


```

80
81 Solution count 7: 647 707 727 ... 1527
82
83 Optimal solution found (tolerance 1.00e-10)
84 Best objective 6.470000000000e+02, best bound 6.470000000000e+02, gap 0.0000%
85 Set parameter MIPGap to value 1e-08
86 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
87
88 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
89 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
90
91 Optimize a model with 2481684 rows, 1955335 columns and 17236273 nonzeros
92 Model fingerprint: 0xdd2ae776
93 Variable types: 963295 continuous, 992040 integer (985965 binary)
94 Coefficient statistics:
95   Matrix range    [1e-01, 1e+10]
96   Objective range [6e-05, 5e+01]
97   Bounds range    [1e+00, 8e+01]
98   RHS range       [8e-01, 1e+10]
99 Warning: Model contains large matrix coefficients
100 Warning: Model contains large rhs
101   Consider reformulating model or setting NumericFocus parameter
102   to avoid numerical issues.
103 Presolve removed 2478686 rows and 1954269 columns (presolve time = 5s) ...
104 Presolve removed 2478686 rows and 1954269 columns
105 Presolve time: 5.07s
106 Presolved: 2998 rows, 1066 columns, 7940 nonzeros
107 Variable types: 8 continuous, 1058 integer (626 binary)
108 Found heuristic solution: objective 3251.8528892
109 Found heuristic solution: objective 3465.7100450
110
111 Root simplex log...
112
113 Iteration  Objective    Primal Inf.   Dual Inf.    Time
114      0   7.7662796e+03  5.820592e+03  0.000000e+00   6s
115   1040  4.3839422e+03  0.000000e+00  0.000000e+00   6s
116
117 Root relaxation: objective 4.383942e+03, 1040 iterations, 0.02 seconds (0.01 work units)
118
119   Nodes | Current Node | Objective Bounds | Work
120 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
121
122    0    0 4383.94217    0 22 3465.71005 4383.94217 26.5%   -   6s
123 H  0    0           4358.0671749 4383.94217 0.59%   -   6s
124 H  0    0           4378.0671749 4383.94217 0.13%   -   6s
125    0    0 4383.17520    0 18 4378.06717 4383.17520 0.12%   -   6s
126    0    0 4383.17520    0 14 4378.06717 4383.17520 0.12%   -   6s
127    0    0 4383.17520    0  9 4378.06717 4383.17520 0.12%   -   6s
128 H  0    0           4381.8528892 4383.17520 0.03%   -   6s
129
130 Cutting planes:
131   Learned: 2
132   MIR: 2
133
134 Explored 1 nodes (1936 simplex iterations) in 6.75 seconds (7.57 work units)
135 Thread count was 8 (of 8 available processors)
136
137 Solution count 5: 4381.85 4378.07 4358.07 ... 3251.85
138
139 Optimal solution found (tolerance 1.00e-08)
140 Best objective 4.381852889165e+03, best bound 4.381852889165e+03, gap 0.0000%
141 SP is solved
142 SP's optimal solution is'□4381
143
144   Itr = 0
145   Collect_LB = [647.0]
146   Collect_UB = [9410.70577833071]
147   Collect_Hua = [0.0]
148   Collect_SPObjVal = [4381.852889165355]
149   Collect_MPObjValNHua = [647.0]
150
151
152 Set parameter MIPGap to value 0.05
153 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
154
155 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
156 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
157
158 Optimize a model with 1140514 rows, 303661 columns and 3363968 nonzeros
159 Model fingerprint: 0x4fad03a4
160 Variable types: 1 continuous, 303660 integer (292257 binary)
161 Coefficient statistics:
162   Matrix range    [1e-01, 1e+10]
163   Objective range [1e+00, 2e+01]

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164 Bounds range [1e+00, 1e+00]
165 RHS range [1e+00, 2e+10]
166 Warning: Model contains large matrix coefficients
167 Warning: Model contains large rhs
168 Consider reformulating model or setting NumericFocus parameter
169 to avoid numerical issues.
