

MEASUREMENTS

NOTES

Downloaded From www.gatenotes.in

GATE 2009

JANARDHANARAO

* SAT. 15/11/08 *

MEASUREMENTS

BASICS :

$$A_t = 10 \text{ A} \quad (\text{True value})$$

$$A_m = 9.8 \text{ A} \quad (\text{Measured value}).$$

$$\boxed{\text{static error} = A_m - A_t}$$

$$(8 \text{ A}) \quad = 9.8 - 10 = (-)0.2 \text{ A}$$

$$\text{static correction (SC)} = -8 \text{ A}$$

$$= -(-0.2) = 0.2 \text{ A}.$$

Correction is to be done for A_m to get A_t .

$$\begin{array}{l} 2 \text{ A} \pm 1 \text{ A} \\ \rightarrow 50\% \text{ error} \end{array} \left. \begin{array}{l} \text{not good} \\ \text{good} \end{array} \right\} }$$

$$\begin{array}{l} 1000 \text{ A} \pm 10 \text{ A} \\ \rightarrow 1\% \text{ error.} \end{array} \left. \begin{array}{l} \text{good.} \\ \text{good.} \end{array} \right\}$$

$$\boxed{\text{Relative static error} = \frac{A_m - A_t}{A_t}}$$

Accuracy :

It is a measure of closeness with which an instrument reading approaches the true value of the quantity being measured (Measurand).

Precision :

Reproducibility of measurements.

Measurand : quantity under measurement.

Sensitivity :-

It is the ratio of magnitude of output signal to the mag. of input signal under measurement.

Dead time :-

It is the time required by a measurement system to respond to change in the measurement.

dead time depends on damping factor selected

for meter range : 0.6 to 0.8. ($\xi < 1$
under damped
with $\xi, 0.6 \text{ to } 0.8$)
Dead zone :-

It is the largest change of imp quantity for which there is no o/p of the instr.

Resolution or Discrimination :-

The smallest increment in imp which can be detected with certainty by an instr. is known as Resolution.

$$R_1 = 1000 \Omega \pm 10\Omega \quad 990 \quad 1010$$

$$R_2 = 500 \Omega \pm 5\Omega \quad 495 \quad 505$$

$$R_1 + R_2 = 1500 \pm 15 \quad (990+495) \quad (1010+505)$$

$$R_1 - R_2 = 500 \pm 15 \quad 485 \quad 515 \quad (990-505) \quad (1010-495)$$

* Resultant error in addition & subtraction of quantity can be obtained by adding all individual errors. They should be expressed in absolute values.

$$V = 230V \pm 2\%$$

$$I = 10A \pm 1\%$$

$$P = 2300 \pm 3\% \quad (V \cdot I)$$

$$R = 23 \pm 3\% \quad \left(\frac{V}{I}\right)$$

* Resultant error in product & division of quantities can be obtained by adding all individual errors and they should be expressed in percentage values.

$$I = 10 \text{ A} \pm 2\%$$

$$R = 500 \Omega \pm 3\%$$

Then power $P = \frac{I^2 R}{}$

$$= \frac{50000 \pm [2 \times 2\% + 1 \times 3\%]}{}$$

$$= 50000 \pm 7\%$$

Resultant error in polynomials can be obtained by the above method.

NOTE:

It is preferable to measure the quantity instead of calculation. In the calculation of quantity the error will be more.

eg: $V \Rightarrow 2\%$ By calculation,
By meters $I \Rightarrow 1\%$ $P_f = \frac{P}{V^2} = 6\%$.
 $P \Rightarrow 3\%$
 $\Rightarrow P_f = 2\%$.

Types of errors :-

(a). Gross errors :-

This class of errors mainly comes by human mistakes in reading, recording and calculating the measurements.

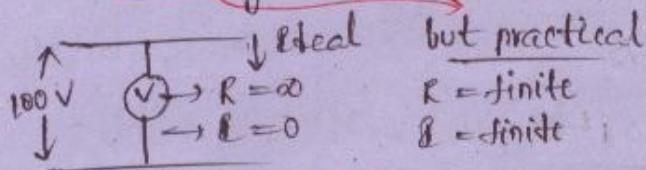
(b). Systematic errors :

(i). Instrumental errors :-

→ Due to inherent short comings { errors in instr. }

→ Misuse of instr. $\frac{1.2 \text{ A}}{0-5 \text{ A} \textcircled{I}} \checkmark$
 $\frac{}{0-100 \text{ A} \textcircled{II}}$

→ Loading effects



(2). Environmental Errors :-

Due to temp, electro magnetic effects.

(3). Observational errors :-

↳ parallax errors

(c). Random Errors :-

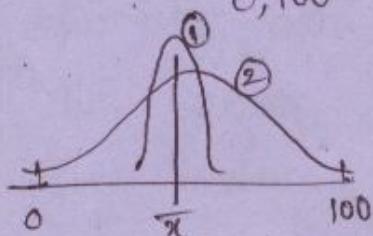
→ These errors occur due to unknown source or cumulative of different sources together.

↙ Random errors can be compensated by statistical Analysis.

↳ Mean $\bar{x} = \frac{x_1 + x_2 + \dots + x_n}{n}$

$$\text{eg: } 51, 49 \rightarrow \bar{x} = 50$$

$$0, 100 \rightarrow \bar{x} = 50 \leftarrow \text{not advisable.}$$



$$d_1 = x_1 - \bar{x}$$

$$d_2 = x_2 - \bar{x}$$

:

$$d_n = x_n - \bar{x}$$

$$\text{Avg. deviation} = \frac{|d_1| + |d_2| + \dots + |d_n|}{n}$$

$$(6) \text{ Std. deviation} = \sqrt{\frac{d_1^2 + d_2^2 + \dots + d_n^2}{n}}$$

$$\text{variance} = (\text{s.d.})^2$$

True value of the quantity to be measured may be ~~still~~ defined as an avg. of infinite no. of measured values when the avg. deviation due to various contributing factors tends to be zero.

$$1.1) \quad A_m = 6.7 A$$

$$A_t = 6.54 A$$

$$\text{error} = A_m - A_t$$

$$(8A) = 0.16 A$$

$$\text{correction factor } \delta C = -8A$$

$$= -0.16 A$$

$$1.2) \quad \text{Range : } 0 - 2.5V$$

$$A_t = 1.5V$$

$$A_m = 1.46V$$

$$\text{error } 8A = A_m - A_t \\ = -0.04V$$

$$\text{correction } \delta C = -8A \\ = 0.04V$$

$$\% \text{ error} = \frac{-0.04}{1.5} \times 100 \\ = -2.67\%$$

$$\% \text{ error} = \frac{-0.04}{2.5} \times 100 \quad (\text{w.r.t. full scale}) \\ = -1.6\%$$

1.3)

$$R = 5000 \pm 10\%$$

$$= (5000 \pm 500) \Omega$$

$$\rightarrow R = 4500 \Omega \text{ to } 5500 \Omega$$

1.4)

$$(0 - 10)A \rightarrow 1.5\%$$

$$\text{error} = 10 \times \frac{1.5}{100}$$

$$= 0.15 A$$

$$A_m = 2.5 A$$

$$I = 2.5 \pm 0.15 \Rightarrow 2.35 \text{ to } 2.65 A$$

$$\text{Relative error} = \frac{0.15}{2.5} \times 100 \\ = 6\%$$

1.5) Diameter = 100 mm
= 0.1 m $\pm 1\%$.

Velocity = 1 m/s $\pm 3\%$.

$$\begin{aligned}\text{flow rate} &= \text{Area} \times \text{velocity} \\ &= \frac{\pi D^2}{4} \times v \\ &= \frac{\pi}{4} (0.1)^2 \times 1 \\ &= 0.785 \times 10^{-4} \text{ m}^3/\text{s} \\ &= 7.85 \times 10^{-5} \text{ m}^3/\text{s.} \pm [2 \times 1\% + 1 \times 3\%] \\ &= 7.85 \times 10^{-5} \pm 5\%.\end{aligned}$$

1.6) $R_4 = \frac{R_1 R_2}{R_3}$.

$$R_1 = 500 \Omega \pm 1\%. \quad R_2 = 615 \pm 1\%. \quad R_3 = 100 \pm 0.5\%$$

$$(a). \quad R_4 = \frac{500 \times 615}{100} = 3075 \Omega$$

$$\begin{aligned}(b). \quad R_4 &= 3075 \pm (1+1+0.5)\% \\ &= 3075 \pm 2.5\% \\ &= 3075 \pm 76.88 \Omega.\end{aligned}$$

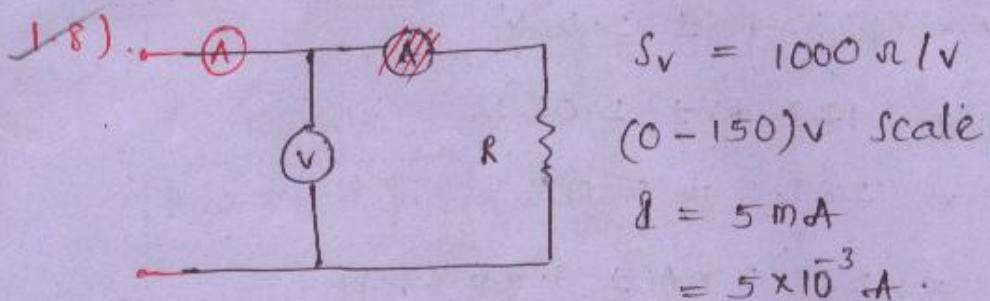
1.7) $\theta_{IP} = 6250 \omega \pm 2\%$

$$= 6250 \pm 125 \omega$$

$$\omega_{IP} = 5000 \omega \pm 3\% = 5000 \pm 150 \omega$$

$$\begin{aligned}\text{Losses} &= \text{U.P} - \text{o.l.p} \\ &= (1250 \pm 275) \omega \\ &= 1250 \omega \pm 22\%.\end{aligned}$$

$$\eta = \frac{\text{o.l.p}}{\text{U.P}} = \frac{5000}{6250} = 0.8 \pm 5\%.$$



$$\begin{aligned}(\text{a}). \text{ Apparent resistance} &= \frac{V}{I} \\ &= \frac{100}{5 \times 10^{-3}} = 20 \text{ k}\Omega.\end{aligned}$$

(b). Resistance of voltmeter

$$\begin{aligned}R_v &= S_v \times 150 \\ &= 1000 \times 150 = 150 \text{ k}\Omega.\end{aligned}$$

$$(\text{c}). \frac{1}{R_T} = \frac{1}{R_v} + \frac{1}{R}$$

$$\Rightarrow \frac{1}{20} = \frac{1}{150} + \frac{1}{R}$$

$$\Rightarrow R = 23 \text{ k}\Omega. \quad 23.077 \text{ k}\Omega$$

$$\begin{aligned}\therefore \text{error} &= \frac{A_m - A_t}{A_t} \\ &= \frac{20 - 23}{23} \times 100 \\ &= -118\%. \quad -13.33\%.\end{aligned}$$

1.9). $V = 123.4 \text{ V}$ Range : $(0 - 250) \text{ V} \rightarrow 1\%$
 $I = 283.5 \text{ mA}$ Range : $(0 - 500) \text{ mA} \rightarrow 1\%$
 $\text{error} = 250 \times \frac{1}{100} = 2.5 \text{ V}$
 $\text{Error} = 500 \times \frac{1}{100} = 5 \text{ mA}$

$$V = 123.4 \pm 2.5 \text{ V}$$

$$= 123.4 \text{ V} \pm 2.02\%$$

$$I = 283.5 \pm 5 \text{ mA}$$

$$= 283.5 \text{ mA} \pm 1.76\%$$

$$R = \frac{V}{I} = \frac{123.4}{283.5 \text{ mA}} = 435.2 \Omega$$

$$R = 435.2 \pm (2.02 + 1.76)\%$$

$$= 435.2 \pm 3.78\%$$

1.10). $A_t = 2.5 \text{ V}$

$$A_m = 2.46 \text{ V}$$

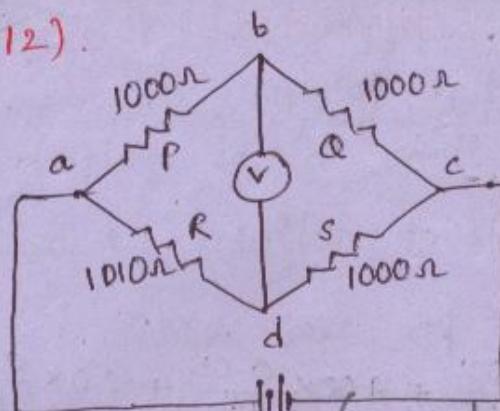
$$\text{Error} = A_m - A_t = -0.04$$

$$\% \text{ Error} = \frac{-0.04}{2.5} \times 100 \\ (\text{True value}) \\ = -1.6\%$$

$$\% \text{ error} = \frac{-0.04}{4} \times 100 \\ (\text{f.s.d}) \\ = -1\%$$

1.11). Resolution = $\frac{100}{400} \times \frac{1}{5}$
 $= 0.05 \text{ V}$
 $= 50 \text{ mV}$

1.12).



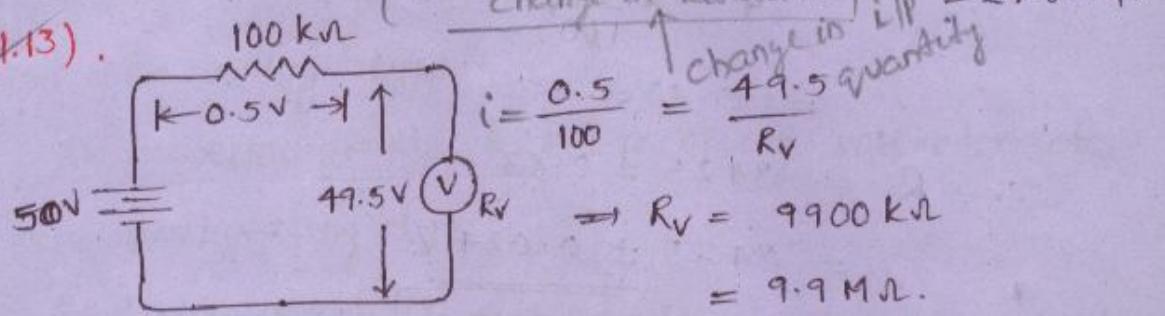
$$V_{bd} = V_b - V_d$$

$$= 50 - \left[100 - \frac{100}{1000+100} \times 100 \right]$$

*change in
Bridge sensitivity*

$$S_B = \frac{\text{change in Volt.}}{\text{change in Resistance}} = \frac{0.248}{10} = 0.0248 \text{ v/ohm}$$

1.13).



$$i = \frac{0.5}{100} = \frac{49.5}{R_V}$$

$$\Rightarrow R_V = 9900 \text{ k}\Omega \\ = 9.9 \text{ M}\Omega.$$

1.14).

$$\begin{aligned} \text{Resolution} &= \frac{50}{100} \times \frac{1}{5} \quad 100 \text{ div} \rightarrow 50 \text{ kN/m}^2 \\ &= 0.1 \text{ kN/m}^2 \quad \frac{1}{5} \text{ div} \rightarrow ? \end{aligned}$$

1.15).

$$(0-10) \text{ A}$$

$$\text{Error} = 10 \times \frac{1.5}{100} = 0.15$$

$$(a). I = 1.5 \text{ A}$$

$$\therefore \text{Error} = \frac{0.15}{1.5} \times 100$$

$$= 10\%$$

$$(b). I = 5 \text{ A}$$

$$\therefore \text{Error} = \frac{0.15}{5} \times 100 = 3\%$$

$$(c). I = 2.5 \text{ A}$$

$$\therefore \text{Error} = \frac{0.15}{2.5} \times 100 \\ = 6\%$$

1.16). units : $\pm 0.2\%$.

Hundreds : $\pm 0.05\%$.

Tens : $\pm 0.1\%$.

Thousands : $\pm 0.02\%$.

$$R = 3425 \Omega.$$

$$\begin{aligned} \text{ERROR} &= 3000 \times \frac{0.02}{100} + 400 \times \frac{0.05}{100} + 20 \times \frac{0.1}{100} \\ &\quad + 5 \times \frac{0.2}{100} \\ &= 0.83 \Omega. \end{aligned}$$

$$\therefore R = 3425 \pm 0.83$$

$$= 3425 \pm \underline{\underline{0.024\%}}$$

1.17). $P \Rightarrow 2\%$.

$g \Rightarrow 1\%$.

$V \Rightarrow 1\%$.

$$P_f = \frac{\sqrt{P}}{\sqrt{g} \sqrt{V}}$$

$$\Rightarrow (2+1+1)\%$$

$$\Rightarrow \underline{\underline{4\%}}$$

Absolute Instruments:

These instrs give the mag. of the quantity in terms of physical constraints of the instr.

ex:- Tangent Galvanometer.

Rayleigh's current balance.

Secondary Instruments:

These instrs use the measurand value directly by the o/p indicated by the instr.

ex:- Ammeter, voltmeter, wattmeter etc.

Analog Instruments:

An analog instr. in which the o/p or display is a conti. fun. of time and having const. relation to its i/p.

These are of 3 types.

(1). Indicating type:

Ex:- Ammeter, voltmeter, pf meter, wattmeter

(2). Recording type:

Ex:- Seismograph, ECG, recording voltmeter etc.

(3). Integrating type:

Ex:- Energymeter $\rightarrow \int pdt = \text{Energy} \Rightarrow \text{kWh}$

$$1 \text{ kWh} = 1000 \times 3600 = 3.6 \times 10^6 \text{ J}$$

charge meter $\rightarrow \int idt = \text{charge} \Rightarrow 1 \text{ coulomb}$

$$1 \text{ coulomb} = 1 \text{ Ampere - sec} \quad \int v dt = \text{flux}$$

$$1 \text{ Amp hour} = 3600 \text{ coulombs}$$

odo meter $\rightarrow \int N dt = \text{distance}$

Total flow meter $\rightarrow \int \text{flow rate. dt} = \text{Total flow}$

Indicating Type Instruments:

The following 3 torques are responsible for the operation of an indicating instr.

(1). Deflecting torque:

It is responsible for the required deflection of pointer or moving system. for a given value of the measurand.

It will be produced by any of the effects caused by flow of current through ckt's.

\Rightarrow At this position,
 $(T_d = T_c)$

control torque :

It is responsible for the control of the movement of pointer and make definite deflection for a given value of measurand.

It is useful to bring back moving system to zero position once the measurand is removed.

There are 2 types of getting the control torque.

(i). Gravity control :-

$$\text{control torque} = \omega l \sin\theta$$

The control torque is proportional to $\sin \theta$ of deflection angle.

The gravity control instr. should always operate in vertical position.

(ii). spring control:

Hair springs made up of silicon bronze, hard rolled silver, platinum silver etc are used for getting the control torque.

$$T_c \propto \theta \rightarrow (\text{deflection angle})$$

(control torque)

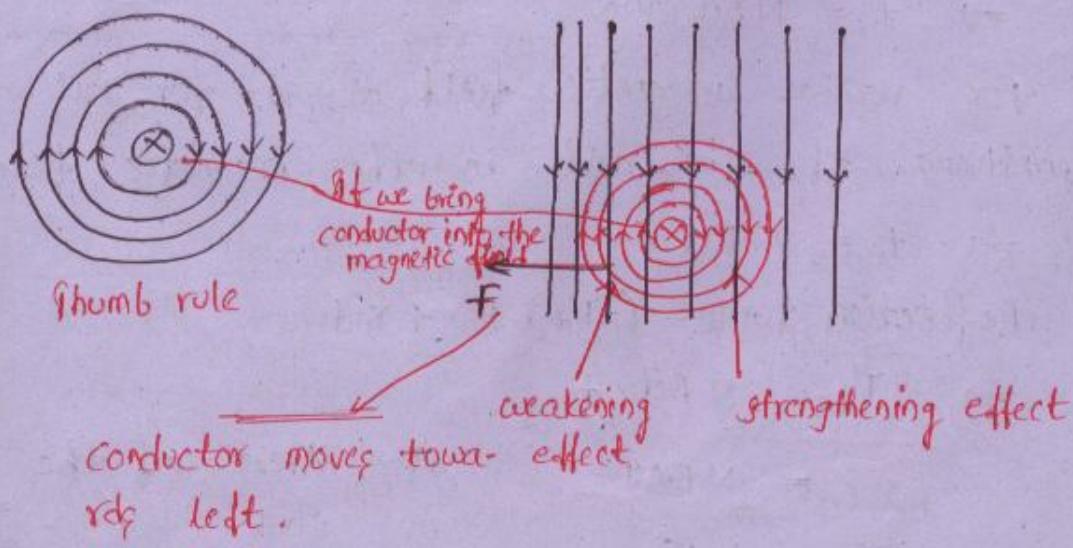
Damping torque :

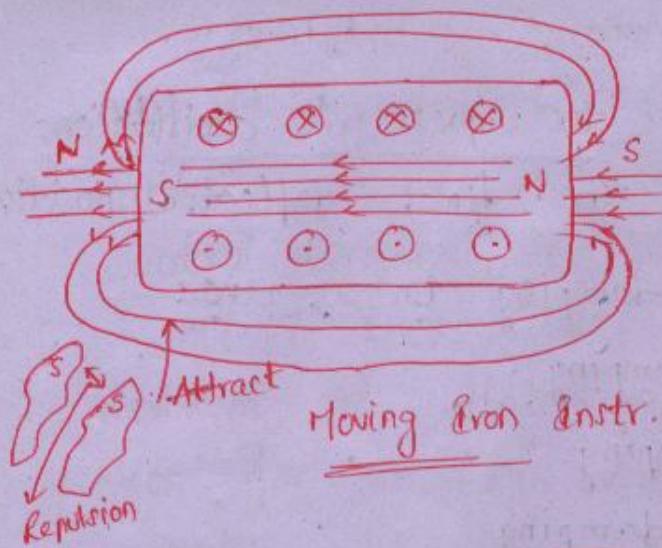
It is responsible to suppress the oscillations of the pointer at the final deflected position various types of damping torques are:

- (i). Eddy current damping
- (ii). Air friction damping
- (iii). fluid friction damping
- (iv). electro magnetic damping

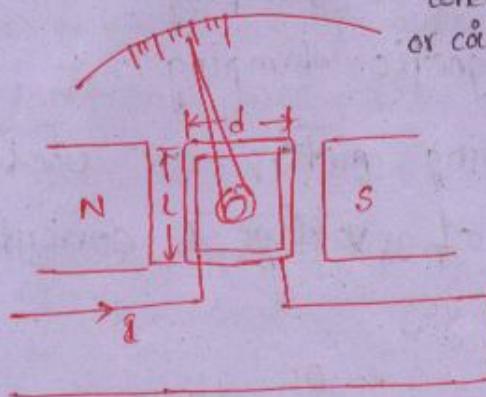
⇒ The following meters are used for the measurement of voltage & current.

- (1). PMMC → DC
 - (2). MI → AC & DC
 - (3). dynamo meter instr.
 - (4). electro static instr.
 - (5). Thermal instr.
 - (6). Rectifier type instr.
 - (7). Induction type instr. → only AC
- Both AC & DC





PMHC :-



when a current carrying conductor or coil

As per field theory mech. force on a conductor can be $\hat{f} = \hat{B} \times \hat{i}l$

$$\Rightarrow f = BIL \sin\alpha ; \alpha = LB, il$$

let the coil consists of 'N' no. of turns, force on each coil side is expressed as

$$\Rightarrow f = NBil \sin\alpha$$

for radial magnetic field $\alpha = 90^\circ$, for all positions of the coil in the magnetic field

$$\Rightarrow f = NBil$$

Deflection torque (T_d) = $f \times d$

$$\Rightarrow T_d = NBil \cdot d$$

$$= NBA\theta.$$

A - Area of the coil.

$$\Rightarrow T_d = k_d \theta$$

k_d - deflection const.

$K_d = NBA$ units: Nm/Amp
springs are used for getting the control torque.

$$T_c \propto \theta \Rightarrow T_c = k_c \theta$$

k_c → spring const. units: Nm/rad or Nm/deg
At final deflected position,

$$T_d = T_c \\ \Rightarrow NBA\theta = k_c \theta \rightarrow \text{PMMC.}$$

$$\Rightarrow \theta \propto \theta \rightarrow \text{scale is uniform \& linear.}$$

→ Eddy current damping is employed in PMMC.

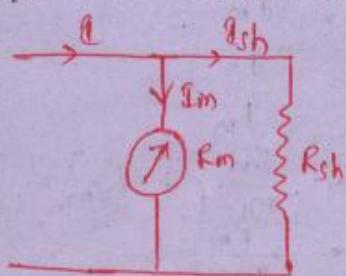
for this purpose an Al metallic frame is used.

In the case of Ammeter, coil carries the current to be measured. In the case of voltmeter a current proportional to volt. pass through the coil. By measuring this current volt. can be evaluated.

The basic PMMC meter current carrying capacity max. of 1A. This is due to presence of spring in the physical part of the current from external ckt to moving coil.

Ammeter shunts:-

These are the small resistances connected across the moving coil (basic meter). to increase the current measuring capacity.



$$I_m R_m = I_{sh} R_{sh}$$

$$= (\delta - I_m) R_{sh}$$

$$\rightarrow I_m [R_m + R_{sh}] = I R_{sh}$$

$$\Rightarrow \frac{I}{I_m} = m = \frac{R_m + R_{sh}}{R_{sh}}$$

$$\Rightarrow m = \frac{R_m}{R_{sh}} + 1$$

$$\Rightarrow m - 1 = \frac{R_m}{R_{sh}}$$

$$\Rightarrow R_{sh} = \frac{R_m}{m-1}; \quad m - \text{multiplying power} = \frac{I}{I_m} \quad (m > 1)$$

* shunt resistance is always less than the meter resistance.

* Manganin is the material used for the preparation of dc shunts. since it possess negligible temp. coe. of resistance.

