



```

80 0 0 684.00000 0 150 1084.00000 684.00000 36.9% - 43s
81 H 0 0 924.0000000 684.00000 26.0% - 43s
82 0 0 684.00000 0 206 924.00000 684.00000 26.0% - 45s
83 0 0 684.00000 0 43 924.00000 684.00000 26.0% - 46s
84 0 0 684.00000 0 43 924.00000 684.00000 26.0% - 49s
85 0 0 684.00000 0 229 924.00000 684.00000 26.0% - 51s
86 0 0 684.00000 0 226 924.00000 684.00000 26.0% - 51s
87 0 0 684.00000 0 347 924.00000 684.00000 26.0% - 51s
88 H 0 0 684.0000000 684.00000 0.00% - 53s
89 0 0 684.00000 0 25 684.00000 684.00000 0.00% - 53s
90
91 Cutting planes:
92 Gomory: 2
93 Cover: 103
94 Implied bound: 977
95 Clique: 56
96 MIR: 25
97 StrongCG: 17
98 GUB cover: 21
99 RLT: 6
100 Relax-and-lift: 10
101 PSD: 2
102
103 Explored 1 nodes (69720 simplex iterations) in 53.60 seconds (80.64 work units)
104 Thread count was 8 (of 8 available processors)
105
106 Solution count 7: 684 924 1084 ... 5844
107
108 Optimal solution found (tolerance 1.00e-10)
109 Best objective 6.840000000000e+02, best bound 6.840000000000e+02, gap 0.0000%
110 Set parameter MIPGap to value 1e-08
111 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
112
113 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
114 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
115
116 Optimize a model with 654199 rows, 16030 columns and 1337705 nonzeros
117 Model fingerprint: 0xac4201cf
118 Variable types: 40 continuous, 15990 integer (9240 binary)
119 Coefficient statistics:
120 Matrix range [1e-01, 1e+10]
121 Objective range [6e-05, 5e+01]
122 Bounds range [1e+00, 1e+00]
123 RHS range [8e-01, 1e+10]
124 Warning: Model contains large matrix coefficients
125 Warning: Model contains large rhs
126 Consider reformulating model or setting NumericFocus parameter
127 to avoid numerical issues.
128 Presolve removed 651695 rows and 15083 columns
129 Presolve time: 0.47s
130 Presolved: 2504 rows, 947 columns, 6695 nonzeros
131 Variable types: 10 continuous, 937 integer (563 binary)
132 Found heuristic solution: objective 3279.6104410
133 Found heuristic solution: objective 3440.6104410
134
135 Root relaxation: objective 4.894859e+03, 753 iterations, 0.00 seconds (0.01 work units)
136
137 Nodes | Current Node | Objective Bounds | Work
138 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
139
140 0 0 4894.85898 0 58 3440.61044 4894.85898 42.3% - 0s
141 H 0 0 4862.0258092 4894.85898 0.68% - 0s
142 H 0 0 4891.7251799 4894.85898 0.06% - 0s
143 0 0 4893.27025 0 34 4891.72518 4893.27025 0.03% - 0s
144 0 0 4893.27025 0 20 4891.72518 4893.27025 0.03% - 0s
145 0 0 4893.27025 0 13 4891.72518 4893.27025 0.03% - 0s
146 0 0 4893.27025 0 10 4891.72518 4893.27025 0.03% - 0s
147 H 0 0 4892.3829521 4893.27025 0.02% - 0s
148 0 0 4893.27025 0 7 4892.38295 4893.27025 0.02% - 0s
149 0 0 cutoff 0 4892.38295 4892.38295 0.00% - 0s
150
151 Cutting planes:
152 Gomory: 2
153 Relax-and-lift: 1
154
155 Explored 1 nodes (1525 simplex iterations) in 0.69 seconds (0.92 work units)
156 Thread count was 8 (of 8 available processors)
157
158 Solution count 5: 4892.38 4891.73 4862.03 ... 3279.61
159
160 Optimal solution found (tolerance 1.00e-08)
161 Best objective 4.892382952071e+03, best bound 4.892382952071e+03, gap 0.0000%
162 SP is solved
163 SP's optimal solution is' 4892

```

```

164
165 Itr = 0
166 Collect_LB = [684.0]
167 Collect_UB = [10468.765904142507]
168 Collect_Hua = [0.0]
169 Collect_SPObjVal = [4892.382952071253]
170 Collect_MPObjValNHua = [684.0]
171
172
173 Set parameter MIPGap to value 1e-10
174 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
175
176 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
177 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
178
179 Optimize a model with 654151 rows, 344301 columns and 1811078 nonzeros
180 Model fingerprint: 0x0015e6e2
181 Variable types: 1 continuous, 344300 integer (344260 binary)
182 Coefficient statistics:
183   Matrix range    [1e+00, 1e+10]
184   Objective range [1e+00, 2e+01]
185   Bounds range   [1e+00, 1e+00]
186   RHS range      [1e+00, 2e+10]
187 Warning: Model contains large matrix coefficients
188 Warning: Model contains large rhs
189   Consider reformulating model or setting NumericFocus parameter
190   to avoid numerical issues.
