


```

80
81 Optimal solution found (tolerance 1.00e-10)
82 Best objective 6.4900000000000e+02, best bound 6.4900000000000e+02, gap 0.0000%
83 Set parameter MIPGap to value 1e-08
84 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
85
86 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
87 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
88
89 Optimize a model with 3035470 rows, 2395885 columns and 21184668 nonzeros
90 Model fingerprint: 0x906aec28
91 Variable types: 1181973 continuous, 1213912 integer (1207162 binary)
92 Coefficient statistics:
93   Matrix range    [1e-01, 1e+10]
94   Objective range [6e-05, 5e+01]
95   Bounds range    [1e+00, 8e+01]
96   RHS range       [8e-01, 1e+10]
97 Warning: Model contains large matrix coefficients
98 Warning: Model contains large rhs
99   Consider reformulating model or setting NumericFocus parameter
100   to avoid numerical issues.
101 Presolve removed 3032023 rows and 2394662 columns (presolve time = 5s) ...
102 Presolve removed 3033149 rows and 2394999 columns
103 Presolve time: 6.22s
104 Presolved: 2321 rows, 886 columns, 6181 nonzeros
105 Variable types: 10 continuous, 876 integer (524 binary)
106 Found heuristic solution: objective 3987.9062900
107
108 Root simplex log...
109
110 Iteration   Objective    Primal Inf.   Dual Inf.    Time
111      0   8.4772222e+03   2.469038e+03   0.000000e+00   8s
112     734   5.0084444e+03   0.000000e+00   0.000000e+00   8s
113
114 Root relaxation: objective 5.008444e+03, 734 iterations, 0.01 seconds (0.01 work units)
115
116   Nodes | Current Node | Objective Bounds | Work
117 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
118
119    0   0 5008.44444   0 38 3987.90629 5008.44444 25.6% - 7s
120 H  0   0           4071.6766934 5008.44444 23.0% - 7s
121 H  0   0           4115.0100267 5008.44444 21.7% - 7s
122   0   0 5008.44444   0 19 4115.01003 5008.44444 21.7% - 7s
123 H  0   0           5004.9115810 5008.44444 0.07% - 7s
124 H  0   0           5007.5041736 5008.44444 0.02% - 7s
125   0   0 5008.30159   0 12 5007.50417 5008.30159 0.02% - 7s
126   0   0 5008.30159   0 10 5007.50417 5008.30159 0.02% - 7s
127 H  0   0           5008.3015873 5008.30159 0.00% - 8s
128
129 Cutting planes:
130   Learned: 1
131   Cover: 12
132   Implied bound: 19
133   Clique: 8
134   MIR: 11
135   Zero half: 2
136   RLT: 2
137   Relax-and-lift: 16
138
139 Explored 1 nodes (1461 simplex iterations) in 8.33 seconds (8.99 work units)
140 Thread count was 8 (of 8 available processors)
141
142 Solution count 6: 5008.3 5007.5 5004.91 ... 3987.91
143
144 Optimal solution found (tolerance 1.00e-08)
145 Best objective 5.008301587302e+03, best bound 5.008301587302e+03, gap 0.0000%
146 SP is solved
147 SP's optimal solution is'□5008
148
149 Itr = 0
150 Collect_LB = [649.0]
151 Collect_UB = [10665.603174603173]
152 Collect_Hua = [0.0]
153 Collect_SPObjVal = [5008.301587301587]
154 Collect_MPObjValNHua = [649.0]
155
156
157 Set parameter MIPGap to value 0.05
158 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
159
160 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
161 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
162
163 Optimize a model with 1220537 rows, 366171 columns and 3647638 nonzeros

```

```

164 Model fingerprint: 0xdd4eae35
165 Variable types: 1 continuous, 366170 integer (353500 binary)
166 Coefficient statistics:
167   Matrix range   [1e-01, 1e+10]
168   Objective range [1e+00, 2e+01]
169   Bounds range   [1e+00, 1e+00]
170   RHS range      [1e+00, 2e+10]
171 Warning: Model contains large matrix coefficients
172 Warning: Model contains large rhs
173   Consider reformulating model or setting NumericFocus parameter
174       to avoid numerical issues.
