


```

80 Objective range [6e-05, 5e+01]
81 Bounds range [1e+00, 8e+01]
82 RHS range [8e-01, 1e+10]
83 Warning: Model contains large matrix coefficients
84 Warning: Model contains large rhs
85 Consider reformulating model or setting NumericFocus parameter
86 to avoid numerical issues.
87 Presolve removed 1151447 rows and 900977 columns
88 Presolve time: 2.79s
89 Presolved: 2395 rows, 836 columns, 6371 nonzeros
90 Variable types: 3 continuous, 833 integer (499 binary)
91 Found heuristic solution: objective 3476.666667
92
93 Root relaxation: objective 4.538684e+03, 706 iterations, 0.00 seconds (0.01 work units)
94
95 Nodes | Current Node | Objective Bounds | Work
96 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
97
98 0 0 4538.68421 0 65 3476.66667 4538.68421 30.5% - 3s
99 H 0 0 4450.6666667 4538.68421 1.98% - 3s
100 H 0 0 4470.6666667 4538.68421 1.52% - 3s
101 H 0 0 4498.6666667 4528.00000 0.65% - 3s
102 0 0 4528.00000 0 4 4498.66667 4528.00000 0.65% - 3s
103 H 0 0 4528.0000000 4528.00000 0.00% - 3s
104 0 0 4528.00000 0 4 4528.00000 4528.00000 0.00% - 3s
105
106 Cutting planes:
107 Learned: 4
108 Gomory: 8
109 Cover: 15
110 Implied bound: 14
111 Clique: 2
112 MIR: 5
113 StrongCG: 3
114 Flow cover: 4
115 Zero half: 1
116 RLT: 5
117 Relax-and-lift: 2
118 PSD: 11
119
120 Explored 1 nodes (1155 simplex iterations) in 3.76 seconds (3.38 work units)
121 Thread count was 8 (of 8 available processors)
122
123 Solution count 5: 4528 4498.67 4470.67 ... 3476.67
124
125 Optimal solution found (tolerance 1.00e-08)
126 Best objective 4.528000000000e+03, best bound 4.528000000000e+03, gap 0.0000%
127 SP is solved
128 SP's optimal solution is'□4528
129
130 Itr = 0
131 Collect_LB = [692.0]
132 Collect_UB = [9748.000000000000]
133 Collect_Hua = [0.0]
134 Collect_SPObjVal = [4528.000000000000]
135 Collect_MPObjValNHua = [692.0]
136
137
138 Set parameter MIPGap to value 0.05
139 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
140
141 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
142 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
143
144 Optimize a model with 660171 rows, 150727 columns and 1927792 nonzeros
145 Model fingerprint: 0x9188e543
146 Variable types: 1 continuous, 150726 integer (143124 binary)
147 Coefficient statistics:
148 Matrix range [1e-01, 1e+10]
149 Objective range [1e+00, 2e+01]
150 Bounds range [1e+00, 1e+00]
151 RHS range [1e+00, 2e+10]
152 Warning: Model contains large matrix coefficients
153 Warning: Model contains large rhs
154 Consider reformulating model or setting NumericFocus parameter
155 to avoid numerical issues.
156 Presolve removed 487127 rows and 130334 columns (presolve time = 5s) ...
157 Presolve removed 495456 rows and 131126 columns (presolve time = 10s) ...
158 Presolve removed 582170 rows and 139584 columns
159 Presolve time: 13.91s
160 Presolved: 78001 rows, 11143 columns, 239254 nonzeros
161 Variable types: 0 continuous, 11143 integer (9212 binary)
162
163 Deterministic concurrent LP optimizer: primal and dual simplex (primal and dual model)

```

```

