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80 Optimal solution found (tolerance 1.00e-10)
81 Best objective 6.490000000000e+02, best bound 6.490000000000e+02, gap 0.0000%
82 Set parameter MIPGap to value 1e-08
83 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
84
85 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
86 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
87
88 Optimize a model with 3035724 rows, 2395885 columns and 21185430 nonzeros
89 Model fingerprint: 0xddb9f384
90 Variable types: 1181973 continuous, 1213912 integer (1207162 binary)
91 Coefficient statistics:
92   Matrix range    [1e-01, 1e+10]
93   Objective range [6e-05, 5e+01]
94   Bounds range    [1e+00, 8e+01]
95   RHS range       [8e-01, 1e+10]
96 Warning: Model contains large matrix coefficients
97 Warning: Model contains large rhs
98   Consider reformulating model or setting NumericFocus parameter
99     to avoid numerical issues.
100 Presolve removed 3032277 rows and 2394662 columns (presolve time = 5s) ...
101 Presolve removed 3033403 rows and 2394999 columns
102 Presolve time: 6.32s
103 Presolved: 2321 rows, 886 columns, 6181 nonzeros
104 Variable types: 10 continuous, 876 integer (524 binary)
105 Found heuristic solution: objective 3987.9062900
106
107 Root simplex log...
108
109 Iteration   Objective      Primal Inf.   Dual Inf.    Time
110      0   8.4772222e+03   2.469038e+03   0.000000e+00   8s
111     734  5.0084444e+03   0.000000e+00   0.000000e+00   8s
112
113 Root relaxation: objective 5.008444e+03, 734 iterations, 0.02 seconds (0.01 work units)
114
115   Nodes | Current Node | Objective Bounds | Work
116 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
117
118    0    0 5008.44444    0 38 3987.90629 5008.44444 25.6% - 7s
119 H  0    0           4071.6766934 5008.44444 23.0% - 7s
120 H  0    0           4115.0100267 5008.44444 21.7% - 8s
121    0    0 5008.44444    0 19 4115.01003 5008.44444 21.7% - 8s
122 H  0    0           5004.9115810 5008.44444 0.07% - 8s
123 H  0    0           5007.5041736 5008.44444 0.02% - 8s
124    0    0 5008.30159    0 12 5007.50417 5008.30159 0.02% - 8s
125    0    0 5008.30159    0 10 5007.50417 5008.30159 0.02% - 8s
126 H  0    0           5008.3015873 5008.30159 0.00% - 8s
127
128 Cutting planes:
129   Learned: 1
130   Cover: 12
131   Implied bound: 19
132   Clique: 8
133   MIR: 11
134   Zero half: 2
135   RLT: 2
136   Relax-and-lift: 16
137
138 Explored 1 nodes (1461 simplex iterations) in 8.46 seconds (8.98 work units)
139 Thread count was 8 (of 8 available processors)
140
141 Solution count 6: 5008.3 5007.5 5004.91 ... 3987.91
142
143 Optimal solution found (tolerance 1.00e-08)
144 Best objective 5.008301587302e+03, best bound 5.008301587302e+03, gap 0.0000%
145 SP is solved
146 SP's optimal solution is'□5008
147
148 Itr = 0
149 Collect_LB = [649.0]
150 Collect_UB = [10665.603174603173]
151 Collect_Hua = [0.0]
152 Collect_SPObjVal = [5008.301587301587]
153 Collect_MPObjValNHua = [649.0]
154
155
156 Set parameter TimeLimit to value 12000
157 Set parameter MIPGap to value 0.0005
158 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
159
160 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
161 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
162
163 Optimize a model with 566499 rows, 344301 columns and 1585480 nonzeros

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164 Model fingerprint: 0x58f0b5ee
165 Variable types: 1 continuous, 344300 integer (344260 binary)
166 Coefficient statistics:
167   Matrix range   [1e+00, 1e+10]
168   Objective range [1e+00, 2e+01]
169   Bounds range   [1e+00, 1e+00]
170   RHS range      [1e+00, 2e+10]
171 Warning: Model contains large matrix coefficients
172 Warning: Model contains large rhs
173   Consider reformulating model or setting NumericFocus parameter
174   to avoid numerical issues.
