


```

80 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
81
82 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
83 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
84
85 Optimize a model with 1153828 rows, 901813 columns and 7829795 nonzeros
86 Model fingerprint: 0x44d2dd13
87 Variable types: 441325 continuous, 460488 integer (456438 binary)
88 Coefficient statistics:
89   Matrix range    [1e-01, 1e+10]
90   Objective range [6e-05, 5e+01]
91   Bounds range    [1e+00, 8e+01]
92   RHS range       [8e-01, 1e+10]
93 Warning: Model contains large matrix coefficients
94 Warning: Model contains large rhs
95   Consider reformulating model or setting NumericFocus parameter
96   to avoid numerical issues.
97 Presolve removed 1151379 rows and 900916 columns
98 Presolve time: 2.47s
99 Presolved: 2449 rows, 897 columns, 6631 nonzeros
100 Variable types: 0 continuous, 897 integer (507 binary)
101 Found heuristic solution: objective 3134.6666667
102 Found heuristic solution: objective 3194.6666667
103
104 Root relaxation: objective 4.522667e+03, 799 iterations, 0.00 seconds (0.01 work units)
105
106   Nodes | Current Node | Objective Bounds | Work
107   Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
108
109 H   0   0           4522.6666667 9482.66667 110%   -   3s
110   0   0   -   0   4522.66667 4522.66667 0.00%   -   3s
111
112 Explored 1 nodes (1042 simplex iterations) in 3.30 seconds (3.47 work units)
113 Thread count was 8 (of 8 available processors)
114
115 Solution count 3: 4522.67 3194.67 3134.67
116
117 Optimal solution found (tolerance 1.00e-08)
118 Best objective 4.522666666667e+03, best bound 4.522666666667e+03, gap 0.0000%
119 SP is solved
120 SP's optimal solution is'□4522
121
122   Itr = 0
123   Collect_LB = [682.0]
124   Collect_UB = [9727.333333333332]
125   Collect_Hua = [0.0]
126   Collect_SPObjVal = [4522.666666666666]
127   Collect_MPObjValNHua = [682.0]
128
129
130 Set parameter MIPGap to value 0.05
131 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
132
133 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
134 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
135
136 Optimize a model with 617649 rows, 150727 columns and 1816556 nonzeros
137 Model fingerprint: 0xdba43eca
138 Variable types: 1 continuous, 150726 integer (143124 binary)
139 Coefficient statistics:
140   Matrix range    [1e-01, 1e+10]
141   Objective range [1e+00, 2e+01]
142   Bounds range    [1e+00, 1e+00]
143   RHS range       [1e+00, 2e+10]
144 Warning: Model contains large matrix coefficients
145 Warning: Model contains large rhs
146   Consider reformulating model or setting NumericFocus parameter
147   to avoid numerical issues.
