



Semester Two Examination, 2017

Question/Answer booklet

MATHEMATICS APPLICATIONS UNITS 3 AND 4

Section Two:

Calculator-assumed

If required by your examination administrator, please place your student identification label in this box

Student Number: In figures

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In words

Your name

Time allowed for this section

Reading time before commencing work: ten minutes
Working time: one hundred minutes

Materials required/recommended for this section

To be provided by the supervisor

This Question/Answer booklet
Formula sheet (retained from Section One)

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items: drawing instruments, templates, notes on two unfolded sheets of A4 paper, and up to three calculators approved for use in this examination

Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	7	7	50	52	35
Section Two: Calculator-assumed	12	12	100	98	65
Total					100

Instructions to candidates

- The rules for the conduct of examinations are detailed in the school handbook. Sitting this examination implies that you agree to abide by these rules.
- Write your answers in this Question/Answer booklet.
- You must be careful to confine your response to the specific question asked and to follow any instructions that are specified to a particular question.
- Additional working space pages at the end of this Question/Answer booklet are for planning or continuing an answer. If you use these pages, indicate at the original answer, the page number it is planned/continued on and write the question number being planned/continued on the additional working space page.
- Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- It is recommended that you do not use pencil, except in diagrams.
- The Formula sheet is not to be handed in with your Question/Answer booklet.

Markers use only		
Question	Maximum	Mark
8	5	
9	9	
10	8	
11	10	
12	12	
13	9	
14	8	
15	9	
16	7	
17	9	
18	6	
19	6	
S2 Total	98	
S2 Wt ($\times 0.6633$)	65%	

Section Two: Calculator-assumed

65% (98 Marks)

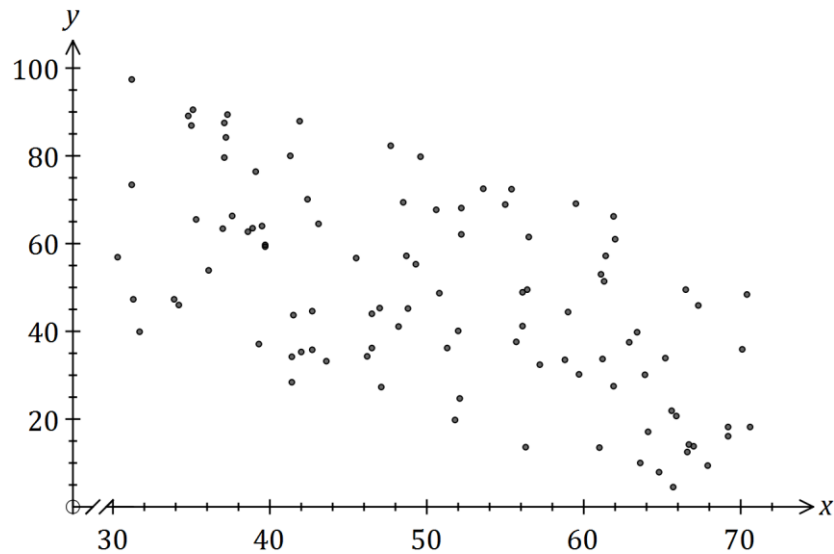
This section has **twelve (12)** questions. Answer **all** questions. Write your answers in the spaces provided.

Working time: 100 minutes.

Question 8

(5 marks)

The scatterplot below shows the daily sales of take-away coffees on the x -axis and canned drinks on the y -axis for a market stall.



- (a) Describe the association between the variables in terms of strength and direction. (2 marks)
- (b) The equation of the least-squares line that fits the data is $y = 108 - 1.2x$. Interpret the slope of this line. (2 marks)
- (c) Identify a possible non-causal explanation for the association between the variables. (1 mark)

Question 9**(9 marks)**

A researcher sought to determine whether a person's support for a particular political party affected their approval of a proposal to expand the Snowy Hydro scheme.

