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80 Cover: 23
81 Implied bound: 442
82 Clique: 2
83 MIR: 13
84 StrongCG: 8
85 Flow cover: 3
86 GUB cover: 5
87 RLT: 19
88 Relax-and-lift: 2
89
90 Explored 1 nodes (25193 simplex iterations) in 28.16 seconds (46.88 work units)
91 Thread count was 8 (of 8 available processors)
92
93 Solution count 9: 712 732 772 ... 7012
94
95 Optimal solution found (tolerance 1.00e-10)
96 Best objective 7.120000000000e+02, best bound 7.120000000000e+02, gap 0.0000%
97 Set parameter MIPGap to value 1e-08
98 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
99
100 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
101 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
102
103 Optimize a model with 536247 rows, 14427 columns and 1098668 nonzeros
104 Model fingerprint: 0x126a090d
105 Variable types: 36 continuous, 14391 integer (8316 binary)
106 Coefficient statistics:
107   Matrix range    [1e-01, 1e+10]
108   Objective range [6e-05, 5e+01]
109   Bounds range    [1e+00, 1e+00]
110   RHS range       [8e-01, 1e+10]
111 Warning: Model contains large matrix coefficients
112 Warning: Model contains large rhs
113   Consider reformulating model or setting NumericFocus parameter
114   to avoid numerical issues.
115 Presolve removed 533369 rows and 13482 columns
116 Presolve time: 0.39s
117 Presolved: 2878 rows, 945 columns, 7637 nonzeros
118 Variable types: 8 continuous, 937 integer (551 binary)
119 Found heuristic solution: objective 3593.0500186
120 Found heuristic solution: objective 3842.0500186
121
122 Root relaxation: objective 5.056670e+03, 876 iterations, 0.02 seconds (0.01 work units)
123
124   Nodes | Current Node | Objective Bounds | Work
125   Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
126
127    0    0 5056.67026    0 88 3842.05002 5056.67026 31.6% - 0s
128 H    0    0          3862.0500186 5056.67026 30.9% - 0s
129 H    0    0          4926.6702574 5056.67026 2.64% - 0s
130 H    0    0          4978.6702574 5056.67026 1.57% - 0s
131 *    0    0          0 5056.6702574 5056.67026 0.00% - 0s
132
133 Cutting planes:
134   Learned: 23
135   Gomory: 9
136   Cover: 29
137   Implied bound: 34
138   Clique: 11
139   MIR: 8
140   StrongCG: 1
141   Flow cover: 11
142   GUB cover: 1
143   Zero half: 12
144   RLT: 13
145   Relax-and-lift: 13
146   PSD: 2
147
148 Explored 1 nodes (1799 simplex iterations) in 0.62 seconds (0.80 work units)
149 Thread count was 8 (of 8 available processors)
150
151 Solution count 6: 5056.67 4978.67 4926.67 ... 3593.05
152
153 Optimal solution found (tolerance 1.00e-08)
154 Best objective 5.056670257367e+03, best bound 5.056670257367e+03, gap 0.0000%
155 SP is solved
156 SP's optimal solution is'□5056
157
158 Itr = 0
159 Collect_LB = [712.0]
160 Collect_UB = [10825.340514734511]
161 Collect_Hua = [0.0]
162 Collect_SPObjVal = [5056.6702573672555]
163 Collect_MPObjValNHua = [712.0]

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164
165
166 Set parameter MIPGap to value 1e-10
167 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
168
169 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
170 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
171
172 Optimize a model with 552257 rows, 283978 columns and 1530693 nonzeros
173 Model fingerprint: 0xd76ce765
174 Variable types: 1 continuous, 283977 integer (283941 binary)
175 Coefficient statistics:
176   Matrix range    [1e+00, 1e+10]
177   Objective range [1e+00, 2e+01]
178   Bounds range    [1e+00, 1e+00]
179   RHS range       [1e+00, 2e+10]
180 Warning: Model contains large matrix coefficients
181 Warning: Model contains large rhs
182   Consider reformulating model or setting NumericFocus parameter
183   to avoid numerical issues.
