

Derivates of BFS & DFS

1) Algorithm Explores the graph

→ (BFS):- BFS explores the graph level by level. it begins at a source vertex, visit all neighbours. then moves to neighbour to those neighbours & continue until all reachable vertices are visited.

→ (DFS):- Explores the graph in depth-oriented manner, starting from a source. it follows one path as possible before backtracking and explores unvisited vertices.

2) Data Structure used:-

→ BFS:- Use a queue (FIFO) to maintain the order of vertices to be visited array/set to mark explored vertices.

→ DFS:- Use stack and a visited array/set to mark explored vertices.

3) Derivation of Time complexity

(BFS):- Each vertex is enqueued and dequeued once → $O(N)$ operation every vertex. all its adjacency list edges traversed across the graph edge once → $O(E)$ operations. hence time complexity $O(N+E)$

(DFS):- Each vertex pushed popped from stack, most one operation, each adjacency scanned once. & every edge exactly once → $O(E)$ operation hence space time complexity $O(N+E)$

4) Derivation of space complexity

(BFS):- Queue store up to $O(N)$ vertices, visited array requires $O(N)$ and adjacency list requires $O(N+E)$ total space = $O(N+E)$

(DFS):- Recursion stack can go deep as $O(N)$, visited array $O(N)$ adjacency list requires $O(N+E)$ total space = $O(N+E)$

5) sparse vs Dense graph compare

→ sparse graph ($E = O(N)$) → BFS and DFS take $O(N)$

→ Dense graph ($E = O(N^2)$) → BFS and DFS take $O(N^2)$