170 Presolve removed 887295 rows and 275736 columns (presolve time = 5s) ...
171 Presolve removed 909924 rows and 277610 columns (presolve time = 10s) ...
172 Presolve removed 909924 rows and 277610 columns (presolve time = 15s) ...
173 Presolve removed 1010309 rows and 287903 columns
174 Presolve time: 17.29s
175 Presolved: 130205 rows, 15758 columns, 395077 nonzeros
176 Variable types: 1 continuous, 15757 integer (13150 binary)
177
178 Deterministic concurrent LP optimizer: primal and dual simplex (primal and dual model)
179 Showing first log only...
180
181 Root relaxation presolved: 15758 rows, 145963 columns, 410835 nonzeros
182
183
184 Root simplex log...
185
186 Iteration Objective Primal Inf. Dual Inf. Time
187 0 5.0288529e+03 0.000000e+00 8.172938e+03 18s
188 Concurrent spin time: 0.28s
189
190 Solved with dual simplex (primal model)
191
192 Root relaxation: objective 5.028853e+03, 8662 iterations, 1.97 seconds (3.15 work units)
193 Total elapsed time = 23.23s
194 Total elapsed time = 25.36s
195
196 Nodes | Current Node | Objective Bounds | Work
197 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
198
199 0 0 5028.85289 0 258 - 5028.85289 - - 26s
200 0 0 5028.85289 0 746 - 5028.85289 - - 31s
201 0 0 5028.85289 0 720 - 5028.85289 - - 31s
202 0 0 5028.85289 0 727 - 5028.85289 - - 32s
203 0 0 5028.85289 0 723 - 5028.85289 - - 33s
204 0 0 5028.85289 0 698 - 5028.85289 - - 33s
205 0 0 5028.85289 0 217 - 5028.85289 - - 45s
206 0 0 5028.85289 0 237 - 5028.85289 - - 45s
207 0 0 5028.85289 0 276 - 5028.85289 - - 46s
208 0 0 5028.85289 0 275 - 5028.85289 - - 46s
209 0 0 5028.85289 0 190 - 5028.85289 - - 53s
210 0 0 5028.85289 0 218 - 5028.85289 - - 54s
211 0 0 5028.85289 0 184 - 5028.85289 - - 58s
212 0 0 5028.85289 0 186 - 5028.85289 - - 59s
213 0 0 5028.85289 0 304 - 5028.85289 - - 68s
214 0 0 5028.85289 0 327 - 5028.85289 - - 68s
215 0 0 5028.85289 0 316 - 5028.85289 - - 69s
216 0 0 5028.85289 0 317 - 5028.85289 - - 69s
217 0 0 5028.85289 0 318 - 5028.85289 - - 77s
218 0 0 5028.85289 0 316 - 5028.85289 - - 78s
219 0 0 5028.85289 0 316 - 5028.85289 - - 78s
220 0 0 5028.85289 0 292 - 5028.85289 - - 81s
221 H 0 0 5028.8528892 5028.85289 0.00% - 91s
222 0 0 5028.85289 0 292 5028.85289 5028.85289 0.00% - 91s
223
224 Cutting planes:
225 Gomory: 1
226 Cover: 210
227 Implied bound: 57
228 Clique: 1050
229 MIR: 475
230 StrongCG: 81
231 Flow cover: 11
232 GUB cover: 26
233 Zero half: 27
234 RLT: 60
235 Relax-and-lift: 357
236 BQP: 47
237
238 Explored 1 nodes (186645 simplex iterations) in 91.36 seconds (267.10 work units)
239 Thread count was 8 (of 8 available processors)
240
241 Solution count 1: 5028.85
242
243 Optimal solution found (tolerance 5.00e-02)
244 Best objective 5.028852889165e+03, best bound 5.028852889165e+03, gap 0.0000%
245 Set parameter MIPGap to value 1e-08
246 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
247

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248 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
249 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
250
251 Optimize a model with 2481684 rows, 1955335 columns and 17236273 nonzeros
252 Model fingerprint: 0xb66ebb75
253 Variable types: 963295 continuous, 992040 integer (985965 binary)
254 Coefficient statistics:
255   Matrix range   [1e-01, 1e+10]
256   Objective range [6e-05, 5e+01]
257   Bounds range   [1e+00, 8e+01]
258   RHS range      [8e-01, 1e+10]
259 Warning: Model contains large matrix coefficients
260 Warning: Model contains large rhs
261   Consider reformulating model or setting NumericFocus parameter
262   to avoid numerical issues.
