


```

80 Cover: 77
81 Implied bound: 1
82 MIR: 7
83 StrongCG: 4
84 GUB cover: 26
85 RLT: 2
86 Relax-and-lift: 24
87 BQP: 1
88
89 Explored 1 nodes (25603 simplex iterations) in 26.80 seconds (46.24 work units)
90 Thread count was 8 (of 8 available processors)
91
92 Solution count 4: 803 1003 2123 3583
93
94 Optimal solution found (tolerance 1.00e-10)
95 Best objective 8.030000000000e+02, best bound 8.030000000000e+02, gap 0.0000%
96 Set parameter MIPGap to value 1e-08
97 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
98
99 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
100 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
101
102 Optimize a model with 2481701 rows, 1955335 columns and 17236208 nonzeros
103 Model fingerprint: 0x1e50b9ec
104 Variable types: 963295 continuous, 992040 integer (985965 binary)
105 Coefficient statistics:
106 Matrix range [1e-01, 1e+10]
107 Objective range [6e-05, 5e+01]
108 Bounds range [1e+00, 8e+01]
109 RHS range [8e-01, 1e+10]
110 Warning: Model contains large matrix coefficients
111 Warning: Model contains large rhs
112 Consider reformulating model or setting NumericFocus parameter
113 to avoid numerical issues.
114 Presolve removed 2479011 rows and 1954367 columns (presolve time = 5s) ...
115 Presolve removed 2479389 rows and 1954500 columns
116 Presolve time: 5.98s
117 Presolved: 2312 rows, 835 columns, 6149 nonzeros
118 Variable types: 5 continuous, 830 integer (502 binary)
119 Found heuristic solution: objective 3536.0500186
120
121 Root simplex log...
122
123 Iteration Objective Primal Inf. Dual Inf. Time
124 0 5.9982796e+03 2.982021e+03 0.000000e+00 7s
125 699 4.3290500e+03 0.000000e+00 0.000000e+00 7s
126
127 Root relaxation: objective 4.329050e+03, 699 iterations, 0.01 seconds (0.01 work units)
128
129 Nodes | Current Node | Objective Bounds | Work
130 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
131
132 H 0 0 4329.0500186 8215.74099 89.8% - 7s
133 0 0 - 0 4329.05002 4329.05002 0.00% - 7s
134
135 Explored 1 nodes (979 simplex iterations) in 7.75 seconds (7.88 work units)
136 Thread count was 8 (of 8 available processors)
137
138 Solution count 2: 4329.05 3536.05
139
140 Optimal solution found (tolerance 1.00e-08)
141 Best objective 4.329050018628e+03, best bound 4.329050018628e+03, gap 0.0000%
142 SP is solved
143 SP's optimal solution is'□4329
144
145 Itr = 0
146 Collect_LB = [803.0]
147 Collect_UB = [9461.100037255623]
148 Collect_Hua = [0.0]
149 Collect_SPObjVal = [4329.050018627811]
150 Collect_MPObjValNHua = [803.0]
151
152
153 Set parameter TimeLimit to value 12000
154 Set parameter MIPGap to value 0.0005
155 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
156
157 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
158 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
159
160 Optimize a model with 563248 rows, 283978 columns and 1563500 nonzeros
161 Model fingerprint: 0x52047408
162 Variable types: 1 continuous, 283977 integer (283941 binary)
163 Coefficient statistics:

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164 Matrix range [1e+00, 1e+10]
165 Objective range [1e+00, 2e+01]
166 Bounds range [1e+00, 1e+00]
167 RHS range [1e+00, 2e+10]
168 Warning: Model contains large matrix coefficients
169 Warning: Model contains large rhs
170 Consider reformulating model or setting NumericFocus parameter
171 to avoid numerical issues.
