


```

80 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
81
82 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
83 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
84
85 Optimize a model with 430104 rows, 12824 columns and 883384 nonzeros
86 Model fingerprint: 0xf10bcb56
87 Variable types: 32 continuous, 12792 integer (7392 binary)
88 Coefficient statistics:
89   Matrix range    [1e-01, 1e+10]
90   Objective range [6e-05, 5e+01]
91   Bounds range    [1e+00, 1e+00]
92   RHS range       [8e-01, 1e+10]
93 Warning: Model contains large matrix coefficients
94 Warning: Model contains large rhs
95   Consider reformulating model or setting NumericFocus parameter
96   to avoid numerical issues.
97 Presolve removed 427006 rows and 11788 columns
98 Presolve time: 0.32s
99 Presolved: 3098 rows, 1036 columns, 8188 nonzeros
100 Variable types: 6 continuous, 1030 integer (594 binary)
101 Found heuristic solution: objective 3236.4887888
102
103 Root relaxation: objective 4.128552e+03, 946 iterations, 0.01 seconds (0.01 work units)
104
105   Nodes | Current Node | Objective Bounds | Work
106 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
107
108   0   0 4128.55187   0   9 3236.48879 4128.55187 27.6%   -   0s
109 H   0   0           4114.5518738 4128.55187 0.34%   -   0s
110   0   0 4120.15188   0  39 4114.55187 4120.15188 0.14%   -   0s
111   0   0 cutoff   0   4114.55187 4114.55187 0.00%   -   0s
112
113 Cutting planes:
114   Learned: 2
115   Gomory: 3
116   Cover: 1
117   Implied bound: 8
118   Clique: 1
119   MIR: 4
120   Flow cover: 5
121   GUB cover: 1
122   Zero half: 4
123   RLT: 5
124   Relax-and-lift: 3
125
126 Explored 1 nodes (1656 simplex iterations) in 0.51 seconds (0.68 work units)
127 Thread count was 8 (of 8 available processors)
128
129 Solution count 2: 4114.55 3236.49
130
131 Optimal solution found (tolerance 1.00e-08)
132 Best objective 4.114551873823e+03, best bound 4.114551873823e+03, gap 0.0000%
133 SP is solved
134 SP's optimal solution is'□4114
135
136 Itr = 0
137 Collect_LB = [610.0]
138 Collect_UB = [8839.103747646237]
139 Collect_Hua = [0.0]
140 Collect_SPObjVal = [4114.5518738231185]
141 Collect_MPObjValNHua = [610.0]
142
143
144 Set parameter MIPGap to value 1e-10
145 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
146
147 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
148 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
149
150 Optimize a model with 566809 rows, 229425 columns and 1551729 nonzeros
151 Model fingerprint: 0xdb73789d
152 Variable types: 1 continuous, 229424 integer (229392 binary)
153 Coefficient statistics:
154   Matrix range    [1e+00, 1e+10]
155   Objective range [1e+00, 2e+01]
156   Bounds range    [1e+00, 1e+00]
157   RHS range       [1e+00, 2e+10]
158 Warning: Model contains large matrix coefficients
159 Warning: Model contains large rhs
160   Consider reformulating model or setting NumericFocus parameter
161   to avoid numerical issues.
162 Presolve removed 467875 rows and 216529 columns (presolve time = 5s) ...
163 Presolve removed 533351 rows and 223346 columns

```

```