175 Presolve removed 414857 rows and 324178 columns (presolve time = 5s) ...
176 Presolve removed 512797 rows and 334811 columns
177 Presolve time: 8.50s
178 Presolved: 53702 rows, 9490 columns, 140676 nonzeros
179 Variable types: 0 continuous, 9490 integer (9460 binary)
180 Root relaxation presolved: 9490 rows, 63192 columns, 150166 nonzeros
181
182
183 Root simplex log...
184
185 Iteration   Objective      Primal Inf.   Dual Inf.    Time
186      0      handle free variables                9s
187   6890   5.6657666e+03   1.544375e+01   0.000000e+00   10s
188   6928   5.6644444e+03   0.000000e+00   0.000000e+00   10s
189   6928   5.6644444e+03   0.000000e+00   0.000000e+00   10s
190
191 Root relaxation: objective 5.664444e+03, 6928 iterations, 1.24 seconds (2.54 work units)
192
193   Nodes | Current Node | Objective Bounds | Work
194 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
195
196   0   0 5664.44444 0 11 - 5664.44444 - - 10s
197 H 0 0 6324.4444444 5664.44444 10.4% - 11s
198   0   0 5664.44444 0 120 6324.44444 5664.44444 10.4% - 11s
199 H 0 0 6044.4444444 5664.44444 6.29% - 11s
200   0   0 5664.44444 0 34 6044.44444 5664.44444 6.29% - 12s
201   0   0 5664.44444 0 33 6044.44444 5664.44444 6.29% - 12s
202   0   0 5664.44444 0 56 6044.44444 5664.44444 6.29% - 12s
203 H 0 0 5864.4444444 5664.44444 3.41% - 12s
204   0   0 5664.44444 0 61 5864.44444 5664.44444 3.41% - 12s
205   0   0 5664.44444 0 174 5864.44444 5664.44444 3.41% - 13s
206   0   0 5664.44444 0 25 5864.44444 5664.44444 3.41% - 13s
207   0   0 5664.44444 0 164 5864.44444 5664.44444 3.41% - 14s
208   0   0 5664.44444 0 160 5864.44444 5664.44444 3.41% - 14s
209   0   0 5664.44444 0 160 5864.44444 5664.44444 3.41% - 14s
210   0   0 5664.44444 0 75 5864.44444 5664.44444 3.41% - 14s
211   0   0 5664.44444 0 72 5864.44444 5664.44444 3.41% - 15s
212   0   0 5664.44444 0 119 5864.44444 5664.44444 3.41% - 15s
213   0   0 5664.44444 0 118 5864.44444 5664.44444 3.41% - 15s
214 H 0 0 5664.4444444 5664.44444 0.00% - 15s
215   0   0 5664.44444 0 69 5664.44444 5664.44444 0.00% - 15s
216
217 Cutting planes:
218   Learned: 2
219   Gomory: 3
220   Cover: 120
221   Implied bound: 1200
222   Clique: 285
223   MIR: 71
224   StrongCG: 45
225   GUB cover: 8
226   Zero half: 11
227   RLT: 42
228   Relax-and-lift: 8
229   BQP: 6
230   PSD: 2
231
232 Explored 1 nodes (40964 simplex iterations) in 15.65 seconds (24.12 work units)
233 Thread count was 8 (of 8 available processors)
234
235 Solution count 4: 5664.44 5864.44 6044.44 6324.44
236
237 Optimal solution found (tolerance 5.00e-04)
238 Best objective 5.664444444444e+03, best bound 5.664444444444e+03, gap 0.0000%
239 Set parameter MIPGap to value 1e-08
240 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
241
242 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
243 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
244
245 Optimize a model with 3035724 rows, 2395885 columns and 21185430 nonzeros
246 Model fingerprint: 0x71f00d4f
247 Variable types: 1181973 continuous, 1213912 integer (1207162 binary)

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248 Coefficient statistics:
249   Matrix range   [1e-01, 1e+10]
250   Objective range [6e-05, 5e+01]
251   Bounds range   [1e+00, 8e+01]
252   RHS range      [8e-01, 1e+10]
253 Warning: Model contains large matrix coefficients
254 Warning: Model contains large rhs
255     Consider reformulating model or setting NumericFocus parameter
256     to avoid numerical issues.
