


```

80 Bounds range [1e+00, 8e+01]
81 RHS range [8e-01, 1e+10]
82 Warning: Model contains large matrix coefficients
83 Warning: Model contains large rhs
84 Consider reformulating model or setting NumericFocus parameter
85 to avoid numerical issues.
86 Presolve removed 1152440 rows and 901330 columns
87 Presolve time: 2.64s
88 Presolved: 1427 rows, 483 columns, 3802 nonzeros
89 Variable types: 0 continuous, 483 integer (274 binary)
90 Found heuristic solution: objective 2803.6666667
91
92 Root relaxation: objective 3.220667e+03, 293 iterations, 0.01 seconds (0.00 work units)
93
94 Nodes | Current Node | Objective Bounds | Work
95 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
96
97 H 0 0 3220.6666667 6180.66667 91.9% - 3s
98 0 0 - 0 3220.66667 3220.66667 0.00% - 3s
99
100 Explored 1 nodes (445 simplex iterations) in 3.48 seconds (3.65 work units)
101 Thread count was 8 (of 8 available processors)
102
103 Solution count 2: 3220.67 2803.67
104
105 Optimal solution found (tolerance 1.00e-08)
106 Best objective 3.220666666667e+03, best bound 3.220666666667e+03, gap 0.00000%
107 SP is solved
108 SP's optimal solution is'□3220
109
110 Itr = 0
111 Collect_LB = [666.0]
112 Collect_UB = [7107.3333333333285]
113 Collect_Hua = [0.0]
114 Collect_SPObjVal = [3220.6666666666642]
115 Collect_MPObjValNHua = [666.0]
116
117
118 Set parameter TimeLimit to value 12000
119 Set parameter MIPGap to value 0.0005
120 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
121
122 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
123 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
124
125 Optimize a model with 382145 rows, 137605 columns and 1048210 nonzeros
126 Model fingerprint: 0xbadabcd3
127 Variable types: 1 continuous, 137604 integer (137580 binary)
128 Coefficient statistics:
129 Matrix range [1e+00, 1e+10]
130 Objective range [1e+00, 2e+01]
131 Bounds range [1e+00, 1e+00]
132 RHS range [1e+00, 2e+10]
133 Warning: Model contains large matrix coefficients
134 Warning: Model contains large rhs
135 Consider reformulating model or setting NumericFocus parameter
136 to avoid numerical issues.
137 Presolve removed 355841 rows and 133024 columns
138 Presolve time: 4.51s
139 Presolved: 26304 rows, 4581 columns, 69310 nonzeros
140 Variable types: 0 continuous, 4581 integer (4566 binary)
141 Root relaxation presolved: 4581 rows, 30885 columns, 73891 nonzeros
142
143
144 Root relaxation: objective 4.066667e+03, 3466 iterations, 0.21 seconds (0.33 work units)
145
146 Nodes | Current Node | Objective Bounds | Work
147 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
148
149 0 0 4066.66667 0 7 -4066.66667 - - 5s
150 0 0 4066.66667 0 169 -4066.66667 - - 5s
151 0 0 4066.66667 0 162 -4066.66667 - - 5s
152 H 0 0 4146.6666667 4066.66667 1.93% - 5s
153 0 0 4066.66667 0 99 4146.66667 4066.66667 1.93% - 5s
154 0 0 4066.66667 0 102 4146.66667 4066.66667 1.93% - 5s
155 0 0 4066.66667 0 63 4146.66667 4066.66667 1.93% - 5s
156 H 0 0 4066.6666667 4066.66667 0.00% - 6s
157
158 Cutting planes:
159 Cover: 105
160 Implied bound: 660
161 Clique: 25
162 MIR: 8
163 StrongCG: 2

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164 GUB cover: 6
165 Zero half: 3
166 RLT: 1
167 Relax-and-lift: 49
168
169 Explored 1 nodes (7800 simplex iterations) in 6.14 seconds (9.60 work units)
170 Thread count was 8 (of 8 available processors)
171
172 Solution count 2: 4066.67 4146.67
173
174 Optimal solution found (tolerance 5.00e-04)
175 Best objective 4.06666666667e+03, best bound 4.06666666667e+03, gap 0.0000%
176 Set parameter MIPGap to value 1e-08
177 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
178
179 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
180 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
181
182 Optimize a model with 1153867 rows, 901813 columns and 7829844 nonzeros
183 Model fingerprint: 0x1926e721
184 Variable types: 441325 continuous, 460488 integer (456438 binary)
185 Coefficient statistics:
186 Matrix range [1e-01, 1e+10]
187 Objective range [6e-05, 5e+01]
188 Bounds range [1e+00, 8e+01]
189 RHS range [8e-01, 1e+10]
190 Warning: Model contains large matrix coefficients
191 Warning: Model contains large rhs
192 Consider reformulating model or setting NumericFocus parameter
193 to avoid numerical issues.
