



WA Exams Practice Paper E, 2016

Question/Answer Booklet

MATHEMATICS SPECIALIST UNIT 3

Section One: Calculator-free

If required by your examination administrator, please
place your student identification label in this box

Student Number: In figures

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In words

Your name

Time allowed for this section

Reading time before commencing work: five minutes

Working time for section: fifty minutes

Materials required/recommended for this section

To be provided by the supervisor

This Question/Answer Booklet

Formula Sheet

To be provided by the candidate

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items: nil

Important note to candidates

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised notes or other items of a non-personal nature in the examination room. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

Structure of this paper

Section	Number of questions available	Number of questions to be answered	Working time (minutes)	Marks available	Percentage of exam
Section One: Calculator-free	7	7	50	53	35
Section Two: Calculator-assumed	12	12	100	97	65
Total				150	100

Instructions to candidates

1. The rules for the conduct of examinations are detailed in the school handbook. Sitting this examination implies that you agree to abide by these rules.
2. Write your answers in this Question/Answer Booklet.
3. You must be careful to confine your response to the specific question asked and to follow any instructions that are specified to a particular question.
4. Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.
 - Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
 - Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number. Fill in the number of the question that you are continuing to answer at the top of the page.
5. **Show all your working clearly.** Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
6. It is recommended that you **do not use pencil**, except in diagrams.
7. The Formula Sheet is **not** to be handed in with your Question/Answer Booklet.

Section One: Calculator-free**35% (53 Marks)**

This section has **seven (7)** questions. Answer **all** questions. Write your answers in the spaces provided.

Working time for this section is 50 minutes.

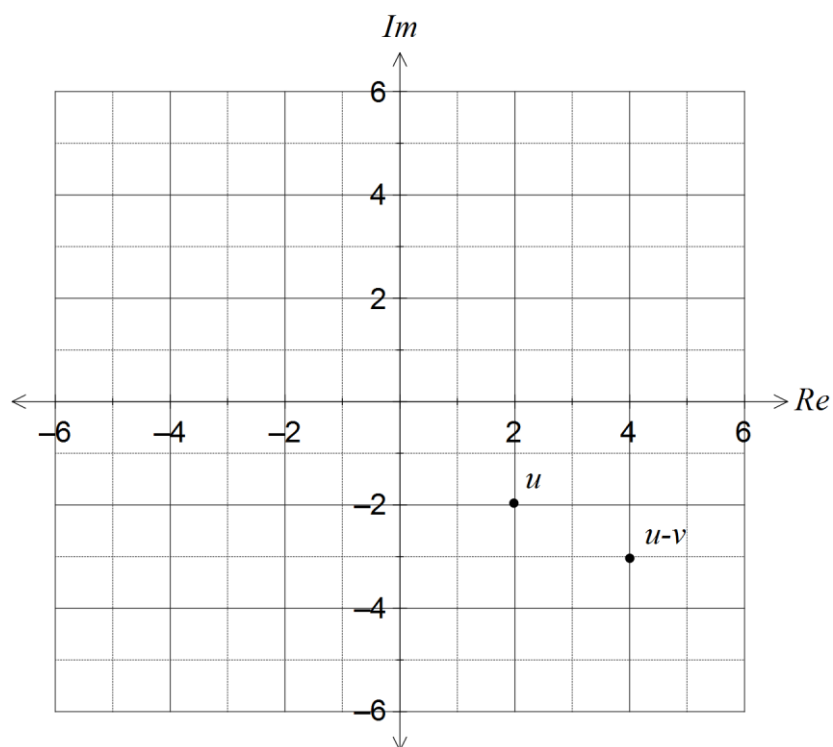
Question 1**(5 marks)**

Determine the vector equation of the plane passing through the three points $(-1, 1, 2)$, $(2, 2, 1)$ and $(1, 2, 3)$.

Question 2

(6 marks)

The Argand diagram below shows the complex numbers u and $u - v$.



On the same diagram plot and label the four complex numbers given by v , w , x and y , where

$$w = 2i - 2 + u - v, \quad x = \frac{5u}{v} \quad \text{and} \quad y = i^2 uv.$$

Question 3

(8 marks)

Two complex numbers are given by $w = 2cis\frac{\pi}{3}$ and $z = \sqrt{3} - i$.

(a) Express in polar form

(i) z . (1 mark)

(ii) $w \cdot z$. (1 mark)

(b) State the

(i) argument of $\frac{z}{w}$. (1 mark)

(ii) modulus of $\frac{1}{z}$. (1 mark)

(c) Show that the product $w \cdot \bar{w}$ is purely real. (2 marks)

(d) For what positive values of n is v_n purely real, given $v_{n+1} = v_n \times w$, $v_1 = w$? (2 marks)

Question 4

(10 marks)

The function f is defined by $f(x) = \frac{x^2 - 6x + 9}{x - 2}$.

The first derivative of f is $f'(x) = \frac{x^2 - 4x + 3}{(x - 2)^2}$.

