


```

80  Clique: 4
81  MIR: 102
82  StrongCG: 56
83  GUB cover: 11
84  Zero half: 5
85  RLT: 10
86  Relax-and-lift: 612
87  BQP: 8
88
89  Explored 117 nodes (126391 simplex iterations) in 33.90 seconds (65.83 work units)
90  Thread count was 8 (of 8 available processors)
91
92  Solution count 5: 991 1311 2611 ... 6691
93
94  Optimal solution found (tolerance 1.00e-10)
95  Best objective 9.910000000000e+02, best bound 9.910000000000e+02, gap 0.0000%
96  Set parameter MIPGap to value 1e-08
97  Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
98
99  CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
100 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
101
102 Optimize a model with 654086 rows, 16030 columns and 1337366 nonzeros
103 Model fingerprint: 0x45aafa6f
104 Variable types: 40 continuous, 15990 integer (9240 binary)
105 Coefficient statistics:
106   Matrix range    [1e-01, 1e+10]
107   Objective range [6e-05, 5e+01]
108   Bounds range    [1e+00, 1e+00]
109   RHS range       [8e-01, 1e+10]
110 Warning: Model contains large matrix coefficients
111 Warning: Model contains large rhs
112   Consider reformulating model or setting NumericFocus parameter
113   to avoid numerical issues.
114 Presolve removed 650289 rows and 14621 columns
115 Presolve time: 0.56s
116 Presolved: 3797 rows, 1409 columns, 10130 nonzeros
117 Variable types: 10 continuous, 1399 integer (819 binary)
118 Found heuristic solution: objective 4594.6120144
119 Found heuristic solution: objective 4599.2524802
120
121 Root relaxation: objective 6.569244e+03, 1373 iterations, 0.02 seconds (0.01 work units)
122
123   Nodes | Current Node | Objective Bounds | Work
124   Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
125
126   0   0 6569.24444   0 33 4599.25248 6569.24444 42.8% - 0s
127 H  0   0           6539.4691941 6569.24444 0.46% - 0s
128 H  0   0           6546.4552604 6569.24444 0.35% - 0s
129 * 0   0           0 6566.4444444 6566.44444 0.00% - 0s
130
131 Cutting planes:
132   Learned: 1
133   Gomory: 5
134   Cover: 2
135   Implied bound: 3
136   MIR: 2
137   Flow cover: 4
138   RLT: 2
139   Relax-and-lift: 1
140   PSD: 1
141
142 Explored 1 nodes (1867 simplex iterations) in 0.78 seconds (1.03 work units)
143 Thread count was 8 (of 8 available processors)
144
145 Solution count 5: 6566.44 6546.46 6539.47 ... 4594.61
146
147 Optimal solution found (tolerance 1.00e-08)
148 Best objective 6.566444444444e+03, best bound 6.566444444444e+03, gap 0.0000%
149 SP is solved
150 SP's optimal solution is'□6566
151
152 Itr = 0
153 Collect_LB = [991.0]
154 Collect_UB = [14123.888888888883]
155 Collect_Hua = [0.0]
156 Collect_SPObjVal = [6566.444444444442]
157 Collect_MPObjValNHua = [991.0]
158
159
160 Set parameter MIPGap to value 1e-10
161 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
162
163 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]

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164 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
165
166 Optimize a model with 628195 rows, 344301 columns and 1747990 nonzeros
167 Model fingerprint: 0x0c2e46f6
168 Variable types: 1 continuous, 344300 integer (344260 binary)
169 Coefficient statistics:
170   Matrix range    [1e+00, 1e+10]
171   Objective range [1e+00, 2e+01]
172   Bounds range   [1e+00, 1e+00]
173   RHS range      [1e+00, 2e+10]
174 Warning: Model contains large matrix coefficients
175 Warning: Model contains large rhs
176   Consider reformulating model or setting NumericFocus parameter
177   to avoid numerical issues.
