


```

80  MIR: 49
81  StrongCG: 27
82  GUB cover: 8
83  Zero half: 2
84  RLT: 17
85  Relax-and-lift: 18
86  BQP: 9
87  PSD: 1
88
89  Explored 1 nodes (25963 simplex iterations) in 15.76 seconds (21.52 work units)
90  Thread count was 8 (of 8 available processors)
91
92  Solution count 8: 779 1439 1479 ... 5139
93
94  Optimal solution found (tolerance 1.00e-10)
95  Best objective 7.790000000000e+02, best bound 7.790000000000e+02, gap 0.0000%
96  Set parameter MIPGap to value 1e-08
97  Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
98
99  CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
100 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
101
102 Optimize a model with 430077 rows, 12824 columns and 883303 nonzeros
103 Model fingerprint: 0xb9c41de0
104 Variable types: 32 continuous, 12792 integer (7392 binary)
105 Coefficient statistics:
106   Matrix range    [1e-01, 1e+10]
107   Objective range [6e-05, 5e+01]
108   Bounds range    [1e+00, 1e+00]
109   RHS range       [8e-01, 1e+10]
110 Warning: Model contains large matrix coefficients
111 Warning: Model contains large rhs
112   Consider reformulating model or setting NumericFocus parameter
113   to avoid numerical issues.
114 Presolve removed 427801 rows and 11997 columns
115 Presolve time: 0.30s
116 Presolved: 2276 rows, 827 columns, 6068 nonzeros
117 Variable types: 6 continuous, 821 integer (486 binary)
118 Found heuristic solution: objective 3611.0215813
119
120 Root relaxation: objective 5.040577e+03, 637 iterations, 0.02 seconds (0.00 work units)
121
122   Nodes | Current Node | Objective Bounds | Work
123   Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
124
125   0   0 5040.57714   0   8 3611.02158 5040.57714 39.6%   -   0s
126 H   0   0           4980.5771368 5040.57714 1.20%   -   0s
127 H   0   0           5010.5771368 5040.57714 0.60%   -   0s
128 H   0   0           5028.5771368 5040.57714 0.24%   -   0s
129 *   0   0           0 5040.5771368 5040.57714 0.00%   -   0s
130
131 Cutting planes:
132 Gomory: 1
133 Cover: 4
134 Implied bound: 1
135 Clique: 9
136 MIR: 1
137 Zero half: 3
138 RLT: 2
139 Relax-and-lift: 2
140
141 Explored 1 nodes (982 simplex iterations) in 0.44 seconds (0.61 work units)
142 Thread count was 8 (of 8 available processors)
143
144 Solution count 5: 5040.58 5028.58 5010.58 ... 3611.02
145
146 Optimal solution found (tolerance 1.00e-08)
147 Best objective 5.040577136846e+03, best bound 5.040577136846e+03, gap 0.0000%
148 SP is solved
149 SP's optimal solution is'□5040
150
151 Itr = 0
152 Collect_LB = [779.0]
153 Collect_UB = [10860.154273692304]
154 Collect_Hua = [0.0]
155 Collect_SPObjVal = [5040.577136846152]
156 Collect_MPObjValNHua = [779.0]
157
158
159 Set parameter MIPGap to value 1e-10
160 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
161
162 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
163 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads

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164
165 Optimize a model with 548213 rows, 229425 columns and 1504321 nonzeros
166 Model fingerprint: 0x8473f465
167 Variable types: 1 continuous, 229424 integer (229392 binary)
168 Coefficient statistics:
169   Matrix range   [1e+00, 1e+10]
170   Objective range [1e+00, 2e+01]
171   Bounds range   [1e+00, 1e+00]
172   RHS range      [1e+00, 2e+10]
173 Warning: Model contains large matrix coefficients
174 Warning: Model contains large rhs
175   Consider reformulating model or setting NumericFocus parameter
176   to avoid numerical issues.
