



```

80 H 345 211          941.0000000 761.00000 19.1% 613 48s
81   398 242 761.00000 21 62 941.00000 761.00000 19.1% 674 52s
82   479 256 761.00000 43 218 941.00000 761.00000 19.1% 656 57s
83 H 603 256          761.0000000 761.00000 0.00% 623 57s
84
85 Cutting planes:
86 Gomory: 2
87 Cover: 120
88 Implied bound: 3989
89 Clique: 2
90 MIR: 71
91 StrongCG: 42
92 GUB cover: 11
93 Zero half: 1
94 RLT: 9
95 Relax-and-lift: 3
96 BQP: 7
97
98 Explored 639 nodes (419113 simplex iterations) in 57.99 seconds (100.96 work units)
99 Thread count was 8 (of 8 available processors)
100
101 Solution count 9: 761 941 1021 ... 2461
102
103 Optimal solution found (tolerance 1.00e-10)
104 Best objective 7.610000000000e+02, best bound 7.610000000000e+02, gap 0.0000%
105 Set parameter MIPGap to value 1e-08
106 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
107
108 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
109 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
110
111 Optimize a model with 335549 rows, 11221 columns and 691192 nonzeros
112 Model fingerprint: 0xaca662b3
113 Variable types: 28 continuous, 11193 integer (6468 binary)
114 Coefficient statistics:
115 Matrix range [1e-01, 1e+10]
116 Objective range [6e-05, 5e+01]
117 Bounds range [1e+00, 1e+00]
118 RHS range [8e-01, 1e+10]
119 Warning: Model contains large matrix coefficients
120 Warning: Model contains large rhs
121 Consider reformulating model or setting NumericFocus parameter
122 to avoid numerical issues.
123 Presolve removed 331672 rows and 9941 columns
124 Presolve time: 0.22s
125 Presolved: 3877 rows, 1280 columns, 10556 nonzeros
126 Variable types: 3 continuous, 1277 integer (755 binary)
127
128 Root relaxation: objective 5.038445e+03, 1654 iterations, 0.03 seconds (0.05 work units)
129
130 Nodes | Current Node | Objective Bounds | Work
131 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
132
133 0 0 5038.44514 0 346 - 5038.44514 - - 0s
134 H 0 0 4608.0006962 5038.44514 9.34% - 0s
135 H 0 0 4843.0006962 5038.44514 4.04% - 0s
136 0 0 4996.23141 0 420 4843.00070 4996.23141 3.16% - 0s
137 0 0 4996.21675 0 408 4843.00070 4996.21675 3.16% - 0s
138 H 0 0 4884.0006962 4996.21675 2.30% - 0s
139 H 0 0 4889.0006962 4996.21675 2.19% - 0s
140 H 0 0 4891.0006962 4996.21675 2.15% - 0s
141 0 0 4996.21675 0 404 4891.00070 4996.21675 2.15% - 0s
142 H 0 0 4910.0006962 4996.21675 1.76% - 0s
143 H 0 0 4938.0006962 4988.72585 1.03% - 0s
144 H 0 0 4958.0006962 4988.72585 0.62% - 0s
145 0 0 4986.73403 0 362 4958.00070 4986.73403 0.58% - 0s
146 0 0 4986.73403 0 369 4958.00070 4986.73403 0.58% - 0s
147 0 0 4986.73403 0 364 4958.00070 4986.73403 0.58% - 0s
148 H 0 0 4972.0006962 4980.66746 0.17% - 0s
149 0 0 4972.00070 0 152 4972.00070 4972.00070 0.00% - 0s
150
151 Cutting planes:
152 Learned: 6
153 Gomory: 15
154 Cover: 64
155 Implied bound: 78
156 Clique: 29
157 MIR: 3
158 StrongCG: 1
159 Flow cover: 10
160 GUB cover: 5
161 Zero half: 11
162 Network: 1
163 RLT: 39

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164 Relax-and-lift: 2
165 PSD: 23
166
167 Explored 1 nodes (3166 simplex iterations) in 0.61 seconds (0.77 work units)
168 Thread count was 8 (of 8 available processors)
169
170 Solution count 9: 4972 4958 4938 ... 4608
171
172 Optimal solution found (tolerance 1.00e-08)
173 Best objective 4.972000696225e+03, best bound 4.972000696225e+03, gap 0.0000%
174 SP is solved
175 SP's optimal solution is'□4972
176
177 Itr = 0
178 Collect_LB = [761.0]
179 Collect_UB = [10705.001392450096]
180 Collect_Hua = [0.0]
181 Collect_SPObjVal = [4972.000696225048]
182 Collect_MPObjValNHua = [761.0]
183
184
185 Set parameter MIPGap to value 1e-10
186 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
187
188 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
189 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
190
191 Optimize a model with 489539 rows, 180636 columns and 1336540 nonzeros
192 Model fingerprint: 0x2843198e
193 Variable types: 1 continuous, 180635 integer (180607 binary)
194 Coefficient statistics:
195   Matrix range    [1e+00, 1e+10]
196   Objective range [1e+00, 2e+01]
197   Bounds range    [1e+00, 1e+00]
198   RHS range       [1e+00, 2e+10]
199 Warning: Model contains large matrix coefficients
200 Warning: Model contains large rhs
201   Consider reformulating model or setting NumericFocus parameter
202   to avoid numerical issues.
