```
this paper\Scripts\python.exe" "D:\Python\Pycharm\setroute\PyCharm Community Edition 2021.2.3\plugins\python-ce\helpers\pydev\pydevconsole.py" --mode=
     client --port=23018
 3
     import sys; print('Python %s on %s' % (sys.version, sys.platform))
     sys.path.extend(|'E:\\1 000\\3 0000\\1 00000\\1 000000\\1 00000\\1 LW 0000\\4 0000\\3 python code\\9 Code for this
     6
     PyDev console: starting.
     Python 3.9.7 (tags/v3.9.7:1016ef3, Aug 30 2021, 20:19:38) [MSC v.1929 64 bit (AMD64)] on win32
 8
     >>> runfile('E:/1 000/3 0000/1 00000/1 00000/1 00000/1 00000/1 LW_000/4 000/3 python_code/9 Code for this paper/main_RO_CCG.py', wdir='E:/1 0000/3 0000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 000000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 000000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00000/1 00
     this paper')
     Backend TkAgg is interactive backend. Turning interactive mode on.
     Waiting 5s.....
     Set parameter MIPGap to value 1e-10
12
     Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
13
15
     CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
     Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
16
17
     Optimize a model with 546361 rows, 52642 columns and 1529305 nonzeros
19
     Model fingerprint: 0x080f55c9
     Variable types: 1 continuous, 52641 integer (52605 binary)
20
21
     Coefficient statistics:
      Matrix range [1e+00, 1e+10]
       Objective range [1e+00, 2e+01]
23
24
       Bounds range [1e+00, 1e+00]
                            [1e+00, 2e+10]
       RHS range
26
      Warning: Model contains large matrix coefficients
27
     Warning: Model contains large rhs
28
             Consider reformulating model or setting NumericFocus parameter
29
             to avoid numerical issues.
30
     Presolve removed 323914 rows and 24616 columns (presolve time = 5s) ...
31
     Presolve removed 462566 rows and 35488 columns
     Presolve time: 8.63s
     Presolved: 83795 rows, 17154 columns, 258615 nonzeros
34
      Variable types: 0 continuous, 17154 integer (17127 binary)
35
     Deterministic concurrent LP optimizer: primal and dual simplex (primal and dual model)
     Showing first log only...
37
38
39
     Root relaxation presolved: 17154 rows, 100949 columns, 275769 nonzeros
40
41
42
     Root simplex log...
43
44
     Iteration Objective
                                      Primal Inf. Dual Inf.
           0 7.8000000e+02 0.000000e+00 1.001000e+03
45
46
     Concurrent spin time: 0.00s
48
     Solved with dual simplex (primal model)
49
50
     Root relaxation: objective 7.800000e+02, 2393 iterations, 0.35 seconds (0.38 work units)
51
52
         Nodes | Current Node | Objective Bounds
                                                                              Work
53
      Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
54
55
               0.780.00000 0.14
                                                    - 780.00000
                                                    - 780.00000 - - 10s
56
         0 0 780.00000 0 38
                                   1740.0000000 780.00000 55.2% - 10s
57
     H \quad 0 \quad 0
               0 780.00000 0 6 1740.00000 780.00000 55.2%
59
               0 780.00000 0 36 1740.00000 780.00000 55.2%
         0
                                                                                          - 12s
               0 780,00000 0 33 1740,00000 780,00000 55,2%
60
         0
               0 780.00000 0 51 1740.00000 780.00000 55.2%
          0
               0 780.00000 0 88 1740.00000 780.00000 55.2%
                                                                                          - 14s
62
              0 780.00000 0 86 1740.00000 780.00000 55.2% - 14s
63
         0
64 H 0 0
                                    780.0000000 780.00000 0.00%
                                                                                  - 14s
              0 780.00000 0 2 780.00000 780.00000 0.00% - 14s
65
66
67
     Cutting planes:
68
69
       Implied bound: 1178
70
       Clique: 21
       MIR: 117
       StrongCG: 84
73
       GUB cover: 6
74
       Zero half: 7
       Mod-K: 15
76
       RLT: 18
       Relax-and-lift: 16
77
78
       BQP: 3
79
```

```
80 Explored 1 nodes (24632 simplex iterations) in 14.91 seconds (27.90 work units)
 81 Thread count was 8 (of 8 available processors)
 83 Solution count 2: 780 1740
 85 Optimal solution found (tolerance 1.00e-10)
 86 Best objective 7.800000000000e+02, best bound 7.80000000000e+02, gap 0.0000%
 87 Set parameter MIPGap to value 1e-08
 88 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
 89
 90 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
 91
    Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
 93 Optimize a model with 2481516 rows, 1955335 columns and 17235685 nonzeros
 94 Model fingerprint: 0xb0da9aa6
 95 Variable types: 963295 continuous, 992040 integer (985965 binary)
 96 Coefficient statistics:
     Matrix range [1e-01, 1e+10]
 97
 98
     Objective range [6e-05, 5e+01]
     Bounds range [1e+00, 8e+01]
                   [8e-01, 1e+10]
100
     RHS range
    Warning: Model contains large matrix coefficients
101
    Warning: Model contains large rhs
102
103
         Consider reformulating model or setting NumericFocus parameter
104
         to avoid numerical issues.
105 Presolve removed 2478485 rows and 1954208 columns (presolve time = 5s) ...
106 Presolve removed 2478485 rows and 1954207 columns
107 Presolve time: 5.21s
108 Presolved: 3031 rows, 1128 columns, 8112 nonzeros
109 Variable types: 6 continuous, 1122 integer (664 binary)
110 Found heuristic solution: objective 3035.0500186
111 Found heuristic solution: objective 3411.0500186
112
113 Root simplex log...
114
115 Iteration Objective
                           Primal Inf. Dual Inf.
116
        0 8.9062796e+03 4.419845e+03 0.000000e+00
       900 4.8910500e+03 0.000000e+00 0.000000e+00
117
118
Root relaxation: objective 4.891050e+03, 900 iterations, 0.02 seconds (0.01 work units)
120
121
       Nodes | Current Node | Objective Bounds
                                                          Work
     Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
122
123
       0 0 4891.05002 0 24 3411.05002 4891.05002 43.4%
124
125 H 0 0
                       4825.0500186 4891.05002 1.37% - 6s
                     0 4891.0500186 4891.05002 0.00%
126 *
       0 0
127
128 Cutting planes:
129
     Learned: 1
130
     Gomory: 3
131
     Cover: 2
     Implied bound: 7
132
133
     Clique: 3
134
     MIR: 4
135
     Flow cover: 7
136
     Zero half: 1
137
     RLT: 2
138
      Relax-and-lift: 1
139
140 Explored 1 nodes (1364 simplex iterations) in 6.85 seconds (7.31 work units)
141 Thread count was 8 (of 8 available processors)
142
143 Solution count 4: 4891.05 4825.05 3411.05 3035.05
144
145 Optimal solution found (tolerance 1.00e-08)
146 Best objective 4.891050018628e+03, best bound 4.891050018628e+03, gap 0.0000%
147 SP is solved
148 SP's optimal solution is' □4891
149
150 Itr = 0
151 Collect_LB = [780.0]
152 Collect_UB = [10562.10003725563]
153 Collect Hua = [0.0]
154 Collect SPObjVal = [4891.050018627815]
155 Collect MPObjValNHua = [780.0]
156
157
158 Set parameter MIPGap to value 0.05
159 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
160
161 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
162 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
163
```

```
164 Optimize a model with 1090262 rows, 303661 columns and 3235440 nonzeros
165 Model fingerprint: 0xbe15e602
166 Variable types: 1 continuous, 303660 integer (292257 binary)
167 Coefficient statistics:
     Matrix range [1e-01, 1e+10]
169
      Objective range [1e+00, 2e+01]
     Bounds range [1e+00, 1e+00]
170
171
     RHS range
                   [1e+00, 2e+10]
172
    Warning: Model contains large matrix coefficients
    Warning: Model contains large rhs
173
          Consider reformulating model or setting NumericFocus parameter
174
175
         to avoid numerical issues.