178 Presolve removed 471430 rows and 325200 columns (presolve time = 5s) ...
179 Presolve removed 578969 rows and 335642 columns
180 Presolve time: 9.16s
181 Presolved: 49226 rows, 8659 columns, 127720 nonzeros
182 Variable types: 0 continuous, 8659 integer (8636 binary)
183 Root relaxation presolved: 8659 rows, 57885 columns, 136379 nonzeros
184
185
186 Root simplex log...
187
188 Iteration   Objective    Primal Inf.   Dual Inf.    Time
189    0      handle free variables                10s
190  4785    8.7463773e+03  3.681598e+03  0.000000e+00  10s
191   7610    7.9174444e+03  0.000000e+00  0.000000e+00  11s
192   7610    7.9174444e+03  0.000000e+00  0.000000e+00  11s
193
194 Root relaxation: objective 7.917444e+03, 7610 iterations, 1.03 seconds (1.55 work units)
195
196   Nodes | Current Node | Objective Bounds | Work
197 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
198
199   0   0 7917.44444  0  45      -7917.44444  -  - 11s
200   0   0 7917.44444  0 198      -7917.44444  -  - 12s
201   0   0 7917.44444  0 162      -7917.44444  -  - 12s
202   0   0 7917.44444  0 377      -7917.44444  -  - 13s
203   0   0 7917.44444  0  27      -7917.44444  -  - 15s
204   0   0 7917.44444  0 238      -7917.44444  -  - 16s
205   0   0 7917.44444  0 131      -7917.44444  -  - 17s
206   0   0 7917.44444  0 130      -7917.44444  -  - 17s
207   0   0 7917.44444  0 250      -7917.44444  -  - 17s
208   0   0 7917.44444  0 154      -7917.44444  -  - 19s
209   0   0 7917.44444  0 248      -7917.44444  -  - 19s
210   0   0 7917.44444  0 245      -7917.44444  -  - 19s
211 H   0   0              7917.4444444 7917.44444 0.00%  - 21s
212   0   0 7917.44444  0 211 7917.44444 7917.44444 0.00%  - 21s
213
214 Cutting planes:
215   Learned: 4
216   Gomory: 3
217   Cover: 186
218   Implied bound: 1306
219   Clique: 443
220   MIR: 193
221   StrongCG: 125
222   GUB cover: 43
223   Zero half: 13
224   RLT: 35
225   Relax-and-lift: 104
226   BQP: 25
227
228 Explored 1 nodes (40537 simplex iterations) in 21.90 seconds (27.92 work units)
229 Thread count was 8 (of 8 available processors)
230
231 Solution count 1: 7917.44
232
233 Optimal solution found (tolerance 1.00e-10)
234 Best objective 7.91744444444e+03, best bound 7.91744444444e+03, gap 0.0000%
235 Set parameter MIPGap to value 1e-08
236 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
237
238 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
239 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
240
241 Optimize a model with 654086 rows, 16030 columns and 1337366 nonzeros
242 Model fingerprint: 0x81e05b7d
243 Variable types: 40 continuous, 15990 integer (9240 binary)
244 Coefficient statistics:
245   Matrix range    [1e-01, 1e+10]
246   Objective range [6e-05, 5e+01]
247   Bounds range    [1e+00, 1e+00]

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248 RHS range      [8e-01, 1e+10]
249 Warning: Model contains large matrix coefficients
250 Warning: Model contains large rhs
251     Consider reformulating model or setting NumericFocus parameter
252     to avoid numerical issues.