203 Presolve removed 331540 rows and 163404 columns (presolve time = 5s) ...
204 Presolve removed 463485 rows and 173505 columns
205 Presolve time: 7.29s
206 Presolved: 26054 rows, 7131 columns, 97661 nonzeros
207 Variable types: 0 continuous, 7131 integer (7111 binary)
208
209 Root simplex log...
210
211 Iteration   Objective    Primal Inf.   Dual Inf.    Time
212      0    5.7330007e+03  8.4300000e+02  0.000000e+00  8s
213    3541  5.7330007e+03  0.0000000e+00  0.000000e+00  8s
214
215 Root relaxation: objective 5.733001e+03, 3541 iterations, 0.10 seconds (0.14 work units)
216
217   Nodes | Current Node | Objective Bounds | Work
218 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
219
220 0 0 5733.00070 0 25 -5733.00070 - - 7s
221 0 0 5733.00070 0 90 -5733.00070 - - 8s
222 0 0 5733.00070 0 77 -5733.00070 - - 9s
223 0 0 5733.00070 0 296 -5733.00070 - - 9s
224 0 0 5733.00070 0 233 -5733.00070 - - 10s
225 0 0 5733.00070 0 204 -5733.00070 - - 10s
226 0 0 5733.00070 0 101 -5733.00070 - - 14s
227 0 0 5733.00070 0 99 -5733.00070 - - 14s
228 0 0 5733.00070 0 147 -5733.00070 - - 14s
229 0 0 5733.00070 0 206 -5733.00070 - - 19s
230 0 0 5733.00070 0 201 -5733.00070 - - 19s
231 0 0 5733.00070 0 187 -5733.00070 - - 20s
232 0 2 5733.00070 0 149 -5733.00070 - - 23s
233 3 8 5733.00070 2 316 -5733.00070 - 6266 26s
234 15 19 5733.00070 4 455 -5733.00070 - 3927 30s
235 60 66 5753.05230 15 2000 -5733.00070 - 2716 36s
236 120 133 5735.06836 18 1327 -5733.00070 - 1765 40s
237 444 397 5734.33591 5 1511 -5733.00070 - 589 45s
238 1224 891 6213.00070 192 187 -5733.00070 - 265 61s
239 H 1225 847 7833.0006962 5733.00070 26.8% 264 62s
240 1227 848 6453.00070 29 149 7833.00070 5733.00070 26.8% 264 65s
241 1229 849 5753.00070 4 661 7833.00070 5733.00070 26.8% 263 75s
242 1231 851 6833.00070 288 1751 7833.00070 5733.99048 26.8% 263 88s
243 1232 851 7233.00070 344 1904 7833.00070 5733.99778 26.8% 263 90s
244 1234 853 6133.00070 231 2089 7833.00070 5733.99778 26.8% 262 95s
245 H 1234 810 7473.0006962 5733.99778 23.3% 262 104s
246 1235 810 6253.00070 252 571 7473.00070 5753.00068 23.0% 262 105s
247 H 1236 770 6873.0006962 5753.00068 16.3% 262 115s

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248 H 1236 732          6713.0006962 5753.00068 14.3% 262 115s
249 H 1236 695          6673.0006962 5753.00068 13.8% 262 115s
250 H 1236 660          6633.0006962 5753.00068 13.3% 262 115s
251 H 1236 627          6593.0006962 5753.00068 12.7% 262 115s
252 H 1236 595          6553.0006962 5753.00068 12.2% 262 115s
253 H 1236 565          6513.0006962 5753.00068 11.7% 262 115s
254 H 1236 537          5993.0006962 5753.00068 4.00% 262 115s
255 H 1236 510          5973.0006962 5753.00068 3.68% 262 122s
256 1240 514 5973.00070 272 187 5973.00070 5753.00068 3.68% 352 128s
257 1243 516 5973.00070 137 729 5973.00070 5753.00068 3.68% 351 132s
258 1244 517 5973.00070 135 1031 5973.00070 5753.00068 3.68% 351 135s
259 1246 518 5973.00070 25 968 5973.00070 5753.00068 3.68% 351 142s
260 1248 519 5973.00070 190 1036 5973.00070 5753.00070 3.68% 350 146s
261 1250 521 5973.00070 259 1110 5973.00070 5753.00070 3.68% 349 151s
262 1253 523 5973.00070 152 775 5973.00070 5753.00070 3.68% 349 155s
263 1256 530 5753.00070 30 890 5973.00070 5753.00070 3.68% 148 160s
264 1282 544 5773.00070 33 639 5973.00070 5755.71501 3.64% 221 165s
265 * 1340 503          46 5933.0006962 5761.71343 2.89% 258 169s
266 1344 495 cutoff 36 5933.00070 5762.10330 2.88% 260 171s
267 * 1349 469          38 5913.0006962 5770.26450 2.41% 263 171s
268
269 Cutting planes:
270   Learned: 1
271   Gomory: 126
272   Cover: 566
273   Implied bound: 262
274   Projected implied bound: 152
275   Clique: 111
276   MIR: 144
277   StrongCG: 62
278   Flow cover: 329
279   GUB cover: 75