164 Showing first log only...
165
166 Root relaxation presolved: 11143 rows, 89144 columns, 250397 nonzeros
167
168
169 Root simplex log...
170
171 Iteration   Objective   Primal Inf.   Dual Inf.   Time
172      0  5.2200000e+03  0.000000e+00  2.645188e+04  15s
173    4311  5.2232508e+03  0.000000e+00  5.894858e+04  15s
174 Concurrent spin time: 0.47s
175
176 Solved with dual simplex (primal model)
177
178 Root relaxation: objective 5.220000e+03, 5824 iterations, 1.73 seconds (1.60 work units)
179
180 Nodes | Current Node | Objective Bounds | Work
181 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
182
183 0 0 5220.00000 0 206 - 5220.00000 - - 19s
184 0 0 5220.00000 0 436 - 5220.00000 - - 22s
185 0 0 5220.00000 0 429 - 5220.00000 - - 22s
186 0 0 5220.00000 0 448 - 5220.00000 - - 23s
187 0 0 5220.00000 0 304 - 5220.00000 - - 30s
188 0 0 5220.00000 0 321 - 5220.00000 - - 31s
189 0 0 5220.00000 0 298 - 5220.00000 - - 31s
190 0 0 5220.00000 0 298 - 5220.00000 - - 31s
191 0 0 5220.00000 0 138 - 5220.00000 - - 37s
192 0 0 5220.00000 0 148 - 5220.00000 - - 37s
193 0 0 5220.00000 0 107 - 5220.00000 - - 39s
194 0 0 5220.00000 0 269 - 5220.00000 - - 40s
195 0 0 5220.00000 0 241 - 5220.00000 - - 40s
196 0 0 5220.00000 0 79 - 5220.00000 - - 43s
197 0 0 5220.00000 0 265 - 5220.00000 - - 44s
198 0 0 5220.00000 0 107 - 5220.00000 - - 46s
199 0 0 5220.00000 0 142 - 5220.00000 - - 47s
200 0 0 5220.00000 0 218 - 5220.00000 - - 49s
201 0 0 5220.00000 0 228 - 5220.00000 - - 49s
202 0 0 5220.00000 0 211 - 5220.00000 - - 51s
203 0 2 5220.00000 0 156 - 5220.00000 - - 58s
204 3 8 5220.00000 2 478 - 5220.00000 - 3578 61s
205 11 16 5220.00000 3 817 - 5220.00000 - 3073 66s
206 19 24 5220.00000 5 550 - 5220.00000 - 2887 71s
207 28 45 5220.00000 6 538 - 5220.00000 - 2387 77s
208 45 66 5220.00000 10 241 - 5220.00000 - 2027 85s
209 77 125 5220.00000 16 286 - 5220.00000 - 1700 97s
210 155 267 5220.00000 25 342 - 5220.00000 - 1047 113s
211 360 499 5220.00000 73 309 - 5220.00000 - 679 133s
212 687 955 5220.00000 134 407 - 5220.00000 - 445 150s
213 1278 1436 5220.00000 238 286 - 5220.00000 - 286 163s
214 1833 1864 5353.41385 318 398 - 5220.00000 - 236 173s
215 2330 2799 infeasible 357 - 5220.00000 - 208 184s
216 3438 3512 5960.00000 398 167 - 5220.00000 - 153 194s
217 * 3647 3486 406 6040.0000000 5220.00000 13.6% 149 194s
218 H 3686 3452 6000.0000000 5220.00000 13.0% 148 194s
219 H 4387 3053 5960.0000000 5220.00000 12.4% 128 195s
220 4388 3044 5220.00000 295 211 5960.00000 5220.00000 12.4% 128 221s
221 4390 3045 5400.00000 419 401 5960.00000 5220.00000 12.4% 128 233s
222 4391 3046 5220.00000 355 346 5960.00000 5220.00000 12.4% 128 246s
223 4392 3047 5240.00000 589 341 5960.00000 5220.00000 12.4% 128 253s
224 4393 3047 5240.00000 529 429 5960.00000 5220.00000 12.4% 128 272s
225 4394 3048 5600.00000 472 473 5960.00000 5220.00000 12.4% 128 279s
226 H 4394 2895 5220.0000000 5220.00000 0.00% 128 287s
227
228 Cutting planes:
229 Gomory: 2
230 Cover: 572
231 Implied bound: 194
232 Projected implied bound: 29
233 Clique: 1000
234 MIR: 295
235 StrongCG: 251
236 Flow cover: 69
237 GUB cover: 42
238 Zero half: 39
239 RLT: 32
240 Relax-and-lift: 134
241 BQP: 8
242 PSD: 3
243
244 Explored 4394 nodes (736777 simplex iterations) in 287.16 seconds (470.05 work units)
245 Thread count was 8 (of 8 available processors)
246
247 Solution count 4: 5220 5960 6000 6040

```

```

248
249 Optimal solution found (tolerance 5.00e-02)
250 Best objective 5.2200000000000e+03, best bound 5.2200000000000e+03, gap 0.0000%
251 Set parameter MIPGap to value 1e-08
252 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
253
254 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
255 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
256
257 Optimize a model with 1153842 rows, 901813 columns and 7829844 nonzeros
258 Model fingerprint: 0x0eeda109
259 Variable types: 441325 continuous, 460488 integer (456438 binary)
260 Coefficient statistics:
261   Matrix range    [1e-01, 1e+10]
262   Objective range [6e-05, 5e+01]
263   Bounds range    [1e+00, 8e+01]
264   RHS range       [8e-01, 1e+10]
265 Warning: Model contains large matrix coefficients
266 Warning: Model contains large rhs
267   Consider reformulating model or setting NumericFocus parameter
268   to avoid numerical issues.
