

# AI1110 Assignment 1

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## Question 4a

Solve the following inequation, write down the solution set and represent it on the real number line:

$$-2 + 10x \leq 13x + 10 < 24 + 10x, x \in \mathbb{Z}$$

## Solution

$$-2 + 10x \leq 13x + 10 < 24 + 10x, x \in \mathbb{Z}$$

Let us solve the above expression geometrically.

now consider each equation in this expression as a line equation

$$y_1 = 10x - 2$$

$$y_2 = 13x + 10$$

$$y_3 = 10x + 24$$

clearly slopes of  $y_1$  and  $y_3$  are same i.e.,  $slope = 10$

and  $y_1 \leq y_2 < y_3$ , so the integral values of  $x$  on  $x$ -axis satisfying this inequality are the required solution set

so we need to find the range of  $x$  at where the line  $y_2$  lies between between line  $y_1$  and the line  $y_3$

We can obtain the  $x$  value at intersection point of  $y_1$  and  $y_2$  by equating them that is,

$$y_1 = y_2$$

$$\Rightarrow 10x - 2 = 13x + 10$$

$$\Rightarrow -10 - 2 = 13x - 10x$$

$$\Rightarrow -12 = 3x$$

$$\Rightarrow x = -4$$

Similary we get the  $x$  value at intersection point of  $y_2$  and  $y_3$  by equating  $y_2$  and  $y_3$

$$y_3 = y_2$$

$$\Rightarrow 10x + 24 = 13x + 10$$

$$\Rightarrow 24 - 10 = 13x - 10x$$

$$\Rightarrow 14 = 3x$$

$$\Rightarrow x = 4.67$$

Since  $y_1 \leq y_2 < y_3$ , this implies  $-4 \leq x < 4.67$

Now let us draw the corresponding lines

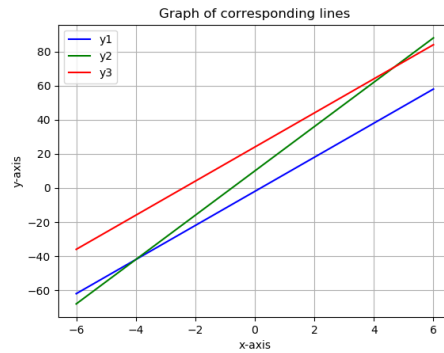


Figure 1: lines  $y_1$ ,  $y_2$  and  $y_3$

If we observe this graph, it is clear that the lines  $y_1$  and  $y_2$  are intersecting at  $x = -4$  and the lines  $y_2$  and  $y_3$  are intersecting at some point where  $x > 4$

Hence the required range of  $x$  is  $[4, 4.67)$

Therefore the integers in this range are,

$$\{-4, -3, -2, -1, 0, 1, 2, 3, 4\}$$

here is the plot of corresponding points on the real number line

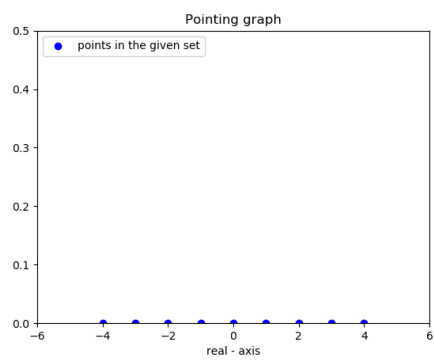


Figure 2: set of points that obey given expression on real number line