194 Presolve removed 1152286 rows and 901234 columns
195 Presolve time: 2.36s
196 Presolved: 1581 rows, 579 columns, 4212 nonzeros
197 Variable types: 4 continuous, 575 integer (337 binary)
198 Found heuristic solution: objective 2624.3818887
199
200 Root relaxation: objective 3.444667e+03, 417 iterations, 0.00 seconds (0.00 work units)
201
202 Nodes | Current Node | Objective Bounds | Work
203 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
204
205 H 0 0 3444.6666667 6522.00000 89.3% - 3s
206 0 0 - 0 3444.66667 3444.66667 0.00% - 3s
207
208 Explored 1 nodes (569 simplex iterations) in 3.14 seconds (3.18 work units)
209 Thread count was 8 (of 8 available processors)
210
211 Solution count 2: 3444.67 2624.38
212
213 Optimal solution found (tolerance 1.00e-08)
214 Best objective 3.44466666667e+03, best bound 3.44466666667e+03, gap 0.0000%
215 SP is solved
216 SP's optimal solution is'□3444
217
218 Itr = 1
219 Collect_LB = [666.0, 4066.6666666666642]
220 Collect_UB = [7107.3333333333285, 4290.666666666664]
221 Collect_Hua = [0.0, 3220.6666666666642]
222 Collect_SPObjVal = [3220.6666666666642, 3444.6666666666642]
223 Collect_MPObjValNHua = [666.0, 846.0]
224
225
226 Set parameter TimeLimit to value 12000
227 Set parameter MIPGap to value 0.0005
228 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
229
230 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
231 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
232
233 Optimize a model with 382146 rows, 137605 columns and 1048223 nonzeros
234 Model fingerprint: 0x66aa3021
235 Variable types: 1 continuous, 137604 integer (137580 binary)
236 Coefficient statistics:
237 Matrix range [1e+00, 1e+10]
238 Objective range [1e+00, 2e+01]
239 Bounds range [1e+00, 1e+00]
240 RHS range [1e+00, 2e+10]
241 Warning: Model contains large matrix coefficients
242 Warning: Model contains large rhs
243 Consider reformulating model or setting NumericFocus parameter
244 to avoid numerical issues.
245 Presolve removed 355842 rows and 133024 columns
246 Presolve time: 4.48s
247 Presolved: 26304 rows, 4581 columns, 69310 nonzeros

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248 Variable types: 0 continuous, 4581 integer (4566 binary)
249 Root relaxation presolved: 4581 rows, 30885 columns, 73891 nonzeros
250
251
252 Root relaxation: objective 4.290667e+03, 3466 iterations, 0.21 seconds (0.33 work units)
253
254 Nodes | Current Node | Objective Bounds | Work
255 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
256
257 0 0 4290.66667 0 7 -4290.66667 - - 4s
258 0 0 4290.66667 0 169 -4290.66667 - - 5s
259 0 0 4290.66667 0 162 -4290.66667 - - 5s
260 H 0 0 4370.6666667 4290.66667 1.83% - 5s
261 0 0 4290.66667 0 99 4370.66667 4290.66667 1.83% - 5s
262 0 0 4290.66667 0 102 4370.66667 4290.66667 1.83% - 5s
263 0 0 4290.66667 0 63 4370.66667 4290.66667 1.83% - 5s
264 H 0 0 4290.6666667 4290.66667 0.00% - 5s
265
266 Cutting planes:
267 Cover: 105
268 Implied bound: 660
269 Clique: 25
270 MIR: 8
271 StrongCG: 2
272 GUB cover: 6
273 Zero half: 3
274 RLT: 1
275 Relax-and-lift: 49
276
277 Explored 1 nodes (7800 simplex iterations) in 5.98 seconds (9.60 work units)
278 Thread count was 8 (of 8 available processors)
279
280 Solution count 2: 4290.67 4370.67
281
282 Optimal solution found (tolerance 5.00e-04)
283 Best objective 4.29066666667e+03, best bound 4.29066666667e+03, gap 0.0000%
284 Set parameter MIPGap to value 1e-08
285 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
286
287 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
288 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
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290 Optimize a model with 1153867 rows, 901813 columns and 7829844 nonzeros
291 Model fingerprint: 0x1926e721
292 Variable types: 441325 continuous, 460488 integer (456438 binary)
293 Coefficient statistics:
294 Matrix range [1e-01, 1e+10]
295 Objective range [6e-05, 5e+01]
296 Bounds range [1e+00, 8e+01]
297 RHS range [8e-01, 1e+10]
298 Warning: Model contains large matrix coefficients
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301 to avoid numerical issues.
