```
this paper\Scripts\python.exe" "D:\Python\Pycharm\setroute\PyCharm Community Edition 2021.2.3\plugins\python-ce\helpers\pydev\pydevconsole.py" --mode=
       client --port=30274
       import sys; print('Python %s on %s' % (sys.version, sys.platform))
       sys.path.extend([F:\\\] ===\\\\3 python_code\\9 Code for this paper', 'E:/1 ===\\3 ===\\1 ===\\1 ===\\1 ===\\1 ===\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 ==\\1 =\\1 ==\\1 ==\\1 ==\\1 ==\\1 =\\1 ==\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\1 =\\
  4
 6
       PyDev console: starting.
       Python 3.9.7 (tags/v3.9.7:1016ef3, Aug 30 2021, 20:19:38) [MSC v.1929 64 bit (AMD64)] on win32
  8
       >>> runfile('E:/1 = 1 = 0/3 = 0 = 0/1 = 0 = 0 = 0/1 = 0 = 0 = 0/1 = 0 = 0/1 = 0 = 0/1 = 0 = 0/1 = 0 = 0/1 = 0 = 0/1 = 0 = 0/1 = 0 = 0/1 = 0 = 0/1 = 0 = 0/1 = 0 = 0/1 = 0 = 0/1 = 0 = 0/1 = 0 = 0/1 = 0 = 0/1 = 0 = 0/1 = 0 = 0/1 = 0 = 0/1 = 0 = 0/1 = 0 = 0/1 = 0 = 0/1 = 0/1 = 0 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 = 0/1 
       Code for this paper')
10 Backend TkAgg is interactive backend. Turning interactive mode on.
       Waiting 5s...
      Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
12
13
      CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
15
       Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
16
17
       Optimize a model with 624623 rows, 47910 columns and 1843346 nonzeros
       Model fingerprint: 0xcb3b5a71
19
       Variable types: 0 continuous, 47910 integer (40308 binary)
20 Coefficient statistics:
21
         Matrix range [1e-01, 1e+15]
         Objective range [1e+00, 5e+01]
23
         Bounds range [1e+00, 1e+00]
24
         RHS range
                                      [1e+00, 2e+15]
       Warning: Model contains large matrix coefficient range
26
       Warning: Model contains large rhs
27
                  Consider reformulating model or setting NumericFocus parameter
28
                  to avoid numerical issues.
29
       Presolve removed 469292 rows and 28825 columns (presolve time = 5s) ...
       Presolve removed 531953 rows and 34624 columns (presolve time = 10s) ...
30
31
       Presolve removed 531957 rows and 34628 columns
       Presolve time: 10.07s
       Presolved: 92666 rows, 13282 columns, 275500 nonzeros
33
34
        Variable types: 0 continuous, 13282 integer (13081 binary)
35
       Deterministic concurrent LP optimizer: primal and dual simplex (primal and dual model)
37
       Showing first log only...
38
39
       Root relaxation presolved: 13274 rows, 105924 columns, 288269 nonzeros
40
41
42
       Root simplex log...
43
44
                                                   Primal Inf. Dual Inf.
       Iteration Objective
                                                                                                   Time
               0 -9.0620000e+03 0.000000e+00 7.255502e+04
45
                                                                                                                   11s
46
       Concurrent spin time: 0.10s
48
       Solved with dual simplex (primal model)
49
50
       Root relaxation: objective 6.043834e+02, 2008 iterations, 0.80 seconds (0.70 work units)
51
            Nodes | Current Node | Objective Bounds
52

↓ Work

53
        Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
54
55
                     0 604.38345 0 112
                                                                        - 604.38345
56
             0
                     0 616.78806 0 780
                                                                        - 616.78806
                                                                                                            - 14s
                                                                                                            - 14s
57
             0
                     0 616.78806
                                                 0 776
                                                                        - 616.78806
58
                     0 622.17500
                                               0 682
                                                                        - 622.17500
                                                                                                      - - 14s
59
                     0 622.21658
                                               0 653
                                                                        - 622.21658
                                                                                                            - 15s
             0
60
             0
                     0 622.25991
                                                 0 647
                                                                        - 622.25991
                                                                                                            - 15s
                     0 622.30005
                                                                        - 622.30005
                                                                                                      - - 15s
                                                 0 561
62
             0
                     0 622.30005
                                                 0 559
                                                                        - 622.30005
                                                                                                      - - 15s
63
                     0 629.28369
                                                 0 387
                                                                        - 629.28369
                                                                                                     - - 17s
             0
64
             0
                     0 629.28369
                                                 0 382
                                                                        - 629.28369
                                                                                                            - 17s
65
             0
                     0 629.30706
                                                 0 430
                                                                        - 629.30706
                                                                                                                  17s
                                               0 424
                    0 632.91250
                                                                        - 632.91250
                                                                                                      - - 18s
66
             0
                                                                        - 632.91250
67
             0
                     0 632.91250
                                                 0 407
                                                                                                      - - 18s
68
             0
                     0 637.99999
                                                 0 311
                                                                        - 637.99999
                                                                                                                  20s
69
                     0 637.99999