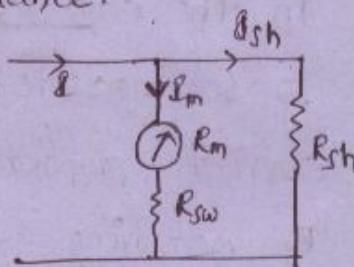
* swamping resistance

will be connected in

series with the meter and

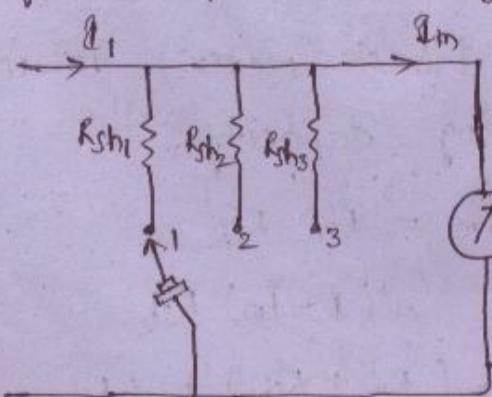
is prepared with same material

as that of shunt. It is suitable for minimizing the errors due to temp. variations.



Multi range Ammeters :-

In this independent shunts are employed for independent ranges.



$$m_1 = \frac{I_1}{I_m}$$

$$m_2 = \frac{I_2}{I_m}$$

$$m_3 = \frac{I_3}{I_m}$$

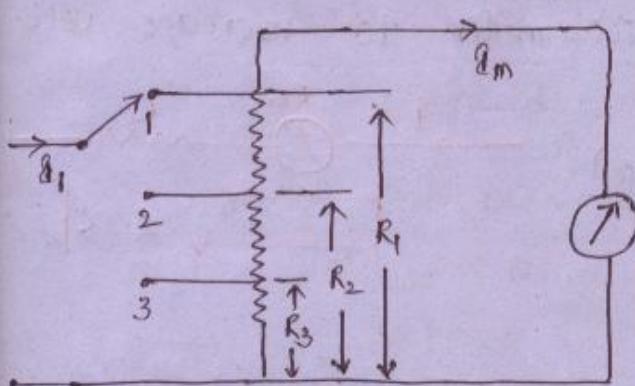
$$R_{sh1} = \frac{R_m}{m_1 - 1}; \quad R_{sh2} = \frac{R_m}{m_2 - 1}$$

$$R_{sh3} = \frac{R_m}{m_3 - 1}$$

The switch to be employed in this meter is "make before break".

There is a possibility of damaging the meter due to passage of heavy current during the transition from one range to another range.

Universal shunt of Ammeter



$$m_1 = \frac{I_1}{I_m} ; m_2 = \frac{I_2}{I_m}$$

$$m_3 = \frac{I_3}{I_m}$$

Let switch is at pos. 1.

$$(I_m - I_m) R_1$$

$$\Rightarrow I_m [R_m + R_1] = I_1 R_1$$

$$\Rightarrow \frac{I_1}{I_m} = m_1 = \frac{R_m + R_1}{R_1}$$

$$\Rightarrow m_1 = \frac{R_m}{R_1} + 1$$

$$\Rightarrow m_1 - 1 = \frac{R_m}{R_1}$$

$$\Rightarrow R_1 = \frac{R_m}{m_1 - 1}$$

Let switch is at pos. 2:-

$$(I_2 - I_m) R_2 = I_m (R_m + R_1 - R_2)$$

$$\Rightarrow I_2 R_2 = I_m (R_m + R_1 - R_2 + R_2)$$

$$\Rightarrow \frac{I_2}{I_m} = \frac{R_m + R_1}{R_2} - m_2$$

$$\Rightarrow m_2 = \frac{R_1 + R_m}{R_2}$$

$$\Rightarrow R_2 = \frac{R_m + R_1}{m_2}$$

Let switch is at pos. 3 :-

$$(I_3 - I_m) R_3 = I_m (R_m + R_i - R_3)$$

$$\Rightarrow \frac{I_3}{I_m} = m_3 = \frac{R_m + R_i}{R_3}$$

$$\Rightarrow R_3 = \frac{R_m + R_i}{m_3}$$

Voltage Multipliers :-

These are the high resistances connected in series with basic meter to increase volt. measuring capacity.

$$m = \frac{V}{V_m} = \frac{\theta (R_m + R_{se})}{\theta R_m}$$

$$\Rightarrow m = 1 + \frac{R_{se}}{R_m}$$

$$\Rightarrow \frac{R_{se}}{R_m} = m - 1 \Rightarrow R_{se} = R_m (m - 1). \quad m > 1$$

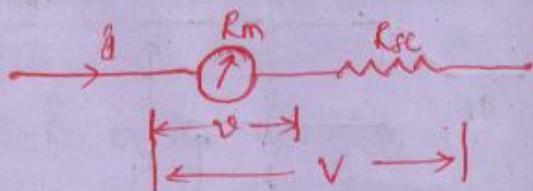
* series resistance is always more than the meter resistance.

MOVING IRON :-

whenever an iron piece is placed in the vicinity of MF produced by a current carrying coil then it will be subjected to mech. force.

M& meter operation is based on change in self inductance of coil. Deflection torque expression can be obtained by conservation of energy principle
electrical energy supplied = change in stored energy + mech. work. done.

$$\begin{aligned} \Rightarrow \text{Electrical energy supplied} &= V \theta dt \\ &= (L \cdot \frac{d\theta}{dt} + \theta \cdot \frac{dL}{dt}) dt \\ &= L \theta d\theta + \theta^2 dL. \end{aligned}$$



$$\text{stored energy} = \frac{1}{2} L \theta^2$$

$$\begin{aligned}\text{change in stored energy} &= d\left[\frac{1}{2} L \theta^2\right] \\ &= \frac{1}{2} \theta^2 dL + \frac{1}{2} L \cdot 2\theta \cdot d\theta \\ &= \frac{1}{2} \theta^2 dL + L\theta d\theta\end{aligned}$$

$$\text{mech. work done} = T_d \cdot d\theta$$

$$\Rightarrow L\theta d\theta + \theta^2 dL = \frac{1}{2} \theta^2 dL + L\theta d\theta + T_d \cdot d\theta$$

$$\Rightarrow \frac{1}{2} \theta^2 dL = T_d \cdot d\theta$$

$$\Rightarrow T_d = \frac{1}{2} \theta^2 \cdot \frac{dL}{d\theta}$$

Springs are used for getting the control torque. So $T_c \propto \theta$

$$\Rightarrow T_c = k\theta.$$

At final deflected position

$$T_d = T_c$$

$$\Rightarrow \frac{1}{2} \theta^2 \frac{dL}{d\theta} = k_c \theta \rightarrow MI$$

Henry/rad.

where $\frac{dL}{d\theta}$ is change in self inductance of coil w.r.t deflection angle.

$\theta \propto \theta^2 \rightarrow$ Scale is non-linear & it varies in square fashion.

It is assumed that $\frac{dL}{d\theta}$ is const.

* Suitable for both AC & DC measurements.

* Air friction damping is employed for MI meter.

→ Linear scale with the MI Meter :-

$$\theta \propto I \quad \frac{1}{2} \theta^2 \frac{dL}{d\theta} = k_c \theta$$

$$\Rightarrow I \propto \theta \quad \Rightarrow I = k_1 \theta \quad \Rightarrow \frac{1}{2} (k_1 \theta)^2 \cdot \frac{dL}{d\theta} = k_c \cdot \theta$$

$$\Rightarrow \frac{1}{2} \cdot \theta \cdot \frac{dL}{d\theta} = \frac{k_c}{k_i^2}$$

$$\Rightarrow \theta \cdot \frac{dL}{d\theta} = \frac{2 k_c}{k_i^2} = \text{const.}$$

$$\Rightarrow \theta \cdot \frac{dL}{d\theta} = \uparrow \text{constant}$$

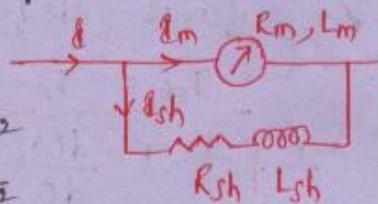
* To obtain a linear scale with MΩ meters, $\frac{dL}{d\theta}$ should be variable and has to vary while satisfying the condi $\theta \cdot \frac{dL}{d\theta} = \text{const.}$

* Current measuring capacity of MΩ, is more than PMMC. [may a max. of 20 A].

* To increase the current measuring capacity shunts may be employed.

* Constantan is employed for preparation of AC shunts:

$$\frac{\delta_m}{I_{sh}} = \frac{Z_{sh}}{Z_m} = \sqrt{\frac{R_{sh}^2 + (\omega L_{sh})^2}{R_m^2 + (\omega L_m)^2}}$$

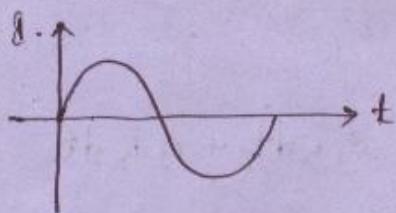


$$\frac{\text{Time const. of shunt}}{\text{Time const. of meter.}} = \frac{R_{sh} \sqrt{1 + \left(\frac{\omega L_{sh}}{R_{sh}}\right)^2}}{R_m \sqrt{1 + \left(\frac{\omega L_m}{R_m}\right)^2}}$$

* If $\frac{L_{sh}}{R_{sh}} = \frac{L_m}{R_m}$ $\Rightarrow \frac{\delta_m}{I_{sh}} = \frac{R_{sh}}{R_m}$

The error due to freq. variation can be eliminated by making the time const.s of meter & shunt should be equal.

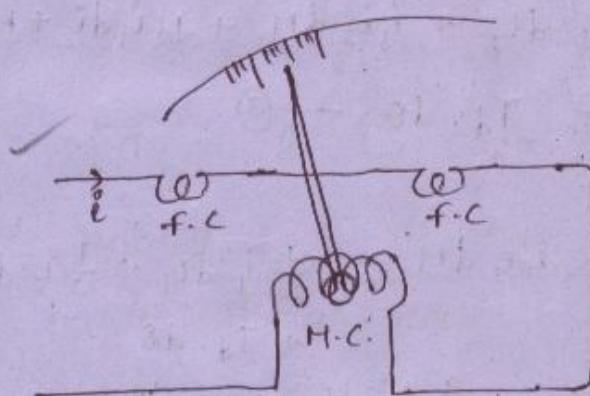
$T_d = NBA \cdot I$. If PMMC subjected to AC:



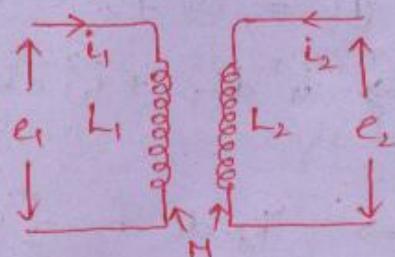
If PMMC is subjected to AC quantity, the following may occur.

- (1). pointer will be oscillating around zero position if the freq. is low.
- (2). pointer is at stand still at zero pos. if the freq. is high.
- (3). To get unidire. torque in moving coil instr. it is required to replace permanent magnets by electromagnets.

ELECTRO DYNAMO METER TYPE INSTRUMENTS:



f.c. → fixed coil
MC → Moving coil



Operating principle is based on change in M b/w the two coils.

- * In the case of ammeter & voltmeter both the coils are connect in series and carries the same current.

Let i_1, i_2 be the instantaneous currents passing through FC & MC res.

Acc. to Energy conservation principle
Electrical energy supplied. = change in stored energy + mech. work done.

$$\begin{aligned}
 \Psi_1 &= L_1 i_1 + M i_2 \\
 \Psi_2 &= L_2 i_2 + M i_1 \\
 \text{electrical energy supplied} &= e_1 i_1 dt + e_2 i_2 dt \\
 &= \frac{d\Psi_1}{dt} i_1 dt + \frac{d\Psi_2}{dt} i_2 dt \\
 &= i_1 d\Psi_1 + i_2 d\Psi_2 \\
 &= i_1 d[L_1 i_1 + M i_2] + i_2 d[L_2 i_2 + M i_1] \\
 &= i_1^2 dL_1 + i_1^2 dL_2 + i_1 i_2 dM + M i_1 d i_2 + L_2 i_2 d i_2 \\
 &\quad + i_2^2 dL_2 + i_1 i_2 dM + M i_2 d i_1
 \end{aligned}$$

$$\text{stored energy} = \frac{1}{2} L_1 i_1^2 + \frac{1}{2} L_2 i_2^2 + M i_1 i_2$$

$$\begin{aligned}
 \text{change in stored energy} &= L_1 i_1 d i_1 + \frac{1}{2} i_1^2 d L_1 \\
 &\quad + L_2 i_2 d i_2 + \frac{1}{2} i_2^2 d L_2 + i_1 i_2 d M + M i_1 d i_2 + M i_2 d i_1
 \end{aligned}$$

$$\text{mech. work done} = T_d \cdot d\theta \quad \text{--- (3)}$$

$$\textcircled{1} = \textcircled{2} + \textcircled{3}$$

$$\Rightarrow i_1^2 d L_1 + i_2^2 d L_2 + i_1 i_2 d M = \frac{1}{2} i_1^2 d L_1 + \frac{1}{2} i_2^2 d L_2 + T_d \cdot d\theta$$

$$\Rightarrow T_d \cdot d\theta = \frac{1}{2} i_1^2 d L_1 + \frac{1}{2} i_2^2 d L_2 + i_1 i_2 d M$$

The change in self inductances are neglected compare to mutual inductance.

$$\rightarrow T_d \cdot d\theta = i_1 i_2 d M$$

$$\Rightarrow T_d = i_1 i_2 \cdot \boxed{\frac{d M}{d\theta}}$$

DC :

$$i_1 = \varnothing_1 ; \quad i_2 = \varnothing_2$$

$$T_d = \varnothing_1 \varnothing_2 \cdot \frac{d M}{d\theta}$$

AC:

$$\text{Let } i_1 = I_m \sin \omega t$$

$$i_2 = I_m \sin(\omega t - \alpha)$$

$$T_d (\text{instantaneous}) = i_1 i_2 \frac{dM}{d\theta}$$

$$= I_m \sin \omega t \cdot I_m \sin(\omega t - \alpha) \cdot \frac{dM}{d\theta}.$$

$$\text{Avg. deflection torque } (T_d) = \frac{1}{2\pi} \int_0^{2\pi} (i_1 i_2 \frac{dM}{d\theta}) d\omega t$$

$$T_d = \frac{1}{2\pi} \int_0^{2\pi} I_m I_m \sin \omega t \sin(\omega t - \alpha) \frac{dM}{d\theta} d\omega t$$

$$= \frac{I_m I_m}{4\pi} \int_0^{2\pi} \cos \alpha - \cos(2\omega t - \alpha) d\omega t \cdot \frac{dM}{d\theta}$$

$$= \frac{I_m I_m}{4\pi} \cdot \frac{dM}{d\theta} \left[\cos \alpha \cdot 2\pi - \frac{1}{2} \sin(2\omega t - \alpha) \right]_0^{2\pi}$$

$$= \frac{I_m}{\sqrt{2}} \cdot \frac{I_m}{\sqrt{2}} \cdot \frac{1}{2\pi} \cdot \frac{dM}{d\theta} [\cos \alpha \cdot 2\pi]$$

$$\Rightarrow T_d = I_1 \cdot I_2 \cdot \cos \alpha \cdot \frac{dM}{d\theta}.$$

Here I_1, I_2 be the rms values of the currents passing through coils and having an angle θ/ω I_1 & I_2 if α .

DC AMMETER:

$$I_1 = I_2 = I.$$

$$T_d = I^2 \cdot \frac{dM}{d\theta}.$$

AC AMMETER:

$$I_1 = I_2 = I \& \alpha = 0.$$

$$T_d = I^2 \cdot \frac{dM}{d\theta}.$$

springs are used for control purpose so

$$T_c = k_c \theta.$$

At final deflection position,

$$T_d = T_c$$

$$\Rightarrow I^2 \cdot \frac{dM}{d\theta} = k_c \cdot \theta \rightarrow \text{Dynamometer}$$

$\frac{dM}{d\theta}$ is, the change in M b/w two coils w.r.t. deflection angle. units Henry/rad.

$$* \quad \boxed{\theta \propto I^2}$$

scale is non-linear and varies in square (I^2) fashion

* Air friction damping is employed for the dynamo meter type instr.

→ STANDARD FOR DC VOLT:

STANDARD CELL.

→ STANDARD FOR AC VOLT: Rayleigh's current balance

In the calibration of AC meters transfer type instr.s are used. Dynamo meter type is useful

at high freq. transfer instr. at power freq. range, since thermionic transfer instr. possess good accuracy for both DC & AC.

ELECTRO STATIC TYPE INSTRUMENTS:-

Operating principle is based on change of capacitance. $C = \frac{\epsilon A}{d}$.

capacitance of a shunt capacitor can be varied either by overlapping area b/w the plates or distance b/w the plates.

* These are best suitable for measurement of high voltages.

deflection torque can be obtained by the principle of conservation of energy law.

electrical energy supplied = change in stored energy + mech. work done.

electrical energy supplied = $v \cdot dt$

$$= v \left[C \cdot \frac{dv}{dt} + v \cdot \frac{dc}{dt} \right] dt$$

$$= Cv \cdot dv + v^2 dc \quad \text{--- (1)}$$

$$\text{stored energy} = \frac{1}{2} Cv^2.$$

$$\text{change in stored energy} = d \left[\frac{1}{2} Cv^2 \right]$$

$$= Cv \cdot dv + \frac{1}{2} v^2 \cdot dc \quad \text{--- (2)}$$

linear motion:

$$cvdv + v^2 dc = cv \cdot dv + \frac{1}{2} v^2 dc + f dx$$

$$\Rightarrow f = \frac{1}{2} v^2 \cdot \frac{dc}{dx}$$

Angular motion:

$$cvdv + v^2 dc = cv \cdot dv + \frac{1}{2} v^2 dc + T_d \cdot d\theta$$

$$\Rightarrow T_d = \frac{1}{2} v^2 \cdot \frac{dc}{d\theta}$$

Spring control is used, so $T_c \propto \theta$

At final deflection position,

$$T_d = T_c$$

$$\Rightarrow \frac{1}{2} v^2 \cdot \frac{dc}{d\theta} = k_c \cdot \theta \Rightarrow \theta \propto v^2$$

$\frac{dc}{d\theta}$ is change in capacitance w.r.t. deflection
and unit: farad/rad.

→ There are 2 types of electrostatic meters,

(1). Quadrant electrometer:-

suitable for measurement of high voltages.

(2). Kelvin multi cellular:-

suitable for measurement of low voltages.

* MON. 17/11/08 *

THERMAL TYPE :

- (1). Suitable for high freq. applications.
- (2). capable to measure current which is of non-sinusoidal nature also.
- (3). These instr.s employ heating effect the flow of current through the ckt.

3 Types:

- (1). Hot wire instr.s
- (2). Bolo meter.
- (3). Thermo couple instr.s

HOT WIRE :

In this meter expansion of metal caused by flow of current through sensitive element. This element is prepared with metal having more value of coe. of expansion.

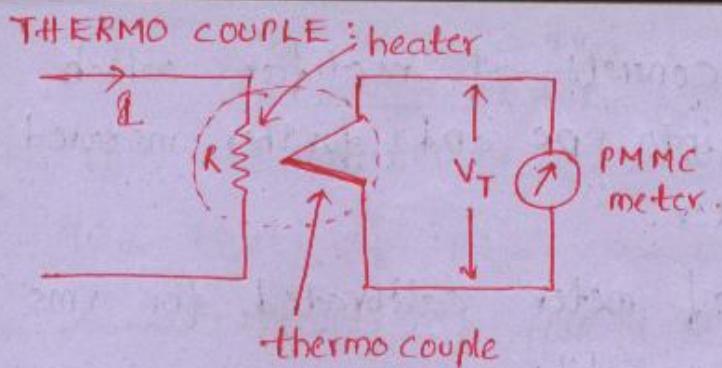
- * The sensitive element is prepared by platinum irradiium alloy.

BOLO METER :

In this instr. change in Resis. caused by heating effect of current employed for the evaluation of the current.

If the sensitive element with +ve temp coe. then its resistance increases with increment of temp.

If element having -ve temp. coe., its resistance decreases with increment in temp.



- (1) It is a joint of two dissimilar junctions. As the temp. of the junction increases it generates a volt. known as thermal emf. This effect known as seebeck effect.
- (2) deflection of PMMC meter $\theta \propto V_T$.
 $\rightarrow \theta \propto a(t^2 R) + \dots$
 $\Rightarrow \theta \propto t^2$
 deflection of PMMC is proportional to t^2 , hence it is suitable for ac & dc measurement.
- (3) Thermal instrs are suitable as transfer instrs for high freq. operation.

* Some of the combination of metals for making thermo couple

- (i) iron - constantan
- (ii) platinum - chromium
- (iii) chromel - alumel

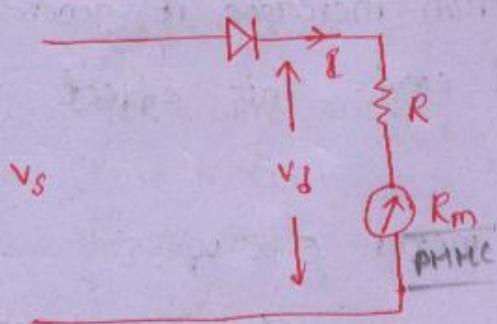
RECTIFIER TYPE :

- (1) suitable for electronic measurements ie lower magnitude of volt.
- (2) 2 types:
 - (a) Amplifier - rectifier type
 - (b) rectifier - Amplifier type

* The meter consists of rectifier which converts Ac into dc and further measured by PMMC meter.

* The reading of meter calibrated for rms value of Ac quantity.

HALF WAVE RECTIFIER TYPE:



DC:

If meter is fed with de volt. of V_s then

$$\frac{V_d}{I} = \frac{V_d}{R + R_m} = \frac{V_s}{R + R_m}$$

AC:

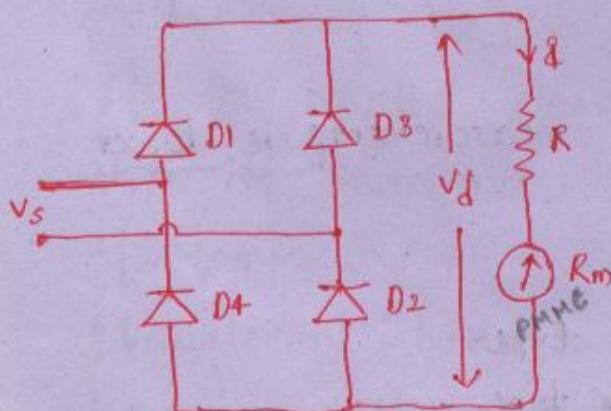
$$V_d = \frac{V_m}{\pi} = \frac{\sqrt{2} V_s}{\pi} = 0.45 V_s$$

$$I = \frac{V_d}{R + R_m} = \frac{0.45 V_s}{R + R_m}$$

If the meter is fed with ac volt. V_s which is same that of dc volt. Then,

* The sensitivity for Ac of HWR type instr. is 45% that of dc.

FULL WAVE RECTIFIER TYPE:



DC:

$$V_d = V_s$$

$$I = \frac{V_d}{R + R_m} = \frac{V_s}{R + R_m}$$

AC:

$$V_d = \frac{2V_m}{\pi} = \frac{2\sqrt{2}}{\pi} V_s = 0.9 V_s$$

$$I = \frac{V_d}{R + R_m} = \frac{0.9 V_s}{R + R_m}$$

- * The AC sensitivity of FWR type instr. is 90% that of DC.
- * AC sensitivity of FWR type instr. is 2 times that of HWR type instr.
- * The ^{DC}sensitivity of FWR type instr. is same as that of HWR instr.
- * Form factor = $\frac{\text{RMS}}{\text{Average}}$.
- * Deflection of PMMC is proportional to avg. value
- * ∵ scale of the meter is calibrated for rms value by multiplying avg. value with ff. usually it will be taken as 1.11
for sinusoidal wave ff = 1.11.
for square wave ff = 1.

