



```

80 StrongCG: 56
81 GUB cover: 11
82 Zero half: 5
83 RLT: 10
84 Relax-and-lift: 612
85 BQP: 8
86
87 Explored 117 nodes (126391 simplex iterations) in 28.67 seconds (65.83 work units)
88 Thread count was 8 (of 8 available processors)
89
90 Solution count 5: 991 1311 2611 ... 6691
91
92 Optimal solution found (tolerance 1.00e-10)
93 Best objective 9.910000000000e+02, best bound 9.910000000000e+02, gap 0.0000%
94 Set parameter MIPGap to value 1e-08
95 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
96
97 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
98 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
99
100 Optimize a model with 3035720 rows, 2395885 columns and 21185414 nonzeros
101 Model fingerprint: 0xf2f7ca95
102 Variable types: 1181973 continuous, 1213912 integer (1207162 binary)
103 Coefficient statistics:
104   Matrix range    [1e-01, 1e+10]
105   Objective range [6e-05, 5e+01]
106   Bounds range   [1e+00, 8e+01]
107   RHS range      [8e-01, 1e+10]
108 Warning: Model contains large matrix coefficients
109 Warning: Model contains large rhs
110   Consider reformulating model or setting NumericFocus parameter
111   to avoid numerical issues.
112 Presolve removed 3030782 rows and 2394157 columns (presolve time = 5s) ...
113 Presolve removed 3031923 rows and 2394476 columns
114 Presolve time: 6.71s
115 Presolved: 3797 rows, 1409 columns, 10130 nonzeros
116 Variable types: 10 continuous, 1399 integer (819 binary)
117 Found heuristic solution: objective 4594.6120144
118 Found heuristic solution: objective 4599.2524802
119
120 Root simplex log...
121
122 Iteration   Objective    Primal Inf.   Dual Inf.    Time
123      0  1.1568222e+04  6.702269e+03  0.000000e+00  8s
124    1350  6.5692444e+03  0.000000e+00  0.000000e+00  8s
125
126 Root relaxation: objective 6.569244e+03, 1350 iterations, 0.02 seconds (0.01 work units)
127
128   Nodes | Current Node | Objective Bounds | Work
129 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
130
131      0  0 6569.24444  0 46 4599.25248 6569.24444 42.8% - 8s
132 H  0  0              6539.4691941 6569.24444 0.46% - 8s
133      0  0 6566.44444  0 6 6539.46919 6566.44444 0.41% - 8s
134 H  0  0              6566.4444444 6566.44444 0.00% - 8s
135      0  0 6566.44444  0 6 6566.44444 6566.44444 0.00% - 8s
136
137 Cutting planes:
138   Learned: 2
139   Gomory: 6
140   Cover: 4
141   Implied bound: 12
142   Clique: 1
143   MIR: 1
144   Flow cover: 1
145   RLT: 1
146   PSD: 2
147
148 Explored 1 nodes (1855 simplex iterations) in 8.74 seconds (9.79 work units)
149 Thread count was 8 (of 8 available processors)
150
151 Solution count 4: 6566.44 6539.47 4599.25 4594.61
152
153 Optimal solution found (tolerance 1.00e-08)
154 Best objective 6.566444444444e+03, best bound 6.566444444444e+03, gap 0.0000%
155 SP is solved
156 SP's optimal solution is'□6566
157
158   Itr = 0
159 Collect_LB = [991.0]
160 Collect_UB = [14123.888888888869]
161 Collect_Hua = [0.0]
162 Collect_SPObjVal = [6566.444444444434]
163 Collect_MPObjValNHua = [991.0]

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164
165
166 Set parameter TimeLimit to value 12000
167 Set parameter MIPGap to value 0.0005
168 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
169
170 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
171 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
172
173 Optimize a model with 628196 rows, 344301 columns and 1748011 nonzeros
174 Model fingerprint: 0x9b065119
175 Variable types: 1 continuous, 344300 integer (344260 binary)
176 Coefficient statistics:
177   Matrix range    [1e+00, 1e+10]
178   Objective range [1e+00, 2e+01]
179   Bounds range    [1e+00, 1e+00]
180   RHS range       [1e+00, 2e+10]
181 Warning: Model contains large matrix coefficients
182 Warning: Model contains large rhs
183   Consider reformulating model or setting NumericFocus parameter
184   to avoid numerical issues.