176 Presolve removed 882742 rows and 279312 columns (presolve time = 5s) ...
    Presolve removed 910058 rows and 281966 columns (presolve time = 10s) ...
177
178 Presolve removed 989696 rows and 289734 columns
179 Presolve time: 13.95s
180
    Presolved: 100566 rows, 13927 columns, 312209 nonzeros
181
    Variable types: 1 continuous, 13926 integer (11631 binary)
182
183 Deterministic concurrent LP optimizer: primal and dual simplex (primal and dual model)
184
    Showing first log only...
185
186 Root relaxation presolved: 13927 rows, 114493 columns, 326136 nonzeros
187
188
189 Root simplex log...
190
191 Iteration Objective
                          Primal Inf. Dual Inf.
                                                 Time
        0 5.6710500e+03 0.000000e+00 1.498109e+04
192
                                                         15s
193
       4120 5.6734311e+03 0.000000e+00 1.168913e+06 15s
194 Concurrent spin time: 0.47s
195
196 Solved with dual simplex (primal model)
197
198 Root relaxation: objective 5.671050e+03, 6500 iterations, 1.48 seconds (1.78 work units)
199
200
       Nodes | Current Node | Objective Bounds
                                                        Work
201
     Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
202
                                    - 5671.05002
203
           0 5671.05002 0 328
204
           0 5671.05002
                         0 803
                                    - 5671.05002
205
       0
           0 5671.05002 0 738
                                    - 5671.05002
                                                       - 22s
                                                      - 22s
206
           0.5671.05002
                         0.735
                                    - 5671.05002
       0
207
       0
           0 5671.05002 0 988
                                    - 5671.05002
                                                       - 25s
       0
           0 5671.05002
                         0 975
                                    - 5671.05002
208
           0 5671.05002 0 298
                                    - 5671.05002
                                                       - 32s
209
       0
                                    - 5671.05002
           0 5671.05002
210
       0
                         0 291
                                                       - 32s
211
       0
           0 5671.05002
                         0 366
                                    - 5671.05002
                                                       - 33s
212
           0 5671.05002
                         0 289
                                    - 5671.05002
                                                       - 41s
       0
           0 5671.05002
                                    - 5671.05002
                         0 271
213
       0
                                                       - 41s
214
       0
           0 5671.05002 0 308
                                    - 5671.05002
                                                       - 41s
215
           0 5671.05002
                                    - 5671.05002
                         0 180
           0 5671.05002 0 185
                                    - 5671.05002
                                                       - 46s
216
       0
                                                       - 49s
                                    - 5671.05002
           0.5671.05002 0.154
217
       0
218
       0
           0 5671.05002
                         0 228
                                    - 5671.05002
                                                       - 49s
219
       0
           0 5671.05002 0 180
                                    - 5671.05002
                                                       - 54s
                                                       - 55s
220
       0
           0 5671.05002 0 176
                                    - 5671.05002
                        5671.0500186 5671.05002 0.00%
221 H 0 0
222
          223
224 Cutting planes:
225
      Gomory: 5
226
     Lift-and-project: 1
227
      Cover: 399
228
     Implied bound: 359
229
      Clique: 5276
230
      MIR: 267
      StrongCG: 127
231
232
      Flow cover: 5
233
      GUB cover: 34
234
      Zero half: 17
235
      RLT: 74
236
      Relax-and-lift: 340
237
      BQP: 39
238
239 Explored 1 nodes (131018 simplex iterations) in 63.41 seconds (168.50 work units)
240 Thread count was 8 (of 8 available processors)
241
242 Solution count 1: 5671.05
243
244 Optimal solution found (tolerance 5.00e-02)
245 Best objective 5.671050018628e+03, best bound 5.671050018628e+03, gap 0.0000%
246 Set parameter MIPGap to value 1e-08
247 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
```

```
248
249 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
250 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
251
252 Optimize a model with 2481516 rows, 1955335 columns and 17235685 nonzeros
253 Model fingerprint: 0x45240a06
254 Variable types: 963295 continuous, 992040 integer (985965 binary)
255 Coefficient statistics:
256 Matrix range [1e-01, 1e+10]
     Objective range [6e-05, 5e+01]
257
258
     Bounds range [1e+00, 8e+01]
259
      RHS range
                    [8e-01, 1e+10]
260 Warning: Model contains large matrix coefficients
261 Warning: Model contains large rhs
262
          Consider reformulating model or setting NumericFocus parameter
          to avoid numerical issues.