191 Presolve removed 342655 rows and 308396 columns (presolve time = 5s) ...
192 Presolve removed 342655 rows and 308396 columns (presolve time = 10s) ...
193 Presolve removed 342655 rows and 308396 columns (presolve time = 15s) ...
194 Presolve removed 342655 rows and 308396 columns (presolve time = 20s) ...
195 Presolve removed 500437 rows and 327624 columns (presolve time = 25s) ...
196 Presolve removed 577228 rows and 327628 columns
197 Presolve time: 26.00s
198 Presolved: 76923 rows, 16673 columns, 242083 nonzeros
199 Variable types: 0 continuous, 16673 integer (16643 binary)
200
201 Deterministic concurrent LP optimizer: primal and dual simplex (primal and dual model)
202 Showing first log only...
203
204 Root relaxation presolved: 16673 rows, 93596 columns, 258756 nonzeros
205
206
207 Root simplex log...
208
209 Iteration   Objective      Primal Inf.   Dual Inf.    Time
210      0  5.5810258e+03  0.000000e+00  5.837000e+03  28s
211 Concurrent spin time: 0.02s
212
213 Solved with dual simplex (primal model)
214
215 Root relaxation: objective 5.581026e+03, 7662 iterations, 1.30 seconds (1.76 work units)
216
217   Nodes | Current Node | Objective Bounds | Work
218 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
219
220 0 0 5581.02581 0 29 - 5581.02581 - - 29s
221 0 0 5581.02581 0 99 - 5581.02581 - - 31s
222 0 0 5581.02581 0 211 - 5581.02581 - - 31s
223 0 0 5581.02581 0 103 - 5581.02581 - - 35s
224 H 0 0 8281.0258092 5581.02581 32.6% - 35s
225 0 0 5581.02581 0 128 8281.02581 5581.02581 32.6% - 35s
226 0 0 5581.02581 0 107 8281.02581 5581.02581 32.6% - 37s
227 H 0 0 8201.0258092 5581.02581 31.9% - 37s
228 H 0 0 7561.0258092 5581.02581 26.2% - 37s
229 0 0 5581.02581 0 241 7561.02581 5581.02581 26.2% - 38s
230 0 0 5581.02581 0 165 7561.02581 5581.02581 26.2% - 40s
231 0 0 5581.02581 0 207 7561.02581 5581.02581 26.2% - 40s
232 0 0 5581.02581 0 371 7561.02581 5581.02581 26.2% - 41s
233 0 0 5581.02581 0 221 7561.02581 5581.02581 26.2% - 45s
234 0 0 5581.02581 0 170 7561.02581 5581.02581 26.2% - 45s
235 H 0 0 7181.0258092 5581.02581 22.3% - 48s
236 H 0 0 5581.0258092 5581.02581 0.00% - 50s
237 0 0 5581.02581 0 170 5581.02581 5581.02581 0.00% - 50s
238
239 Cutting planes:
240   Learned: 1
241   Gomory: 1
242   Cover: 49
243   Implied bound: 32
244   Clique: 446
245   MIR: 81
246   StrongCG: 54
247   GUB cover: 7

```

```
248 Zero half: 3
249 RLT: 9
250 Relax-and-lift: 17
251 BQP: 79
252 PSD: 1
253
254 Explored 1 nodes (100005 simplex iterations) in 50.47 seconds (79.33 work units)
255 Thread count was 8 (of 8 available processors)
256
257 Solution count 5: 5581.03 7181.03 7561.03 ... 8281.03
258
259 Optimal solution found (tolerance 1.00e-10)
260 Best objective 5.581025809214e+03, best bound 5.581025809214e+03, gap 0.0000%
261 Set parameter MIPGap to value 1e-08
262 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
