


```

80  MIR: 49
81  StrongCG: 27
82  GUB cover: 8
83  Zero half: 2
84  RLT: 17
85  Relax-and-lift: 18
86  BQP: 9
87  PSD: 1
88
89  Explored 1 nodes (25963 simplex iterations) in 12.42 seconds (21.52 work units)
90  Thread count was 8 (of 8 available processors)
91
92  Solution count 8: 779 1439 1479 ... 5139
93
94  Optimal solution found (tolerance 1.00e-10)
95  Best objective 7.790000000000e+02, best bound 7.790000000000e+02, gap 0.0000%
96  Set parameter MIPGap to value 1e-08
97  Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
98
99  CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
100 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
101
102 Optimize a model with 1983368 rows, 1559473 columns and 13693931 nonzeros
103 Model fingerprint: 0x1ad678e8
104 Variable types: 766961 continuous, 792512 integer (787112 binary)
105 Coefficient statistics:
106   Matrix range    [1e-01, 1e+10]
107   Objective range [6e-05, 5e+01]
108   Bounds range    [1e+00, 8e+01]
109   RHS range       [8e-01, 1e+10]
110 Warning: Model contains large matrix coefficients
111 Warning: Model contains large rhs
112   Consider reformulating model or setting NumericFocus parameter
113   to avoid numerical issues.
114 Presolve removed 1981092 rows and 1558646 columns
115 Presolve time: 3.97s
116 Presolved: 2276 rows, 827 columns, 6068 nonzeros
117 Variable types: 6 continuous, 821 integer (486 binary)
118 Found heuristic solution: objective 3611.0215813
119
120 Root simplex log...
121
122 Iteration   Objective    Primal Inf.   Dual Inf.   Time
123      0    7.6070000e+03   2.825420e+03   0.000000e+00   5s
124     637   5.0405771e+03   0.000000e+00   0.000000e+00   5s
125
126 Root relaxation: objective 5.040577e+03, 637 iterations, 0.00 seconds (0.00 work units)
127
128   Nodes | Current Node | Objective Bounds | Work
129 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
130
131    0    0 5040.57714    0 8 3611.02158 5040.57714 39.6% - 5s
132 H  0    0           4980.5771368 5040.57714 1.20% - 5s
133 H  0    0           5010.5771368 5040.57714 0.60% - 5s
134 H  0    0           5028.5771368 5040.57714 0.24% - 5s
135 *  0    0           0 5040.5771368 5040.57714 0.00% - 5s
136
137 Cutting planes:
138 Gomory: 1
139 Cover: 4
140 Implied bound: 1
141 Clique: 9
142 MIR: 1
143 Zero half: 3
144 RLT: 2
145 Relax-and-lift: 2
146
147 Explored 1 nodes (982 simplex iterations) in 5.28 seconds (5.87 work units)
148 Thread count was 8 (of 8 available processors)
149
150 Solution count 5: 5040.58 5028.58 5010.58 ... 3611.02
151
152 Optimal solution found (tolerance 1.00e-08)
153 Best objective 5.040577136846e+03, best bound 5.040577136846e+03, gap 0.0000%
154 SP is solved
155 SP's optimal solution is'□5040
156
157 Itr = 0
158 Collect_LB = [779.0]
159 Collect_UB = [10860.154273692304]
160 Collect_Hua = [0.0]
161 Collect_SPObjVal = [5040.577136846152]
162 Collect_MPObjValNHua = [779.0]
163

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164
165 Set parameter MIPGap to value 0.05
166 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
167
168 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
169 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
170
171 Optimize a model with 978249 rows, 246921 columns and 2874075 nonzeros
172 Model fingerprint: 0x6669dd3c
173 Variable types: 1 continuous, 246920 integer (236784 binary)
174 Coefficient statistics:
175   Matrix range    [1e-01, 1e+10]
176   Objective range [1e+00, 2e+01]
177   Bounds range    [1e+00, 1e+00]
178   RHS range       [1e+00, 2e+10]
179 Warning: Model contains large matrix coefficients
180 Warning: Model contains large rhs
181   Consider reformulating model or setting NumericFocus parameter
182   to avoid numerical issues.
