


```

80 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
81
82 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
83 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
84
85 Optimize a model with 252585 rows, 9618 columns and 522097 nonzeros
86 Model fingerprint: 0x1148f118
87 Variable types: 24 continuous, 9594 integer (5544 binary)
88 Coefficient statistics:
89   Matrix range    [1e-01, 1e+10]
90   Objective range [6e-05, 5e+01]
91   Bounds range    [1e+00, 1e+00]
92   RHS range       [8e-01, 1e+10]
93 Warning: Model contains large matrix coefficients
94 Warning: Model contains large rhs
95   Consider reformulating model or setting NumericFocus parameter
96   to avoid numerical issues.
97 Presolve removed 250214 rows and 8762 columns
98 Presolve time: 0.23s
99 Presolved: 2371 rows, 856 columns, 6316 nonzeros
100 Variable types: 0 continuous, 856 integer (503 binary)
101 Found heuristic solution: objective 4207.6666667
102
103 Root relaxation: objective 5.149667e+03, 652 iterations, 0.00 seconds (0.01 work units)
104
105   Nodes | Current Node | Objective Bounds | Work
106 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
107
108 * 0 0 0 0 5149.6666667 5149.66667 0.00% - 0s
109
110 Explored 1 nodes (652 simplex iterations) in 0.30 seconds (0.45 work units)
111 Thread count was 8 (of 8 available processors)
112
113 Solution count 2: 5149.67 4207.67
114
115 Optimal solution found (tolerance 1.00e-08)
116 Best objective 5.149666666667e+03, best bound 5.149666666667e+03, gap 0.0000%
117 SP is solved
118 SP's optimal solution is'□5149
119
120 Itr = 0
121 Collect_LB = [804.0]
122 Collect_UB = [11103.333333333336]
123 Collect_Hua = [0.0]
124 Collect_SPObjVal = [5149.666666666668]
125 Collect_MPObjValNHua = [804.0]
126
127
128 Set parameter MIPGap to value 1e-10
129 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
130
131 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
132 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
133
134 Optimize a model with 367234 rows, 137605 columns and 1009043 nonzeros
135 Model fingerprint: 0x484429d0
136 Variable types: 1 continuous, 137604 integer (137580 binary)
137 Coefficient statistics:
138   Matrix range    [1e+00, 1e+10]
139   Objective range [1e+00, 2e+01]
140   Bounds range    [1e+00, 1e+00]
141   RHS range       [1e+00, 2e+10]
142 Warning: Model contains large matrix coefficients
143 Warning: Model contains large rhs
144   Consider reformulating model or setting NumericFocus parameter
145   to avoid numerical issues.
146 Presolve removed 229129 rows and 122378 columns (presolve time = 5s) ...
147 Presolve removed 343024 rows and 131193 columns
148 Presolve time: 6.12s
149 Presolved: 24210 rows, 6412 columns, 85890 nonzeros
150 Variable types: 0 continuous, 6412 integer (6395 binary)
151
152 Root simplex log...
153
154 Iteration Objective Primal Inf. Dual Inf. Time
155 0 6.0736667e+03 8.510000e+02 0.000000e+00 6s
156 2440 6.0736667e+03 0.000000e+00 0.000000e+00 6s
157
158 Root relaxation: objective 6.073667e+03, 2440 iterations, 0.08 seconds (0.14 work units)
159
160   Nodes | Current Node | Objective Bounds | Work
161 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
162
163 0 0 6073.66667 0 9 - 6073.66667 - - 6s

```

```

164 0 0 6073.66667 0 8 - 6073.66667 - - 6s
165 0 0 6073.66667 0 109 - 6073.66667 - - 7s
166 0 0 6073.66667 0 101 - 6073.66667 - - 7s
167 0 0 6073.66667 0 156 - 6073.66667 - - 7s
168 0 0 6073.66667 0 146 - 6073.66667 - - 7s
169 0 0 6073.66667 0 13 - 6073.66667 - - 8s
170 0 0 6073.66667 0 20 - 6073.66667 - - 8s
171 0 0 6073.66667 0 1 - 6073.66667 - - 9s
172 0 0 6073.66667 0 13 - 6073.66667 - - 9s
173 0 0 6073.66667 0 1 - 6073.66667 - - 9s
174 0 0 6073.66667 0 1 - 6073.66667 - - 9s
175 H 0 0 6073.6666667 6073.66667 0.00% - 10s
176 0 0 6073.66667 0 1 6073.66667 6073.66667 0.00% - 10s
177
178 Cutting planes:
179 Gomory: 2
180 Cover: 229
181 Implied bound: 510
182 Clique: 145
183 MIR: 24
184 StrongCG: 15
185 GUB cover: 35
186 RLT: 1
187 Relax-and-lift: 11
188
189 Explored 1 nodes (17849 simplex iterations) in 10.20 seconds (13.47 work units)
190 Thread count was 8 (of 8 available processors)
191
192 Solution count 1: 6073.67
193
194 Optimal solution found (tolerance 1.00e-10)
195 Best objective 6.073666666667e+03, best bound 6.073666666667e+03, gap 0.0000%
196 Set parameter MIPGap to value 1e-08
197 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
198
199 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
200 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
201
202 Optimize a model with 252585 rows, 9618 columns and 522097 nonzeros
203 Model fingerprint: 0xe3457418
204 Variable types: 24 continuous, 9594 integer (5544 binary)
205 Coefficient statistics:
206 Matrix range [1e-01, 1e+10]
207 Objective range [6e-05, 5e+01]
208 Bounds range [1e+00, 1e+00]
209 RHS range [8e-01, 1e+10]
210 Warning: Model contains large matrix coefficients
211 Warning: Model contains large rhs
212 Consider reformulating model or setting NumericFocus parameter
213 to avoid numerical issues.