263
264 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
265 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
266
267 Optimize a model with 654199 rows, 16030 columns and 1337705 nonzeros
268 Model fingerprint: 0xeb8c930a
269 Variable types: 40 continuous, 15990 integer (9240 binary)
270 Coefficient statistics:
271   Matrix range    [1e-01, 1e+10]
272   Objective range [6e-05, 5e+01]
273   Bounds range    [1e+00, 1e+00]
274   RHS range       [8e-01, 1e+10]
275 Warning: Model contains large matrix coefficients
276 Warning: Model contains large rhs
277   Consider reformulating model or setting NumericFocus parameter
278   to avoid numerical issues.
279 Presolve removed 649536 rows and 14510 columns
280 Presolve time: 0.48s
281 Presolved: 4663 rows, 1520 columns, 12447 nonzeros
282 Variable types: 10 continuous, 1510 integer (884 binary)
283 Found heuristic solution: objective 3772.3644878
284 Found heuristic solution: objective 3801.2533767
285
286 Root relaxation: objective 5.409944e+03, 1893 iterations, 0.03 seconds (0.04 work units)
287
288   Nodes | Current Node | Objective Bounds | Work
289 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
290
291   0   0 5409.94444   0   4 3801.25338 5409.94444 42.3% - 0s
292 H   0   0           5407.9005126 5409.94444 0.04% - 0s
293 *   0   0           5409.9444444 5409.94444 0.00% - 0s
294
295 Cutting planes:
296 Gomory: 1
297 GUB cover: 1
298 RLT: 1
299
300 Explored 1 nodes (2544 simplex iterations) in 0.73 seconds (0.92 work units)
301 Thread count was 8 (of 8 available processors)
302
303 Solution count 4: 5409.94 5407.9 3801.25 3772.36
304
305 Optimal solution found (tolerance 1.00e-08)
306 Best objective 5.409944444444e+03, best bound 5.409944444444e+03, gap 0.0000%
307 SP is solved
308 SP's optimal solution is'□5409
309
310 Itr = 1
311 Collect_LB = [684.0, 5581.02580921411]
312 Collect_UB = [10468.765904142507, 6098.587301587302]
313 Collect_Hua = [0.0, 4892.382952071253]
314 Collect_SPObjVal = [4892.382952071253, 5409.944444444445]
315 Collect_MPObjValNHua = [684.0, 688.6428571428569]
316
317
318 Set parameter MIPGap to value 1e-10
319 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
320
321 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
322 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
323
324 Optimize a model with 654151 rows, 344301 columns and 1811078 nonzeros
325 Model fingerprint: 0x81a87e59
326 Variable types: 1 continuous, 344300 integer (344260 binary)
327 Coefficient statistics:
328   Matrix range    [1e+00, 1e+10]
329   Objective range [1e+00, 2e+01]
330   Bounds range    [1e+00, 1e+00]
331   RHS range       [1e+00, 2e+10]
```

```

332 Warning: Model contains large matrix coefficients
333 Warning: Model contains large rhs
334   Consider reformulating model or setting NumericFocus parameter
335   to avoid numerical issues.