164 Presolve time: 6.31s
165 Presolved: 33458 rows, 6079 columns, 89413 nonzeros
166 Variable types: 0 continuous, 6079 integer (6058 binary)
167 Root relaxation presolved: 6079 rows, 39537 columns, 95492 nonzeros
168
169
170 Root simplex log...
171
172 Iteration   Objective      Primal Inf.   Dual Inf.    Time
173      0      handle free variables                7s
174    5322    4.8245519e+03  0.0000000e+00  0.0000000e+00    7s
175    5322    4.8245519e+03  0.0000000e+00  0.0000000e+00    7s
176
177 Root relaxation: objective 4.824552e+03, 5322 iterations, 0.58 seconds (0.97 work units)
178
179   Nodes | Current Node | Objective Bounds | Work
180 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
181
182   0   0 4824.55187   0 23      -4824.55187   - -   7s
183   0   0 4824.55187   0 40      -4824.55187   - -   8s
184   0   0 4824.55187   0 130     -4824.55187   - -   8s
185   0   0 4824.55187   0 253     -4824.55187   - -   9s
186   0   0 4824.55187   0 290     -4824.55187   - -   9s
187   0   0 4824.55187   0 112     -4824.55187   - -  10s
188   0   0 4824.55187   0 139     -4824.55187   - -  10s
189   0   0 4824.55187   0 447     -4824.55187   - -  11s
190   0   0 4824.55187   0 336     -4824.55187   - -  11s
191   0   0 4824.55187   0 121     -4824.55187   - -  12s
192   0   0 4824.55187   0 267     -4824.55187   - -  13s
193   0   0 4824.55187   0 91      -4824.55187   - -  14s
194 H  0   0          7304.5518738 4824.55187 34.0%   - 14s
195   0   0 4824.55187   0 91 7304.55187 4824.55187 34.0%   - 14s
196 H  0   0          6004.5518738 4824.55187 19.7%   - 15s
197   0   2 4824.55187   0 91 6004.55187 4824.55187 19.7%   - 15s
198  36  34 4824.55187  10 208 6004.55187 4824.55187 19.7% 1248 21s
199  113  83 4824.55187  21 194 6004.55187 4824.55187 19.7%  736 26s
200  171 124 4824.55187  31 347 6004.55187 4824.55187 19.7%  859 31s
201  223 206 4824.55187  38 340 6004.55187 4824.55187 19.7%  867 37s
202 H 326 206          5344.5518738 4824.55187 9.73%  747 37s
203 H 367 225          5224.5518738 4824.55187 7.66%  692 41s
204 H 436 259          5184.5518738 4824.55187 6.94%  759 48s
205  566 308 infeasible 83   5184.55187 4824.55187 6.94%  800 56s
206  764 532 4824.55187  11 237 5184.55187 4824.55187 6.94%  735 65s
207 1180 716 4924.55187 108 330 5184.55187 4824.55187 6.94%  607 71s
208 1437 717 4924.55187  66 91 5184.55187 4824.55187 6.94%  576 77s
209 1441 720 4924.55187  63 339 5184.55187 4824.55187 6.94%  575 80s
210 1444 722 4924.55187 189 339 5184.55187 4824.55187 6.94%  573 87s
211 1446 723 5024.55187 228 293 5184.55187 4824.55187 6.94%  573 91s
212 H 1447 687          5064.5518738 4824.55187 4.74%  572 94s
213 1448 687 4984.55187  23 490 5064.55187 4824.55187 4.74%  572 96s
214 1451 689 5024.55187 180 676 5064.55187 4824.55187 4.74%  571 101s
215 1454 691 4828.08129  75 441 5064.55187 4824.55187 4.74%  570 106s
216 H 1455 657          5024.5518738 4824.55187 3.98%  569 110s
217 H 1455 624          5004.5518738 4826.64905 3.55%  569 111s
218 H 1455 593          4984.5518738 4826.64905 3.17%  569 111s
219 H 1455 563          4964.5518738 4826.64905 2.78%  569 111s
220 1459 567 4924.55187  86 91 4964.55187 4826.64905 2.78%  639 115s
221 1467 574 4964.55187  73 435 4964.55187 4826.64905 2.78%  640 121s
222 1482 584 4964.55187  83 654 4964.55187 4847.00932 2.37%  633 125s
223 1502 597 4964.55187  28 751 4964.55187 4853.01411 2.25%  625 130s
224 1519 609 4864.55187  96 808 4964.55187 4864.55187 2.01%  618 135s
225 H 1520 577          4924.5518738 4864.55187 1.22%  618 136s
226 1532 585 4924.55187 189 798 4924.55187 4865.18043 1.21%  613 140s
227 1547 596 4924.55187  67 627 4924.55187 4904.55187 0.41%  652 145s
228
229 Cutting planes:
230   Learned: 4
231   Gomory: 8
232   Cover: 134
233   Implied bound: 37
234   Projected implied bound: 71
235   Clique: 38
236   MIR: 31
237   StrongCG: 13