214 Presolve removed 247302 rows and 7837 columns
215 Presolve time: 0.22s
216 Presolved: 5283 rows, 1781 columns, 14070 nonzeros
217 Variable types: 4 continuous, 1777 integer (1024 binary)
218 Found heuristic solution: objective 3689.6666667
219
220 Root relaxation: objective 5.402667e+03, 1412 iterations, 0.00 seconds (0.01 work units)
221
222 Nodes | Current Node | Objective Bounds | Work
223 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
224
225 H 0 0 5402.6666667 15700.0000 191% - 0s
226 0 0 - 0 5402.66667 5402.66667 0.00% - 0s
227
228 Explored 1 nodes (1853 simplex iterations) in 0.30 seconds (0.47 work units)
229 Thread count was 8 (of 8 available processors)
230
231 Solution count 2: 5402.67 3689.67
232
233 Optimal solution found (tolerance 1.00e-08)
234 Best objective 5.402666666667e+03, best bound 5.402666666667e+03, gap 0.0000%
235 SP is solved
236 SP's optimal solution is'□5402
237
238 Itr = 1
239 Collect_LB = [804.0, 6073.666666666668]
240 Collect_UB = [11103.333333333336, 6326.666666666668]
241 Collect_Hua = [0.0, 5149.666666666668]
242 Collect_SPObjVal = [5149.666666666668, 5402.666666666668]
243 Collect_MPObjValNHua = [804.0, 924.0]
244
245
246 Set parameter MIPGap to value 1e-10
247 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)

```

```

248
249 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
250 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
251
252 Optimize a model with 367234 rows, 137605 columns and 1009043 nonzeros
253 Model fingerprint: 0xbf277ce8
254 Variable types: 1 continuous, 137604 integer (137580 binary)
255 Coefficient statistics:
256   Matrix range    [1e+00, 1e+10]
257   Objective range [1e+00, 2e+01]
258   Bounds range   [1e+00, 1e+00]
259   RHS range      [1e+00, 2e+10]
260 Warning: Model contains large matrix coefficients
261 Warning: Model contains large rhs
262   Consider reformulating model or setting NumericFocus parameter
263   to avoid numerical issues.
264 Presolve removed 229129 rows and 122378 columns (presolve time = 5s) ...
265 Presolve removed 343024 rows and 131193 columns
266 Presolve time: 6.17s
267 Presolved: 24210 rows, 6412 columns, 85890 nonzeros
268 Variable types: 0 continuous, 6412 integer (6395 binary)
269
270 Root simplex log...
271
272 Iteration   Objective      Primal Inf.   Dual Inf.    Time
273      0    6.3266667e+03  8.510000e+02  0.000000e+00   6s
274    2440    6.3266667e+03  0.000000e+00  0.000000e+00   6s
275
276 Root relaxation: objective 6.326667e+03, 2440 iterations, 0.08 seconds (0.14 work units)
277
278   Nodes | Current Node | Objective Bounds | Work
279 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
280
281   0   0 6326.66667   0   9    -6326.66667   -   -   6s
282   0   0 6326.66667   0   8    -6326.66667   -   -   6s
283   0   0 6326.66667   0 109    -6326.66667   -   -   7s
284   0   0 6326.66667   0 101    -6326.66667   -   -   7s
285   0   0 6326.66667   0 156    -6326.66667   -   -   7s
286   0   0 6326.66667   0 146    -6326.66667   -   -   7s
287   0   0 6326.66667   0  13    -6326.66667   -   -   8s
288   0   0 6326.66667   0  20    -6326.66667   -   -   8s
289   0   0 6326.66667   0   1    -6326.66667   -   -   9s
290   0   0 6326.66667   0  13    -6326.66667   -   -   9s
291   0   0 6326.66667   0   1    -6326.66667   -   -   9s
292   0   0 6326.66667   0   1    -6326.66667   -   -  10s
293 H   0   0                6326.6666667 6326.66667 0.00%   - 10s
294   0   0 6326.66667   0   1 6326.66667 6326.66667 0.00%   - 10s
295
296 Cutting planes:
297   Gomory: 2
298   Cover: 229
299   Implied bound: 510
300   Clique: 145
301   MIR: 24
302   StrongCG: 15
303   GUB cover: 35
304   RLT: 1
305   Relax-and-lift: 11
306
307 Explored 1 nodes (17849 simplex iterations) in 10.32 seconds (13.47 work units)
308 Thread count was 8 (of 8 available processors)
309
310 Solution count 1: 6326.67
311
312 Optimal solution found (tolerance 1.00e-10)
313 Best objective 6.326666666667e+03, best bound 6.326666666667e+03, gap 0.0000%
314 Set parameter MIPGap to value 1e-08
315 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
316
317 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
318 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
319
320 Optimize a model with 252585 rows, 9618 columns and 522097 nonzeros
321 Model fingerprint: 0xe3457418
322 Variable types: 24 continuous, 9594 integer (5544 binary)
323 Coefficient statistics:
324   Matrix range    [1e-01, 1e+10]
325   Objective range [6e-05, 5e+01]
326   Bounds range   [1e+00, 1e+00]
327   RHS range      [8e-01, 1e+10]
328 Warning: Model contains large matrix coefficients
329 Warning: Model contains large rhs
330   Consider reformulating model or setting NumericFocus parameter
331   to avoid numerical issues.