280   Zero half: 270
281   RLT: 17
282   Relax-and-lift: 791
283   BQP: 7
284
285 Explored 1414 nodes (798842 simplex iterations) in 172.56 seconds (326.03 work units)
286 Thread count was 8 (of 8 available processors)
287
288 Solution count 10: 5913 5933 5973 ... 6713
289
290 Optimal solution found (tolerance 1.00e-10)
291 Best objective 5.913000696225e+03, best bound 5.913000696225e+03, gap 0.0000%
292 Set parameter MIPGap to value 1e-08
293 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
294
295 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
296 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
297
298 Optimize a model with 335549 rows, 11221 columns and 691192 nonzeros
299 Model fingerprint: 0x968c3766
300 Variable types: 28 continuous, 11193 integer (6468 binary)
301 Coefficient statistics:
302   Matrix range    [1e-01, 1e+10]
303   Objective range [6e-05, 5e+01]
304   Bounds range    [1e+00, 1e+00]
305   RHS range       [8e-01, 1e+10]
306 Warning: Model contains large matrix coefficients
307 Warning: Model contains large rhs
308   Consider reformulating model or setting NumericFocus parameter
309   to avoid numerical issues.
310 Presolve removed 330561 rows and 9627 columns
311 Presolve time: 0.26s
312 Presolved: 4988 rows, 1594 columns, 13299 nonzeros
313 Variable types: 3 continuous, 1591 integer (918 binary)
314 Found heuristic solution: objective 3905.0006962
315
316 Root relaxation: objective 5.933334e+03, 1743 iterations, 0.03 seconds (0.04 work units)
317
318   Nodes | Current Node | Objective Bounds | Work
319 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
320
321   0   0 5933.33403   0 126 3905.00070 5933.33403 51.9% - 0s
322 H   0   0          5808.0006962 5933.33403 2.16% - 0s
323 H   0   0          5822.0006962 5929.00070 1.84% - 0s
324   0   0 5929.00070   0 125 5822.00070 5929.00070 1.84% - 0s
325   0   0 5929.00070   0 56 5822.00070 5929.00070 1.84% - 0s
326 H   0   0          5877.0006962 5929.00070 0.88% - 0s
327 H   0   0          5916.0006962 5929.00070 0.22% - 0s
328 *   0   0          0 5929.0006962 5929.00070 0.00% - 0s
329
330 Cutting planes:
331   Learned: 1
```

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332 Gomory: 6
333 Cover: 5
334 Implied bound: 24
335 Clique: 14
336 MIR: 1
337 Flow cover: 1
338 Zero half: 5
339 Network: 1
340 RLT: 25
341 PSD: 3
342
343 Explored 1 nodes (2900 simplex iterations) in 0.47 seconds (0.74 work units)
344 Thread count was 8 (of 8 available processors)
345
346 Solution count 6: 5929 5916 5877 ... 3905
347
348 Optimal solution found (tolerance 1.00e-08)
349 Best objective 5.929000696225e+03, best bound 5.929000696225e+03, gap 0.0000%
350 SP is solved
351 SP's optimal solution is' 5929
352
353 Itr = 1
354 Collect_LB = [761.0, 5913.000696225048]
355 Collect_UB = [10705.001392450096, 6870.0006962250445]
356 Collect_Hua = [0.0, 4972.000696225048]
357 Collect_SPObjVal = [4972.000696225048, 5929.0006962250445]
358 Collect_MPObjValNHua = [761.0, 941.0]
359
360
361 Set parameter MIPGap to value 1e-10
362 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
363
364 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
365 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
366
367 Optimize a model with 489539 rows, 180636 columns and 1336540 nonzeros
368 Model fingerprint: 0x1b791173
369 Variable types: 1 continuous, 180635 integer (180607 binary)
370 Coefficient statistics:
371 Matrix range [1e+00, 1e+10]
372 Objective range [1e+00, 2e+01]
373 Bounds range [1e+00, 1e+00]
374 RHS range [1e+00, 2e+10]
375 Warning: Model contains large matrix coefficients
376 Warning: Model contains large rhs
377 Consider reformulating model or setting NumericFocus parameter
378 to avoid numerical issues.
