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80 Bounds range [1e+00, 1e+00]
81 RHS range [8e-01, 1e+10]
82 Warning: Model contains large matrix coefficients
83 Warning: Model contains large rhs
84 Consider reformulating model or setting NumericFocus parameter
85 to avoid numerical issues.
86 Presolve removed 247826 rows and 8144 columns
87 Presolve time: 0.83s
88 Presolved: 4785 rows, 1474 columns, 12785 nonzeros
89 Variable types: 4 continuous, 1470 integer (840 binary)
90 Found heuristic solution: objective 3668.6666667
91 Found heuristic solution: objective 3808.6666667
92
93 Root relaxation: objective 5.138792e+03, 1365 iterations, 0.08 seconds (0.03 work units)
94
95 Nodes | Current Node | Objective Bounds | Work
96 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
97
98 0 0 5138.79167 0 33 3808.66667 5138.79167 34.9% - 1s
99 H 0 0 4760.1666667 5136.16667 7.90% - 1s
100 0 0 5136.16667 0 12 4760.16667 5136.16667 7.90% - 1s
101 H 0 0 5136.1666667 5136.16667 0.00% - 1s
102 0 0 5136.16667 0 12 5136.16667 5136.16667 0.00% - 1s
103
104 Cutting planes:
105 Gomory: 3
106 Implied bound: 3
107 Clique: 26
108 MIR: 4
109 Flow cover: 1
110 Zero half: 1
111 RLT: 1
112 Relax-and-lift: 2
113
114 Explored 1 nodes (2790 simplex iterations) in 1.38 seconds (0.66 work units)
115 Thread count was 8 (of 8 available processors)
116
117 Solution count 4: 5136.17 4760.17 3808.67 3668.67
118
119 Optimal solution found (tolerance 1.00e-08)
120 Best objective 5.136166666667e+03, best bound 5.136166666667e+03, gap 0.0000%
121 SP is solved
122 SP's optimal solution is'□5136
123
124 Itr = 0
125 Collect_LB = [957.0]
126 Collect_UB = [11229.333333333343]
127 Collect_Hua = [0.0]
128 Collect_SPObjVal = [5136.1666666666715]
129 Collect_MPObjValNHua = [957.0]
130
131
132 Set parameter MIPGap to value 0.05
133 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
134
135 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
136 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
137
138 Optimize a model with 403795 rows, 137605 columns and 1103944 nonzeros
139 Model fingerprint: 0x14abc000
140 Variable types: 1 continuous, 137604 integer (137580 binary)
141 Coefficient statistics:
142 Matrix range [1e+00, 1e+10]
143 Objective range [1e+00, 2e+01]
144 Bounds range [1e+00, 1e+00]
145 RHS range [1e+00, 2e+10]
146 Warning: Model contains large matrix coefficients
147 Warning: Model contains large rhs
148 Consider reformulating model or setting NumericFocus parameter
149 to avoid numerical issues.
