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80 Gomory: 1
81 Cover: 23
82 Implied bound: 442
83 Clique: 2
84 MIR: 13
85 StrongCG: 8
86 Flow cover: 3
87 GUB cover: 5
88 RLT: 19
89 Relax-and-lift: 2
90
91 Explored 1 nodes (25193 simplex iterations) in 28.31 seconds (46.88 work units)
92 Thread count was 8 (of 8 available processors)
93
94 Solution count 9: 712 732 772 ... 7012
95
96 Optimal solution found (tolerance 1.00e-10)
97 Best objective 7.120000000000e+02, best bound 7.120000000000e+02, gap 0.0000%
98 Set parameter MIPGap to value 1e-08
99 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
100
101 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
102 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
103
104 Optimize a model with 2481762 rows, 1955335 columns and 17236452 nonzeros
105 Model fingerprint: 0xe5f662ad
106 Variable types: 963295 continuous, 992040 integer (985965 binary)
107 Coefficient statistics:
108   Matrix range    [1e-01, 1e+10]
109   Objective range [6e-05, 5e+01]
110   Bounds range    [1e+00, 8e+01]
111   RHS range       [8e-01, 1e+10]
112 Warning: Model contains large matrix coefficients
113 Warning: Model contains large rhs
114   Consider reformulating model or setting NumericFocus parameter
115   to avoid numerical issues.
116 Presolve removed 2477808 rows and 1953996 columns (presolve time = 5s) ...
117 Presolve removed 2478884 rows and 1954390 columns
118 Presolve time: 5.36s
119 Presolved: 2878 rows, 945 columns, 7637 nonzeros
120 Variable types: 8 continuous, 937 integer (551 binary)
121 Found heuristic solution: objective 3593.0500186
122 Found heuristic solution: objective 3842.0500186
123
124 Root simplex log...
125
126 Iteration   Objective      Primal Inf.   Dual Inf.    Time
127      0    7.4314519e+03  2.380082e+03  0.000000e+00   7s
128     794   5.0566703e+03  0.000000e+00  0.000000e+00   7s
129
130 Root relaxation: objective 5.056670e+03, 794 iterations, 0.00 seconds (0.01 work units)
131
132   Nodes | Current Node | Objective Bounds | Work
133 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
134
135 H  0  0          5056.6702574 10385.7410 105% - 6s
136   0  0    -  0    5056.67026 5056.67026 0.00% - 6s
137
138 Explored 1 nodes (1210 simplex iterations) in 7.06 seconds (7.16 work units)
139 Thread count was 8 (of 8 available processors)
140
141 Solution count 3: 5056.67 3842.05 3593.05
142
143 Optimal solution found (tolerance 1.00e-08)
144 Best objective 5.056670257367e+03, best bound 5.056670257367e+03, gap 0.0000%
145 SP is solved
146 SP's optimal solution is'□5056
147
148 Itr = 0
149 Collect_LB = [712.0]
150 Collect_UB = [10825.340514734511]
151 Collect_Hua = [0.0]
152 Collect_SPObjVal = [5056.6702573672555]
153 Collect_MPObjValNHua = [712.0]
154
155
156 Set parameter TimeLimit to value 12000
157 Set parameter MIPGap to value 0.0005
158 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
159
160 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
161 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
162
163 Optimize a model with 552258 rows, 283978 columns and 1530712 nonzeros

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164 Model fingerprint: 0xcbac55c2
165 Variable types: 1 continuous, 283977 integer (283941 binary)
166 Coefficient statistics:
167   Matrix range   [1e+00, 1e+10]
168   Objective range [1e+00, 2e+01]
169   Bounds range   [1e+00, 1e+00]
170   RHS range      [1e+00, 2e+10]
171 Warning: Model contains large matrix coefficients
172 Warning: Model contains large rhs
173   Consider reformulating model or setting NumericFocus parameter
174   to avoid numerical issues.
