



```

80 0 0 684.00000 0 150 1084.00000 684.00000 36.9% - 39s
81 H 0 0 924.0000000 684.00000 26.0% - 39s
82 0 0 684.00000 0 206 924.00000 684.00000 26.0% - 41s
83 0 0 684.00000 0 43 924.00000 684.00000 26.0% - 42s
84 0 0 684.00000 0 43 924.00000 684.00000 26.0% - 45s
85 0 0 684.00000 0 229 924.00000 684.00000 26.0% - 46s
86 0 0 684.00000 0 226 924.00000 684.00000 26.0% - 46s
87 0 0 684.00000 0 347 924.00000 684.00000 26.0% - 47s
88 H 0 0 684.0000000 684.00000 0.00% - 48s
89 0 0 684.00000 0 25 684.00000 684.00000 0.00% - 48s
90
91 Cutting planes:
92 Gomory: 2
93 Cover: 103
94 Implied bound: 977
95 Clique: 56
96 MIR: 25
97 StrongCG: 17
98 GUB cover: 21
99 RLT: 6
100 Relax-and-lift: 10
101 PSD: 2
102
103 Explored 1 nodes (69720 simplex iterations) in 48.81 seconds (80.64 work units)
104 Thread count was 8 (of 8 available processors)
105
106 Solution count 7: 684 924 1084 ... 5844
107
108 Optimal solution found (tolerance 1.00e-10)
109 Best objective 6.840000000000e+02, best bound 6.840000000000e+02, gap 0.0000%
110 Set parameter MIPGap to value 1e-08
111 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
112
113 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
114 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
115
116 Optimize a model with 3035833 rows, 2395885 columns and 21185866 nonzeros
117 Model fingerprint: 0x4fb8607a
118 Variable types: 1181973 continuous, 1213912 integer (1207162 binary)
119 Coefficient statistics:
120 Matrix range [1e-01, 1e+10]
121 Objective range [6e-05, 5e+01]
122 Bounds range [1e+00, 8e+01]
123 RHS range [8e-01, 1e+10]
124 Warning: Model contains large matrix coefficients
125 Warning: Model contains large rhs
126 Consider reformulating model or setting NumericFocus parameter
127 to avoid numerical issues.
128 Presolve removed 3033045 rows and 2394852 columns (presolve time = 5s) ...
129 Presolve removed 3033329 rows and 2394938 columns
130 Presolve time: 6.36s
131 Presolved: 2504 rows, 947 columns, 6695 nonzeros
132 Variable types: 10 continuous, 937 integer (563 binary)
133 Found heuristic solution: objective 3279.6104410
134 Found heuristic solution: objective 3440.6104410
135
136 Root simplex log...
137
138 Iteration Objective Primal Inf. Dual Inf. Time
139 0 8.2792222e+03 2.755776e+03 0.000000e+00 8s
140 783 4.8948590e+03 0.000000e+00 0.000000e+00 8s
141
142 Root relaxation: objective 4.894859e+03, 783 iterations, 0.02 seconds (0.01 work units)
143
144 Nodes | Current Node | Objective Bounds | Work
145 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
146
147 0 0 4894.85898 0 54 3440.61044 4894.85898 42.3% - 8s
148 H 0 0 4891.7251799 4894.85898 0.06% - 8s
149 0 0 4893.27025 0 23 4891.72518 4893.27025 0.03% - 8s
150 0 0 4893.27025 0 12 4891.72518 4893.27025 0.03% - 8s
151 0 0 4893.27025 0 9 4891.72518 4893.27025 0.03% - 8s
152 H 0 0 4892.3829521 4893.27025 0.02% - 8s
153 0 0 cutoff 0 4892.38295 4892.38295 0.00% - 8s
154
155 Cutting planes:
156 Gomory: 1
157 MIR: 1
158 RLT: 1
159 Relax-and-lift: 1
160
161 Explored 1 nodes (1478 simplex iterations) in 8.43 seconds (9.28 work units)
162 Thread count was 8 (of 8 available processors)
163

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164 Solution count 4: 4892.38 4891.73 3440.61 3279.61
165
166 Optimal solution found (tolerance 1.00e-08)
167 Best objective 4.892382952071e+03, best bound 4.892382952071e+03, gap 0.0000%
168 SP is solved
169 SP's optimal solution is'□4892
170
171 Itr = 0
172 Collect_LB = [684.0]
173 Collect_UB = [10468.7659041425]
174 Collect_Hua = [0.0]
175 Collect_SPObjVal = [4892.38295207125]
176 Collect_MPObjValNHua = [684.0]
177
178
179 Set parameter TimeLimit to value 12000
180 Set parameter MIPGap to value 0.0005
181 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
182
183 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
184 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
185
186 Optimize a model with 654152 rows, 344301 columns and 1811099 nonzeros
187 Model fingerprint: 0x0f17104a
188 Variable types: 1 continuous, 344300 integer (344260 binary)
189 Coefficient statistics:
190 Matrix range [1e+00, 1e+10]
191 Objective range [1e+00, 2e+01]
192 Bounds range [1e+00, 1e+00]
193 RHS range [1e+00, 2e+10]
194 Warning: Model contains large matrix coefficients
195 Warning: Model contains large rhs
196 Consider reformulating model or setting NumericFocus parameter
197 to avoid numerical issues.
