


```

80 Relax-and-lift: 4
81 BQP: 4
82
83 Explored 1 nodes (19221 simplex iterations) in 23.65 seconds (45.71 work units)
84 Thread count was 8 (of 8 available processors)
85
86 Solution count 4: 1017 2257 2637 3217
87
88 Optimal solution found (tolerance 1.00e-10)
89 Best objective 1.017000000000e+03, best bound 1.017000000000e+03, gap 0.0000%
90 Set parameter MIPGap to value 1e-08
91 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
92
93 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
94 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
95
96 Optimize a model with 2481560 rows, 1955335 columns and 17235839 nonzeros
97 Model fingerprint: 0x8f6094e5
98 Variable types: 963295 continuous, 992040 integer (985965 binary)
99 Coefficient statistics:
100 Matrix range [1e-01, 1e+10]
101 Objective range [6e-05, 5e+01]
102 Bounds range [1e+00, 8e+01]
103 RHS range [8e-01, 1e+10]
104 Warning: Model contains large matrix coefficients
105 Warning: Model contains large rhs
106 Consider reformulating model or setting NumericFocus parameter
107 to avoid numerical issues.
108 Presolve removed 2478308 rows and 1954170 columns
109 Presolve time: 4.82s
110 Presolved: 3252 rows, 1165 columns, 8595 nonzeros
111 Variable types: 8 continuous, 1157 integer (659 binary)
112 Found heuristic solution: objective 4309.8302838
113
114 Root simplex log...
115
116 Iteration Objective Primal Inf. Dual Inf. Time
117 0 8.9802796e+03 8.166827e+03 0.000000e+00 6s
118 925 5.5971303e+03 0.000000e+00 0.000000e+00 6s
119
120 Root relaxation: objective 5.597130e+03, 925 iterations, 0.00 seconds (0.01 work units)
121
122 Nodes | Current Node | Objective Bounds | Work
123 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
124
125 0 0 5597.13028 0 18 4309.83028 5597.13028 29.9% - 6s
126 H 0 0 5595.3302838 5597.13028 0.03% - 6s
127 * 0 0 0 5596.8302838 5596.83028 0.00% - 6s
128
129 Cutting planes:
130 Learned: 1
131 MIR: 1
132 RLT: 1
133
134 Explored 1 nodes (1299 simplex iterations) in 6.35 seconds (7.56 work units)
135 Thread count was 8 (of 8 available processors)
136
137 Solution count 3: 5596.83 5595.33 4309.83
138
139 Optimal solution found (tolerance 1.00e-08)
140 Best objective 5.596830283766e+03, best bound 5.596830283766e+03, gap 0.0000%
141 SP is solved
142 SP's optimal solution is'□5596
143
144 Itr = 0
145 Collect_LB = [1017.0]
146 Collect_UB = [12210.660567532992]
147 Collect_Hua = [0.0]
148 Collect_SPObjVal = [5596.830283766496]
149 Collect_MPObjValNHua = [1017.0]
150
151
152 Set parameter MIPGap to value 0.05
153 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
154
155 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
156 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
157
158 Optimize a model with 1126481 rows, 303661 columns and 3329693 nonzeros
159 Model fingerprint: 0xc2a3ddbf
160 Variable types: 1 continuous, 303660 integer (292257 binary)
161 Coefficient statistics:
162 Matrix range [1e-01, 1e+10]
163 Objective range [1e+00, 2e+01]

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164 Bounds range [1e+00, 1e+00]
165 RHS range [1e+00, 2e+10]
166 Warning: Model contains large matrix coefficients
167 Warning: Model contains large rhs
168 Consider reformulating model or setting NumericFocus parameter
169 to avoid numerical issues.
