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80 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
81 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
82
83 Optimize a model with 3035761 rows, 2395885 columns and 21185578 nonzeros
84 Model fingerprint: 0xd0db789e
85 Variable types: 1181973 continuous, 1213912 integer (1207162 binary)
86 Coefficient statistics:
87   Matrix range   [1e-01, 1e+10]
88   Objective range [6e-05, 5e+01]
89   Bounds range   [1e+00, 8e+01]
90   RHS range      [8e-01, 1e+10]
91 Warning: Model contains large matrix coefficients
92 Warning: Model contains large rhs
93   Consider reformulating model or setting NumericFocus parameter
94   to avoid numerical issues.
95 Presolve removed 3032478 rows and 2394685 columns (presolve time = 5s) ...
96 Presolve removed 3033528 rows and 2395035 columns
97 Presolve time: 6.70s
98 Presolved: 2233 rows, 850 columns, 6060 nonzeros
99 Variable types: 9 continuous, 841 integer (502 binary)
100 Found heuristic solution: objective 3482.4264926
101
102 Root simplex log...
103
104 Iteration   Objective      Primal Inf.   Dual Inf.    Time
105      0  8.2899365e+03  5.941813e+03  0.000000e+00  8s
106    647  4.8614888e+03  0.000000e+00  0.000000e+00  8s
107
108 Root relaxation: objective 4.861489e+03, 647 iterations, 0.02 seconds (0.01 work units)
109
110 Nodes | Current Node | Objective Bounds | Work
111 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
112
113   0   0 4861.48879   0 45 3482.42649 4861.48879 39.6% - 8s
114 H   0   0           4854.6166146 4861.48879 0.14% - 8s
115   0   0 4861.07693   0 7 4854.61661 4861.07693 0.13% - 8s
116   0   0 4861.07693   0 8 4854.61661 4861.07693 0.13% - 8s
117 H   0   0           4860.4829105 4861.07693 0.01% - 8s
118 H   0   0           4861.0769320 4861.07693 0.00% - 8s
119
120 Explored 1 nodes (1204 simplex iterations) in 8.79 seconds (9.77 work units)
121 Thread count was 8 (of 8 available processors)
122
123 Solution count 4: 4861.08 4860.48 4854.62 3482.43
124
125 Optimal solution found (tolerance 1.00e-08)
126 Best objective 4.861076932024e+03, best bound 4.861076933877e+03, gap 0.0000%
127 SP is solved
128 SP's optimal solution is'□4861
129
130 Itr = 0
131 Collect_LB = [743.0]
132 Collect_UB = [10465.153864048996]
133 Collect_Hua = [0.0]
134 Collect_SPObjVal = [4861.076932024498]
135 Collect_MPObjValNHua = [743.0]
136
137
138 Set parameter TimeLimit to value 12000
139 Set parameter MIPGap to value 0.0005
140 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
141
142 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
143 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
144
145 Optimize a model with 603390 rows, 344301 columns and 1681663 nonzeros
146 Model fingerprint: 0x6ffc1c11
147 Variable types: 1 continuous, 344300 integer (344260 binary)
148 Coefficient statistics:
149   Matrix range   [1e+00, 1e+10]
150   Objective range [1e+00, 2e+01]
151   Bounds range   [1e+00, 1e+00]
152   RHS range      [1e+00, 2e+10]
153 Warning: Model contains large matrix coefficients
154 Warning: Model contains large rhs
155   Consider reformulating model or setting NumericFocus parameter
156   to avoid numerical issues.
157 Presolve removed 413625 rows and 321128 columns (presolve time = 5s) ...
158 Presolve removed 413625 rows and 321128 columns (presolve time = 10s) ...
159 Presolve removed 535578 rows and 333380 columns
160 Presolve time: 11.59s
161 Presolved: 67812 rows, 10921 columns, 173175 nonzeros
162 Variable types: 0 continuous, 10921 integer (10891 binary)
163

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164 Deterministic concurrent LP optimizer: primal and dual simplex (primal and dual model)