183 Presolve removed 814101 rows and 226888 columns (presolve time = 5s) ...
184 Presolve removed 888229 rows and 235283 columns (presolve time = 10s) ...
185 Presolve removed 901510 rows and 235288 columns
186 Presolve time: 10.72s
187 Presolved: 76739 rows, 11633 columns, 238449 nonzeros
188 Variable types: 1 continuous, 11632 integer (9629 binary)
189
190 Deterministic concurrent LP optimizer: primal and dual simplex (primal and dual model)
191 Showing first log only...
192
193 Root relaxation presolved: 11633 rows, 88372 columns, 250082 nonzeros
194
195
196 Root simplex log...
197
198 Iteration   Objective    Primal Inf.   Dual Inf.   Time
199      0   5.8395771e+03  0.000000e+00  1.706797e+04  11s
200 Concurrent spin time: 0.40s
201
202 Solved with dual simplex (primal model)
203
204 Root relaxation: objective 5.839577e+03, 5949 iterations, 1.30 seconds (1.91 work units)
205
206 Nodes | Current Node | Objective Bounds | Work
207 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
208
209 0 0 5839.57714 0 235 - 5839.57714 - - 14s
210 0 0 5839.57714 0 659 - 5839.57714 - - 15s
211 0 0 5839.57714 0 601 - 5839.57714 - - 16s
212 0 0 5839.57714 0 482 - 5839.57714 - - 16s
213 0 0 5839.57714 0 479 - 5839.57714 - - 16s
214 0 0 5839.57714 0 124 - 5839.57714 - - 20s
215 0 0 5839.57714 0 293 - 5839.57714 - - 21s
216 0 0 5839.57714 0 314 - 5839.57714 - - 21s
217 0 0 5839.57714 0 159 - 5839.57714 - - 25s
218 0 0 5839.57714 0 129 - 5839.57714 - - 26s
219 0 0 5839.57714 0 126 - 5839.57714 - - 26s
220 0 0 5839.57714 0 153 - 5839.57714 - - 29s
221 0 0 5839.57714 0 115 - 5839.57714 - - 29s
222 0 0 5839.57714 0 269 - 5839.57714 - - 29s
223 0 0 5839.57714 0 117 - 5839.57714 - - 31s
224 0 0 5839.57714 0 100 - 5839.57714 - - 31s
225 0 0 5839.57714 0 233 - 5839.57714 - - 32s
226 0 0 5839.57714 0 126 - 5839.57714 - - 33s
227 0 0 5839.57714 0 246 - 5839.57714 - - 34s
228 0 0 5839.57714 0 241 - 5839.57714 - - 34s
229 0 0 5839.57714 0 63 - 5839.57714 - - 35s
230 0 0 5839.57714 0 70 - 5839.57714 - - 35s
231 0 0 5839.57714 0 131 - 5839.57714 - - 36s
232 0 0 5839.57714 0 67 - 5839.57714 - - 37s
233 0 2 5839.57714 0 67 - 5839.57714 - - 40s
234 19 22 6008.46603 5 389 - 5839.57714 - - 1744 45s
235 41 41 6039.57714 11 146 - 5839.57714 - - 1615 50s
236 61 60 6039.57714 17 168 - 5839.57714 - - 1471 55s
237 112 117 6039.57714 26 310 - 5839.57714 - - 1064 60s
238 223 224 6039.57714 34 306 - 5839.57714 - - 696 66s
239 340 314 6039.57714 54 276 - 5839.57714 - - 512 70s
240 686 705 6039.57714 94 197 - 5839.57714 - - 294 76s
241 967 850 6039.57714 137 238 - 5839.57714 - - 228 80s
242 1163 1106 6039.57714 172 254 - 5839.57714 - - 226 86s
243 * 1470 499 80 5839.5771368 5839.57714 0.00% 200 89s
244
245 Cutting planes:
246 Learned: 15
247 Gomory: 2

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248 Cover: 519
249 Implied bound: 441
250 Clique: 123
251 MIR: 102
252 StrongCG: 49
253 Flow cover: 11
254 GUB cover: 307
255 Zero half: 22
256 RLT: 78
257 Relax-and-lift: 232
258 BQP: 17
259
260 Explored 1694 nodes (432903 simplex iterations) in 89.69 seconds (218.45 work units)
261 Thread count was 8 (of 8 available processors)
262
263 Solution count 1: 5839.58
264
265 Optimal solution found (tolerance 5.00e-02)
266 Best objective 5.839577136846e+03, best bound 5.839577136846e+03, gap 0.0000%
267 Set parameter MIPGap to value 1e-08
268 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
269
270 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
271 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
272
273 Optimize a model with 1983368 rows, 1559473 columns and 13693931 nonzeros
274 Model fingerprint: 0x4b2e84e9
275 Variable types: 766961 continuous, 792512 integer (787112 binary)
276 Coefficient statistics:
277   Matrix range    [1e-01, 1e+10]
278   Objective range [6e-05, 5e+01]
279   Bounds range    [1e+00, 8e+01]
280   RHS range       [8e-01, 1e+10]
281 Warning: Model contains large matrix coefficients
282 Warning: Model contains large rhs
283   Consider reformulating model or setting NumericFocus parameter
284   to avoid numerical issues.
