```
this paper\Scripts\python.exe" "D:\Python\Pycharm\setroute\PyCharm Community Edition 2021.2.3\plugins\python-ce\helpers\pydev\pydevconsole.py" --mode=
     client --port=5243
     import sys; print('Python %s on %s' % (sys.version, sys.platform))
     sys.path.extend(|'E:\\1 000\\3 0000\\1 00000\\1 000000\\1 00000\\1 LW 0000\\4 0000\\3 python code\\9 Code for this
     6
     PyDev console: starting.
     Python 3.9.7 (tags/v3.9.7:1016ef3, Aug 30 2021, 20:19:38) [MSC v.1929 64 bit (AMD64)] on win32
 8
     >>> runfile('E:/1 000/3 0000/1 00000/1 00000/1 00000/1 00000/1 LW_000/4 000/3 python_code/9 Code for this paper/main_RO_CCG.py', wdir='E:/1 0000/3 0000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 000000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 000000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00
     this paper')
10 Backend TkAgg is interactive backend. Turning interactive mode on.
     Waiting 5s....
     Set parameter MIPGap to value 1e-10
12
     Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
13
15
     CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
     Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
16
17
     Optimize a model with 375969 rows, 34789 columns and 1042007 nonzeros
19
     Model fingerprint: 0x36dd4b10
     Variable types: 1 continuous, 34788 integer (34764 binary)
20
21 Coefficient statistics:
      Matrix range [1e+00, 1e+10]
       Objective range [1e+00, 2e+01]
23
24
       Bounds range [1e+00, 1e+00]
                            [1e+00, 2e+10]
       RHS range
26
      Warning: Model contains large matrix coefficients
27
     Warning: Model contains large rhs
28
             Consider reformulating model or setting NumericFocus parameter
29
             to avoid numerical issues.
30
     Presolve removed 326897 rows and 23704 columns
31
     Presolve time: 4.77s
     Presolved: 49072 rows, 11085 columns, 174856 nonzeros
33
     Variable types: 0 continuous, 11085 integer (11070 binary)
34
35
     Deterministic concurrent LP optimizer: primal and dual simplex (primal and dual model)
     Showing first log only...
37
38
     Root relaxation presolved: 49072 rows, 11085 columns, 174856 nonzeros
39
40
     Concurrent spin time: 0.02s
41
42
     Solved with dual simplex (primal model)
43
44
     Root relaxation: objective 6.660000e+02, 1309 iterations, 0.16 seconds (0.16 work units)
45
46
         Nodes | Current Node | Objective Bounds
47
      Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
48
49
         0 0 666.00000 0 3
                                                   - 666.00000
50 H 0 0
                                   1106.0000000 666.00000 39.8%
51 H 0
                                    666.0000000 666.00000 0.00%
52
53
     Cutting planes:
54
       Gomory: 1
55
       Cover: 1
       StrongCG: 1
56
57
       GUB cover: 1
58
       RLT: 2
59
60
     Explored 1 nodes (2694 simplex iterations) in 5.72 seconds (10.09 work units)
     Thread count was 8 (of 8 available processors)
62
     Solution count 2: 666 1106
63
64
65
     Optimal solution found (tolerance 1.00e-10)
     Best objective 6.660000000000e+02, best bound 6.66000000000e+02, gap 0.0000%
66
67
     Set parameter MIPGap to value 1e-08
     Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
68
70 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
     Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
73
     Optimize a model with 1153692 rows, 901813 columns and 7829319 nonzeros
     Model fingerprint: 0x8c49f5d5
74
     Variable types: 441325 continuous, 460488 integer (456438 binary)
76
     Coefficient statistics:
       Matrix range [1e-01, 1e+10]
78
       Objective range [6e-05, 5e+01]
                             [1e+00, 8e+01]
79
       Bounds range
```

```
RHS range
                   [8e-01, 1e+10]
 80
 81
    Warning: Model contains large matrix coefficients
    Warning: Model contains large rhs
 82
 83
         Consider reformulating model or setting NumericFocus parameter
         to avoid numerical issues.