	Vote Labour	Vote Lib/Nat	Vote other	Total
Approve	156	187		416
Disapprove	38	21	22	81
Don't know	80	52	45	
Total	274	260		674

(a) Complete the three missing entries in the table above. (2 marks)

(b) State which is the response variable and which is the explanatory variable. (2 marks)

(c) Explain why creating a table of column percentages, rather than row percentages, is appropriate in this instance. (1 mark)

(d) Complete the table of column percentages below. (2 marks)

%	Vote Labour	Vote Lib/Nat	Vote other
Approve	57		52
Disapprove	14		16
Don't know		20	32
Total	100		100

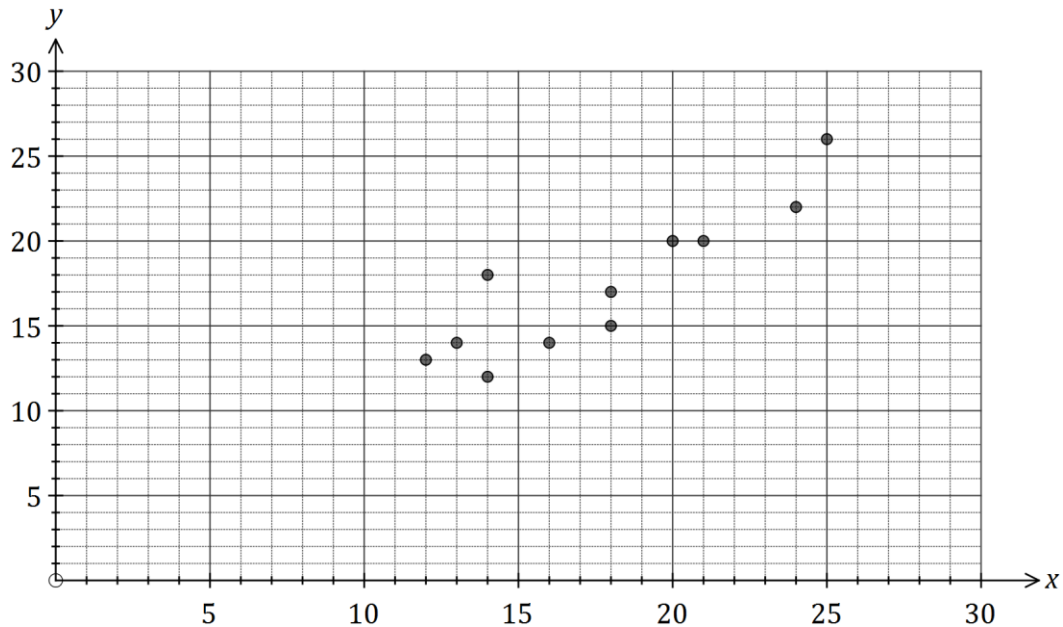
(e) Comment, with reasons, on whether any evidence exists to suggest that a person's support for a particular political party affected their approval of the proposal to expand the Snowy Hydro scheme. (2 marks)

Question 10

(8 marks)

A student was asked to estimate the length of lines generated at random on a computer screen. The actual and estimated lengths, in cm, are shown in the graph and table below.

Actual length, x	18	14	25	20	24	21	18	12	16	14	13
Estimated length, y	17	18	26	20	22	20	15	13	14	12	14