285 Presolve removed 1978553 rows and 1557793 columns
286 Presolve time: 3.84s
287 Presolved: 4815 rows, 1680 columns, 12856 nonzeros
288 Variable types: 6 continuous, 1674 integer (967 binary)
289 Found heuristic solution: objective 3627.0215813
290
291 Root relaxation: objective 5.338777e+03, 1290 iterations, 0.01 seconds (0.01 work units)
292
293   Nodes | Current Node | Objective Bounds | Work
294 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
295
296   0   0 5338.77678   0 48 3627.02158 5338.77678 47.2% - 4s
297 H  0   0           5104.0843674 5338.77678 4.60% - 4s
298 H  0   0           5328.4064055 5338.77678 0.19% - 4s
299   0   0 cutoff   0   5328.40641 5328.40641 0.00% - 4s
300
301 Cutting planes:
302 Gomory: 2
303 Cover: 1
304 Clique: 9
305 Zero half: 7
306 RLT: 1
307
308 Explored 1 nodes (2068 simplex iterations) in 5.14 seconds (5.66 work units)
309 Thread count was 8 (of 8 available processors)
310
311 Solution count 3: 5328.41 5104.08 3627.02
312
313 Optimal solution found (tolerance 1.00e-08)
314 Best objective 5.328406405495e+03, best bound 5.328406405495e+03, gap 0.0000%
315 SP is solved
316 SP's optimal solution is' □ 5328
317
318 Itr = 1
319 Collect_LB = [779.0, 5839.577136846152]
320 Collect_UB = [10860.154273692304, 6127.40640549518]
321 Collect_Hua = [0.0, 5040.577136846152]
322 Collect_SPObjVal = [5040.577136846152, 5328.40640549518]
323 Collect_MPObjValNHua = [779.0, 799.0]
324
325
326 Set parameter MIPGap to value 0.05
327 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
328
329 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
330 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
331

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332 Optimize a model with 1408285 rows, 264417 columns and 4243829 nonzeros
333 Model fingerprint: 0x3c12c4ec
334 Variable types: 1 continuous, 264416 integer (244176 binary)
335 Coefficient statistics:
336   Matrix range   [1e-01, 1e+10]
337   Objective range [1e+00, 2e+01]
338   Bounds range   [1e+00, 1e+00]
339   RHS range      [1e+00, 2e+10]
340 Warning: Model contains large matrix coefficients
341 Warning: Model contains large rhs
342   Consider reformulating model or setting NumericFocus parameter
343   to avoid numerical issues.