 85 Presolve removed 1152265 rows and 901330 columns
 86 Presolve time: 2.66s
 87 Presolved: 1427 rows, 483 columns, 3802 nonzeros
    Variable types: 0 continuous, 483 integer (274 binary)
 89 Found heuristic solution: objective 2803.6666667
 90
 91
    Root relaxation: objective 3.220667e+03, 293 iterations, 0.00 seconds (0.00 work units)
 92
 93
      Nodes | Current Node | Objective Bounds
                                                     Work
 94
     Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
                        3220.6666667 6180.66667 91.9% - 3s
 96 H 0 0
 97
                  - 0 3220.66667 3220.66667 0.00% - 3s
       0 0
 98
 99 Explored 1 nodes (445 simplex iterations) in 3.39 seconds (3.65 work units)
100 Thread count was 8 (of 8 available processors)
101
102 Solution count 2: 3220.67 2803.67
103
104 Optimal solution found (tolerance 1.00e-08)
105 Best objective 3.220666666667e+03, best bound 3.220666666667e+03, gap 0.0000%
106 SP is solved
107 SP's optimal solution is' □ 3220
108
109 	 Itr = 0
110 Collect LB = [666.0]
111 Collect_UB = [7107.33333333333285]
112 Collect_Hua = [0.0]
113 Collect_SPObjVal = [3220.666666666642]
114 Collect MPObjValNHua = [666.0]
115
116
117 Set parameter MIPGap to value 0.05
118 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
119
120 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
121 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
122
123 Optimize a model with 634702 rows, 150727 columns and 1865101 nonzeros
124 Model fingerprint: 0xda7a6469
125 Variable types: 1 continuous, 150726 integer (143124 binary)
126 Coefficient statistics:
127
     Matrix range [1e-01, 1e+10]
128 Objective range [1e+00, 2e+01]
     Bounds range [1e+00, 1e+00]
129
130
     RHS range
                   [1e+00, 2e+10]
131 Warning: Model contains large matrix coefficients
132 Warning: Model contains large rhs
133
         Consider reformulating model or setting NumericFocus parameter
134
         to avoid numerical issues.
135 Presolve removed 547726 rows and 138921 columns (presolve time = 5s) ...
136 Presolve removed 591872 rows and 143227 columns
137 Presolve time: 6.19s
138 Presolved: 42830 rows, 7500 columns, 132585 nonzeros
139 Variable types: 0 continuous, 7500 integer (6236 binary)
140 Root relaxation presolved: 7500 rows, 50330 columns, 140085 nonzeros
141
142
143 Root simplex log...
144
145 Iteration Objective
                         Primal Inf. Dual Inf.
