```
this paper\Scripts\python.exe" "D:\Python\Pycharm\setroute\PyCharm Community Edition 2021.2.3\plugins\python-ce\helpers\pydev\pydevconsole.py" --mode=
   client --port=42649
 3
   import sys; print('Python %s on %s' % (sys.version, sys.platform))
 4
   6
   PyDev console: starting.
   Python 3.9.7 (tags/v3.9.7:1016ef3, Aug 30 2021, 20:19:38) [MSC v.1929 64 bit (AMD64)] on win32
 8
   paper')
10
   Backend TkAgg is interactive backend. Turning interactive mode on.
   Waiting 5s.....
12
13
   Warning: your license will expire in 14 days
14
15
16
17
   Set parameter TimeLimit to value 10800
   Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
19
20
   CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
21
   Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
23
   Optimize a model with 1205076 rows, 80570 columns and 3612810 nonzeros
   Model fingerprint: 0xa930af42
24
   Variable types: 0 continuous, 80570 integer (67900 binary)
26
   Coefficient statistics:
    Matrix range [1e-01, 1e+15]
27
28
    Objective range [1e+00, 5e+01]
    Bounds range [1e+00, 1e+00]
29
30
    RHS range
                [1e+00, 2e+15]
   Warning: Model contains large matrix coefficient range
31
32
   Warning: Model contains large rhs
33
       Consider reformulating model or setting NumericFocus parameter
       to avoid numerical issues.
34
35
   Presolve removed 868436 rows and 44277 columns (presolve time = 5s) ...
   Presolve removed 922040 rows and 46882 columns (presolve time = 10s) ...
   Presolve removed 922040 rows and 46882 columns (presolve time = 15s) ...
   Presolve removed 1005086 rows and 56581 columns
38
39
   Presolve time: 16.87s
   Presolved: 199990 rows, 23989 columns, 620753 nonzeros
40
41
   Variable types: 0 continuous, 23989 integer (23595 binary)
42
43
   Deterministic concurrent LP optimizer: primal simplex, dual simplex, and barrier
44
   Showing barrier log only...
45
46
   Root relaxation presolved: 23975 rows, 223937 columns, 642784 nonzeros
48
   Root barrier log...
49
50
  Ordering time: 4.87s
51
52
   Barrier statistics:
53
   Dense cols: 78
   Free vars: 404
   AA' NZ : 1.064e+06
   Factor NZ: 7.342e+07 (roughly 700 MB of memory)
56
57
    Factor Ops: 4.333e+11 (roughly 12 seconds per iteration)
58
    Threads: 1
59
   Barrier performed 0 iterations in 24.42 seconds (35.89 work units)
60
   Barrier solve interrupted - model solved by another algorithm
62
63
   Concurrent spin time: 1.26s (can be avoided by choosing Method=3)
64
65
   Solved with primal simplex
66
67
   Root relaxation: objective 5.432609e+02, 16690 iterations, 6.24 seconds (6.80 work units)
68
   Total elapsed time = 25.98s
69
70
                            Objective Bounds
                                                Work
     Nodes | Current Node |
71
   Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
73
         0 543.26091 0 1114
                               - 543.26091
                                           - - 28s
74
         0 543 27074
                              - 543.27074
                                           - - 29s
     0
                     0.962
75
         0 550.80138
                     0 1088
                               - 550.80138
                                               - 33s
76
         0 550.80138
                     0.1078
                               - 550.80138
                                                 34s
         0 558.43696 0 998
                                          - - 35s
                              - 558.43696
77
     0
         0 560.96476 0 1248
                               - 560.96476
                                           - - 36s
