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80 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
81
82 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
83 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
84
85 Optimize a model with 1983520 rows, 1559473 columns and 13694414 nonzeros
86 Model fingerprint: 0xa050e9b1
87 Variable types: 766961 continuous, 792512 integer (787112 binary)
88 Coefficient statistics:
89   Matrix range    [1e-01, 1e+10]
90   Objective range [6e-05, 5e+01]
91   Bounds range    [1e+00, 8e+01]
92   RHS range       [8e-01, 1e+10]
93 Warning: Model contains large matrix coefficients
94 Warning: Model contains large rhs
95   Consider reformulating model or setting NumericFocus parameter
96   to avoid numerical issues.
97 Presolve removed 1980422 rows and 1558437 columns
98 Presolve time: 4.38s
99 Presolved: 3098 rows, 1036 columns, 8188 nonzeros
100 Variable types: 6 continuous, 1030 integer (594 binary)
101 Found heuristic solution: objective 3236.4887888
102
103 Root simplex log...
104
105 Iteration   Objective    Primal Inf.   Dual Inf.    Time
106      0   6.5912222e+03   4.623986e+03   0.000000e+00   6s
107    1009   4.1285519e+03   0.000000e+00   0.000000e+00   6s
108
109 Root relaxation: objective 4.128552e+03, 1009 iterations, 0.02 seconds (0.01 work units)
110
111   Nodes | Current Node | Objective Bounds | Work
112 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
113
114    0   0 4128.55187   0 25 3236.48879 4128.55187 27.6% - 5s
115 H  0   0               4069.9910418 4128.55187 1.44% - 5s
116    0   0 4123.88521   0 35 4069.99104 4123.88521 1.32% - 5s
117    0   0 4123.88521   0 9 4069.99104 4123.88521 1.32% - 5s
118 H  0   0               4108.5518738 4123.88521 0.37% - 5s
119 H  0   0               4114.5518738 4123.88521 0.23% - 5s
120    0   0 cutoff   0 4114.55187 4114.55187 0.00% - 5s
121
122 Cutting planes:
123   Learned: 2
124   Gomory: 3
125   Implied bound: 16
126   Clique: 7
127   MIR: 2
128   Zero half: 1
129   Network: 1
130   RLT: 2
131   PSD: 1
132
133 Explored 1 nodes (1416 simplex iterations) in 5.85 seconds (6.01 work units)
134 Thread count was 8 (of 8 available processors)
135
136 Solution count 4: 4114.55 4108.55 4069.99 3236.49
137
138 Optimal solution found (tolerance 1.00e-08)
139 Best objective 4.114551873823e+03, best bound 4.114551873823e+03, gap 0.0000%
140 SP is solved
141 SP's optimal solution is'□4114
142
143 Itr = 0
144 Collect_LB = [610.0]
145 Collect_UB = [8839.103747646237]
146 Collect_Hua = [0.0]
147 Collect_SPObjVal = [4114.5518738231185]
148 Collect_MPObjValNHua = [610.0]
149
150
151 Set parameter TimeLimit to value 12000
152 Set parameter MIPGap to value 0.0005
153 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
154
155 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
156 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
157
158 Optimize a model with 566810 rows, 229425 columns and 1551746 nonzeros
159 Model fingerprint: 0x94356014
160 Variable types: 1 continuous, 229424 integer (229392 binary)
161 Coefficient statistics:
162   Matrix range    [1e+00, 1e+10]
163   Objective range [1e+00, 2e+01]

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164 Bounds range [1e+00, 1e+00]
165 RHS range [1e+00, 2e+10]
166 Warning: Model contains large matrix coefficients
167 Warning: Model contains large rhs
168 Consider reformulating model or setting NumericFocus parameter
169 to avoid numerical issues.