170 Presolve removed 977131 rows and 283914 columns (presolve time = 5s) ...
171 Presolve removed 991673 rows and 285175 columns (presolve time = 10s) ...
172 Presolve removed 1059124 rows and 292247 columns
173 Presolve time: 10.90s
174 Presolved: 67357 rows, 11414 columns, 216560 nonzeros
175 Variable types: 1 continuous, 11413 integer (9486 binary)
176
177 Deterministic concurrent LP optimizer: primal and dual simplex (primal and dual model)
178 Showing first log only...
179
180 Root relaxation presolved: 11414 rows, 78771 columns, 227974 nonzeros
181
182
183 Root simplex log...
184
185 Iteration Objective Primal Inf. Dual Inf. Time
186 0 7.0313303e+03 0.000000e+00 3.090231e+04 12s
187 Concurrent spin time: 0.32s
188
189 Solved with dual simplex (primal model)
190
191 Root relaxation: objective 7.031330e+03, 7092 iterations, 1.23 seconds (1.43 work units)
192
193 Nodes | Current Node | Objective Bounds | Work
194 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
195
196 0 0 7031.33028 0 387 -7031.33028 - - 15s
197 0 0 7031.33028 0 387 -7031.33028 - - 15s
198 0 0 7031.33028 0 540 -7031.33028 - - 17s
199 0 0 7031.33028 0 540 -7031.33028 - - 17s
200 0 0 7031.33028 0 540 -7031.33028 - - 17s
201 0 0 7031.33028 0 555 -7031.33028 - - 18s
202 0 0 7031.33028 0 496 -7031.33028 - - 18s
203 0 0 7031.33028 0 347 -7031.33028 - - 27s
204 0 0 7031.33028 0 420 -7031.33028 - - 29s
205 0 0 7031.33028 0 424 -7031.33028 - - 29s
206 0 0 7031.33028 0 268 -7031.33028 - - 37s
207 0 0 7031.33028 0 352 -7031.33028 - - 38s
208 0 0 7031.33028 0 219 -7031.33028 - - 45s
209 0 0 7031.33028 0 216 -7031.33028 - - 45s
210 0 0 7031.33028 0 222 -7031.33028 - - 46s
211 0 0 7031.33028 0 192 -7031.33028 - - 52s
212 0 0 7031.33028 0 231 -7031.33028 - - 52s
213 0 0 7031.33028 0 342 -7031.33028 - - 53s
214 0 0 7031.33028 0 320 -7031.33028 - - 53s
215 H 0 0 7071.3302838 7031.33028 0.57% - 57s
216 0 0 7031.33028 0 329 7071.33028 7031.33028 0.57% - 57s
217
218 Cutting planes:
219 Learned: 15
220 Gomory: 4
221 Cover: 440
222 Implied bound: 219
223 Clique: 1654
224 MIR: 163
225 StrongCG: 48
226 Flow cover: 17
227 GUB cover: 311
228 Zero half: 63
229 Network: 1
230 RLT: 88
231 Relax-and-lift: 320
232 BQP: 63
233
234 Explored 1 nodes (117042 simplex iterations) in 57.15 seconds (100.30 work units)
235 Thread count was 8 (of 8 available processors)
236
237 Solution count 1: 7071.33
238
239 Optimal solution found (tolerance 5.00e-02)
240 Best objective 7.071330283766e+03, best bound 7.031330283766e+03, gap 0.5657%
241 Set parameter MIPGap to value 1e-08
242 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
243
244 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
245 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
246
247 Optimize a model with 2481560 rows, 1955335 columns and 17235839 nonzeros

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248 Model fingerprint: 0xa71d478b
249 Variable types: 963295 continuous, 992040 integer (985965 binary)
250 Coefficient statistics:
251   Matrix range   [1e-01, 1e+10]
252   Objective range [6e-05, 5e+01]
253   Bounds range   [1e+00, 8e+01]
254   RHS range      [8e-01, 1e+10]
255 Warning: Model contains large matrix coefficients
256 Warning: Model contains large rhs
257   Consider reformulating model or setting NumericFocus parameter
258   to avoid numerical issues.