78
     0
79
     0
         0 561.12169
                     0 1217
                               - 561.12169
                                               - 37s
```

unkno	wn			
90	0	0.561.27040 0	1222 561 27040	270
80	U		1222 - 561.27040	37s
81	0	0 561.33904 0	1230 - 561.33904	38s
82	0	0 561.35895 0	1129 - 561.35895	38s
83	0			39s
84	0	0 561.45425 0	916 - 561.45425	39s
85	0	0 561.45425 0	910 - 561.45425	39s
86	0		1178 - 567.79973	44s
87	0	0 574.16872 0	1223 - 574.16872	45s
88	0	0 576.92504 0	1303 - 576.92504	46s
89	0		1295 - 577.27821	46s
90	0	0 577.66451 0	1308 - 577.66451	47s
91	0	0 577.66983 0	1323 - 577.66983	47s
92	0		1320 - 577.67130	
93	0	0 596.45949 0	1234 - 596.45949	51s
94	0	0 596.49611 0	1231 - 596.49611	51s
95	0		1020 - 598.02666	53s
96	0	0 598.02666 0	1011 - 598.02666	53s
97	0	0 598.33971 0	1021 - 598.33971	53s
98	0		1143 - 598.55505	54s
99	0	0 598.55505 0	1137 - 598.55505	54s
100	0	0 598.55505 0	1104 - 598.55505	54s
101	0	0 612.96885 0	1168 - 612.96885	59s
102	0		1147 - 612.96885	59s
103	0	0 613.98576 0	1305 - 613.98576	60s
104	0		1302 - 613.98576	60s
	_			
105	0		1066 - 614.29871	60s
106	0	0 614.40210 0	957 - 614.40210	61s
107	0		891 - 614.40210	61s
108	_			
	0		1224 - 618.92023	64s
109	0	0 619.03770 0	1068 - 619.03770	64s
110	0	0 619.03770 0	1067 - 619.03770	64s
111	0		1092 - 619.07062	65s
112	0		1415 - 619.07197	66s
113	0	0 619.10990 0	1297 - 619.10990	68s
114	0	0 619.11088 0	1331 - 619.11088	68s
115	0		1066 - 621.25472	71s
116	0	0 621.25472 0	982 - 621.25472	72s
117	0	0 621.99588 0	1060 - 621.99588	73s
	0		1310 - 622.04985	74s
118				
119	0	0 622.06616 0	1221 - 622.06616	74s
120	0	0 622.06616 0	1243 - 622.06616	75s
121	0		1421 - 622.25645	77s
122	0		1339 - 622.25645	77s
123	0	0 622.34673 0	1454 - 622.34673	80s
124	0		1277 - 622.35822	80s
125	0		1561 - 622.50248	83s
126	0	0 622.50248 0	1560 - 622.50248	84s
127	0	0 622.63881 0	1427 - 622.63881	86s
	0			
128	0		1424 - 622.63881	86s
129	0	0 622.64116 0	1367 - 622.64116	87s
130	0	0 622.76466 0	961 - 622.76466	89s
	0		906 - 622.76466	90s
131				
132	0	0 622.88349 0	1315 - 622.88349	92s
133	0	0 622.88455 0	874 - 622.88455	93s
134	0		1287 - 623.05082	96s
135	0		1280 - 623.05082	96s
136	0	0 623.05082 0	1309 - 623.05082	97s
137	0	0 623.05082 0	1308 - 623.05082	97s
138	0		1220 - 623.19735	99s
139	0		1505 - 623.20288	100s
140	0	0 623.36399 0	1328 - 623.36399	102s
141	0	0 623.36399 0	1303 - 623.36399	102s
142	0		1458 - 623.55141	104s
143	0		1446 - 623.55141	104s
144	0	0 623.55141 0	1515 - 623.55141	105s
145	0		1448 - 623.76001	107s
	_			
146	0		1553 - 623.76001	
147	0	0 623.76001 0	1548 - 623.76001	109s
148	0	0 623.97420 0	1431 - 623.97420	111s
149	0		1421 - 623.97420	111s
150	0		1387 - 623.98417	112s
151	0	0 624.23011 0	1390 - 624.23011	114s
152	0		1371 - 624.23011	115s
	_			
153	0		1500 - 624.40737	117s
154	0	0 624.40737 0	1499 - 624.40737	117s
155	0		1443 - 624.42406	118s
156	0		1598 - 624.45877	1198
157	0	0 624.46929 0	1440 - 624.46929	120s
158	0		1439 - 624.65003	121s
	_			
159	0		1438 - 624.65003	122s
160	0	0 624.65003 0	1515 - 624.65003	122s
161	0	0 624.81953 0	1549 - 624.81953	125s
162	0		1628 - 624.84807	126s
163	0	0 624.85050 0	1427 - 624.85050	127s

```
164
          0 624.96686 0 1591
                                  - 624.96686
                                                  - 129s
       0
165
          0 625.01796 0 1582
                                  - 625.01796
                                                 - 130s
                                  - 625.03494
          0 625.03494 0 1586
                                               - - 130s
166
167
       0
          0 625.04960 0 1622
