

Date=19/08/2020

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Subject ⇒ Revision of Heaps

IN PREVIOUS LECTURE (QUICK RECAP) Date-18/08/2020	In Today's Lecture (Overview)
⇒ Heaps in Python ⇒ MCQS ⇒ Questions for self Practice // CC for the day	Heapify in Heap Types of Heaps Minimum Heap Maximum Heap Questions For Self Practice // Assignment for the Day

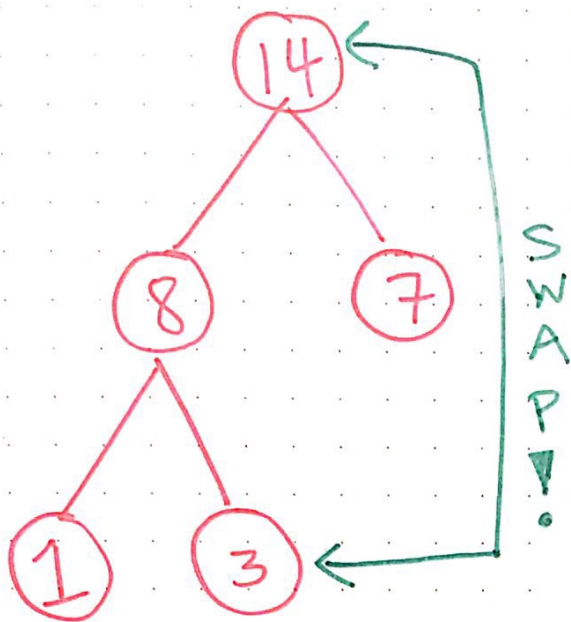
Heapify in Heap

Heapify is the process of converting a binary tree into a Heap data structure. A binary tree being a tree data structure where each node has at most two child nodes. A Heap must be a complete binary tree, that is each level of the tree is completely filled

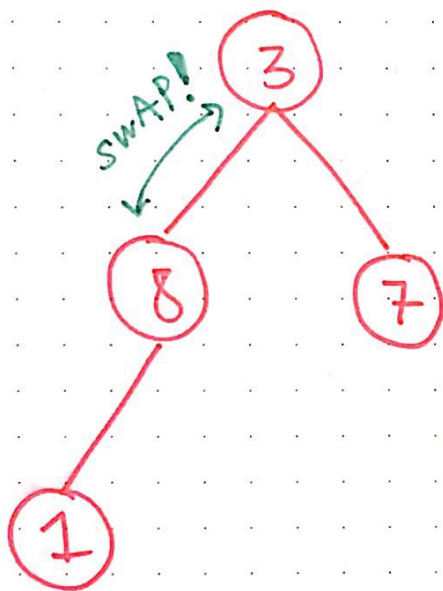
This function converts a regular list to a heap.

In the resulting heap the smallest element gets pushed to the index position 0.

But the rest of the data elements are not necessarily sorted.



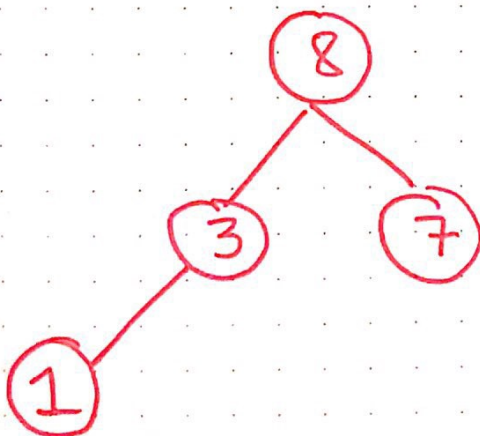
* Once we are back in a max heap state, we can continue repeating the same steps until we are left with a heap size of 1:



→ swap first + last elements.