184 Presolve removed 305127 rows and 255611 columns (presolve time = 5s) ...
185 Presolve removed 305127 rows and 255611 columns (presolve time = 10s) ...
186 Presolve removed 305127 rows and 255611 columns (presolve time = 15s) ...
187 Presolve removed 498316 rows and 271277 columns
188 Presolve time: 16.73s
189 Presolved: 53941 rows, 12701 columns, 182064 nonzeros
190 Variable types: 0 continuous, 12701 integer (12674 binary)
191
192 Deterministic concurrent LP optimizer: primal and dual simplex (primal and dual model)
193 Showing first log only...
194
195 Root relaxation presolved: 53921 rows, 12721 columns, 182004 nonzeros
196
197
198 Root simplex log...
199
200 Iteration   Objective    Primal Inf.   Dual Inf.    Time
201      0   5.7686703e+03  3.265000e+02  4.047642e+08  18s
202 Concurrent spin time: 0.14s
203
204 Solved with dual simplex (primal model)
205
206 Root relaxation: objective 5.768670e+03, 6266 iterations, 0.88 seconds (1.44 work units)
207
208   Nodes | Current Node | Objective Bounds | Work
209 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
210
211   0   0 5768.67026   0 29      -5768.67026   -   - 19s
212   0   0 5768.67026   0 72      -5768.67026   -   - 20s
213 H   0   0              7608.6702574 5768.67026 24.2%   - 21s
214 H   0   0              7568.6702574 5768.67026 23.8%   - 21s
215   0   0 5768.67026   0 188 7568.67026 5768.67026 23.8%   - 21s
216   0   0 5768.67026   0 179 7568.67026 5768.67026 23.8%   - 21s
217   0   0 5768.67026   0  83 7568.67026 5768.67026 23.8%   - 28s
218   0   0 5768.67026   0 318 7568.67026 5768.67026 23.8%   - 30s
219   0   0 5768.67026   0  81 7568.67026 5768.67026 23.8%   - 33s
220 H   0   0              7388.6702574 5768.67026 21.9%   - 33s
221   0   0 5768.67026   0 242 7388.67026 5768.67026 21.9%   - 34s
222   0   0 5768.67026   0 162 7388.67026 5768.67026 21.9%   - 34s
223 H   0   0              6808.6702574 5768.67026 15.3%   - 38s
224   0   0 5768.67026   0  96 6808.67026 5768.67026 15.3%   - 39s
225   0   0 5768.67026   0  93 6808.67026 5768.67026 15.3%   - 39s
226   0   0 5768.67026   0 232 6808.67026 5768.67026 15.3%   - 40s
227   0   0 5768.67026   0 226 6808.67026 5768.67026 15.3%   - 40s
228   0   0 5768.67026   0 386 6808.67026 5768.67026 15.3%   - 41s
229   0   0 5768.67026   0 364 6808.67026 5768.67026 15.3%   - 41s
230   0   0 5768.67026   0 185 6808.67026 5768.67026 15.3%   - 45s
231   0   0 5768.67026   0 151 6808.67026 5768.67026 15.3%   - 46s
232 H   0   0              5768.6702574 5768.67026 0.00%   - 49s
233   0   0 5768.67026   0 151 5768.67026 5768.67026 0.00%   - 49s
234
235 Cutting planes:
236   Learned: 1
237   Gomory: 2
238   Cover: 62
239   Implied bound: 37
240   Clique: 735
241   MIR: 46
242   StrongCG: 34
243   GUB cover: 15
244   Zero half: 3
245   RLT: 7
246   Relax-and-lift: 28
247   BQP: 24

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248
249 Explored 1 nodes (125472 simplex iterations) in 49.44 seconds (71.19 work units)
250 Thread count was 8 (of 8 available processors)
251
252 Solution count 5: 5768.67 6808.67 7388.67 ... 7608.67
253
254 Optimal solution found (tolerance 1.00e-10)
255 Best objective 5.768670257367e+03, best bound 5.768670257367e+03, gap 0.0000%
256 Set parameter MIPGap to value 1e-08
257 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
258
259 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
260 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
261
262 Optimize a model with 536247 rows, 14427 columns and 1098668 nonzeros
263 Model fingerprint: 0x756949ba
264 Variable types: 36 continuous, 14391 integer (8316 binary)
265 Coefficient statistics:
266   Matrix range    [1e-01, 1e+10]
267   Objective range [6e-05, 5e+01]
268   Bounds range    [1e+00, 1e+00]
269   RHS range       [8e-01, 1e+10]
270 Warning: Model contains large matrix coefficients
271 Warning: Model contains large rhs
272   Consider reformulating model or setting NumericFocus parameter
273   to avoid numerical issues.
