

Power System

Bala J.

(I) Transmission

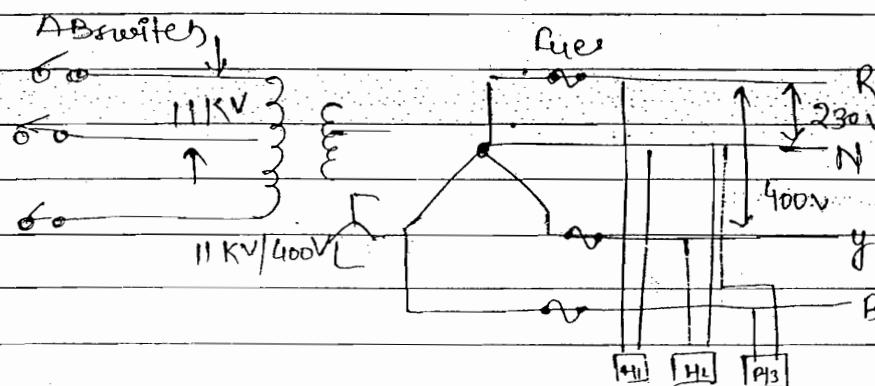
- ↳ Basics
- ↳ voltage / Reactive Power control
- ↳ Power flow through Tr-line
- ↳ Tr. line parameters
- ↳ " " performance
- ↳ Travelling waves
- ↳ Corona

• II

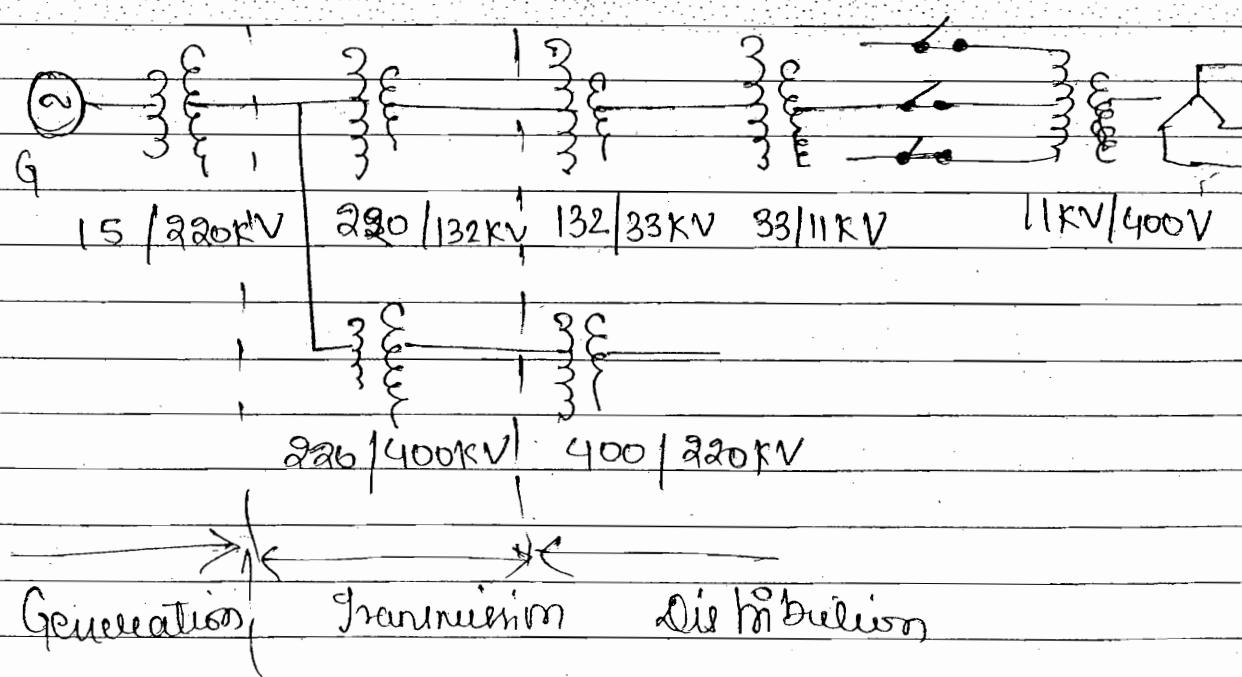
- ↳ Power generation
- ↳ Economic factors
- ↳ load freq. Control

• III.

- ↳ Switchgear and protection



↳ When the power cut take place in any one phase, then AB switch are get open, after replacing fuc AB switch again closed.



↳ Rms line (or) line-line voltage $[V_{ll}/V_l]$

400V, 11KV, 33, 132, 220, 400, 765 KV

↳ Rms phase voltage (V_{ph}) $V_{ph} = 230V$

• Objective of Power system:-

(1) Cost of electrical energy per unit must be minimum

→ Economic load dispatch

→ Economic factors

→ Generation Method.

(2) Rated voltage and freq. has to be supplied to the consumers.

→ Voltage control

→ Load freq. Control

(3) Reliable power supply has to be available

→ Generation Methods

→ Transmission

→ HVdc.

(4) Most efficient protection system has to be available for faster identification and isolation of faulty section from the healthy section.

→ Fault analysis

→ Switch gear and protection

(5) Most efficient generator has to be used which has to be most stable, should not lose synchronism under faulty condition

→ Stability

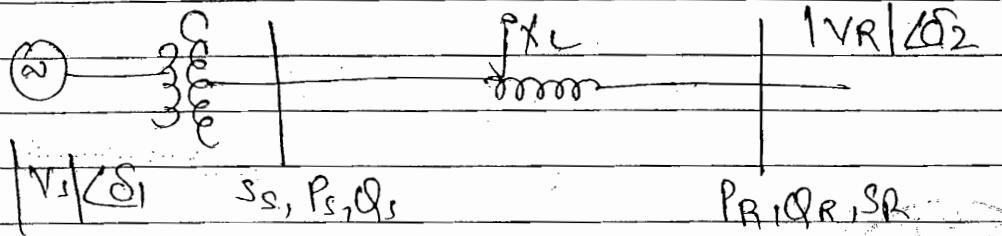
(6) Flexible power transfer has to be available

→ Power cables.

Transmission :- By using transmission line line etc. power is transferred from the remote generating generating station to the load centre where the electrical power is utilised.

Objectives :-

(1) Transmission line must be capable of transferring maximum power with minimum transmission line losses and more.



$$P_s = P_R = \frac{V_s \times V_R}{X_L} \sin \delta = \frac{V_s^2}{X_L} \sin (\delta_1 - \delta_2)$$

Let $\delta = \delta_1 - \delta_2$.

$$P_R = \frac{V_s V_R}{X_L} \sin \delta \quad \text{Assume } V_R = V_s$$

$$P_R = \frac{V_s^2}{X_L} \sin \delta = P_{\max} \sin \delta \quad P_{\max} = \frac{V_s^2}{X_L}$$

$$P_{\max} = \frac{V_s^2}{X_L}$$

Advantage of higher V_s :-

(1) $P_{\max} \propto V_s^2$. By $\uparrow V_s$, maximum power can be transferred.

$$P_{\max} \propto V_s^2$$

(2) Transmission losses are minimised

line

$$P = VI \cos \phi$$

$$I = \frac{P}{V \cos \phi}$$

$$P_{loss} = I^2 R$$

$$P_L = \frac{P^2 \cdot R}{V^2 \cos^2 \phi} \quad \text{--- (1)}$$

$$P_L \propto \frac{1}{V^2}$$

Condition:- $P_L, R, \cos \phi = \text{constant}$.

(3) Area of cross section and volume of conductor is minimised.

$$R = \frac{\rho l}{A} \quad A = \frac{I P_L}{R} = \frac{\rho l \cdot P_L^2}{V^2 \cos^2 \phi P_L} \quad [\text{from (1)}]$$

$$A \propto \frac{1}{V^2}$$

$$\text{Volume} = \rho \cdot A \cdot l \quad K \propto A \propto \frac{1}{V^2}$$

Condition:- $\rho, l, \rho \cdot P_L, \cos \phi = \text{constant}$

(4) By reducing volume material requirement will be reduce. So the cost is minimised.

Because of above advantage we operating voltage of x-section sys. is ranges from 11-33-132-220-400-765 KV.

• Limitations: (1) Beyond 765 KV more insulation required which increases the cost of x-section

• Methods of Reducing X_L :

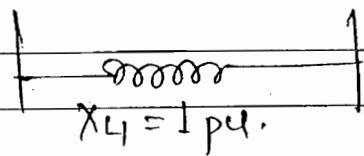
$$\text{Prms} \propto \frac{1}{X_L}$$

By reducing X_L , P_{max} is increased.

(a) By using parallel (or) double circuit line

Single line

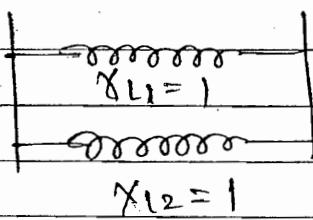
$$|V_s|=1 \quad |V_R|=1$$



$$P_{max1} = \frac{1X1}{1} = 1 \text{ p.u.}$$

Double line

$$|V_s|=1 \quad |V_R|=1$$



$$X_L = \frac{1X1}{1+1} = 0.5$$

$$P_{max2} = \frac{1X1}{0.5} = 2$$

$$\left[P_{max} \propto \frac{1}{X_L} \right]$$

$$P_{max2} > P_{max1}$$

(b) By using series capacitor

Without Series Capacitor

$$|V_s|=1 \quad |V_R|=1$$

$$X_{L1} = 1 \text{ p.u.}$$

$$P_{max1} = \frac{1X1}{1} = 1 \text{ p.u.}$$

With Series Capacitor

$$\begin{array}{c} |V_s|=1 \\ \text{---} \\ \text{wavy line} \\ \text{---} \\ |V_R|=1 \end{array} \quad \begin{array}{c} C_{se} \\ \parallel \\ \text{wavy line} \\ \parallel \\ |V_R|=1 \end{array}$$

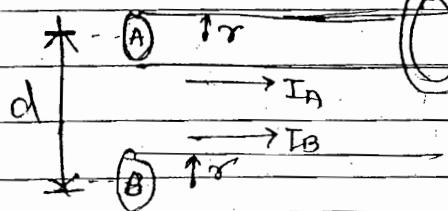
$$jX_{L1} = j1 \quad jX_C = j0.5$$

$$X_L = 1 - 0.5 = 0.5$$

$$P_{max2} = \frac{1X1}{0.5} = 2 > P_{max1}$$

(c) By using Bundle Conductors :-

corona.



$$J_L A = L_B = 2 \times 10^{-7} \ln(d/r) \quad (0.7788 \text{ N})$$

$$\downarrow X_L = 2\pi f L A \downarrow$$

$\uparrow P_{max}$ \downarrow X_L \downarrow \uparrow P_{max} \downarrow X_L

Bundle
conductors

By $\downarrow X_L$ we can $\uparrow P_{max}$, we can $\downarrow X_L$ by $\downarrow L_A$
 L_A can be \downarrow by (1) $\downarrow d$ (2) $\uparrow r$.

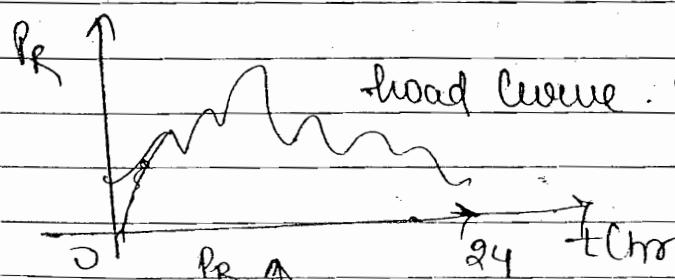
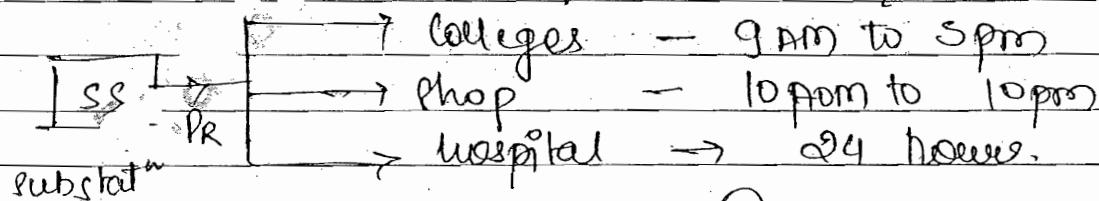
0.7788 \rightarrow Bundle Conductors.

By $\uparrow d$ (diameter) \rightarrow effect corona losses \downarrow we r

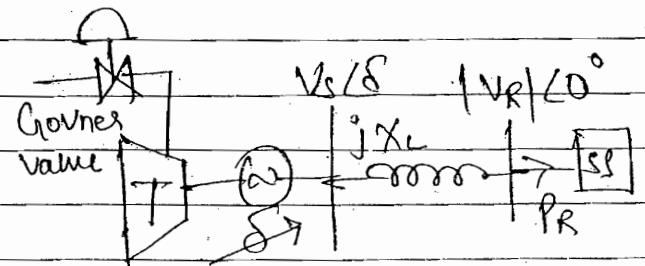
By using Bundle conductor effective radius of conductor is \uparrow so that L and X_L are \downarrow P_{max} increases.

~~book~~

$$P_s = P_R = P_{max} \sin \delta \quad P_R = \frac{|V_s|^2}{X_L} \sin \delta$$



load curve: Governing value



$$P_R = \frac{|V_s V_R|}{X_L} \sin \delta$$

can't use as changing parallel

Importance of δ ° -

- (1) Load demand is continuously variable parameter w.r.t time for supplying this variable load, load or power angle δ is selected as variable.

Practical value of $\delta \rightarrow 30^\circ$ to 45° due to stability limitation.

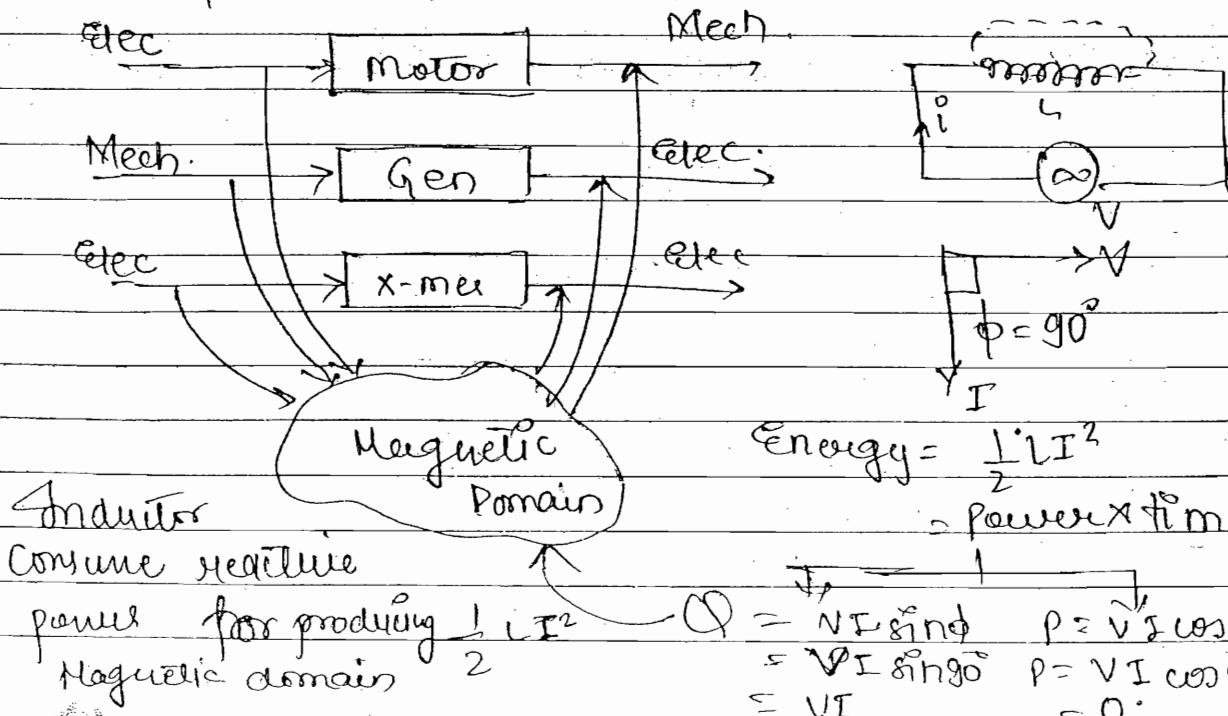
- (2) Voltage Regulation is to be minimum or zero.

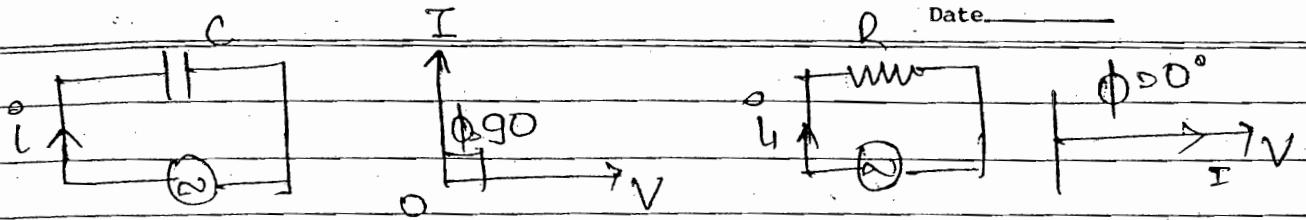
$$\% V_{REG} = \frac{|V_s| - |V_R|}{|V_R|} \times 100.$$

$$\text{If } |V_s| = |V_R| \Rightarrow V_{REG} = 0\%$$

- For controlling the voltage Reactive power of the supply has to be control.

Important of Reactive Power:-





$$\text{Energy} = \frac{1}{2} CV^2$$

= Power \times time

$$\text{Heat} = I^2 RT$$

= Power \times time

$$P = VI \cos\phi$$

$$= VI \cos 90^\circ$$

$$= 0$$

$$Q = VI \sin\phi$$

$$= VI \sin 90^\circ$$

$$(Q = VI)$$

$$P = VI \cos\phi$$

$$= VI \cos 0^\circ$$

$$(P = VI)$$

$$Q = VI \sin\phi$$

$$= VI \sin 0^\circ$$

$$Q = 0$$

$$\frac{1}{2} CV^2$$

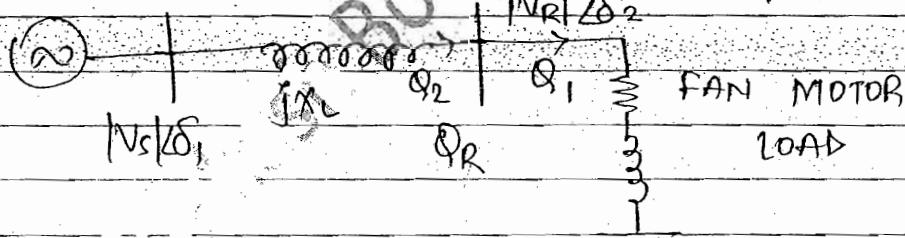
Capacitor consume reactive power

for storing energy

Resistor consume

active power for
giving heating effect.

Relation Between Reactive Power and Voltage



Q_1 = Reactive power demand by load

Q_2 = " " supply by source

$$Q_R = Q_1 - Q_2$$

$$Q_R = \left| \frac{V_s V_R}{X_L} \right| \cos(\delta_1 - \delta_2) = \left| \frac{V_R^2}{X_L} \right|$$

Assume $(\delta_1 - \delta_2) \approx 0$

$$Q_R = \left| \frac{V_s V_R}{X_L} \right| - \left| \frac{V_R^2}{X_L} \right|$$

$$V_R^2 - V_s V_R + X_L \cdot Q_R = 0 \quad [ax^2 + bx + c = 0]$$

$$V_R = \frac{V_s}{2} \pm \frac{\sqrt{V_s^2 - 4X_L Q_R}}{2}$$

(1) $V_R = \frac{V_s}{2} + \frac{\sqrt{V_s^2 - 4X_L Q_R}}{2}$

(a) If $Q_R = 0 \Rightarrow Q_1 = Q_2$

$$V_R = V_s \Rightarrow V_{REG} = 0\%$$

(b) If $Q_R > 0 \Rightarrow Q_1 > Q_2$
 $V_R < V_s$

(c) If $Q_R < 0 \Rightarrow Q_1 < Q_2$
 $V_R > V_s$

$$\Rightarrow V_{REG} = +ve$$

$$\Rightarrow V_{REG} = -ve$$

• Occur during Peak load
Timing

• Occur during OPP Peak
load timing.
(Ferranti Effect)

(2) $V_R = \frac{V_s}{2} - \frac{\sqrt{V_s^2 - 4X_L Q_R}}{2}$ Not a valid eqⁿ.

Q A x-line has a reactance of 0.5 p.u. operating at $V_s = 3$ p.u. and receiving end Reactive power = 0.5 p.u. find voltage drop across the line.

Solution

$$+ \text{----} \text{----} \text{----} \text{----} \text{----} \\ j0.5$$

$$V_s = 3 \text{ p.u.}$$

$$Q_R = 0.5.$$

$$V_R = ?$$

$$V_R = \frac{V_s}{2} + \frac{\sqrt{V_s^2 - 4X_L Q_R}}{2}$$

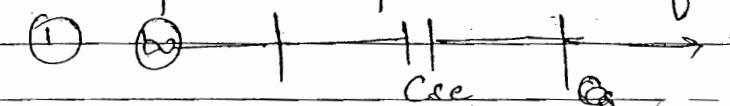
$$= \frac{3}{2} + \frac{\sqrt{3^2 - 4 \times 0.5 \times 0.5}}{2} = 2.914$$

$$\Delta V = V_s - V_R = 3 - 2.9 = 0.1 \text{ p.u.}$$

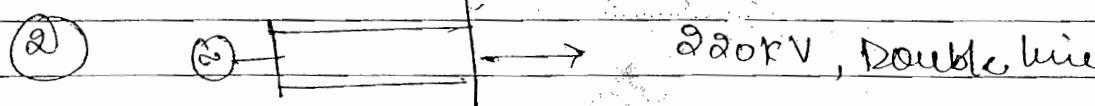
$$\% N_{REG} = \frac{V_s - V_R \times 100}{V_R} = \frac{3 - 2.9 \times 100}{2.9} = 3.41 \text{ A.U.}$$

Q A Nuclear power gen. stat. is generating 500MW to a load center which of the following is more suitable for the power transfer

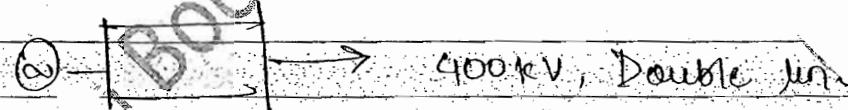
Solution



132 KV, 30% Cee



132 KV Double line



400 KV, Double line

Q A 133 KV X-line is delivering 10MW. If the line voltage is change to 133.8 KV then the power delivered by line is

Solution $P = \frac{V_s^2}{X_L} \quad P \propto V_s^2$

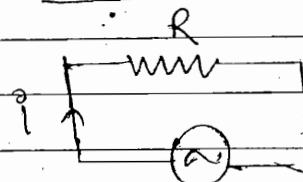
$$\frac{P_1}{P_2} = \frac{V_{s1}^2}{V_{s2}^2} \quad P_2 = P_1 \frac{V_{s2}^2}{V_{s1}^2} = 160 \text{ MW.}$$

$$P_2 = \frac{(132)^2 \times 10}{133.8} = 160 \text{ MW.}$$

- Power Factor :- for controlling of the voltage. Reactive power has to be control which is controlled by using power factor compensator Methods like
 - (1) Shunt capacitor
 - (2) Shunt reactor
 - (3) Syn. Phase Modifier
 - (4) Tap changing X-mers etc.

$\checkmark \delta$ is a degree at which a given load (R_L, R_C) matches with that of pure resistive load.

(1) R-load :-



$$v = V_m \sin \omega t$$

$$P = \frac{V_m^2}{R} \sin^2 \omega t$$

$$i = I_m \sin \omega t$$

• Instantaneous power.

$$P = V_i \cdot i$$

$$= V_m I_m \sin \omega t \sin \omega t$$

$$= \frac{V_m I_m}{2} (1 - \cos 2\omega t)$$

$$= \frac{V_m \cdot I_m}{\sqrt{2} \cdot \sqrt{2}} (1 - \cos 2\omega t)$$

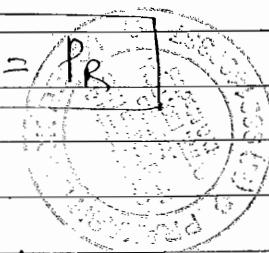
$$= V_{rms} \cdot I_{rms} (1 - \cos 2\omega t)$$

$$P = VI (1 - \cos 2\omega t)$$

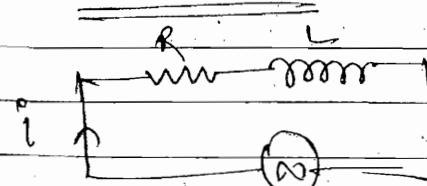
• Average Power

$$P_{avg} = \frac{1}{2\pi} \int_0^{2\pi} P \cdot d(\omega t)$$

$$P_{avg} = VI = PR$$



(2) R_L load :-



$$v = V_m \sin \omega t$$

$$i = I_m \sin(\omega t - \phi)$$

$$I_m = \frac{V_m}{Z} = \frac{V_m}{\sqrt{R^2 + \omega^2 L^2}}$$

$$\phi = \tan^{-1} \left(\frac{\omega L}{R} \right)$$

• Instantaneous Power:-

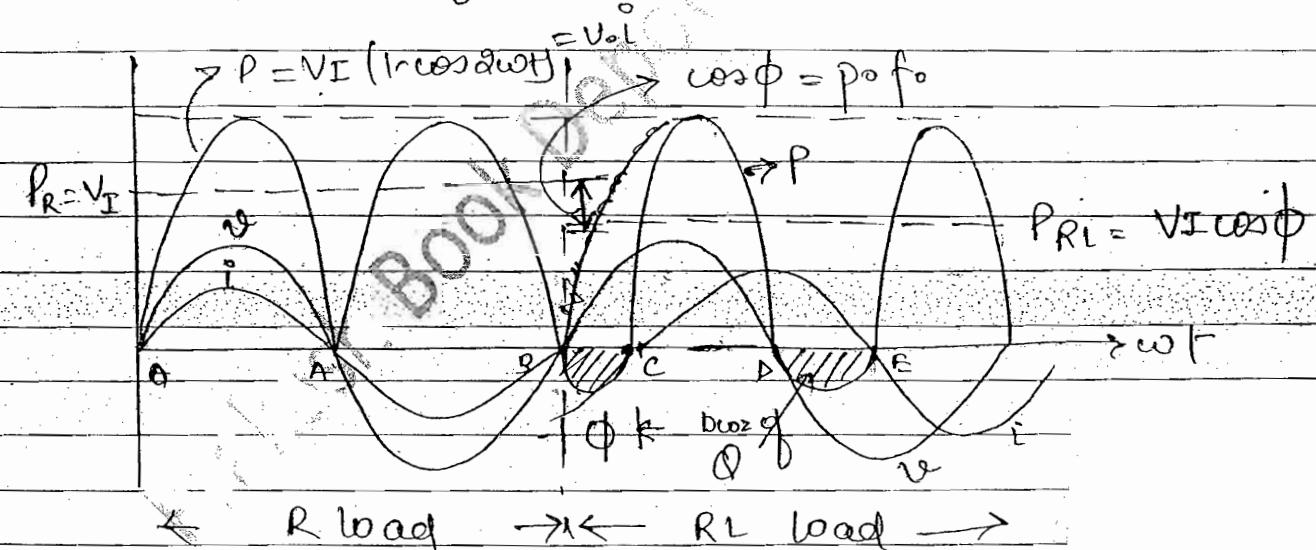
$$\begin{aligned}
 p &= V \cdot i = V_m I_m \sin \omega t \sin(\omega t - \phi) \\
 &= \frac{V_m I_m}{2} (\cos \phi - \cos(2\omega t - \phi)) \\
 &= \frac{V_m I_m}{2} (\cos(1 - \cos 2\omega t)) - \frac{V_m I_m \sin \phi \sin 2\omega t}{2}
 \end{aligned}$$

$$P = P(1 - \cos 2\omega t) - Q \sin 2\omega t$$

where $P = VI \cos \phi$, $Q = VI \sin \phi$

• Avg. Power:-

$$P_{avg} = \frac{1}{2\pi} \int_0^{2\pi} p \cdot d(\omega t) \quad P_{avg} = NI \cos \phi = P_{RL}$$

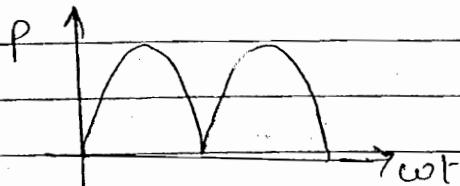
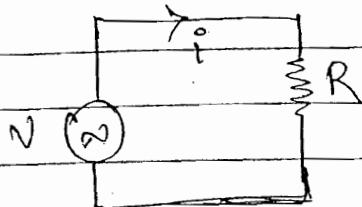


$$P_{RL} = \frac{VI \cos \phi}{VI} = \cos \phi = \rho_0 f$$

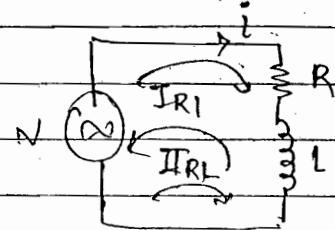
\rightarrow average power of RL load reduces due to negative power. (This P_R due to reactive power)

\rightarrow In-ree position power delivered by L to source

• R-load :-



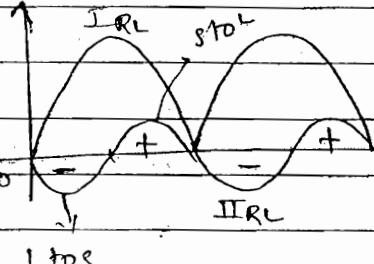
• R L load :-



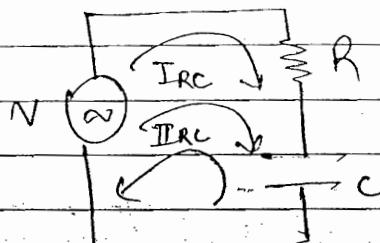
$$P = \overbrace{P(1 - \cos 2\omega t)}^{\text{I}_{RL}}$$

- $Q \sin 2\omega t$

I_{RL}



• RC load :-

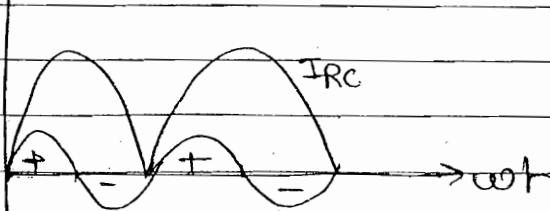


$$P = V_I$$

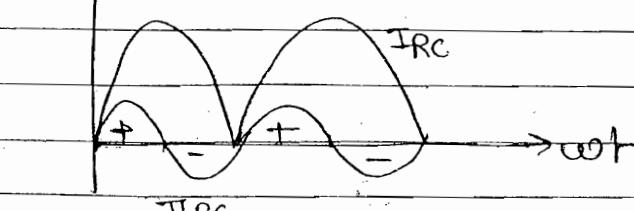
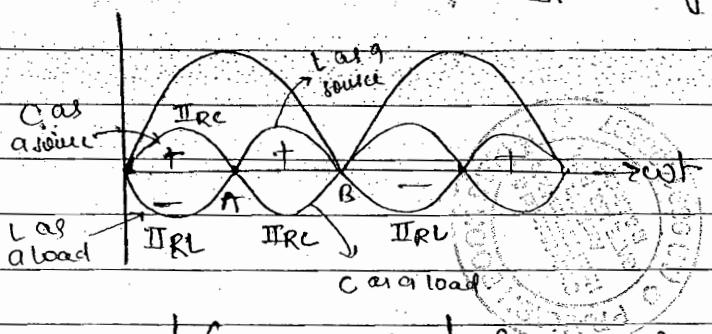
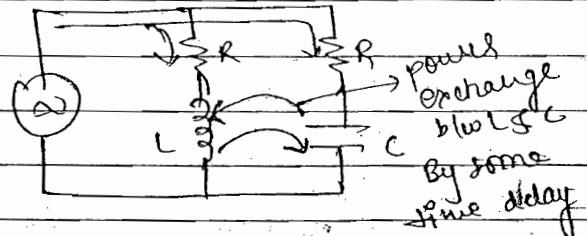
$$= P(1 - \cos 2\omega t) + \frac{I_{RC}}{I_{RC}}$$

$Q \sin 2\omega t$

$$I_{RC}$$



• RL & RC combine :-



(Deliver) Source

L heading VARs

C lagging VARs

(Absorb) Sink

L lagging VARs

C heading VARs

→ Inductor absorb lagging power and deliver leading power.

→ Capacitor absorb leading power and deliver lagging power.

VARs

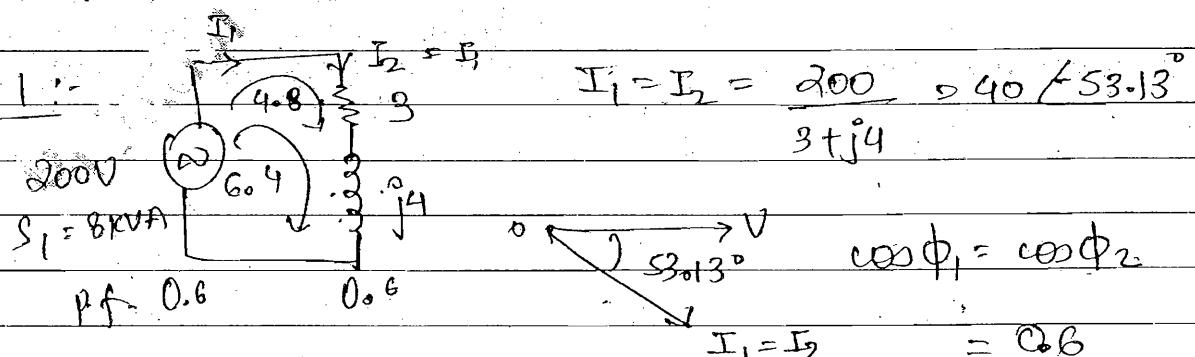
VARs

- If the voltage regulation is +ve indicates lagging VAR's demand is more than supply. By using a capacitor lagging VAR's can be compensated so that voltage regulation is zero and improvement of power factor can be achieved.
- If the voltage regulation is -ve indicates lagging VAR's demand is less than supply. For absorbing this excess lagging VAR's inductor or shunt reactor has to be used so that zero voltage regulation can be achieved.

Q1 A single- ϕ Induction Motor having Impedance of $3+j4$ is connected to 200V supply. Find currents and power and power factor of the load and source.

Q2 If the capacitance of $-j6.4$ is connected parallel to S.M. Find currents, p.f. and powers across each device.

Solution 1 :-



$$S_1 = S_2 = V \cdot I_1 \times$$

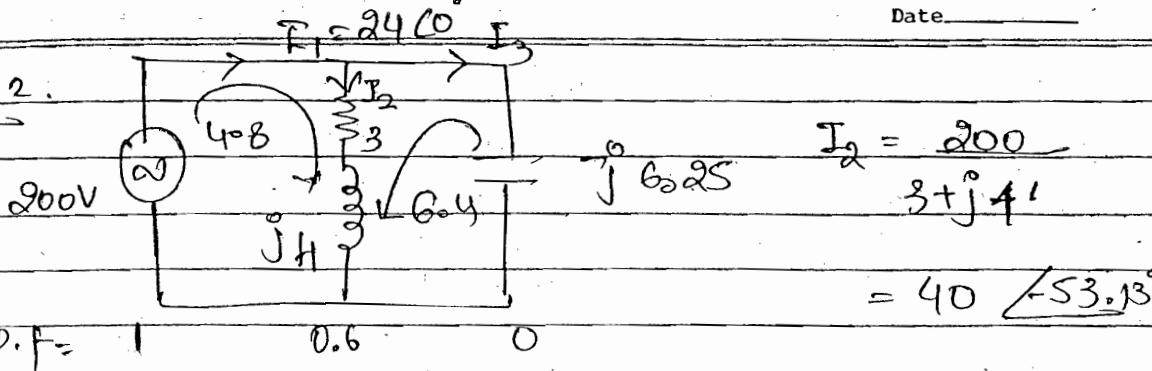
$$= 200 \times (40 / -53.13^\circ)^2$$

$$= (40.8 + j6.4) \text{ kVA}$$

$$P_2 = 40.8 \text{ kW}$$

$$Q_2 = 6.4 \text{ kVAR}$$

$$|S_1| = 8 \text{ kVA}$$

Solution 2:

$$\cos \phi = \cos 53.13^\circ = 0.6$$

$$S_2 = V_a I_2^* = 200 \times (40 \angle -53.13^\circ)^*$$

$$= (40.8 + j6.4) \text{ kVA.}$$

$$I_3 = \frac{200}{-j6.25} \Rightarrow 32 \angle 90^\circ$$

$$\cos \phi_3 = \cos 90^\circ = 0$$

$$S_3 = V_a I_3^* = 200 \times 32 \angle 90^\circ$$

$$= -j6.4 \text{ kVA}$$

$$= 0 - j6.4 \text{ kVAR}$$

$$I_1 = I_2 + I_3$$

$$= 40 \angle -53.13^\circ + 32 \angle 90^\circ$$

$$= 24 \angle 0^\circ$$

$$\cos \phi_1 = \cos 0^\circ = 1$$

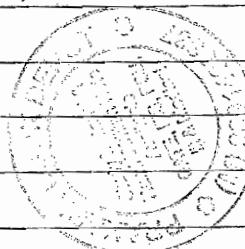
$$S_1 = V_a I_1^*$$

$$= 200 \times 24 \angle 0^\circ$$

$$= 408 \text{ kW.}$$

$$= 408 + j0 \text{ kVA}$$

$$|S_1| = 408 \text{ kVA.}$$



Advantage of Higher P.F.:-

(1) Current through x-line reduce

(2) x-section of line improves.

(3) Power loss is reduce.

(4) Voltage regulation can be minimised.

(5) Rated of generator is minimised.

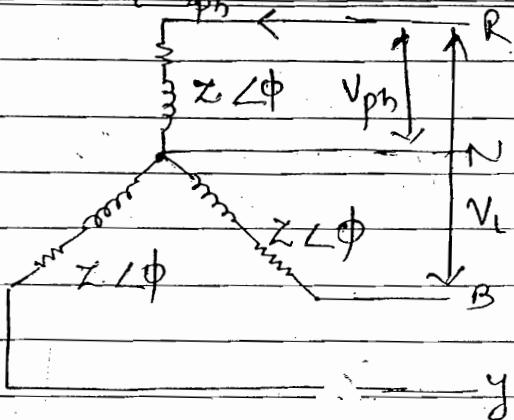
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• Star

$$V_{ph} = \frac{V_L}{\sqrt{3}}, I_{ph} = I_L$$

$$P_{3\phi} = \sqrt{3} V_L I_L \cos \phi$$

$$= \left| \frac{V_L^2}{Z} \right|^2 \cos \phi$$



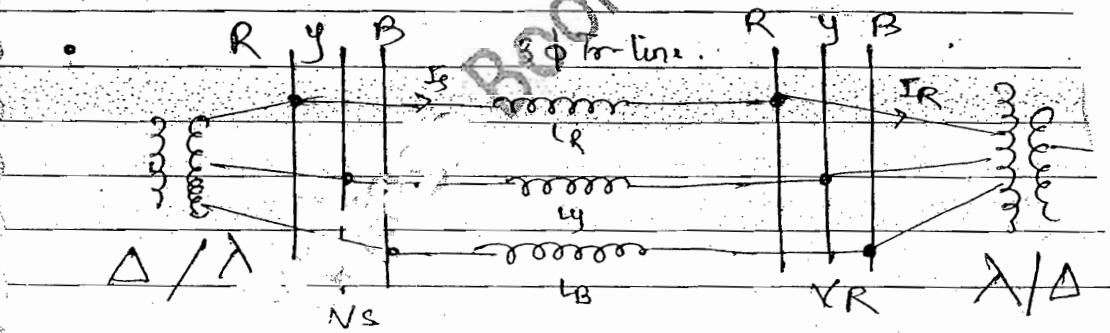
$$\Phi_{3\phi} = \left| \frac{V_L^2}{Z} \right|^2 \sin \phi.$$

• Delta $V_{ph} = V_L$ $I_{ph} = I_L / \sqrt{3}$

$$P_{3\phi} = \sqrt{3} V_L I_L \cos \phi = 3 \left| \frac{V_L^2}{Z} \right|^2 \cos \phi$$

$$\Phi_{3\phi} = 3 \left| \frac{V_L^2}{Z} \right|^2 \sin \phi$$

$$\boxed{\Phi_{3\phi} = P_{3\phi} \cdot \tan \phi}$$



→ Y & Δ are neither series connected nor parallel connected.

R, L, C, G } \rightarrow 3φ Tr-line are represented in
or
 A, B, C, D } per phase only

OX

$$V_s = A V_R + B I_R$$

↓ ↓ ↓
ph ph ph ?

→ convert all terms in phase values.

$$V_{\text{eph}} = A \frac{V_R}{\sqrt{3}} + B, I_R$$

By N.R related
to $\sqrt{3}$. I_R
remain same.

$$V_{SL} = \sqrt{3} V_{\text{eph}}$$

$$I_S = C V_R + D I_R$$

↓ ↓ ↓ ↓ ↓
? ph V_L ph ?

$$I_{\text{eph}} = C \frac{V_R}{\sqrt{3}} + D_0 I_R$$

$$I_{SL} = \sqrt{3} I_{\text{eph}}$$

AS V_R related to $\sqrt{3}$. $I_{SL} = I_{\text{eph}}$

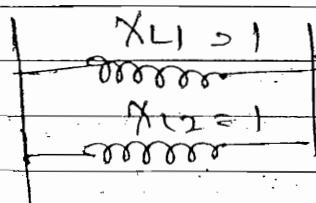
Ex:- 2 $P_R = \left| \begin{matrix} V_S & V_R \\ X_L \end{matrix} \right| \sin \delta$

$$P_{R\text{ph}} = \left| \begin{matrix} V_{\text{eph}}, V_{R\text{ph}} \\ X_{L\text{ph}} \end{matrix} \right| \sin \delta$$

$$P_{R,3\phi} = 3 \left| \begin{matrix} V_{\text{eph}}, V_{R\text{ph}} \\ X_{L\text{ph}} \end{matrix} \right| \sin \delta = 3 \left| \begin{matrix} V_{SL} & V_{RL} \\ \sqrt{3} & \sqrt{3} \end{matrix} \right| \sin \delta$$

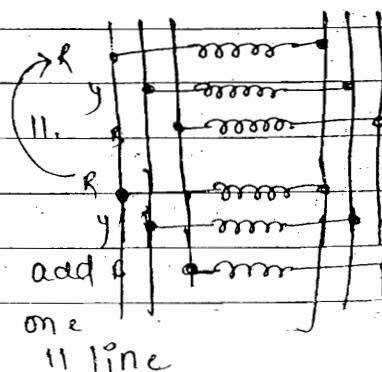
$$P_{R,3\phi} = \left| \begin{matrix} V_{SL} & V_{RL} \\ X_{L\text{ph}} \end{matrix} \right| \sin \delta$$

- voltages are always line values whereas R, L, C, G , A, B, C, D parameters are always in per phase values. in 3ϕ



$$X = 1X1 = 0.5$$

1+1



Methods of Reactive Power Control :-

Receiving End Methods.

Source End Method.

(1) Shunt Capacitor

(1) Gen. Excitation Control.

(2) Shunt Reactor

(3) Series Capacitor

(4) Syn. Phase Modifier
(SPM)

(5) On-load Tap changing
(OLTC) X-mes

(6) Booster X-mes

(1) Shunt Capacitor Compensation :-

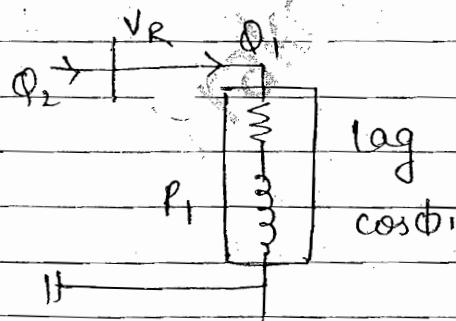
Shunt Capacitor is used for:-

(1) Improve voltage regulation

(2) Improve power factor

(3) Improve system stability. By increasing load angle δ .

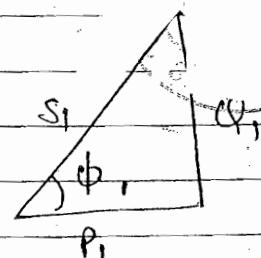
(a) without Shunt Capacitor:-



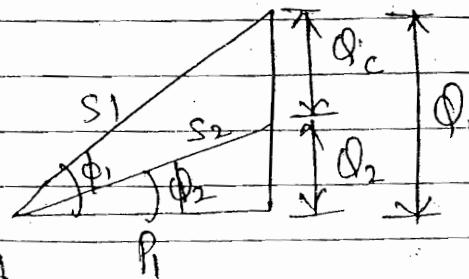
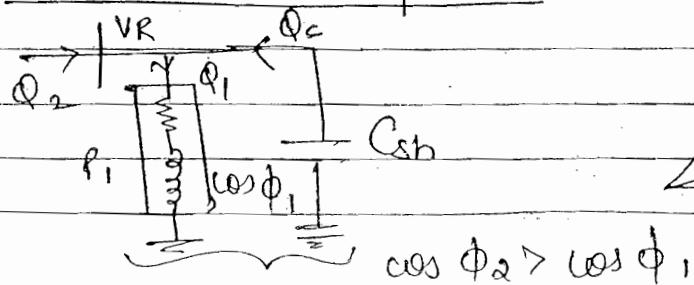
Assume

$$Q_1 > Q_2$$

$$V_R < V_S$$



(b) with Shunt Capacitor :-



$Q_c = \text{VAR Rating of Csh}$

$$Q_1 = Q_2 + Q_c$$

$$Q_c = Q_1 - Q_2$$

$$Q_c = P_1 (\tan \phi_1 - \tan \phi_2)$$

$Q_c = 3\phi$ VAR Rating of Csh.

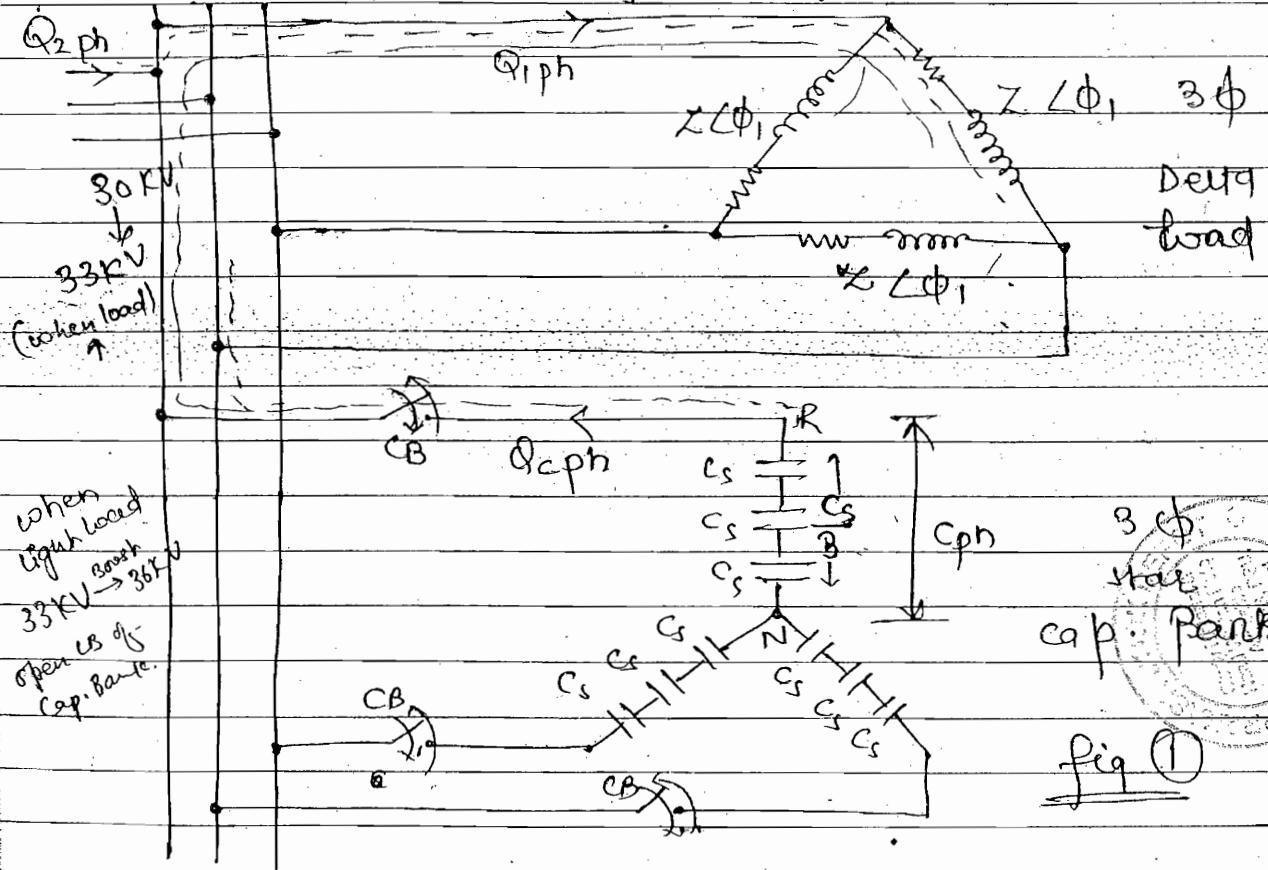
$P_1 = 3\phi$ Input Active power to load.

$$= P_0$$

η

- Practical Arrangement of Cap. Bank In Substation:-

R Y B 33 KV (Maintaining Rated Voltage)



- Capacitor per phase [Cph]:-

$$Q_{cph} = V_{ph} \cdot I_{ph} \cdot \sin \phi$$

For pure capacitor $\phi = 90^\circ$, $I_{ph} = \frac{V_{ph}}{X_C} = 2\pi f C_{ph} V_{ph}$

$$Q_{ph} = V_{ph} (2\pi f C_{ph} V_{ph}) \sin 90^\circ$$

$$Q_{ph} = 2\pi f C_{ph} \cdot V_{ph}^2$$

$$C_{ph} = \frac{Q_{ph}}{2\pi f V_{ph}^2} = \frac{\Phi_C}{3(2\pi f P V_{ph}^2)}$$

$$C_{ph} = \frac{P_i (\tan \phi_1 - \tan \phi_2)}{3(2\pi f V_{ph}^2)}$$

$$(1) Star Cap. Bank = V_{ph} = \frac{V_L}{\sqrt{3}}$$

$$(2) Delta Cap. Bank = V_{ph} = V_L$$

- Capacitance of Each Cell :- [C_s] :-

$$C_s = n C_{ph}$$

$n = \text{No. of Cells/phase}$

- In cap. Bank, multiple capacitor are used b/c if we use single capacitor insulation ↑, cost ↑.

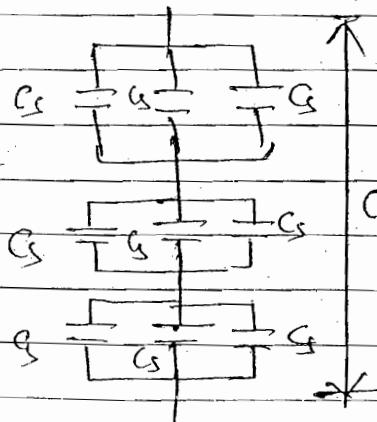


fig ① can also show us,

Q A 3φ 3M having $\text{pf} = 0.6 \text{ lag}$ is connected to a load of 9 MW and has η of 90%. Find the rating of shunt capacitor required for improving the power factor to 0.8 lagging.

Solution $\eta = \frac{\text{O/p}}{\text{S/p}}$ $\text{S/p} = \frac{\text{O/p}}{\eta} = \frac{9}{0.90} = 10 \text{ MW}$

$$\begin{aligned} Q_c &= 10 [\tan \phi_1 - \tan \phi_2] \\ &= 10 [\tan \cos^{-1} 0.6 - \tan \cos^{-1} 0.8] \\ &= 50.8 \text{ MVAR.} \end{aligned}$$

Q A 3φ 3M connected in Δ across 11 KV and the Motor has impedance of $3 + j4 \Omega/\text{phase}$ a star connected cap. Bank is used for improving pf to 0.9 lag if the capacitor bank has 5 cells per phase calculate capacitance of each cell.

Solution $C_s = 5 \text{ Cph}$ $Q = 2\pi f Cph V_{pn}^2$

$$\Delta \text{ load: } P_1 = \frac{3V_i^2 \cos \phi}{Z} = \frac{3 \cdot 11^2 \cos [j4]}{\sqrt{3^2 + 4^2}} = 43.56 \text{ MW}$$

$$C_s = n Cph = \frac{n \cdot P_1 (\tan \phi_1 - \tan \phi_2)}{3 (2\pi f V_{pn}^2)}$$

$$= 5 \times 43.56 (\tan \cos^{-1} 0.6 - \tan \cos^{-1} 0.9) / (2\pi \times 50 \times (1/\sqrt{3})^2)$$

$$C_s = \frac{217.8 (0.8490)}{38013.27} = 4.86 \times 10^{-3}$$

- Capacitor Banks are used in the 33 and 132 KV substation.

(2) Shunt Reactor [Lsh]:-

Shunt Reactor is used:-

- (1) For compensation of Ferranti Effect.
- (2) Changes the factor from leading to lagging.
That is pf is reduce.
- (3) System stability is reduce by increasing S.

Ferranti Effect: - Neglecting R, f, G parallel.

In case of NO LOAD or LIGHT LOAD due to RC component of the Tr-line $V_R > V_s$ occurs and this is dominant in medium and long Tr-line.

For compensating this ferranti effect shunt reactor is used.

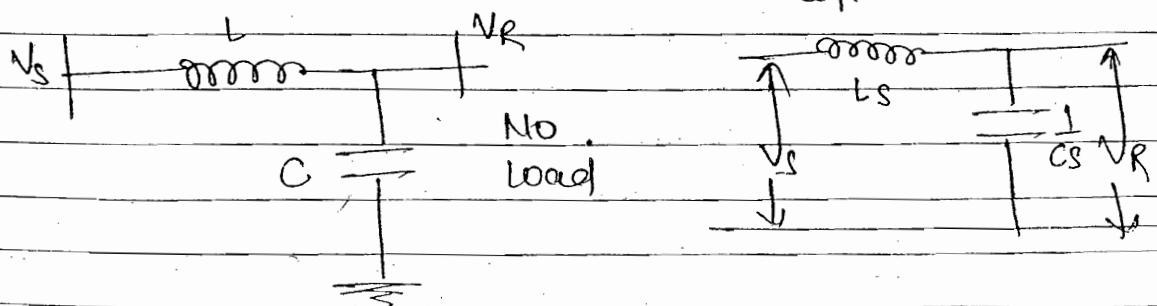
- Voltage is more dangerous than current.

Voltage $\uparrow \rightarrow$ Insulating Breakdown

Current $\uparrow \rightarrow I^2 R$ losses \rightarrow insulation failure
delay.

- Shunt Reactor are used in 400 KV and 765 KV substation.

Lapace.



$L, C = Tr\text{-line parameters}$

$$V_R = \frac{V_s V_{cs}}{I_s + V_{cs}} = \frac{V_s}{Ls^2 + 1}$$

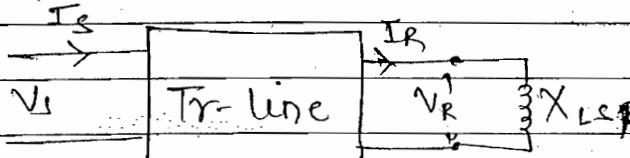
$$V_R = V_s + V_s \cdot \omega^2 L C$$

$$V_R = V_s + \Delta V_R$$

$$\Delta V_R = V_s \omega^2 L C$$

$$V_R > V_s$$

Compensation of Ferranti Effect :-



$$X_{sh} = \text{Reactance of } L_{sh} = \frac{V_R}{I_R}$$

$$\text{At No load } V_R > V_s$$

$$\text{with } L_{sh} \therefore V_R = V_s$$

$$V_R = A V_R + B I_R \quad [V_s = A V_R + B I_R]$$

$$V_R(1-A) = B \cdot I_R$$

$$X_{sh} = \frac{V_R}{I_R} = \frac{B}{(1-A)}$$

$$V_s = A V_R + B I_R$$

$$\text{At No load: } I_R = 0 \Rightarrow V_s = A V_R$$

$$V_R = V_s / A$$

$V_R \rightarrow$ Receiving end voltage

$$I_s = C V_R + D I_R$$

$$\text{At No load } I_R = 0 \Rightarrow I_s = C V_R$$

$$I_s = \text{Charging current} = I_c$$

$$\frac{V_{Rph}}{A_{ph}} = \frac{V_{Sph}}{A_{ph}} \Rightarrow \frac{\sqrt{3} V_{RL}}{\sqrt{3} A_{ph}} = V_{SL}$$

$$\boxed{V_{R1} = \frac{V_{SL}}{A}}$$

$A \rightarrow$ phase value.

$$\frac{I_S}{A_{ph}} = \frac{C \cdot V_R}{A_{ph}} \quad | \quad I_C = C \cdot \frac{V_{RL}}{\sqrt{3}}$$

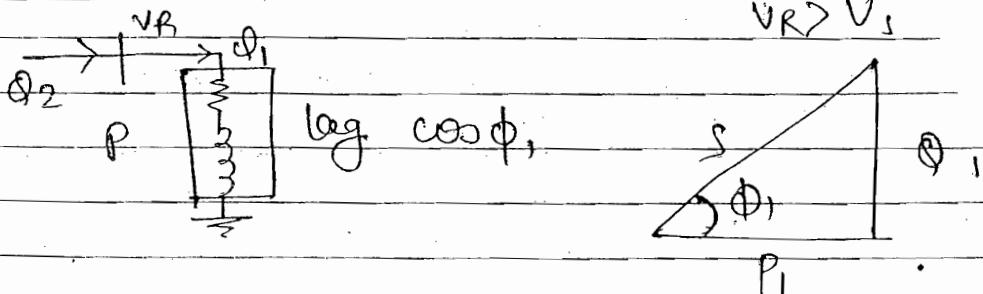
- (Q) A 3 ϕ Tr-line has $V_s = 400 \text{ kV}$ $A = D = 0.8 \angle 0^\circ$
 $B = 100 \angle 90^\circ \Omega$, $C = 0.5 \times 10^{-6} \text{ F}$ Calculate V_R and
 Ic at no load (2) Shunt Reactor required
 for compensating ferroanti effect.

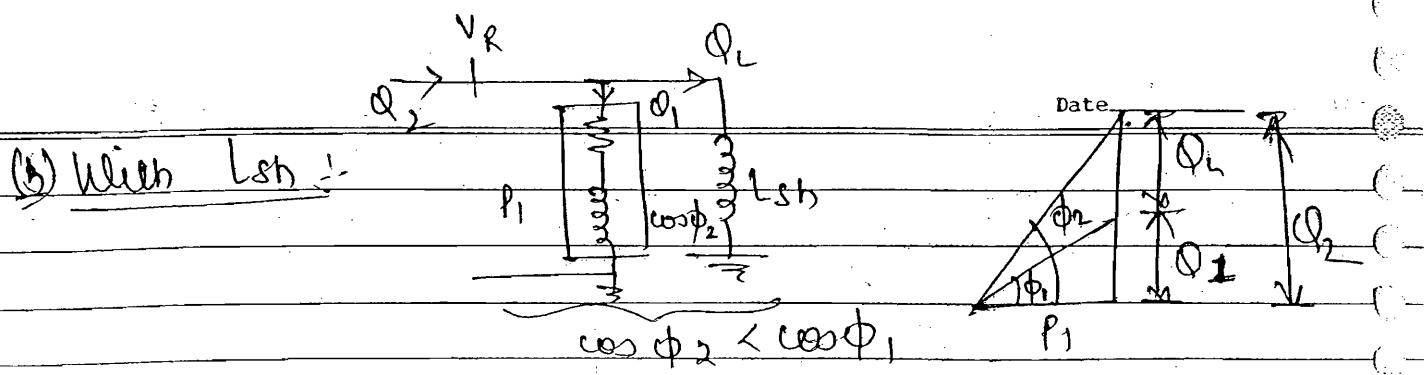
Calculation $V_R = \frac{V_s}{A} = \frac{400}{0.8 \angle 0^\circ} = 500 \text{ kV}$

$$X_{Lsh} = \frac{B}{(1-A)} = \frac{100 \angle 90^\circ}{(1 - 0.8 \angle 0^\circ)} = \frac{100 \angle 90^\circ}{0.2} \\ = 500 \angle 90^\circ$$

$$I_C = C \times \frac{V_{RL}}{\sqrt{3}} = 0.5 \times 10^{-6} \times \frac{500 \times 10^3}{\sqrt{3}} \\ = 0.14 \text{ A/phase.}$$

(Q) Without Lsh: Assume $\Phi_1 < \Phi_2$ $V_R > V_s$





(b) With Lsh :-

$$Q_L = 3\phi \text{ VAR Rating of Lsh} : \quad Q_L = Q_2 - Q_1$$

$$Q_L = P_1 (\tan \phi_2 - \tan \phi_1)$$

Inductance per phase [Lph] :-

$$Q_{Lph} = V_{ph} \cdot I_{ph} \sin \phi$$

$$\text{For pure Lsh, } \phi = 90^\circ, \quad I_{ph} = \frac{V_{ph}}{2\pi f L_{ph}}$$

$$Q_{Lph} = \frac{V_{ph}^2}{2\pi f L_{ph}}$$

$$L_{ph} = \frac{V_{ph}^2}{2\pi f Q_{Lph}}$$

~~From previous~~ $Q_{Lph} = Q_L / 3$

• Relation Between Q, f, V :-

(1) Shunt Capacitor :-

$$Q_{Cph} = 2\pi f V_{ph}^2 C_{ph}$$

$$Q \propto f V^2$$

$$\frac{Q_2}{Q_1} = \left(\frac{V_2}{V_1}\right)^2 \left(\frac{f_2}{f_1}\right)$$

(2) Shunt Reactor :-

$$Q_{Rph} = \frac{V_{ph}^2}{2\pi f L_{ph}}$$

$$\frac{Q_2}{Q_1} \propto \frac{V^2}{f}$$

$$\frac{Q_2}{Q_1} = \left(\frac{V_2}{V_1} \right)^2 \left(\frac{f_1}{f_2} \right)$$

If the voltage \uparrow by 10%, $f \downarrow$ by 5%. How much of Reactive power has to be compensated using

- ① Shunt Capacitor.
- ② Shunt Reactor

Soln: (i) Shunt Capacitor (ii) Shunt Reactor.

$$\frac{Q_2}{Q_1} = \left(\frac{1.1V_1}{V_1} \right)^2 \times \left(\frac{0.95f_1}{f_1} \right)$$

$$\frac{Q_2}{Q_1} = \left(\frac{1.1V_1}{V_1} \right)^2 \times f_1 / 0.95f_1$$

$$Q_2 = 1.15Q_1, 15\% \text{ Excess}$$

$$Q_2 = 1.27Q_1, 27\% \text{ Excess}$$

(3) Series Capacitor Compensation:

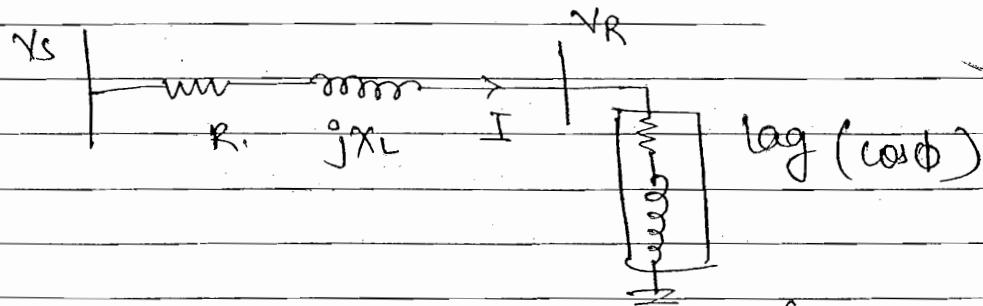
By using series capacitor :- system also

(1) System stability \uparrow

(2) Power transferred to the Tr. line \uparrow

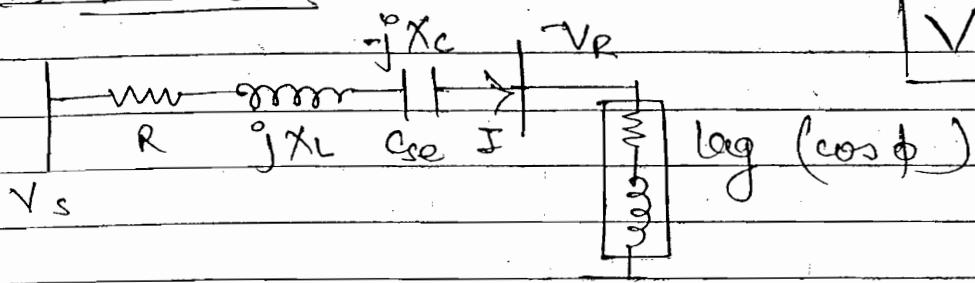
(3) Voltage regulation is reduced

(a) Without Cse :-



$$\% \text{ VREG} = \frac{V_s - V_R \times 100}{V_R} = \frac{I(R \cos \phi + X_L \sin \phi)}{V_R} \times 100$$

(b) with Cse :-



$$V_{REG2} < V_{REG1}$$

$$\% V_{REG} = \frac{I(R \cos \phi + (X_L - X_C) \sin \phi)}{V_R} \times 100$$

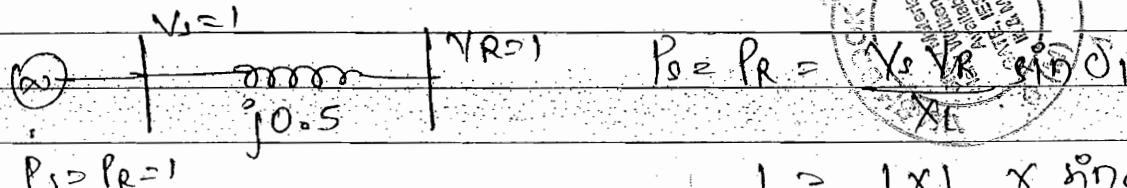
Q At Tr-line a reactance $X = 0.5 \text{ p.u}$ is connected

to a generator and load center operating $V_s = V_R = 1 \text{ p.u}$
if the load 1 p.u is delivered by the line.