175 Presolve removed 1014941 rows and 340355 columns (presolve time = 5s) ...
176 Presolve removed 1049608 rows and 343084 columns (presolve time = 10s) ...
177 Presolve removed 1111170 rows and 350920 columns
178 Presolve time: 14.86s
179 Presolved: 109367 rows, 15251 columns, 341893 nonzeros
180 Variable types: 1 continuous, 15250 integer (12772 binary)
181
182 Deterministic concurrent LP optimizer: primal and dual simplex (primal and dual model)
183 Showing first log only...
184
185 Root relaxation presolved: 15251 rows, 124618 columns, 357144 nonzeros
186
187
188 Root simplex log...
189
190 Iteration   Objective   Primal Inf.   Dual Inf.   Time
191      0   5.6644444e+03  0.000000e+00  2.920602e+04  16s
192  14924  5.6644444e+03  0.000000e+00  0.000000e+00  17s
193  14924  5.6644444e+03  0.000000e+00  0.000000e+00  17s
194 Concurrent spin time: 0.32s
195
196 Solved with primal simplex
197
198 Root relaxation: objective 5.664444e+03, 14924 iterations, 1.93 seconds (2.77 work units)
199 Total elapsed time = 20.05s
200
201   Nodes | Current Node | Objective Bounds | Work
202 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
203
204   0   0 5664.44444  0 389   -5664.44444  - - 21s
205   0   0 5664.44444  0 389   -5664.44444  - - 21s
206   0   0 5664.44444  0 402   -5664.44444  - - 21s
207   0   0 5664.44444  0 391   -5664.44444  - - 21s
208   0   0 5664.44444  0 767   -5664.44444  - - 24s
209   0   0 5664.44444  0 754   -5664.44444  - - 24s
210   0   0 5664.44444  0 650   -5664.44444  - - 26s
211   0   0 5664.44444  0 592   -5664.44444  - - 26s
212   0   0 5664.44444  0 380   -5664.44444  - - 33s
213   0   0 5664.44444  0 368   -5664.44444  - - 34s
214   0   0 5664.44444  0 441   -5664.44444  - - 42s
215   0   0 5664.44444  0 503   -5664.44444  - - 44s
216   0   0 5664.44444  0 427   -5664.44444  - - 52s
217   0   0 5664.44444  0 371   -5664.44444  - - 53s
218 H   0   0           5664.4444444 5664.44444 0.00%  - 64s
219   0   0 5664.44444  0 371 5664.44444 5664.44444 0.00%  - 64s
220
221 Cutting planes:
222   Learned: 2
223   Gomory: 2
224   Cover: 421
225   Implied bound: 506
226   Clique: 773
227   MIR: 65
228   StrongCG: 19
229   Flow cover: 4
230   GUB cover: 25
231   Zero half: 7
232   RLT: 44
233   Relax-and-lift: 275
234   BQP: 31
235
236 Explored 1 nodes (142560 simplex iterations) in 64.21 seconds (166.74 work units)
237 Thread count was 8 (of 8 available processors)
238
239 Solution count 1: 5664.44
240
241 Optimal solution found (tolerance 5.00e-02)
242 Best objective 5.664444444444e+03, best bound 5.664444444444e+03, gap 0.0000%
243 Set parameter MIPGap to value 1e-08
244 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
245
246 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
247 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads

```

```

248
249 Optimize a model with 3035470 rows, 2395885 columns and 21184668 nonzeros
250 Model fingerprint: 0xb434f964
251 Variable types: 1181973 continuous, 1213912 integer (1207162 binary)
252 Coefficient statistics:
253   Matrix range   [1e-01, 1e+10]
254   Objective range [6e-05, 5e+01]
255   Bounds range   [1e+00, 8e+01]
256   RHS range      [8e-01, 1e+10]
257 Warning: Model contains large matrix coefficients
258 Warning: Model contains large rhs
259   Consider reformulating model or setting NumericFocus parameter
260   to avoid numerical issues.
