

A practical guide to dimensionality reduction and feature selection

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Schedule

- Day 1

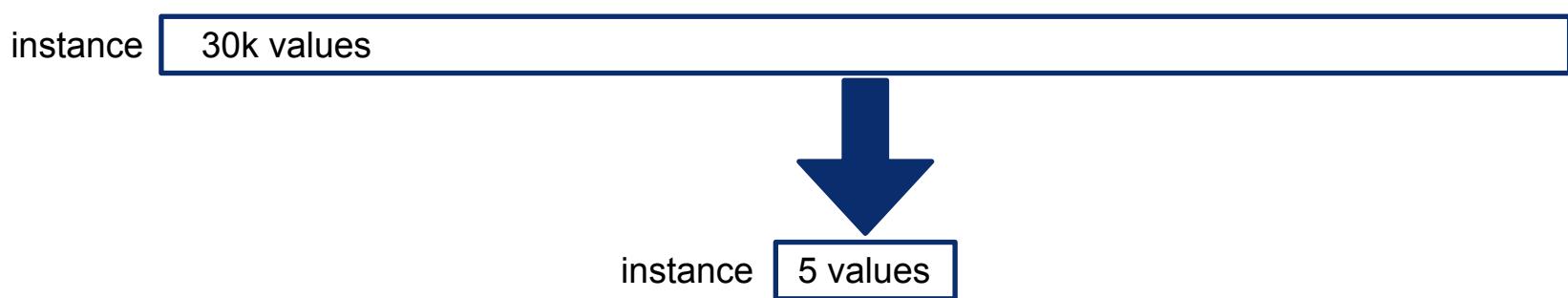
09:00 - 09:20	Introduction (slides will be made available)
09:20 - 10:00	Breakout rooms: feature transformation notebooks
10:00 - 11:00	Self-study: feature aggregation & autoencoder notebooks
11:00 - 12:00	Breakout rooms: discussion of questions and tasks

- Day 2

09:00 - 09:15	Questions regarding Day 1 material, introduction Day 2
09:15 - 10:30	Self-study: feature selection & stability optimization
10:30 - 11:45	Breakout rooms: discussion of questions and tasks
11:45 - 12:00	Wrap-up and conclusions

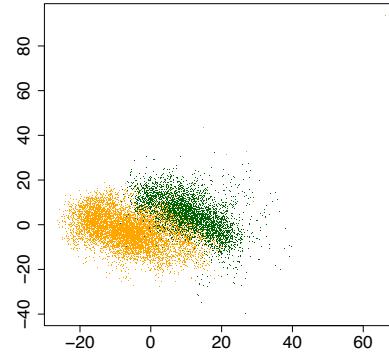
Definition of dimensionality reduction

- Given a dataset of n instances with p -dimensional measurement profiles, use a transformation to represent the n instances by k -dimensional feature profiles, with $k \ll p$
- Example: gene expression measurements
 - $n=24$ biological samples
 - $p=30k$ genes
- Can we reduce the 30k-dimensional profile of each instance to a 5-dimensional profile?



Purpose of dimensionality reduction

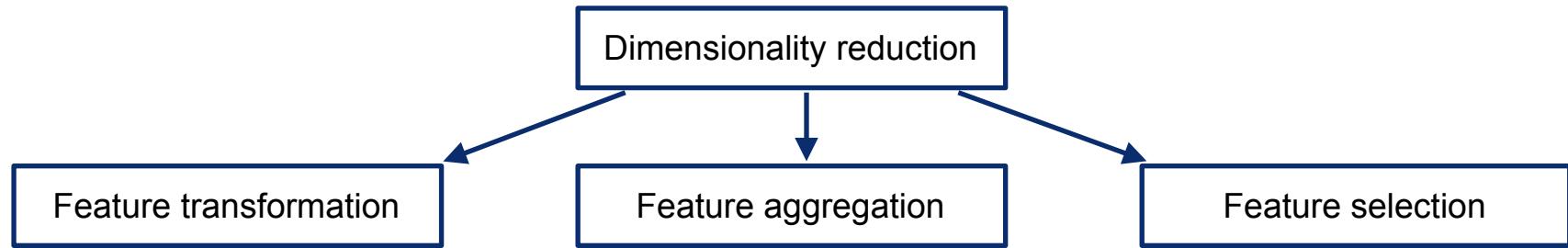
- Visualize the main dissimilarities between instances (e.g., a subgroup structure)
 - Allowing humans to visually grasp the data
 - Not only useful for scatterplots of instances but also for heatmaps (number of columns) etc.
 - Also quality control of data (e.g. batch effects)
- Facilitate machine learning analysis of instances
 - Clustering for detection of subgroups
 - Robust classification, e.g. healthy vs. cancer
 - Trajectory identification, e.g. cell development



Purpose of dimensionality reduction: further remarks

- Dimensionality reduction facilitates data visualization but not necessarily scientific interpretation: it is different from explainable AI (XAI)!
 - E.g. transformed features are composed of contributions from all original variables, so the influence of single variables may not be easy to trace
- Dimensionality reduction counteracts the curse of dimensionality in machine learning
 - As p increases, the neighborhood at a fixed distance of a specific point becomes less and less populated by instances; thus, instance similarities and groupings get harder and harder to detect
- Dimensionality reduction leads to computational advantages: less storage space, more efficient training of models

Overview of dimensionality reduction approaches



- Linear methods
 - PCA
 - ICA
 - CCA (multimodal)
 - Nonlinear methods
 - MDS
 - t-SNE
 - UMAP
 - Autoencoders
 - Data-driven methods
 - kMedoid clustering
 - Graph partitioning
 - Knowledge-based methods
 - GO slim categories
 - Molecular pathways
- Filter methods
 - ReliefF
 - Correlation
 - Wrapper methods
 - Forward selection
 - Backward elimination
 - Embedded methods
 - Elastic net

Mostly unsupervised: no target variable taken into account

Mostly supervised prediction

Remarks on supervised vs. unsupervised analysis

- Most often, feature transformation and feature aggregation are performed in an unsupervised manner, i.e. no target variable for the instances (e.g. class label, continuous output) is taken into account during dimensionality reduction
- However, there also exist supervised feature transformation methods, e.g. linear discriminant analysis, and feature aggregation may be targeted toward supervised tasks
- Feature selection methods are typically supervised, but there are also unsupervised methods, e.g. variance-based filters

References

- Altman, N., Krzywinski, M. The curse(s) of dimensionality. *Nat Methods* 15, 399–400 (2018). <https://doi.org/10.1038/s41592-018-0019-x>
- Hamer, V., Dupont, P. An importance weighted feature selection stability measure. *Journal of Machine Learning Research* 22, 1-57 (2021)
- Huang, S.H. (2015). Supervised feature selection: A tutorial. *Artif. Intell. Res.*, 4, 22-37.
- <https://www.frontiersin.org/articles/10.3389/fgene.2021.646936>