175 Presolve removed 305128 rows and 255611 columns (presolve time = 5s) ...
176 Presolve removed 305128 rows and 255611 columns (presolve time = 10s) ...
177 Presolve removed 305128 rows and 255611 columns (presolve time = 15s) ...
178 Presolve removed 498317 rows and 271277 columns
179 Presolve time: 17.15s
180 Presolved: 53941 rows, 12701 columns, 182064 nonzeros
181 Variable types: 0 continuous, 12701 integer (12674 binary)
182
183 Deterministic concurrent LP optimizer: primal and dual simplex (primal and dual model)
184 Showing first log only...
185
186 Root relaxation presolved: 53921 rows, 12721 columns, 182004 nonzeros
187
188
189 Root simplex log...
190
191 Iteration   Objective   Primal Inf.   Dual Inf.   Time
192      0   5.7686703e+03   3.265000e+02   4.047642e+08   18s
193 Concurrent spin time: 0.14s
194
195 Solved with dual simplex (primal model)
196
197 Root relaxation: objective 5.768670e+03, 6266 iterations, 0.92 seconds (1.44 work units)
198
199   Nodes | Current Node | Objective Bounds | Work
200 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
201
202   0   0 5768.67026   0 29   - 5768.67026   -   - 19s
203   0   0 5768.67026   0 72   - 5768.67026   -   - 21s
204 H  0   0           7608.6702574 5768.67026 24.2%   - 21s
205 H  0   0           7568.6702574 5768.67026 23.8%   - 21s
206   0   0 5768.67026   0 188 7568.67026 5768.67026 23.8%   - 22s
207   0   0 5768.67026   0 179 7568.67026 5768.67026 23.8%   - 22s
208   0   0 5768.67026   0  83 7568.67026 5768.67026 23.8%   - 29s
209   0   0 5768.67026   0 318 7568.67026 5768.67026 23.8%   - 31s
210   0   0 5768.67026   0  81 7568.67026 5768.67026 23.8%   - 34s
211 H  0   0           7388.6702574 5768.67026 21.9%   - 34s
212   0   0 5768.67026   0 242 7388.67026 5768.67026 21.9%   - 35s
213   0   0 5768.67026   0 162 7388.67026 5768.67026 21.9%   - 36s
214 H  0   0           6808.6702574 5768.67026 15.3%   - 39s
215   0   0 5768.67026   0  96 6808.67026 5768.67026 15.3%   - 40s
216   0   0 5768.67026   0  93 6808.67026 5768.67026 15.3%   - 40s
217   0   0 5768.67026   0 232 6808.67026 5768.67026 15.3%   - 41s
218   0   0 5768.67026   0 226 6808.67026 5768.67026 15.3%   - 41s
219   0   0 5768.67026   0 386 6808.67026 5768.67026 15.3%   - 43s
220   0   0 5768.67026   0 364 6808.67026 5768.67026 15.3%   - 43s
221   0   0 5768.67026   0 185 6808.67026 5768.67026 15.3%   - 46s
222   0   0 5768.67026   0 151 6808.67026 5768.67026 15.3%   - 47s
223 H  0   0           5768.6702574 5768.67026 0.00%   - 50s
224   0   0 5768.67026   0 151 5768.67026 5768.67026 0.00%   - 50s
225
226 Cutting planes:
227   Learned: 1
228   Gomory: 2
229   Cover: 62
230   Implied bound: 37
231   Clique: 735
232   MIR: 46
233   StrongCG: 34
234   GUB cover: 15
235   Zero half: 3
236   RLT: 7
237   Relax-and-lift: 28
238   BQP: 24
239
240 Explored 1 nodes (125472 simplex iterations) in 50.96 seconds (71.19 work units)
241 Thread count was 8 (of 8 available processors)
242
243 Solution count 5: 5768.67 6808.67 7388.67 ... 7608.67
244
245 Optimal solution found (tolerance 5.00e-04)
246 Best objective 5.768670257367e+03, best bound 5.768670257367e+03, gap 0.0000%
247 Set parameter MIPGap to value 1e-08

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248 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
249
250 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
251 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
252
253 Optimize a model with 2481762 rows, 1955335 columns and 17236452 nonzeros
254 Model fingerprint: 0x73e2def3
255 Variable types: 963295 continuous, 992040 integer (985965 binary)
256 Coefficient statistics:
257   Matrix range    [1e-01, 1e+10]
258   Objective range [6e-05, 5e+01]
259   Bounds range    [1e+00, 8e+01]
260   RHS range       [8e-01, 1e+10]
261 Warning: Model contains large matrix coefficients
262 Warning: Model contains large rhs
263   Consider reformulating model or setting NumericFocus parameter
264   to avoid numerical issues.
265 Presolve removed 2477083 rows and 1953782 columns (presolve time = 5s) ...
266 Presolve removed 2477083 rows and 1953782 columns
267 Presolve time: 5.21s
268 Presolved: 4679 rows, 1553 columns, 12419 nonzeros
269 Variable types: 8 continuous, 1545 integer (897 binary)
270 Found heuristic solution: objective 3675.0646186
271
272 Root simplex log...
273
274 Iteration  Objective    Primal Inf.   Dual Inf.   Time
275      0   8.9524519e+03   3.695526e+03   0.000000e+00   7s
276   1583   5.3206703e+03   0.000000e+00   0.000000e+00   7s
277
278 Root relaxation: objective 5.320670e+03, 1583 iterations, 0.01 seconds (0.02 work units)
279
280   Nodes | Current Node | Objective Bounds | Work
281 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
282
283 H  0  0           5320.6702574 13891.7410 161% - 6s
284  0  0  -  0   5320.67026 5320.67026 0.00% - 6s
285
286 Explored 1 nodes (2262 simplex iterations) in 6.87 seconds (7.06 work units)
287 Thread count was 8 (of 8 available processors)
288
289 Solution count 2: 5320.67 3675.06
290
291 Optimal solution found (tolerance 1.00e-08)
292 Best objective 5.320670257367e+03, best bound 5.320670257367e+03, gap 0.0000%
293 SP is solved
294 SP's optimal solution is'□5320
295
296 Itr = 1
297 Collect_LB = [712.0, 5768.6702573672555]
298 Collect_UB = [10825.340514734511, 6032.6702573672555]
299 Collect_Hua = [0.0, 5056.6702573672555]
300 Collect_SPObjVal = [5056.6702573672555, 5320.6702573672555]
301 Collect_MPObjValNHua = [712.0, 712.0]
302
303
304 Set parameter TimeLimit to value 12000
305 Set parameter MIPGap to value 0.0005
306 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
307
308 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
309 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
310
311 Optimize a model with 552259 rows, 283978 columns and 1530731 nonzeros
312 Model fingerprint: 0x2d4ad06b
313 Variable types: 1 continuous, 283977 integer (283941 binary)
314 Coefficient statistics:
315   Matrix range    [1e+00, 1e+10]
316   Objective range [1e+00, 2e+01]
317   Bounds range    [1e+00, 1e+00]
318   RHS range       [1e+00, 2e+10]
319 Warning: Model contains large matrix coefficients
320 Warning: Model contains large rhs
321   Consider reformulating model or setting NumericFocus parameter
322   to avoid numerical issues.
323 Presolve removed 305578 rows and 255677 columns (presolve time = 5s) ...
324 Presolve removed 305578 rows and 255677 columns (presolve time = 10s) ...
325 Presolve removed 305578 rows and 255677 columns (presolve time = 15s) ...
326 Presolve removed 447505 rows and 271325 columns (presolve time = 20s) ...
327 Presolve removed 498941 rows and 271325 columns
328 Presolve time: 20.69s
329 Presolved: 53318 rows, 12653 columns, 181007 nonzeros
330 Variable types: 0 continuous, 12653 integer (12626 binary)
331

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332 Deterministic concurrent LP optimizer: primal and dual simplex (primal and dual model)
333 Showing first log only...
334
335 Root relaxation presolved: 53299 rows, 12672 columns, 180950 nonzeros
336
337
338 Root simplex log...
339
340 Iteration   Objective   Primal Inf.   Dual Inf.   Time
341      0   6.0326703e+03   3.243750e+02   4.038423e+08   22s
342 Concurrent spin time: 0.16s
343
344 Solved with dual simplex (primal model)
345
346 Root relaxation: objective 6.032670e+03, 5942 iterations, 1.32 seconds (1.48 work units)
347
348   Nodes | Current Node | Objective Bounds | Work
349 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
350
351   0   0 6032.67026   0 39   -6032.67026   -   - 23s
352   0   0 6032.67026   0 71   -6032.67026   -   - 27s
353   0   0 6032.67026   0 64   -6032.67026   -   - 27s
354   0   0 6032.67026   0 273   -6032.67026   -   - 29s
355   0   0 6032.67026   0 262   -6032.67026   -   - 29s
356   0   0 6032.67026   0 119   -6032.67026   -   - 37s
357   0   0 6032.67026   0 210   -6032.67026   -   - 37s
358   0   0 6032.67026   0 224   -6032.67026   -   - 52s
359   0   0 6032.67026   0 213   -6032.67026   -   - 53s
360   0   0 6032.67026   0 77   -6032.67026   -   - 61s
361 H   0   0           9972.6702574 6032.67026 39.5%   - 61s
362   0   0 6032.67026   0 77 9972.67026 6032.67026 39.5%   - 62s
363 H   0   0           7752.6702574 6032.67026 22.2%   - 64s
364 H   0   0           6032.6702574 6032.67026 0.00%   - 67s
365   0   0 6032.67026   0 77 6032.67026 6032.67026 0.00%   - 68s
366
367 Cutting planes:
368   Learned: 4
369   Cover: 15
370   Implied bound: 406
371   Clique: 275
372   MIR: 91
373   StrongCG: 40
374   GUB cover: 4
375   RLT: 14
376   Relax-and-lift: 58
377   BQP: 38
378
379 Explored 1 nodes (98657 simplex iterations) in 68.04 seconds (71.47 work units)
380 Thread count was 8 (of 8 available processors)
381
382 Solution count 3: 6032.67 7752.67 9972.67
383
384 Optimal solution found (tolerance 5.00e-04)
385 Best objective 6.032670257367e+03, best bound 6.032670257367e+03, gap 0.0000%
386 Set parameter MIPGap to value 1e-08
387 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
388
389 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
390 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
391
392 Optimize a model with 2481762 rows, 1955335 columns and 17236452 nonzeros
393 Model fingerprint: 0xc551aa33
394 Variable types: 963295 continuous, 992040 integer (985965 binary)
395 Coefficient statistics:
396   Matrix range    [1e-01, 1e+10]
397   Objective range [6e-05, 5e+01]
398   Bounds range    [1e+00, 8e+01]
399   RHS range       [8e-01, 1e+10]
400 Warning: Model contains large matrix coefficients
401 Warning: Model contains large rhs
402   Consider reformulating model or setting NumericFocus parameter
403   to avoid numerical issues.