146
            handle free variables
       7587 4.0666667e+03 0.000000e+00 0.000000e+00
147
148
      7587 4.0666667e+03 0.000000e+00 0.000000e+00
149
150 Root relaxation: objective 4.066667e+03, 7587 iterations, 0.81 seconds (1.22 work units)
151
152
       Nodes | Current Node | Objective Bounds | Work
153
     Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
154
155
           0\ 4066.66667 \quad 0 \quad 74
                                    - 4066.66667
156
           0 4066.66667 0 102
                                    - 4066.66667
157
       0 0 4066.66667 0 63
                                    - 4066.66667
                                                   - - 8s
158 H 0 0
                       4686.6666667 4066.66667 13.2% - 9s
       0 0 4066.66667 0 4 4686.66667 4066.66667 13.2%
159
                     0 4066.6666667 4066.66667 0.00%
160 *
       0 0
161
162 Cutting planes:
163
     Learned: 15
```

```
unknown
164
      Gomory: 14
165
      Cover: 250
      Implied bound: 108
166
167
      Clique: 1026
      MIR: 201
168
169
      StrongCG: 56
170
     Flow cover: 2
171
      GUB cover: 294
      Zero half: 18
172
      RLT: 9
173
      Relax-and-lift: 188
174
175
      BQP: 7
176
177 Explored 1 nodes (20003 simplex iterations) in 10.10 seconds (17.19 work units)
178 Thread count was 8 (of 8 available processors)
180 Solution count 2: 4066.67 4686.67
181
182 Optimal solution found (tolerance 5.00e-02)
183 Best objective 4.0666666666667e+03, best bound 4.06666666667e+03, gap 0.0000%
184 Set parameter MIPGap to value 1e-08
185 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
186
187 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
188 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
189
190 Optimize a model with 1153692 rows, 901813 columns and 7829319 nonzeros
191 Model fingerprint: 0x5e3e0d87
192 Variable types: 441325 continuous, 460488 integer (456438 binary)
193 Coefficient statistics:
194
     Matrix range [1e-01, 1e+10]
195 Objective range [6e-05, 5e+01]
196 Bounds range [1e+00, 8e+01]
197
      RHS range
                    [8e-01, 1e+10]
198 Warning: Model contains large matrix coefficients
199 Warning: Model contains large rhs
200
          Consider reformulating model or setting NumericFocus parameter
201
          to avoid numerical issues.
202 Presolve removed 1151411 rows and 901028 columns
203 Presolve time: 2.58s
204 Presolved: 2281 rows, 785 columns, 6036 nonzeros
205 Variable types: 4 continuous, 781 integer (448 binary)
206 Found heuristic solution: objective 2808.3818887
207
208 Root relaxation: objective 3.722667e+03, 644 iterations, 0.00 seconds (0.00 work units)
209
210
       Nodes | Current Node | Objective Bounds

↓ Work

211
     Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
212
        0 0 3722.66667 0 14 2808.38189 3722.66667 32.6% - 3s
213
214 H 0 0
                         2918.6666667 3722.66667 27.5% - 3s
215 H 0 0
                        3252.6666667 3722.66667 14.4%
       0 0 3722.66667 0 4 3252.66667 3722.66667 14.4% - 3s
216
                       3722.6666667 3722.66667 0.00% - 3s
217 H 0 0
218
       0 0 3722.66667 0 4 3722.66667 3722.66667 0.00% -
219
220 Cutting planes:
221
      Gomory: 1
222
      Clique: 4
223
      RLT: 1
224
225 Explored 1 nodes (939 simplex iterations) in 3.48 seconds (3.21 work units)
226 Thread count was 8 (of 8 available processors)
227
228 Solution count 4: 3722.67 3252.67 2918.67 2808.38
229
230 Optimal solution found (tolerance 1.00e-08)
231 Best objective 3.722666666667e+03, best bound 3.722666666667e+03, gap 0.0000%
232 SP is solved
233 SP's optimal solution is'□3722
234
235
     Itr = 1
236 Collect LB = [666.0, 4066.666666666642]
237 Collect_UB = [7107.333333333285, 4568.666666666664]
238 Collect_Hua = [0.0, 3220.666666666642]
239 Collect_SPObjVal = [3220.66666666642, 3722.666666666642]
240 Collect_MPObjValNHua = [666.0, 846.0]
241
242
243 Set parameter MIPGap to value 0.05
244 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
245
246 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
     Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
247
```

```
248
249 Optimize a model with 887260 rows, 163849 columns and 2682005 nonzeros
250 Model fingerprint: 0x928f4c29
251 Variable types: 1 continuous, 163848 integer (148668 binary)
252 Coefficient statistics:
253
     Matrix range [1e-01, 1e+10]
254
     Objective range [1e+00, 2e+01]
255 Bounds range [1e+00, 1e+00]
256
     RHS range
                   [1e+00, 2e+10]
     Warning: Model contains large matrix coefficients
257
258 Warning: Model contains large rhs
259
          Consider reformulating model or setting NumericFocus parameter
260
          to avoid numerical issues.