253 Presolve removed 647393 rows and 13825 columns
254 Presolve time: 0.50s
255 Presolved: 6693 rows, 2205 columns, 17882 nonzeros
256 Variable types: 10 continuous, 2195 integer (1261 binary)
257 Found heuristic solution: objective 4878.5754258
258
259 Root relaxation: objective 7.123111e+03, 1790 iterations, 0.02 seconds (0.02 work units)
260
261 Nodes | Current Node | Objective Bounds | Work
262 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
263
264 0 0 7123.11111 0 17 4878.57543 7123.11111 46.0% - 0s
265 H 0 0 7104.4444444 7123.11111 0.26% - 0s
266 * 0 0 0 7120.4444444 7120.44444 0.00% - 0s
267
268 Cutting planes:
269 Learned: 2
270 Gomory: 5
271 Cover: 1
272 Implied bound: 2
273 Flow cover: 3
274 Zero half: 1
275 RLT: 4
276 Relax-and-lift: 5
277 PSD: 1
278
279 Explored 1 nodes (2545 simplex iterations) in 0.77 seconds (1.06 work units)
280 Thread count was 8 (of 8 available processors)
281
282 Solution count 3: 7120.44 7104.44 4878.58
283
284 Optimal solution found (tolerance 1.00e-08)
285 Best objective 7.12044444444e+03, best bound 7.12044444444e+03, gap 0.0000%
286 SP is solved
287 SP's optimal solution is '7120
288
289 Itr = 1
290 Collect_LB = [991.0, 7917.444444444442]
291 Collect_UB = [14123.888888888883, 8471.444444444445]
292 Collect_Hua = [0.0, 6566.444444444442]
293 Collect_SPObjVal = [6566.444444444442, 7120.444444444445]
294 Collect_MPObjValNHua = [991.0, 1351.0]
295
296
297 Set parameter MIPGap to value 1e-10
298 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
299
300 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
301 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
302
303 Optimize a model with 628195 rows, 344301 columns and 1747990 nonzeros
304 Model fingerprint: 0x59b64541
305 Variable types: 1 continuous, 344300 integer (344260 binary)
306 Coefficient statistics:
307 Matrix range [1e+00, 1e+10]
308 Objective range [1e+00, 2e+01]
309 Bounds range [1e+00, 1e+00]
310 RHS range [1e+00, 2e+10]
311 Warning: Model contains large matrix coefficients
312 Warning: Model contains large rhs
313     Consider reformulating model or setting NumericFocus parameter
314     to avoid numerical issues.
315 Presolve removed 472886 rows and 325364 columns (presolve time = 5s) ...
316 Presolve removed 579366 rows and 335687 columns
317 Presolve time: 9.20s
318 Presolved: 48829 rows, 8614 columns, 126604 nonzeros
319 Variable types: 0 continuous, 8614 integer (8591 binary)
320 Root relaxation presolved: 8614 rows, 57443 columns, 135218 nonzeros
321
322
323 Root simplex log...
324
325 Iteration Objective Primal Inf. Dual Inf. Time
326 0 handle free variables 10s
327 5415 8.8213760e+03 1.846503e+03 0.000000e+00 10s
328 7450 8.5114444e+03 0.000000e+00 0.000000e+00 11s
329 7450 8.5114444e+03 0.000000e+00 0.000000e+00 11s
330
331 Root relaxation: objective 8.511444e+03, 7450 iterations, 1.08 seconds (1.56 work units)

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332
333   Nodes | Current Node | Objective Bounds | Work
334 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
335
336   0   0 8511.44444 0 48   -8511.44444 - - 11s
337   0   0 8511.44444 0 359 -8511.44444 - - 12s
338   0   0 8511.44444 0 371 -8511.44444 - - 12s
339   0   0 8511.44444 0 168 -8511.44444 - - 13s
340   0   0 8511.44444 0 198 -8511.44444 - - 13s
341   0   0 8511.44444 0 170 -8511.44444 - - 15s
342   0   0 8511.44444 0 211 -8511.44444 - - 16s
343   0   0 8511.44444 0 221 -8511.44444 - - 16s
344   0   0 8511.44444 0 404 -8511.44444 - - 17s
345   0   0 8511.44444 0 379 -8511.44444 - - 17s