148 Presolve removed 494748 rows and 133532 columns (presolve time = 5s) ...
149 Presolve removed 552593 rows and 140369 columns
150 Presolve time: 9.18s
151 Presolved: 65056 rows, 10358 columns, 203340 nonzeros
152 Variable types: 0 continuous, 10358 integer (8623 binary)
153
154 Deterministic concurrent LP optimizer: primal and dual simplex (primal and dual model)
155 Showing first log only...
156
157 Root relaxation presolved: 10358 rows, 75414 columns, 213698 nonzeros
158
159
160 Root simplex log...
161
162 Iteration Objective Primal Inf. Dual Inf. Time
163   0 5.3396667e+03 0.000000e+00 2.270395e+04 10s

```

```

164 3562 5.3429611e+03 0.000000e+00 3.213694e+04 10s
165 8796 5.3396667e+03 0.000000e+00 0.000000e+00 11s
166 8796 5.3396667e+03 0.000000e+00 0.000000e+00 11s
167 Concurrent spin time: 0.09s
168
169 Solved with primal simplex
170
171 Root relaxation: objective 5.339667e+03, 8796 iterations, 1.39 seconds (1.44 work units)
172
173 Nodes | Current Node | Objective Bounds | Work
174 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
175
176 0 0 5339.66667 0 225 - 5339.66667 - - 13s
177 0 0 5339.66667 0 533 - 5339.66667 - - 16s
178 0 0 5339.66667 0 493 - 5339.66667 - - 17s
179 H 0 0 5339.6666667 5339.66667 0.00% - 24s
180 0 0 5339.66667 0 178 5339.66667 5339.66667 0.00% - 25s
181
182 Cutting planes:
183 Learned: 1
184 Gomory: 11
185 Lift-and-project: 17
186 Cover: 144
187 Implied bound: 234
188 Clique: 3749
189 MIR: 99
190 StrongCG: 39
191 Flow cover: 4
192 GUB cover: 69
193 Zero half: 68
194 RLT: 39
195 Relax-and-lift: 123
196 BQP: 65
197
198 Explored 1 nodes (41774 simplex iterations) in 25.13 seconds (33.60 work units)
199 Thread count was 8 (of 8 available processors)
200
201 Solution count 1: 5339.67
202
203 Optimal solution found (tolerance 5.00e-02)
204 Best objective 5.339666666667e+03, best bound 5.339666666667e+03, gap 0.0000%
205 Set parameter MIPGap to value 1e-08
206 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
207
208 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
209 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
210
211 Optimize a model with 1153828 rows, 901813 columns and 7829795 nonzeros
212 Model fingerprint: 0x05f8cccd
213 Variable types: 441325 continuous, 460488 integer (456438 binary)
214 Coefficient statistics:
215 Matrix range [1e-01, 1e+10]
216 Objective range [6e-05, 5e+01]
217 Bounds range [1e+00, 8e+01]
218 RHS range [8e-01, 1e+10]
219 Warning: Model contains large matrix coefficients
220 Warning: Model contains large rhs
221 Consider reformulating model or setting NumericFocus parameter
222 to avoid numerical issues.
223 Presolve removed 1150527 rows and 900729 columns
224 Presolve time: 2.50s
225 Presolved: 3301 rows, 1084 columns, 9052 nonzeros
226 Variable types: 0 continuous, 1084 integer (604 binary)
227
228 Root relaxation: objective 4.752667e+03, 1117 iterations, 0.02 seconds (0.02 work units)
229
230 Nodes | Current Node | Objective Bounds | Work
231 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
232
233 H 0 0 4752.6666667 11412.6667 140% - 3s
234 0 0 - 0 4752.66667 4752.66667 0.00% - 3s
235
236 Explored 1 nodes (1360 simplex iterations) in 3.29 seconds (3.42 work units)
237 Thread count was 8 (of 8 available processors)
238
239 Solution count 1: 4752.67
240
241 Optimal solution found (tolerance 1.00e-08)
242 Best objective 4.752666666667e+03, best bound 4.752666666667e+03, gap 0.0000%
243 SP is solved
244 SP's optimal solution is'□4752
245
246 Itr = 1
247 Collect_LB = [682.0, 5339.666666666666]

```

```

248 Collect_UB = [9727.33333333332, 5569.666666666666]
249 Collect_Hua = [0.0, 4522.666666666666]
250 Collect_SPObjVal = [4522.666666666666, 4752.666666666666]
251 Collect_MPObjValNHua = [682.0, 817.0]
252
253
254 Set parameter MIPGap to value 0.05
255 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
256
257 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
258 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
259
260 Optimize a model with 870275 rows, 163849 columns and 2633664 nonzeros
261 Model fingerprint: 0xd1a1d38d
262 Variable types: 1 continuous, 163848 integer (148668 binary)
263 Coefficient statistics:
264   Matrix range    [1e-01, 1e+10]
265   Objective range [1e+00, 2e+01]
266   Bounds range    [1e+00, 1e+00]
267   RHS range       [1e+00, 2e+10]
268 Warning: Model contains large matrix coefficients
269 Warning: Model contains large rhs
270   Consider reformulating model or setting NumericFocus parameter
271   to avoid numerical issues.