238   Flow cover: 127
239   GUB cover: 50
240   Zero half: 60
241   RLT: 37
242   Relax-and-lift: 175
243   BQP: 4
244   PSD: 1
245
246 Explored 1563 nodes (1066273 simplex iterations) in 150.16 seconds (224.96 work units)
247 Thread count was 8 (of 8 available processors)

```

```

248
249 Solution count 10: 4924.55 4964.55 4964.55 ... 5344.55
250
251 Optimal solution found (tolerance 1.00e-10)
252 Best objective 4.924551873823e+03, best bound 4.924551873823e+03, gap 0.0000%
253 Set parameter MIPGap to value 1e-08
254 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
255
256 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
257 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
258
259 Optimize a model with 430104 rows, 12824 columns and 883384 nonzeros
260 Model fingerprint: 0x09a69def
261 Variable types: 32 continuous, 12792 integer (7392 binary)
262 Coefficient statistics:
263   Matrix range    [1e-01, 1e+10]
264   Objective range [6e-05, 5e+01]
265   Bounds range    [1e+00, 1e+00]
266   RHS range       [8e-01, 1e+10]
267 Warning: Model contains large matrix coefficients
268 Warning: Model contains large rhs
269   Consider reformulating model or setting NumericFocus parameter
270   to avoid numerical issues.
271 Presolve removed 426112 rows and 11533 columns
272 Presolve time: 0.31s
273 Presolved: 3992 rows, 1291 columns, 10640 nonzeros
274 Variable types: 6 continuous, 1285 integer (746 binary)
275 Found heuristic solution: objective 3254.6554554
276 Found heuristic solution: objective 3262.4332332
277
278 Root relaxation: objective 4.535111e+03, 1259 iterations, 0.02 seconds (0.02 work units)
279
280   Nodes | Current Node | Objective Bounds | Work
281 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
282
283   0   0 4535.11111 0 54 3262.43323 4535.11111 39.0% - 0s
284 H 0 0          3677.11111 4535.11111 23.3% - 0s
285   0   0 4535.11111 0 68 3677.11111 4535.11111 23.3% - 0s
286 H 0 0          3815.11111 4535.11111 18.9% - 0s
287 H 0 0          4152.98895 4535.11111 9.20% - 0s
288 H 0 0          4392.32437 4535.11111 3.25% - 0s
289 H 0 0          4469.11111 4535.11111 1.48% - 0s
290 H 0 0          4533.61111 4535.11111 0.03% - 0s
291 H 0 0          4535.11111 4535.11111 0.00% - 0s
292   0   0 4535.11111 0 25 4535.11111 4535.11111 0.00% - 0s
293
294 Cutting planes:
295 Gomory: 11
296 Lift-and-project: 2
297 Cover: 6
298 Implied bound: 2
299 Clique: 42
300 MIR: 8
301 Flow cover: 2
302 Zero half: 4
303
304 Explored 1 nodes (2844 simplex iterations) in 0.56 seconds (0.74 work units)
305 Thread count was 8 (of 8 available processors)
306
307 Solution count 9: 4535.11 4533.61 4469.11 ... 3254.66
308
309 Optimal solution found (tolerance 1.00e-08)
310 Best objective 4.535111111111e+03, best bound 4.535111111111e+03, gap 0.0000%
311 SP is solved
312 SP's optimal solution is'□4535
313
314 Itr = 1
315 Collect_LB = [610.0, 4924.5518738231185]
316 Collect_UB = [8839.103747646237, 5345.111111111111]
317 Collect_Hua = [0.0, 4114.5518738231185]
318 Collect_SPObjVal = [4114.5518738231185, 4535.111111111111]
319 Collect_MPObjValNHua = [610.0, 810.0]
320
321
322 Set parameter MIPGap to value 1e-10
323 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
324
325 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
326 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
327
328 Optimize a model with 566809 rows, 229425 columns and 1551729 nonzeros
329 Model fingerprint: 0x0c879806
330 Variable types: 1 continuous, 229424 integer (229392 binary)
331 Coefficient statistics:

```

```

332 Matrix range [1e+00, 1e+10]
333 Objective range [1e+00, 2e+01]
334 Bounds range [1e+00, 1e+00]
335 RHS range [1e+00, 2e+10]
336 Warning: Model contains large matrix coefficients
337 Warning: Model contains large rhs
338 Consider reformulating model or setting NumericFocus parameter
339 to avoid numerical issues.