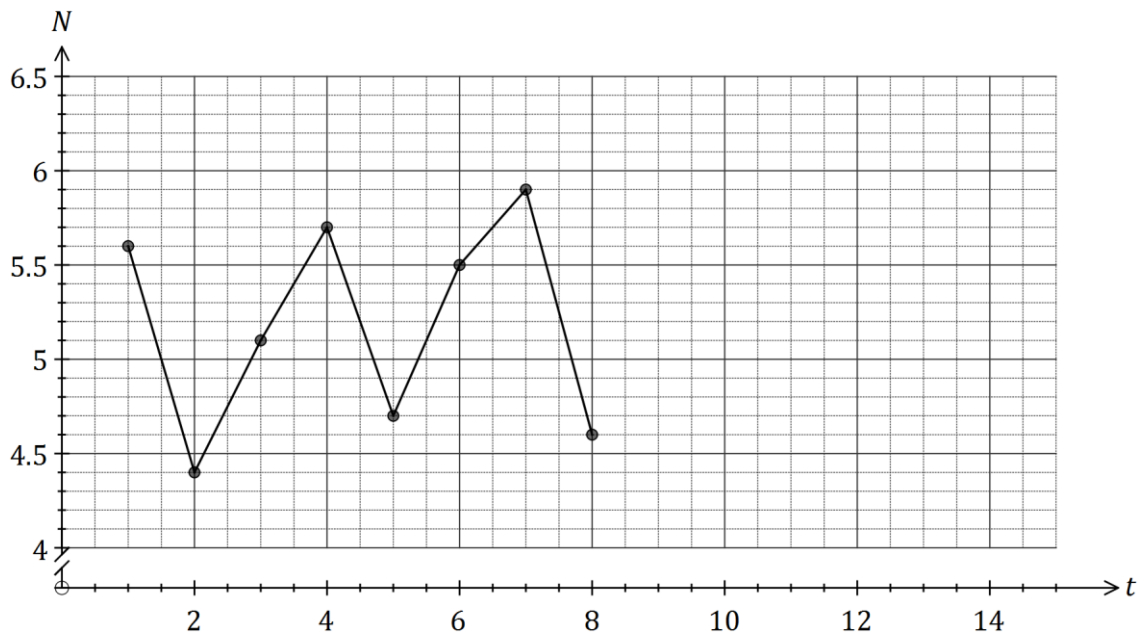
- (a) Calculate the correlation coefficient between the variables x and y . (1 mark)
- (b) A least-squares line can be used to model the relationship between x and y .
- (i) Determine the equation of this line. (2 marks)
- (ii) Draw this line on the graph. (2 marks)
- (c) Predict the student's estimate, to the nearest cm, when the actual length of the line was 8 cm and comment on factors affecting the reliability of this prediction. (3 marks)

Question 11**(10 marks)**

The number of page views, in thousands, of an international website were recorded in the morning (4 am to noon), afternoon (noon to 8 pm) and night (8 pm to 4 am) over several consecutive days.

Day	Period	Time, t	Page views, N , (000's)
Mon	Morning	1	5.6
	Afternoon	2	4.4
	Night	3	5.1
Tue	Morning	4	5.7
	Afternoon	5	4.7
	Night	6	5.5
Wed	Morning	7	5.9
	Afternoon	8	4.6
	Night	9	5.4
Thu	Morning	10	6.0
	Afternoon	11	4.8
	Night	12	5.6
Fri	Morning	13	5.4
	Afternoon	14	4.9
	Night	15	5.7

- (a) Use the above data to complete the time series plot on the axes below.

(2 marks)

- (b) One of the data points was suspected of being an outlier. Circle this point on the graph and explain why you chose it.

(2 marks)

(c) Describe the trend and seasonality of the time series plot. (2 marks)

(d) Calculate the number of page views representing

(i) the three-point moving average for Tuesday afternoon. (2 marks)

(ii) the six-point centred moving average for Wednesday night. (2 marks)

Question 12**(12 marks)**

Every afternoon, 20 litres of water is taken from a tank and poured into a small garden pond. At the start of the first day the tank contains 260 L and the pond contains 50 L.