272 Presolve removed 714204 rows and 142528 columns (presolve time = 5s) ...
273 Presolve removed 725770 rows and 143165 columns (presolve time = 10s) ...
274 Presolve removed 778334 rows and 149548 columns
275 Presolve time: 13.32s
276 Presolved: 91941 rows, 14301 columns, 308920 nonzeros
277 Variable types: 0 continuous, 14301 integer (10861 binary)
278
279 Deterministic concurrent LP optimizer: primal and dual simplex (primal and dual model)
280 Showing first log only...
281
282 Root relaxation presolved: 14301 rows, 106242 columns, 323221 nonzeros
283
284
285 Root simplex log...
286
287 Iteration   Objective      Primal Inf.   Dual Inf.    Time
288      0  5.5946667e+03  0.000000e+00  4.448889e+04  14s
289    8213  5.6008226e+03  0.000000e+00  6.014557e+05  15s
290   14725  5.5946667e+03  0.000000e+00  0.000000e+00  16s
291   14725  5.5946667e+03  0.000000e+00  0.000000e+00  16s
292 Concurrent spin time: 0.20s
293
294 Solved with primal simplex
295
296 Root relaxation: objective 5.594667e+03, 14725 iterations, 2.62 seconds (2.73 work units)
297 Total elapsed time = 20.28s
298
299   Nodes | Current Node | Objective Bounds | Work
300 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
301
302   0   0 5594.66667   0 513    -5594.66667   -   - 22s
303   0   0 5594.66667   0 528    -5594.66667   -   - 22s
304   0   0 5594.66667   0 530    -5594.66667   -   - 22s
305   0   0 5594.66667   0 707    -5594.66667   -   - 27s
306   0   0 5594.66667   0 922    -5594.66667   -   - 30s
307   0   0 5594.66667   0 924    -5594.66667   -   - 30s
308   0   0 5594.66667   0 372    -5594.66667   -   - 42s
309   0   0 5594.66667   0 444    -5594.66667   -   - 43s
310   0   0 5594.66667   0 362    -5594.66667   -   - 50s
311   0   0 5594.66667   0 386    -5594.66667   -   - 50s
312   0   0 5594.66667   0 512    -5594.66667   -   - 51s
313   0   0 5594.66667   0 183    -5594.66667   -   - 58s
314   0   0 5594.66667   0 184    -5594.66667   -   - 59s
315   0   0 5594.66667   0 175    -5594.66667   -   - 59s
316   0   0 5594.66667   0 301    -5594.66667   -   - 63s
317   0   0 5594.66667   0 348    -5594.66667   -   - 63s
318   0   0 5594.66667   0 350    -5594.66667   -   - 63s
319   0   0 5594.66667   0 319    -5594.66667   -   - 64s
320   0   0 5594.66667   0 179    -5594.66667   -   - 68s
321   0   0 5594.66667   0 187    -5594.66667   -   - 68s
322   0   0 5594.66667   0 187    -5594.66667   -   - 70s
323   0   2 5594.66667   0 187    -5594.66667   -   - 79s
324   1   4 5594.66667   1 193    -5594.66667   - 7622  80s
325   7  12 5594.66667   3 269    -5594.66667   - 3549  86s
326  11  16 5594.66667   3 1050    -5594.66667   - 3984  94s
327  15  19 5594.66667   4 274    -5594.66667   - 5793  97s
328  19  23 5594.66667   5 244    -5594.66667   - 5208 101s
329  29  45 5594.66667   8 238    -5594.66667   - 4349 110s
330  47  77 5594.66667  15 180    -5594.66667   - 3556 120s
331 103 193 5594.66667  37 125    -5594.66667   - 2181 132s

```

```

332 284 463 5594.66667 88 108 - 5594.66667 - 897 144s
333 618 748 6114.66667 184 396 - 5594.66667 - 462 156s
334 * 858 496 368 5594.6666667 5594.66667 0.00% 370 157s
335
336 Cutting planes:
337 Learned: 21
338 Gomory: 2
339 Cover: 554
340 Implied bound: 347
341 Clique: 6033
342 MIR: 235
343 StrongCG: 86
344 Flow cover: 17
345 GUB cover: 62
346 Zero half: 28
347 Network: 1
348 RLT: 129
349 Relax-and-lift: 565
350 BQP: 53
351 PSD: 4
352
353 Explored 964 nodes (498809 simplex iterations) in 157.12 seconds (343.88 work units)
354 Thread count was 8 (of 8 available processors)
355
356 Solution count 1: 5594.67
357
358 Optimal solution found (tolerance 5.00e-02)
359 Best objective 5.594666666667e+03, best bound 5.594666666667e+03, gap 0.0000%
360 Warning: linear constraint 365024 and linear constraint 617650 have the same name "ConSP25_1[0,0]"
361 Set parameter MIPGap to value 1e-08
362 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
363
364 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
365 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
366
367 Optimize a model with 1153828 rows, 901813 columns and 7829795 nonzeros
368 Model fingerprint: 0xf2f10219
369 Variable types: 441325 continuous, 460488 integer (456438 binary)
370 Coefficient statistics:
371 Matrix range [1e-01, 1e+10]
372 Objective range [6e-05, 5e+01]
373 Bounds range [1e+00, 8e+01]
374 RHS range [8e-01, 1e+10]
375 Warning: Model contains large matrix coefficients
376 Warning: Model contains large rhs
377 Consider reformulating model or setting NumericFocus parameter
378 to avoid numerical issues.