344 Presolve removed 1198810 rows and 238844 columns (presolve time = 5s) ...
345 Presolve removed 1230112 rows and 241557 columns (presolve time = 10s) ...
346 Presolve removed 1295650 rows and 248172 columns (presolve time = 15s) ...
347 Presolve removed 1295686 rows and 248177 columns
348 Presolve time: 15.88s
349 Presolved: 112599 rows, 16240 columns, 370426 nonzeros
350 Variable types: 1 continuous, 16239 integer (12268 binary)
351
352 Deterministic concurrent LP optimizer: primal and dual simplex (primal and dual model)
353 Showing first log only...
354
355 Root relaxation presolved: 16240 rows, 128839 columns, 386666 nonzeros
356
357
358 Root simplex log...
359
360 Iteration   Objective      Primal Inf.   Dual Inf.    Time
361      0  6.1274064e+03  0.000000e+00  4.055143e+04  17s
362  15632  6.1274064e+03  0.000000e+00  0.000000e+00  18s
363  15632  6.1274064e+03  0.000000e+00  0.000000e+00  18s
364 Concurrent spin time: 0.26s
365
366 Solved with primal simplex
367
368 Root relaxation: objective 6.127406e+03, 15632 iterations, 2.14 seconds (2.98 work units)
369 Total elapsed time = 20.56s
370
371   Nodes | Current Node | Objective Bounds | Work
372 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
373
374   0   0 6127.40641   0 490    - 6127.40641   -   - 22s
375   0   0 6127.40641   0 766    - 6127.40641   -   - 26s
376   0   0 6127.40641   0 663    - 6127.40641   -   - 26s
377   0   0 6127.40641   0 746    - 6127.40641   -   - 28s
378   0   0 6127.40641   0 752    - 6127.40641   -   - 28s
379   0   0 6127.40641   0 478    - 6127.40641   -   - 37s
380   0   0 6127.40641   0 510    - 6127.40641   -   - 38s
381   0   0 6127.40641   0 200    - 6127.40641   -   - 44s
382   0   0 6127.40641   0 221    - 6127.40641   -   - 44s
383   0   0 6127.40641   0 265    - 6127.40641   -   - 45s
384   0   0 6127.40641   0 261    - 6127.40641   -   - 52s
385   0   0 6127.40641   0 496    - 6127.40641   -   - 53s
386   0   0 6127.40641   0 425    - 6127.40641   -   - 53s
387   0   0 6127.40641   0 229    - 6127.40641   -   - 59s
388   0   0 6127.40641   0 202    - 6127.40641   -   - 59s
389   0   0 6127.40641   0 202    - 6127.40641   -   - 61s
390   0   2 6127.40641   0 202    - 6127.40641   -   - 72s
391   3   8 6127.40641   2 490    - 6127.40641   - 4980 76s
392  11  15 6127.40641   3 628    - 6127.40641   - 4053 80s
393  23  29 6127.40641   5 519    - 6127.40641   - 3005 85s
394  36  43 6127.40641   8 500    - 6127.40641   - 2271 92s
395  43  68 6127.40641  11 288    - 6127.40641   - 3141 100s
396  71 125 6127.40641  23 319    - 6127.40641   - 2830 113s
397 149 272 6127.40641  67 132    - 6127.40641   - 2090 132s
398 * 231 272      141 6127.4064055 6127.40641 0.00% 1412 132s
399
400 Cutting planes:
401   Learned: 29
402   Gomory: 3
403   Lift-and-project: 1
404   Cover: 587
405   Implied bound: 1348
406   Clique: 3610
407   MIR: 266
408   StrongCG: 100
409   Flow cover: 48
410   GUB cover: 82
411   Zero half: 44
412   RLT: 112
413   Relax-and-lift: 483
414   BQP: 24
415   PSD: 6

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416
417 Explored 370 nodes (609654 simplex iterations) in 132.52 seconds (380.88 work units)
418 Thread count was 8 (of 8 available processors)
419
420 Solution count 1: 6127.41
421
422 Optimal solution found (tolerance 5.00e-02)
423 Best objective 6.127406405495e+03, best bound 6.127406405495e+03, gap 0.0000%
424 Warning: linear constraint 548214 and linear constraint 978250 have the same name "ConSP25_1[0,0]"
425 Set parameter MIPGap to value 1e-08
426 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
427
428 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
429 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
430
431 Optimize a model with 1983368 rows, 1559473 columns and 13693931 nonzeros
432 Model fingerprint: 0x464f5980
433 Variable types: 766961 continuous, 792512 integer (787112 binary)
434 Coefficient statistics:
435   Matrix range    [1e-01, 1e+10]
436   Objective range [6e-05, 5e+01]
437   Bounds range    [1e+00, 8e+01]
438   RHS range       [8e-01, 1e+10]
439 Warning: Model contains large matrix coefficients
440 Warning: Model contains large rhs
441   Consider reformulating model or setting NumericFocus parameter
442   to avoid numerical issues.
