



PARUL UNIVERSITY - FACULTY OF ENGINEERING & TECHNOLOGY

Department of Applied Science & Humanities

3rd Semester B. Tech (CSE, IT)

Discrete Mathematics (203191202)

Tutorial-3(A) Propositional Logic

Q.1.	Which of these sentences are propositions? What are the truth values of those that are propositions? a) Boston is the capital of Massachusetts. b) Miami is the capital of Florida. c) $2 + 3 = 5$. d) $5 + 7 = 10$. e) $x + 2 = 11$. f) Answer this question.
Q.2	What is the negation of each of these propositions? a) Jennifer and Teja are friends. b) There are 13 items in a baker's dozen. c) 121 is a perfect square. d) Abby sent more than 100 text messages everyday.
Q.3	Suppose that Smartphone A has 256MB RAM and 32GB ROM, and the resolution of its camera is 8 MP; Smartphone B has 288 MB RAM and 64 GB ROM, and the resolution of its camera is 4 MP; and Smartphone C has 128 MB RAM and 32 GB ROM, and the resolution of its camera is 5 MP. Determine the truth value of each of these propositions. a) Smartphone B has the most RAM of these three smartphones. b) Smartphone C has more ROM or a higher resolution camera than Smartphone B. c) Smartphone B has more RAM, more ROM, and a higher resolution camera than Smartphone A. d) If Smartphone B has more RAM and more ROM than Smartphone C, then it also has a higher resolution camera. e) Smartphone A has more RAM than Smartphone B if and only if Smartphone B has more RAM than Smartphone A.
Q.4	Let p and q be the propositions "The election is decided" and "The votes have been counted," respectively. Express each of these compound propositions as an English sentence. a) $\neg p$ b) $p \vee q$ c) $\neg p \wedge q$ d) $q \rightarrow p$ e) $\neg q \vee (\neg p \wedge q)$ f) $\neg p \rightarrow \neg q$ g) $p \leftrightarrow q$ h) $\neg q \rightarrow \neg p$
Q.5	Let p , q , and r be the propositions p : You get an A on the final exam. q : You do every exercise in this book. r : You get an A in this class. Write these propositions using p , q , and r and logical connectives (including negations). a) You get an A in this class, but you do not do every exercise in this book. b) You get an A on the final, you do every exercise in this book, and you get an A in this class. c) To get an A in this class, it is necessary for you to get an A on the final. d) You get an A on the final, but you don't do every exercise in this book; nevertheless, you get an A in this class. e) Getting an A on the final and doing every exercise in this book is sufficient for getting an A in this class. f) You will get an A in this class if and only if you either do every exercise in this book or you get an A on the final.

	Q.6	Construct a truth table for each of these compound propositions. a) $((p \rightarrow q) \rightarrow r) \rightarrow s$ b) $(p \wedge q) \rightarrow (p \vee q)$
	Q.7	Find the bitwise <i>OR</i> , bitwise <i>AND</i> , and bitwise <i>XOR</i> of each of these pairs of bit strings. a) 00 0111 0001, 10 0100 1000 b) 11 1111 1111, 00 0000 0000
	Q.8	a) Show that $\neg p \leftrightarrow q$ and $p \leftrightarrow \neg q$ are logically equivalent. b) Show that $\neg(p \oplus q)$ and $p \leftrightarrow q$ are logically equivalent.
	Q.9	Determine whether each of these compound propositions is satisfiable. a) $(p \vee \neg q) \wedge (\neg p \vee q) \wedge (\neg p \vee \neg q)$ b) $(p \vee q \vee r) \wedge (\neg p \vee \neg q \vee \neg r)$
	Q.10	Let $C(x)$ be the statement “ x has a cat,” let $D(x)$ be the statement “ x has a dog,” and let $F(x)$ be the statement “ x has a ferret.” Express each of these statements in terms of $C(x)$, $D(x)$, $F(x)$, quantifiers, and logical connectives. Let the domain consist of all students in your class. a) A student in your class has a cat, a dog, and a ferret. b) All students in your class have a cat, a dog, or a ferret. c) Some student in your class has a cat and a ferret, but not a dog. d) No student in your class has a cat, a dog, and a ferret. e) For each of the three animals, cats, dogs, and ferrets, there is a student in your class who has this animal as a pet.