2.1)

$$N = 100$$

$$d = 20 \text{ mm}$$

$$l = 30 \text{ mm}$$

$$B = 0.1 \text{ T}$$

$$I = 10 \text{ mA}$$

$$k_c = 2 \times 10^6 \text{ N-m/deg.}$$

$$T_d = NBA \cdot I$$

$$= 100 \times 0.1 \times 30 \times 20 \times 10^6 \times 10 \times 10^{-3}$$

$$= 60 \mu \text{Nm}$$

$$\frac{NBA \cdot I}{60 \times 10^6} = k_c \theta \rightarrow \text{Moving coil}$$

$$\Rightarrow \frac{60 \times 10^6}{60 \times 10^6} = \frac{2 \times 10^6 \times 0}{60 \times 10^6} \Rightarrow \theta = 30^\circ$$

$$2.2). \quad R = 10000 \Omega$$

$$A = 30 \times 30 \text{ mm}^2$$

$$N = 100$$

$$B = 0.08 \text{ wb/m}^2$$

$$k_c = 3 \times 10^{-6} \text{ Nm/l deg.}$$

$$V = 200 \text{ V.}$$

$$NBA \cdot \theta = k_c \theta$$

$$\Rightarrow 100 \times 0.08 \times 30 \times 30 \times 10^{-6} \times \left(\frac{200}{10000} \right) = 3 \times 10^{-6} \cdot \theta$$

$$\Rightarrow \theta = 48^\circ.$$

2.3).

$$R_m = 1 \Omega$$

$$V = 250 \text{ V}$$

$$R_{se} = 4999 \Omega$$

$$I_m = \frac{250}{4999 + 1} = 0.05 \text{ A.}$$

$$(a). \quad R_{sh} = \frac{1}{499} \Omega ; \quad \frac{l}{I_m} = 500$$

$$R_{sh} = \frac{R_m}{m-1} \quad l = 500 \times 0.05$$

$$\Rightarrow \frac{1}{499} = \frac{1}{m-1} \quad = 25 \text{ A.}$$

$$\Rightarrow m = 500.$$

$$(b). \quad I = 50 \text{ A}$$

$$m = \frac{l}{I_m} = \frac{50}{0.05} = 1000$$

$$R_{sh} = \frac{R_m}{m-1}$$

$$= \frac{1}{1000-1} = \frac{1}{999} \Omega$$

$$2.4). A = 40 \times 30 \text{ mm}^2$$

$$N = 100$$

$$T_c = 0.25 \times 10^3 \text{ Nm}$$

$$50 \text{ divisions} \quad I \cdot NBA = k_c \theta$$

$$B = 1 \text{ T} \quad \rightarrow \quad I = 2.083 \times 10^{-3} \text{ A}$$

$$1 \text{ V / div} \quad 1 \text{ div} = 1 \text{ V}$$

$$R_V = 10000 \Omega \quad 50 \text{ div} = ? = 50 \text{ V}$$

$$V = 50 \text{ V} \quad \therefore R_{\text{Total}} = \frac{50}{2.083 \times 10^{-3}} = 24000 \Omega$$

$$NBA \cdot I = k_c \theta$$

$$\Rightarrow 100 \times 1 \times \frac{50}{R_T} = 0.25 \times 10^{-3}$$

$$\Rightarrow R_T = 24000 \Omega$$

$$R_{\text{sc}} = 24000 - 10000$$

$$= 14000 \Omega.$$

$$2.5). I_m = 10 \text{ mA}$$

$$V_m = 100 \text{ mV}$$

$$R_m = \frac{V_m}{I_m} = 10 \Omega$$

$$(a). m = \frac{I}{I_m} = \frac{100}{10 \times 10^{-3}}$$

$$= 10000$$

$$R_{sh} = \frac{R_m}{m-1} = \frac{10}{9999} \Omega$$

$$= 0.001 \Omega$$

$$(b). m = \frac{V}{V_m}$$

$$= \frac{1000}{100 \times 10^{-3}}$$

$$= 10000$$

$$R_{sc} = R_m(m-1)$$

$$= 10(9999)$$

$$= 99.99 \text{ k}\Omega$$

$$I_{mA} = 10 \times \frac{0.02}{1000 + 0.02}$$

$$= 0.2 \text{ mA}$$

$$I_{mB} = 10 \times \frac{0.01}{1500 + 0.01}$$

$$= 0.0667 \text{ mA}$$

If shunts are interchanged, then

$$I_{mA} = 10 \times \frac{0.01}{1000 + 0.01} = 0.1 \text{ mA} \Rightarrow \left(\frac{0.2}{2} \text{ mA} \right)$$

$$I_{mB} = 10 \times \frac{0.02}{1500 + 0.02} = 0.133 \text{ mA} \Rightarrow \left(0.0667 \times 2 \right)$$

Ammeter A shows only 5A b'coz current through the meter is half
 Ammeter B shows 20A since the current is doubled.

2.7).

$$L = \left(8 + 4\theta - \frac{1}{2}\theta^2 \right) \mu\text{H}$$

$$k_c = 12 \times 10^6 \text{ Nm/rad.}$$

$$\frac{1}{2} \theta^2 \cdot \frac{dL}{d\theta} = k_c \cdot \theta \rightarrow \text{moving iron}$$

$$\Rightarrow \frac{dL}{d\theta} = (4 - \theta) \mu\text{H/rad.}$$

$$(a). I = 1\text{A}$$

$$\frac{1}{2} (1)^2 [4 - \theta] \times 10^{-6} = 12 \times 10^6 \times \theta$$

$$\Rightarrow \theta = 0.16 \text{ rad}$$

$$(b). I = 2\text{A}$$

$$\Rightarrow \frac{1}{2} (2)^2 [4 - \theta] \times 10^{-6} = 12 \times 10^6 \times \theta$$

$$\Rightarrow \theta = 0.57 \text{ rad}$$

$$(c). I = 3\text{A}$$

$$\frac{1}{2} (3)^2 [4 - \theta] \times 10^{-6} = 12 \times 10^6 \cdot \theta$$

$$\Rightarrow \theta = 1.16 \text{ rad}$$

$$(d). I = 5\text{A}$$

$$\frac{1}{2} (5)^2 [4 - \theta] \times 10^{-6} = 12 \times 10^6 \times \theta$$

$$\Rightarrow \theta = 2.04 \text{ rad}$$

$$2.8). \quad L = (0.01 + c\theta)^2 \text{ mH}$$

$$I_1 = 1.5 \text{ A}; \quad \theta_1 = 90^\circ$$

$$I_2 = 2 \text{ A}; \quad \theta_2 = 120^\circ.$$

$$\frac{1}{2} I^2 \cdot \frac{dL}{d\theta} = k_c \cdot \theta$$

$$\frac{dL}{d\theta} = 2c [0.01 + c\theta] \text{ mH/rad.}$$

$$\Rightarrow \frac{\frac{1}{2} (1.5)^2 [2c(0.01 + c\theta)]}{90^\circ} = k_c \times 90^\circ$$

$$\frac{1}{2} (2)^2 [2c(0.01 + 120^\circ c)] = k_c \times 120^\circ$$

$$\Rightarrow c = -47.6 \times 10^6$$

2.9).

$$I = 25 \text{ A}$$

$$\frac{dM}{d\theta} = 0.0035 \text{ mH/deg.} = \frac{0.035}{\pi/180} \text{ mH/rad.}$$

$$k_c = 10^6 \text{ Nm/deg.}$$

$$\underbrace{I^2 \cdot \frac{dM}{d\theta}}_{\text{Electro dynamo meter.}} = k_c \cdot \theta$$

$$\Rightarrow (25)^2 \cdot 0.0035 \times 10^6 \times \frac{180}{\pi} = 10^6 \times \theta$$

$$\Rightarrow \theta = 125^\circ.$$

2.10).

$$I = 10 \text{ A}$$

$$k_c = 0.1 \times 10^6 \text{ Nm/deg}$$

$$\theta = 110^\circ$$

$$I^2 \frac{dM}{d\theta} = k_c \cdot \theta$$

$$\Rightarrow (10)^2 \cdot \frac{dM}{d\theta} = 0.1 \times 10^6 \times 110$$

$$\Rightarrow \frac{dM}{d\theta} = 0.11 \text{ mH/rad.}$$

$$M = 2 \mu H + \left(0.11 \times 10^{-6} \times [110 \times \frac{\pi}{180}] \right)$$

$$\Rightarrow M = 2.21 \mu H$$

2.11).

$$V_m = 100 V$$

$$\text{HWR: } R = 10 \Omega \text{ measured}$$

$$(a). \text{ Hot wire: } V_{or} = \frac{V_m}{2} = \frac{100}{2} = 50 V$$

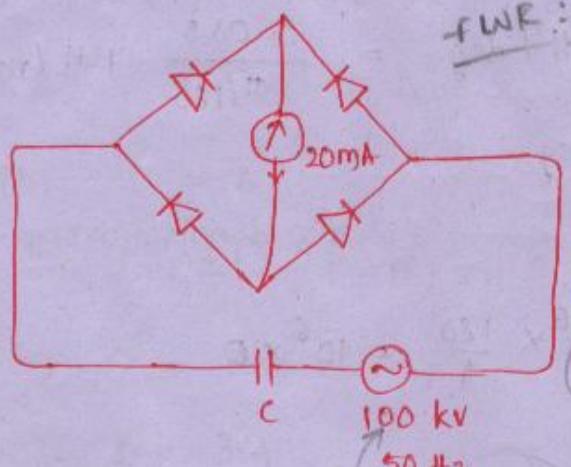
$$I = \frac{50}{10} = 5 A$$

$$(b). \text{ moving coil: } V_o = \frac{V_m}{\pi} \text{ measured avg. values}$$

$$V_o = \frac{V_m}{\pi} = \frac{100}{\pi}$$

$$I = \frac{100}{\pi \times 10} = 3.183 A \quad (\sqrt{V_{rms}} = \frac{V_m}{\sqrt{2}})$$

2.12).



$$\text{FWF: } V_{dc} = \frac{2V_m}{\pi} = \frac{2\sqrt{2}V_s}{\pi}$$

$$= \frac{2\sqrt{2} \times 100 \times 10^3}{\pi}$$

$$= 90.03 \text{ kV}$$

$$20 \times 10^{-3} = \frac{90.03 \times 10^3}{X_C}$$

$$\Rightarrow X_C = 4.5 \times 10^6 \Omega$$

$$\Rightarrow C = \frac{1}{\omega X_C}$$

$$= \frac{1}{2\pi \times 50 \times 4.5 \times 10^6}$$

$$= 707 \text{ pf}$$

$$= 707 \times 10^{-12} F$$

2.14). $R_m = 250 \Omega$ (At a time 2 diodes are conducting. So)

$$I_m = 1mA$$

$$R_D = 50 \Omega$$

$$(rms) V = 25V$$

$$V_{dc} = \frac{2V_m}{\pi}$$

$$= \frac{2\sqrt{2} \times 25}{\pi} = 22.5V$$

$$I_m = \frac{V_{dc}}{R_T} \quad (R_T = 2R_f + R_{dc} + R_m)$$

$$\Rightarrow R_T = \frac{22.5}{1 \times 10^{-3}} = 22.5 k\Omega$$

$$R_{dc} = 22500 - (250 + 2 \times 50)$$

$$= 22.15 k\Omega$$

$$\text{v/v} = \frac{22500}{25}$$

$$= 900 \text{ v/v}$$

2.15). Electro static

$$\text{diameter} = 8 \text{ cm}$$

$$x = 4 \text{ mm}$$

$$f = 0.002 \text{ N}$$

$$f = \frac{1}{2} \nu^2 \cdot \frac{dc}{dx}$$

$$c = \frac{\epsilon A}{x}$$

$$\frac{dc}{dx} = -\frac{\epsilon A}{x^2}$$

$$A = \frac{\pi d^2}{4}$$

$$\Rightarrow 0.002 = \frac{1}{2} \nu^2 \left[-\frac{8.854 \times 10^{-12} \times 1 \times \pi \left(\frac{0.08}{4} \right)^2}{(4 \times 10^{-3})^2} \right]$$

$$\Rightarrow \nu = 1199 \text{ V}$$

$$2.16) \quad V = 1000 \text{ V}$$

$$k_c = 10^7 \text{ Nm/deg}$$

$$\theta = 80^\circ$$

$$C = 10 \text{ pF}$$

$$\frac{1}{2} V^2 \frac{dC}{d\theta} = k_c \theta \longrightarrow \text{Electro static}$$

$$\Rightarrow \frac{1}{2} (1000)^2 \cdot \frac{dC}{d\theta} = 10^7 \times 80$$

$$\Rightarrow \frac{dC}{d\theta} = 0.16 \text{ pF/rad}$$

$$\Rightarrow C = 10 + (0.16 \times 80 \times \frac{\pi}{180})$$

$$= 32.34 \text{ pF}$$

2.17).

$$V = 3000 \text{ V}$$

$$k_c = 7.6 \times 10^{-6} \text{ Nm/deg}$$

$$\theta = 80^\circ = 80 \times \frac{\pi}{180} \text{ rad.} = 1.39 \text{ rad}$$

$$\frac{1}{2} V^2 \cdot \frac{dC}{d\theta} = k_c \cdot \theta$$

$$\Rightarrow \frac{1}{2} (3000)^2 \cdot \frac{dC}{d\theta} = 7.6 \times 10^{-6} \times 80 \times \frac{\pi}{180}$$

$$\Rightarrow \frac{dC}{d\theta} = 2.358 \times 10^{-12} \text{ f/rad}$$

$$\Rightarrow dC = 2.358 \times 10^{-12} \times 1.39$$

$$= 3.29 \text{ pF}$$

2.18).

$$\theta \propto I^2$$

$$I_1 = 10 \text{ A}$$

$$\theta_1 = \theta$$

$$I_2 = ?$$

$$\theta_2 = \frac{\theta}{2}$$

$$\frac{\theta_1}{\theta_2} = \frac{I_1^2}{I_2^2} \Rightarrow I_2 = \sqrt{50} = 7.07 \text{ A}$$

* TUE. 18/11/08 *

MEASUREMENT OF RESISTANCE :

RESISTANCES :

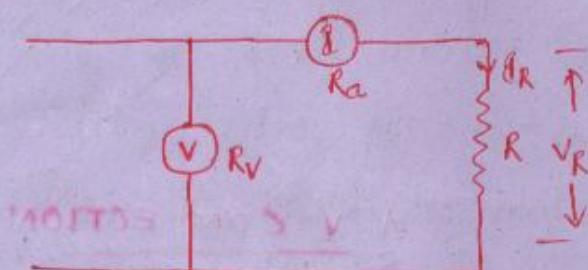
- (1). Low resistance : < 1 Ω, below 1Ω.
- (2). Medium : ~~1Ω/1000/100~~ 1Ω to 100 kΩ
- (3). High : greater than 100 kΩ

Medium resistance is represented by a two terminal resistive element. — M —.

* Medium resistance can be measured by,

- (1). Ammeter - voltmeter method
- (2). Substitution method
- (3). Wheatstone bridge
- (4). Ohmmeter.

AMMETER- VOLTMETER METHOD:



$$\text{Measured resistance } (R_{m1}) = \frac{V}{I}$$

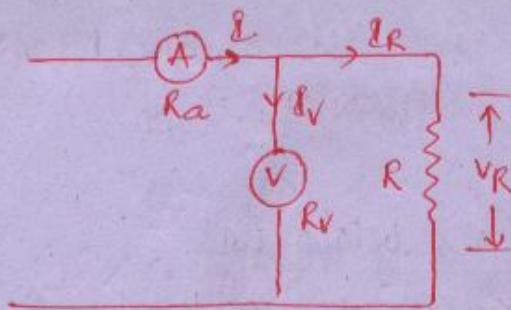
$$\begin{aligned} R_{m1} &= \frac{V_R + V_a}{I_R} \\ &= \frac{I_R \cdot R + I_R \cdot R_a}{I_R} = R + R_a \end{aligned}$$

$$\text{True resistance } R = R_{m1} - R_a$$

$$\therefore \text{error} = \frac{A_m - A_t}{A_t}$$

$$= \frac{R_{m1} - R}{R}$$

$$= \frac{R_a}{R}$$



$$\begin{aligned} R_{m2} &= \frac{V}{I} \\ &= \frac{V_R}{I_R + \delta_V} \\ &= \frac{V_R}{\frac{V_R}{R} + \frac{V_R}{R_V}} \end{aligned}$$

$$\begin{aligned} R_{m2} &= \frac{1}{\frac{1}{R} + \frac{1}{R_V}} \\ &= \frac{1}{\frac{1}{R} \left[1 + \frac{R}{R_V} \right]} \\ &= \frac{R}{1 + \frac{R}{R_V}} \end{aligned}$$

$$\begin{aligned} \Rightarrow \frac{1}{R_{m2}} &= \frac{1}{R} + \frac{1}{R_V} \\ \Rightarrow \frac{1}{R} &= \frac{1}{R_{m2}} - \frac{1}{R_V} \end{aligned}$$

$$\Rightarrow R_{m2} \left[1 + \frac{R}{R_V} \right] = R \quad \Rightarrow R_{m2} - R = - \frac{R_{m2} \cdot R}{R_V}$$

$$\begin{aligned} \% \text{ Error} &= \frac{R_{m2} - R}{R} \\ &= - \frac{R_{m2}}{R_V} \\ &\approx - \frac{R}{R_V} \end{aligned}$$

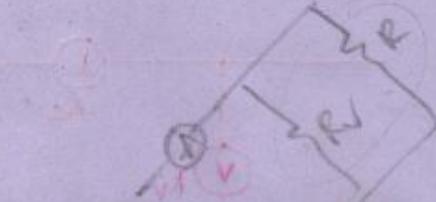
$$\frac{R_{m2} - R}{R} = - \frac{R_{m2}}{R_V}$$

V-A METHOD

* Measured resistance is always more than true resistance.

* This method of connection is suitable for measurement of high resistance in the specified band.

$$\therefore \% \text{ Error} = \frac{R_A}{R} \uparrow$$



A-V CONNECTION

* Measured resistance is always less than the true resistance.

* This method of connection is suitable for measurement of low resistance.

$$\therefore \% \text{ Error} = - \frac{R}{R_V} \downarrow$$

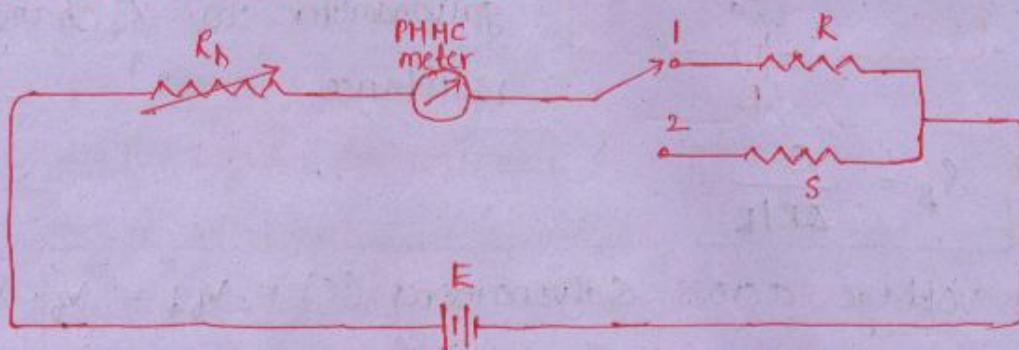
* Resistance for which both the methods give equal error can be obtained as follows:

$$\frac{R_a}{R} = \frac{R}{R_v}$$

$$\Rightarrow R = \sqrt{R_a R_v}$$

If R high adopt V-A conn.
If R if low \rightarrow A-V connection

SUBSTITUTION METHOD:



R - unknown

s - std known variable resistance

keep the switch in (1) pos. and vary the R_b till a finite current passing through Ammeter.

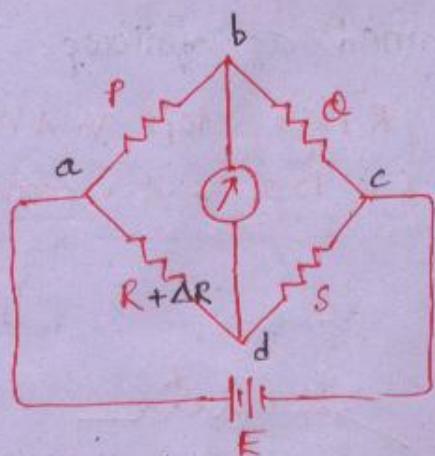
Change the pos. of switch to (2) and then vary the known resistance till same current passing through meter. In this R_b should not be disturb. At this condi. unknown resistance is equal to the known resistance.

Let $G_1 = \frac{1}{R} + \frac{1}{r}$ be the total conductance of the meter and the rheostat in parallel.

$$I_S = " " " " " S \text{ is in ckt.}$$

$$\frac{dr}{ds} = \frac{s+g}{r+g}$$

WHEAT STONE BRIDGE :-



Under Balance condition,

$$\frac{P}{Q} = \frac{R}{S}$$

* Bridge sensitivity is the ratio of deflection of galvanometer to % change in resistance.

$$S_B = \frac{\Theta}{\Delta R/R}$$

$$\text{voltage across Galvanometer } (\epsilon) = V_{bd} = V_b - V_d$$

$$= \left[E - \frac{E}{P+Q} P \right] - \left[E - \frac{E}{R+\Delta R+S} (R+\Delta R) \right]$$

$$= E \left[\frac{R+\Delta R}{R+\Delta R+S} - \frac{P}{P+Q} \right]$$

$$= E \left[\frac{R+\Delta R}{R+\Delta R+S} - \frac{R}{R+S} \right]$$

$$\epsilon = E \left[\frac{R^2 + RS + R\Delta R + S\Delta R - R^2 - R\Delta R - RS}{(R+S)^2 + \Delta R(R+S)} \right]$$

$$= E \left[\frac{S \cdot \Delta R}{(R+S)^2} \right]$$

$$\text{Let } S_V = \text{sensitivity of Galvanometer} = \frac{\Theta}{\epsilon}$$

$$\Theta = S_V \cdot \epsilon = S_V \cdot \frac{E \cdot S \cdot \Delta R}{(R+S)^2}$$

$$S_B = \frac{\Theta}{\Delta R/R} = \frac{S_V \cdot E \cdot S \cdot R}{(R+S)^2}$$

$$S_B = S_V \cdot E \cdot \frac{RS}{R^2 + 2RS + S^2}$$

$$\Rightarrow S_B = \frac{S_V \cdot E}{\frac{R}{S} + 2 + \frac{S}{R}}$$

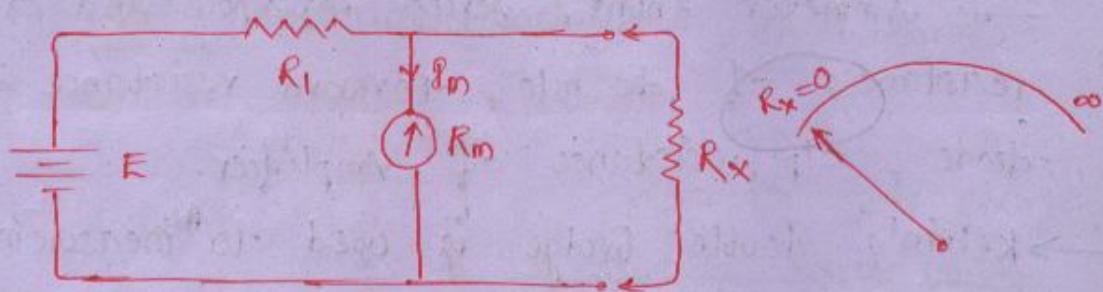
(or)

$$S_B = \frac{S_V \cdot E}{\frac{P}{Q} + 2 + \frac{Q}{P}}$$

Bridge sensitivity would be max. if $\frac{P}{Q} = \frac{R}{S} = 1$.

$$\Rightarrow S_{B_{max}} = \frac{S_V \cdot E}{4}$$

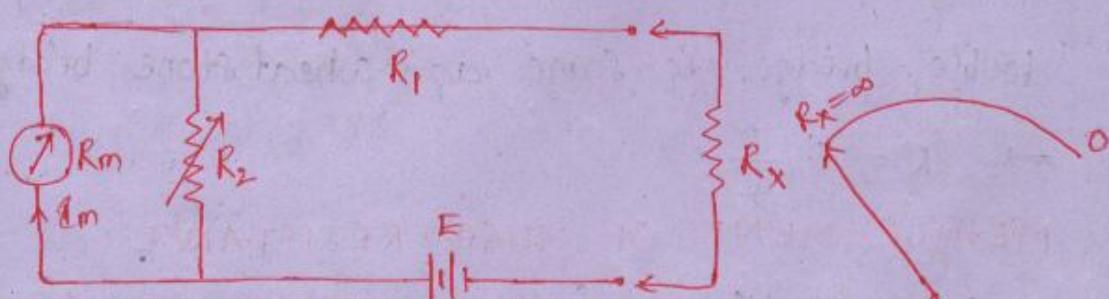
SHUNT TYPE OHMMETER:



If $R_x = 0$, the current passing through the meter is zero, hence the pointer occupies left most position on the scale.

If $R_x = \infty$, then max current will pass through meter, pointer occupies right most position on the scale.

SERIES TYPE OHMMETER:-



If $R_x = \infty$, then the current passing through the meter is zero and it remains on left

most on the scale.

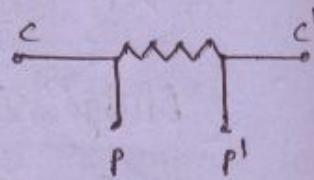
If $R_x = 0$, current passing through the meter is max, then pointer deflects to right most.

MEASUREMENT OF LOW RESISTANCE:

Low resistance is represented by

4 terminals, P & P' \rightarrow voltmeter connection,

C & C' \rightarrow Ammeter connection.



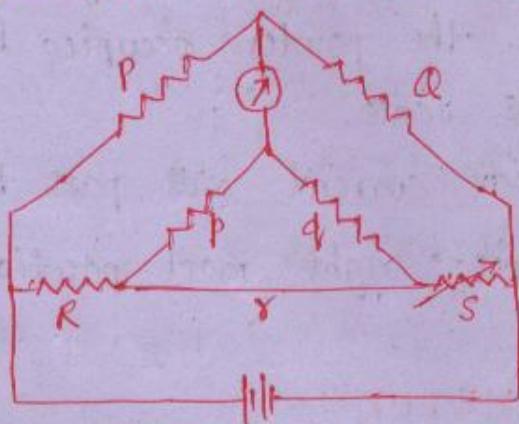
These eliminates error due to leads & contacts.

Eg:- Ammeter shunt, series, interpole and arm.

resistance of dc m/c, forward resistance of diode, ilp resistance of Amplifier.

→ Kelvin's double bridge is used to ^{the} measurement of low resistance.

KELVIN'S DOUBLE BRIDGE:



under balance condi.

$$R = s \cdot \frac{P}{Q} + \frac{qr}{p+q+r} \left(\frac{P}{Q} - \frac{r}{q} \right)$$

* If external arms ratio = inner arms ratio then Kelvin's

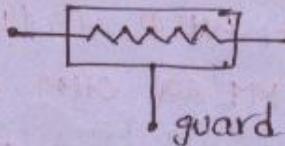
double bridge is same as Wheatstone bridge.

$$\Rightarrow R = s \cdot \frac{P}{Q}$$

MEASUREMENT OF HIGH RESISTANCE:

Eg:- Insulation resistance, Reverse resistance of diode, ilp resistance of amplifier.

High resistance is represented by 3 terminals resistive element.

