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80
81 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
82 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
83
84 Optimize a model with 3035544 rows, 2395885 columns and 21184927 nonzeros
85 Model fingerprint: 0x091910e1
86 Variable types: 1181973 continuous, 1213912 integer (1207162 binary)
87 Coefficient statistics:
88   Matrix range    [1e-01, 1e+10]
89   Objective range [6e-05, 5e+01]
90   Bounds range    [1e+00, 8e+01]
91   RHS range       [8e-01, 1e+10]
92 Warning: Model contains large matrix coefficients
93 Warning: Model contains large rhs
94   Consider reformulating model or setting NumericFocus parameter
95   to avoid numerical issues.
96 Presolve removed 3032248 rows and 2394679 columns (presolve time = 5s) ...
97 Presolve removed 3033311 rows and 2395035 columns
98 Presolve time: 6.88s
99 Presolved: 2233 rows, 850 columns, 6060 nonzeros
100 Variable types: 9 continuous, 841 integer (502 binary)
101 Found heuristic solution: objective 3482.4264926
102
103 Root simplex log...
104
105 Iteration   Objective    Primal Inf.   Dual Inf.    Time
106           0 8.2899365e+03 5.941813e+03 0.000000e+00 9s
107           647 4.8614888e+03 0.000000e+00 0.000000e+00 9s
108
109 Root relaxation: objective 4.861489e+03, 647 iterations, 0.00 seconds (0.01 work units)
110
111   Nodes | Current Node | Objective Bounds | Work
112 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
113
114   0   0 4861.48879   0 45 3482.42649 4861.48879 39.6% - 8s
115 H  0   0           4854.6166146 4861.48879 0.14% - 8s
116   0   0 4861.07693   0 7 4854.61661 4861.07693 0.13% - 8s
117   0   0 4861.07693   0 8 4854.61661 4861.07693 0.13% - 8s
118 H  0   0           4860.4829105 4861.07693 0.01% - 8s
119 H  0   0           4861.0769320 4861.07693 0.00% - 8s
120
121 Explored 1 nodes (1204 simplex iterations) in 8.98 seconds (9.78 work units)
122 Thread count was 8 (of 8 available processors)
123
124 Solution count 4: 4861.08 4860.48 4854.62 3482.43
125
126 Optimal solution found (tolerance 1.00e-08)
127 Best objective 4.861076932024e+03, best bound 4.861076933877e+03, gap 0.0000%
128 SP is solved
129 SP's optimal solution is'□4861
130
131 Itr = 0
132 Collect_LB = [743.0]
133 Collect_UB = [10465.153864048996]
134 Collect_Hua = [0.0]
135 Collect_SPObjVal = [4861.076932024498]
136 Collect_MPObjValNHua = [743.0]
137
138
139 Set parameter TimeLimit to value 7200
140 Set parameter MIPGap to value 0.05
141 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
142
143 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
144 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
145
146 Optimize a model with 1257465 rows, 366171 columns and 3743932 nonzeros
147 Model fingerprint: 0xe18f9445
148 Variable types: 1 continuous, 366170 integer (353500 binary)
149 Coefficient statistics:
150   Matrix range    [1e-01, 1e+10]
151   Objective range [1e+00, 2e+01]
152   Bounds range    [1e+00, 1e+00]
153   RHS range       [1e+00, 2e+10]
154 Warning: Model contains large matrix coefficients
155 Warning: Model contains large rhs
156   Consider reformulating model or setting NumericFocus parameter
157   to avoid numerical issues.
