



Semester One Examination, 2017

Question/Answer booklet

MATHEMATICS METHODS UNIT 1

Section Two:

Calculator-assumed

If required by your examination administrator, please place your student identification label in this box

Student Number: In figures

--	--	--	--	--	--	--	--

In words

Your name

Time allowed for this section

Reading time before commencing work: ten minutes
Working time: one hundred minutes

Materials required/recommended for this section

To be provided by the supervisor

This Question/Answer booklet
Formula sheet (retained from Section One)

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items: drawing instruments, templates, notes on two unfolded sheets of A4 paper, and up to three calculators approved for use in this examination

Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of examination
Section One: Calculator-free	7	7	50	52	35
Section Two: Calculator-assumed	13	13	100	98	65
Total					100

Instructions to candidates

- The rules for the conduct of examinations are detailed in the school handbook. Sitting this examination implies that you agree to abide by these rules.
- Write your answers in this Question/Answer booklet.
- You must be careful to confine your response to the specific question asked and to follow any instructions that are specified to a particular question.
- Additional working space pages at the end of this Question/Answer booklet are for planning or continuing an answer. If you use these pages, indicate at the original answer, the page number it is planned/continued on and write the question number being planned/continued on the additional working space page.
- Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
- It is recommended that you do not use pencil, except in diagrams.
- The Formula sheet is not to be handed in with your Question/Answer booklet.

Markers use only		
Question	Maximum	Mark
8	6	
9	9	
10	6	
11	6	
12	8	
13	5	
14	8	
15	8	
16	8	
17	9	
18	8	
19	8	
20	9	
S2 Total	98	

Section Two: Calculator-assumed

65% (98 Marks)

This section has **thirteen (13)** questions. Answer **all** questions. Write your answers in the spaces provided.

Working time: 100 minutes.

Question 8

(6 marks)

- (a) The variables C and n are directly proportional to each other, so that when $n = 10$, it is known that $C = 25$. Sketch a graph of the relationship between C and n on the axes below. (3 marks)



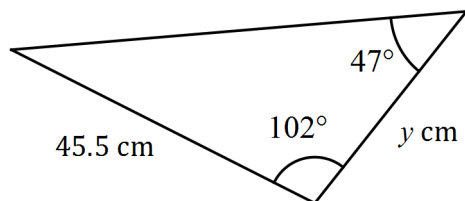
- (b) The variables A and n are inversely proportional to each other, so that when $n = 10$, it is known that $A = 60$.
- (i) Write an equation that relates A and n . (2 marks)

- (ii) Determine the value of n when $A = 15$. (1 mark)

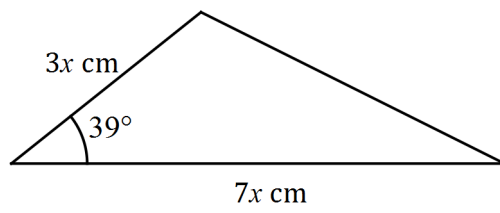
Question 9**(9 marks)**

- (a) Determine the size, to the nearest degree, of the largest angle in a triangle with sides of lengths 23 cm, 28 cm and 31 cm. (3 marks)

- (b) Determine the value of y in the diagram below. (3 marks)



- (c) The area of the triangle shown below is 280 cm^2 . Determine the value of x . (3 marks)

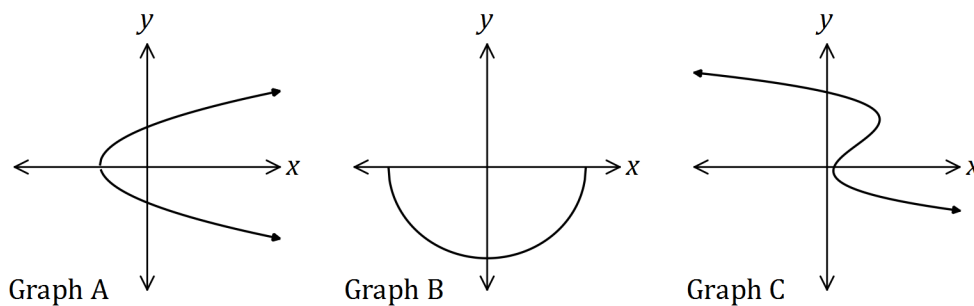


Question 10

(6 marks)