259 Presolve removed 2475686 rows and 1953401 columns
260 Presolve time: 4.84s
261 Presolved: 5874 rows, 1934 columns, 15651 nonzeros
262 Variable types: 8 continuous, 1926 integer (1111 binary)
263 Found heuristic solution: objective 4273.8302838
264
265 Root simplex log...
266
267 Iteration   Objective      Primal Inf.   Dual Inf.    Time
268      0  1.1567280e+04  6.736059e+03  0.000000e+00  6s
269    1911  6.0871303e+03  0.000000e+00  0.000000e+00  6s
270
271 Root relaxation: objective 6.087130e+03, 1911 iterations, 0.03 seconds (0.02 work units)
272
273   Nodes | Current Node | Objective Bounds | Work
274 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
275
276      0  0 6087.13028  0 17 4273.83028 6087.13028 42.4% - 6s
277 H  0  0          6086.8302838 6087.13028 0.00% - 6s
278
279 Cutting planes:
280   Learned: 2
281   Cover: 10
282   Implied bound: 10
283   MIR: 2
284
285 Explored 1 nodes (2436 simplex iterations) in 6.37 seconds (7.52 work units)
286 Thread count was 8 (of 8 available processors)
287
288 Solution count 2: 6086.83 4273.83
289
290 Optimal solution found (tolerance 1.00e-08)
291 Best objective 6.086830283766e+03, best bound 6.086830283766e+03, gap 0.0000%
292 SP is solved
293 SP's optimal solution is'□6086
294
295   Itr = 1
296 Collect_LB = [1017.0, 7071.330283766496]
297 Collect_UB = [12210.660567532992, 7561.330283766496]
298 Collect_Hua = [0.0, 5596.830283766496]
299 Collect_SPObjVal = [5596.830283766496, 6086.830283766496]
300 Collect_MPObjValNHua = [1017.0, 1474.5]
301
302
303 Set parameter MIPGap to value 0.05
304 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
305
306 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
307 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
308
309 Optimize a model with 1662675 rows, 323344 columns and 5028129 nonzeros
310 Model fingerprint: 0xddc6c696
311 Variable types: 1 continuous, 323343 integer (300573 binary)
312 Coefficient statistics:
313   Matrix range   [1e-01, 1e+10]
314   Objective range [1e+00, 2e+01]
315   Bounds range   [1e+00, 1e+00]
316   RHS range      [1e+00, 2e+10]
317 Warning: Model contains large matrix coefficients
318 Warning: Model contains large rhs
319   Consider reformulating model or setting NumericFocus parameter
320   to avoid numerical issues.
321 Presolve removed 1469762 rows and 298513 columns (presolve time = 5s) ...
322 Presolve removed 1501741 rows and 300551 columns (presolve time = 10s) ...
323 Presolve removed 1564235 rows and 307490 columns
324 Presolve time: 14.40s
325 Presolved: 98440 rows, 15854 columns, 334414 nonzeros
326 Variable types: 1 continuous, 15853 integer (12018 binary)
327
328 Deterministic concurrent LP optimizer: primal and dual simplex (primal and dual model)
329 Showing first log only...
330
331 Root relaxation presolved: 15854 rows, 114276 columns, 350152 nonzeros

```

```

332
333
334 Root simplex log...
335
336 Iteration   Objective   Primal Inf.   Dual Inf.   Time
337      0    7.5213303e+03  0.000000e+00  1.605501e+05  15s
338    23521  7.5213303e+03  0.000000e+00  0.000000e+00  17s
339    23521  7.5213303e+03  0.000000e+00  0.000000e+00  17s
340    23521  7.5213303e+03  0.000000e+00  0.000000e+00  17s
341 Concurrent spin time: 1.09s
342
343 Solved with primal simplex
344
345 Root relaxation: objective 7.521330e+03, 23521 iterations, 2.97 seconds (4.07 work units)
346 Total elapsed time = 20.81s
347
348   Nodes | Current Node | Objective Bounds | Work