336 Presolve removed 343648 rows and 308501 columns (presolve time = 5s) ...
337 Presolve removed 343648 rows and 308501 columns (presolve time = 10s) ...
338 Presolve removed 343648 rows and 308501 columns (presolve time = 15s) ...
339 Presolve removed 343648 rows and 308501 columns (presolve time = 20s) ...
340 Presolve removed 518051 rows and 327685 columns (presolve time = 25s) ...
341 Presolve removed 583689 rows and 327685 columns
342 Presolve time: 25.75s
343 Presolved: 70462 rows, 16616 columns, 235024 nonzeros
344 Variable types: 0 continuous, 16616 integer (16586 binary)
345
346 Deterministic concurrent LP optimizer: primal and dual simplex (primal and dual model)
347 Showing first log only...
348
349 Root relaxation presolved: 16616 rows, 87078 columns, 251640 nonzeros
350
351
352 Root simplex log...
353
354 Iteration   Objective    Primal Inf.   Dual Inf.    Time
355      0  6.1084444e+03  0.000000e+00  5.838000e+03  27s
356 Concurrent spin time: 0.23s
357
358 Solved with dual simplex (primal model)
359
360 Root relaxation: objective 6.108444e+03, 7058 iterations, 1.46 seconds (1.98 work units)
361
362   Nodes | Current Node | Objective Bounds | Work
363   Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
364
365   0   0 6108.44444  0  44    -6108.44444  -  - 29s
366   0   0 6108.44444  0  47    -6108.44444  -  - 29s
367   0   0 6108.44444  0 114    -6108.44444  -  - 31s
368   0   0 6108.44444  0 112    -6108.44444  -  - 31s
369   0   0 6108.44444  0 142    -6108.44444  -  - 32s
370   0   0 6108.44444  0 200    -6108.44444  -  - 36s
371   0   0 6108.44444  0 249    -6108.44444  -  - 37s
372   0   0 6108.44444  0 166    -6108.44444  -  - 42s
373   0   0 6108.44444  0 333    -6108.44444  -  - 43s
374   0   0 6108.44444  0 178    -6108.44444  -  - 47s
375 H   0   0          12528.444444 6108.44444 51.2%  - 47s
376   0   0 6108.44444  0 178 12528.4444 6108.44444 51.2%  - 48s
377 H   0   0          8408.444444 6108.44444 27.4%  - 49s
378 H   0   0          6108.444444 6108.44444 0.00%  - 51s
379   0   0 6108.44444  0 178 6108.44444 6108.44444 0.00%  - 51s
380
381 Cutting planes:
382 Gomory: 2
383 Cover: 72
384 Implied bound: 24
385 Clique: 1837
386 MIR: 109
387 StrongCG: 67
388 GUB cover: 32
389 Zero half: 3
390 RLT: 8
391 Relax-and-lift: 13
392 BQP: 71
393 PSD: 1
394
395 Explored 1 nodes (73307 simplex iterations) in 51.94 seconds (64.68 work units)
396 Thread count was 8 (of 8 available processors)
397
398 Solution count 3: 6108.44 8408.44 12528.4
399
400 Optimal solution found (tolerance 1.00e-10)
401 Best objective 6.108444444444e+03, best bound 6.108444444444e+03, gap 0.0000%
402 Set parameter MIPGap to value 1e-08
403 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
404
405 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
406 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
407
408 Optimize a model with 654199 rows, 16030 columns and 1337705 nonzeros
409 Model fingerprint: 0xcc24e1f7
410 Variable types: 40 continuous, 15990 integer (9240 binary)
411 Coefficient statistics:
412 Matrix range    [1e-01, 1e+10]
413 Objective range [6e-05, 5e+01]
414 Bounds range    [1e+00, 1e+00]
415 RHS range      [8e-01, 1e+10]

```

```

416 Warning: Model contains large matrix coefficients
417 Warning: Model contains large rhs
418   Consider reformulating model or setting NumericFocus parameter
419   to avoid numerical issues.
