


```

80 Warning: Model contains large matrix coefficients
81 Warning: Model contains large rhs
82   Consider reformulating model or setting NumericFocus parameter
83   to avoid numerical issues.
84 Presolve removed 3642254 rows and 2879733 columns (presolve time = 5s) ...
85 Presolve removed 3644301 rows and 2880702 columns
86 Presolve time: 8.06s
87 Presolved: 1173 rows, 421 columns, 3135 nonzeros
88 Variable types: 0 continuous, 421 integer (258 binary)
89 Found heuristic solution: objective 4065.0394527
90 Found heuristic solution: objective 4110.0394527
91
92 Root simplex log...
93
94 Iteration   Objective      Primal Inf.   Dual Inf.    Time
95      0  5.6910395e+03  4.299375e+02  0.000000e+00  10s
96    395  4.5860395e+03  0.000000e+00  0.000000e+00  10s
97
98 Root relaxation: objective 4.586039e+03, 395 iterations, 0.02 seconds (0.00 work units)
99
100  Nodes | Current Node | Objective Bounds | Work
101  Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
102
103 H  0  0           4586.0394527 6851.03945 49.4% - 10s
104   0  0   -  0    4586.03945 4586.03945 0.00% - 10s
105
106 Explored 1 nodes (596 simplex iterations) in 10.62 seconds (11.03 work units)
107 Thread count was 8 (of 8 available processors)
108
109 Solution count 3: 4586.04 4110.04 4065.04
110
111 Optimal solution found (tolerance 1.00e-08)
112 Best objective 4.586039452672e+03, best bound 4.586039452672e+03, gap 0.0000%
113 SP is solved
114 SP's optimal solution is'□4586
115
116 Itr = 0
117 Collect_LB = [553.0]
118 Collect_UB = [9725.078905344453]
119 Collect_Hua = [0.0]
120 Collect_SPObjVal = [4586.039452672227]
121 Collect_MPObjValNHua = [553.0]
122
123
124 Set parameter TimeLimit to value 7200
125 Set parameter MIPGap to value 0.05
126 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
127
128 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
129 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
130
131 Optimize a model with 653155 rows, 410400 columns and 1827334 nonzeros
132 Model fingerprint: 0x0a247f4a
133 Variable types: 1 continuous, 410399 integer (410355 binary)
134 Coefficient statistics:
135   Matrix range    [1e+00, 1e+10]
136   Objective range [1e+00, 2e+01]
137   Bounds range    [1e+00, 1e+00]
138   RHS range       [1e+00, 2e+10]
139 Warning: Model contains large matrix coefficients
140 Warning: Model contains large rhs
141   Consider reformulating model or setting NumericFocus parameter
142   to avoid numerical issues.
