


```

80 Relax-and-lift: 4
81 BQP: 4
82
83 Explored 1 nodes (19221 simplex iterations) in 30.56 seconds (45.71 work units)
84 Thread count was 8 (of 8 available processors)
85
86 Solution count 4: 1017 2257 2637 3217
87
88 Optimal solution found (tolerance 1.00e-10)
89 Best objective 1.017000000000e+03, best bound 1.017000000000e+03, gap 0.0000%
90 Set parameter MIPGap to value 1e-08
91 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
92
93 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
94 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
95
96 Optimize a model with 2481755 rows, 1955335 columns and 17236424 nonzeros
97 Model fingerprint: 0xf2c50956
98 Variable types: 963295 continuous, 992040 integer (985965 binary)
99 Coefficient statistics:
100 Matrix range [1e-01, 1e+10]
101 Objective range [6e-05, 5e+01]
102 Bounds range [1e+00, 8e+01]
103 RHS range [8e-01, 1e+10]
104 Warning: Model contains large matrix coefficients
105 Warning: Model contains large rhs
106 Consider reformulating model or setting NumericFocus parameter
107 to avoid numerical issues.
108 Presolve removed 2478498 rows and 1954166 columns (presolve time = 5s) ...
109 Presolve removed 2478503 rows and 1954170 columns
110 Presolve time: 5.21s
111 Presolved: 3252 rows, 1165 columns, 8595 nonzeros
112 Variable types: 8 continuous, 1157 integer (659 binary)
113 Found heuristic solution: objective 4309.8302838
114
115 Root simplex log...
116
117 Iteration Objective Primal Inf. Dual Inf. Time
118 0 8.9802796e+03 8.166827e+03 0.000000e+00 7s
119 925 5.5971303e+03 0.000000e+00 0.000000e+00 7s
120
121 Root relaxation: objective 5.597130e+03, 925 iterations, 0.02 seconds (0.01 work units)
122
123 Nodes | Current Node | Objective Bounds | Work
124 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
125
126 0 0 5597.13028 0 18 4309.83028 5597.13028 29.9% - 6s
127 H 0 0 5595.3302838 5597.13028 0.03% - 6s
128 * 0 0 0 5596.8302838 5596.83028 0.00% - 6s
129
130 Cutting planes:
131 Learned: 1
132 MIR: 1
133 RLT: 1
134
135 Explored 1 nodes (1299 simplex iterations) in 6.87 seconds (7.57 work units)
136 Thread count was 8 (of 8 available processors)
137
138 Solution count 3: 5596.83 5595.33 4309.83
139
140 Optimal solution found (tolerance 1.00e-08)
141 Best objective 5.596830283766e+03, best bound 5.596830283766e+03, gap 0.0000%
142 SP is solved
143 SP's optimal solution is'□5596
144
145 Itr = 0
146 Collect_LB = [1017.0]
147 Collect_UB = [12210.660567532992]
148 Collect_Hua = [0.0]
149 Collect_SPObjVal = [5596.830283766496]
150 Collect_MPObjValNHua = [1017.0]
151
152
153 Set parameter TimeLimit to value 12000
154 Set parameter MIPGap to value 0.0005
155 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
156
157 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
158 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
159
160 Optimize a model with 590288 rows, 283978 columns and 1631276 nonzeros
161 Model fingerprint: 0xe1e5281d
162 Variable types: 1 continuous, 283977 integer (283941 binary)
163 Coefficient statistics:

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164 Matrix range [1e+00, 1e+10]
165 Objective range [1e+00, 2e+01]
166 Bounds range [1e+00, 1e+00]
167 RHS range [1e+00, 2e+10]
168 Warning: Model contains large matrix coefficients
169 Warning: Model contains large rhs
170 Consider reformulating model or setting NumericFocus parameter
171 to avoid numerical issues.