172 Presolve removed 404286 rows and 266303 columns (presolve time = 5s) ...
173 Presolve removed 537987 rows and 276495 columns
174 Presolve time: 8.39s
175 Presolved: 25261 rows, 7483 columns, 100784 nonzeros
176 Variable types: 0 continuous, 7483 integer (7461 binary)
177
178 Root simplex log...
179
180 Iteration Objective Primal Inf. Dual Inf. Time
181 0 5.1320500e+03 8.8900000e+02 0.0000000e+00 9s
182 4703 5.1320500e+03 0.0000000e+00 0.0000000e+00 9s
183
184 Root relaxation: objective 5.132050e+03, 4703 iterations, 0.17 seconds (0.23 work units)
185
186 Nodes | Current Node | Objective Bounds | Work
187 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
188
189 0 0 5132.05002 0 36 - 5132.05002 - - 9s
190 0 0 5132.05002 0 134 - 5132.05002 - - 10s
191 0 0 5132.05002 0 132 - 5132.05002 - - 10s
192 0 0 5132.05002 0 448 - 5132.05002 - - 11s
193 0 0 5132.05002 0 418 - 5132.05002 - - 11s
194 0 0 5132.05002 0 454 - 5132.05002 - - 11s
195 0 0 5132.05002 0 156 - 5132.05002 - - 14s
196 0 0 5132.05002 0 565 - 5132.05002 - - 15s
197 0 0 5132.05002 0 507 - 5132.05002 - - 15s
198 0 0 5132.05002 0 303 - 5132.05002 - - 19s
199 0 0 5132.05002 0 297 - 5132.05002 - - 19s
200 0 0 5132.05002 0 514 - 5132.05002 - - 21s
201 0 0 5132.05002 0 340 - 5132.05002 - - 27s
202 H 0 0 7652.0500186 5132.05002 32.9% - 28s
203 0 0 5132.05002 0 303 7652.05002 5132.05002 32.9% - 29s
204 H 0 0 7052.0500186 5132.05002 27.2% - 30s
205 H 0 0 6972.0500186 5132.05002 26.4% - 30s
206 H 0 0 6572.0500186 5132.05002 21.9% - 30s
207 0 2 5132.05002 0 303 6572.05002 5132.05002 21.9% - 31s
208 3 8 5132.05002 2 493 6572.05002 5132.05002 21.9% 7035 35s
209 15 20 5134.13314 4 1219 6572.05002 5132.05002 21.9% 5430 42s
210 23 29 5132.05002 5 704 6572.05002 5132.05002 21.9% 4692 45s
211 57 43 infeasible 9 6572.05002 5132.05002 21.9% 2834 52s
212 84 72 5142.74236 12 1073 6572.05002 5132.05002 21.9% 2650 56s
213 185 196 5492.05002 24 366 6572.05002 5132.05002 21.9% 1533 60s
214 H 225 234 5932.0500186 5132.05002 13.5% 1272 60s
215 H 391 264 5852.0500186 5132.05002 12.3% 758 62s
216 528 392 5150.86988 8 1944 5852.05002 5132.05002 12.3% 613 65s
217 H 592 228 5412.0500186 5132.05002 5.17% 584 67s
218 599 240 5141.30069 12 753 5412.05002 5132.05002 5.17% 609 70s
219 763 215 5152.05002 44 610 5412.05002 5132.05002 5.17% 563 75s
220 H 807 229 5332.0500186 5132.05002 3.75% 591 77s
221 821 238 5152.05002 52 608 5332.05002 5132.05002 3.75% 609 80s
222 888 154 5152.05002 55 303 5332.05002 5132.05002 3.75% 624 91s
223 894 158 5302.05002 5 646 5332.05002 5175.18834 2.94% 620 95s
224 901 163 5272.05002 7 557 5332.05002 5192.05002 2.63% 615 100s
225 H 905 156 5232.0500186 5192.05002 0.76% 612 104s
226
227 Cutting planes:
228 Learned: 1
229 Gomory: 27
230 Cover: 426
231 Implied bound: 40
232 Projected implied bound: 43
233 Clique: 68
234 MIR: 98
235 StrongCG: 34
236 Flow cover: 231
237 GUB cover: 53
238 Zero half: 92
239 RLT: 13
240 Relax-and-lift: 115
241 BQP: 2
242
243 Explored 906 nodes (712058 simplex iterations) in 104.99 seconds (234.58 work units)
244 Thread count was 8 (of 8 available processors)
245
246 Solution count 9: 5232.05 5332.05 5412.05 ... 7652.05
247

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248 Optimal solution found (tolerance 5.00e-04)
249 Best objective 5.232050018628e+03, best bound 5.232050018628e+03, gap 0.0000%
250 Set parameter MIPGap to value 1e-08
251 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
252
253 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
254 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
255
256 Optimize a model with 2481701 rows, 1955335 columns and 17236208 nonzeros
257 Model fingerprint: 0x9ac0419f
258 Variable types: 963295 continuous, 992040 integer (985965 binary)
259 Coefficient statistics:
260   Matrix range    [1e-01, 1e+10]
261   Objective range [6e-05, 5e+01]
262   Bounds range    [1e+00, 8e+01]
263   RHS range       [8e-01, 1e+10]
264 Warning: Model contains large matrix coefficients
265 Warning: Model contains large rhs
266   Consider reformulating model or setting NumericFocus parameter
267   to avoid numerical issues.