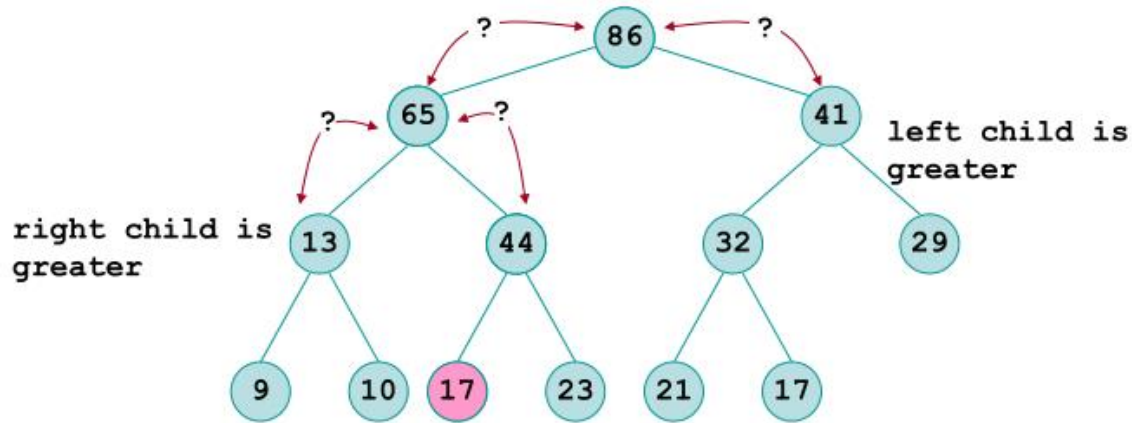
→ remove last node as it is already in its sorted position in the array.

→ heapify until back at a max heap state.



0	1	2	3	4	5
8	3	7	1	14	19

Max-Heapify Example



children of 2002*22*2*22*1*14 = 8, 3

index	1	2	3	4	5	6	7	8	8	10	11	12
value	86	65	41	13	44	32	29	9	10	17	23	21

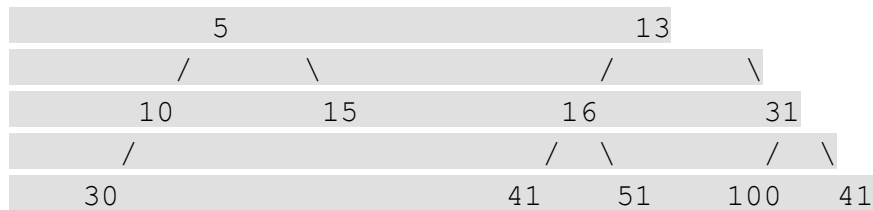
Types of Heaps

Minimum Heap

A Min-heap is a complete binary tree in which the value in each internal node is smaller than or equal to the values in the children of that node.

Mapping the elements of a heap into an array is trivial: if a node is stored a index k , then its left child is stored at index $2k + 1$ and its right child at index $2k + 2$.

Example of Min Heap :



How is Min Heap represented ?

A Min Heap is a Complete Binary Tree. A Min heap is typically represented as an array.

The root element will be at **Arr[0]**. For any *i*th node, i.e., **Arr[i]**:

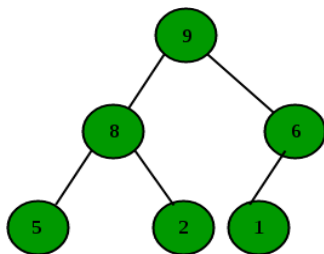
- **Arr[(i - 1) / 2]** returns its parent node.
- **Arr[(2 * i) + 1]** returns its left child node.
- **Arr[(2 * i) + 2]** returns its right child node.

Maximum Heap

A Max-heap is a complete binary tree in which the value in each internal node is greater than or equal to the values in the children of that node.

Mapping the elements of a heap into an array is trivial: if a node is stored a index *k*, then its left child is stored at index **2*k* + 1** and its right child at index **2*k* + 2**.

Examples of Max Heap :



How is Max Heap represented ?

A Max Heap is a Complete Binary Tree. A Max heap is typically represented as an array.

The root element will be at $\text{Arr}[0]$. Below table shows indexes of other nodes for the i th node, i.e., $\text{Arr}[i]$:

$\text{Arr}[(i-1)/2]$ Returns the parent node.

$\text{Arr}[2*i+1]$ Returns the left child node.

$\text{Arr}[2*i+2]$ Returns the right child node.

Questions For Self Practice // Assignment for the Day

Q 1-> Design a heap with Heapify method