                                  - 625.04960
                                                  - 131s
          0 625.07992 0 1579
                                  - 625.07992
                                                  - 133s
168
169
       0
          0 625.07992 0 1563
                                  - 625.07992
                                               - - 133s
          0 625.07992 0 1010
                                  - 625.07992
                                               - - 136s
170
       0
                                  - 625.07992
171
       0
          2 625.07992 0 1010
                                               - - 146s
          24 661.56714 5 924
                                  - 633.35543
172
      19
                                                - 718 151s
          43 641.12142 10 1032
                                   - 633.35543
173
      38
                                                - 895 155s
                                    - 633.35543
174
      119 128 662.45263 25 751
                                                 - 412 160s
                                                 - 291 165s
175
          240 669.00000 43 266
                                    - 633.35543
      220
176
      317 333 669.00000 56 172
                                    - 633.35543
                                                 - 280 170s
177
      400 422 669,00000 64 146
                                    - 633.35543
                                                 - 275 175s
178
      574 594 709.00000 104 124
                                    - 634.15904
                                                 - 222 181s
                                    - 634.15904
179
          702 677.17101 14 156
180
      841
          797 684.00000 39 174
                                    - 634.15904
                                                 - 202 190s
          886 684.00000 56 105
                                                 - 213 195s
                                    - 634.15904
181
      957
182
     1041 923 684.00000 25 1010
                                    - 634.15904 - 236 271s
183
     1043 924 709.00000 108 920
                                    - 634.15904
                                                  - 235 290s
     1044 925 650.66667 23 562
                                    - 634.15904
                                                 - 235 307s
184
                                     - 634.15904
185
     1045 926 704.00000 37 1120
                                                  - 235 315s
                          829.0000000 634.15904 23.5% 235 318s
186
    H 1045 879
187
     1046 879 705.50200 66 958 829.00000 634.15904 23.5% 235 320s
     1049 881 724.00000 59 1067 829.00000 634.15904 23.5% 234 325s
188
189
     1050 882 644.00000 46 1057 829.00000 634.15904 23.5% 234 331s
     1051 883 664.00000 46 791 829.00000 636.02966 23.3% 234 348s
                          784.0000000 636.02966 18.9% 234 349s
191 H 1051 839
     1052 839 744.00000 150 804 784.00000 636.67725 18.8% 233 350s
192
193
     1055 841 664.00000 61 781 784.00000 636.85615 18.8% 233 356s
194 H 1055 799
                          724.0000000 637.84890 11.9% 233 377s
     1057 801 711.96296 107 877 724.00000 638.33664 11.8% 232 386s
195
196
     1058\ \ 801\ \ 664.00000\ \ 68\ \ 843\ \ 724.00000\ \ 638.34013\ \ 11.8\%\ \ 232\ \ 393s
           802 664.00000 55 503 724.00000 638.37349 11.8% 232 406s
197
198
     1060 803 698.16667 56 737 724.00000 638.38221 11.8% 232 414s
199
           803 724.00000 24 531 724.00000 638.39346 11.8% 231 425s
     1061
200
     1062