261 Presolve removed 791336 rows and 149706 columns (presolve time = 5s) ...
262 Presolve removed 829808 rows and 153437 columns
263 Presolve time: 9.15s
264 Presolved: 57452 rows, 10412 columns, 193926 nonzeros
265 Variable types: 0 continuous, 10412 integer (7900 binary)
266
267 Deterministic concurrent LP optimizer: primal and dual simplex (primal and dual model)
268 Showing first log only...
269
270 Root relaxation presolved: 10412 rows, 67864 columns, 204338 nonzeros
271
272
273 Root simplex log...
274
275 Iteration Objective
                           Primal Inf. Dual Inf.
                                                   Time
276
        0 4.5686667e+03 0.000000e+00 2.884902e+04
277 Concurrent spin time: 0.04s
278
279 Solved with dual simplex (primal model)
280
281 Root relaxation: objective 4.568667e+03, 4742 iterations, 0.51 seconds (0.47 work units)
282
283

↓ Work

       Nodes | Current Node | Objective Bounds
284
     Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
285
286
       0
           0.4568.66667 0 71
                                     - 4568.66667
                                                    - - 10s
287
       0
           0 4568.66667 0 421
                                     - 4568.66667
                                                    - - 13s
288
           0 4568.66667 0 405
                                     - 4568.66667
                                                    - - 13s
289
       0
           0 4568.66667 0 19
                                     - 4568.66667
                                                    - - 15s
- - 16s
           0 4568.66667 0 206
290
       0
                                     - 4568,66667
291 H 0
            0
                        4648.6666667 4568.66667 1.72% - 17s
292
293 Cutting planes:
294
     Learned: 8
295
      Gomory: 14
296
     Lift-and-project: 2
297
      Cover: 296
298
      Implied bound: 176
299
      Clique: 1663
300
      MIR: 185
301
      StrongCG: 23
302
      Flow cover: 247
303
      GUB cover: 22
304
      Zero half: 36
305
      RLT: 57
306
      Relax-and-lift: 331
307
      BQP: 12
308
      PSD: 2
309
310 Explored 1 nodes (26421 simplex iterations) in 17.40 seconds (26.25 work units)
311 Thread count was 8 (of 8 available processors)
312
313 Solution count 1: 4648.67
314
315 Optimal solution found (tolerance 5.00e-02)
316 Best objective 4.64866666667e+03, best bound 4.568666666667e+03, gap 1.7209%
317 Warning: linear constraint 382145 and linear constraint 634703 have the same name "ConSP25_1[0,0]"
318 Set parameter MIPGap to value 1e-08
319 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
320
321 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
322 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
323
324 Optimize a model with 1153692 rows, 901813 columns and 7829319 nonzeros
325 Model fingerprint: 0x0eda2133
326 Variable types: 441325 continuous, 460488 integer (456438 binary)
327 Coefficient statistics:
328
     Matrix range [1e-01, 1e+10]
329
      Objective range [6e-05, 5e+01]
      Bounds range [1e+00, 8e+01]
330
331
      RHS range
                    [8e-01, 1e+10]
```

```
332 Warning: Model contains large matrix coefficients
333 Warning: Model contains large rhs
          Consider reformulating model or setting NumericFocus parameter
334
335
          to avoid numerical issues.