346   0   0 8511.44444 0 250 -8511.44444 - - 23s
347   0   0 8511.44444 0 248 -8511.44444 - - 23s
348   0   0 8511.44444 0 562 -8511.44444 - - 24s
349   0   0 8511.44444 0 424 -8511.44444 - - 24s
350   0   0 8511.44444 0 421 -8511.44444 - - 24s
351   0   0 8511.44444 0 279 -8511.44444 - - 27s
352   0   0 8511.44444 0 109 -8511.44444 - - 27s
353   0   2 8511.44444 0 109 -8511.44444 - - 30s
354  15  18 8511.44444 5 429 -8511.44444 - 2420 35s
355  42  47 8518.40097 11 697 -8511.44444 - 2133 41s
356  61  62 8551.44444 13 852 -8511.44444 - 2035 45s
357  83  87 infeasible 21 -8511.44444 - 1874 50s
358  217 241 8831.44444 77 190 -8511.44444 - 1115 58s
359  320 352 8831.44444 128 192 -8511.44444 - 836 62s
360  561 573 8871.44444 256 193 -8511.44444 - 541 67s
361  723 611 8831.44444 4 438 -8511.44444 - 473 70s
362  887 753 infeasible 24 -8511.44444 - 430 76s
363  1077 952 8911.44444 20 399 -8511.44444 - 396 81s
364  1373 1259 8911.44444 230 148 -8511.44444 - 353 87s
365  1604 1415 8911.44444 252 260 -8511.44444 - 325 90s
366  1786 1416 8547.50078 56 109 -8511.44444 - 312 106s
367  1789 1418 8951.44444 257 223 -8511.44444 - 311 112s
368  1790 1419 8511.44444 7 439 -8511.44444 - 311 116s
369  1791 1419 9111.44444 480 375 -8511.44444 - 311 121s
370  1793 1421 8751.44444 162 597 -8511.44444 - 311 130s
371  1795 1422 9231.44444 42 317 -8511.44444 - 310 139s
372  1796 1423 8951.44444 572 716 -8511.44444 - 310 142s
373  1797 1423 8511.44444 22 507 -8511.44444 - 310 148s
374  1798 1424 8871.44444 353 999 -8511.44444 - 310 153s
375  1799 1425 9791.44444 181 665 -8511.44444 - 310 158s
376  1800 1425 8911.44444 295 904 -8511.44444 - 310 161s
377 H 1800 1353 8631.4444444 8511.44444 1.39% 310 169s
378  1802 1355 8591.44444 211 645 8631.44444 8511.44444 1.39% 309 172s
379  1805 1358 8552.62092 38 109 8631.44444 8511.44444 1.39% 385 176s
380  1810 1363 8631.44444 231 109 8631.44444 8511.44444 1.39% 389 181s
381  1813 1365 8631.44444 511 427 8631.44444 8511.44444 1.39% 388 185s
382  1816 1367 8631.44444 170 497 8631.44444 8511.44444 1.39% 388 190s
383 H 1818 1299 8591.4444444 8511.44444 0.93% 387 196s
384
385 Cutting planes:
386   Learned: 1
387   Gomory: 53
388   Cover: 175
389   Implied bound: 45
390   Projected implied bound: 9
391   Clique: 74
392   MIR: 54
393   StrongCG: 15
394   Flow cover: 117
395   GUB cover: 86
396   Zero half: 15
397   RLT: 60
398   Relax-and-lift: 98
399   BQP: 2
400
401 Explored 1818 nodes (810195 simplex iterations) in 196.21 seconds (299.91 work units)
402 Thread count was 8 (of 8 available processors)
403
404 Solution count 2: 8591.44 8631.44
405
406 Optimal solution found (tolerance 1.00e-10)
407 Best objective 8.591444444444e+03, best bound 8.591444444444e+03, gap 0.0000%
408 Set parameter MIPGap to value 1e-08
409 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
410
411 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
412 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
413
414 Optimize a model with 654086 rows, 16030 columns and 1337366 nonzeros
415 Model fingerprint: 0xba419400

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416 Variable types: 40 continuous, 15990 integer (9240 binary)
417 Coefficient statistics:
418   Matrix range   [1e-01, 1e+10]
419   Objective range [6e-05, 5e+01]
420   Bounds range   [1e+00, 1e+00]
421   RHS range      [8e-01, 1e+10]
422 Warning: Model contains large matrix coefficients
423 Warning: Model contains large rhs
424   Consider reformulating model or setting NumericFocus parameter
425   to avoid numerical issues.