Find the load angle of the generator

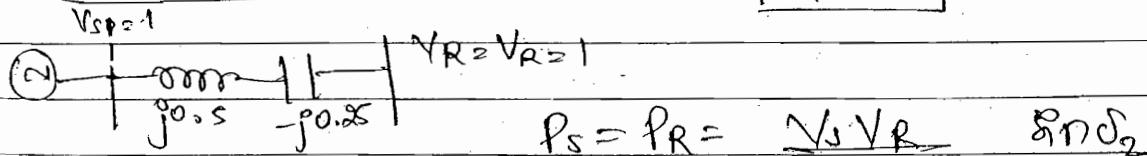
- ① Without compensation ② With compensation of 0.25 p.u.

Solution ① Without Cse :-

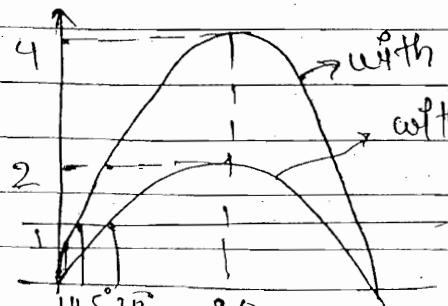


$$I = \frac{1}{0.5} \times \sin \delta_1 = 2 \sin \delta_1$$

② With Cse :-



$$P_L = P_R = \frac{V_s V_R}{(X_L - X_C)} \sin \delta_2$$



$$I = \frac{1}{0.5 - 0.25} \sin \delta_2 = 4 \sin \delta_2$$

$$\delta_2 = 140.5^\circ$$

$$\delta_2 < \delta_1$$

$\delta_2 \rightarrow$ More Stable

(4) Synchronous Phase Modifier :- (SPM)

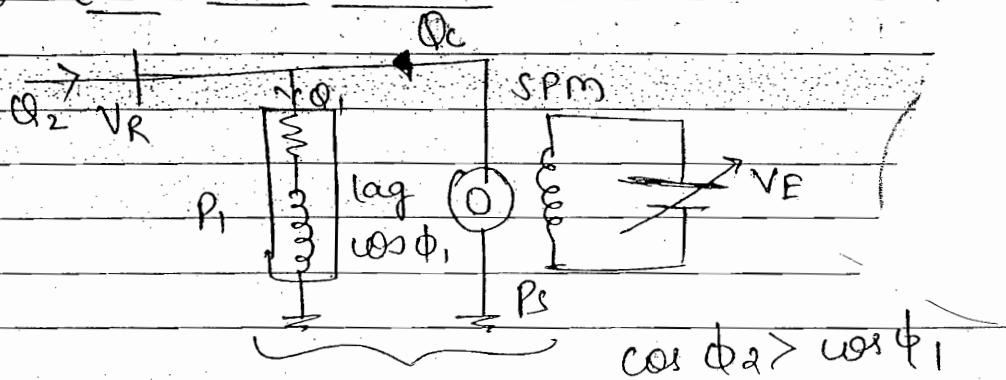
SPM is basically a syn Motor. It is used for

- (1) Driving Mechanical load
- (2) Controlling the reactive power voltage and pof.
- (3) If it is used for driving any mechanical load with than the load angle $\neq 0$ and maintaining b/w 30° to 45° due to stability limit.
- (4) If it is used for pf or voltage control it is normally normally maintaining at NO LOAD so that $\delta = 0$.

(5) The over excited SPM is used for supply lagging VAR's and working similar to the shunt capacitor.

(6) Under excited SPM is used for absorbing lagging VAR's or delivering leading VAR's. It is working similar to the Hunt Reactor.

(a) Over Excited SPM: Assume $VR < V_s$



- Rating of SPM:-

① If $P_s \neq 0$

$$Q_c = P_l \cdot \tan \phi_1 - (P_l + P_s) \cdot \tan \phi_2$$

$$\text{Rating of SPM} = (P_s + jQ_c) \dots \text{VA} \quad V_F = VR$$

② If $P_s = 0$

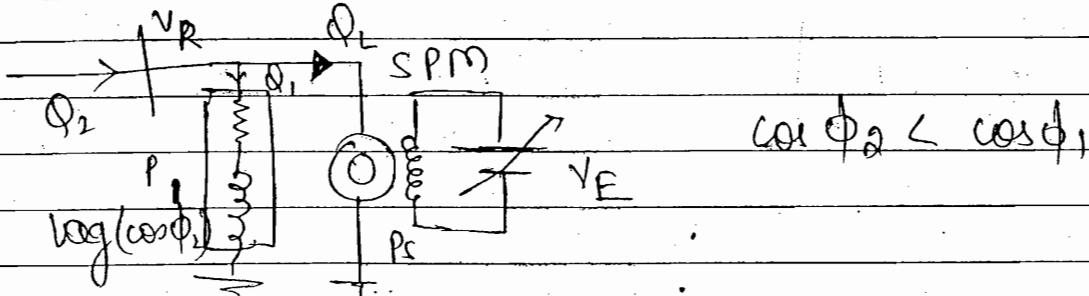
$V_A > V_R$

Date _____

$$Q_c = P_1 (\tan \phi_1 - \tan \phi_2)$$

$$\text{Rating of SPM} = Q_c - \dots V_A$$

(b) Under Excited SPM: - Assume $V_B < V_R$



• Rating of SPM: -

$$\textcircled{1} \text{ If } P_S \neq 0$$

$$\textcircled{2} \text{ If } P_S = 0$$

$$Q_c = (P_1 + P_S) + \tan \phi_2 - \tan \phi_1 P_1$$

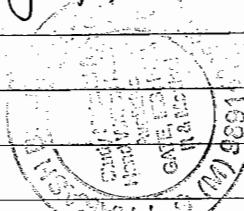
$$Q_c = P_1 (\tan \phi_2 - \tan \phi_1)$$

$$\text{Rating of SPM} = P_S + j Q_c \quad \text{Rating of SPM} = Q_c - V_A$$

A 3φ SM having a rating of 10 MW at 0.6 lagging is connected with SPM for improving pf to 0.8 lag. Find the rating of SPM if SPM

(1) consumes 1 MW of active power

(2) running under no-load.



~~$$\text{Value } \textcircled{1} Q_c = P_1 \tan \phi_1 - (P_1 + P_S) \tan \phi_2$$~~

$$= 10 \tan \cos^{-1} 0.6 - (10+1) \tan \cos^{-1} 0.8$$

$$= 5.083$$

$$\text{Rating of SPM} = (P_S + j Q_c) \text{ MVA R}$$

$$= (1 + j 5.083) \text{ MVA P}$$

② no load . $\delta_c = P_1 (\tan \phi_1 - \tan \phi_2)$
 $= 10 [\tan \cos^{-1} 0.6 - \tan \cos^{-1} 0.8]$
 $= 5.833 \text{ MVA}$

Rating of SPM = $\delta_c = 5.833 \text{ MVA}$

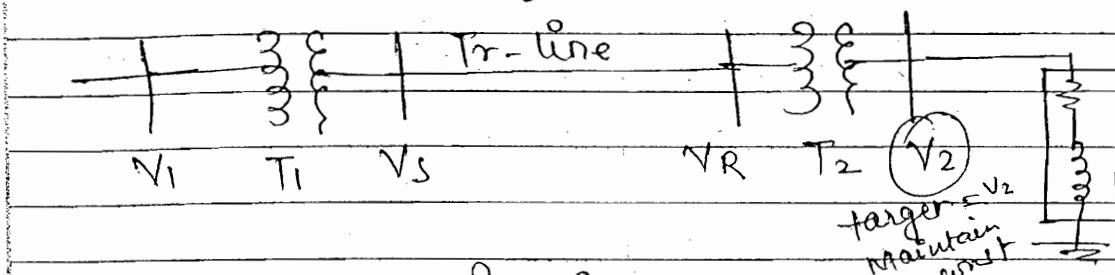
• Comparison Between SPM and Shunt Compensation

SPM

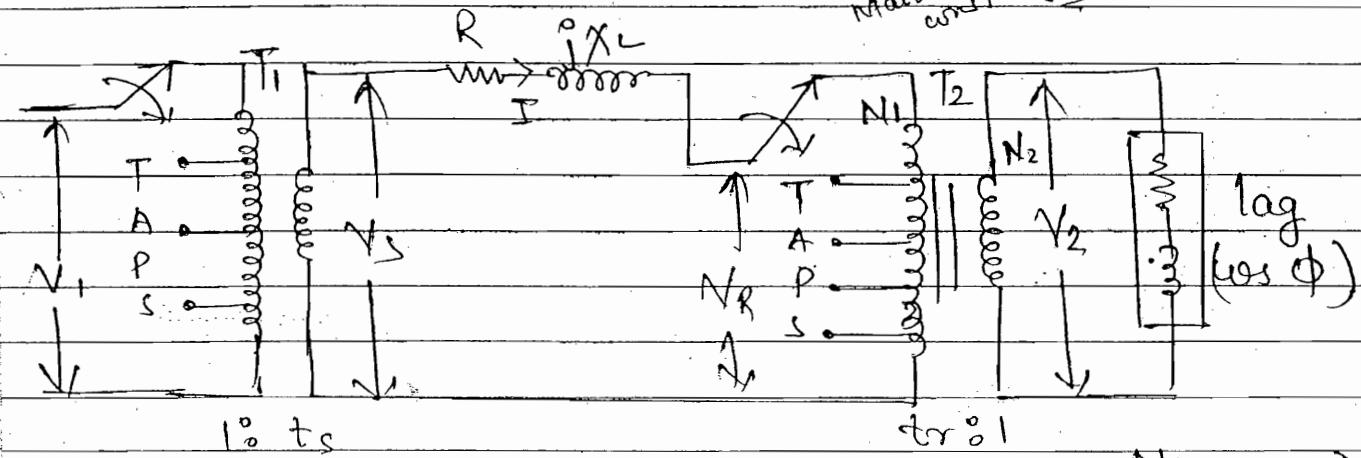
Shunt Compensation

- | | |
|--|---|
| (1) A single unit of SPM can be used both inductors and capacitor by adjusting excitation. | (1) Two separate units are required that is inductor & capacitor for adjustment of voltage. |
| (2) Smooth voltage regulation is possible. | (2) Step by step voltage regulation is possible. |
| (3) Initial cost of SPM is higher. | (3) Initial cost is lower. |
| (4) SPM requires more maintenance. | (4) It requires less maintenance. |
| (5) Initial starting methods are required for bringing the syn. Motor up to synchronous speed. | (5) There is no starting mechanism required. |
| (6) It consumes both active & reactive power. | (6) Consumes only Reactive power. |
| (7) Due to above缺点, SPM is practically not preferred in the substations. | (7) It is most practically used in substation for the voltage control. |

(5) OLTC Transformer :-



target
maintain
const



$$\frac{V_1}{V_s} = \frac{1}{t_s} \Rightarrow N_1 = V_s t_s \quad \text{①}$$

$$\frac{V_2}{V_R} = \frac{1}{tr} \Rightarrow N_R = V_R tr$$

$$V_s - V_R = RI \cos \phi + X_L I \sin \phi$$

$$I \cos \phi = \frac{P_R}{N_R}, \quad I \sin \phi = \frac{Q_R}{N_R}$$

$$V_s - V_R = \frac{P_R R}{N_R} + \frac{X_L Q_R}{N_R}$$

$$V_R V_s - V_R^2 = R P_R + X_L Q_R$$

$$\Rightarrow V_R^2 - V_s V_R + R P_R + X_L Q_R = 0 \quad \text{②}$$

Substitute ① in ②

$$V_2^2 t_r^2 - V_1 V_2 t_r t_s + R P_r + X_L Q_r = 0$$

$\chi_2 = f [t_r, t_s]$; χ_2 is controlled by controlling
transformer tap & $t_r t_s$.

[Off Normal Setting = $t_r t_s = 1$]

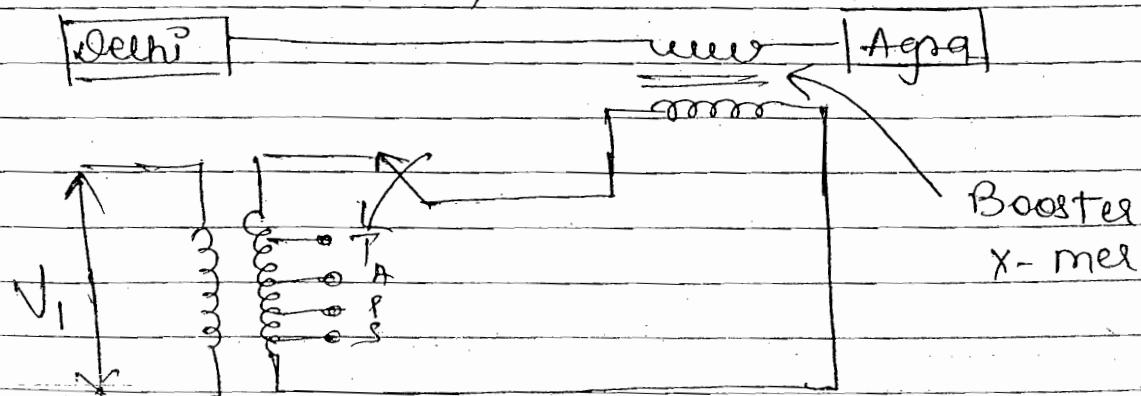
- tap changing at H.V. bcoz current value is small, less heating, less heat produce.

- OLTC is most practically used for the voltage control in the substation.
- It is used in all voltage levels like 400 / 220, 220 / 132, 132 / 33 and 33 / 11 KV
- X-met normally provided on the H.V side where current is small so that the intensity of wiring is minimized which enhances the life of the X-met.

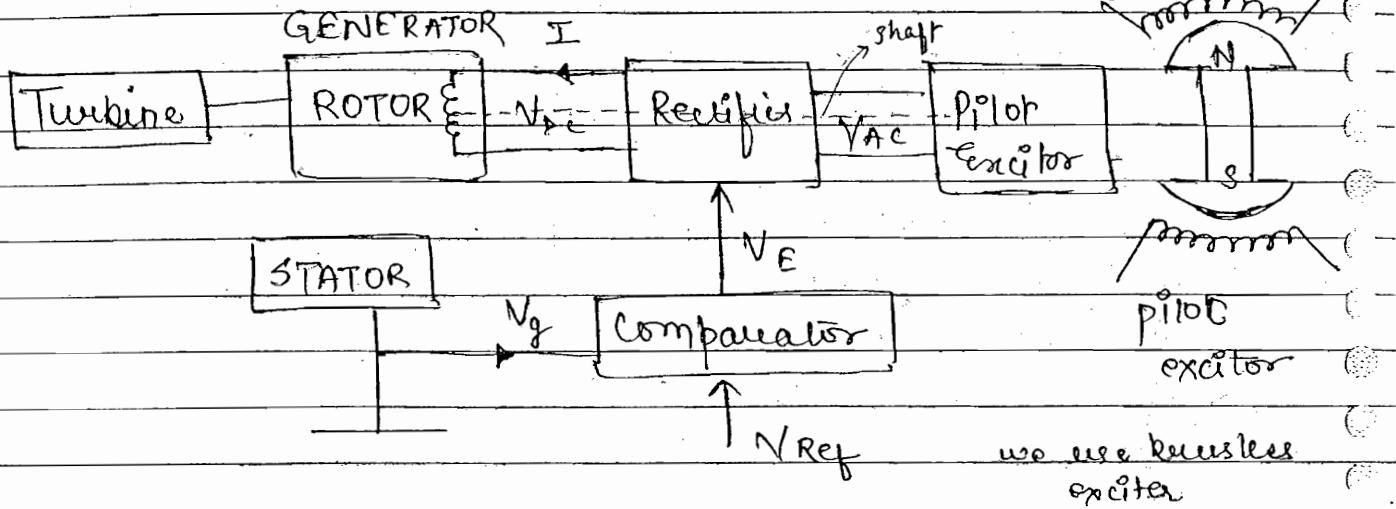
BOOSTER TRANSFORMER: - (for line side)

previous desired are
for load side)

- (1) It is used to maintain uniform voltage throughout the Tr-line
- (2) It is practically used in remote substations and in traction applicat. for maintaining uniform voltage



Generator Excitation Control:-



$$V_E = V_g - V_{Ref}$$

- ① If $V_g = V_{Ref} \Rightarrow V_E = 0 \Rightarrow$ Constant excitation.
- ② If $V_g > V_{Ref} \Rightarrow V_E > 0 \Rightarrow$ Reduce excitation until $V_E = 0$
- ③ If $V_g < V_{Ref} \Rightarrow V_E < 0 \Rightarrow$ Increase excitation until $V_E = 0$

- Generator excitation control is most practically used for maintaining constant voltage at the terminals of the generator. This method is adopted after applying shunt capacitors and OLTC operation of the X-mu. Because the consumer needs to be do not experience over voltage. The type of voltage control is called automatic voltage regulation.
- C_{sh1} to C_{sh4} are capacitor Bank used to maintain the voltage.

- When there is a voltage drop in 33 kV Bus, C_{sh2} or C_{sh3} or both are switch ON, when still there is not maintaining 33 kV (ex:- 30 kV) go for OLTC-1, when still OLTC-1 get fail to maintain voltage constant, C_{sh1} or C_{sh3} or both

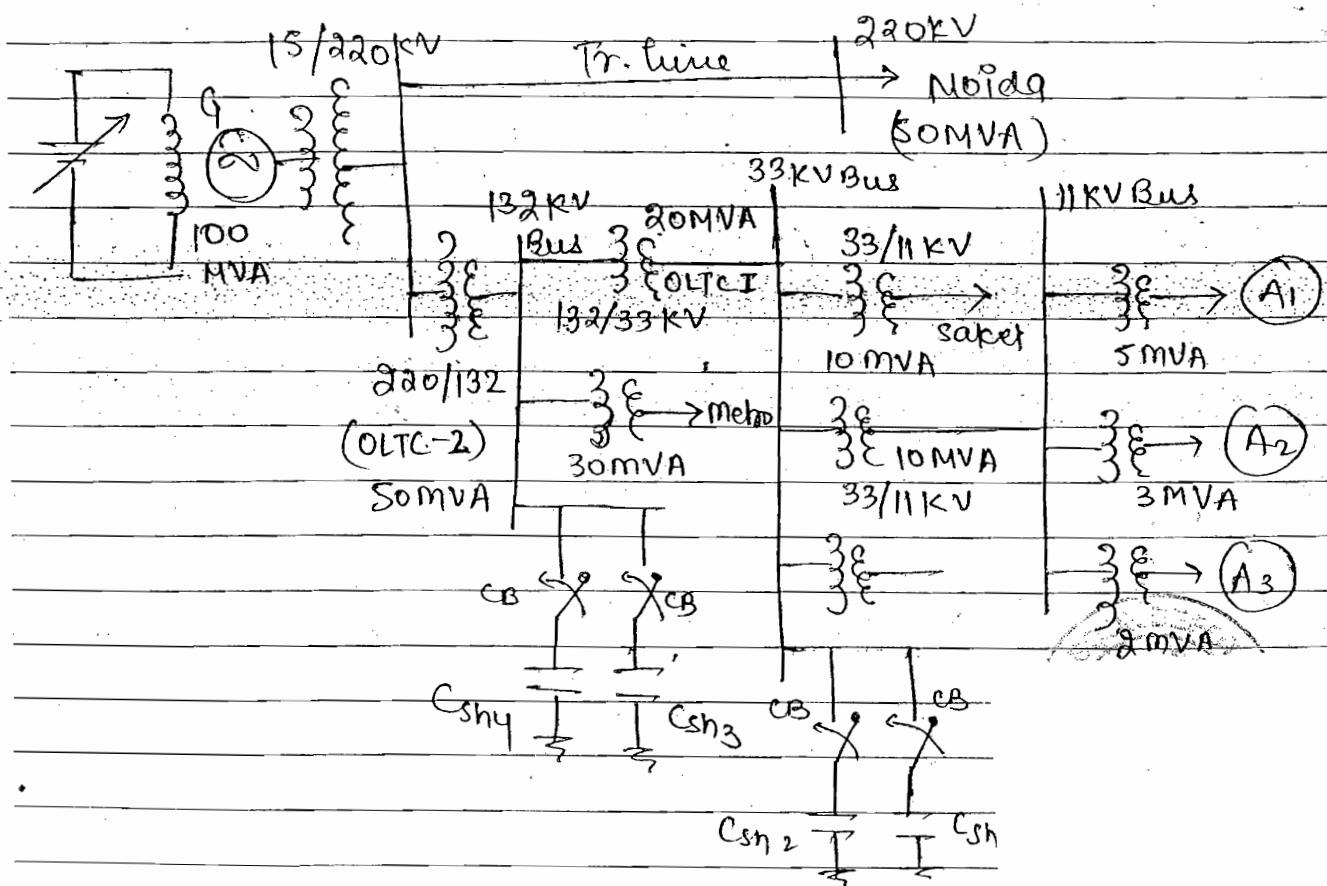
are switch ON. Before switch ON these two capac. bank, first they check, whether incoming voltage is 132 kV or not. Then they switch ON the the cap. Bank when not maintaining 132 kV, go for OLTC-2. When it is not also fail to maintain 220, check the Pneumatic voltage is 220 kV or not, then finally go for generator exciter case.

- When there is over voltage same sequence will follow, in this case, cap. Banks are removed.

Sequence:- \rightarrow Cap. Bank

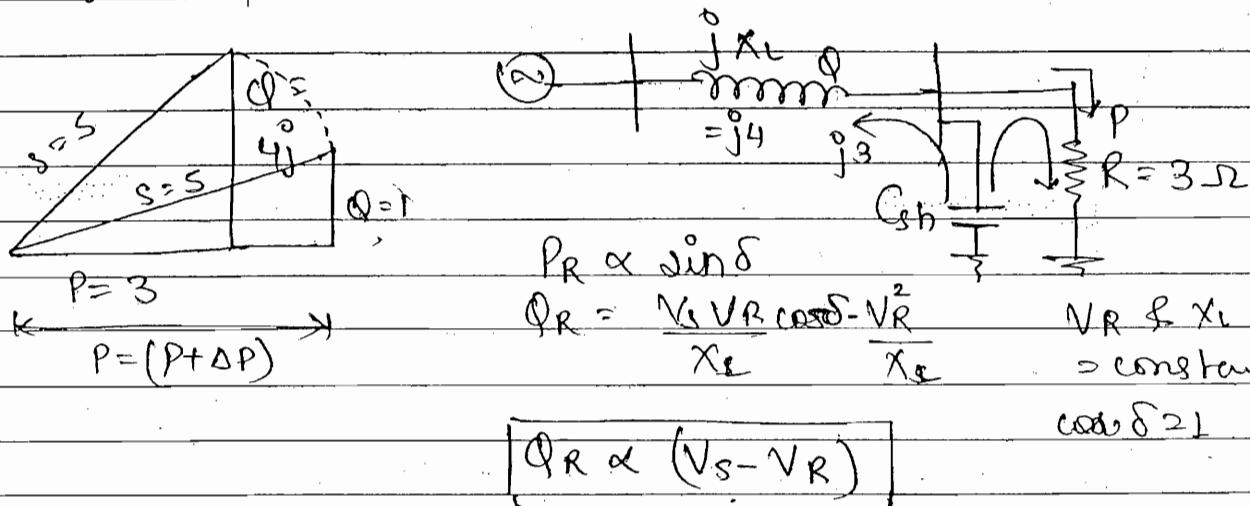
\Rightarrow OLTC

\Rightarrow Gen. Excitation.

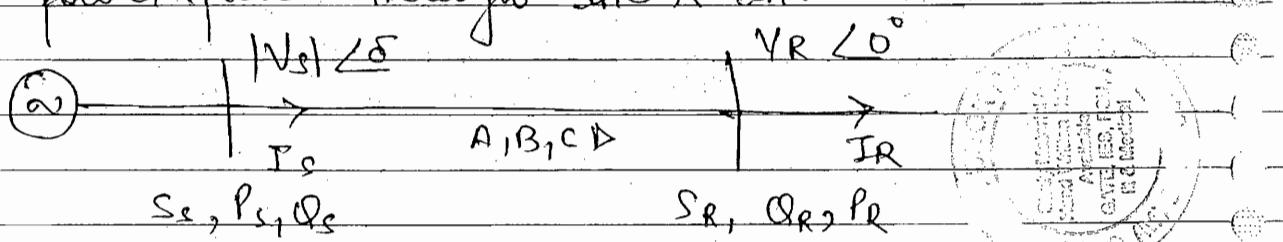


Power Flow through Tr-lines:-

- When install C_{sh} , burden of reactive power on generator will reduce. and convert into active power.
- Gen \rightarrow only active power, Reactive power by other means.
- Aim \rightarrow transfer maximum active power through X-line.
- Compensator deliver reactive power to X-line as well as load.



- Relationship Between ABCD parameter, voltage and power flow through the X-line.



$$\text{Let } A = |A| \angle \alpha \quad B = |B| \angle \beta \quad C = |C| \angle \gamma \quad D = |D| \angle \delta \\ V_s = |V_s| \angle \delta \quad V_R = |V_R| \angle 0^\circ$$

$$AD - BC = 1$$

Receiving End Power :- $V_s > AVR + BIR$

$$IR = \frac{V_s - AVR}{B} - ①$$

$$= \frac{|V_s| \angle \delta}{|B| \angle \beta} - |A| \angle \alpha \cdot |V_R| \angle 0^\circ$$

$$I_R = \left| \frac{V_s}{B} \right| \angle \delta - \left| \frac{A V_R}{B} \right| \angle \alpha - \beta.$$

$$I_R^* = \left| \frac{V_s}{B} \right| \angle \beta - \delta - \left| \frac{A V_R}{B} \right| \angle \beta - \alpha \quad \text{--- (3)}$$

$$S_R = P_R + j Q_R = V_R \cdot I_R^* \quad \text{--- (2)}$$

Substitute (2) in (3):

$$P_R + j Q_R = \left| \frac{V_s V_R}{B} \right| \angle \beta - \delta - \left| \frac{A V_R^2}{B} \right| \angle \beta - \alpha.$$

Separate Real and Imaginary terms.

$$\boxed{\begin{aligned} P_R &= \left| \frac{V_s V_R}{B} \right| \cos(\beta - \delta) - \left| \frac{A V_R^2}{B} \right| \cos(\beta - \alpha) \\ Q_R &= \left| \frac{V_s V_R}{B} \right| \sin(\beta - \delta) - \left| \frac{A V_R^2}{B} \right| \sin(\beta - \alpha) \end{aligned}}$$

Sending End powers:-

$$I_S = C V_R + D I_R \quad \text{--- (4)}$$

Substitute (1) in (4)

$$I_S = C V_R + D \left(\frac{V_s}{B} - \frac{A V_R}{B} \right)$$

$$= \frac{D V_s}{B} + \left(BC - AD \right) V_R$$

$$= \frac{D V_s}{B} - \frac{V_R}{B} = \frac{|D| \angle \alpha |V_s| \angle \delta - |V_R| \angle 0^\circ}{|B| \angle \beta} \quad \text{--- (1)}$$

$$I_S = \left| \frac{D V_s}{B} \right| \angle \alpha + \delta - \beta - \frac{V_R}{B} \angle \beta$$

$$I_S^* = \left| \frac{D V_s}{B} \right| \angle \beta - \alpha - \delta - \left| \frac{V_R}{B} \right| \angle \beta \quad \text{--- (5)}$$

$$S_s = P_s + j Q_s = V_s I_s^*$$

$$= V_s \angle \delta \cdot I_s^* \quad \text{--- (6)}$$

Substitute (5) in (6)

$$S_s = P_s + j Q_s = \left| \frac{D V_s^2}{B} \right| \left(\beta - \alpha \right) - \left| \frac{V_s V_R}{B} \right| \left(\beta + \delta \right)$$

Separate Real and Imaginary terms.

$$P_s = \left| \frac{D V_s^2}{B} \right| \cos(\beta - \alpha) - \left| \frac{V_s V_R}{B} \right| \cos(\beta + \delta)$$

$$Q_s = \left| \frac{D V_s^2}{B} \right| \sin(\beta - \alpha) - \left| \frac{V_s V_R}{B} \right| \sin(\beta + \delta)$$

• Condition for Receiving Maximum Active Power :-

$$P_R = \left| \frac{V_s V_R}{B} \right| \cos(\beta - \delta) - \left| \frac{A V_R^2}{B} \right| \cos(\beta - \alpha)$$

δ is variable.

for Receiving max. PR.

$$\frac{dP_R}{d\delta} = 0$$

$$\Rightarrow - \left| \frac{V_s V_R}{B} \right| \sin(\beta - \delta) = 0 \quad \left| \frac{V_s V_R}{B} \right| \neq 0$$

$$\text{At } \beta = \delta$$

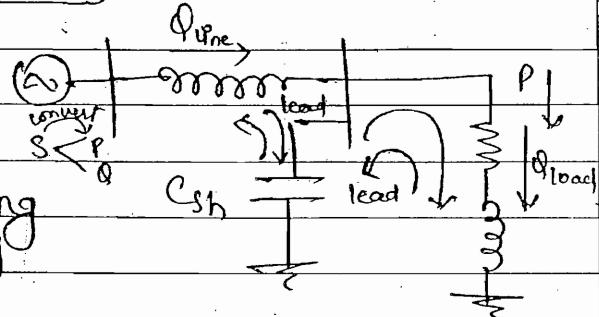
$$P_{R\max} = \left| \frac{V_s V_R}{B} \right| - \left| \frac{A V_R^2}{B} \right| \cos(\beta - \alpha)$$

$$\text{At } \delta = \beta$$

$$Q_R = \left| \frac{V_s V_R}{B} \right| \sin(\beta - \beta) - \left| \frac{A V_R^2}{B} \right| \sin(\beta - \alpha)$$

$$\varphi_R = - \left| \frac{\sqrt{V_R^2 A}}{B} \sin(\beta - \alpha) \right|$$

NOTE:- $\varphi_R = -$ ve indicates leading nature of load and for this leading load leading VARs have to be supplied for Receiving Pmax.



• LOCUS OF POWER:-

$$P_R + \left| \frac{AV_R^2}{B} \cos(\beta - \alpha) \right| = \left| \frac{V_L V_R}{B} \right| \cos(\beta - \delta) \quad \text{--- (1)}$$

$$\varphi_R + \left| \frac{AV_R^2}{B} \sin(\beta - \alpha) \right| = \left| \frac{V_L V_R}{B} \right| \sin(\beta - \delta) \quad \text{--- (2)}$$

Squaring and adding eqⁿ (1) & (2)

$$\left[P_R + \left| \frac{AV_R^2}{B} \cos(\beta - \alpha) \right|^2 \right]^2 + \left[\varphi_R + \left| \frac{AV_R^2}{B} \sin(\beta - \alpha) \right|^2 \right] = \left(\frac{V_L V_R}{B} \right)^2$$

eqⁿ (3) represents circle equatn.

$$(x-a)^2 + (y-b)^2 = r^2$$

$r = \text{Radius of circle } \left| \frac{V_L V_R}{B} \right|$

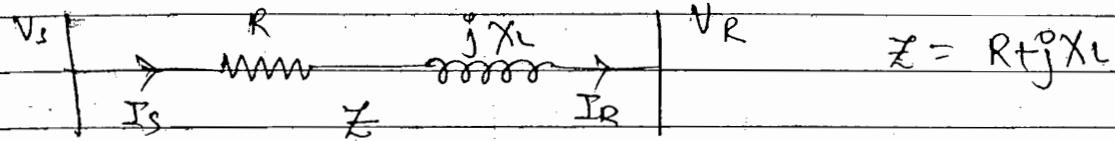
Center of circle

$$(a, b) = \left[- \left| \frac{\sqrt{V_R^2 A}}{B} \cos(\beta - \alpha) \right|, - \left| \frac{AV_R^2}{B} \sin(\beta - \alpha) \right| \right]$$

NOTE:- locus of P_R, φ_R is a circle at constant $|V_L|$, $|V_R|$ similarly locus of P_S, φ_S is a circle at constant $|V_L|, |V_R|$.

• Generalised Equation of Power :-

Assume short Tr. line : (C, G are neglected)



$$\begin{aligned} & \text{Current } I_s \text{ enters the line, } V_s \text{ is at the source end, } V_R \text{ is at the receiving end.} \\ & V_s = V_R + I_R \cdot Z \\ & V_s = I \cdot V_R + Z \cdot I_R \\ & I_s = I_R = (0) V_R + 1 \cdot I_R \end{aligned}$$

$$\begin{bmatrix} V_s \\ I_s \end{bmatrix} = \begin{bmatrix} 1 & Z \\ 0 & 1 \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix}$$

Assume $R \ll X_L$

$$Z = jX_L = X_L \angle 90^\circ = B \angle B \quad A \angle \alpha = 1 \angle 0^\circ \Rightarrow C = 0 \quad \text{--- eqn ①}$$

Receiving End power :-

(A, B, C, D) given

$$P_R = \left| \frac{V_s V_R}{B} \right| \cos(\beta - \delta) - \left| \frac{V_s^2 A}{B} \right| \cos(\beta - \alpha) \quad \text{--- ②}$$

Substitute ① in ②

$$P_R = \left| \frac{V_s V_R}{X_L} \right| \cos(90^\circ - \delta) - \left| \frac{V_s^2 A}{X_L} \right| \cos(90^\circ - 0)$$

(C, D) given

$$P_R = \left| \frac{V_s V_R}{X_L} \right| \sin \delta$$

$$P_R \propto \sin \delta$$

(A, B) given

$$P_R = \left| \frac{V_s V_R}{B} \right| \sin(\beta - \delta) - \left| \frac{A V_s^2}{B} \right| \sin(\beta - \alpha) \quad \text{--- ③}$$

Substitute ① in ③

when δ is small

$$Q_R = \left| \frac{V_s V_R \cos \delta}{X_L} - \frac{V_R^2}{X_L} \right|$$

If δ is small, $\cos \delta \approx 1$

$$Q_R = \left| \frac{V_s (V_s - V_R)}{X_L} \right|$$

$$Q_R \propto (V_s - V_R)$$

- sending End power:-

Substitute ① in P_s, Q_s

Average Real Power :-

$$P_{avg} = \frac{Q_R + Q_s}{2}$$

$$P_s = \left| \frac{V_s V_R}{X_L} \right| \sin \delta = P_R$$

$$Q_s = \left| \frac{V_s^2}{X_L} - \frac{V_s V_R}{X_L} \cos \delta \right|$$

$$P_{avg} = \frac{V_s^2 - V_R^2}{2 X_L}$$

- From the following Now calculate the active power and reactive power flow through the x-line.

~~Book~~

10 30	90	10 10
90	10 10	

Solution $V_s = 10 \angle 30^\circ$ $V_R = 10 \angle 10^\circ$

$$P_R = \left| \frac{V_s V_R}{X_L} \right| \sin \delta$$

$$= \frac{10 \times 10}{2} \sin(30 - 10) = 25 \text{ W}$$

$$Q_R = \left| \frac{V_s V_R \cos \delta - V_R^2}{X_L} \right| = \frac{10 \times 10 \cos(30 - 10) - 10^2}{2}$$

$$= 6.7 \text{ VARs}$$

$$Q_s = \left| \frac{V_s^2 - V_s V_R \cos \delta}{X_L} \right| = 6.7 \text{ VARs}$$

- The sequence of impedance of equipment is equal to the equipment original equipment's impedance.

$$Z_{p.u} = \frac{Z_{\infty} (\text{MVA})_b}{(KV_b)^2}$$

$Z_{p.u.} \rightarrow R_{p.u.}$

- Q 1 Tr-line impedance of 90.5 p.u is connected to a load of 1 p.u UPF. If $V_R = 1 / 0^\circ$. Calculate V_s and δ .

Solution

$\text{Tr. } V_s / \delta = ? \quad V_R / \delta = 1 / 0^\circ$

$P_R = 1 \text{ p.u.} \quad Q_R = 0.8 \text{ lag.}$

$$P_R = \frac{V_s V_R}{X_L} \sin \delta$$

$$\phi_{load} = P \tan \delta \\ = 1 \times \tan 10^\circ 8 \\ = 0.75 \text{ p.u.}$$

$$I = \frac{V_s X_L}{0.5} \sin \delta$$

$$V_s \sin \delta = 0.5 \quad \text{--- (1)}$$

$$Q_R = \left| \frac{V_s V_R}{X_L} \cos \delta - \frac{V_R^2}{X_L} \right|$$

load is resistive UPF $Q_R = 0$

$$Q_R = 0 \Rightarrow \left| \frac{V_s X_L}{0.5} \cos \delta - \frac{1^2}{0.5} \right| = 0.8 \text{ p.u.}$$

$$V_s \cos \delta = 1 \quad \text{--- (2)}$$

Solving (1) & (2)

$$\frac{V_s \sin \delta}{V_s \cos \delta} = \frac{0.5}{1} \quad \tan \delta = 0.5 \\ \delta = 26.56^\circ$$

$$V_s \sin 26.56^\circ = 0.5$$

$$V_s = 1.011823 = 1.012 \text{ p.u. Ans.}$$

- $V_s = 1.012 \quad V_R = 1$ Maintain the voltage for induction.

Q, which is diff.

Date _____

HJ

Q In the previous problem if $V_s = V_R = 1 \text{ p.u}$ is maintained by using compensators, find the rating of compensator required for

- (i) 1 p.u. UPF load
- (ii) 1 p.u. 0.6 lagging load.
- (iii) 1 p.u. 0.6 leading load.
- (iv) 1 p.u. 0.995 leading load.

Solution:- (i) $P_R = 1 \text{ p.u. UPF}$, $|V_s| = |V_R| = 1$

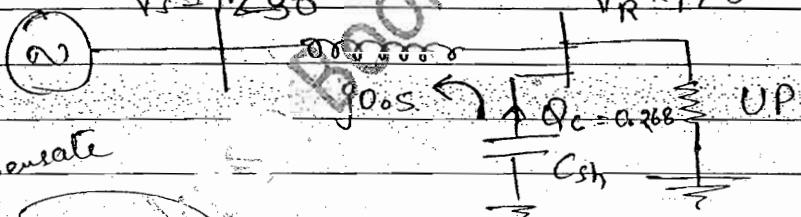
$$P_R = \frac{|V_s - V_R|}{X_L} \sin \delta$$

$$1 = \frac{|X|}{0.5} \sin \delta, \sin \delta = 0.5, \delta = 30^\circ$$

$$Q_R = \frac{|V_s V_R| \cos \delta}{X_L} = \frac{|V_R|^2}{X_L} \quad \text{demanding}$$

$$\Rightarrow \frac{|X|}{0.5} \cos 30^\circ = \frac{1^2}{0.5} = -0.268 \text{ p.u.}$$

$V_s = 1 / 30^\circ$ $V_R = 1 / 0^\circ$ indicating delivering leading VAR

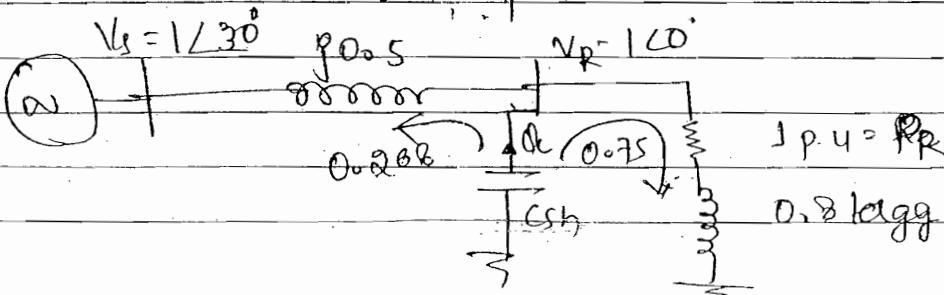


To compensate
 -0.268

$$Q_c = -Q_R = -(-0.268) = 0.268 \text{ p.u.} = Q_{line}$$

(ii) $P_R = 1 \text{ p.u. } 0.8 \text{ lagging load.}$

$$\text{Q load} = P_R \times \tan \phi = 1 \times \tan \cos^{-1} 0.8 = 0.75 \text{ p.u.}$$



$$Q_c = Q_{\text{line}} + Q_{\text{load}} = 0.268 + 0.75 = 1.018 \text{ p.u.}$$

(3) $P_R = 1 \cdot \text{p.u.}, 0.6 \text{ load}$

$$Q_{\text{load}} = 1 \times \tan(\cot^{-1} 0.6) = 1.38 \text{ p.u.}$$

$$V_s = 1 \angle 30^\circ \text{ p.u.}$$

(2)

mmmm

0.268

$$V_R = 1 \angle 0^\circ$$

$$Q_L = 1.112 \text{ p.u.}$$

$$Q_c = 1.38 - 0.268 \\ = 1.112 \text{ p.u.}$$

Lsh

3.

3.

1 p.u.

delivers lagging VAR

of 1.38

(4) $P_R = 1 \cdot \text{p.u.}, 0.995 \text{ load}$

$$Q_{\text{load}} = 1 \times \tan \cot^{-1} 0.995 = 0.1 \text{ p.u.}$$

$$V_s = 1 \angle 30^\circ \text{ p.u.}$$

(2)

mmmm

0.268

$$V_R = 1 \angle 0^\circ$$

0.1 p.u.

1 p.u.

$$Q_c = 0.268 - 0.1$$

$$= 0.168 \text{ p.u.}$$

Csh.

0.995 lead

- Refer 1 p.u. $\rightarrow 0.995 \rightarrow$ Near to unity leading \rightarrow Resistive more, capacitive less.

\rightarrow 0.6 leading \rightarrow far to unity

\rightarrow less Resistive, capacitive more

we require more reactive power.

Q) A - Tr-line has an impedance of $5+j25 \Omega/\text{phase}$ is operating at $V_s = V_R = 33 \text{ KV}$. Find rating of compensator required for a load of

(1) 15 MW U.P.F.

$$\delta = 21.7^\circ$$

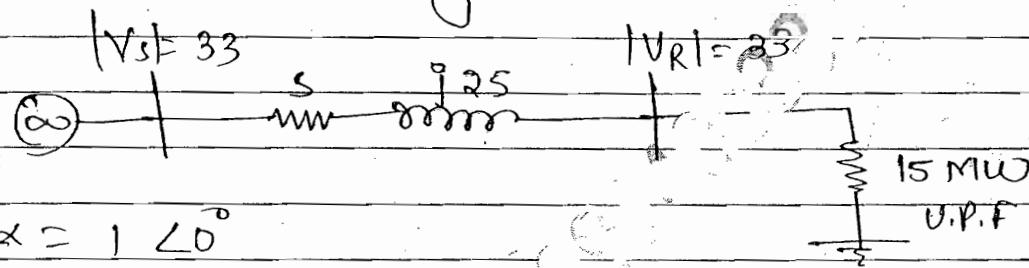
(2) 15 MW 0.8 lagging

$$\phi_{\text{line}} = 6.13^\circ$$

(3) 15 MW 0.8 leading

(4) 15 MW. 0.95 leading

Solution :



$$A \angle \alpha = 1 \angle 0^\circ$$

$$B \angle \beta = Z = 5+j25 = 25.55 \angle 78.7^\circ$$

$$P_R = \left| \frac{V_s V_R}{B} \right| \cos(\beta - \delta) = \left| \frac{A V_R^2}{B} \right| \cos(\beta - \alpha)$$

$$15 = \frac{33^2}{25.55} \cos(78.7^\circ - \delta) - \left| \frac{1 \times 33^2}{25.55} \right| \cos(78.7^\circ - 0)$$

$$8.3516$$

$$15 + 8.3516 = \frac{33^2}{25.55} \cos(78.7^\circ - \delta) \quad 1 + 8.3516 = \frac{33^2}{25.55} \cos(78.7^\circ - 0)$$

$$23.035 \times 25.55 = \cos(78.7^\circ - \delta) \quad \cos(78.7^\circ - 0)$$

$$\cos^{-1} 0.9478 = 78.7^\circ - \delta$$

$$\delta = 78.7^\circ - 56.77^\circ = 21.9^\circ$$

$$\left\{ \begin{aligned} Q_R &= \left| \frac{V_s V_R}{B} \right| \sin(\beta - \delta) = \left| \frac{V_R^2 A}{B} \right| \sin(\beta - \alpha) \\ &= - \end{aligned} \right.$$

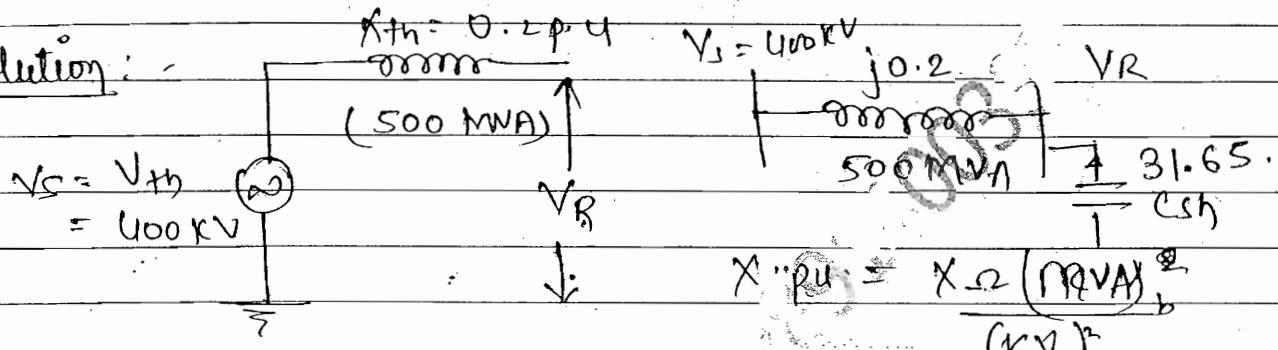
$$\left. \begin{aligned} Q_C &= - Q_R = \\ &= \phi_{\text{line}} \end{aligned} \right.$$

Date _____

(C) The Shreven's equivalent Imped. of a Bus Bar with 3-Φ 400kV sys. if 0.2 p.u as a base of 500 MVA calculate the reactive power needed.

- ① To Boost the voltage by 5kV at the Bus Bar
 - ② Reduce the voltage By 4kV at the Bus Bar
- What equipment is needed in each case.

Solution:



- ① Boost By 5kV

$$V_R = 400 + 5 = 405 \text{ kV}$$

$$X_{L2} = 64 \Omega$$

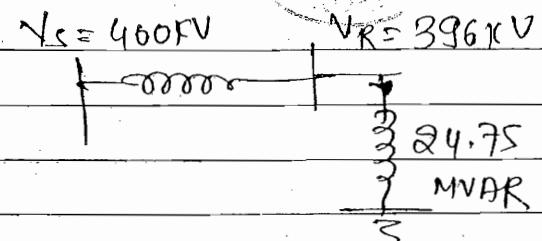
No. of parallel lines = 6.

$$Q_R = \frac{V_S V_R}{X_L} = \frac{400 \times 405}{64} = 400 \times 405 - 405^2 / 64 \\ \Rightarrow -31.65 \text{ MVAR}$$

$$Q_C = -(-31.65) = +31.65$$

- ② Reducing by 4kV

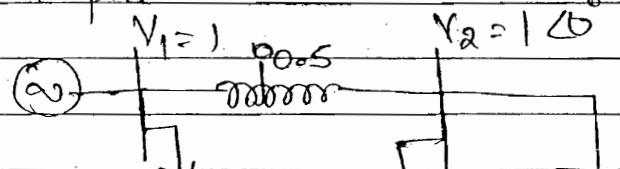
$$V_R = 400 - 4 = 396 \text{ kV}$$



$$Q_R = -400 = -400 \text{ MVAR.}$$

Q) A complex power flow can represent on the NW.
Find the compensator rating required for maintaining $V_1 = V_2 = 1$ p.u.

Solution $\gamma_s = +16^\circ$



$$S_D = 1 = P_R \\ = \frac{V_1 V_2 \sin \delta}{X_L}$$

$$I = \frac{1 X_1 \sin \delta}{0.5} \Rightarrow \sin \delta = 0.5 \quad \delta = 30^\circ$$

$$Q_R = \left| \frac{V_1 V_2 \cos \delta - V_2^2}{X_L} \right| \\ \Rightarrow \frac{1 X_1 \cos 30^\circ - 1^2}{0.5} = -0.268$$

$$Q_C = -(-0.268) = 0.268 \text{ compensate.}$$

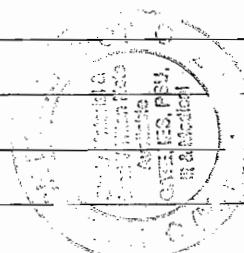
Q) Page No. \rightarrow 52 Q: 39, 40, 41, 42, 43, 44, 45, 51, 53, 54

(53) \rightarrow Correct $900 \text{ k}\Omega$ 75W .

(39) \rightarrow List I

(d) Reduce ferromagnetic effect

Pg No. \rightarrow 43 Q: 41, 42, 43



* 30P

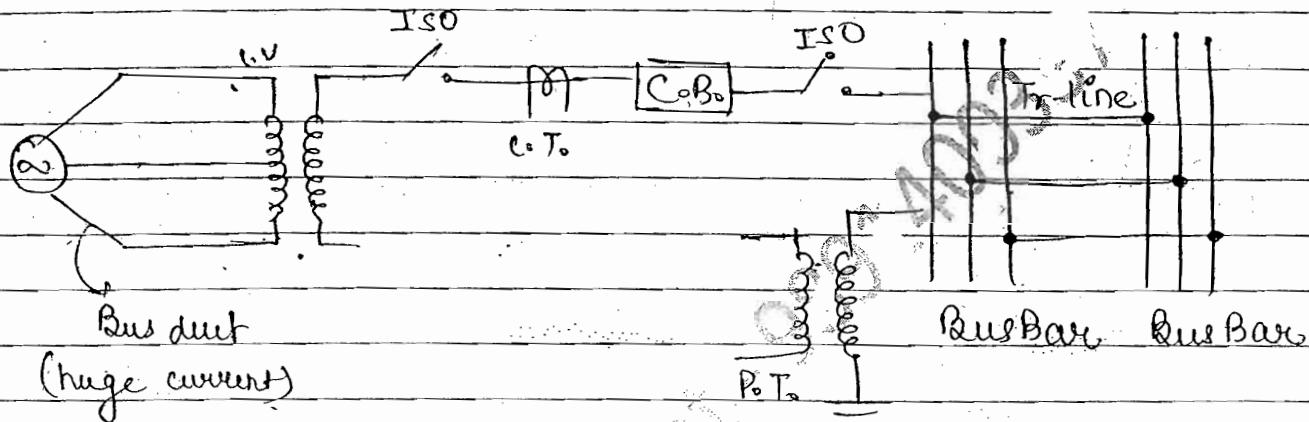
Transmission-line Parameters

Types of Conductor :-

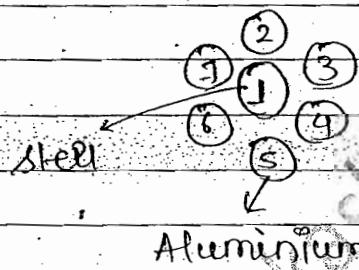
(1) SOLID → Copper → CB, CT, PT terminals

(2) HOLLOW → Copper → Isolators, Bus duct

(3) STRANDED → ACSR → Tr-line, Bus Bar.



ACSR :- Steel Coated Reinforced Aluminium



$$\text{NO. of strands} = N = (3x^2 - 3x + 1)$$

Total Diameter of conductor

$$D = (2x - 1)d$$

x = Larger Number

d = diameter of each strand

7-strand ACSR
Conductor

$2x$	N	\Rightarrow	Arrangement
1	1	d	

2 7 $3d$

$D = 3d$

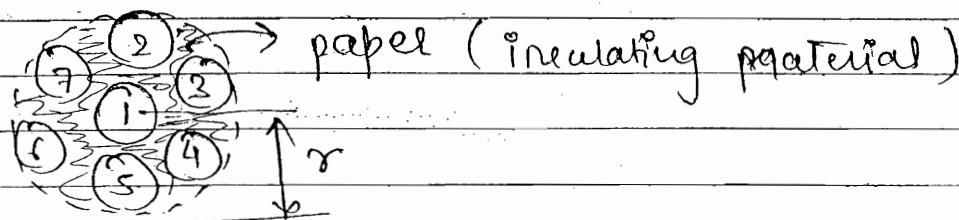
3 19 $5d$

$D = 5d$

• Tech. Name of ACSR:-

Zebra, Panther, Moore, Fox, Dog

Expanded ACSR :- In expanded ACSR, insulation material is kept b/w the strands so that effective radius will be increase and hence inductance and inductive resistance reduce, power transfer capacity ↑



8/7/2014

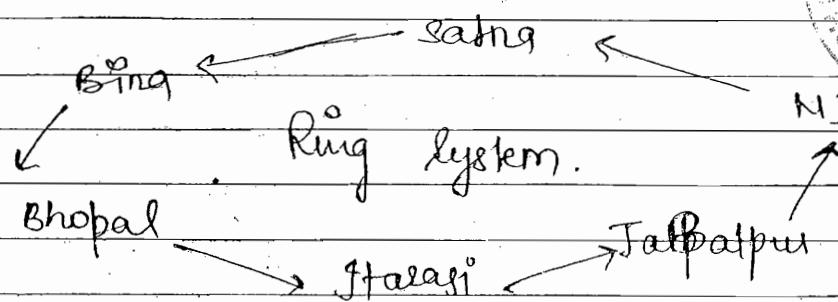
Ring System :- Ad. ① Uniform voltage maintain.

(closed loop) ② Reliable.. (Alternate supply possible)

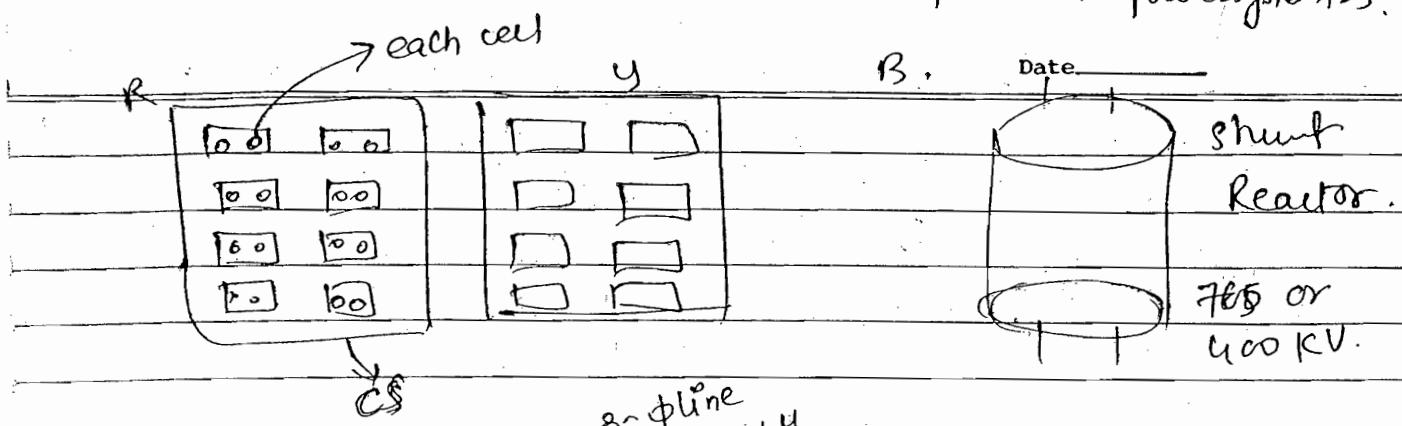
(Open loop) → Radial feeder :- Alternate supply not possible

Ad:- Gen-less, demand more, freq. will fall
then load will isolates, so open. so freq. ↑

For isolate we can call arc word



Isolates → open when maintenance required.

Morse \rightarrow 54

CSR each

 $R =$ same phase $y =$ carrying $\frac{R}{2}$ current.

g-ph line

R

Y

B

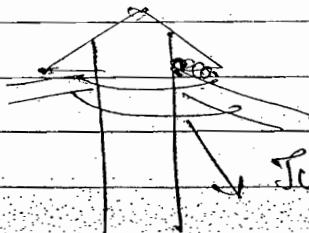
Y

B

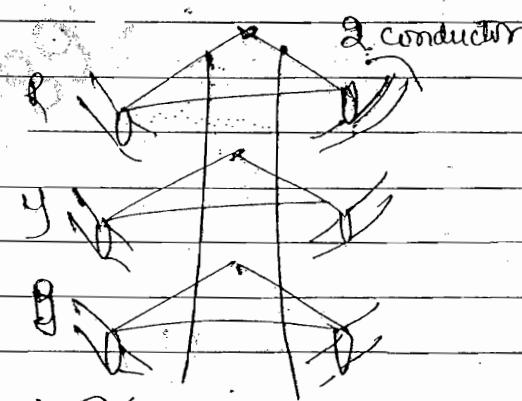
R

 Δ configurationInductance will be
minimise.∴ power ~~maximum~~ P $B =$ 2-Bundle Tr-line:

4 Bundle conductor



Jumper for power transfer



- Coloured Ball used in Tr-line which are crossing the river, when fault occurs, line will fall into river, for floating the line we use Ball, or for indicator also.

- Corona \rightarrow voltage greater than air dielectric strength

- Counter pole \rightarrow discharging the lightning.

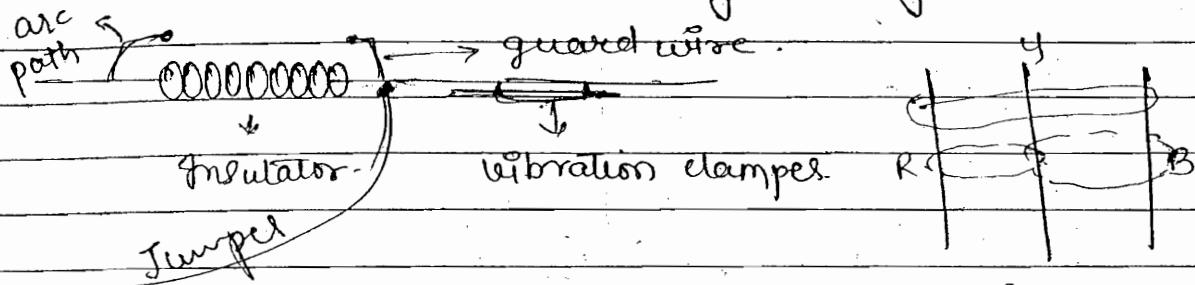
Earth electrode \rightarrow deeper length \uparrow , partly discharge

 \rightarrow arc rod.

 \rightarrow insulator

 \rightarrow Guard Ring, uniform voltage maintain

- String Insulator → used in river and road crossing reducing the sag.

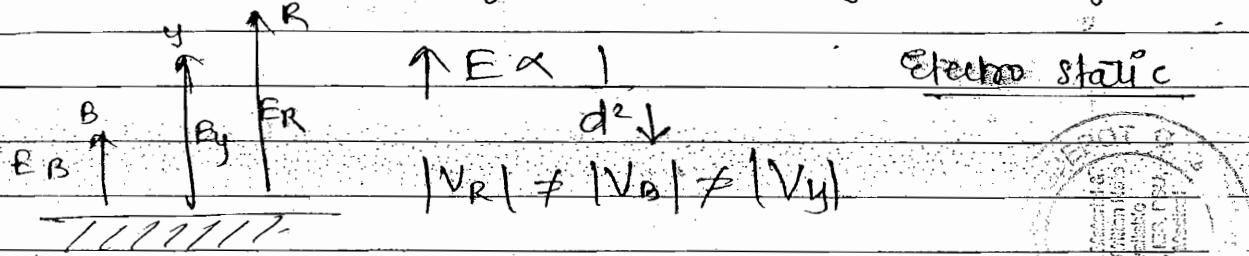


\rightarrow flux linkage
 $I_R = -I_y = -I_B$ → Electromagnetic
linkage.

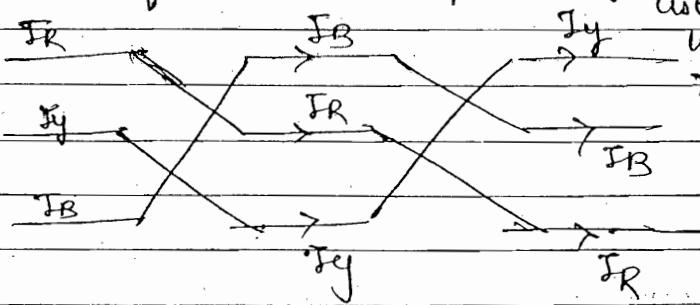
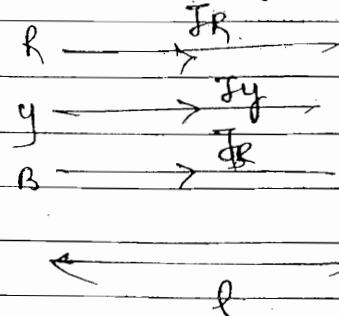
$$\uparrow V_R = \frac{d\phi}{dt} \propto I_y \uparrow \quad \nabla \times \mathbf{B} = \mu_0 \mathbf{J} \quad \nabla \times \mathbf{B} = \mu_0 (\mathbf{J}_R + \mathbf{J}_y + \mathbf{J}_B) \quad \downarrow I_y = \frac{V}{X_L}$$

$$|I_R| \neq |I_y| \neq |I_B| \rightarrow I_R + I_y + I_B \neq 0 \quad \text{unbalanced fault!}$$

Radio interference bcoz of Magnetic interference.