           804 700.50200 62 655 724.00000 638.39887 11.8% 231 430s
     1063 805 709.00000 103 519 724.00000 638.40338 11.8% 231 436s
201
           806 704.00000 127 507 724.00000 638.41213 11.8% 231 447s
202
     1065
           807 714.00000 99 557 724.00000 638.41213 11.8% 230 450s
203
     1066
204
           807 669.00000 51 522 724.00000 638.41213 11.8% 230 456s
205
     1069 809 664.00000 59 583 724.00000 638.41321 11.8% 230 466s
     1070 809 709.00000 102 657 724.00000 638.42329 11.8% 230 471s
206
207
     1071 810 724.00000 188 619 724.00000 638.42514 11.8% 229 479s
     1072 811 704.00000 84 571 724.00000 638.42514 11.8% 229 486s
208
     1074 813 724.00000 90 1010 724.00000 638.42514 11.8% 314 521s
209
     1076 814 677.57540 64 425 724.00000 638.42514 11.8% 313 528s
210
      1077 815 644.00000 43 349 724.00000 638.42514 11.8% 313 540s
212
     1079 816 714.00000 106 591 724.00000 638.42514 11.8% 313 548s
     1082 818 717.33333 99 676 724.00000 638.47701 11.8% 312 552s
213
     1083 819 724.00000 198 439 724.00000 638.50937 11.8% 311 559s
214
           820 724.00000 33 482 724.00000 638.52208 11.8% 311 561s
     1085 820 711.96296 107 446 724.00000 638.53946 11.8% 311 567s
216
     1086 821 682.00000 62 579 724.00000 638.55041 11.8% 310 571s
217
218
     1087 822 705.48930 79 412 724.00000 639.19530 11.7% 310 580s
219
     1089 823 724.00000 179 518 724.00000 639.22447 11.7% 310 590s
     1091 824 724.00000 26 403 724.00000 639.52896 11.7% 309 599s
220
221
     1093 826 704.00000 127 392 724.00000 639.58637 11.7% 309 603s
222
     1094 826 724.00000 195 364 724.00000 639.81055 11.6% 308 611s
    H 1094 784
                          704.0000000 639.81055 9.12% 308 612s
     1095 785 644.00000 38 413 704.00000 639.84782 9.11% 308 615s
224
225
    H 1095 745
                          684.0000000 639.84782 6.45% 308 620s
     1096 746 639.86358 25 308 684.00000 639.86358 6.45% 308 625s
227 H 1096 709
                          664.0000000 639.86358 3.64% 308 625s
228
     1098 710 664.00000 67 407 664.00000 644.00000 3.01% 307 635s
229
     1099 711 664.00000 57 432 664.00000 644.00000 3.01% 307 640s
230
     1100 711 664.00000 82 307 664.00000 644.00000 3.01% 307 646s
231
     1102 713 650 66667 29 291 664 00000 644 00000 3 01% 306 653s
     1105 715 664.00000 57 378 664.00000 644.00000 3.01% 305 657s
232
233
     1106 715 644.00000 42 114 664.00000 644.00000 3.01% 305 660s
234 H 1106 678
                          644.0000000 644.00000 0.00% 305 662s
235
    Cutting planes:
236
237
     Learned: 23
238
     Gomory: 51
239
     Lift-and-project: 2
240
     Cover: 137
241
     Implied bound: 199
242
     Projected implied bound: 8
243
     Clique: 112
244
     MIR: 22
245
     StrongCG: 15
246
     Flow cover: 96
     GUB cover: 79
247
```

```
unknown
248
       Zero half: 44
249
       Network: 3
250
       RLT: 164
251
       Relax-and-lift: 24
252
       BQP: 47
253
254 Explored 1106 nodes (508507 simplex iterations) in 662.93 seconds (1128.93 work units)
255 Thread count was 8 (of 8 available processors)
256
257 Solution count 7: 644 664 684 ... 829
258
259 Optimal solution found (tolerance 1.00e-04)
260 Best objective 6.440000000000e+02, best bound 6.44000000000e+02, gap 0.0000%
261 Optimal Obj: 644.0
262 \text{ Obj} = 644.0
263 Solutions
                            pi: 19-24,
                                        ai-di: 9-20,
                                                                                       taoPi SP-deltaPi SP: 9-12, periodPi: 3, betaNi: 6, bi: 9, Txijt: 45
264 Vessel i: 0:
                   li: 5.
                                                      taoi-deltai: 9-18.