426 Presolve removed 647707 rows and 13921 columns
427 Presolve time: 0.50s
428 Presolved: 6379 rows, 2109 columns, 17146 nonzeros
429 Variable types: 10 continuous, 2099 integer (1212 binary)
430 Found heuristic solution: objective 4929.7421607
431 Found heuristic solution: objective 4933.6310496
432
433 Root relaxation: objective 7.128444e+03, 1822 iterations, 0.02 seconds (0.02 work units)
434
435   Nodes | Current Node | Objective Bounds | Work
436 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
437
438 H  0  0           7128.444444 19593.7778 175% - 0s
439   0  0 - 0  7128.44444 7128.44444 0.00% - 0s
440
441 Explored 1 nodes (2536 simplex iterations) in 0.74 seconds (1.00 work units)
442 Thread count was 8 (of 8 available processors)
443
444 Solution count 3: 7128.44 4933.63 4929.74
445
446 Optimal solution found (tolerance 1.00e-08)
447 Best objective 7.128444444444e+03, best bound 7.128444444444e+03, gap 0.00000%
448 SP is solved
449 SP's optimal solution is'□7128
450
451 Itr = 2
452 Collect_LB = [991.0, 7917.444444444442, 8591.444444444445]
453 Collect_UB = [14123.888888888883, 8471.444444444445, 8471.444444444445]
454 Collect_Hua = [0.0, 6566.444444444442, 7120.444444444445]
455 Collect_SPObjVal = [6566.444444444442, 7120.444444444445, 7128.444444444445]
456 Collect_MPObjValNHua = [991.0, 1351.0, 1471.0]
457
458
459 Ops, stop iteration
460 Values adopted from the Itr-1' th iteration, and Itr = {2}, judgeCount = {1}
461
462 ~~~~~judgeCount = 1, SPObj_SPF = 7120.444444444445
463 Vessel i: 0: pi: 12-18, ai-di: 2-15, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 2-15, taoi-deltai: 2-15, taoPi_SP-deltaPi_SP: 2-15, betaNi: 13
, bi: 13
464 Vessel i: 1: pi: 6-12, ai-di: 14-36, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 14-36, taoi-deltai: 14-37, taoPi_SP-deltaPi_SP: 14-37, betaNi
: 23, bi: 23
465 Vessel i: 2: pi: 18-25, ai-di: 14-25, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 14-25, taoi-deltai: 14-21, taoPi_SP-deltaPi_SP: 14-21,
betaNi: 7, bi: 7
466 Vessel i: 3: pi: 12-17, ai-di: 20-44, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 20-44, taoi-deltai: 20-41, taoPi_SP-deltaPi_SP: 20-41,
betaNi: 21, bi: 21
467 Vessel i: 4: pi: 17-24, ai-di: 24-30, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 24-30, taoi-deltai: 24-29, taoPi_SP-deltaPi_SP: 24-29,
betaNi: 5, bi: 5
468 Vessel i: 5: pi: 17-23, ai-di: 29-48, gi_SP-gpi_SP: 0.200000-1.000000, ai_SP-di: 30-48, taoi-deltai: 32-50, taoPi_SP-deltaPi_SP: 32-50,
betaNi: 18, bi: 18
469 Vessel i: 6: pi: 9-15, ai-di: 34-63, gi_SP-gpi_SP: 1.000000-0.600000, ai_SP-di: 42-63, taoi-deltai: 42-71, taoPi_SP-deltaPi_SP: 42-71, betaNi
: 29, bi: 29
470 Vessel i: 7: pi: 28-34, ai-di: 34-43, gi_SP-gpi_SP: 0.800000-0.400000, ai_SP-di: 42-43, taoi-deltai: 38-45, taoPi_SP-deltaPi_SP: 42-45,
betaNi: 7, bi: 7
471 Vessel i: 8: pi: 28-34, ai-di: 47-66, gi_SP-gpi_SP: 0.000000-1.000000, ai_SP-di: 47-66, taoi-deltai: 47-67, taoPi_SP-deltaPi_SP: 47-67,
betaNi: 20, bi: 20
472 Vessel i: 9: pi: 17-23, ai-di: 50-68, gi_SP-gpi_SP: 1.000000-0.000000, ai_SP-di: 57-68, taoi-deltai: 57-74, taoPi_SP-deltaPi_SP: 57-74,
betaNi: 17, bi: 17
473
474 round LB = [991, 7917, 8591]
475 round UB = [14124, 8471, 8471]
476 round Hua = [0, 6566, 7120]
477 round SPObjVal = [6566, 7120, 7128]
478 round MPObjValNHua = [991, 1351, 1471]
479
480 OptimalObj = 8591.444444444445
481 Time: 334.000000
482
483
484
485

```