379 Presolve removed 1151061 rows and 900846 columns
380 Presolve time: 2.39s
381 Presolved: 2767 rows, 967 columns, 7422 nonzeros
382 Variable types: 0 continuous, 967 integer (548 binary)
383 Found heuristic solution: objective 3999.6666667
384
385 Root relaxation: objective 4.762667e+03, 753 iterations, 0.01 seconds (0.01 work units)
386
387 Nodes | Current Node | Objective Bounds | Work
388 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
389
390 0 0 4762.66667 0 8 3999.66667 4762.66667 19.1% - 3s
391 H 0 0 4762.6666667 4762.66667 0.00% - 3s
392 0 0 4762.66667 0 8 4762.66667 4762.66667 0.00% - 3s
393
394 Explored 1 nodes (753 simplex iterations) in 3.14 seconds (3.34 work units)
395 Thread count was 8 (of 8 available processors)
396
397 Solution count 2: 4762.67 3999.67
398
399 Optimal solution found (tolerance 1.00e-08)
400 Best objective 4.762666666667e+03, best bound 4.762666666667e+03, gap 0.0000%
401 SP is solved
402 SP's optimal solution is' 4762
403
404 Itr = 2
405 Collect_LB = [682.0, 5339.666666666666, 5594.666666666666]
406 Collect_UB = [9727.333333333332, 5569.666666666666, 5569.666666666666]
407 Collect_Hua = [0.0, 4522.666666666666, 4752.666666666666]
408 Collect_SPObjVal = [4522.666666666666, 4752.666666666666, 4762.666666666666]
409 Collect_MPObjValNHua = [682.0, 817.0, 842.0]
410
411
412 Reach the termination conditions, stop iteration
413 Values adopted from the judgeCount's th iteration, and Itr = {2}, judgeCount = {1}
414
415 ~~~~~judgeCount = 1, SPObj_SPF = 4752.666666666666

```

unknown

416	Vessel i: 0: , bi: 33	pi: 8-13,	ai-di: 1-37,	gi_SP-gpi_SP: 0.000000-0.000000,	ai_SP-di: 1-37,	taoi-deltai: 1-34,	taoPi_SP-deltaPi_SP: 1-34,	betaNi: 33
417	Vessel i: 1: betaNi: 22,	pi: 13-19, bi: 22	ai-di: 10-30,	gi_SP-gpi_SP: 0.000000-0.000000,	ai_SP-di: 10-30,	taoi-deltai: 10-32,	taoPi_SP-deltaPi_SP: 10-32,	
418	Vessel i: 2: betaNi: 16,	pi: 19-24, bi: 16	ai-di: 11-24,	gi_SP-gpi_SP: 0.000000-0.000000,	ai_SP-di: 11-24,	taoi-deltai: 11-27,	taoPi_SP-deltaPi_SP: 11-27,	
419	Vessel i: 3: betaNi: 9,	pi: 24-29, bi: 9	ai-di: 13-26,	gi_SP-gpi_SP: 0.000000-0.000000,	ai_SP-di: 13-26,	taoi-deltai: 13-22,	taoPi_SP-deltaPi_SP: 13-22,	
420	Vessel i: 4: betaNi: 22,	pi: 17-22, bi: 22	ai-di: 38-63,	gi_SP-gpi_SP: 0.200000-1.000000,	ai_SP-di: 39-63,	taoi-deltai: 41-63,	taoPi_SP-deltaPi_SP: 41-63,	
421	Vessel i: 5: betaNi: 10,	pi: 12-17, bi: 10	ai-di: 40-50,	gi_SP-gpi_SP: 1.000000-0.200000,	ai_SP-di: 47-50,	taoi-deltai: 46-56,	taoPi_SP-deltaPi_SP: 48-56,	
422								
423	round LB = [682, 5340, 5595]							
424	round UB = [9727, 5570, 5570]							
425	round Hua = [0, 4523, 4753]							
426	round SPObjVal = [4523, 4753, 4763]							
427	round MPObjValNHua = [682, 817, 842]							
428								
429	Time: 434.000000							
430								
431								
432								
433								