336 Presolve removed 1151297 rows and 901015 columns
337 Presolve time: 2.39s
338 Presolved: 2395 rows, 798 columns, 6324 nonzeros
339 Variable types: 4 continuous, 794 integer (449 binary)
340 Found heuristic solution: objective 2907.9278404
341
Root relaxation: objective 3.722667e+03, 524 iterations, 0.00 seconds (0.00 work units)
343
344
       Nodes | Current Node | Objective Bounds
345 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
346
347 H 0 0
                         3722.6666667 9040.00000 143% - 3s
348
       0 0
                  - 0
                         3722.66667 3722.66667 0.00% - 3s
349
350 Explored 1 nodes (722 simplex iterations) in 3.17 seconds (3.20 work units)
351 Thread count was 8 (of 8 available processors)
352
353 Solution count 2: 3722.67 2907.93
354
355 Optimal solution found (tolerance 1.00e-08)
356 Best objective 3.722666666667e+03, best bound 3.722666666667e+03, gap 0.0000%
357 SP is solved
358 SP's optimal solution is'□3722
359
360 	 Itr = 2
361 Collect_LB = [666.0, 4066.66666666642, 4648.66666666664]
362 Collect_UB = [7107.3333333333333285, 4568.66666666664, 4568.66666666664]
363 Collect Hua = [0.0, 3220.66666666642, 3722.66666666642]
364 Collect_SPObjVal = [3220.666666666642, 3722.66666666642, 3722.66666666642]
365 Collect_MPObjValNHua = [666.0, 846.0, 926.0]
366
367
368
     Ops, stop iteration
369
     Values adopted from the Itr-1' th iteration, and Itr = \{2\}, judgeCount = \{1\}
370
371
                ~judgeCount = 1, SPObj_SPF = 3722.666666666642
372 Vessel i: 0:
                             ai-di: 2-23,
                                           gi_SP-gpi_SP: 0.000000-0.000000,
                                                                               ai_SP-di: 2-23,
                                                                                                taoi-deltai: 2-25,
                                                                                                                   taoPi_SP-deltaPi_SP: 2-25,
                  pi: 14-20,
                                                                                                                                             betaNi: 23
        bi: 23
373
    Vessel i: 1:
                  pi: 7-14, ai-di: 8-17, gi_SP-gpi_SP: 0.000000-0.000000,
                                                                              ai_SP-di: 8-17, taoi-deltai: 8-16, taoPi_SP-deltaPi_SP: 8-16, betaNi: 8
        bi: 8
     Vessel i: 2:
                  pi: 7-14,
                             ai-di: 34-42,
                                           gi_SP-gpi_SP: 0.000000-0.000000,
                                                                               ai_SP-di: 34-42,
                                                                                                 taoi-deltai: 34-41,
                                                                                                                     taoPi_SP-deltaPi_SP: 34-41,
                                                                                                                                                  betaNi
     : 7, bi: 7
    Vessel i: 3:
                  pi: 16-23,
                              ai-di: 40-58,
                                            gi_SP-gpi_SP: 0.000000-0.000000,
                                                                                ai_SP-di: 40-58,
                                                                                                  taoi-deltai: 40-56,
                                                                                                                      taoPi_SP-deltaPi_SP: 40-56,
     betaNi: 16,
                  bi: 16
                  pi: 8-14,
    Vessel i: 4:
                             ai-di: 47-59,
                                           gi_SP-gpi_SP: 0.200000-1.000000,
                                                                               ai SP-di: 48-59,
                                                                                                 taoi-deltai: 48-61,
                                                                                                                     taoPi_SP-deltaPi_SP: 48-61,
                                                                                                                                                  betaNi
           bi: 13
     : 13.
     Vessel i: 5:
                  pi: 14-21, ai-di: 50-67, gi SP-gpi SP: 1.000000-0.200000,
                                                                                ai SP-di: 58-67,
                                                                                                  taoi-deltai: 58-77,
                                                                                                                    taoPi SP-deltaPi SP: 58-77,
                  bi: 19
     betaNi: 19,
378
379 round LB = [666, 4067, 4649]
380 round UB = [7107, 4569, 4569]
381 round Hua = [0, 3221, 3723]
382 round SPObjVal = [3221, 3723, 3723]
383 round MPObjValNHua = [666, 846, 926]
384
385 Time: 271.000000
386
387
388
389
```