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80 Optimize a model with 1153935 rows, 901813 columns and 7830116 nonzeros
81 Model fingerprint: 0x30e6b2a7
82 Variable types: 441325 continuous, 460488 integer (456438 binary)
83 Coefficient statistics:
84   Matrix range    [1e-01, 1e+10]
85   Objective range [6e-05, 5e+01]
86   Bounds range    [1e+00, 8e+01]
87   RHS range       [8e-01, 1e+10]
88 Warning: Model contains large matrix coefficients
89 Warning: Model contains large rhs
90   Consider reformulating model or setting NumericFocus parameter
91   to avoid numerical issues.
92 Presolve removed 1151486 rows and 900916 columns
93 Presolve time: 2.91s
94 Presolved: 2449 rows, 897 columns, 6631 nonzeros
95 Variable types: 0 continuous, 897 integer (507 binary)
96 Found heuristic solution: objective 3134.6666667
97 Found heuristic solution: objective 3194.6666667
98
99 Root relaxation: objective 4.522667e+03, 799 iterations, 0.01 seconds (0.01 work units)
100
101   Nodes | Current Node | Objective Bounds | Work
102 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
103
104 H  0  0          4522.6666667 9482.66667 110% - 3s
105   0  0 - 0  4522.66667 4522.66667 0.00% - 3s
106
107 Explored 1 nodes (1042 simplex iterations) in 3.78 seconds (3.47 work units)
108 Thread count was 8 (of 8 available processors)
109
110 Solution count 3: 4522.67 3194.67 3134.67
111
112 Optimal solution found (tolerance 1.00e-08)
113 Best objective 4.522666666667e+03, best bound 4.522666666667e+03, gap 0.0000%
114 SP is solved
115 SP's optimal solution is'□4522
116
117   Itr = 0
118 Collect_LB = [682.0]
119 Collect_UB = [9727.333333333332]
120 Collect_Hua = [0.0]
121 Collect_SPObjVal = [4522.666666666666]
122 Collect_MPObjValNHua = [682.0]
123
124
125 Set parameter TimeLimit to value 12000
126 Set parameter MIPGap to value 0.0005
127 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
128
129 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
130 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
131
132 Optimize a model with 365024 rows, 137605 columns and 999461 nonzeros
133 Model fingerprint: 0x57dda685
134 Variable types: 1 continuous, 137604 integer (137580 binary)
135 Coefficient statistics:
136   Matrix range    [1e+00, 1e+10]
137   Objective range [1e+00, 2e+01]
138   Bounds range    [1e+00, 1e+00]
139   RHS range       [1e+00, 2e+10]
140 Warning: Model contains large matrix coefficients
141 Warning: Model contains large rhs
142   Consider reformulating model or setting NumericFocus parameter
143   to avoid numerical issues.
144 Presolve removed 253026 rows and 123425 columns (presolve time = 5s) ...
145 Presolve removed 346407 rows and 131233 columns
146 Presolve time: 6.48s
147 Presolved: 18617 rows, 6372 columns, 76982 nonzeros
148 Variable types: 0 continuous, 6372 integer (6358 binary)
149
150 Root simplex log...
151
152 Iteration Objective Primal Inf. Dual Inf. Time
153   0  5.3396667e+03 6.250000e+02 0.000000e+00 7s
154 2302 5.3396667e+03 0.000000e+00 0.000000e+00 7s
155
156 Root relaxation: objective 5.339667e+03, 2302 iterations, 0.06 seconds (0.07 work units)
157
158   Nodes | Current Node | Objective Bounds | Work
159 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
160
161   0  0 5339.66667 0 15 - 5339.66667 - - 6s
162   0  0 5339.66667 0 133 - 5339.66667 - - 7s
163   0  0 5339.66667 0 129 - 5339.66667 - - 7s

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164 0 0 5339.66667 0 65 - 5339.66667 - - 7s
165 H 0 0 5339.6666667 5339.66667 0.00% - 8s
166 0 0 5339.66667 0 9 5339.66667 5339.66667 0.00% - 8s
167
168 Cutting planes:
169 Learned: 4
170 Gomory: 7
171 Cover: 47
172 Implied bound: 367
173 Clique: 572
174 MIR: 133
175 StrongCG: 94
176 GUB cover: 2
177 Zero half: 9
178 RLT: 8
179 Relax-and-lift: 18
180
181 Explored 1 nodes (8532 simplex iterations) in 8.88 seconds (11.02 work units)
182 Thread count was 8 (of 8 available processors)
183
184 Solution count 1: 5339.67
185
186 Optimal solution found (tolerance 5.00e-04)
187 Best objective 5.339666666667e+03, best bound 5.339666666667e+03, gap 0.0000%
188 Set parameter MIPGap to value 1e-08
189 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
190
191 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
192 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
193
194 Optimize a model with 1153935 rows, 901813 columns and 7830116 nonzeros
195 Model fingerprint: 0xe360a0c9
196 Variable types: 441325 continuous, 460488 integer (456438 binary)
197 Coefficient statistics:
198 Matrix range [1e-01, 1e+10]
199 Objective range [6e-05, 5e+01]
200 Bounds range [1e+00, 8e+01]
201 RHS range [8e-01, 1e+10]
202 Warning: Model contains large matrix coefficients
203 Warning: Model contains large rhs
204 Consider reformulating model or setting NumericFocus parameter
205 to avoid numerical issues.