257 Presolve removed 3030763 rows and 2394247 columns (presolve time = 5s) ...
258 Presolve removed 3031130 rows and 2394373 columns
259 Presolve time: 6.18s
260 Presolved: 4594 rows, 1512 columns, 12213 nonzeros
261 Variable types: 10 continuous, 1502 integer (875 binary)
262 Found heuristic solution: objective 4059.8240692
263
264 Root simplex log...
265
266 Iteration   Objective      Primal Inf.   Dual Inf.    Time
267      0  9.7032222e+03  6.479138e+03  0.000000e+00  8s
268    1388  5.6174444e+03  0.000000e+00  0.000000e+00  8s
269
270 Root relaxation: objective 5.617444e+03, 1388 iterations, 0.02 seconds (0.02 work units)
271
272   Nodes | Current Node | Objective Bounds | Work
273 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
274
275    0  0 5617.44444  0 40 4059.82407 5617.44444 38.4% - 7s
276 H  0  0          4579.6044479 5617.44444 22.7% - 7s
277 H  0  0          5081.6470308 5617.44444 10.5% - 7s
278    0  0 5617.44444  0 37 5081.64703 5617.44444 10.5% - 7s
279 H  0  0          5614.0544382 5617.44444 0.06% - 8s
280    0  0 5617.17864  0 20 5614.05444 5617.17864 0.06% - 8s
281
282 Cutting planes:
283   Cover: 3
284   Clique: 12
285   MIR: 3
286   Flow cover: 1
287   Zero half: 3
288   RLT: 2
289
290 Explored 1 nodes (2401 simplex iterations) in 8.33 seconds (8.86 work units)
291 Thread count was 8 (of 8 available processors)
292
293 Solution count 4: 5614.05 5081.65 4579.6 4059.82
294
295 Optimal solution found (tolerance 1.00e-08)
296 Best objective 5.614054438168e+03, best bound 5.614054438168e+03, gap 0.0000%
297 SP is solved
298 SP's optimal solution is'□5614
299
300 Itr = 1
301 Collect_LB = [649.0, 5664.444444444443]
302 Collect_UB = [10665.603174603173, 6270.1972953106]
303 Collect_Hua = [0.0, 5008.301587301587]
304 Collect_SPObjVal = [5008.301587301587, 5614.054438167743]
305 Collect_MPObjValNHua = [649.0, 656.1428571428569]
306
307
308 Set parameter TimeLimit to value 12000
309 Set parameter MIPGap to value 0.0005
310 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
311
312 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
313 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
314
315 Optimize a model with 566500 rows, 344301 columns and 1585501 nonzeros
316 Model fingerprint: 0x92266547
317 Variable types: 1 continuous, 344300 integer (344260 binary)
318 Coefficient statistics:
319   Matrix range   [1e+00, 1e+10]
320   Objective range [1e+00, 2e+01]
321   Bounds range   [1e+00, 1e+00]
322   RHS range      [1e+00, 2e+10]
323 Warning: Model contains large matrix coefficients
324 Warning: Model contains large rhs
325     Consider reformulating model or setting NumericFocus parameter
326     to avoid numerical issues.
327 Presolve removed 415073 rows and 324162 columns (presolve time = 5s) ...
328 Presolve removed 513001 rows and 334836 columns
329 Presolve time: 8.51s
330 Presolved: 53499 rows, 9465 columns, 140196 nonzeros
331 Variable types: 0 continuous, 9465 integer (9435 binary)

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332 Root relaxation presolved: 9465 rows, 62964 columns, 149661 nonzeros
