

Min C_{max}
$$\begin{aligned} \text{st } y_{21} - y_{11} &\geq 9, y_{31} - y_{21} \geq 8, y_{22} - y_{12} \geq 5, y_{42} - y_{22} \geq 6, y_{13} - y_{33} \geq 10, y_{23} - y_{13} \geq 4 \\ C_{\max} - y_{11} &\geq 9, C_{\max} - y_{21} \geq 8, C_{\max} - y_{31} \geq 4, C_{\max} - y_{12} \geq 5, C_{\max} - y_{22} \geq 6, C_{\max} - y_{42} \geq 3, \\ C_{\max} - y_{33} &\geq 10, C_{\max} - y_{44} \geq 4, C_{\max} - y_{23} \geq 9 \end{aligned}$$
$$y_{11} - y_{12} \geq 5 \text{ OR } y_{12} - y_{11} \geq 9$$
$$y_{11} - y_{13} \geq 4 \text{ OR } y_{13} - y_{11} \geq 9$$
$$y_{12} - y_{13} \geq 4 \text{ OR } y_{13} - y_{12} \geq 5$$
$$y_{21} - y_{22} \geq 6 \text{ OR } y_{22} - y_{21} \geq 8$$
$$y_{21} - y_{23} \geq 9 \text{ OR } y_{23} - y_{21} \geq 8$$
$$y_{22} - y_{23} \geq 9 \text{ OR } y_{23} - y_{22} \geq 6$$
$$y_{31} - y_{33} \geq 10 \text{ OR } y_{33} - y_{31} \geq 4$$
$$y_{ij} \geq 0 \forall i, j$$

... $(c-1)$. Then apply

- (a) If you apply LPT to this problem you will get the following schedule for each machine with $C_{max} = 23$.

Machine 1: Job 13, Job 2, Job 1

Machine 2: Job 12, Job 3

Machine 3: Job 11, Job 4

Machine 4: Job 10, Job 5

Machine 5: Job 9, Job 6

Machine 6: Job 8, Job 7

- (b) It is easy to see that the optimal schedule for this problem is the following sequence with $C_{max} = 18$.

Machine 1: Job 13, Job 5

Machine 2: Job 12, Job 4

Machine 3: Job 11, Job 7

Machine 4: Job 10, Job 6

Machine 5: Job 9, Job 8

Machine 6: Job 1, Job 2, Job 3

Graph G'

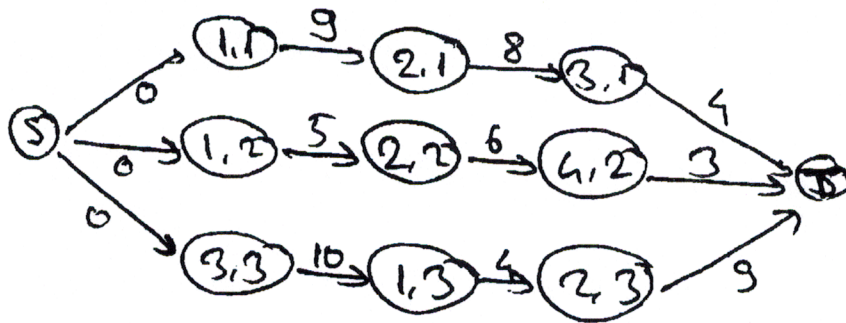


Fig 1.

Iteration 1:

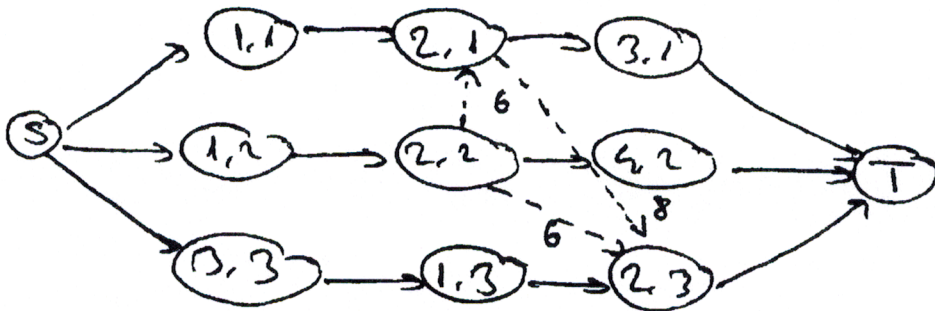


Fig 2.

Iteration 2:

