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80 Optimize a model with 252634 rows, 9618 columns and 522244 nonzeros
81 Model fingerprint: 0x879bae13
82 Variable types: 24 continuous, 9594 integer (5544 binary)
83 Coefficient statistics:
84   Matrix range    [1e-01, 1e+10]
85   Objective range [6e-05, 5e+01]
86   Bounds range    [1e+00, 1e+00]
87   RHS range       [8e-01, 1e+10]
88 Warning: Model contains large matrix coefficients
89 Warning: Model contains large rhs
90   Consider reformulating model or setting NumericFocus parameter
91   to avoid numerical issues.
92 Presolve removed 250362 rows and 8728 columns
93 Presolve time: 0.23s
94 Presolved: 2272 rows, 890 columns, 6112 nonzeros
95 Variable types: 4 continuous, 886 integer (498 binary)
96 Found heuristic solution: objective 3850.3983806
97
98 Root relaxation: objective 5.221000e+03, 582 iterations, 0.00 seconds (0.00 work units)
99
100  Nodes | Current Node | Objective Bounds | Work
101  Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
102
103    0  0 5221.00000  0  8 3850.39838 5221.00000 35.6%  - 0s
104 H  0  0          5221.0000000 5221.00000 0.00%  - 0s
105    0  0 5221.00000  0  8 5221.00000 5221.00000 0.00%  - 0s
106
107 Explored 1 nodes (582 simplex iterations) in 0.31 seconds (0.46 work units)
108 Thread count was 8 (of 8 available processors)
109
110 Solution count 2: 5221 3850.4
111
112 Optimal solution found (tolerance 1.00e-08)
113 Best objective 5.221000000000e+03, best bound 5.221000000000e+03, gap 0.0000%
114 SP is solved
115 SP's optimal solution is'□5221
116
117 Itr = 0
118 Collect_LB = [788.0]
119 Collect_UB = [11230.0000000000004]
120 Collect_Hua = [0.0]
121 Collect_SPObjVal = [5221.0000000000002]
122 Collect_MPObjValNHua = [788.0]
123
124
125 Set parameter MIPGap to value 1e-10
126 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
127
128 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
129 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
130
131 Optimize a model with 382373 rows, 137605 columns and 1045776 nonzeros
132 Model fingerprint: 0xe7894bd1
133 Variable types: 1 continuous, 137604 integer (137580 binary)
134 Coefficient statistics:
135   Matrix range    [1e+00, 1e+10]
136   Objective range [1e+00, 2e+01]
137   Bounds range    [1e+00, 1e+00]
138   RHS range       [1e+00, 2e+10]
139 Warning: Model contains large matrix coefficients
140 Warning: Model contains large rhs
141   Consider reformulating model or setting NumericFocus parameter
142   to avoid numerical issues.
143 Presolve removed 247724 rows and 121850 columns (presolve time = 5s) ...
144 Presolve removed 364020 rows and 131279 columns
145 Presolve time: 5.87s
146 Presolved: 18353 rows, 6326 columns, 77807 nonzeros
147 Variable types: 0 continuous, 6326 integer (6312 binary)
148
149 Root simplex log...
150
151 Iteration Objective Primal Inf. Dual Inf. Time
152    0  6.0610000e+03 7.871250e+02 0.000000e+00 6s
153  2660 6.0610000e+03 0.000000e+00 0.000000e+00 6s
154
155 Root relaxation: objective 6.061000e+03, 2660 iterations, 0.06 seconds (0.07 work units)
156
157  Nodes | Current Node | Objective Bounds | Work
158  Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
159
160    0  0 6061.00000  0 19  -6061.00000  -  - 6s
161    0  0 6061.00000  0 268  -6061.00000  -  - 7s
162    0  0 6061.00000  0 269  -6061.00000  -  - 7s
163    0  0 6061.00000  0 245  -6061.00000  -  - 7s

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164 0 0 6061.00000 0 243 - 6061.00000 - - 7s
165 0 0 6061.00000 0 54 - 6061.00000 - - 8s
166 0 0 6061.00000 0 52 - 6061.00000 - - 8s
167 H 0 0 6061.0000000 6061.00000 0.00% - 9s
168 0 0 6061.00000 0 134 6061.00000 6061.00000 0.00% - 9s
169
170 Cutting planes:
171 Learned: 2
172 Gomory: 1
173 Cover: 267
174 Implied bound: 14
175 Clique: 58
176 MIR: 28
177 StrongCG: 7
178 GUB cover: 38
179 RLT: 1
180 Relax-and-lift: 5
181 BQP: 3
182
183 Explored 1 nodes (16800 simplex iterations) in 9.15 seconds (12.74 work units)
184 Thread count was 8 (of 8 available processors)
185
186 Solution count 1: 6061
187
188 Optimal solution found (tolerance 1.00e-10)
189 Best objective 6.061000000000e+03, best bound 6.061000000000e+03, gap 0.0000%
190 Set parameter MIPGap to value 1e-08
191 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
192
193 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
194 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
195
196 Optimize a model with 252634 rows, 9618 columns and 522244 nonzeros
197 Model fingerprint: 0xca8aaa3d
198 Variable types: 24 continuous, 9594 integer (5544 binary)
199 Coefficient statistics:
200 Matrix range [1e-01, 1e+10]
201 Objective range [6e-05, 5e+01]
202 Bounds range [1e+00, 1e+00]
203 RHS range [8e-01, 1e+10]
204 Warning: Model contains large matrix coefficients
205 Warning: Model contains large rhs
206 Consider reformulating model or setting NumericFocus parameter
207 to avoid numerical issues.
208 Presolve removed 247378 rows and 7875 columns
209 Presolve time: 0.22s
210 Presolved: 5256 rows, 1743 columns, 14014 nonzeros
211 Variable types: 4 continuous, 1739 integer (994 binary)
212 Found heuristic solution: objective 3874.6085125
213 Found heuristic solution: objective 3894.6085125
214
215 Root relaxation: objective 5.472000e+03, 1514 iterations, 0.03 seconds (0.02 work units)
216
217 Nodes | Current Node | Objective Bounds | Work
218 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
219
220 0 0 5472.00000 0 14 3894.60851 5472.00000 40.5% - 0s
221 H 0 0 4539.9153674 5472.00000 20.5% - 0s
222 H 0 0 4567.0000000 5472.00000 19.8% - 0s
223 0 0 5472.00000 0 4 4567.00000 5472.00000 19.8% - 0s
224 H 0 0 5472.0000000 5472.00000 0.00% - 0s
225 0 0 5472.00000 0 4 5472.00000 5472.00000 0.00% - 0s
226
227 Cutting planes:
228 Gomory: 3
229 Cover: 1
230 Clique: 3
231 Zero half: 1
232
233 Explored 1 nodes (2419 simplex iterations) in 0.38 seconds (0.57 work units)
234 Thread count was 8 (of 8 available processors)
235
236 Solution count 5: 5472 4567 4539.92 ... 3874.61
237
238 Optimal solution found (tolerance 1.00e-08)
239 Best objective 5.472000000000e+03, best bound 5.472000000000e+03, gap 0.0000%
240 SP is solved
241 SP's optimal solution is'□5472
242
243 Itr = 1
244 Collect_LB = [788.0, 6061.0000000000002]
245 Collect_UB = [11230.0000000000004, 6312.0000000000002]
246 Collect_Hua = [0.0, 5221.0000000000002]
247 Collect_SPObjVal = [5221.0000000000002, 5472.0000000000002]

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248 Collect_MPObjValNHua = [788.0, 840.0]
249
250
251 Set parameter MIPGap to value 1e-10
252 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
253
254 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
255 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
256
257 Optimize a model with 382373 rows, 137605 columns and 1045776 nonzeros
258 Model fingerprint: 0x5b09e65d
259 Variable types: 1 continuous, 137604 integer (137580 binary)
260 Coefficient statistics:
261   Matrix range    [1e+00, 1e+10]
262   Objective range [1e+00, 2e+01]
263   Bounds range   [1e+00, 1e+00]
264   RHS range      [1e+00, 2e+10]
265 Warning: Model contains large matrix coefficients
266 Warning: Model contains large rhs
267   Consider reformulating model or setting NumericFocus parameter
268   to avoid numerical issues.
269 Presolve removed 247724 rows and 121850 columns (presolve time = 5s) ...
270 Presolve removed 364020 rows and 131279 columns
271 Presolve time: 5.81s
272 Presolved: 18353 rows, 6326 columns, 77807 nonzeros
273 Variable types: 0 continuous, 6326 integer (6312 binary)
274
275 Root simplex log...
276
277 Iteration   Objective    Primal Inf.   Dual Inf.    Time
278      0   6.3120000e+03  7.871250e+02  0.000000e+00   6s
279   2660   6.3120000e+03  0.000000e+00  0.000000e+00   6s
280
281 Root relaxation: objective 6.312000e+03, 2660 iterations, 0.05 seconds (0.07 work units)
282
283   Nodes | Current Node | Objective Bounds | Work
284 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
285
286    0    0 6312.00000  0 19    - 6312.00000    -    -   6s
287    0    0 6312.00000  0 268    - 6312.00000    -    -   7s
288    0    0 6312.00000  0 269    - 6312.00000    -    -   7s
289    0    0 6312.00000  0 245    - 6312.00000    -    -   7s
290    0    0 6312.00000  0 243    - 6312.00000    -    -   7s
291    0    0 6312.00000  0 54    - 6312.00000    -    -   8s
292    0    0 6312.00000  0 52    - 6312.00000    -    -   8s
293 H  0    0          6312.0000000 6312.00000 0.00%    -   9s
294    0    0 6312.00000  0 134 6312.00000 6312.00000 0.00%    -   9s
295
296 Cutting planes:
297   Learned: 2
298   Gomory: 1
299   Cover: 267
300   Implied bound: 14
301   Clique: 58
302   MIR: 28
303   StrongCG: 7
304   GUB cover: 38
305   RLT: 1
306   Relax-and-lift: 5
307   BQP: 3
308
309 Explored 1 nodes (16800 simplex iterations) in 9.16 seconds (12.74 work units)
310 Thread count was 8 (of 8 available processors)
311
312 Solution count 1: 6312
313
314 Optimal solution found (tolerance 1.00e-10)
315 Best objective 6.312000000000e+03, best bound 6.312000000000e+03, gap 0.0000%
316 Set parameter MIPGap to value 1e-08
317 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
318
319 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
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325 Coefficient statistics:
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327   Objective range [6e-05, 5e+01]
328   Bounds range   [1e+00, 1e+00]
329   RHS range      [8e-01, 1e+10]
330 Warning: Model contains large matrix coefficients
331 Warning: Model contains large rhs

```

```
332     Consider reformulating model or setting NumericFocus parameter
333     to avoid numerical issues.