404 Presolve removed 2477053 rows and 1953772 columns (presolve time = 5s) ...
405 Presolve removed 2477059 rows and 1953772 columns
406 Presolve time: 5.47s
407 Presolved: 4703 rows, 1563 columns, 12438 nonzeros
408 Variable types: 8 continuous, 1555 integer (901 binary)
409 Found heuristic solution: objective 3687.8601380
410
411 Root simplex log...
412
413 Iteration   Objective   Primal Inf.   Dual Inf.   Time
414      0   8.9924519e+03   3.690101e+03   0.000000e+00   7s
415   1269   5.3328601e+03   0.000000e+00   0.000000e+00   7s

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416
417 Root relaxation: objective 5.332860e+03, 1269 iterations, 0.01 seconds (0.01 work units)
418
419   Nodes | Current Node | Objective Bounds | Work
420 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
421
422    0    0 5332.86014    0  5 3687.86014 5332.86014 44.6%   -   6s
423 H    0    0          5312.8601380 5332.86014 0.38%   -   6s
424 H    0    0          5332.8601380 5332.86014 0.00%   -   7s
425    0    0 5332.86014    0  5 5332.86014 5332.86014 0.00%   -   7s
426
427 Explored 1 nodes (1866 simplex iterations) in 7.28 seconds (7.07 work units)
428 Thread count was 8 (of 8 available processors)
429
430 Solution count 3: 5332.86 5312.86 3687.86
431
432 Optimal solution found (tolerance 1.00e-08)
433 Best objective 5.332860137998e+03, best bound 5.332860137998e+03, gap 0.0000%
434 SP is solved
435 SP's optimal solution is'□5332
436
437 Itr = 2
438 Collect_LB = [712.0, 5768.6702573672555, 6032.6702573672555]
439 Collect_UB = [10825.340514734511, 6032.6702573672555, 6032.6702573672555]
440 Collect_Hua = [0.0, 5056.6702573672555, 5320.6702573672555]
441 Collect_SPObjVal = [5056.6702573672555, 5320.6702573672555, 5332.8601379975335]
442 Collect_MPObjValNHua = [712.0, 712.0, 712.0]
443
444
445 Reach the termination conditions, stop iteration
446 Values adopted from the Itr' th iteration, and Itr = {2}, judgeCount = {2}
447
448 ~~~~~judge = 2, SPObj_SPF = 5332.8601379975335
449 Vessel i: 0: pi: 0-5, ai-di: 38-81, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 38-81, taoi-deltai: 38-50, taoPi_SP-deltaPi_SP: 38-50, betaNi:
12, bi: 12
450 Vessel i: 1: pi: 0-5, ai-di: 8-18, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 8-18, taoi-deltai: 8-13, taoPi_SP-deltaPi_SP: 11-13, betaNi: 5
, bi: 5
451 Vessel i: 2: pi: 5-11, ai-di: 32-67, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 32-67, taoi-deltai: 32-53, taoPi_SP-deltaPi_SP: 32-53, betaNi:
21, bi: 21
452 Vessel i: 3: pi: 5-10, ai-di: 12-38, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 12-38, taoi-deltai: 12-25, taoPi_SP-deltaPi_SP: 12-25, betaNi:
13, bi: 13
453 Vessel i: 4: pi: 13-18, ai-di: 43-81, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 43-81, taoi-deltai: 43-54, taoPi_SP-deltaPi_SP: 43-54,
betaNi: 11, bi: 11
454 Vessel i: 5: pi: 20-25, ai-di: 11-45, gi_SP-gpi_SP: 0.000000-0.600000, ai_SP-di: 11-45, taoi-deltai: 11-26, taoPi_SP-deltaPi_SP: 11-26,
betaNi: 15, bi: 15
455 Vessel i: 6: pi: 11-18, ai-di: 3-60, gi_SP-gpi_SP: 1.000000-0.000000, ai_SP-di: 11-60, taoi-deltai: 11-39, taoPi_SP-deltaPi_SP: 11-39, betaNi:
28, bi: 28
456 Vessel i: 7: pi: 18-23, ai-di: 31-79, gi_SP-gpi_SP: 0.600000-1.000000, ai_SP-di: 37-79, taoi-deltai: 35-39, taoPi_SP-deltaPi_SP: 37-39,
betaNi: 4, bi: 4
457 Vessel i: 8: pi: 28-34, ai-di: 19-68, gi_SP-gpi_SP: 0.800000-0.800000, ai_SP-di: 24-68, taoi-deltai: 26-41, taoPi_SP-deltaPi_SP: 26-41,
betaNi: 15, bi: 15
458
459 round LB = [712, 5769, 6033]
460 round UB = [10825, 6033, 6033]
461 round Hua = [0, 5057, 5321]
462 round SPObjVal = [5057, 5321, 5333]
463 round MPObjValNHua = [712, 712, 712]
464
465 OptimalObj = 6032.6702573672555
466 Time: 635.000000
467
468
469
470

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