143 Presolve removed 503592 rows and 390398 columns (presolve time = 5s) ...
144 Presolve removed 503592 rows and 390398 columns (presolve time = 10s) ...
145 Presolve removed 594472 rows and 400285 columns
146 Presolve time: 10.97s
147 Presolved: 58683 rows, 10115 columns, 150647 nonzeros
148 Variable types: 0 continuous, 10115 integer (10082 binary)
149
150 Deterministic concurrent LP optimizer: primal and dual simplex (primal and dual model)
151 Showing first log only...
152
153 Root relaxation presolved: 10115 rows, 68798 columns, 160762 nonzeros
154
155
156 Root simplex log...
157
158 Iteration   Objective      Primal Inf.   Dual Inf.    Time
159      0  5.1461823e+03  0.000000e+00  3.886000e+03  11s
160 Concurrent spin time: 0.06s
161
162 Solved with dual simplex (primal model)
163

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164 Root relaxation: objective 5.146182e+03, 3316 iterations, 0.33 seconds (0.30 work units)
165
166   Nodes | Current Node | Objective Bounds | Work
167 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
168
169   0   0 5146.18231   0 21      -5146.18231   -   - 11s
170   0   0 5146.18231   0 113     -5146.18231   -   - 13s
171   0   0 5146.18231   0 83      -5146.18231   -   - 13s
172   0   0 5146.18231   0 57      -5146.18231   -   - 14s
173   0   0 5146.18231   0 86      -5146.18231   -   - 15s
174   0   0 5146.18231   0 86      -5146.18231   -   - 15s
175   0   0 5146.18231   0 88      -5146.18231   -   - 16s
176   0   0 5146.18231   0 76      -5146.18231   -   - 16s
177   0   0 5146.18231   0 107     -5146.18231   -   - 16s
178   0   0 5146.18231   0 81      -5146.18231   -   - 17s
179   0   0 5146.18231   0 180     -5146.18231   -   - 17s
180   0   0 5146.18231   0 179     -5146.18231   -   - 17s
181   0   0 5146.18231   0 82      -5146.18231   -   - 18s
182   0   0 5146.18231   0 82      -5146.18231   -   - 19s
183 H 0 0          5146.1823098 5146.18231 0.00%   - 22s
184   0   0 5146.18231   0 82 5146.18231 5146.18231 0.00%   - 22s
185
186 Cutting planes:
187   Learned: 1
188   Gomory: 3
189   Cover: 111
190   Implied bound: 21
191   Clique: 292
192   MIR: 76
193   StrongCG: 64
194   GUB cover: 5
195   Zero half: 4
196   RLT: 5
197   Relax-and-lift: 11
198   BQP: 29
199   PSD: 2
200
201 Explored 1 nodes (38559 simplex iterations) in 22.24 seconds (30.08 work units)
202 Thread count was 8 (of 8 available processors)
203
204 Solution count 1: 5146.18
205
206 Optimal solution found (tolerance 5.00e-02)
207 Best objective 5.146182309815e+03, best bound 5.146182309815e+03, gap 0.00000%
208 Set parameter MIPGap to value 1e-08
209 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
210
211 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
212 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
213
214 Optimize a model with 3645474 rows, 2881123 columns and 25541618 nonzeros
215 Model fingerprint: 0xf07e9e51
216 Variable types: 1422995 continuous, 1458128 integer (1450703 binary)
217 Coefficient statistics:
218   Matrix range    [1e-01, 1e+10]
219   Objective range [6e-05, 5e+01]
220   Bounds range    [1e+00, 8e+01]
221   RHS range       [8e-01, 1e+10]
222 Warning: Model contains large matrix coefficients
223 Warning: Model contains large rhs
224   Consider reformulating model or setting NumericFocus parameter
225   to avoid numerical issues.