349 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
350
351   0   0 7521.33028  0 630      -7521.33028  - - 23s
352   0   0 7521.33028  0 641      -7521.33028  - - 23s
353   0   0 7521.33028  0 1301     -7521.33028  - - 29s
354   0   0 7521.33028  0 1159     -7521.33028  - - 29s
355   0   0 7521.33028  0 1030     -7521.33028  - - 33s
356   0   0 7521.33028  0 1023     -7521.33028  - - 33s
357   0   0 7521.33028  0 574      -7521.33028  - - 46s
358   0   0 7521.33028  0 914      -7521.33028  - - 50s
359   0   0 7521.33028  0 338      -7521.33028  - - 59s
360   0   0 7521.33028  0 640      -7521.33028  - - 60s
361   0   0 7521.33028  0 630      -7521.33028  - - 60s
362   0   0 7521.33028  0 465      -7521.33028  - - 68s
363   0   0 7521.33028  0 420      -7521.33028  - - 68s
364   0   0 7521.33028  0 440      -7521.33028  - - 69s
365   0   0 7521.33028  0 599      -7521.33028  - - 75s
366   0   0 7521.33028  0 648      -7521.33028  - - 75s
367   0   0 7521.33028  0 810      -7521.33028  - - 79s
368   0   0 7521.33028  0 567      -7521.33028  - - 85s
369   0   0 7521.33028  0 454      -7521.33028  - - 87s
370   0   2 7521.33028  0 454      -7521.33028  - - 95s
371   3   8 7521.33028  2 572      -7521.33028  - 6444 101s
372  11  16 7521.33028  3 1114     -7521.33028  - 6404 108s
373  19  24 7521.33028  5 707      -7521.33028  - 4880 119s
374  23  29 7521.33028  6 605      -7521.33028  - 5922 122s
375  28  40 7521.33028  8 600      -7521.33028  - 5882 127s
376  39  59 7521.33028 10 798      -7521.33028  - 5261 136s
377  64  97 7521.33028 17 997      -7521.33028  - 4469 155s
378 111 180 7521.33028 23 718      -7521.33028  - 4451 178s
379 257 253 7561.33028 53 769      -7521.33028  - 2820 194s
380 413 369 7561.33028 121 676     -7521.33028  - 2018 210s
381 613 491 7561.33028 205 356     -7521.33028  - 1522 222s
382 H 774 295          7561.3302838 7521.33028 0.53% 1305 234s
383
384 Cutting planes:
385   Learned: 26
386   Gomory: 5
387   Cover: 768
388   Implied bound: 725
389   Clique: 3771
390   MIR: 324
391   StrongCG: 70
392   Flow cover: 34
393   GUB cover: 471
394   Zero half: 53
395   RLT: 177
396   Relax-and-lift: 316
397   BQP: 159
398   PSD: 3
399
400 Explored 928 nodes (1350217 simplex iterations) in 234.86 seconds (775.17 work units)
401 Thread count was 8 (of 8 available processors)
402
403 Solution count 1: 7561.33
404
405 Optimal solution found (tolerance 5.00e-02)
406 Best objective 7.561330283766e+03, best bound 7.521330283766e+03, gap 0.5290%
407 Warning: linear constraint 590288 and linear constraint 1126482 have the same name "ConSP25_1[0,0]"
408 Set parameter MIPGap to value 1e-08
409 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
410
411 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
412 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
413
414 Optimize a model with 2481560 rows, 1955335 columns and 17235839 nonzeros
415 Model fingerprint: 0x5fae8a5d

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```

416 Variable types: 963295 continuous, 992040 integer (985965 binary)
417 Coefficient statistics:
418   Matrix range   [1e-01, 1e+10]
419   Objective range [6e-05, 5e+01]
420   Bounds range   [1e+00, 8e+01]
421   RHS range      [8e-01, 1e+10]
422 Warning: Model contains large matrix coefficients
423 Warning: Model contains large rhs
424   Consider reformulating model or setting NumericFocus parameter
425   to avoid numerical issues.