170 Presolve removed 467876 rows and 216529 columns (presolve time = 5s) ...
171 Presolve removed 533352 rows and 223346 columns
172 Presolve time: 6.62s
173 Presolved: 33458 rows, 6079 columns, 89413 nonzeros
174 Variable types: 0 continuous, 6079 integer (6058 binary)
175 Root relaxation presolved: 6079 rows, 39537 columns, 95492 nonzeros
176
177
178 Root simplex log...
179
180 Iteration Objective Primal Inf. Dual Inf. Time
181 0 handle free variables 7s
182 5322 4.8245519e+03 0.000000e+00 0.000000e+00 8s
183 5322 4.8245519e+03 0.000000e+00 0.000000e+00 8s
184
185 Root relaxation: objective 4.824552e+03, 5322 iterations, 0.55 seconds (0.97 work units)
186
187 Nodes | Current Node | Objective Bounds | Work
188 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
189
190 0 0 4824.55187 0 23 -4824.55187 - - 7s
191 0 0 4824.55187 0 40 -4824.55187 - - 8s
192 0 0 4824.55187 0 130 -4824.55187 - - 8s
193 0 0 4824.55187 0 253 -4824.55187 - - 9s
194 0 0 4824.55187 0 290 -4824.55187 - - 9s
195 0 0 4824.55187 0 112 -4824.55187 - - 10s
196 0 0 4824.55187 0 139 -4824.55187 - - 10s
197 0 0 4824.55187 0 447 -4824.55187 - - 11s
198 0 0 4824.55187 0 336 -4824.55187 - - 11s
199 0 0 4824.55187 0 121 -4824.55187 - - 12s
200 0 0 4824.55187 0 267 -4824.55187 - - 12s
201 0 0 4824.55187 0 91 -4824.55187 - - 13s
202 H 0 0 7304.5518738 4824.55187 34.0% - 13s
203 0 0 4824.55187 0 91 7304.55187 4824.55187 34.0% - 13s
204 H 0 0 6004.5518738 4824.55187 19.7% - 14s
205 0 2 4824.55187 0 91 6004.55187 4824.55187 19.7% - 14s
206 3 5 4824.55187 2 274 6004.55187 4824.55187 19.7% 1747 15s
207 41 49 4824.55187 11 213 6004.55187 4824.55187 19.7% 1134 20s
208 138 96 4824.55187 27 379 6004.55187 4824.55187 19.7% 777 25s
209 223 206 4824.55187 38 340 6004.55187 4824.55187 19.7% 867 33s
210 H 326 206 5344.5518738 4824.55187 9.73% 747 33s
211 H 367 225 5224.5518738 4824.55187 7.66% 692 37s
212 H 436 259 5184.5518738 4824.55187 6.94% 759 43s
213 566 308 infeasible 83 5184.55187 4824.55187 6.94% 800 50s
214 764 532 4824.55187 11 237 5184.55187 4824.55187 6.94% 735 57s
215 1180 716 4924.55187 108 330 5184.55187 4824.55187 6.94% 607 62s
216 1437 717 4924.55187 66 91 5184.55187 4824.55187 6.94% 576 69s
217 1439 718 5144.55187 30 31 5184.55187 4824.55187 6.94% 575 70s
218 1443 721 5024.55187 196 368 5184.55187 4824.55187 6.94% 574 76s
219 1445 722 4924.55187 33 475 5184.55187 4824.55187 6.94% 573 80s
220 H 1447 687 5064.5518738 4824.55187 4.74% 572 86s
221 1450 689 5004.55187 142 641 5064.55187 4824.55187 4.74% 571 90s
222 1454 691 4828.08129 75 441 5064.55187 4824.55187 4.74% 570 96s
223 H 1455 657 5024.5518738 4824.55187 3.98% 569 100s
224 H 1455 624 5004.5518738 4826.64905 3.55% 569 100s
225 H 1455 593 4984.5518738 4826.64905 3.17% 569 100s
226 H 1455 563 4964.5518738 4826.64905 2.78% 569 100s
227 1461 568 4964.55187 83 201 4964.55187 4826.64905 2.78% 638 105s
228 1467 574 4964.55187 73 435 4964.55187 4826.64905 2.78% 640 110s
229 1489 589 4849.55397 61 677 4964.55187 4849.55397 2.32% 630 115s
230 1508 601 4964.55187 28 648 4964.55187 4864.55187 2.01% 622 120s
231 H 1520 577 4924.5518738 4864.55187 1.22% 618 123s
232 1527 582 4904.55187 22 753 4924.55187 4864.55187 1.22% 615 125s
233 1541 592 4924.55187 63 687 4924.55187 4904.55187 0.41% 654 130s
234 1558 604 4904.55187 35 698 4924.55187 4904.55187 0.41% 647 135s
235
236 Cutting planes:
237 Learned: 4
238 Gomory: 8
239 Cover: 134
240 Implied bound: 37
241 Projected implied bound: 71
242 Clique: 38
243 MIR: 31
244 StrongCG: 13
245 Flow cover: 127
246 GUB cover: 50
247 Zero half: 60

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248 RLT: 37
249 Relax-and-lift: 175
250 BQP: 4
251 PSD: 1
252
253 Explored 1563 nodes (1066273 simplex iterations) in 135.90 seconds (224.96 work units)
254 Thread count was 8 (of 8 available processors)