206 Presolve removed 1151122 rows and 900850 columns
207 Presolve time: 2.49s
208 Presolved: 2813 rows, 963 columns, 7625 nonzeros
209 Variable types: 0 continuous, 963 integer (547 binary)
210
211 Root relaxation: objective 4.752667e+03, 918 iterations, 0.01 seconds (0.01 work units)
212
213 Nodes | Current Node | Objective Bounds | Work
214 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
215
216 0 0 4752.66667 0 4 - 4752.66667 - - 3s
217 H 0 0 4752.6666667 4752.66667 0.00% - 3s
218
219 Explored 1 nodes (1447 simplex iterations) in 3.31 seconds (3.38 work units)
220 Thread count was 8 (of 8 available processors)
221
222 Solution count 1: 4752.67
223
224 Optimal solution found (tolerance 1.00e-08)
225 Best objective 4.752666666667e+03, best bound 4.752666666667e+03, gap 0.0000%
226 SP is solved
227 SP's optimal solution is'□4752
228
229 Itr = 1
230 Collect_LB = [682.0, 5339.666666666666]
231 Collect_UB = [9727.333333333332, 5569.666666666666]
232 Collect_Hua = [0.0, 4522.666666666666]
233 Collect_SPObjVal = [4522.666666666666, 4752.666666666666]
234 Collect_MPObjValNHua = [682.0, 817.0]
235
236
237 Set parameter TimeLimit to value 12000
238 Set parameter MIPGap to value 0.0005
239 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
240
241 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
242 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
243
244 Optimize a model with 365025 rows, 137605 columns and 999474 nonzeros
245 Model fingerprint: 0xb3039aa5
246 Variable types: 1 continuous, 137604 integer (137580 binary)
247 Coefficient statistics:
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248 Matrix range [1e+00, 1e+10]
249 Objective range [1e+00, 2e+01]
250 Bounds range [1e+00, 1e+00]
251 RHS range [1e+00, 2e+10]
252 Warning: Model contains large matrix coefficients
253 Warning: Model contains large rhs
254 Consider reformulating model or setting NumericFocus parameter
255 to avoid numerical issues.
256 Presolve removed 252853 rows and 123411 columns (presolve time = 5s) ...
257 Presolve removed 346401 rows and 131231 columns
258 Presolve time: 6.23s
259 Presolved: 18624 rows, 6374 columns, 77004 nonzeros
260 Variable types: 0 continuous, 6374 integer (6359 binary)
261
262 Root simplex log...
263
264 Iteration Objective Primal Inf. Dual Inf. Time
265 0 5.5946667e+03 6.260000e+02 0.000000e+00 6s
266 2260 5.5946667e+03 0.000000e+00 0.000000e+00 7s
267
268 Root relaxation: objective 5.594667e+03, 2260 iterations, 0.06 seconds (0.06 work units)
269
270 Nodes | Current Node | Objective Bounds | Work
271 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
272
273 0 0 5594.66667 0 6 -5594.66667 - - 6s
274 H 0 0 7294.6666667 5594.66667 23.3% - 7s
275 0 0 5594.66667 0 166 7294.66667 5594.66667 23.3% - 7s
276 0 0 5594.66667 0 124 7294.66667 5594.66667 23.3% - 7s
277 H 0 0 6814.6666667 5594.66667 17.9% - 7s
278 0 0 5594.66667 0 104 6814.66667 5594.66667 17.9% - 7s
279 H 0 0 5594.6666667 5594.66667 0.00% - 8s
280 0 0 5594.66667 0 3 5594.66667 5594.66667 0.00% - 8s
281
282 Cutting planes:
283 Learned: 1
284 Gomory: 4
285 Cover: 190
286 Implied bound: 401
287 Clique: 261
288 MIR: 112
289 StrongCG: 98
290 GUB cover: 2
291 Zero half: 14
292 RLT: 3
293 Relax-and-lift: 7
294
295 Explored 1 nodes (14662 simplex iterations) in 8.99 seconds (11.06 work units)
296 Thread count was 8 (of 8 available processors)
297
298 Solution count 3: 5594.67 6814.67 7294.67
299
300 Optimal solution found (tolerance 5.00e-04)
301 Best objective 5.594666666667e+03, best bound 5.594666666667e+03, gap 0.0000%
302 Set parameter MIPGap to value 1e-08
303 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
304
305 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
306 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
307
308 Optimize a model with 1153935 rows, 901813 columns and 7830116 nonzeros
309 Model fingerprint: 0xbdf6f2f
310 Variable types: 441325 continuous, 460488 integer (456438 binary)
311 Coefficient statistics:
312 Matrix range [1e-01, 1e+10]
313 Objective range [6e-05, 5e+01]
314 Bounds range [1e+00, 8e+01]
315 RHS range [8e-01, 1e+10]
316 Warning: Model contains large matrix coefficients
317 Warning: Model contains large rhs
318 Consider reformulating model or setting NumericFocus parameter
319 to avoid numerical issues.
