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80 Set parameter MIPGap to value 1e-08
81 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
82
83 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
84 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
85
86 Optimize a model with 1153684 rows, 901813 columns and 7829291 nonzeros
87 Model fingerprint: 0x84063345
88 Variable types: 441325 continuous, 460488 integer (456438 binary)
89 Coefficient statistics:
90   Matrix range    [1e-01, 1e+10]
91   Objective range [6e-05, 5e+01]
92   Bounds range   [1e+00, 8e+01]
93   RHS range      [8e-01, 1e+10]
94 Warning: Model contains large matrix coefficients
95 Warning: Model contains large rhs
96   Consider reformulating model or setting NumericFocus parameter
97   to avoid numerical issues.
98 Presolve removed 1151313 rows and 900957 columns
99 Presolve time: 2.74s
100 Presolved: 2371 rows, 856 columns, 6316 nonzeros
101 Variable types: 0 continuous, 856 integer (503 binary)
102 Found heuristic solution: objective 4207.6666667
103
104 Root relaxation: objective 5.149667e+03, 652 iterations, 0.01 seconds (0.01 work units)
105
106   Nodes | Current Node | Objective Bounds | Work
107   Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
108
109 *    0     0          0  5149.6666667 5149.66667 0.00%   -   3s
110
111 Explored 1 nodes (652 simplex iterations) in 3.58 seconds (3.48 work units)
112 Thread count was 8 (of 8 available processors)
113
114 Solution count 2: 5149.67 4207.67
115
116 Optimal solution found (tolerance 1.00e-08)
117 Best objective 5.14966666667e+03, best bound 5.14966666667e+03, gap 0.0000%
118 SP is solved
119 SP's optimal solution is'□5149
120
121   Itr = 0
122 Collect_LB = [804.0]
123 Collect_UB = [11103.333333333336]
124 Collect_Hua = [0.0]
125 Collect_SPObjVal = [5149.666666666668]
126 Collect_MPObjValNHua = [804.0]
127
128
129 Set parameter MIPGap to value 0.05
130 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
131
132 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
133 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
134
135 Optimize a model with 619788 rows, 150727 columns and 1825935 nonzeros
136 Model fingerprint: 0x6b305609
137 Variable types: 1 continuous, 150726 integer (143124 binary)
138 Coefficient statistics:
139   Matrix range    [1e-01, 1e+10]
140   Objective range [1e+00, 2e+01]
141   Bounds range   [1e+00, 1e+00]
142   RHS range      [1e+00, 2e+10]
143 Warning: Model contains large matrix coefficients
144 Warning: Model contains large rhs
145   Consider reformulating model or setting NumericFocus parameter
146   to avoid numerical issues.