226 Presolve removed 3641418 rows and 2879511 columns (presolve time = 6s) ...
227 Presolve removed 3642213 rows and 2879962 columns
228 Presolve time: 8.39s
229 Presolved: 3261 rows, 1161 columns, 8732 nonzeros
230 Variable types: 10 continuous, 1151 integer (683 binary)
231 Found heuristic solution: objective 3620.2813655
232
233 Root simplex log...
234
235 Iteration Objective Primal Inf. Dual Inf. Time
236   0 8.4090000e+03 3.016512e+03 0.000000e+00 10s
237 969 4.9582444e+03 0.000000e+00 0.000000e+00 11s
238
239 Root relaxation: objective 4.958244e+03, 969 iterations, 0.01 seconds (0.01 work units)
240
241   Nodes | Current Node | Objective Bounds | Work
242 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
243
244   0   0 4958.24444   0 61 3620.28137 4958.24444 37.0%   - 10s
245 H 0 0          4000.4444444 4958.24444 23.9%   - 10s
246 H 0 0          4852.4444444 4958.24444 2.18%   - 10s
247   0   0 4957.44444   0 47 4852.44444 4957.44444 2.16%   - 10s

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unknown

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248 H 0 0 4952.7202709 4957.44444 0.10% - 10s
249 H 0 0 4954.1111111 4957.44444 0.07% - 10s
250 0 0 4957.23839 0 56 4954.11111 4957.23839 0.06% - 10s
251 0 0 4956.35478 0 9 4954.11111 4956.35478 0.05% - 10s
252 0 0 4956.35478 0 6 4954.11111 4956.35478 0.05% - 10s
253 H 0 0 4956.1241966 4956.35478 0.00% - 10s
254 H 0 0 4956.2202709 4956.35478 0.00% - 10s
255
256 Cutting planes:
257 MIR: 1
258
259 Explored 1 nodes (2046 simplex iterations) in 11.19 seconds (10.51 work units)
260 Thread count was 8 (of 8 available processors)
261
262 Solution count 6: 4956.22 4954.11 4952.72 ... 3620.28
263
264 Optimal solution found (tolerance 1.00e-08)
265 Best objective 4.956220270938e+03, best bound 4.956220270938e+03, gap 0.0000%
266 SP is solved
267 SP's optimal solution is'□4956
268
269 Itr = 1
270 Collect_LB = [553.0, 5146.1823098150835]
271 Collect_UB = [9725.078905344453, 5516.3631280805985]
272 Collect_Hua = [0.0, 4586.039452672227]
273 Collect_SPObjVal = [4586.039452672227, 4956.220270937742]
274 Collect_MPObjValNHua = [553.0, 560.1428571428569]
275
276
277 Set parameter TimeLimit to value 7200
278 Set parameter MIPGap to value 0.05
279 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
280
281 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
282 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
283
284 Optimize a model with 653156 rows, 410400 columns and 1827357 nonzeros
285 Model fingerprint: 0xa86c8ccc
286 Variable types: 1 continuous, 410399 integer (410355 binary)
287 Coefficient statistics:
288 Matrix range [1e+00, 1e+10]
289 Objective range [1e+00, 2e+01]
290 Bounds range [1e+00, 1e+00]
291 RHS range [1e+00, 2e+10]
292 Warning: Model contains large matrix coefficients
293 Warning: Model contains large rhs
294 Consider reformulating model or setting NumericFocus parameter
295 to avoid numerical issues.
296 Presolve removed 503364 rows and 390303 columns (presolve time = 5s) ...
297 Presolve removed 503364 rows and 390303 columns (presolve time = 10s) ...
298 Presolve removed 594492 rows and 400287 columns
299 Presolve time: 11.78s
300 Presolved: 58664 rows, 10113 columns, 150605 nonzeros
301 Variable types: 0 continuous, 10113 integer (10080 binary)
302
303 Deterministic concurrent LP optimizer: primal and dual simplex (primal and dual model)
304 Showing first log only...
305
