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WAEP Semester One Examination, 2017

Question/Answer booklet

MATHEMATICS METHODS UNIT 1

Section One: Calculator-free

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Student Number:	In figures	
	In words	
	Your name	

Time allowed for this section

Reading time before commencing work: five minutes Working time: fifty minutes

Materials required/recommended for this section

To be provided by the supervisor

This Question/Answer booklet Formula sheet

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction

fluid/tape, eraser, ruler, highlighters

Special items: nil

Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	7	7	50	52	35
Section Two: Calculator-assumed	13	13	100	98	65
			55"	Total	100

Instructions to candidates

- 1. The rules for the conduct of examinations are detailed in the school handbook. Sitting this examination implies that you agree to abide by these rules.
- 2. Write your answers in this Question/Answer booklet.
- 3. You must be careful to confine your response to the specific question asked and to follow any instructions that are specified to a particular question.
- 4. Additional working space pages at the end of this Question/Answer booklet are for planning or continuing an answer. If you use these pages, indicate at the original answer, the page number it is planned/continued on and write the question number being planned/continued on the additional working space page.
- 5. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- 6. It is recommended that you do not use pencil, except in diagrams.
- 7. The Formula sheet is not to be handed in with your Question/Answer booklet.

Section One: Calculator-free

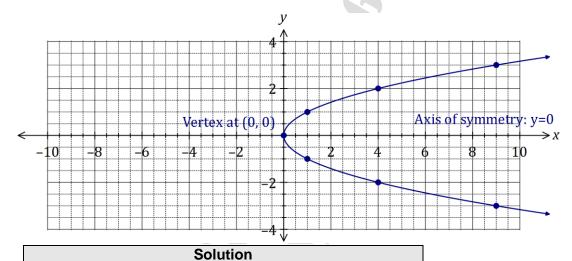
35% (52 Marks)

This section has **seven (7)** questions. Answer **all** questions. Write your answers in the spaces provided.

Working time: 50 minutes.

Question 1 (6 marks)

(a) On the axes below, sketch the graph of the relation $y^2 = x$, labelling all key features with their coordinates or equations. (3 marks)

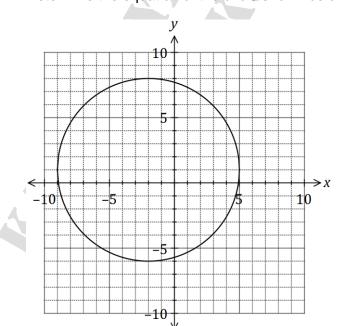


See graph

Specific behaviours

- √ smooth curve through at least 5 out of 7 marked points
- √ labels vertex
- √ labels axis of symmetry
- (b) Determine the equation of the circle shown below.

(3 marks)



Solution	
$(x+2)^2 + (y-1)^2 = 49$	

- ✓ uses standard form for circle
- √ uses correct centre
- √ uses correct radius

9 marks) A.

Question 2 (9 marks)

(a) The point M(8,1) is the midpoint of A and B(20,7). Determine the coordinates of A.

(2 marks)

Solution

$$\frac{20+x}{2} = 8 \text{ and } \frac{7+y}{2} = 1$$

 $x = -4, y = -5 \Rightarrow A(-4, -5)$

Specific behaviours

- ✓ writes equations
- ✓ states coordinates of A

- (b) A relationship between x and y is given by x = 2y 3
 - (i) Determine y when x = 25.

(1 mark)



$$25 = 2y - 3 \Rightarrow y = 14$$

Specific behaviours

√ states value

(ii) State, with justification, whether x is a function of y.

(2 marks)

Solution

Yes

All values of the domain (y) are mapped to one value of the range (x).

- ✓ states yes
- ✓ reasoning includes one output for each input

(c) A straight line passes through points C(2, -5) and D(-2, 2). Determine the equation of the straight line that is perpendicular to this line and passes through C, expressing your answer in the form ax + by + c = 0, where a, b and c are integers. (4 marks)

5

Solution $m_{CD} = -\frac{7}{4} \Rightarrow m_{\perp} = \frac{4}{7}$ $y - (-5) = \frac{4}{7}(x - 2) \Rightarrow -4x + 7y + 43 = 0$

- √ determines gradient of CD
- √ determines perp. Gradient
- ✓ writes equation of line
- ✓ writes equation in required form

Question 3

(7 marks)

Solve each of the following equations for the variable x.

(a)
$$3(1-x)+4=2(2x-7)$$
.

(2 marks)

Solution

$$3 - 3x + 4 = 4x - 14$$
$$21 = 7x \Rightarrow x = 3$$

Specific behaviours

- √ expands
- √ simplifies and solves

(b)
$$\frac{x}{2} = 1 + \frac{2x}{5}$$
.

(2 marks)

$$\frac{x}{2} = \frac{5+2x}{5}$$

$$5x = 10+4x$$

$$x = 10$$

Specific behaviours

- √ eliminates denominators
- √ solves

(c)
$$\frac{4}{x} = 3 + x$$
.

(3 marks)

$$4 = 3x + x^{2} \Rightarrow x^{2} + 3x - 4 = 0$$
$$(x + 4)(x - 1) = 0$$
$$x = -4, x = 1$$

- ✓ equates to zero
- √ factors
- ✓ solves

DO NOT WRITE IN THIS AREA AS IT WILL BE CUT OFF

Question 4 (8 marks)

(a) Solve the equation $x^3 = 7x^2 + 30x$.

(4 marks)

Solution

$$x^{3} - 7x^{2} - 30x = 0$$

$$x(x^{2} - 7x - 30) = 0$$

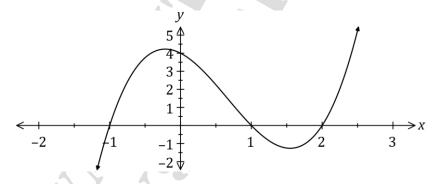
$$x(x - 10)(x + 3) = 0$$

$$x = 0, x = 10, x = -3$$

Specific behaviours

- √ equates to zero
- √ factors out x
- √ factors quadratic
- ✓ states all solutions

(b) The graph of $y = ax^3 + bx^2 + cx + d$ is shown below. Determine the values of the constants a, b, c and d. (4 marks)



Solution

$$y = a(x+1)(x-1)(x-2)$$

$$x = 0, y = 4 \Rightarrow 4 = 2a, a = 2$$

$$y = 2(x^{2}-1)(x-2) = 2(x^{3}-2x^{2}-x+2)$$

$$a = 2, b = -4, c = -2, d = 4$$

- ✓ writes factors from roots
- \checkmark determines a
- √ expands
- √ states all values

Question 5

(6 marks)

(a) Evaluate $\binom{6}{2}\binom{5}{3}$.

(2 marks)

Solution

$$\binom{6}{2}\binom{5}{3} = \frac{6!}{2! \ 4!} \times \frac{5!}{3! \ 2!} = \frac{6 \times 5 \times 5 \times 4}{2 \times 2}$$
$$= 150$$

Specific behaviours

✓ expands using factorials

(b) Expand $(2 - x)^4$.

(4 marks)

Solution

$$\frac{1(2)^4(-x)^0 + 4(2)^3(-x)^1 + 6(2)^2(-x)^2 + 4(2)^1(-x)^3 + 1(2)^0(-x)^4}{16 - 32x + 24x^2 - 8x^3 + x^4}$$

- √ coefficients (from Pascal's triangle) in first row
- √ correct terms in first row
- √ expands with alternating signs
- √ simplifies

Question 6 (8 marks)

- (a) For the graph with equation y = (x + 1)(x 3), determine the coordinates of
 - (i) all axes intercepts.

(2 marks)

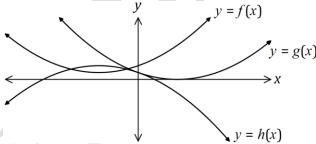
	Solution
y-inte	ercept: $(0, -3)$. <i>x</i> -intercepts: $(-1, 0)$ and $(3, 0)$
	Specific behaviours
✓ <i>y</i> -i	intercept
/ / .	intercepts and all answers written as coordinates

(ii) the turning point.

(2 marks)

	Solution	
Liı	ne of symmetry: $x = 1$	
y	=(1+1)(1-3)=-4	
TF	P at (1, -4)	
	Specific behaviours	
✓	<i>x</i> -coordinate	
✓	turning point in coordinate form	

(b) The graphs of three quadratic functions with discriminants of 0, 1 and -2 are shown below.



)	Solution (i)
	see table
	Specific behaviours
	✓ at least one correct
	✓ all correct

(i) Underneath each function in this table, write the value of it's discriminant.

(2 marks)

Function	f(x)	g(x)	h(x)
Discriminant	-2	0	1

(ii) Clearly explain your choices in part (i).

(2 marks)

Solution (ii)
f has no roots, g has 1 root and h has two roots.
Discriminant is: -ve, no roots; 0, one root; and +ve, two roots.
Specific behaviours
✓ states number of roots of each function
✓ explains use of discriminant

Question 7 (8 marks)

(a) If α and β are acute angles such that $\cos \alpha = \frac{2}{3}$ and $\sin \beta = \frac{3}{5}$, determine the value of $\cos(\alpha - \beta)$ as a single fraction. (4 marks)

Solution

From 3-4-5 right-triangle, $\cos \beta = \frac{4}{5}$

From 2- $\sqrt{5}$ -3 right-triangle, $\sin \alpha = \frac{\sqrt{5}}{3}$

Using identity, $\cos(\alpha - \beta) = \frac{2}{3} \times \frac{4}{5} + \frac{\sqrt{5}}{3} \times \frac{3}{5} = \frac{8 + 3\sqrt{5}}{15}$

Specific behaviours

- ✓ states cos β
- ✓ states $\sin \alpha$
- √ uses identity
- √ simplifies

(b) Solve the following equations.

(i) $\sqrt{2}\sin x = -1$ where $0 \le x \le 2\pi$.

(2 marks)

Solution

$$\sin x = -\frac{1}{\sqrt{2}}$$

$$x = \frac{5\pi}{4}, x = \frac{7\pi}{4}$$

Specific behaviours

- ✓ both solutions located in 3rd and 4th quadrants
- ✓ correct angles using radians

(ii)
$$tan(2x) = 0.4$$
 where $0 \le x \le 180^\circ$ and given that $tan 22^\circ = 0.4$. (2 marks)

Solution $tan(22^\circ) = 0.4 \Rightarrow 2x = 22^\circ, 2x = 22^\circ + 180^\circ$ $x = 11^\circ, x = 101^\circ$

- √ first solution
- ✓ second solution

Additional working space

Question number: _____

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