185 Presolve removed 471431 rows and 325200 columns (presolve time = 5s) ...
186 Presolve removed 578970 rows and 335642 columns
187 Presolve time: 8.31s
188 Presolved: 49226 rows, 8659 columns, 127720 nonzeros
189 Variable types: 0 continuous, 8659 integer (8636 binary)
190 Root relaxation presolved: 8659 rows, 57885 columns, 136379 nonzeros
191
192
193 Root simplex log...
194
195 Iteration   Objective      Primal Inf.   Dual Inf.    Time
196      0      handle free variables                9s
197    7610    7.9174444e+03  0.000000e+00  0.000000e+00  10s
198    7610    7.9174444e+03  0.000000e+00  0.000000e+00  10s
199
200 Root relaxation: objective 7.917444e+03, 7610 iterations, 0.83 seconds (1.55 work units)
201
202   Nodes |   Current Node |   Objective Bounds |   Work
203 Expl Unexpl | Obj Depth IntInf | Incumbent   BestBd   Gap | It/Node Time
204
205    0    0 7917.44444  0  45      -7917.44444   -   -   9s
206    0    0 7917.44444  0 198      -7917.44444   -   -  11s
207    0    0 7917.44444  0 162      -7917.44444   -   -  11s
208    0    0 7917.44444  0 377      -7917.44444   -   -  11s
209    0    0 7917.44444  0  27      -7917.44444   -   -  13s
210    0    0 7917.44444  0 238      -7917.44444   -   -  14s
211    0    0 7917.44444  0 131      -7917.44444   -   -  14s
212    0    0 7917.44444  0 130      -7917.44444   -   -  14s
213    0    0 7917.44444  0 250      -7917.44444   -   -  14s
214    0    0 7917.44444  0 154      -7917.44444   -   -  15s
215    0    0 7917.44444  0 248      -7917.44444   -   -  16s
216    0    0 7917.44444  0 245      -7917.44444   -   -  16s
217 H    0    0          7917.4444444 7917.44444 0.00%   - 17s
218    0    0 7917.44444  0 211 7917.44444 7917.44444 0.00%   - 17s
219
220 Cutting planes:
221   Learned: 4
222   Gomory: 3
223   Cover: 186
224   Implied bound: 1306
225   Clique: 443
226   MIR: 193
227   StrongCG: 125
228   GUB cover: 43
229   Zero half: 13
230   RLT: 35
231   Relax-and-lift: 104
232   BQP: 25
233
234 Explored 1 nodes (40537 simplex iterations) in 17.62 seconds (27.92 work units)
235 Thread count was 8 (of 8 available processors)
236
237 Solution count 1: 7917.44
238
239 Optimal solution found (tolerance 5.00e-04)
240 Best objective 7.91744444444e+03, best bound 7.91744444444e+03, gap 0.0000%
241 Set parameter MIPGap to value 1e-08
242 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
243
244 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
245 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
246
247 Optimize a model with 3035720 rows, 2395885 columns and 21185414 nonzeros

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248 Model fingerprint: 0x7213566c
249 Variable types: 1181973 continuous, 1213912 integer (1207162 binary)
250 Coefficient statistics:
251   Matrix range   [1e-01, 1e+10]
252   Objective range [6e-05, 5e+01]
253   Bounds range   [1e+00, 8e+01]
254   RHS range      [8e-01, 1e+10]
255 Warning: Model contains large matrix coefficients
256 Warning: Model contains large rhs
257   Consider reformulating model or setting NumericFocus parameter
258   to avoid numerical issues.