147 Presolve removed 457892 rows and 131808 columns (presolve time = 5s) ...
148 Presolve removed 457892 rows and 131808 columns (presolve time = 10s) ...
149 Presolve removed 457892 rows and 131808 columns (presolve time = 15s) ...
150 Presolve removed 540701 rows and 140038 columns (presolve time = 20s) ...
151 Presolve removed 568819 rows and 140043 columns
152 Presolve time: 20.78s
153 Presolved: 50969 rows, 10684 columns, 198392 nonzeros
154 Variable types: 0 continuous, 10684 integer (8834 binary)
155
156 Deterministic concurrent LP optimizer: primal and dual simplex (primal and dual model)
157 Showing first log only...
158
159 Root relaxation presolved: 50969 rows, 10684 columns, 198392 nonzeros
160
161
162 Root simplex log...
163

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164 Iteration Objective Primal Inf. Dual Inf. Time
165 0 9.2400000e+02 2.328407e+03 1.517823e+09 22s
166 Concurrent spin time: 0.17s
167
168 Solved with dual simplex (primal model)
169
170 Root relaxation: objective 6.073667e+03, 4608 iterations, 0.87 seconds (0.64 work units)
171
172 Nodes | Current Node | Objective Bounds | Work
173 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
174
175 0 0 6073.66667 0 151 -6073.66667 - - 23s
176 0 0 6073.66667 0 427 -6073.66667 - - 27s
177 0 0 6073.66667 0 570 -6073.66667 - - 27s
178 0 0 6073.66667 0 493 -6073.66667 - - 28s
179 0 0 6073.66667 0 491 -6073.66667 - - 28s
180 0 0 6073.66667 0 402 -6073.66667 - - 29s
181 0 0 6073.66667 0 133 -6073.66667 - - 33s
182 0 0 6073.66667 0 133 -6073.66667 - - 33s
183 0 0 6073.66667 0 244 -6073.66667 - - 34s
184 0 0 6073.66667 0 117 -6073.66667 - - 43s
185 0 0 6073.66667 0 97 -6073.66667 - - 43s
186 0 0 6073.66667 0 152 -6073.66667 - - 45s
187 0 0 6073.66667 0 148 -6073.66667 - - 45s
188 H 0 0 6073.6666667 6073.66667 0.00% - 53s
189 0 0 6073.66667 0 202 6073.66667 6073.66667 0.00% - 53s
190
191 Cutting planes:
192 Gomory: 10
193 Cover: 407
194 Implied bound: 825
195 Clique: 1465
196 MIR: 194
197 StrongCG: 15
198 Flow cover: 2
199 GUB cover: 41
200 Zero half: 30
201 RLT: 35
202 Relax-and-lift: 890
203 BQP: 18
204 PSD: 1
205
206 Explored 1 nodes (48234 simplex iterations) in 53.14 seconds (37.31 work units)
207 Thread count was 8 (of 8 available processors)
208
209 Solution count 1: 6073.67
210
211 Optimal solution found (tolerance 5.00e-02)
212 Best objective 6.07366666667e+03, best bound 6.073666666667e+03, gap 0.0000%
213 Set parameter MIPGap to value 1e-08
214 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
215
216 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
217 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
218
219 Optimize a model with 1153684 rows, 901813 columns and 7829291 nonzeros
220 Model fingerprint: 0x03399a85
221 Variable types: 441325 continuous, 460488 integer (456438 binary)
222 Coefficient statistics:
223 Matrix range [1e-01, 1e+10]
224 Objective range [6e-05, 5e+01]
225 Bounds range [1e+00, 8e+01]
226 RHS range [8e-01, 1e+10]
227 Warning: Model contains large matrix coefficients
228 Warning: Model contains large rhs
229 Consider reformulating model or setting NumericFocus parameter
230 to avoid numerical issues.
231 Presolve removed 1148884 rows and 900158 columns
232 Presolve time: 2.71s
233 Presolved: 4800 rows, 1655 columns, 12735 nonzeros
234 Variable types: 4 continuous, 1651 integer (960 binary)
235 Found heuristic solution: objective 3772.8300722
236
237 Root relaxation: objective 5.402667e+03, 1384 iterations, 0.02 seconds (0.01 work units)
238
239 Nodes | Current Node | Objective Bounds | Work
240 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
241
242 H 0 0 5402.6666667 14440.0000 167% - 3s
243 0 0 - 0 5402.66667 5402.66667 0.00% - 3s
244
245 Explored 1 nodes (1986 simplex iterations) in 3.60 seconds (3.30 work units)
246 Thread count was 8 (of 8 available processors)
247

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248 Solution count 2: 5402.67 3772.83
249
250 Optimal solution found (tolerance 1.00e-08)
251 Best objective 5.40266666667e+03, best bound 5.402666666667e+03, gap 0.0000%
252 SP is solved
253 SP's optimal solution is'□5402
254
255 Itr = 1
256 Collect_LB = [804.0, 6073.666666666666]
257 Collect_UB = [11103.333333333336, 6326.666666666668]
258 Collect_Hua = [0.0, 5149.666666666666]
259 Collect_SPObjVal = [5149.666666666668, 5402.666666666668]
260 Collect_MPObjValNHua = [804.0, 924.0]
261
262
263 Set parameter MIPGap to value 0.05
264 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
265
266 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
267 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
268
269 Optimize a model with 872342 rows, 163849 columns and 2642827 nonzeros
270 Model fingerprint: 0x2336ce8c
271 Variable types: 1 continuous, 163848 integer (148668 binary)
272 Coefficient statistics:
273 Matrix range [1e-01, 1e+10]
274 Objective range [1e+00, 2e+01]
275 Bounds range [1e+00, 1e+00]
276 RHS range [1e+00, 2e+10]
277 Warning: Model contains large matrix coefficients
278 Warning: Model contains large rhs
279 Consider reformulating model or setting NumericFocus parameter
280 to avoid numerical issues.