268 Presolve removed 2476584 rows and 1953678 columns (presolve time = 5s) ...
269 Presolve removed 2476913 rows and 1953807 columns
270 Presolve time: 5.16s
271 Presolved: 4788 rows, 1528 columns, 12871 nonzeros
272 Variable types: 8 continuous, 1520 integer (882 binary)
273 Found heuristic solution: objective 3697.0500186
274
275 Root simplex log...
276
277 Iteration   Objective      Primal Inf.   Dual Inf.    Time
278      0    9.3735808e+03   3.644842e+03  0.000000e+00   7s
279    1353   5.2855807e+03   0.000000e+00  0.000000e+00   7s
280
281 Root relaxation: objective 5.285581e+03, 1353 iterations, 0.03 seconds (0.02 work units)
282
283   Nodes | Current Node | Objective Bounds | Work
284 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
285
286 H  0  0           5285.5807430 13966.7410 164% - 6s
287   0  0   -  0    5285.58074 5285.58074 0.00% - 6s
288
289 Explored 1 nodes (2074 simplex iterations) in 6.83 seconds (7.05 work units)
290 Thread count was 8 (of 8 available processors)
291
292 Solution count 2: 5285.58 3697.05
293
294 Optimal solution found (tolerance 1.00e-08)
295 Best objective 5.285580742960e+03, best bound 5.285580742960e+03, gap 0.0000%
296 SP is solved
297 SP's optimal solution is' 5285
298
299 Itr = 1
300 Collect_LB = [803.0, 5232.050018627811]
301 Collect_UB = [9461.100037255623, 6188.580742959544]
302 Collect_Hua = [0.0, 4329.050018627811]
303 Collect_SPObjVal = [4329.050018627811, 5285.580742959544]
304 Collect_MPObjValNHua = [803.0, 903.0]
305
306
307 Set parameter TimeLimit to value 12000
308 Set parameter MIPGap to value 0.0005
309 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
310
311 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
312 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
313
314 Optimize a model with 563249 rows, 283978 columns and 1563519 nonzeros
315 Model fingerprint: 0x11d1c01e
316 Variable types: 1 continuous, 283977 integer (283941 binary)
317 Coefficient statistics:
318   Matrix range    [1e+00, 1e+10]
319   Objective range [1e+00, 2e+01]
320   Bounds range    [1e+00, 1e+00]
321   RHS range       [1e+00, 2e+10]
322 Warning: Model contains large matrix coefficients
323 Warning: Model contains large rhs
324   Consider reformulating model or setting NumericFocus parameter
325   to avoid numerical issues.
326 Presolve removed 413430 rows and 267080 columns (presolve time = 5s) ...
327 Presolve removed 539041 rows and 276661 columns
328 Presolve time: 7.76s
329 Presolved: 24208 rows, 7317 columns, 96550 nonzeros
330 Variable types: 0 continuous, 7317 integer (7295 binary)
331

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332 Root simplex log...
