

Trial Examination 2023

VCE Specialist Mathematics Units 3&4

Written Examination 1

Question and Answer Booklet

Reading time: 15 minutes

Writing time: 1 hour

Student's Name: _____

Teacher's Name: _____

Structure of booklet

<i>Number of questions</i>	<i>Number of questions to be answered</i>	<i>Number of marks</i>
10	10	40

Students are permitted to bring into the examination room: pens, pencils, highlighters, erasers, sharpeners and rulers.

Students are NOT permitted to bring into the examination room: any technology (calculators or software), notes of any kind, blank sheets of paper and/or correction fluid/tape.

Materials supplied

Question and answer booklet of 13 pages

Formula sheet

Working space is provided throughout the booklet.

Instructions

Write your **name** and your **teacher's name** in the space provided above on this page.

Unless otherwise indicated, the diagrams in this booklet are **not** drawn to scale.

All written responses must be in English.

At the end of the examination

You may keep the formula sheet.

Students are NOT permitted to bring mobile phones and/or any other unauthorised electronic devices into the examination room.

Students are advised that this is a trial examination only and cannot in any way guarantee the content or the format of the 2023 VCE Specialist Mathematics Units 3&4 Written Examination 1.

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Instructions

Answer **all** questions in the spaces provided.

Unless otherwise specified, an **exact** answer is required to a question.

In questions where more than one mark is available, appropriate working **must** be shown.

Unless otherwise indicated, diagrams in this booklet are **not** drawn to scale.

Take the **acceleration due to gravity** to have magnitude $g \text{ ms}^{-2}$, where $g = 9.8$.

Question 1 (2 marks)

X and Y are independent random variables. The mean and the variance of X are 3 and 2, respectively; the mean and the variance of Y are 5 and 4, respectively.

Find the mean and variance of $X + 2X - 4Y$.

Question 2 (3 marks)

Given that $p, q \in \mathbb{Z}$, consider the following statement.

If $p^2 + q^2 + 1$ is odd, then $p + q$ is even.

- a.** Write down the contrapositive of the statement. 1 mark

- b.** Prove that the contrapositive is true. 2 marks

Question 4 (3 marks)

Find the cube roots of -64 . Express your answers in polar form using the principal values of the argument.

This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.

- c.** Find the particle's maximum acceleration.

2 marks

Question 7 (4 marks)

Consider points $A(-2, 1, 0)$, $B(3, 4, -2)$ and $C(-5, -2, 1)$.

- a.** Use proof by contradiction to prove that points A , B and C are not collinear. 2 marks

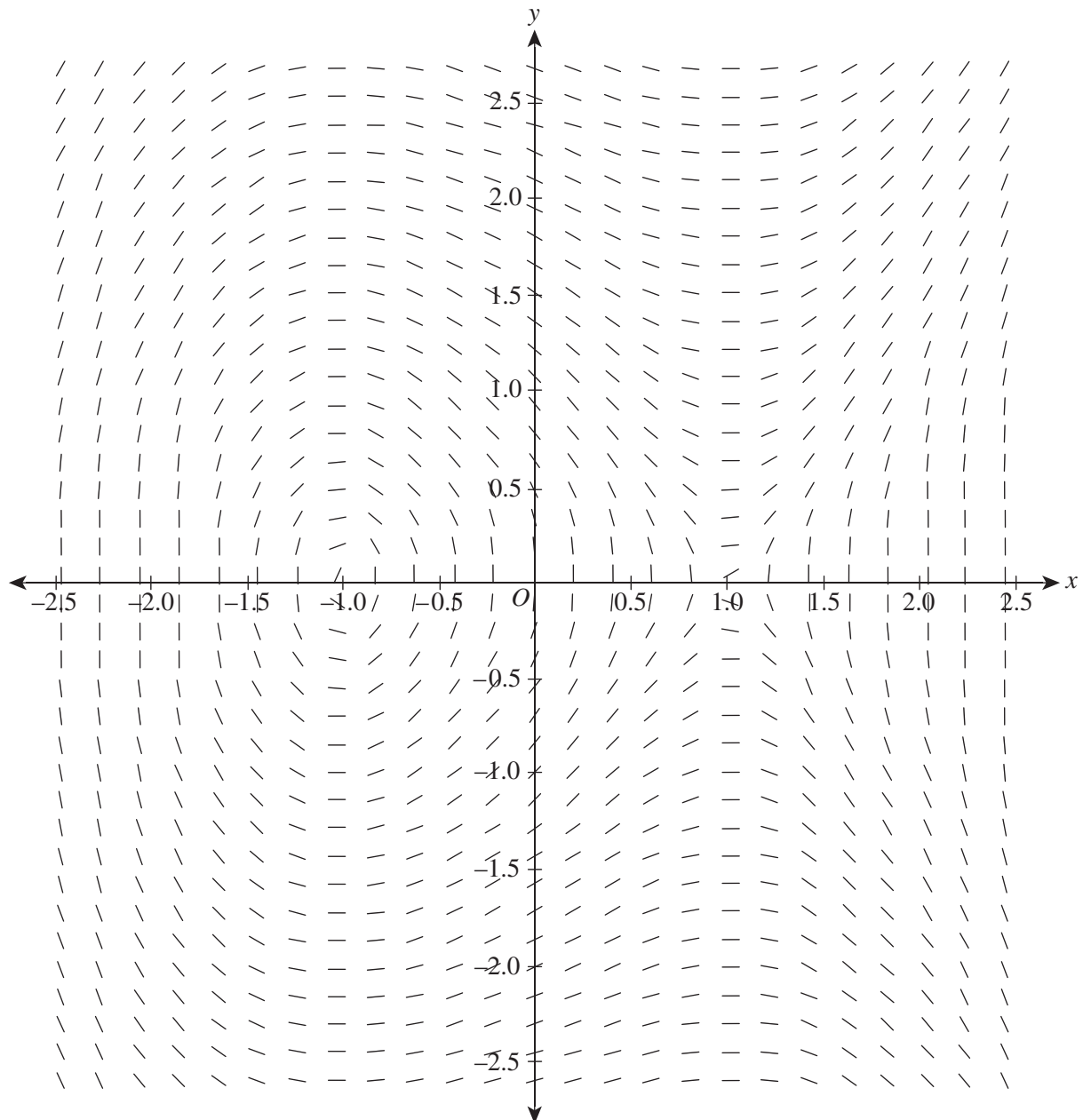
[illegible]

- b.** Find the area of triangle ABC . 2 marks

This image shows a single sheet of white paper with horizontal blue or grey ruling lines. The lines are evenly spaced and run across the width of the page. There are approximately 20 lines visible. The paper has a slight shadow on the right side, suggesting it's resting on a surface.

Question 10 (8 marks)

A direction field representing the differential equation $\frac{dy}{dx} = \frac{x^2 - 1}{y}$ is shown below.



- a. On the direction field above, sketch the solution curve of the differential equation given that $y(0) = 2$.

2 marks

- in the form $ay^2 = bx^3 + cx + d$, where a, b, c and d are integers.

This image shows a blank sheet of white paper with horizontal ruling lines. The lines are evenly spaced and extend across the width of the page. There are no margins, text, or other markings on the paper.