281 Presolve removed 670594 rows and 139786 columns (presolve time = 5s) ...
282 Presolve removed 681093 rows and 140834 columns (presolve time = 10s) ...
283 Presolve removed 681093 rows and 140834 columns (presolve time = 15s) ...
284 Presolve removed 768112 rows and 148889 columns
285 Presolve time: 17.62s
286 Presolved: 104230 rows, 14960 columns, 337457 nonzeros
287 Variable types: 0 continuous, 14960 integer (11278 binary)
288
289 Deterministic concurrent LP optimizer: primal and dual simplex (primal and dual model)
290 Showing first log only...
291
292 Root relaxation presolved: 14960 rows, 119190 columns, 352417 nonzeros
293
294
295 Root simplex log...
296
297 Iteration Objective Primal Inf. Dual Inf. Time
298 0 6.3266667e+03 0.000000e+00 6.277989e+04 19s
299 Concurrent spin time: 0.50s
300
301 Solved with dual simplex (primal model)
302
303 Root relaxation: objective 6.326667e+03, 6079 iterations, 2.04 seconds (1.63 work units)
304
305 Nodes | Current Node | Objective Bounds | Work
306 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
307
308 0 0 6326.66667 0 115 - 6326.66667 - - 23s
309 0 0 6326.66667 0 607 - 6326.66667 - - 27s
310 0 0 6326.66667 0 521 - 6326.66667 - - 28s
311 0 0 6326.66667 0 699 - 6326.66667 - - 30s
312 0 0 6326.66667 0 688 - 6326.66667 - - 30s
313 0 0 6326.66667 0 106 - 6326.66667 - - 34s
314 0 0 6326.66667 0 105 - 6326.66667 - - 34s
315 0 0 6326.66667 0 155 - 6326.66667 - - 35s
316 0 0 6326.66667 0 77 - 6326.66667 - - 38s
317 0 0 6326.66667 0 112 - 6326.66667 - - 38s
318 0 0 6326.66667 0 228 - 6326.66667 - - 40s
319 0 0 6326.66667 0 258 - 6326.66667 - - 40s
320 0 0 6326.66667 0 130 - 6326.66667 - - 43s
321 0 0 6326.66667 0 133 - 6326.66667 - - 44s
322 0 0 6326.66667 0 72 - 6326.66667 - - 46s
323 0 2 6326.66667 0 70 - 6326.66667 - - 53s
324 1 4 6326.66667 1 136 - 6326.66667 - 5278 55s
325 7 12 6326.66667 3 183 - 6326.66667 - 3235 60s
326 15 20 6326.66667 4 369 - 6326.66667 - 2722 67s
327 23 28 6326.66667 6 497 - 6326.66667 - 2714 70s
328 33 38 6326.66667 7 518 - 6326.66667 - 2566 76s
329 37 48 6326.66667 7 510 - 6326.66667 - 3102 81s
330 47 83 6326.66667 11 125 - 6326.66667 - 3380 90s
331 102 144 6326.66667 29 31 - 6326.66667 - 2174 102s

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332 * 148 144      72 6326.6666667 6326.66667 0.00% 1502 102s
333
334 Cutting planes:
335   Learned: 1
336   Gomory: 6
337   Cover: 412
338   Implied bound: 66
339   Clique: 2611
340   MIR: 94
341   StrongCG: 26
342   Flow cover: 4
343   GUB cover: 41
344   Zero half: 37
345   RLT: 46
346   Relax-and-lift: 623
347   BQP: 22
348   PSD: 4
349
350 Explored 201 nodes (325493 simplex iterations) in 102.36 seconds (153.47 work units)
351 Thread count was 8 (of 8 available processors)
352
353 Solution count 1: 6326.67
354
355 Optimal solution found (tolerance 5.00e-02)
356 Best objective 6.32666666667e+03, best bound 6.32666666667e+03, gap 0.0000%
357 Warning: linear constraint 367235 and linear constraint 619789 have the same name "ConSP25_1[0,0]"
358 Set parameter MIPGap to value 1e-08
359 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
360
361 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
362 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
363
364 Optimize a model with 1153684 rows, 901813 columns and 7829291 nonzeros
365 Model fingerprint: 0xc36b8a52
366 Variable types: 441325 continuous, 460488 integer (456438 binary)
367 Coefficient statistics:
368   Matrix range    [1e-01, 1e+10]
369   Objective range [6e-05, 5e+01]
370   Bounds range    [1e+00, 8e+01]
371   RHS range       [8e-01, 1e+10]
372 Warning: Model contains large matrix coefficients
373 Warning: Model contains large rhs
374   Consider reformulating model or setting NumericFocus parameter
375   to avoid numerical issues.