165 Showing first log only...
166
167 Root relaxation presolved: 10921 rows, 78733 columns, 184096 nonzeros
168
169
170 Root simplex log...
171
172 Iteration   Objective    Primal Inf.   Dual Inf.    Time
173      0  5.6040769e+03  0.000000e+00  5.338000e+03  12s
174 Concurrent spin time: 0.03s
175
176 Solved with dual simplex (primal model)
177
178 Root relaxation: objective 5.604077e+03, 4299 iterations, 0.48 seconds (0.62 work units)
179
180 Nodes | Current Node | Objective Bounds | Work
181 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
182
183 0 0 5604.07693 0 10 - 5604.07693 - - 12s
184 0 0 5604.07693 0 75 - 5604.07693 - - 13s
185 0 0 5604.07693 0 68 - 5604.07693 - - 14s
186 0 0 5604.07693 0 24 - 5604.07693 - - 15s
187 0 0 5604.07693 0 35 - 5604.07693 - - 15s
188 0 0 5604.07693 0 78 - 5604.07693 - - 16s
189 0 0 5604.07693 0 75 - 5604.07693 - - 16s
190 0 0 5604.07693 0 68 - 5604.07693 - - 19s
191 0 0 5604.07693 0 68 - 5604.07693 - - 20s
192 H 0 0 5604.0769320 5604.07693 0.00% - 20s
193 0 0 5604.07693 0 68 5604.07693 5604.07693 0.00% - 20s
194
195 Cutting planes:
196 Learned: 2
197 Gomory: 2
198 Cover: 217
199 Implied bound: 18
200 Clique: 678
201 MIR: 158
202 StrongCG: 167
203 GUB cover: 11
204 RLT: 2
205 Relax-and-lift: 9
206 BQP: 2
207
208 Explored 1 nodes (29914 simplex iterations) in 20.62 seconds (28.74 work units)
209 Thread count was 8 (of 8 available processors)
210
211 Solution count 1: 5604.08
212
213 Optimal solution found (tolerance 5.00e-04)
214 Best objective 5.604076932024e+03, best bound 5.604076932024e+03, gap 0.0000%
215 Set parameter MIPGap to value 1e-08
216 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
217
218 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
219 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
220
221 Optimize a model with 3035761 rows, 2395885 columns and 21185578 nonzeros
222 Model fingerprint: 0xfa611190
223 Variable types: 1181973 continuous, 1213912 integer (1207162 binary)
224 Coefficient statistics:
225 Matrix range [1e-01, 1e+10]
226 Objective range [6e-05, 5e+01]
227 Bounds range [1e+00, 8e+01]
228 RHS range [8e-01, 1e+10]
229 Warning: Model contains large matrix coefficients
230 Warning: Model contains large rhs
231 Consider reformulating model or setting NumericFocus parameter
232 to avoid numerical issues.
233 Presolve removed 3029879 rows and 2393977 columns (presolve time = 5s) ...
234 Presolve removed 3029927 rows and 2393995 columns
235 Presolve time: 5.76s
236 Presolved: 5834 rows, 1890 columns, 15471 nonzeros
237 Variable types: 10 continuous, 1880 integer (1090 binary)
238 Found heuristic solution: objective 4133.9680293
239
240 Root simplex log...
241
242 Iteration   Objective    Primal Inf.   Dual Inf.    Time
243      0  1.2304000e+04  5.034479e+03  0.000000e+00  7s
244    1816  5.9878730e+03  0.000000e+00  0.000000e+00  7s
245
246 Root relaxation: objective 5.987873e+03, 1816 iterations, 0.02 seconds (0.02 work units)
247

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248 Nodes | Current Node | Objective Bounds | Work
249 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
250
251 0 0 5987.87302 0 89 4133.96803 5987.87302 44.8% - 7s
252 H 0 0 5607.1254678 5987.87302 6.79% - 7s
253 H 0 0 5980.5533893 5986.94444 0.11% - 7s
254 0 0 5986.94444 0 54 5980.55339 5986.94444 0.11% - 7s
255 0 0 5986.94444 0 40 5980.55339 5986.94444 0.11% - 7s
256 0 0 5986.94444 0 26 5980.55339 5986.94444 0.11% - 7s
257 H 0 0 5986.9444444 5986.94444 0.00% - 7s
258 0 0 5986.94444 0 26 5986.94444 5986.94444 0.00% - 7s
259
260 Cutting planes:
261 Learned: 2
262 Gomory: 4
263 Cover: 2
264 Implied bound: 5
265 Clique: 7
266 MIR: 4
267 Flow cover: 1
268 Zero half: 2
269 RLT: 4
270 Relax-and-lift: 1
271
272 Explored 1 nodes (3762 simplex iterations) in 7.83 seconds (8.49 work units)
273 Thread count was 8 (of 8 available processors)
274
275 Solution count 4: 5986.94 5980.55 5607.13 4133.97
276
277 Optimal solution found (tolerance 1.00e-08)
278 Best objective 5.986944444444e+03, best bound 5.986944444444e+03, gap 0.0000%
279 SP is solved
280 SP's optimal solution is' 5986
281
282 Itr = 1
283 Collect_LB = [743.0, 5604.076932024498]
284 Collect_UB = [10465.153864048996, 6729.944444444442]
285 Collect_Hua = [0.0, 4861.076932024498]
286 Collect_SPObjVal = [4861.076932024498, 5986.944444444442]
287 Collect_MPObjValNHua = [743.0, 743.0]
288
289
290 Set parameter TimeLimit to value 12000
291 Set parameter MIPGap to value 0.0005
292 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
293
294 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
295 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
296
297 Optimize a model with 603391 rows, 344301 columns and 1681684 nonzeros
298 Model fingerprint: 0x4b281349
299 Variable types: 1 continuous, 344300 integer (344260 binary)
300 Coefficient statistics:
301 Matrix range [1e+00, 1e+10]
302 Objective range [1e+00, 2e+01]
303 Bounds range [1e+00, 1e+00]
304 RHS range [1e+00, 2e+10]
305 Warning: Model contains large matrix coefficients
306 Warning: Model contains large rhs
307 Consider reformulating model or setting NumericFocus parameter
308 to avoid numerical issues.