306 Root relaxation presolved: 10113 rows, 68777 columns, 160718 nonzeros
307
308
309 Root simplex log...
310
311 Iteration Objective Primal Inf. Dual Inf. Time
312 0 5.5117203e+03 0.000000e+00 3.883000e+03 12s
313 Concurrent spin time: 0.01s
314
315 Solved with dual simplex (primal model)
316
317 Root relaxation: objective 5.511720e+03, 3485 iterations, 0.38 seconds (0.39 work units)
318
319 Nodes | Current Node | Objective Bounds | Work
320 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
321
322 0 0 5511.72027 0 31 - 5511.72027 - - 12s
323 0 0 5511.72027 0 130 - 5511.72027 - - 13s
324 0 0 5511.72027 0 155 - 5511.72027 - - 14s
325 0 0 5511.72027 0 148 - 5511.72027 - - 14s
326 0 0 5511.72027 0 67 - 5511.72027 - - 17s
327 0 0 5511.72027 0 34 - 5511.72027 - - 21s
328 0 0 5511.72027 0 235 - 5511.72027 - - 21s
329 0 0 5511.72027 0 232 - 5511.72027 - - 21s
330 0 0 5511.72027 0 54 - 5511.72027 - - 23s
331 0 0 5511.72027 0 83 - 5511.72027 - - 23s
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332 H 0 0 5771.7202709 5511.72027 4.50% - 24s
333 0 0 5511.72027 0 56 5771.72027 5511.72027 4.50% - 24s
334
335 Cutting planes:
336 Learned: 3
337 Gomory: 4
338 Cover: 113
339 Implied bound: 33
340 Clique: 609
341 MIR: 202
342 StrongCG: 147
343 GUB cover: 17
344 Zero half: 18
345 RLT: 10
346 Relax-and-lift: 29
347 BQP: 15
348 PSD: 3
349
350 Explored 1 nodes (50277 simplex iterations) in 24.79 seconds (29.30 work units)
351 Thread count was 8 (of 8 available processors)
352
353 Solution count 1: 5771.72
354
355 Optimal solution found (tolerance 5.00e-02)
356 Best objective 5.771720270938e+03, best bound 5.511720270938e+03, gap 4.5047%
357 Set parameter MIPGap to value 1e-08
358 Gurobi Optimizer version 10.0.2 build v10.0.2rc0 (win64)
359
360 CPU model: 11th Gen Intel(R) Core(TM) i7-11370H @ 3.30GHz, instruction set [SSE2|AVX|AVX2|AVX512]
361 Thread count: 4 physical cores, 8 logical processors, using up to 8 threads
362
363 Optimize a model with 3645474 rows, 2881123 columns and 25541618 nonzeros
364 Model fingerprint: 0x9ec232ca
365 Variable types: 1422995 continuous, 1458128 integer (1450703 binary)
366 Coefficient statistics:
367 Matrix range [1e-01, 1e+10]
368 Objective range [6e-05, 5e+01]
369 Bounds range [1e+00, 8e+01]
370 RHS range [8e-01, 1e+10]
371 Warning: Model contains large matrix coefficients
372 Warning: Model contains large rhs
373 Consider reformulating model or setting NumericFocus parameter
374 to avoid numerical issues.
375 Presolve removed 3640530 rows and 2879269 columns (presolve time = 5s) ...
376 Presolve removed 3642376 rows and 2880070 columns
377 Presolve time: 7.71s
378 Presolved: 3098 rows, 1053 columns, 8257 nonzeros
379 Variable types: 10 continuous, 1043 integer (613 binary)
380 Found heuristic solution: objective 3978.8594268
381
382 Root simplex log...
383
384 Iteration Objective Primal Inf. Dual Inf. Time
385 0 9.1190000e+03 4.289887e+03 0.000000e+00 10s
386 878 4.9942444e+03 0.000000e+00 0.000000e+00 10s
387
388 Root relaxation: objective 4.994244e+03, 878 iterations, 0.02 seconds (0.01 work units)
389
390 Nodes | Current Node | Objective Bounds | Work
391 Expl Unexpl | Obj Depth IntInf | Incumbent BestBd Gap | It/Node Time
392
393 0 0 4994.24444 0 61 3978.85943 4994.24444 25.5% - 9s
394 H 0 0 4867.4444444 4994.24444 2.61% - 9s
395 H 0 0 4967.4444444 4994.24444 0.54% - 9s
396 0 0 4993.44444 0 24 4967.44444 4993.44444 0.52% - 9s
397 0 0 4993.44444 0 22 4967.44444 4993.44444 0.52% - 9s