376 Presolve removed 1148165 rows and 899983 columns
377 Presolve time: 2.96s
378 Presolved: 5519 rows, 1830 columns, 14680 nonzeros
379 Variable types: 4 continuous, 1826 integer (1050 binary)
380 Found heuristic solution: objective 3825.2733636
381
382 Root relaxation: objective 5.402667e+03, 1469 iterations, 0.02 seconds (0.02 work units)
383
384   Nodes | Current Node | Objective Bounds | Work
385   Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
386
387 H  0  0          5402.666667 16220.0000 200% - 3s
388   0  0 - 0      5402.66667 5402.66667 0.00% - 3s
389
390 Explored 1 nodes (1867 simplex iterations) in 4.10 seconds (3.29 work units)
391 Thread count was 8 (of 8 available processors)
392
393 Solution count 2: 5402.67 3825.27
394
395 Optimal solution found (tolerance 1.00e-08)
396 Best objective 5.40266666667e+03, best bound 5.40266666667e+03, gap 0.0000%
397 SP is solved
398 SP's optimal solution is' 5402
399
400 Itr = 2
401 Collect_LB = [804.0, 6073.666666666666, 6326.666666666666]
402 Collect_UB = [11103.333333333336, 6326.666666666668, 6326.666666666668]
403 Collect_Hua = [0.0, 5149.666666666666, 5402.666666666666]
404 Collect_SPObjVal = [5149.666666666668, 5402.666666666668, 5402.666666666668]
405 Collect_MPObjValNHua = [804.0, 924.0, 924.0]
406
407
408 Reach the termination conditions, stop iteration
409 Values adopted from the Itr' th iteration, and Itr = {2}, judgeCount = {2}
410
411 ~~~~~judge = 2, SPObj_SPF = 5402.666666666668
412 Vessel i: 0: pi: 7-13, ai-di: 3-37, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 3-37, taoi-deltai: 3-35, taoPi_SP-deltaPi_SP: 3-35, betaNi: 32
, bi: 32
413 Vessel i: 1: pi: 13-20, ai-di: 17-33, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 17-33, taoi-deltai: 17-31, taoPi_SP-deltaPi_SP: 17-31,
betaNi: 14, bi: 14
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414	Vessel i: 2: betaNi: 24,	pi: 20-26, bi: 24	ai-di: 23-49,	gi_SP-gpi_SP: 0.000000-0.000000,	ai_SP-di: 23-49,	taoi-deltai: 23-47,	taoPi_SP-deltaPi_SP: 23-47,
415	Vessel i: 3: betaNi: 14,	pi: 11-17, bi: 14	ai-di: 41-57,	gi_SP-gpi_SP: 0.000000-0.000000,	ai_SP-di: 41-57,	taoi-deltai: 41-55,	taoPi_SP-deltaPi_SP: 41-55,
416	Vessel i: 4: betaNi: 22,	pi: 17-23, bi: 22	ai-di: 50-74,	gi_SP-gpi_SP: 0.200000-1.000000,	ai_SP-di: 51-74,	taoi-deltai: 51-73,	taoPi_SP-deltaPi_SP: 51-73,
417	Vessel i: 5: betaNi: 22,	pi: 10-17, bi: 22	ai-di: 51-75,	gi_SP-gpi_SP: 1.000000-0.200000,	ai_SP-di: 58-75,	taoi-deltai: 59-81,	taoPi_SP-deltaPi_SP: 59-81,
418							
419	round LB = [804, 6074, 6327]						
420	round UB = [11103, 6327, 6327]						
421	round Hua = [0, 5150, 5403]						
422	round SPObjVal = [5150, 5403, 5403]						
423	round MPObjValNHua = [804, 924, 924]						
424							
425	Time: 495.000000						
426							
427							
428							
429							