198 Presolve removed 342656 rows and 308396 columns (presolve time = 5s) ...
199 Presolve removed 342656 rows and 308396 columns (presolve time = 10s) ...
200 Presolve removed 342656 rows and 308396 columns (presolve time = 15s) ...
201 Presolve removed 342656 rows and 308396 columns (presolve time = 20s) ...
202 Presolve removed 577229 rows and 327628 columns
203 Presolve time: 24.14s
204 Presolved: 76923 rows, 16673 columns, 242083 nonzeros
205 Variable types: 0 continuous, 16673 integer (16643 binary)
206
207 Deterministic concurrent LP optimizer: primal and dual simplex (primal and dual model)
208 Showing first log only...
209
210 Root relaxation presolved: 16673 rows, 93596 columns, 258756 nonzeros
211
212
213 Root simplex log...
214
215 Iteration Objective Primal Inf. Dual Inf. Time
216 0 5.5810258e+03 0.000000e+00 5.837000e+03 26s
217 Concurrent spin time: 0.00s
218
219 Solved with dual simplex (primal model)
220
221 Root relaxation: objective 5.581026e+03, 7662 iterations, 0.94 seconds (1.76 work units)
222
223 Nodes | Current Node | Objective Bounds | Work
224 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
225
226 0 0 5581.02581 0 29 -5581.02581 - - 27s
227 0 0 5581.02581 0 99 -5581.02581 - - 28s
228 0 0 5581.02581 0 211 -5581.02581 - - 28s
229 0 0 5581.02581 0 103 -5581.02581 - - 31s
230 H 0 0 8281.0258092 5581.02581 32.6% - 32s
231 0 0 5581.02581 0 128 8281.02581 5581.02581 32.6% - 32s
232 0 0 5581.02581 0 107 8281.02581 5581.02581 32.6% - 33s
233 H 0 0 8201.0258092 5581.02581 31.9% - 33s
234 H 0 0 7561.0258092 5581.02581 26.2% - 34s
235 0 0 5581.02581 0 241 7561.02581 5581.02581 26.2% - 34s
236 0 0 5581.02581 0 165 7561.02581 5581.02581 26.2% - 36s
237 0 0 5581.02581 0 207 7561.02581 5581.02581 26.2% - 36s
238 0 0 5581.02581 0 371 7561.02581 5581.02581 26.2% - 38s
239 0 0 5581.02581 0 221 7561.02581 5581.02581 26.2% - 41s
240 0 0 5581.02581 0 170 7561.02581 5581.02581 26.2% - 41s
241 H 0 0 7181.0258092 5581.02581 22.3% - 43s
242 H 0 0 5581.0258092 5581.02581 0.00% - 46s
243 0 0 5581.02581 0 170 5581.02581 5581.02581 0.00% - 46s
244
245 Cutting planes:
246 Learned: 1
247 Gomory: 1

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248 Cover: 49
249 Implied bound: 32
250 Clique: 446
251 MIR: 81
252 StrongCG: 54
253 GUB cover: 7
254 Zero half: 3
255 RLT: 9
256 Relax-and-lift: 17
257 BQP: 79
258 PSD: 1
259
260 Explored 1 nodes (100005 simplex iterations) in 46.08 seconds (79.33 work units)
261 Thread count was 8 (of 8 available processors)
262
263 Solution count 5: 5581.03 7181.03 7561.03 ... 8281.03
264
265 Optimal solution found (tolerance 5.00e-04)
266 Best objective 5.581025809214e+03, best bound 5.581025809214e+03, gap 0.0000%
267 Set parameter MIPGap to value 1e-08
268 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
269
270 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
271 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
272
273 Optimize a model with 3035833 rows, 2395885 columns and 21185866 nonzeros
274 Model fingerprint: 0x144eec69
275 Variable types: 1181973 continuous, 1213912 integer (1207162 binary)
276 Coefficient statistics:
277   Matrix range    [1e-01, 1e+10]
278   Objective range [6e-05, 5e+01]
279   Bounds range    [1e+00, 8e+01]
280   RHS range       [8e-01, 1e+10]
281 Warning: Model contains large matrix coefficients
282 Warning: Model contains large rhs
283   Consider reformulating model or setting NumericFocus parameter
284   to avoid numerical issues.