269 Presolve removed 1150027 rows and 900679 columns
270 Presolve time: 2.74s
271 Presolved: 3815 rows, 1134 columns, 10062 nonzeros
272 Variable types: 4 continuous, 1130 integer (640 binary)
273 Found heuristic solution: objective 3326.4013898
274 Found heuristic solution: objective 4038.8027795
275
276 Root relaxation: objective 4.824000e+03, 1110 iterations, 0.02 seconds (0.02 work units)
277
278   Nodes | Current Node | Objective Bounds | Work
279 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
280
281   0   0 4824.00000  0   8 4038.80278 4824.00000 19.4%  - 3s
282 H   0   0           4726.0680564 4824.00000 2.07%  - 3s
283 H   0   0           4821.9569453 4824.00000 0.04%  - 3s
284   0   0 4824.00000  0  12 4821.95695 4824.00000 0.04%  - 3s
285 H   0   0           4824.0000000 4824.00000 0.00%  - 3s
286
287 Cutting planes:
288   Clique: 1
289   RLT: 1
290
291 Explored 1 nodes (2194 simplex iterations) in 3.83 seconds (3.48 work units)
292 Thread count was 8 (of 8 available processors)
293
294 Solution count 5: 4824 4821.96 4726.07 ... 3326.4
295
296 Optimal solution found (tolerance 1.00e-08)
297 Best objective 4.8240000000000e+03, best bound 4.8240000000000e+03, gap 0.0000%
298 SP is solved
299 SP's optimal solution is'□4824
300
301   Itr = 1
302 Collect_LB = [692.0, 5220.0]
303 Collect_UB = [9748.0000000000004, 5516.0000000000002]
304 Collect_Hua = [0.0, 4528.0]
305 Collect_SPObjVal = [4528.0000000000002, 4824.0000000000002]
306 Collect_MPObjValNHua = [692.0, 692.0]
307
308
309 Set parameter MIPGap to value 0.05
310 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
311
312 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
313 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
314
315 Optimize a model with 912804 rows, 163849 columns and 2744921 nonzeros
316 Model fingerprint: 0x65773ea4
317 Variable types: 1 continuous, 163848 integer (148668 binary)
318 Coefficient statistics:
319   Matrix range    [1e-01, 1e+10]
320   Objective range [1e+00, 2e+01]
321   Bounds range    [1e+00, 1e+00]
322   RHS range       [1e+00, 2e+10]
323 Warning: Model contains large matrix coefficients
324 Warning: Model contains large rhs
325   Consider reformulating model or setting NumericFocus parameter
326   to avoid numerical issues.
327 Presolve removed 703900 rows and 139184 columns (presolve time = 5s) ...
328 Presolve removed 722888 rows and 140888 columns (presolve time = 10s) ...
329 Presolve removed 722888 rows and 140888 columns (presolve time = 15s) ...
330 Presolve removed 800700 rows and 148443 columns
331 Presolve time: 19.47s

```

```