274 Presolve removed 531574 rows and 12874 columns
275 Presolve time: 0.36s
276 Presolved: 4673 rows, 1553 columns, 12409 nonzeros
277 Variable types: 8 continuous, 1545 integer (897 binary)
278 Found heuristic solution: objective 3675.0646186
279
280 Root relaxation: objective 5.320670e+03, 1641 iterations, 0.02 seconds (0.02 work units)
281
282   Nodes | Current Node | Objective Bounds | Work
283   Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
284
285   0   0 5320.67026   0   8 3675.06462 5320.67026 44.8%   -   0s
286 H   0   0           5090.6702574 5320.67026 4.52%   -   0s
287 H   0   0           5320.6702574 5320.67026 0.00%   -   0s
288   0   0 5320.67026   0   8 5320.67026 5320.67026 0.00%   -   0s
289
290 Explored 1 nodes (2190 simplex iterations) in 0.53 seconds (0.79 work units)
291 Thread count was 8 (of 8 available processors)
292
293 Solution count 3: 5320.67 5090.67 3675.06
294
295 Optimal solution found (tolerance 1.00e-08)
296 Best objective 5.320670257367e+03, best bound 5.320670257367e+03, gap 0.0000%
297 SP is solved
298 SP's optimal solution is'□5320
299
300 Itr = 1
301 Collect_LB = [712.0, 5768.6702573672555]
302 Collect_UB = [10825.340514734511, 6032.6702573672555]
303 Collect_Hua = [0.0, 5056.6702573672555]
304 Collect_SPObjVal = [5056.6702573672555, 5320.6702573672555]
305 Collect_MPObjValNHua = [712.0, 712.0]
306
307
308 Set parameter MIPGap to value 1e-10
309 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
310
311 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
312 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
313
314 Optimize a model with 552257 rows, 283978 columns and 1530693 nonzeros
315 Model fingerprint: 0x958e2f1f
316 Variable types: 1 continuous, 283977 integer (283941 binary)
317 Coefficient statistics:
318   Matrix range    [1e+00, 1e+10]
319   Objective range [1e+00, 2e+01]
320   Bounds range    [1e+00, 1e+00]
321   RHS range       [1e+00, 2e+10]
322 Warning: Model contains large matrix coefficients
323 Warning: Model contains large rhs
324   Consider reformulating model or setting NumericFocus parameter
325   to avoid numerical issues.