285 Presolve removed 3031118 rows and 2394350 columns (presolve time = 5s) ...
286 Presolve removed 3031170 rows and 2394365 columns
287 Presolve time: 5.99s
288 Presolved: 4663 rows, 1520 columns, 12447 nonzeros
289 Variable types: 10 continuous, 1510 integer (884 binary)
290 Found heuristic solution: objective 3772.3644878
291 Found heuristic solution: objective 3801.2533767
292
293 Root simplex log...
294
295 Iteration   Objective    Primal Inf.   Dual Inf.    Time
296      0    8.8640000e+03  4.513912e+03  0.000000e+00  8s
297   1893  5.4099444e+03  0.000000e+00  0.000000e+00  8s
298
299 Root relaxation: objective 5.409944e+03, 1893 iterations, 0.03 seconds (0.04 work units)
300
301   Nodes | Current Node | Objective Bounds | Work
302 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
303
304      0  0 5409.94444  0  4 3801.25338 5409.94444 42.3% - 7s
305 H  0  0           5407.9005126 5409.94444 0.04% - 7s
306 *  0  0           5409.9444444 5409.94444 0.00% - 7s
307
308 Cutting planes:
309 Gomory: 1
310 GUB cover: 1
311 RLT: 1
312
313 Explored 1 nodes (2544 simplex iterations) in 8.06 seconds (8.63 work units)
314 Thread count was 8 (of 8 available processors)
315
316 Solution count 4: 5409.94 5407.9 3801.25 3772.36
317
318 Optimal solution found (tolerance 1.00e-08)
319 Best objective 5.409944444444e+03, best bound 5.409944444444e+03, gap 0.0000%
320 SP is solved
321 SP's optimal solution is'□5409
322
323 Itr = 1
324 Collect_LB = [684.0, 5581.025809214107]
325 Collect_UB = [10468.7659041425, 6098.587301587302]
326 Collect_Hua = [0.0, 4892.38295207125]
327 Collect_SPObjVal = [4892.38295207125, 5409.944444444445]
328 Collect_MPObjValNHua = [684.0, 688.6428571428569]
329
330
331 Set parameter TimeLimit to value 12000

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332 Set parameter MIPGap to value 0.0005
333 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
334
335 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
336 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
337
338 Optimize a model with 654153 rows, 344301 columns and 1811120 nonzeros
339 Model fingerprint: 0x91b3b71d
340 Variable types: 1 continuous, 344300 integer (344260 binary)
341 Coefficient statistics:
342   Matrix range    [1e+00, 1e+10]
343   Objective range [1e+00, 2e+01]
344   Bounds range    [1e+00, 1e+00]
345   RHS range       [1e+00, 2e+10]
346 Warning: Model contains large matrix coefficients
347 Warning: Model contains large rhs
348   Consider reformulating model or setting NumericFocus parameter
349   to avoid numerical issues.