Negligible Radio Interference Transposition



$$V_R + V_B + V_y \neq 0$$

(Done for Balancing).

$$J_R + J_y + J_B \neq 0$$

Earth

Parameters of Tr-line :-

(1) Inductance (L)

(2) Capacitance (C)

(3) Resistance (R)

(4) Conductance (G)

(1) Inductance (L) :-

$$P_R \propto I$$

$$\propto L$$

Steps:-

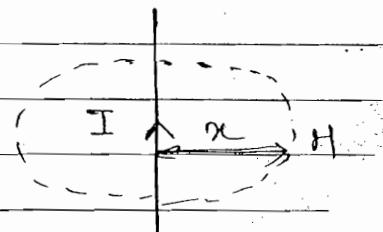
$$\textcircled{1} \quad \oint H \cdot d\ell = I$$

$$\textcircled{2} \quad B = \mu_0 \mu_r H$$

$$\textcircled{3} \quad \Phi = B \cdot A$$

$$\textcircled{4} \quad \lambda = n\Phi$$

$$\textcircled{5} \quad L = \frac{\lambda}{I}$$



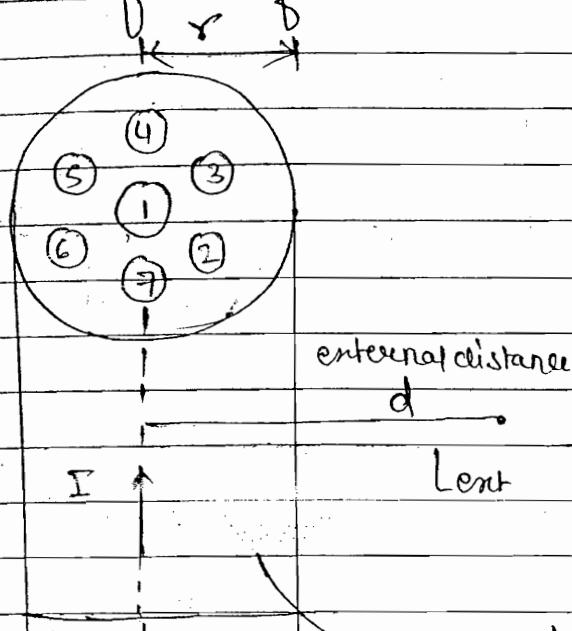
• Inductance of Single Conductor :-

- Assumption :- (1) ACSR are solid conductor is considered.
- (2) Skin and Proximity effect are neglected
- (3) ACSR are solid conductor consisting of
 - (a) Internal inductance
 - (b) External inductance

INTERNAL INDUCTANCE - Internal inductance is due to flux linkage occurs within the conductor areas due to the current flowing in the strands of the conductor.

- This internal inductance proportional to the relative permeability of the conductor material and it is independent of radius or size of conductor i.e. It is mainly because flux linkage or the flux density increases linearly is proportional

to the current from the center of conductor to the surface of conductor.



- Internal Inductance : (L_{int})

$$L_{int} = \frac{\mu_r}{2} \times 10^{-7} \text{ H/m}$$

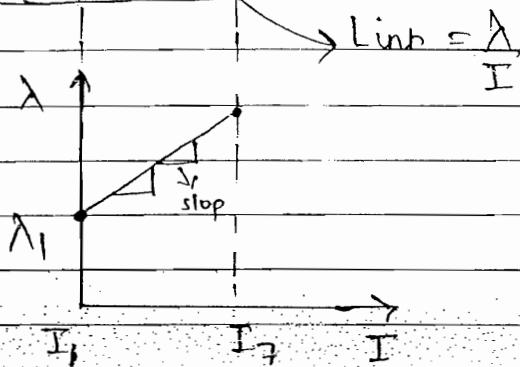
$$L_{int} \propto \mu_r$$

$$\text{If } \mu_r = 1$$

$$L_{int} = \frac{1}{2} \times 10^{-7} \text{ H/m}$$

$$= 0.05 \text{ mH/km}$$

- Independent of value of radius.



- External Inductance : (L_{ext})

$$L_{ext} = \frac{\mu_0}{2\pi} \ln\left(\frac{d}{r}\right) \text{ H/m}$$

$$\mu_0 = 4\pi \times 10^{-7}$$

- Total Inductance (L) :-

$$L = L_{int} + L_{ext}$$

$$L = 0.05 + 0.2 \ln \frac{d}{r} \text{ mH/km}$$

$$L_{ext} = \frac{2}{2} \times 10^{-7} \ln\left(\frac{d}{r}\right) \text{ H/m}$$

$$= 0.2 \ln\left(\frac{d}{r}\right) \text{ mH/km}$$

(OR)

$$L = \frac{1}{2} \times 10^{-7} + 2 \times 10^{-7} \ln\left(\frac{d}{r}\right)$$

$$= 2 \times 10^{-7} \left[\frac{1}{4} + \ln\left(\frac{d}{r}\right) \right]$$

$$= 2 \times 10^{-7} \left[\ln e^{\frac{1}{4}} + \ln\left(\frac{d}{r}\right) \right]$$

for hollow conductor

$$L = 2 \times 10^{-7} \ln \frac{d}{r} \text{ H/m.}$$

Date _____

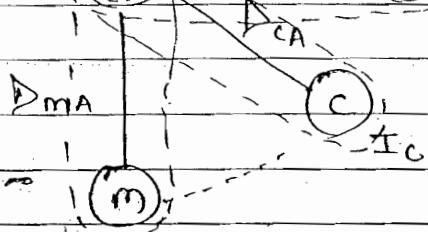
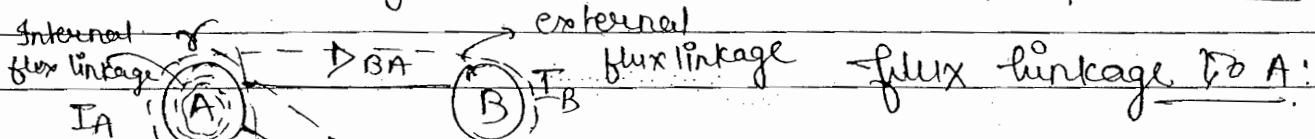
$$L = 2 \pi 10^{-7} \ln \left[\frac{de^{1/4}}{r} \right] = 2 \pi 10^{-7} \ln \left(\frac{d}{re^{1/4}} \right)$$

$$L = 2 \times 10^{-7} \ln \left(\frac{d}{0.7788r} \right) \text{ H/m.} \quad e^{1/4} = 0.7788.$$

$$r' = 0.7788r$$

$$L = 2 \times 10^{-7} \ln \frac{d}{r'} \text{ H/m.}$$

• Flux linkage to a Conductor in a Group of Conductor:



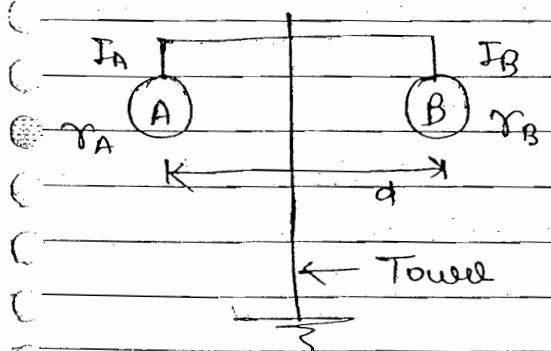
$$\Delta_A = \frac{\mu_0}{2\pi} \left[I_A \ln \frac{1}{r_A} + I_B \ln \frac{1}{r_B} + I_m \ln \frac{1}{r_m} \right]$$

At Balance:

$$I_A + I_B + \dots + I_m = 0$$

CASE I:- Inductance of a Single φ or 2 wire line

Inductance of A [L_A]:-

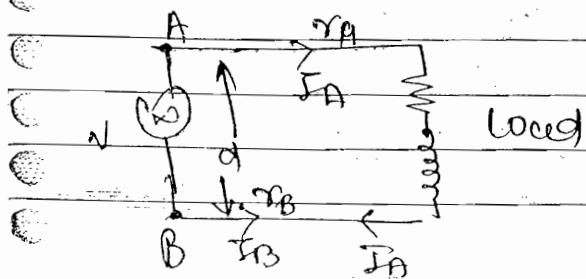


Flux linkage to A:-

$$\Delta_A = \frac{\mu_0}{2\pi} \left[I_A \ln \frac{1}{r_A} + I_B \ln \frac{1}{r_B} \right]$$

At Balance:-

$$I_A + I_B = 0 \Rightarrow I_A = -I_B$$



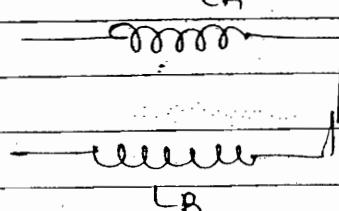
$$\Delta_A = \frac{\mu_0 I_A}{2\pi} \ln \left(\frac{d}{r'_A} \right)$$

$$L_A = \frac{\lambda_A}{I_A} = \frac{\mu_0}{2\pi} \ln \left(\frac{d}{r'_A} \right) \text{ H/m.}$$

• Inductance of B (L_B): -

$$L_B = \frac{\lambda_B}{I_B} = \frac{\mu_0}{2\pi} \ln \left(\frac{d}{r'_B} \right) \text{ H/m.}$$

• Total / loop / Circuit Inductance:-

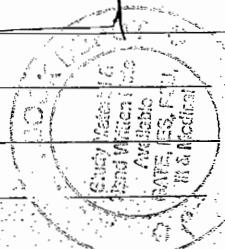
$$L = L_A + L_B = \frac{\mu_0}{\pi} \ln \left(\frac{d}{\sqrt{r'_A r'_B}} \right) \text{ H/m.}$$


$$\text{If } r'_A = r'_B = r \quad L = \frac{\mu_0}{\pi} \ln \left(\frac{d}{r} \right) \text{ H/m}$$

d = length of line . . . (metres)

$$L = L \cdot l \text{ . . . (Henry)}$$

$$X_L = \omega f L \quad \Omega$$



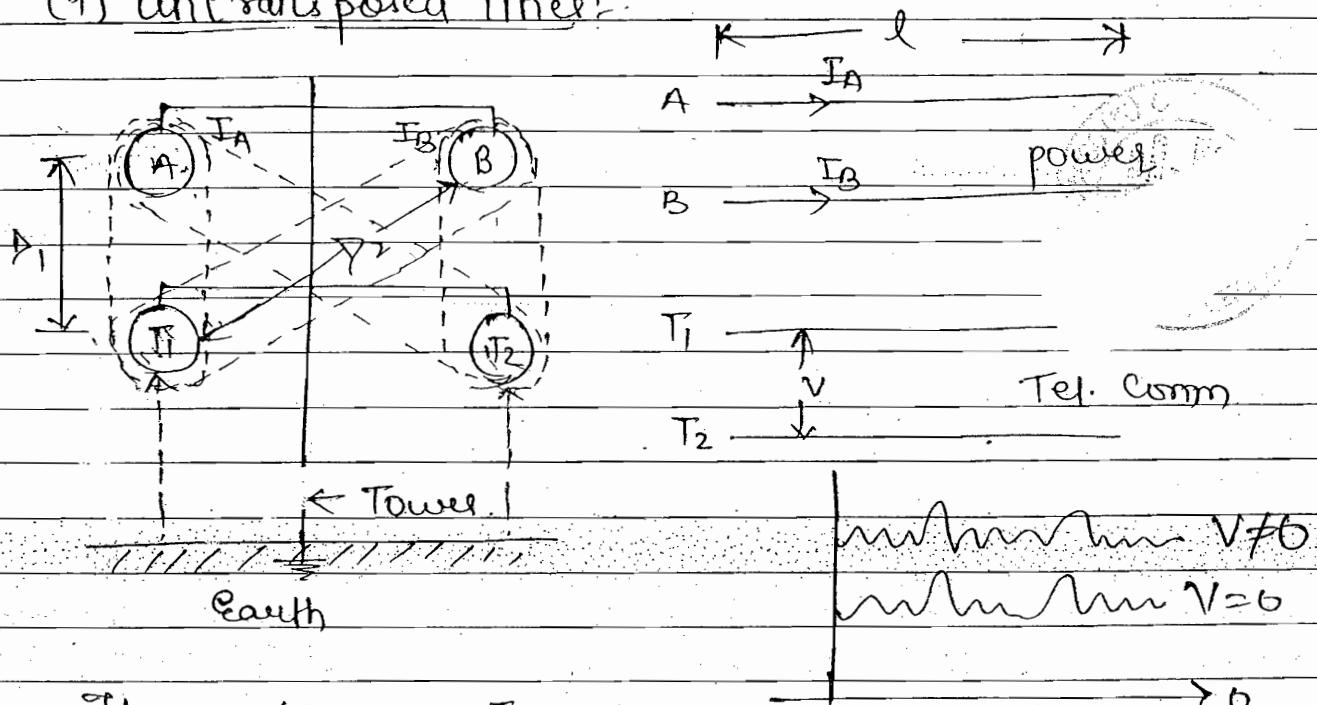
CASE II:- Radio Interference in telecommunication line due to power line

- If the power and telecommunication line are running close to each other. The current flowing in the power line reduces the magnetic flux linkage with the communication line. This will produce an emf in the communication line conductors. Similarly due to earth charges produce electric field on the communication line conductor which will induces emf between the communication line conductor which is called electro static induction.

Both this electro static and electro magnetic produce interference for the communication signals passing through the communication line. This is called RADIO INTERFERENCE in the communication line.

- (1) either power and both, power and communication line are transposed at regular intervals of length of the Tr. line.

(9) Untransposed Lines:



Flux linkage to T_1 and T_2

$$\lambda \times T_1 = \frac{\mu_0}{2\pi} \left[I_A \ln \frac{1}{D_1} + I_B \ln \frac{1}{D_2} \right]$$

$$\lambda T_2 = \frac{\mu_0}{2\pi} \left[I_A \ln \frac{1}{D_2} + I_B \ln \frac{1}{D_1} \right]$$

$$\text{Net } \lambda_T = \lambda_{T_1} - \lambda_{T_2}$$

$$= \frac{\mu_0}{2\pi} \left[I_A \ln \frac{D_2}{D_1} + I_B \ln \frac{D_1}{D_2} \right]$$

At Balance $I_A + I_B = 0$, $I_B = -I_A$

$$\lambda_T = \frac{\mu_0 I_A}{2\pi} \ln \left(\frac{D_2}{D_1} \right)^2$$

$$= \frac{\mu_0 I_A}{\pi} \ln \left(\frac{D_2}{D_1} \right)$$

$$L = \lambda_A = \frac{\mu_0}{\pi} \ln \left(\frac{D_2}{D_1} \right)$$

Voltage induced b/w communication line due to I_A is

$$V = (2\pi f L) I_A$$

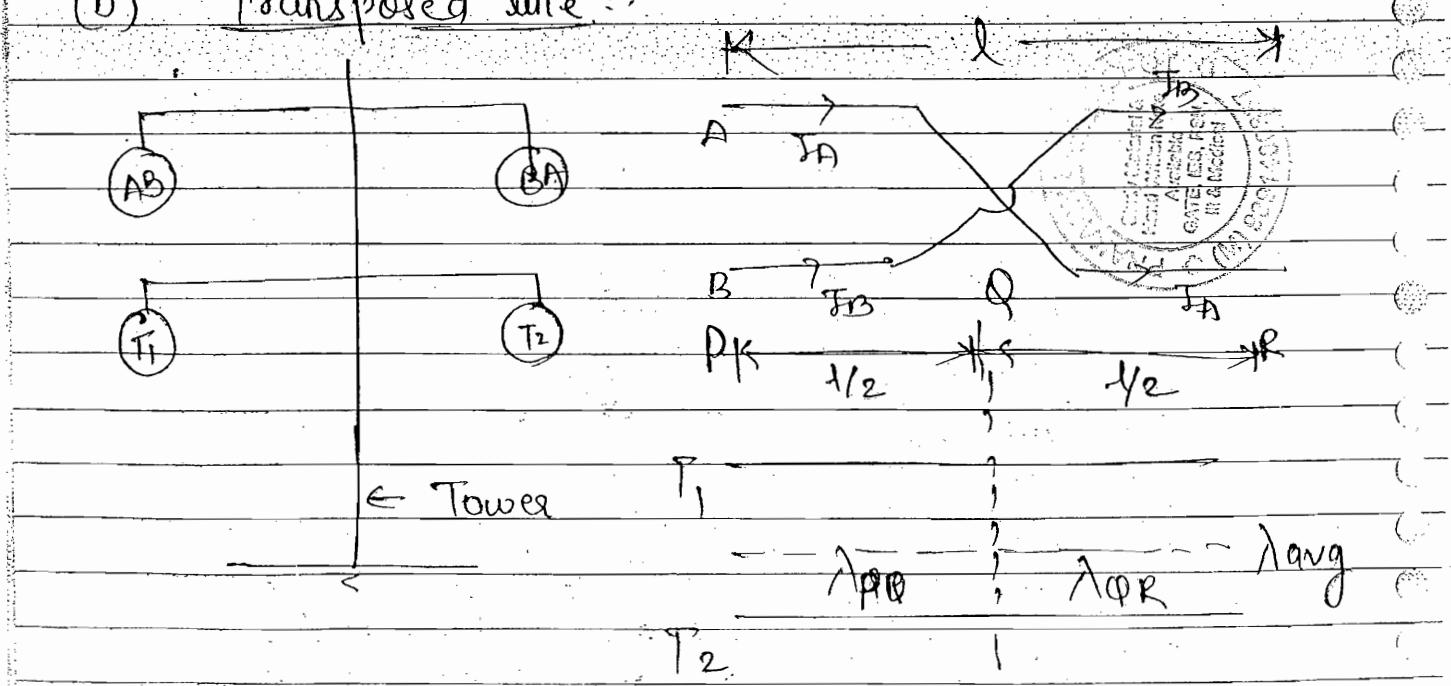
$$= 2\pi f I_A \cdot \frac{\mu_0}{\pi} \ln \left(\frac{D_2}{D_1} \right)$$

$$V = 2\mu_0 f I_A \ln \left(\frac{D_2}{D_1} \right) \text{ V/m.}$$

D_1 = shortest distance

D_2 = longest distance

(b) Transposed line:



Flux linkage b/w PQ and QR.

$$\lambda_{PQ} = \frac{\mu_0}{2\pi} \left[I_A \ln \left(\frac{D_2}{D_1} \right) + I_B \ln \left(\frac{D_1}{D_2} \right) \right]$$

$$\lambda_{QR} = \frac{\mu_0}{2\pi} \left[I_B \ln \left(\frac{D_2}{D_1} \right) + I_A \ln \left(\frac{D_1}{D_2} \right) \right]$$

$$\lambda_{avg} = \frac{\lambda_{PQ} * l/2 + \lambda_{QR} * l/2}{l} = \frac{1}{2} [\lambda_{PQ} + \lambda_{QR}]$$

$$\lambda_{avg} = \frac{1}{2} \cdot \frac{\mu_0}{2\pi} \left[(I_A + I_B) \ln \frac{D_2}{D_1} + (I_A + I_B) \ln \frac{D_1}{D_2} \right]$$

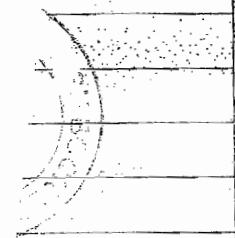
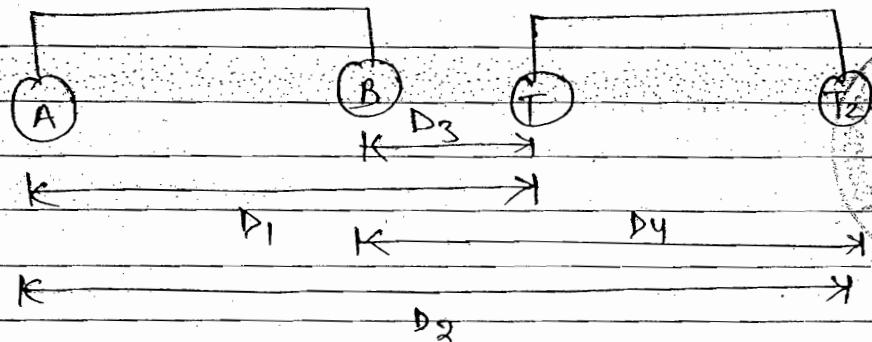
At Balance $(I_A + I_B) = 0$

$$\bullet \lambda_{avg} = 0$$

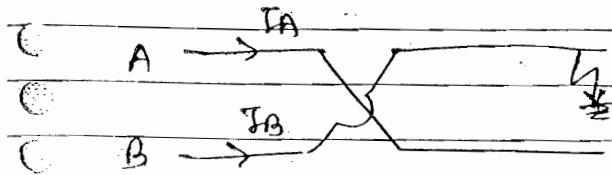
$$\bullet \frac{l}{I_A} = \lambda_{avg} = 0$$

$$\bullet V = 2\pi f L \cdot I_A = 0$$

practical case:



• Through distance we can't make $\lambda_{avg} = 0$. In this case $(I_A + I_B)$ help in making $\lambda_{avg} = 0$



$$LG, LL, LLG \quad (I_A + I_B) \neq 0$$

$$\therefore V \neq 0$$

for making voltage $= 0$

Telecommunication line

AC

at regular interval

are also transpose, so that V can be reduce.

case III:- Radio Interference in 3 ϕ power Tr-line

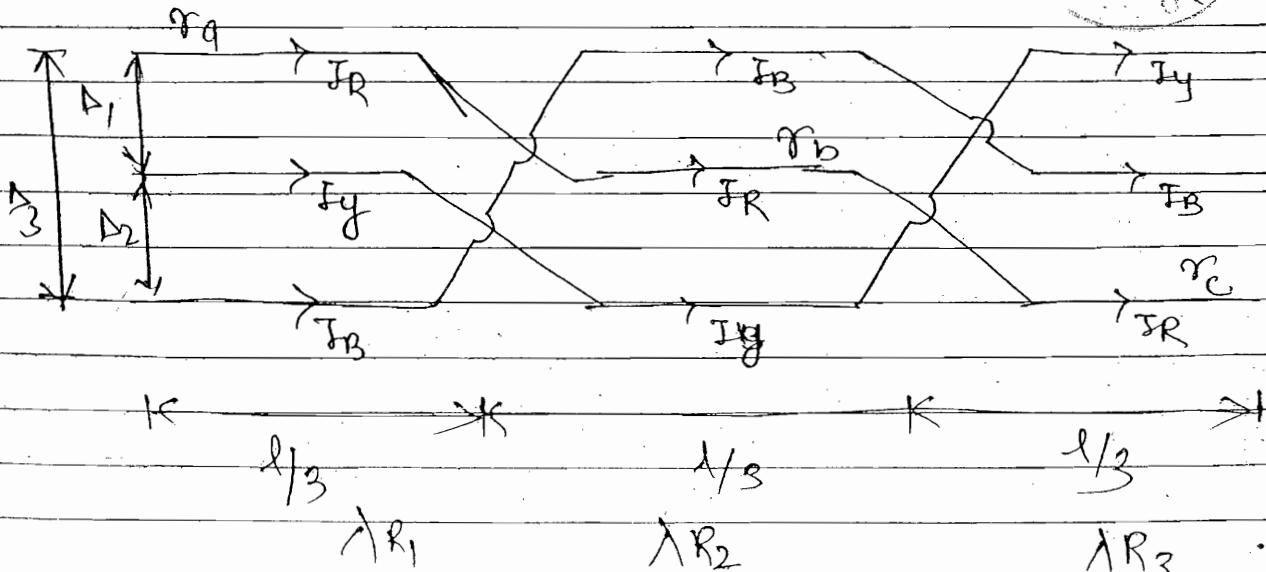
In case of 3- ϕ Tr-line due to electro-magnetic induction the middle conductor experiences maximum flux linkage so that $X_L f L$ increase so that current reduce. This will produce unbalance in the system currents that is $I_R + I_Y + I_B \neq 0$ occurs.

- The bottom most conductor which is nearer to the earth experience maximum electric field stress compare to the other conductors causing unbalance in the voltage i.e. $V_R + V_Y + V_B \neq 0$ occurs. This is called electrostatic induction

Both electro static and electromagnetic produces unbalance in $\delta \phi$ which is called radio interference in the 3 ϕ line.

- To reduce this effect and maintain balanced in voltages and currents Tr-line is transpose at regular intervals of length of the line

- Consider transposed line for unbalance it is mentioned.



Flux linkage to R-phase:-

$$\lambda_{R_1} = \frac{\mu_0}{2\pi} \left[I_R \ln \frac{1}{r_a'} + I_y \ln \frac{1}{D_1} + I_B \ln \frac{1}{D_3} \right]$$

$$\lambda_{R_2} = \frac{\mu_0}{2\pi} \left[I_R \ln \frac{1}{r_b'} + I_y \ln \frac{1}{D_2} + I_B \ln \frac{1}{D_1} \right]$$

$$\lambda_{R_3} = \frac{\mu_0}{2\pi} \left[I_R \ln \frac{1}{r_c'} + I_y \ln \frac{1}{D_3} + I_B \ln \frac{1}{D_2} \right]$$

$$\lambda_{avg} = \frac{\lambda_{R_1} + \lambda_{R_2} + \lambda_{R_3}}{3}$$

$$\lambda_{avg} = \frac{1}{3} \frac{\mu_0}{2\pi} \left[I_R \ln \frac{1}{r_a' r_b' r_c'} + (I_y + I_B) \ln \frac{1}{D_1 D_2 D_3} \right]$$

$$\text{At Balance } I_y + I_B = -I_R$$

$$\lambda_{avg} = \frac{\mu_0}{2\pi} I_R \ln \left(\frac{D_1 D_2 D_3}{r_a' r_b' r_c'} \right)^{1/3}$$

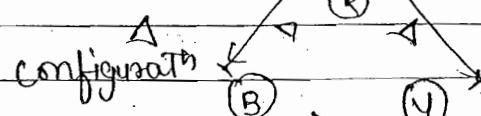
$$L_R = l_{ph} = \frac{\lambda_{avg}}{I_R} = \frac{\mu_0}{2\pi} \ln \left(\frac{D_1 D_2 D_3}{r_a' r_b' r_c'} \right)^{1/3}$$

H/m/phase.

$$(1) \quad \text{If } r_a' = r_b' = r_c' = r'$$

$$l_{ph} = \frac{\mu_0}{2\pi} \frac{\ln (D_1 D_2 D_3)^{1/3}}{r'} \quad \text{H/m/phase}$$

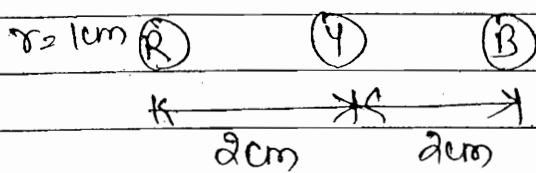
$$(2) \quad \text{If } D_1 = D_2 = D_3 = D$$



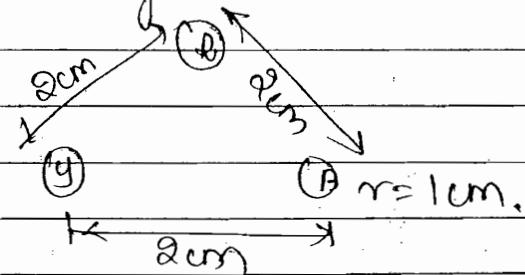
$$l_{ph} = \frac{\mu_0}{2\pi} \ln \left(\frac{D}{r'} \right) \quad \text{H/m/phase}$$

Q Find the inductance / phase for the following configuration.

(1) Horizontal



(2) Triangular



Solution

$$L_{ph} = \frac{4\pi \times 10^{-7}}{2\pi} \ln \left(\frac{2 \times 2 \times 2}{0.7788 \times 1 \times 10^{-2}} \right)$$

$$= 1.15 \times 10^{-6} \text{ H/m}$$

$$= 1.15 \text{ mH/cm}$$

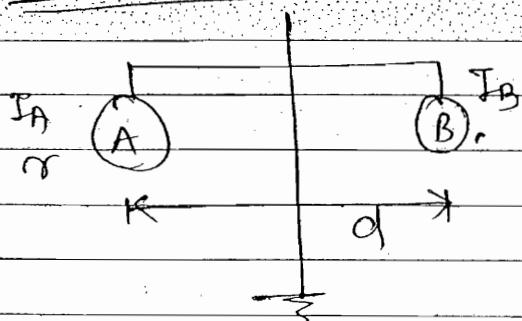
$$L_{ph} = \frac{4\pi \times 10^{-7}}{2\pi} \ln \left(\frac{2}{0.7788 \times 10^{-2}} \right)$$

$$= 1.10 \text{ mH/cm}$$

$$\boxed{L_A < L_H}$$

$$\boxed{P_A > P_H}$$

Case IV for Bundle Conductor:-



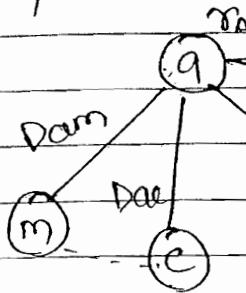
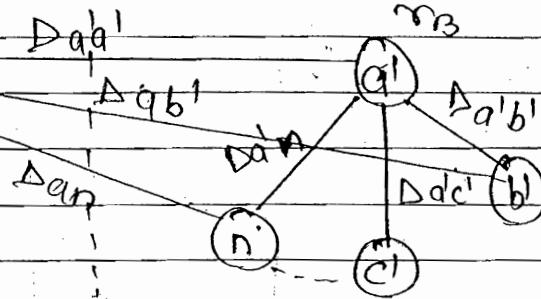
$$L_A = L_B = 2 \times 10^{-7} \ln \frac{d}{r}$$

$$L_A = L_B = 2 \times 10^{-7} \ln \frac{D_m}{D_s}$$

$D_m = \text{Mutual geometric Mean Distance (GMD)}$

$D_s = \text{Self GMD (or)}$

$= \text{GMR} [\text{Geometric Mean Radius}]$

Phase A (I_A)Phase B (I_B) $m = \text{No. of Conductor Bundle of phase A}$ $n = \text{No. of Conductor Bundle of phase B}.$

$$L_A = 2 \times 10^{-7} \ln \left(\frac{D_{mAB}}{D_{sa}} \right)$$

$$L_B = 2 \times 10^{-7} \ln \left(\frac{D_{mnB}}{D_{sb}} \right)$$

$$D_{mAB} = D_{mnB} = \left[(D_{aa'} D_{ab'} \dots D_{an}) (D_{ba'} D_{bb'} \dots D_{bn}) \dots (D_{ma'} D_{mb'} \dots D_{mn}) \right]^{\frac{1}{m+n}}$$

$$D_{sa} = \left[(D_{aa} D_{ab} \dots D_{am}) (D_{ba} D_{bb} \dots D_{bm}) \dots (D_{ma} D_{mb} \dots D_{mm}) \right]^{\frac{1}{m^2}}$$

$$\text{where } D_{aa} = D_{bb} = \dots = D_{mm} = \gamma'_A = 0.7788 \gamma_n$$

$$D_{sb} = \left[(D_{ba'} D_{ab'} \dots D_{b'n}) (D_{bb'} D_{bb'} \dots D_{bn}) \dots (D_{na'} D_{nb'} \dots D_{nn}) \right]^{\frac{1}{n^2}}$$

$$\text{where } D_{ba'} = D_{bb'} = \dots = D_{nn} = \gamma'_B = 0.7788 \gamma_n$$

- Q Find the self GMB for the following conductor configu^u
① Bundle of 2 :-

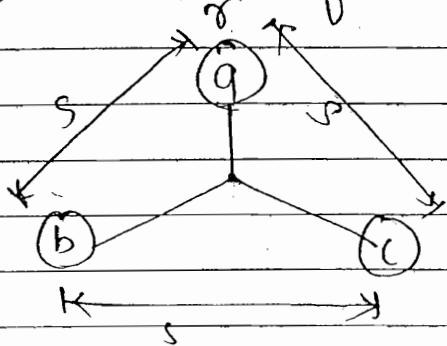
γ (a) - S (b)

$$\Delta_s = \left[(\Delta_{aa} \Delta_{ab}) (\Delta_{bb} \Delta_{ba}) \right]^{1/2 \times 2}$$

$$= [(r' \cdot s) (r' \cdot s)]^{1/4}$$

$$\Delta_s = (r' \cdot s)^{1/2}$$

(2) Bundle of Conductor 3.

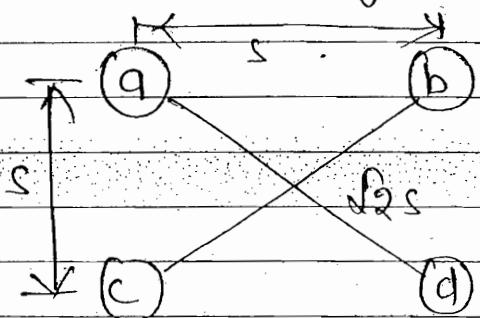


$$\Delta_s = \left[(\Delta_{aa} \Delta_{ab} \Delta_{ac}) (\Delta_{bb} \Delta_{ba} \Delta_{bc}) (\Delta_{cc} \Delta_{ca} \Delta_{cb}) \right]^{1/3 \times 3}$$

$$= [(r' \cdot s \cdot s) (s \cdot s \cdot r') (s \cdot r' \cdot s)]^{1/9}$$

$$= [r' s^2]^{1/3}$$

(3) Bundle of conductor 4.



$$\Delta_s = \left[(\Delta_{aa} \Delta_{ad} \Delta_{ab} \Delta_{ac}) (\Delta_{bb} \Delta_{ba} \Delta_{bc} \Delta_{bd}) (\Delta_{cc} \Delta_{ca} \Delta_{cb} \Delta_{cd}) (\Delta_{dd} \Delta_{dc} \Delta_{da} \Delta_{db}) \right]^{1/4 \times 2}$$

$$= (\sqrt{2} r' \cdot s^3)^{1/4}$$

$$= 1.09 (r' \cdot s^3)^{1/4}$$

Chap:- 1 \rightarrow 1012.

Ques: Comparison of Bundle or Without Bundle | 7/2014.

Q) for the following configuration calculate inductance per phase

(1) without Bundle conductor.

$$L_A = L_B = 2 \times 10^{-7} \ln \left(\frac{d}{r} \right)$$

$$= 2 \times 10^{-7} \ln \frac{2}{0.7788 \times 10^{-2}}$$

$$= 1.109 \text{ mH/km}$$

(2) with Bundle Conductor:-

$$L_A = L_B = 2 \times 10^{-7} \ln D_m$$

$$D_s = (D_{aa'} D_{ab} D_{ba} D_{bb'})^{1/4}$$

$$= \sqrt{(0.7788 \times 1 \times 10^{-2})^2 \times (0.25)^4}$$

$$= 0.044 \text{ m}$$

$$D_m = (D_{aa'} D_{ab} D_{ba} D_{bb'})^{1/4}$$

$$= [2 \times 2.25 \times 1.75 \times 2]^{1/4}$$

$$= 1.99 \approx 2 \text{ m}$$

$$L_A = L_B = 2 \times 10^{-7} \ln \left(\frac{2}{0.044} \right) = 0.768 \text{ mH/km}$$

• with Bundle conductor power - X-feer is more.

Q) To get $L_A = 0.768 \text{ mH/km}$ without Bundle how much r required?

$$L_A = 0.768 \times 10^6 \text{ H/m}$$

$$L_A = 2 \times 10^{-7} \ln \frac{2}{0.7788 \times 9}$$

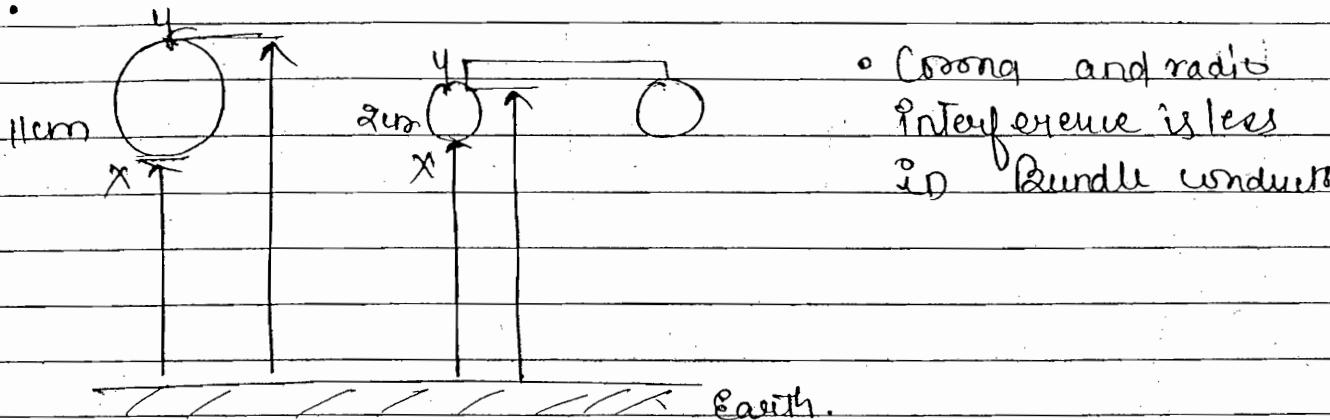
$$\Rightarrow A = \pi r^2 = \pi \times 0.7788^2 \times 9^2$$

$$\approx 100 \text{ cm}^2$$

$$r = 5.6 \text{ cm.}$$

Bundle: $\sigma = 1 \text{ cm} \rightarrow 2\pi\sigma^2 = 2\pi \times 1^2 = 6.28 \text{ cm}^2$

- More area will required without bundle, cost will ↑.



- Corona and radio interference is less in bundle conductor

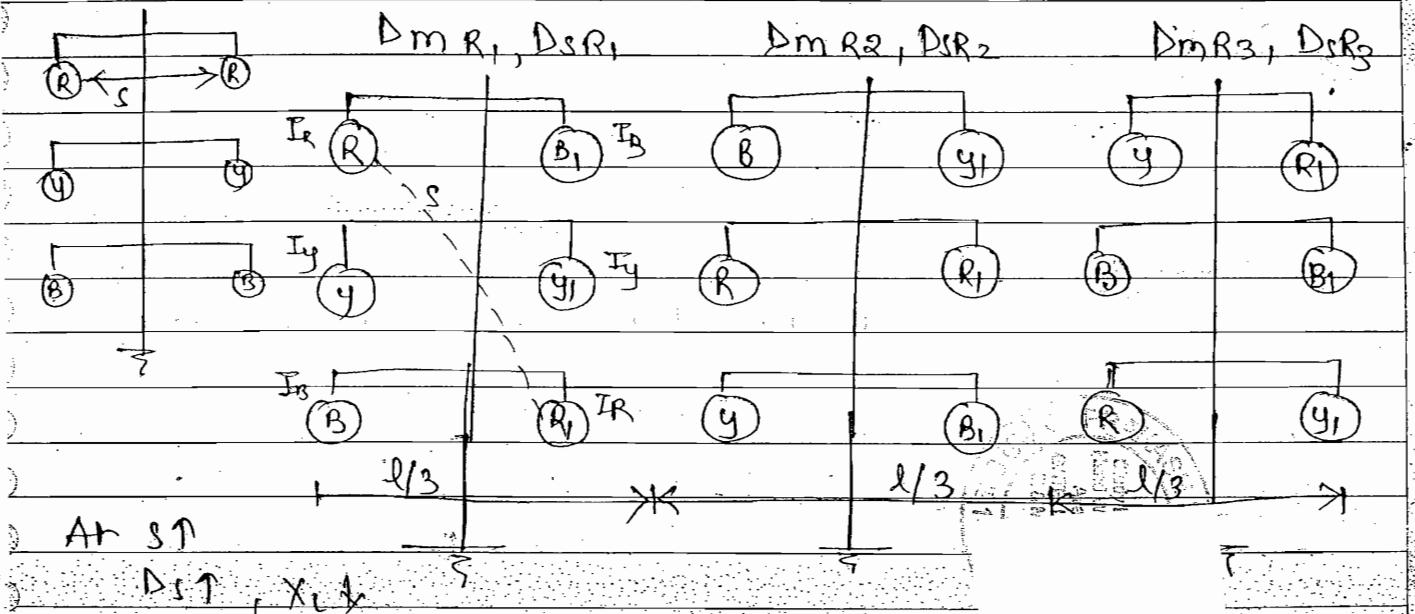
- Advantages of Bundle conductor:-

- (1) Effective Radius of conductor D_e will increase.
- (2) Inductance and inductive reactance are reduced.
- (3) Power transferred capability is increased.
- (4) Volume of the conductor is reduce, so that no. of towers will minimize.
- (5) Electrical field stress on the conductor are minimised.
- (6) Surge impedance is reduce.
- (7) Surge impedance loading is increased.
- (8) Corona power loss is reduce.
- (9) Interference bw adjacent line is minimized.

Because of above advantage Bundle conductors are practically used for power transfer of higher rating in 220 KV and above voltage levels.

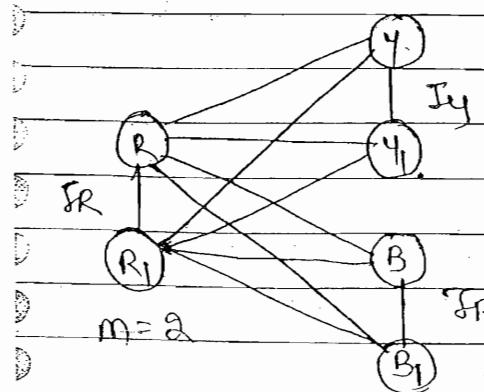
case 5 Double Circuit line :- In case of two conductor bundle $D_s = (\pi' s)^{1/2}$ That is $D_s \propto s^{1/2}$ by $\uparrow s$, $\Delta s \uparrow$ so that ℓ and X_L are reduced. Power transferred is \uparrow . This principle is used in case of double circuit line.

- It consisting of two circuit each has R,Y,B. phases kept one one side of tower.



$$L_B = l_{ph} = 2 \times 10^{-7} \ln \left(\frac{DmR_1, DmR_2, DmR_3}{D_sR_1, D_sR_2, D_sR_3} \right)^{1/3} \text{ H/m/phase}$$

Calculation of DmR



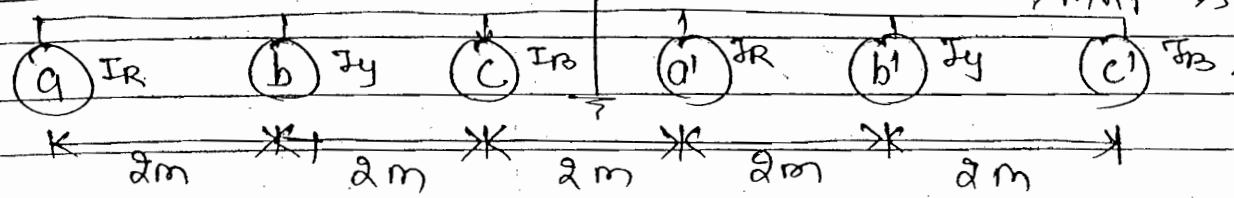
$$DmR_1 = \left[(D_{RY} D_{RY}, D_{RB} D_{RB}) (D_{R1Y} D_{R1Y}, D_{R1B} D_{R1B}) \right]^{1/2} \times Y$$

Similarly calculate DmR_2, DmR_3
Calculation of DsR

$$DsR_1 = \left[D_{RR}, D_{RR}, D_{R1R} D_{R1R} \right]^{1/2}$$

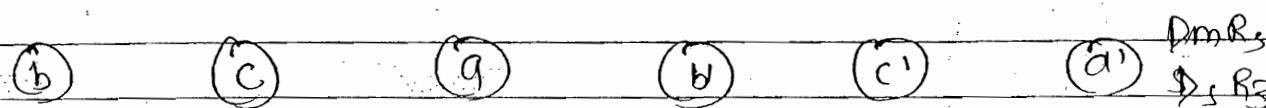
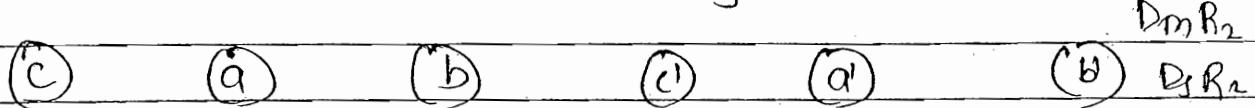
Similarly calculate DsR_2, DsR_3

Conventional L :- Conductor radius = 12 mm.



Assumption → Transposition

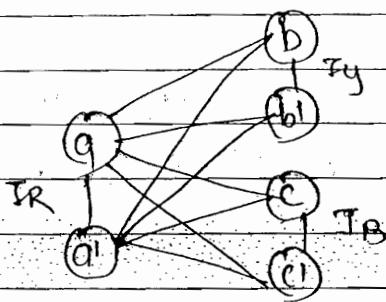
$$aa' \rightarrow I_R \quad bb' \rightarrow I_Y \quad cc' \rightarrow I_B$$



Calculate the ΔmR .

$$\Delta mR_1 = \left[D_{ab} D_{a'b'} D_{ac} D_{a'c'} \right] \left[D_{ab} D_{a'b'} \right]^{1/2} x 4$$

$$= [2 \times 8 \times 4 \times 10 \times 4 \times 2 \times 2 \times 4]^{1/2}$$



$$\Delta mR_2 = \left[2 \times 8 \times 2 \times 4 \times 4 \times 2 \times 8 \times 2 \right]^{1/8} = 3.36 \text{ m}$$

$$\Delta mR_3 = \left[4 \times 2 \times 2 \times 4 \times 10 \times 4 \times 6 \times 2 \right]^{1/8} = 3.77 \text{ m}$$

$$\Delta sR_1 = (D_{aa} D_{aa'} D_{a'a} D_{a'a'})^{1/2}$$

$$= [(0.7788 \times 12 \times 10^{-3})^2 \times 6^2]^{1/4} = 0.236$$

$$= \Delta sR_2 = \Delta sR_3$$

$$L_B = l_{ph} = 2 \times 10^{-7} \ln \left[\frac{\Delta mR_1 \Delta mR_2 \Delta mR_3}{\Delta sR_1 \Delta sR_2 \Delta sR_3} \right]^{1/3}$$

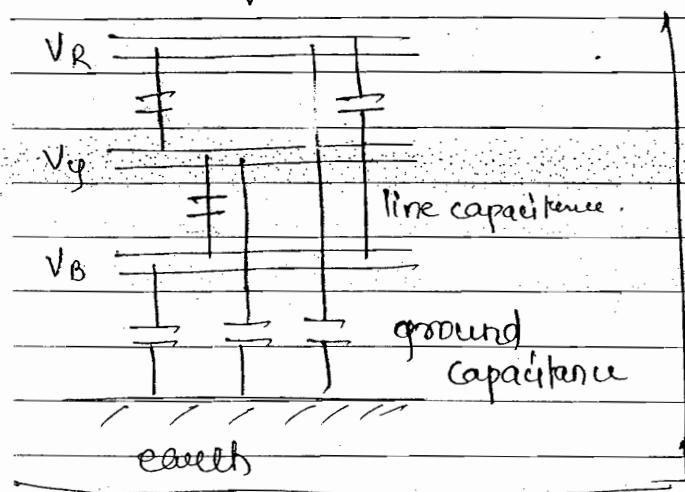
$$= 2 \times 10^{-9} \ln \left[\frac{3.97 \times 3.36 \times 3.97}{(0.236)^3} \right]^{1/3}$$

$$= 0.546 \text{ mH/km/phase}$$

CAPACITANCE:

In case of NO-load or light load condition of a Tr-line charging current flows through the line due to capacitance exist b/w the conductors and conductors to the ground.

Due to capacitance effect under no load $V_R > V_s$ (Ferranti effect occurs) for compensating this Ferranti effect shunt reactor capacitor has to be used for designing proper value of shunt reactor line capacitance has to be calculated According to the configuration of the Tr-line



Columb's law

$$F = \frac{Q_1 Q_2}{4\pi G \epsilon_0 d^2}$$

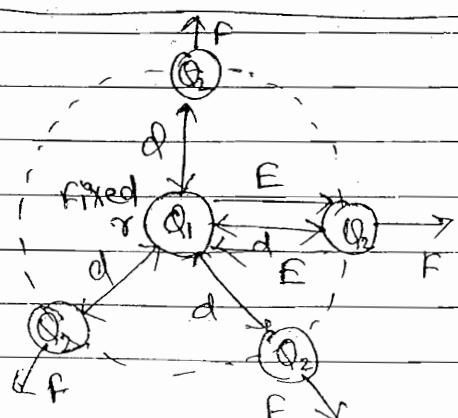
$$E = \frac{F}{Q_2} = \frac{Q_1}{4\pi G \epsilon_0 d^2}$$

Voltage $\Rightarrow QV$ - work done = force \times distance
charge charge

$$= \frac{F}{Q} \cdot dx$$

$$dV = - E \cdot dx$$

bcz E is working in opp. direct



$$V = - \int_d^{\infty} E \cdot d\sigma$$

$$C = \frac{Q}{V}$$

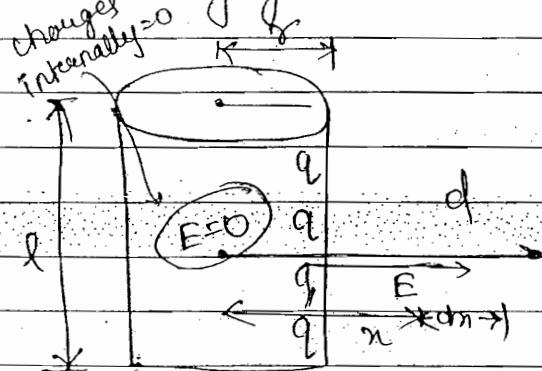
where σ = smaller distance

d = longer distance, it may be ∞ .

- Capacitance due to Single Conductor

Assumption: (1) Tr-line is of ACSR conductor having line charge configuration.

(2) Charge is accumulating on the surface of the conductor bcoz the conductivity is higher so that the electrical field at the center of the conductor is negligible. \therefore charge is neglected at the center.



$$\sigma = \frac{q}{a}$$

$$J = \sigma \cdot E$$

$$E = \frac{J}{\sigma} = \frac{J}{\infty} = 0$$

$E = 0$ inside so charges are at surface, E is not axially, it is radially.

q = line charge C/m .

$$E = \frac{q}{2\pi G_0 \epsilon_0 r^2}$$

$$V = - \int_d^{\infty} E \cdot dr$$

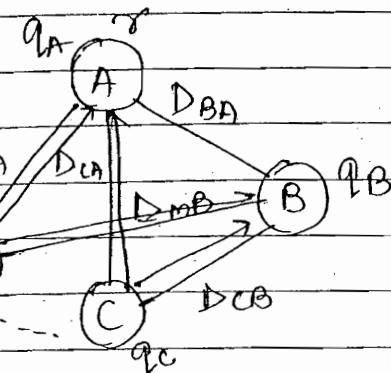
$$= - \int_d^{\infty} \frac{q}{2\pi G_0 \epsilon_0 r^2} dr$$

$$V = \frac{q}{2\pi G_0 \epsilon_0 r} \ln \left(\frac{d}{r} \right)$$

$$C = \frac{q}{V} = \frac{2\pi G_0 \epsilon_0 r}{\ln(d/r)}$$

f/m

Voltage Between 2 Conductors In a group of Conductors



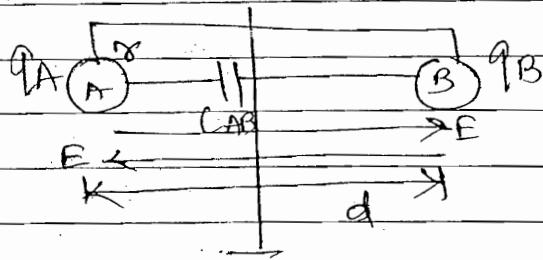
Voltage Between AB:-

$$V_{AB} = \frac{1}{2\pi\epsilon_0 Cr} \left[q_A \ln \frac{D_{AB}}{r} + q_B \ln \frac{D_{BC}}{r} \right]$$

$$+ q_B \ln \frac{r}{D_{BA}} + \dots + q_m \ln \frac{D_{mB}}{D_{mA}}$$

$$\text{At Balance } q_A + q_B + \dots + q_m = 0.$$

Capacitance Between Conductors of single phase 2-wire line



$$C_{AB} = \frac{q_A}{V_{AB}} = \frac{q_B}{V_{BA}}$$

$$V_{AB} = V_A - V_B = \frac{q_A}{2\pi\epsilon_0 Cr} \ln \frac{d}{r} - \frac{q_B}{2\pi\epsilon_0 Cr} \ln \frac{d}{r}$$

$$V_{AB} = \frac{1}{2\pi\epsilon_0 Cr} \left[q_A \ln \frac{d}{r} - q_B \ln \frac{d}{r} \right]$$

$$= \frac{1}{2\pi\epsilon_0 Cr} \left[q_A \ln \frac{d}{r} + q_B \ln \frac{r}{d} \right]$$

$$\text{at Balance } q_B = -q_A$$

$$V_{AB} = \frac{q_A}{2\pi\epsilon_0 Cr} \ln \left(\frac{d}{r} \right)^2$$

$$V_{AB} = \frac{q_A}{\pi\epsilon_0 Cr} \ln \left(\frac{d}{r} \right)$$

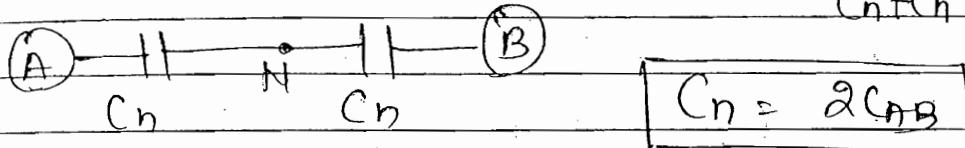
$$C_{AB} = \frac{q_A}{V_{AB}} = \frac{\pi\epsilon_0 Cr}{\ln(d/r)}$$

F/m

- Capacitance to Neutral (C_n) or Capacitance phase-to-

(A) C_{AB} (B)

$$\text{C}_{AB} = \frac{C_n \cdot C_n}{C_n + C_n} = \frac{C_n}{2}$$



$$C_n = \frac{2\pi\epsilon_0 r}{\ln(d/r)}$$

F/m /phase

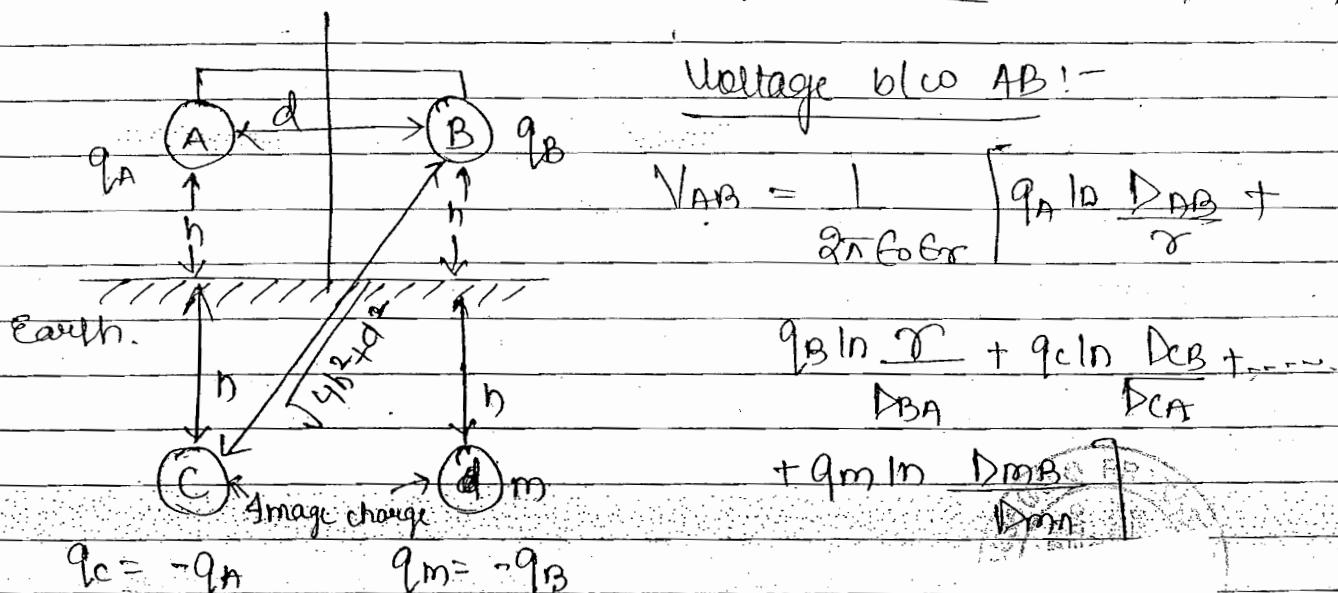
- Effect of Earth on Capacitance b/w Conductors

Earth consisting of ∞ no. of charge carrier of both the +ve and -ve sign. These charge carrier produce additional electrical field on the charges existing in the Tr-line conductor. Due to this capacitance b/w the conductor is increased which causes \uparrow in charging current and Reactive power so that over voltage occurs in the system which causes insulation failure and sometimes initiates corona. If the voltage of the system is higher than critical it may be disruptive voltage. To avoid this abnormality and reduce the capacitance, earth effect the height of tower is \uparrow at the operating voltage.

KV	h (metres)
11	7
33	11
132	20
220	35
400	50
765	65

- Methode of Images :- For calculation of earth effect b/w the conductors of Tr-line method of images is used. It is a mathematical technique adopted from electromagnetic field. In this method image charges are assumed below the ground which are opposite in sign and have equal magnitude with the charges existing on the conductors of Tr-line.

- No. of image charges = No. of conductors existing above the earth.



At Balance $q_A + q_B = 0$, $q_B = -q_A$, $q_c = -q_A$, $q_m = -q_B = q_A$

$$D_{mB} = D_{BA} = q, \quad D_{cA} = D_{mA} = 2h$$

$$D_{mA} = D_{cB} = \sqrt{4h^2 + d^2}$$

$$V_{AB} = \frac{q_A}{2\pi F_0 G_r} \ln \left[\frac{2h \cdot d}{\gamma \sqrt{4h^2 + d^2}} \right]^2$$

$$V_{AB} = \frac{q_A}{\pi F_0 G_r} \ln \left(\frac{d}{\gamma \sqrt{1 + \frac{d^2}{4h^2}}} \right)$$

$$C_{AB} = \frac{q_A}{V_{AB}} = \frac{\pi G_0 \epsilon_r}{\ln \left(\frac{d}{r\sqrt{1+d^2/b^2}} \right)}$$

With
Earth
effect.

NOTE :- If height of tower (h) is ↑ . $h \gg d$

$$\Rightarrow \frac{d^2}{4h^2} \approx 0$$

$$C_{AB} = \frac{\pi G_0 \epsilon_r}{\ln \left(\frac{d}{r} \right)}$$

without Earth effect.

• At $h \downarrow$, $\sqrt{1+d^2/b^2} \downarrow$, $\ln \left(\frac{d}{r\sqrt{1+d^2/b^2}} \right) \downarrow$, $C_{AB} \uparrow$.

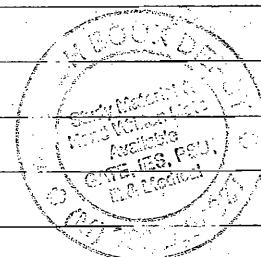
• Generalised Equation :-

(1) 3Φ Transposed line :-

$$C_n = \frac{2\pi G_0 \epsilon_r}{\ln \left[\frac{(D_1 D_2 D_3)^{1/3}}{r} \right]} \quad \text{F/m/phase}$$

(2) If $D_1 = D_2 = D_3 = D$

$$C_n = \frac{2\pi G_0 \epsilon_r}{\ln(D/r)}$$



• (3) Bundled Conductors :-

$$C_n = \frac{2\pi G_0 \epsilon_r}{\ln \left(\frac{D_m}{D_s} \right)}$$

(4) Double ckt line :-

$$C_n = \frac{2\pi \epsilon_0 \epsilon_r}{\ln \left(\frac{D_{M1} D_{M2} D_{M3}}{D_{S1} D_{S2} D_{S3}} \right)^{1/3}}$$

(5) Capacitance Reactance.

$$X_C = \frac{1}{2\pi f C_n} \Omega/m/phase$$

(6) Capacitance Susceptance.

$$B = \frac{1}{X_C} = 2\pi f C_n \text{ -v/m/phase}$$

(7) Charging Current.

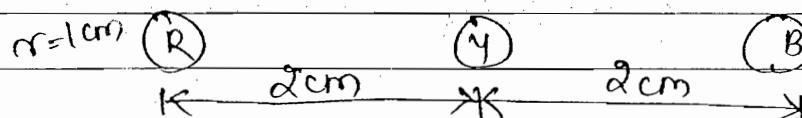
$$I_C = 2\pi f C_n V_{ph} \text{ A/m/phase}$$

(8) Reactive Power:-

$$Q_C = 2\pi f C_n V_{ph}^2 \text{ VARs/m/phase}$$

Q) Find the capacitance / phase for the following configuration

① Horizontal



$$C_n = \frac{2\pi \epsilon_0 \epsilon_r}{\ln \left(\frac{(2\pi r)(2\pi R)}{1} \right)^{1/3}}$$

$$\ln \left(\frac{(2\pi r)(2\pi R)}{1} \right)^{1/3}$$

$$= \frac{2 \times 3.14 \times 8.854 \times 10^{-12} \times 1}{1} \Rightarrow 10 \text{ pF/m/phase}$$

$$\left(\frac{(2\pi r)(2\pi R)}{1} \right)^{1/3}$$

$$\Rightarrow C_H$$

(v) Triangular :-

$$C_n = \frac{2\pi \epsilon_0 \ell}{\ln \left(\frac{\ell}{r} \right)}$$

$$= \frac{2\pi \times 8.854 \times 10^{-12} \text{ F}}{\ln \left(\frac{2}{\pi \times 10^{-2}} \right)}$$

$$= 10.5 \text{ pF/m/phase}$$

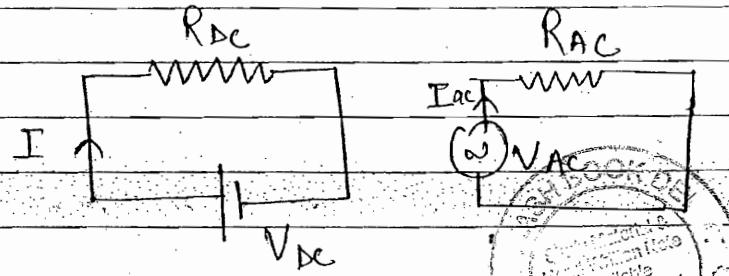
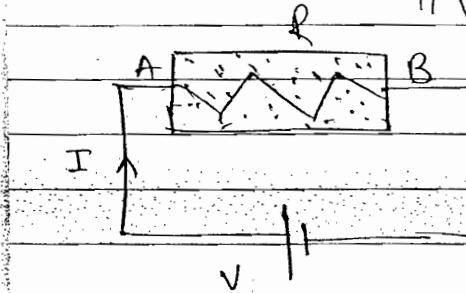
$$= C_\Delta$$

$$C_\Delta > C_H$$

$$L_\Delta < L_H$$

prefer Δ one even C_n has disadv.