333
334 Iteration   Objective      Primal Inf.   Dual Inf.    Time
335      0  6.1071522e+03  8.840000e+02  0.000000e+00  8s
336   3521  6.1071522e+03  0.000000e+00  0.000000e+00  8s
337
338 Root relaxation: objective 6.107152e+03, 3521 iterations, 0.08 seconds (0.10 work units)
339
340 Nodes | Current Node | Objective Bounds | Work
341 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
342
343  0  0 6107.15217  0  34      -6107.15217  -  -  8s
344  0  0 6107.15217  0 136      -6107.15217  -  -  9s
345  0  0 6107.15217  0 147      -6107.15217  -  -  9s
346  0  0 6107.15217  0 127      -6107.15217  -  -  9s
347  0  0 6107.15217  0 264      -6107.15217  -  -  9s
348  0  0 6107.15217  0 258      -6107.15217  -  -  9s
349  0  0 6107.15217  0 226      -6107.15217  -  - 10s
350  0  0 6107.15217  0 224      -6107.15217  -  - 10s
351  0  0 6107.15217  0 427      -6107.15217  -  - 11s
352  0  0 6107.15217  0 458      -6107.15217  -  - 11s
353  0  0 6107.15217  0 198      -6107.15217  -  - 14s
354  0  0 6107.15217  0 244      -6107.15217  -  - 15s
355  0  0 6107.15217  0 220      -6107.15217  -  - 15s
356  0  0 6107.15217  0 284      -6107.15217  -  - 15s
357  0  0 6107.15217  0 264      -6107.15217  -  - 15s
358  0  0 6107.15217  0 113      -6107.15217  -  - 17s
359 H  0  0              8827.1521715 6107.15217 30.8%  - 17s
360  0  0 6107.15217  0  67 8827.15217 6107.15217 30.8%  - 17s
361 H  0  0              7087.1521715 6107.15217 13.8%  - 18s
362 H  0  0              6707.1521715 6107.15217 8.95%  - 19s
363  0  2 6107.15217  0  67 6707.15217 6107.15217 8.95%  - 19s
364  7 10 6107.15217  3 149 6707.15217 6107.15217 8.95% 1245 20s
365 50 47 6107.15217 11 205 6707.15217 6107.15217 8.95% 1304 25s
366 H 69  65              6567.1521715 6107.15217 7.00% 1251 26s
367 H 117 100              6367.1521715 6107.15217 4.08%  930 28s
368 174 121 6107.15217 31 249 6367.15217 6107.15217 4.08%  794 30s
369 H 368 214              6307.1521715 6107.15217 3.17%  523 33s
370 H 529 255              6267.1521715 6107.15217 2.55%  439 34s
371 552 264 6107.15217 61 311 6267.15217 6107.15217 2.55%  422 35s
372 H 557 264              6247.1521715 6107.15217 2.24%  420 35s
373 H 562 264              6207.1521715 6107.15217 1.61%  417 35s
374 H 642 275              6167.1521715 6107.15217 0.97%  372 35s
375 1003 75 6107.15217 18 565 6167.15217 6107.15217 0.97%  288 40s
376 H 1016 75              6127.1521715 6107.15217 0.33%  285 40s
377
378 Explored 1120 nodes (365288 simplex iterations) in 41.75 seconds (85.45 work units)
379 Thread count was 8 (of 8 available processors)
380
381 Solution count 10: 6127.15 6167.15 6207.15 ... 7087.15
382
383 Optimal solution found (tolerance 5.00e-04)
384 Best objective 6.127152171531e+03, best bound 6.127152171531e+03, gap 0.0000%
385 Set parameter MIPGap to value 1e-08
386 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
387
388 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
389 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
390
391 Optimize a model with 2481701 rows, 1955335 columns and 17236208 nonzeros
392 Model fingerprint: 0x23d88fe7
393 Variable types: 963295 continuous, 992040 integer (985965 binary)
394 Coefficient statistics:
395   Matrix range    [1e-01, 1e+10]
396   Objective range [6e-05, 5e+01]
397   Bounds range    [1e+00, 8e+01]
398   RHS range       [8e-01, 1e+10]
399 Warning: Model contains large matrix coefficients
400 Warning: Model contains large rhs
401   Consider reformulating model or setting NumericFocus parameter
402   to avoid numerical issues.