263
264 Presolve removed 2476261 rows and 1953584 columns
265 Presolve time: 4.73s
266 Presolved: 5255 rows, 1751 columns, 13911 nonzeros
267
    Variable types: 8 continuous, 1743 integer (1002 binary)
268 Found heuristic solution: objective 3514.0500186
269
270 Root simplex log...
271
272 Iteration Objective
                           Primal Inf. Dual Inf.
                                                  Time
        0 1.1657452e+04 5.988458e+03 0.000000e+00
273
274
       1579 5.3506703e+03 0.000000e+00 0.000000e+00
275
276 Root relaxation: objective 5.350670e+03, 1579 iterations, 0.01 seconds (0.02 work units)
277
278
       Nodes | Current Node | Objective Bounds
                                                          Work
279
     Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
280
        0 0 5350.67026 0 18 3514.05002 5350.67026 52.3%
281
282 H 0 0
                         5325.6702574 5350.67026 0.47% - 6s
                         5345.6702574 5350.67026 0.09%
283 H 0 0
284 *
       0 0
                     0 5350.6702574 5350.67026 0.00%
285
286 Cutting planes:
287
      Learned: 2
288
      Gomory: 1
289
      Implied bound: 7
290
      MIR: 6
291
      Flow cover: 4
292
      Zero half: 1
293
      RLT: 1
294
      Relax-and-lift: 2
295
296
297 Explored 1 nodes (2407 simplex iterations) in 6.35 seconds (6.91 work units)
298 Thread count was 8 (of 8 available processors)
299
300 Solution count 4: 5350.67 5345.67 5325.67 3514.05
301
302 Optimal solution found (tolerance 1.00e-08)
303 Best objective 5.350670257367e+03, best bound 5.350670257367e+03, gap 0.0000%
304 SP is solved
305 SP's optimal solution is' ☐ 5350
306
307
308 Collect LB = [780.0, 5671.050018627815]
309 Collect UB = [10562.10003725563, 6130.670257367259]
310 Collect Hua = [0.0, 4891.050018627815]
311 Collect_SPObjVal = [4891.050018627815, 5350.670257367259]
312 Collect_MPObjValNHua = [780.0, 780.0]
313
314
315 Set parameter MIPGap to value 0.05
316 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
318 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
319 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
320
321 Optimize a model with 1626434 rows, 323344 columns and 4933810 nonzeros
322 Model fingerprint: 0xd9d0d6a5
323 Variable types: 1 continuous, 323343 integer (300573 binary)
324 Coefficient statistics:
325
     Matrix range [1e-01, 1e+10]
326
     Objective range [1e+00, 2e+01]
327
      Bounds range [1e+00, 1e+00]
328
     RHS range
                   [1e+00, 2e+10]
329 Warning: Model contains large matrix coefficients
330 Warning: Model contains large rhs
          Consider reformulating model or setting NumericFocus parameter
331
```

```
332
         to avoid numerical issues.
333 Presolve removed 1361413 rows and 293461 columns (presolve time = 5s) ...
334 Presolve removed 1403783 rows and 296603 columns (presolve time = 10s) ...
335 Presolve removed 1403783 rows and 296603 columns (presolve time = 15s) ...
336 Presolve removed 1481581 rows and 304349 columns
337 Presolve time: 19.36s
338 Presolved: 144853 rows, 18995 columns, 478549 nonzeros
339 Variable types: 1 continuous, 18994 integer (14511 binary)
340
341 Deterministic concurrent LP optimizer: primal and dual simplex (primal and dual model)
342 Showing first log only...
343
344 Root relaxation presolved: 18995 rows, 163848 columns, 497544 nonzeros
345
346
347 Root simplex log...
348
                          Primal Inf. Dual Inf.