RESISTANCE :-



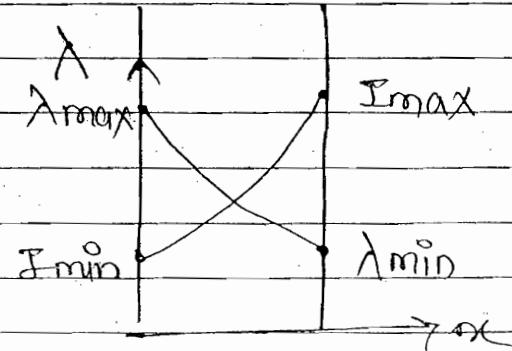
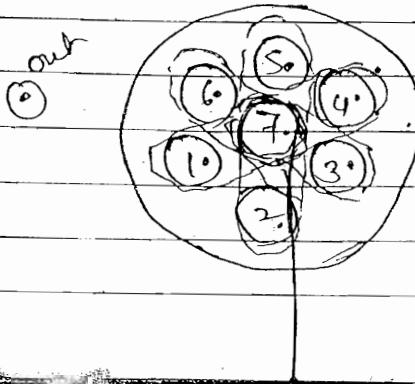
$$R_{AC} > R_{DC}$$

$$\approx 1.5 R_{DC}$$

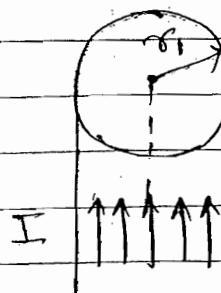
→ ① Skin effect

→ ② Proximity effect

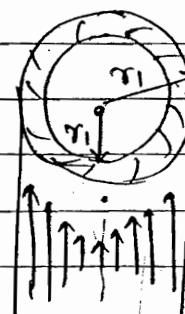
(i) Skin Effect :-



HVDC



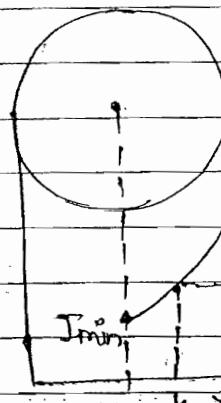
HVAC



$$R_{dc} = \frac{\rho l}{\pi (r_1^2 - r_2^2)}$$

$$R_{dc} = \frac{\rho l}{\pi r_1^2}$$

$$R_{ac} > R_{dc}$$

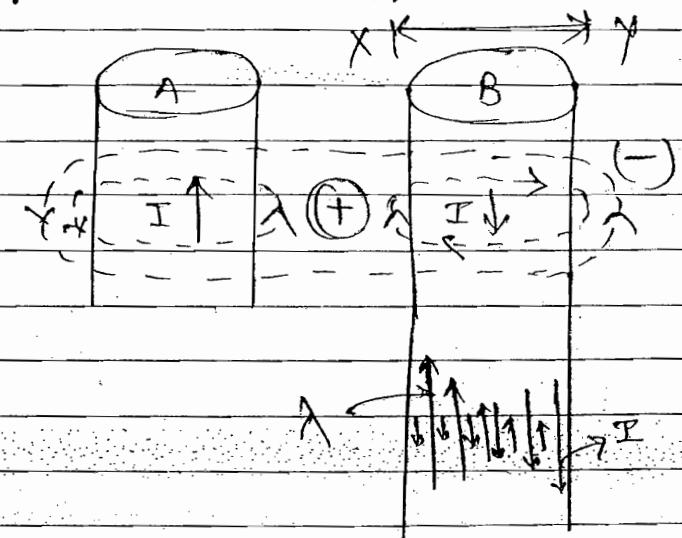
Skin Depth:

$$J_{max} = 27.18 A$$

$$J_{max} = \frac{27.18}{e} = 10 A$$

$$\delta = \sqrt{\frac{H_0 H_r \sigma}{\pi f}}$$

$$\text{Skin effect } \propto \frac{1}{\delta}$$

Proximity Effect:

Blw → flows in same dirⁿ +
Surf → flows in opp. dirⁿ → -

$$\boxed{\text{Skin effect } \propto \frac{1}{\delta}}$$

- accumulation of current on the surface of conductor is called skin effect.

- Due to skin effect effective area of current flowing path is \downarrow which causes $R_{ac} > R_{dc}$

- Skin Depth :- The depth of the conductor at which the surface current is reduced to $\frac{1}{e}$ times the surface value. As the skin depth is \uparrow skin effect is \downarrow . In case of communication lines frequency is very high so that skin depth is small skin effect is larger.

- Skin effect depends on

- (1) Frequency (2) Conductivity (3) μ_r
- (4) Size of the conductor

- Proximity Effect : It will occur due to current flowing in the adjacent conductor produces Non-uniform flux linkage so that non-uniform current flows and the effective already current flowing path is reduced which causes $R_{ac} > R_{dc}$.

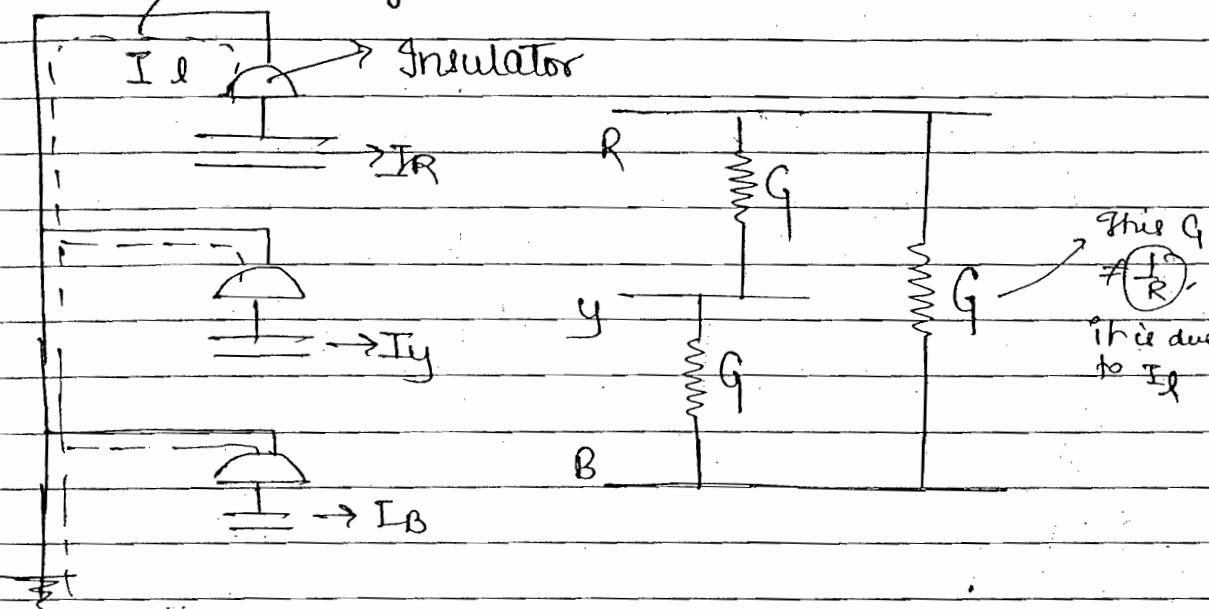
- Proximity effect depends on:-

- (1) Frequency (2) σ (3) μ_r (4) Distance b/w the conductors

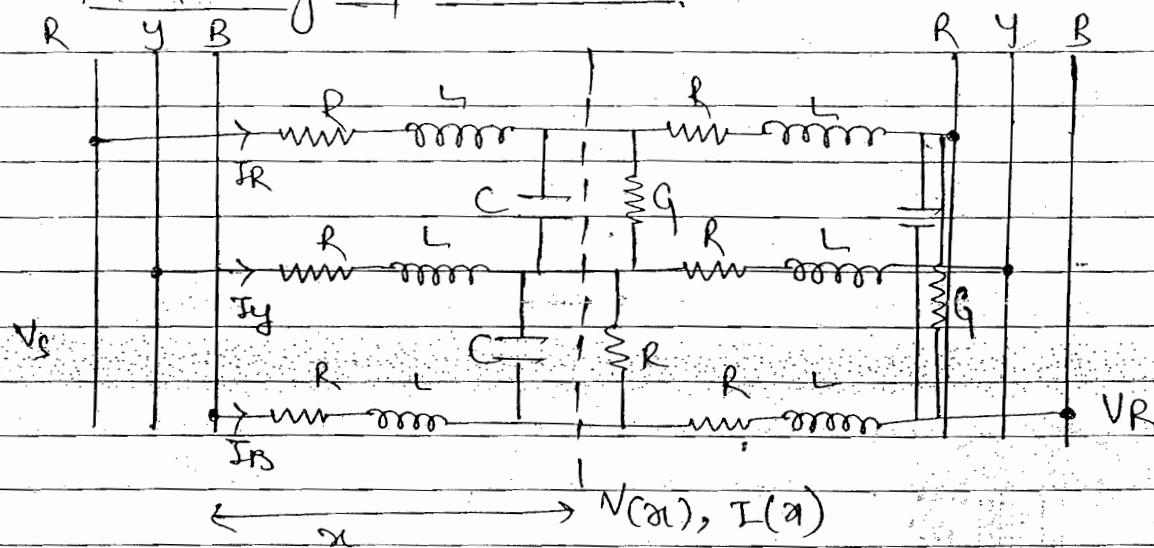
- Proximity effect is more if the distance is small b/w the conductor ex:- power cables. In overhead lines distance b/w the conductors is larger so that proximity effect is negligible

- (4) Conductances :- The leakage current flowing b/w conductor and the insulation is represented with electrical equivalence of conductor parameters G . G value is neglected in case of short and medium lines and it is considered in case of long lines.

→ leakage current

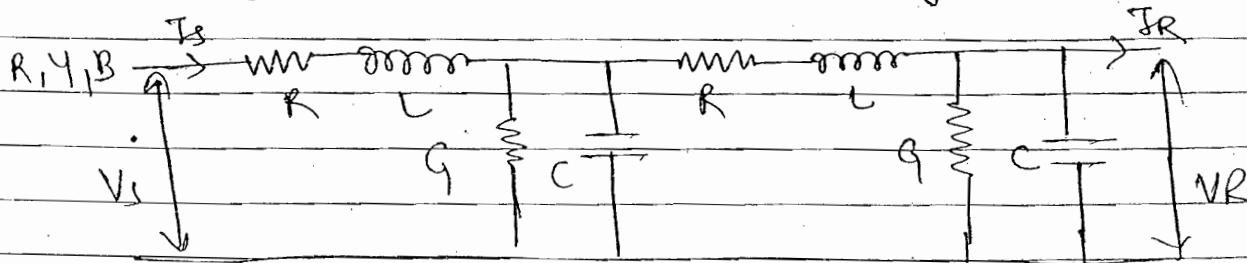


• Modelling Of Tr-line:-



Assumption :-

- ① System is balanced ($|I_{RL}| = |I_{YL}| = |I_{BL}|$)



Distributed N.W.

(2) Lumped NW:-

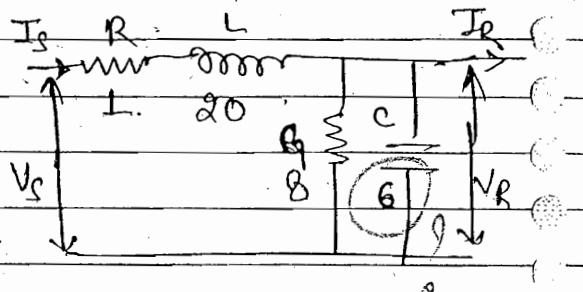
$$l = 100 \text{ km}$$

$$R = 0.001 \times 100 = 1 \Omega$$

$$L = 0.2 \times 100 = 20 \text{ H}$$

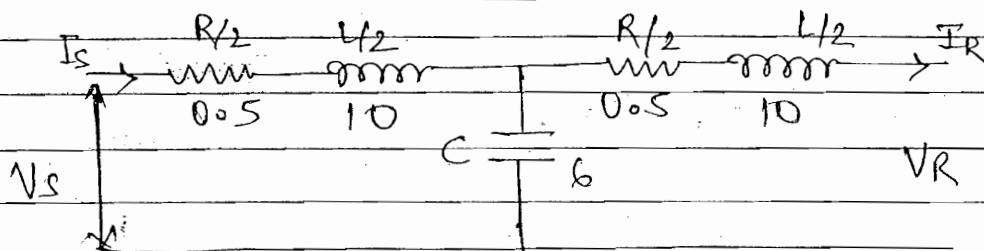
$$C = 0.04 \times 100 = 4 \text{ M F}$$

$$G = 0.08 \times 100 = 8 \text{ n}^{-1}$$

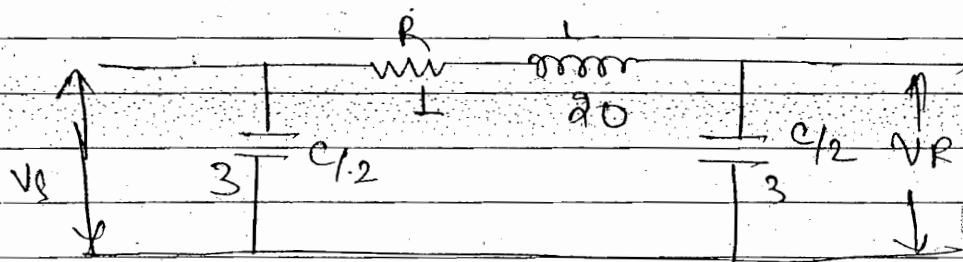


(3) Medium line :- [G is neglected]

(a) Nominal TNW. :-



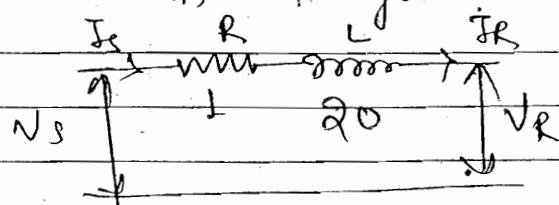
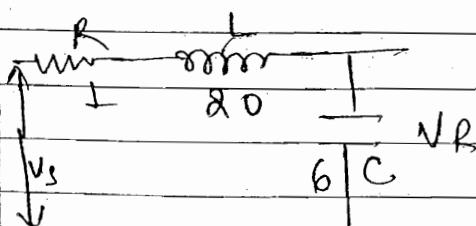
(b) Nominal π NW:-



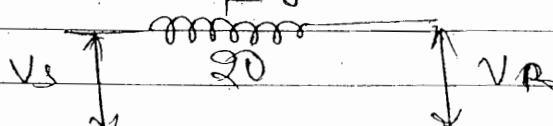
(c) End Condense:-

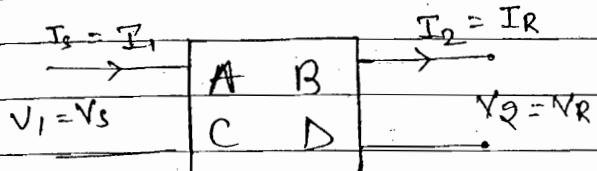
(d) Short line

(G, C, neglected)



(e) Fault analysis Eq. (R < X_L)

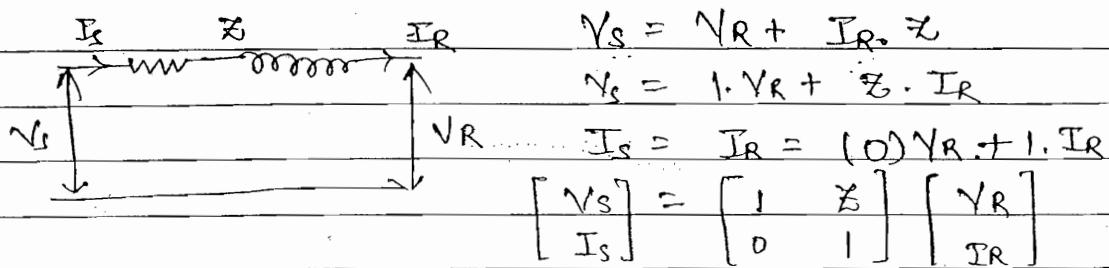


A B C D or T₂. LINE PARAMETERS

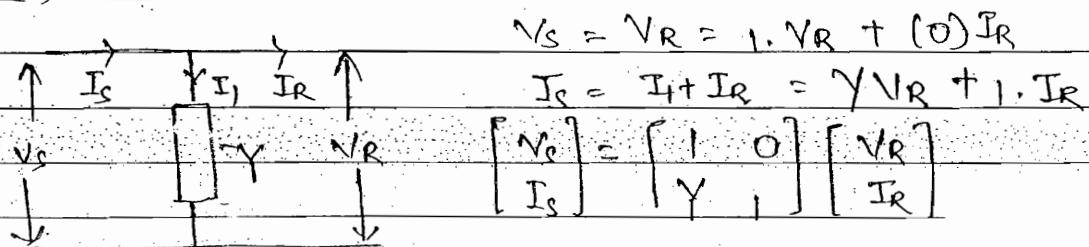
$$\begin{bmatrix} V_1 \\ I_1 \end{bmatrix} = \begin{bmatrix} A & B \\ C & D \end{bmatrix} \begin{bmatrix} V_2 \\ I_2 \end{bmatrix}$$

$A = D \Rightarrow$ symmetrical co., $AD - BC = 1 \Rightarrow$ Reciprocal

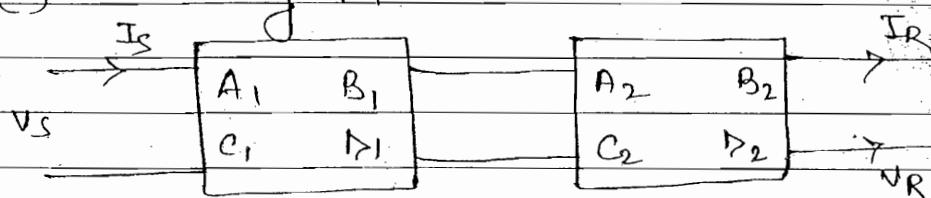
(1) Z Network :- (short Tr line)



(2) Y Network:-

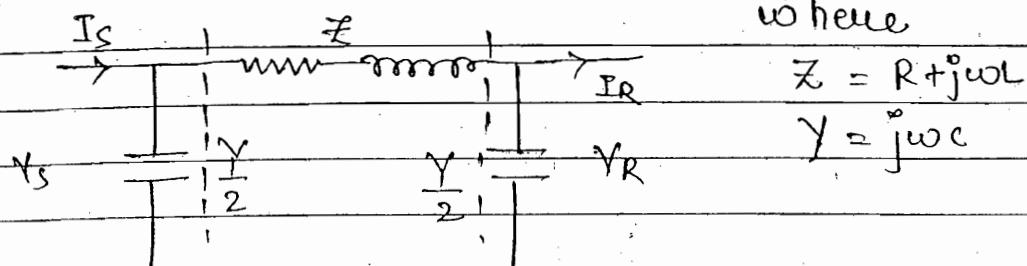


(3) Cascading Netw: -



$$\begin{bmatrix} V_S \\ I_S \end{bmatrix} = \begin{bmatrix} A_1 & B_1 \\ C_1 & D_1 \end{bmatrix} \begin{bmatrix} A_2 & B_2 \\ C_2 & D_2 \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix}$$

• Reciprocal :- By reversing - value will remain same.
 e.g. V_S, V_R are reversed, values remain same.

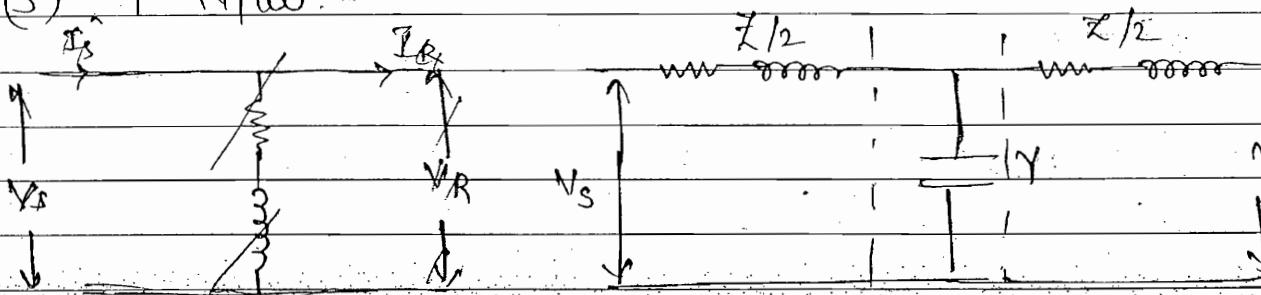
(4) Nominal π N/w:-

$$\begin{bmatrix} V_s \\ I_s \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ Y_2 & 1 \end{bmatrix} \begin{bmatrix} 1 & Z \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ Y_2 & 1 \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix}$$

$$\begin{bmatrix} V_s \\ I_s \end{bmatrix} = \begin{bmatrix} \left(1 + \frac{YZ}{2}\right) & Z \\ Y\left(1 + \frac{YZ}{4}\right) & \left(1 + \frac{YZ}{2}\right) \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix}$$

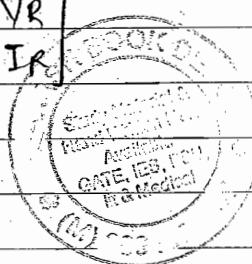
Nominal

(5) T N/w:-

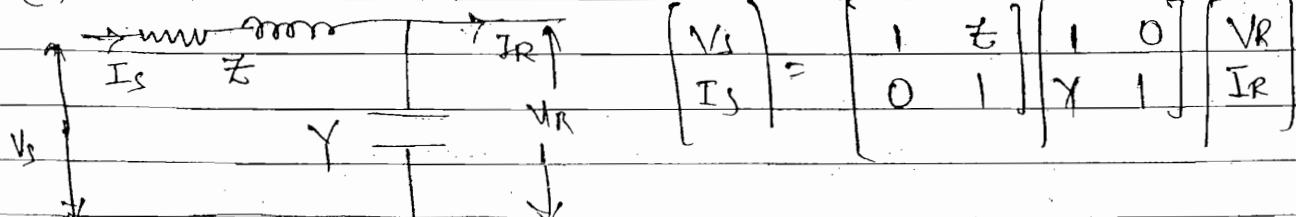


$$\begin{bmatrix} V_s \\ I_s \end{bmatrix} = \begin{bmatrix} 1 & Z/2 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ Y & 1 \end{bmatrix} \begin{bmatrix} 1 & Z/2 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix}$$

$$\begin{bmatrix} V_s \\ I_s \end{bmatrix} = \begin{bmatrix} \left(1 + \frac{YZ}{2}\right) & Z\left(1 + \frac{YZ}{4}\right) \\ Y & \left(1 + \frac{YZ}{2}\right) \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix}$$



(6) End Condenser N/w:-



$$\begin{bmatrix} V_s \\ I_s \end{bmatrix} = \begin{bmatrix} (1+\gamma z) & z \\ \gamma & 1 \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix}$$

$A \neq D$
unsymmetrical.

Transmission Line Performance Parameter:-

(1) Transmission η :-

$$\% \eta = \frac{P_R \times 100}{P_s} = \left| \frac{V_R I_R}{V_s I_s} \right| \frac{\cos \phi_R \times 100}{\cos \phi_s}$$

$$= \frac{P_R}{P_R + P_L} \times 100$$

$$P_L = \text{Tr line loss} = P_s - P_R$$

↳ fideal: $\eta = 100\%$. ↳ practical $\eta > 90\%$.

• Calculation of I_R if V_R , P_R are given:-

$$|I_R| = \frac{P_R}{V_R \cos \phi_R}$$

V_R = phase voltage

P_R = 1- ϕ power

$$|I_R| = \frac{P_R}{\sqrt{3} V_R \cos \phi_R}$$

$V_R = V_L$ = line voltage

P_R = 3 ϕ power

(2) Voltage Regulation:-

$$\% V_{REG} = \frac{|V_{RNL}| - |V_{RFL}|}{|V_{RFL}|} \times 100$$

V_{RNL} = No load Receiving End Voltage

$$V_i = A Y_R + B I_R$$

At no load $I_R = 0 \Rightarrow V_s = A V_{RNL}$

$$|V_{RNL}| = \frac{|V_s|}{A}$$

V_{RFL} = full load or rated Receiving End Voltage
 $= |V_R|$

$$\% \text{ } V_{\text{REG}} = \left| \frac{V_s}{A} - |V_R| \right| \times 100$$

$|V_R|$

for short line
 $A=1$

valid for short / medium / long lines

\hookrightarrow Ideal V_{REG} : 0% , \hookrightarrow Practical $V_{\text{REG}} = \pm 5\%$.

• Classification of Transmission line:-

(1) Short Tr. line $\rightarrow l < 80 \text{ km}$, $f < 4000$

(2) Medium Tr. line $\rightarrow 80 \leq l \leq 200 \text{ km}$, $4000 \leq f \leq 10,000$

(3) Long Tr. line $\rightarrow l > 200 \text{ km}$, $f > 10,000$

Ex:- $l = 80 \text{ km}$; $f = 50 \text{ Hz}$.

$$lf = 80 \times 50 = 4000$$

• Communication lines are operation in MHz range so that they are considered long line equivalent circuit throughout

• All the parameters R, L, C, G are distributed ~~throughout~~ along the length of line

Q A Tr line has a length of 10km is excited by

- (i) 50 Hz (ii) 500 Hz (iii) 5 kHz .

Find the type of Tr line.

Solution $l = 10 \text{ km}$,

$$(i) f = 50 \text{ Hz} \quad (ii) f = 500 \quad (iii) f = 5 \times 10^3$$

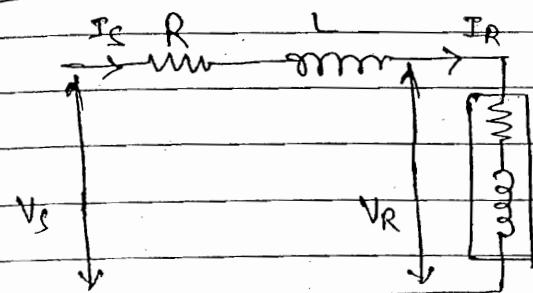
$$lf = 10 \times 50 \quad lf = 10 \times 500 \quad lf = 10 \times 10^3 \times 5 \\ = 500 \quad = 5000 \quad = 5 \times 10^4$$

Short

Medium

long.

(1) Short Tr-line :-



$$\begin{bmatrix} V_s \\ I_s \end{bmatrix} = \begin{bmatrix} 1 & jZ \\ 0 & 1 \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix}$$

$$\text{(1) \% VEG} = \frac{|V_s| - |V_R|}{|V_R|} \times 100$$

for short line $A = 1$

$$(Z) = (R + jXL)$$

$$\% \text{ VEG} = \frac{|V_s| - |V_R|}{|V_R|} \times 100$$

$$(2) \% \eta = \frac{P_R}{P_R + P_L} \times 100$$

$$\bullet \frac{1 - \phi}{R = R_0 I_R^2} \quad \bullet \frac{3 - \phi}{P_L = 3R I_R^2}$$

Pg NO. → 45

Conventional 2 $\lambda = 40 \text{ km} \quad 220 \text{ KV}, 30^\circ$

$$R = 0.15 \Omega/\text{km} \quad f = 50 \text{ Hz}$$

$$l_f = 40 \times 50$$

$$L = 1.5923 \text{ mH/km}$$

→ 2000 short

$$S_R = 381 \text{ MVA}$$

$$\cos \phi_R = 0.8$$

(1) Convert into lumped Nw.

default = lagging.

$$R = 0.15 \times 40 = 6 \Omega$$

$$L = (2\pi f L) \cdot l = 2\pi \times 50 \times 1.5923 \times 10^{-3} \times 40 = 20 \Omega$$

$$Z = 6 + j20 = 20.8 / 73.3^\circ \Omega$$

For short line $B = Z = 60 + j20$

$$A = D = 1$$

$$I_R = \frac{P_R}{\sqrt{3} V_R \cos \phi_R} = \frac{B S_R \cos \phi_R}{\sqrt{3} V_R \cos \phi_R}$$

$$= \frac{381 \times 10^6 \times 0.8}{\sqrt{3} \times 220 \times 0.8 \times 10^3}$$

$$|I_R| = 1000 \text{ A}$$

$$\cos \phi_R = 0.8 \text{ lag}, Q_R = 36.86^\circ$$

$$I_R = 1000 \angle -36.86^\circ A = I_s$$

Remember
these

$$(1) (a) V_s = A V_R + B I_R$$

$$= 1 \times 220 \times 10^3 + 20.8 \angle 73.3^\circ \times 1000 \angle -36.86^\circ$$

J3

$$= 144.8 \angle 4.8^\circ \text{ kV phase.}$$

$$V_{SL} = \sqrt{3} \times 144.8 \angle 4.8^\circ$$

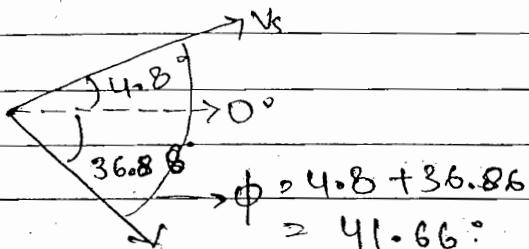
$$= 250 \angle 4.8^\circ \text{ kV}$$

$$(b) P_s = \sqrt{3} |V_s I_s| \cos \phi$$

$$V_s = 250 \angle 4.8^\circ \text{ kV.}$$

$$I_s = I_R = 1000 \angle -36.86^\circ$$

A



$$P_s = \sqrt{3} \times 250 \times 10^3 \times 1000$$

$$\times \cos(36.86 + 4.8^\circ)$$

$$P_s = 323 \text{ MW}$$

(2)

$$(a) \% V_{REG} = \frac{(V_s - V_R) \times 100}{V_R}$$

$$\Rightarrow 250 - 220 \times 100$$

$$290$$

$$= \frac{30 \times 100}{220}$$

$$V_{REG} \% = 13.64 \%$$

$$(b) \% \eta = \frac{P_R}{P_s} \times 100 = \frac{381 \times 0.8}{323} \times 100$$

$$\% \eta = 94\%$$

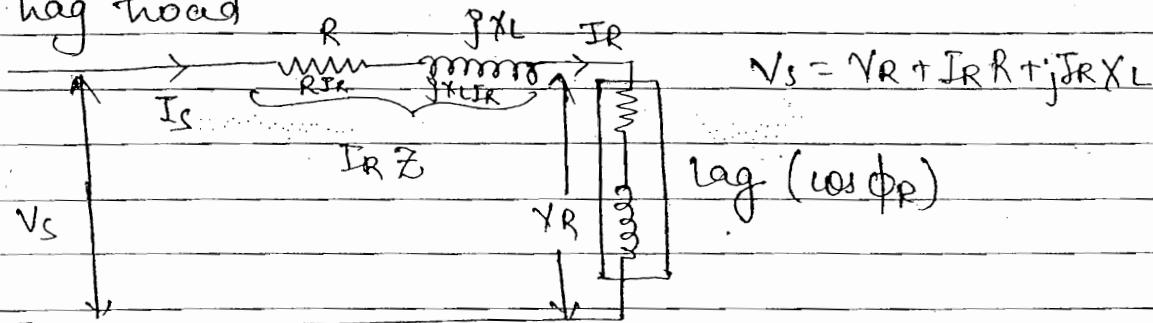
$$(OR) P_L = 3 R I_R^2 = 3 \times 6 \times (1000)^2 = 18 \text{ MW}$$

$$\% \eta = \frac{P_R \times 100}{P_R + P_L} = \frac{381 \times 0.8}{381 \times 0.8 + 18} \times 100 \approx 94\%$$

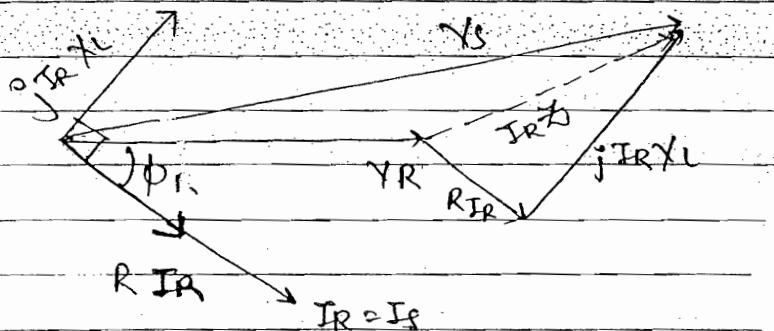
1.18

Phasor Diagram:-

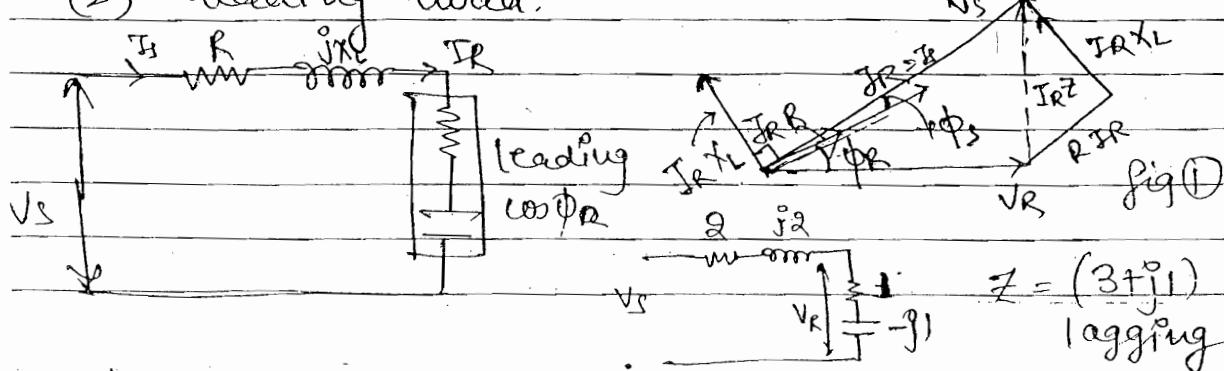
(1) lag load



Start from Receiving end, add all drop, final reach to sending end

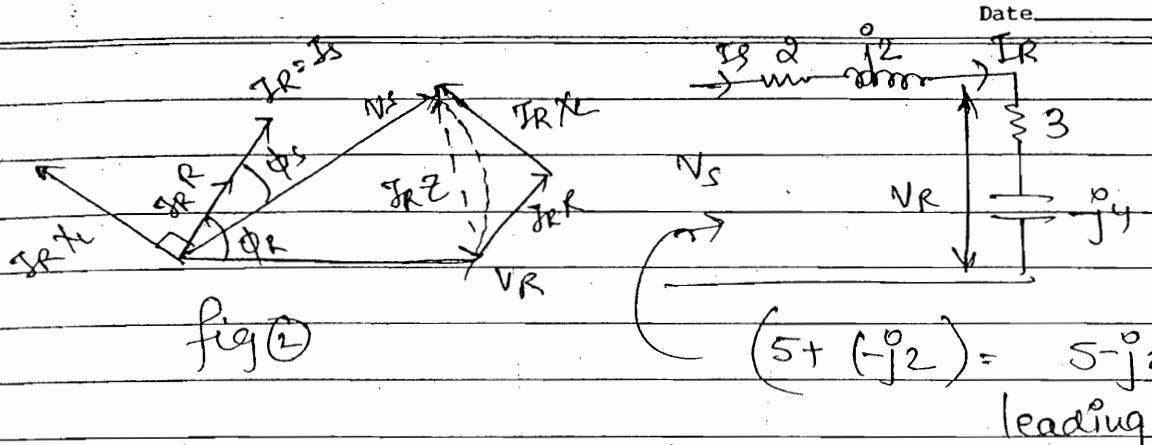


(2) leading load:-

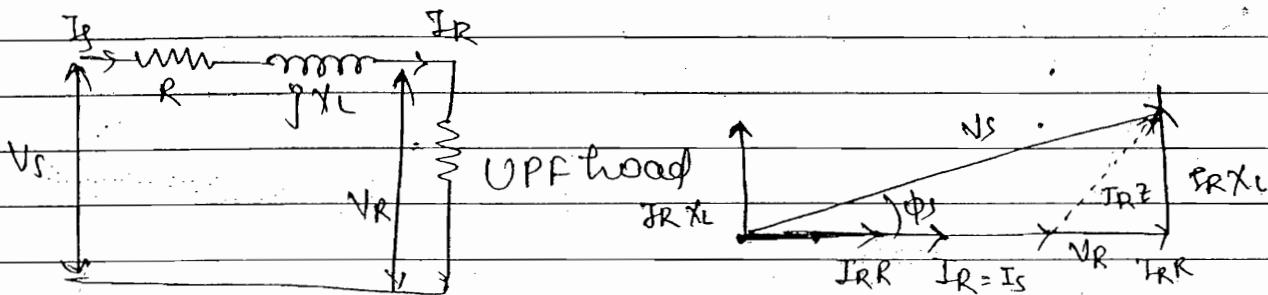


$$Z = (3 + j1) \text{ ohms}$$

lagging



- (3) UPF load.



- In lagging load:- $\phi_s > \phi_R$. Bcoz More lagging load.

$$V_s > V_R$$

+ve V_{REG}

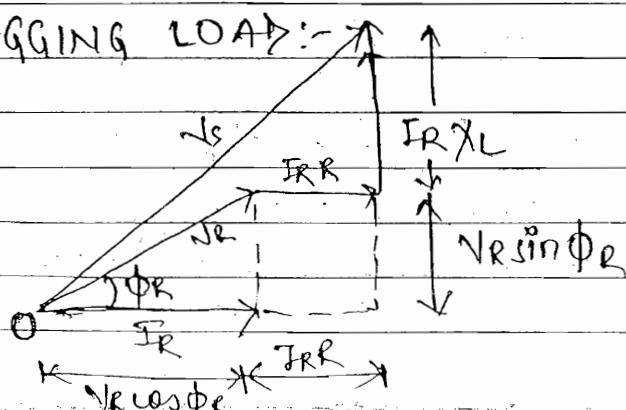
$$V_{REG} \neq 0$$

- UPF load:- $V_s > V_R$ $V_{REG} \neq 0$

- Heading load:- possibility of $V_{REG} \approx 0$
 $V_s \approx V_R$

- Effect of load Power factor ON Voltage Regulation

(1) LAGGING LOAD:-



$$V_s^2 = (V_R \cos \phi_R + I_R R)^2 + (V_R \sin \phi_R + I_R X_L \sin \phi_R)^2$$

$$= V_R^2 + I_R^2 (R^2 + X_L^2) + 2 V_R I_R (R \cos \phi_R + X_L \sin \phi_R) \quad (1)$$

Assume $I_R^2 (R^2 + X_L^2) \ll V_R^2$

$$V_s = \left[V_R^2 + 2 V_R I_R (R \cos \phi_R + X_L \sin \phi_R) \right]^{1/2}$$

$$= V_R \left[1 + \frac{2 I_R}{V_R} (R \cos \phi_R + X_L \sin \phi_R) \right]^{1/2}$$

$$\text{use } (1+x)^{1/2} \approx 1 + \frac{x}{2}$$

$$V_s = V_R \left[1 + \frac{2 I_R}{2 V_R} (R \cos \phi_R + X_L \sin \phi_R) \right]$$

$$V_s - V_R = I_R (R \cos \phi_R + X_L \sin \phi_R)$$

$$\% V_{REG} = \frac{V_s - V_R}{V_R} \times 100$$

$$\boxed{\% V_{REG} = \frac{I_R (R \cos \phi_R + X_L \sin \phi_R)}{V_R} \times 100}$$

Condition for Max. V_{REG} :-

$$\frac{d}{d\phi_R} [R \cos \phi_R + X_L \sin \phi_R] = 0$$

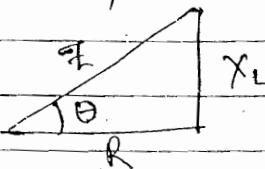
$$-R \sin \phi_R + X_L \cos \phi_R = 0$$

$$\boxed{\phi_R = \tan^{-1} \left(\frac{X_L}{R} \right)} \quad \text{condition for Max } V_{REG}$$

$R, X_L \rightarrow$ Tr line parameter, $\phi_R =$ load pofo angle

If $Z = (R + j X_L) =$ Tr. line impedance.

$$\theta = \tan^{-1} \left(\frac{X_L}{R} \right)$$



$$\theta = \phi_R = \tan^{-1} \left(\frac{X_L}{R} \right)$$

- p.f. of lag load for Max. V_{REG} .

$$\cos \phi_R = \cos \theta = \frac{R}{Z}$$

(2) lead load.

$$\phi_R = -\theta$$

$$\% V_{REG} = \frac{I_R (R \cos(-\phi_R) + X_L \sin(-\phi_R)) \times 100}{V_R} \rightarrow V_R$$

$$\% V_{REG} = \frac{I_R (R \cos \phi_R - X_L \sin \phi_R) \times 100}{V_R}$$

Condition for $V_{REG} = 0\%$.

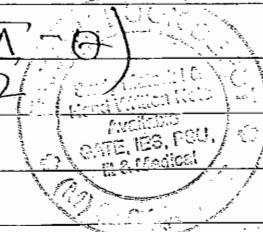
$$R \cos \phi_R - X_L \sin \phi_R = 0$$

$$\phi_R = \tan^{-1} \frac{R}{X_L}$$

$$\text{If } \theta = \tan^{-1} \left(\frac{X_L}{R} \right) \text{ then } (\phi_R = \frac{\pi}{2} - \theta)$$

p.f. of lead load for $V_{REG} = 0\%$

$$\cos \phi_R = \sin \theta = \frac{X_L}{Z}$$



$$(3) \frac{V_{REG}(\text{lead})}{V_{REG}(\text{lag})} = \frac{R \cos \phi_R - X_L \sin \phi_R}{R \cos \phi_R + X_L \sin \phi_R}$$

↓
lag.

(4) Cal. of I_R, P_R if $V_{REG} = 0$, or $|V_s| = |V_R|$ gives
from ①

$$V_s^2 = V_R^2 + I_R^2 (R^2 + X_L^2) + 2 V_R I_R [R \cos \phi_R + X_L \sin \phi_R]$$

$$\text{If } |V_R| = |V_s|$$

$$|I_R| = \frac{2 V_R (R \cos \phi_R + X_L \sin \phi_R)}{(R^2 + X_L^2)}$$

lag ahead

$$|I_R| = \frac{2 V_R (R \cos \phi_R - X_L \sin \phi_R)}{(R^2 + X_L^2)}$$

lead ahead

where $V_R, R, X_L \Rightarrow$ phase values.

$$P_R = \sqrt{3} V_R I_R \cos \phi_R$$

where $V_R = V_L = \text{line voltage}$

Q A Δ -line has an impedance of $3+j4 \Omega/\text{phase}$ p.f of load required for maintaining maximum and zero voltage regulation or respectively

- (a) 0.3 lead, 0.6 lag.
- (b) 0.6 lag, 0.3 lead
- (c) 0.6 lead, 0.3 lag
- (d) 0.3 lag, 0.3 lead

$$\text{Max: } \frac{S}{s} = 0.6 \text{ lag.}$$

$$s$$

$$\text{Zero: } \frac{4}{S} = 0.8 \text{ lead}$$

Q Tr-line impedance = 10° the load p.f. angle required for zero maximum voltage regulation is respectively.

Sol. $\text{p.f.} = \text{zero}$. $\frac{\pi}{2} - \theta = \theta$

Q Tr-line is an impedance of $2+j8$ is connected with 0.8 lagging load produces 10% of voltage regulation find the voltage Regulation for a leading load of 0.907.

Soln. $Z = 2+j8$ 0.8 lagging 10% VR.
Leading =

$$V_{\text{REG lead}} = 2 \times 0.707 - 8 \times 0.407$$

$$V_{\text{REG lag.}} = 2 \times 0.8 + 8 \times 0.6 \\ = -5^\circ$$

Q A 3φ Tr-line having $Z = 3+j4$ connected with a 0.8 lagging load and operating $V_s = 11kV$ find the active power drawn by load

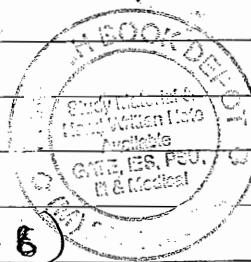
Sol.

$$\text{P}_r = \frac{2 \times V_r (R \cos \phi_r + X_l \sin \phi_r)}{X_l^2 + R^2}$$

$$= \frac{2 \times 11 \times (3 \cos 0.8 + 4 \sin 0.8)}{(4^2 + 3^2)}$$

$$= 2.68$$

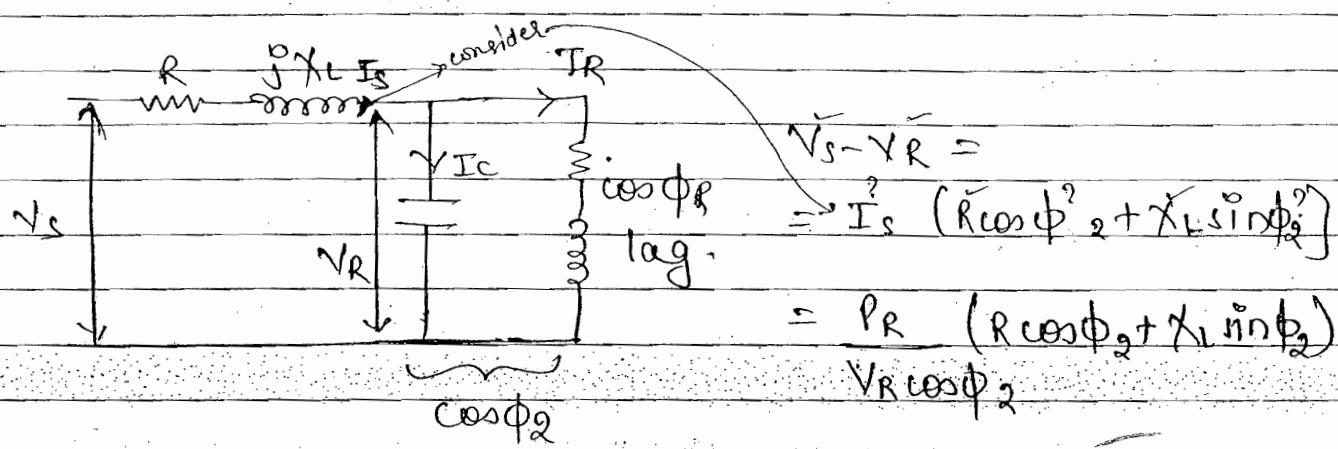
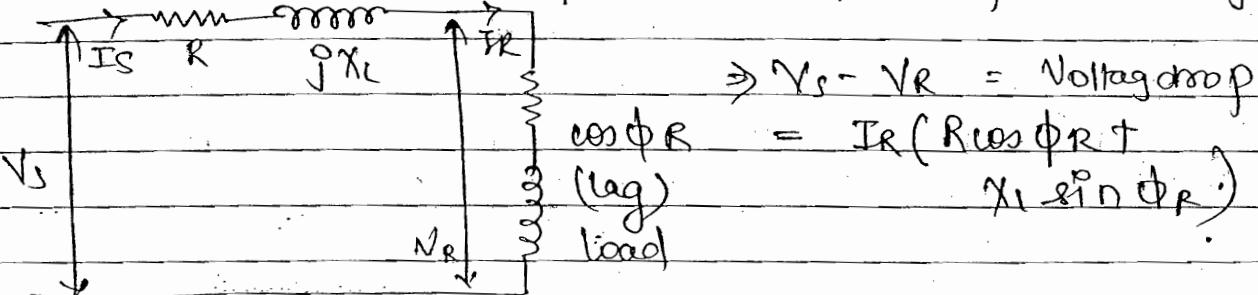
$$\text{P}_r = \sqrt{3} V_r I_r \cos \phi \\ = \sqrt{3} \times 2.68 \times 11 \times \cos 0.8$$



$$I_R = \frac{2 \times 11\sqrt{3} \times 10^3 (3 \times 0.8 + 4 \times 0.6)}{(3^2 + 4^2)} = 2.4 \text{ kA}$$

$$P_R = \sqrt{3} V_R I_R \cos \phi_R \\ = \sqrt{3} \times 11\sqrt{3} 10^3 \times 2.4 \times 10^3 \times 0.8 = 37.1 \text{ MW.}$$

- Calculation of Compensator (Capacitor) for Reducing V_R :



$$V_s - V_R = \frac{R P_R}{V_R} + \frac{P_R X_L}{V_R} \tan \phi_2$$

$$\tan \phi_2 = \frac{|V_s V_R| - |V_R|^2 - |R P_R|}{|P_R X_L|}$$

$$\phi_2 = \tan^{-1} \left(\frac{|V_s V_R| - |V_R|^2 - |R P_R|}{|P_R X_L|} \right)$$

$$|I_s| = \frac{P_R}{V_R \cos \phi_2}$$

$$I_s / \phi_2 = I_R / -\phi_R + j I_c$$

$$I_c = I_s / \phi_2 - I_R / -\phi_R$$

$$2\pi f C V_R = I_c$$

$$\boxed{C = \frac{I_c}{2\pi f V_R}}$$

check whether

I_c angle coming

90° or not

as it pure capacitive

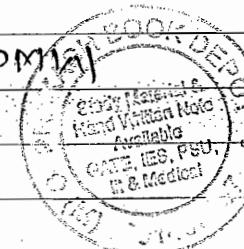
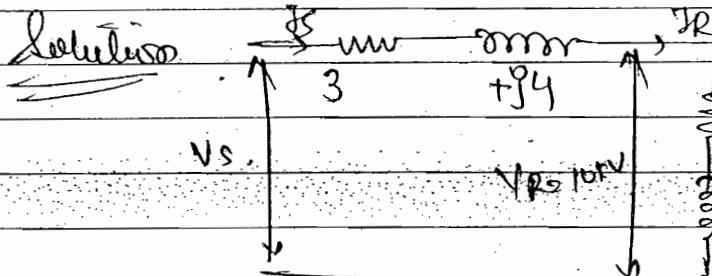
Q 1-Φ Tr-line has an $Z = 3 + j4 \Omega$ operating at $V_R = 10kV$ connected with load of $10MW$ 0.8 lagging. Calculate Assume $N_R = \text{const}$

(1) Voltage Regulation

(2) How much capa. compensator required for reducing voltage regulat.

(3) 50%

(4) 25%



$$TR = \frac{P_R}{V_R \cos \phi_R} = \frac{10 \times 10^6}{10 \times 10^3 \cos 0.8} = 1250 \Omega$$

$$\% V_{reg} = \left| \frac{I_R (R \cos \phi_R + X_L \sin \phi_R)}{V_R} \right| \times 100$$

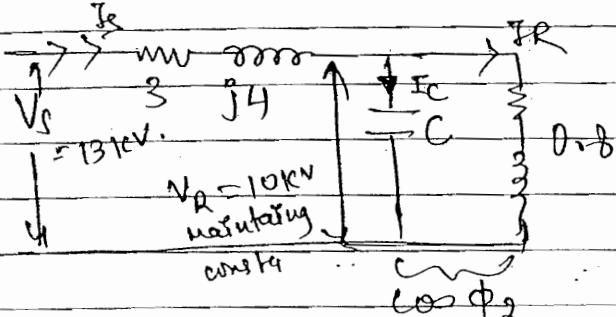
$$= \frac{1250 (3 \times 0.8 + 4 \times 0.6)}{10 \times 10^3} \times 100$$

$$= 60 \%$$

$$\Rightarrow \frac{V_s - V_R}{V_R} = 60\% = 0.6$$

$$N_s = [0.6 \times 10 \times 10^3] + (10 \times 10^3) \\ = 16 \text{ KV}.$$

(⑨) with compensator:



9 V_{REG} reduce of 50% of 60V.

$$\frac{V_S - V_R}{V_R} \times 1000 = \frac{0.6}{2} = 0.3$$

$$\frac{Y_s - 10}{10} = 0.3$$

$$V_s = 13 \text{ kV}$$

$$\textcircled{16} \quad \phi_2 = \tan^{-1} \left(\frac{|V_s| |N_R| - |V_R| H_R R_R}{|P_R X_L|} \right)$$

$$= \tan^{-1} \left(\frac{[13 \times 10] - [(10)^2] - [3 \times 10]}{10 \times 4} \right)$$

O^-

$$I_S = \frac{P_R}{V_R \cos \phi_2} = \frac{10 \times 10^6}{10 \times 10^3 \times 1} \Rightarrow 1000 \text{ A}$$

$$I_C = I_S / \phi_2 - I_R / \phi_R$$

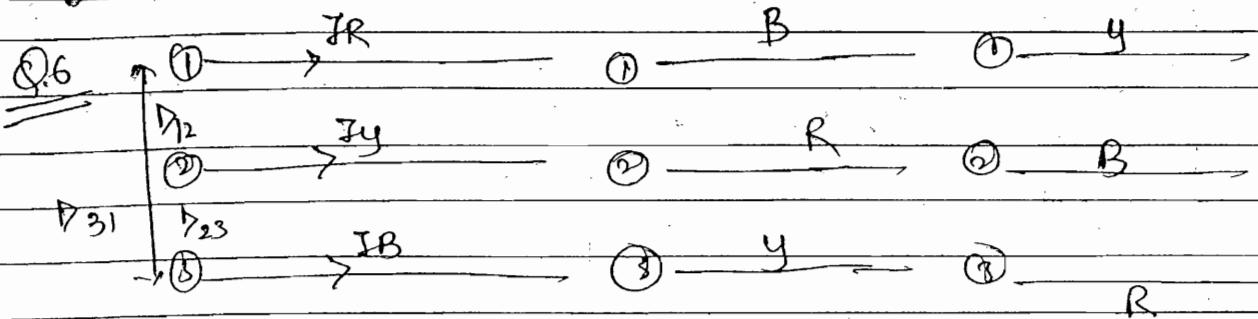
$$= 1000 \angle 0^\circ - 1250 \angle 36.86^\circ$$

$$= 750 \angle 90^\circ \text{ Amp}$$

$$C = T_e - 750$$

$$2\pi f \times V_R \quad 2\pi f \times 50 \times 10 \times 10^3$$

$$= 238 \text{ } \mu\text{F.}$$



$$\lambda_1 = \frac{\mu_0}{2\pi} \left[\frac{I_R \ln \frac{1}{r_1}}{D_{12}} + \frac{I_y \ln \frac{1}{r_1}}{D_{12}} + \frac{I_B \ln \frac{1}{r_1}}{D_{13}} \right]$$

$$\lambda_2 = \frac{\mu_0}{2\pi} \left[\frac{I_R \ln \frac{1}{r_1}}{D_{23}} + \frac{I_y \ln \frac{1}{r_1}}{D_{23}} + \frac{I_B \ln \frac{1}{r_1}}{D_{12}} \right]$$

$$\lambda_3 = \frac{\mu_0}{2\pi} \left[\frac{I_R \ln \frac{1}{r_1}}{D_{13}} + \frac{I_y \ln \frac{1}{r_1}}{D_{13}} + \frac{I_B \ln \frac{1}{r_1}}{D_{23}} \right]$$

$$I_y = I_R / -120^\circ = -0.5 - j0.866 I_R$$

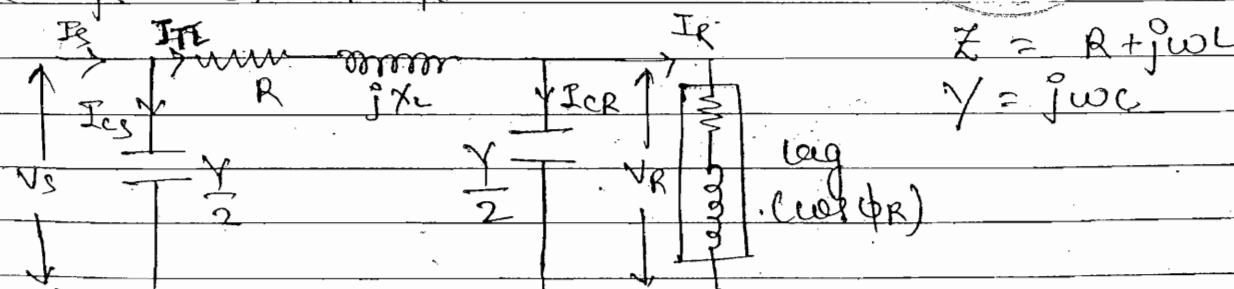
$$I_B = I_R / -240^\circ = -0.5 + j0.866 I_R$$

Take these aug. value. Real terms will cancel out only R will left.

11/7/2011

(2) Medium Tr-line:

(1) Nominal π form: -



$$\begin{bmatrix} V_s \\ I_s \end{bmatrix} \rightarrow \begin{bmatrix} 1 + \frac{YZ}{2} & Z \\ Y(1 + \frac{YZ}{4}) & (1 + \frac{YZ}{2}) \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix}$$

$$(1) \% V_{REG} = \left| \frac{V_s}{A} - |V_R| \right| \times 100$$

where $A = \left(1 + \frac{\gamma Z}{2} \right)$

$$(2) \% \eta = \frac{P_R}{P_R + P_L} \times 100$$

where $P_R = R I_{T_L}^2$ for 1-φ, $= 3R I_{T_L}^2$ for 3-φ

$$I_R = I_R + I_{CR}$$

$$= I_R + \frac{\gamma}{2} V_R$$

Steps:

(1) V_R as Ref

(2) I_R lags V_R by ϕ_R

(3) $I_{CR} = V_R \gamma / 2$

(4) $I_{T_L} = I_R + I_{CR}$

I_{CR} leads V_R by 90°

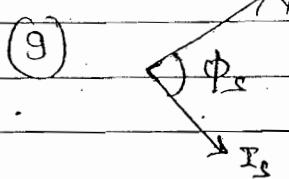
(5) $I_{T_L} Z = R I_{T_L} + j I_{T_L} \chi_1$

(6) $V_s = V_R + I_{T_L} Z$

(7) $I_{CS} = \frac{V_s \gamma}{2}$

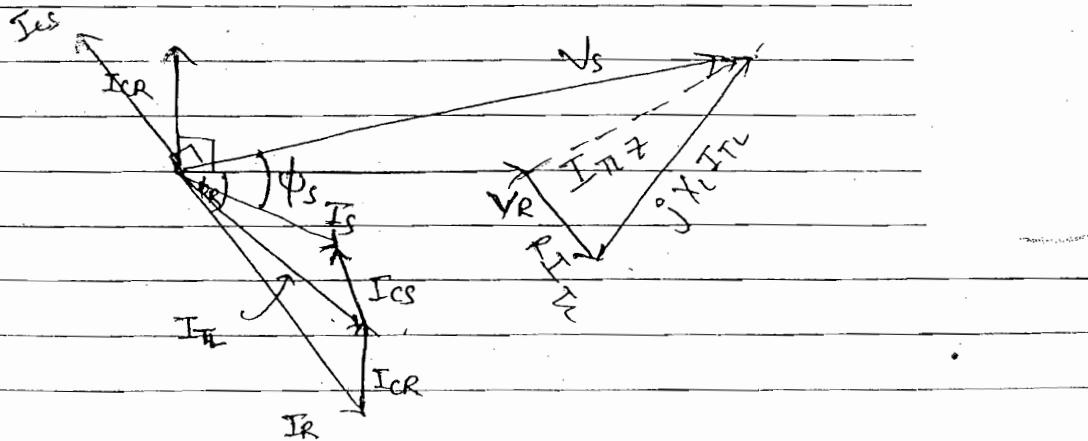
(8) $I_s = I_{CS} + I_{T_L}$

I_{CS} leads V_R by 90°

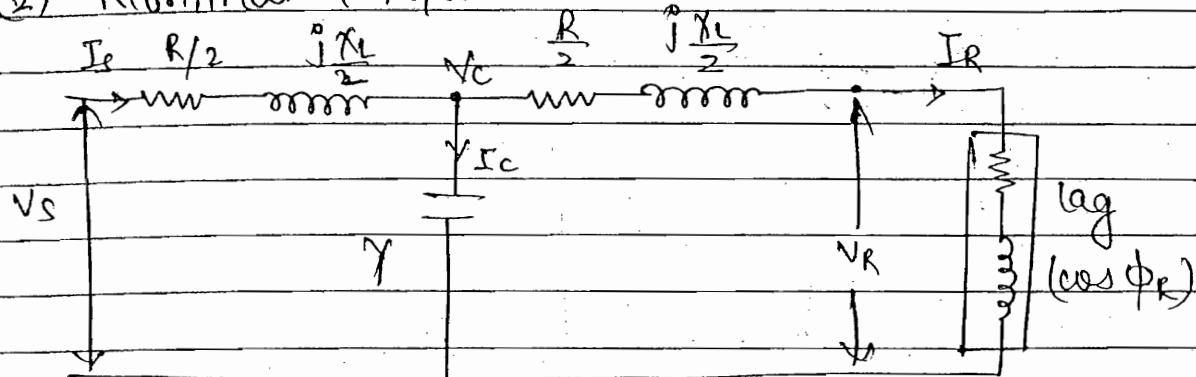


If the load current I_R and voltage is V_R lag by ϕ_R

PHASOR DIAGRAM



(2) Nominal T N/w/o:-



$$Z = R + jX_L \quad \gamma = j\omega C$$

Steps. (1) V_R as Ref.(2) I_R lags V_R by ϕ_R

$$(3) I_R \frac{Z}{2} = I_R \cdot \frac{R}{2} + j I_R \frac{X_L}{2}$$

$$(4) V_c = V_R + I_R \frac{Z}{2}$$

$$(5) I_c = V_c \gamma$$

$$(6) I_s = I_c + I_R$$

I_c leads V_c by 90°

$$(7) I_s \frac{Z}{2} = I_s \frac{R}{2} + j I_s \frac{X_L}{2}$$

$$(8) V_s = V_c + I_s \frac{Z}{2}$$

$$(9)$$

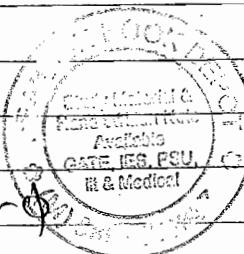
$$\begin{bmatrix} V_s \\ I_s \end{bmatrix} = \begin{bmatrix} \left(1 + \frac{\gamma Z}{2}\right) & \gamma \left(1 + \frac{\gamma Z}{4}\right) \\ \gamma & \left(1 + \frac{\gamma Z}{2}\right) \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix}$$

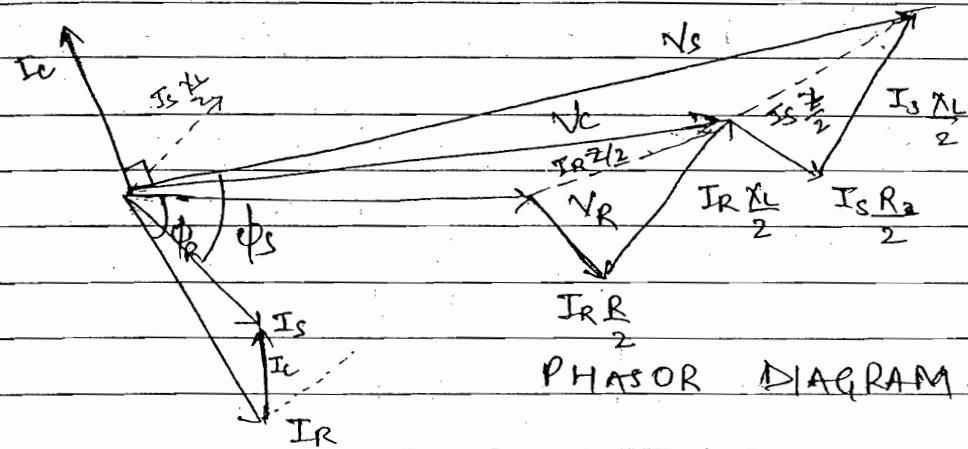
$$(1) \% V_{REG} = \frac{|V_s| - |V_R|}{|V_R|} \times 100 \quad \text{where } A = 1 + \frac{\gamma Z}{2}$$

$$(2) \% \eta = \frac{P_R}{P_R + P_L} \times 100$$

$$\text{where } P_L = \frac{R}{2} \left(I_R^2 + I_s^2 \right) \quad \text{for } 1-\phi$$

$$= \frac{3R}{2} \left[I_R^2 + I_s^2 \right] \quad \text{for } 3-\phi$$



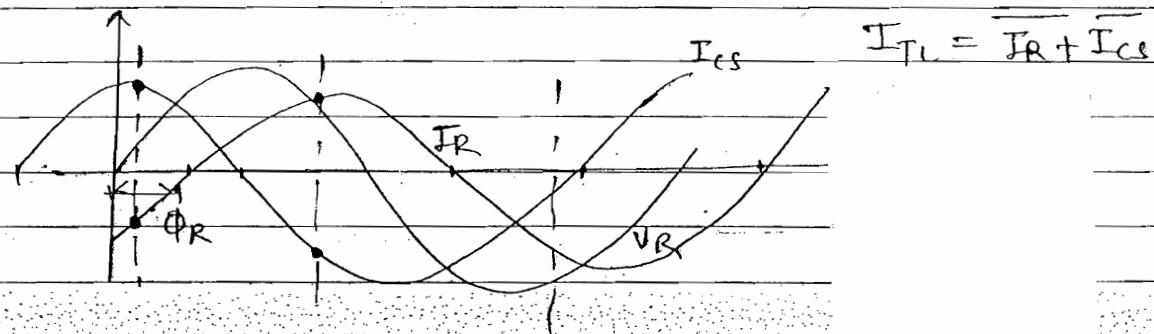


$$I_S = I_R + I_C = |I_R \angle -\phi_R + [I_C] \angle 90^\circ| \\ = I_R \cos \phi_R + j I_R \sin \phi_R + j I_C$$

$$I_S = I_R \cos \phi_R + j (I_C - I_R \sin \phi_R) \downarrow$$

$$|I_S| < |I_R|$$

$\left\{ \begin{array}{l} \text{Imaginary part} \\ \text{is } \downarrow \text{ so} \\ |I_S| \downarrow \end{array} \right.$



- Comparison Short R Medium Tr-line:

PARAMETER

SHORT LINE

MEDIUM LINE

I_S

$|I_S| = |I_R|$

$|I_S| < |I_R|$ due to I_C

P_L

More

Less "

η

less

More "

% V_{REG}

More

Less "

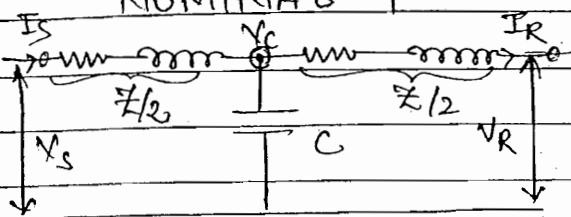
P_S

More

Less "

- Comparison b/w Nominal T and Nominal Δ Nwo.