158 Presolve removed 988820 rows and 335656 columns (presolve time = 5s) ...
159 Presolve removed 1026022 rows and 339091 columns (presolve time = 10s) ...
160 Presolve removed 1026022 rows and 339091 columns (presolve time = 15s) ...
161 Presolve removed 1026022 rows and 339091 columns (presolve time = 20s) ...
162 Presolve removed 1116433 rows and 348798 columns
163 Presolve time: 21.05s

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164 Presolved: 141032 rows, 17373 columns, 430785 nonzeros
165 Variable types: 1 continuous, 17372 integer (14574 binary)
166
167 Deterministic concurrent LP optimizer: primal and dual simplex (primal and dual model)
168 Showing first log only...
169
170 Root relaxation presolved: 17373 rows, 158405 columns, 448158 nonzeros
171
172
173 Root simplex log...
174
175 Iteration   Objective      Primal Inf.   Dual Inf.    Time
176      0  5.6040769e+03  0.000000e+00  9.635125e+03  22s
177 Concurrent spin time: 0.97s
178
179 Solved with dual simplex (primal model)
180
181 Root relaxation: objective 5.604077e+03, 8072 iterations, 2.79 seconds (4.27 work units)
182 Total elapsed time = 29.37s
183 Total elapsed time = 30.10s
184
185 Nodes | Current Node | Objective Bounds | Work
186 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
187
188 0 0 5604.07693 0 303 -5604.07693 - - 32s
189 0 0 5604.07693 0 678 -5604.07693 - - 36s
190 0 0 5604.07693 0 583 -5604.07693 - - 38s
191 0 0 5604.07693 0 219 -5604.07693 - - 45s
192 0 0 5604.07693 0 295 -5604.07693 - - 45s
193 0 0 5604.07693 0 385 -5604.07693 - - 51s
194 0 0 5604.07693 0 304 -5604.07693 - - 52s
195 0 0 5604.07693 0 88 -5604.07693 - - 57s
196 0 0 5604.07693 0 166 -5604.07693 - - 58s
197 0 0 5604.07693 0 140 -5604.07693 - - 68s
198 0 0 5604.07693 0 197 -5604.07693 - - 68s
199 0 0 5604.07693 0 173 -5604.07693 - - 69s
200 0 0 5604.07693 0 178 -5604.07693 - - 75s
201 0 0 5604.07693 0 210 -5604.07693 - - 75s
202 0 0 5604.07693 0 93 -5604.07693 - - 78s
203 0 0 5604.07693 0 93 -5604.07693 - - 80s
204 H 0 0 5604.0769320 5604.07693 0.00% - 90s
205 0 0 5604.07693 0 93 5604.07693 5604.07693 0.00% - 90s
206
207 Cutting planes:
208 Learned: 4
209 Gomory: 5
210 Cover: 228
211 Implied bound: 73
212 Clique: 1667
213 MIR: 335
214 StrongCG: 139
215 Flow cover: 265
216 GUB cover: 36
217 Zero half: 18
218 RLT: 78
219 Relax-and-lift: 200
220 BQP: 62
221 PSD: 1
222
223 Explored 1 nodes (146488 simplex iterations) in 90.08 seconds (214.72 work units)
224 Thread count was 8 (of 8 available processors)
225
226 Solution count 1: 5604.08
227
228 Optimal solution found (tolerance 5.00e-02)
229 Best objective 5.604076932024e+03, best bound 5.604076932024e+03, gap 0.0000%
230 Set parameter MIPGap to value 1e-08
231 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
232
233 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
234 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
235
236 Optimize a model with 3035544 rows, 2395885 columns and 21184927 nonzeros
237 Model fingerprint: 0x64085dca
238 Variable types: 1181973 continuous, 1213912 integer (1207162 binary)
239 Coefficient statistics:
240 Matrix range [1e-01, 1e+10]
241 Objective range [6e-05, 5e+01]
242 Bounds range [1e+00, 8e+01]
243 RHS range [8e-01, 1e+10]
244 Warning: Model contains large matrix coefficients
245 Warning: Model contains large rhs
246 Consider reformulating model or setting NumericFocus parameter
247 to avoid numerical issues.

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248 Presolve removed 3029984 rows and 2394037 columns (presolve time = 5s) ...
