonzeros
465 Variable types: 6 continuous, 1954 integer (1122 binary)
466 Found heuristic solution: objective 3988.111111
467
468 Root relaxation: objective 5.783111e+03, 1966 iterations, 0.03 seconds (0.02 work units)
469
470   Nodes | Current Node | Objective Bounds | Work
471   Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
472
473 H   0   0          5783.111111 17677.7778 206%   -   4s
474   0   0   -   0    5783.11111 5783.11111 0.00%   -   4s
475
476 Explored 1 nodes (2788 simplex iterations) in 5.09 seconds (5.56 work units)
477 Thread count was 8 (of 8 available processors)
478
479 Solution count 2: 5783.11 3988.11
480
481 Optimal solution found (tolerance 1.00e-08)
482 Best objective 5.783111111111e+03, best bound 5.783111111111e+03, gap 0.0000%
483 SP is solved
484 SP's optimal solution is'□5783
485
486   Itr = 2
487 Collect_LB = [843.0, 6448.111111111113, 6926.111111111113]
488 Collect_UB = [12053.222222222226, 6626.111111111113, 6626.111111111113]
489 Collect_Hua = [0.0, 5605.111111111113, 5783.111111111113]
490 Collect_SPObjVal = [5605.111111111113, 5783.111111111113, 5783.111111111113]
491 Collect_MPObjValNHua = [843.0, 843.0, 1143.0]
492
493
494 Reach the termination conditions, stop iteration
495 Values adopted from the judgeCount's th iteration, and Itr = {2}, judgeCount = {1}
496
497 ~~~~~judgeCount = 1, SPObj_SPF = 5783.111111111113
498 Vessel i: 0:   pi: 0-7,   ai-di: 3-34,   gi_SP-gpi_SP: 0.000000-0.000000,   ai_SP-di: 3-34,   taoi-deltai: 3-32,   taoPi_SP-deltaPi_SP: 3-32,   betaNi: 29
499   ,   bi: 29

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unknown

499 Vessel i: 1: pi: 13-18, ai-di: 12-22, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 12-22, taoi-deltai: 12-20, taoPi_SP-deltaPi_SP: 12-20,
betaNi: 8, bi: 8
500 Vessel i: 2: pi: 14-19, ai-di: 27-35, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 27-35, taoi-deltai: 27-33, taoPi_SP-deltaPi_SP: 27-33,
betaNi: 6, bi: 6
501 Vessel i: 3: pi: 7-14, ai-di: 24-60, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 24-60, taoi-deltai: 24-58, taoPi_SP-deltaPi_SP: 24-58, betaNi
: 34, bi: 34
502 Vessel i: 4: pi: 14-19, ai-di: 35-41, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 35-41, taoi-deltai: 35-39, taoPi_SP-deltaPi_SP: 35-39,
betaNi: 4, bi: 4
503 Vessel i: 5: pi: 20-26, ai-di: 31-60, gi_SP-gpi_SP: 0.000000-1.000000, ai_SP-di: 31-60, taoi-deltai: 31-46, taoPi_SP-deltaPi_SP: 31-46,
betaNi: 15, bi: 15
504 Vessel i: 6: pi: 15-21, ai-di: 40-80, gi_SP-gpi_SP: 1.000000-0.600000, ai_SP-di: 48-80, taoi-deltai: 48-72, taoPi_SP-deltaPi_SP: 48-72,
betaNi: 24, bi: 24
505 Vessel i: 7: pi: 28-34, ai-di: 43-72, gi_SP-gpi_SP: 0.800000-0.200000, ai_SP-di: 51-72, taoi-deltai: 51-64, taoPi_SP-deltaPi_SP: 51-64,
betaNi: 13, bi: 13
506
507 round LB = [843, 6448, 6926]
508 round UB = [12053, 6626, 6626]
509 round Hua = [0, 5605, 5783]
510 round SPObjVal = [5605, 5783, 5783]
511 round MPObjValNHua = [843, 843, 1143]
512
513 Time: 1696.000000
514
515
516
517