302 Presolve removed 1152286 rows and 901234 columns
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304 Presolved: 1581 rows, 579 columns, 4212 nonzeros
305 Variable types: 4 continuous, 575 integer (337 binary)
306 Found heuristic solution: objective 2624.3818887
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308 Root relaxation: objective 3.444667e+03, 417 iterations, 0.00 seconds (0.00 work units)
309
310 Nodes | Current Node | Objective Bounds | Work
311 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
312
313 H 0 0 3444.6666667 6522.00000 89.3% - 2s
314 0 0 - 0 3444.66667 3444.66667 0.00% - 2s
315
316 Explored 1 nodes (569 simplex iterations) in 3.12 seconds (3.18 work units)
317 Thread count was 8 (of 8 available processors)
318
319 Solution count 2: 3444.67 2624.38
320
321 Optimal solution found (tolerance 1.00e-08)
322 Best objective 3.44466666667e+03, best bound 3.44466666667e+03, gap 0.0000%
323 SP is solved
324 SP's optimal solution is'□3444
325
326 Itr = 2
327 Collect_LB = [666.0, 4066.6666666666642, 4290.666666666664]
328 Collect_UB = [7107.3333333333285, 4290.666666666664, 4290.666666666664]
329 Collect_Hua = [0.0, 3220.6666666666642, 3444.6666666666642]
330 Collect_SPObjVal = [3220.6666666666642, 3444.6666666666642, 3444.6666666666642]
331 Collect_MPObjValNHua = [666.0, 846.0, 846.0]
```

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332
333
334   Reach the termination conditions, stop iteration
335   Values adopted from the Itr' th iteration, and Itr = {2}, judgeCount = {2}
336
337   ~~~~~judge = 2, SPObj_SPF = 3444.66666666666642
338   Vessel i: 0:   pi: 0-6,   ai-di: 2-23,   gi_SP-gpi_SP: 0.000000-0.000000,   ai_SP-di: 2-23,   taoi-deltai: 2-25,   taoPi_SP-deltaPi_SP: 2-21,   betaNi: 23
339   ,   bi: 23
339   Vessel i: 1:   pi: 6-13,   ai-di: 8-17,   gi_SP-gpi_SP: 0.000000-0.000000,   ai_SP-di: 8-17,   taoi-deltai: 8-16,   taoPi_SP-deltaPi_SP: 8-16,   betaNi: 8
340   ,   bi: 8
340   Vessel i: 2:   pi: 3-10,   ai-di: 34-42,   gi_SP-gpi_SP: 0.000000-0.000000,   ai_SP-di: 34-42,   taoi-deltai: 34-41,   taoPi_SP-deltaPi_SP: 34-39,   betaNi: 7
341   : 7,   bi: 7
341   Vessel i: 3:   pi: 12-19,   ai-di: 40-58,   gi_SP-gpi_SP: 0.000000-0.000000,   ai_SP-di: 40-58,   taoi-deltai: 40-56,   taoPi_SP-deltaPi_SP: 40-56,   betaNi: 16
342   betaNi: 16,   bi: 16
342   Vessel i: 4:   pi: 6-12,   ai-di: 47-59,   gi_SP-gpi_SP: 0.200000-1.000000,   ai_SP-di: 48-59,   taoi-deltai: 48-61,   taoPi_SP-deltaPi_SP: 48-61,   betaNi: 13
343   : 13,   bi: 13
343   Vessel i: 5:   pi: 27-34,   ai-di: 50-67,   gi_SP-gpi_SP: 1.000000-0.200000,   ai_SP-di: 58-67,   taoi-deltai: 58-77,   taoPi_SP-deltaPi_SP: 58-77,   betaNi: 19
344   betaNi: 19,   bi: 19
344
345   round LB = [666, 4067, 4291]
346   round UB = [7107, 4291, 4291]
347   round Hua = [0, 3221, 3445]
348   round SPObjVal = [3221, 3445, 3445]
349   round MPObjValNHua = [666, 846, 846]
350
351   OptimalObj = 4290.6666666666664
352   Time: 248.000000
353
354
355
356
```