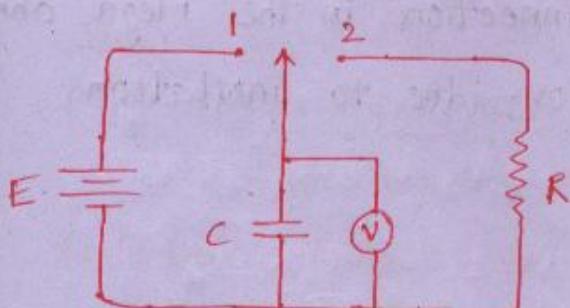


3rd terminal is guard terminal, and it is useful for eliminating errors due to insulation.
 → High resistance can be measured by

(1). Direct deflection method :-

This method is suitable for measurement of volume resistivity, surface resistivity of any insulating material available in sheet form.

(2). LOSS OF CHARGE METHOD:



capacitor gets charge towards supply voltage by connecting to pos. 1.

At pos. 2, capacitor starts discharging through unknown resistance.

Let v be the voltage across capacitor after a finite time T .

$$e = E \cdot e^{-t/RC}$$

$$R = \frac{T}{C \cdot 2.303 \log_{10} \frac{E}{v}}$$

$$\text{At } t = T; e = v$$

$$v = E \cdot e^{-T/RC}$$

$$\Rightarrow \frac{v}{E} = e^{-T/RC}$$

$$\Rightarrow e^{T/RC} = \frac{E}{v}$$

$$\Rightarrow \frac{T}{RC} = \ln \frac{E}{v}$$

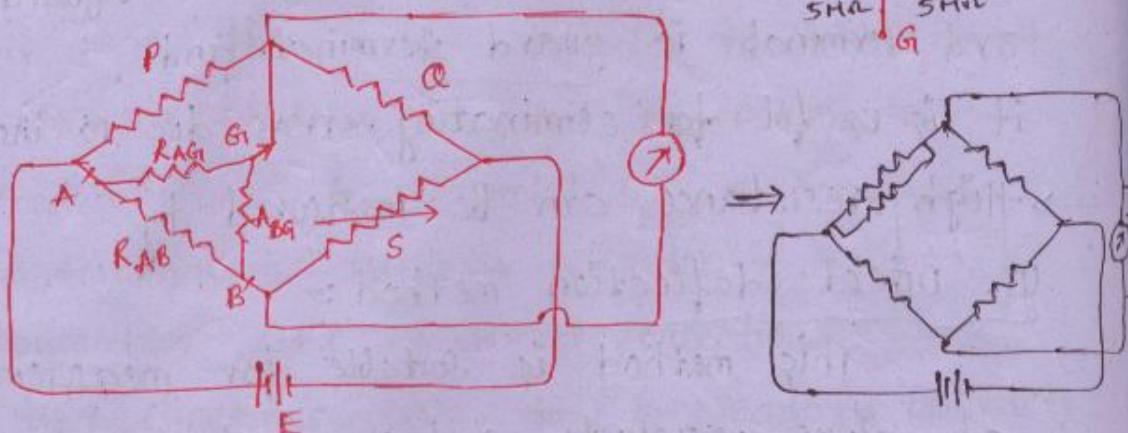
$$T = RC \cdot \ln \frac{E}{v}$$

$$\log_{10} x = 0.4343 \ln x$$

* WED. 19/11/08 *

MEGA OHM BRIDGE:

If it is measured with Wheatstone
then it will give 5M Ω but with guard \rightarrow 10M Ω .



- (1). Wheatstone bridge with guard terminal is the Megohm bridge.
- (2). Guard terminal connection in the Mega ohm bridge eliminates error due to insulation resistance.

MEGGER:

- (1). Operating voltage of the megger is more than the multimeter. It may be 500V, 1000V, 2000V, 5000V etc.
- (2). Due to high operating voltage it results into finite value of current due to unknown resistance.
- (3). Megger consists of self driven generator or pre charged capacitor for generating high voltage.
- (4). Its principle based on Ratiometer Ohmmeter.

AC BRIDGES:

APPLICATIONS:

Measurement of inductance, capacitance, freq., Q-factor, D-factor, dielectric const. of insulating materials.

DETECTORS:

In wheatstone bridge \rightarrow D'Arsonval Galvanometer.

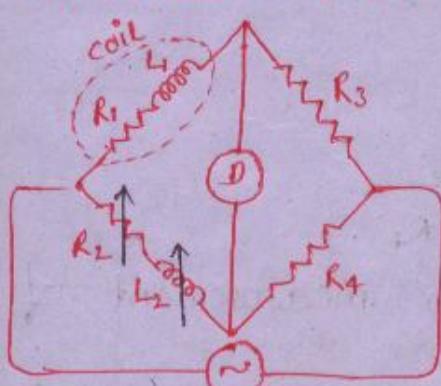
- (1). Vibration galvanometer
- (2). Head phones
- (3). Tunable amplifier

SOURCES:

power freq. AC source, electronic oscillators
 ↑ for low freq. ↑ for more freq.

Inductance Bridges \rightarrow MATH/OM

MAXWELL'S INDUCTANCE BRIDGE:



Under balanced condi:

$$Z_1 Z_4 = Z_2 Z_3$$

$$[R_1 + j\omega L_1] R_4 = [R_2 + j\omega L_2] R_3$$

Equate real parts,

$$R_1 R_4 = R_2 R_3$$

$$\Rightarrow R_1 = \frac{R_2 R_3}{R_4} = \frac{R_3}{R_4} \cdot R_2$$

equating d.m.a. parts

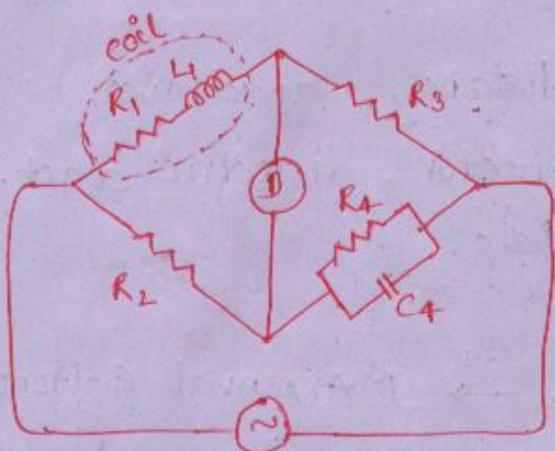
$$\omega L_1 R_4 = \omega L_2 R_3$$

$$\Rightarrow L_1 = \frac{R_3}{R_4} \cdot L_2$$

Variable quantities : R_2, L_2

Balanced eq.g are ind. in nature hence balance can be achieved very easily

MAXWELL'S INDUCTANCE - CAPACITANCE BRIDGE:



under balance condition :

$$Z_1 Z_4 = Z_2 Z_3$$

$$Z = \frac{R_4}{R + \frac{1}{j\omega C}}$$

$$Z_1 Z_4 = Z_2 Z_3$$

$$(R_1 + j\omega L_1) \left(\frac{R_4}{1 + j\omega C_4 R_4} \right) = R_2 R_3 = \frac{R}{1 + j\omega R C}$$

$$\Rightarrow (R_1 + j\omega L_1) R_4 = R_2 R_3 (1 + j\omega R_4 C_4)$$

equate Real ,

$$R_1 R_4 = R_2 R_3$$

$$\Rightarrow R_1 = \frac{R_3}{R_4} \cdot R_2$$

Q-factor:

$$\frac{\omega L_1}{R_1}$$

$$= \omega R_2 R_3 C_4 \times \frac{R_4}{R_3 R_2}$$

$$\Rightarrow Q\text{-factor} = \omega C_4 R_4.$$

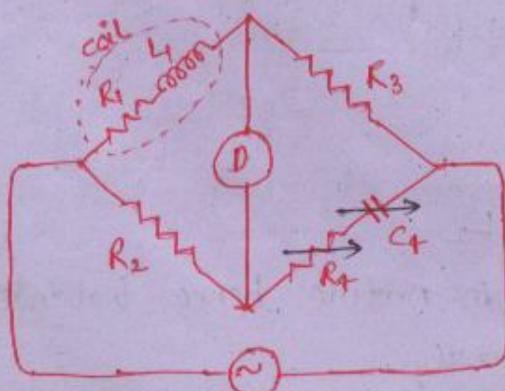
equate imaginary ,

$$\omega L_1 R_4 = \omega R_4 C_4 R_2 R_3$$

$$\Rightarrow L_1 = R_2 R_3 \cdot C_4$$

this bridge is suitable for measurement of low Q coils [$Q < 10$].

HAY'S BRIDGE:



Under balance condition

$$Z_1 Z_4 = Z_2 Z_3$$

$$(R_1 + j\omega L_1)(R_4 + \frac{1}{j\omega C_4}) = R_2 R_3$$

$$\Rightarrow (R_1 + j\omega L_1)(1 + j\omega R_4 C_4) = j\omega R_2 R_3 C_4$$

Equate real parts,

$$R_1 - \omega^2 L_1 R_4 C_4 = 0$$

$$\Rightarrow R_1 = \omega^2 L_1 C_4 R_4$$

$$R_1 = \omega^2 C_4 R_4 \times \frac{R_2 R_3 C_4}{1 + \omega^2 R_4^2 C_4^2}$$

$$R_1 = \frac{\omega^2 R_2 R_3 R_4 C_4^2}{1 + \omega^2 R_4^2 C_4^2}$$

α -factor: $\frac{\omega L_1}{R_1}$

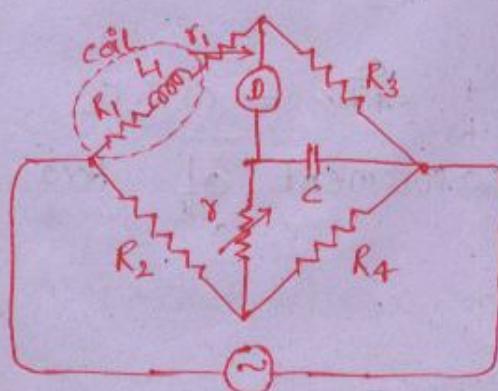
$$= \omega \cdot \frac{R_2 R_3 C_4}{1 + \omega^2 R_4^2 C_4^2} \times \frac{1 + \omega^2 R_4^2 C_4^2}{\omega^2 R_2 R_3 R_4 C_4^2}$$

α -factor = $\frac{1}{\omega R_4 C_4}$

It is suitable for the measurement of high α -coil [$\alpha > 10$].

Balance eq-s are not ind. hence it is very diff. to get the balance of the bridge.

ANDERSON'S BRIDGE:



Under balanced condi.

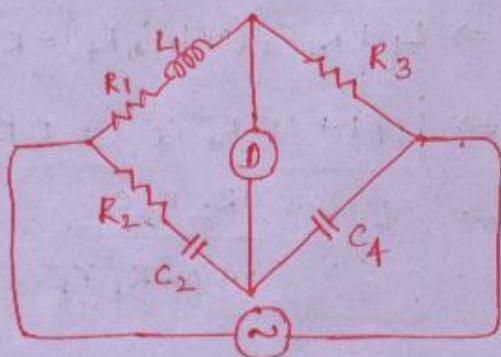
$$R_1 = \frac{R_2 R_3}{R_4} - r_1$$

$$L_1 = C \frac{R_3}{R_4} \left[r(R_2 + R_4) + R_2 R_4 \right]$$

It is very difficult to derive the balance eqn.

It is very easy to achieve balance of bridge since it employs 2 variable resistances for getting balance.

OWEN'S BRIDGE:



This is only ^{inductance} bridge which consists of two capacitances.

under balance condi.

$$Z_1 Z_4 = Z_2 Z_3$$

$$(R_1 + j\omega L_1) \left(\frac{1}{j\omega C_4} \right) = R_3 \left[R_2 + \frac{1}{j\omega C_2} \right]$$

$$\Rightarrow \frac{R_1}{j\omega C_4} + \frac{L_1}{C_4} = R_2 R_3 + \frac{R_3}{j\omega C_2}$$

equate real parts,

$$\frac{L_1}{C_4} = R_2 R_3$$

$$\Rightarrow L_1 = R_2 R_3 C_4$$

$$Q\text{-factor} = \frac{\omega L_1}{R_1}$$

$$= \frac{\omega}{\omega} \cdot \frac{R_2 R_3 C_4}{C_4 \cdot R_3} \cancel{R_1 R_3} = \omega R_2 C_2$$

equate imaginary,

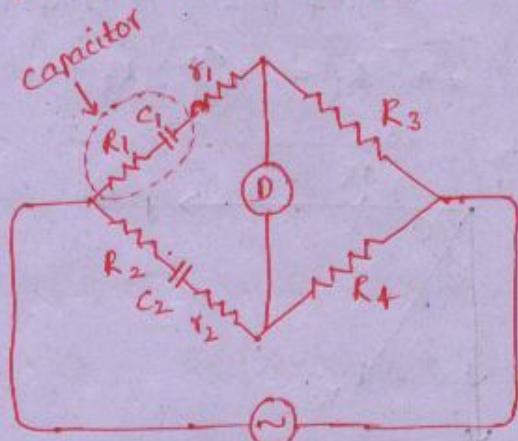
$$\frac{R_1}{\omega C_4} = \frac{R_3}{\omega C_2}$$

$$\Rightarrow R_1 = \frac{C_4}{C_2} \cdot R_3$$

suitable for the measurement of ~~loss~~
Q-coil.

CAPACITANCE BRIDGES:

DESAUTY'S BRIDGE:



under balance condition,

$$Z_1 Z_4 = Z_2 Z_3$$

$$(R_1 + r_1 + \frac{1}{j\omega C_1}) R_4 = (R_2 + r_2 + \frac{1}{j\omega C_2}) R_3$$

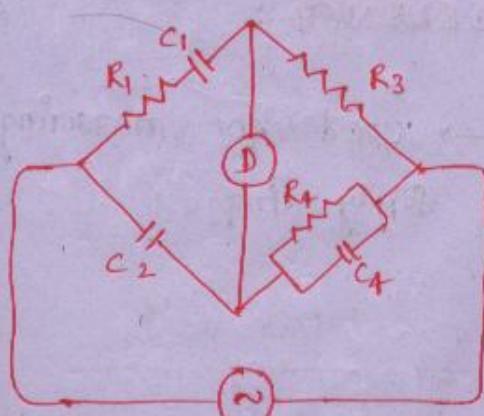
equate real parts,

$$(R_1 + r_1) R_4 = (R_2 + r_2) R_3$$

$$\Rightarrow R_1 = \frac{R_3}{R_4} (R_2 + r_2) - r_1 \quad \Rightarrow \frac{R_4}{C_1} = \frac{R_3}{C_2}$$

It is suitable for the measurement of practical capacitor.

SCHERRING BRIDGE:



→ Having 3 capacitors.

under balance condi.

$$Z_1 Z_4 = Z_2 Z_3$$

$$\left(R_1 + \frac{1}{j\omega C_1} \right) \left(\frac{R_4}{1 + j\omega R_4 C_4} \right) = \frac{R_3}{j\omega C_2}$$

$$\Rightarrow \left(\frac{1 + j\omega R_1 C_1}{j\omega C_1} \right) \left(\frac{R_4}{1 + j\omega R_4 C_4} \right) = \frac{R_3}{j\omega C_2}$$

$$\Rightarrow (1 + j\omega R_1 C_1) R_4 C_2 = R_3 C_1 (1 + j\omega R_4 C_4)$$

Equate real parts,

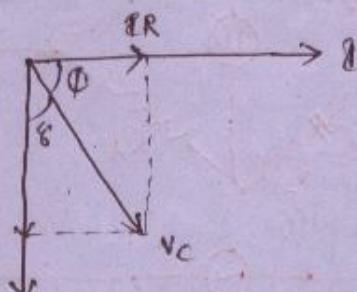
$$R_1 C_2 = R_3 C_1$$

$$\Rightarrow C_1 = \frac{R_4}{R_3} C_2$$

Equate imaginary,

$$\omega R_1 R_4 C_1 C_2 = \omega R_3 R_4 C_1 C_2$$

$$\Rightarrow R_1 = \frac{C_4}{C_2} \cdot R_3$$



$$\text{Loss angle } (\theta) = 90^\circ - \phi$$

$$D\text{-factor} = \tan \theta$$

$$= \frac{IR}{I/\omega C}$$

$$\Rightarrow D\text{-factor} = \omega R C. \quad [\text{Dissipation factor}]$$

$$D\text{-factor} = \omega R_1 C_1$$

$$= \omega \cdot \frac{C_4}{C_2} \cdot R_3 \cdot \frac{R_4}{R_3} \cdot C_2$$

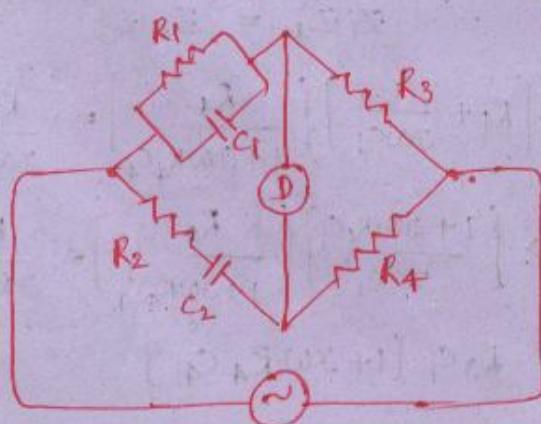
$$= \omega \cdot C_4 R_4$$

for the measurement of low capacitances,
high voltage Schering bridge is preferable.
wagner earth device is used to protect the
operator under open circuit condition.

MEASUREMENT OF FREQUENCY:

WIEN'S BRIDGE:

→ Used for measuring supply freq.



Under balance condition,

$$Z_1 Z_4 = Z_2 Z_3$$

$$\left[\frac{R_1}{1+j\omega R_1 C_1} \right] R_4 = \left[R_2 + \frac{1}{j\omega C_2} \right] \cdot R_3$$

$$\Rightarrow R_1 R_4 (j\omega C_2) = (1 + j\omega R_2 C_2) R_3 (1 + j\omega R_1 C_1)$$

Equate real parts,

$$0 = R_3 [1 - \omega^2 R_1 R_2 C_1 C_2]$$

$$\Rightarrow 1 - \omega^2 R_1 R_2 C_1 C_2 = 0.$$

$$\Rightarrow \omega = \frac{1}{\sqrt{R_1 R_2 C_1 C_2}}$$

$$\Rightarrow f = \frac{1}{2\pi \sqrt{R_1 R_2 C_1 C_2}}; \text{ when } R_1 = R_2 = R \text{ and } C_1 = C_2 = C, \text{ then } f = \frac{1}{2\pi RC}$$

(1). Harmonic distortion analyser

(2). Audio & high freq. oscillator.

* THU. 20/11/08 *

MUTUAL INDUCTANCE BRIDGES:

(1). Heaviside Mutual Inductance bridge

(2). Campbell's Modification of Heaviside bridge

(3). Heaviside campbell's bridge.

(4). Carey foster bridge - Hodweller bridge

3.1).

$$R_V = 500 \Omega$$

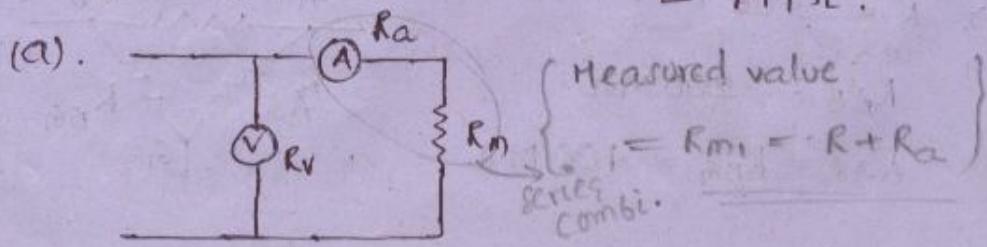
$$R_{M1} = \frac{20}{0.1} = 200 \Omega$$

$$R_a = 1 \Omega$$

$$R = R_{M1} - R_a$$

$$I = 0.1 A$$

$$= 199 \Omega$$



(b).

$$R_{m2} = \frac{20}{0.1} = 200 \Omega$$

$$\text{Req'd.} \left[\frac{1}{R_{m2}} = \frac{1}{R} + \frac{1}{R_V} \right]$$

$$R = \sqrt{R_a R_V}$$

$$= \sqrt{1 \times 500}$$

$$\Rightarrow \frac{1}{200} = \frac{1}{R} + \frac{1}{500}$$

$$\Rightarrow R = 333.33 \Omega.$$

$$= 22.36 \Omega.$$

3.2) $S = 100 \text{ k}\Omega$

$$G = 2000 \Omega$$

$$\frac{\delta_R}{\delta_s} = 46 \text{ div}$$

$$\frac{\delta_s}{\delta_s} = 40 \text{ div}$$

$$\frac{\delta_R}{\delta_s} = \frac{s+G}{R+G}$$

$$\Rightarrow \frac{46}{40} = \frac{100+2}{R+2}$$

$$\Rightarrow R = 86.7 \text{ k}\Omega.$$

3.3) $S = 500 \text{ k}\Omega$

$$G = 10 \text{ k}\Omega$$

$$\frac{\delta_R}{\delta_s} = 41; \quad \frac{\delta_s}{\delta_s} = 51.$$

$$\frac{\delta_R}{\delta_s} = \frac{s+G}{R+G}$$

$$\Rightarrow \frac{41}{51} = \frac{R+10}{500+10}$$

$$\Rightarrow R = 400 \text{ k}\Omega.$$

3.5) $R_{AB} = 200 \text{ M}\Omega$

$$R_{AG} = R_{BG} = 400 \text{ M}\Omega$$

3.4) $P = 100 \Omega$

$$Q = 1000 \Omega$$

$$P = 99.92 \Omega$$

$$q = 1000.6 \Omega$$

$$r = 0.1 \Omega$$

$$s = 0.00377 \Omega$$

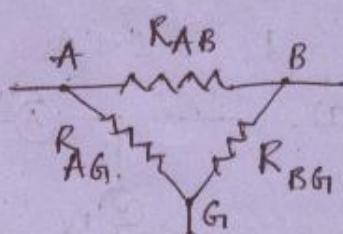
$$R = s \cdot \frac{P}{Q} + \frac{qr}{P+q+r} \left(\frac{P}{Q} - \frac{p}{q} \right)$$

$$= \frac{100}{1000} \times 0.00377$$

$$+ \frac{1000.6 \times 0.1}{99.92 + 1000.6 + 0.1}$$

$$* \left[\frac{100}{1000} - \frac{99.92}{1000.6} \right]$$

$$= 389.7 \mu\Omega$$



$$R_m = 200 \parallel [400 + 400]$$

$$= 160 \text{ M}\Omega$$

$$\therefore \text{Error} = \frac{A_m - A_t}{A_t} \times 100$$

$$= \frac{160 - 200}{200} \times 100$$

$$= -20\%$$

3.6).

$$C = 6 \times 10^{-4} \mu F$$

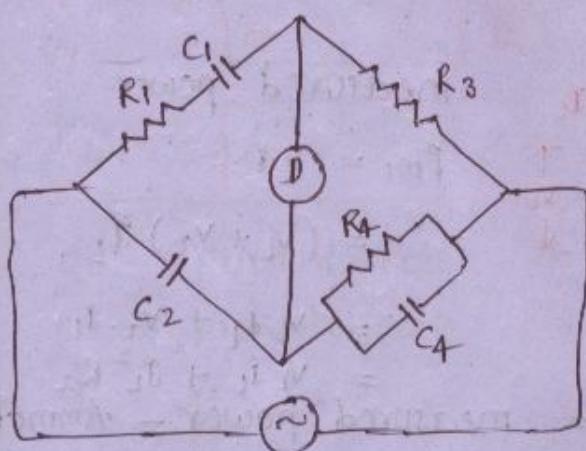
$$E = 250 \text{ V}$$

$$V = 92 \text{ V}$$

$$t = 60 \text{ sec.}$$

$$R = \frac{t}{C \cdot \log_e \left(\frac{E}{V} \right)} = \frac{60}{6 \times 10^{-4} \times 10^{-6} \ln \left[\frac{250}{92} \right]} \\ = 1,00,000 \text{ M}\Omega.$$

3.8).



$$C_2 = 106 \text{ pF}$$

$$R_4 = 1000/\pi \text{ }\Omega$$

$$C_4 = 0.5 \text{ mF}$$

$$R_3 = 260 \text{ }\Omega$$

$$R_1 = \frac{C_4}{C_2} \times R_3 \\ = \frac{0.5 \times 10^{-6}}{106 \times 10^{-12}} \times 260 \\ = 1.22 \text{ M}\Omega$$

$$C_1 = \frac{R_4 \times C_2}{R_3} \\ = \frac{1000/\pi}{260} \times 106 \times 10^{-12} \\ = 1.29 \text{ pF}$$

$$\rho_f = \cos\phi = \frac{R}{Z}$$

$$X_C = \frac{1}{\omega C} = \frac{1}{2\pi \times 50 \times 129 \times 10^{12}} = 24.6 \text{ M}\Omega$$

$$\tan\phi = \frac{X_C}{R}$$

$$= \frac{24.6}{1.22} \Rightarrow \phi = 87.16^\circ$$

$$\rho_f = \cos(87.16)$$

$$= 0.05$$

$$C = \frac{\epsilon A}{d}$$

$$\Rightarrow 129 \times 10^{12} = \frac{8.85 \times 10^{-12} \times \epsilon_r \times \frac{\pi (0.12)^2}{4}}{4.5 \times 10^3}$$

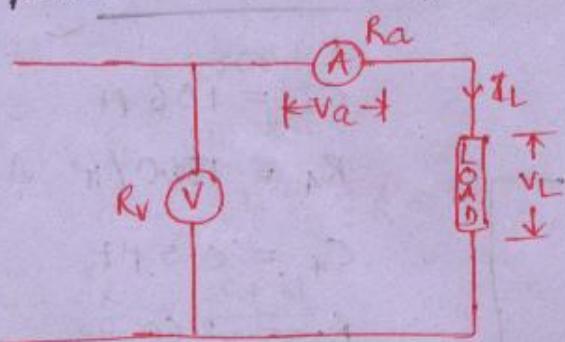
$$\Rightarrow \epsilon_r = 5.8$$

Author: problems by
parker smith

MEASUREMENT OF POWER:

MEASUREMENT OF POWER IN DC CIRCUIT:

- * A-V method is useful to measure the power in DC ckt.



measured power

$$P_{m1} = V I_A$$

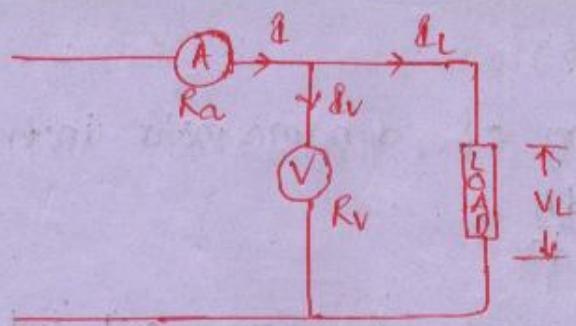
$$= (V_L + v_a) I_L$$

$$= V_L I_L + v_a I_L$$

$$= V_L I_L + I_L^2 R_a$$

$$\Rightarrow * \text{True power } (P_t) = \text{measured power} - \text{Ammeter power loss.}$$

$$\Rightarrow P_t = P_{m1} - P_a.$$

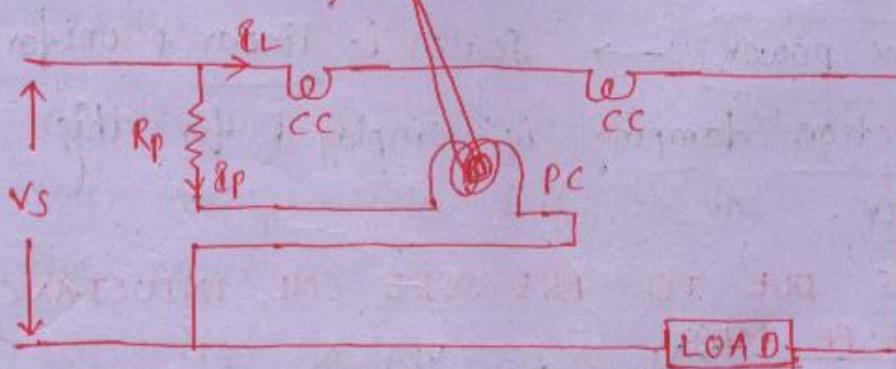


$$\begin{aligned}
 P_{m2} &= V \delta \\
 &= V_L (\delta_L + \delta_V) \\
 &= V_L \delta_L + V_L \cdot \delta_V \\
 &= V_L \delta_L + V_L \cdot \frac{V_L}{R_V} \\
 &= V_L \delta_L + \frac{V_L^2}{R_V}
 \end{aligned}$$

- * True power = measured power - power loss in voltmeter.
- * In both methods measured power is more than the true power. true power can be obtained by subtracting power loss of the meter connected near to load.

