



```

80  MIR: 49
81  StrongCG: 27
82  GUB cover: 8
83  Zero half: 2
84  RLT: 17
85  Relax-and-lift: 18
86  BQP: 9
87  PSD: 1
88
89  Explored 1 nodes (25963 simplex iterations) in 13.42 seconds (21.52 work units)
90  Thread count was 8 (of 8 available processors)
91
92  Solution count 8: 779 1439 1479 ... 5139
93
94  Optimal solution found (tolerance 1.00e-10)
95  Best objective 7.790000000000e+02, best bound 7.790000000000e+02, gap 0.0000%
96  Set parameter MIPGap to value 1e-08
97  Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
98
99  CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
100 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
101
102 Optimize a model with 1983493 rows, 1559473 columns and 13694306 nonzeros
103 Model fingerprint: 0x6dd88b20
104 Variable types: 766961 continuous, 792512 integer (787112 binary)
105 Coefficient statistics:
106   Matrix range    [1e-01, 1e+10]
107   Objective range [6e-05, 5e+01]
108   Bounds range    [1e+00, 8e+01]
109   RHS range       [8e-01, 1e+10]
110 Warning: Model contains large matrix coefficients
111 Warning: Model contains large rhs
112   Consider reformulating model or setting NumericFocus parameter
113   to avoid numerical issues.
114 Presolve removed 1981217 rows and 1558646 columns
115 Presolve time: 4.23s
116 Presolved: 2276 rows, 827 columns, 6068 nonzeros
117 Variable types: 6 continuous, 821 integer (486 binary)
118 Found heuristic solution: objective 3611.0215813
119
120 Root simplex log...
121
122 Iteration   Objective    Primal Inf.   Dual Inf.   Time
123      0    7.6070000e+03   2.825420e+03   0.000000e+00   5s
124    637    5.0405771e+03   0.000000e+00   0.000000e+00   5s
125
126 Root relaxation: objective 5.040577e+03, 637 iterations, 0.00 seconds (0.00 work units)
127
128   Nodes | Current Node | Objective Bounds | Work
129 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
130
131    0    0 5040.57714    0 8 3611.02158 5040.57714 39.6% - 5s
132 H  0    0          4980.5771368 5040.57714 1.20% - 5s
133 H  0    0          5010.5771368 5040.57714 0.60% - 5s
134 H  0    0          5028.5771368 5040.57714 0.24% - 5s
135 *  0    0          0 5040.5771368 5040.57714 0.00% - 5s
136
137 Cutting planes:
138 Gomory: 1
139 Cover: 4
140 Implied bound: 1
141 Clique: 9
142 MIR: 1
143 Zero half: 3
144 RLT: 2
145 Relax-and-lift: 2
146
147 Explored 1 nodes (982 simplex iterations) in 5.63 seconds (5.87 work units)
148 Thread count was 8 (of 8 available processors)
149
150 Solution count 5: 5040.58 5028.58 5010.58 ... 3611.02
151
152 Optimal solution found (tolerance 1.00e-08)
153 Best objective 5.040577136846e+03, best bound 5.040577136846e+03, gap 0.0000%
154 SP is solved
155 SP's optimal solution is'□5040
156
157 Itr = 0
158 Collect_LB = [779.0]
159 Collect_UB = [10860.154273692304]
160 Collect_Hua = [0.0]
161 Collect_SPObjVal = [5040.577136846152]
162 Collect_MPObjValNHua = [779.0]
163

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164
165 Set parameter TimeLimit to value 12000
166 Set parameter MIPGap to value 0.0005
167 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
168
169 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
170 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
171
172 Optimize a model with 548214 rows, 229425 columns and 1504338 nonzeros
173 Model fingerprint: 0xd3702332
174 Variable types: 1 continuous, 229424 integer (229392 binary)
175 Coefficient statistics:
176   Matrix range    [1e+00, 1e+10]
177   Objective range [1e+00, 2e+01]
178   Bounds range    [1e+00, 1e+00]
179   RHS range       [1e+00, 2e+10]
180 Warning: Model contains large matrix coefficients
181 Warning: Model contains large rhs
182   Consider reformulating model or setting NumericFocus parameter
183   to avoid numerical issues.