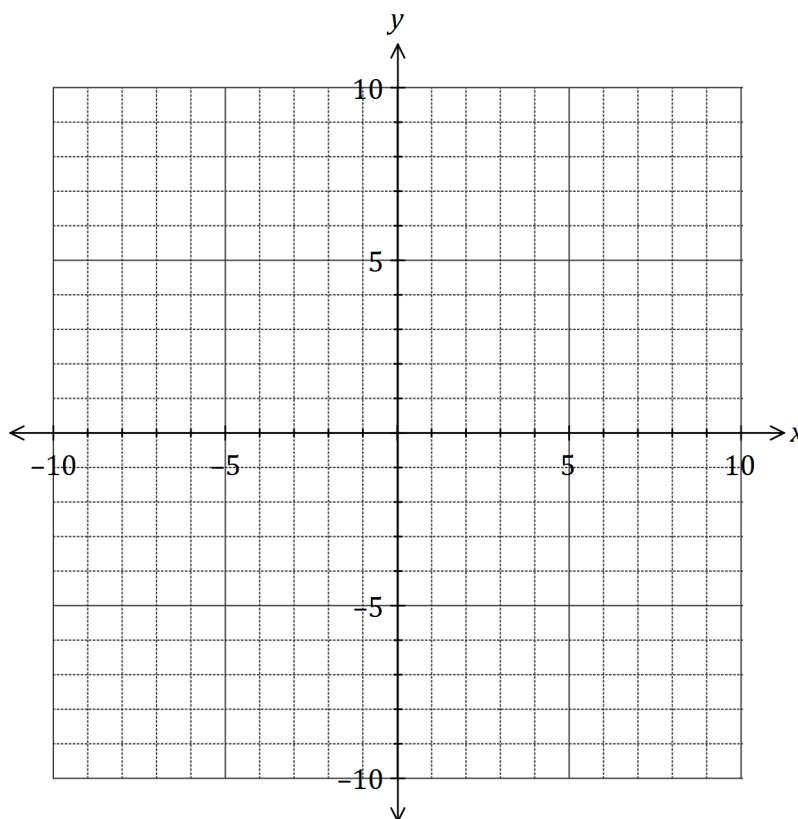
- (a) State, with reasoning, which of the graphs shown below are **not** those of a function.

(3 marks)



- (b) Draw the graph of the relation $x^2 + y^2 = 2x - 6y + 26$.

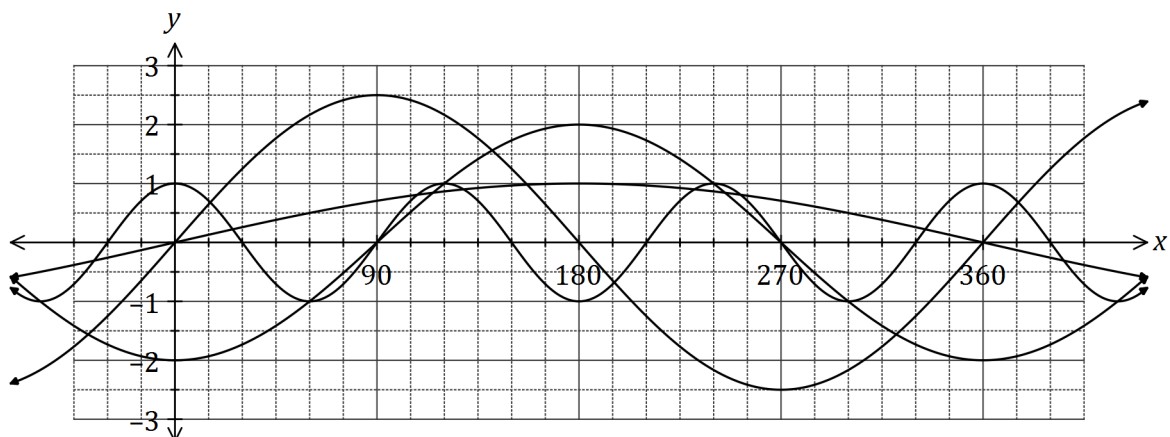
(3 marks)



