

Neural Networks and Deep Learning

Generative Models II

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A GAN is a zero-sum game between two adversaries, a generator (G) and a discriminator (D).

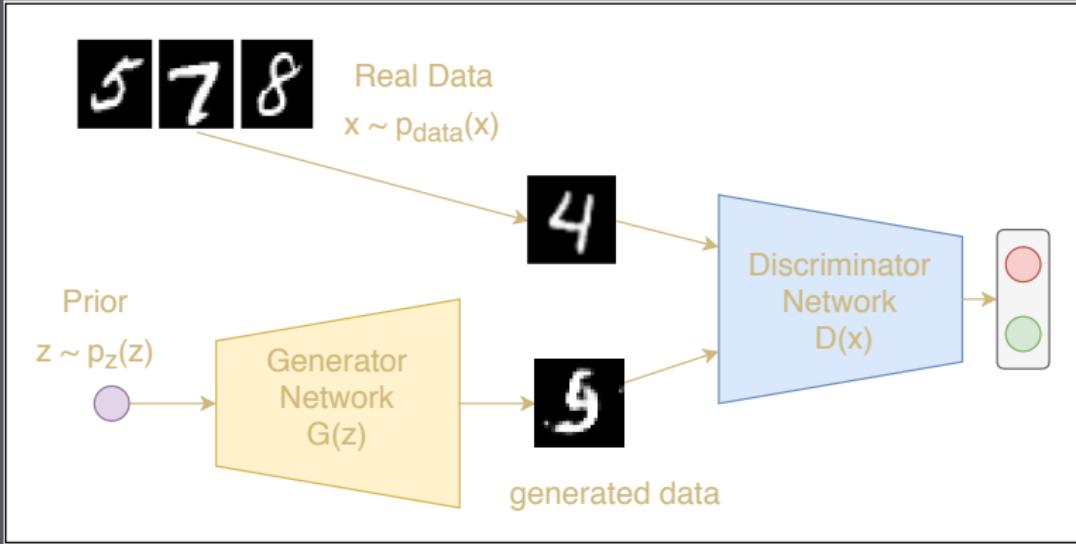
G generates samples from a learned distribution p_G and tries to trick D into believing they are from p_{data} , the true data distribution.

D tries not to be deceived.

	Generator	Discriminator
Input	A random vector	A sample from p_G or p_{data}
Output	Sample generated from p_G	Probability that input $\sim p_{data}$
Task	Make p_G close to p_{data}	Distinguish between p_G and p_{data}

G and D are neural networks – typically, though not necessarily, ConvNets.





Generative Adversarial Networks [Mark Chang](#)



Within a training iteration, repeat the following k times to optimize the weights of the discriminator D .

Given

- a minibatch of m noise samples $\{ \mathbf{z}^{(1)}, \mathbf{z}^{(2)}, \dots, \mathbf{z}^{(m)} \}$ from noise prior $p_g(\mathbf{z})$, and
- a minibatch of m examples from $\{ \mathbf{x}^{(1)}, \mathbf{x}^{(2)}, \dots, \mathbf{x}^{(m)} \}$ from data generating distribution $p_{data}(\mathbf{x})$

update D with gradient *ascent*:

$$\nabla_{d_\theta} \frac{1}{m} \sum_{i=1}^m \left[\log D\left(\mathbf{x}^{(i)}\right) + \log\left(1 - D\left(G\left(\mathbf{z}^{(i)}\right)\right)\right) \right].$$



Within a training iteration, do the following *once* to optimize the weights of the generator G .

Given a minibatch of m noise samples $\{ \mathbf{z}^{(1)}, \mathbf{z}^{(2)}, \dots, \mathbf{z}^{(m)} \}$ from noise prior $p_g(\mathbf{z})$, update G with gradient *descent*:

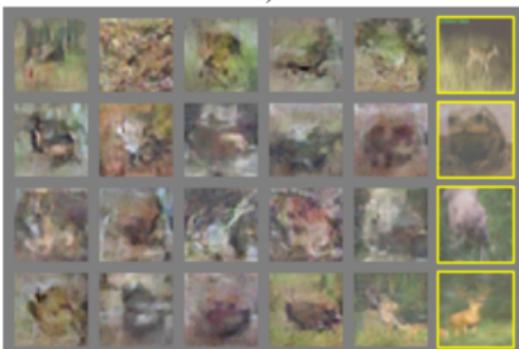
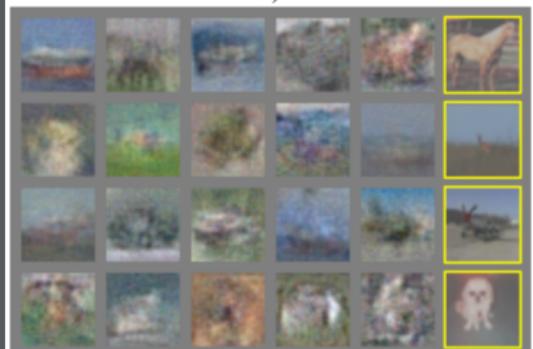
$$\nabla_{g_\theta} \frac{1}{m} \sum_{i=1}^m \log\left(1 - D\left(G\left(\mathbf{z}^{(i)}\right)\right)\right).$$



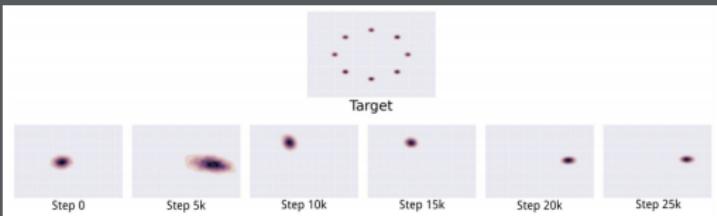
$$\min_G \max_D V(D, G) = \mathbb{E}_{x \sim P_{data}}[\log D(x)] + \mathbb{E}_{z \sim P_{noise}}[\log(1 - D(G(z)))]$$



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- Non-convergence - in the zero-sum game played by the generator and discriminator, the equilibrium can be evasive. The progress made by one player may, in turn and repeatedly, be undone by the other player.
- Mode collapse, mode dropping. Real data are multimodal. Mode collapse occurs when the generator settles into a state where it outputs samples from one or a small number of modes. The effect is that the generator creates samples that are far less diverse than those found in the real data.



Goodfellow, 2016



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It is common to add noise during training of generative models.



How does noise affect the manifolds?

Manifolds of p_{data} and p_g



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It is common to add noise during training of generative models.



Manifolds of p_{data} and p_g



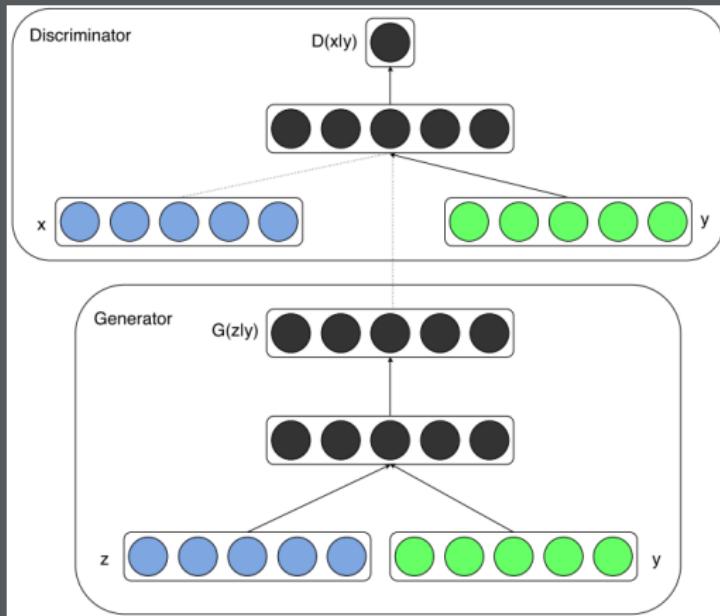
Manifolds of p_{data} and p_g with noise



- Eliminates lack of common support between p_{data} and p_g .
- Makes D perform worse (initially), so gradients of D are non-zero
- Ensures that KL-divergence is defined and the GAN convergence proof holds (modulo comment at end of original GAN proof)

See [Sonderby et al, 2017](#)

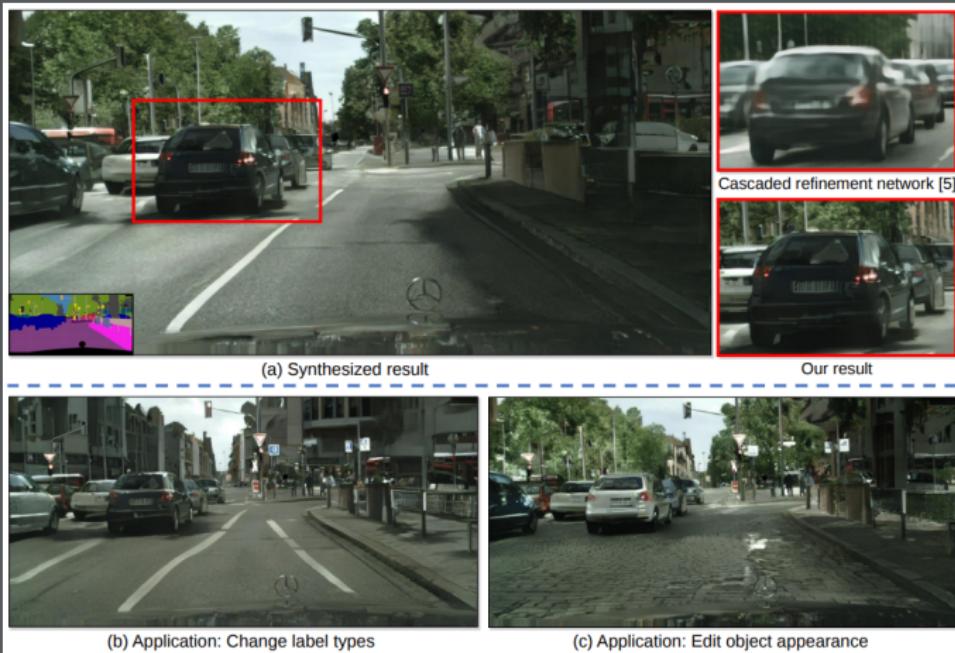




Mizra and Osindero, 2014



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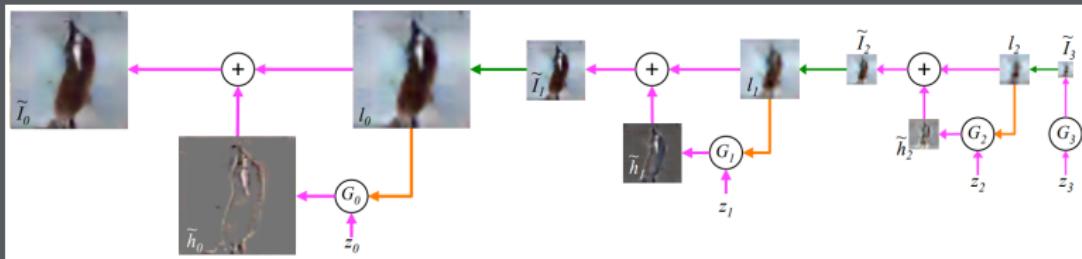


Wang et al, 2018



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First flavor of GANs to scale to “high resolution” images (64×64).



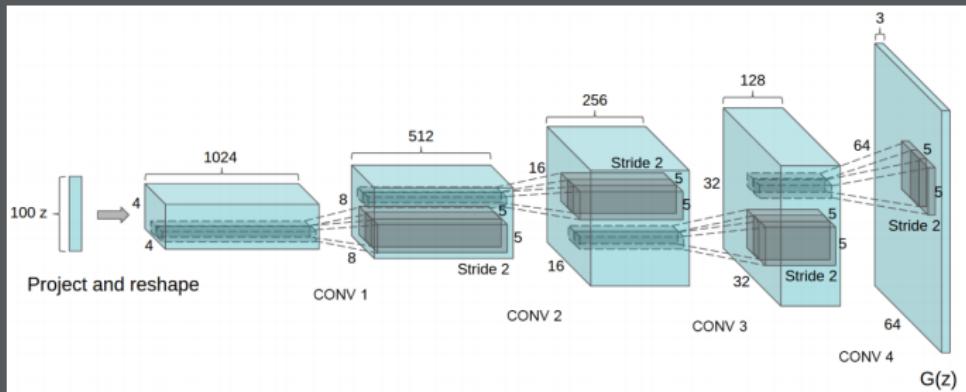
Sampling procedure for LAPGAN [Denton et al, 2015](#)



Training procedure for LAPGAN [Denton et al, 2015](#)



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Generator for deep convolutional generative adversarial network [Radford et al., 2015](#)

Increase quality of generator G , by

- adding batch normalization layers to G and D
- optimizing using Adam instead of SGD





Generated bedrooms after one training pass through the dataset [Radford et al., 2015](#)