309 Presolve removed 417667 rows and 321479 columns (presolve time = 5s) ...
310 Presolve removed 417667 rows and 321479 columns (presolve time = 10s) ...
311 Presolve removed 536165 rows and 333455 columns
312 Presolve time: 11.42s
313 Presolved: 67226 rows, 10846 columns, 170827 nonzeros
314 Variable types: 0 continuous, 10846 integer (10816 binary)
315
316 Deterministic concurrent LP optimizer: primal and dual simplex (primal and dual model)
317 Showing first log only...
318
319 Root relaxation presolved: 10846 rows, 78072 columns, 181673 nonzeros
320
321
322 Root simplex log...
323
324 Iteration Objective Primal Inf. Dual Inf. Time
325 0 6.7324444e+03 0.000000e+00 5.338000e+03 12s
326 Concurrent spin time: 0.09s
327
328 Solved with dual simplex (primal model)
329
330 Root relaxation: objective 6.732444e+03, 4502 iterations, 0.44 seconds (0.67 work units)
331
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332 Nodes | Current Node | Objective Bounds | Work
333 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
334
335 0 0 6732.44444 0 23 - 6732.44444 - - 12s
336 0 0 6732.44444 0 353 - 6732.44444 - - 14s
337 0 0 6732.44444 0 296 - 6732.44444 - - 14s
338 0 0 6732.44444 0 201 - 6732.44444 - - 14s
339 0 0 6732.44444 0 93 - 6732.44444 - - 17s
340 0 0 6732.44444 0 101 - 6732.44444 - - 17s
341 0 0 6732.44444 0 47 - 6732.44444 - - 18s
342 0 0 6732.44444 0 101 - 6732.44444 - - 18s
343 0 0 6732.44444 0 64 - 6732.44444 - - 19s
344 H 0 0 6832.4444444 6732.44444 1.46% - 19s
345 H 0 0 6812.4444444 6732.44444 1.17% - 19s
346 H 0 0 6732.4444444 6732.44444 0.00% - 21s
347 0 0 6732.44444 0 64 6732.44444 6732.44444 0.00% - 21s
348
349 Cutting planes:
350 Learned: 1
351 Gomory: 1
352 Cover: 89
353 Implied bound: 394
354 Clique: 1070
355 MIR: 26
356 StrongCG: 19
357 GUB cover: 8
358 Zero half: 2
359 RLT: 2
360 Relax-and-lift: 20
361 BQP: 9
362
363 Explored 1 nodes (29232 simplex iterations) in 21.37 seconds (32.16 work units)
364 Thread count was 8 (of 8 available processors)
365
366 Solution count 3: 6732.44 6812.44 6832.44
367
368 Optimal solution found (tolerance 5.00e-04)
369 Best objective 6.732444444444e+03, best bound 6.732444444444e+03, gap 0.0000%
370 Set parameter MIPGap to value 1e-08
371 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
372
373 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
374 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
375
376 Optimize a model with 3035761 rows, 2395885 columns and 21185578 nonzeros
377 Model fingerprint: 0x4b39522e
378 Variable types: 1181973 continuous, 1213912 integer (1207162 binary)
379 Coefficient statistics:
380 Matrix range [1e-01, 1e+10]
381 Objective range [6e-05, 5e+01]
382 Bounds range [1e+00, 8e+01]
383 RHS range [8e-01, 1e+10]
384 Warning: Model contains large matrix coefficients
385 Warning: Model contains large rhs
386 Consider reformulating model or setting NumericFocus parameter
387 to avoid numerical issues.
388 Presolve removed 3030796 rows and 2394227 columns (presolve time = 5s) ...
389 Presolve removed 3031116 rows and 2394327 columns
390 Presolve time: 6.12s
391 Presolved: 4645 rows, 1558 columns, 12363 nonzeros
392 Variable types: 10 continuous, 1548 integer (906 binary)
393
394 Root simplex log...
395
396 Iteration Objective Primal Inf. Dual Inf. Time
397 0 1.1149000e+04 5.079458e+03 0.000000e+00 8s
398 1283 5.8269444e+03 0.000000e+00 0.000000e+00 8s
399
400 Root relaxation: objective 5.826944e+03, 1283 iterations, 0.01 seconds (0.01 work units)
401
402 Nodes | Current Node | Objective Bounds | Work
403 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
404
405 H 0 0 5826.9444444 14682.7778 152% - 7s
406 0 0 - 0 5826.94444 5826.94444 0.00% - 7s
407
408 Explored 1 nodes (1978 simplex iterations) in 8.04 seconds (8.97 work units)
409 Thread count was 8 (of 8 available processors)
410
411 Solution count 1: 5826.94
412
413 Optimal solution found (tolerance 1.00e-08)
414 Best objective 5.826944444444e+03, best bound 5.826944444444e+03, gap 0.0000%
415 SP is solved

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416 SP's optimal solution is'□5826
417
418 Itr = 2
419 Collect_LB = [743.0, 5604.076932024498, 6732.444444444442]
420 Collect_UB = [10465.153864048996, 6729.944444444442, 6572.444444444442]
421 Collect_Hua = [0.0, 4861.076932024498, 5986.944444444442]
422 Collect_SPObjVal = [4861.076932024498, 5986.944444444442, 5826.944444444442]
423 Collect_MPObjValNHua = [743.0, 743.0, 745.5]
424
425
426 Ops, stop iteration
427 Values adopted from the Itr-1' th iteration, and Itr = {2}, judgeCount = {1}
428
429 ~~~~~judgeCount = 1, SPObj_SPF = 5986.944444444442
430 Vessel i: 0: pi: 0-5, ai-di: 5-15, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 5-15, taoi-deltai: 5-10, taoPi_SP-deltaPi_SP: 5-10, betaNi: 5,
bi: 5
431 Vessel i: 1: pi: 0-7, ai-di: 22-44, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 22-44, taoi-deltai: 22-34, taoPi_SP-deltaPi_SP: 22-34, betaNi:
12, bi: 12
432 Vessel i: 2: pi: 5-10, ai-di: 8-26, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 8-26, taoi-deltai: 8-19, taoPi_SP-deltaPi_SP: 8-19, betaNi: 11
, bi: 11
433 Vessel i: 3: pi: 3-8, ai-di: 41-62, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 41-62, taoi-deltai: 41-53, taoPi_SP-deltaPi_SP: 41-53, betaNi:
12, bi: 12
434 Vessel i: 4: pi: 3-10, ai-di: 55-82, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 55-82, taoi-deltai: 55-75, taoPi_SP-deltaPi_SP: 55-75, betaNi
: 20, bi: 20
435 Vessel i: 5: pi: 17-22, ai-di: 18-61, gi_SP-gpi_SP: 0.000000-1.000000, ai_SP-di: 18-61, taoi-deltai: 21-46, taoPi_SP-deltaPi_SP: 21-46,
betaNi: 25, bi: 25
436 Vessel i: 6: pi: 15-20, ai-di: 9-39, gi_SP-gpi_SP: 0.875000-0.400000, ai_SP-di: 15-39, taoi-deltai: 11-20, taoPi_SP-deltaPi_SP: 16-20, betaNi
: 9, bi: 9
437 Vessel i: 7: pi: 10-16, ai-di: 35-77, gi_SP-gpi_SP: 1.000000-0.600000, ai_SP-di: 45-77, taoi-deltai: 40-59, taoPi_SP-deltaPi_SP: 45-59,
betaNi: 19, bi: 19
438 Vessel i: 8: pi: 10-15, ai-di: 5-41, gi_SP-gpi_SP: 0.553571-1.000000, ai_SP-di: 8-41, taoi-deltai: 12-25, taoPi_SP-deltaPi_SP: 12-25, betaNi:
13, bi: 13
439 Vessel i: 9: pi: 10-15, ai-di: 29-55, gi_SP-gpi_SP: 0.571429-0.000000, ai_SP-di: 33-55, taoi-deltai: 33-39, taoPi_SP-deltaPi_SP: 33-39,
betaNi: 6, bi: 6
440
441 round LB = [743, 5604, 6732]
442 round UB = [10465, 6730, 6572]
443 round Hua = [0, 4861, 5987]
444 round SPObjVal = [4861, 5987, 5827]
445 round MPObjValNHua = [743, 743, 746]
446
447 OptimalObj = 6732.444444444442
448 Time: 591.000000
449
450
451
452

```