172 Presolve removed 461689 rows and 268157 columns (presolve time = 5s) ...
173 Presolve removed 552239 rows and 276983 columns
174 Presolve time: 6.50s
175 Presolved: 38049 rows, 6995 columns, 100890 nonzeros
176 Variable types: 0 continuous, 6995 integer (6976 binary)
177 Root relaxation presolved: 6995 rows, 45044 columns, 107885 nonzeros
178
179
180 Root simplex log...
181
182 Iteration Objective Primal Inf. Dual Inf. Time
183 0 handle free variables 7s
184 5945 7.0313303e+03 0.000000e+00 0.000000e+00 7s
185 5945 7.0313303e+03 0.000000e+00 0.000000e+00 7s
186
187 Root relaxation: objective 7.031330e+03, 5945 iterations, 0.50 seconds (0.96 work units)
188
189 Nodes | Current Node | Objective Bounds | Work
190 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
191
192 0 0 7031.33028 0 24 - 7031.33028 - - 7s
193 0 0 7031.33028 0 232 - 7031.33028 - - 8s
194 0 0 7031.33028 0 220 - 7031.33028 - - 8s
195 H 0 0 8511.3302838 7031.33028 17.4% - 8s
196 H 0 0 8471.3302838 7031.33028 17.0% - 8s
197 0 0 7031.33028 0 165 8471.33028 7031.33028 17.0% - 8s
198 0 0 7031.33028 0 69 8471.33028 7031.33028 17.0% - 9s
199 0 0 7031.33028 0 57 8471.33028 7031.33028 17.0% - 9s
200 0 0 7031.33028 0 108 8471.33028 7031.33028 17.0% - 9s
201 0 0 7031.33028 0 180 8471.33028 7031.33028 17.0% - 11s
202 0 0 7031.33028 0 140 8471.33028 7031.33028 17.0% - 11s
203 0 0 7031.33028 0 291 8471.33028 7031.33028 17.0% - 11s
204 0 0 7031.33028 0 142 8471.33028 7031.33028 17.0% - 11s
205 0 0 7031.33028 0 66 8471.33028 7031.33028 17.0% - 11s
206 0 0 7031.33028 0 35 8471.33028 7031.33028 17.0% - 12s
207 0 0 7031.33028 0 240 8471.33028 7031.33028 17.0% - 13s
208 0 0 7031.33028 0 231 8471.33028 7031.33028 17.0% - 13s
209 0 0 7031.33028 0 249 8471.33028 7031.33028 17.0% - 13s
210 0 0 7031.33028 0 222 8471.33028 7031.33028 17.0% - 13s
211 0 0 7031.33028 0 22 8471.33028 7031.33028 17.0% - 15s
212 0 0 7031.33028 0 118 8471.33028 7031.33028 17.0% - 15s
213 0 0 7031.33028 0 35 8471.33028 7031.33028 17.0% - 15s
214 0 0 7031.33028 0 118 8471.33028 7031.33028 17.0% - 16s
215 0 0 7031.33028 0 353 8471.33028 7031.33028 17.0% - 16s
216 0 0 7031.33028 0 322 8471.33028 7031.33028 17.0% - 16s
217 0 0 7031.33028 0 81 8471.33028 7031.33028 17.0% - 17s
218 0 0 7031.33028 0 81 8471.33028 7031.33028 17.0% - 17s
219 0 2 7031.33028 0 77 8471.33028 7031.33028 17.0% - 18s
220 35 36 7031.33028 8 213 8471.33028 7031.33028 17.0% 890 20s
221 238 237 7031.33028 41 152 8471.33028 7031.33028 17.0% 674 26s
222 H 248 237 7511.3302838 7031.33028 6.39% 680 26s
223 484 614 7031.33028 65 193 7511.33028 7031.33028 6.39% 478 30s
224 H 732 614 7071.3302838 7031.33028 0.57% 336 30s
225 * 1510 323 74 7031.3302838 7031.33028 0.00% 212 32s
226
227 Cutting planes:
228 Learned: 14
229 Gomory: 7
230 Lift-and-project: 1
231 Cover: 502
232 Implied bound: 2063
233 Clique: 101
234 MIR: 151
235 StrongCG: 98
236 GUB cover: 57
237 Zero half: 16
238 RLT: 13
239 Relax-and-lift: 34
240 BQP: 8
241
242 Explored 1592 nodes (402587 simplex iterations) in 32.99 seconds (65.75 work units)
243 Thread count was 8 (of 8 available processors)
244
245 Solution count 5: 7031.33 7071.33 7511.33 ... 8511.33
246
247 Optimal solution found (tolerance 5.00e-04)

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248 Best objective 7.031330283766e+03, best bound 7.031330283766e+03, gap 0.0000%
249 Set parameter MIPGap to value 1e-08
250 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
251
252 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
253 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
254
255 Optimize a model with 2481755 rows, 1955335 columns and 17236424 nonzeros
256 Model fingerprint: 0xdc66fb85
257 Variable types: 963295 continuous, 992040 integer (985965 binary)
258 Coefficient statistics:
259   Matrix range    [1e-01, 1e+10]
260   Objective range [6e-05, 5e+01]
261   Bounds range    [1e+00, 8e+01]
262   RHS range       [8e-01, 1e+10]
263 Warning: Model contains large matrix coefficients
264 Warning: Model contains large rhs
265   Consider reformulating model or setting NumericFocus parameter
266   to avoid numerical issues.