261 Presolve removed 3030928 rows and 2394307 columns (presolve time = 5s) ...
262 Presolve removed 3030986 rows and 2394324 columns
263 Presolve time: 5.80s
264 Presolved: 4484 rows, 1561 columns, 11921 nonzeros
265 Variable types: 10 continuous, 1551 integer (916 binary)
266 Found heuristic solution: objective 4081.0564092
267
268 Root simplex log...
269
270 Iteration   Objective      Primal Inf.   Dual Inf.    Time
271      0  1.0648222e+04  4.021325e+03  0.000000e+00  7s
272    1367  5.8024444e+03  0.000000e+00  0.000000e+00  7s
273
274 Root relaxation: objective 5.802444e+03, 1367 iterations, 0.01 seconds (0.01 work units)
275
276   Nodes | Current Node | Objective Bounds | Work
277 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
278
279   0  0 5802.44444  0 29 4081.05641 5802.44444 42.2% - 7s
280 H  0  0          5462.3314436 5802.44444 6.23% - 7s
281   0  0 5802.44444  0 21 5462.33144 5802.44444 6.23% - 7s
282 H  0  0          5802.0420358 5802.44444 0.01% - 7s
283 H  0  0          5802.2686653 5802.44444 0.00% - 7s
284 H  0  0          5802.3314436 5802.44444 0.00% - 7s
285   0  0 5802.44444  0 13 5802.33144 5802.44444 0.00% - 7s
286   0  0 5802.44444  0  8 5802.33144 5802.44444 0.00% - 7s
287   0  0 5802.44444  0  3 5802.33144 5802.44444 0.00% - 7s
288 H  0  0          5802.4444444 5802.44444 0.00% - 7s
289
290 Explored 1 nodes (2051 simplex iterations) in 7.89 seconds (8.61 work units)
291 Thread count was 8 (of 8 available processors)
292
293 Solution count 6: 5802.44 5802.33 5802.27 ... 4081.06
294
295 Optimal solution found (tolerance 1.00e-08)
296 Best objective 5.802444444444e+03, best bound 5.802444444444e+03, gap 0.0000%
297 SP is solved
298 SP's optimal solution is'□5802
299
300 Itr = 1
301 Collect_LB = [649.0, 5664.444444444443]
302 Collect_UB = [10665.603174603173, 6458.587301587302]
303 Collect_Hua = [0.0, 5008.301587301587]
304 Collect_SPObjVal = [5008.301587301587, 5802.444444444445]
305 Collect_MPObjValNHua = [649.0, 656.1428571428569]
306
307
308 Set parameter MIPGap to value 0.05
309 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
310
311 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
312 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
313
314 Optimize a model with 1874576 rows, 388041 columns and 5709817 nonzeros
315 Model fingerprint: 0x4359ac0d
316 Variable types: 1 continuous, 388040 integer (362740 binary)
317 Coefficient statistics:
318   Matrix range   [1e-01, 1e+10]
319   Objective range [1e+00, 2e+01]
320   Bounds range   [1e+00, 1e+00]
321   RHS range      [1e+00, 2e+10]
322 Warning: Model contains large matrix coefficients
323 Warning: Model contains large rhs
324   Consider reformulating model or setting NumericFocus parameter
325   to avoid numerical issues.
326 Presolve removed 1601563 rows and 355589 columns (presolve time = 5s) ...
327 Presolve removed 1658364 rows and 360770 columns (presolve time = 10s) ...
328 Presolve removed 1667407 rows and 361529 columns (presolve time = 16s) ...
329 Presolve removed 1704406 rows and 367164 columns (presolve time = 20s) ...
330 Presolve removed 1711492 rows and 367164 columns
331 Presolve time: 20.49s

```

```