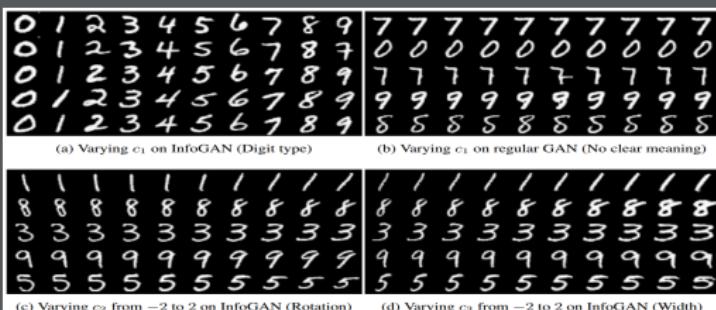
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GAN loss

$$\min_G \max_D V(D, G) = \mathbb{E}_{x \sim P_{data}} [\log D(x)] + \mathbb{E}_{z \sim P_{noise}} [\log(1 - D(G(z)))]$$

InfoGAN loss

$$\min_G \max_D V_I(D, G) = V(D, G) - \lambda I(c; G(z, c))$$



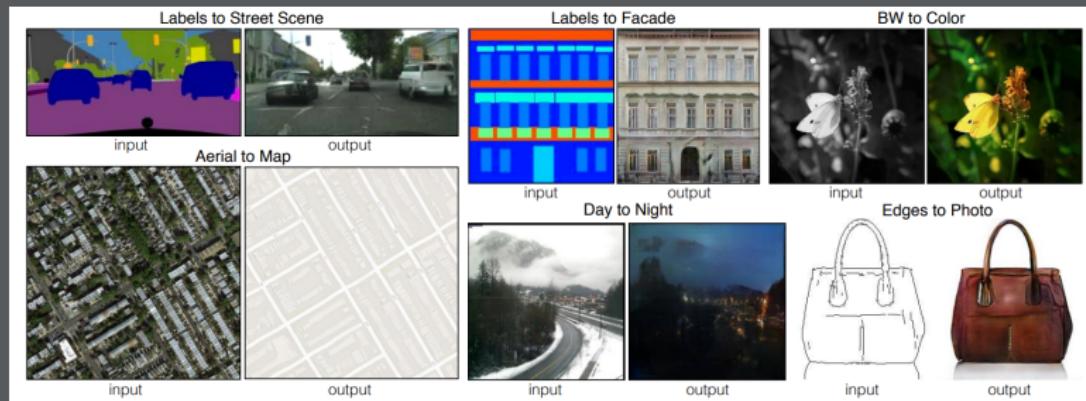
Chen et al, 2016



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Image-to-image translation using conditional GANs and paired images.

An online [demo](#) illustrates the basic approach well – particularly the building facades.

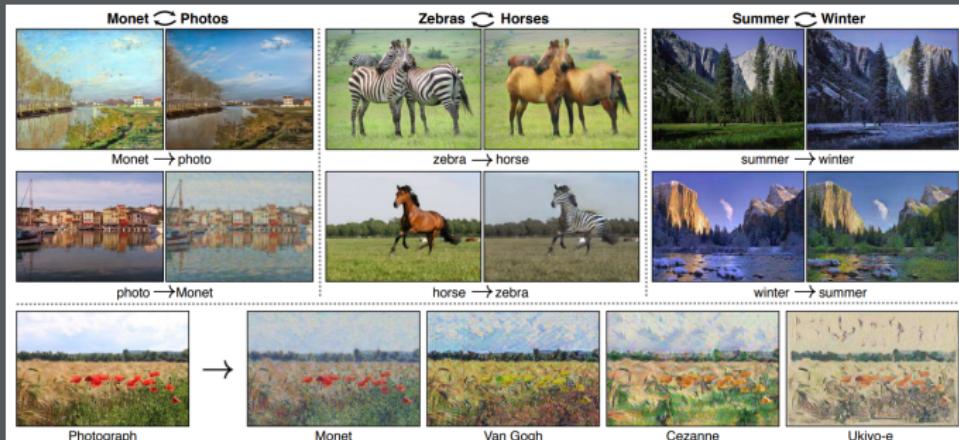


[Isola et al, 2016](#)



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In CycleGAN, the authors use the GAN framework and corpora of unpaired images to learn to translate salient features between domains.