177 Presolve removed 409079 rows and 213250 columns (presolve time = 5s) ...
178 Presolve removed 507827 rows and 222586 columns
179 Presolve time: 7.49s
180 Presolved: 40386 rows, 6839 columns, 104525 nonzeros
181 Variable types: 0 continuous, 6839 integer (6815 binary)
182 Root relaxation presolved: 6839 rows, 47225 columns, 111364 nonzeros
183
184
185 Root simplex log...
186
187 Iteration   Objective      Primal Inf.   Dual Inf.    Time
188    0      handle free variables                8s
189   5248   5.8395771e+03  0.000000e+00  0.000000e+00   8s
190   5248   5.8395771e+03  0.000000e+00  0.000000e+00   8s
191
192 Root relaxation: objective 5.839577e+03, 5248 iterations, 0.50 seconds (0.84 work units)
193
194   Nodes | Current Node | Objective Bounds | Work
195   Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
196
197    0    0 5839.57714    0 11      - 5839.57714    - - 8s
198    0    0 5839.57714    0 124     - 5839.57714    - - 9s
199    0    0 5839.57714    0 135     - 5839.57714    - - 9s
200 H    0    0              7839.5771368 5839.57714 25.5%    - 9s
201    0    0 5839.57714    0 44 7839.57714 5839.57714 25.5%    - 9s
202    0    0 5839.57714    0 15 7839.57714 5839.57714 25.5%    - 11s
203 H    0    0              6299.5771368 5839.57714 7.30%    - 11s
204    0    0 5839.57714    0 71 6299.57714 5839.57714 7.30%    - 11s
205    0    0 5839.57714    0 132 6299.57714 5839.57714 7.30%    - 12s
206    0    0 5839.57714    0 129 6299.57714 5839.57714 7.30%    - 12s
207    0    0 5839.57714    0 127 6299.57714 5839.57714 7.30%    - 12s
208    0    0 5839.57714    0 125 6299.57714 5839.57714 7.30%    - 12s
209    0    0 5839.57714    0 137 6299.57714 5839.57714 7.30%    - 12s
210    0    0 5839.57714    0 131 6299.57714 5839.57714 7.30%    - 12s
211    0    0 5839.57714    0 81 6299.57714 5839.57714 7.30%    - 13s
212    0    0 5839.57714    0 150 6299.57714 5839.57714 7.30%    - 13s
213    0    0 5839.57714    0 104 6299.57714 5839.57714 7.30%    - 13s
214    0    0 5839.57714    0 105 6299.57714 5839.57714 7.30%    - 13s
215    0    0 5839.57714    0 140 6299.57714 5839.57714 7.30%    - 13s
216    0    0 5839.57714    0 138 6299.57714 5839.57714 7.30%    - 13s
217    0    0 5839.57714    0 113 6299.57714 5839.57714 7.30%    - 14s
218    0    0 5839.57714    0 89 6299.57714 5839.57714 7.30%    - 14s
219    0    0 5839.57714    0 49 6299.57714 5839.57714 7.30%    - 15s
220 H    0    0              5839.5771368 5839.57714 0.00%    - 16s
221    0    0 5839.57714    0 49 5839.57714 5839.57714 0.00%    - 16s
222
223 Cutting planes:
224   Learned: 3
225   Gomory: 2
226   Cover: 139
227   Implied bound: 19
228   Clique: 132
229   MIR: 25
230   StrongCG: 16
231   GUB cover: 9
232   Zero half: 16
233   RLT: 5
234   Relax-and-lift: 1
235   BQP: 7
236
237 Explored 1 nodes (41513 simplex iterations) in 16.51 seconds (22.64 work units)
238 Thread count was 8 (of 8 available processors)
239
240 Solution count 3: 5839.58 6299.58 7839.58
241
242 Optimal solution found (tolerance 1.00e-10)
243 Best objective 5.839577136846e+03, best bound 5.839577136846e+03, gap 0.0000%
244 Set parameter MIPGap to value 1e-08
245 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
246
247 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]

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248 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
249
250 Optimize a model with 430077 rows, 12824 columns and 883303 nonzeros
251 Model fingerprint: 0x11cbd79b
252 Variable types: 32 continuous, 12792 integer (7392 binary)
253 Coefficient statistics:
254   Matrix range   [1e-01, 1e+10]
255   Objective range [6e-05, 5e+01]
256   Bounds range   [1e+00, 1e+00]
257   RHS range      [8e-01, 1e+10]
258 Warning: Model contains large matrix coefficients
259 Warning: Model contains large rhs
260   Consider reformulating model or setting NumericFocus parameter
261   to avoid numerical issues.