249 Presolve removed 3030042 rows and 2394055 columns
250 Presolve time: 6.13s
251 Presolved: 5502 rows, 1830 columns, 14558 nonzeros
252 Variable types: 10 continuous, 1820 integer (1058 binary)
253 Found heuristic solution: objective 4232.1031942
254
255 Root simplex log...
256
257 Iteration   Objective      Primal Inf.   Dual Inf.    Time
258      0  1.2604000e+04  1.911614e+04  0.000000e+00  8s
259    1860  5.9878730e+03  0.000000e+00  0.000000e+00  8s
260
261 Root relaxation: objective 5.987873e+03, 1860 iterations, 0.02 seconds (0.02 work units)
262
263   Nodes | Current Node | Objective Bounds | Work
264 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
265
266   0   0 5987.87302   0 11 4232.10319 5987.87302 41.5% - 7s
267 H  0   0           5986.3015873 5987.87302 0.03% - 7s
268   0   0 5987.87302   0 10 5986.30159 5987.87302 0.03% - 7s
269   0   0 5987.87302   0  8 5986.30159 5987.87302 0.03% - 7s
270 H  0   0           5986.9444444 5987.87302 0.02% - 7s
271
272 Cutting planes:
273 Gomory: 1
274 MIR: 1
275
276 Explored 1 nodes (2792 simplex iterations) in 8.21 seconds (8.69 work units)
277 Thread count was 8 (of 8 available processors)
278
279 Solution count 3: 5986.94 5986.3 4232.1
280
281 Optimal solution found (tolerance 1.00e-08)
282 Best objective 5.986944444444e+03, best bound 5.986944444444e+03, gap 0.0000%
283 SP is solved
284 SP's optimal solution is'□5986
285
286 Itr = 1
287 Collect_LB = [743.0, 5604.076932024498]
288 Collect_UB = [10465.153864048996, 6729.944444444442]
289 Collect_Hua = [0.0, 4861.076932024498]
290 Collect_SPObjVal = [4861.076932024498, 5986.944444444442]
291 Collect_MPObjValNHua = [743.0, 743.0]
292
293
294 Set parameter TimeLimit to value 7200
295 Set parameter MIPGap to value 0.05
296 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
297
298 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
299 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
300
301 Optimize a model with 1911541 rows, 388041 columns and 5806222 nonzeros
302 Model fingerprint: 0x7e63c969
303 Variable types: 1 continuous, 388040 integer (362740 binary)
304 Coefficient statistics:
305 Matrix range [1e-01, 1e+10]
306 Objective range [1e+00, 2e+01]
307 Bounds range [1e+00, 1e+00]
308 RHS range [1e+00, 2e+10]
309 Warning: Model contains large matrix coefficients
310 Warning: Model contains large rhs
311 Consider reformulating model or setting NumericFocus parameter
312 to avoid numerical issues.