184 Presolve removed 409080 rows and 213250 columns (presolve time = 5s) ...
185 Presolve removed 507828 rows and 222586 columns
186 Presolve time: 6.94s
187 Presolved: 40386 rows, 6839 columns, 104525 nonzeros
188 Variable types: 0 continuous, 6839 integer (6815 binary)
189 Root relaxation presolved: 6839 rows, 47225 columns, 111364 nonzeros
190
191
192 Root simplex log...
193
194 Iteration   Objective      Primal Inf.   Dual Inf.    Time
195      0      handle free variables              7s
196    5248    5.8395771e+03  0.000000e+00  0.000000e+00  8s
197    5248    5.8395771e+03  0.000000e+00  0.000000e+00  8s
198
199 Root relaxation: objective 5.839577e+03, 5248 iterations, 0.47 seconds (0.84 work units)
200
201   Nodes | Current Node | Objective Bounds | Work
202 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
203
204   0   0 5839.57714   0 11    - 5839.57714   - - 7s
205   0   0 5839.57714   0 124    - 5839.57714   - - 8s
206   0   0 5839.57714   0 135    - 5839.57714   - - 8s
207 H  0   0              7839.5771368 5839.57714 25.5% - 8s
208   0   0 5839.57714   0 44 7839.57714 5839.57714 25.5% - 8s
209   0   0 5839.57714   0 15 7839.57714 5839.57714 25.5% - 10s
210 H  0   0              6299.5771368 5839.57714 7.30% - 10s
211   0   0 5839.57714   0 71 6299.57714 5839.57714 7.30% - 10s
212   0   0 5839.57714   0 132 6299.57714 5839.57714 7.30% - 10s
213   0   0 5839.57714   0 129 6299.57714 5839.57714 7.30% - 10s
214   0   0 5839.57714   0 127 6299.57714 5839.57714 7.30% - 10s
215   0   0 5839.57714   0 125 6299.57714 5839.57714 7.30% - 10s
216   0   0 5839.57714   0 137 6299.57714 5839.57714 7.30% - 10s
217   0   0 5839.57714   0 131 6299.57714 5839.57714 7.30% - 10s
218   0   0 5839.57714   0 81 6299.57714 5839.57714 7.30% - 11s
219   0   0 5839.57714   0 150 6299.57714 5839.57714 7.30% - 11s
220   0   0 5839.57714   0 104 6299.57714 5839.57714 7.30% - 11s
221   0   0 5839.57714   0 105 6299.57714 5839.57714 7.30% - 11s
222   0   0 5839.57714   0 140 6299.57714 5839.57714 7.30% - 12s
223   0   0 5839.57714   0 138 6299.57714 5839.57714 7.30% - 12s
224   0   0 5839.57714   0 113 6299.57714 5839.57714 7.30% - 12s
225   0   0 5839.57714   0 89 6299.57714 5839.57714 7.30% - 12s
226   0   0 5839.57714   0 49 6299.57714 5839.57714 7.30% - 13s
227 H  0   0              5839.5771368 5839.57714 0.00% - 14s
228   0   0 5839.57714   0 49 5839.57714 5839.57714 0.00% - 14s
229
230 Cutting planes:
231   Learned: 3
232   Gomory: 2
233   Cover: 139
234   Implied bound: 19
235   Clique: 132
236   MIR: 25
237   StrongCG: 16
238   GUB cover: 9
239   Zero half: 16
240   RLT: 5
241   Relax-and-lift: 1
242   BQP: 7
243
244 Explored 1 nodes (41513 simplex iterations) in 14.28 seconds (22.64 work units)
245 Thread count was 8 (of 8 available processors)
246
247 Solution count 3: 5839.58 6299.58 7839.58

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248
249 Optimal solution found (tolerance 5.00e-04)
250 Best objective 5.839577136846e+03, best bound 5.839577136846e+03, gap 0.0000%
251 Set parameter MIPGap to value 1e-08
252 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
253
254 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
255 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
256
257 Optimize a model with 1983493 rows, 1559473 columns and 13694306 nonzeros
258 Model fingerprint: 0x026351fc
259 Variable types: 766961 continuous, 792512 integer (787112 binary)
260 Coefficient statistics:
261   Matrix range    [1e-01, 1e+10]
262   Objective range [6e-05, 5e+01]
263   Bounds range    [1e+00, 8e+01]
264   RHS range       [8e-01, 1e+10]
265 Warning: Model contains large matrix coefficients
266 Warning: Model contains large rhs
267   Consider reformulating model or setting NumericFocus parameter
268   to avoid numerical issues.