403 Presolve removed 2476869 rows and 1953786 columns (presolve time = 5s) ...
404 Presolve removed 2476901 rows and 1953806 columns
405 Presolve time: 5.17s
406 Presolved: 4800 rows, 1529 columns, 12833 nonzeros
407 Variable types: 8 continuous, 1521 integer (884 binary)
408 Found heuristic solution: objective 3487.2950287
409
410 Root simplex log...
411
412 Iteration   Objective      Primal Inf.   Dual Inf.    Time
413      0  9.0775808e+03  3.707917e+03  0.000000e+00  7s
414   1505  5.0582241e+03  0.000000e+00  0.000000e+00  7s
415

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416 Root relaxation: objective 5.058224e+03, 1505 iterations, 0.01 seconds (0.02 work units)
417
418   Nodes | Current Node | Objective Bounds | Work
419 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
420
421   0    0 5058.22411   0 22 3487.29503 5058.22411 45.0% - 6s
422 H   0    0          5057.8528892 5058.22411 0.01% - 6s
423
424 Cutting planes:
425 Gomory: 1
426 Clique: 2
427 MIR: 3
428 Flow cover: 1
429 Zero half: 1
430
431 Explored 1 nodes (2015 simplex iterations) in 6.85 seconds (7.46 work units)
432 Thread count was 8 (of 8 available processors)
433
434 Solution count 2: 5057.85 3487.3
435
436 Optimal solution found (tolerance 1.00e-08)
437 Best objective 5.057852889165e+03, best bound 5.057852889165e+03, gap 0.0000%
438 SP is solved
439 SP's optimal solution is'□5057
440
441 Itr = 2
442 Collect_LB = [803.0, 5232.050018627811, 6127.152171530973]
443 Collect_UB = [9461.100037255623, 6188.580742959544, 5899.424317736787]
444 Collect_Hua = [0.0, 4329.050018627811, 5285.580742959544]
445 Collect_SPObjVal = [4329.050018627811, 5285.580742959544, 5057.852889165359]
446 Collect_MPObjValNHua = [803.0, 903.0, 841.5714285714284]
447
448
449 Ops, stop iteration
450 Values adopted from the Itr-1' th iteration, and Itr = {2}, judgeCount = {1}
451
452 ~~~~~judgeCount = 1, SPObj_SPF = 5285.580742959544
453 Vessel i: 0: pi: 0-6, ai-di: 70-81, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 70-81, taoi-deltai: 70-81, taoPi_SP-deltaPi_SP: 70-81, betaNi:
11, bi: 11
454 Vessel i: 1: pi: 0-6, ai-di: 13-31, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 13-31, taoi-deltai: 13-31, taoPi_SP-deltaPi_SP: 13-31, betaNi:
18, bi: 18
455 Vessel i: 2: pi: 6-13, ai-di: 27-50, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 27-50, taoi-deltai: 27-50, taoPi_SP-deltaPi_SP: 27-50, betaNi:
23, bi: 23
456 Vessel i: 3: pi: 13-20, ai-di: 25-49, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 25-49, taoi-deltai: 25-49, taoPi_SP-deltaPi_SP: 25-49,
betaNi: 24, bi: 24
457 Vessel i: 4: pi: 20-26, ai-di: 31-37, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 31-37, taoi-deltai: 31-37, taoPi_SP-deltaPi_SP: 31-37,
betaNi: 6, bi: 6
458 Vessel i: 5: pi: 28-34, ai-di: 16-38, gi_SP-gpi_SP: 0.214286-0.700000, ai_SP-di: 17-38, taoi-deltai: 21-32, taoPi_SP-deltaPi_SP: 21-32,
betaNi: 11, bi: 11
459 Vessel i: 6: pi: 14-19, ai-di: 6-24, gi_SP-gpi_SP: 1.000000-0.000000, ai_SP-di: 14-24, taoi-deltai: 10-16, taoPi_SP-deltaPi_SP: 14-16, betaNi:
6, bi: 6
460 Vessel i: 7: pi: 27-34, ai-di: 30-49, gi_SP-gpi_SP: 0.900000-0.700000, ai_SP-di: 39-49, taoi-deltai: 36-41, taoPi_SP-deltaPi_SP: 39-41,
betaNi: 5, bi: 5
461 Vessel i: 8: pi: 27-34, ai-di: 40-73, gi_SP-gpi_SP: 0.285714-1.000000, ai_SP-di: 42-73, taoi-deltai: 42-61, taoPi_SP-deltaPi_SP: 42-61,
betaNi: 19, bi: 19
462
463 round LB = [803, 5232, 6127]
464 round UB = [9461, 6189, 5899]
465 round Hua = [0, 4329, 5286]
466 round SPObjVal = [4329, 5286, 5058]
467 round MPObjValNHua = [803, 903, 842]
468
469 OptimalObj = 6127.152171530973
470 Time: 636.000000
471
472
473
474

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