313 Presolve removed 1567892 rows and 350836 columns (presolve time = 5s) ...
314 Presolve removed 1605053 rows and 353839 columns (presolve time = 10s) ...
315 Presolve removed 1620237 rows and 354849 columns (presolve time = 21s) ...
316 Presolve removed 1620237 rows and 363560 columns (presolve time = 25s) ...
317 Presolve removed 1707010 rows and 364580 columns
318 Presolve time: 26.36s
319 Presolved: 204531 rows, 23461 columns, 659633 nonzeros
320 Variable types: 1 continuous, 23460 integer (18006 binary)
321
322 Deterministic concurrent LP optimizer: primal simplex, dual simplex, and barrier
323 Showing barrier log only...
324
325 Root relaxation presolved: 23461 rows, 227992 columns, 683094 nonzeros
326
327 Root barrier log...
328
329 Ordering time: 2.74s
330
331 Barrier statistics:
```

```

332 Dense cols : 32
333 Free vars : 816
334 AA' NZ : 7.154e+05
335 Factor NZ : 2.597e+07 (roughly 300 MB of memory)
336 Factor Ops : 7.723e+10 (roughly 2 seconds per iteration)
337 Threads : 1
338
339 Objective Residual
340 Iter Primal Dual Primal Dual Compl Time
341 0 -6.72569266e+07 3.62289678e+04 2.77e+04 1.85e+03 8.91e+04 34s
342
343 Barrier performed 0 iterations in 33.58 seconds (54.98 work units)
344 Barrier solve interrupted - model solved by another algorithm
345
346 Concurrent spin time: 1.80s (can be avoided by choosing Method=3)
347
348 Solved with primal simplex
349
350 Root relaxation: objective 6.732444e+03, 25869 iterations, 6.15 seconds (7.49 work units)
351 Total elapsed time = 40.31s
352
353 Nodes | Current Node | Objective Bounds | Work
354 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
355
356 0 0 6732.44444 0 686 - 6732.44444 - - 46s
357 0 0 6732.44444 0 677 - 6732.44444 - - 46s
358 0 0 6732.44444 0 1067 - 6732.44444 - - 57s
359 0 0 6732.44444 0 885 - 6732.44444 - - 61s
360 0 0 6732.44444 0 642 - 6732.44444 - - 86s
361 0 0 6732.44444 0 643 - 6732.44444 - - 89s
362 0 0 6732.44444 0 654 - 6732.44444 - - 89s
363 0 0 6732.44444 0 340 - 6732.44444 - - 105s
364 0 0 6732.44444 0 370 - 6732.44444 - - 107s
365 0 0 6732.44444 0 215 - 6732.44444 - - 114s
366 0 0 6732.44444 0 251 - 6732.44444 - - 116s
367 0 0 6732.44444 0 327 - 6732.44444 - - 128s
368 0 0 6732.44444 0 468 - 6732.44444 - - 129s
369 0 0 6732.44444 0 426 - 6732.44444 - - 142s
370 0 0 6732.44444 0 171 - 6732.44444 - - 151s
371 H 0 0 6732.4444444 6732.44444 0.00% - 177s
372 0 0 6732.44444 0 171 6732.44444 6732.44444 0.00% - 177s
373
374 Cutting planes:
375 Learned: 7
376 Gomory: 7
377 Cover: 460
378 Implied bound: 632
379 Clique: 3839
380 MIR: 851
381 StrongCG: 169
382 Flow cover: 29
383 GUB cover: 429
384 Zero half: 40
385 Network: 1
386 RLT: 152
387 Relax-and-lift: 453
388 BQP: 59
389 PSD: 2
390
391 Explored 1 nodes (232805 simplex iterations) in 177.43 seconds (472.86 work units)
392 Thread count was 8 (of 8 available processors)
393
394 Solution count 1: 6732.44
395
396 Optimal solution found (tolerance 5.00e-02)
397 Best objective 6.73244444444e+03, best bound 6.73244444444e+03, gap 0.0000%
398 Warning: linear constraint 603390 and linear constraint 1257466 have the same name "ConSP25_1[0,0]"
399 Set parameter MIPGap to value 1e-08
400 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
401
402 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
403 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
404
405 Optimize a model with 3035544 rows, 2395885 columns and 21184927 nonzeros
406 Model fingerprint: 0xad74d263
407 Variable types: 1181973 continuous, 1213912 integer (1207162 binary)
408 Coefficient statistics:
409 Matrix range [1e-01, 1e+10]
410 Objective range [6e-05, 5e+01]
411 Bounds range [1e+00, 8e+01]
412 RHS range [8e-01, 1e+10]
413 Warning: Model contains large matrix coefficients
414 Warning: Model contains large rhs
415 Consider reformulating model or setting NumericFocus parameter

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```

416         to avoid numerical issues.