259 Presolve removed 3028876 rows and 2393635 columns (presolve time = 5s) ...
260 Presolve removed 3029027 rows and 2393680 columns
261 Presolve time: 6.12s
262 Presolved: 6693 rows, 2205 columns, 17882 nonzeros
263 Variable types: 10 continuous, 2195 integer (1261 binary)
264 Found heuristic solution: objective 4878.5754258
265
266 Root simplex log...
267
268 Iteration   Objective      Primal Inf.   Dual Inf.    Time
269      0    1.3784000e+04   7.285388e+03  0.000000e+00   8s
270    1770   7.1231111e+03  0.000000e+00  0.000000e+00   8s
271
272 Root relaxation: objective 7.123111e+03, 1770 iterations, 0.02 seconds (0.02 work units)
273
274   Nodes | Current Node | Objective Bounds | Work
275 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
276
277    0    0 7123.11111    0 17 4878.57543 7123.11111 46.0% - 7s
278 H  0    0           7104.4444444 7123.11111 0.26% - 7s
279 *  0    0           0 7120.4444444 7120.44444 0.00% - 7s
280
281 Cutting planes:
282   Learned: 2
283   Gomory: 5
284   Cover: 1
285   Implied bound: 2
286   MIR: 2
287   Flow cover: 4
288   RLT: 4
289   Relax-and-lift: 5
290   PSD: 1
291
292 Explored 1 nodes (2452 simplex iterations) in 8.17 seconds (9.15 work units)
293 Thread count was 8 (of 8 available processors)
294
295 Solution count 3: 7120.44 7104.44 4878.58
296
297 Optimal solution found (tolerance 1.00e-08)
298 Best objective 7.120444444444e+03, best bound 7.120444444444e+03, gap 0.0000%
299 SP is solved
300 SP's optimal solution is'□7120
301
302 Itr = 1
303 Collect_LB = [991.0, 7917.444444444444]
304 Collect_UB = [14123.888888888869, 8471.444444444456]
305 Collect_Hua = [0.0, 6566.444444444434]
306 Collect_SPObjVal = [6566.444444444434, 7120.444444444445]
307 Collect_MPObjValNHua = [991.0, 1351.000000000001]
308
309
310 Set parameter TimeLimit to value 12000
311 Set parameter MIPGap to value 0.0005
312 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
313
314 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
315 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
316
317 Optimize a model with 628197 rows, 344301 columns and 1748032 nonzeros
318 Model fingerprint: 0x8a7cb295
319 Variable types: 1 continuous, 344300 integer (344260 binary)
320 Coefficient statistics:
321   Matrix range   [1e+00, 1e+10]
322   Objective range [1e+00, 2e+01]
323   Bounds range   [1e+00, 1e+00]
324   RHS range      [1e+00, 2e+10]
325 Warning: Model contains large matrix coefficients
326 Warning: Model contains large rhs
327   Consider reformulating model or setting NumericFocus parameter
328   to avoid numerical issues.
329 Presolve removed 472888 rows and 325364 columns (presolve time = 5s) ...
330 Presolve removed 579368 rows and 335687 columns
331 Presolve time: 8.37s

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332 Presolved: 48829 rows, 8614 columns, 126604 nonzeros
333 Variable types: 0 continuous, 8614 integer (8591 binary)
334 Root relaxation presolved: 8614 rows, 57443 columns, 135218 nonzeros
335
336
337 Root simplex log...
338
339 Iteration   Objective   Primal Inf.   Dual Inf.   Time
340    0   handle free variables                9s
341   7450  8.5114444e+03  0.0000000e+00  0.0000000e+00  9s
342   7450  8.5114444e+03  0.0000000e+00  0.0000000e+00  9s
343
344 Root relaxation: objective 8.511444e+03, 7450 iterations, 0.83 seconds (1.56 work units)
345
346 Nodes | Current Node | Objective Bounds | Work
347 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
348
349  0  0 8511.44444  0  48  - 8511.44444  -  -  9s
350  0  0 8511.44444  0 359  - 8511.44444  -  - 10s
351  0  0 8511.44444  0 371  - 8511.44444  -  - 11s
352  0  0 8511.44444  0 168  - 8511.44444  -  - 11s