350 Presolve removed 343650 rows and 308501 columns (presolve time = 5s) ...
351 Presolve removed 343650 rows and 308501 columns (presolve time = 10s) ...
352 Presolve removed 343650 rows and 308501 columns (presolve time = 15s) ...
353 Presolve removed 343650 rows and 308501 columns (presolve time = 20s) ...
354 Presolve removed 583691 rows and 327685 columns
355 Presolve time: 23.90s
356 Presolved: 70462 rows, 16616 columns, 235024 nonzeros
357 Variable types: 0 continuous, 16616 integer (16586 binary)
358
359 Deterministic concurrent LP optimizer: primal and dual simplex (primal and dual model)
360 Showing first log only...
361
362 Root relaxation presolved: 16616 rows, 87078 columns, 251640 nonzeros
363
364
365 Root simplex log...
366
367 Iteration   Objective    Primal Inf.   Dual Inf.    Time
368           0 6.1084444e+03 0.000000e+00 5.838000e+03 25s
369 Concurrent spin time: 0.20s
370
371 Solved with dual simplex (primal model)
372
373 Root relaxation: objective 6.108444e+03, 7058 iterations, 1.16 seconds (1.98 work units)
374
375   Nodes | Current Node | Objective Bounds | Work
376   Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
377
378   0 0 6108.44444 0 44 -6108.44444 - - 26s
379   0 0 6108.44444 0 47 -6108.44444 - - 26s
380   0 0 6108.44444 0 114 -6108.44444 - - 28s
381   0 0 6108.44444 0 112 -6108.44444 - - 28s
382   0 0 6108.44444 0 142 -6108.44444 - - 29s
383   0 0 6108.44444 0 200 -6108.44444 - - 32s
384   0 0 6108.44444 0 249 -6108.44444 - - 33s
385   0 0 6108.44444 0 166 -6108.44444 - - 36s
386   0 0 6108.44444 0 333 -6108.44444 - - 38s
387   0 0 6108.44444 0 178 -6108.44444 - - 40s
388 H 0 0 12528.444444 6108.44444 51.2% - 41s
389   0 0 6108.44444 0 178 12528.4444 6108.44444 51.2% - 42s
390 H 0 0 8408.4444444 6108.44444 27.4% - 42s
391 H 0 0 6108.4444444 6108.44444 0.00% - 45s
392   0 0 6108.44444 0 178 6108.44444 6108.44444 0.00% - 45s
393
394 Cutting planes:
395 Gomory: 2
396 Cover: 72
397 Implied bound: 24
398 Clique: 1837
399 MIR: 109
400 StrongCG: 67
401 GUB cover: 32
402 Zero half: 3
403 RLT: 8
404 Relax-and-lift: 13
405 BQP: 71
406 PSD: 1
407
408 Explored 1 nodes (73307 simplex iterations) in 45.41 seconds (64.68 work units)
409 Thread count was 8 (of 8 available processors)
410
411 Solution count 3: 6108.44 8408.44 12528.4
412
413 Optimal solution found (tolerance 5.00e-04)
414 Best objective 6.108444444444e+03, best bound 6.108444444444e+03, gap 0.0000%
415 Set parameter MIPGap to value 1e-08

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416 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
417
418 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
419 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
420
421 Optimize a model with 3035833 rows, 2395885 columns and 21185866 nonzeros
422 Model fingerprint: 0x1582cf2e
423 Variable types: 1181973 continuous, 1213912 integer (1207162 binary)
424 Coefficient statistics:
425   Matrix range    [1e-01, 1e+10]
426   Objective range [6e-05, 5e+01]
427   Bounds range    [1e+00, 8e+01]
428   RHS range       [8e-01, 1e+10]
429 Warning: Model contains large matrix coefficients
430 Warning: Model contains large rhs
431   Consider reformulating model or setting NumericFocus parameter
432   to avoid numerical issues.