267 Presolve removed 2476484 rows and 1953532 columns
268 Presolve time: 4.99s
269 Presolved: 5271 rows, 1803 columns, 14076 nonzeros
270 Variable types: 8 continuous, 1795 integer (1042 binary)
271 Found heuristic solution: objective 4233.8302838
272 Found heuristic solution: objective 4253.8302838
273
274 Root simplex log...
275
276 Iteration   Objective      Primal Inf.   Dual Inf.    Time
277      0   1.1487280e+04  8.733382e+03  0.000000e+00  6s
278   1576  6.0871303e+03  0.000000e+00  0.000000e+00  6s
279
280 Root relaxation: objective 6.087130e+03, 1576 iterations, 0.02 seconds (0.02 work units)
281
282   Nodes | Current Node | Objective Bounds | Work
283 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
284
285      0   0 6087.13028   0 17 4253.83028 6087.13028 43.1% - 6s
286 H   0   0           6086.8302838 6087.13028 0.00% - 6s
287
288 Cutting planes:
289   Learned: 2
290   Gomory: 1
291   Cover: 10
292   Implied bound: 15
293   MIR: 2
294
295 Explored 1 nodes (2136 simplex iterations) in 6.62 seconds (7.38 work units)
296 Thread count was 8 (of 8 available processors)
297
298 Solution count 3: 6086.83 4253.83 4233.83
299
300 Optimal solution found (tolerance 1.00e-08)
301 Best objective 6.086830283766e+03, best bound 6.086830283766e+03, gap 0.0000%
302 SP is solved
303 SP's optimal solution is'□6086
304
305 Itr = 1
306 Collect_LB = [1017.0, 7031.330283766496]
307 Collect_UB = [12210.660567532992, 7521.330283766496]
308 Collect_Hua = [0.0, 5596.830283766496]
309 Collect_SPObjVal = [5596.830283766496, 6086.830283766496]
310 Collect_MPObjValNHua = [1017.0, 1434.5]
311
312
313 Set parameter TimeLimit to value 12000
314 Set parameter MIPGap to value 0.0005
315 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
316
317 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
318 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
319
320 Optimize a model with 590289 rows, 283978 columns and 1631295 nonzeros
321 Model fingerprint: 0x9da4c12a
322 Variable types: 1 continuous, 283977 integer (283941 binary)
323 Coefficient statistics:
324   Matrix range    [1e+00, 1e+10]
325   Objective range [1e+00, 2e+01]
326   Bounds range    [1e+00, 1e+00]
327   RHS range       [1e+00, 2e+10]
328 Warning: Model contains large matrix coefficients
329 Warning: Model contains large rhs
330   Consider reformulating model or setting NumericFocus parameter
331   to avoid numerical issues.