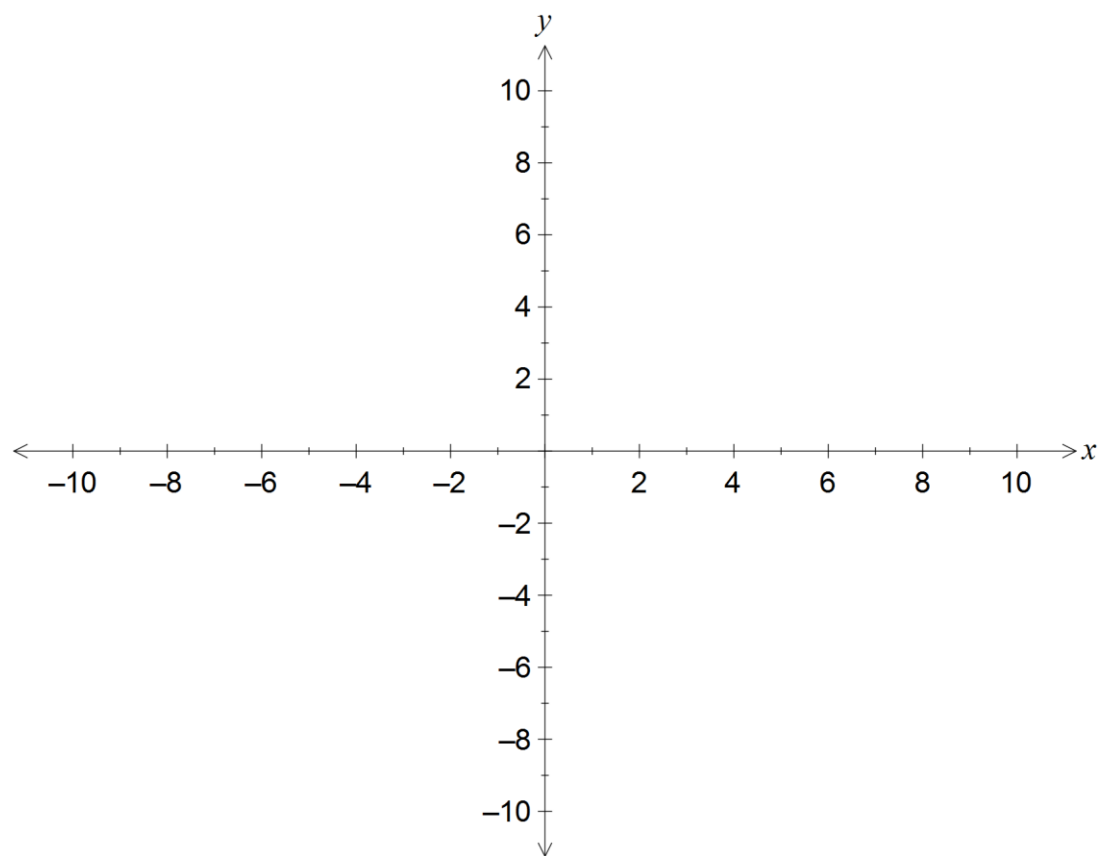
(a) State the coordinates of the y -axes intercept. (1 mark)

(b) Determine the coordinates of the stationary points of the graph of $y = f(x)$. (3 marks)

(c) Determine the equations of all asymptotes of the graph of $y = f(x)$. (3 marks)

(d) Sketch the graph of $y = f(x)$ on the axes below.

(3 marks)



Question 5

(9 marks)

Consider the function defined by $f(x) = \frac{1}{2x-1}$.