353  0  0 8511.44444  0 198  - 8511.44444  -  - 11s
354  0  0 8511.44444  0 170  - 8511.44444  -  - 13s
355  0  0 8511.44444  0 211  - 8511.44444  -  - 13s
356  0  0 8511.44444  0 221  - 8511.44444  -  - 13s
357  0  0 8511.44444  0 404  - 8511.44444  -  - 14s
358  0  0 8511.44444  0 379  - 8511.44444  -  - 14s
359  0  0 8511.44444  0 250  - 8511.44444  -  - 18s
360  0  0 8511.44444  0 248  - 8511.44444  -  - 18s
361  0  0 8511.44444  0 562  - 8511.44444  -  - 19s
362  0  0 8511.44444  0 424  - 8511.44444  -  - 19s
363  0  0 8511.44444  0 421  - 8511.44444  -  - 19s
364  0  0 8511.44444  0 279  - 8511.44444  -  - 21s
365  0  0 8511.44444  0 109  - 8511.44444  -  - 22s
366  0  2 8511.44444  0 109  - 8511.44444  -  - 24s
367  1  4 8511.44444  1 254  - 8511.44444  - 1005 25s
368 31 28 8511.44444  8 456  - 8511.44444  - 1733 30s
369 61 62 8551.44444 13 852  - 8511.44444  - 2035 36s
370 126 157 8831.44444 40 259  - 8511.44444  - 1540 43s
371 217 241 8831.44444 77 190  - 8511.44444  - 1115 46s
372 451 441 8871.44444 188 267  - 8511.44444  -  643 51s
373 723 611 8831.44444  4 438  - 8511.44444  -  473 55s
374 978 836 8865.78404 56 484  - 8511.44444  -  415 61s
375 1213 1065 8911.44444 121 296  - 8511.44444  -  380 65s
376 1604 1415 8911.44444 252 260  - 8511.44444  -  325 70s
377 1786 1416 8547.50078  56 109  - 8511.44444  -  312 84s
378 1788 1417 8631.44444 424  56  - 8511.44444  -  312 86s
379 1790 1419 8511.44444  7 439  - 8511.44444  -  311 91s
380 1791 1419 9111.44444 480 375  - 8511.44444  -  311 95s
381 1793 1421 8751.44444 162 597  - 8511.44444  -  311 102s
382 1794 1421 8951.44444 246 783  - 8511.44444  -  311 105s
383 1796 1423 8951.44444 572 716  - 8511.44444  -  310 111s
384 1797 1423 8511.44444  22 507  - 8511.44444  -  310 116s
385 1799 1425 9791.44444 181 665  - 8511.44444  -  310 124s
386 1800 1425 8911.44444 295 904  - 8511.44444  -  310 126s
387 H 1800 1353 8631.4444444 8511.44444 1.39% 310 132s
388 1802 1355 8591.44444 211 645 8631.44444 8511.44444 1.39% 309 135s
389 1810 1363 8631.44444 231 109 8631.44444 8511.44444 1.39% 389 142s
390 1813 1365 8631.44444 511 427 8631.44444 8511.44444 1.39% 388 145s
391 1817 1368 8631.44444 201 317 8631.44444 8511.44444 1.39% 387 151s
392 H 1818 1299 8591.4444444 8511.44444 0.93% 387 153s
393
394 Cutting planes:
395   Learned: 1
396   Gomory: 53
397   Cover: 175
398   Implied bound: 45
399   Projected implied bound: 9
400   Clique: 74
401   MIR: 54
402   StrongCG: 15
403   Flow cover: 117
404   GUB cover: 86
405   Zero half: 15
406   RLT: 60
407   Relax-and-lift: 98
408   BQP: 2
409
410 Explored 1818 nodes (810195 simplex iterations) in 153.71 seconds (299.91 work units)
411 Thread count was 8 (of 8 available processors)
412
413 Solution count 2: 8591.44 8631.44
414
415 Optimal solution found (tolerance 5.00e-04)

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416 Best objective 8.591444444444e+03, best bound 8.591444444444e+03, gap 0.0000%
417 Set parameter MIPGap to value 1e-08
418 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
419
420 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
421 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
422
423 Optimize a model with 3035720 rows, 2395885 columns and 21185414 nonzeros
424 Model fingerprint: 0xa3e69282
425 Variable types: 1181973 continuous, 1213912 integer (1207162 binary)
426 Coefficient statistics:
427   Matrix range    [1e-01, 1e+10]
428   Objective range [6e-05, 5e+01]
429   Bounds range    [1e+00, 8e+01]
430   RHS range       [8e-01, 1e+10]
431 Warning: Model contains large matrix coefficients
432 Warning: Model contains large rhs
433   Consider reformulating model or setting NumericFocus parameter
434   to avoid numerical issues.