150 Presolve removed 238372 rows and 120798 columns (presolve time = 5s) ...
151 Presolve removed 384612 rows and 130917 columns
152 Presolve time: 8.57s
153 Presolved: 19183 rows, 6688 columns, 85979 nonzeros
154 Variable types: 0 continuous, 6688 integer (6670 binary)
155
156 Root simplex log...
157
158 Iteration Objective Primal Inf. Dual Inf. Time
159 0 6.0406667e+03 9.430000e+02 0.000000e+00 9s
160 4654 6.0406667e+03 0.000000e+00 0.000000e+00 9s
161
162 Root relaxation: objective 6.040667e+03, 4654 iterations, 0.09 seconds (0.13 work units)
163

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164 Nodes | Current Node | Objective Bounds | Work
165 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
166
167 0 0 6040.66667 0 16 - 6040.66667 - - 8s
168 0 0 6040.66667 0 67 - 6040.66667 - - 10s
169 0 0 6040.66667 0 169 - 6040.66667 - - 10s
170 0 0 6040.66667 0 115 - 6040.66667 - - 14s
171 0 0 6040.66667 0 494 - 6040.66667 - - 15s
172 0 0 6040.66667 0 489 - 6040.66667 - - 15s
173 0 0 6040.66667 0 154 - 6040.66667 - - 19s
174 0 0 6040.66667 0 396 - 6040.66667 - - 21s
175 0 0 6040.66667 0 123 - 6040.66667 - - 23s
176 0 0 6040.66667 0 123 - 6040.66667 - - 24s
177 0 2 6040.66667 0 117 - 6040.66667 - - 26s
178 16 11 6040.66667 6 376 - 6040.66667 - 2591 30s
179 43 32 6040.66667 13 275 - 6040.66667 - 2381 35s
180 197 204 6040.66667 30 248 - 6040.66667 - 736 40s
181 * 235 204 67 6740.6666667 6040.66667 10.4% 620 40s
182 396 230 6060.66667 54 382 6740.66667 6040.66667 10.4% 457 45s
183 881 575 6060.66667 245 230 6740.66667 6040.66667 10.4% 233 50s
184 * 938 523 113 6540.6666667 6040.66667 7.64% 221 50s
185 H 969 390 6380.6666667 6040.66667 5.33% 233 51s
186 H 996 279 6300.6666667 6040.66667 4.13% 231 52s
187 H 996 227 6260.6666667 6040.66667 3.51% 231 52s
188
189 Cutting planes:
190 Learned: 922
191 Gomory: 1
192 Cover: 588
193 Implied bound: 289
194 Clique: 173
195 MIR: 204
196 StrongCG: 94
197 GUB cover: 6
198 Zero half: 16
199 RLT: 13
200 Relax-and-lift: 64
201 BQP: 4
202
203 Explored 1013 nodes (326652 simplex iterations) in 52.26 seconds (93.03 work units)
204 Thread count was 8 (of 8 available processors)
205
206 Solution count 5: 6260.67 6300.67 6380.67 ... 6740.67
207
208 Optimal solution found (tolerance 5.00e-02)
209 Best objective 6.26066666667e+03, best bound 6.04066666667e+03, gap 3.5140%
210 Set parameter MIPGap to value 1e-08
211 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
212
213 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
214 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
215
216 Optimize a model with 252611 rows, 9618 columns and 522175 nonzeros
217 Model fingerprint: 0x07d1d5c2
218 Variable types: 24 continuous, 9594 integer (5544 binary)
219 Coefficient statistics:
220 Matrix range [1e-01, 1e+10]
221 Objective range [6e-05, 5e+01]
222 Bounds range [1e+00, 1e+00]
223 RHS range [8e-01, 1e+10]
224 Warning: Model contains large matrix coefficients
225 Warning: Model contains large rhs
226 Consider reformulating model or setting NumericFocus parameter
227 to avoid numerical issues.
228 Presolve removed 246863 rows and 7848 columns
229 Presolve time: 0.23s
230 Presolved: 5748 rows, 1770 columns, 15223 nonzeros
231 Variable types: 4 continuous, 1766 integer (1017 binary)
232 Found heuristic solution: objective 3714.7551108
233
234 Root relaxation: objective 5.283667e+03, 1862 iterations, 0.02 seconds (0.02 work units)
235
236 Nodes | Current Node | Objective Bounds | Work
237 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
238
239 * 0 0 0 5283.6666667 5283.66667 0.00% - 0s
240
241 Explored 1 nodes (2851 simplex iterations) in 0.36 seconds (0.59 work units)
242 Thread count was 8 (of 8 available processors)
243
244 Solution count 2: 5283.67 3714.76
245
246 Optimal solution found (tolerance 1.00e-08)
247 Best objective 5.28366666667e+03, best bound 5.28366666667e+03, gap 0.0000%

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248 SP is solved
249 SP's optimal solution is'□5283
250
251 Itr = 1
252 Collect_LB = [957.0, 6260.6666666666715]
253 Collect_UB = [11229.333333333343, 6408.166666666668]
254 Collect_Hua = [0.0, 5136.1666666666715]
255 Collect_SPObjVal = [5136.1666666666715, 5283.666666666668]
256 Collect_MPObjValNHua = [957.0, 1124.5]
257
258
259 Set parameter MIPGap to value 0.05
260 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
261
262 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
263 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
264
265 Optimize a model with 403795 rows, 137605 columns and 1103944 nonzeros
266 Model fingerprint: 0x3730fd1c
267 Variable types: 1 continuous, 137604 integer (137580 binary)
268 Coefficient statistics:
269   Matrix range    [1e+00, 1e+10]
270   Objective range [1e+00, 2e+01]
271   Bounds range    [1e+00, 1e+00]
272   RHS range       [1e+00, 2e+10]
273 Warning: Model contains large matrix coefficients
274 Warning: Model contains large rhs
275   Consider reformulating model or setting NumericFocus parameter
276   to avoid numerical issues.