320 Presolve removed 1151375 rows and 900926 columns
321 Presolve time: 2.68s
322 Presolved: 2560 rows, 887 columns, 6934 nonzeros
323 Variable types: 0 continuous, 887 integer (512 binary)
324
325 Root relaxation: objective 4.582667e+03, 831 iterations, 0.01 seconds (0.01 work units)
326
327 Nodes | Current Node | Objective Bounds | Work
328 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
329
330 H 0 0 4582.6666667 9662.66667 111% - 3s
331 0 0 - 0 4582.66667 4582.66667 0.00% - 3s

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332
333 Explored 1 nodes (1127 simplex iterations) in 3.49 seconds (3.44 work units)
334 Thread count was 8 (of 8 available processors)
335
336 Solution count 1: 4582.67
337
338 Optimal solution found (tolerance 1.00e-08)
339 Best objective 4.582666666667e+03, best bound 4.582666666667e+03, gap 0.0000%
340 SP is solved
341 SP's optimal solution is'□4582
342
343 Itr = 2
344 Collect_LB = [682.0, 5339.666666666666, 5594.666666666666]
345 Collect_UB = [9727.333333333332, 5569.666666666666, 5424.666666666666]
346 Collect_Hua = [0.0, 4522.666666666666, 4752.666666666666]
347 Collect_SPObjVal = [4522.666666666666, 4752.666666666666, 4582.666666666666]
348 Collect_MPObjValNHua = [682.0, 817.0, 842.0]
349
350
351 Ops, stop iteration
352 Values adopted from the Itr-1' th iteration, and Itr = {2}, judgeCount = {1}
353
354 ~~~~~judgeCount = 1, SPObj_SPF = 4752.666666666666
355 Vessel i: 0: pi: 0-5, ai-di: 1-37, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 1-37, taoi-deltai: 1-34, taoPi_SP-deltaPi_SP: 1-34, betaNi: 33
, bi: 33
356 Vessel i: 1: pi: 5-11, ai-di: 10-30, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 10-30, taoi-deltai: 10-32, taoPi_SP-deltaPi_SP: 10-32, betaNi
: 22, bi: 22
357 Vessel i: 2: pi: 16-21, ai-di: 11-24, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 11-24, taoi-deltai: 11-27, taoPi_SP-deltaPi_SP: 11-27,
betaNi: 16, bi: 16
358 Vessel i: 3: pi: 11-16, ai-di: 13-26, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 13-26, taoi-deltai: 13-22, taoPi_SP-deltaPi_SP: 13-22,
betaNi: 9, bi: 9
359 Vessel i: 4: pi: 14-19, ai-di: 38-63, gi_SP-gpi_SP: 0.200000-1.000000, ai_SP-di: 39-63, taoi-deltai: 41-63, taoPi_SP-deltaPi_SP: 41-63,
betaNi: 22, bi: 22
360 Vessel i: 5: pi: 8-13, ai-di: 40-50, gi_SP-gpi_SP: 1.000000-0.200000, ai_SP-di: 47-50, taoi-deltai: 46-56, taoPi_SP-deltaPi_SP: 48-56, betaNi
: 10, bi: 10
361
362 round LB = [682, 5340, 5595]
363 round UB = [9727, 5570, 5425]
364 round Hua = [0, 4523, 4753]
365 round SPObjVal = [4523, 4753, 4583]
366 round MPObjValNHua = [682, 817, 842]
367
368 OptimalObj = 5594.666666666666
369 Time: 272.000000
370
371
372
373
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