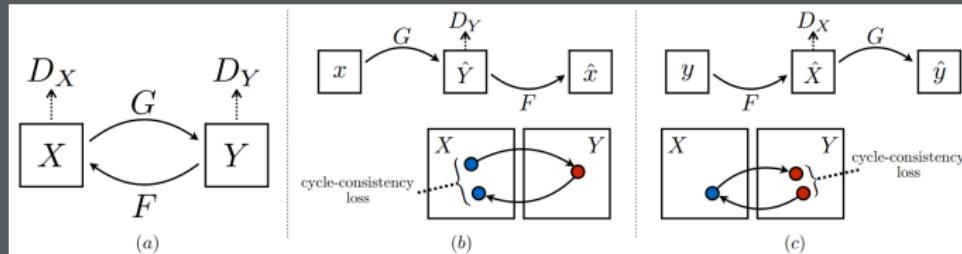


Zhu et al, 2017



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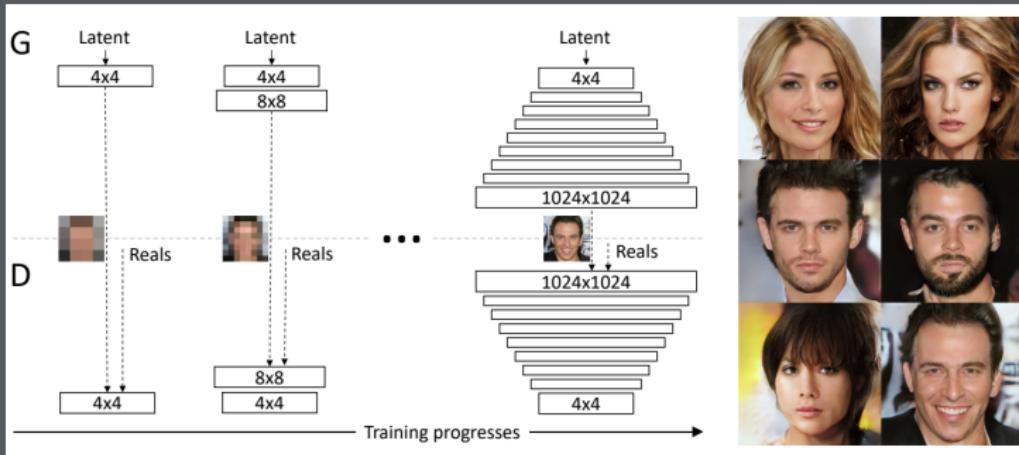
The pair of generators G and F map between domains (i.e. $G : X \rightarrow Y$ and $F : Y \rightarrow X$).



Zhu et al, 2017

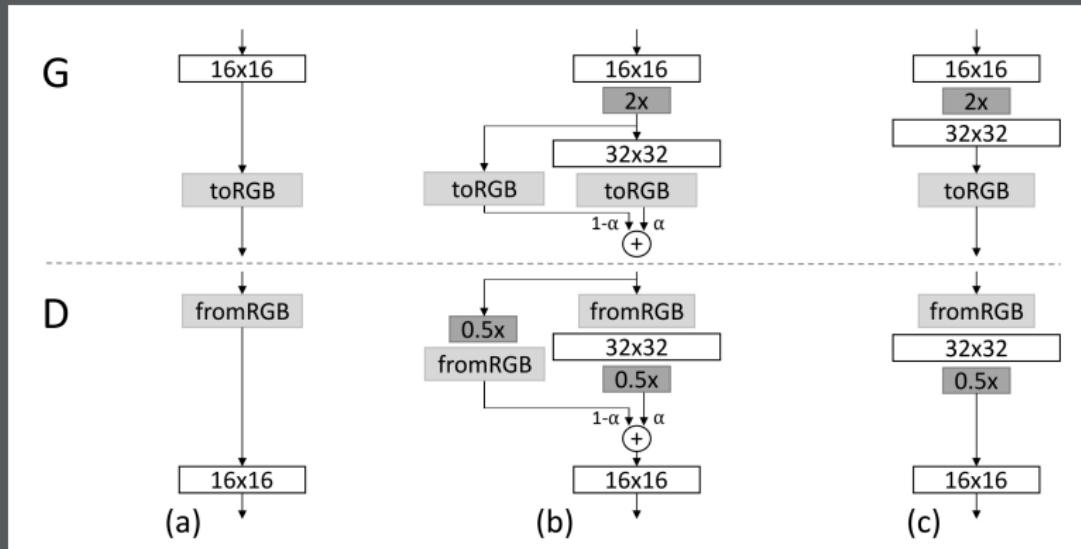
The study showed by ablation that a cycle consistency loss that ensured $F(G(X)) \sim X$ and $(G(F(Y)) \sim Y$ substantially improved the quality of generated images.