```

```
332 Presolve removed 247302 rows and 7837 columns
333 Presolve time: 0.20s
334 Presolved: 5283 rows, 1781 columns, 14070 nonzeros
335 Variable types: 4 continuous, 1777 integer (1024 binary)
336 Found heuristic solution: objective 3689.6666667
337
338 Root relaxation: objective 5.402667e+03, 1412 iterations, 0.00 seconds (0.01 work units)
339
340 Nodes | Current Node | Objective Bounds | Work
341 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
342
343 H 0 0 5402.6666667 15700.0000 191% - 0s
344 0 0 - 0 5402.66667 5402.66667 0.00% - 0s
345
346 Explored 1 nodes (1853 simplex iterations) in 0.31 seconds (0.47 work units)
347 Thread count was 8 (of 8 available processors)
348
349 Solution count 2: 5402.67 3689.67
350
351 Optimal solution found (tolerance 1.00e-08)
352 Best objective 5.40266666667e+03, best bound 5.402666666667e+03, gap 0.0000%
353 SP is solved
354 SP's optimal solution is'□5402
355
356 Itr = 2
357 Collect_LB = [804.0, 6073.666666666668, 6326.666666666668]
358 Collect_UB = [11103.333333333336, 6326.666666666668, 6326.666666666668]
359 Collect_Hua = [0.0, 5149.666666666668, 5402.666666666668]
360 Collect_SPObjVal = [5149.666666666668, 5402.666666666668, 5402.666666666668]
361 Collect_MPObjValNHua = [804.0, 924.0, 924.0]
362
363
364 Reach the termination conditions, stop iteration
365 Values adopted from the Itr' th iteration, and Itr = {2}, judgeCount = {2}
366
367 ~~~~~judge = 2, SPObj_SPF = 5402.666666666668
368 Vessel i: 0: pi: 0-6, ai-di: 3-37, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 3-37, taoi-deltai: 3-35, taoPi_SP-deltaPi_SP: 3-35, betaNi: 32, bi: 32
369 Vessel i: 1: pi: 6-13, ai-di: 17-33, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 17-33, taoi-deltai: 17-31, taoPi_SP-deltaPi_SP: 17-31, betaNi: 14, bi: 14
370 Vessel i: 2: pi: 13-19, ai-di: 23-49, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 23-49, taoi-deltai: 23-47, taoPi_SP-deltaPi_SP: 23-47, betaNi: 24, bi: 24
371 Vessel i: 3: pi: 7-13, ai-di: 41-57, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 41-57, taoi-deltai: 41-55, taoPi_SP-deltaPi_SP: 41-55, betaNi: 14, bi: 14
372 Vessel i: 4: pi: 20-26, ai-di: 50-74, gi_SP-gpi_SP: 0.200000-1.000000, ai_SP-di: 51-74, taoi-deltai: 51-73, taoPi_SP-deltaPi_SP: 51-73, betaNi: 22, bi: 22
373 Vessel i: 5: pi: 12-19, ai-di: 51-75, gi_SP-gpi_SP: 1.000000-0.200000, ai_SP-di: 59-75, taoi-deltai: 59-81, taoPi_SP-deltaPi_SP: 59-81, betaNi: 22, bi: 22
374
375 round LB = [804, 6074, 6327]
376 round UB = [11103, 6327, 6327]
377 round Hua = [0, 5150, 5403]
378 round SPObjVal = [5150, 5403, 5403]
379 round MPObjValNHua = [804, 924, 924]
380
381 OptimalObj = 6326.666666666668
382 Time: 73.000000
383
384
385
386
```