340 Presolve removed 471487 rows and 216970 columns (presolve time = 5s) ...
341 Presolve removed 535232 rows and 223431 columns
342 Presolve time: 6.41s
343 Presolved: 31577 rows, 5994 columns, 86462 nonzeros
344 Variable types: 0 continuous, 5994 integer (5973 binary)
345 Root relaxation presolved: 5994 rows, 37571 columns, 92456 nonzeros
346
347
348 Root simplex log...
349
350 Iteration Objective Primal Inf. Dual Inf. Time
351 0 handle free variables 7s
352 4761 5.3851111e+03 0.000000e+00 0.000000e+00 7s
353 4761 5.3851111e+03 0.000000e+00 0.000000e+00 7s
354
355 Root relaxation: objective 5.385111e+03, 4761 iterations, 0.55 seconds (0.92 work units)
356
357 Nodes | Current Node | Objective Bounds | Work
358 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
359
360 0 0 5385.11111 0 19 - 5385.11111 - - 7s
361 0 0 5385.11111 0 64 - 5385.11111 - - 8s
362 0 0 5385.11111 0 179 - 5385.11111 - - 8s
363 0 0 5385.11111 0 146 - 5385.11111 - - 8s
364 0 0 5385.11111 0 43 - 5385.11111 - - 9s
365 0 0 5385.11111 0 103 - 5385.11111 - - 10s
366 0 0 5385.11111 0 88 - 5385.11111 - - 10s
367 0 0 5385.11111 0 82 - 5385.11111 - - 11s
368 0 0 5385.11111 0 133 - 5385.11111 - - 11s
369 H 0 0 8345.1111111 5385.11111 35.5% - 11s
370 0 0 5385.11111 0 133 8345.11111 5385.11111 35.5% - 12s
371 H 0 0 7185.1111111 5385.11111 25.1% - 12s
372 H 0 0 5385.1111111 5385.11111 0.00% - 13s
373 0 0 5385.11111 0 133 5385.11111 5385.11111 0.00% - 13s
374
375 Cutting planes:
376 Cover: 218
377 Implied bound: 240
378 Clique: 15
379 MIR: 44
380 StrongCG: 21
381 GUB cover: 7
382 Zero half: 1
383 Relax-and-lift: 2
384 BQP: 3
385 PSD: 1
386
387 Explored 1 nodes (27518 simplex iterations) in 13.86 seconds (20.58 work units)
388 Thread count was 8 (of 8 available processors)
389
390 Solution count 3: 5385.11 7185.11 8345.11
391
392 Optimal solution found (tolerance 1.00e-10)
393 Best objective 5.3851111111111e+03, best bound 5.3851111111111e+03, gap 0.0000%
394 Set parameter MIPGap to value 1e-08
395 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
396
397 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
398 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
399
400 Optimize a model with 430104 rows, 12824 columns and 883384 nonzeros
401 Model fingerprint: 0xdc9b68f4
402 Variable types: 32 continuous, 12792 integer (7392 binary)
403 Coefficient statistics:
404 Matrix range [1e-01, 1e+10]
405 Objective range [6e-05, 5e+01]
406 Bounds range [1e+00, 1e+00]
407 RHS range [8e-01, 1e+10]
408 Warning: Model contains large matrix coefficients
409 Warning: Model contains large rhs
410 Consider reformulating model or setting NumericFocus parameter
411 to avoid numerical issues.