Question 11

(6 marks)

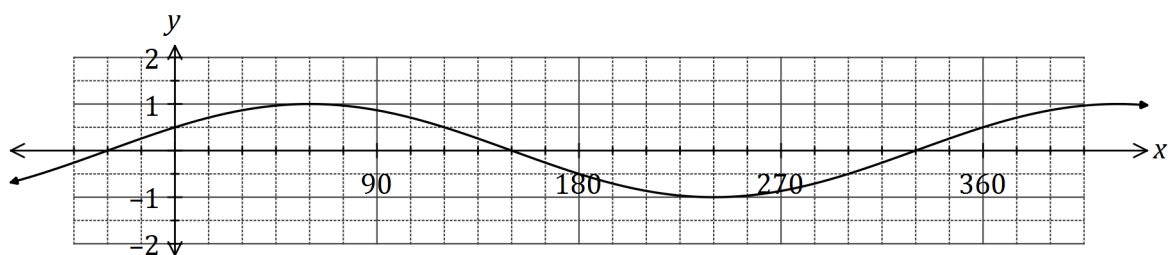
(a) The graphs of $y = a \sin(x)$, $y = \sin(bx)$, $y = d \cos(x)$ and $y = \cos(ex)$ are shown below.



Determine the values of the constants a , b , d and e .

(4 marks)

(b) The graph of $y = \cos(x - \alpha)$ is drawn below.



(i) State the value of the constant α , where $0^\circ < \alpha < 360^\circ$.

(1 mark)

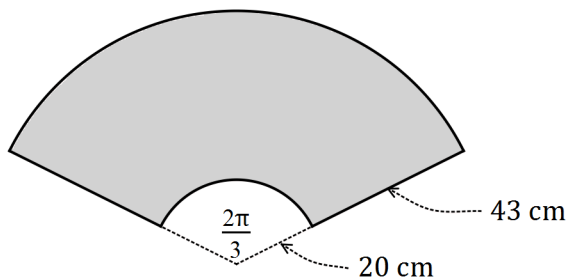
(ii) The graph is also that of $y = \sin(x + \beta)$. State the value of the constant β , where $0^\circ < \beta < 360^\circ$.

(1 mark)

Question 12**(8 marks)**

- (a) At 3 pm, the length of the shadow of a thin vertical pole standing on level ground is the same as the height of the pole. A while later, the angle of elevation of the sun has decreased by 12° and the length of the shadow has increased by 95 cm. Determine the height of the pole. (4 marks)

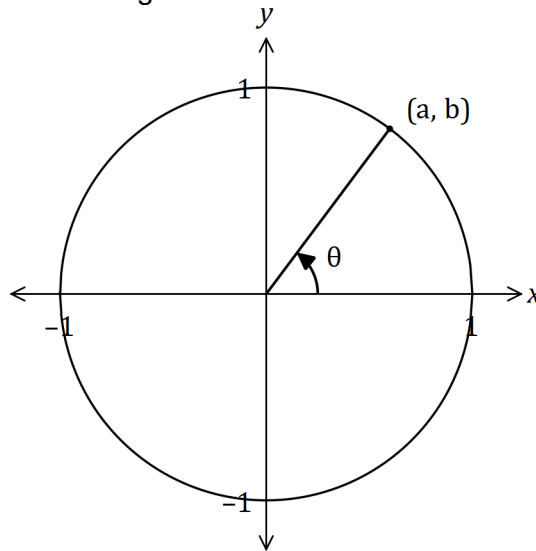
- (b) A windscreen wiper on a car is 43 cm long and rotates through one-third of a circle, as shown below. The inner and outer radii of the arcs are 20 cm and 63 cm. Determine the shaded area, rounding your answer to a reasonable degree of accuracy. (4 marks)



Question 13

(5 marks)

- (a) Using the unit circle shown, determine the following in terms of a and/or b , given that θ is an acute angle measured in degrees.