433 Presolve removed 3031525 rows and 2394433 columns (presolve time = 5s) ...
434 Presolve removed 3031569 rows and 2394448 columns
435 Presolve time: 5.81s
436 Presolved: 4264 rows, 1437 columns, 11446 nonzeros
437 Variable types: 10 continuous, 1427 integer (841 binary)
438 Found heuristic solution: objective 3740.9042488
439 Found heuristic solution: objective 3780.9042488
440
441 Root simplex log...
442
443 Iteration   Objective      Primal Inf.   Dual Inf.    Time
444      0  8.8770000e+03  3.924648e+03  0.000000e+00   7s
445    1595  5.4249444e+03  0.000000e+00  0.000000e+00   7s
446
447 Root relaxation: objective 5.424944e+03, 1595 iterations, 0.03 seconds (0.03 work units)
448
449   Nodes | Current Node | Objective Bounds | Work
450 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
451
452 * 0 0 0 0 5424.9444444 5424.94444 0.00% - 7s
453
454 Explored 1 nodes (2055 simplex iterations) in 7.82 seconds (8.12 work units)
455 Thread count was 8 (of 8 available processors)
456
457 Solution count 3: 5424.94 3780.9 3740.9
458
459 Optimal solution found (tolerance 1.00e-08)
460 Best objective 5.424944444444e+03, best bound 5.424944444444e+03, gap 0.0000%
461 SP is solved
462 SP's optimal solution is'□5424
463
464 Itr = 2
465 Collect_LB = [684.0, 5581.025809214107, 6108.444444444445]
466 Collect_UB = [10468.7659041425, 6098.587301587302, 6098.587301587302]
467 Collect_Hua = [0.0, 4892.38295207125, 5409.944444444445]
468 Collect_SPObjVal = [4892.38295207125, 5409.944444444445, 5424.944444444445]
469 Collect_MPObjValNHua = [684.0, 688.6428571428569, 698.5]
470
471
472 Ops, stop iteration
473 Values adopted from the Itr-1' th iteration, and Itr = {2}, judgeCount = {1}
474
475 ~~~~~judgeCount = 1, SPObj_SPF = 5409.944444444445
476 Vessel i: 0: pi: 0-5, ai-di: 28-81, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 28-81, taoi-delta: 28-35, taoPi_SP-deltaPi_SP: 28-35, betaNi:
7, bi: 7
477 Vessel i: 1: pi: 0-5, ai-di: 15-45, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 15-45, taoi-delta: 15-21, taoPi_SP-deltaPi_SP: 15-21, betaNi:
6, bi: 6
478 Vessel i: 2: pi: 5-10, ai-di: 19-50, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 19-50, taoi-delta: 19-28, taoPi_SP-deltaPi_SP: 19-28, betaNi:
9, bi: 9
479 Vessel i: 3: pi: 10-16, ai-di: 9-55, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 9-55, taoi-delta: 9-35, taoPi_SP-deltaPi_SP: 9-35, betaNi: 26
, bi: 26
480 Vessel i: 4: pi: 22-27, ai-di: 20-42, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 20-42, taoi-delta: 20-25, taoPi_SP-deltaPi_SP: 20-25,
betaNi: 5, bi: 5
481 Vessel i: 5: pi: 17-22, ai-di: 3-61, gi_SP-gpi_SP: 0.000000-1.000000, ai_SP-di: 3-61, taoi-delta: 4-12, taoPi_SP-deltaPi_SP: 4-12, betaNi: 8
, bi: 8
482 Vessel i: 6: pi: 16-22, ai-di: 9-72, gi_SP-gpi_SP: 0.875000-0.200000, ai_SP-di: 16-72, taoi-delta: 16-33, taoPi_SP-deltaPi_SP: 16-33, betaNi:
17, bi: 17
483 Vessel i: 7: pi: 24-29, ai-di: 2-77, gi_SP-gpi_SP: 0.800000-0.800000, ai_SP-di: 10-77, taoi-delta: 6-12, taoPi_SP-deltaPi_SP: 10-12, betaNi:
6, bi: 6
484 Vessel i: 8: pi: 28-34, ai-di: 22-62, gi_SP-gpi_SP: 0.325000-1.000000, ai_SP-di: 24-62, taoi-delta: 26-36, taoPi_SP-deltaPi_SP: 26-36,
betaNi: 10, bi: 10
485 Vessel i: 9: pi: 17-24, ai-di: 28-79, gi_SP-gpi_SP: 1.000000-0.000000, ai_SP-di: 35-79, taoi-delta: 35-58, taoPi_SP-deltaPi_SP: 35-58,
betaNi: 23, bi: 23
486
487 round LB = [684, 5581, 6108]
488 round UB = [10469, 6099, 6099]
489 round Hua = [0, 4892, 5410]

```

unknown

```
490 round SPObjVal = [4892, 5410, 5425]
491 round MPObjValNHua = [684, 689, 698]
492
493 OptimalObj = 6108.444444444445
494 Time: 679.000000
495
496
497
498
```