263 Presolve removed 2477274 rows and 1953860 columns
264 Presolve time: 4.77s
265 Presolved: 4410 rows, 1475 columns, 11768 nonzeros
266 Variable types: 8 continuous, 1467 integer (850 binary)
267 Found heuristic solution: objective 3227.8528892
268
269 Root simplex log...
270
271 Iteration   Objective      Primal Inf.   Dual Inf.    Time
272      0   9.0534085e+03   3.964725e+03   0.000000e+00   6s
273    1268   4.7955672e+03   0.000000e+00   0.000000e+00   6s
274
275 Root relaxation: objective 4.795567e+03, 1268 iterations, 0.01 seconds (0.01 work units)
276
277   Nodes | Current Node | Objective Bounds | Work
278 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
279
280 H  0  0           4795.5671749 13146.7410 174% - 6s
281   0  0   -  0   4795.56717 4795.56717 0.00% - 6s
282
283 Explored 1 nodes (1906 simplex iterations) in 6.35 seconds (6.97 work units)
284 Thread count was 8 (of 8 available processors)
285
286 Solution count 2: 4795.57 3227.85
287
288 Optimal solution found (tolerance 1.00e-08)
289 Best objective 4.795567174880e+03, best bound 4.795567174880e+03, gap 0.0000%
290 SP is solved
291 SP's optimal solution is '[4795
292
293 Itr = 1
294 Collect LB = [647.0, 5028.852889165355]
295 Collect UB = [9410.70577833071, 5442.567174879641]
296 Collect Hua = [0.0, 4381.852889165355]
297 Collect_SPObjVal = [4381.852889165355, 4795.567174879641]
298 Collect_MPObjValNHua = [647.0, 647.0]
299
300
301 Set parameter MIPGap to value 0.05
302 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
303
304 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
305 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
306
307 Optimize a model with 1676770 rows, 323344 columns and 5062590 nonzeros
308 Model fingerprint: 0xd1f3e031
309 Variable types: 1 continuous, 323343 integer (300573 binary)
310 Coefficient statistics:
311   Matrix range   [1e-01, 1e+10]
312   Objective range [1e+00, 2e+01]
313   Bounds range   [1e+00, 1e+00]
314   RHS range      [1e+00, 2e+10]
315 Warning: Model contains large matrix coefficients
316 Warning: Model contains large rhs
317   Consider reformulating model or setting NumericFocus parameter
318   to avoid numerical issues.
319 Presolve removed 1346036 rows and 288770 columns (presolve time = 5s) ...
320 Presolve removed 1380501 rows and 291938 columns (presolve time = 10s) ...
321 Presolve removed 1394517 rows and 292727 columns (presolve time = 18s) ...
322 Presolve removed 1456034 rows and 301032 columns (presolve time = 20s) ...
323 Presolve removed 1474511 rows and 301032 columns
324 Presolve time: 20.62s
325 Presolved: 202259 rows, 22312 columns, 647473 nonzeros
326 Variable types: 1 continuous, 22311 integer (17164 binary)
327
328 Deterministic concurrent LP optimizer: primal simplex, dual simplex, and barrier
329 Showing barrier log only...
330
331 Root relaxation presolved: 22312 rows, 224571 columns, 669785 nonzeros