255
256 Solution count 10: 4924.55 4964.55 4964.55 ... 5344.55
257
258 Optimal solution found (tolerance 5.00e-04)
259 Best objective 4.924551873823e+03, best bound 4.924551873823e+03, gap 0.0000%
260 Set parameter MIPGap to value 1e-08
261 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
262
263 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
264 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
265
266 Optimize a model with 1983520 rows, 1559473 columns and 13694414 nonzeros
267 Model fingerprint: 0x695455f3
268 Variable types: 766961 continuous, 792512 integer (787112 binary)
269 Coefficient statistics:
270   Matrix range    [1e-01, 1e+10]
271   Objective range [6e-05, 5e+01]
272   Bounds range    [1e+00, 8e+01]
273   RHS range       [8e-01, 1e+10]
274 Warning: Model contains large matrix coefficients
275 Warning: Model contains large rhs
276   Consider reformulating model or setting NumericFocus parameter
277   to avoid numerical issues.
278 Presolve removed 1979528 rows and 1558182 columns
279 Presolve time: 4.26s
280 Presolved: 3992 rows, 1291 columns, 10640 nonzeros
281 Variable types: 6 continuous, 1285 integer (746 binary)
282 Found heuristic solution: objective 3254.6554554
283 Found heuristic solution: objective 3262.4332332
284
285 Root simplex log...
286
287 Iteration  Objective    Primal Inf.  Dual Inf.  Time
288      0  7.7280000e+03  2.184281e+03  0.000000e+00  6s
289  1262  4.5351111e+03  0.000000e+00  0.000000e+00  6s
290
291 Root relaxation: objective 4.535111e+03, 1262 iterations, 0.02 seconds (0.02 work units)
292
293   Nodes | Current Node | Objective Bounds | Work
294 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
295
296   0  0 4535.11111  0  50 3262.43323 4535.11111 39.0% - 5s
297 H  0  0          3768.111111 4535.11111 20.4% - 5s
298 H  0  0          3815.111111 4535.11111 18.9% - 5s
299   0  0 4535.11111  0  29 3815.11111 4535.11111 18.9% - 5s
300 H  0  0          4529.9777997 4535.11111 0.11% - 5s
301 H  0  0          4535.111111 4535.11111 0.00% - 5s
302   0  0 4535.11111  0  29 4535.11111 4535.11111 0.00% - 5s
303
304 Cutting planes:
305 Gomory: 2
306 Cover: 1
307 Implied bound: 2
308 Clique: 22
309 MIR: 1
310 Flow cover: 2
311 Relax-and-lift: 2
312
313 Explored 1 nodes (2188 simplex iterations) in 5.87 seconds (5.83 work units)
314 Thread count was 8 (of 8 available processors)
315
316 Solution count 6: 4535.11 4529.98 3815.11 ... 3254.66
317
318 Optimal solution found (tolerance 1.00e-08)
319 Best objective 4.535111111111e+03, best bound 4.535111111111e+03, gap 0.0000%
320 SP is solved
321 SP's optimal solution is'□4535
322
323 Itr = 1
324 Collect_LB = [610.0, 4924.5518738231185]
325 Collect_UB = [8839.103747646237, 5345.1111111111095]
326 Collect_Hua = [0.0, 4114.5518738231185]
327 Collect_SPObjVal = [4114.5518738231185, 4535.1111111111095]
328 Collect_MPObjValNHua = [610.0, 810.0]
329
330
331 Set parameter TimeLimit to value 12000

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332 Set parameter MIPGap to value 0.0005
333 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
334
335 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
336 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
337
338 Optimize a model with 566811 rows, 229425 columns and 1551763 nonzeros
339 Model fingerprint: 0x1d12fe8e
340 Variable types: 1 continuous, 229424 integer (229392 binary)
341 Coefficient statistics:
342   Matrix range    [1e+00, 1e+10]
343   Objective range [1e+00, 2e+01]
344   Bounds range    [1e+00, 1e+00]
345   RHS range       [1e+00, 2e+10]
346 Warning: Model contains large matrix coefficients
347 Warning: Model contains large rhs
348   Consider reformulating model or setting NumericFocus parameter
349   to avoid numerical issues.