NOMINAL T

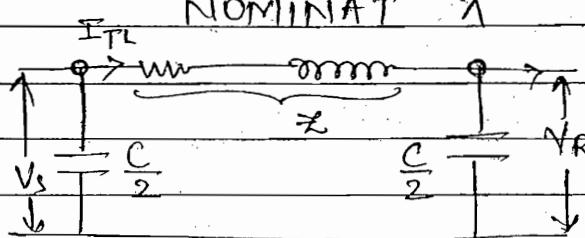


$$I_S = \frac{V_S - V_C}{Z/2}, I_R = \frac{V_C - V_R}{Z/2}$$

$$\text{Node } 3 \quad \text{Eqn} = 2$$

- No. of Nodes are 3, so that No. of Eqn are more

NOMINAL Δ



$$I_{TL} = \frac{V_S - V_R}{Z/2}$$

$$\text{Node } 2 \quad \text{Eqn} = 1$$

- No. of Nodes are only 2 so that No. of Eqn are less

- The external shunt capacitor can't be easily combined with the line capacitance.

- It is easily combine with the line capacitance.

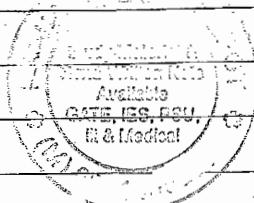
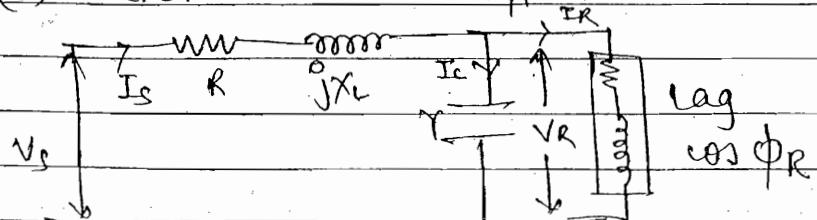
- The line capacitance is concentrated at the middle of the line.

- Line capacitance is distributed at both sending and receiving end.

- It is used for analysing the effect of capacitor at the middle of the line.

- It is used in the load flow analysis as an equivalent ck due to no. of eqn are less so that faster calculation is possible.

(3) End Condenser Nwo:



$$\begin{bmatrix} V_s \\ I_s \end{bmatrix} = \begin{bmatrix} (1 + YZ) & Z \\ Y & 1 \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix}$$

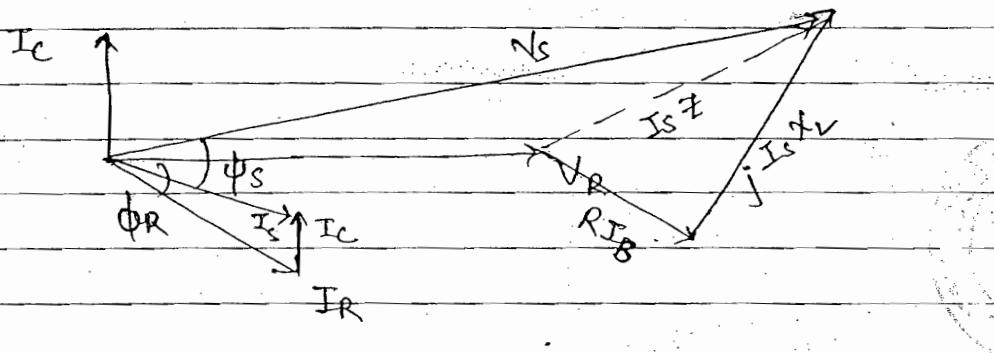
$$(1) \% \text{ VREG} = \left| \frac{V_s / A - V_R}{V_R} \right| \times 100$$

where $A = (1 + YZ)$

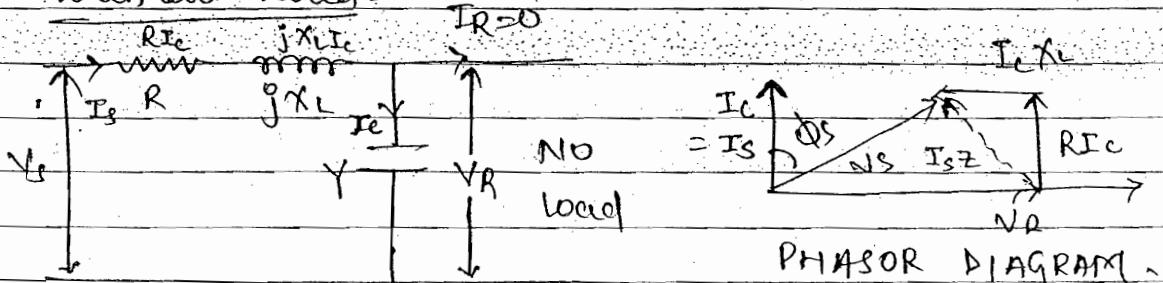
$$(2) \% \eta = \frac{P_L}{P_R + P_L} \times 100 \quad P_L = R I_s^2 \text{ for } 1-\phi$$

$$P_L = 3R I_s^2 \text{ for } 3-\phi$$

PHASOR DIAGRAM:-



With out load:-



Ferranti effect.

$|V_c| < |V_R|$

- Ferranti effect occurs in case of Medium and long Tr-line under No load or light load condition
- If the loading of line is more than surge impedance loading ($\sqrt{S} I_L$) than $|V_R| < |V_s|$ occurs

- If the loading of line is equal to SIL Then $V_R = V_s$ occurs.
- If the loading of line is less than SIL Then $V_R > V_s$ i.e. ferranti effect occurs. For compensation of this ferranti effect shunt reactor is connected at the load end. The value of shunt reactor $X_{sh} = \frac{B}{(1-A)}$
- The overhead T_r -line can be loaded more than SIL .
- In case of power cables, these should be operate less than SIL for safe operation of the power cable.

Increment of V_R (ΔV_R)

Diagram of a transmission line section with voltage V_s at the source end. A shunt load $\frac{1}{Cs}$ is connected between the line and ground. A shunt reactor V_R is connected across the line. The total voltage drop across the line is $V_R = V_s + V_o \cdot \omega^2 LC$, where $V_o = V_s + (\Delta V_R)$. The increment of V_R is given by $\Delta V_R = V_s \cdot \omega^2 LC$ (1).

Velocity of signal (v_s):-

$$L_1 = \frac{\mu_0 \mu_r}{2\pi} \ln \left(\frac{d}{r} \right) \text{ H/m}$$

Assume $r' \approx r$

$$L_1 = \frac{\mu_0 \mu_r}{2\pi} \ln \left(\frac{d}{r} \right) \text{ H/m}$$

$$C_1 = \frac{2\pi \epsilon_0 \epsilon_r}{\ln(d/r)} \text{ F/m}$$

$$L_1 C_1 = \mu_0 \mu_r \epsilon_0 \epsilon_r$$

$$V = \frac{l}{\sqrt{L_1 C_1}} = \frac{3 \times 10^8}{\sqrt{\mu_0 \mu_r \epsilon_0 \epsilon_r}} \text{ m/sec}$$

l = length of line

$$X_L = \text{Total inductive reactance} \\ = 2\pi f L_1 l$$

$$L_1 = \frac{X_L}{2\pi f l} \quad (3)$$

B = Total capacitive susceptance

$C_1 = \frac{B}{2\pi f l}$	— (4)
----------------------------	-------

Substitute (3), (4) in (2)

$\theta = \frac{2\pi f l}{\sqrt{B \cdot X_L}}$	— (5)
--	-------

Substitute (5) in eqn (1).

$$\Delta V_R = V_s \cos^2 \theta \rightarrow V_s (\alpha \pi f)^2 L_1 L C_1 l$$

$$\Delta V_R = 4\pi^2 f^2 l^2 L_1 C_1 V_s$$

$\Delta V_R = \frac{4\pi^2 f^2 l^2 V_s}{v^2} \rightarrow (6)$

Substitute (5) in (6)

$$\Delta V_R = V_s \cdot B \cdot X_L$$

$$V_R = V_s + \Delta V_R$$

(1) Ideal: $v = 3 \times 10^8 \text{ m/s} = 300 \text{ km/}\mu\text{s}$

(2) Practical: overhead line $v = 200 - 250 \text{ m/}\mu\text{s}$

(3) car (Fr $\gg 1$) $v = 40 - 50 \text{ m/}\mu\text{s}$

Q A 300 km long line is operating at NO load at a freq. of 50 Hz at $V_s = 2 \text{ p.u.}$ calculate receiving end voltage.

Solve $\Delta V_R = \frac{4 \times 3.14^2 \times 60^2 \times (300 \times 10^3)^2 \times 2}{(3 \times 10^8)^2} = 0.98$

$$V_R = V_s + \Delta V_R = 2.98 \text{ p.u.}$$

$$\text{Q.13} \quad f = 50\text{Hz} \quad X_L = 0.045 \quad B = 1.2 \text{ p.u} \\ v = 3 \times 10^5 \quad l = ?$$

$$V = \frac{2\pi f l}{\sqrt{B \cdot X_L}}$$

$$l = \frac{v \times \sqrt{B \cdot X_L}}{2\pi f} = \frac{3 \times 10^5 \times \sqrt{1.2 \times 0.045}}{2 \times 3.14 \times 50} \\ = 222.0 \text{ km} \quad \underline{\text{Ans}}$$

Q A ~~for~~ 220 kV Tr-line operating at $V_s = 220 \text{ kV}$ and $A = D = 0.9 \angle 0^\circ$, $B = 150 \angle 90^\circ \Omega$

$C = 0.4 \times 10^{-6} \text{ F}$, calculate

① N_R and I_c at no load

② shunt reactor required for maintaining $V_s = V_R$

Solution

$$N_s = AN_R + \sqrt{B I_R}$$

$$\textcircled{1} \quad V_R = \frac{V_s}{A} = \frac{220}{0.9 \angle 0^\circ} \quad I_s = \frac{V_R}{R + jX} = \frac{220}{0.4 \times 10^{-6} \times 244.4 \times 10^3}$$

$$= 244.4$$

$$\textcircled{2} \quad I_s > I_c = C N_R = 0.4 \times 10^{-6} \times 244.4 \times 10^3 \quad \sqrt{3}$$

$$= 0.056$$

$$\textcircled{3} \quad X_{sh} = \frac{B}{(1-A)} = \frac{150 \angle 90^\circ}{(1 - 0.9 \angle 0^\circ)}$$

~~Conventional
IEE
group~~

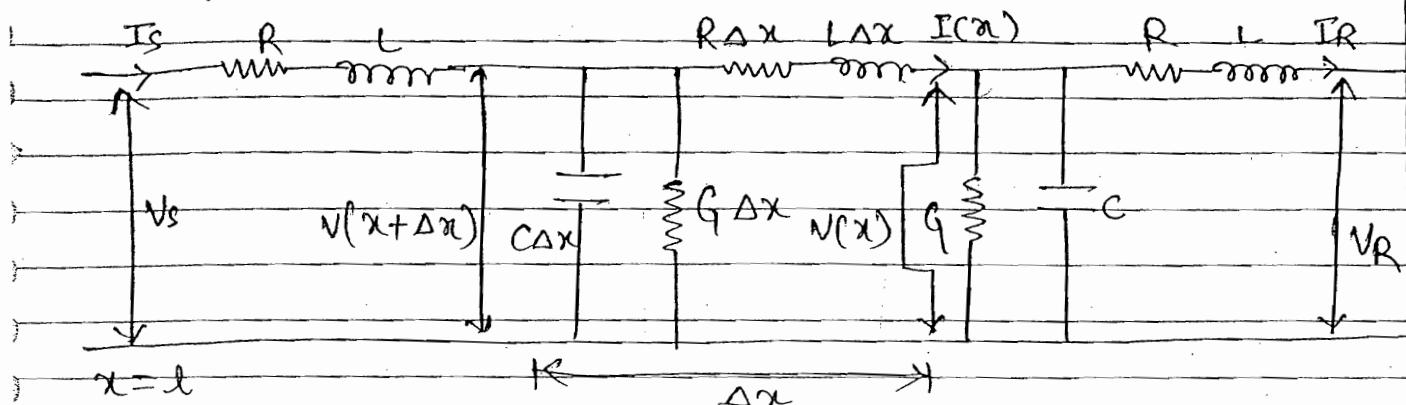
(3) long Tr-line :-

• ABCD parameter using long Tr-line Rigorous solution Method :-

(Repeat and extend on both sides)

Boundary Condition :- At $x=0 \quad V(x) = V_R$
 $I(x) = I_R$

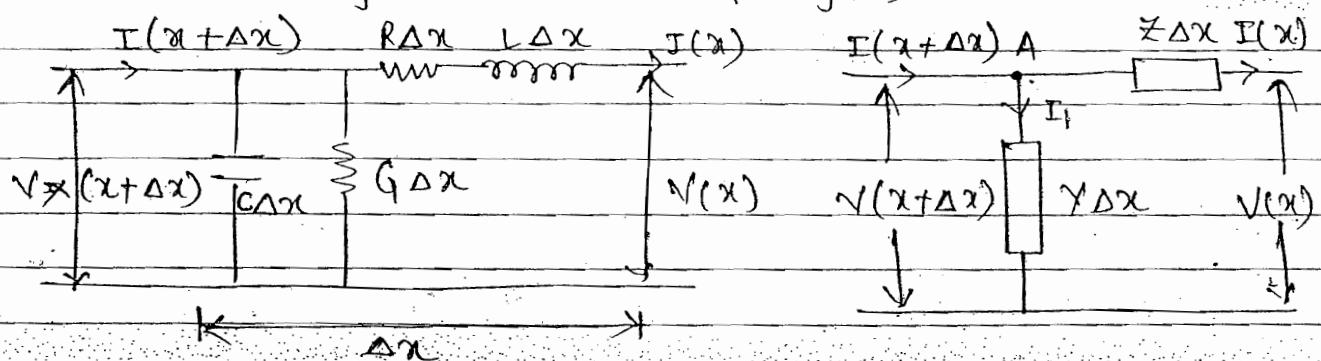
$$x = l, V(x) = V_s \quad I(x) = I_s$$



$$\text{Propagation Constant} = \gamma = \alpha + j\beta = \sqrt{Z \cdot Y}$$

$$\text{Characteristic Impedance} = Z_c = \sqrt{\frac{Z}{Y}}$$

$$Z = (R + j\omega L), \quad \gamma = (G + j\omega C)$$



$$\text{Apply KVL} \quad V(x+\Delta x) = V(x) + Z \Delta x \cdot I(x)$$

$$\lim_{\Delta x \rightarrow 0} \frac{V(x+\Delta x)}{\Delta x} = \lim_{\Delta x \rightarrow 0} Z I(x)$$

$$\frac{dV}{dx} = Z I(x)$$

Apply KCL at Node A.

$$I(x+\Delta x) = I_1 + I(x)$$

$$I(x+\Delta x) - I(x) = Y \Delta x \cdot V(x+\Delta x)$$

$$\lim_{\Delta x \rightarrow 0} \frac{I(x+\Delta x) - I(x)}{\Delta x} = \lim_{\Delta x \rightarrow 0} Y V(x+\Delta x)$$

$$\frac{dI}{dx} = Y V(x) \quad \text{--- (2)}$$

$$\text{from } (1) : \frac{d}{dx} \left[\frac{dv}{dx} \right] = \frac{d}{dx} [Z I(x)]$$

$$\frac{d^2 V}{dx^2} = Z \cdot \frac{d I(x)}{dx} = Z \gamma V(x)$$

$$\frac{d^2 V}{dx^2} = \gamma^2 V(x) \quad \dots (3)$$

$$\therefore \gamma = \sqrt{ZY}$$

Solution of (3)

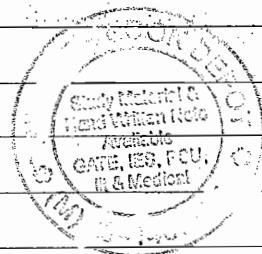
$$V(x) = A_1 e^{\gamma x} + A_2 e^{-\gamma x} \quad \dots (4)$$

$$\frac{d V(x)}{dx} = Z I(x) = \gamma [A_1 e^{\gamma x} - A_2 e^{-\gamma x}]$$

$$I(x) = \frac{\gamma}{Z} [A_1 e^{\gamma x} - A_2 e^{-\gamma x}]$$

$$I(x) = \frac{1}{ZC} [A_1 e^{\gamma x} - A_2 e^{-\gamma x}]$$

$$\therefore \frac{\gamma}{Z} = \frac{\sqrt{ZY}}{Z} = \sqrt{\frac{Y}{Z}} = \frac{1}{ZC}$$



Apply at $x=0$

$$V(0) = V_R, I(0) = I_R$$

in eqn (4) and (5)

$$V_R = A_1 + A_2 \quad \dots (5)$$

$$I_R = \frac{1}{ZC} (A_1 - A_2)$$

$$I_R Z_C = A_1 - A_2 \quad \dots (6)$$

By solving (5) & (6)

$$A_1 = \frac{V_R + I_R Z_C}{2} \quad \dots (8)$$

$$A_2 = \frac{V_R - I_R Z_C}{2} \quad \dots (9)$$

Substitute (8), (9) in (5)

$$I(x) = \frac{1}{ZC} \left[\frac{V_R + I_R Z_C}{2} e^{\gamma x} - \frac{1}{ZC} \left(\frac{V_R - I_R Z_C}{2} \right) e^{-\gamma x} \right] \quad \dots (10)$$

Substitute (8), (9) in (4)

$$V(x) = \left[\frac{V_R + I_R Z_C}{2} e^{\gamma x} + \frac{V_R - I_R Z_C}{2} e^{-\gamma x} \right] \quad \dots (11)$$

$$= V_R \left[\frac{e^{\gamma x} + e^{-\gamma x}}{2} \right] + I_R Z_C \left[\frac{e^{\gamma x} - e^{-\gamma x}}{2} \right]$$

$$= V_R \cosh \gamma x + I_R Z_C \sinh \gamma x$$

$$\text{Apply at } x=l, V(x) = V_s \text{ in (11)}$$

$$V_s = V_R \overbrace{\cosh \gamma x l}^A + I_R Z_C \overbrace{\sinh \gamma x l}^B \quad \dots (12)$$

$$= \frac{V_R}{Z_C} \left[\frac{e^{\gamma x} - e^{-\gamma x}}{2} \right] + I_R \left[\frac{e^{\gamma x} + e^{-\gamma x}}{2} \right]$$

$$= \frac{V_R}{Z_C} \sinh \gamma x + I_R \cosh \gamma x \quad \text{--- (14)}$$

Apply at $x = l$, $I(x) = I_s$ in (14).

$$\boxed{I_s = \frac{V_R \sinh \gamma l + I_R \cosh \gamma l}{Z_C}} \quad \text{--- (15)}$$

from (12) and (15)

$$\begin{bmatrix} V_s \\ I_s \end{bmatrix} = \begin{bmatrix} \cosh \gamma l & Z_C \sinh \gamma l \\ \sinh \gamma l & \cosh \gamma l \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix}$$

$$A = D = \cosh \gamma l, \quad AD - BC = 1$$

$$(1) \% V_{REQ} = \frac{|V_s/A| - |V_R|}{|V_R|} \times 100$$

$$\text{where } A = \cosh \gamma l$$

$$(2) \% \eta = \frac{P_R \times 100}{P_s} = \frac{|V_R I_R \cos \phi|}{|V_s I_s \cos \phi|} \times 100$$

$$P_i = P_s - P_R$$

① Equivalent π Network of long line :-

From long line:-

$$\begin{bmatrix} V_s \\ I_s \end{bmatrix} = \begin{bmatrix} \cosh \gamma l & Z_C \sinh \gamma l \\ \sinh \gamma l & \cosh \gamma l \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix} \quad \text{--- (1)}$$

From Nominal π Network:-

$$\begin{bmatrix} V_s \\ I_s \end{bmatrix} = \begin{bmatrix} \left(1 + \frac{YZ}{2}\right) & Z \\ Y \left(1 + \frac{YZ}{4}\right) & \left(1 + \frac{YZ}{2}\right) \end{bmatrix} \begin{bmatrix} V_R \\ I_R \end{bmatrix} \quad \text{--- (2)}$$

Comparing ① & ②

$$Z = Z_c \sinh(\gamma l)$$

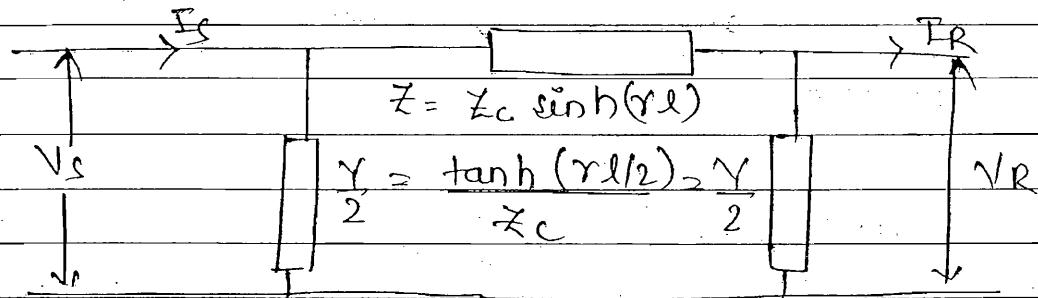
$$1 + \frac{Y}{2} Z = \cosh(\gamma l), \quad \frac{Y}{2} = \frac{\cosh(\gamma l) - 1}{Z}$$

$$\left| \frac{Y}{2} \right| = \frac{1 - 2 \sinh^2(\gamma l/2) - 1}{Z_c \sinh(\gamma l)}$$

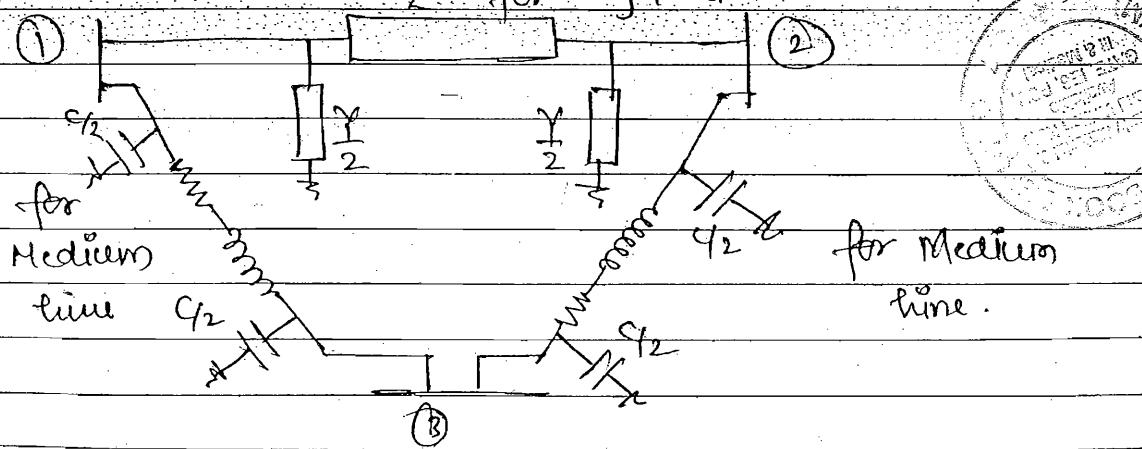
$$= \frac{2 \sinh^2(\gamma l/2)}{Z_c}$$

$$\therefore \frac{Y}{2} = \frac{2 \sinh(\gamma l)}{Z_c \cosh(\gamma l/2) \cdot \cosh(\gamma l/2)}$$

$$\left| \frac{Y}{2} \right| = \frac{\tanh(\gamma l/2)}{Z_c}$$



Z for long Tr-line



- for Representing the long Tr-line in the load, flow analysis equivalent π Nwo is used

Pg NO. 53.

Date _____

$$(41) \quad Q_C = P_1 (\tan \phi_1 - \tan \phi_2) \Rightarrow 2 = 4 [\tan \phi_1 - \tan \cos^{-1} 0.99] \\ \phi_1 = 36.86^\circ, \cos \phi_1 = 0.8 \text{ laggy.}$$

$$(42) \quad \begin{array}{c} \text{mmr} \\ | \\ N_S = 1.2 \end{array} \quad \begin{array}{c} VR \\ | \\ X_L = j0.2 \\ | \\ P_R = 0.3 \end{array} \quad VR = \frac{V_S}{2} + \sqrt{\frac{V_S^2 - 4X_L P_D}{4}} = 1.47 \text{ p.u.}$$

$$\Delta V = V_S - VR = 0.053 = 0.05 \text{ p.u.}$$

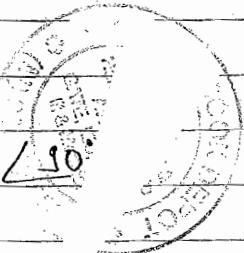
$$(43) \quad \frac{Q_2}{Q_1} = \left(\frac{V_2}{V_1} \right)^2 \cdot \left(\frac{f_1}{f_2} \right) \Rightarrow \frac{Q_2}{100} = \left(\frac{0.98 V_1}{V_1} \right)^2 \cdot \frac{f_1}{0.96 f_1} \\ \Rightarrow Q_2 = 100.04$$

$$(44) \quad \begin{array}{c} 11 \text{ KV} \\ | \\ 0.2 \text{ p.u.} \\ | \\ \text{mmr} \\ | \\ 100 \text{ MVA} \\ | \\ \text{Csh } j10.1 \end{array} \quad VR = 11 \text{ KV} \quad X_L = 0.5 \text{ p.u.} \\ 100 \text{ MW U.P.F.} \quad X_p.u = \frac{X_{12} (\text{MVA})_b}{(KV_b)^2} \\ P_R = \frac{V_S V_R}{X_L} \times \sin \delta \quad 0.2 = \frac{X_{12} \cdot (100)^2}{(11)^2} \\ 100 = \frac{11 \times 11}{0.242} \times \sin \delta \quad X_L = 0.242 \Omega \\ \sin \delta = 1.2 \quad \boxed{\delta = 11.53^\circ} \quad X_{12} = 0.242 \Omega$$

$$Q = \left| \frac{V_S V_R}{X_L} \cos \delta - \left| \frac{V_R^2}{X_L} \right| \right| \frac{0.11 \times 11 \cos(11.53)}{0.242} = 11 \\ = -10.1 \text{ MVAR.}$$

$$Q_C = -(-Q_R) = +10.1 \text{ MVAR.}$$

$$(45) \quad X_{12m} = \frac{B}{(1-A)} = \frac{200 \angle 90^\circ}{1-0.9} = 2000 \angle 90^\circ$$



$$(46) \quad \begin{array}{c} P_1 \quad P_2 \quad P_3 \quad P_4 \\ | \quad | \quad | \quad | \\ \text{mmr} \quad | \quad | \quad | \quad | \\ j0.1 \quad j0.15 \quad j0.1 \quad j0.1 \\ | \quad | \quad | \quad | \\ N_S = 1 \quad V_2 \quad V_3 \quad V_4 \\ | \quad | \quad | \quad | \\ \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \\ VR, \text{U.P.F.} \end{array} \quad \begin{array}{l} VR = 1 \quad V_3 = VR + j0.1X \\ = VR + j0.1 \\ V_2 = V_3 - j0.15X \\ = VR + j0.1 - j0.15 \\ = VR - j0.05 \\ = VR + j0.05 \end{array}$$

$\cancel{\text{maximum}}$

$$(51) Z = 8+j6, V = 400V \cos\phi_1 = 0.9 \text{ lagg.}$$

$$Q_C = P_1 (\tan\phi_1 - \tan\phi_2)$$

$$= \frac{3V^2}{Z} (\tan\phi_1 - \tan\phi_2)$$

$$= 3 \times \frac{400^2}{\sqrt{8^2+6^2}} \left(\tan\phi_1 - \tan\phi_2 \right) = \tan^{-1}(0.9)$$

$$= 10.2 \text{ kVAR}$$

Burst OFF

$$(53) C_{pn} > \frac{P_1 (\tan\phi_1 - \tan\phi_2)}{3 (2\pi f V_{pn})} = \frac{200 \times 10^3 [\tan^{-1}(0.8) - \tan^{-1}(0.9)]}{3 \times (2\pi \times 50 \times 1) \times 10^3}$$

cap. Bank

$$= 1.316 \mu F$$

$$(54) (a) P_s = \frac{|V_s V_R| \sin\delta}{X_L} = \frac{100^2}{5} \sin 30 = 1000 \text{ W}$$

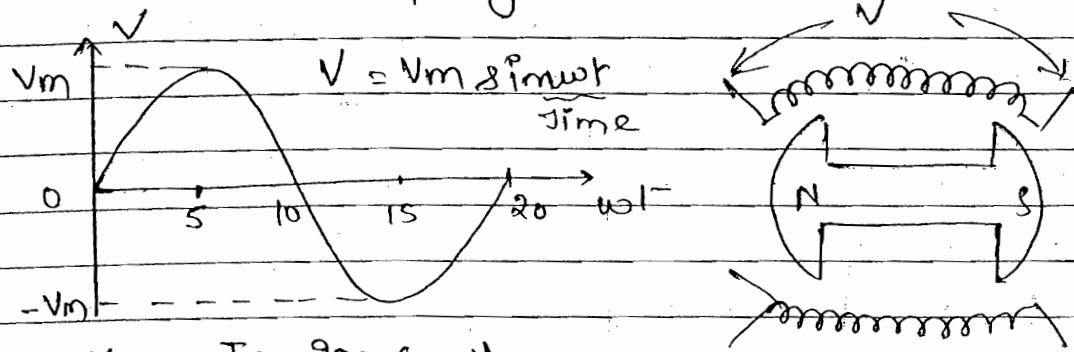
$$Q_s = \frac{|V_s V_R| \cos\delta - |V_R^2|}{X_L} \Rightarrow 268 \text{ VARs.}$$

12/7/2014.

Travelling Waves OR Transient In Tr-lines

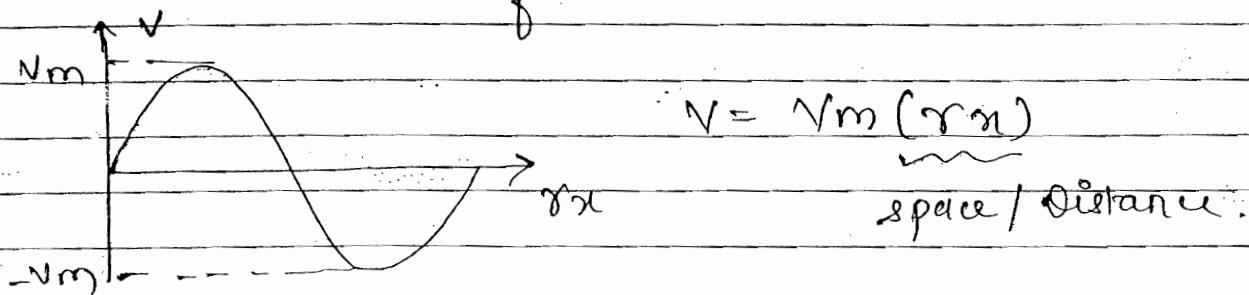
Power sys. may experiences abnormalities like short circuit, open circuit and lightning swells so that power flow within the line is disturbed produces transient in the sys. These transients causes over voltages, over currents so that damaging of electrical appliances and equipments like Transformer, Tr-line, generators, bus, etc. These equipment must be protected from this transient abnormalities. For designing and location of protecting equipment lightning arrestors, surge diverters, earth conductors, ground rods, counter poise, airing horns.

has to be properly located.

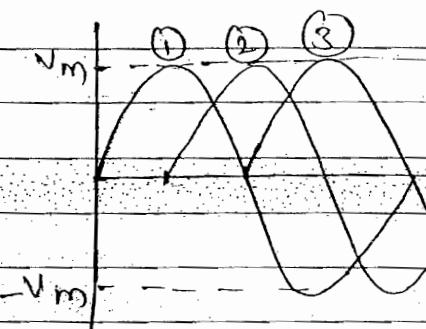


$$\leftarrow T = 20 \text{ ms} \rightarrow$$

$$f = 50 \text{ Hz} \quad T = \frac{1}{f} = 20 \text{ ms} = 1 \text{ cycle.}$$



$$V = Vm (\omega t - \rho x)$$



$$V = Vm \sin(\omega t - \rho x)$$

Travelling wave equation

	ρx	V
①	0	$Vm \sin \omega t$
②	90°	$-Vm \cos \omega t$
③	180°	$-Vm \sin \omega t$

$$V_{\text{res}} = Vm \sin(\omega t \pm \rho x)$$

$$\left| \frac{dV_m}{dx} \right| = + \gamma Vm \cos(\omega t \pm \rho x)$$

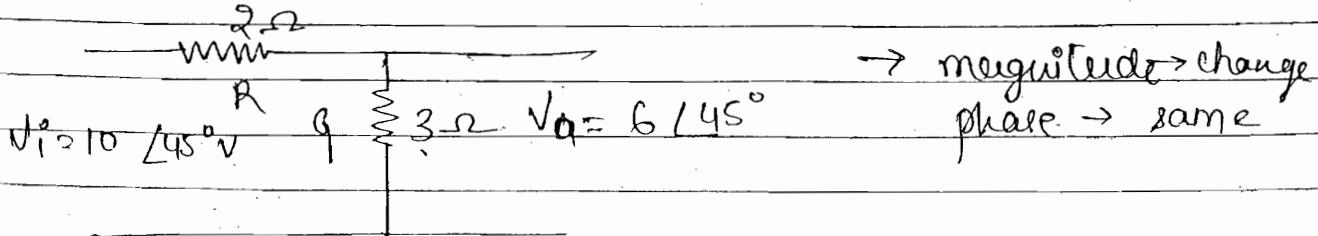
$$\left| \frac{d^2V_m}{dx^2} \right| = \gamma^2 Vm \sin(\omega t \pm \rho x)$$

$$\therefore Vm \sin(\omega t \pm \rho x) = V$$

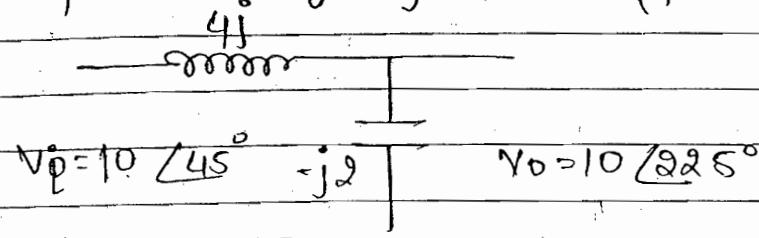
$$\frac{d^2V}{dx^2} = \gamma^2 V$$

eqn ③ in long Tr-line.

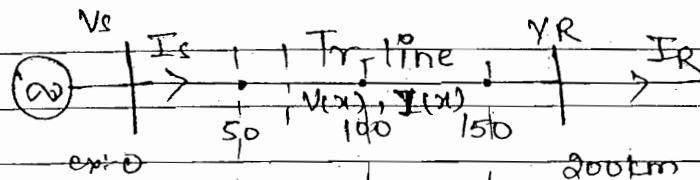
- $V = V_m \sin(\omega t + \varphi_2)$ represents Travelling wave equation, $+V$ indicates wave is travelling on +ve x axis, $-V$ indicates wave is travelling on -ve x axis
- During travelling or propagating voltage or current signal through the Tr-line due to R and G parameters attenuation of signal occurs. This is measured in dB represented as α
- Due to LC components phase shift of the signals occurs it is measured in degrees or radians represented as β
- This attenuation and phase shift occurs if the voltage and current signals are travelling through the Tr-line. This is also called propagation represented as γ which is a constant.
- The relation between voltage and currents are depending on the values of R, G, L, C which are depends on type of configuration used so that characteristic behaviour of current and voltages are depends on characteristic impedance of line which are represented by Z_c measured in ohm
- Attenuation Network (α):-



• Phase shifting N/w: - (B)



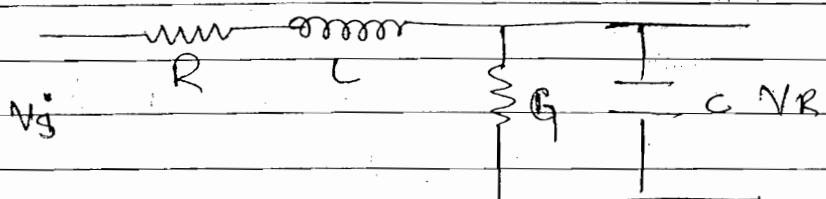
magnitude → same
phase → change.



at any point I_R
 π -line Z_C remain
same. Independent of
length of π -line.

$$Z_o = \sqrt{\frac{L}{C}} = \sqrt{\frac{L}{C}} = \sqrt{\frac{E}{C}}$$

• Combining both the N/L: -



losses occur
mainly due to
 R, G .

$$\gamma = \alpha + j\beta = \sqrt{Z} = \sqrt{(R+j\omega L)(L+j\omega C)}$$

$$Z_C = \frac{V(x)}{I(x)} = \frac{\sqrt{Z}}{\sqrt{Y}} = \sqrt{\frac{(R+j\omega L)}{(G+j\omega C)}}$$

• loss less / loss free line: - $G = R = 0$ \Rightarrow loss less line

• α, β, γ for loss less line: -

$$\gamma = \alpha + j\beta = \sqrt{(\alpha + j\omega L)(\alpha + j\omega C)}$$

$$\gamma = \alpha + j\beta = j\omega \sqrt{LC}$$

$$\boxed{\alpha = 0}$$

$$\boxed{\beta = \omega \sqrt{LC}}$$

$$\gamma = j\beta \quad \because \alpha = 0$$

$$\begin{aligned} j\omega \sqrt{LC} &= j\beta \\ \beta &= \omega \sqrt{LC} \end{aligned}$$

v = velocity Date: 3×10^8

$$\beta = 2\pi f \sqrt{L C_{1/2}}$$

$$\beta = \frac{2\pi f l}{v}$$

$$\beta = \frac{360 f l}{v}$$

radiane

Degrees

A, D for lossless line:

$$A = D = 1 + \frac{\gamma Z}{2}$$

For loss less line $Z = j\omega L$, $\gamma = j\omega c$

$$A = D = 1 + (j\omega L)(j\omega c)$$

$$= 1 - \frac{\omega^2 LC}{2}$$

$$A = D = 1 - \frac{\beta^2}{2}$$

$\beta \Rightarrow$ radian $\beta = \omega \sqrt{LC}$

Swage / loss less / loss free / Turned line / Flat line
 / Infinite line / Reasonant Impedance (Z_s)
 $[R = G = 0]$

$$Z_c = Z_s = \sqrt{\frac{L}{C}} = \sqrt{\frac{L \epsilon}{C_0 \epsilon}} = \sqrt{\frac{L}{C}}$$

$L = L_1 l$

$C = C_0 l$

- ① Overhead line: - $Z_s = 300 - 500 \Omega$
- ② cable : - $Z_s = 40 - 50 \Omega$
- Swage impedance is independent to length of the Tr-line
- Distortion-less line: - line independent to frequency
is called distortion less line.
It is practically used in communication line.

$$Z_c = \sqrt{\frac{R + j\omega L}{G + j\omega C}}$$

\hookrightarrow freq. depend
neglect them.

$$Z_D = \sqrt{\frac{R}{G}}$$

$Z_D \Rightarrow$ distortion less impedance

Q 600 km long Tr. line operating at 50Hz Calculate phase shift of signal at 300km.

Solution. $f = 50 \text{ Hz}$. $\beta = \frac{2\pi fl}{v} = \frac{360fl}{v}$

$$\beta = \frac{360 \times 50 \times 300 \times 10^3}{3 \times 10^8} = 18^\circ$$

$$= 18 \times \frac{\pi}{180} \text{ rad} = 0.314 \text{ rad}$$

Q A loss less Tr line has $\beta = 200 \angle 90^\circ$ $V_s = 400 \text{ kV}$

$l = 800 \text{ km}$ Find the voltage at 500km at ~~at far end length~~

at 800 km : calculate shunt reactor required for compensating feranti effect

Solution. $V_s = 400 \text{ kV}$ $\beta = 200 \angle 90^\circ$

$$C_A = \frac{\beta}{2\pi f l} = \frac{200 \angle 90^\circ}{2 \times 3.14 \times 50 \times 800}$$

① $l = 500 \text{ km}$ $\beta = \frac{2\pi f l}{v} = \frac{2 \times 3.14 \times 50 \times 500 \times 10^3}{3 \times 10^8} = 0.523 \text{ rad.}$

② $l = 800 \text{ km}$ $\beta = \frac{2 \times 3.14 \times 50 \times 800 \times 10^3}{3 \times 10^8} = 0.837 \text{ rad.}$

$$l = 500 \text{ km} \quad A = 1 - \frac{\beta^2}{2} = 1 - \frac{(0.523)^2}{2} = 0.863$$

$$X_{sh} = \frac{\beta}{(1-A)} = \frac{200 \angle 90^\circ}{1 - 0.863} = 1459.85 \angle 90^\circ$$

$$V_R = \frac{V_s}{A} = \frac{400}{0.863} = 463.49$$

$l = 800 \text{ km}$ $A = 1 - \frac{\beta^2}{2} = 1 - \frac{(0.837)^2}{2} = 0.649$

$$V_R = \frac{V_s}{A} = \frac{400}{0.649} = 616.33$$

$$X_{sh} = \frac{\beta}{1-A} = \frac{200 \angle 90^\circ}{1 - 0.649} = 569.19^\circ$$

Q) A 400 km long Tr-line has a surge impedance of 4 p.u if the length of line is reduced to 300 km then its surge impedance is 400 km.

$$\beta = \frac{2\pi f l}{v} \Rightarrow \frac{2\pi f l}{\lambda f}$$

$$\beta = \frac{2\pi f}{\lambda}$$

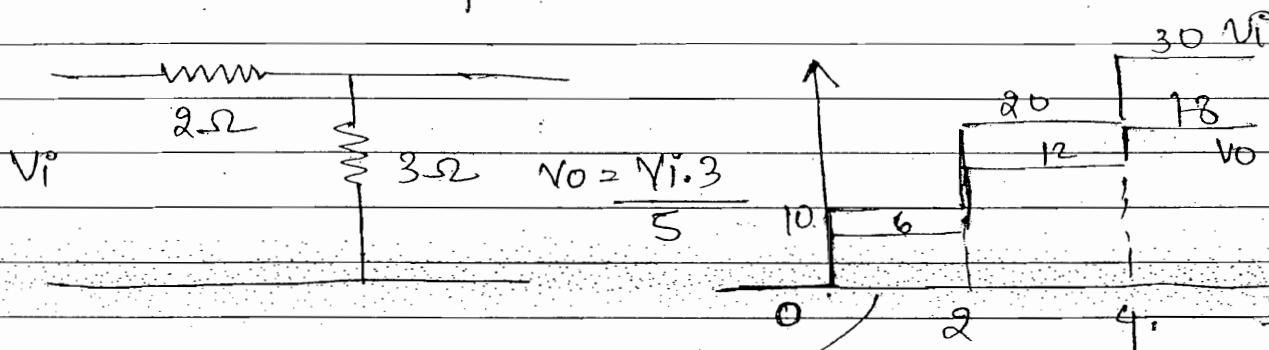
$$\left\{ \begin{array}{l} v = \lambda f \\ \lambda = \text{wave length} \end{array} \right.$$

$$\left\{ \begin{array}{l} v = \lambda f \\ \lambda = \text{wave length} \end{array} \right.$$

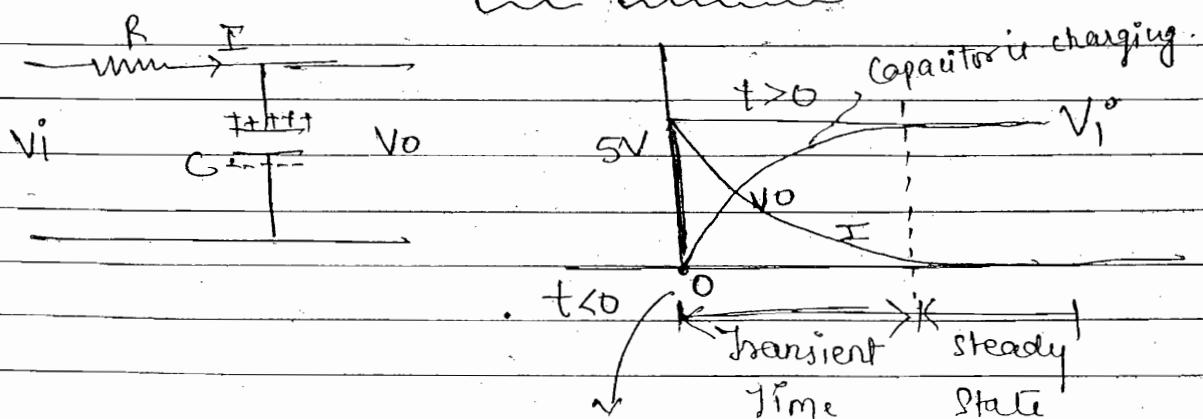
• Transient → when δ/ρ change (sudden) δ/ρ will not change sudden, it will cause delay in δ/ρ w.r.t δ/ρ called Transient.

↳ R, G → do not response to Transient.

↳ L, C → response to Transient.



No Transient Zero ORDER



$T=0$

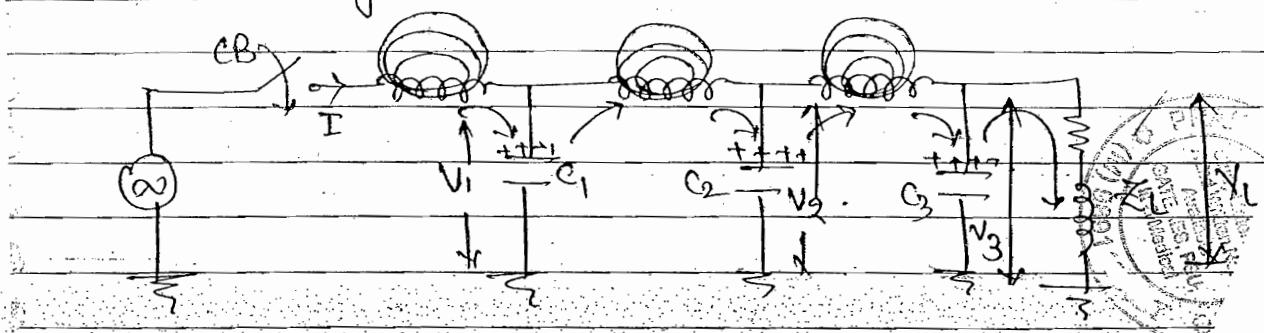
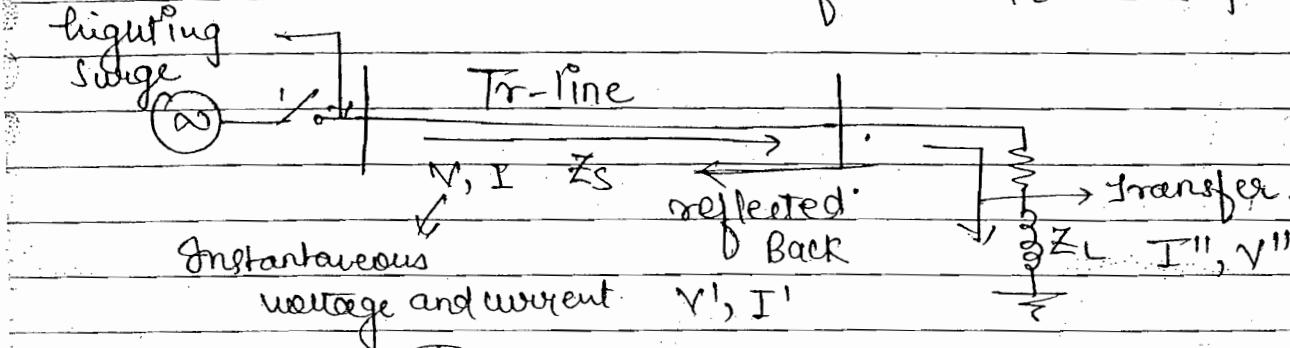
$$f = \frac{1}{T} = \frac{1}{0} = \infty$$

When $f = \infty$ $C \rightarrow \text{short. vi } \therefore V_o = 0$

- Energy storing device responsible for transient. Energy dissipating device don't responsible for \rightarrow

$$X_C = \frac{1}{2\pi f C} \quad DC \Rightarrow f=0 \Rightarrow X_C = \infty \text{ (Open)} \\ AC \Rightarrow f=\infty \Rightarrow X_C = 0 \text{ (short)}$$

$$X_L = 2\pi f L \quad DC \Rightarrow f=0 \Rightarrow X_L = 0 \text{ (short)} \\ AC \Rightarrow f=\infty \Rightarrow X_L = \infty \text{ (open)}$$



$$t=0, CB-\underline{\text{closed}} \quad t>0 \quad \frac{1}{2}LI^2 = \frac{1}{2}CV^2$$

- when CB closed at $t=0$

$$L=\text{Open} \quad C=\infty$$

$$V_1 = V_2 = V_3 = 0 \quad V_L = 0$$

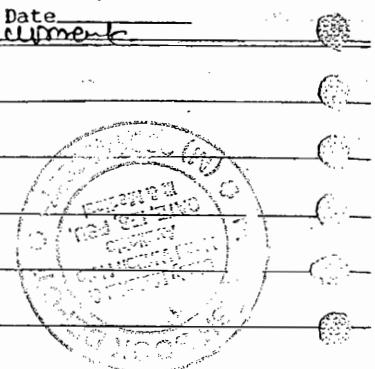
$$Z_C = \frac{V}{I} = \sqrt{\frac{L}{C}}$$

- When $t>0$ L short, $C=\text{Open}$, inductor store energy and charged the capacitor, current will start falling, charged capacitor gives it energy to next inductor, this inductor gives it energy to next capacitor and so on..., and finally reach to load. This way waves are travelling.

$$V = V' + V''$$

$$I = I' + I''$$

Transmission coefficient of current



$$T_V = \frac{V''}{V}, \quad T_I = \frac{I''}{I}$$

Transmission coefficient of voltage

$$R_V = \frac{V'}{V}, \quad R_I = \frac{I'}{I}$$

Reflected coeff. of voltage

Reflected coeff. of current.

Z_L

- | | | |
|--------------------|---------------------------|------------------------------------|
| (1) $Z_L \neq Z_s$ | (4) $Z_L = \infty$ | (7) $Z_L = \text{parallel lines.}$ |
| (2) $Z_L = Z_s$ | (5) $Z_L = L_s S$ | |
| (3) $Z_L = 0$ | (6) $Z_L = \frac{1}{G_s}$ | |

- Incident Wave:- The voltage and current signal travelling from source to the load through the Tr-line is called incident wave

$$I = \frac{V}{Z_s}$$

- Reflected Wave:- Voltage and current signals travelling from load to source are called reflected waves.

$$I' = -\frac{V'}{Z_s}$$

where Z_s = Source Impedance.

$$\text{of Tr-line.} = \sqrt{\frac{L}{C}}$$

- The voltage and current signals which are transmitting into the load are called transmitted or reflected wave

$$I'' = \frac{V''}{Z_L}$$

where Z_L = Load Impedance

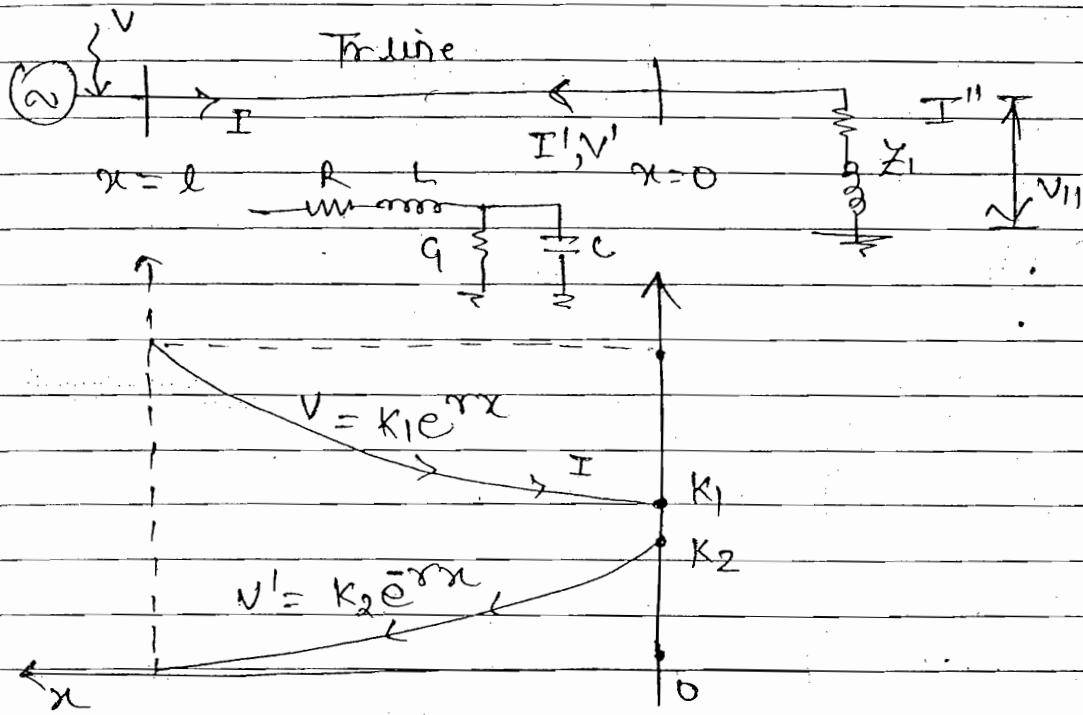
from long line eqn (10) & (13).

$$V(x) = \left(\frac{V_R + J_R Z_C}{2} \right) e^{jrx} + \left(\frac{V_R - J_R Z_C}{2} \right) e^{-jrx}$$

$$= k_1 e^{rx} + k_2 e^{-rx}$$

$$I(x) = \frac{1}{Z_c} \left(\frac{VR + IRZ_c}{2} \right) e^{rx} - \frac{1}{Z_c} \left(\frac{VR + IRZ_c}{2} \right) e^{-rx}$$

$$= \frac{1}{Z_c} k_1 e^{rx} - \frac{1}{Z_c} k_2 e^{-rx}$$



$$\textcircled{1} \quad I = \frac{V}{Z_c}, R, G \neq 0$$

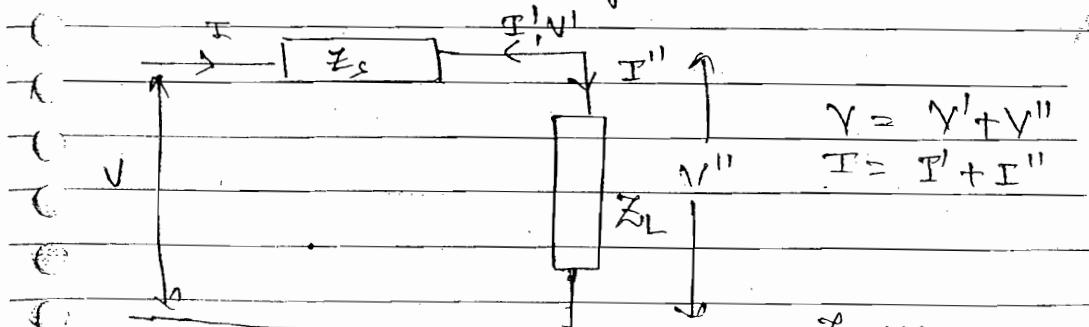
$$\textcircled{2} \quad I' = \frac{-V'}{Z_c}; R \neq 0, G \neq 0$$

$$= \frac{V}{Z_s}, R = G = 0$$

$$= \frac{-V'}{Z_s} \text{ if } G = R = 0$$

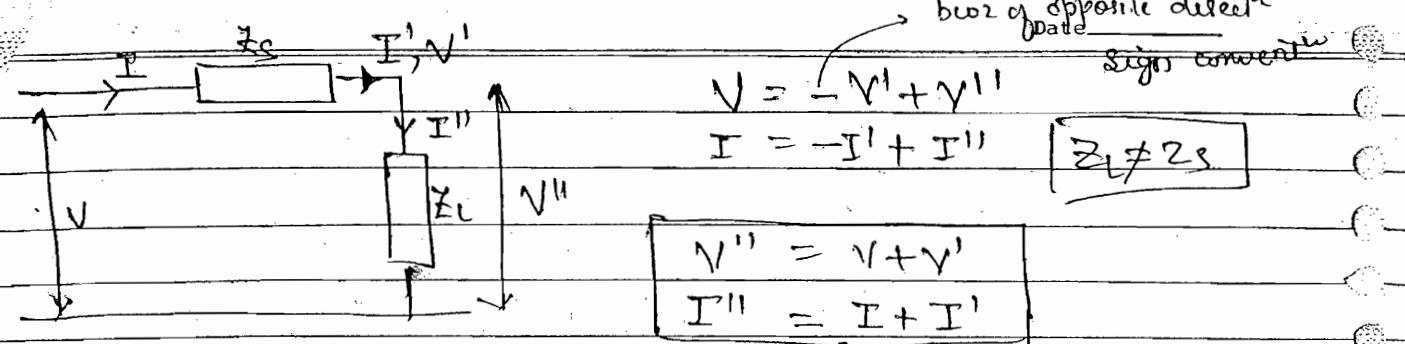
we get constant
straight line

$$\textcircled{3} \quad I'' = \frac{V''}{Z_L}$$



$Z_s \neq Z_L$ so reflectⁱⁿ.

In infinite lines \rightarrow No Reflect.



Coefficients:-

$$\text{Reflection coefficient of voltage} = R_V = \frac{V''}{V}$$

$$\text{Reflection Coefficient of Current} = R_I = \frac{I''}{I}$$

$$\text{Transmitted / Refracted Coefficient of Voltage} = T_V = \frac{V''}{V}$$

$$\text{Transmitted / Refracted Coefficient of Current} = T_I = \frac{I''}{I}$$

Relation Between Coefficients:-

$$(1) \quad V'' = V + V^I \Rightarrow \frac{V''}{V} = 1 + \frac{V^I}{V}$$
$$\boxed{T_V = 1 + R_V}$$

$$(2) \quad I'' = I + I^I \Rightarrow \frac{I''}{I} = 1 + \frac{I^I}{I}$$
$$\boxed{T_I = 1 + R_I}$$

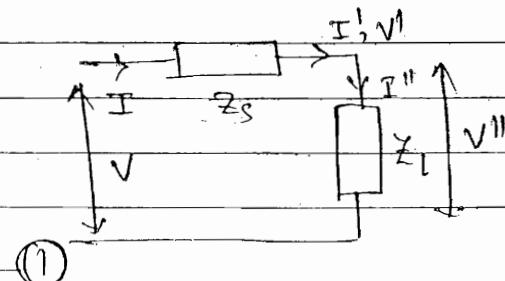
$$(3) \quad R_V = \frac{V''}{V} = -\frac{I^I Z_s}{I Z_s} \quad \boxed{R_V = -R_I}$$

$$(4) \quad T_I = \frac{I''}{I} = \frac{V''/Z_L}{V/Z_s} \quad \boxed{T_I = T_V \cdot \frac{Z_L}{Z_s}}$$

Case (1): $Z_L \neq Z_s$

$$V'' = V + V^I$$

$$\text{Ans} \quad V^I = V'' - V$$



$$I'' = I + I' \quad , \quad V'' = V - \frac{V'}{Z_L} - \frac{V'}{Z_S} \quad (2)$$

Substituti ① in eqn ② ..

$$\frac{V''}{Z_L} = \frac{V}{Z_S} - \frac{(V'' - V)}{Z_S}$$

$$\left[\frac{1+1}{Z_L Z_S} \right] V'' = \frac{2V}{Z_S}$$

$$T_V = \frac{V''}{V} = \frac{2Z_L}{Z_L + Z_S}$$

• By Using Relation: $R_V = T_V - 1$

$$R_V = \frac{Z_L - Z_S}{(Z_L + Z_S)} = \frac{V'}{V}$$

$$R_I = \frac{I'}{I} = -R_V$$

$$T_I = 1 + R_I = 1 - R_V$$

$$T_I = \frac{2Z_S}{(Z_L + Z_S)} = \frac{I''}{I}$$

• Conclusion ($Z_L \neq Z_S$)

$$T_V = \frac{V''}{V} = \frac{2Z_L}{(Z_L + Z_S)}$$

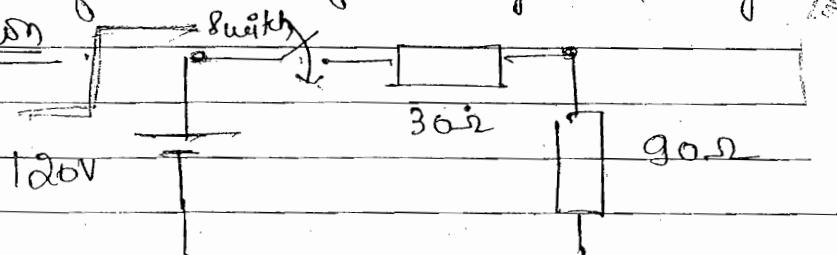
$$T_I = \frac{I''}{I} = \frac{2Z_S}{(Z_L + Z_S)}$$

$$R_V = \frac{V'}{V} = \frac{Z_L - Z_S}{Z_L + Z_S}$$

$$R_I = \frac{I'}{I} = -R_V$$

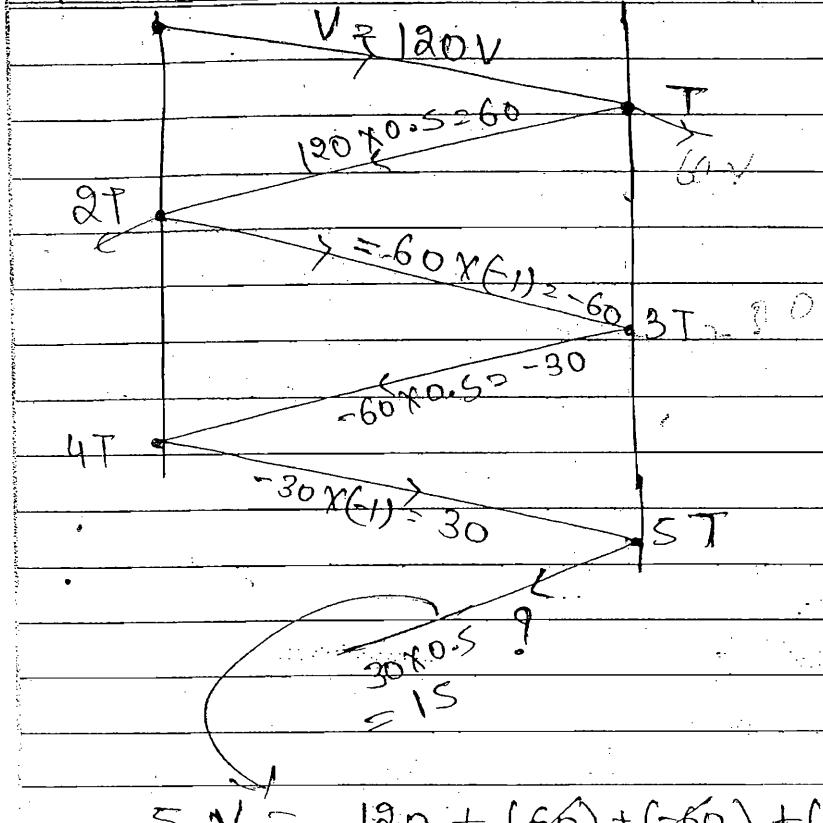
Q A dc voltage of 120V magnitude is applied to the line shown in fig. Calculate the voltage reflecting from the load end at the end of ST where T = Time of travel of the signal through the line.