426 Presolve removed 2475620 rows and 1953381 columns
427 Presolve time: 4.80s
428 Presolved: 5940 rows, 1954 columns, 15773 nonzeros
429 Variable types: 8 continuous, 1946 integer (1121 binary)
430 Found heuristic solution: objective 4320.8302838
431 Found heuristic solution: objective 4340.8302838
432
433 Root simplex log...
434
435 Iteration   Objective      Primal Inf.   Dual Inf.   Time
436    0  1.2007280e+04  8.760652e+03  0.000000e+00  6s
437  2042  6.0871303e+03  0.000000e+00  0.000000e+00  6s
438
439 Root relaxation: objective 6.087130e+03, 2042 iterations, 0.03 seconds (0.03 work units)
440
441   Nodes | Current Node | Objective Bounds | Work
442 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
443
444    0  0 6087.13028  0 17 4340.83028 6087.13028 40.2% - 6s
445 H  0  0          6086.8302838 6087.13028 0.00% - 6s
446
447 Cutting planes:
448   Learned: 2
449   Cover: 10
450   Implied bound: 10
451   MIR: 2
452
453 Explored 1 nodes (2811 simplex iterations) in 6.38 seconds (7.54 work units)
454 Thread count was 8 (of 8 available processors)
455
456 Solution count 3: 6086.83 4340.83 4320.83
457
458 Optimal solution found (tolerance 1.00e-08)
459 Best objective 6.086830283766e+03, best bound 6.086830283766e+03, gap 0.0000%
460 SP is solved
461 SP's optimal solution is'□6086
462
463 Itr = 2
464 Collect_LB = [1017.0, 7071.330283766496, 7561.330283766496]
465 Collect_UB = [12210.660567532992, 7561.330283766496, 7561.330283766496]
466 Collect_Hua = [0.0, 5596.830283766496, 6086.830283766496]
467 Collect_SPObjVal = [5596.830283766496, 6086.830283766496, 6086.830283766496]
468 Collect_MPObjValNHua = [1017.0, 1474.5, 1474.5]
469
470
471 Reach the termination conditions, stop iteration
472 Values adopted from the Itr' th iteration, and Itr = {2}, judgeCount = {2}
473
474 ~~~~~judge = 2, SPObj_SPF = 6086.830283766496
475 Vessel i: 0: pi: 0-6, ai-di: 7-27, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 7-27, taoi-deltai: 7-29, taoPi_SP-deltaPi_SP: 7-29, betaNi: 22
, bi: 22
476 Vessel i: 1: pi: 14-20, ai-di: 9-18, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 9-18, taoi-deltai: 9-18, taoPi_SP-deltaPi_SP: 9-18, betaNi: 9
, bi: 9
477 Vessel i: 2: pi: 8-14, ai-di: 11-40, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 11-40, taoi-deltai: 11-42, taoPi_SP-deltaPi_SP: 11-42, betaNi
: 31, bi: 31
478 Vessel i: 3: pi: 21-27, ai-di: 17-31, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 17-31, taoi-deltai: 17-27, taoPi_SP-deltaPi_SP: 17-27,
betaNi: 10, bi: 30
479 Vessel i: 4: pi: 14-20, ai-di: 18-23, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 18-23, taoi-deltai: 19-24, taoPi_SP-deltaPi_SP: 19-24,
betaNi: 5, bi: 5
480 Vessel i: 5: pi: 27-34, ai-di: 26-30, gi_SP-gpi_SP: 0.025000-1.000000, ai_SP-di: 26-30, taoi-deltai: 27-32, taoPi_SP-deltaPi_SP: 27-32,
betaNi: 5, bi: 5
481 Vessel i: 6: pi: 18-24, ai-di: 33-42, gi_SP-gpi_SP: 0.375000-0.200000, ai_SP-di: 36-42, taoi-deltai: 36-45, taoPi_SP-deltaPi_SP: 36-45,
betaNi: 9, bi: 9
482 Vessel i: 7: pi: 14-20, ai-di: 37-68, gi_SP-gpi_SP: 1.000000-0.600000, ai_SP-di: 47-68, taoi-deltai: 47-77, taoPi_SP-deltaPi_SP: 47-77,
betaNi: 30, bi: 30
483 Vessel i: 8: pi: 28-34, ai-di: 46-64, gi_SP-gpi_SP: 1.000000-0.600000, ai_SP-di: 53-64, taoi-deltai: 53-74, taoPi_SP-deltaPi_SP: 53-74,
betaNi: 21, bi: 21
484
485 round LB = [1017, 7071, 7561]
486 round UB = [12211, 7561, 7561]
487 round Hua = [0, 5597, 6087]
488 round SPObjVal = [5597, 6087, 6087]
489 round MPObjValNHua = [1017, 1474, 1474]
490

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unknown

491 Time: 779.000000
492
493
494
495