349 Iteration Objective
                                                 Time
350
        0 6.1306703e+03 0.000000e+00 2.636725e+04
351
      20012 6.1306703e+03 0.000000e+00 0.000000e+00
                                                          23s
      20012 6.1306703e+03 0.000000e+00 0.000000e+00 23s
352
353 Concurrent spin time: 1.14s
354
355
    Solved with primal simplex
356
Root relaxation: objective 6.130670e+03, 20012 iterations, 3.72 seconds (5.34 work units)
358
    Total elapsed time = 27.10s
359
360
       Nodes | Current Node | Objective Bounds

↓ Work

361
     Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
362
           0.6130.67026 0.600
                                    - 6130.67026
                                                  - - 30s
363
364
       0
           0.6130.67026 \quad 0.837
                                    - 6130.67026
                                                     - 34s
365
       0
           0 6130.67026
                                    - 6130.67026
                                                      - 34s
                         0 813
366
       0
           0 6130.67026 0 850
                                    - 6130.67026
                                                      - 37s
367
           0.6130.67026 0.440
                                    - 6130.67026
                                                      - 47s
       0
368
       0
           0 6130.67026
                         0 447
                                    - 6130.67026
                                                      - 47s
369
           0 6130.67026 0 490
                                    - 6130.67026
                                                      - 48s
370
       0
           0.6130.67026 0.366
                                    - 6130.67026
                                                      - 59s
371
       0
           0 6130.67026 0 419
                                    - 6130.67026
                                                      - 61s
           0 6130.67026
                                    - 6130.67026
372
                         0 410
373
       0
           0 6130.67026 0 290
                                    - 6130.67026
                                                      - 66s
                                                      - 66s
374
           0.6130.67026 0.289
                                    - 6130.67026
       0
375
       0
           0 6130.67026 0 446
                                    - 6130.67026
                                                      - 68s
       0
           0 6130.67026
376
                         0 451
                                    - 6130.67026
                                                         68s
           0 6130.67026 0 320
                                                      - 74s
377
       0
                                    - 6130.67026
                                    - 6130.67026
           0 6130.67026
378
       0
                         0 288
                                                      - 74s
379
       0
           0 6130.67026
                         0 508
                                    - 6130.67026
                                                         77s
380
           0 6130.67026 0 470
                                    - 6130.67026
                                                      - 77s
       0
381
           0 6130.67026 0 277
                                    - 6130.67026
       0
                                                      - 83s
382
       0
           0 6130.67026
                         0 276
                                    - 6130.67026
                                                      - 83s
           0 6130.67026
                                    - 6130.67026
383
                         0 683
384
           0 6130.67026 0 99
                                   - 6130.67026
                                                      - 90s
       0
                                                      - 91s
385
           0 6130.67026 0 192
       0
                                    - 6130.67026
386
       0
           0 6130.67026 0 123
                                    - 6130.67026
                                                      - 91s
387
       0
           0 6130.67026 0 167
                                    - 6130.67026
                                                      - 95s
                                                  - - 95s
388
       0
           0.6130.67026 0.161
                                    - 6130.67026
389
           0.6130.67026 \quad 0.113
                                    - 6130.67026
                                                  - - 98s
390
       0
           2 6130.67026 0 65
                                    - 6130.67026