Solution



$$RV_3 = -1$$

Laurie



$$RN_R \approx 0.5$$

load

Date _____

$$RN_R = \frac{Z_L - Z_S}{Z_L + Z_S}$$

$$= \frac{90 - 30}{90 + 30} \Rightarrow \frac{60}{120}$$

> 0.5

$$RV_s = \frac{Z_L - Z_S}{Z_L + 2s} > \frac{0 - 30}{0 + 30}$$

$$= -1$$

$$\frac{N'}{V} = R N_R \cdot \frac{N'_S R V_R V}{V}$$

$$N' = RV_s \cdot V$$

wad
hole.

$$N' = RV_s \cdot V$$

wad
hole.

$$\sum V = 120 + (60) + (-60) + (-30) + 30 + 15 \quad \text{source side}$$

$$= 135 \text{ V} \quad \text{Ans}$$

- Q A Tr. line has a surge impedance of 400Ω is terminated with a cable having surge impedance of 80Ω . If a lightning surge of 100 kV magnitude is travelling from the Tr. line towards the cable Calculate

- (1) All the coefficients
 - (2) Incident voltage and current
 - (3) Reflected voltage and current
 - (4) Transmitted voltage and current

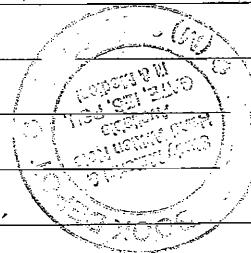
Sodium

$$\textcircled{1} \quad f_s = 400 \Omega \quad Z_L = 50 \Omega$$

$$RV = \frac{Z_L - Z_S}{Z_L + Z_S} = \frac{50 - 400}{50 + 400} = -35\%$$

$$= -0.77$$

$$R_I = -R_N \approx 0.77$$



100Ω 50Ω

$$T_V = \frac{2Z_L}{Z_L + Z_S} = 2 \times 50$$

$$= \frac{100}{50+400}$$

$$= 0.222$$

 $N = 100\text{ kV}$

$$T_T = \frac{2Z_S}{Z_L + Z_S} = 2 \times 400$$

$$= \frac{800}{50+400}$$

$$= 0.977$$

$$T_I = T_V \cdot Z_L = 0.22 \times \frac{50}{400}$$

$$= 0.0275$$

(2) $V = 100\text{ kV}$

$$I = \frac{100 \times 10^3}{400} = 250\text{ A}$$

$$(4) V'' = T_V \cdot V$$

$$= 0.22 \times 100 \times 10^3$$

(3) $V' = R_N \cdot N$

$$= (-0.977) \times 100$$

$$= -97.7 \text{ kV}$$

$$I' = -V' = \frac{-97.7 \times 10^3}{400}$$

$$= 23 \text{ kV}$$

$$I'' = \frac{V''}{Z_L}$$

$$= 23 \times 10^3$$

$$= 50$$

$$= 1940.25$$

$$= 460$$

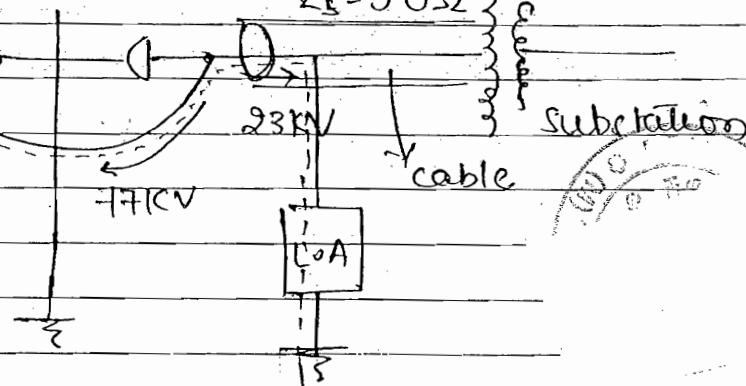
Application

100 kV lightning

$$Z_S = 400\Omega$$

Power x-mel

$$Z_L = 50\Omega$$

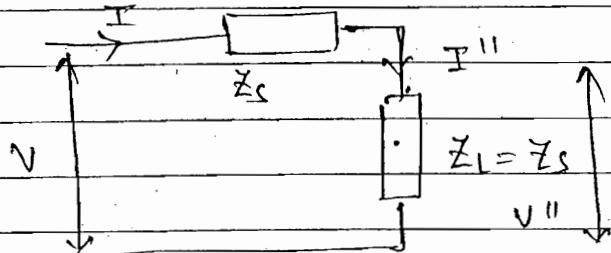


Advantages :- (1) $|V_{swage}| \downarrow$ (2) velocity \downarrow

(3) \leftarrow steepness \downarrow

→ In hilly areas where lightning occurs mostly, cables are used for reducing the magnitude of surge voltage so that rating of 10A. cas to be reduced, esp. 23KV through I_{1A} and 7KV is effected.

case 2 : $Z_L = Z_s$



$$T_V = \frac{V''}{V} = \frac{Z_s}{Z_s + Z_L}$$

$$T_V = \frac{V''}{V} = \frac{Z_s}{Z_s + Z_L} > 1$$

$$R_N = T_V - 1 = 1 - 1 = 0$$

$$R_I = -R_N = 0$$

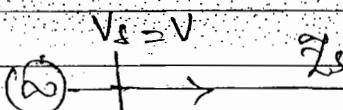
$$T_I = 1 + R_I = 1$$

Conclusion ($Z_L = Z_s$):-

$$\begin{cases} T_V = 1 \Rightarrow V'' = V \\ R_N = 0 \Rightarrow V' = 0 \end{cases}$$

$$\begin{cases} T_I = 1 \Rightarrow I'' = I \\ R_I = 0 \Rightarrow I' = 0 \end{cases}$$

∴ $V_s = V$



$$V_R = V''$$

$$I_R = I''$$

$$Z_L = Z_s$$

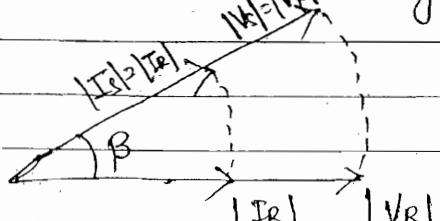
$$|V_R| = |V_3|$$

$$V_R$$

$$|I_R| = |I_3|$$

$$l$$

Flat voltage & current profile



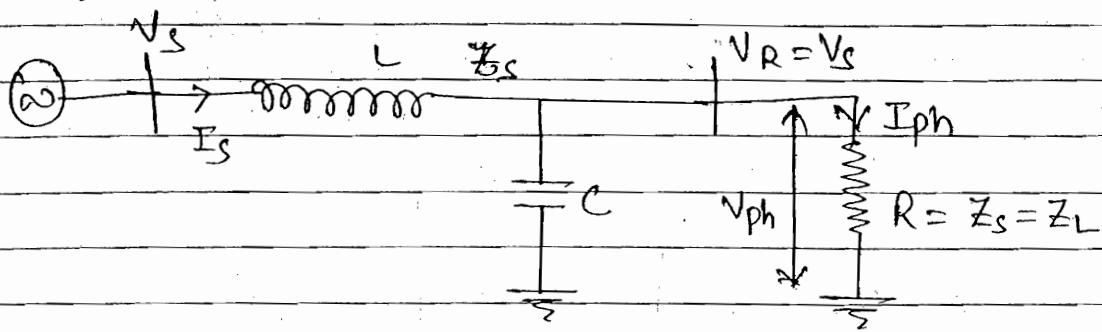
$$\beta = \omega \sqrt{LC}$$

I_s, V_s lead I_R, V_R by β But mag. remain same

Dear Sir
convert into active power, ($\phi = 0^\circ$)

Date _____

• Swage Impedance loading (SIL):-



3 φ active power supplied to pure R load [$\cos\phi = 1$] } = $3 V_{ph} I_{ph}$.

$$I_{ph} = \frac{V_{ph}}{R} = \frac{V_{ph}}{Z_s} = \frac{V_L}{\sqrt{3} Z_s};$$

$$|SIL| = P_{3\phi} = 3 \cdot \frac{V_L}{\sqrt{3}} \cdot \frac{V_L}{\sqrt{3} Z_s} = \frac{V_L^2}{Z_s} = \frac{V_s^2}{Z_s}$$

$$\boxed{SIL = \frac{V_s^2}{Z_s}}$$

where $Z_s = \sqrt{\frac{L}{C}}$, $L, C \Rightarrow$ phase values.

$V_s = V_L =$ line voltage

$$\boxed{SIL = \frac{V_s^2}{Z_s} = V_s^2 \sqrt{\frac{C}{L}}}$$

(1) $SIL \propto V_s^2$
(2) $SIL \propto \sqrt{C}$

(3) $SIL \propto \frac{1}{\sqrt{L}}$

- ① If $Z_L = Z_s$:- ① Transmission coefficient $T_V = T_I = 1$
② reflection coefficient $R_V = R_I = 0$

Hence line is called Infinite line

(3) $V_R = V_s =$, $I_R = I_s$ is maintained so that transmission line produce flat voltage and current profile.

(4) V_s lead V_R by β , I_s lead I_R by β

(5) V_s and I_s and V_R and I_R are in phase produced unity works as unity p.f. load.

(6) Inductance of line required reactive power is supplied by capacitance of the line. There is no need of reactive power from the source.

(7) Maximum three phase active power is transmitting through the transmission line which is called

$$S_{IL}^0 = \frac{V_s^2}{Z_s}$$

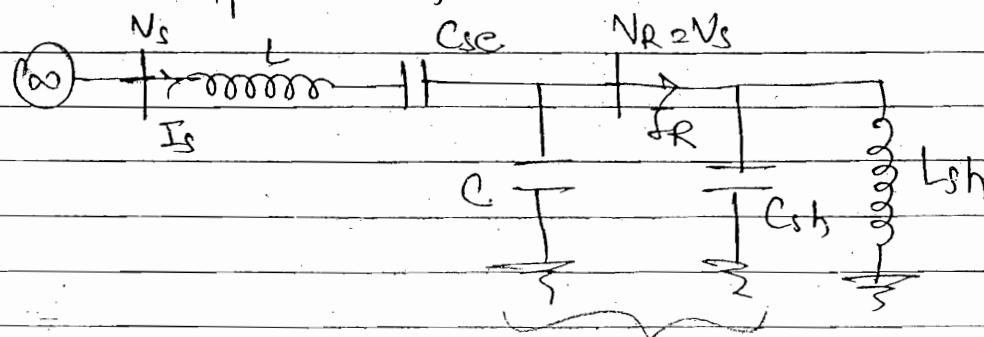
(8) Because of $V_s = V_R$ uniform voltage i.e. uniform insulation level for all the equipment like X-mere PT and CT can be maintained at both ends of line.

Effect of Compensation on S_{IL}^0

(1) Without Compensation:-

$$Z_{SI} = \sqrt{\frac{L}{C}} \quad (SIL)_1 = V_s^2 \sqrt{\frac{C}{L}}$$

(2) With Compensation



$$G_T = C + C_{sh} = C \left(1 + \frac{1}{C_{sh}} \right)$$

$$K_{se} = \frac{1}{\omega^2 L C_{se}} = \% \text{ or Degree of } C_{se}$$

$$K_{csh} = \frac{C_{sh}}{C} = \% \text{ or Degree of } C_{sh}$$

$$K_{Lsh} = \frac{1}{\omega^2 L_{sh} C} = \% \text{ or Degree of } L_{sh}$$

$(SIL)_c = SIL \text{ with compensation}$

$Z_{sc} = \text{Swege impedance with Compensation}$

$$Z_{sc} = Z_{s1} \sqrt{(1 - K_{se})} \\ \sqrt{(1 + K_{csh})(1 - K_{Lsh})}$$

$$(SIL)_c = \frac{V_s^2}{Z_{sc}} = (SIL)_{s1} \sqrt{\frac{(1 + K_{csh})(1 - K_{Lsh})}{(1 - K_{se})}}$$

Q A 3 ϕ Tr. Line Swage Impedance = 400Ω applied at 400 kV find

① Swage Imp. loadding without Compensation

② If the line is compensated with 30% of shunt capacitor. Calculate Z_s and SIL with compensation

Q ③ If the generator is connected at source end delivering 200 MW through these lines calculate load angle δ .

① without compensation ② with compensation

Solution (1)

Without Compensation :- $V_s = 400 \text{ kV}$ $Z_{s1} = 400 \Omega$

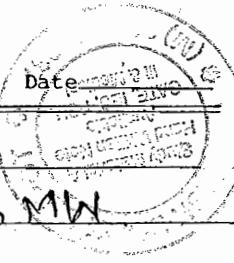
$$SIL = \frac{V_s^2}{Z_{s1}} = \frac{400^2}{400} = 400 \text{ MW}$$

(2) With Csh :- $K_{csh} = 30\% = 0.03$

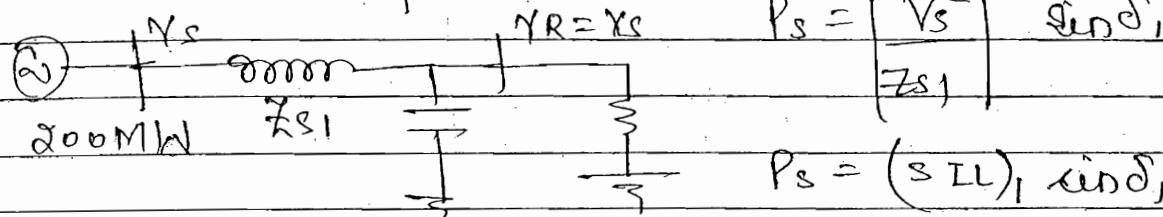
$$Z_{sc} = \frac{Z_{s1}}{\sqrt{1 + K_{csh}}} = \frac{400}{\sqrt{1 + 0.3}} = 350.8 \Omega$$

$$(SIL)_c = (SIL)_1 \cdot \sqrt{1 + K_{sh}}$$

$$= 400 \cdot \sqrt{1 + 0.3} = 456 \text{ MW}$$



(3) (a) without compensation

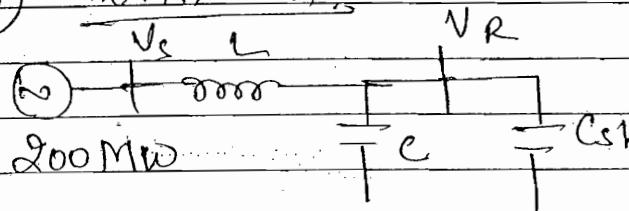


$$P_s = (SIL)_1 \sin \delta_1$$

$$200 = 400 \sin \delta_1$$

$$\delta_1 = 30^\circ$$

(b) with Csh :-

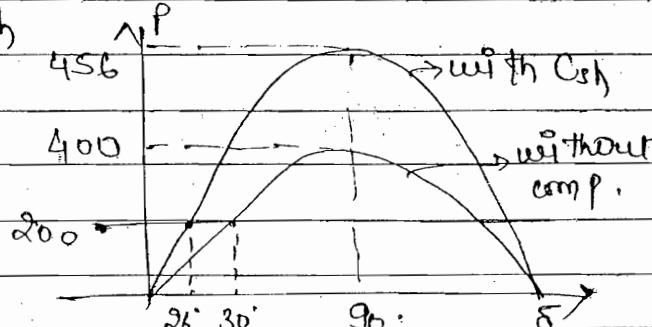


$$P_s > (SIL)_c \sin \delta_2$$

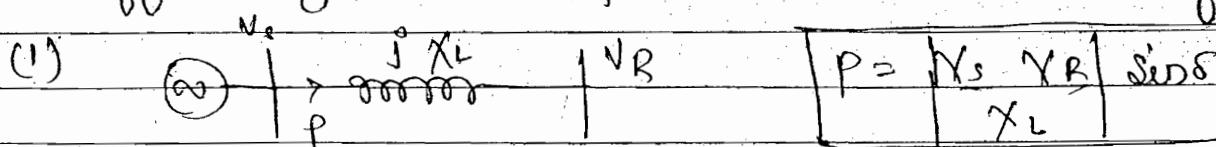
$$200 = 456 \cdot \sin \delta_2$$

$$\delta_2 = 26^\circ < \delta_1$$

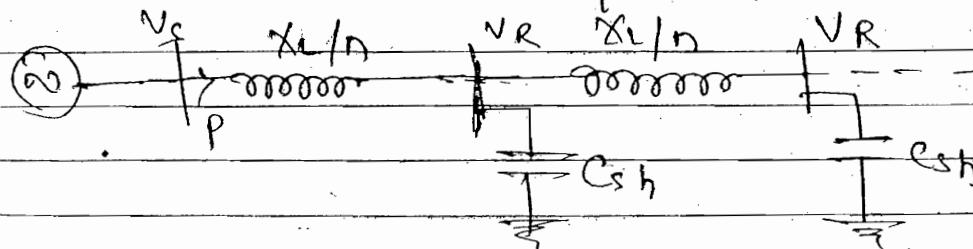
stability ↑



• Effect of Csh Compensation in n Section of line



(2) line divided in n-equal sections



$$P = \left| \frac{V_s V_R}{\left(\frac{jX_L}{n} \right)} \right| \sin \left(\frac{\delta}{n} \right) = \left| \frac{n V_s V_R}{jX_L} \right| \sin \left(\frac{\delta}{n} \right)$$

$$\text{If } V_s = V_R \Rightarrow P = \frac{\eta V_s^2}{X_L} \sin \delta$$

Max (or) Ideal or steady state Power :-

$$P_{\max} = \frac{\eta V_s V_R}{X_L}$$

$$\text{If } V_R = V_s \quad P_{\max} = \frac{\eta V_s^2}{X_L}$$

Pg No. 54.

$$\text{Q. 50} \quad X_L = 0.4 \quad N_{\text{indpt}} = 0.96$$

$$P = \frac{\eta V_s^2}{X_L} = \frac{\eta \times 1000}{0.4 \times 0.2} \quad P_{\max} = 4.8 \text{ p.u.}$$

$$\text{Q. 47} \quad (SIC)_c = \frac{(SIL)_i}{\sqrt{1 - k_{se}}} = \frac{2280}{\sqrt{1 - 0.3}} = 2725 \text{ MW.}$$

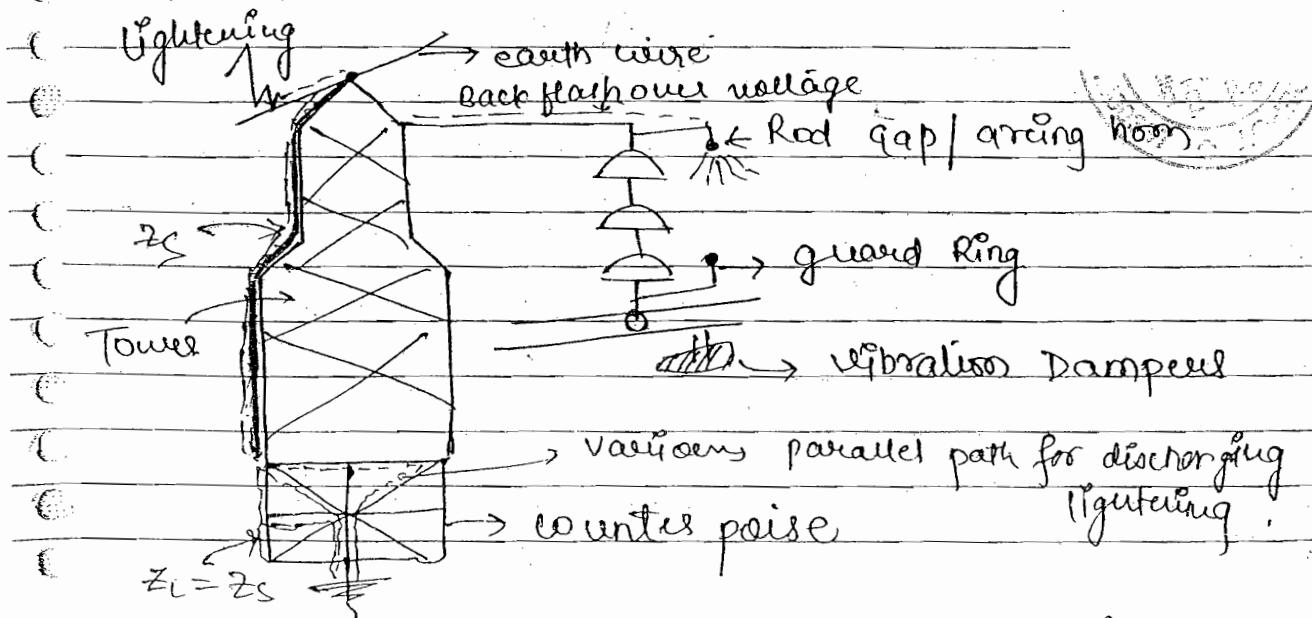
$$\text{Q. 48} \quad SIL = \frac{V_s^2}{\sqrt{L}} = \frac{800^2}{\sqrt{1.1 \times 10^{-3}}} = 2085 \text{ MW}$$

$$\text{Pg. No. 41, (33)} \quad Z_s = 250 \Omega \quad V_s = 400 \text{ kV} \quad \left. \begin{array}{l} 400 \text{ kV} \\ 10 \text{ KA} \end{array} \right\}$$

$$V = 10 \times 250 = 2500 \text{ kV Ans.}$$

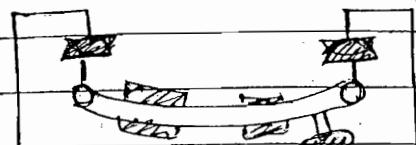
(36) (d) 1, 2 and 3

$$\text{Pg. No. 51} \quad \omega = 2\pi f l = \frac{1}{J.B. \cdot X_L \cdot \sqrt{L C}} = \frac{1}{0.201 \times 10^{-6} \times 196.2 \times 10^{-12}} = 159.24 \text{ rad/s.}$$



we have to maintain $Z_L = \infty$ for no reflection.

- As the depth $\uparrow Z \downarrow$ so use earth rod
- guard ring \rightarrow for improving η , uniform voltage can maintain



When snow will

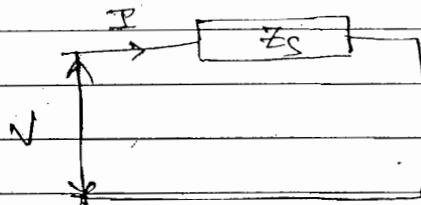
accumulated over the conductor

V_D or stock bridge which causes vibration

because of non-uniform accumulatn of snow. So we use vibration damper for reducing the vibratn.

- For protecting insulating disc from flash over voltage zinc horn are used which discharge the arc in air. And not pass to next one.

case 3 :- $Z_L = 0$



$$T_V = \frac{2Z_L}{Z_L + Z_S} = \frac{2(0)}{0 + Z_S} = 0$$

$$R_V = T_V - 1 = 0 - 1 = -1$$

$$R_I = -R_V = +1$$

$$T_I = 1 + R_I = 1 + 1 = 2$$

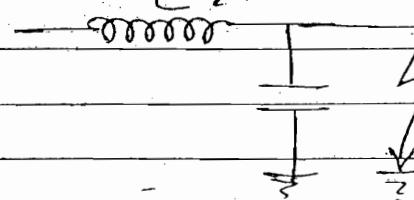
$$T_V = Q \Rightarrow V'' = 20$$

$$T_I = Q \Rightarrow I'' = 2$$

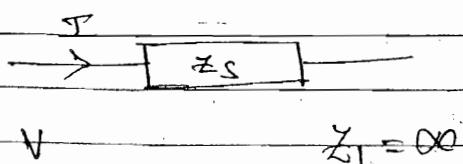
$$R_V = -1 \Rightarrow V' = -V$$

$$R_I = 1 \Rightarrow I' = I$$

\rightarrow Inductor is dominating



case 4 :- $Z_L = \infty$



$$T_V = \frac{2Z_L}{Z_L + Z_S} = \frac{2}{\infty + Z_S} = \frac{2}{\infty}$$

$$= \frac{2}{1+0}$$

$$= 2$$

$$R_N = T_N - 1 = 2 - 1 = 1$$

$$T_I = 1 + R_I = 1 - 1$$

$$R_I = -R_N = -1$$

$$= 0$$

$$T_N = 2 \Rightarrow V'' = 2V, T_I = 0 \Rightarrow I'' = 0$$

$$R_N = 1 \Rightarrow V' = V, R_I = -1 \Rightarrow I' = -I$$

$$C \parallel Z_L$$

capacitor is dominating

- Counter pole is used at the bottom of the tower for discharging of lightning surge. It is containing parallel paths for effective discharging of lightning surge.

- In place of counter pole Ground Rods can also be used which has thinner in diameter and higher length and used because earth resistance reduces as the depth of the earth increases.

- Earth Arcing horn are used for protecting the insulating disc from the Back flash over voltage produce due to lightning surge.

- Guard Ring is used for maintaining uniform voltage in the disc so that stringency is ↑

- Vibration dampers are used for protecting the reducing the vibrations only conductors which are produce due to non-uniform ice loading

- When $Z_L = 0$ Tr-line behaves as highly lagging N/w demanding for the lagging VAR's

- When $Z_L = \infty$ Tr-line behaves as highly leading N/w demand causes the receiving voltage to ↑

If $\underline{Z_0 = Z_L = Z_s}$ Tr-line has unity power factor.

Case 5 $Z_L = L_1 S$:

Assume Step range

$$V(s) = V_s$$

$$V''(s) = \frac{2Z_L \cdot V(s)}{Z_L + Z_s}$$

$$= \frac{2L_1 S}{(L_1 S + Z_s)} \cdot V$$

$$V''(s) = \frac{2V_K}{K_1 \left[s + \frac{Z_s}{L_1} \right]}$$

$$V''(t) = L^{-1} [V''(s)]$$

$$= L^{-1} \left[\frac{2V}{s + \frac{Z_s}{L_1}} \right]$$

$$Z_s = \text{Surge Imp. of line} = \sqrt{L_1 C}$$

$$V''(t) = 2V e^{-\frac{Z_s t}{L_1}}$$

L_1 \rightarrow load inductance

- (1) at $t = T_1 = 0$ \Rightarrow instant at which step range surge touching $Z_L = L_1 S$

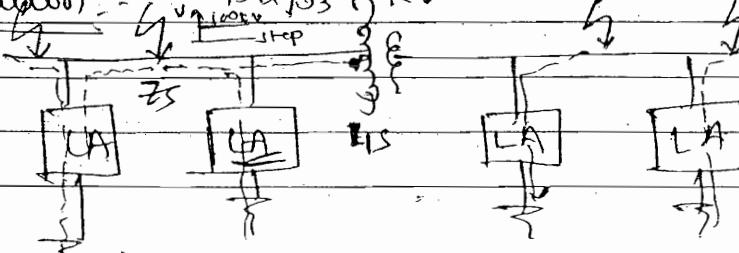
$$V''(t) = 2V e^{-0} = 2V$$

- (2) at $t = \infty$

$$V''(t) = 2V e^{-\infty} = 0$$

$$2V$$

Application: - 132/33 KV



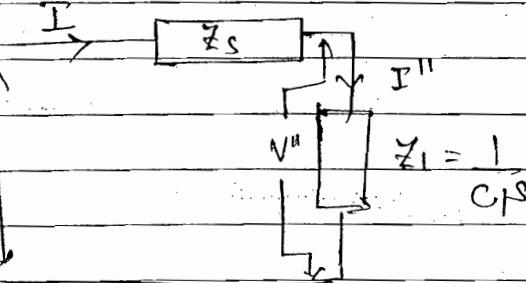
$$2V$$

- When L.A is not present and lightning of 100kV surge is occurs, it will hit the x-mel wdg. x-mel has inductor behavior as load of L.S. (Voltage will rise up) x-mel has insulation protect upto 132 kV + 10%, and the surge is of $2 \times 100 \text{ kV} = 200 \text{ kV}$, damage x-mel. so we kept LA on both side of x-mel.

Case 6:- $Z_L = \frac{1}{C_1 s}$

Assume step surge

$$V(s) = V/s$$



$$\begin{aligned} V''(s) &= 2Z_L \cdot V(s) \\ &= 2 \frac{1}{C_1 s} \cdot V \\ &= \frac{2}{C_1 s} V \end{aligned}$$

Step surge

$$V''(s) = 2V$$

$$V''(t) = [s(1 + sC_1 Z_s)]^{-1}$$

$$t = T_1 = 0$$

$$= [s(1 + sC_1 Z_s)]^{-1}$$

$$= \frac{s}{s + sC_1 Z_s}$$

Time constant $T = C_1 Z_s$

$$Z_s = \text{Surge Imp. of line} = \sqrt{\frac{L}{C}}$$

C_1 = Load Capacitance.

$$V''(t) = 2V [1 - e^{-t/T}]$$

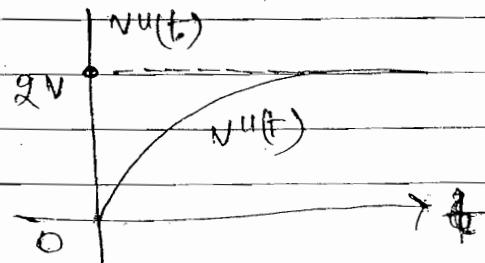
① At $t = T_1 = 0 \Rightarrow$ instant at which step surge reaching

$$Z_L = 1/C_1 s$$

$$V''(t) = 2V [1 - e^0] = 0$$

② At $t = \infty$

$$V''(t) = 2V [1 - e^{-\infty}] = 2V$$



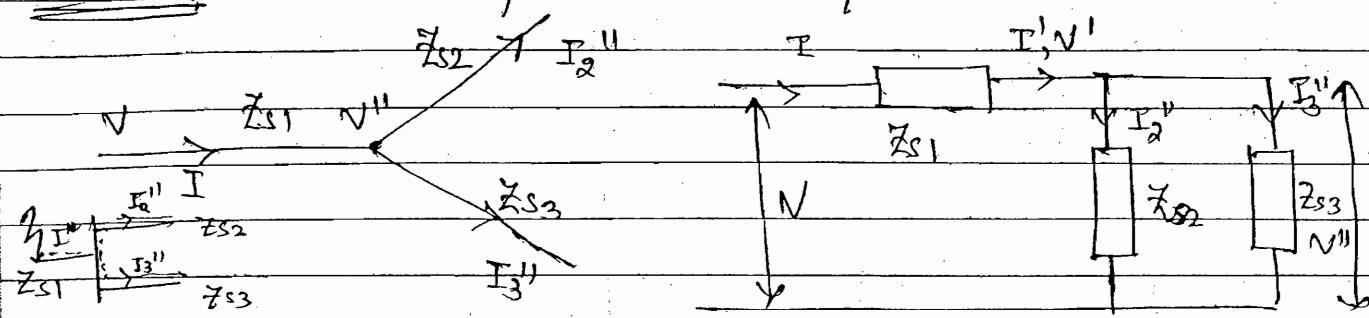
* No protecting device used.

because $V > 0$ at $t = 0$

for
Conventional
AMP

Date _____

Case 7.8- $Z_L = \text{parallel lines} / T \text{ Junction!}$



For parallel voltage is equal.

$$N'' = V + V'$$

$$V' = V'' - V \quad \text{---(1)}$$

$$I'' = I_2'' + I_3'' = I + I'$$

$$\frac{V'' + V'}{Z_{S2} Z_{S3}} = \frac{V}{Z_{S1}} \quad \text{---(2)}$$

Substitute (1) in (2).

$$V'' \left[\frac{1}{Z_{S2}} + \frac{1}{Z_{S3}} \right] = V - V'' - V$$

$$V'' \left[\frac{1}{Z_{S1}} + \frac{1}{Z_{S2}} + \frac{1}{Z_{S3}} \right] = \frac{2V}{Z_{S1}}$$

$$T_N = \frac{V''}{V} = \frac{2/Z_{S1}}{\left(\frac{1}{Z_{S1}} + \frac{1}{Z_{S2}} + \frac{1}{Z_{S3}} \right)}$$

$$R_V = \frac{V'}{V} = T_V - 1, \quad R_P = \frac{I'}{I} = -R_V$$

$$T_{I_2} = \frac{I_2''}{I} = \frac{V''/Z_{S2}}{V/Z_{S1}}, \quad T_{I_3} = \frac{I_3''}{I} = \frac{V''/Z_{S3}}{V/Z_{S1}}$$

$$= T_V \frac{Z_{S1}}{Z_{S2}}$$

$$= T_V \cdot \frac{Z_{S1}}{Z_{S3}}$$

Page No. 45 Q. 9

$$T_V = \frac{V''}{V} = \frac{2/Z_{S1}}{\left(\frac{1}{Z_{S1}} + \frac{1}{Z_{S2}} + \frac{1}{Z_{S3}} \right)}$$

$$Z_{S1} = 600$$

$$V = 100kV$$

$$I_2'' = \frac{V''}{Z_{S2}} = 200$$

$$V'' = 42.1kV$$

$$Z_{S3} = 800$$

$$I_3'' = \frac{V''}{Z_{S3}} = \frac{42.1kV}{800} = 0.210kA$$

$$I_2'' = \frac{N''}{Z_{S3}} = \frac{42.11 \text{ kV}}{800} = 52.5 \text{ A}$$

Layer MU 41 (34) $N = 20 \text{ kV}$ $L = ?$

$$L_1 = 0.4 \times 10^{-3}$$

$$C_1 = 0.5 \times 10^{-6}$$

cable

$$Z_{S1} = \sqrt{\frac{L_1}{C_1}}$$

$$= 28.28$$

$$N'' = \alpha \times 20 = 33.93 \text{ kV}$$

$$28.28 \left[\frac{1}{28.28} + \frac{1}{316.2} + \frac{1}{316.2} \right]$$

(32)

$$Z_L = \infty$$

$$N' = V = 1000$$

(c) $1000 \text{ kV}/\mu\text{s}$

200 N

100 kN

1

2

10

t

1

2

3

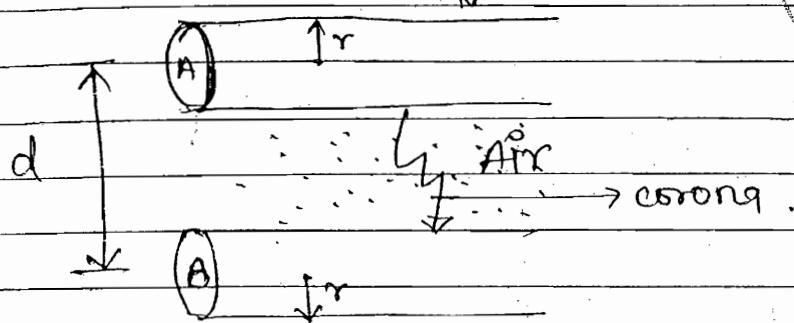
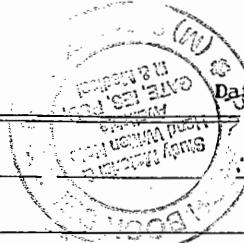
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7

CORONA:-



$$g = 21 \text{ KV/cm (RMS)}$$

Peek Empirical
Name of scientist.

- Corona is self electrical discharge of atmospheric air.
- If the operating voltage is b/w the conductor is more than dielectric strength of atmospheric air. The air molecules get ionised and initiates corona.
- The corona is form ozone gas is released.
- Critical disruptive voltage: - V_c :- The voltage at which corona is just initiated is called V_c . The sound can be heard at this voltage.

$$V_c = mg\gamma\delta \ln \left(\frac{d}{r} \right) \text{ KV/phase (RMS)}$$

m = Surface factor

= 0.8 - 0.9 for ACSR / Rough Conductors

= 0.9 - 1 for hollow / smooth conductor

g = Dielectric strength of air = 21 KV (cm RMS)

r = Radius of conductor in cm.

d = Distance between conductors in cm.

δ = Air density factor

= $\frac{392}{(273+T)}$

b = barometric pressure of air in cm of Hg

T = Atm. Temp. °C.

Critical Visual Voltage: - V_V :- The voltage at which corona is visible with violet or blue colour is called V_V .

$$V_V = mg\gamma \delta \left(1 + \frac{0.3}{J\gamma\delta} \right) \ln \frac{d}{r} \quad [\text{kV/phase (RMS)}]$$

Power loss Due to Corona: If Corona is formed power loss will occur which is given by peck empirical formula.

$$P_L = 241 \times 10^{-5} \left(\frac{f+25}{\delta} \right) \sqrt{\frac{r}{d}} (V_{ph} - V_c)^2$$

$\therefore \text{kWh/km/phase}$

$$P \propto (f+25)$$

V_{ph} = Tr-line voltage / phase

V_c = Critical Disruptive Voltage

NOTE:- i) If $V_{ph} > V_c$ CORONA OCCURS

$$P_L \neq 0$$

ii) If $V_{ph} \leq V_c$ NO CORONA

$$P_L = 0$$

Q 1-Φ Tr-line with conductor $A = 0.5 \text{ cm}^2$ distance $d/20$ conductor is 40cm operating at voltage of 30kV

Calculate ① V_c Assume $m = \delta = 1$

② Power loss at 50H_L

Solution

$$A \rightarrow \pi r^2$$

$$0.5 \rightarrow \pi r^2$$

$$r^2 \rightarrow \frac{0.5}{\pi}$$

$$r = 0.39$$

$$V_c \geq 1 \times 21 \times 0.5 \times 1 \times \ln \frac{40}{0.5}$$

$$= 46.011 \text{ kV/phase}$$

② $V_{pn} = 30 \text{ KV} < V_c \Rightarrow \text{No corona loss}$
 $\therefore P_L \neq 0$

Factors affecting Corona and Methods of Reducing

- (1) Higher value of V_c preferred so that corona does not occur and $P_L = 0$
- (2) $V_c \propto m$, m is higher for hollow and smooth conductor so that corona is less compare to ACSR or rough conductor
- (3) $N_c \propto r$, Bundle conductor radius \uparrow , $V_c \uparrow$.
By using Bundle conductor effective radius of conductor is \uparrow so that corona is minimised.
- (4) at higher V_c $P_L = 0$ and hence do not consider $P_L \propto \sqrt{r}$
- (5) $N_c \propto \delta \propto b$. In hill areas b is smaller so that corona is more frequent compare to plain areas.
 $b \rightarrow$ pressure \downarrow $b \downarrow$ in hilly areas
- (6) As the operating voltage \uparrow , distance b/w conductor are \uparrow , (d), for maintaining higher N_c because $V_c \propto \ln d$
- (7) By \uparrow height of tower corona is reduced. (capac \uparrow if weight is less, $X_L \uparrow$ over voltage cause, and greater than N_c , corona starts.)
- (8) By using Transposition corona is reduce
- (9) $P_L \propto (f + 25)$, corona power loss is more in HV AC compare to HV DC.

Disadvantages:-

- (1) Power loss occurs
- (2) Produces Interference to other lines
- (3) Too charging current \uparrow

Advantage :-

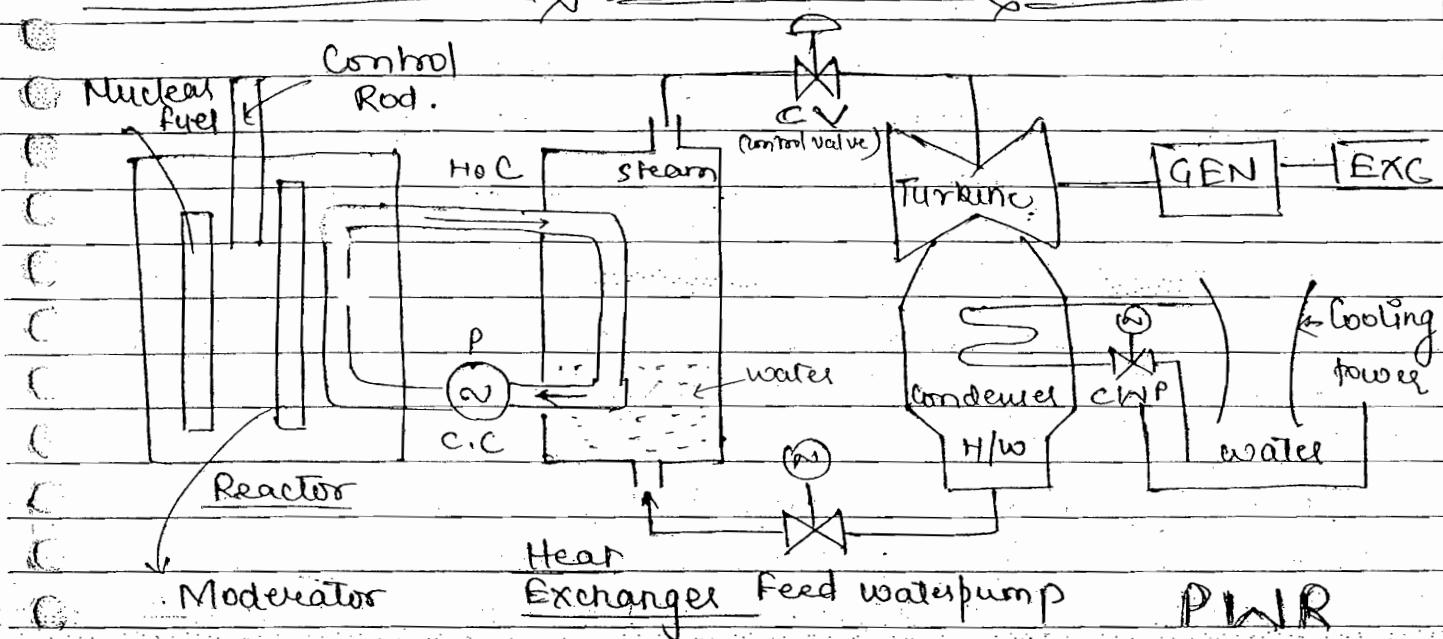
- (1) Intensity or Peak voltage of lightning surge is reduced if lightning surge initiate corona.
(Lightning is $> V_c$, start corona, it changes into corona)
so peak value of lightning of surge is ↓.

Hydro Power Plant

- Surge Tank:- It is used in the medium and high head hydro power stations. It is mainly used for protection of penstock from the water hammering effect.
→ It is used to supply water to the turbine in case of emergency load demands.
- Spillway :- It is used as a safety valve for the hydro station for protection of hydro plant from the excess water due to heavy rain. This water is diverted using spillway.
- Trash Track:- It is used for collecting waste materials from the water so that turbine blades are protected.
- Hydrograph:- It is a graph b/w discharge of a water tank. By using this hydrograph the power generated by the plant can be predicted so that scheduling of the maintenance for the hydro, thermal & nuclear are programmed.
- Pumped Storage plant:- It is one of the type of hydro plant containing two tanks i.e. downstream and upstream tanks during peak load demand water flows from upstream to downstream through the turbine for supplying peak load demand.
→ During off peak load time water will revert from downstream to upstream. During this time turbine is working as pump and gen. working as motor. Taking the power from other parallel generator.

Advantages of Pumped Storage:-

- (1) Most economical as a peak load supply plant.
- (2) Used as load frequency control unit.
- (3) If it is combine with thermal plants, plant load factor is increased.
- (4) Pollution free.
- (5) Easily adoptable for remote control operation.



Nuclear Power Plant (Layout)

CC → Cold coolant HC → Hot coolant P = pump

	BWR	PWR	CANDU	Liquid Na	FBK
Fuel.	Enriched	Enriched	Natural	Enriched	Enriched
Coolant	Water	Water	Heavy water	Liquid Na	Liquid Na
Moderator	Water	Water	Heavy water	Graphite	—
Control Rod	Cadmium	Cadmium	—	Boron	Water

enriched fuel → 99% USA

natural fuel → 0.07% India

BWR = Boiling water Reactor

PWR = Pressurized water Reactor

CANDU = Canadian Deuterium Uranium

FBR = Fast Breeder Reactor

Enriched:



Natural:



Principle: - Nuclear Fission.

→ Mostly use CANDU, PWR.

→ Liquid Na, FBR → laboratory purpose.

→ Pressure is less than thermal p.p. But flow Rate is high.

→ Moderator → Ordinary water → to moderate control the speed of neutron.



BWR: - In BWR \Rightarrow we don't use the Heat exchanger.

water is directly goes to Reactor where it will change into steam. This steam will send to turbine.

PWR,

Working: - When fuel get hot, (after fission), It hotness is collected by the cold coolant, which is circulated through pump. Cold coolant get converted into hot coolant, Heat exchanger having the water, The heat of hot coolant transfer to water. Water will convert into steam. This steam will sent to turbine.

Remaining steam will condense and convert into water again. This water is again used in heat exchanger for converting into steam.

disadvantage

- If feed water pump get damage: - (for BWR), water level will goes down, If Moderator and control rod also not working, then neutron produce heat extreme high, which Burst the Reactor.

Ex: Happened in Japan 4 out of 6 \rightarrow Burst.

Reproduction and Multiplication factors - (K)

$$K = \frac{\text{No. of Neutrons released in present cycle}}{\text{No. of Neutrons released in previous cycle}}$$

$K = 1 \Rightarrow$ Constant power 0/p

$K > 1 \Rightarrow$ Increased power 0/p.

$K < 1 \Rightarrow$ Decreased power 0/p

practical value of K^0 is
just higher than 1

e.g.: 09:00 - 100MW - 100 Neutron -

$$10:00 - 100\text{MW} - 100 \text{Neutron} - K = \frac{100}{100} = 1$$

$$11:00 - 120\text{MW} - 120 \text{Neutron} - K = \frac{120}{100} = 1.2 > 1$$

$$18:00 - 80\text{MW} - 80 \text{Neutron} - K = \frac{80}{120} = \frac{80}{120} < 1$$

- In nuclear reactor heat is produced due to nuclear fission chain reaction

This heat is absorbed by coolant which is used to convert water into steam in heat exchanger. This steam admitting into turbine for producing power generation.

- The amount of heat released is depending on velocity of neutron and No. of Neutrons released.

• Moderator is used for moderating the speed of the neutron. The molecular weight of the moderator is to be minimum

- Ordinary water is used as moderator in the enriched uranium plants.

• Control Rod : It is used for absorbing excess neutrons released during Nuclear fission chain reaction.

Load Frequency Control

Date _____

Rated value of freq. = 50 Hz.

Range: Ideal: $50 \pm 1\%$. ($49.5 - 50.5$ Hz)

: Practical: $50 \pm 2\%$. ($48.5 - 51.5$ Hz)

Disadvantages of frequency variation:-

(1) For maintaining constant voltage at low freq. The flux to the X-mu core has to be increased. This will increase the causes saturation of the X-mu core.

(2) All the electrical Motor speeds are freq. dependent

By changing the frequency. The performances of electrical motor are effected

(3) Due to core saturation of CoT. at low frequency, relays produces trip signals without any fault

(4) PA, FD and ID fans are runned by induction Motor. If the freq. changes the performance will be effected. So that thermal efficiency is effected.

(5) The turbine blades are damaged at higher frequency & speed. [at low speed blades will compress and at high speed blades will come out due to centrifugal force]

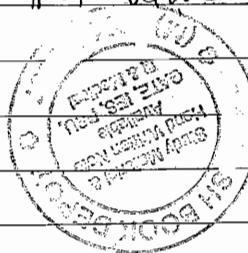
Methods of Frequency Control :-

(1) Primary control: - Speed governing control valve

(2) Secondary control: -

(A) Pumped storage plant

(B) load regulation.

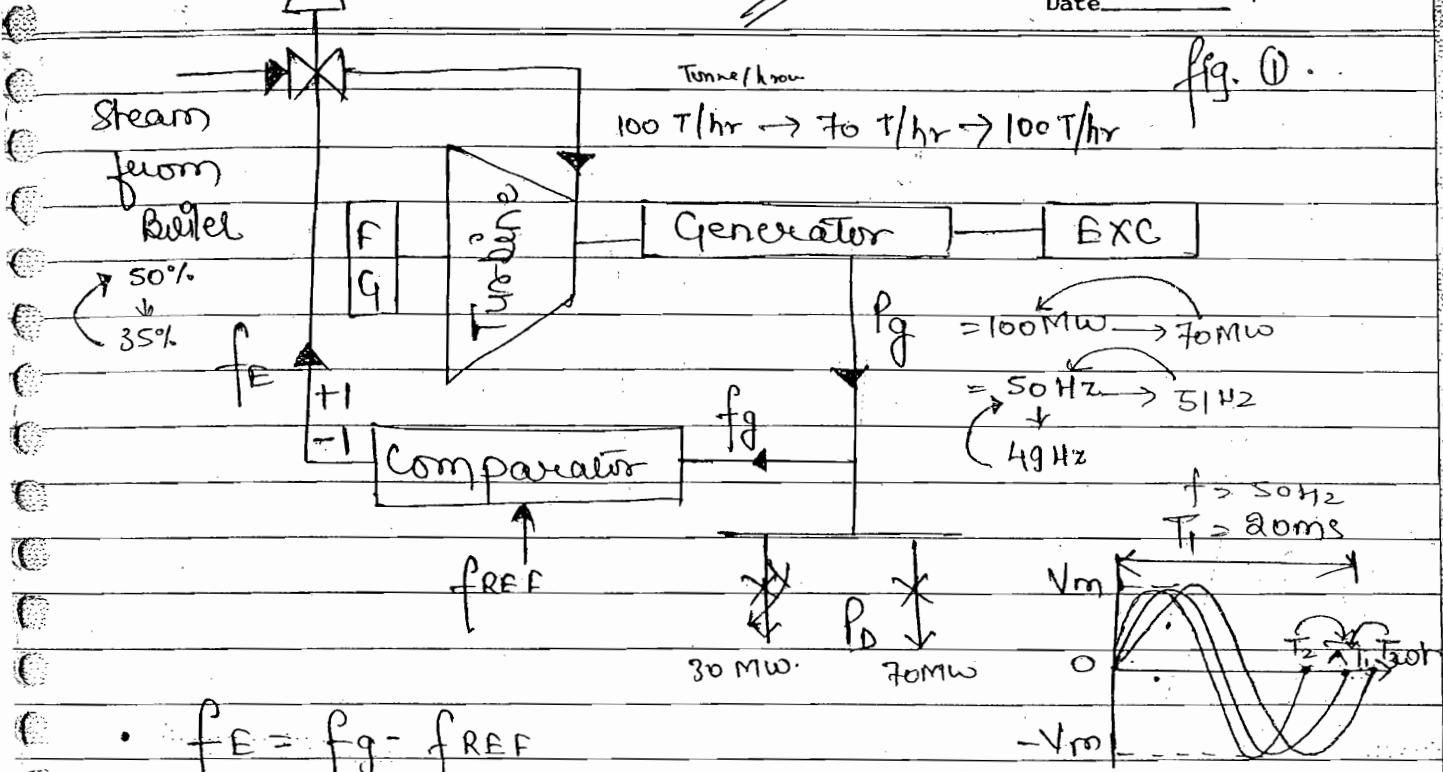


Speed Governing Control Valve :-

Diagram in Next page.

Govt. Valve (HP/IPCv)

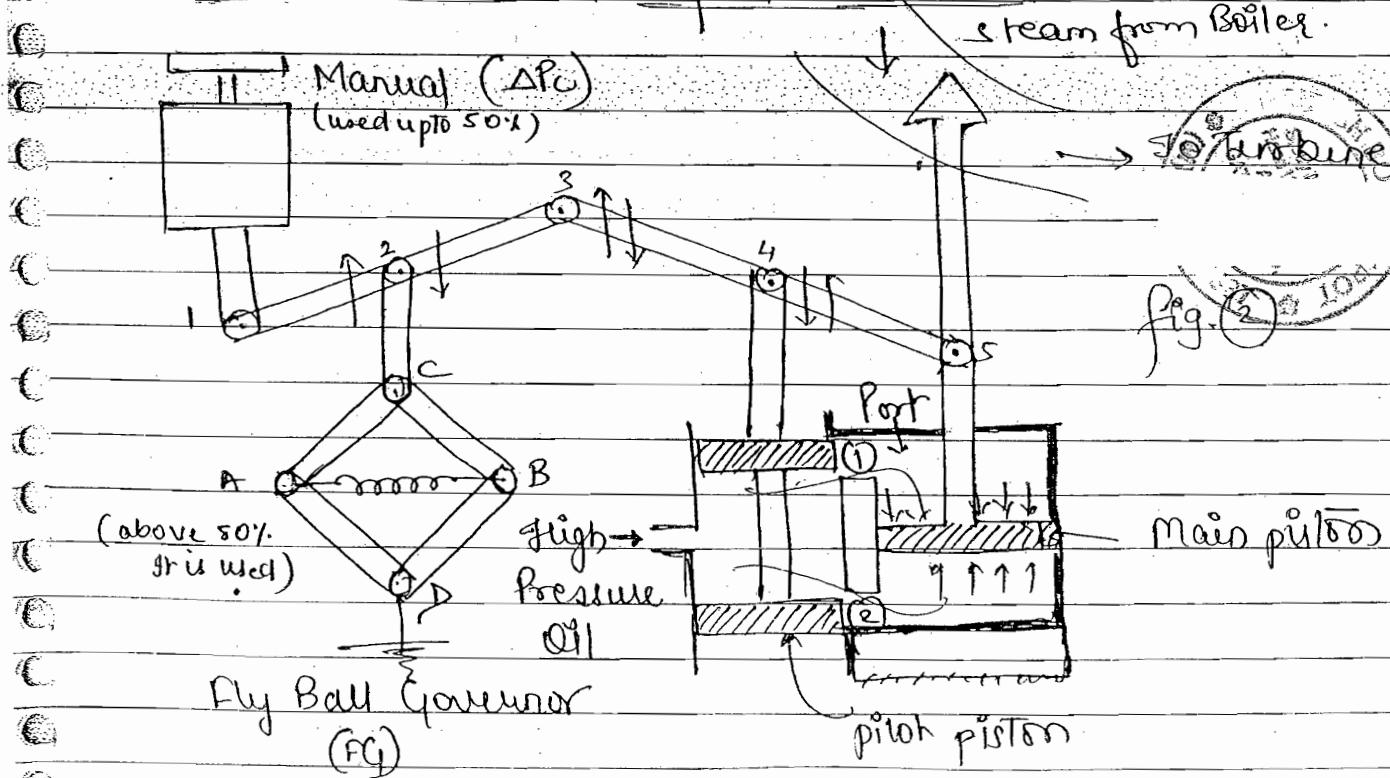
This process take some time
delay. ($\leq 1 \text{ sec}$)



- $$f_E = f_g - f_{REF}$$

- ① If $f_g = f_{REF} \Rightarrow f_E = 0 \Rightarrow$ Constant opening position of Govt. Val.
 - ② If $f_g > f_{REF} \Rightarrow f_E > 0 \Rightarrow$ close valve until $E = 0$
 - ③ If $f_g < f_{REF} \Rightarrow f_E < 0 \Rightarrow$ open valve until $E = 0$

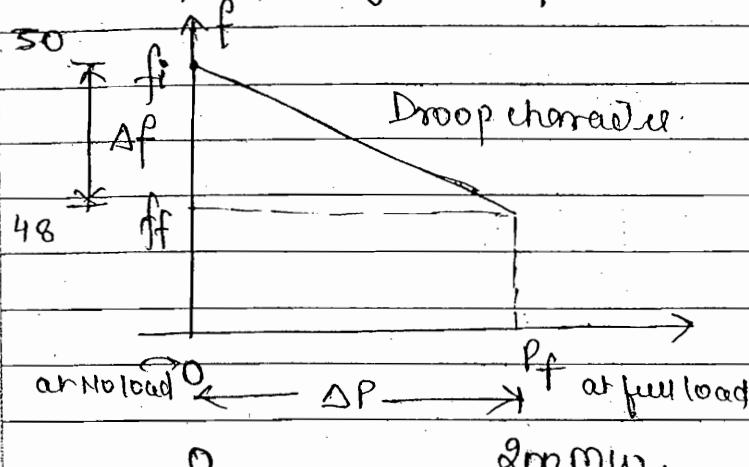
Internal Structure of Govt. Nalve



practically freq. at No. load $\Rightarrow > 50\text{ Hz}$.

Date _____

Speed Regulation Parameter



$$R = - \frac{\Delta f}{\Delta P} \text{ Hz/MW}$$

$$\text{Ex:- } R = - \frac{(50 - 48)}{200 - 0} = -1 \text{ Hz/MW}$$

$$\Rightarrow -0.01 \text{ Hz/MW}$$

$$\frac{\Delta f_2}{\Delta P_2} = \frac{\Delta f_1}{\Delta P_1}$$

Speed Regulation Constant:

$$\Delta f \rightarrow \%$$

Ex:- 4% of speed regulation
or (0.04 p.u.).

$$f_i - f_f \Rightarrow \Delta f$$

$$\frac{f_i - f_f}{f_i} \Rightarrow \frac{\Delta f}{f_i} \%$$

$$\frac{\Delta f}{50} = 4\% \Rightarrow \Delta f = 2 \text{ Hz}$$

Q. Ques. t at 200 MW. How much freq. will added?

① A 200 MW turbo gen. have speed regu. of 8%. How much of turbine tip has to be \uparrow for steady state operating for freq. drop. of 0.05 Hz.

Soln. $R = 0.1 \Rightarrow 0.08$

$$\frac{f_2 - f_f}{f_2} \Rightarrow 0.08$$

$$|R| + \frac{\Delta f}{\Delta P} = \frac{8\% \times 50}{200} = \frac{8 \times 50}{200} = \frac{4}{200} = \frac{4}{200} \text{ Hz/MW}$$

$$\frac{\Delta f}{\Delta P_2} \Rightarrow \frac{\Delta f_1}{\Delta P_1}$$

$$\frac{0.05}{\Delta P_2} = \frac{4}{200}$$

$$\Delta P_2 = \frac{200 \times 5}{100 \times 4} = 2.5 \text{ MW}$$

Fig. ① Explanation :- Suppose the generated power $P_g = 100 \text{ MW}$ and demand $P_d = 100 \text{ MW}$, for this 100 Tonnes/hour coal is required for which 50% valve is opened [freq. set to 50 Hz]. Time period of 1 cycle is $T_1 = 20 \text{ ms}$.

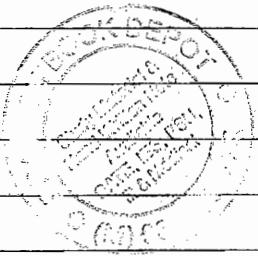
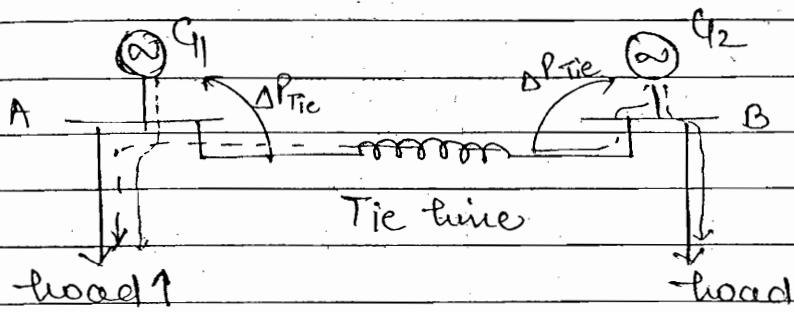
- ✓ Suppose CB of 30 MW get opened due to fault. $P_d > 70 \text{ MW}$ and $P_g = 100 \text{ MW}$, motor speed get high R.E. $\propto \omega^2$ because of which freq get \uparrow 51 Hz. Compensator will generate of an error of +1, which send to gvn. valve. It will open the valve upto 35%, Now coal requirement will be 70 T/hr. [51 Hz set to again 50 Hz]
- ✓ Suppose CB of 30 MW get closed, Now $P_d = 100 \text{ MW}$ But $P_g = 70 \text{ MW}$, rotor speed get \downarrow due to which freq. will \downarrow and become 49 Hz. $T_3 = \frac{1}{f} = \text{more than } T_1$

$T_1 = 20 \text{ ms}$. Compensator will generate error of -1. and send signal to gvn. valve. It will open the valve, Now coal requirement \uparrow , 70 T/hr \rightarrow 100 T/hr freq. will again set to 50 Hz \rightarrow 50 Hz. To maintain the freq.

Fig ② Explanation :-

- ✓ for \downarrow in demand, FG will expand pull c down, 2 \downarrow , 3 \uparrow , 4 \downarrow , high pressure oil will enter through (2) gate and close the valve.
- ✓ for \uparrow in demand, FG will compressed push c upward, 2 \uparrow , 3 \downarrow , 4 \uparrow , oil will enter through ~~(3)~~ gate and open the valve.

Area frequency Control:-



- ✓ (1) Flat frequency control
- ✓ (2) Flat Tie line / Tie Bias Control
- ✓ (3) Parallel frequency control.

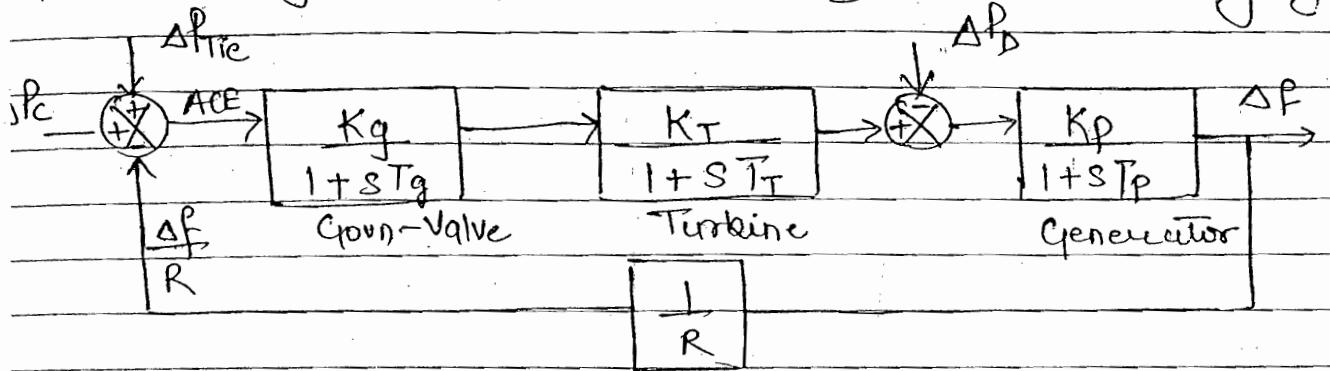
• Area freq. control is used to maintain constant frequency for an interconnected grid sys. containing more generators connected in parallel.

(1) Flat frequency control: - load changes of Bus Bus A is supplied by the generator G_2 for maintaining constant frequency. In this method the tie line may be over loaded.

(2) Flat Tie line / Tie Bias control: - load changes of Bus Bus A or B supplied by G_1 and G_2 without over loading of the tie-line so that the control signal is proportional to changes in the tie line power and frequency.