326 Presolve removed 305576 rows and 255677 columns (presolve time = 5s) ...
327 Presolve removed 305576 rows and 255677 columns (presolve time = 10s) ...
328 Presolve removed 305576 rows and 255677 columns (presolve time = 15s) ...
329 Presolve removed 498934 rows and 271325 columns
330 Presolve time: 16.38s
331 Presolved: 53323 rows, 12653 columns, 181012 nonzeros

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332 Variable types: 0 continuous, 12653 integer (12626 binary)
333
334 Deterministic concurrent LP optimizer: primal and dual simplex (primal and dual model)
335 Showing first log only...
336
337 Root relaxation presolved: 53304 rows, 12672 columns, 180955 nonzeros
338
339
340 Root simplex log...
341
342 Iteration   Objective   Primal Inf.   Dual Inf.   Time
343      0   6.0326703e+03   3.243750e+02   4.038423e+08   17s
344 Concurrent spin time: 0.09s
345
346 Solved with dual simplex (primal model)
347
348 Root relaxation: objective 6.032670e+03, 5729 iterations, 0.70 seconds (1.21 work units)
349
350 Nodes | Current Node | Objective Bounds | Work
351 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
352
353 0 0 6032.67026 0 39 - 6032.67026 - - 18s
354 0 0 6032.67026 0 167 - 6032.67026 - - 21s
355 0 0 6032.67026 0 76 - 6032.67026 - - 21s
356 0 0 6032.67026 0 198 - 6032.67026 - - 22s
357 0 0 6032.67026 0 152 - 6032.67026 - - 22s
358 0 0 6032.67026 0 100 - 6032.67026 - - 27s
359 0 0 6032.67026 0 87 - 6032.67026 - - 28s
360 0 0 6032.67026 0 167 - 6032.67026 - - 28s
361 0 0 6032.67026 0 104 - 6032.67026 - - 30s
362 0 0 6032.67026 0 229 - 6032.67026 - - 31s
363 0 0 6032.67026 0 131 - 6032.67026 - - 34s
364 H 0 0 9812.6702574 6032.67026 38.5% - 34s
365 0 0 6032.67026 0 131 9812.67026 6032.67026 38.5% - 35s
366 H 0 0 7672.6702574 6032.67026 21.4% - 36s
367 H 0 0 6032.6702574 6032.67026 0.00% - 38s
368 0 0 6032.67026 0 131 6032.67026 6032.67026 0.00% - 38s
369
370 Cutting planes:
371 Learned: 4
372 Cover: 297
373 Implied bound: 31
374 Clique: 2223
375 MIR: 176
376 StrongCG: 146
377 GUB cover: 34
378 RLT: 10
379 Relax-and-lift: 75
380 BQP: 26
381
382 Explored 1 nodes (70091 simplex iterations) in 38.33 seconds (57.06 work units)
383 Thread count was 8 (of 8 available processors)
384
385 Solution count 3: 6032.67 7672.67 9812.67
386
387 Optimal solution found (tolerance 1.00e-10)
388 Best objective 6.032670257367e+03, best bound 6.032670257367e+03, gap 0.0000%
389 Set parameter MIPGap to value 1e-08
390 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
391
392 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
393 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
394
395 Optimize a model with 536247 rows, 14427 columns and 1098668 nonzeros
396 Model fingerprint: 0x2384fc6a
397 Variable types: 36 continuous, 14391 integer (8316 binary)
398 Coefficient statistics:
399 Matrix range [1e-01, 1e+10]
400 Objective range [6e-05, 5e+01]
401 Bounds range [1e+00, 1e+00]
402 RHS range [8e-01, 1e+10]
403 Warning: Model contains large matrix coefficients
404 Warning: Model contains large rhs
405 Consider reformulating model or setting NumericFocus parameter
406 to avoid numerical issues.