332 Presolved: 112104 rows, 15406 columns, 363551 nonzeros
333 Variable types: 0 continuous, 15406 integer (11619 binary)
334
335 Deterministic concurrent LP optimizer: primal and dual simplex (primal and dual model)
336 Showing first log only...
337
338 Root relaxation presolved: 15406 rows, 127510 columns, 378957 nonzeros
339
340
341 Root simplex log...
342
343 Iteration   Objective      Primal Inf.   Dual Inf.    Time
344      0  5.5260000e+03  0.000000e+00  6.622339e+04  21s
345  15161  5.5260000e+03  0.000000e+00  0.000000e+00  23s
346  15161  5.5260000e+03  0.000000e+00  0.000000e+00  23s
347 Concurrent spin time: 0.89s
348
349 Solved with primal simplex
350
351 Root relaxation: objective 5.526000e+03, 15161 iterations, 3.78 seconds (3.31 work units)
352 Total elapsed time = 26.52s
353
354 Nodes | Current Node | Objective Bounds | Work
355 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
356
357  0  0 5526.00000  0 582  - 5526.00000  - - 29s
358  0  0 5526.00000  0 486  - 5526.00000  - - 30s
359  0  0 5526.00000  0 520  - 5526.00000  - - 30s
360  0  0 5526.00000  0 842  - 5526.00000  - - 39s
361  0  0 5526.00000  0 798  - 5526.00000  - - 40s
362  0  0 5526.00000  0 801  - 5526.00000  - - 43s
363  0  0 5526.00000  0 449  - 5526.00000  - - 53s
364  0  0 5526.00000  0 449  - 5526.00000  - - 53s
365  0  0 5526.00000  0 646  - 5526.00000  - - 55s
366  0  0 5526.00000  0 643  - 5526.00000  - - 55s
367  0  0 5526.00000  0 362  - 5526.00000  - - 66s
368  0  0 5526.00000  0 364  - 5526.00000  - - 66s
369  0  0 5526.00000  0 431  - 5526.00000  - - 68s
370  0  0 5526.00000  0 468  - 5526.00000  - - 68s
371  0  0 5526.00000  0 537  - 5526.00000  - - 80s
372  0  0 5526.00000  0 474  - 5526.00000  - - 80s
373  0  0 5526.00000  0 473  - 5526.00000  - - 80s
374  0  0 5526.00000  0 397  - 5526.00000  - - 81s
375  0  0 5526.00000  0 230  - 5526.00000  - - 89s
376  0  0 5526.00000  0 234  - 5526.00000  - - 90s
377  0  0 5526.00000  0 304  - 5526.00000  - - 91s
378  0  0 5526.00000  0 268  - 5526.00000  - - 91s
379  0  0 5526.00000  0 287  - 5526.00000  - - 102s
380  0  0 5526.00000  0 372  - 5526.00000  - - 102s
381  0  0 5526.00000  0 254  - 5526.00000  - - 105s
382  0  2 5526.00000  0 251  - 5526.00000  - - 117s
383  3  7 5526.00000  2 960  - 5526.00000  - 5716 125s
384 15 19 5526.00000  4 1254  - 5526.00000  - 3502 135s
385 23 27 5526.00000  5 789  - 5526.00000  - 3677 140s
386 33 45 5526.00000  8 735  - 5526.00000  - 3075 152s
387 45 69 5526.00000 11 627  - 5526.00000  - 3466 167s
388 69 140 5526.00000 13 477  - 5526.00000  - 2899 190s
389 205 333 5526.00000 31 302  - 5526.00000  - 1499 228s
390 513 724 5526.00000 110 312  - 5526.00000  - 703 252s
391 1022 1191 5566.00000 257 100  - 5526.00000  - 402 270s
392 * 1080 903 308 5566.000000 5526.00000 0.72% 385 270s
393
394 Cutting planes:
395 Gomory: 3
396 Cover: 618
397 Implied bound: 334
398 Clique: 5934
399 MIR: 192
400 StrongCG: 33
401 Flow cover: 21
402 GUB cover: 89
403 Zero half: 46
404 RLT: 117
405 Relax-and-lift: 644
406 BQP: 76
407 PSD: 9
408
409 Explored 1594 nodes (668193 simplex iterations) in 271.23 seconds (537.04 work units)
410 Thread count was 8 (of 8 available processors)
411
412 Solution count 1: 5566
413
414 Optimal solution found (tolerance 5.00e-02)
415 Best objective 5.566000000000e+03, best bound 5.526000000000e+03, gap 0.7186%

```

```
416 Warning: linear constraint 407539 and linear constraint 660172 have the same name "ConSP25_1[0,0]"
417 Set parameter MIPGap to value 1e-08
418 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
419
420 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
421 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
422
423 Optimize a model with 1153842 rows, 901813 columns and 7829844 nonzeros
424 Model fingerprint: 0x08d0e291
425 Variable types: 441325 continuous, 460488 integer (456438 binary)
426 Coefficient statistics:
427   Matrix range    [1e-01, 1e+10]
428   Objective range [6e-05, 5e+01]
429   Bounds range    [1e+00, 8e+01]
430   RHS range       [8e-01, 1e+10]
431 Warning: Model contains large matrix coefficients
432 Warning: Model contains large rhs
433   Consider reformulating model or setting NumericFocus parameter
434   to avoid numerical issues.