379 Presolve removed 437034 rows and 174747 columns (presolve time = 5s) ...
380 Presolve removed 455528 rows and 174765 columns
381 Presolve time: 5.29s
382 Presolved: 34011 rows, 5871 columns, 86318 nonzeros
383 Variable types: 0 continuous, 5871 integer (5851 binary)
384 Root relaxation presolved: 5871 rows, 39882 columns, 92189 nonzeros
385
386
387 Root simplex log...
388
389 Iteration Objective Primal Inf. Dual Inf. Time
390 0 handle free variables 6s
391 4192 7.4100007e+03 0.000000e+00 0.000000e+00 6s
392 4192 7.4100007e+03 0.000000e+00 0.000000e+00 6s
393 4192 7.4100007e+03 0.000000e+00 0.000000e+00 6s
394
395 Root relaxation: objective 7.410001e+03, 4192 iterations, 0.29 seconds (0.54 work units)
396
397 Nodes | Current Node | Objective Bounds | Work
398 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
399
400 0 0 7410.00070 0 7 -7410.00070 - - 5s
401 0 0 7410.00070 0 77 -7410.00070 - - 6s
402 0 0 7410.00070 0 68 -7410.00070 - - 6s
403 0 0 7410.00070 0 269 -7410.00070 - - 7s
404 0 0 7410.00070 0 261 -7410.00070 - - 7s
405 0 0 7410.00070 0 39 -7410.00070 - - 8s
406 0 0 7410.00070 0 37 -7410.00070 - - 8s
407 0 0 7410.00070 0 40 -7410.00070 - - 8s
408 0 0 7410.00070 0 29 -7410.00070 - - 9s
409 0 0 7410.00070 0 36 -7410.00070 - - 9s
410 0 0 7410.00070 0 41 -7410.00070 - - 9s
411 0 0 7410.00070 0 36 -7410.00070 - - 10s
412 0 0 7410.00070 0 78 -7410.00070 - - 10s
413 0 0 7410.00070 0 29 -7410.00070 - - 10s
414 H 0 0 9310.0006962 7410.00070 20.4% - 10s
415 0 0 7410.00070 0 29 9310.00070 7410.00070 20.4% - 10s

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unknown

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416 H 0 0 8290.0006962 7410.00070 10.6% - 11s
417 0 2 7410.00070 0 28 8290.00070 7410.00070 10.6% - 11s
418 * 24 20 7 8250.0006962 7410.00070 10.2% 443 12s
419 H 30 20 7930.0006962 7410.00070 6.56% 385 13s
420 37 21 7410.00070 9 89 7930.00070 7410.00070 6.56% 473 15s
421 * 88 53 22 7410.0006962 7410.00070 0.00% 876 18s
422
423 Cutting planes:
424 Learned: 2
425 Cover: 340
426 Implied bound: 1293
427 Clique: 25
428 MIR: 37
429 StrongCG: 19
430 GUB cover: 16
431 Zero half: 6
432 RLT: 3
433 Relax-and-lift: 27
434 BQP: 3
435
436 Explored 108 nodes (114381 simplex iterations) in 18.70 seconds (31.36 work units)
437 Thread count was 8 (of 8 available processors)
438
439 Solution count 5: 7410 7930 8250 ... 9310
440
441 Optimal solution found (tolerance 1.00e-10)
442 Best objective 7.410000696225e+03, best bound 7.410000696225e+03, gap 0.0000%
443 Set parameter MIPGap to value 1e-08
444 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
445
446 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
447 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
448
449 Optimize a model with 335549 rows, 11221 columns and 691192 nonzeros
450 Model fingerprint: 0x92ccdf29
451 Variable types: 28 continuous, 11193 integer (6468 binary)
452 Coefficient statistics:
453 Matrix range [1e-01, 1e+10]
454 Objective range [6e-05, 5e+01]
455 Bounds range [1e+00, 1e+00]
456 RHS range [8e-01, 1e+10]
457 Warning: Model contains large matrix coefficients
458 Warning: Model contains large rhs
459 Consider reformulating model or setting NumericFocus parameter
460 to avoid numerical issues.