Progressively adding layers of the generator and discriminator allows scaling up to images of size 1024×1024 .



Training starts with both the generator (G) and discriminator (D) having a low spatial resolution of 4×4 pixels. As the training advances, we incrementally add layers to G and D, thus increasing the spatial resolution of the generated images. All existing layers remain trainable throughout the process. [Karras et al, 2017](#)

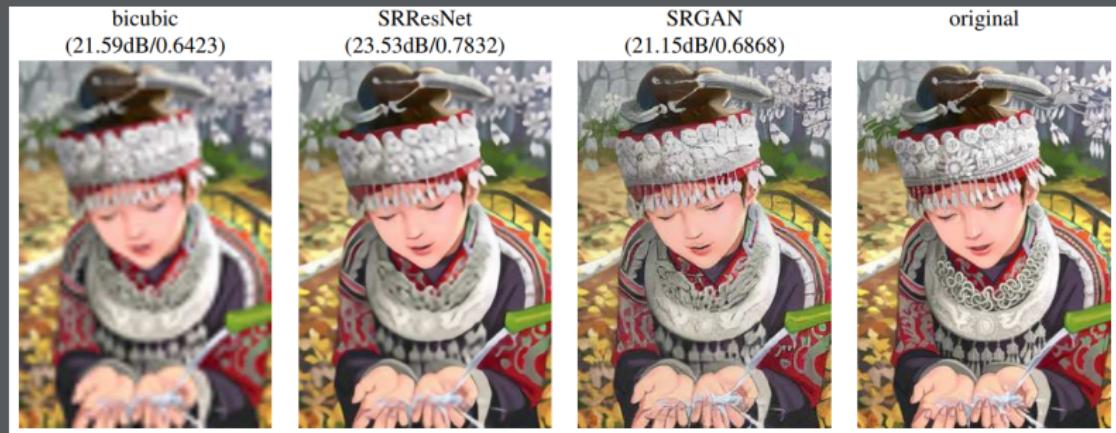




Karras et al, 2017



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Ledig et al, 2017

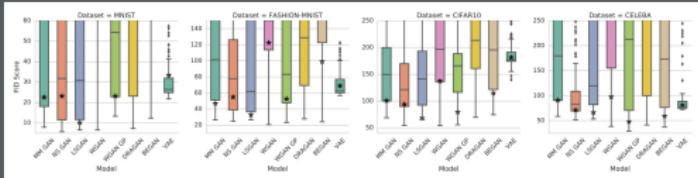


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Some methods for measuring generator quality. See [Lucic et al, 2018](#).

- *Inception Score* takes into account the entropy of the distribution of labels (i.e. softmax output) of generated samples ($p(y|x)$) and the variance of the classes using an Inception model trained on ImageNet.
- *Fréchet Inception Distance* is the Fréchet distance between two multivariate Gaussians, $\mathcal{N}(\mu_x, \Sigma_x)$ and $\mathcal{N}(\mu_g, \Sigma_g)$, where the parameters of the distributions are estimates from the Inception embeddings of the real and generated data.





Sensitivity of GANs to hyperparameters [Lucic et al, 2018](#)

	MNIST	FASHION	CIFAR	CELEBA
MM GAN	9.8 ± 0.9	29.6 ± 1.6	72.7 ± 3.6	65.6 ± 4.2
NS GAN	6.8 ± 0.5	26.5 ± 1.6	58.5 ± 1.9	55.0 ± 3.3
LSGAN	$7.8 \pm 0.6^*$	30.7 ± 2.2	87.1 ± 47.5	$53.9 \pm 2.8^*$
WGAN	6.7 ± 0.4	21.5 ± 1.6	55.2 ± 2.3	41.3 ± 2.0
WGAN GP	20.3 ± 5.0	24.5 ± 2.1	55.8 ± 0.9	30.0 ± 1.0
DRAGAN	7.6 ± 0.4	27.7 ± 1.2	69.8 ± 2.0	42.3 ± 3.0
BEGAN	13.1 ± 1.0	22.9 ± 0.9	71.4 ± 1.6	38.9 ± 0.9
VAE	23.8 ± 0.6	58.7 ± 1.2	155.7 ± 11.6	85.7 ± 3.8

Best performance of GANs on various datasets [Lucic et al, 2018](#)