332 Presolved: 163084 rows, 20877 columns, 536262 nonzeros
333 Variable types: 1 continuous, 20876 integer (15974 binary)
334
335 Deterministic concurrent LP optimizer: primal simplex, dual simplex, and barrier
336 Showing barrier log only...
337
338 Root relaxation presolved: 20877 rows, 183961 columns, 557139 nonzeros
339
340 Root barrier log...
341
342 Ordering time: 2.44s
343
344 Barrier statistics:
345 Dense cols : 32
346 Free vars : 769
347 AA' NZ : 6.006e+05
348 Factor NZ : 2.022e+07 (roughly 240 MB of memory)
349 Factor Ops : 4.862e+10 (roughly 1 second per iteration)
350 Threads : 1
351
352           Objective      Residual
353 Iter   Primal      Dual      Primal Dual   Compl   Time
354 0 -7.35797780e+07 3.21168556e+04 2.77e+04 1.11e+03 7.73e+04 27s
355
356 Barrier performed 0 iterations in 26.52 seconds (46.92 work units)
357 Barrier solve interrupted - model solved by another algorithm
358
359 Concurrent spin time: 1.28s (can be avoided by choosing Method=3)
360
361 Solved with primal simplex
362
363 Root relaxation: objective 6.461444e+03, 23618 iterations, 5.48 seconds (6.82 work units)
364 Total elapsed time = 31.61s
365
366 Nodes | Current Node | Objective Bounds | Work
367 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
368
369 0 0 6461.44444 0 717 -6461.44444 - - 35s
370 0 0 6461.44444 0 733 -6461.44444 - - 35s
371 0 0 6461.44444 0 733 -6461.44444 - - 35s
372 0 0 6461.44444 0 1194 -6461.44444 - - 44s
373 0 0 6461.44444 0 1194 -6461.44444 - - 51s
374 0 0 6461.44444 0 646 -6461.44444 - - 68s
375 0 0 6461.44444 0 744 -6461.44444 - - 74s
376 0 0 6461.44444 0 599 -6461.44444 - - 89s
377 0 0 6461.44444 0 554 -6461.44444 - - 94s
378 0 0 6461.44444 0 604 -6461.44444 - - 104s
379 0 0 6461.44444 0 498 -6461.44444 - - 106s
380 0 0 6461.44444 0 438 -6461.44444 - - 116s
381 0 0 6461.44444 0 520 -6461.44444 - - 118s
382 0 0 6461.44444 0 223 -6461.44444 - - 126s
383 0 0 6461.44444 0 223 -6461.44444 - - 127s
384 0 0 6461.44444 0 223 -6461.44444 - - 132s
385 0 0 6461.44444 0 193 -6461.44444 - - 134s
386 0 2 6461.44444 0 193 -6461.44444 - - 144s
387 1 4 6461.44444 1 333 -6461.44444 - 3952 146s
388 3 8 6461.44444 2 343 -6461.44444 - 3043 156s
389 11 16 6461.44444 3 523 -6461.44444 - 3339 161s
390 19 24 6461.44444 5 477 -6461.44444 - 2805 166s
391 27 32 6461.44444 6 557 -6461.44444 - 2953 170s
392 31 37 6461.44444 6 492 -6461.44444 - 3042 181s
393 36 56 6461.44444 7 594 -6461.44444 - 4636 196s
394 56 110 6461.44444 11 283 -6461.44444 - 4886 220s
395 129 197 6461.44444 49 335 -6461.44444 - 3410 255s
396 303 379 6481.44444 129 432 -6461.44444 - 2043 290s
397 571 648 6481.44444 265 400 -6461.44444 - 1294 318s
398 900 867 6481.44444 408 337 -6461.44444 - 915 342s
399 H 970 430 6481.4444444 6461.44444 0.31% 856 342s
400
401 Cutting planes:
402 Learned: 9
403 Gomory: 6
404 Cover: 975
405 Implied bound: 1278
406 Clique: 2897
407 MIR: 512
408 StrongCG: 136
409 Flow cover: 39
410 GUB cover: 139
411 Zero half: 52
412 RLT: 169
413 Relax-and-lift: 624
414 BQP: 74
415 PSD: 2

```

```

416
417 Explored 1217 nodes (1193463 simplex iterations) in 342.92 seconds (952.67 work units)
418 Thread count was 8 (of 8 available processors)
419
420 Solution count 1: 6481.44
421
422 Optimal solution found (tolerance 5.00e-02)
423 Best objective 6.481444444444e+03, best bound 6.461444444444e+03, gap 0.3086%
424 Warning: linear constraint 566499 and linear constraint 1220538 have the same name "ConSP25_1[0,0]"
425 Set parameter MIPGap to value 1e-08
426 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
427
428 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
429 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
430
431 Optimize a model with 3035470 rows, 2395885 columns and 21184668 nonzeros
432 Model fingerprint: 0x32f9e72f
433 Variable types: 1181973 continuous, 1213912 integer (1207162 binary)
434 Coefficient statistics:
435   Matrix range    [1e-01, 1e+10]
436   Objective range [6e-05, 5e+01]
437   Bounds range    [1e+00, 8e+01]
438   RHS range       [8e-01, 1e+10]
439 Warning: Model contains large matrix coefficients
440 Warning: Model contains large rhs
441   Consider reformulating model or setting NumericFocus parameter
442   to avoid numerical issues.