334 Presolve removed 247378 rows and 7875 columns
335 Presolve time: 0.22s
336 Presolved: 5256 rows, 1743 columns, 14014 nonzeros
337 Variable types: 4 continuous, 1739 integer (994 binary)
338 Found heuristic solution: objective 3874.6085125
339 Found heuristic solution: objective 3894.6085125
340
341 Root relaxation: objective 5.472000e+03, 1514 iterations, 0.02 seconds (0.02 work units)
342
343 Nodes | Current Node | Objective Bounds | Work
344 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
345
346 0 0 5472.00000 0 14 3894.60851 5472.00000 40.5% - 0s
347 H 0 0 4539.9153674 5472.00000 20.5% - 0s
348 H 0 0 4567.0000000 5472.00000 19.8% - 0s
349 0 0 5472.00000 0 4 4567.00000 5472.00000 19.8% - 0s
350 H 0 0 5472.0000000 5472.00000 0.00% - 0s
351 0 0 5472.00000 0 4 5472.00000 5472.00000 0.00% - 0s
352
353 Cutting planes:
354 Gomory: 3
355 Cover: 1
356 Clique: 3
357 Zero half: 1
358
359 Explored 1 nodes (2419 simplex iterations) in 0.38 seconds (0.57 work units)
360 Thread count was 8 (of 8 available processors)
361
362 Solution count 5: 5472 4567 4539.92 ... 3874.61
363
364 Optimal solution found (tolerance 1.00e-08)
365 Best objective 5.472000000000e+03, best bound 5.472000000000e+03, gap 0.0000%
366 SP is solved
367 SP's optimal solution is'□5472
368
369 Itr = 2
370 Collect_LB = [788.0, 6061.0000000000002, 6312.0000000000002]
371 Collect_UB = [11230.0000000000004, 6312.0000000000002, 6312.0000000000002]
372 Collect_Hua = [0.0, 5221.0000000000002, 5472.0000000000002]
373 Collect_SPObjVal = [5221.0000000000002, 5472.0000000000002, 5472.0000000000002]
374 Collect_MPObjValNHua = [788.0, 840.0, 840.0]
375
376
377 Reach the termination conditions, stop iteration
378 Values adopted from the Itr' th iteration, and Itr = {2}, judgeCount = {2}
379
380 ~~~~~judge = 2, SPObj_SPF = 5472.0000000000002
381 Vessel i: 0: pi: 0-7, ai-di: 8-25, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 8-25, taoi-deltai: 8-25, taoPi_SP-deltaPi_SP: 8-25, betaNi: 17
, bi: 17
382 Vessel i: 1: pi: 22-28, ai-di: 14-24, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 14-24, taoi-deltai: 14-25, taoPi_SP-deltaPi_SP: 14-25,
betaNi: 11, bi: 11
383 Vessel i: 2: pi: 16-22, ai-di: 14-49, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 14-49, taoi-deltai: 14-47, taoPi_SP-deltaPi_SP: 14-47,
betaNi: 33, bi: 33
384 Vessel i: 3: pi: 11-16, ai-di: 22-48, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 22-48, taoi-deltai: 22-49, taoPi_SP-deltaPi_SP: 22-49,
betaNi: 27, bi: 27
385 Vessel i: 4: pi: 16-22, ai-di: 43-56, gi_SP-gpi_SP: 1.000000-0.600000, ai_SP-di: 48-56, taoi-deltai: 48-58, taoPi_SP-deltaPi_SP: 48-58,
betaNi: 10, bi: 10
386 Vessel i: 5: pi: 22-27, ai-di: 35-75, gi_SP-gpi_SP: 0.200000-0.600000, ai_SP-di: 35-75, taoi-deltai: 36-70, taoPi_SP-deltaPi_SP: 36-70,
betaNi: 34, bi: 34
387
388 round LB = [788, 6061, 6312]
389 round UB = [11230, 6312, 6312]
390 round Hua = [0, 5221, 5472]
391 round SPObjVal = [5221, 5472, 5472]
392 round MPObjValNHua = [788, 840, 840]
393
394 OptimalObj = 6312.0000000000002
395 Time: 70.000000
396
397
398
399
```