- (i) $\sin(\theta)$. (1 mark)
- (ii) $\cos(180 - \theta)$. (1 mark)
- (iii) $\tan(90 + \theta)$. (1 mark)
- (b) Determine x in each of the following cases, where $0 \leq x \leq \frac{\pi}{2}$.
- (i) $\sin x = \sin 17\pi$. (1 mark)
- (ii) $\cos x = \cos \frac{23\pi}{6}$. (1 mark)

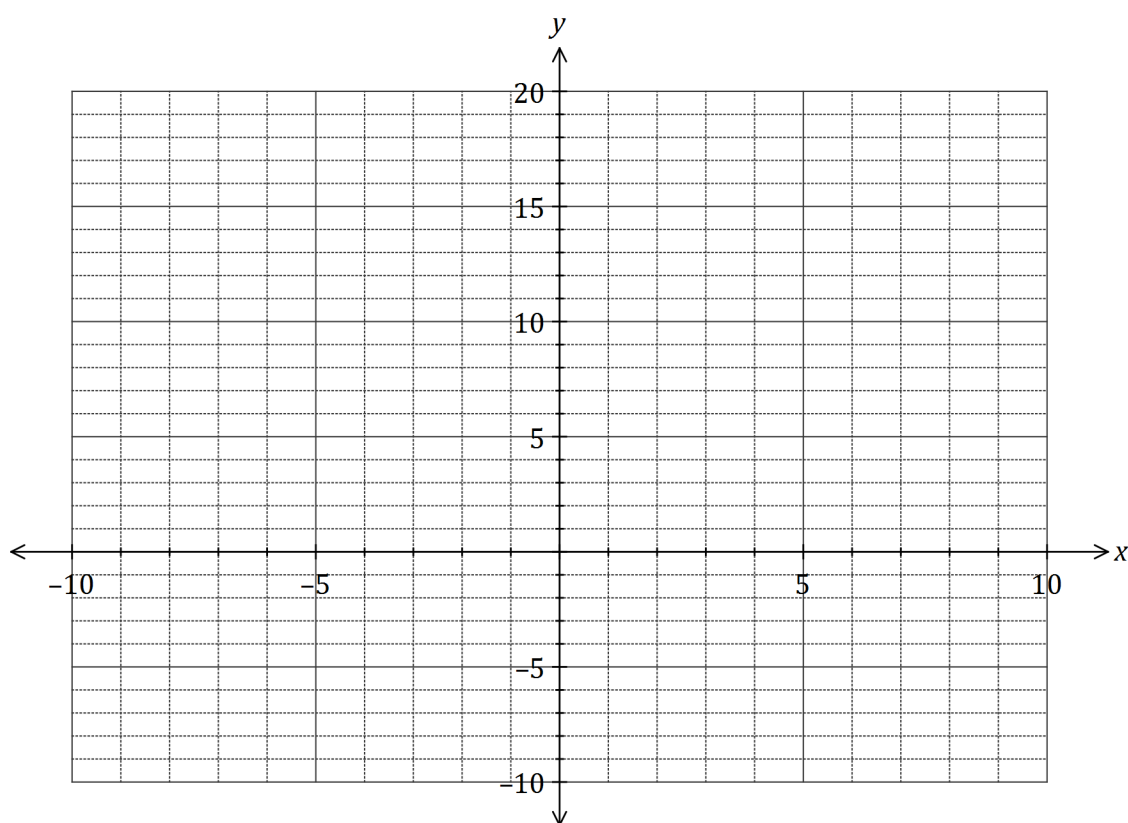
Question 14**(8 marks)**

(a) The graph of $y = 2x^2 + bx + 16$ has a line of symmetry with equation $x = 3$.

(i) Determine the value of b .

(2 marks)

(ii) Draw the graph of the parabola on the axes below.