350 Presolve removed 471489 rows and 216970 columns (presolve time = 5s) ...
351 Presolve removed 535234 rows and 223431 columns
352 Presolve time: 6.48s
353 Presolved: 31577 rows, 5994 columns, 86462 nonzeros
354 Variable types: 0 continuous, 5994 integer (5973 binary)
355 Root relaxation presolved: 5994 rows, 37571 columns, 92456 nonzeros
356
357
358 Root simplex log...
359
360 Iteration   Objective      Primal Inf.   Dual Inf.    Time
361      0      handle free variables                7s
362   4761   5.3851111e+03  0.000000e+00  0.000000e+00  7s
363   4761   5.3851111e+03  0.000000e+00  0.000000e+00  7s
364
365 Root relaxation: objective 5.385111e+03, 4761 iterations, 0.53 seconds (0.92 work units)
366
367   Nodes | Current Node | Objective Bounds | Work
368 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
369
370   0   0 5385.11111  0 19   - 5385.11111  - - 7s
371   0   0 5385.11111  0 64   - 5385.11111  - - 8s
372   0   0 5385.11111  0 179  - 5385.11111  - - 8s
373   0   0 5385.11111  0 146  - 5385.11111  - - 8s
374   0   0 5385.11111  0 43   - 5385.11111  - - 9s
375   0   0 5385.11111  0 103  - 5385.11111  - - 9s
376   0   0 5385.11111  0 88   - 5385.11111  - - 10s
377   0   0 5385.11111  0 82   - 5385.11111  - - 10s
378   0   0 5385.11111  0 133  - 5385.11111  - - 11s
379 H  0   0      8345.111111 5385.11111 35.5% - 11s
380   0   0 5385.11111  0 133 8345.11111 5385.11111 35.5% - 11s
381 H  0   0      7185.111111 5385.11111 25.1% - 11s
382 H  0   0      5385.111111 5385.11111 0.00% - 12s
383   0   0 5385.11111  0 133 5385.11111 5385.11111 0.00% - 13s
384
385 Cutting planes:
386 Cover: 218
387 Implied bound: 240
388 Clique: 15
389 MIR: 44
390 StrongCG: 21
391 GUB cover: 7
392 Zero half: 1
393 Relax-and-lift: 2
394 BQP: 3
395 PSD: 1
396
397 Explored 1 nodes (27518 simplex iterations) in 13.04 seconds (20.58 work units)
398 Thread count was 8 (of 8 available processors)
399
400 Solution count 3: 5385.11 7185.11 8345.11
401
402 Optimal solution found (tolerance 5.00e-04)
403 Best objective 5.385111111111e+03, best bound 5.385111111111e+03, gap 0.0000%
404 Set parameter MIPGap to value 1e-08
405 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
406
407 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
408 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
409
410 Optimize a model with 1983520 rows, 1559473 columns and 13694414 nonzeros
411 Model fingerprint: 0xd1541698
412 Variable types: 766961 continuous, 792512 integer (787112 binary)
413 Coefficient statistics:
414   Matrix range    [1e-01, 1e+10]
415   Objective range [6e-05, 5e+01]

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416 Bounds range [1e+00, 8e+01]
417 RHS range [8e-01, 1e+10]
418 Warning: Model contains large matrix coefficients
419 Warning: Model contains large rhs
420 Consider reformulating model or setting NumericFocus parameter
421 to avoid numerical issues.