435 Presolve removed 3029068 rows and 2393693 columns (presolve time = 5s) ...
436 Presolve removed 3029341 rows and 2393776 columns
437 Presolve time: 6.22s
438 Presolved: 6379 rows, 2109 columns, 17146 nonzeros
439 Variable types: 10 continuous, 2099 integer (1212 binary)
440 Found heuristic solution: objective 4929.7421607
441 Found heuristic solution: objective 4933.6310496
442
443 Root simplex log...
444
445 Iteration   Objective      Primal Inf.   Dual Inf.    Time
446      0    1.3020000e+04  5.535106e+03  0.000000e+00   8s
447    1898    7.1284444e+03  0.000000e+00  0.000000e+00   8s
448
449 Root relaxation: objective 7.128444e+03, 1898 iterations, 0.02 seconds (0.02 work units)
450
451   Nodes | Current Node | Objective Bounds | Work
452 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
453
454      0    0 7128.44444    0 15 4933.63105 7128.44444 44.5% -   7s
455 H   0    0           7102.4444444 7128.44444 0.37% -   7s
456 H   0    0           7124.4444444 7128.44444 0.06% -   8s
457 *   0    0           0 7128.4444444 7128.44444 0.00% -   8s
458
459 Cutting planes:
460   Learned: 1
461   Implied bound: 6
462   MIR: 2
463   Flow cover: 2
464   Zero half: 3
465   RLT: 2
466   Relax-and-lift: 1
467
468 Explored 1 nodes (2719 simplex iterations) in 8.35 seconds (9.14 work units)
469 Thread count was 8 (of 8 available processors)
470
471 Solution count 5: 7128.44 7124.44 7102.44 ... 4929.74
472
473 Optimal solution found (tolerance 1.00e-08)
474 Best objective 7.128444444444e+03, best bound 7.128444444444e+03, gap 0.0000%
475 SP is solved
476 SP's optimal solution is'□7128
477
478 Itr = 2
479 Collect_LB = [991.0, 7917.444444444444, 8591.444444444445]
480 Collect_UB = [14123.888888888869, 8471.444444444456, 8471.444444444445]
481 Collect_Hua = [0.0, 6566.444444444434, 7120.444444444445]
482 Collect_SPObjVal = [6566.444444444434, 7120.444444444445, 7128.444444444445]
483 Collect_MPObjValNHua = [991.0, 1351.000000000001, 1471.0]
484
485
486 Ops, stop iteration
487 Values adopted from the Itr-1' th iteration, and Itr = {2}, judgeCount = {1}
488
489 ~~~~~judgeCount = 1, SPObj_SPF = 7120.444444444445
490 Vessel i: 0:   pi: 12-18,   ai-di: 2-15,   gi_SP-gpi_SP: 0.000000-0.000000,   ai_SP-di: 2-15,   taoi-delta: 2-15,   taoPi_SP-deltaPi_SP: 2-15,   betaNi: 13
,      bi: 13
491 Vessel i: 1:   pi: 6-12,    ai-di: 14-36,   gi_SP-gpi_SP: 0.000000-0.000000,   ai_SP-di: 14-36,   taoi-delta: 14-37,   taoPi_SP-deltaPi_SP: 14-37,   betaNi
: 23,      bi: 23
492 Vessel i: 2:   pi: 18-25,   ai-di: 14-25,   gi_SP-gpi_SP: 0.000000-0.000000,   ai_SP-di: 14-25,   taoi-delta: 14-21,   taoPi_SP-deltaPi_SP: 14-21,
betaNi: 7,      bi: 7
493 Vessel i: 3:   pi: 12-17,   ai-di: 20-44,   gi_SP-gpi_SP: 0.000000-0.000000,   ai_SP-di: 20-44,   taoi-delta: 20-41,   taoPi_SP-deltaPi_SP: 20-41,
betaNi: 21,     bi: 21
494 Vessel i: 4:   pi: 17-24,   ai-di: 24-30,   gi_SP-gpi_SP: 0.000000-0.000000,   ai_SP-di: 24-30,   taoi-delta: 24-29,   taoPi_SP-deltaPi_SP: 24-29,
betaNi: 5,      bi: 5

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unknown

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495 Vessel i: 5: pi: 17-23, ai-di: 29-48, gi_SP-gpi_SP: 0.200000-1.000000, ai_SP-di: 30-48, taoi-deltai: 32-50, taoPi_SP-deltaPi_SP: 32-50,
    betaNi: 18, bi: 18
496 Vessel i: 6: pi: 9-15, ai-di: 34-63, gi_SP-gpi_SP: 1.000000-0.600000, ai_SP-di: 42-63, taoi-deltai: 42-71, taoPi_SP-deltaPi_SP: 42-71, betaNi
    : 29, bi: 29
497 Vessel i: 7: pi: 28-34, ai-di: 34-43, gi_SP-gpi_SP: 0.800000-0.400000, ai_SP-di: 42-43, taoi-deltai: 38-45, taoPi_SP-deltaPi_SP: 42-45,
    betaNi: 7, bi: 7
498 Vessel i: 8: pi: 28-34, ai-di: 47-66, gi_SP-gpi_SP: 0.000000-1.000000, ai_SP-di: 47-66, taoi-deltai: 47-67, taoPi_SP-deltaPi_SP: 47-67,
    betaNi: 20, bi: 20
499 Vessel i: 9: pi: 17-23, ai-di: 50-68, gi_SP-gpi_SP: 1.000000-0.000000, ai_SP-di: 57-68, taoi-deltai: 57-74, taoPi_SP-deltaPi_SP: 57-74,
    betaNi: 17, bi: 17
500
501 round LB = [991, 7917, 8591]
502 round UB = [14124, 8471, 8471]
503 round Hua = [0, 6566, 7120]
504 round SPObjVal = [6566, 7120, 7128]
505 round MPObjValNHua = [991, 1351, 1471]
506
507 OptimalObj = 8591.444444444445
508 Time: 739.000000
509
510
511
512
```