262 Presolve removed 425713 rows and 11330 columns
263 Presolve time: 0.33s
264 Presolved: 4364 rows, 1494 columns, 11603 nonzeros
265 Variable types: 6 continuous, 1488 integer (870 binary)
266 Found heuristic solution: objective 3698.4064055
267
268 Root relaxation: objective 5.325111e+03, 1274 iterations, 0.02 seconds (0.01 work units)
269
270   Nodes | Current Node | Objective Bounds | Work
271 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
272
273 H  0  0           5325.111111 13319.7778 150% - 0s
274   0  0   -  0   5325.1111 5325.1111 0.00% - 0s
275
276 Explored 1 nodes (1726 simplex iterations) in 0.49 seconds (0.64 work units)
277 Thread count was 8 (of 8 available processors)
278
279 Solution count 2: 5325.11 3698.41
280
281 Optimal solution found (tolerance 1.00e-08)
282 Best objective 5.325111111111e+03, best bound 5.325111111111e+03, gap 0.0000%
283 SP is solved
284 SP's optimal solution is'□5325
285
286 Itr = 1
287 Collect_LB = [779.0, 5839.577136846152]
288 Collect_UB = [10860.154273692304, 6124.111111111111]
289 Collect_Hua = [0.0, 5040.577136846152]
290 Collect_SPObjVal = [5040.577136846152, 5325.111111111111]
291 Collect_MPObjValNHua = [779.0, 799.0]
292
293
294 Set parameter MIPGap to value 1e-10
295 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
296
297 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
298 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
299
300 Optimize a model with 548213 rows, 229425 columns and 1504321 nonzeros
301 Model fingerprint: 0x930c8a0b
302 Variable types: 1 continuous, 229424 integer (229392 binary)
303 Coefficient statistics:
304   Matrix range   [1e+00, 1e+10]
305   Objective range [1e+00, 2e+01]
306   Bounds range   [1e+00, 1e+00]
307   RHS range      [1e+00, 2e+10]
308 Warning: Model contains large matrix coefficients
309 Warning: Model contains large rhs
310   Consider reformulating model or setting NumericFocus parameter
311   to avoid numerical issues.