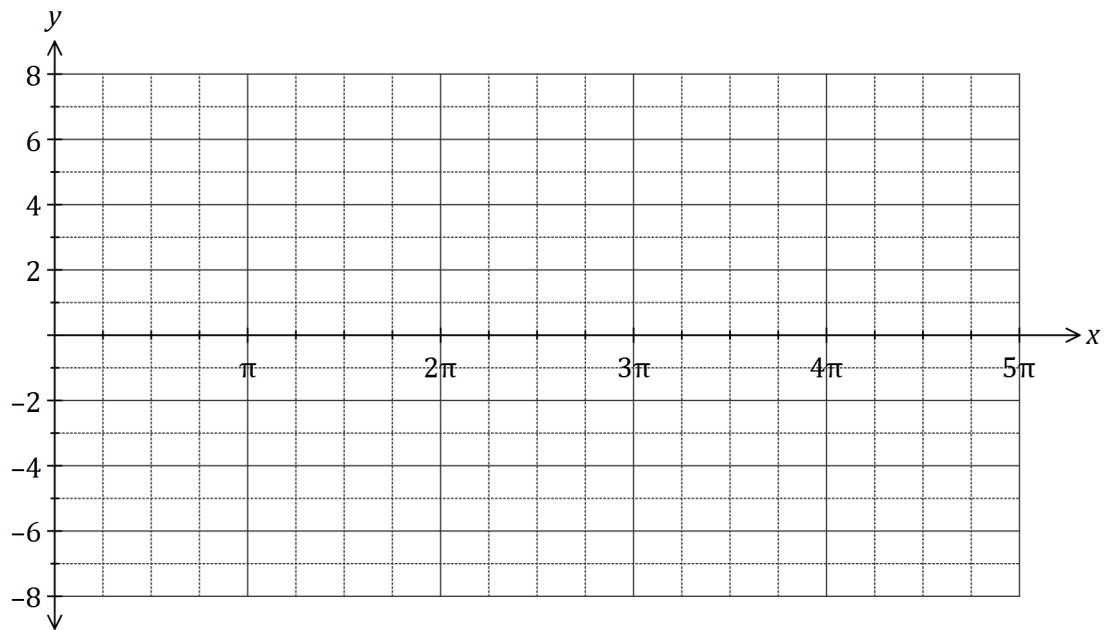
(3 marks)

- (b) One of the solutions to the equation $2x^3 + 21x^2 + cx - 495 = 0$ is $x = 5$. Determine the value of c and all other solutions. (3 marks)

Question 15

(8 marks)

- (a) On the axes below, draw the graph of $y = \tan\left(\frac{x}{3}\right)$ over the interval $0 \leq x \leq 5\pi$, clearly indicating the equations of any asymptotes. (3 marks)



- (b) Solve the following equations over the interval $0 \leq x \leq 5\pi$.

(i) $\tan\left(\frac{x}{3}\right) = -1$. (1 mark)

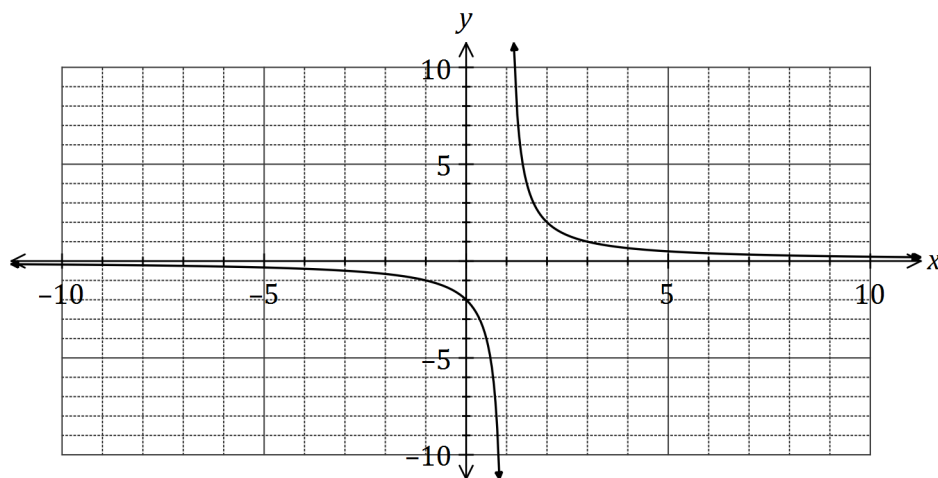
(ii) $\tan\left(\frac{x}{3}\right) - \sqrt{3} = 0$. (2 marks)

- (c) Determine the smallest positive value of α so that $\tan\left(x - \frac{5\pi}{6}\right) = \tan(x + \alpha)$. (2 marks)

Question 16

(8 marks)

The graph of the function is defined by $f(x) = \frac{a}{x+b}$ is shown below.