420 Presolve removed 649935 rows and 14593 columns
421 Presolve time: 0.39s
422 Presolved: 4264 rows, 1437 columns, 11446 nonzeros
423 Variable types: 10 continuous, 1427 integer (841 binary)
424 Found heuristic solution: objective 3740.9042488
425 Found heuristic solution: objective 3780.9042488
426
427 Root relaxation: objective 5.424944e+03, 1595 iterations, 0.02 seconds (0.03 work units)
428
429   Nodes | Current Node | Objective Bounds | Work
430 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
431
432 * 0 0 0 5424.9444444 5424.94444 0.00% - 0s
433
434 Explored 1 nodes (2055 simplex iterations) in 0.59 seconds (0.80 work units)
435 Thread count was 8 (of 8 available processors)
436
437 Solution count 3: 5424.94 3780.9 3740.9
438
439 Optimal solution found (tolerance 1.00e-08)
440 Best objective 5.42494444444e+03, best bound 5.42494444444e+03, gap 0.0000%
441 SP is solved
442 SP's optimal solution is'□5424
443
444 Itr = 2
445 Collect_LB = [684.0, 5581.02580921411, 6108.444444444445]
446 Collect_UB = [10468.765904142507, 6098.587301587302, 6098.587301587302]
447 Collect_Hua = [0.0, 4892.382952071253, 5409.944444444445]
448 Collect_SPObjVal = [4892.382952071253, 5409.944444444445, 5424.944444444445]
449 Collect_MPObjValNHua = [684.0, 688.6428571428569, 698.5]
450
451
452 Ops, stop iteration
453 Values adopted from the Itr-1' th iteration, and Itr = {2}, judgeCount = {1}
454
455 ~~~~~judgeCount = 1, SPObj_SPF = 5409.944444444445
456 Vessel i: 0: pi: 0-5, ai-di: 28-81, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 28-81, taoi-deltai: 28-35, taoPi_SP-deltaPi_SP: 28-35, betaNi:
7, bi: 7
457 Vessel i: 1: pi: 0-5, ai-di: 15-45, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 15-45, taoi-deltai: 15-21, taoPi_SP-deltaPi_SP: 15-21, betaNi:
6, bi: 6
458 Vessel i: 2: pi: 5-10, ai-di: 19-50, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 19-50, taoi-deltai: 19-28, taoPi_SP-deltaPi_SP: 19-28, betaNi:
9, bi: 9
459 Vessel i: 3: pi: 10-16, ai-di: 9-55, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 9-55, taoi-deltai: 9-35, taoPi_SP-deltaPi_SP: 9-35, betaNi: 26
, bi: 26
460 Vessel i: 4: pi: 22-27, ai-di: 20-42, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 20-42, taoi-deltai: 20-25, taoPi_SP-deltaPi_SP: 20-25,
betaNi: 5, bi: 5
461 Vessel i: 5: pi: 17-22, ai-di: 3-61, gi_SP-gpi_SP: 0.000000-1.000000, ai_SP-di: 3-61, taoi-deltai: 4-12, taoPi_SP-deltaPi_SP: 4-12, betaNi: 8
, bi: 8
462 Vessel i: 6: pi: 16-22, ai-di: 9-72, gi_SP-gpi_SP: 0.875000-0.200000, ai_SP-di: 16-72, taoi-deltai: 16-33, taoPi_SP-deltaPi_SP: 16-33, betaNi:
17, bi: 17
463 Vessel i: 7: pi: 24-29, ai-di: 2-77, gi_SP-gpi_SP: 0.800000-0.800000, ai_SP-di: 10-77, taoi-deltai: 6-12, taoPi_SP-deltaPi_SP: 10-12, betaNi:
6, bi: 6
464 Vessel i: 8: pi: 28-34, ai-di: 22-62, gi_SP-gpi_SP: 0.325000-1.000000, ai_SP-di: 24-62, taoi-deltai: 26-36, taoPi_SP-deltaPi_SP: 26-36,
betaNi: 10, bi: 10
465 Vessel i: 9: pi: 17-24, ai-di: 28-79, gi_SP-gpi_SP: 1.000000-0.000000, ai_SP-di: 35-79, taoi-deltai: 35-58, taoPi_SP-deltaPi_SP: 35-58,
betaNi: 23, bi: 23
466
467 round LB = [684, 5581, 6108]
468 round UB = [10469, 6099, 6099]
469 round Hua = [0, 4892, 5410]
470 round SPObjVal = [4892, 5410, 5425]
471 round MPObjValNHua = [684, 689, 698]
472
473 OptimalObj = 6108.444444444445
474 Time: 239.000000
475
476
477
478

```