312 Presolve removed 409079 rows and 213250 columns (presolve time = 5s) ...
313 Presolve removed 507827 rows and 222586 columns
314 Presolve time: 7.25s
315 Presolved: 40386 rows, 6839 columns, 104525 nonzeros
316 Variable types: 0 continuous, 6839 integer (6815 binary)
317 Root relaxation presolved: 6839 rows, 47225 columns, 111364 nonzeros
318
319
320 Root simplex log...
321
322 Iteration Objective Primal Inf. Dual Inf. Time
323   0 handle free variables 8s
324  5248 6.1241111e+03 0.000000e+00 0.000000e+00 8s
325  5248 6.1241111e+03 0.000000e+00 0.000000e+00 8s
326
327 Root relaxation: objective 6.124111e+03, 5248 iterations, 0.52 seconds (0.84 work units)
328
329   Nodes | Current Node | Objective Bounds | Work
330 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
331

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332 0 0 6124.11111 0 11 - 6124.11111 - - 8s
333 0 0 6124.11111 0 124 - 6124.11111 - - 9s
334 0 0 6124.11111 0 135 - 6124.11111 - - 9s
335 H 0 0 8124.1111111 6124.11111 24.6% - 9s
336 0 0 6124.11111 0 44 8124.11111 6124.11111 24.6% - 9s
337 0 0 6124.11111 0 15 8124.11111 6124.11111 24.6% - 11s
338 H 0 0 6584.1111111 6124.11111 6.99% - 11s
339 0 0 6124.11111 0 71 6584.11111 6124.11111 6.99% - 11s
340 0 0 6124.11111 0 132 6584.11111 6124.11111 6.99% - 11s
341 0 0 6124.11111 0 129 6584.11111 6124.11111 6.99% - 11s
342 0 0 6124.11111 0 127 6584.11111 6124.11111 6.99% - 12s
343 0 0 6124.11111 0 125 6584.11111 6124.11111 6.99% - 12s
344 0 0 6124.11111 0 137 6584.11111 6124.11111 6.99% - 12s
345 0 0 6124.11111 0 131 6584.11111 6124.11111 6.99% - 12s
346 0 0 6124.11111 0 81 6584.11111 6124.11111 6.99% - 13s
347 0 0 6124.11111 0 150 6584.11111 6124.11111 6.99% - 13s
348 0 0 6124.11111 0 104 6584.11111 6124.11111 6.99% - 13s
349 0 0 6124.11111 0 105 6584.11111 6124.11111 6.99% - 13s
350 0 0 6124.11111 0 140 6584.11111 6124.11111 6.99% - 13s
351 0 0 6124.11111 0 138 6584.11111 6124.11111 6.99% - 13s
352 0 0 6124.11111 0 113 6584.11111 6124.11111 6.99% - 14s
353 0 0 6124.11111 0 89 6584.11111 6124.11111 6.99% - 14s
354 0 0 6124.11111 0 49 6584.11111 6124.11111 6.99% - 15s
355 H 0 0 6124.1111111 6124.11111 0.00% - 16s
356 0 0 6124.11111 0 49 6124.11111 6124.11111 0.00% - 16s
357
358 Cutting planes:
359 Learned: 3
360 Gomory: 2
361 Cover: 139
362 Implied bound: 19
363 Clique: 132
364 MIR: 25
365 StrongCG: 16
366 GUB cover: 9
367 Zero half: 16
368 RLT: 5
369 Relax-and-lift: 1
370 BQP: 7
371
372 Explored 1 nodes (41513 simplex iterations) in 16.34 seconds (22.64 work units)
373 Thread count was 8 (of 8 available processors)
374
375 Solution count 3: 6124.11 6584.11 8124.11
376
377 Optimal solution found (tolerance 1.00e-10)
378 Best objective 6.124111111111e+03, best bound 6.124111111111e+03, gap 0.0000%
379 Set parameter MIPGap to value 1e-08
380 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
381
382 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
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389 Matrix range [1e-01, 1e+10]
390 Objective range [6e-05, 5e+01]
391 Bounds range [1e+00, 1e+00]
392 RHS range [8e-01, 1e+10]
393 Warning: Model contains large matrix coefficients
394 Warning: Model contains large rhs
395 Consider reformulating model or setting NumericFocus parameter
396 to avoid numerical issues.