269 Presolve removed 1979129 rows and 1557979 columns
270 Presolve time: 4.04s
271 Presolved: 4364 rows, 1494 columns, 11603 nonzeros
272 Variable types: 6 continuous, 1488 integer (870 binary)
273 Found heuristic solution: objective 3698.4064055
274
275 Root simplex log...
276
277 Iteration   Objective    Primal Inf.   Dual Inf.    Time
278      0   9.8620000e+03   5.348047e+03   0.000000e+00   5s
279   1274   5.3251111e+03   0.000000e+00   0.000000e+00   5s
280
281 Root relaxation: objective 5.325111e+03, 1274 iterations, 0.00 seconds (0.01 work units)
282
283   Nodes | Current Node | Objective Bounds | Work
284 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
285
286 H  0  0           5325.111111 13319.7778 150% - 5s
287   0  0   -  0   5325.1111 5325.1111 0.00% - 5s
288
289 Explored 1 nodes (1726 simplex iterations) in 5.35 seconds (5.60 work units)
290 Thread count was 8 (of 8 available processors)
291
292 Solution count 2: 5325.11 3698.41
293
294 Optimal solution found (tolerance 1.00e-08)
295 Best objective 5.325111111111e+03, best bound 5.325111111111e+03, gap 0.0000%
296 SP is solved
297 SP's optimal solution is' 5325
298
299 Itr = 1
300 Collect_LB = [779.0, 5839.577136846152]
301 Collect_UB = [10860.154273692304, 6124.111111111111]
302 Collect_Hua = [0.0, 5040.577136846152]
303 Collect_SPObjVal = [5040.577136846152, 5325.111111111111]
304 Collect_MPObjValNHua = [779.0, 799.0]
305
306
307 Set parameter TimeLimit to value 12000
308 Set parameter MIPGap to value 0.0005
309 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
310
311 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
312 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
313
314 Optimize a model with 548215 rows, 229425 columns and 1504355 nonzeros
315 Model fingerprint: 0x7603653e
316 Variable types: 1 continuous, 229424 integer (229392 binary)
317 Coefficient statistics:
318   Matrix range    [1e+00, 1e+10]
319   Objective range [1e+00, 2e+01]
320   Bounds range    [1e+00, 1e+00]
321   RHS range       [1e+00, 2e+10]
322 Warning: Model contains large matrix coefficients
323 Warning: Model contains large rhs
324   Consider reformulating model or setting NumericFocus parameter
325   to avoid numerical issues.
326 Presolve removed 409081 rows and 213250 columns (presolve time = 5s) ...
327 Presolve removed 507829 rows and 222586 columns
328 Presolve time: 6.92s
329 Presolved: 40386 rows, 6839 columns, 104525 nonzeros
330 Variable types: 0 continuous, 6839 integer (6815 binary)
331 Root relaxation presolved: 6839 rows, 47225 columns, 111364 nonzeros