MEASUREMENT OF POWER IN 1-Φ AC:

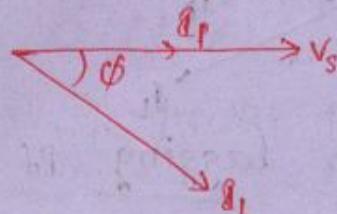
Electro dynamo meter type is useful for the measurement of power.



CC - current coil

PC - pressure coil

$$\delta_P = \frac{V_s}{R_p}$$



Wattmeter consists of 2 coils
fixed coil is in series with load and carries load current hence it is known as cc.
Moving coil is connected across supply lines and carries current proportional to supply volt. hence

it is known as PC.

from the theory of dynamo meter instr.

$$T_d = \theta_1 \theta_2 \cos \alpha \cdot \frac{dH}{d\theta}$$

$$\theta_1 = \theta_L$$

$$\theta_2 = \theta_P = \frac{V_s}{R_p}$$

$$\alpha = \phi$$

[pressure coil inductance
is neglected].

$$\therefore T_d = \frac{V_s}{R_p} \cdot \theta_L \cdot \cos \phi \cdot \frac{dH}{d\theta}$$

$$T_d \propto V_s \theta_L \cos \phi$$

$$T_d \propto \text{power}$$

Springs are used for control purpose, hence

$$T_c \propto \theta \Rightarrow T_c = k_c \theta$$

At balanced condition,

$$T_d = T_c$$

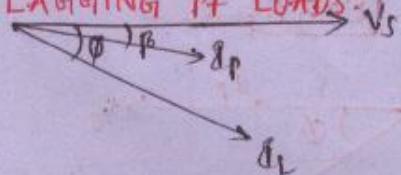
$$\Rightarrow k_c \cdot \text{power} = k_c \cdot \theta$$

$$\Rightarrow \theta \propto \text{power} \rightarrow \text{Scale is linear & uniform.}$$

* Air friction damping is employed for this wattmeter.

ERRORS DUE TO PRESSURE COIL INDUCTANCE:

LAGGING PF LOADS:



$$\theta_P = \frac{V_s}{Z_p}$$

$$\cos \beta = \frac{R_p}{Z_p}$$

on lagging pf loads, effective angles seen by currents (α) is $<$ pf angle hence wattmeter shows more reading

$$\alpha = \phi - \beta$$

$$\text{wattmeter reading (Am)} = \theta_L \theta_P \cos \alpha \cdot \frac{dH}{d\theta}$$

$$(\text{Pm}) = \theta_L \cdot \frac{V_s}{Z_p} \cos(\phi - \beta) \cdot \frac{dH}{d\theta}$$

$$= \frac{V_s \cdot I_L}{R_p} \cdot \cos \beta \cdot \cos(\phi - \beta) \cdot \frac{dH}{d\theta}$$

$$\text{True power } (P_t) = I_L \cdot I_p \cdot \cos \alpha \cdot \frac{dH}{d\theta}$$

$$= \frac{V_s \cdot I_L}{R_p} \cdot \cos \alpha \cdot \frac{dH}{d\theta}$$

$$\frac{\text{True power}}{\text{Wattmeter reading}} = \frac{\frac{V_s \cdot I_L}{R_p} \cdot \cos \alpha \cdot \frac{dH}{d\theta}}{\frac{V_s \cdot I_L}{R_p} \cdot \cos \beta \cdot \cos(\phi - \beta) \cdot \frac{dH}{d\theta}}$$

$$= \frac{\cos \alpha}{\cos \beta \cdot \cos(\phi - \beta)}$$

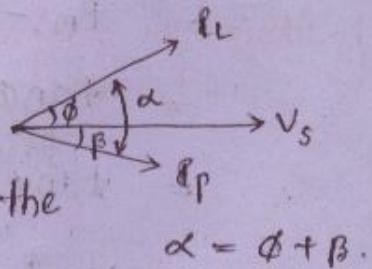
$$\Rightarrow P_t = \frac{\cos \alpha}{\cos \beta \cdot \cos(\phi - \beta)} \cdot P_m$$

↑
correction factor.

on lagging pf loads, correction factor is always less than 1.

LEADING PF LOADS:

on leading pf loads, watt meter always shows less than the true power.



$$\text{correction factor} = \frac{\cos \alpha}{\cos \beta \cdot \cos(\phi + \beta)}$$

On leading pf loads, cf is greater than 1.

$$\frac{P_t}{P_m} = \frac{\cos \alpha}{\cos \beta \cdot \cos(\phi + \beta)}$$

$$\approx \frac{\cos \alpha}{\cos(\phi - \beta)}$$

$$\approx \frac{\cos \alpha}{(\cos \phi \cdot \cos \beta + \sin \phi \cdot \sin \beta)}$$

$$= \frac{\cos\phi}{\cos\phi \cdot \cos\beta [1 + \tan\phi \tan\beta]}$$

$$\left[\frac{P_m}{P_t} \right] = \frac{1}{1 + \tan\phi \tan\beta} = \frac{P_t}{P_m}$$

$$\Rightarrow P_t [1 + \tan\phi \tan\beta] = P_m$$

$$\Rightarrow P_m - P_t = \tan\phi \tan\beta \times P_t$$

$$\% \text{ error} = \frac{A_m - A_t}{A_t}$$

$$= \frac{P_m - P_t}{P_t}$$

$$= \tan\phi \tan\beta$$

$$\boxed{\% \text{ error} = \tan\phi \tan\beta.}$$

$$\underline{\text{error}} = A_m - A_t$$

$$= P_m - P_t$$

$$= \underline{\tan\phi \tan\beta \times \text{true power}}$$

$$= \tan\phi \tan\beta \times V_s I_L \cos\phi$$

$$= \boxed{V_s \cdot I_L \cdot \sin\phi \tan\beta.}$$

FERRO DYNAMIC WATT METER:

operating torque in electro dynamo meter is weak, due to presence of air cored coils.

So improve the strength of HF, iron cored coils may be employed. Then this meter is known as ferro dynamic wattmeter.

LOW PF WATT METER: $T_d = \frac{V_s}{R_p} \cdot R_e \cdot \cos\phi$ (0.01)

If normal wattmeter is employed for the measurement of power in low pf ckt then the amount of T_d is very less which may not be able to deflect the moving system.

→ The following modifications are suggested in low pf wattmeter.

(1). Reduce the resistance value connected in series with PC (R_p). Due to this T_d magnitude can be increased.

(2). By applying (employing) small control torque. Hall effect multiplier is useful to generate an electrical signal (hall volt.) (V_H) \propto to power consumption in the circuit.

$$V_H \propto k_H B i t \rightarrow \left\{ \begin{array}{l} \text{for Automatic} \\ \text{correction} \end{array} \right\}$$

where t = thickness of element

$B \propto$ voltage

$i \propto i_L$

$$V_H \propto V_s \cdot i_L$$

$\Rightarrow V_H \propto$ power.

wattmeter along with CT & PT is used for the measurement of large amount of power circuits.

* power = ratio of CT \times ratio of PT

\times wattmeter reading

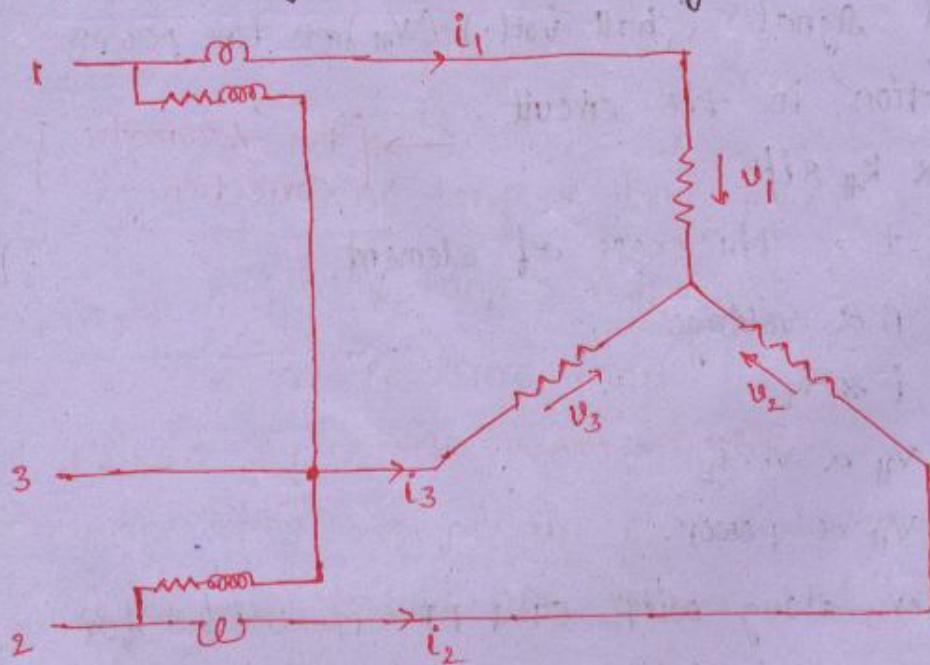
$$\text{where } k = \frac{\cos\phi}{\cos\beta \cdot \cos(\phi + B)}$$

MEASUREMENT OF POWER IN POLY PHASE CIRCUITS:

Blondel's theorem is useful to decide the no. of wattmeters to be connected in the measurement of power of poly phase circuit.

THEOREM:

If a nw is supplied through 'n' conductors, the total power is measured by summing the readings of 'n' wattmeters so arranged that current element of wattmeter is in each line and corr. voltage element is connected b/w that line and a common point, if the common point is located on one of the line then the power may be measured by 'n-1' wattmeters.



$$P_1 \propto i_1 v_{13}$$

$$\propto i_1 (v_1 - v_3)$$

$$P_2 \propto i_2 v_{23}$$

$$\propto i_2 (v_2 - v_3)$$

$$P_1 + P_2 = i_1 (v_1 - v_3) + i_2 (v_2 - v_3)$$

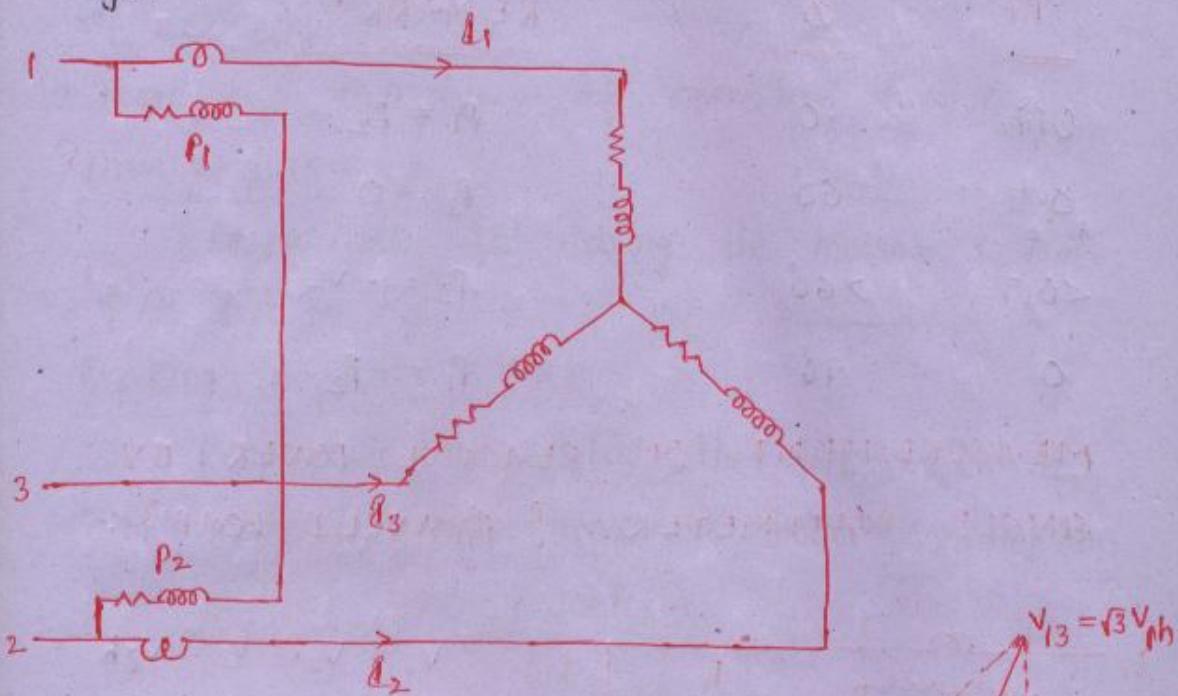
$$= i_1 v_1 + i_2 v_2 - v_3 (i_1 + i_2)$$

TS:

$$= v_1 i_1 + v_2 i_2 + v_3 i_3 \quad \{ \because i_1 + i_2 + i_3 = 0 \}$$

$$\Rightarrow P_1 + P_2 = P.$$

Two wattmeter method is suitable for measurement of power in both balanced & unbalanced 3-φ system.



$$v_1 = v_2 = v_3 = v_{ph}$$

$$\delta_1 = \delta_2 = \delta_3 = \delta_{ph}$$

$$\text{wattmeter reading } P_1 = \delta_1 v_{ph} \cos(\nu_{13}, \delta_1)$$

$$P_1 = \delta_{ph} \cdot \sqrt{3} \cdot v_{ph} \cdot \cos(30 - \phi)$$

$$P_1 = \sqrt{3} v_{ph} \cdot \delta_{ph} \cdot \cos(30 - \phi)$$

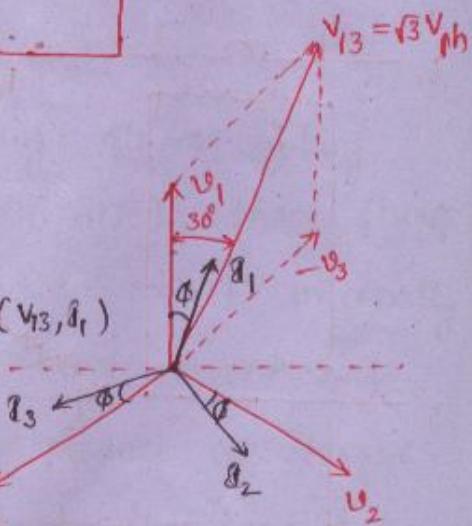
$$\text{wattmeter reading } P_2 = \delta_2 v_{23} \cdot \cos(\nu_{23}, \delta_2)$$

$$P_2 = \sqrt{3} v_{ph} \cdot \delta_{ph} \cdot \cos(30 + \phi)$$

$$P_1 + P_2 = 3 \cdot v_{ph} \cdot \delta_{ph} \cdot \cos \phi$$

= total power

$$\therefore P = P_1 + P_2$$



$$P = \sqrt{3} v_{ph} \delta_{ph} \cos \phi$$

$$P_1 - P_2 = \sqrt{3} \cdot v_{ph} \cdot \delta_{ph} \cdot \sin \phi$$

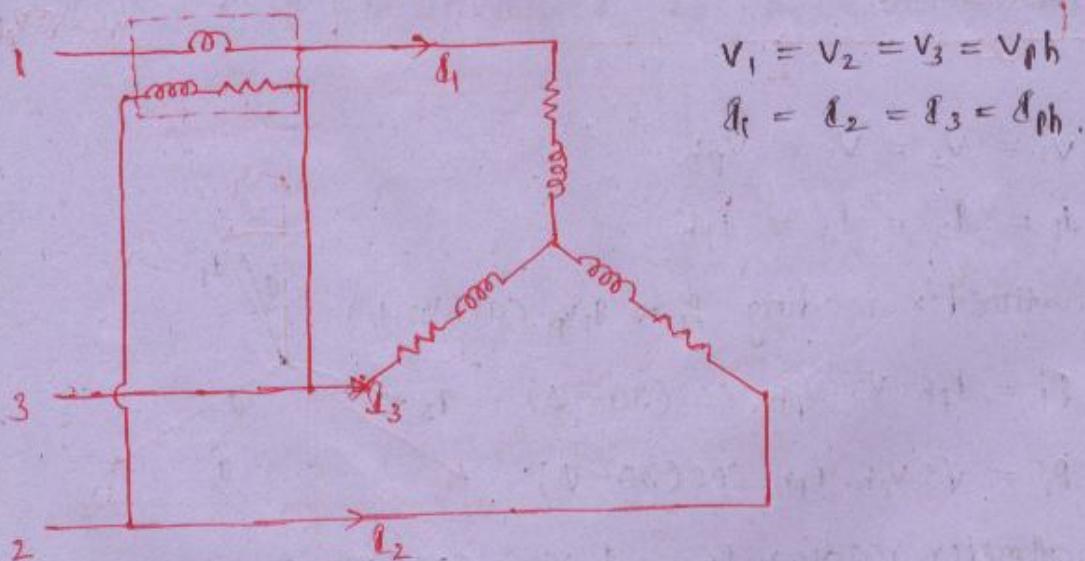
$$\text{Reactive power (Q)} = \sqrt{3} \cdot (P_1 - P_2)$$

$$\frac{Q}{P} = \frac{\sin \phi}{\cos \phi} = \frac{\sqrt{3}(P_1 - P_2)}{P_1 + P_2}$$

$$\Rightarrow \tan \phi = \frac{\sqrt{3}(P_1 - P_2)}{P_1 + P_2}$$

<u>PF</u>	<u>ϕ</u>	<u>REMARKS.</u>
UPF	0	$P_1 = P_2$
0.5	60°	$P_2 = 0$
<0.5	>60°	$P_2 = -ve$
0	90°	$P_1 = -P_2$

MEASUREMENT OF REACTIVE POWER BY SINGLE WATTMETER [BALANCED LOAD] :



wattmeter reading $P = \delta_1 V_{23} \cos(\delta_{23}, \delta_1)$

$$= \delta_{ph} \cdot \sqrt{3} \cdot V_{ph} \cdot \cos(90 - \phi)$$

$$= \sqrt{3} \cdot V_{ph} \cdot \delta_{ph} \cdot \sin \phi$$

Reactive power (Q) = $\sqrt{3} \cdot \text{wattmeter reading}$

MEASUREMENT OF ENERGY:

→ Integrating type instrg are useful for the measurement of energy.

Motor meters are useful for the measurement of energy.

→ There are two types of operating torques:

Driving torque:-

Responsible for driving the moving system.

[Al disc].

Braking torque:-

Responsible to control the disc movement and make it proportional to power consumption in case of energy meter.

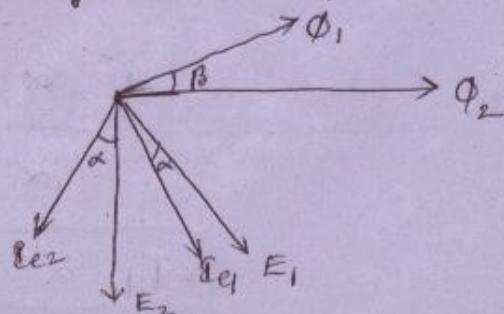
THEORY OF INDUCTION:

It consists of 2 alternating fluxes linking with common conducting media (disc). These fluxes produce 2 emf's (eddy emf's), which internally circulates 2 eddy currents. First current I_1 & second flux ϕ_2 interact to produce one torque T_{d1} , second current I_2 and first flux ϕ_1 interact to produce another torque T_{d2} . These two torques act in opp. dire to produce resultant torque known as driving torque T_d .

$$e_1 \propto \frac{d\psi_1}{dt}$$

$$e_1 \propto \frac{d\phi_1}{dt}$$

$$\phi_1 = \phi_{m1} \sin \omega t$$



$$\begin{aligned}\phi_2 &= \phi_{m2} \sin(\omega t - \beta) & e_2 &\propto \frac{d\phi_2}{dt} \\ \Rightarrow e_1 &\propto \phi_{m1} \omega \cdot \frac{\cos}{\sin} \omega t & &\propto \phi_{m2} \omega \cdot \cos(\omega t - \beta) \\ E_1 &\propto \frac{\phi_{m1} \omega}{\sqrt{2}} & E_2 &\propto \frac{\phi_{m2} \omega}{\sqrt{2}} \\ &\propto \phi_1 \cdot 2\pi f & &\propto \phi_2 \cdot 2\pi f \\ E_1 &\propto \phi_1 \cdot f & &\propto \phi_2 \cdot f \\ \theta_{e1} &\propto \frac{\phi_1 t}{Z} & \theta_{e2} &\propto \frac{\phi_2 t}{Z}\end{aligned}$$

Avg. deflection torque produced by interaction of θ_{e1} & ϕ_2 is T_{d1} .

$$T_{d1} \propto \phi_2 \theta_{e1} \cos(\phi_2, \theta_{e1})$$

$$T_{d1} \propto \phi_2 \theta_{e1} \cos(90 - \beta + \alpha) \Rightarrow T_{d1} \propto \frac{\phi_1 \phi_2 f}{Z} \cos(90 - \beta + \alpha)$$

Avg. deflection torque T_{d2} produced by interaction θ_{e2} & ϕ_1 is,

$$T_{d2} \propto \phi_1 \theta_{e2} \cos(\phi_1, \theta_{e2})$$

$$\propto \phi_1 \theta_{e2} \cdot \cos(90 + \beta + \alpha)$$

$$\propto \frac{\phi_1 \phi_2 f}{Z} \cdot \cos(90 + \beta + \alpha)$$

Driving torque $T_d = T_{d1} - T_{d2}$

$$\propto \frac{\phi_1 \phi_2 f}{Z} \{ \cos(90 - \beta + \alpha) \}$$

$$- \cos(90 + \beta + \alpha)$$

$$\propto \frac{\phi_1 \phi_2 f}{Z} \{ \sin(\beta - \alpha) + \sin(\beta + \alpha) \}$$

$$\propto \frac{\phi_1 \phi_2 f}{Z} \cdot 2 \sin \beta \cdot \cos \alpha$$

$$\propto \frac{\phi_1 \phi_2 f}{Z} \cdot \sin \beta \cdot \cos \alpha$$

$$T_d \propto \phi_1 \phi_2 \sin \beta$$

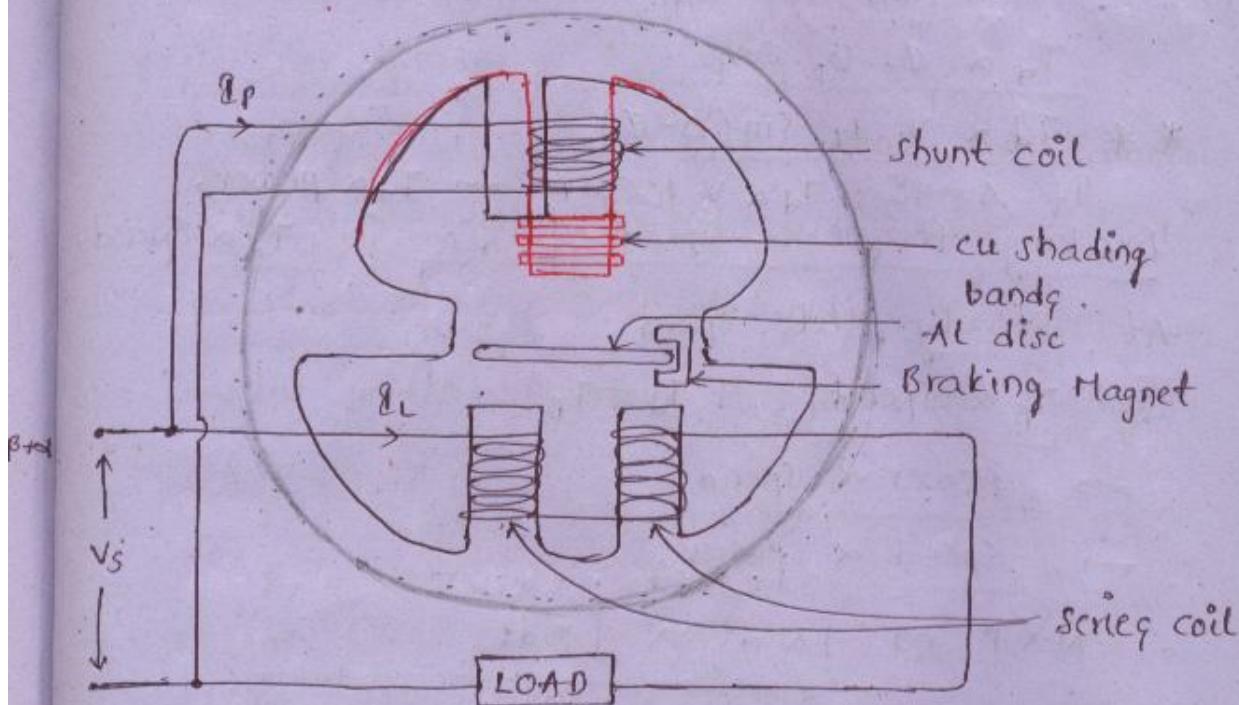
for Al disc path ' α ' is fixed hence $\cos\alpha$ and impedance can be assumed to be const.