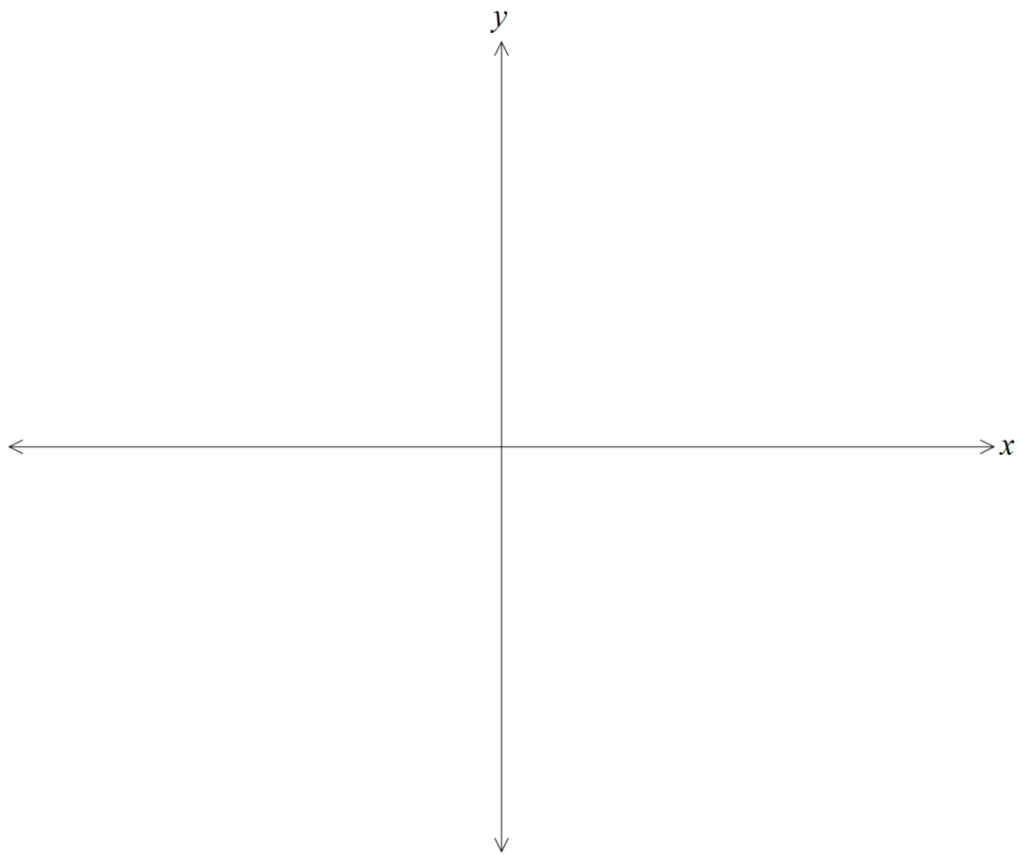
(a) State the natural domain for the function $f(x)$. (1 mark)

(b) Determine the inverse of $f(x)$. (2 marks)

(c) Determine the composite function $f \circ f(x)$, expressing your answer as a single rational function. (3 marks)

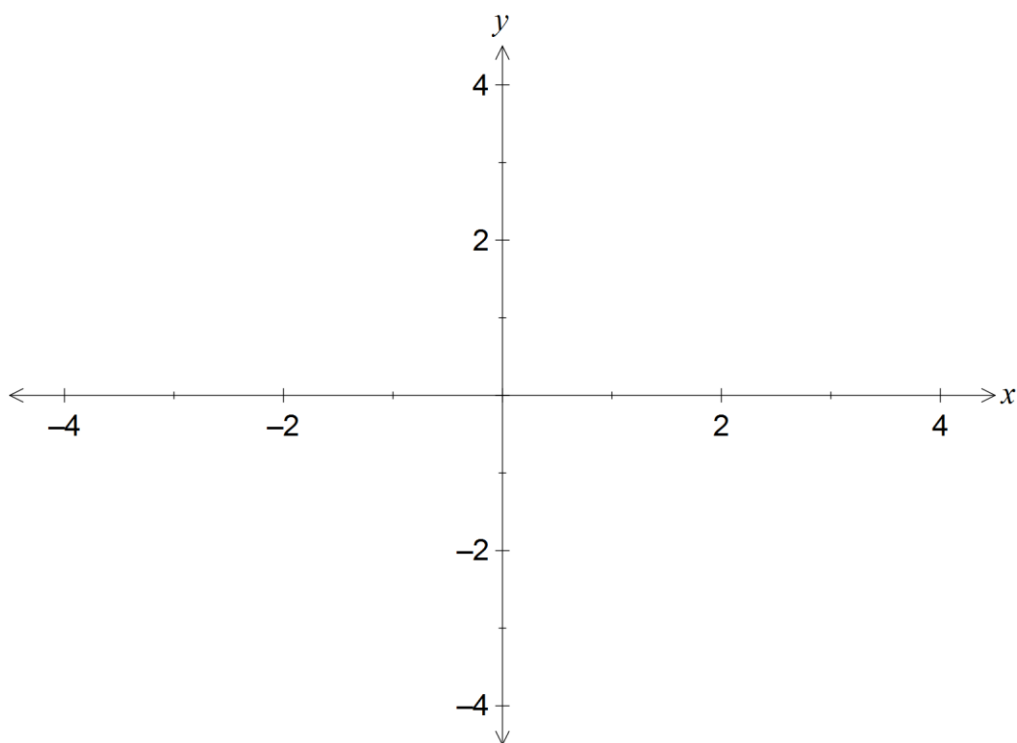
(d) Sketch the graph of $y = f \circ f(x)$ on the axes below.

(3 marks)



Question 6**(7 marks)**

On the axes below sketch the graphs of $y = 2 - |x + 1|$ and $y = |3x + 2|$, and hence solve the inequality $2 - |x + 1| > |3x + 2|$.



Question 7

(8 marks)

- (a) Two factors of $x^3 + ax^2 + bx + c$ are $x - 2$ and $x + 1 + 2i$. Determine the values of the real constants a , b and c . (3 marks)

- (b) Consider $g(z) = 2z^3 - 10z^2 + 34z - 26$, $z \in \mathbb{C}$. Solve $g(z) = 0$ over \mathbb{C} . (5 marks)

Additional working space

Question number: _____

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