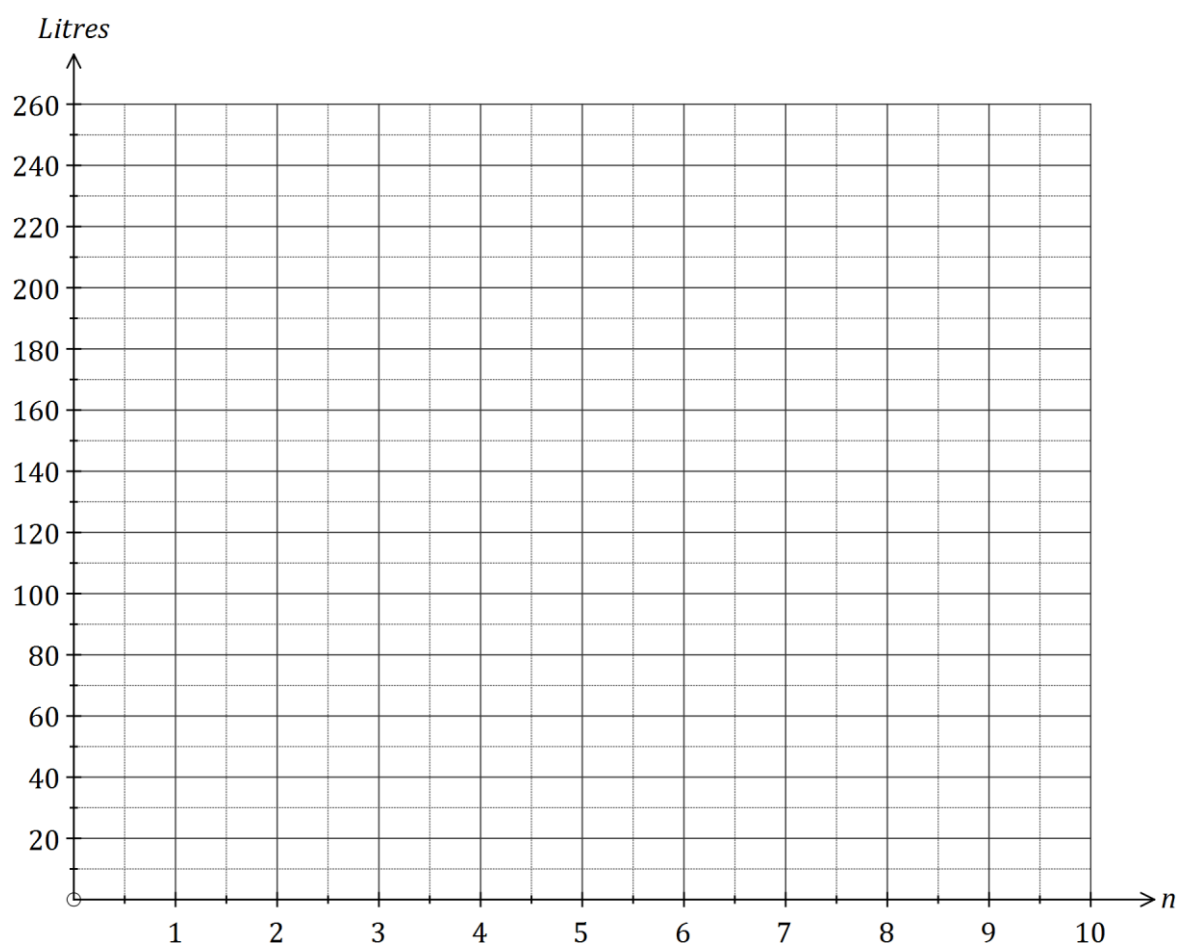
The amount of water in the tank at the start of day n is given by $T_{n+1} = T_n - 20, T_1 = 260$.

- (a) Complete the table below. (1 mark)

n	1	2	3	4	5	6	7	8
T_n (L)	260	240						

- (b) Deduce a rule for the amount of water in the tank at the start of the n^{th} day. (2 marks)

- (c) Graph the amount of water in the tank at the start of day n on the axes below. (2 marks)



Due to the combined effects of evaporation and water being added from the tank, the amount of water in the pond, in litres, at the start of day n is given by $P_{n+1} = 0.9P_n + 20, P_1 = 50, n \leq 14$.

- (d) Complete the table below, writing all amounts to the nearest litre. (2 marks)

n	1	2	3	4	5	6	7	8
P_n (L)					102	111	120	128

- (e) Add the amount of water in the pond at the start of day n to the graph in (c). (2 marks)

- (f) At the start of which day did the amount of water in the pond first exceed the amount of water in the tank? (1 mark)

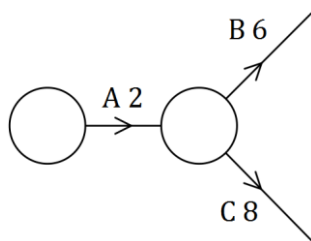
- (g) Determine the maximum amount of water in the pond and when this occurs. (2 marks)

Question 13**(9 marks)**

The tasks involved in a construction project are shown in the table below.

Task	A	B	C	D	E	F	G	H	J
Duration (days)	2	6	8	8	10	4	7	4	3
Immediate predecessors	-	A	A	B	B	B	F, C	D, E	H, G

(a) Complete the project network below.

(3 marks)

(b) List the tasks on the critical path and state the minimum completion time for the project.