417 Presolve removed 3029642 rows and 2393966 columns (presolve time = 5s) ...
418 Presolve removed 3029700 rows and 2393984 columns
419 Presolve time: 6.17s
420 Presolved: 5844 rows, 1901 columns, 15495 nonzeros
421 Variable types: 10 continuous, 1891 integer (1095 binary)
422 Found heuristic solution: objective 4347.4490078
423
424 Root simplex log...
425
426 Iteration   Objective      Primal Inf.   Dual Inf.    Time
427      0  1.2724000e+04  1.924820e+04  0.000000e+00   8s
428    1703  6.0419444e+03  0.000000e+00  0.000000e+00   8s
429
430 Root relaxation: objective 6.041944e+03, 1703 iterations, 0.02 seconds (0.01 work units)
431
432   Nodes | Current Node | Objective Bounds | Work
433 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
434
435 H  0  0           6041.9444444 17457.7778 189% - 7s
436   0  0   -  0    6041.94444 6041.94444 0.00% - 7s
437
438 Explored 1 nodes (2252 simplex iterations) in 8.17 seconds (8.65 work units)
439 Thread count was 8 (of 8 available processors)
440
441 Solution count 2: 6041.94 4347.45
442
443 Optimal solution found (tolerance 1.00e-08)
444 Best objective 6.041944444444e+03, best bound 6.041944444444e+03, gap 0.0000%
445 SP is solved
446 SP's optimal solution is'□6041
447
448 Itr = 2
449 Collect_LB = [743.0, 5604.076932024498, 6732.444444444442]
450 Collect_UB = [10465.153864048996, 6729.944444444442, 6729.944444444442]
451 Collect_Hua = [0.0, 4861.076932024498, 5986.944444444442]
452 Collect_SPObjVal = [4861.076932024498, 5986.944444444442, 6041.944444444442]
453 Collect_MPObjValNHua = [743.0, 743.0, 745.5]
454
455
456 Reach the termination conditions, stop iteration
457 Values adopted from the judgeCount's th iteration, and Itr = {2}, judgeCount = {1}
458
459 ~~~~~judgeCount = 1, SPObj_SPF = 5986.944444444442
460 Vessel i: 0: pi: 0-5, ai-di: 5-15, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 5-15, taoi-deltai: 5-10, taoPi_SP-deltaPi_SP: 5-10, betaNi: 5,
bi: 5
461 Vessel i: 1: pi: 0-7, ai-di: 22-44, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 22-44, taoi-deltai: 22-34, taoPi_SP-deltaPi_SP: 22-34, betaNi:
12, bi: 12
462 Vessel i: 2: pi: 7-12, ai-di: 8-26, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 8-26, taoi-deltai: 8-19, taoPi_SP-deltaPi_SP: 8-19, betaNi: 11
, bi: 11
463 Vessel i: 3: pi: 5-10, ai-di: 41-62, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 41-62, taoi-deltai: 41-53, taoPi_SP-deltaPi_SP: 41-53, betaNi:
: 12, bi: 12
464 Vessel i: 4: pi: 7-14, ai-di: 55-82, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 55-82, taoi-deltai: 55-75, taoPi_SP-deltaPi_SP: 55-75, betaNi:
: 20, bi: 20
465 Vessel i: 5: pi: 10-15, ai-di: 18-61, gi_SP-gpi_SP: 0.000000-1.000000, ai_SP-di: 18-61, taoi-deltai: 21-46, taoPi_SP-deltaPi_SP: 21-46,
betaNi: 25, bi: 25
466 Vessel i: 6: pi: 12-17, ai-di: 9-39, gi_SP-gpi_SP: 0.875000-0.400000, ai_SP-di: 16-39, taoi-deltai: 11-20, taoPi_SP-deltaPi_SP: 16-20, betaNi:
: 9, bi: 9
467 Vessel i: 7: pi: 15-21, ai-di: 35-77, gi_SP-gpi_SP: 1.000000-0.600000, ai_SP-di: 45-77, taoi-deltai: 40-59, taoPi_SP-deltaPi_SP: 45-59,
betaNi: 19, bi: 19
468 Vessel i: 8: pi: 18-23, ai-di: 5-41, gi_SP-gpi_SP: 0.553571-1.000000, ai_SP-di: 8-41, taoi-deltai: 12-25, taoPi_SP-deltaPi_SP: 12-25, betaNi:
13, bi: 13
469 Vessel i: 9: pi: 15-20, ai-di: 29-55, gi_SP-gpi_SP: 0.571429-0.000000, ai_SP-di: 33-55, taoi-deltai: 33-39, taoPi_SP-deltaPi_SP: 33-39,
betaNi: 6, bi: 6
470
471 round LB = [743, 5604, 6732]
472 round UB = [10465, 6730, 6730]
473 round Hua = [0, 4861, 5987]
474 round SPObjVal = [4861, 5987, 6042]
475 round MPObjValNHua = [743, 743, 746]
476
477 Time: 1371.000000
478
479
480
481

```