333
334
335 Root simplex log...
336
337 Iteration   Objective      Primal Inf.   Dual Inf.    Time
338      0      handle free variables                9s
339    6991    6.2790544e+03  0.000000e+00  0.000000e+00  10s
340    6991    6.2790544e+03  0.000000e+00  0.000000e+00  10s
341
342 Root relaxation: objective 6.279054e+03, 6991 iterations, 1.16 seconds (2.34 work units)
343 Total elapsed time = 10.08s
344
345   Nodes | Current Node | Objective Bounds | Work
346 Expl Unexpl | Obj Depth IntInf | Incumbent  BestBd  Gap | It/Node Time
347
348   0   0 6279.05444   0  29      -6279.05444   -   -  10s
349   0   0 6279.05444   0  29      -6279.05444   -   -  10s
350   0   0 6279.05444   0  96      -6279.05444   -   -  10s
351   0   0 6279.05444   0  91      -6279.05444   -   -  10s
352   0   0 6279.05444   0  68      -6279.05444   -   -  11s
353   0   0 6279.05444   0 102      -6279.05444   -   -  11s
354 H   0   0                6299.0544382 6279.05444  0.32%   -  12s
355   0   0 6279.05444   0  26 6299.05444 6279.05444  0.32%   -  13s
356 H   0   0                6279.0544382 6279.05444  0.00%   -  13s
357   0   0 6279.05444   0  26 6279.05444 6279.05444  0.00%   -  13s
358
359 Cutting planes:
360   Learned: 1
361   Gomory: 5
362   Cover: 68
363   Implied bound: 1057
364   Clique: 224
365   MIR: 22
366   StrongCG: 13
367   GUB cover: 2
368   Zero half: 8
369   RLT: 2
370   Relax-and-lift: 201
371
372 Explored 1 nodes (25706 simplex iterations) in 13.39 seconds (21.83 work units)
373 Thread count was 8 (of 8 available processors)
374
375 Solution count 2: 6279.05 6299.05
376
377 Optimal solution found (tolerance 5.00e-04)
378 Best objective 6.279054438168e+03, best bound 6.279054438168e+03, gap 0.0000%
379 Set parameter MIPGap to value 1e-08
380 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
381
382 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
383 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
384
385 Optimize a model with 3035724 rows, 2395885 columns and 21185430 nonzeros
386 Model fingerprint: 0xf1374b93
387 Variable types: 1181973 continuous, 1213912 integer (1207162 binary)
388 Coefficient statistics:
389   Matrix range    [1e-01, 1e+10]
390   Objective range [6e-05, 5e+01]
391   Bounds range    [1e+00, 8e+01]
392   RHS range       [8e-01, 1e+10]
393 Warning: Model contains large matrix coefficients
394 Warning: Model contains large rhs
395   Consider reformulating model or setting NumericFocus parameter
396   to avoid numerical issues.