443 Presolve removed 3030053 rows and 2394143 columns (presolve time = 5s) ...
444 Presolve removed 3030081 rows and 2394151 columns
445 Presolve time: 5.74s
446 Presolved: 5389 rows, 1734 columns, 14476 nonzeros
447 Variable types: 10 continuous, 1724 integer (1002 binary)
448
449 Root simplex log...
450
451 Iteration   Objective      Primal Inf.   Dual Inf.    Time
452      0  1.0384000e+04  5.309060e+03  0.000000e+00  7s
453  1447  5.8204444e+03  0.000000e+00  0.000000e+00  7s
454
455 Root relaxation: objective 5.820444e+03, 1447 iterations, 0.02 seconds (0.01 work units)
456
457   Nodes | Current Node | Objective Bounds | Work
458 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
459
460    0    0 5820.44444  0 18      -5820.44444  - - 7s
461 H    0    0      5820.4444444 5820.44444 0.00%  - 7s
462
463 Explored 1 nodes (2036 simplex iterations) in 7.67 seconds (8.61 work units)
464 Thread count was 8 (of 8 available processors)
465
466 Solution count 1: 5820.44
467
468 Optimal solution found (tolerance 1.00e-08)
469 Best objective 5.820444444444e+03, best bound 5.820444444444e+03, gap 0.0000%
470 SP is solved
471 SP's optimal solution is'□5820
472
473 Itr = 2
474 Collect_LB = [649.0, 5664.444444444443, 6481.444444444445]
475 Collect_UB = [10665.603174603173, 6458.587301587302, 6458.587301587302]
476 Collect_Hua = [0.0, 5008.301587301587, 5802.444444444445]
477 Collect_SPObjVal = [5008.301587301587, 5802.444444444445, 5820.444444444445]
478 Collect_MPObjValNHua = [649.0, 656.1428571428569, 679.0]
479
480
481 Reach the termination conditions, stop iteration
482 Values adopted from the judgeCount's th iteration, and Itr = {2}, judgeCount = {1}
483
484 ~~~~~judgeCount = 1, SPObj_SPF = 5802.444444444445
485 Vessel i: 0: pi: 0-5, ai-di: 9-20, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 9-20, taoi-deltai: 9-18, taoPi_SP-deltaPi_SP: 9-18, betaNi: 9, bi: 9
486 Vessel i: 1: pi: 0-5, ai-di: 33-51, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 33-51, taoi-deltai: 33-49, taoPi_SP-deltaPi_SP: 33-49, betaNi: 16, bi: 16
487 Vessel i: 2: pi: 10-15, ai-di: 57-67, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 57-67, taoi-deltai: 57-65, taoPi_SP-deltaPi_SP: 57-65, betaNi: 8, bi: 8
488 Vessel i: 3: pi: 6-11, ai-di: 15-27, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 15-27, taoi-deltai: 15-25, taoPi_SP-deltaPi_SP: 15-25, betaNi: 10, bi: 10
489 Vessel i: 4: pi: 5-10, ai-di: 42-62, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 42-62, taoi-deltai: 42-60, taoPi_SP-deltaPi_SP: 42-60, betaNi: 18, bi: 18
490 Vessel i: 5: pi: 22-28, ai-di: 17-40, gi_SP-gpi_SP: 0.000000-1.000000, ai_SP-di: 17-40, taoi-deltai: 18-28, taoPi_SP-deltaPi_SP: 18-28, betaNi: 10, bi: 10
491 Vessel i: 6: pi: 19-24, ai-di: 21-48, gi_SP-gpi_SP: 1.000000-0.480650, ai_SP-di: 29-48, taoi-deltai: 29-42, taoPi_SP-deltaPi_SP: 29-42, betaNi: 13, bi: 13
492 Vessel i: 7: pi: 13-19, ai-di: 37-57, gi_SP-gpi_SP: 0.500000-0.519350, ai_SP-di: 42-57, taoi-deltai: 40-44, taoPi_SP-deltaPi_SP: 42-44,

```

unknown

492 betaNi: 4, bi: 4
493 Vessel i: 8: pi: 14-19, ai-di: 8-41, gi_SP-gpi_SP: 0.500000-1.000000, ai_SP-di: 11-41, taoi-deltai: 12-29, taoPi_SP-deltaPi_SP: 12-29, betaNi
: 17, bi: 17
494 Vessel i: 9: pi: 24-29, ai-di: 25-58, gi_SP-gpi_SP: 1.000000-0.000000, ai_SP-di: 32-58, taoi-deltai: 32-54, taoPi_SP-deltaPi_SP: 32-54,
betaNi: 22, bi: 22
495
496 round LB = [649, 5664, 6481]
497 round UB = [10666, 6459, 6459]
498 round Hua = [0, 5008, 5802]
499 round SPObjVal = [5008, 5802, 5820]
500 round MPObjValNHua = [649, 656, 679]
501
502 Time: 1079.000000
503
504
505
506