412 Presolve removed 426038 rows and 11516 columns
413 Presolve time: 0.31s
414 Presolved: 4066 rows, 1308 columns, 10903 nonzeros
415 Variable types: 6 continuous, 1302 integer (752 binary)

```

```
416 Found heuristic solution: objective 3271.9442784
417
418 Root relaxation: objective 4.482111e+03, 1182 iterations, 0.01 seconds (0.02 work units)
419
420 Nodes | Current Node | Objective Bounds | Work
421 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
422
423 * 0 0 0 4482.111111 4482.1111 0.00% - 0s
424
425 Explored 1 nodes (1590 simplex iterations) in 0.45 seconds (0.66 work units)
426 Thread count was 8 (of 8 available processors)
427
428 Solution count 2: 4482.11 3271.94
429
430 Optimal solution found (tolerance 1.00e-08)
431 Best objective 4.482111111111e+03, best bound 4.482111111111e+03, gap 0.0000%
432 SP is solved
433 SP's optimal solution is'□4482
434
435 Itr = 2
436 Collect_LB = [610.0, 4924.5518738231185, 5385.111111111111]
437 Collect_UB = [8839.103747646237, 5345.111111111111, 5332.111111111111]
438 Collect_Hua = [0.0, 4114.5518738231185, 4535.111111111111]
439 Collect_SPObjVal = [4114.5518738231185, 4535.111111111111, 4482.111111111111]
440 Collect_MPObjValNHua = [610.0, 810.0, 850.0]
441
442
443 Ops, stop iteration
444 Values adopted from the Itr' th iteration, and Itr = {2}, judgeCount = {2}
445
446 ~~~~~judge = 2, SPObj_SPF = 4482.111111111111
447 Vessel i: 0: pi: 0-7, ai-di: 1-7, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 1-7, taoi-deltai: 1-6, taoPi_SP-deltaPi_SP: 1-4, betaNi: 5, bi: 5
448 Vessel i: 1: pi: 13-18, ai-di: 2-8, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 2-8, taoi-deltai: 2-6, taoPi_SP-deltaPi_SP: 2-6, betaNi: 4, bi
: 4
449 Vessel i: 2: pi: 7-13, ai-di: 6-28, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 6-28, taoi-deltai: 6-26, taoPi_SP-deltaPi_SP: 6-26, betaNi: 20
, bi: 20
450 Vessel i: 3: pi: 18-24, ai-di: 10-20, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 10-20, taoi-deltai: 10-18, taoPi_SP-deltaPi_SP: 10-18,
betaNi: 8, bi: 8
451 Vessel i: 4: pi: 13-18, ai-di: 9-39, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 9-39, taoi-deltai: 9-37, taoPi_SP-deltaPi_SP: 9-37, betaNi: 28
, bi: 28
452 Vessel i: 5: pi: 27-34, ai-di: 16-37, gi_SP-gpi_SP: 0.000000-1.000000, ai_SP-di: 16-37, taoi-deltai: 16-35, taoPi_SP-deltaPi_SP: 17-35,
betaNi: 19, bi: 19
453 Vessel i: 6: pi: 28-34, ai-di: 29-44, gi_SP-gpi_SP: 1.000000-0.600000, ai_SP-di: 37-44, taoi-deltai: 37-50, taoPi_SP-deltaPi_SP: 37-50,
betaNi: 13, bi: 13
454 Vessel i: 7: pi: 14-20, ai-di: 33-41, gi_SP-gpi_SP: 0.800000-0.200000, ai_SP-di: 41-41, taoi-deltai: 41-47, taoPi_SP-deltaPi_SP: 41-47,
betaNi: 6, bi: 6
455
456 round LB = [610, 4925, 5385]
457 round UB = [8839, 5345, 5332]
458 round Hua = [0, 4115, 4535]
459 round SPObjVal = [4115, 4535, 4482]
460 round MPObjValNHua = [610, 810, 850]
461
462 OptimalObj = 5385.111111111111
463 Time: 236.000000
464
465
466
467 libpng warning: iCCP: known incorrect sRGB profile
468 libpng warning: iCCP: known incorrect sRGB profile
469 libpng warning: iCCP: known incorrect sRGB profile
470 libpng warning: iCCP: known incorrect sRGB profile
471 libpng warning: iCCP: known incorrect sRGB profile
472 libpng warning: iCCP: known incorrect sRGB profile
473 libpng warning: iCCP: known incorrect sRGB profile
474 libpng warning: iCCP: known incorrect sRGB profile
475 libpng warning: iCCP: known incorrect sRGB profile
476 libpng warning: iCCP: known incorrect sRGB profile
477 libpng warning: iCCP: known incorrect sRGB profile
478 libpng warning: iCCP: known incorrect sRGB profile
479 libpng warning: iCCP: known incorrect sRGB profile
480
```