461 Presolve removed 330833 rows and 9649 columns
462 Presolve time: 0.26s
463 Presolved: 4716 rows, 1572 columns, 12564 nonzeros
464 Variable types: 3 continuous, 1569 integer (913 binary)
465 Found heuristic solution: objective 4678.0006962
466
467 Root relaxation: objective 6.786584e+03, 1975 iterations, 0.03 seconds (0.04 work units)
468
469 Nodes | Current Node | Objective Bounds | Work
470 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
471
472 0 0 6786.58403 0 28 4678.00070 6786.58403 45.1% - 0s
473 H 0 0 6779.0006962 6786.58403 0.11% - 0s
474 0 0 cutoff 0 6779.00070 6779.00070 0.00% - 0s
475
476 Cutting planes:
477 Learned: 10
478 Gomory: 7
479 Implied bound: 2
480 MIR: 3
481 StrongCG: 1
482 Flow cover: 4
483 GUB cover: 1
484 Zero half: 2
485 RLT: 3
486 Relax-and-lift: 2
487 PSD: 2
488
489 Explored 1 nodes (2633 simplex iterations) in 0.43 seconds (0.67 work units)
490 Thread count was 8 (of 8 available processors)
491
492 Solution count 2: 6779 4678
493
494 Optimal solution found (tolerance 1.00e-08)
495 Best objective 6.779000696225e+03, best bound 6.779000696225e+03, gap 0.0000%
496 SP is solved
497 SP's optimal solution is'□6779
498
499 Itr = 2
```

```

500 Collect_LB = [761.0, 5913.000696225048, 7410.0006962250445]
501 Collect_UB = [10705.001392450096, 6870.0006962250445, 6870.0006962250445]
502 Collect_Hua = [0.0, 4972.000696225048, 5929.0006962250445]
503 Collect_SPObjVal = [4972.000696225048, 5929.0006962250445, 6779.0006962250445]
504 Collect_MPObjValNHua = [761.0, 941.0, 1481.0]
505
506
507 Ops, stop iteration
508 Values adopted from the Itr-1' th iteration, and Itr = {2}, judgeCount = {1}
509
510 ~~~~~judgeCount = 1, SPObj_SPF = 5929.0006962250445
511 Vessel i: 0: pi: 0-5, ai-di: 8-17, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 8-17, taoi-deltai: 8-15, taoPi_SP-deltaPi_SP: 8-13, betaNi: 7,
bi: 7
512 Vessel i: 1: pi: 13-20, ai-di: 10-35, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 10-35, taoi-deltai: 10-33, taoPi_SP-deltaPi_SP: 10-33,
betaNi: 23, bi: 23
513 Vessel i: 2: pi: 7-13, ai-di: 16-38, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 16-38, taoi-deltai: 16-36, taoPi_SP-deltaPi_SP: 16-36, betaNi
: 20, bi: 20
514 Vessel i: 3: pi: 21-26, ai-di: 17-26, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 17-26, taoi-deltai: 17-24, taoPi_SP-deltaPi_SP: 17-24,
betaNi: 7, bi: 7
515 Vessel i: 4: pi: 20-27, ai-di: 12-63, gi_SP-gpi_SP: 0.000030-1.000000, ai_SP-di: 52-63, taoi-deltai: 31-63, taoPi_SP-deltaPi_SP: 52-63,
betaNi: 32, bi: 32
516 Vessel i: 5: pi: 13-20, ai-di: 15-59, gi_SP-gpi_SP: 0.000017-0.800000, ai_SP-di: 51-59, taoi-deltai: 34-57, taoPi_SP-deltaPi_SP: 51-57,
betaNi: 23, bi: 23
517 Vessel i: 6: pi: 29-34, ai-di: 25-55, gi_SP-gpi_SP: 0.000002-0.000000, ai_SP-di: 30-55, taoi-deltai: 27-32, taoPi_SP-deltaPi_SP: 30-32,
betaNi: 5, bi: 5
518
519 round LB = [761, 5913, 7410]
520 round UB = [10705, 6870, 6870]
521 round Hua = [0, 4972, 5929]
522 round SPObjVal = [4972, 5929, 6779]
523 round MPObjValNHua = [761, 941, 1481]
524
525 OptimalObj = 7410.0006962250445
526 Time: 302.000000
527
528
529
530

```