                                                                          periodi: 9,
                                                    Ti: 75
                   o2i: 60,
         oli: 45,
                             o3i: -150, o4i: 120,
265 Vessel i: 1:
                   li: 5,
                            pi: 29-34,
                                         ai-di: 33-51,
                                                        taoi-deltai: 33-49,
                                                                            periodi: 16,
                                                                                          taoPi_SP-deltaPi_SP: 33-37,
                                                                                                                         periodPi: 4,
                                                                                                                                       betaNi: 10,
                                                                                                                                                     bi: 16,
      Txijt: 80, o1i: 80,
                            o2i: 80, o3i: -300, o4i: 200, Ti: 60
     Vessel i: 2:
                                        ai-di: 57-67,
266
                                                                                         taoPi_SP-deltaPi_SP: 57-59,
                            pi: 18-23,
                                                        taoi-deltai: 57-65,
                                                                            periodi: 8,
                                                                                                                        periodPi: 2,
                                                                                                                                      betaNi: 5,
                                                                                                                                                   bi: 8, Txijt
                  li: 5,
            o1i: 40, o2i: 40, o3i: -150, o4i: 100,
      : 40,
                                                        Ti: 30
     Vessel i: 3: li: 5,
                            pi: 14-19,
                                        ai-di: 15-27,
                                                                                          taoPi_SP-deltaPi_SP: 15-18,
                                                                                                                                                    bi: 10,
                                                        taoi-deltai: 15-25,
                                                                            periodi: 10,
                                                                                                                         periodPi: 3,
                                                                                                                                        betaNi: 6,
      Txijt: 50, o1i: 50,
                            o2i: 60, o3i: -175, o4i: 120, Ti: 55
                            pi: 12-17,
                                        ai-di: 42-62,
268
     Vessel i: 4: li: 5,
                                                                                          taoPi_SP-deltaPi_SP: 42-47,
                                                                                                                         periodPi: 5,
                                                                                                                                       betaNi: 11,
                                                        taoi-deltai: 42-60,
                                                                            periodi: 18,
                                                                                                                                                     bi: 18,
      Txijt: 90, o1i: 90,
                            o2i: 100,
                                       o3i: -325, o4i: 220,
                                                              Ti: 85
                                       ai-di: 17-40, taoi-deltai: 17-27,
     Vessel i: 5: li: 6,
                            pi: 8-14,
                                                                           periodi: 10,
                                                                                         taoPi SP-deltaPi SP: 17-20,
                                                                                                                        periodPi: 3,
                                                                                                                                      betaNi: 6,
                                                                                                                                                   bi: 10,
                 o1i: 60,
                                     o3i: -182, o4i: 120, Ti: 58
      Txijt: 60.
                            o2i: 60.
270
     Vessel i: 6:
                  li: 5,
                            pi: 24-29,
                                         ai-di: 21-48,
                                                        taoi-deltai: 21-34,
                                                                            periodi: 13,
                                                                                          taoPi_SP-deltaPi_SP: 21-25,
                                                                                                                         periodPi: 4,
                                                                                                                                       betaNi: 8,
                                                                                                                                                    bi: 13,
     Txijt: 65, 01i: 65,
                            o2i: 80, o3i: -225, o4i: 160, Ti: 80
     Vessel i: 7:
                  li: 6,
                            pi: 11-17,
                                        ai-di: 37-57,
                                                        taoi-deltai: 37-41,
                                                                            periodi: 4,
                                                                                         taoPi SP-deltaPi SP: 37-38,
                                                                                                                        periodPi: 1,
                                                                                                                                      betaNi: 3,
                                                                                                                                                   bi: 4, Txijt
            o1i: 24, o2i: 20, o3i: -78, o4i: 60,
      : 24,
                                                      Ti: 26
272
     Vessel i: 8: li: 5,
                            pi: 29-34, ai-di: 8-41,
                                                      taoi-deltai: 8-25,
                                                                          periodi: 17,
                                                                                        taoPi_SP-deltaPi_SP: 8-13, periodPi: 5,
                                                                                                                                    betaNi: 10,
                                                                                                                                                  bi: 17, Txijt
            o1i: 85, o2i: 100, o3i: -300, o4i: 200, Ti: 85
     Vessel i: 9: li: 5, pi: 19-24, ai-di: 25-58,
                                                        taoi-deltai: 25-47,
                                                                            periodi: 22,
                                                                                          taoPi SP-deltaPi SP: 25-31,
                                                                                                                        periodPi: 6,
                                                                                                                                       betaNi: 13,
                                                                                                                                                     bi: 22,
                  o1i: 110, o2i: 120, o3i: -400, o4i: 260,
                                                                Ti: 90
     Txijt: 110,
274
     TimeSolveModel: 688.000000
275
276
277
278 TimeAll: 692.000000
279
280
281
282
```