277 Presolve removed 238307 rows and 120806 columns (presolve time = 5s) ...
278 Presolve removed 384613 rows and 130917 columns
279 Presolve time: 8.33s
280 Presolved: 19182 rows, 6688 columns, 85971 nonzeros
281 Variable types: 0 continuous, 6688 integer (6670 binary)
282
283 Root simplex log...
284
285 Iteration   Objective      Primal Inf.   Dual Inf.    Time
286      0    6.1806667e+03   9.4300000e+02  0.0000000e+00   9s
287    4622    6.1806667e+03   0.0000000e+00  0.0000000e+00   9s
288
289 Root relaxation: objective 6.180667e+03, 4622 iterations, 0.11 seconds (0.13 work units)
290
291   Nodes | Current Node | Objective Bounds | Work
292 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
293
294    0    0 6180.66667    0 16      -6180.66667    - - 8s
295    0    0 6180.66667    0 167     -6180.66667    - - 9s
296    0    0 6180.66667    0 183     -6180.66667    - - 10s
297    0    0 6180.66667    0 191     -6180.66667    - - 10s
298    0    0 6180.66667    0 125     -6180.66667    - - 10s
299    0    0 6180.66667    0 191     -6180.66667    - - 16s
300    0    0 6180.66667    0 170     -6180.66667    - - 16s
301    0    0 6180.66667    0 488     -6180.66667    - - 18s
302    0    0 6180.66667    0 185     -6180.66667    - - 21s
303    0    0 6180.66667    0 564     -6180.66667    - - 22s
304    0    0 6180.66667    0 419     -6180.66667    - - 26s
305    0    0 6180.66667    0 402     -6180.66667    - - 27s
306    0    2 6180.66667    0 374     -6180.66667    - - 29s
307    5    6 6630.66667    3 177     -6180.66667    - 2930 31s
308   31   23 6756.83688    8 382      -6180.66667    - 2279 35s
309 H  46   33          6920.6666667 6180.66667 10.7% 1809 37s
310 *  76   35          6900.6666667 6180.66667 10.4% 1764 39s
311   77   41  cutoff  14    6900.66667 6180.66667 10.4% 1741 40s
312 H 165  124          6860.6666667 6180.66667 9.91%  921 41s
313 H 220  158          6780.6666667 6180.66667 8.85%  705 42s
314 H 262  196          6700.6666667 6180.72116 7.76%  628 43s
315 H 277  196          6660.6666667 6180.72116 7.21%  598 43s
316 H 284  196          6620.6666667 6180.72116 6.65%  584 43s
317 H 326  247          6580.6666667 6180.72116 6.08%  525 45s
318 H 354  247          6500.6666667 6180.72116 4.92%  485 45s
319
320 Cutting planes:
321   Learned: 3
322   Gomory: 8
323   Cover: 614
324   Implied bound: 312
325   Clique: 174
326   MIR: 177
327   StrongCG: 109
328   GUB cover: 66
329   Zero half: 51
330   RLT: 14
331   Relax-and-lift: 223

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332 BQP: 2
333
334 Explored 368 nodes (268675 simplex iterations) in 45.17 seconds (78.08 work units)
335 Thread count was 8 (of 8 available processors)
336
337 Solution count 9: 6500.67 6580.67 6620.67 ... 6920.67
338
339 Optimal solution found (tolerance 5.00e-02)
340 Best objective 6.500666666667e+03, best bound 6.200666666667e+03, gap 4.6149%
341 Set parameter MIPGap to value 1e-08
342 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
343
344 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
345 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
346
347 Optimize a model with 252611 rows, 9618 columns and 522175 nonzeros
348 Model fingerprint: 0x8b05bbc5
349 Variable types: 24 continuous, 9594 integer (5544 binary)
350 Coefficient statistics:
351   Matrix range    [1e-01, 1e+10]
352   Objective range [6e-05, 5e+01]
353   Bounds range    [1e+00, 1e+00]
354   RHS range       [8e-01, 1e+10]
355 Warning: Model contains large matrix coefficients
356 Warning: Model contains large rhs
357   Consider reformulating model or setting NumericFocus parameter
358   to avoid numerical issues.