B)

β - angle b/w two phases.

* FRI. 21/11/08 *

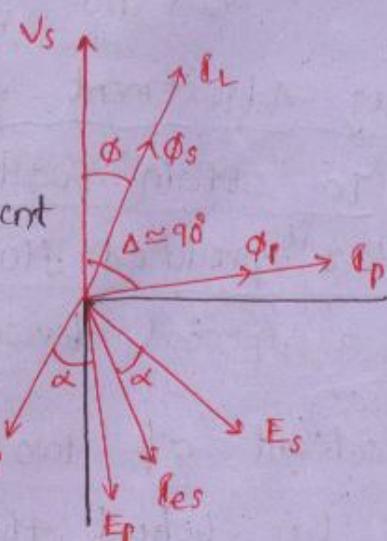
1- ϕ ENERGY METER:



Energy meter consists of,
coil in series with load
and carries the load current
is known as series coil.

coil which is connected
across supply and draws
current is known as
shunt coil.

* current through shunt coil I_p lagging V by Δ
nearly = 90° ($\Delta \approx 90^\circ$).



As per theory of Induction meter

$$T_d \propto \phi_1 \phi_2 \sin \beta$$

$$\phi_L \propto \phi_s = \phi_1$$

$$\phi_1 = \phi_s \propto \delta_L$$

$$\phi_2 = \phi_p \propto \delta_p \propto v_s$$

$$T_d \propto \phi_s \cdot \phi_p \cdot \sin \beta$$

$$** T_d \propto v_s \cdot \delta_L \sin(\Delta - \phi)$$

If $\Delta = 90^\circ$; $T_d \propto v_s \delta_L \cos \phi \rightarrow T_d \propto \text{power}$.

Braking torque \propto Speed of disc ie $T_d \propto \text{Speed}$

At steady state speed,

$$T_B \propto \text{speed} ; T_d = T_B$$

\Rightarrow power \propto speed.

\rightarrow speed \propto power.

$$\therefore N \propto r \Rightarrow \int N dt \propto \int r dt$$

\Rightarrow no. of revolutions \propto energy.

Lag Adjustment devices :-

To obtain quadrature relation b/w supply volt & its produced flux, another flux is created by a special device known as Lag adjustment device.

Resultant of two fluxes makes resultant flux 90° lag behind the supply voltage.

Eg: cu shading bands

No. of revolutions made per kWh \rightarrow meter const.

CREEPING:

Some times energy meter shows more reading under low load conditions. Record some reading under NL condi. This is known as creeping.

→ Creeping is due to,

(1). Over compensation for friction

(2). Over voltage

→ Creeping can overcome by drilling to diametrically oppo. holes on Al disc.

→ Testing of EM is carried out by indirect loading method phantom or fictitious loading.

~~4.1).~~

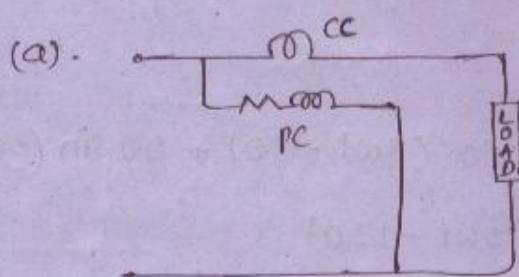
$$R_C = 0.5 \Omega$$

$$R_p = 12500 \Omega$$

$$\text{pf} = 1.$$

$$V_s = 250V$$

$$I_L = 4A$$



$$\text{Power loss in CC} = I^2 R_C$$

$$= 4^2 (0.5)$$

$$= 8 \text{ Watts}$$

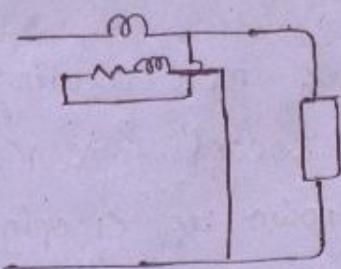
$$\% \text{ error} = \frac{A_m - A_t}{A_t}$$

$$P_t = V_s I_L \cos \phi$$

$$= 250 \times 4 \times 1 = 1000 \text{ W}$$

$$\% \text{ error} = \frac{8}{1000} \times 100$$

$$= 0.8 \%$$



$$\text{power loss in PC} = \frac{V^2}{R_p}$$

$$= \frac{250^2}{12500} = 500.$$

$$\% \text{ Error} = \frac{5}{1000} \times 100$$

$$= 0.5\%.$$

4.2). $x_p = 0.01 R_p$

(a). $\phi = \cos^{-1}(0.8)$ $\tan \beta = \frac{x_p}{R_p}$
 $= 36.86^\circ$ $= 0.01$

$$\begin{aligned}\% \text{ error} &= \tan \phi \cdot \tan \beta \times 100 \\ &= \tan 36.86^\circ \cdot \tan \beta \times 100 \\ &= 0.75\end{aligned}$$

(b). $\phi = \cos^{-1}(0.5) = 60^\circ$

$$\begin{aligned}\% \text{ error} &= \tan \phi \cdot \tan \beta \times 100 \\ &= 1.732\%\end{aligned}$$

(c). $\phi = \cos^{-1}(0.1) = 84.26^\circ$

$$\% \text{ error} = 9.95\%$$

4.3).

$$V = 100 \sin \omega t + 40 \cos(3\omega t - 30) + 50 \sin(5\omega t + 45)$$

$$i = 8 \sin \omega t + 6 \cos(5\omega t - 120)$$

$$P = \frac{1}{2\pi} \int_0^{2\pi} v \cdot i \cdot d(\omega t)$$

$$\begin{aligned}*& \frac{1}{2\pi} \int_0^{2\pi} A \sin(\omega t + \alpha) \cdot B \sin(\omega t + \beta) d(\omega t) \\ &= \frac{1}{2} AB \cos(\alpha - \beta).\end{aligned}$$

$$\begin{aligned}*& \frac{1}{2\pi} \int_0^{2\pi} A \sin(\omega t + \alpha) \cdot B \cos(\omega t + \beta) d(\omega t) \\ &= \frac{1}{2} AB \sin(\alpha - \beta).\end{aligned}$$

$$*\frac{1}{2\pi} \int_0^{2\pi} A \sin(m\omega t + \alpha) \cdot B \sin(n\omega t + \beta) d(\omega t) = 0.$$

$$*\frac{1}{2\pi} \int_0^{2\pi} A \cdot \sin(m\omega t + \alpha) \cdot B \cdot \cos(n\omega t + \beta) d(\omega t) = 0.$$

$$\therefore \text{power} = \frac{1}{2} \times 100 \times 8 \cos(0) + 0 + \\ \frac{1}{2} \times 50 \times 6 \sin(165) \\ = \underline{400} + 38.9 = 438.9 \omega$$

$$\therefore \text{fundamental} = \frac{400}{438.9} \\ = 91.13 \%$$

4.4). $P_1 = 5000 \omega$

$$P_2 = 1000 \omega$$

$$P = P_1 + P_2 = 6000 \omega$$

$$\tan \phi = \frac{\sqrt{3}(P_1 - P_2)}{P_1 + P_2}$$

$$\Rightarrow \phi = 49.1^\circ$$

$$\therefore P_f = \cos 49.1 = 0.654 \text{ lag}$$

(b). $P_1 = 5000 \omega$

$$P_2 = -1000 \omega$$

$$P = P_1 + P_2 = 4000 \omega$$

$$\tan \phi = \frac{\sqrt{3}(P_1 - P_2)}{P_1 + P_2}$$

$$\Rightarrow \phi = 69^\circ$$

$$P_f = \cos 69^\circ = 0.359 \text{ lag}$$

4.5). $P_f = 0.4$

$$P = 30 \text{ kW} = P_1 + P_2$$

$$\phi = \cos^{-1}(0.4) = 66.4^\circ$$

$$\tan \phi = \frac{\sqrt{3}(P_1 - P_2)}{P_1 + P_2}$$

$$\Rightarrow \tan 66.4 = \frac{\sqrt{3}(P_1 - P_2)}{30}$$

$$\Rightarrow P_1 - P_2 = 39.68 \text{ kW}$$

$$P_1 + P_2 = 30 \text{ kW}$$

$$\Rightarrow P_1 = 34.84 \text{ kW}$$

$$P_2 = -4.84 \text{ kW}$$

4.6). $V_L = 400 \text{ V}$

$$I_L = 30 \text{ A}$$

$$P_{\text{ph}} = V_{\text{ph}} \cdot I_{\text{ph}} \cdot \cos \phi = 5540 \text{ W}$$

$$\Rightarrow \frac{400}{\sqrt{3}} \times 30 \times \cos \phi = 5540$$

$$\Rightarrow \cos \phi = 0.8$$

$$\sin \phi = 0.6$$

$$\text{wattmeter reading} = \sqrt{3} \cdot V_{\text{ph}} \cdot I_{\text{ph}} \cdot \sin \phi$$

$$= \sqrt{3} \times \frac{400}{\sqrt{3}} \times 30 \times 0.6$$

$$= 7.2 \text{ kVAR}$$

4.7).

COMPENSATION FOR PRESSURE COIL INDUCTANCE:

[WATT METER]:

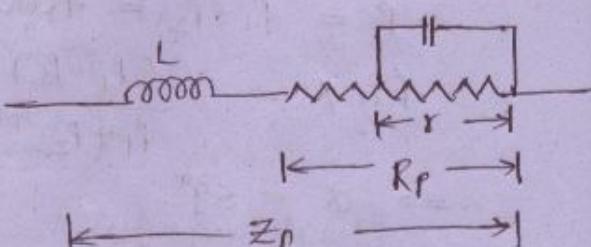
$$Z_p = R_p - r + j\omega L$$

$$+ \frac{r}{1 + j\omega RC}$$

$$= R_p - r + j\omega L + \frac{r(1 - j\omega RC)}{1 + \omega^2 R^2 C^2}$$

for power freq. $\omega^2 R^2 C^2 \ll 1$.

$$\Rightarrow Z_p = R_p - r + j\omega L + r - j\omega r^2 C$$



$$Z_p = R_p + j\omega [L - r^2 C]$$

$$\Rightarrow Z_p = R_p \quad \text{if } L = r^2 C \quad \left(\frac{L}{R} = r^2 \right)$$

$$\Rightarrow C = \frac{L}{\omega^2}$$

4.7).

$$C = 20 \text{ pF}$$

$R_s = 10000 \Omega$ ← series resistance in
 $R_p = 400 \Omega$. the pressure coil circuit.

$$C = \frac{L}{r^2}$$

$$\Rightarrow 20 \times 10^{-12} = \frac{L}{(10000)^2}$$

$$\Rightarrow L = 2 \text{ mH}$$

4.8).

4.9).

$$L_p = 8 \text{ mH}$$

$$R = 2000 \Omega$$

$$\phi = 89^\circ$$

$$f = 50 \text{ Hz}$$

$$X_p = 2\pi f \cdot L_p$$

$$= 2\pi \times 50 \times 8 \times 10^{-3}$$

$$= 2.513 \Omega$$

$$\% \text{ error} = \tan \phi \cdot \tan \beta \cdot 100$$

$$\tan \beta = \frac{X_p}{R_p} = \frac{2.513}{2000} = 0.00125$$

$$\% \text{ error} = \tan 89 \times 0.00125 \times 100$$

$$= 7.19 \%$$

$$4.10). A_m = 250 \omega = R_m$$

$$V = 200V$$

$$R_p = 2000 \Omega$$

$$\text{True power} = \frac{P_m}{\cancel{R}_x} \text{ measured power} - \text{power loss in voltage coil.}$$

$$= 250 - \frac{\frac{V^2}{R_p}}{2000}$$

$$= 230 \text{ W.}$$

5.1) Rating = 220V, 5A.

3275 rev/kwh \leftarrow meter constant.

$$\text{power} = 220 \times 5 = 1100 \text{ W.}$$

Let f_L is taken for 1 hr. then energy

$$\text{consumption} = \frac{1100}{1000} \times 1 = 1.1 \text{ kwh}$$

$$\text{No. of revolutions} = 3275 \times 1.1 = 3602.5 \text{ rev.}$$

$$\text{Speed} = \frac{3602.5}{3600} \approx 1 \text{ rps.}$$

$$I = 2.5 \text{ A}$$

$$t = 59.5 \text{ sec}$$

30 revolutions

$$\text{Energy} = \frac{220 \times 2.5}{1000} \times \frac{59.5}{3600}$$

$$= 0.00909 \text{ kwh}$$

$$\text{No. of revolutions to be made} = 0.00909 \times 3275$$

$$= 29.77$$

$$\% \text{ error} = \frac{30 - 29.77}{29.77} \times 100 = 0.77 \% \text{ fast}$$

5.2) $V = 230 \text{ V}$

$$I = 50 \text{ A}$$

61 revolutions

$$t = 37 \text{ sec.}$$

$$\text{meter constant} = 520 \text{ rev/kwh}$$

$$\text{Energy} = \frac{230 \times 50}{1000} \times \frac{37}{3600}$$

$$= 0.11819 \text{ Wh}$$

$$\begin{aligned}\text{No. of revolutions} &= 0.11819 \times 520 \\ \text{to be made} &= 61.4\end{aligned}$$

$$\% \text{ Error} = \frac{61 - 61.4}{61.4} \times 100 = 0.65\% \text{ slow.}$$

5.3) $V = 250 \text{ V}$

$$I = 15 \text{ A}$$

$$t = 5 \text{ hr.}$$

$$\text{PF} = 1.$$

$$\begin{aligned}\text{Reading} &= 8253.13 - 8234.21 \\ &= 18.92 \text{ kWh}\end{aligned}$$

$$\text{Energy} = \frac{250 \times 15}{1000} \times 5 = 18.75 \text{ kWh}$$

$$\begin{aligned}\% \text{ Error} &= \frac{18.92 - 18.75}{18.75} \times 100 \\ &= 0.9\% \text{ high}\end{aligned}$$

$$\text{Revolutions} = 290$$

$$t = 5 \text{ min}$$

$$I = 20 \text{ A}$$

$$V = 250 \text{ V}$$

$$\text{PF} = 0.87$$

$$\begin{aligned}\text{Energy} &= \frac{250 \times 20 \times 0.87}{1000} \times \frac{5}{60} \\ &= 0.3625 \text{ kWh}\end{aligned}$$

$$\text{meter constant} = \frac{290}{0.3625} \Rightarrow 800$$

$$5.4) \quad \Delta = 87^\circ$$

$$fL, \text{ UPF} \longrightarrow N = 40$$

$\frac{1}{4}$ fL, 0.5 pf lagging

$$T_d \propto V_s \cdot I_L \sin(\Delta - \phi)$$

$$T_B \propto N$$

$$N \propto V_s I_L \sin(\Delta - \phi)$$

$$I_1 = I$$

$$I_2 = \frac{I}{4}$$

$$\phi = 0$$

$$\phi = 60^\circ$$

$$N_1 = 40$$

$$N_2 = ?$$

$$\frac{N_2}{N_1} = \frac{I_{L2} \cdot \sin(\Delta - \phi_2)}{I_{L1} \cdot \sin(\Delta - \phi_1)}$$

$$\Rightarrow \frac{N_2}{40} = \frac{\frac{I}{4} \cdot \sin(87 - 60)}{I \cdot \sin(87 - 0)}$$

$$\Rightarrow N_2 = 40 \times \frac{1}{4} \cdot \frac{\sin 27}{\sin 87}$$

$$= 4.54$$

$$5.5) \quad \Delta = 90^\circ$$

$$I_1 = I \quad I_2 = \frac{I}{4}$$

$$\phi = 0 \quad \phi = 60^\circ$$

$$N_1 = N \quad N_2 = ?$$

$$\frac{N_2}{N_1} = \frac{\frac{I}{4}}{I} \cdot \frac{\sin(90 - 60)}{\sin(90 - 0)}$$

$$\Rightarrow N_2 = 0.125 N_1$$

$$\Delta = 87^\circ$$

$$\frac{N_2}{N_1} = \frac{\frac{I}{4}}{I} \cdot \frac{\sin(87 - 60)}{\sin(87 - 0)}$$

$$\Rightarrow N_2 = 0.113 N_1$$

$$\% \text{ Error} = \frac{0.113 N_1 - 0.125 N_1}{0.125 N_1} \times 100 \\ = 9\% \text{ slow}$$

MEASUREMENT OF FREQUENCY:

Freq. Meters:

- (1). Mech. resonance
- (2). Electrical resonance
- (3). weston type
- (4). Ratio meter type
- (5). saturable core type

MECHANICAL RESONANCE TYPE:

Operating principle is based on mech. resonance.

It mainly consists of thin steel trips (reed^g)

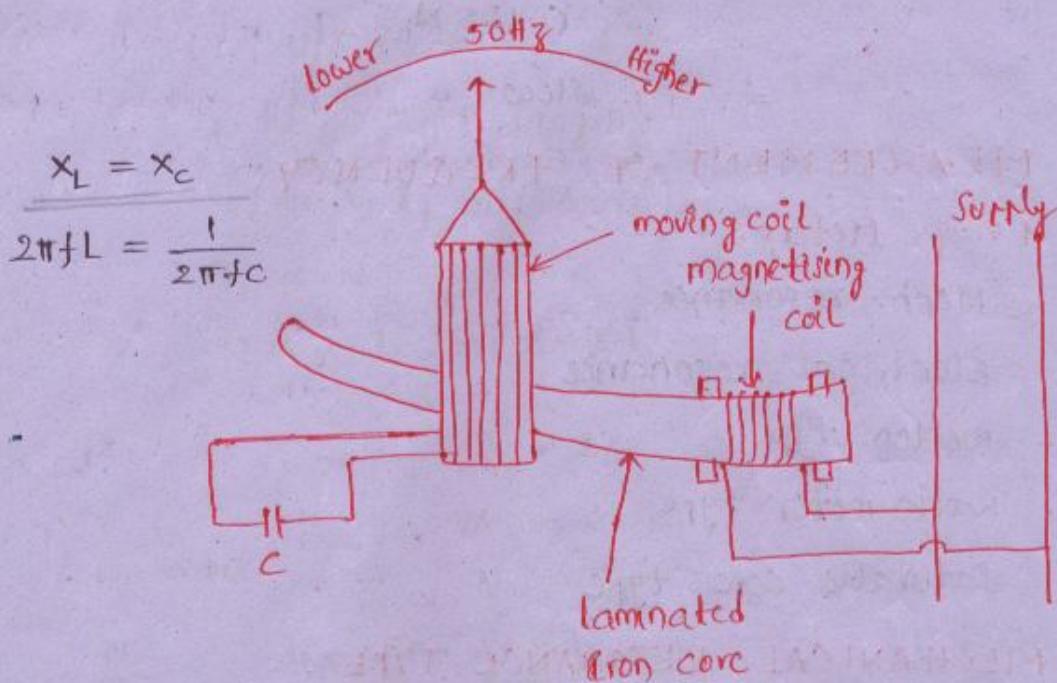
The electromagnet has laminated iron core and its coil is connected across the supply whose freq. is to be measured.

All reed^g have slight diff in dimensions and weights due to which these exhibit^d diff in natural freq.

- * In unpolarized freq. meter the reed whose freq. is 2 times^r the supply freq. will make more vibrations.
- * In polarized freq. meter the reed whose natural freq. is same as supply freq. make more vibrations.

Range: 6 Hz [47 Hz to 53 Hz].

ELECTRICAL RESONANCE FREQ. METER:



Operating principle based on electrical resonance.

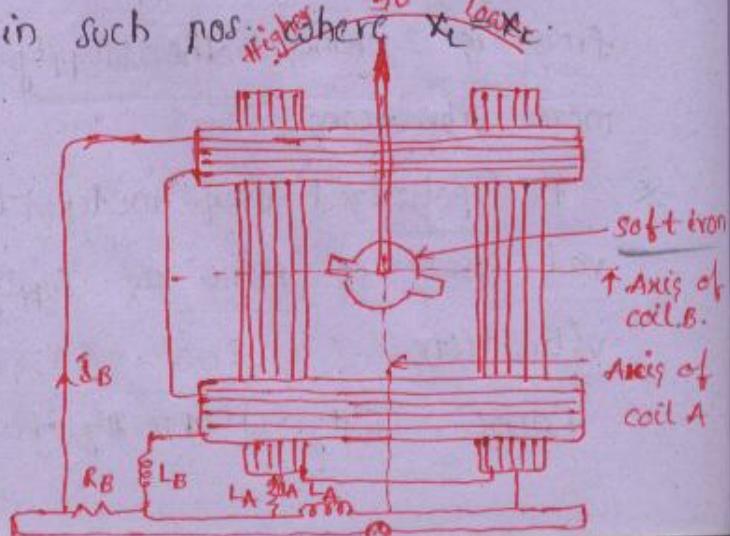
The magnetising coil mounted on laminated iron core whose cross section varies gradually over the length, being ~~max~~ near the end where magnetizing coil mounted and min at the other end.

The inductance offered by moving coil is variable which depends on pos. of moving coil on iron core. For 50 Hz freq, coil occupies central location.

As and when freq changes torque develops which brings moving coil in such pos. ~~where $X_L = X_C$~~ .

* SAT. 22/11/08 *

WESTON TYPE:



The meter consists of 2 coils mounted \perp^{er} to each other. Each coil is divided into 2 parts. coil A is connected in series with resistance R_A and whole setup placed across L_A .

coil B is connected in series with inductance and whole ~~current~~ arrangement placed across L_B .

for a normal freq., pointer takes vertical pos. If Δ when freq varies there will be diff in the magnitude of through coils based mag. of i pointer takes up new pos. This indicates present value of freq.

RATIO METER TYPE:

It consists of ratio meter which gives a linear relation b/w current ratio and deflection.

It is suitable for wide range of voltages.

It may be used for a freq range upto 5000 Hz.

SATURABLE CORE TYPE:

It is particularly suitable for tachometer system.

suitable for wide range of freqs.

MEASUREMENT OF POWER FACTOR:

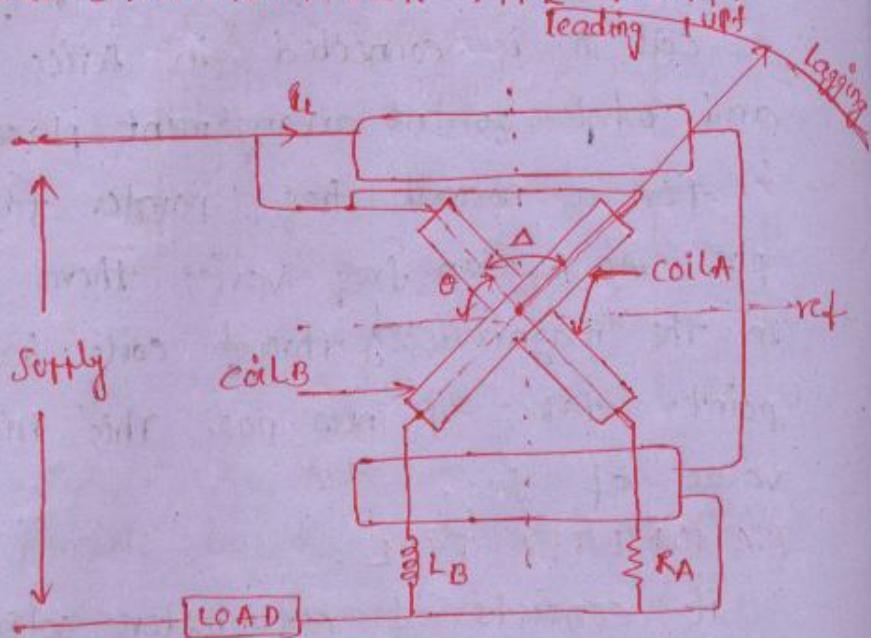
PF meter indicates directly by a single reading, the pf of the ckt to be measured.

The moving system of pf meter is perfectly balanced at equilibrium by 2 opposing forces
 \therefore There no need for control torque.

2 Types:

- (1). Electro dynamo meter type.
- (2). Moving iron type.