397 Presolve removed 3030897 rows and 2394264 columns (presolve time = 5s) ...
398 Presolve removed 3030979 rows and 2394287 columns
399 Presolve time: 6.17s
400 Presolved: 4745 rows, 1598 columns, 12583 nonzeros
401 Variable types: 10 continuous, 1588 integer (927 binary)
402 Found heuristic solution: objective 4046.4907358
403
404 Root simplex log...
405
406 Iteration   Objective      Primal Inf.   Dual Inf.    Time
407      0    1.0449000e+04  3.783137e+03  0.000000e+00   8s
408    1405    5.7134444e+03  0.000000e+00  0.000000e+00   8s
409
410 Root relaxation: objective 5.713444e+03, 1405 iterations, 0.01 seconds (0.01 work units)
411
412   Nodes | Current Node | Objective Bounds | Work
413 Expl Unexpl | Obj Depth IntInf | Incumbent  BestBd  Gap | It/Node Time
414
415   0   0 5713.44444   0  38 4046.49074 5713.44444  41.2%   -   7s

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416 0 0 5713.44444 0 18 4046.49074 5713.44444 41.2% - 7s
417 H 0 0 5073.3521103 5713.44444 12.6% - 7s
418 H 0 0 5388.0187770 5713.44444 6.04% - 8s
419 H 0 0 5708.3928106 5713.44444 0.09% - 8s
420 0 0 5713.17864 0 10 5708.39281 5713.17864 0.08% - 8s
421 0 0 cutoff 0 5708.39281 5708.39281 0.00% - 8s
422
423 Cutting planes:
424 Gomory: 7
425 Cover: 4
426 Implied bound: 2
427 Clique: 40
428 MIR: 2
429 Zero half: 3
430 RLT: 1
431
432 Explored 1 nodes (2669 simplex iterations) in 8.36 seconds (8.77 work units)
433 Thread count was 8 (of 8 available processors)
434
435 Solution count 4: 5708.39 5388.02 5073.35 4046.49
436
437 Optimal solution found (tolerance 1.00e-08)
438 Best objective 5.708392810563e+03, best bound 5.708392810563e+03, gap 0.0000%
439 SP is solved
440 SP's optimal solution is'□5708
441
442 Itr = 2
443 Collect_LB = [649.0, 5664.444444444443, 6279.054438167743]
444 Collect_UB = [10665.603174603173, 6270.1972953106, 6270.1972953106]
445 Collect_Hua = [0.0, 5008.301587301587, 5614.054438167743]
446 Collect_SPObjVal = [5008.301587301587, 5614.054438167743, 5708.392810563291]
447 Collect_MPObjValNHua = [649.0, 656.1428571428569, 665.0]
448
449
450 Ops, stop iteration
451 Values adopted from the Itr-1' th iteration, and Itr = {2}, judgeCount = {1}
452
453 ~~~~~judgeCount = 1, SPObj_SPF = 5614.054438167743
454 Vessel i: 0: pi: 0-5, ai-di: 9-20, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 9-20, taoi-deltai: 9-18, taoPi_SP-deltaPi_SP: 9-18, betaNi: 9, bi: 9
455 Vessel i: 1: pi: 0-5, ai-di: 33-51, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 33-51, taoi-deltai: 33-49, taoPi_SP-deltaPi_SP: 33-49, betaNi: 16, bi: 16
456 Vessel i: 2: pi: 0-5, ai-di: 57-67, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 57-67, taoi-deltai: 57-65, taoPi_SP-deltaPi_SP: 57-65, betaNi: 8, bi: 8
457 Vessel i: 3: pi: 5-10, ai-di: 15-27, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 15-27, taoi-deltai: 15-25, taoPi_SP-deltaPi_SP: 15-25, betaNi: 10, bi: 10
458 Vessel i: 4: pi: 5-10, ai-di: 42-62, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 42-62, taoi-deltai: 42-60, taoPi_SP-deltaPi_SP: 42-56, betaNi: 18, bi: 18
459 Vessel i: 5: pi: 12-18, ai-di: 17-40, gi_SP-gpi_SP: 0.000000-0.891036, ai_SP-di: 17-40, taoi-deltai: 18-28, taoPi_SP-deltaPi_SP: 18-28, betaNi: 10, bi: 10
460 Vessel i: 6: pi: 10-15, ai-di: 21-48, gi_SP-gpi_SP: 1.000000-0.339615, ai_SP-di: 29-48, taoi-deltai: 29-42, taoPi_SP-deltaPi_SP: 29-42, betaNi: 13, bi: 13
461 Vessel i: 7: pi: 28-34, ai-di: 37-57, gi_SP-gpi_SP: 0.400000-0.769350, ai_SP-di: 41-57, taoi-deltai: 40-44, taoPi_SP-deltaPi_SP: 41-44, betaNi: 4, bi: 4
462 Vessel i: 8: pi: 21-26, ai-di: 8-41, gi_SP-gpi_SP: 0.600000-1.000000, ai_SP-di: 12-41, taoi-deltai: 12-29, taoPi_SP-deltaPi_SP: 13-29, betaNi: 17, bi: 17
463 Vessel i: 9: pi: 16-21, ai-di: 25-58, gi_SP-gpi_SP: 1.000000-0.000000, ai_SP-di: 31-58, taoi-deltai: 32-54, taoPi_SP-deltaPi_SP: 32-54, betaNi: 22, bi: 22
464
465 round LB = [649, 5664, 6279]
466 round UB = [10666, 6270, 6270]
467 round Hua = [0, 5008, 5614]
468 round SPObjVal = [5008, 5614, 5708]
469 round MPObjValNHua = [649, 656, 665]
470
471 OptimalObj = 6279.054438167743
472 Time: 583.000000
473
474
475
476

```