(3) Parallel freq. control: - load changes of Bus Bus A or B is supplied simultaneously by both the generators without overloading for maintaining constant freq. this method is most practically used in area freq. control.

Block Diagram Representation of Speed Governing System



ACE = Area Control Error

$$\Delta P_c + \Delta P_{tie} - \Delta f / R$$

For auto control $\Delta P_c = \text{constant}$

$$\text{Bias Coefficient} = b = -\frac{1}{R}$$

$$\boxed{\text{ACE} = \Delta P_{tie} + b \cdot \Delta f}$$

Time Constants: T_p, T_g, T_T

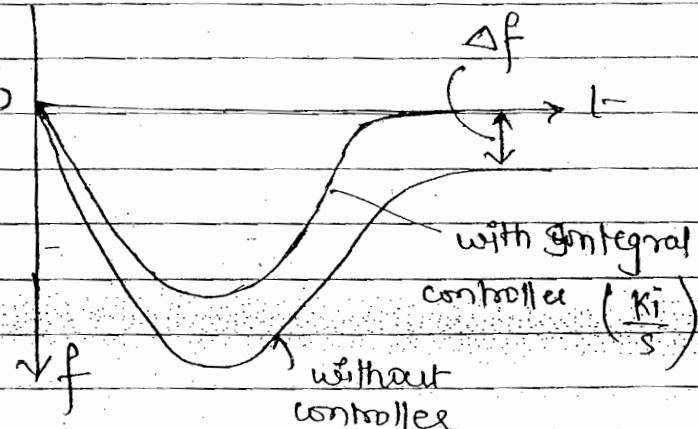
Gain Constants: K_p, K_g, K_T

$$T_p = 0.1 - 0.2 \text{ sec}$$

$$T_T = 0.1 - 0.3 \text{ sec}$$

$$T_g = 0.1 - 0.2 \text{ sec}$$

Δf = steady state freq. deviation / drop



- Integral controller eliminates steady state freq. drop

~~Steady state freq. drop (Δf): -~~

$$\Delta f = (f_N - f_i)$$

① Isolated Generator

(a) Sudden load Demand :- (ΔP_D)

$$f_N = f_i \left[\text{H.o.S.} - (\Delta P_D) T_d \right] \cdot Y_2$$

H.o.S.

(b) Sudden load loss (ΔP_d) (Trip of load)

$$f_N = f_i \left[\frac{H \cdot S + (\Delta P_d) \cdot T_d}{H \cdot S} \right]^{1/2}$$

H = Inertia constant of Gen. MW Sec/mVA.

S = Rating of Generator in MVA.

ΔP_d = -ve for Load Demand in MW.

T_d = Time Delay in Govt. Sys. in Sec.

f_N = New frequency

f_i = Initial frequency.

(2) Area Control: -

$$\Delta P = - \frac{\Delta P_d}{(\beta + \gamma R)}$$

β = Rated value \times % change in power

Rated freq. \times % change in frequency.

R = Speed Reg. parameter in Hz/MW

ΔP_d = -ve for load loss

= +ve for load demand.

Q An interconnected power sys. N/W. As the pow of 1500 MW at 50Hz. The freq. is changing 2.5% for a load change of 1.5%. Calculate the steady state freq. drop

If a 200 MW of industrial load is trip. Assumed $R = 0.005$ Hz/MW

Solution: $\Delta P_d = - 200$

$$\frac{1500 \times 1.5}{100} + \frac{1}{0.005} = \frac{200}{200} + \frac{1000}{2.5}$$

$$\Delta f = 0.917 \text{ Hz}$$

$$f_N - f_i = 0.917$$

$$f_N - 50 = 0.917$$

$$\therefore f_N = 50.917 \text{ Hz}$$

Q 200 MVA 50 Hz Turbo gen. is operating at No load if a load of 700 MW is applied at the terminals of generator. Calculate

(1) Steady state freq. drop

(2) New freqe. due to time delay of gov. sys. of 0.5 sec. Assume. Intertia const. of the generators

is 4 M W Sec / MVA

$$\text{Solution: } f_N = \frac{4 \times 200 + 700 \times 0.5}{4 \times 200}^{1/2} \times 50$$

$$= 48.89 \text{ Hz}$$

$$\Delta f = 50 - 48.89 = 1.11 \text{ Hz}$$

Load Sharing of Parallel Generator

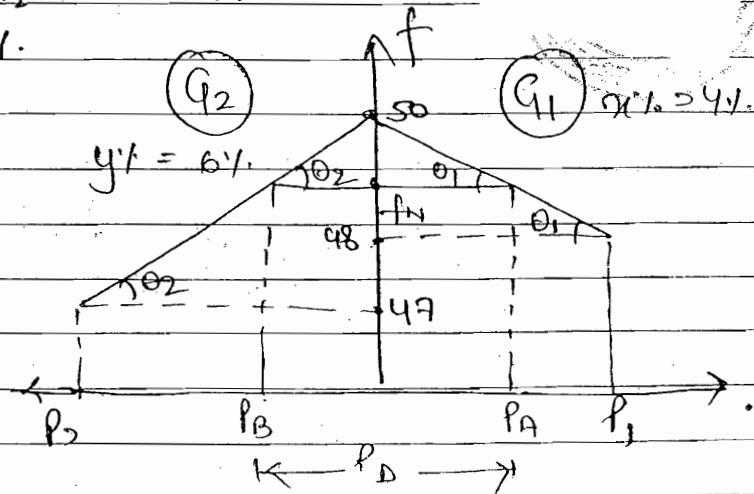
① with different drooping characteristic

$$P_1 = 250 \text{ MW} \quad \text{at } 0\% \quad P_2 = 250 \text{ MW} \quad \text{at } 4\%$$

$$P_A = 4\% \quad P_B = 6\%$$

$$P_A + P_B = P_D = 400$$

$$P_D = 400.$$



G₁G₂

$$\tan \theta_1 = \frac{50 - f_N}{P_A} = \frac{50 - 48}{250} = \frac{1}{125}$$

$$\tan \theta_2 = \frac{50 - f_N}{P_B} = \frac{50 - 47}{250} = \frac{3}{250}$$

→ (1)

→ (2)

$$\therefore P_A + P_B = 400 \text{ given}$$

$$P_B = 400 - P_A$$

Put in eqn (2).

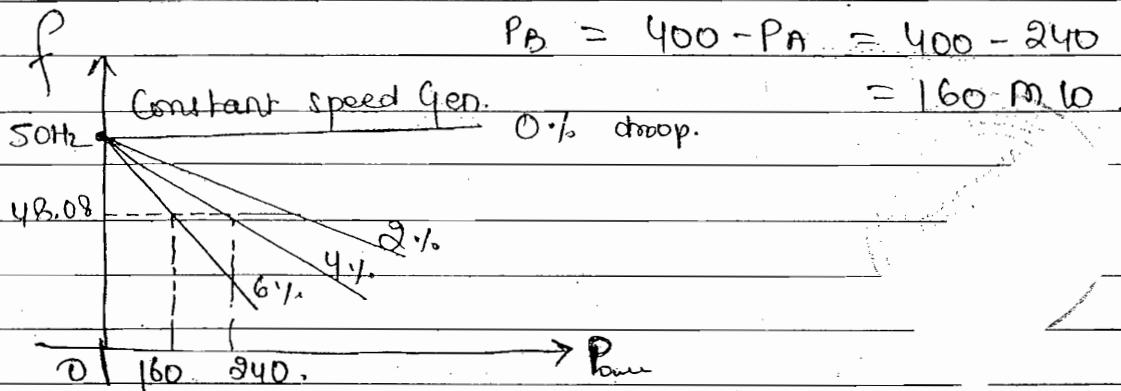
$$\frac{50 - f_N}{400 - P_A} = \frac{3}{250} \quad \text{--- (2)}$$

$$\text{Solve (1) & (2)} \quad f_N = 48.08 \text{ Hz.}$$

$$P_A = 240 \text{ MW}$$

$$P_B = 400 - P_A = 400 - 240$$

$$= 160 \text{ MW.}$$



- In parallel operation generators, The generator with lower % of droop character. will share maximum load.
- If a 0% or Constant Speed Gen. is connected in parallel to the other generators with 2, 4, 6%. drop characters then 0% generator can supply entire load changes with loading other generator. This is an ideal generator.

Note

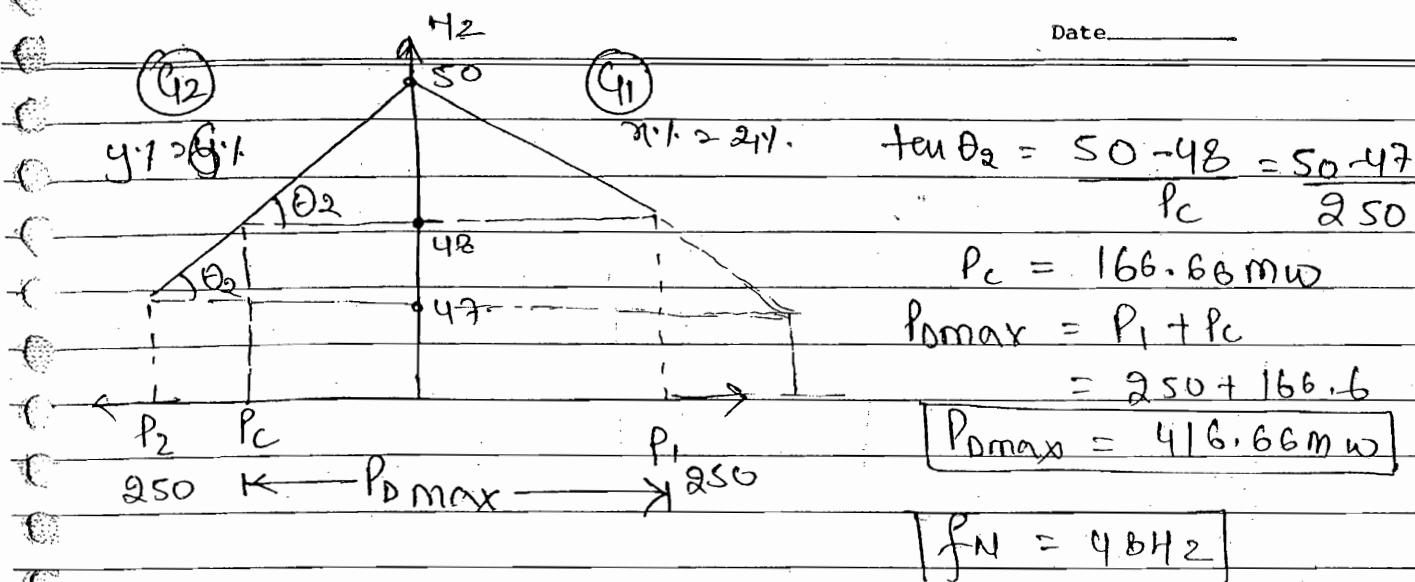
(1) Maximum load supply by gen. without overloading

$$4\% > 2\% \quad P_1 = 250 \text{ MW}$$

$$P_{\max} = P_A + P_B = ?$$

$$2\% > 4\% \quad G_1 \quad G_2$$

$$P_2 = 250 \text{ MW}$$



• If operate at 47 Hz freq. P_1 deliver More than 250
so we can't take this condition.

- ⇒ Because of different drooping characteristic. Generators are not able of loaded to the maximum full load capacity.
- ⇒ The lowest drooping character is loaded to full load capacity

~~(a)~~ Both Generator has Same droop Character

$$P_1 > 250 \quad (\textcircled{1})$$

$$P_2 = 250 \quad (\textcircled{2})$$

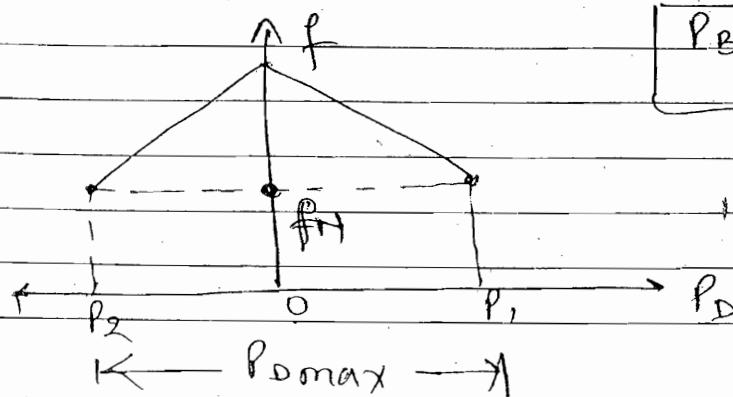
$$4\% \cdot 4\% > 4\% \quad P_A = \frac{P_1 \times P_D}{P_1 + P_2}$$

$$P_B = \frac{P_2 \times P_D}{P_1 + P_2} = \frac{250 \times 400}{250 + 250}$$

$$P_D > P_A + P_B$$

$$P_A = 200 \text{ MW}$$

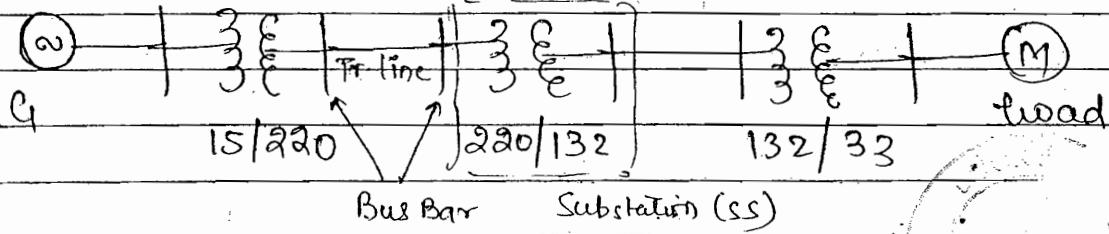
$$P_B = \frac{P_2 \times P_D}{P_1 + P_2} = 200 \text{ MW}$$



- If both generator have equal droop character can supply the load demand as per their capacity proportionately.
- Maximum demand = Sum of their individual fuel load capacity.

30/10/14

Protection And Switchgear



→ shown only for R phase (Next page fig).

→ We have protected → low X-mes 220/132 kV, 132 kV Bus Bar, 132 kV Bus Bar.

→ (1) Identification of fault (2) Isolation of fault from healthy part.

→ Tr-line → SF₆, Distributⁿ → Vacuum. CB.

• lock out conditⁿ :- CB do not operate, even fault is present

BCO₂ pressure (sufficient) is not present, if open CB get Blast

ex:- R₂ Operate for fault occur across R₁)

• Non-unit Protection: Identify the fault not only its own unit (area) But also outside. (also called Backup protection)

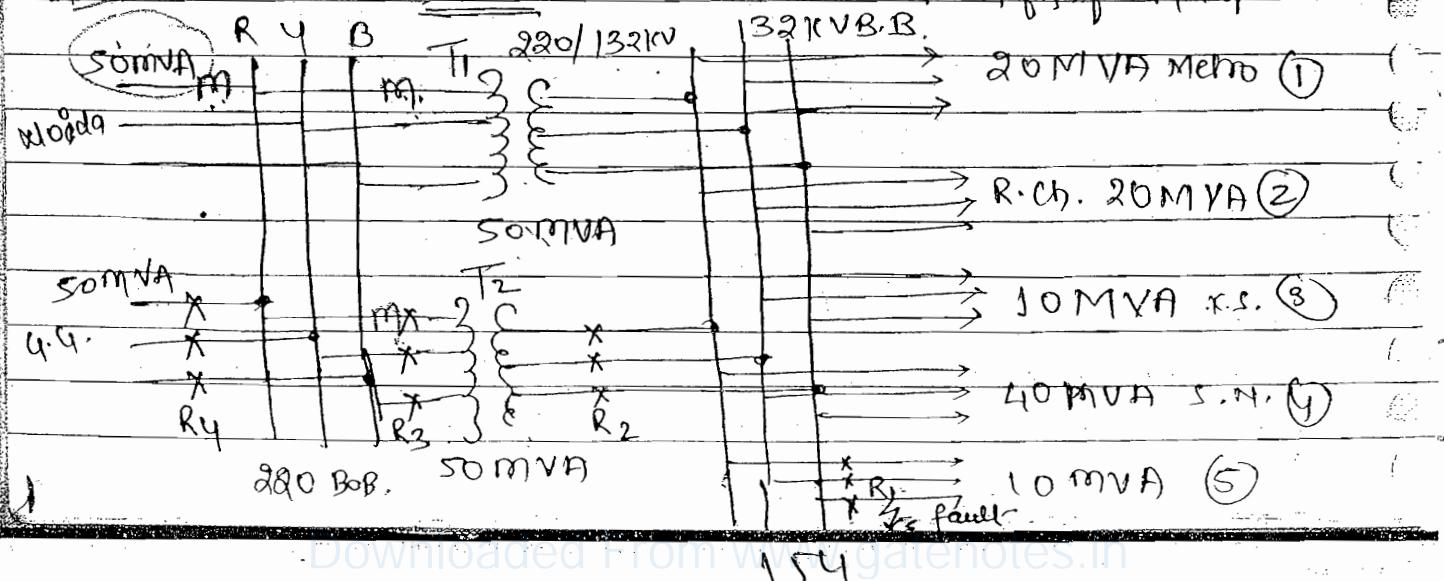
• Unit Protectⁿ: ex:- Buchholz Relay which operate only

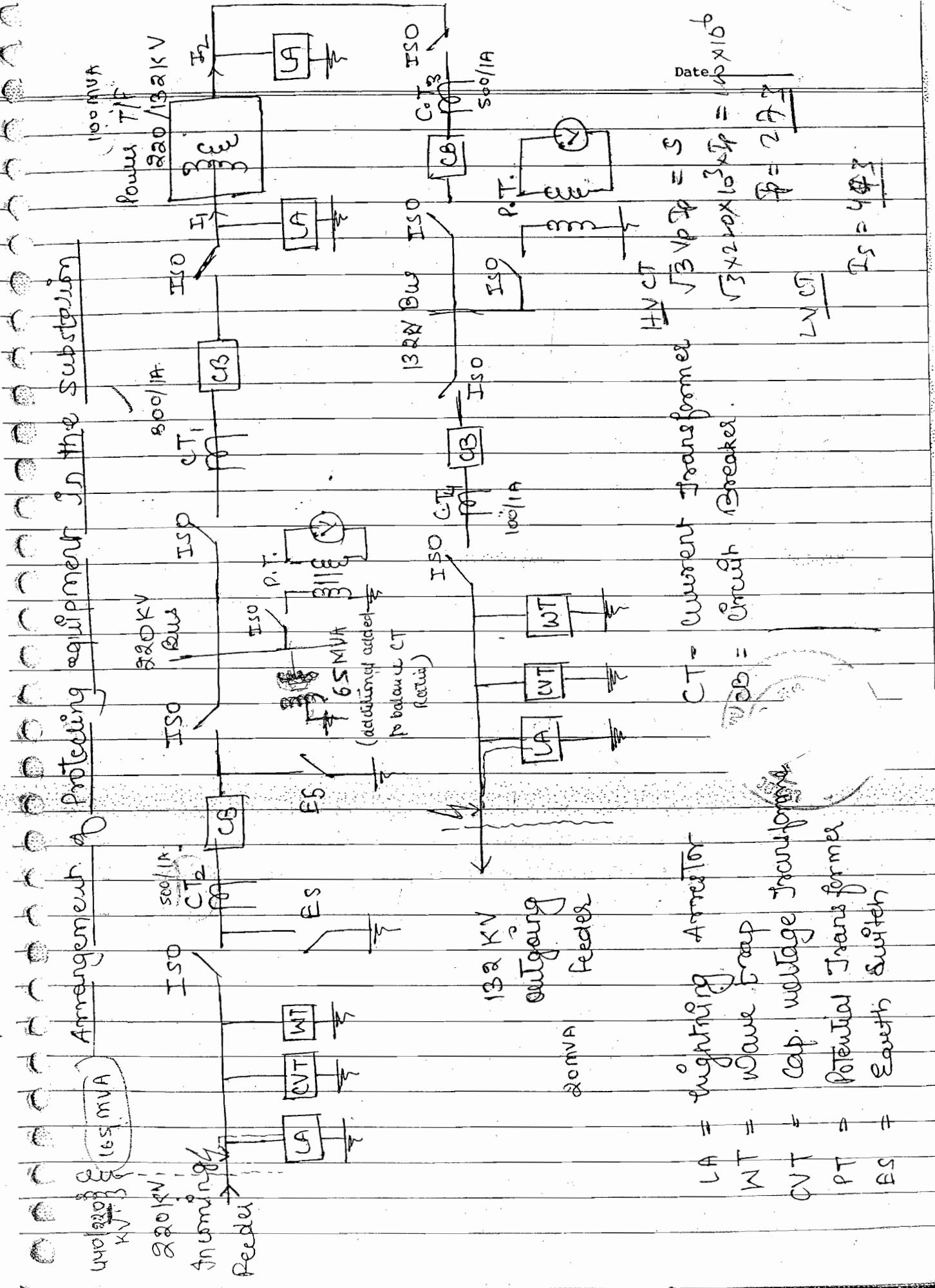
in specified area

100.

Delhi

if R₁ get failed R₂ will operate, if R₂ fail, R₃ operate, if R₃ fail R₄ operate





- Suppose (G.4.) generator fail, then gen. is out of service and demand is 100 MVA, Then area (5) and (4) are disconnected, [G₂ is fail due to fault of Relay R₁]

Date _____

- Power sys N/W consisting of generators, x-mei, Bus Bars & x-line and electrical Motors etc These equipments are to be protected from the abnormal condition like short circuit, open circuit, faults and lightning surges.

- Non-Unit Protection: - The protecting equip. like Relays, CB etc are operating for the faults within in own zone and also in the other zone equipment and faults is known as N.U.P. ex:- overcurrent and distances relays.

- Unit Protection: - The protecting equipments are operating within for the fault within some physical space with in or equipments is called U.P.
ex:- Differential Relay or Buchholz Relay

- LA: The first and last protecting device of the substation is LA used for diverting the lightning surge occur outside the substation.
 - Two more LA are kept on both side of pow-x-mei for discharging the surge occur within the substation
 - LA are made of metal oxide like - Zinc Oxide, Silicon carbide (SiC) which offer low resistance for the lightning surge and high resistance for normal voltages

LA have impulse Ratio of unity

$$\text{Impulse Ratio} = \frac{\text{Mag. of lightning surge with high freq.}}{\text{Mag. of lightning surge with low freq.}}$$

- P.T → only in Bus Bar
- CT → each feeder.

• CVT: It is working on principle of capacitance using for Reducing the high voltage of 220 kV / 132 kV etc. to a low voltage. The standard low voltage is of 110V. It provides voltage signal for

(i) Voltmeter.

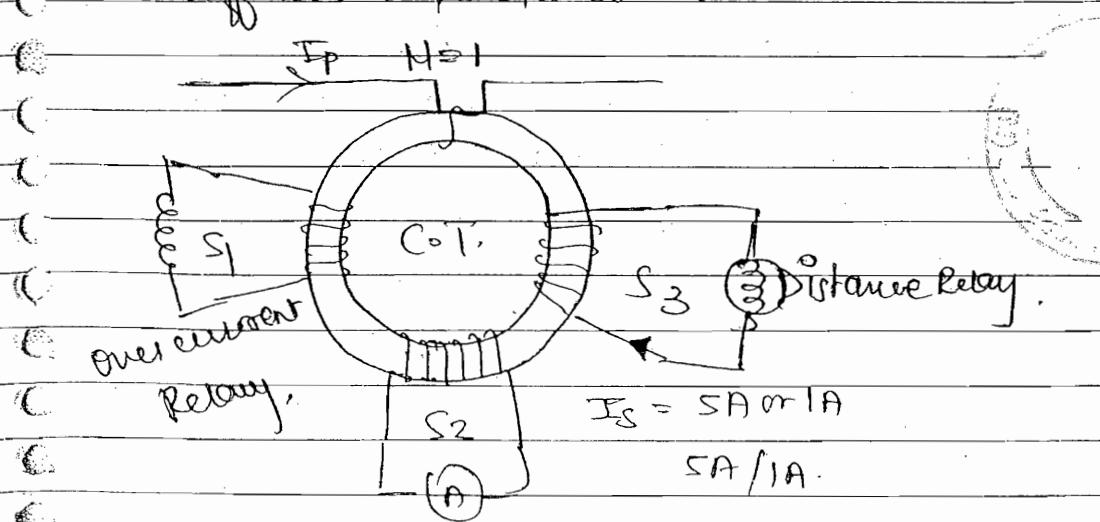
(ii) Wattmeter and energy meter

(iii) Distance and directional relay.

Each phase has one CVT. The cost of CVT is less than compare to PT.

• P.T. ⇒ It is working on principle of \propto -mer, used to measure high voltage. The standard secondary voltage of the PT is 110V. It provides voltage signal for voltmeter, energy wattmeter and relays like directional and distance. It can used as a Backup for CVT's

• CT: It consist of single turn primary and multiple secondary turns with different ratio used for measuring high currents. The standard sec. currents is of 1A or 5A. It provide signals for ammeter, wattmeter and energy meters, and relay like overcurrent differential, distance etc.



• Power X-Mel. \rightarrow 220/132 KV capacity of X-Mel = 100 MVA

$$I_1 = \frac{100 \times 10^6}{\sqrt{3} V_1} = \frac{100 \times 10^6}{\sqrt{3} \times 220 \times 10^3} = 262.43 \quad I_2 = \frac{100 \times 10^6}{\sqrt{3} \times 132 \times 10^3} = 433.38$$

Then Current value of CoT - $\approx 300/1A$ in primary (CT_1)
 $= 500/1A$ in secondary (CT_2)

• Let 132/33 KV having capacity of X-Mel = 20 MVA.

$$I_1 = \frac{20 \times 10^6}{\sqrt{3} \times 132 \times 10^3} = 87.4 \quad \text{So value of C.T Ratio} \\ \Rightarrow 100/1A (CT_1)$$

• Suppose another power-X-Mel of 165 MVA capacity 440/220 KV

$$I_2 = \frac{165 \times 10^6}{\sqrt{3} \times 220 \times 10^3} = 445.6 A$$

So CoT. ratio will become (CT_2) $\approx 500/1A$.

• As CoT. ratio are not same, $CT_2 = 500/1A$, $CT_1 = 300/1A$, to make equal we add 65 mVA capacity X-Mel at Bus Bar of 220 KV.

• C.B \Rightarrow C.B are filled with arc quenching medium like SF₆, oil, vacuum air etc so that this can be open or closed at NO load or full load.

✓ This can be operated by relay or manual

• Isolator - It must be opened or closed on No load only because it does not contain any arc quenching medium.

• Earth Switch: It is used to discharge residual energy present in the electrical equipment

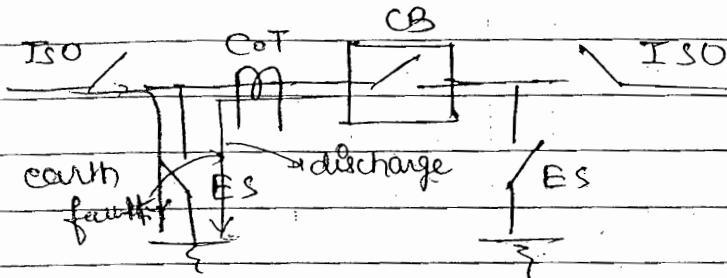
✓ It has to be ^{open} position under normal condition.

✓ Sequence used Before attending the maintenance of the equipment:

- (1) Open C.B under No load or full load
- (2) Open Isolator under No load.
- (3) Close Earth Switch

Sequence used before charging of the equipment:

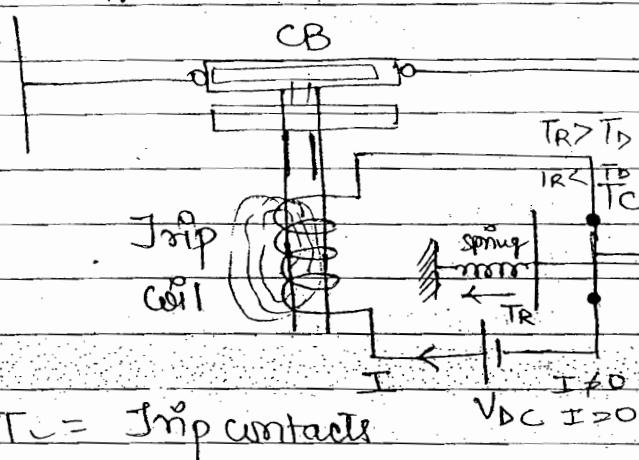
- (1) Open Earth switch
- (2) Close isolator
- (3) Close CB.



After maintenance,
if ES is not open and
 $I_{SO} \rightarrow$ closed, intentionally created earth fault.

Relation B/w C.B and Relays:-

Bus Bar



(1) Block (Healthy Condition)

$T_c \rightarrow$ open (Normal open - N.O.)

$CB \rightarrow$ close.

(2) Trip (Faulty Condition)

$T_c \rightarrow$ close (Normal close - N.C.)

$CB \rightarrow$ open.

- After fault is removed, Manually reset is pressed to open the T_c

- How to identify which relay get operate after the fault.

In Normal condition, CB are closed, when a particular CB is get operated, it will pull down and can see the identification by which we get know which CB get operate.

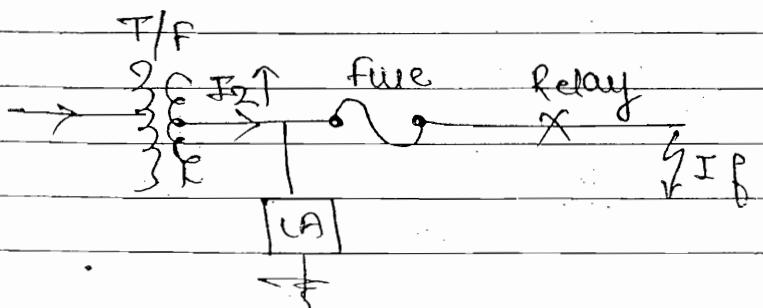
• Types of Relays-

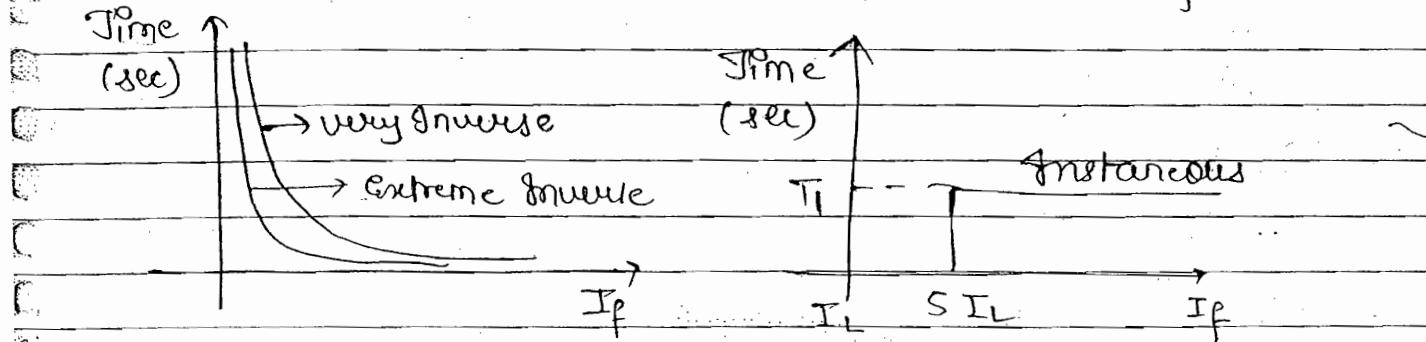
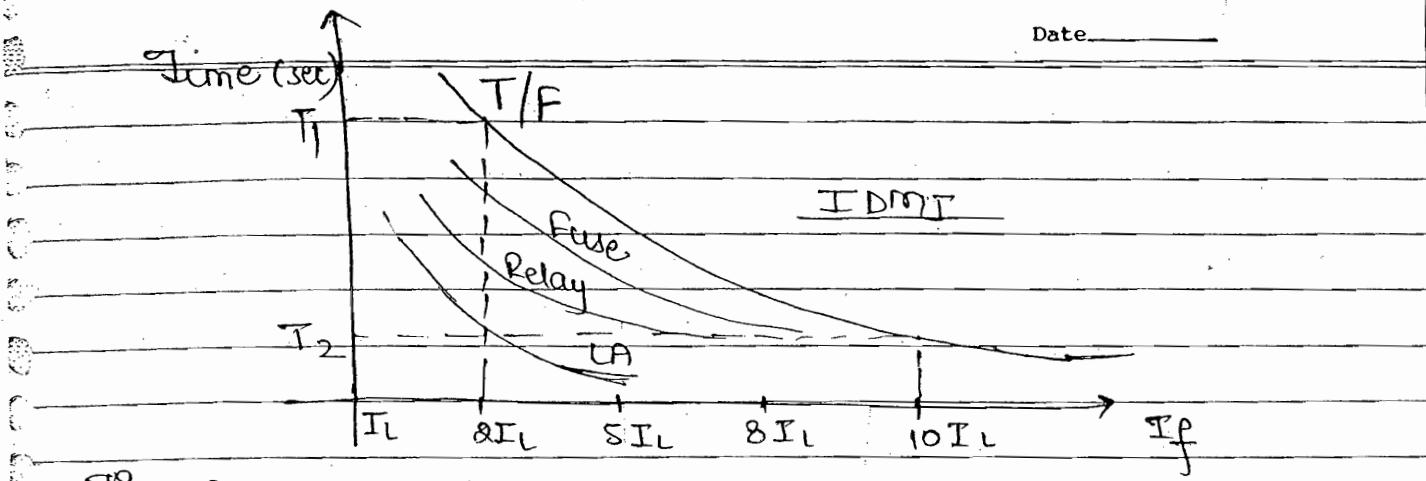
<u>Depends on:</u> <u>PRINCIPLE</u>	<u>Equipment Protected</u>	<u>Sensing Element</u>	<u>Time</u> (IMPT)
(1) Electromagnetic	Generator	over current	Inverse Definite Minimum Time
(2) Thermal	x-mer	Over Voltage	
(3) Static	Tr-line Bus-Bar Motor	over flux over speed Earth fault Distance Directional Differential	Very Inverse Preset Inverse Instantaneous

• Total fault clearing Time =

$$\text{Relay Time} + \text{Circuit Breaker Mechanical operating time} \\ + \text{arc quenching time}$$

- The minimum fault clearing time required 5 to 6 cycles.
(100 - 120 milliseconds)





① Electromagnetic Relay:-

Attraction
Dependent on frequency.

Induction (Independent to freq.).

Watthour Meter Shaded pole Induction Cup

IDMT

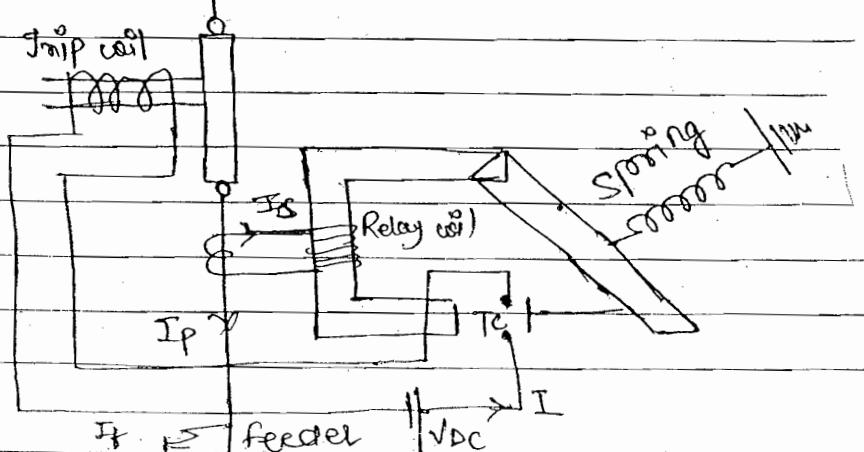
over current,
Differential

Instantaneous

Directional,
Distance

Electromagnetic Attraction

BulB or



$$\phi \propto I_s \propto I_p \propto I_f$$

$$I_f = I_m \sin \omega t$$

$$T_d \propto I_f^2$$

$$\propto I_m^2 \sin^2 \omega t$$

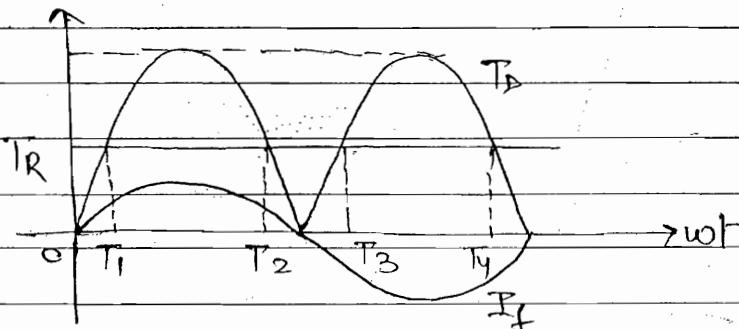
$$T_d = \frac{K I_m^2}{2} (1 - \cos 2\omega t)$$

T_d = Operating / Deflecting Torque

T_r = Restraining / Control Torque.

trip: $T_d > T_r$

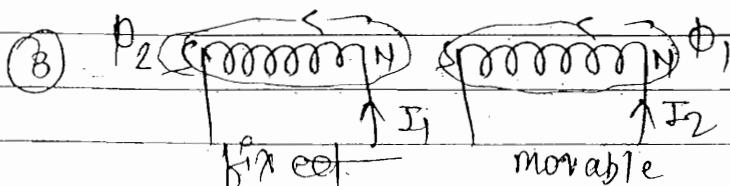
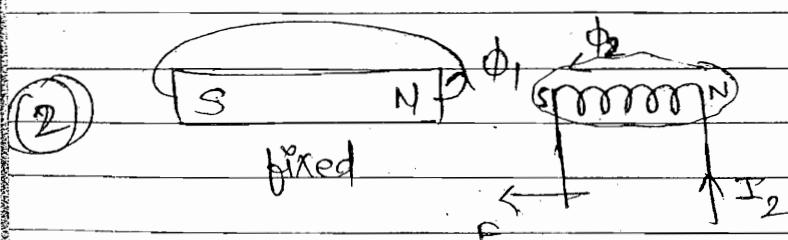
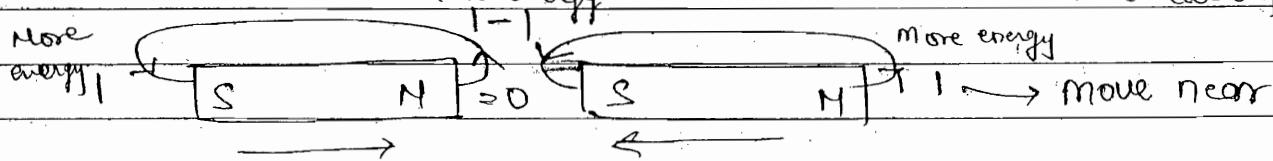
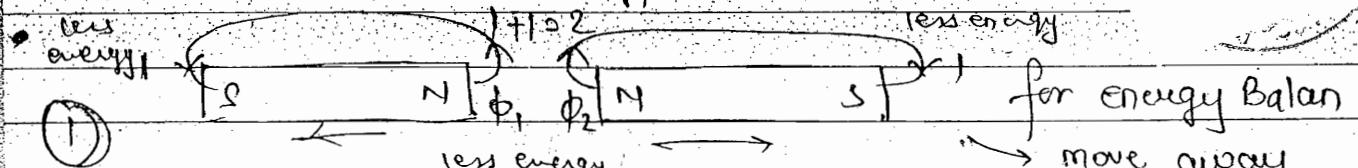
Block: $T_d \leq T_r$



• Attraction Type \rightarrow Not in use now.

Problem \Rightarrow Doubling effect.

More energy

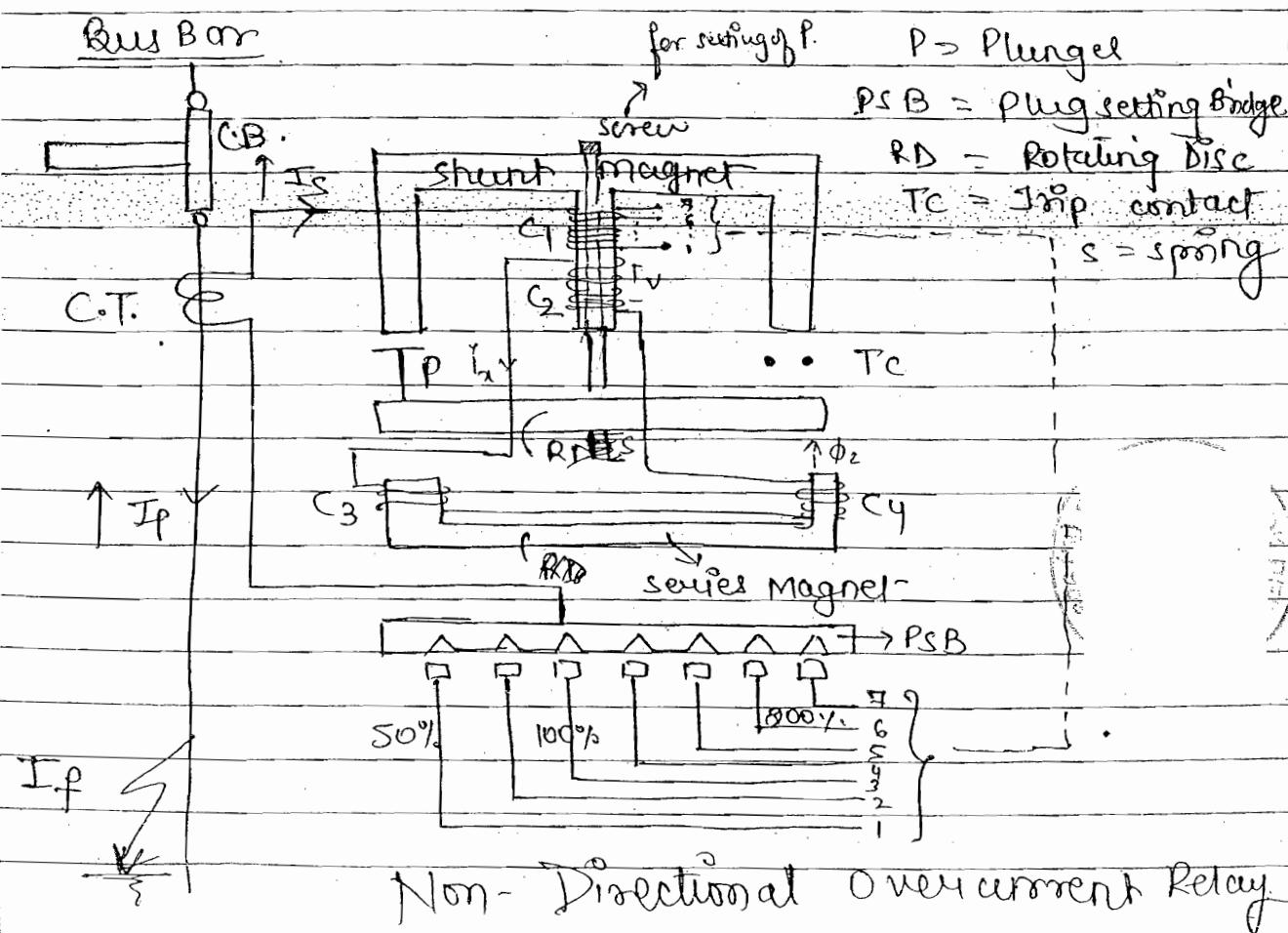


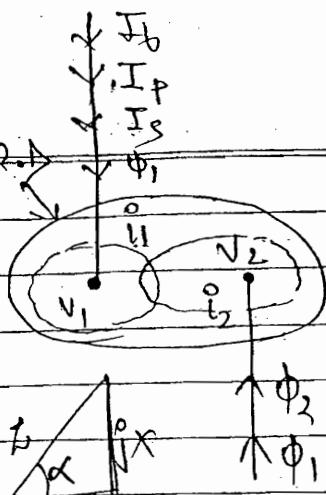
Doubling effect: - In electromagnetic attraction relay $T_D \propto (I^2 \cos \omega t)$ ie in one cycle of fault current, trip contacts open twice, so that arcing is produced b/w the trip contacts and the plunger. This will cause overheating and damage the relay trip contacts. This effect is called doubling effect. Due to this effect electromagnetic relays are practically not used.

b/w T_2 to $T_3 \rightarrow$ contact open \rightarrow produce arc, after T_4 again open.

• Electromagnetic Induction Relay:

✓ Watt-hour Meter Relay: - Problem of doubling effect can be eliminated in the electromagnetic Relays. Hence, these are used most practically in the substation.





$$I_f = \text{Im } \sin \omega t$$

$$\phi_1 \propto I_s \propto I_p \propto I_f$$

$$\phi_1 = \phi_m \sin \omega t$$

$$V_1 = -\frac{d\phi_1}{dt} = \phi_m \omega \sin(\omega t - 90^\circ)$$

$$i_1 \propto V_1 \propto \phi_m \sin(\omega t - 90^\circ - \alpha)$$

$$\phi_2 = \phi_{m2} \sin(\omega t - \theta)$$

disc having same
impedance

$$V_2 = -\frac{d\phi_2}{dt} = \phi_{m2} \omega \sin(\omega t - \theta - 90^\circ)$$

$$i_2 \propto V_2 \propto \phi_{m2} \sin(\omega t - \theta - 90^\circ - \alpha)$$

$$T_D \propto (\phi_1 i_2 - \phi_2 i_1) \propto \phi_{m1} \phi_{m2} [\sin \omega t \cos(\omega t - \theta) - \cos \omega t \sin(\omega t - \theta)]$$

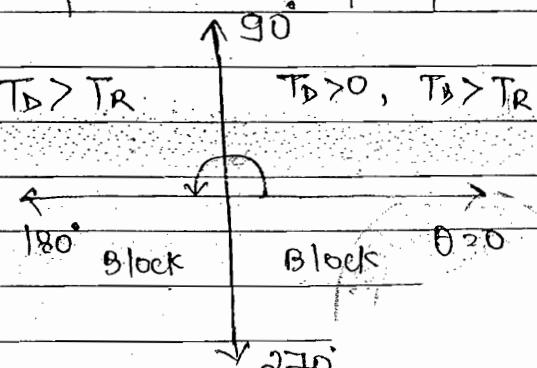
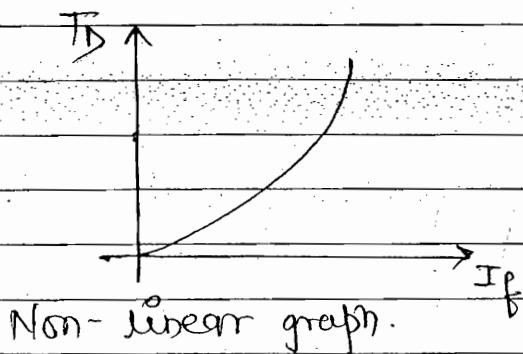
$$T_D \propto \phi_{m1} \phi_{m2} \sin \theta$$

$$\phi_{m1} \propto I_{f1} \quad ; \quad \phi_{m2} \propto I_f$$

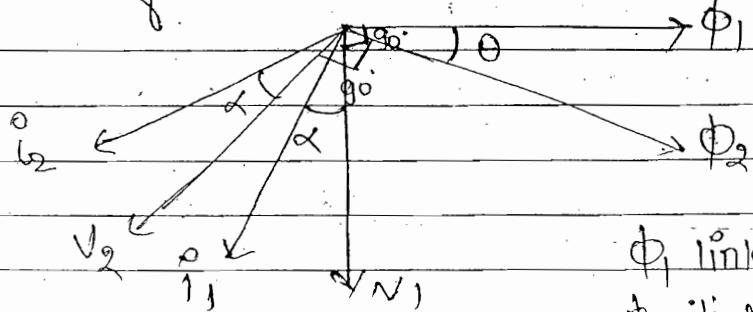
$\theta \rightarrow$ Impedance Angle
due to C_2, C_3, C_4

$$T_D \propto I_f^2 \sin \theta$$

Independent to frequency.



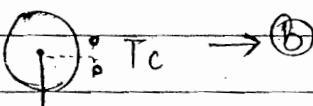
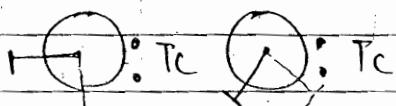
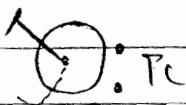
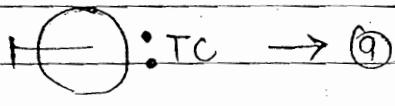
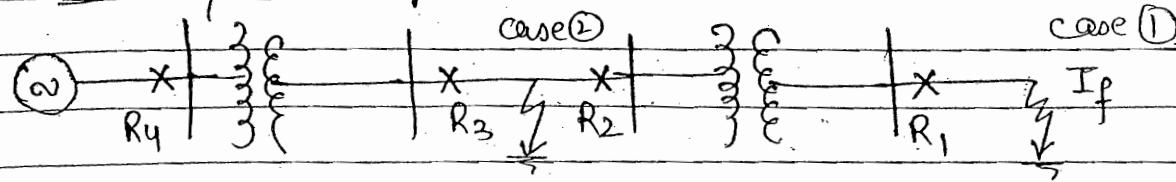
- ϕ_2 due to i_2 , i_2 due to V_1 , V_1 due to ϕ_1 , ϕ_1 due to I_s , I_s due to I_p
- I_p due to I_f



ϕ_1 link with i_2
 ϕ_2 link with i_1

Time Grading

Date _____

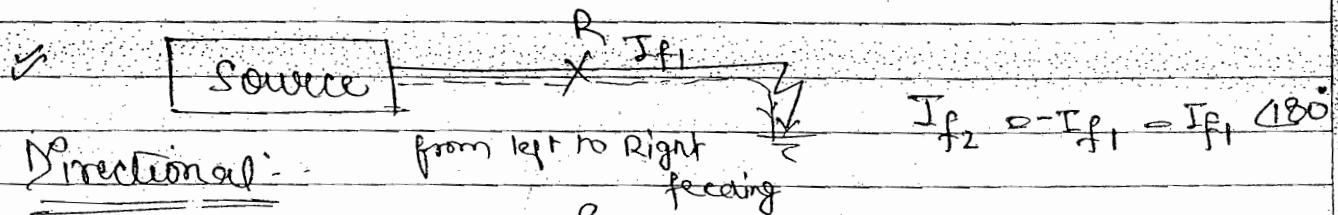


Case (a) :-

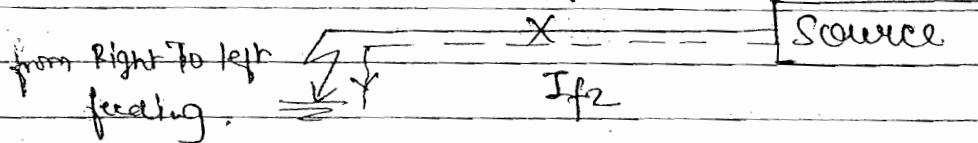
(I_f value low)

In (a) condition, plunger are arranged in this manner, fault is away from source, R_4 will operate first, then $R_3 \rightarrow R_2 \rightarrow R_1$. Not a good sys. So arrangement is done in (b) condition manner. At fault, Sequence of operating Relay $\rightarrow R_1, R_2, R_3, R_4$. When fault occurs, all relay will simultaneously operate, if R_1 get fail, then seq. of operating of Relay $\rightarrow R_2, R_3, R_4$.

Case (2) :- If fault occur b/w R_3 & R_2 , near the source, as $T_D \propto I_m^2$ fault current value is more, so R_3 will operate quickly in less time.
= fault near the source. If value more, away the source I_f value is low



Directional:-



• Symbol Non directional Relay

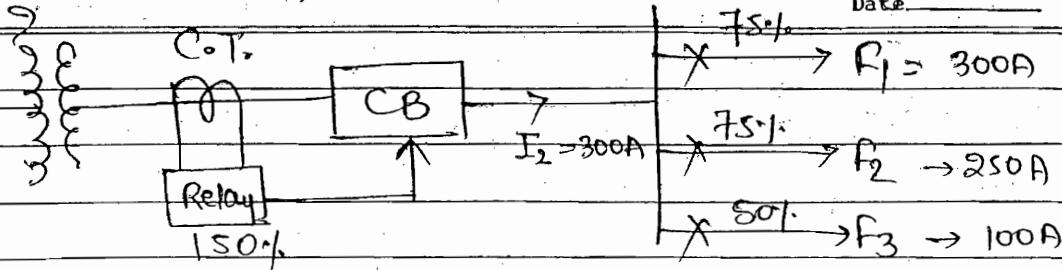
\Rightarrow CB will operate in either direction of fault current.

Current Grading

500/5A

Individually

Date _____



PSB

250 375 500A 625 750 825 1000A

1 2 3 4 5 6 7

50% 75% 100% 125% 150% 175% 200%

$$\text{For } 300\text{A} \rightarrow 100\% = 500 \\ 5\text{A}$$

Now added $F_2 \Rightarrow 300 + 250 = 550$ & it will set to

$$4 \text{ Nob.} = 625\text{A} (125\%) \Rightarrow 125\% \times 5 = 6.25$$

Now again added a feeder F_3 of demand 100A.

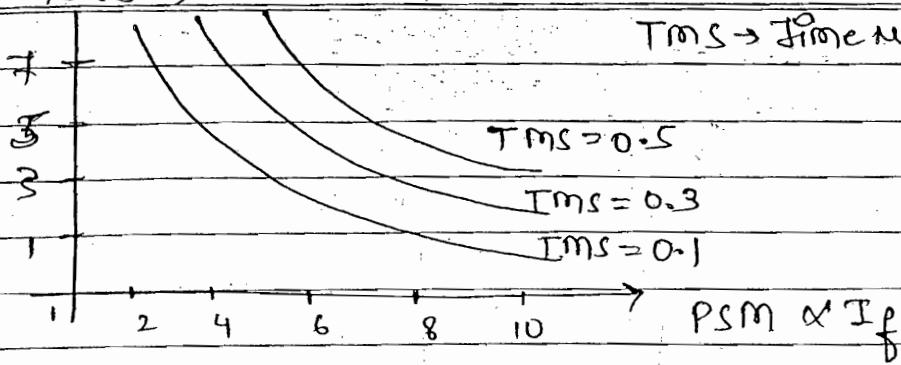
$$\text{Total} = 300 + 250 + 100 = 650 \text{A}, \text{ set to } 180\%. \\ 150\% \times 5\text{A} = 7.5.$$

Now it will get connected to nob. 5.

Time (sec)

Date _____

T_{MS} → Time multiplier setting



IDMT (character of odc Relay)

(1) Pick up current of Relay:-

$$I_{PK} = \% \text{ setting of Relay} \times C.T \text{ Sec Current}$$

(2) Plug setting Multiplier (PSM)

$$PSM = \frac{I_f}{I_{PK}}$$

$I_{PK} \times C.T.$ Ratio

(3) Time of operation of any Relay:-

$$T_o = T_{MS} \times (\text{Time calculated from IDMT graph / Table corresponding to PSM})$$

(4) Time of operation of Back up Relay:-

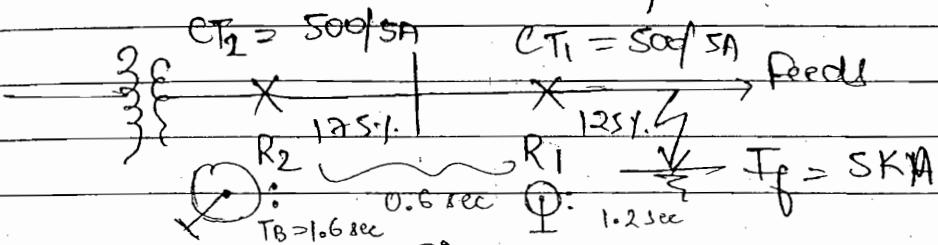
$$T_B = (T_p + T_d)$$

T_p = Time of operation of primary Relay

T_d = Time delay b/w Primary and Back up Relay.

Q Part of pow sys n/w u shown in the fig. The primary relay R₁ has T_{MS} of 0.3. The time delay b/w primary and Back up relay R₁ & R₂ is 0.8 sec. Both Relays having CT Ratio of 500/5A. The IDMT character is given in the Table for the R₁ and R₂. Calculate

- (i) Time of operation of Primary Relay
 (ii) PMS of Back up Relay.



PSM	10	8	5.7	4.5
Time (sec)	2	4	5	8

Solution:- for Relay 1 :- $I_{pk} = \frac{125}{100} \times 5 = 6.25A$

$$\text{PSM} = \frac{I_p}{I_{pk} \times CT \text{ Ratio}} = \frac{5000}{6.25 \times 500} = 8$$

$$T_o = 0.3 \times 4 = 1.2 \text{ sec.}$$

$$\text{for Relay 2 :- } I_{pk} = \frac{125}{100} \times 5 = 8.75A$$

$$\text{PSM} = \frac{5000}{8.75 \times 500} = 5.7$$

$$T_o = T_B = T_p + T_d = 1.2 + 0.8 = 1.8 \text{ sec}$$

Ques for primary or
back up relay

$$TMS \times 5 = 1.8 \text{ sec}$$

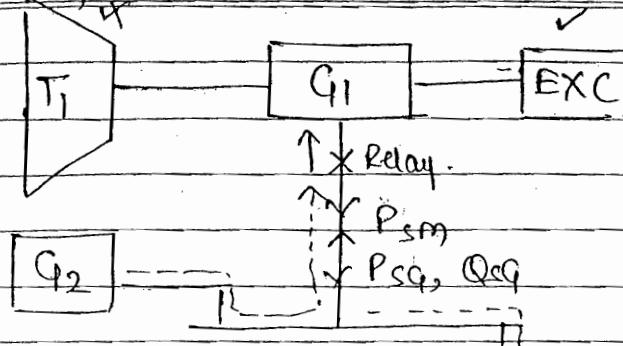
$$TMS = 0.366$$

31/10/14

• Directional OR Reverse Power OR Whitmetric Relay

When the prime mover get fail or stop delivering the power to gen. G₁, G₁ will draw the huge amount of active power from G₂ to drive the Turbine bcoz now it will work as motor bcoz it has flux. It will damage the G₁ wdg, so we use Reverse power relay to watch the flow of power direction.

fail)

 $\uparrow X \text{ Relay.}$ $\uparrow X P_{sm}$ $\uparrow X P_{sg}, Q_{sg}$ Relay \rightarrow Block when powerflows from G_1 to load.

(syn. Gen.)

Relay \rightarrow operate when powerflows from G_2 to G_1 .

(syn. Motor)

- Non directional overcurrent relay: -

$$T_D \propto \Phi_m, \Phi_{m2} \sin \theta.$$

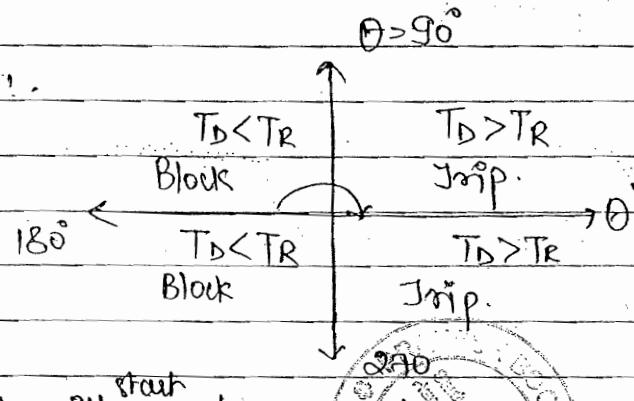
Directional / Reverse power relay:

$$\Phi_{m1} \propto V, \Phi_{m2} \propto I$$

$\sin \theta \longrightarrow \cos \theta$

$$\text{Ideal } \rightarrow [T_D \propto VI \cos \theta]$$

$$[T_D \propto P]$$



- Relay must operate before it will work as motor. ^{start}
speed must be high.

• To get Maximum Torque θ must equal to 0° , for this V and I are in same phase, for this we use Resistive coil, (such RC arrangement).

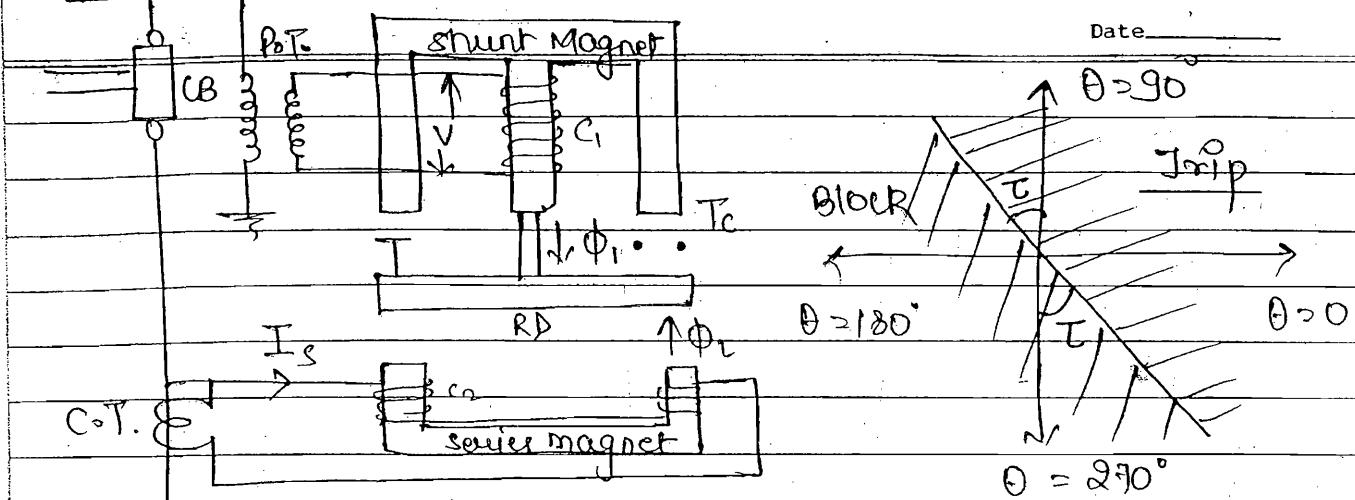
- practically:- $[T_D \propto VI \cos(\theta - \tau)]$

τ = Max. Torque adjustment angle

$$\text{If } \tau = \theta \Rightarrow T_D \Rightarrow T_{D\max} = VI$$

- Never use $\tau = 90^\circ$, otherwise $T_D = VI \cos(90^\circ - 90^\circ) = VI \sin 0^\circ$ which is non directional condition.

Bul-Baz



- T value should lie b/w 0 to 90°

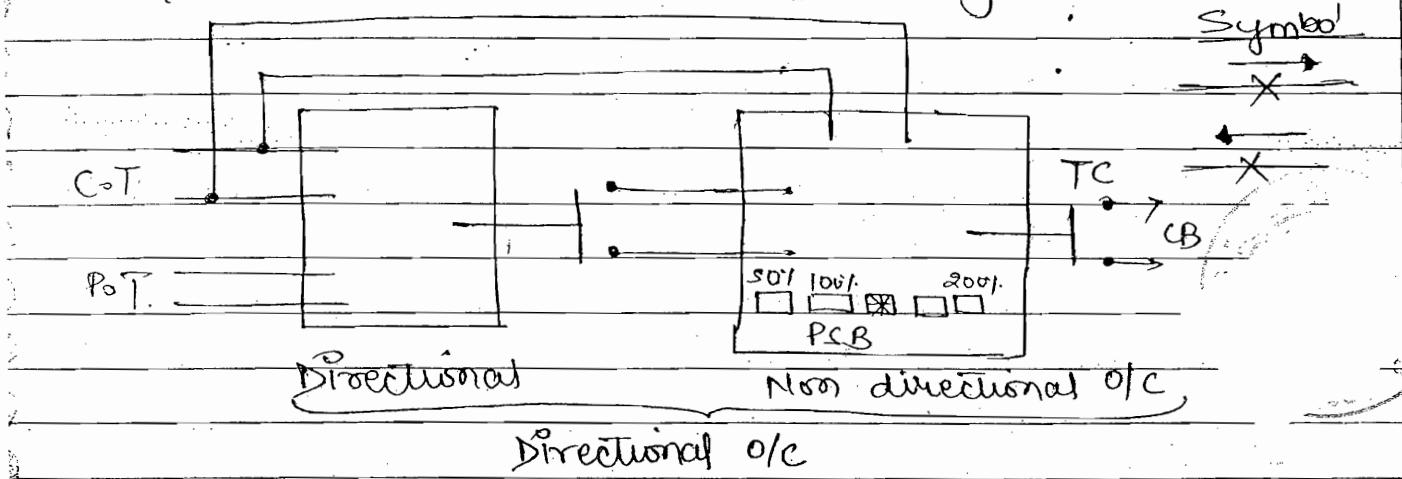
- We make C_1 very highly inductive so we get now $\theta = 90^\circ$ which make $\sin \theta \Rightarrow \sin(90^\circ) = \cos 0^\circ$
To make VI core in phase τ must = 0, (Resistive nature)
for this ϕ_1 and ϕ_2 have phase displacement 90° , to
make phase displacement we use other value.
 T_d max when $\theta = \tau$.