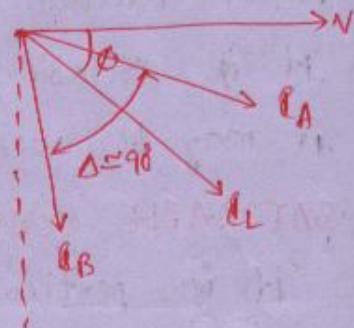
1-Φ ELECTRO DYNAMO METER TYPE P.F.M:



At Supply freq.

$$R_A = \omega L_B.$$

Hence $I_A = I_B$, but both currents displaced by very near to 90° ($\Delta \approx 90^\circ$).



By the interaction of I_A , I_L torque will be generated on coil A and I_L & I_B → torque will be on coil B.

$$\text{Deflecting torque on coil A} = T_{dA} = \Phi_1 \Phi_2 \cos \theta \frac{dM}{d\theta}$$

$$\rightarrow T_{dA} = I_L \cdot I_A \cdot \cos(\theta) \left(\frac{dM}{d\theta} \right) \rightarrow M_{max} \sin(\theta).$$

$$\Rightarrow T_{dA} \propto I_L I_A \cos \theta \cdot M_{max} \cdot \sin \theta.$$

$$\text{Deflecting torque on coil B} = T_{dB}$$

$$T_{dB} \propto I_L I_B \cos(90 - \theta) \cdot M_{max} \cdot \sin(90 + \theta)$$

At final deflection state,

$$T_{dA} = T_{dB}$$

$$\Rightarrow \cos\phi \cdot \sin\theta = \sin\phi \cdot \cos\theta$$

This eq. is satisfied when $\theta = \phi$.

At final deflection state, deflecting angle
= power factor angle of the ckt.

-for measurement of pf, in 3-φ balanced load,
same construction is suitable, but the angle b/w
their planes is 120° . -fixed coil has to be
connected in one line and 2 moving coils are
connected across this line and other 2 lines
individually.

for 3-φ unbalanced load pf measurement a
2 element pf meter is to be used.

MOVING IRON P.F.M:

(i). There are 2 types of moving iron pf.meters.

(a). Rotating field P.F.M.

(b). Alternating field P.F.M. [Nalder Lipmann type]

In this meter also at steady state cond. $\theta = 0^\circ$.
The deflection of iron beam is direct measure of
ph. angle b/w each line element and corr. ph.
voltage

Adv:

(1). The working forces are very large as compared
with those electrodynamic meter type.

(2). All the coils in H.R are fixed.

DIS. Adv.:

- (1). errors are introduced due to losses in iron parts.
- (2). Calibration of these instrg is effected variations in supply freq, volt & wave form.

POTENTIOMETERS

It is an instr. designed to measure an unknown volt. by comparing it with a known volt. This method is very accurate if volt. of ref source is accurately known.

No current flows under balance condi, hence no power consumption during measurement.

Determination of volt. by a potentiometer is ind. of source resistance.

Applications:

calibration of Ammeter, volt. meter, measurement of current & voltage etc.

BASIC POTENTIOMETER CIRCUIT:

200 CM

$$1 \text{ cm} = 1 \Omega$$

$$101.86 \text{ cm} = 101.86 \Omega$$

$$\frac{R}{R_0} = \frac{1.0186}{101.86}$$

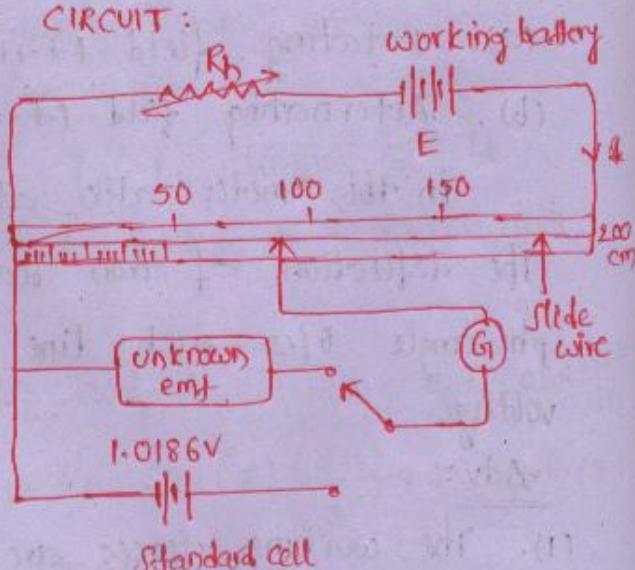
$$= 10 \text{ mA} = 0.01 \text{ A}$$

Eg 150 cm

$$R = 150 \Omega$$

$$V = 150 \times 0.01$$

$$= 1.5 \text{ V}$$

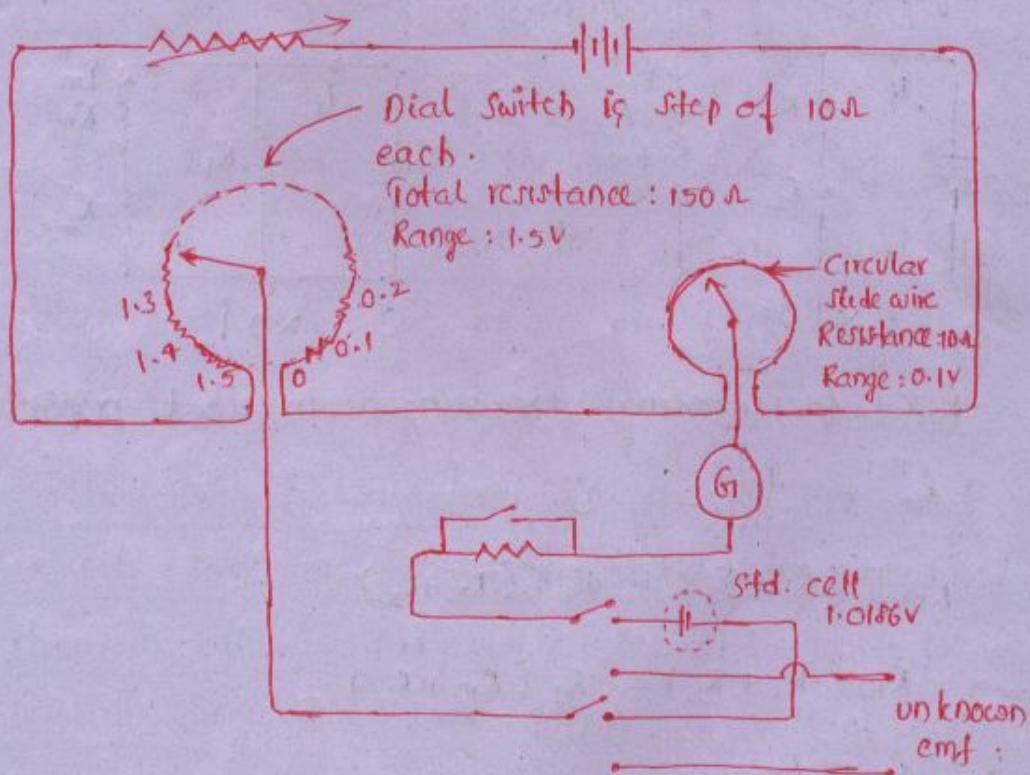


potentiometer is required to be standardised before making measurement by a std. cell.

keep the nos. of slider at 101.86 cm and switch at standardised pos. Adjust until 'G' shows zero reading. while measuring unknown volt. slider is to be varied for its pos. till G shows zero reading.

unknown volt. can be found from the balance length and calibrated current.

LABORATORY TYPE [CROMPTON'S P. M.] :



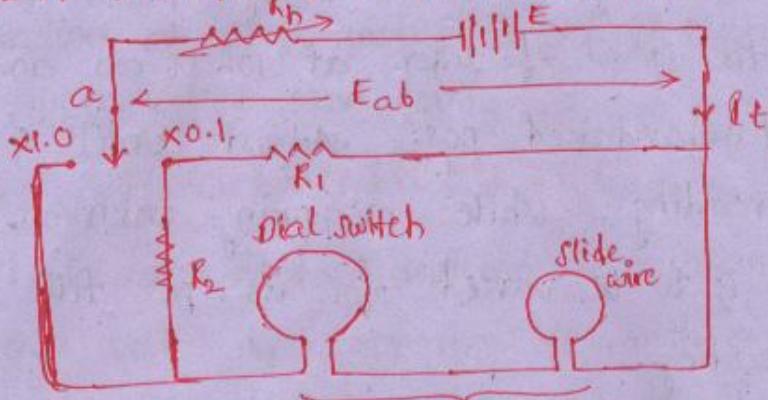
straight slide wire in basic potentiometer is replaced by dial switch & circular slide wire.

circular slide wire provided with 200 cm divisions hence min. volt. (resolution) measured is $\frac{0.1}{200} = 0.5mV$

It is very easy to extend range of potentiometer by adding required no. of deals without

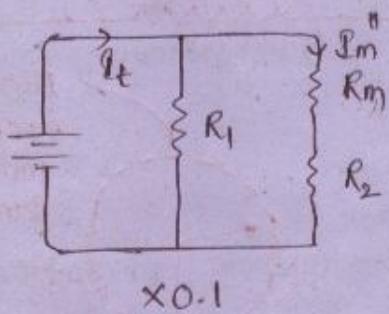
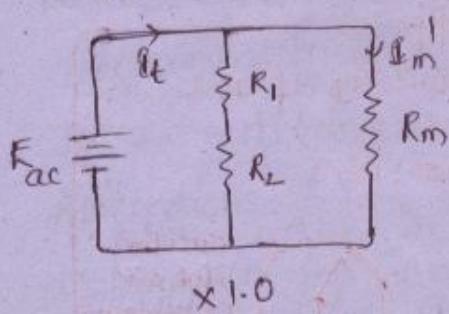
disturbing calibrations.

MULTI RANGE POTENTIOMETER:



This P.M is useful to select two ranges without disturbing the calculations.

equivalent circuit :-



for facilitating the ranges in that proportion,

$$\frac{R_m''}{R_m'} = \frac{R_m'}{10} \quad \text{--- (1)}$$

$$R_m' \parallel (R_1 + R_2) = R_1 \parallel (R_m + R_2)$$

$$\Rightarrow R_m' (R_1 + R_2) = R_1 (R_m + R_2)$$

$$\Rightarrow R_1 = R_m$$

$$\frac{R_m''}{R_m'} = \frac{R_m}{10}$$

$$\Rightarrow \frac{R_t \times \frac{R_1}{R_1 + R_2 + R_m}}{\frac{R_1 + R_2 + R_m}{10}} = \frac{1}{10} \times R_t \times \frac{R_1 + R_2}{R_1 + R_2 + R_m}$$

$$\Rightarrow R_2 = 9 R_1$$

$$\Rightarrow R_2 = 9 R_m$$

All the resistors in potentiometer are made up of MANGANIN (except slide wire).

slide wire is made up of from platinum silver alloy.

sliding contact \rightarrow cu-gold-silver alloy.

There are 2 types of potentiometers:

(1). Vernier P.M.

(2). Brook's deflectional PM.

Brook's d.P.M is used for applications where volt. to be measured is continuously changed.

AC POTENTIOMETER:

In DC PM only the magnitudes of unknown emf and PM drop have to be made equal to obtain balance, but in AC PM both mag & ph. have to be made same to obtain balance.

The freq & wave form in the PM ckt must exactly same as that of volt. being measured. Thus in all ac PM's the PM ckt must be supplied from the same source as volt or current being measured.

A vibrational galvanometer is used as detector. Standardization of ac PM's can be done with the help of std DC source & transfer instr.

2 types of AC PM's:

(1). polar type PM :-

In these instr. the mag. of unknown voltage

is read from one scale and ph. angle w.r.t some ref phasor from a 2nd scale.

(2). co-ordinate type: [Hall - Tinsley PM].

These instrs are provided with 2 scales to read resly in phase comp & quadrature component of unknown voltage.

If higher voltages are to be measured a precision volt. divider called "volt-ratio box."

$$6.5). \quad V = 1.0185 \text{ V}$$

$$l = 50 \text{ cm.}$$

$$(a). \text{ Emf of cell} = \frac{1.0185}{50} \times 72 \\ = 1.467 \text{ V.}$$

$$(b). A_m = 1.33 \text{ V}$$

$$l = 64.5 \text{ } \downarrow \\ A_t = \frac{1.0185}{50} \times 64.5 = 1.314 \text{ V}$$

$$\% \text{ error} = \frac{1.33 - 1.314}{1.314} \times 100 \\ = 1.22 \text{ %}.$$

$$(c). A_m = 0.43 \text{ A}$$

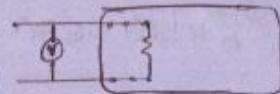
$$\text{voltage} = \frac{1.0185}{50} \times 43.2 \\ = 0.8802 \text{ V}$$

$$A_t = \frac{0.8802}{2} = 0.4401 \text{ A}$$

$$\% \text{ error} = \frac{0.43 - 0.4401}{0.4401} \times 100 \\ = - 2.29 \text{ %}.$$

6.6). P.M \rightarrow 1V

$$R_V = 10000 \times 5 = 50000 \Omega$$



with The connection of voltmeter, volt has become half hence the resultant resistance is also half. It is possible only if resistance of meter = internal ckt resistance.

\therefore Resistance of ckt = 50,000 Ω .

$\Rightarrow * \text{INSTRUMENTATION TRANSFORMERS} *$

These TIF's are used in conjunction with meters for the measurement of high current & high voltage.

2. Types:

(1). current TIF:

It will scale down the current.

(2). potential TIF:

It will scale down the voltage.

Transformation ratio: (R)

Ratio of primary phasor to secondary phasor.

$$R = \frac{\Phi_P}{\Phi_S} \mid_{CT} \quad R = \frac{V_P}{V_S} \mid_{PT}$$

Nominal ratio: (k_n)

Ratio of rated primary phasor to rated secondary phasor.

$$k_n = \frac{\text{rated } \Phi_P}{\text{rated } \Phi_S} \mid_{CT}$$

$$k_n = \frac{\text{rated } V_P}{\text{rated } V_S} \mid_{PT}$$

Turns ratio: (n)

$$n = \frac{N_S}{N_P} \mid_{CT} \swarrow \text{slip}_{TIF} \quad n = \frac{N_P}{N_S} \mid_{PT} \swarrow \begin{matrix} \text{s/down} \\ \text{TIF} \end{matrix} \underline{(n>1)}$$

Ratio correction factor (RCF) = $\frac{R}{k_n}$

Burden:

Load on CT will be specified with the name of burden. It will be expressed in v-A.

CURRENT TRANSFORMER (CT):

The secondary current rating

CT is standardized to

1A or 5A.

Usually 1A will be used

for measurement and

5A for protection.

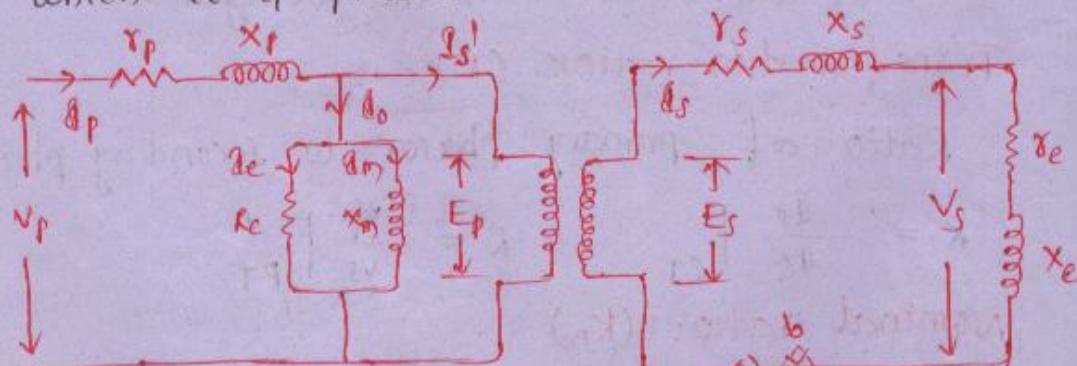
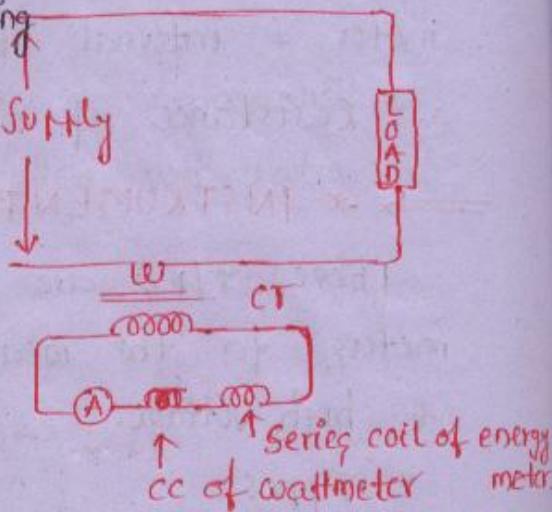
No. of turns on primary

will be less (preferably 1 turn)

at this condi this is known as bar primary CT.

The p. cur. in CT depends on ckt in

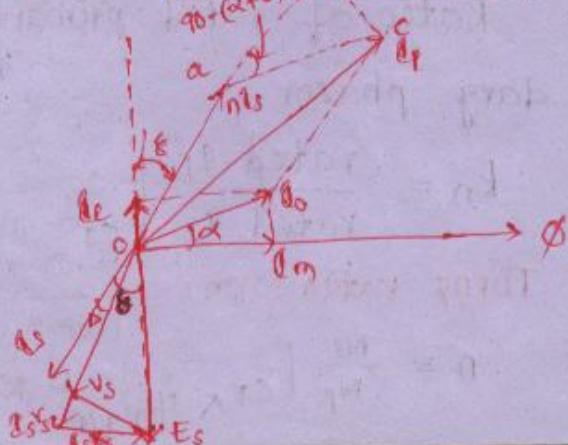
which it is placed.



$$\frac{N_s}{N_p} = \frac{V_s}{V_p} = \frac{I_p}{I_s}$$

$$I_p = \frac{N_s}{N_p} \cdot I_s$$

$$\Rightarrow I_p = n \cdot I_s$$



from the phasor diagram, $\ell_p^2 = (Ob)^2 + (bc)^2$

$$\Rightarrow \ell_p^2 = (Oa + ab)^2 + bc^2$$

$$= (n\ell_s + \ell_0 \cos(90 - (\alpha + \theta)))^2 +$$

$$[\ell_0 \sin(90 - (\alpha + \theta))]^2$$

$$= (n\ell_s + \ell_0 \sin(\alpha + \theta))^2 + (\ell_0 \cos(\alpha + \theta))^2$$

$$= n^2 \ell_s^2 + 2 \ell_0 n \ell_s \cdot \sin(\alpha + \theta) + \ell_0^2$$

$$\approx n^2 \ell_s^2 + 2 \ell_0 n \ell_s \sin(\alpha + \theta) + \ell_0^2 \sin^2(\alpha + \theta)$$

$$\ell_p \approx n \ell_s + \ell_0 \sin(\alpha + \theta)$$

$$\text{Transformation Ratio (R)} = \frac{\ell_p}{\ell_s}$$

$$\Rightarrow R = n + \frac{\ell_0}{\ell_s} \cdot \sin(\alpha + \theta)$$

$$\tan \theta = \frac{bc}{ob} \quad \frac{200 + (1.8)}{198}$$

$$= \frac{\ell_0 \sin(90 - (\alpha + \theta))}{\ell_s}$$

$$= \frac{\ell_0 \cos(\alpha + \theta)}{n \ell_s + \ell_0 \sin(\alpha + \theta)}$$

$$= \frac{\ell_0 \cos(\alpha + \theta)}{n \ell_s + \ell_0 \sin(\alpha + \theta)}$$

$$\tan \theta \approx \frac{\ell_0 \cos(\alpha + \theta)}{n \ell_s}$$

$$\Rightarrow \theta \approx \frac{\ell_0 \cos(\alpha + \theta)}{n \ell_s}$$

$$\text{Ratio Error} = \frac{k_n - R}{R} \times 100$$

$$\text{phase angle error} = \frac{\ell_0 \cos(\alpha + \theta)}{n \ell_s} \text{ rad}$$

$$200/1 \rightarrow CT$$

$$k_n = \frac{200}{1} = 200$$

$$= \frac{180}{\pi} \left[\frac{\ell_0 \cos(\alpha + \theta)}{n \ell_s} \right] \text{ deg}$$

$$N_p = 1$$

$$N_s = \frac{200}{198}$$

$$n = \frac{N_p}{N_s} = \frac{1}{\frac{200}{198}} = \frac{198}{200}$$

In an uncompensated CT, turns ratio will be same as nominal ratio. Then transformation ratio will be more than nominal. resultant ratio error will always be negative.

Turns Compensation:

To appr. equalling the transformation ratio to nominal ratio it is preferable to select no. of turns on secondary to be less. This is known as turns compensation.

The cause of errors in CT is due to NL current of Tlf. It consists of core loss comp. & magnetising component.

CT is also known as series Tlf and its secondary is almost operated under scaled condition.

CT secondary should not be open circuited while primary is energised. It may result into

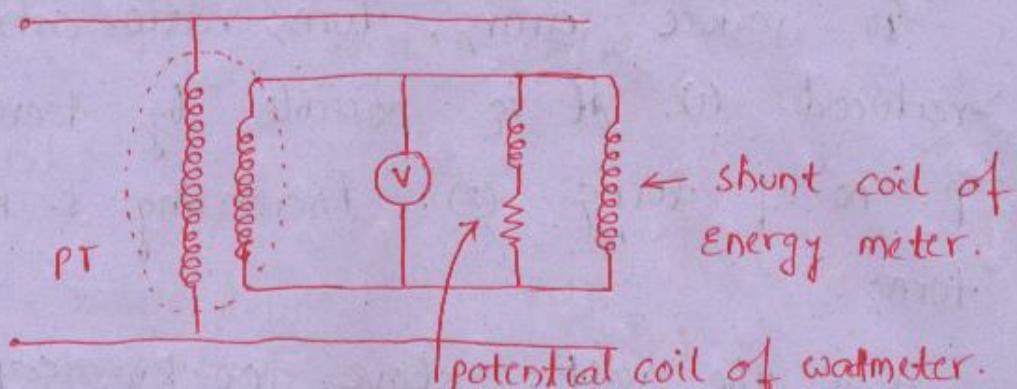
- Generation of high o/c volt. across secondary terminals.
- Core may get saturate
- Insulation of CT may get damage.

* Potential Transformer: (PT):

PT scaled down volt. and electrically equal to sf down Tlf.

It is known as 1st Tlf. and secondary of PT almost operated under o/c

condition.



The s. volt. rating of PT is standardised to 110V.

$$\text{Transformation ratio } R = \frac{V_p}{V_s}$$

$$= D + \frac{\theta_s}{n} [R_p \cos \Delta + X_p \sin \Delta] + \delta_c r_p + \delta_m X_p$$

$$\theta = \frac{\theta_s}{n} \left[X_p \cos \Delta - R_p \sin \Delta \right] + \delta_c X_p - \delta_m r_p \text{ rad.}$$

R_p, X_p = equivalent resistance & reactance refer to primary.

r_p, X_p = resistance, reactance of primary wdg only.

$$\Delta = \tan^{-1} \left(\frac{X_e}{r_e} \right)$$

r_e, X_e = equivalent resistance, reactance coming on PT secondary.

for uncompensated PT turns ratio = nominal ratio then transformation will be more than nominal ratio.

Turns Compensation :-

To reduce errors, turns ratio can be reduced (1). It is possible by decreasing p. no. of turns (2). Increasing s. no. of turns.

for the voltages above 100 kV, capacitive potential transformers [CVT's] are used for measurement purpose.