435 Presolve removed 1150638 rows and 900787 columns
436 Presolve time: 3.02s
437 Presolved: 3204 rows, 1026 columns, 8474 nonzeros
438 Variable types: 4 continuous, 1022 integer (584 binary)
439 Found heuristic solution: objective 4122.6666667
440
441 Root relaxation: objective 4.858667e+03, 1152 iterations, 0.03 seconds (0.02 work units)
442
443   Nodes | Current Node | Objective Bounds | Work
444 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
445
446 * 0 0 0 0 4858.6666667 4858.66667 0.00% - 3s
447
448 Explored 1 nodes (1434 simplex iterations) in 4.06 seconds (3.36 work units)
449 Thread count was 8 (of 8 available processors)
450
451 Solution count 2: 4858.67 4122.67
452
453 Optimal solution found (tolerance 1.00e-08)
454 Best objective 4.858666666667e+03, best bound 4.858666666667e+03, gap 0.0000%
455 SP is solved
456 SP's optimal solution is'□4858
457
458 Itr = 2
459 Collect_LB = [692.0, 5220.0, 5566.0]
460 Collect_UB = [9748.0000000000004, 5516.0000000000002, 5516.0000000000002]
461 Collect_Hua = [0.0, 4528.0, 4824.0]
462 Collect_SPObjVal = [4528.0000000000002, 4824.0000000000002, 4858.6666666666668]
463 Collect_MPObjValNHua = [692.0, 692.0, 742.0]
464
465
466 Ops, stop iteration
467 Values adopted from the Itr-1' th iteration, and Itr = {2}, judgeCount = {1}
468
469 ~~~~~judgeCount = 1, SPObj_SPF = 4824.0000000000002
470 Vessel i: 0: pi: 0-5, ai-di: 3-22, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 3-22, taoi-deltai: 3-21, taoPi_SP-deltaPi_SP: 3-21, betaNi: 18
, bi: 18
471 Vessel i: 1: pi: 7-14, ai-di: 4-25, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 4-25, taoi-deltai: 4-24, taoPi_SP-deltaPi_SP: 4-24, betaNi: 20
, bi: 20
472 Vessel i: 2: pi: 14-20, ai-di: 18-26, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 18-26, taoi-deltai: 18-25, taoPi_SP-deltaPi_SP: 18-25,
betaNi: 7, bi: 7
473 Vessel i: 3: pi: 14-20, ai-di: 26-61, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 26-61, taoi-deltai: 26-60, taoPi_SP-deltaPi_SP: 26-60,
betaNi: 34, bi: 34
474 Vessel i: 4: pi: 8-14, ai-di: 20-68, gi_SP-gpi_SP: 0.700000-0.900000, ai_SP-di: 23-68, taoi-deltai: 25-52, taoPi_SP-deltaPi_SP: 25-52, betaNi
: 27, bi: 27
475 Vessel i: 5: pi: 21-27, ai-di: 35-60, gi_SP-gpi_SP: 0.500000-0.300000, ai_SP-di: 39-60, taoi-deltai: 35-44, taoPi_SP-deltaPi_SP: 39-44,
betaNi: 9, bi: 9
476
477 round LB = [692, 5220, 5566]
478 round UB = [9748, 5516, 5516]
479 round Hua = [0, 4528, 4824]
480 round SPObjVal = [4528, 4824, 4859]
481 round MPObjValNHua = [692, 692, 742]
482
483 Time: 893.000000
484
485
486
487
```