                                                 0 266
                                                                        - 637.99999
                                                                                                                  21s
                     0 637 99999
                                                                        - 637 99999
70
             0
                                                 0.265
                                                                                                                  21s
71
             0
                    0 637.99999
                                                 0.350
                                                                        - 637.99999
                                                                                                             - 22s
      Η
             0
                                                1318.0000000 637.99999 51.6%
73
             0
                    0 637.99999
                                               0 286 1318.00000 637.99999 51.6% -
                                                                                                                                 23s
                                               0 30 1318.00000 637.99999 51.6%
74
             0
                    0 637.99999
75 H 0
                       0
                                                1198.0000000 637.99999 46.7%
             0 0 637.99999 0 46 1198.00000 637.99999 46.7%
76
                                                                                                                             - 26s
                                                 638.0000000 637.99999 0.00% - 27s
77 H 0 0
                    0\ 637.99999\quad 0\ 62\ 638.00000\ 637.99999\ 0.00\%
78
             0
79
```

```
unknown
 80 Cutting planes:
 81
      Learned: 234
      Gomory: 28
 82
 83
      Cover: 305
      Implied bound: 34
 85
      Clique: 116
      MIR: 102
 86
 87
      StrongCG: 40
 88
      Flow cover: 33
 89
      GUB cover: 43
 90
      Zero half: 11
 91
       RLT: 96
      Relax-and-lift: 110
 93
      BQP: 6
 94
 95 Explored 1 nodes (16913 simplex iterations) in 27.70 seconds (37.32 work units)
 96 Thread count was 8 (of 8 available processors)
 97
 98 Solution count 3: 638 1198 1318
 99
100 Optimal solution found (tolerance 1.00e-04)
101 Best objective 6.380000000000e+02, best bound 6.38000000000e+02, gap 0.0000%
102 Optimal Obj: 638.0
103 \text{ Obj} = 638.0
104 Solutions
105 Vessel i: 0:
                   li: 6,
                           pi: 8-14, ai-di: 2-23,
                                                  taoi-deltai: 2-25,
                                                                       periodi: 23,
                                                                                     taoPi_SP-deltaPi_SP: 2-8, periodPi: 6, betaNi: 14,
                                                                                                                                            bi: 23, Txijt
      : 138, o1i: 178, o2i: 120, o3i: -442, o4i: 280, Ti: 136
     Vessel i: 1: li: 7,
                          pi: 14-21,
                                                                                     taoPi_SP-deltaPi_SP: 8-11, periodPi: 3,
                                       ai-di: 8-17,
                                                     taoi-deltai: 8-16,
                                                                        periodi: 8,
                                                                                                                               betaNi: 4,
                                                                                                                                            bi: 8, Txijt:
     56, o1i: 56, o2i: 60, o3i: -135, o4i: 80,
                                                     Ti: 61
107 Vessel i: 2: li: 7,
                         pi: 7-14, ai-di: 34-42,
                                                     taoi-deltai: 34-41,
                                                                         periodi: 7,
                                                                                      taoPi_SP-deltaPi_SP: 34-36,
                                                                                                                    periodPi: 2,
                                                                                                                                  betaNi: 4,
                                                                                                                                              bi: 7,
     Txijt: 49, o1i: 49,
                          o2i: 40, o3i: -135, o4i: 80, Ti: 34
     Vessel i: 3:
                 li: 7,
                           pi: 17-24, ai-di: 40-58, taoi-deltai: 40-56,
                                                                                        taoPi_SP-deltaPi_SP: 40-46,
                                                                          periodi: 16,
                                                                                                                      periodPi: 6,
                                                                                                                                    betaNi: 9,
                                                                                                                                                bi: 16,
     Txijt: 112,
                  o1i: 112, o2i: 120, o3i: -270, o4i: 180, Ti: 142
     Vessel i: 4:
                  li: 6, pi: 11-17,
                                      ai-di: 47-59,
                                                      taoi-deltai: 47-60,
                                                                          periodi: 13,
                                                                                        taoPi_SP-deltaPi_SP: 47-52,
                                                                                                                      periodPi: 5,
                                                                                                                                    betaNi: 8,
                                                                                                                                                 bi: 13,
     Txijt: 78, o1i: 98, o2i: 100, o3i: -208, o4i: 160, Ti: 150
                          pi: 27-34, ai-di: 50-67, taoi-deltai: 50-69,
                 li: 7,
110 Vessel i: 5:
                                                                                        taoPi_SP-deltaPi_SP: 50-55,
                                                                          periodi: 19,
                                                                                                                      periodPi: 5,
                                                                                                                                    betaNi: 11.
                                                                                                                                                  bi: 19
        Txijt: 133, o1i: 173, o2i: 100, o3i: -378, o4i: 220, Ti: 115
     TimeSolveModel: 50.000000
112
113
115 TimeAll: 54.000000
116
117
118
119
```