359 Presolve removed 246724 rows and 7818 columns
360 Presolve time: 0.22s
361 Presolved: 5887 rows, 1800 columns, 15681 nonzeros
362 Variable types: 4 continuous, 1796 integer (1036 binary)
363 Found heuristic solution: objective 971.8435550
364 Found heuristic solution: objective 3879.6666667
365
366 Root relaxation: objective 5.430667e+03, 1594 iterations, 0.02 seconds (0.03 work units)
367
368   Nodes | Current Node | Objective Bounds | Work
369 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
370
371 H  0  0          5430.666667 16108.0000 197% - 0s
372   0  0 -  0  5430.66667 5430.66667 0.00% - 0s
373
374 Explored 1 nodes (2365 simplex iterations) in 0.36 seconds (0.58 work units)
375 Thread count was 8 (of 8 available processors)
376
377 Solution count 3: 5430.67 3879.67 971.844
378
379 Optimal solution found (tolerance 1.00e-08)
380 Best objective 5.430666666667e+03, best bound 5.430666666667e+03, gap 0.0000%
381 SP is solved
382 SP's optimal solution is'□5430
383
384 Itr = 2
385 Collect_LB = [957.0, 6260.666666666715, 6500.666666666668]
386 Collect_UB = [11229.333333333343, 6408.166666666668, 6408.166666666668]
387 Collect_Hua = [0.0, 5136.1666666666715, 5283.666666666668]
388 Collect_SPObjVal = [5136.1666666666715, 5283.666666666668, 5430.666666666668]
389 Collect_MPObjValNHua = [957.0, 1124.5, 1217.0]
390
391
392 Ops, stop iteration
393 Values adopted from the Itr-1' th iteration, and Itr = {2}, judgeCount = {1}
394
395 ~~~~~judgeCount = 1, SPObj_SPF = 5283.666666666668
396 Vessel i: 0: pi: 0-6, ai-di: 4-12, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 4-12, taoi-deltai: 4-10, taoPi_SP-deltaPi_SP: 4-7, betaNi: 6,
bi: 6
397 Vessel i: 1: pi: 0-7, ai-di: 20-54, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 20-54, taoi-deltai: 20-52, taoPi_SP-deltaPi_SP: 22-52, betaNi:
32, bi: 32
398 Vessel i: 2: pi: 7-14, ai-di: 24-60, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 24-60, taoi-deltai: 24-58, taoPi_SP-deltaPi_SP: 24-58, betaNi:
: 34, bi: 34
399 Vessel i: 3: pi: 27-34, ai-di: 31-55, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 31-55, taoi-deltai: 31-53, taoPi_SP-deltaPi_SP: 31-53,
betaNi: 22, bi: 22
400 Vessel i: 4: pi: 14-21, ai-di: 30-68, gi_SP-gpi_SP: 0.200000-1.000000, ai_SP-di: 31-68, taoi-deltai: 42-69, taoPi_SP-deltaPi_SP: 42-69,
betaNi: 27, bi: 27
401 Vessel i: 5: pi: 27-34, ai-di: 50-68, gi_SP-gpi_SP: 1.000000-0.200000, ai_SP-di: 58-68, taoi-deltai: 57-65, taoPi_SP-deltaPi_SP: 58-65,
betaNi: 8, bi: 8
402
403 round LB = [957, 6261, 6501]
404 round UB = [11229, 6408, 6408]
405 round Hua = [0, 5136, 5284]
406 round SPObjVal = [5136, 5284, 5431]
407 round MPObjValNHua = [957, 1124, 1217]
408
409 OptimalObj = 6500.666666666668

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unknown

410 Time: 169.000000
411
412
413
414