443 Presolve removed 1978600 rows and 1557844 columns
444 Presolve time: 3.85s
445 Presolved: 4768 rows, 1629 columns, 12720 nonzeros
446 Variable types: 6 continuous, 1623 integer (941 binary)
447 Found heuristic solution: objective 3738.9989981
448
449 Root relaxation: objective 5.343111e+03, 1303 iterations, 0.02 seconds (0.01 work units)
450
451   Nodes | Current Node | Objective Bounds | Work
452   Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
453
454   0   0 5343.11111  0  8 3738.99900 5343.11111 42.9% - 4s
455 H  0   0          5343.111111 5343.11111 0.00% - 4s
456   0   0 5343.11111  0  8 5343.11111 5343.11111 0.00% - 4s
457
458 Explored 1 nodes (1836 simplex iterations) in 5.09 seconds (5.62 work units)
459 Thread count was 8 (of 8 available processors)
460
461 Solution count 2: 5343.11 3739
462
463 Optimal solution found (tolerance 1.00e-08)
464 Best objective 5.343111111111e+03, best bound 5.343111111111e+03, gap 0.0000%
465 SP is solved
466 SP's optimal solution is'□5343
467
468   Itr = 2
469 Collect_LB = [779.0, 5839.577136846152, 6127.40640549518]
470 Collect_UB = [10860.154273692304, 6127.40640549518, 6127.40640549518]
471 Collect_Hua = [0.0, 5040.577136846152, 5328.40640549518]
472 Collect_SPObjVal = [5040.577136846152, 5328.40640549518, 5343.111111111111]
473 Collect_MPObjValNHua = [779.0, 799.0, 799.0]
474
475
476 Reach the termination conditions, stop iteration
477 Values adopted from the Itr' th iteration, and Itr = {2}, judgeCount = {2}
478
479 Values adopted from the judgeCount's th iteration, and Itr = {2}, judgeCount = {2}
480
481 Values adopted from the judgeCount's th iteration, and Itr = {2}, judgeCount = {1}
482
483 ~~~~~judgeCount = 1, SPObj_SPF = 5328.40640549518
484 Vessel i: 0:   pi: 0-6,   ai-di: 1-20,   gi_SP-gpi_SP: 0.000000-0.000000,   ai_SP-di: 1-20,   taoi-delta: 1-19,   taoPi_SP-deltaPi_SP: 1-19,   betaNi: 18
,   bi: 18
485 Vessel i: 1:   pi: 6-11,   ai-di: 7-14,   gi_SP-gpi_SP: 0.000000-0.000000,   ai_SP-di: 7-14,   taoi-delta: 7-12,   taoPi_SP-deltaPi_SP: 7-12,   betaNi: 5
,   bi: 5
486 Vessel i: 2:   pi: 19-26,   ai-di: 4-30,   gi_SP-gpi_SP: 0.000000-0.000000,   ai_SP-di: 4-30,   taoi-delta: 4-28,   taoPi_SP-deltaPi_SP: 4-28,   betaNi: 24
,   bi: 24
487 Vessel i: 3:   pi: 11-17,   ai-di: 7-20,   gi_SP-gpi_SP: 0.000000-0.000000,   ai_SP-di: 7-20,   taoi-delta: 7-18,   taoPi_SP-deltaPi_SP: 7-18,   betaNi: 11
,   bi: 11
488 Vessel i: 4:   pi: 10-16,   ai-di: 31-44,   gi_SP-gpi_SP: 0.000000-0.000000,   ai_SP-di: 31-44,   taoi-delta: 31-42,   taoPi_SP-deltaPi_SP: 31-42,
betaNi: 11,
bi: 11
489 Vessel i: 5:   pi: 10-15,   ai-di: 21-43,   gi_SP-gpi_SP: 0.000000-0.527349,   ai_SP-di: 21-43,   taoi-delta: 21-27,   taoPi_SP-deltaPi_SP: 21-27,
betaNi: 6,
bi: 6
490 Vessel i: 6:   pi: 10-17,   ai-di: 37-78,   gi_SP-gpi_SP: 1.000000-0.600000,   ai_SP-di: 45-78,   taoi-delta: 45-79,   taoPi_SP-deltaPi_SP: 45-79,
betaNi: 34,
bi: 34
491 Vessel i: 7:   pi: 21-27,   ai-di: 25-57,   gi_SP-gpi_SP: 0.800000-0.672651,   ai_SP-di: 33-57,   taoi-delta: 33-46,   taoPi_SP-deltaPi_SP: 33-46,
betaNi: 13,
bi: 13

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unknown

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492
493 round LB = [779, 5840, 6127]
494 round UB = [10860, 6127, 6127]
495 round Hua = [0, 5041, 5328]
496 round SPObjVal = [5041, 5328, 5343]
497 round MPObjValNHua = [779, 799, 799]
498
499 Time: 608.000000
500
501
502
503
```