(2 marks)

(c) If the project is completed in the minimum possible time, determine

(i) the earliest start time for task G.

(1 mark)

(ii) the latest start time for task F.

(1 mark)

(iii) the task with the largest float time, and what this float time is.

(2 marks)

Question 14

(8 marks)

A student took out a car loan of \$9 500 and made monthly repayments of \$420. The table below shows the progress of the loan for the first few months, with repayments and interest applied at the end of each month.

Month (n)	Balance at start of month (T_n)	Interest	Repayment	Balance carried forward to start of next month
1	9 500.00	104.50	420.00	9 184.50
2	9 184.50	101.03	420.00	8 865.53
3	8 865.53	97.52	420.00	8 543.05
4	8 543.05	A	420.00	B

(a) Determine the monthly interest rate. (1 mark)

(b) The recurrence relation to model the loan balance, T_n , in the second column of the table is $T_{n+1} = aT_n - b$, $T_1 = 9\,500$. State the values of a and b . (2 marks)

(c) Determine the values of A and B in the table. (2 marks)

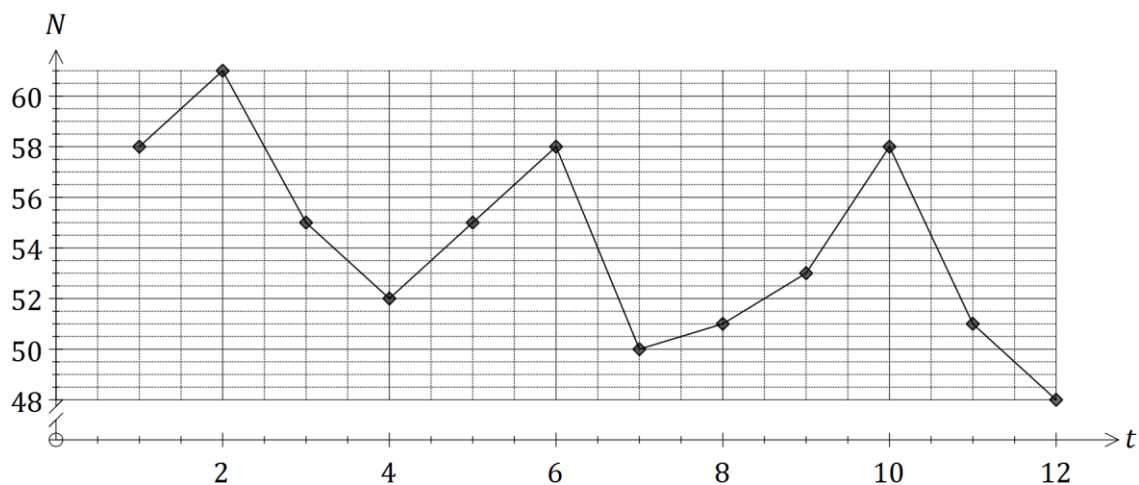
(d) Calculate the balance of the loan at the start of month 6. (2 marks)

(e) If the student increased the amount of each repayment, comment on how this would change the total interest accumulated over the life of the loan. (1 mark)

Question 15

(9 marks)

The number of false alarms received by a monitoring station each quarter over the past three years is shown in the graph and table below.



Year	Quarter	Time period (t)	Number of false alarms (N)	Yearly mean	Percent of yearly mean
2014	1	1	58	56.5	A
	2	2	61		108.0
	3	3	55		97.3
	4	4	52		92.0
2015	1	5	B	53.5	102.8
	2	6	58		108.4
	3	7	50		93.5
	4	8	51		95.3
2016	1	9	53	C	101.0
	2	10	58		110.5
	3	11	51		97.1
	4	12	48		91.4

(a) Calculate the values of the entries **A**, **B** and **C** in the table.

(3 marks)

- (b) Three of the four seasonal indices, calculated using the average percentage method, are shown in the table below. Calculate the missing index for quarter 3 and interpret its value. (2 marks)

Quarter	1	2	3	4
Seasonal index	1.02	1.09		0.93

- (c) Calculate the deseasonalised number of false alarms for the fourth quarter of 2015. (1 mark)

- (d) The equation of the least-squares line to forecast the deseasonalised number of false alarms, n , is $n = 57.1 - 0.45t$.

