## Papers written by Australian Maths Software

#### **SEMESTER TWO**

**YEAR 11** 

# MATHEMATICS METHODS Units 1 & 2 REVISION 1 2016

### Section One (Calculator-free)

| Teacher:                      |  |
|-------------------------------|--|
| TIME ALLOWED FOR THIS SECTION |  |

5 minutes

50 minutes

#### MATERIAL REQUIRED / RECOMMENDED FOR THIS SECTION

#### To be provided by the candidate

Working time for section:

Standard items: pens, pencils, pencil sharpener, highlighter, eraser, ruler.

#### **IMPORTANT NOTE TO CANDIDATES**

Reading time before commencing work:

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised notes or other items of a non–personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

#### To be provided by the supervisor

Question/answer booklet for Section One.

A formula sheet which may also be used for Section Two.

#### Structure of this examination

|                                | Number of questions available | Number of questions to be answered | Working time (minutes) | Marks<br>available | Percentage of exam |
|--------------------------------|-------------------------------|------------------------------------|------------------------|--------------------|--------------------|
| Section One<br>Calculator—free | 7                             | 7                                  | 50                     | 52                 | 35                 |
| Section Two Calculator—assumed | 12                            | 12                                 | 100                    | 98                 | 65                 |
| Total marks                    |                               |                                    |                        | 150                |                    |

#### Instructions to candidates

- 1. The rules for the conduct of this examination are detailed in the Information Handbook. Sitting this examination implies that you agree to abide by these rules.
- 2. Write your answer in the Question/Answer booklet.
- 3. You must be careful to confine your responses to the specific questions asked and to follow any instructions that are specific to a particular question.
- 4. Spare pages are provided at the end of this booklet. If you need to use them, indicate in the original answer space where the answer is continued i.e. give the page number.
- 5. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat an answer to any question, ensure that you cancel the answer you do not wish to have marked.
- 6. It is recommended that you **do not use pencil**, except in diagrams.
- 7. The Formula Sheet is **not** to be handed in with your Question/Answer booklet.

#### Section One: Calculator-free

52 marks

(3)

This section has **seven (7)** questions. Attempt **all** questions. Working time: 50 minutes

Question 1 (6 marks)

Given the function  $f(x) = x^3 + 1.5x^2 - 6x$ 

(a) Find the turning points of the function using calculus.

(b) <u>Sketch</u> the function below showing turning points and the y intercept. (3)

Question 2 (7 marks)

Solve the following equations using the indicated method.

(a) 
$$x^2 - 3x - 4 = 0$$
 by using the quadratic formula. (2)

(b) 
$$x^2 - 3x + 1 = 0$$
 by completing the square. Leave your answer in surds. (2)

(c) Factorise and hence solve 
$$x^3 + x^2 - 16x + 20 = 0$$
. (3)

2)

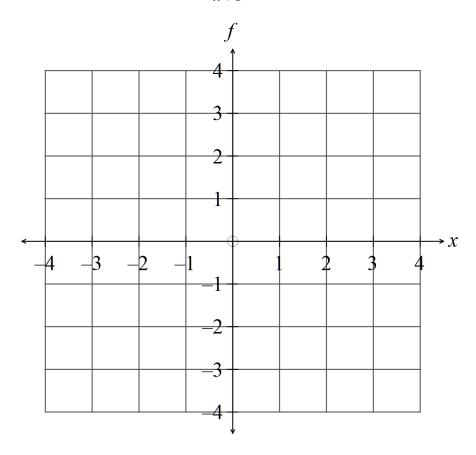
Question 3 (2 marks)

In how many ways can a debating team of one boy and two girls be selected from three boys and five girls?

Question 4 (14 marks)

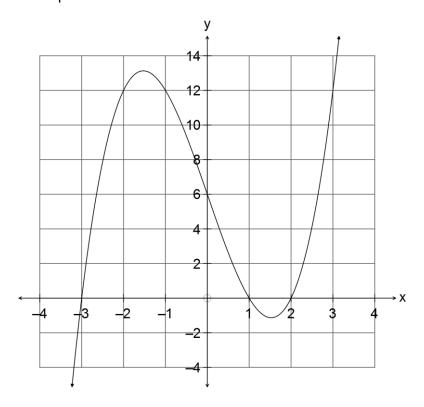
(a) Describe the features of the graph of the function 
$$g(x) = 2(x+2)^2 + 2$$
. (2)

(b) Sketch the function  $f(x) = -\frac{1}{x+1}$  on the set of axes below. (2)

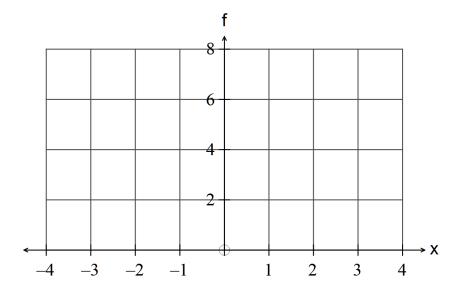


(c) Fully describe the relationship  $(x+2)^2 + (y-1)^2 = 4$ . (2)

(d) Determine the equation of the function shown on the set of axes below. (3)

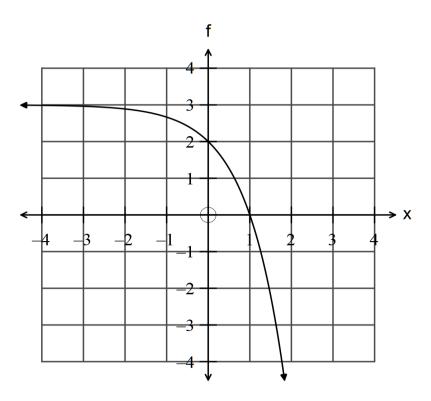


(e) Sketch the function  $f(x) = 2^{1-x}$  on the set of axes below. (2)



(3)

(f) Determine the equation of the function shown on the set of axes below.



Question 5 (10 marks)

(a) Simplify 
$$\frac{2 \times 8^{\frac{1}{3}} - 16^{0.25}}{81^{-\frac{3}{4}}}$$
 (2)

(b) Solve

(i) 
$$\frac{4^{1-2x}}{8^x} = 16$$
 (2)

(3)

(ii) 
$$3^{2x} - 12(3^x) + 3^3 = 0$$

(c) If 
$$a = 4.6 \times 10^2$$
,  $b = 2.3 \times 10^{-2}$  and  $c = 4 \times 10^{-4}$  evaluate  $\frac{a \times \sqrt{c}}{b}$ . (2)

(d) Little Johnny estimated the number of amoeba in a Petra dish to be 6 123 798 432. His teacher said it was impossible to measure amoeba that accurately and asked him to round his number down to two significant figures and use standard form.

What should little Johnny's answer be now?



(1)

Question 6 (6 marks)

- (a) Given the rule  $A_n = 1 + 3n$ ,
  - (i) write down the first four terms.

(2)

(ii) rewrite the rule recursively.

(2)

(b) Given the recursive definition  $T_{n+1}=2T_n$  with  $T_1=3$  , rewrite the expression in terms of n .

(2)

Question 7 (7 marks)

(a) Evaluate 
$$sin\left(\frac{\pi}{6}\right) + sin^2\left(\frac{\pi}{6}\right) + sin^3\left(\frac{\pi}{6}\right) + \dots$$
 (3)

- (b) Given  $P(A \cap B) = 0.2$ , P(A) = 0.3 and P(B) = 0.5 find
  - (i)  $P(A \cup B)$ .

(ii)  $P(A \mid B)$ . (2)

#### **END OF SECTION ONE**