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```
332 Presolve removed 461690 rows and 268157 columns (presolve time = 5s) ...
333 Presolve removed 552240 rows and 276983 columns
334 Presolve time: 6.47s
335 Presolved: 38049 rows, 6995 columns, 100890 nonzeros
336 Variable types: 0 continuous, 6995 integer (6976 binary)
337 Root relaxation presolved: 6995 rows, 45044 columns, 107885 nonzeros
338
339
340 Root simplex log...
341
342 Iteration   Objective      Primal Inf.   Dual Inf.    Time
343      0      handle free variables              7s
344    5945    7.5213303e+03  0.000000e+00  0.000000e+00   7s
345    5945    7.5213303e+03  0.000000e+00  0.000000e+00   7s
346
347 Root relaxation: objective 7.521330e+03, 5945 iterations, 0.50 seconds (0.96 work units)
348
349 Nodes | Current Node | Objective Bounds | Work
350 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
351
352 0 0 7521.33028 0 24 -7521.33028 - - 7s
353 0 0 7521.33028 0 232 -7521.33028 - - 8s
354 0 0 7521.33028 0 220 -7521.33028 - - 8s
355 H 0 0 9001.3302838 7521.33028 16.4% - 8s
356 H 0 0 8961.3302838 7521.33028 16.1% - 8s
357 0 0 7521.33028 0 165 8961.33028 7521.33028 16.1% - 8s
358 0 0 7521.33028 0 69 8961.33028 7521.33028 16.1% - 9s
359 0 0 7521.33028 0 57 8961.33028 7521.33028 16.1% - 9s
360 0 0 7521.33028 0 108 8961.33028 7521.33028 16.1% - 9s
361 0 0 7521.33028 0 180 8961.33028 7521.33028 16.1% - 11s
362 0 0 7521.33028 0 140 8961.33028 7521.33028 16.1% - 11s
363 0 0 7521.33028 0 291 8961.33028 7521.33028 16.1% - 11s
364 0 0 7521.33028 0 142 8961.33028 7521.33028 16.1% - 11s
365 0 0 7521.33028 0 66 8961.33028 7521.33028 16.1% - 11s
366 0 0 7521.33028 0 35 8961.33028 7521.33028 16.1% - 13s
367 0 0 7521.33028 0 240 8961.33028 7521.33028 16.1% - 13s
368 0 0 7521.33028 0 231 8961.33028 7521.33028 16.1% - 13s
369 0 0 7521.33028 0 249 8961.33028 7521.33028 16.1% - 13s
370 0 0 7521.33028 0 222 8961.33028 7521.33028 16.1% - 13s
371 0 0 7521.33028 0 22 8961.33028 7521.33028 16.1% - 15s
372 0 0 7521.33028 0 118 8961.33028 7521.33028 16.1% - 15s
373 0 0 7521.33028 0 35 8961.33028 7521.33028 16.1% - 15s
374 0 0 7521.33028 0 118 8961.33028 7521.33028 16.1% - 16s
375 0 0 7521.33028 0 353 8961.33028 7521.33028 16.1% - 16s
376 0 0 7521.33028 0 322 8961.33028 7521.33028 16.1% - 16s
377 0 0 7521.33028 0 81 8961.33028 7521.33028 16.1% - 17s
378 0 0 7521.33028 0 81 8961.33028 7521.33028 16.1% - 17s
379 0 2 7521.33028 0 77 8961.33028 7521.33028 16.1% - 18s
380 19 21 7521.33028 4 321 8961.33028 7521.33028 16.1% 1492 20s
381 56 58 7521.33028 13 148 8961.33028 7521.33028 16.1% 859 25s
382 238 237 7521.33028 41 152 8961.33028 7521.33028 16.1% 674 30s
383 H 248 237 8001.3302838 7521.33028 6.00% 680 30s
384 * 713 557 115 7561.3302838 7521.33028 0.53% 336 34s
385 987 284 cutoff 127 7561.33028 7521.33028 0.53% 250 35s
386 * 1210 284 53 7521.3302838 7521.33028 0.00% 214 35s
387
388 Cutting planes:
389 Learned: 8
390 Gomory: 6
391 Lift-and-project: 1
392 Cover: 276
393 Implied bound: 2017
394 Clique: 66
395 MIR: 125
396 StrongCG: 75
397 GUB cover: 47
398 Zero half: 9
399 RLT: 10
400 Relax-and-lift: 20
401 BQP: 7
402
403 Explored 1444 nodes (345605 simplex iterations) in 35.75 seconds (61.60 work units)
404 Thread count was 8 (of 8 available processors)
405
406 Solution count 5: 7521.33 7561.33 8001.33 ... 9001.33
407
408 Optimal solution found (tolerance 5.00e-04)
409 Best objective 7.521330283766e+03, best bound 7.521330283766e+03, gap 0.0000%
410 Set parameter MIPGap to value 1e-08
411 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
412
413 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
414 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
415
```

```

416 Optimize a model with 2481755 rows, 1955335 columns and 17236424 nonzeros
417 Model fingerprint: 0x9c1c0565
418 Variable types: 963295 continuous, 992040 integer (985965 binary)
419 Coefficient statistics:
420   Matrix range   [1e-01, 1e+10]
421   Objective range [6e-05, 5e+01]
422   Bounds range   [1e+00, 8e+01]
423   RHS range      [8e-01, 1e+10]
424 Warning: Model contains large matrix coefficients
425 Warning: Model contains large rhs
426   Consider reformulating model or setting NumericFocus parameter
427   to avoid numerical issues.