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332
333
334 Root simplex log...
335
336 Iteration   Objective   Primal Inf.   Dual Inf.   Time
337    0      handle free variables              7s
338    5248    6.1241111e+03  0.000000e+00  0.000000e+00  8s
339    5248    6.1241111e+03  0.000000e+00  0.000000e+00  8s
340
341 Root relaxation: objective 6.124111e+03, 5248 iterations, 0.49 seconds (0.84 work units)
342
343 Nodes | Current Node | Objective Bounds | Work
344 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
345
346 0 0 6124.11111 0 11 -6124.11111 - - 7s
347 0 0 6124.11111 0 124 -6124.11111 - - 8s
348 0 0 6124.11111 0 135 -6124.11111 - - 8s
349 H 0 0 8124.1111111 6124.11111 24.6% - 9s
350 0 0 6124.11111 0 44 8124.11111 6124.11111 24.6% - 9s
351 0 0 6124.11111 0 15 8124.11111 6124.11111 24.6% - 10s
352 H 0 0 6584.1111111 6124.11111 6.99% - 10s
353 0 0 6124.11111 0 71 6584.11111 6124.11111 6.99% - 10s
354 0 0 6124.11111 0 132 6584.11111 6124.11111 6.99% - 10s
355 0 0 6124.11111 0 129 6584.11111 6124.11111 6.99% - 10s
356 0 0 6124.11111 0 127 6584.11111 6124.11111 6.99% - 10s
357 0 0 6124.11111 0 125 6584.11111 6124.11111 6.99% - 10s
358 0 0 6124.11111 0 137 6584.11111 6124.11111 6.99% - 10s
359 0 0 6124.11111 0 131 6584.11111 6124.11111 6.99% - 10s
360 0 0 6124.11111 0 81 6584.11111 6124.11111 6.99% - 11s
361 0 0 6124.11111 0 150 6584.11111 6124.11111 6.99% - 11s
362 0 0 6124.11111 0 104 6584.11111 6124.11111 6.99% - 11s
363 0 0 6124.11111 0 105 6584.11111 6124.11111 6.99% - 11s
364 0 0 6124.11111 0 140 6584.11111 6124.11111 6.99% - 12s
365 0 0 6124.11111 0 138 6584.11111 6124.11111 6.99% - 12s
366 0 0 6124.11111 0 113 6584.11111 6124.11111 6.99% - 12s
367 0 0 6124.11111 0 89 6584.11111 6124.11111 6.99% - 12s
368 0 0 6124.11111 0 49 6584.11111 6124.11111 6.99% - 13s
369 H 0 0 6124.1111111 6124.11111 0.00% - 14s
370 0 0 6124.11111 0 49 6124.11111 6124.11111 0.00% - 14s
371
372 Cutting planes:
373 Learned: 3
374 Gomory: 2
375 Cover: 139
376 Implied bound: 19
377 Clique: 132
378 MIR: 25
379 StrongCG: 16
380 GUB cover: 9
381 Zero half: 16
382 RLT: 5
383 Relax-and-lift: 1
384 BQP: 7
385
386 Explored 1 nodes (41513 simplex iterations) in 14.38 seconds (22.64 work units)
387 Thread count was 8 (of 8 available processors)
388
389 Solution count 3: 6124.11 6584.11 8124.11
390
391 Optimal solution found (tolerance 5.00e-04)
392 Best objective 6.124111111111e+03, best bound 6.124111111111e+03, gap 0.0000%
393 Set parameter MIPGap to value 1e-08
394 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
395
396 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
397 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
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399 Optimize a model with 1983493 rows, 1559473 columns and 13694306 nonzeros
400 Model fingerprint: 0x026351fc
401 Variable types: 766961 continuous, 792512 integer (787112 binary)
402 Coefficient statistics:
403 Matrix range [1e-01, 1e+10]
404 Objective range [6e-05, 5e+01]
405 Bounds range [1e+00, 8e+01]
406 RHS range [8e-01, 1e+10]
407 Warning: Model contains large matrix coefficients
408 Warning: Model contains large rhs
409 Consider reformulating model or setting NumericFocus parameter
410 to avoid numerical issues.