397 Presolve removed 425713 rows and 11330 columns
398 Presolve time: 0.31s
399 Presolved: 4364 rows, 1494 columns, 11603 nonzeros
400 Variable types: 6 continuous, 1488 integer (870 binary)
401 Found heuristic solution: objective 3698.4064055
402
403 Root relaxation: objective 5.325111e+03, 1274 iterations, 0.01 seconds (0.01 work units)
404
405 Nodes | Current Node | Objective Bounds | Work
406 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
407
408 H 0 0 5325.1111111 13319.7778 150% - 0s
409 0 0 - 0 5325.11111 5325.11111 0.00% - 0s
410
411 Explored 1 nodes (1726 simplex iterations) in 0.44 seconds (0.64 work units)
412 Thread count was 8 (of 8 available processors)
413
414 Solution count 2: 5325.11 3698.41
415

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```
416 Optimal solution found (tolerance 1.00e-08)
417 Best objective 5.325111111111e+03, best bound 5.325111111111e+03, gap 0.0000%
418 SP is solved
419 SP's optimal solution is'□5325
420
421 Itr = 2
422 Collect_LB = [779.0, 5839.577136846152, 6124.111111111111]
423 Collect_UB = [10860.154273692304, 6124.111111111111, 6124.111111111111]
424 Collect_Hua = [0.0, 5040.577136846152, 5325.111111111111]
425 Collect_SPObjVal = [5040.577136846152, 5325.111111111111, 5325.111111111111]
426 Collect_MPObjValNHua = [779.0, 799.0, 799.0]
427
428
429 Reach the termination conditions, stop iteration
430 Values adopted from the Itr' th iteration, and Itr = {2}, judgeCount = {2}
431
432 ~~~~~judge = 2, SPObj_SPF = 5325.111111111111
433 Vessel i: 0: pi: 0-6, ai-di: 1-20, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 1-20, taoi-deltai: 1-19, taoPi_SP-deltaPi_SP: 4-19, betaNi: 18
, bi: 18
434 Vessel i: 1: pi: 14-19, ai-di: 7-14, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 7-14, taoi-deltai: 7-12, taoPi_SP-deltaPi_SP: 7-12, betaNi: 5
, bi: 5
435 Vessel i: 2: pi: 7-14, ai-di: 4-30, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 4-30, taoi-deltai: 4-28, taoPi_SP-deltaPi_SP: 4-28, betaNi: 24
, bi: 24
436 Vessel i: 3: pi: 28-34, ai-di: 7-20, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 7-20, taoi-deltai: 7-18, taoPi_SP-deltaPi_SP: 7-18, betaNi: 11
, bi: 11
437 Vessel i: 4: pi: 14-20, ai-di: 31-44, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 31-44, taoi-deltai: 31-42, taoPi_SP-deltaPi_SP: 31-42,
betaNi: 11, bi: 11
438 Vessel i: 5: pi: 24-29, ai-di: 21-43, gi_SP-gpi_SP: 0.000000-1.000000, ai_SP-di: 21-43, taoi-deltai: 21-27, taoPi_SP-deltaPi_SP: 21-27,
betaNi: 6, bi: 6
439 Vessel i: 6: pi: 15-22, ai-di: 37-78, gi_SP-gpi_SP: 1.000000-0.600000, ai_SP-di: 45-78, taoi-deltai: 45-79, taoPi_SP-deltaPi_SP: 45-79,
betaNi: 34, bi: 34
440 Vessel i: 7: pi: 22-28, ai-di: 25-57, gi_SP-gpi_SP: 0.800000-0.200000, ai_SP-di: 33-57, taoi-deltai: 33-46, taoPi_SP-deltaPi_SP: 33-46,
betaNi: 13, bi: 13
441
442 round LB = [779, 5840, 6124]
443 round UB = [10860, 6124, 6124]
444 round Hua = [0, 5041, 5325]
445 round SPObjVal = [5041, 5325, 5325]
446 round MPObjValNHua = [779, 799, 799]
447
448 OptimalObj = 6124.111111111111
449 Time: 113.000000
450
451
452
453 libpng warning: iCCP: known incorrect sRGB profile
454 libpng warning: iCCP: known incorrect sRGB profile
455 libpng warning: iCCP: known incorrect sRGB profile
456 libpng warning: iCCP: known incorrect sRGB profile
457 libpng warning: iCCP: known incorrect sRGB profile
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459 libpng warning: iCCP: known incorrect sRGB profile
460 libpng warning: iCCP: known incorrect sRGB profile
461 libpng warning: iCCP: known incorrect sRGB profile
462 libpng warning: iCCP: known incorrect sRGB profile
463 libpng warning: iCCP: known incorrect sRGB profile
464 libpng warning: iCCP: known incorrect sRGB profile
465 libpng warning: iCCP: known incorrect sRGB profile
466
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