                                                  - - 106s
391
           12 6130.67026 3 230
                                    - 6130.67026
                                                  - 2587 111s
       7
392
                                     - 6130.67026
       19
           20 6130.67026 5 84
                                                   - 1874 117s
393
       33
           27 6130.67026 10 56
                                     - 6130.67026
                                                   - 1701 121s
394
       42
           32 6130.67026 13 36
                                     - 6130.67026
                                                   - 1803 125s
395
           40 6130.67026 21 77
                                     - 6130.67026
                                                   - 1471 131s
      66
396
      86
           45 6130.67026 26 227
                                      - 6130.67026
                                                    - 1192 135s
397
      132
          61 infeasible 35
                                   - 6130.67026 - 953 140s
398
      201 103 infeasible 52
                                   - 6130.67026
                                                  - 771 147s
    * 217 103
399
                      61 6130.6702574 6130.67026 0.00% 717 147s
400
401
    Cutting planes:
402
     Learned: 14
403
     Gomory: 5
404
      Cover: 530
405
     Implied bound: 914
406
      Clique: 8878
407
      MIR: 533
408
      StrongCG: 44
409
      Flow cover: 19
410
      GUB cover: 481
411
      Zero half: 27
412
      Network: 3
413
     RLT: 144
     Relax-and-lift: 925
414
      BQP: 90
415
```

```
416
      PSD: 1
417
418 Explored 275 nodes (383790 simplex iterations) in 147.79 seconds (414.25 work units)
419
    Thread count was 8 (of 8 available processors)
420
421 Solution count 1: 6130.67
422
423 Optimal solution found (tolerance 5.00e-02)
424 Best objective 6.130670257367e+03, best bound 6.130670257367e+03, gap 0.0000%
425 Warning: linear constraint 554091 and linear constraint 1090263 have the same name "ConSP25_1[0,0]"
426 Set parameter MIPGap to value 1e-08
427 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
428
429 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
430 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
431
432 Optimize a model with 2481516 rows, 1955335 columns and 17235685 nonzeros
433 Model fingerprint: 0x0c9b99c3
434 Variable types: 963295 continuous, 992040 integer (985965 binary)
435 Coefficient statistics:
436
      Matrix range [1e-01, 1e+10]
437
      Objective range [6e-05, 5e+01]
      Bounds range [1e+00, 8e+01]
438
439
      RHS range
                     [8e-01, 1e+10]
     Warning: Model contains large matrix coefficients
440
441
     Warning: Model contains large rhs
442
          Consider reformulating model or setting NumericFocus parameter
          to avoid numerical issues.
443
444 Presolve removed 2475218 rows and 1953375 columns
445 Presolve time: 4.85s
446 Presolved: 6298 rows, 1960 columns, 16685 nonzeros
447 Variable types: 8 continuous, 1952 integer (1110 binary)
448
449 Root simplex log...
450
451 Iteration Objective
                            Primal Inf. Dual Inf.
                                                    Time
452
         0 1.2273581e+04 9.557802e+03 0.000000e+00
       1690 5.3894515e+03 0.000000e+00 0.000000e+00
453
454
455 Root relaxation: objective 5.389451e+03, 1690 iterations, 0.02 seconds (0.02 work units)
456
457
       Nodes | Current Node | Objective Bounds
                                                            Work
     Expl\ Unexpl\ |\ \ Obj\ \ Depth\ IntInf\ |\ Incumbent \qquad BestBd \quad Gap\ |\ It/Node\ Time
458
459
                      0 5389.4514539 5389.45145 0.00% - 6s
460
461
462 Explored 1 nodes (2418 simplex iterations) in 6.39 seconds (7.14 work units)
463
    Thread count was 8 (of 8 available processors)
464
465 Solution count 1: 5389.45
466
467 Optimal solution found (tolerance 1.00e-08)
468 Best objective 5.389451453897e+03, best bound 5.389451453897e+03, gap 0.0000%
469 SP is solved
470 SP's optimal solution is' ☐ 5389
471
472
473 Collect_LB = [780.0, 5671.050018627815, 6130.670257367259]
474 Collect_UB = [10562.10003725563, 6130.670257367259, 6130.670257367259]
475 Collect Hua = [0.0, 4891.050018627815, 5350.670257367259]
476 Collect SPObjVal = [4891.050018627815, 5350.670257367259, 5389.451453896585]
477
     Collect MPObjValNHua = [780.0, 780.0, 780.0]
478
479
480
      Reach the termination conditions, stop iteration
481
     Values adopted from the Itr' th iteration, and Itr = \{2\}, judgeCount = \{2\}
482
                 -judge = 2, SPObj SPF = 5389.451453896585
483
484 Vessel i: 0:
                  pi: 14-19,
                               ai-di: 13-26,
                                             gi_SP-gpi_SP: 0.000000-0.000000,