422 Presolve removed 1979454 rows and 1558165 columns
423 Presolve time: 4.24s
424 Presolved: 4066 rows, 1308 columns, 10903 nonzeros
425 Variable types: 6 continuous, 1302 integer (752 binary)
426 Found heuristic solution: objective 3271.9442784
427
428 Root simplex log...
429
430 Iteration Objective Primal Inf. Dual Inf. Time
431 0 8.0740000e+03 4.433505e+03 0.000000e+00 5s
432 1182 4.4821111e+03 0.000000e+00 0.000000e+00 5s
433
434 Root relaxation: objective 4.482111e+03, 1182 iterations, 0.02 seconds (0.02 work units)
435
436 Nodes | Current Node | Objective Bounds | Work
437 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
438
439 * 0 0 0 4482.1111111 4482.11111 0.00% - 5s
440
441 Explored 1 nodes (1590 simplex iterations) in 5.63 seconds (5.63 work units)
442 Thread count was 8 (of 8 available processors)
443
444 Solution count 2: 4482.11 3271.94
445
446 Optimal solution found (tolerance 1.00e-08)
447 Best objective 4.482111111111e+03, best bound 4.482111111111e+03, gap 0.0000%
448 SP is solved
449 SP's optimal solution is'□4482
450
451 Itr = 2
452 Collect_LB = [610.0, 4924.5518738231185, 5385.1111111111095]
453 Collect_UB = [8839.103747646237, 5345.1111111111095, 5332.111111111111]
454 Collect_Hua = [0.0, 4114.5518738231185, 4535.1111111111095]
455 Collect_SPObjVal = [4114.5518738231185, 4535.1111111111095, 4482.111111111111]
456 Collect_MPObjValNHua = [610.0, 810.0, 850.0]
457
458
459 Ops, stop iteration
460 Values adopted from the Itr-1' th iteration, and Itr = {2}, judgeCount = {1}
461
462 ~~~~~judgeCount = 1, SPObj_SPF = 4535.1111111111095
463 Vessel i: 0: pi: 0-7, ai-di: 1-7, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 1-7, taoi-deltai: 1-6, taoPi_SP-deltaPi_SP: 1-6, betaNi: 5, bi: 5
464 Vessel i: 1: pi: 8-13, ai-di: 2-8, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 2-8, taoi-deltai: 2-6, taoPi_SP-deltaPi_SP: 2-6, betaNi: 4, bi: 4
465 Vessel i: 2: pi: 4-10, ai-di: 6-28, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 6-28, taoi-deltai: 7-27, taoPi_SP-deltaPi_SP: 7-27, betaNi: 20
, bi: 20
466 Vessel i: 3: pi: 10-16, ai-di: 10-20, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 10-20, taoi-deltai: 10-18, taoPi_SP-deltaPi_SP: 10-18,
betaNi: 8, bi: 8
467 Vessel i: 4: pi: 18-23, ai-di: 9-39, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 9-39, taoi-deltai: 9-37, taoPi_SP-deltaPi_SP: 9-37, betaNi: 28
, bi: 28
468 Vessel i: 5: pi: 10-17, ai-di: 16-37, gi_SP-gpi_SP: 0.000000-1.000000, ai_SP-di: 16-37, taoi-deltai: 21-40, taoPi_SP-deltaPi_SP: 21-40,
betaNi: 19, bi: 19
469 Vessel i: 6: pi: 28-34, ai-di: 29-44, gi_SP-gpi_SP: 1.000000-0.275896, ai_SP-di: 37-44, taoi-deltai: 32-45, taoPi_SP-deltaPi_SP: 37-45,
betaNi: 13, bi: 13
470 Vessel i: 7: pi: 17-23, ai-di: 33-41, gi_SP-gpi_SP: 0.800000-0.524104, ai_SP-di: 41-41, taoi-deltai: 38-44, taoPi_SP-deltaPi_SP: 41-44,
betaNi: 6, bi: 6
471
472 round LB = [610, 4925, 5385]
473 round UB = [8839, 5345, 5332]
474 round Hua = [0, 4115, 4535]
475 round SPObjVal = [4115, 4535, 4482]
476 round MPObjValNHua = [610, 810, 850]
477
478 OptimalObj = 5385.1111111111095
479 Time: 537.000000
480
481
482
483

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