398 0 0 4993.38228 0 25 4967.44444 4993.38228 0.52% - 9s
399 0 0 4992.88846 0 17 4967.44444 4992.88846 0.51% - 9s
400 H 0 0 4992.2202709 4992.88846 0.01% - 9s
401 0 0 cutoff 0 4992.22027 4992.22027 0.00% - 9s
402
403 Cutting planes:
404 Learned: 3
405 Gomory: 3
406 Cover: 13
407 Implied bound: 9
408 Clique: 18
409 MIR: 3
410 StrongCG: 1
411 Flow cover: 5
412 Zero half: 4
413 RLT: 2
414 Relax-and-lift: 3
415 PSD: 2

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```
416
417 Explored 1 nodes (1795 simplex iterations) in 10.40 seconds (10.47 work units)
418 Thread count was 8 (of 8 available processors)
419
420 Solution count 4: 4992.22 4967.44 4867.44 3978.86
421
422 Optimal solution found (tolerance 1.00e-08)
423 Best objective 4.992220270938e+03, best bound 4.992220270938e+03, gap 0.0000%
424 SP is solved
425 SP's optimal solution is'□4992
426
427 Itr = 2
428 Collect_LB = [553.0, 5146.1823098150835, 5771.720270937742]
429 Collect_UB = [9725.078905344453, 5516.3631280805985, 5516.3631280805985]
430 Collect_Hua = [0.0, 4586.039452672227, 4956.220270937742]
431 Collect_SPObjVal = [4586.039452672227, 4956.220270937742, 4992.220270937742]
432 Collect_MPObjValNHua = [553.0, 560.1428571428569, 815.5]
433
434
435 Ops, stop iteration
436 Values adopted from the judgeCount's th iteration, and Itr = {2}, judgeCount = {1}
437
438 ~~~~~judgeCount = 1, SPObj_SPF = 4956.220270937742
439 Vessel i: 0: pi: 0-5, ai-di: 3-12, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 3-12, taoi-deltai: 3-7, taoPi_SP-deltaPi_SP: 4-6, betaNi: 4, bi
: 4
440 Vessel i: 1: pi: 5-10, ai-di: 4-25, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 4-25, taoi-deltai: 4-18, taoPi_SP-deltaPi_SP: 9-18, betaNi: 14
, bi: 14
441 Vessel i: 2: pi: 21-26, ai-di: 9-27, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 9-27, taoi-deltai: 9-17, taoPi_SP-deltaPi_SP: 9-17, betaNi: 8
, bi: 8
442 Vessel i: 3: pi: 16-21, ai-di: 9-30, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 9-30, taoi-deltai: 9-17, taoPi_SP-deltaPi_SP: 9-17, betaNi: 8
, bi: 8
443 Vessel i: 4: pi: 11-16, ai-di: 14-29, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 14-29, taoi-deltai: 14-18, taoPi_SP-deltaPi_SP: 14-18,
betaNi: 4, bi: 4
444 Vessel i: 5: pi: 28-34, ai-di: 16-28, gi_SP-gpi_SP: 0.000000-0.000000, ai_SP-di: 16-28, taoi-deltai: 16-26, taoPi_SP-deltaPi_SP: 16-26,
betaNi: 10, bi: 10
445 Vessel i: 6: pi: 14-19, ai-di: 25-55, gi_SP-gpi_SP: 0.000000-1.000000, ai_SP-di: 25-55, taoi-deltai: 25-36, taoPi_SP-deltaPi_SP: 25-36,
betaNi: 11, bi: 11
446 Vessel i: 7: pi: 28-34, ai-di: 32-60, gi_SP-gpi_SP: 0.875000-0.501232, ai_SP-di: 39-60, taoi-deltai: 38-46, taoPi_SP-deltaPi_SP: 39-46,
betaNi: 8, bi: 8
447 Vessel i: 8: pi: 20-25, ai-di: 36-80, gi_SP-gpi_SP: 1.000000-0.600000, ai_SP-di: 46-80, taoi-deltai: 46-62, taoPi_SP-deltaPi_SP: 46-62,
betaNi: 16, bi: 16
448 Vessel i: 9: pi: 15-20, ai-di: 41-67, gi_SP-gpi_SP: 0.701232-0.898768, ai_SP-di: 45-67, taoi-deltai: 47-58, taoPi_SP-deltaPi_SP: 47-58,
betaNi: 11, bi: 11
449 Vessel i: 10: pi: 29-34, ai-di: 50-82, gi_SP-gpi_SP: 0.423768-0.000000, ai_SP-di: 52-82, taoi-deltai: 53-66, taoPi_SP-deltaPi_SP: 53-66,
betaNi: 13, bi: 13
450
451 round LB = [553, 5146, 5772]
452 round UB = [9725, 5516, 5516]
453 round Hua = [0, 4586, 4956]
454 round SPObjVal = [4586, 4956, 4992]
455 round MPObjValNHua = [553, 560, 816]
456
457 OptimalObj = 5771.720270937742
458 Time: 848.000000
459
460
461
462
```