                                                                                   ai SP-di: 13-26,
                                                                                                      taoi-deltai: 13-22,
                                                                                                                          taoPi SP-deltaPi SP: 13-22,
     betaNi: 9,
                 bi: 9
485
                              ai-di: 7-21, gi_SP-gpi_SP: 0.000000-0.000000,
                                                                                 ai_SP-di: 7-21, taoi-deltai: 7-17, taoPi_SP-deltaPi_SP: 7-17, betaNi: 10
     Vessel i: 1:
                  pi: 8-14,
         bi: 10
                   pi: 9-14,
     Vessel i: 2:
                              ai-di: 19-34,
                                             gi_SP-gpi_SP: 0.000000-0.000000,
                                                                                  ai_SP-di: 19-34,
                                                                                                    taoi-deltai: 19-30,
                                                                                                                         taoPi_SP-deltaPi_SP: 19-30,
                                                                                                                                                       betaNi
     : 11, bi: 11
    Vessel i: 3:
                   pi: 7-13,
                                             gi_SP-gpi_SP: 0.000000-0.000000,
                                                                                  ai_SP-di: 31-42,
                                                                                                                         taoPi_SP-deltaPi_SP: 31-38,
                              ai-di: 31-42.
                                                                                                    taoi-deltai: 31-38.
                                                                                                                                                       betaNi
          bi: 7
      7,
     Vessel i: 4:
                   pi: 7-14,
                              ai-di: 39-78,
                                             gi_SP-gpi_SP: 0.000000-0.000000,
                                                                                  ai_SP-di: 39-78,
                                                                                                     taoi-deltai: 39-73,
                                                                                                                         taoPi_SP-deltaPi_SP: 39-73,
           bi: 34
     : 34.
                                              gi_SP-gpi_SP: 0.000000-0.600000,
                                                                                                                          taoPi_SP-deltaPi_SP: 14-24,
     Vessel i: 5:
                   pi: 28-34,
                               ai-di: 14-42,
                                                                                   ai_SP-di: 14-42,
                                                                                                      taoi-deltai: 14-24,
     betaNi: 10,
                   bi: 10
     Vessel i: 6:
                   pi: 14-21,
                               ai-di: 17-74,
                                              gi SP-gpi SP: 1.000000-0.000000,
                                                                                   ai SP-di: 25-74,
                                                                                                      taoi-deltai: 25-55,
                                                                                                                          taoPi SP-deltaPi SP: 25-55,
                   bi: 30
     betaNi: 30.
     Vessel i: 7:
                   pi: 22-27,
                               ai-di: 35-62,
                                              gi_SP-gpi_SP: 0.800000-0.800000,
                                                                                   ai_SP-di: 43-62,
                                                                                                      taoi-deltai: 39-46,
                                                                                                                          taoPi_SP-deltaPi_SP: 43-46,
     betaNi: 7,
```

```
unknown
492 Vessel i: 8: pi: 16-21, ai-di: 51-79, gi_SP-gpi_SP: 0.600000-1.000000, ai_SP-di: 55-79, taoi-deltai: 58-65, taoPi_SP-deltaPi_SP: 58-65,
       betaNi: 7, bi: 7
 493
494 round LB = [780, 5671, 6131]

495 round UB = [10562, 6131, 6131]

496 round Hua = [0, 4891, 5351]

497 round SPObjyal = [4891, 5351, 5389]
 498 round MPObjValNHua = [780, 780, 780]
 499
 500 Time: 693.000000
501
502
 503
 504
```