(a) Determine the values of a and b . (2 marks)

(b) State the domain and range of $f(x)$. (2 marks)

(c) Determine the equations of the asymptotes of the graph of $y = f(2x)$. (2 marks)

(d) Describe the transformation required on the graph of $y = f(x)$ to obtain the graph of

(i) $y = f(x + 8)$. (1 mark)

(ii) $y = \frac{1}{2}f(x)$. (1 mark)

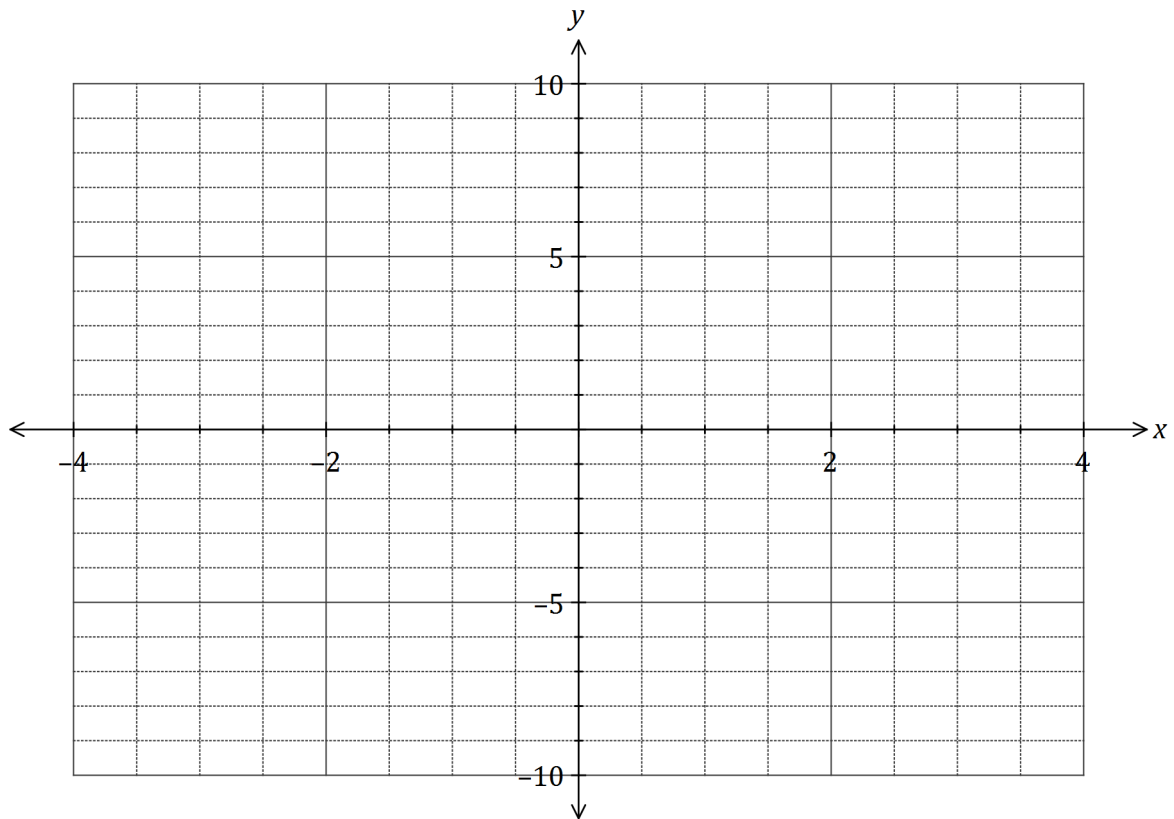
Question 17**(9 marks)**

A straight line with equation $y = mx + n$, a parabola with equation $y = px^2 + qx + r$ and a cubic with equation $y = h(x)$ all pass through the points $E(1, -4)$ and $F(2, 0)$.