428 Presolve removed 2476578 rows and 1953561 columns
429 Presolve time: 4.91s
430 Presolved: 5177 rows, 1774 columns, 13825 nonzeros
431 Variable types: 8 continuous, 1766 integer (1027 binary)
432 Found heuristic solution: objective 4233.8302838
433
434 Root simplex log...
435
436 Iteration   Objective      Primal Inf.   Dual Inf.    Time
437      0  1.1287280e+04  8.580382e+03  0.000000e+00   6s
438    1458  6.0871303e+03  0.000000e+00  0.000000e+00   6s
439
440 Root relaxation: objective 6.087130e+03, 1458 iterations, 0.02 seconds (0.02 work units)
441
442   Nodes | Current Node | Objective Bounds | Work
443 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
444
445    0    0 6087.13028    0 17 4233.83028 6087.13028 43.8% - 6s
446 H    0    0          6086.8302838 6087.13028 0.00% - 6s
447
448 Cutting planes:
449   Learned: 2
450   Cover: 10
451   Implied bound: 15
452   MIR: 2
453
454 Explored 1 nodes (1976 simplex iterations) in 6.52 seconds (7.30 work units)
455 Thread count was 8 (of 8 available processors)
456
457 Solution count 2: 6086.83 4233.83
458
459 Optimal solution found (tolerance 1.00e-08)
460 Best objective 6.086830283766e+03, best bound 6.086830283766e+03, gap 0.0000%
461 SP is solved
462 SP's optimal solution is'□6086
463
464 Itr = 2
465 Collect_LB = [1017.0, 7031.330283766496, 7521.330283766496]
466 Collect_UB = [12210.660567532992, 7521.330283766496, 7521.330283766496]
467 Collect_Hua = [0.0, 5596.830283766496, 6086.830283766496]
468 Collect_SPObjVal = [5596.830283766496, 6086.830283766496, 6086.830283766496]
469 Collect_MPObjValNHua = [1017.0, 1434.5, 1434.5]
470
471
472 Reach the termination conditions, stop iteration
473 Values adopted from the Itr' th iteration, and Itr = {2}, judgeCount = {2}
474
475 ~~~~~judge = 2, SPObj SPF = 6086.830283766496
476 Vessel i: 0: pi: 0-6, ai-di: 7-27, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 7-27, taoi-deltai: 7-29, taoPi_SP-deltaPi_SP: 7-29, betaNi: 22
, bi: 22
477 Vessel i: 1: pi: 12-18, ai-di: 9-18, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 9-18, taoi-deltai: 9-18, taoPi_SP-deltaPi_SP: 9-18, betaNi: 9
, bi: 9
478 Vessel i: 2: pi: 6-12, ai-di: 11-40, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 11-40, taoi-deltai: 11-42, taoPi_SP-deltaPi_SP: 11-42, betaNi
: 31, bi: 31
479 Vessel i: 3: pi: 18-24, ai-di: 17-31, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 17-31, taoi-deltai: 17-27, taoPi_SP-deltaPi_SP: 17-27,
betaNi: 10, bi: 10
480 Vessel i: 4: pi: 28-34, ai-di: 18-23, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 18-23, taoi-deltai: 18-23, taoPi_SP-deltaPi_SP: 18-23,
betaNi: 5, bi: 5
481 Vessel i: 5: pi: 27-34, ai-di: 26-30, gi_SP-gpi_SP: 0.025000-1.000000, ai_SP-di: 26-30, taoi-deltai: 27-32, taoPi_SP-deltaPi_SP: 27-32,
betaNi: 5, bi: 5
482 Vessel i: 6: pi: 16-22, ai-di: 33-42, gi_SP-gpi_SP: 0.375000-0.200000, ai_SP-di: 36-42, taoi-deltai: 36-45, taoPi_SP-deltaPi_SP: 36-45,
betaNi: 9, bi: 9
483 Vessel i: 7: pi: 14-20, ai-di: 37-68, gi_SP-gpi_SP: 1.000000-0.600000, ai_SP-di: 47-68, taoi-deltai: 47-77, taoPi_SP-deltaPi_SP: 47-77,
betaNi: 30, bi: 30
484 Vessel i: 8: pi: 22-28, ai-di: 46-64, gi_SP-gpi_SP: 1.000000-0.600000, ai_SP-di: 53-64, taoi-deltai: 53-74, taoPi_SP-deltaPi_SP: 53-74,
betaNi: 21, bi: 21
485
486 round LB = [1017, 7031, 7521]
487 round UB = [12211, 7521, 7521]
488 round Hua = [0, 5597, 6087]
489 round SPObjVal = [5597, 6087, 6087]
490 round MPObjValNHua = [1017, 1434, 1434]

```

unknown

491
492 OptimalObj = 7521.330283766496
493 Time: 556.000000
494
495
496
497