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332
333 Root barrier log...
334
335 Ordering time: 2.56s
336
337 Barrier statistics:
338 Dense cols : 29
339 Free vars : 748
340 AA' NZ : 7.020e+05
341 Factor NZ : 2.218e+07 (roughly 300 MB of memory)
342 Factor Ops : 5.538e+10 (roughly 2 seconds per iteration)
343 Threads : 1
344
345 Objective Residual
346 Iter Primal Dual Primal Dual Compl Time
347 0 -5.64830474e+07 3.34809857e+04 2.69e+04 1.97e+03 9.11e+04 26s
348
349 Barrier performed 0 iterations in 26.07 seconds (49.16 work units)
350 Barrier solve interrupted - model solved by another algorithm
351
352 Concurrent spin time: 0.97s (can be avoided by choosing Method=3)
353
354 Solved with primal simplex
355
356 Root relaxation: objective 5.456853e+03, 22745 iterations, 4.53 seconds (6.36 work units)
357 Total elapsed time = 30.08s
358 Total elapsed time = 35.88s
359
360 Nodes | Current Node | Objective Bounds | Work
361 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
362
363 0 0 5456.85289 0 548 - 5456.85289 - - 38s
364 0 0 5456.85289 0 690 - 5456.85289 - - 38s
365 0 0 5456.85289 0 914 - 5456.85289 - - 49s
366 0 0 5456.85289 0 923 - 5456.85289 - - 49s
367 0 0 5456.85289 0 911 - 5456.85289 - - 55s
368 0 0 5456.85289 0 912 - 5456.85289 - - 55s
369 0 0 5456.85289 0 673 - 5456.85289 - - 72s
370 0 0 5456.85289 0 666 - 5456.85289 - - 72s
371 0 0 5456.85289 0 783 - 5456.85289 - - 76s
372 0 0 5456.85289 0 785 - 5456.85289 - - 76s
373 0 0 5456.85289 0 450 - 5456.85289 - - 95s
374 0 0 5456.85289 0 462 - 5456.85289 - - 96s
375 0 0 5456.85289 0 462 - 5456.85289 - - 96s
376 0 0 5456.85289 0 423 - 5456.85289 - - 97s
377 0 0 5456.85289 0 405 - 5456.85289 - - 98s
378 0 0 5456.85289 0 377 - 5456.85289 - - 113s
379 0 0 5456.85289 0 487 - 5456.85289 - - 114s
380 0 0 5456.85289 0 484 - 5456.85289 - - 114s
381 0 0 5456.85289 0 459 - 5456.85289 - - 116s
382 0 0 5456.85289 0 491 - 5456.85289 - - 116s
383 0 0 5456.85289 0 489 - 5456.85289 - - 117s
384 0 0 5456.85289 0 316 - 5456.85289 - - 128s
385 0 0 5456.85289 0 323 - 5456.85289 - - 128s
386 0 0 5456.85289 0 307 - 5456.85289 - - 129s
387 0 0 5456.85289 0 377 - 5456.85289 - - 130s
388 0 0 5456.85289 0 379 - 5456.85289 - - 130s
389 0 0 5456.85289 0 374 - 5456.85289 - - 141s
390 0 0 5456.85289 0 388 - 5456.85289 - - 142s
391 0 0 5456.85289 0 388 - 5456.85289 - - 142s
392 0 0 5456.85289 0 274 - 5456.85289 - - 145s
393 H 0 0 5456.8528892 5456.85289 0.00% - 167s
394 0 0 5456.85289 0 274 5456.85289 5456.85289 0.00% - 167s
395
396 Cutting planes:
397 Learned: 15
398 Gomory: 3
399 Cover: 330
400 Implied bound: 102
401 Clique: 3890
402 MIR: 462
403 StrongCG: 260
404 Flow cover: 26
405 GUB cover: 69
406 Zero half: 24
407 Network: 3
408 RLT: 141
409 Relax-and-lift: 463
410 BQP: 51
411 PSD: 3
412
413 Explored 1 nodes (266619 simplex iterations) in 167.41 seconds (527.99 work units)
414 Thread count was 8 (of 8 available processors)
415

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```

416 Solution count 1: 5456.85
417
418 Optimal solution found (tolerance 5.00e-02)
419 Best objective 5.456852889165e+03, best bound 5.456852889165e+03, gap 0.0000%
420 Warning: linear constraint 604259 and linear constraint 1140515 have the same name "ConSP25_1[0,0]"
421 Set parameter MIPGap to value 1e-08
422 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
423
424 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
425 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
426
427 Optimize a model with 2481684 rows, 1955335 columns and 17236273 nonzeros
428 Model fingerprint: 0x622fa79d
429 Variable types: 963295 continuous, 992040 integer (985965 binary)
430 Coefficient statistics:
431   Matrix range    [1e-01, 1e+10]
432   Objective range [6e-05, 5e+01]
433   Bounds range    [1e+00, 8e+01]
434   RHS range       [8e-01, 1e+10]
435 Warning: Model contains large matrix coefficients
436 Warning: Model contains large rhs
437   Consider reformulating model or setting NumericFocus parameter
438   to avoid numerical issues.