Q.1

$$f = 50 \text{ Hz}$$

$$N_p = 1$$

$$N_s = 200$$

$$r_e = 1 \Omega$$

$$I_s = 5 \text{ A}$$

$$AT = 80$$

$$A = 10 \text{ cm}^2$$

$$V_s = I_s \cdot r_e = 5 \times 1 = 5 \text{ V}$$

(Secondary
volt.)

$$(a) V_p = \frac{N_p}{N_s} \times V_s$$

$$(\text{P. volt.}) = \frac{1}{200} \times 5 = 0.025 \text{ V}$$

$$V_p = 4.44 B_m \cdot A f N_p$$

$$0.025 = 4.44 \times 10 \times 10^{-4} \times B_m \times 50 \times 1$$

$$\Rightarrow B_m = 0.1125 \text{ wb/m}^2$$

(b).

$$N_p \times \delta_m = 80$$

$$\Rightarrow \delta_m = \frac{80}{1} = 80 \text{ A}$$

(magnetising current)

$$\begin{aligned} \delta_p &= \sqrt{(n \delta_s)^2 + \delta_m^2} \\ &= \sqrt{(200 \times 5)^2 + (80)^2} \end{aligned}$$

$$= 1003.2 \text{ A}$$

Trans. ratio $R = \frac{\delta_p}{\delta_s} = \frac{1003.2}{5} = 200.64$

$$\tan \theta = \frac{\delta_m}{n \cdot \delta_s} = \frac{80}{5 \times 200}$$

$$\Rightarrow \theta = 45.7^\circ$$

6.2.

$$k_n = \frac{1000}{5} = 200$$

$$f = 50 \text{ Hz}$$

$$r_c = 1.6 \Omega$$

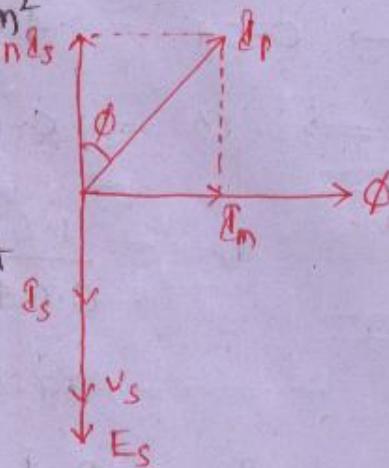
$$N_p = 1$$

$$\text{Iron loss} = 1.5 \omega$$

$$V_s = \delta_s \cdot r_c$$

$$= 5 \times 1.6 = 8 \text{ V}$$

$$\frac{N_p}{N_s} = \frac{V_p}{V_s} \Rightarrow V_p = \frac{1}{200} \times 8 = 0.04 \text{ V}$$



$$V_p = 4.44 \phi f N_p$$

$$\rightarrow 0.04 = 4.44 \times \phi \times 50 \times 1$$

$$\Rightarrow \phi = 0.18 \text{ mwb}$$

(b)

$$I_c = \frac{1.5}{0.04}$$

$$= 37.5 \text{ A}$$

$$I_p = n I_s + I_c$$

$$= (200 \times 5) + 37.5$$

$$= 1037.5 \text{ A}$$

$$R = \frac{I_p}{I_s} = \frac{1037.5}{5} = 207.5$$

$$\text{Ratio error} = \frac{k_n - R}{R} \times 100\%$$

$$= \frac{200 - 207.5}{207.5} \times 100\%$$

$$= -3.6\%$$

6.3.

$$N_p = 1$$

$$k_n = \frac{1000}{5} = 200$$

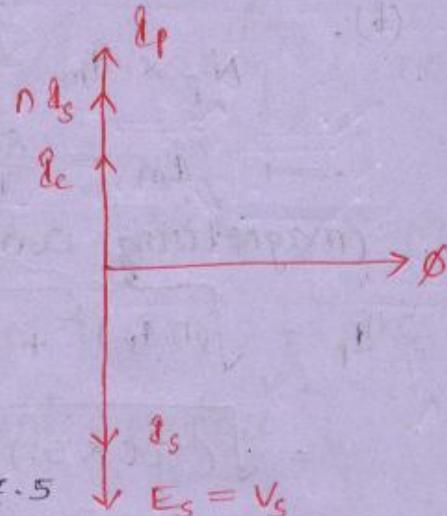
$$r_c = 1 \Omega$$

$$I_o = 1 \text{ A}$$

$$\text{NL pf} = 0.4$$

$$\alpha = 90 - \cos^{-1}(0.4)$$

$$= 23.57^\circ$$



$$R = n + \frac{I_0 \sin(\alpha + \theta)}{I_s}$$

$$= 200 + \frac{1 \times \sin(23.57 + 0)}{5}$$

$$R = 200.08$$

$$\theta = \frac{I_0 \cos(\alpha + \theta)}{n \cdot I_s} \cdot \frac{180}{\pi} \text{ deg.}$$

$$= \frac{1 \times \cos(0 + 23.57)}{200 \times 5} \cdot \frac{180}{\pi}$$

$$= 0.052^\circ$$

$$\text{Ratio Error} = \frac{k_p - R}{R} \times 100\%$$

$$= \frac{200 - 200.08}{200.08} \times 100\%$$

$$= -0.04\%$$

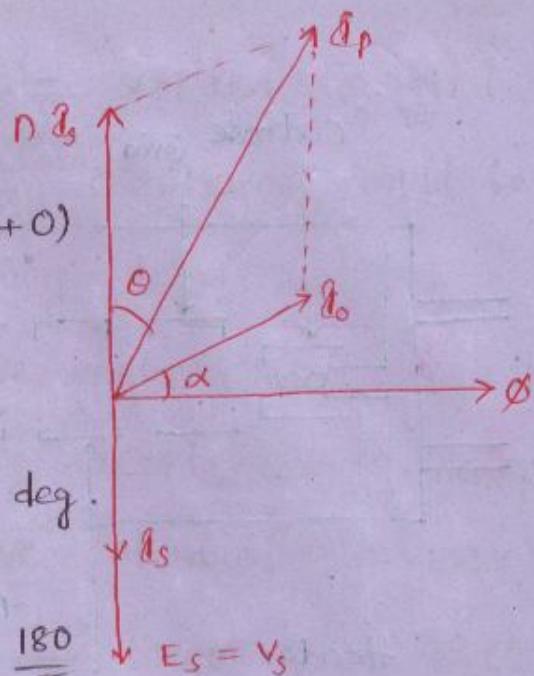
CRO :

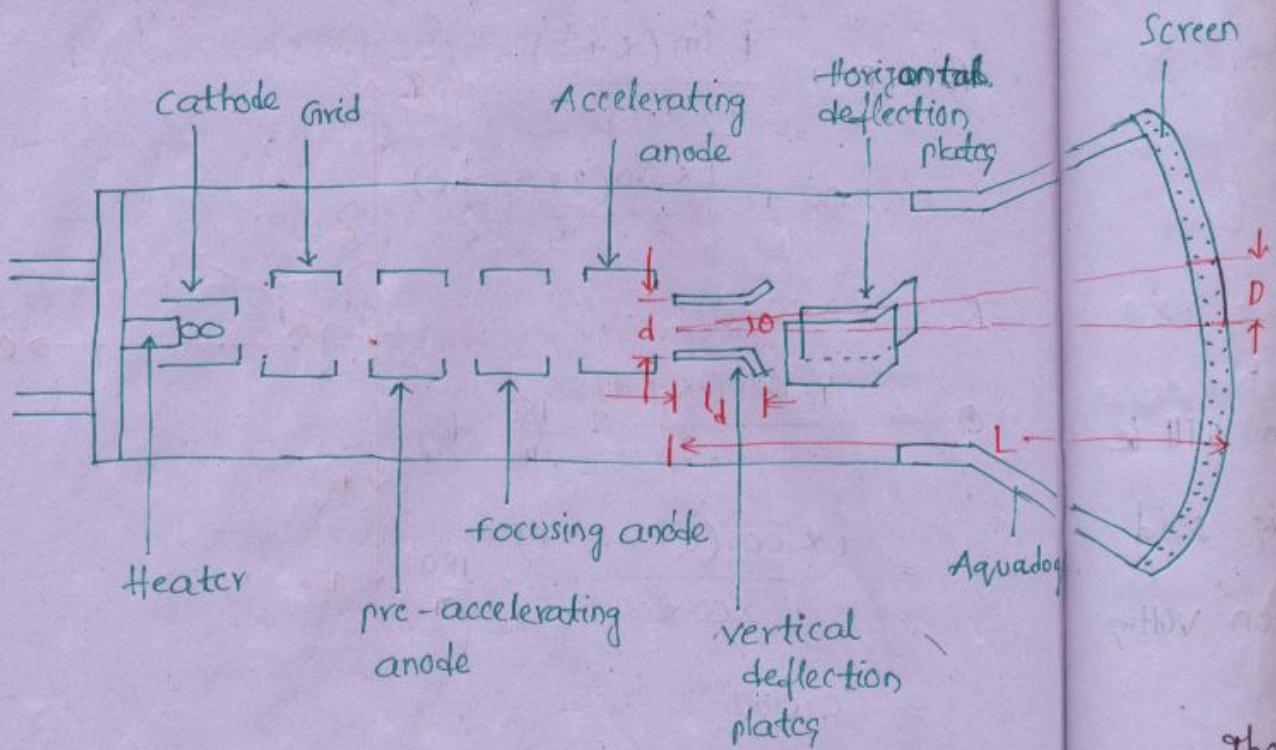
CRO is a very useful laboratory instrument used for display, measurement & analysis of wave form.

CRO can be used for higher freq.

[Duddell's Oscilloscope]

The main element of CRO is CRT.





The main parts of CRT are -

- (a). e^- gun assembly
- (b). deflection plate assembly
- (c). fluorescent screen
- (d). Glass envelope.

e^- gun assembly produces sharp focused beam of e^- s which are accelerated to high velocity with the help of focusing anode, accelerating anode, etc.

focused beam of e^- s strike the screen with sufficient energy to produce luminous spot on screen.



The potentials applied to grid and subsequent electrodes would be in the following range.

- grid → -ve potential
- pre accelerating, accelerating anodes → High +ve potential (1500v).
- focusing anode → lower adjustable +ve voltage [upto 500 v].

The e^- beam focused on the screen in two methods.

- (1). electro static focusing : (used for CRO applications).
- (2). electro magnetic focusing : (for TV applications).

e^- beam will be deflected by the potentials applied to deflection plates.

Electro static means of deflection is employed for the deflection of e^- beam.

Deflection (D) = $\frac{L \cdot d_d}{2d \times E_a} \times E_d$.

Deflection sensitivity (s) = $\frac{D}{E_d}$

$$\Rightarrow s = \frac{L}{2d} \cdot \frac{E_d}{E_a}$$

Deflection factor = $\frac{1}{s}$.

E_a = accelerating anode volt.

E_d = Deflection plate volt.

If E_a is more then the beam will be highly accelerated and then it is said to be hard beam. High deflection voltage required to deflect hard beam.

Aquadog :-

Whenever e beam strikes fluorescent screen it produces secondary emission e_s . To collect these e_s Aquadog is employed. It is an homogeneous soln. of graphite coated around glass envelope.

The e beam needs acceleration after deflection if signals of more than 10 MHz are to be displayed. Post deflection Accelerators are used for this purpose.

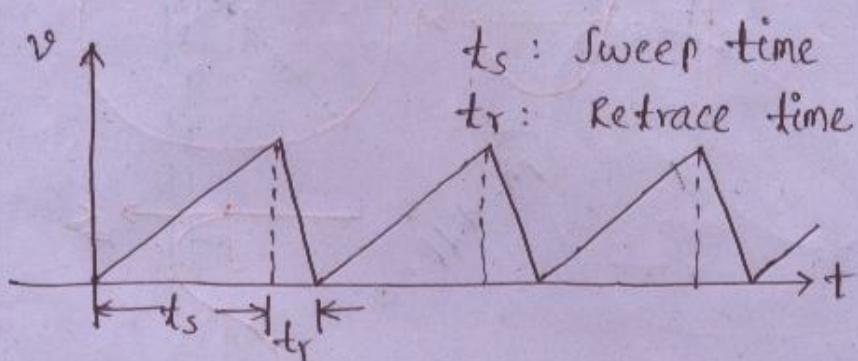
Display of unknown signal :

for the display of any unknown

signal the voltages applied to deflection plates are as follows.

- (1). vertical deflection plates (Y-plate)
— unknown signals.
- (2). Horizontal deflection plates — sweep signals.

In general saw tooth wave is used as a sweep signal.



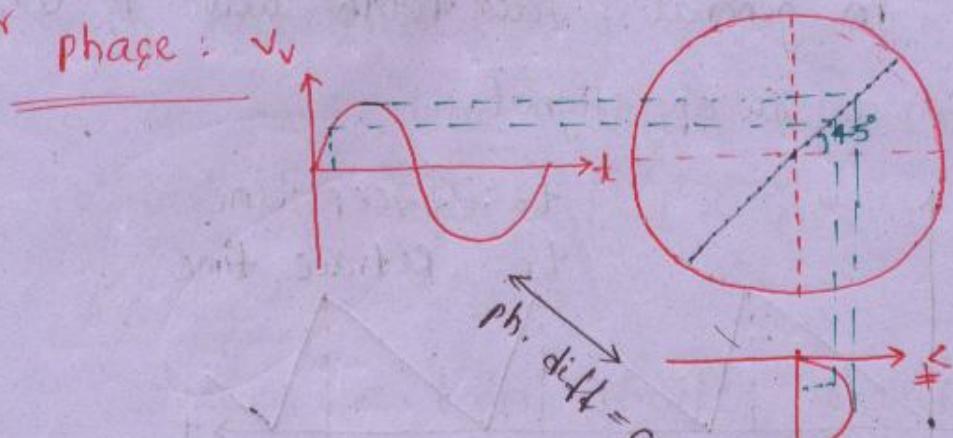
During sweep time beam moves from left to right most pos. on the screen.

During t_r , beam travels from right to left most position. This time required is ^{V.V.} less to avoid retrace pattern appearance over the screen. Some of modern oscilloscope block the beam during retrace time to avoid this problem.

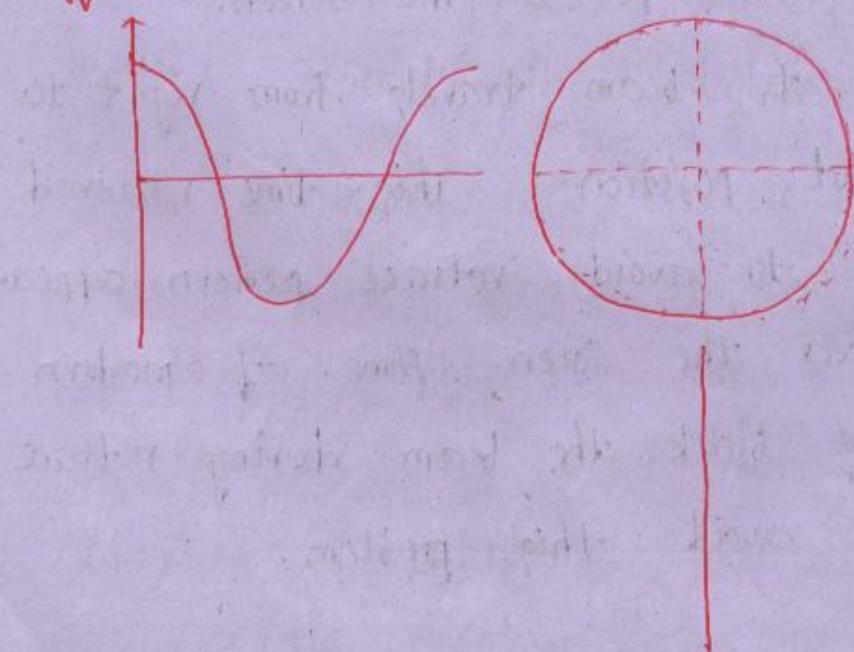
Measurement of phase & freq.:

In the measurement of ph. & freq. sinusoidal voltages will be applied to both horizontal & vertical deflection plates. Then resultant pattern appearance on screen known as Lissajous patterns.

for phase: V_V

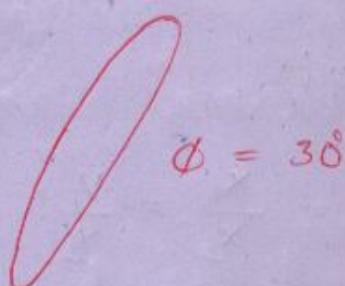


V_V

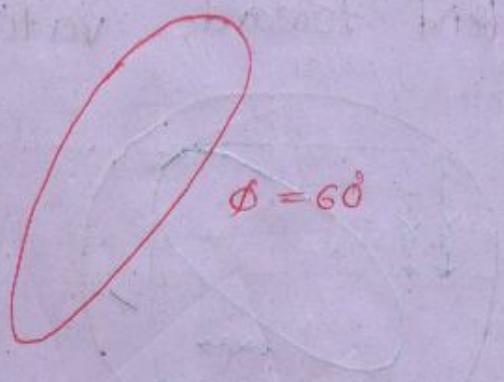


whenever equal amount of voltages are applied to both x-plates & y-plates, the shape of pattern for different ph. angles are as follows.

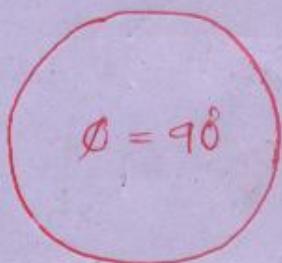
for $\phi = 0 \longrightarrow \dots / 45^\circ \dots$



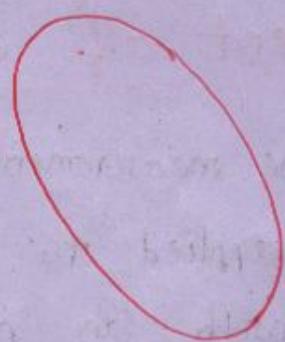
$$\phi = 30^\circ$$



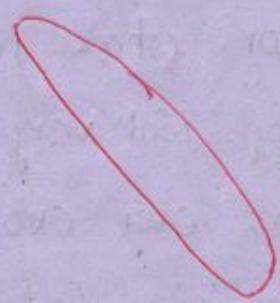
$$\phi = 60^\circ$$



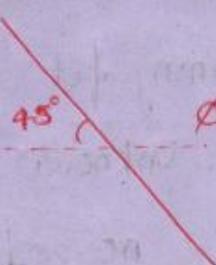
$$\phi = 90^\circ$$



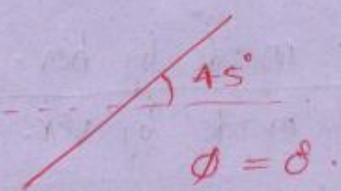
$$\phi = 120^\circ$$



$$\phi = 150^\circ$$



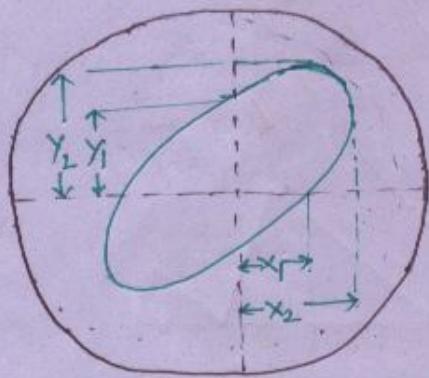
$$\phi = 180^\circ$$



$$\phi = 0^\circ$$

when the mag. of hor. plate volt more than ver. plate volt. then shape of pattern remain same but it bends toward hor. axis.

when mag. of vertical plate volt is more than hor. plate volt. then pattern bend towards vertical axis.



$$\sin\phi = \frac{x_1}{x_2} = \frac{y_1}{y_2}$$

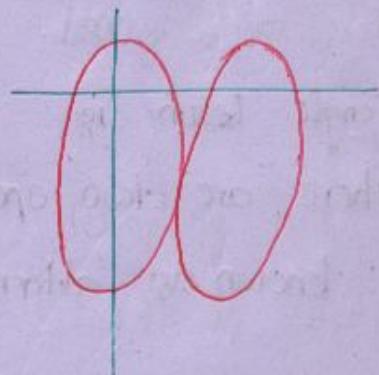
Measurement of frequency:

In the measurement of freq. unknown signal is applied to y-plates. x-plates are fed with an oscillator whose freq. can be varied. This freq. will vary till a meaningful pattern appears over CRO screen. Unknown freq. can be evaluated by

$$\frac{f_y}{f_x} = \frac{\text{no. of intersections made by hor. line}}{\text{no. of intersections made by ver. line}}$$

Two lines are to be drawn on pattern

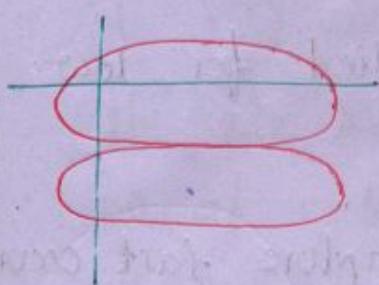
one is hor. & another is ver. These lines are to be drawn in such a way they should not pass through any intersection of curve and pass through whole curve.



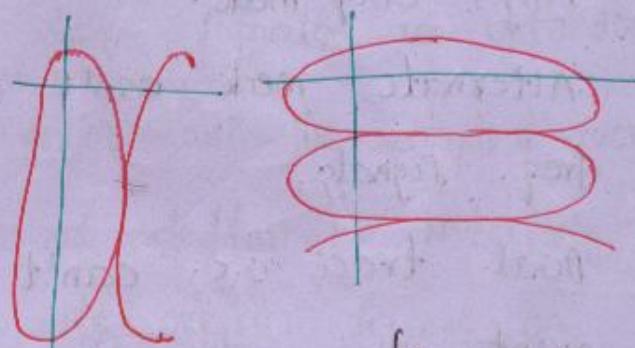
$$f_x = 50 \text{ Hz}$$

$$\frac{f_y}{f_x} = \frac{4}{2}$$

$$\therefore f_y = \frac{4}{2} \times 50 = 100 \text{ Hz.}$$

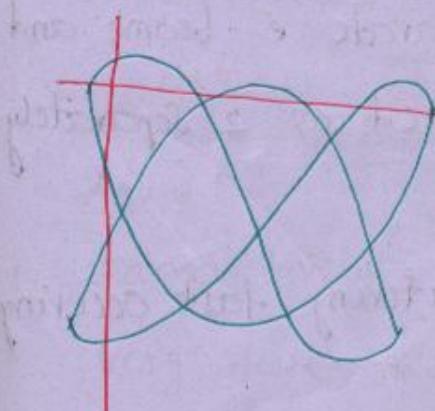


$$\frac{f_y}{f_x} = \frac{2}{4}$$



$$\frac{f_y}{f_x} = \frac{3}{2}$$

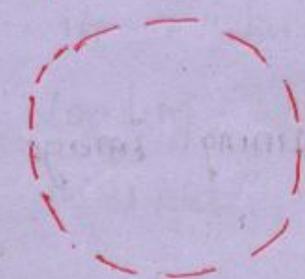
$$\frac{f_y}{f_x} = \frac{2}{5}$$



$$\frac{f_y}{f_x} = \frac{6}{4}$$

$$\rightarrow f_y = \frac{6}{4} \times 50$$

$$\therefore = 75 \text{ Hz.}$$



\rightarrow 12 spikes.

$$\text{so } \frac{f_y}{f_x} = 12$$

Special types of Oscilloscopes:

Dual trace oscilloscopes:

2 types : (a). Dual trace

(b). Dual beam

Dual trace O.S. :

In this CRO, a single beam is splitted into 2 traces. There are two operating modes for operating known as alternating, chop mode.

Alternate mode can't applied for low freq. signals.

Dual trace O.S. can't capture fast occurring events.

Dual beam O.S. :

It has got two separate e⁻ beams and therefore can be considered as 2 separately vertical channels.

It is useful for monitoring fast occurring events also.

Storage O.S. :

It is capable of retaining image on screen for longer time.

It is suitable for capture and storage of non-repetitive waveforms like transients.

Storage mesh may be used to retain image for longer time. Magnesium fluoride is used in making of storage mesh.

Sampling o.s.:

It is suitable to capture and display of very high freq. signals ie upto 300MHz. The i/p waveform will be sampled over no. of cycles at different intervals of time wrt its origin. Based on sampled values the waveform can be reconstructed over CRO screen.

DIGITAL VOLTMETERS [DVM]:

Advantages:

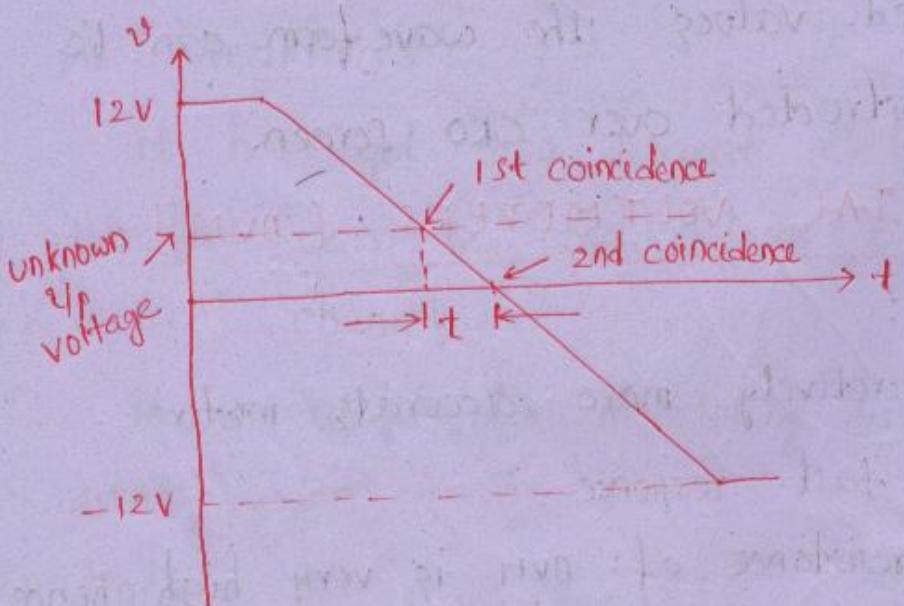
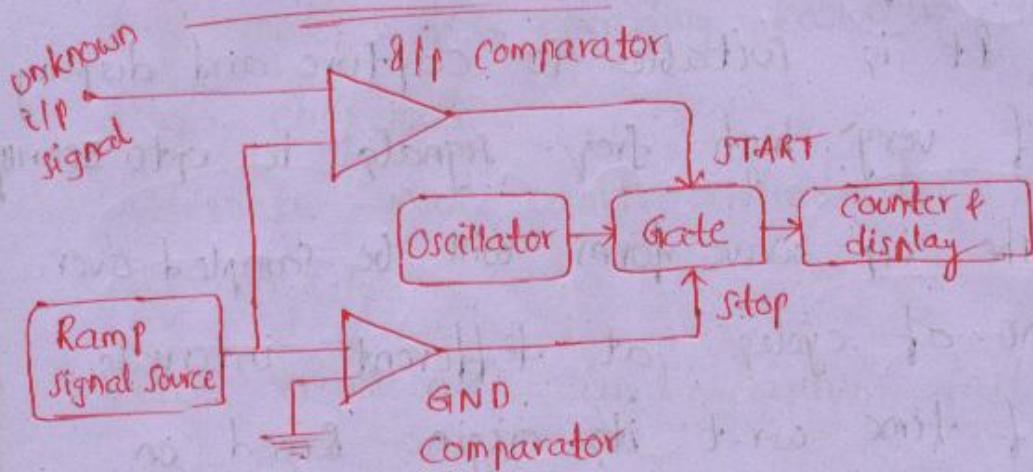
1. comparatively more accurate meters
2. very fast response
3. i/p resistance of DVM is very high hence loading effect on unknown signal is negligible.

3. If volt. range can be varied to reduce errors in the measurement.

DVM's are of 3 types

- ramp type DVM
- Dual slope integrating type DVM.
- Integrating type DVM.

RAMP TYPE DVM:



Operating principle is to measure the time that a linear ramp takes time to change from unknown i/p volt. level to ground

level. [volt to time conversion].
I/p comparator identifies 1st coincidence
and issues start pulse. Ground compa.
identifies 2nd coincidence and issue
stop pulse to gate.

counter counts CP's from START to
STOP pulses of gate. unknown volt. is
evaluated by multiplying time with slope
of ramp signal.

Large errors are possible when noise
is superimposed on i/p signal.