407 Presolve removed 531434 rows and 12838 columns
408 Presolve time: 0.35s
409 Presolved: 4813 rows, 1589 columns, 12782 nonzeros
410 Variable types: 8 continuous, 1581 integer (915 binary)
411 Found heuristic solution: objective 3687.8601380
412
413 Root relaxation: objective 5.332860e+03, 1343 iterations, 0.02 seconds (0.01 work units)
414
415 Nodes | Current Node | Objective Bounds | Work

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```
416 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
417
418 H 0 0          5332.8601380 14291.7410 168% - 0s
419 0 0 - 0 5332.86014 5332.86014 0.00% - 0s
420
421 Explored 1 nodes (1787 simplex iterations) in 0.52 seconds (0.77 work units)
422 Thread count was 8 (of 8 available processors)
423
424 Solution count 2: 5332.86 3687.86
425
426 Optimal solution found (tolerance 1.00e-08)
427 Best objective 5.332860137998e+03, best bound 5.332860137998e+03, gap 0.0000%
428 SP is solved
429 SP's optimal solution is'□5332
430
431 Itr = 2
432 Collect_LB = [712.0, 5768.6702573672555, 6032.6702573672555]
433 Collect_UB = [10825.340514734511, 6032.6702573672555, 6032.6702573672555]
434 Collect_Hua = [0.0, 5056.6702573672555, 5320.6702573672555]
435 Collect_SPObjVal = [5056.6702573672555, 5320.6702573672555, 5332.8601379975335]
436 Collect_MPObjValNHua = [712.0, 712.0, 712.0]
437
438
439 Reach the termination conditions, stop iteration
440 Values adopted from the Itr-1' th iteration, and Itr = {2}, judgeCount = {1}
441
442 ~~~~~judgeCount = 1, SPObj_SPF = 5320.6702573672555
443 Vessel i: 0: pi: 0-5, ai-di: 38-81, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 38-81, taoi-deltai: 38-50, taoPi_SP-deltaPi_SP: 38-50, betaNi: 12, bi: 12
444 Vessel i: 1: pi: 0-5, ai-di: 8-18, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 8-18, taoi-deltai: 8-13, taoPi_SP-deltaPi_SP: 11-13, betaNi: 5, bi: 5
445 Vessel i: 2: pi: 5-11, ai-di: 32-67, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 32-67, taoi-deltai: 32-53, taoPi_SP-deltaPi_SP: 32-53, betaNi: 21, bi: 21
446 Vessel i: 3: pi: 6-11, ai-di: 12-38, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 12-38, taoi-deltai: 12-25, taoPi_SP-deltaPi_SP: 12-25, betaNi: 13, bi: 13
447 Vessel i: 4: pi: 11-16, ai-di: 43-81, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 43-81, taoi-deltai: 43-54, taoPi_SP-deltaPi_SP: 43-54, betaNi: 11, bi: 11
448 Vessel i: 5: pi: 21-26, ai-di: 11-45, gi_SP-gpi_SP: 0.000000-0.800000, ai_SP-di: 11-45, taoi-deltai: 12-27, taoPi_SP-deltaPi_SP: 12-27, betaNi: 15, bi: 15
449 Vessel i: 6: pi: 11-18, ai-di: 3-60, gi_SP-gpi_SP: 1.000000-0.000000, ai_SP-di: 11-60, taoi-deltai: 11-39, taoPi_SP-deltaPi_SP: 11-39, betaNi: 28, bi: 28
450 Vessel i: 7: pi: 18-23, ai-di: 31-79, gi_SP-gpi_SP: 0.400000-1.000000, ai_SP-di: 35-79, taoi-deltai: 33-37, taoPi_SP-deltaPi_SP: 35-37, betaNi: 4, bi: 4
451 Vessel i: 8: pi: 28-34, ai-di: 19-68, gi_SP-gpi_SP: 1.000000-0.600000, ai_SP-di: 26-68, taoi-deltai: 26-41, taoPi_SP-deltaPi_SP: 26-41, betaNi: 15, bi: 15
452
453 round LB = [712, 5769, 6033]
454 round UB = [10825, 6033, 6033]
455 round Hua = [0, 5057, 5321]
456 round SPObjVal = [5057, 5321, 5333]
457 round MPObjValNHua = [712, 712, 712]
458
459 OptimalObj = 6032.6702573672555
460 Time: 184.000000
461
462
463
464
```