439 Presolve removed 2477413 rows and 1953880 columns
440 Presolve time: 4.80s
441 Presolved: 4271 rows, 1455 columns, 11395 nonzeros
442 Variable types: 8 continuous, 1447 integer (841 binary)
443 Found heuristic solution: objective 3253.5671749
444
445 Root simplex log...
446
447 Iteration   Objective      Primal Inf.   Dual Inf.    Time
448      0  9.2334085e+03  4.138363e+03  0.000000e+00   6s
449    1264  4.8105672e+03  0.000000e+00  0.000000e+00   6s
450
451 Root relaxation: objective 4.810567e+03, 1264 iterations, 0.02 seconds (0.01 work units)
452
453   Nodes | Current Node | Objective Bounds | Work
454 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
455
456 H  0  0           4810.5671749 12966.7410 170% - 6s
457   0  0   -  0    4810.56717 4810.56717 0.00% - 6s
458
459 Explored 1 nodes (1895 simplex iterations) in 6.35 seconds (6.95 work units)
460 Thread count was 8 (of 8 available processors)
461
462 Solution count 2: 4810.57 3253.57
463
464 Optimal solution found (tolerance 1.00e-08)
465 Best objective 4.810567174880e+03, best bound 4.810567174880e+03, gap 0.0000%
466 SP is solved
467 SP's optimal solution is' 4810
468
469 Itr = 2
470 Collect_LB = [647.0, 5028.852889165355, 5456.852889165355]
471 Collect_UB = [9410.70577833071, 5442.567174879641, 5442.567174879641]
472 Collect_Hua = [0.0, 4381.852889165355, 4795.567174879641]
473 Collect_SPObjVal = [4381.852889165355, 4795.567174879641, 4810.567174879641]
474 Collect_MPObjValNHua = [647.0, 647.0, 661.2857142857138]
475
476
477 Reach the termination conditions, stop iteration
478 Values adopted from the judgeCount's th iteration, and Itr = {2}, judgeCount = {1}
479
480 ~~~~~judgeCount = 1, SPObj_SPF = 4795.567174879641
481 Vessel i: 0: pi: 0-5, ai-di: 8-25, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 8-25, taoi-deltai: 8-17, taoPi_SP-deltaPi_SP: 8-17, betaNi: 9,
bi: 9
482 Vessel i: 1: pi: 5-10, ai-di: 3-21, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 3-21, taoi-deltai: 3-15, taoPi_SP-deltaPi_SP: 3-15, betaNi: 12
, bi: 12
483 Vessel i: 2: pi: 18-23, ai-di: 13-36, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 13-36, taoi-deltai: 13-28, taoPi_SP-deltaPi_SP: 13-28,
betaNi: 15, bi: 15
484 Vessel i: 3: pi: 9-15, ai-di: 22-49, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 22-49, taoi-deltai: 22-39, taoPi_SP-deltaPi_SP: 22-39, betaNi:
: 17, bi: 17
485 Vessel i: 4: pi: 22-28, ai-di: 35-57, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 35-57, taoi-deltai: 35-48, taoPi_SP-deltaPi_SP: 35-48,
betaNi: 13, bi: 13
486 Vessel i: 5: pi: 11-18, ai-di: 3-35, gi_SP-gpi_SP: 0.257143-0.800000, ai_SP-di: 4-35, taoi-deltai: 6-21, taoPi_SP-deltaPi_SP: 6-21, betaNi: 15
, bi: 15
487 Vessel i: 6: pi: 29-34, ai-di: 2-29, gi_SP-gpi_SP: 1.000000-0.000000, ai_SP-di: 10-29, taoi-deltai: 7-15, taoPi_SP-deltaPi_SP: 10-15, betaNi:
8, bi: 8
488 Vessel i: 7: pi: 15-22, ai-di: 27-68, gi_SP-gpi_SP: 1.000000-0.600000, ai_SP-di: 37-68, taoi-deltai: 37-53, taoPi_SP-deltaPi_SP: 37-53,
betaNi: 16, bi: 16
489 Vessel i: 8: pi: 28-34, ai-di: 29-59, gi_SP-gpi_SP: 0.142857-1.000000, ai_SP-di: 30-59, taoi-deltai: 30-35, taoPi_SP-deltaPi_SP: 30-35,
betaNi: 5, bi: 5
490

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unknown

491 round LB = [647, 5029, 5457]
492 round UB = [9411, 5443, 5443]
493 round Hua = [0, 4382, 4796]
494 round SPObjVal = [4382, 4796, 4811]
495 round MPObjValNHua = [647, 647, 661]
496
497 Time: 739.000000
498
499
500
501