- (a) Determine the values of the constants m and n in the equation of the straight line.
(2 marks)

- (b) Determine the values of the constants p , q and r in the equation of the parabola, given that E is a minimum turning point of the parabola.
(3 marks)

- (c) Draw the graph of the cubic on the axes below, given that E is a point of inflection and F is a maximum turning point of the cubic. (4 marks)



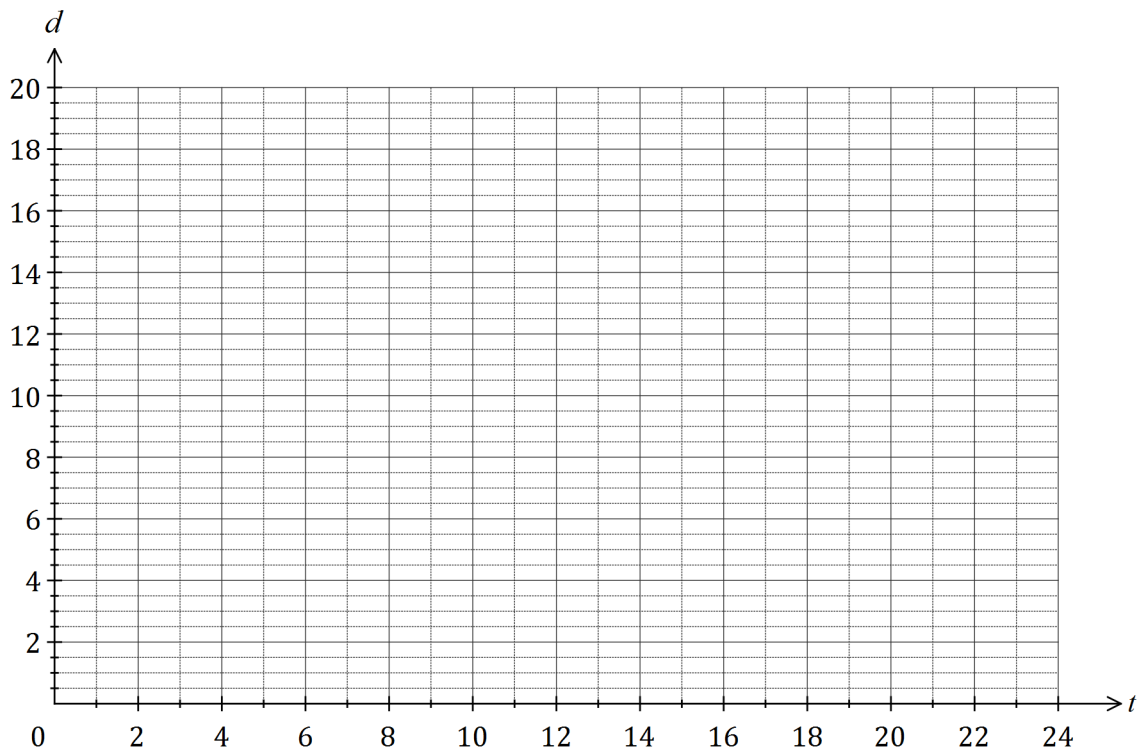
Question 18**(8 marks)**

Over a 24-hour period, the depth of water, d metres, in a harbour at time t hours after midnight was given by

$$d = 7.5 \sin\left(\frac{\pi t}{6}\right) + 9, \quad 0 \leq t \leq 24.$$

- (a) Determine the depth of water at 11 pm. (1 mark)

- (b) Draw the graph of the water depth on the axes below. (3 marks)



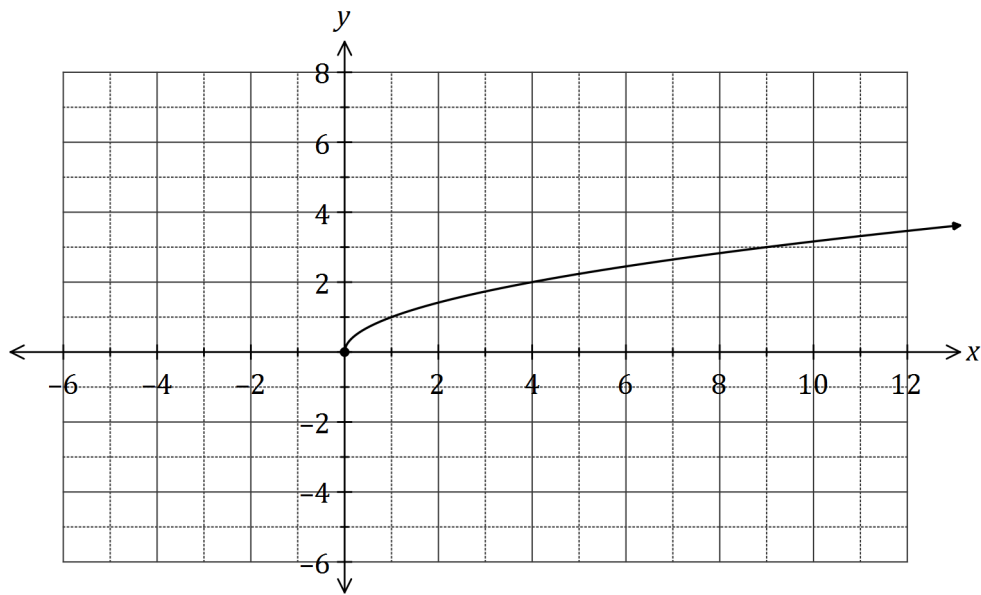
- (c) At what time, in hours and minutes, did the depth of water first exceed 15 metres? (2 marks)

- (d) Determine the fraction of the 24-hour period during which the depth of water exceeded 12.75 m. (2 marks)

Question 19

(8 marks)

The graph of $y = f(x)$ is drawn below over its natural domain, where $f(x) = x^n$.

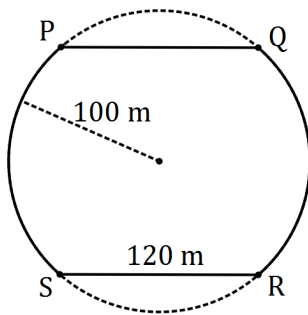


- (a) The value of n is either -2 , -1 , $-\frac{1}{2}$, $\frac{1}{2}$, 1 or 2 . State the correct value of n and justify your choice. (2 marks)
- (b) Explain why the domain of the function f is $\{x: x \in \mathbb{R}, x \geq 0\}$. (2 marks)
- (c) On the axes above, sketch and label the graphs of
- (i) $y = f(x) - 4$. (2 marks)
- (ii) $y = f(-2x)$. (2 marks)

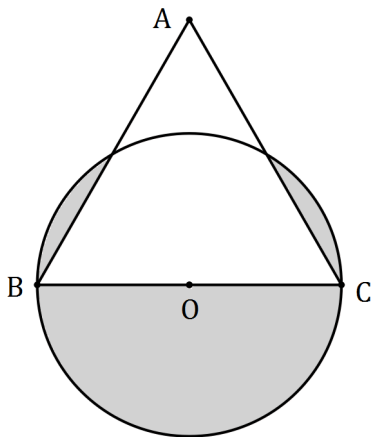
Question 20

(9 marks)

- (a) A running track has circular ends of radius 100 m and two straight, parallel sides PQ and RS that are both 120 m long, as shown below. Determine, to the nearest metre, the total length of the track. (4 marks)



- (b) The diagram shows a circle with centre O and diameter BC , and an equilateral triangle ABC . Determine the exact fraction of the area of the circle that lies outside the triangle. (5 marks)



Additional working space

Question number: _____

© 2017 WA Exam Papers. Narrogin Senior High School has a non-exclusive licence to copy and communicate this paper for non-commercial, educational use within the school. No other copying, communication or use is permitted without the express written permission of WA Exam Papers. SN131-092-7.