

Assignment 2:

18K41A04D2

Find the global minimum point and value for the function $f(x,y) = x^2 + y^2 + 10$.

Step 1: $x = -1$, $y = 1$, $\eta = 0.1$, epochs = 2.

Step 2: iter = 1

Step 3: $\frac{\partial f}{\partial x} = 2x = 2$

$$\frac{\partial f}{\partial y} = 2y = 2$$

Step 4: $\Delta x = -\eta \cdot \frac{\partial f}{\partial x} = -(0.1)(2) = -0.2$

$$\Delta y = -\eta \frac{\partial f}{\partial y} = -(0.1)(2) = -0.2$$

Step 5: $x = x + \Delta x = -1 + 0.2 = -0.8$

$$y = y + \Delta y = 1 - 0.2 = 0.8$$

Step 6: iter = iter + 1 = 1 + 1 = 2

Step 7: if (iter > epochs)
2 \neq 2
goto step 3

Step 3: $\frac{\partial f}{\partial x} = 2x = 2(-0.8) = -1.6$

$$\frac{\partial f}{\partial y} = 2y = 2(0.8) = 1.6$$

Step 4: $\Delta x = -\eta \frac{\partial f}{\partial x} = -(0.1)(-1.6) = 0.16$

$$\Delta y = -\eta \frac{\partial f}{\partial y} = -(0.1)(1.6) = -0.16$$

step 5: $x = x + \Delta x = -0.8 + 0.16 = -0.64$

$$y = y + \Delta y = 0.8 - 0.16 = 0.64$$

step 6: $iter = iter + 1 = 2 + 1 = 3$

step 7: $if (iter > epochs)$

$$3 > 2$$

goto next step

step 8: $x, y = -0.64, 0.64$

$$f(x, y) = x^2 + y^2 + 10$$

$$= (-0.64)^2 + (0.64)^2 + 10$$

$$f(x, y) = 10.81$$