411 Presolve removed 1979129 rows and 1557979 columns
412 Presolve time: 4.11s
413 Presolved: 4364 rows, 1494 columns, 11603 nonzeros
414 Variable types: 6 continuous, 1488 integer (870 binary)
415 Found heuristic solution: objective 3698.4064055

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```

416
417 Root simplex log...
418
419 Iteration   Objective    Primal Inf.   Dual Inf.    Time
420      0  9.8620000e+03  5.348047e+03  0.000000e+00  5s
421    1274  5.3251111e+03  0.000000e+00  0.000000e+00  5s
422
423 Root relaxation: objective 5.325111e+03, 1274 iterations, 0.01 seconds (0.01 work units)
424
425 Nodes | Current Node | Objective Bounds | Work
426 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
427
428 H  0  0          5325.1111111 13319.7778 150% - 5s
429  0  0      -  0    5325.11111 5325.11111 0.00% - 5s
430
431 Explored 1 nodes (1726 simplex iterations) in 5.41 seconds (5.60 work units)
432 Thread count was 8 (of 8 available processors)
433
434 Solution count 2: 5325.11 3698.41
435
436 Optimal solution found (tolerance 1.00e-08)
437 Best objective 5.325111111111e+03, best bound 5.325111111111e+03, gap 0.0000%
438 SP is solved
439 SP's optimal solution is'□5325
440
441 Itr = 2
442 Collect_LB = [779.0, 5839.577136846152, 6124.111111111111]
443 Collect_UB = [10860.154273692304, 6124.111111111111, 6124.111111111111]
444 Collect_Hua = [0.0, 5040.577136846152, 5325.111111111111]
445 Collect_SPObjVal = [5040.577136846152, 5325.111111111111, 5325.111111111111]
446 Collect_MPObjValNHua = [779.0, 799.0, 799.0]
447
448
449 Reach the termination conditions, stop iteration
450 Values adopted from the Itr' th iteration, and Itr = {2}, judgeCount = {2}
451
452 ~~~~~judge = 2, SPObj_SPF = 5325.111111111111
453 Vessel i: 0: pi: 0-6, ai-di: 1-20, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 1-20, taoi-deltai: 1-19, taoPi_SP-deltaPi_SP: 4-19, betaNi: 18
, bi: 18
454 Vessel i: 1: pi: 14-19, ai-di: 7-14, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 7-14, taoi-deltai: 7-12, taoPi_SP-deltaPi_SP: 7-12, betaNi: 5
, bi: 5
455 Vessel i: 2: pi: 7-14, ai-di: 4-30, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 4-30, taoi-deltai: 4-28, taoPi_SP-deltaPi_SP: 4-28, betaNi: 24
, bi: 24
456 Vessel i: 3: pi: 28-34, ai-di: 7-20, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 7-20, taoi-deltai: 7-18, taoPi_SP-deltaPi_SP: 7-18, betaNi: 11
, bi: 11
457 Vessel i: 4: pi: 14-20, ai-di: 31-44, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 31-44, taoi-deltai: 31-42, taoPi_SP-deltaPi_SP: 31-42,
betaNi: 11, bi: 11
458 Vessel i: 5: pi: 24-29, ai-di: 21-43, gi_SP-gpi_SP: 0.000000-1.000000, ai_SP-di: 21-43, taoi-deltai: 21-27, taoPi_SP-deltaPi_SP: 21-27,
betaNi: 6, bi: 6
459 Vessel i: 6: pi: 15-22, ai-di: 37-78, gi_SP-gpi_SP: 1.000000-0.600000, ai_SP-di: 45-78, taoi-deltai: 45-79, taoPi_SP-deltaPi_SP: 45-79,
betaNi: 34, bi: 34
460 Vessel i: 7: pi: 22-28, ai-di: 25-57, gi_SP-gpi_SP: 0.800000-0.200000, ai_SP-di: 33-57, taoi-deltai: 33-46, taoPi_SP-deltaPi_SP: 33-46,
betaNi: 13, bi: 13
461
462 round LB = [779, 5840, 6124]
463 round UB = [10860, 6124, 6124]
464 round Hua = [0, 5041, 5325]
465 round SPObjVal = [5041, 5325, 5325]
466 round MPObjValNHua = [779, 799, 799]
467
468 OptimalObj = 6124.111111111111
469 Time: 407.000000
470
471
472
473

```