Forecast the **actual** number of false alarms in the second quarter of 2018, assuming that the above seasonality and trends continue. (3 marks)

Question 16**(7 marks)**

A retiree plans to start a pension fund with \$750 000 and then withdraw an annuity of \$55 000 one year later and then at subsequent yearly intervals. The fund is expected to grow at a rate of 5.4% per annum.

- (a) Write a linear recurrence relation to model the total amount in the pension fund, T_n , directly after the n^{th} withdrawal. (3 marks)

- (b) Determine the number of years that the retiree can withdraw \$55 000. (2 marks)

- (c) Determine how much can be withdrawn each year if the retiree only wants the fund to last for 10 years. (2 marks)

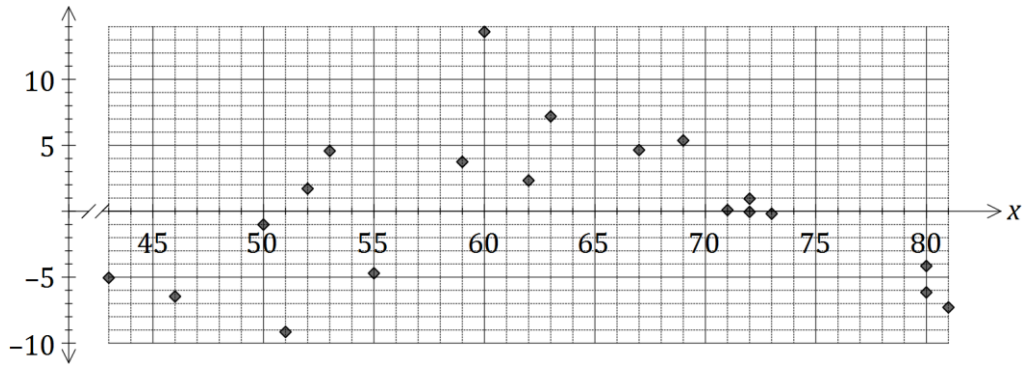
Question 17

(9 marks)

The percentage scores of 20 students in a physics test, x , and a chemistry test, y , were recorded and the following statistics calculated:

- the least-squares line to model the relationship is $\hat{y} = 1.14x - 17.9$
- $r_{xy} = 0.922$

The residual plot for the linear model is shown below.



- (a) Another student scored 65% in the physics test and 67% in the chemistry test. Calculate the residual for this student and plot it on the graph above. (3 marks)
- (b) Use the residual plot to explain whether fitting a linear model to the data is appropriate. (2 marks)
- (c) What percentage of the variation in the chemistry scores can be explained by the variation in the physics scores? (2 marks)
- (d) Are the variables x and y causally related? Explain your answer. (2 marks)

Question 18**(6 marks)**

- (a) \$25 000 is invested in a savings account that earns compound interest of 5.6% per annum. Determine
- (i) the total interest added to the investment over five years, if interest is compounded annually. (2 marks)
 - (ii) the least time, in months, for the investment to accrue a minimum of \$12 000 interest when interest is compounded monthly. (2 marks)
- (b) \$25 000 is invested in a savings account offering 7.8% per annum compounded quarterly.
- (i) Calculate the effective interest rate for this account. (1 mark)
 - (ii) Determine the annual rate that a savings account, compounding interest monthly, would need to offer to achieve the same effective rate as in (i). (1 mark)

Question 19**(6 marks)**

A lottery winner set up a fund on January 1, 2010, with their prize of \$250 000. The balance of the fund grew at an annual rate of 3.5%, compounded monthly. Starting on February 1, 2010, the winner withdrew \$500 from the fund on the first day of each month.

- (a) Determine the balance in the fund just after the withdrawal was made on January 1, 2011. (2 marks)

- (b) Determine the total amount of interest accrued by the fund during 2010. (2 marks)

- (c) From January 1, 2011, the annual interest rate applying to the fund decreased and the winner found that the balance of the fund remained the same from month to month. Determine by how much the annual interest rate fell. (2 marks)

Additional working space

Question number: _____

Additional working space

Question number: _____