- Directional or reverse power relay is used to produce trip signal if the direction of power is reversed.
- operating T is proportional to the power, so that CT and PT o/p. are applied to the relay
- Max T is required so that it is normally make up of induction cup structure which is working on the principle of induction motor.
- In watt-hour meter Relay an extra τ adjustment angle is provide to get max T .

- Application (1) The Reverse power relay used to protect generator from the failure of prime mover (Turbine)
- (2) In Normal condition if prime mover and excitation is present the syn. generator delivers more

active and reactive power to the load. If the excitation is present and prime mover is failed then the gen. absorbs active power from the other parallel gen. and start working as syn. motor. The Turbine is working as Mechanical load for this Motor. Bcoz of huge Mass of the turbine the motor draws heavy current which damages the engg. To protect the gen from this abnormality Reverse power relay is used

- Directional Over Current Relay:-

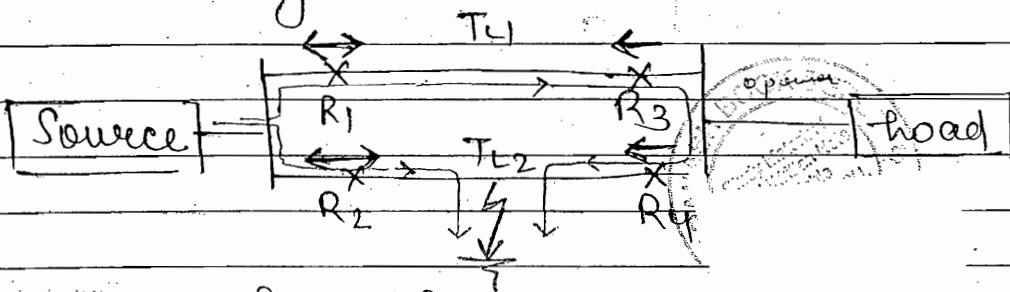


- Directional over current relay containing Both reverse power element and non-directional over current relay In case of power direction is reversed the direction element operates and close the trip contacts which initiates non-directional over current relay. This relay checks whether the reverse current is exceeding the PSN and produce trip signal if it is exceeding which open the CB.

- Application of Non-directional O/C & Directional O/C Relays
 - (1) Protection of parallel feeders :- In case of n feeders source & Relays are Non-directional O/C relay and load and Relays

are directional O/C relays are used.

Under Normal condition power flows from source to load through the parallel feeders. If any fault is occur in one of the line corresponding relay operate isolating the faulty line. so that 50% of power can be transferred from the healthy line.



✓ Relay operate R_2 and R_4 .

✓ If we use R_3 and R_4 also Non-direct then what happens.

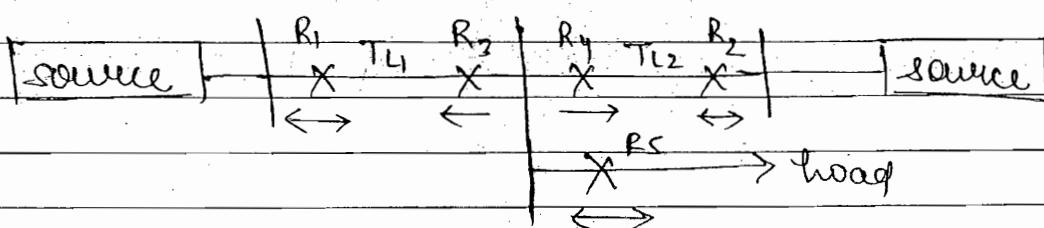
If fault occurs at T_{L2} , R_3 relay get operate \rightarrow Not req.

If we provide time delay $R_4 \geq 0.3$, $R_3 = 0.4$, Then

R_4 will operate, But By this time delay if fault occurs at T_{L1} then T_{L1} will operate which is not required. So we use directional

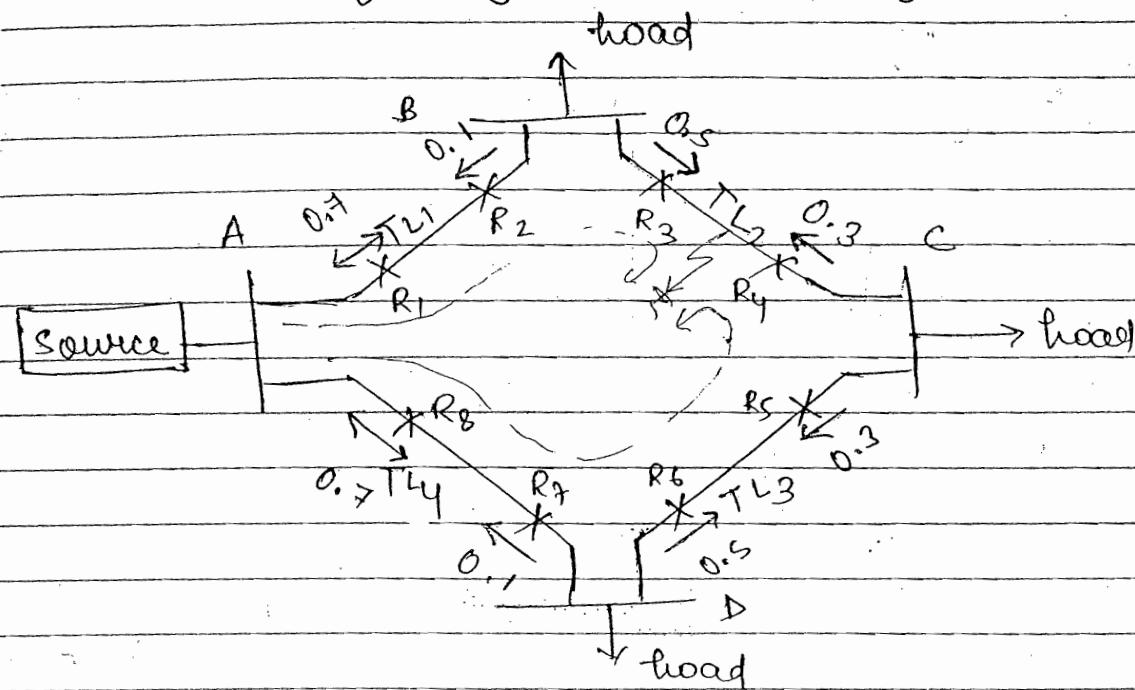
Relay.

Ex:-

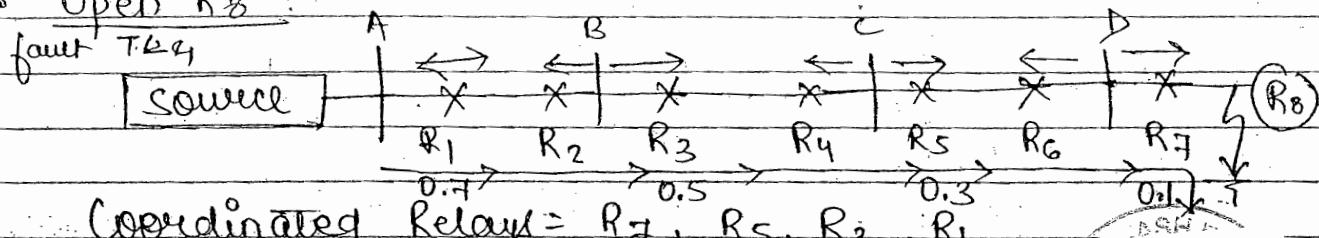


Here R_1 and R_2 are non-direct O/C relay and R_3 and R_4 are direction O/C relay. But in case of R_5 , Bus Bar is source for load so R_5 is non-direct O/C relay.

Protection of Ring Distribution System :-



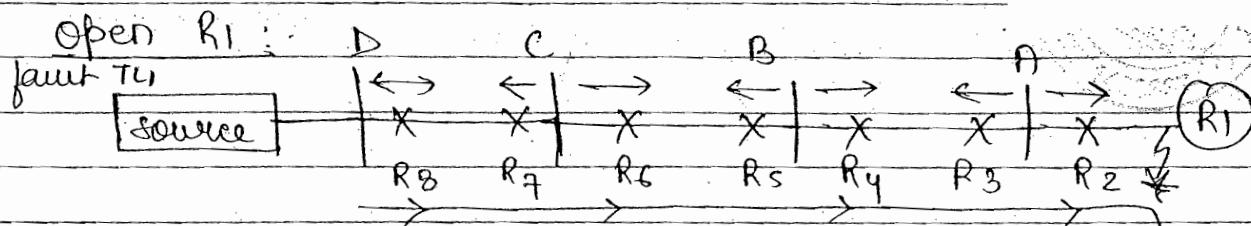
- Open R_3 :



Coordinated Relay = R_7, R_5, R_3, R_1

provide time delay = $0.1, 0.3, 0.5, 0.7$

- Open R_1 :



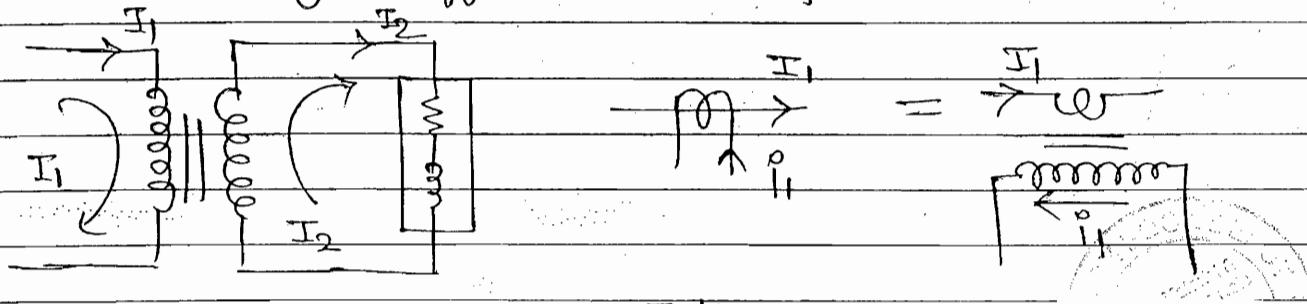
Coordinated Relay = R_2, R_4, R_6, R_8

provide time delay = $0.1, 0.3, 0.5, 0.7$

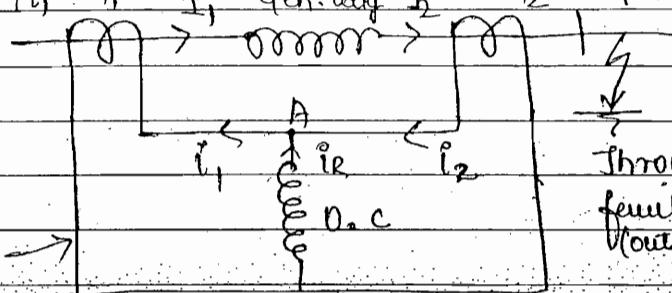
- If fault at $T_{l2} \rightarrow R_4, R_6, R_8$ and R_5, R_7 will operate
time delay $\rightarrow 0.3, 0.5, 0.7, 0.5, 0.7$

- For protection of Ring system Non-directional relays are kept on source side, and directional relays are kept on load side. Time grading is provided b/w the relays for complete protection of Ring system.

- Ordinary Differential Relay :-



I_1/i_1 , C_1 I_1 , Gen. way i_2 C_2 I_2/i_2



At Node A

$$i_R + i_2 = i_1$$

through fault.

(Outside the protect zone)

$$= |i_1| \angle \theta_1 - |i_2| \angle \theta_2$$

$$i_R = I_1 - I_2$$

Ratio C_2 Ratio

If C_1 Ratio = C_2 Ratio = C.Ratio

OC = operating coil of
Diff. Relay.

i_R = Relay current.

$$i_R = \frac{I_1 - I_2}{C\text{ Ratio}}$$

① Trip

$i_R \neq 0$ (Ideal)

$i_R > I_o$ (Practical)

$$i_R = (i_1 - i_2)$$

trip

② Block :-

$i_R = 0$ (Ideal)

$i_R \leq I_o$ (Practical)

$$I_o$$

Block

$I_o >$ Min. pick up current of relay
= spring Restraining Torque

graph: Charact. of Ordinary Diff. Relay.

$$\frac{i_1 + i_2}{2}$$

Power X-Mes have diff. CT Ratios BC02 of voltage up and step-down.

Motor and Gen. have same voltage so same CT ratio.

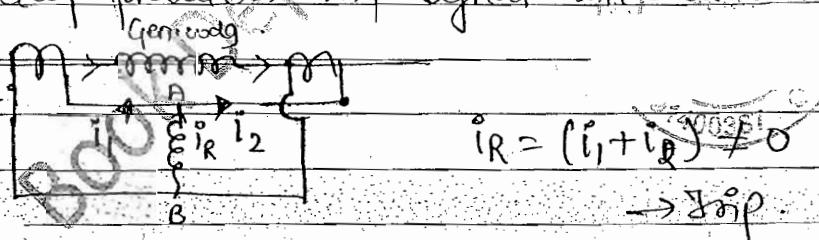
Date _____

- Differential relay is a unit protection relay, used for protection of generator, X-Mes, motor wdg. and Bus Bar protection. Also used to protect X-line. This is called pilot relaying.
- If the phasor difference of two electrical sys. i.e. $I \& V$ exceeding the setting value of relay produces trip signal. This principle is used in the diff. relay.
- Through Fault:- If the fault is occurring outside the unit protection zone is called through fault.
- If the any relay is producing trip signal without any operation is called mal operation of relay.

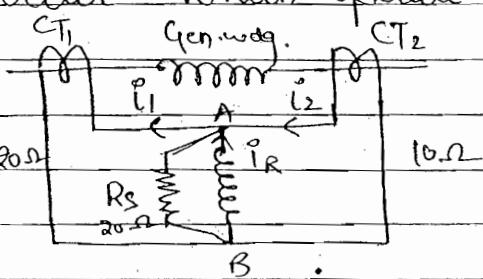
Def. convert

• Disadvantages of Ordinary Diff. Relay:-

- (1) If one of the sides of pilot wire is wrongly connected, Relay produces trip signal without any fault.



- (2) Difference in the length or resistance of pilot wire produces potential difference across the relay coil so that $i_R \neq 0$ occurs which operate the relay without any fault.



To overcome this difficulty a stabilizing resistor is connected in parallel to the relay coil.

$$R_s = \text{Stabilizing Resistor}$$

- Use Π resistor, Not series Becoz we can't cut the cable and place the series Resistor.

(3) If the CT of core of CT is saturated produced trip signal without any fault. But for the outside fault are through fault produce trip.

$$I_f \quad CT_1 \quad CT_2 \quad I_R = i_1 - i_2$$

$$100 \quad 100/1$$

$$100/1$$

$$200 \quad 200/1$$

$$200/2$$

$$400 \quad 400/4$$

$$400/2$$

$$600 \quad 600/6$$

$$600/2$$

$$1-1 = 0 \quad \} \text{ Block}$$

$$2-2 = 0 \quad \}$$

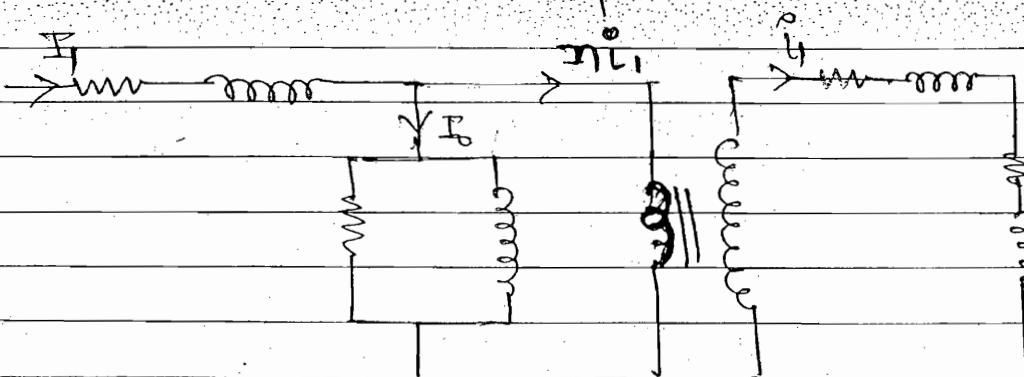
$$4-2 = 2 \quad \} \text{ Trip}$$

$$6-2 = 4 \quad \}$$

↓ saturat?

(4) If CT_1 and CT_2 has different ratio and phase angle error produces trip signal without any fault.

Bcoz of no-load compensation of current phase angle and ratio-error are produce.



$$\begin{array}{c} \rightarrow I_f \\ \rightarrow (I_1 + I_2) \\ C.T_0 \end{array}$$

$$N_1 : N_2$$

$$n = \frac{N_2}{N_1} = \text{Nominal Ratio}$$

$$I_1 = I_0 + n I_2$$

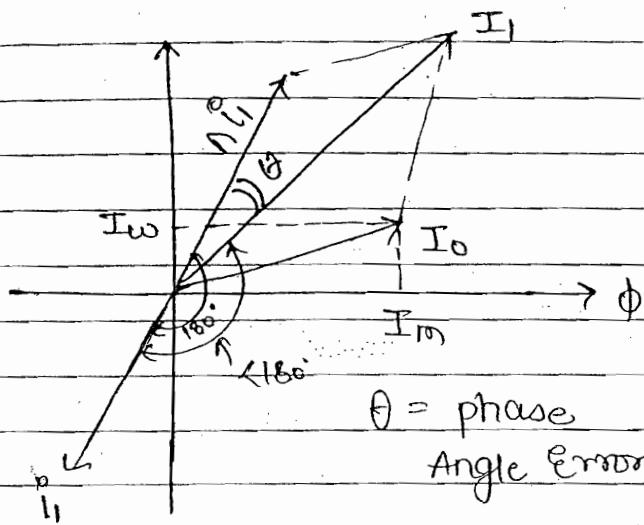
$$I_1 = \text{Actual Ratio}$$

$$\text{Actual Ratio} = \frac{I_1}{i_1} = n + \frac{I_0}{i_1} \quad \text{Ratio Error}$$

Suppose Ideal case.

$$N_1 = 1, N_2 = 100 \quad I_1 = 500; i_1 = 5A$$

$$n = \frac{N_2}{N_1} = 100 > 100 \quad \frac{I_1}{i_1} = \frac{500}{5} = 100$$

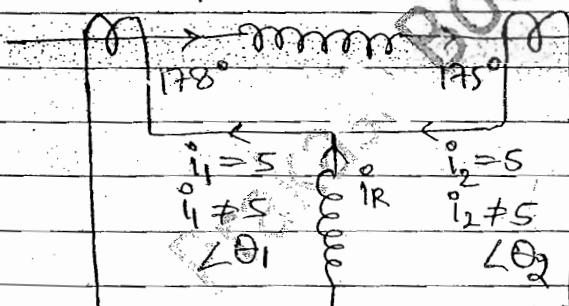


When i_1 transfer to primary it become $n i_1$. Diff b/w $n i_1$ and i_1 $\geq 180^\circ$ (ideal case)

But due to error it is $< 180^\circ$, $\therefore I_0 = n i_1 + I_0$

θ = phase error called Θ
Angle Error

$$CT_1 = \frac{500}{5} = 100 \text{ A.R.} \quad CT_2 = \frac{500}{5} = 100 \text{ A.R.}$$



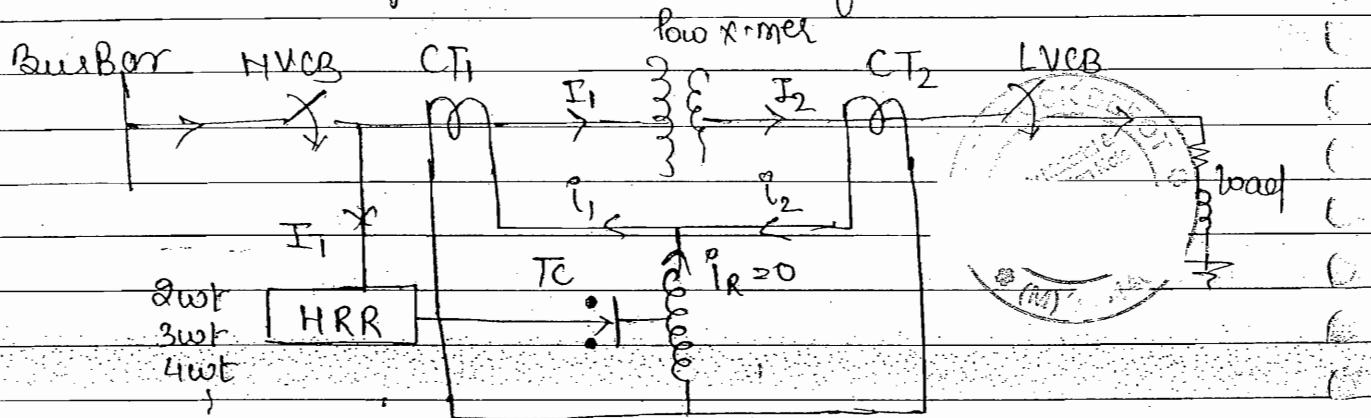
But when the primary current get change, $CT_1 = 101$ and $CT_2 = 99$
 $i_1 \neq 5, i_2 \neq 5$, trip signal
Buz of Ratio Error.

Suppose the angle is 178° in CT_1 side and 175° in CT_2
This causes the phase error.

(5)

(6) During initial charging time of the power X-mel, magnetic inrush current having high magnitude flows, will cause unequal current in the primary and secondary CT's so that relay operates without any fault. To overcome this difficulty harmonic restraining relay is used.

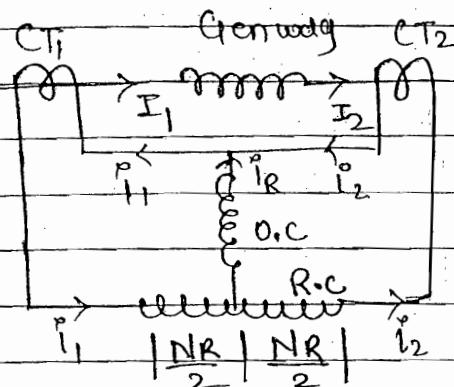
The magnetic inrush current consisting of 2, 3, 4 harmonic signals. These signals are filter by the harmonic restraining relay which will produce additional restraining torque so that relay will not operate during charging time of power X-mel.



- During charging HVCB → closed, current I_1 will flow through CT₁ and HRR. HRR produces additional restraining torque, not to operate the relay with HVCB get close. (2wt, 3wt, 4wt)

$I_1 \neq 0, i_1 \neq 0$ But $I_2 = 0, i_2 = 0, i_R \neq 0$, But restraining torque is not allow the CB to get open, after 10-5 minutes (charging) LVCB also close, so that $I_1 = I_2, i_1 = i_2$ and $i_R = 0$

% Differential / pilot wire / Merz price / Biased Scheme Relay



$$\begin{aligned} \text{operating mmf} &= N_o i_o \\ \text{Restraining mmf} &= \frac{N_R i_1}{2} + \frac{N_R i_2}{2} \\ &= N_R \left(\frac{i_1 + i_2}{2} \right) \end{aligned}$$

$$N_o i_o = N_R \left(\frac{i_1 + i_2}{2} \right)$$

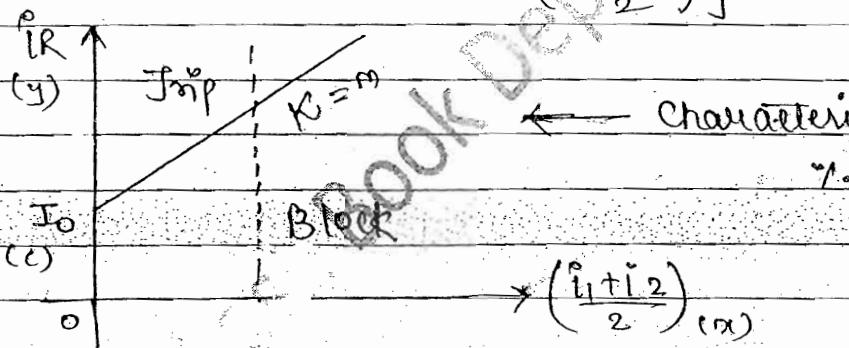
O.C = operating coil

R.C = Restraining coil.

$$\frac{i_o}{N_o} = \frac{N_R}{N_o} \cdot K = \% \text{ setting}$$

$$(1) \text{ Trip } i_o > \left[I_{o\text{set}} + K \left(\frac{i_1 + i_2}{2} \right) \right] ; \text{ spring Torque} \\ ; K \left(\frac{i_1 + i_2}{2} \right) = \text{Restraining coil Torque}$$

$$(2) \text{ Block: } i_o \leq \left[I_{o\text{set}} + K \left(\frac{i_1 + i_2}{2} \right) \right]$$



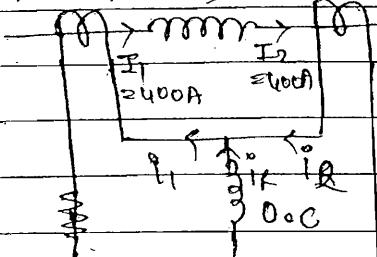
In the % Diff. Relay, during abnormal conditions all when current in R.C flow, spring torque + restraining T also \uparrow with current value so relay will not operate.

But during fault condition, fault current value is very high it will operate the relay as operating T is higher than (spring T + restraining T).

Solution (1) (b) Ordinary Diff. $i_1 = I_1 = 400 \text{ A}$ $\frac{\text{CT Ratio}}{= 5} = 5.06 \text{ A}$

$$\text{CT}_1 = 400/5 = 80$$

$$\text{CT}_2 = 400/5 \quad i_2 = \frac{I_2}{\text{CT}_2 \text{ Ratio}} = \frac{400}{80} = 4.94 \text{ A}$$



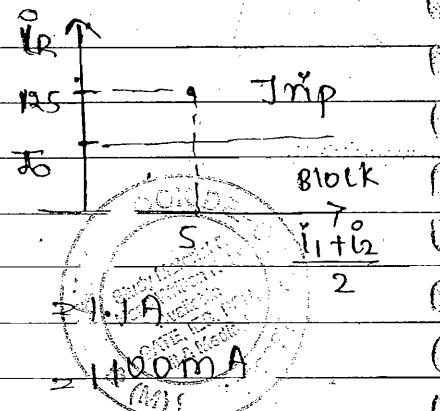
(B1)

CT₂ Ratio

$$\frac{i_1 + i_2}{2} = \frac{5.06 + 4.94}{2} = 5$$

$$i_R = i_1 - i_2 = 5.06 - 4.94 = 0.125 \text{ A}$$

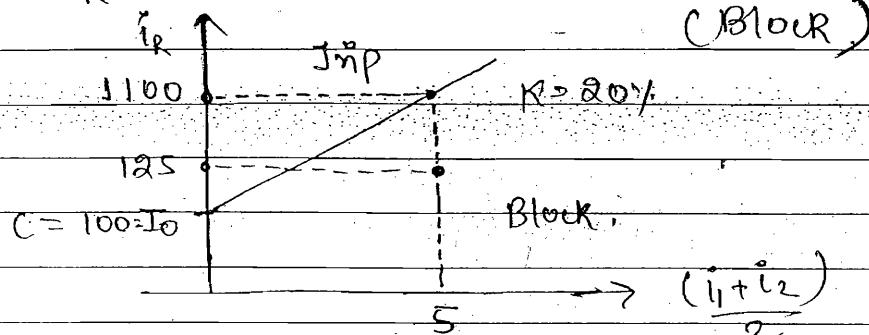
$$= 125 \text{ mA}$$

 $I_0 = 100 \text{ mA}$ (given) $I_R = 125 \text{ mA}, i_R > I_0$ (Trip)③ % Diff. :-

$$K > 20\% > 0.2$$

$$I_0 + K \left(\frac{i_1 + i_2}{2} \right) = 100 \times 10^{-3} + 0.2 \times 5$$

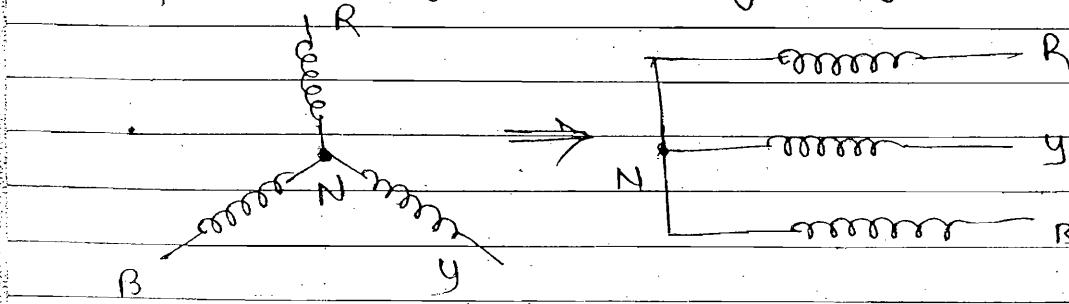
$$i_R = 125 \text{ mA} < 1100 \text{ mA}$$

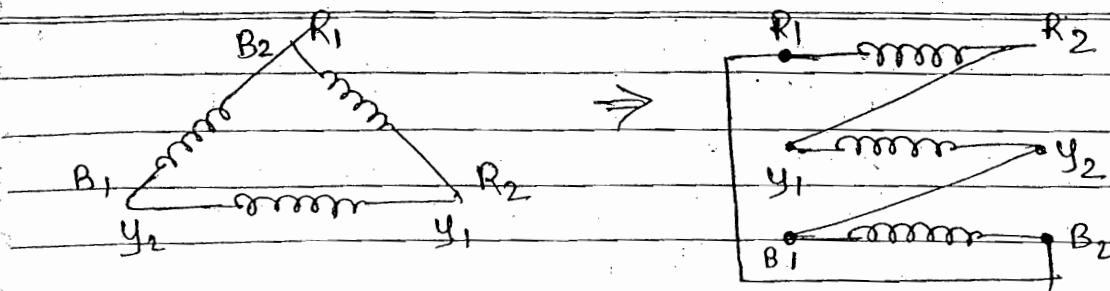


Relay current > 125

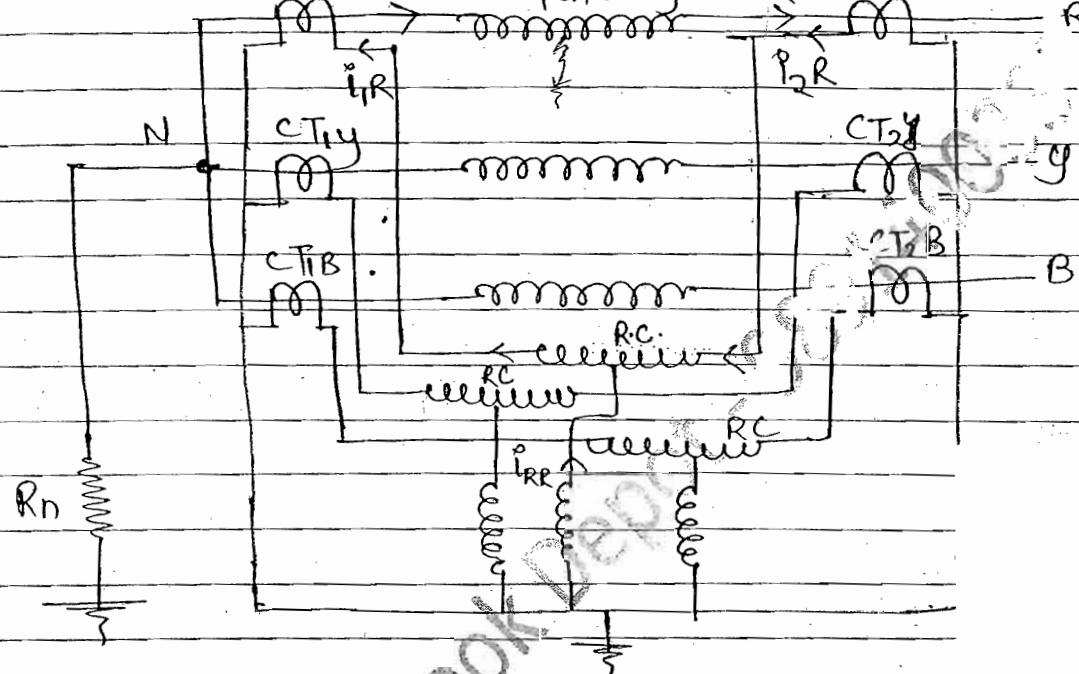
corresponding to 5
value → Block region.

- Protection of 3-Φ Gen wdg using % Diff. Relay :-





CT_{T1} i_R Genwdg. i_R CT_{2R}



• When fault occurs in any phase, for Balance condition all phase CB will get open.

✓ Protection of 3- ϕ X-mel using % Diff Relay:-

POWER X-MER

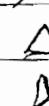
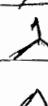
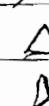
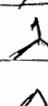
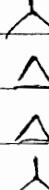
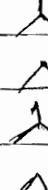
CURRENT X-MER

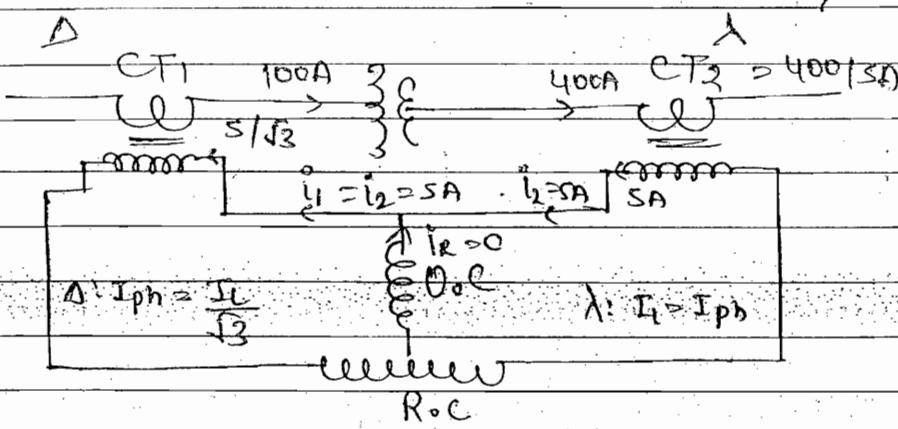
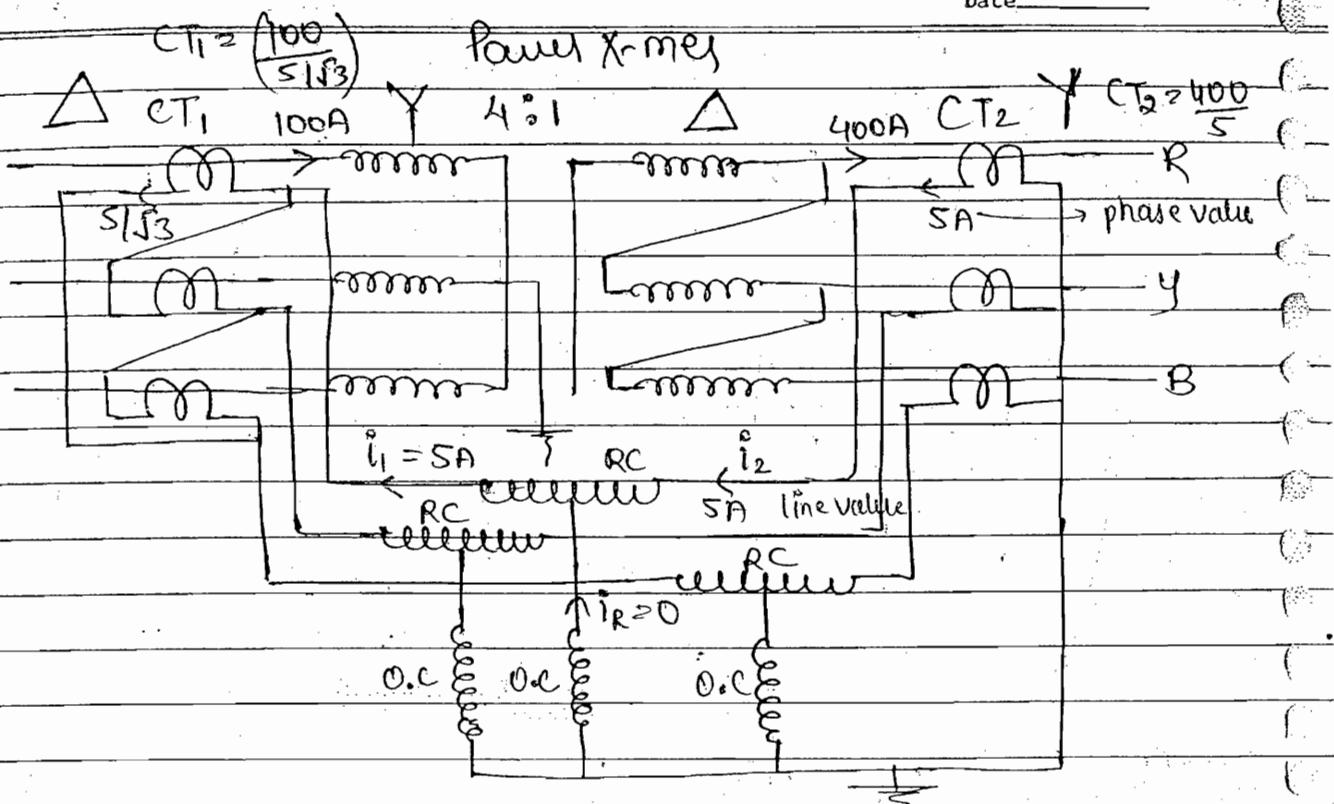
Primary

Secondary

CT_1

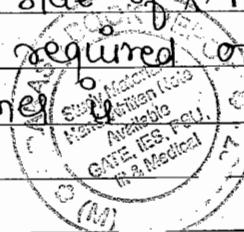
CT_2





Q A 3- ϕ 13.2/33 KV pow x-mel is protected By Merz principle protection. The CT ratio on LV side of x-mel is 400/5A. Calculate the CT ratio required on the HV side of pow-xmel If the x-mel is connected

- ① Y Δ ② $\Delta Y \left(\frac{100}{S\sqrt{3}}\right)$



Solution $13.2/33 = 4:1$
 V_2/V_1 .

$CT_2 = \frac{400}{5} \text{ min}$

$\frac{I_2}{I_1} = \frac{V_1}{V_2} \quad I_1 = \frac{400}{4} > 100$

- Inside the CT, per phase values of current

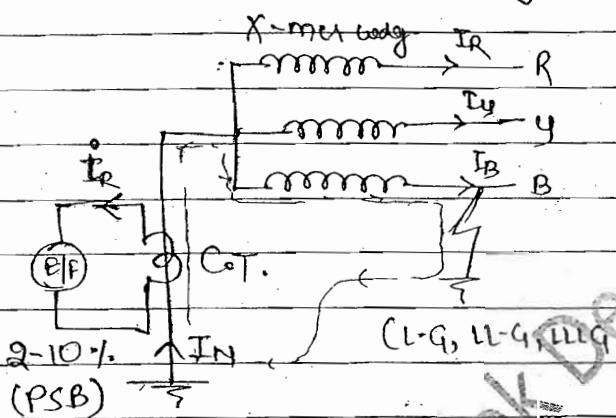
- In RC line value of current need.

- Secondary current at $CT_2 = 5 \text{ A}$. $\lambda \Rightarrow I_{ph} = I_L = 5 \text{ A}$
we required $i_R = 0$ so $i_{ph10} = 5 \text{ A}$.

- $CT_1 \rightarrow \Delta$ connected so $i_{ph} = \frac{5}{\sqrt{3}}$ $I_{ph} = \frac{I_L}{\sqrt{3}} \therefore \Delta$.

3/11/2014

• Earth Fault Relay:-



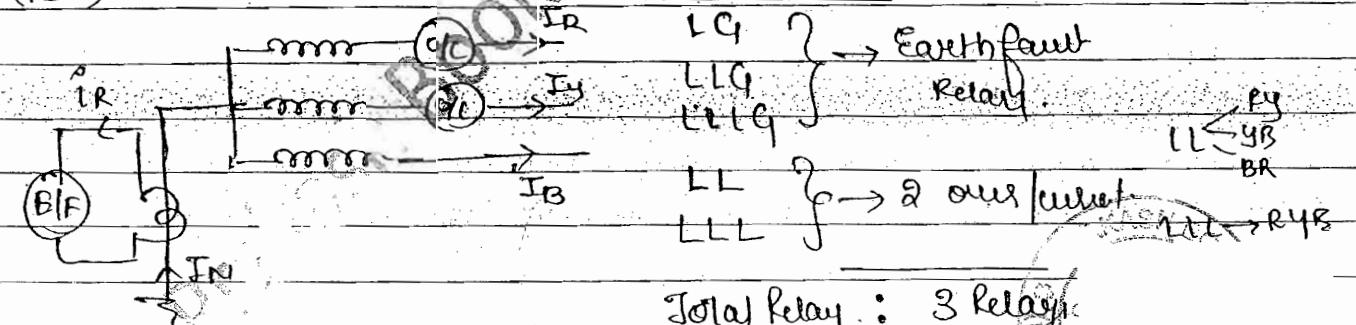
- At No fault $I_N = 0, i_R = 0$

- over-current relay.

- At fault $I_N \neq 0, i_R \neq 0 \rightarrow$ trip

- Only operate at Earth fault. For phase fault. 3 relays required.

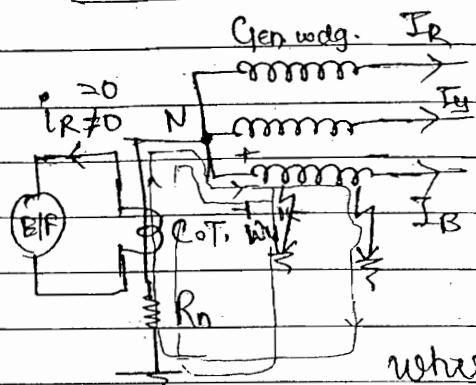
S.O.C Fault.



Total relay : 3 Relays

- Earth fault relay is Basic over current or directional over current relay with flexible value b/w 2 to 10%.
- It is used to identify ground faults like L1-G, L1-Y, L1-B. For complete protection of 3-φ sys. The no. of relays required are 3 relays i.e. one earth fault relay and two over current relays.

• Restricted Earth fault Relay:- (Generator)



% protected

% winding unprotected :-

$$= \% \text{ WU} = \frac{I_0 R_n \times 100}{V_{ph}}$$

where I_0 = mispick up current of Relay \times CT Ratio
 R_n = Neutral Resistance.

V_{ph} = Gen. phase voltage = $N_c / \sqrt{3}$.

$$\boxed{\% \text{ Wdg. protected} = 100 - \% \text{ WU} \cdot 1.}$$

$$\uparrow I_f = \frac{V_{ph}}{X_{th}} \quad \uparrow I_f = \frac{V_{ph}}{X_{th}}$$

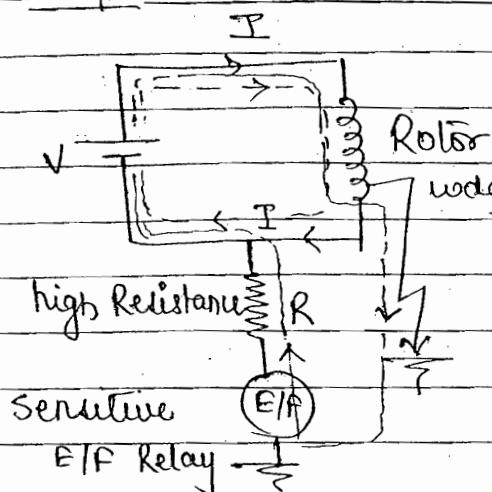
• For improving sys. stability Gen. Neutral is connected to the ground through selector i.e. Resistance grounding is used. Because of this resistance if any ground fault occur some % of wdg. cannot be protected in the generator for complete protection of gen. wdg. % diff. relay is associated with the restricted earth fault relay.

• At less No. of turns, less voltage induce, less I_f value, goes through R_n . But $I_0 > 0$, does not operate the relay.

Q. 8 $\% \text{ WU} = \frac{0.95 \times 1000 \times 5}{5 \times 10^3 / \sqrt{3}} \times 100 = 11.8 \cdot 1.$

Wp V. = $100 - 11.8 = 88.2 \cdot 1.$ Ans.

• Gen. Rotor E/F Relay:



- Normal condition (Blue colour)

- At fault. (Red colour)

- Under Normal condition current do not flow high Relay due to high Resistance. If any fault (ground) occur the fault current flows through sensitive E/F relay and produces trip signal if it is exceeding the setting value of Relay.

• Protection of 3φ - x-mer:

(1) HV O/C

(2) HV directional O/C

(3) HV O/V

(4) HV E/F

HVCB

I_1

I_2

V_1

V_2

oil tank

conservator

Buchholz

Relay

chamber

(5) % Diff relay (6) Buchholz Relay

(7) Over flux Relay (8) LV O/C

(9) LV direction O/C (10) LV O/V

(11) LV E/F

• Buchholz Relay

mercury switch

Gas sample

Gas

float valve

Alarm

J_0

from oil

Tank

J_0

conserv-

ator

oil sample

ALARM OFF (Block)

Mercury
switch

mm

No connection

$I = 0$

Downloaded From www.gatenotes.in

ALARM ON (trip)

conduct

mm

$I \neq 0$

Downloaded From www.gatenotes.in

• Death of fault

Construction parts

winding

OLTC

Core joints

Chemicals

C_2H_2 , H_2

C_2H_2 , CH_4 , H_2

CH_2 , C_2H_6 , H_2 , CO_2

CH_2 , CH_4 , H_2 , CO_2

- Buchholz relay is gas actuated relay used for protection of x-mes from the internal or incipient faults.

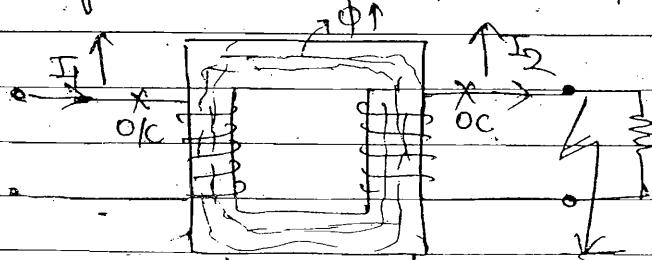
- If the intensity of fault is low value produces alarm signal initially if the intensity of fault is very high produces trip signal by opening LV and HV C.B.
- It is most efficient for identification of internal fault. But the time of operatⁿ is more and hence it is associated with % diff. Relay, for complete protection of power x-mes.

• Over flux Relay :- $V = 4.44 f \Phi_m N$ BOOK DEPT. OF MA (V) P

(1) $V/f > 1.1$ for 2 minutes \Rightarrow Trip

(2) $V/f \leq 1.1 \Rightarrow$ Block.

- At the rated voltage and freq. the flux produce in the x-mel is consider as 100%. If due to fault or freq. variation or internal damage to the x-mel. If the Φ is ↑ By 10% more than the rated value the timer is set for 2 minutes. so that produces trip signal.



$$\uparrow \Phi_m = 110 \text{ wb} \rightarrow 2 \text{ minutes} \rightarrow \text{Trip}$$

~~signature~~

• Protection of Generator :-

STATOR FAULT:-

- 1) Inter-phase fault $\xrightarrow{\text{same phase}}$ Split phase relay
- 2) phase-phase fault $\xrightarrow{\text{op. diff. Relay}}$
- 3) Earth fault $\xrightarrow{\text{Restricted E/F Relay}}$

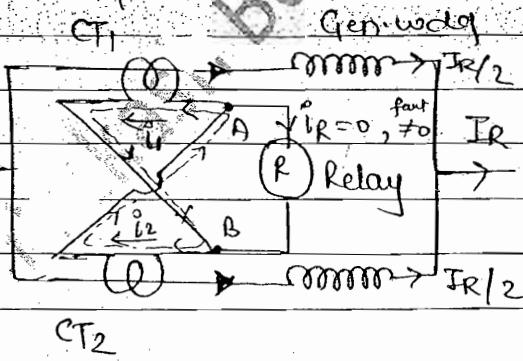
ROTOR FAULT:-

- 4) Rotor earth fault $\xrightarrow{\text{Sensitive E/F Relay}}$.

EXTERNAL FAULT:-

- 5) Failure of prime voltage $\xrightarrow{\text{reverse power Relay}}$
- 6) " Excitation $\xrightarrow{\text{over Mho Relay}}$
- 7) " Cooling Medium $\xrightarrow{\text{Temp. Sensitive Relay}}$
- 8) Over load $\xrightarrow{\text{O/C Relay}}$
- 9) Over speed $\xrightarrow{\text{Mech. Centrifugal Relay (Flyball Governor)}}$
- 10) Unbalanced loading $\xrightarrow{\text{Negative sequence current Relay}}$
- 11) Over voltage $\xrightarrow{\text{O/V Relay}}$.

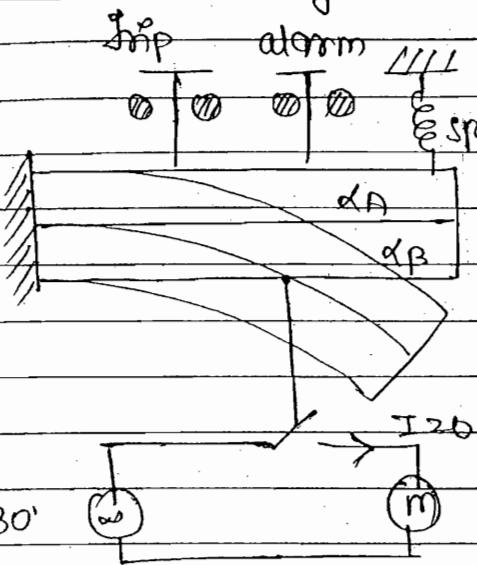
• Split-phase Relay:



- Split phase relay is used to identify the fault occurring within the same phase of the generator.
- Two CT's are connected Back to Back. Under normal condition the current through relay is zero so that relay \rightarrow Block.

- If any S.O.C or O.C fault occurs at any one of II path potential diff. occur. across the relay which produce trip signal.

• Thermal Relay:



→ Thermal relay consisting of Bi-metallic strip made of Ni and chromium.

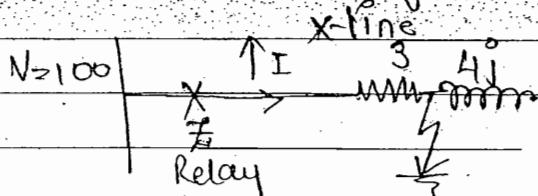
→ the thermal expansion coefficients of these metal are different so that produce bending depending on the temp. change. This principle is used in Bi-metallic switch for :-

(1) Protection of overloading of electrical motors,

Gen. etc. (2) Used in mcb (3) Used in A.C. Refrigerator and iron box for temp. control.

for high capacity gen. more than 5MVA temp. sensitive Relay like thermocouple, RTP are used for protection of engg. from the failure of cooling medium.

• Protection of X-line Using Distance Relay:-



$Z_f = \frac{V}{I}$ Impedance seen by the relay during fault.

$Z_{rl} = \text{Actual or replica impedance of line without any fault.}$

= Setting value of Relay (PSB)

✓ Healthy (No fault)

$$Z_L = R + jX_L \\ = 3 + j4$$

$$|Z_L| = 5$$

$$I = \frac{100}{5} = 20 \text{ A.}$$

✓ Fault $I \uparrow \Rightarrow I = 50 \text{ A.}$

$$Z_f = \frac{100}{50} = 2 \Omega$$

$$|Z_f| \geq |Z_{rl}| \rightarrow \text{Trip}$$

$$|Z_f| < |Z_{rl}| \rightarrow \text{Block}$$

• Universal Torque Equation :-

$$T_D = K_1 I^2 + K_2 V^2 + K_3 VI \cos(\theta - \tau) - K_4$$

where T_D = operating time $K_1 I^2 = \text{O/c}$ $K_2 V^2 = \text{O/v}$

$K_3 VI \cos(\theta - \tau)$ \rightarrow Directional

K_4 = spring.

restraining Torque.

ex:- Over Current Relay:-

$$\text{Assume } K_2 = K_3 = 0, \quad T_D = K_1 I^2 - K_4$$

① Trip. $T_D > 0$

$$K_1 I^2 > K_4$$

$$I > \sqrt{\frac{K_4}{K_1}}$$

② Block $T_D \leq 0$

$$K_1 I^2 \leq K_4$$

$$I \leq \sqrt{\frac{K_4}{K_1}}$$

I = fault current, $\sqrt{K_4/K_1}$ = P.S.B value of O/c relay.

(1) Impedance (Z) Relay:-

Assume $K_3 = 0$, K_4 very small $K_2 = -\infty$

$$T_D = K_1 I^2 - K_2 V^2$$

current \rightarrow Restraining

Impedance Relay \rightarrow Voltage Restraining - over current relay

✓ Trip ($T_D > 0$) \rightarrow Block $T_D \leq 0$ $[Z_f \geq Z_L]$

$$K_1 I \geq K_2 V^2$$

$$\sqrt{\frac{K_1}{K_2}} \rightarrow \left(\frac{V}{I} \right)$$

$$\sqrt{\frac{K_1}{K_2}} = Z_L$$

$$\frac{V}{I} = Z_f$$

$Z_L > Z_f$
$Z_f < Z_L$ or

✓ locus of Z -Relay:-

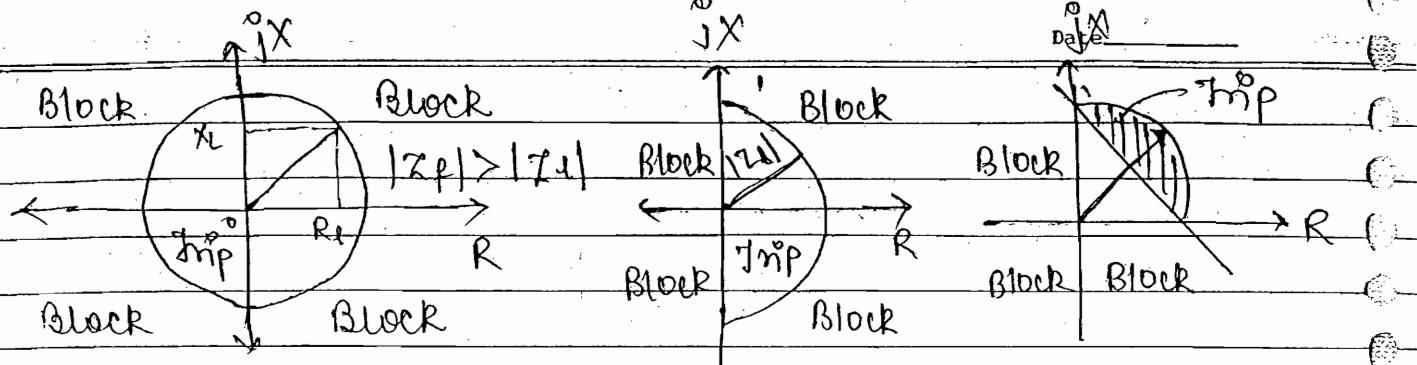
$$Z_L = R_L + j X_L$$

$$|Z_L|^2 = R_L^2 + X_L^2 \rightarrow (1)$$

eqn ① represents circle equation

$$r^2 = x^2 + y^2$$

where $r = |Z_L|$



Non-directional Z -Relay. Directional Z -Relay. Single Imped. relay.
 → all quadrants. 1st & 4th quad. 1st qu. certain appli only.
 if required.

(2) Reactance (X) Relay

Assume $K_2 \geq K_3 \geq 0$

$$T_D = K_1 I^2 - \underbrace{K_3 V I}_{\text{restraining}} \cos(\theta - \tau)$$

① Trip

$$K_1 I^2 > K_3 V I \cos(\theta - \tau)$$

$$\frac{K_1}{K_3} > V \cos(\theta - \tau)$$

Reactance relay is a directional restraint over current relay.

Assume $\tau = 90^\circ$, $\frac{V}{I} = Z_f$.

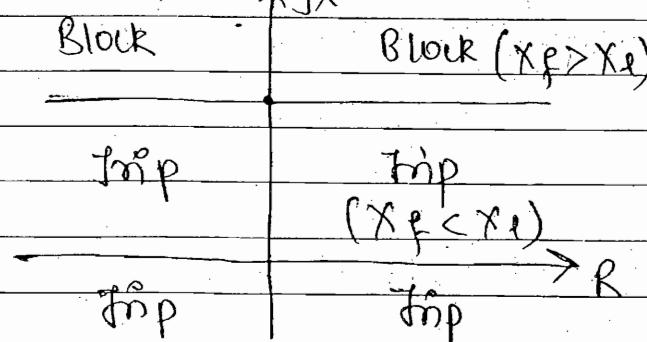
$$\frac{K_1}{K_3} = X_f$$

Zone of X -relay is a straight line passing through $(0, X_f)$

$$X_f > Z_f \cos(0 - 90^\circ)$$

$$X_f > Z_f \sin 0$$

$$Z_f \sin 0 = X_f$$

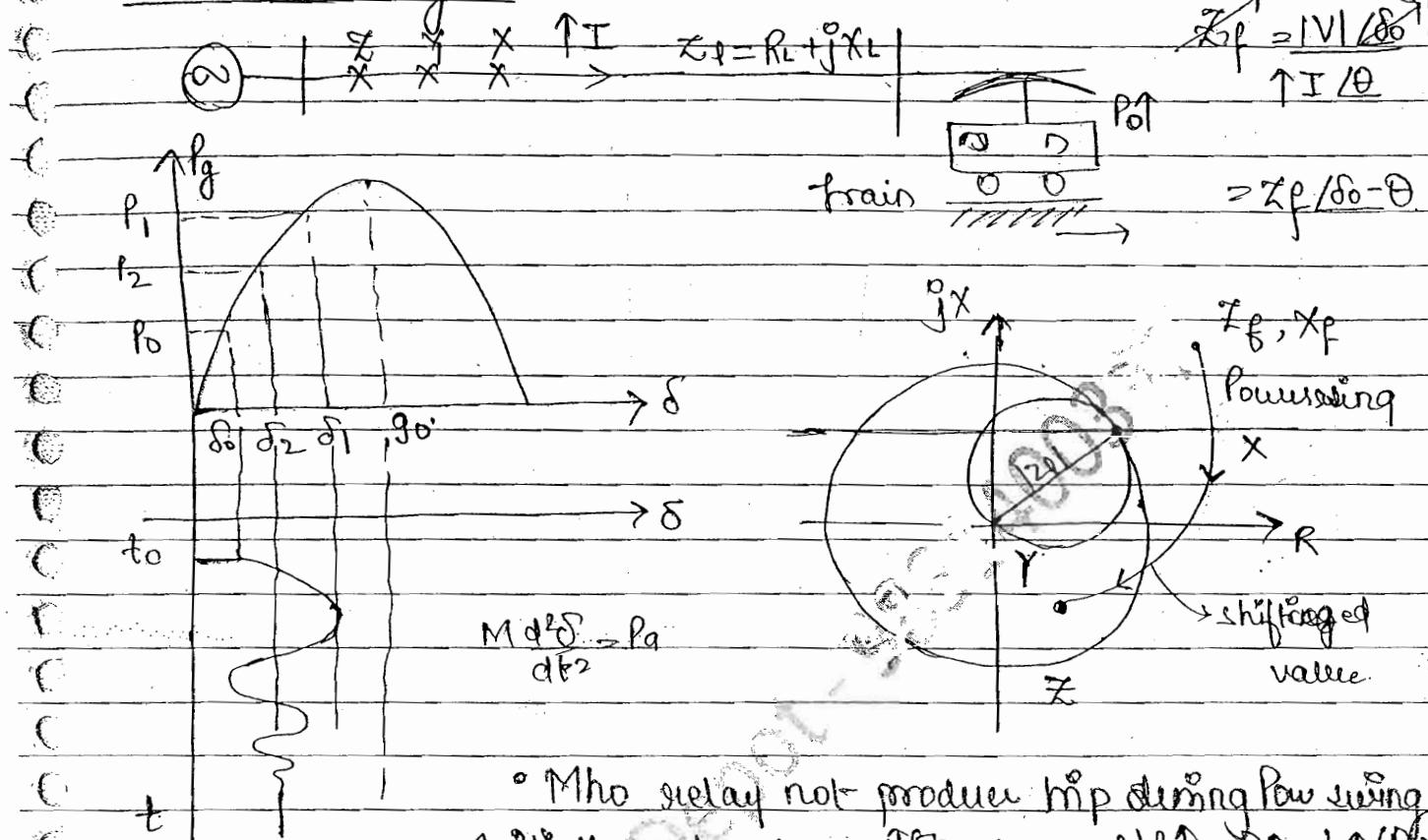


$X_f > X_L$	Trip
$X_f < X_L$	Block

② Block

$$X_f \geq X_L$$

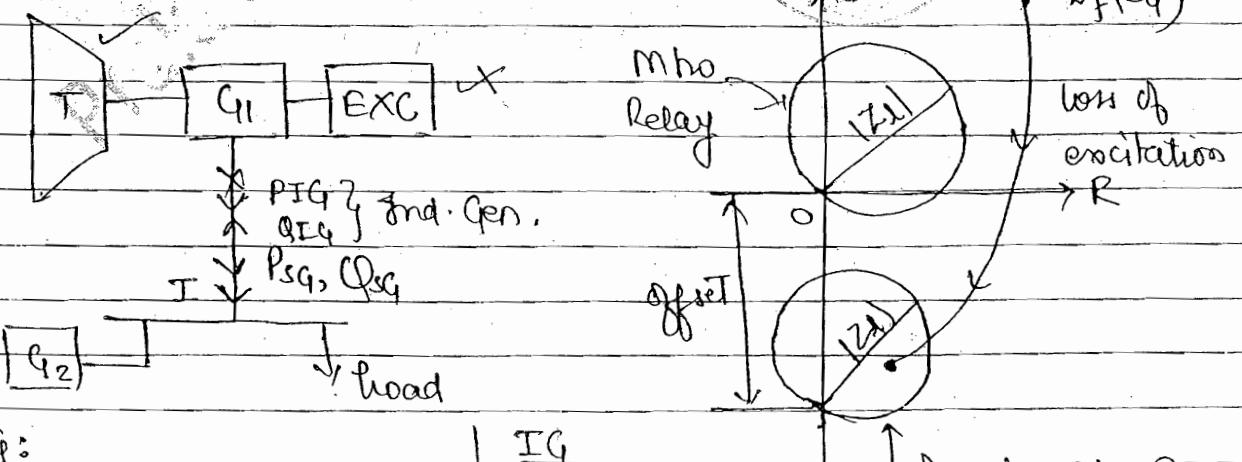
• Power Swings :-



• Mho relay not produce trip during Power swing

- Initially when demand (train start) $P_0 \uparrow$, $\delta \uparrow$, $t \uparrow$ (P_1)
- When train attain speed, Park, $\delta \downarrow$ t_1 and oscillate, and finally settle to stable new pt. (P_2)

• Offset Mho Relay:



SG:

$$Z_f = \frac{|V|}{|I| \angle \theta} = Z_f / \theta$$

IG

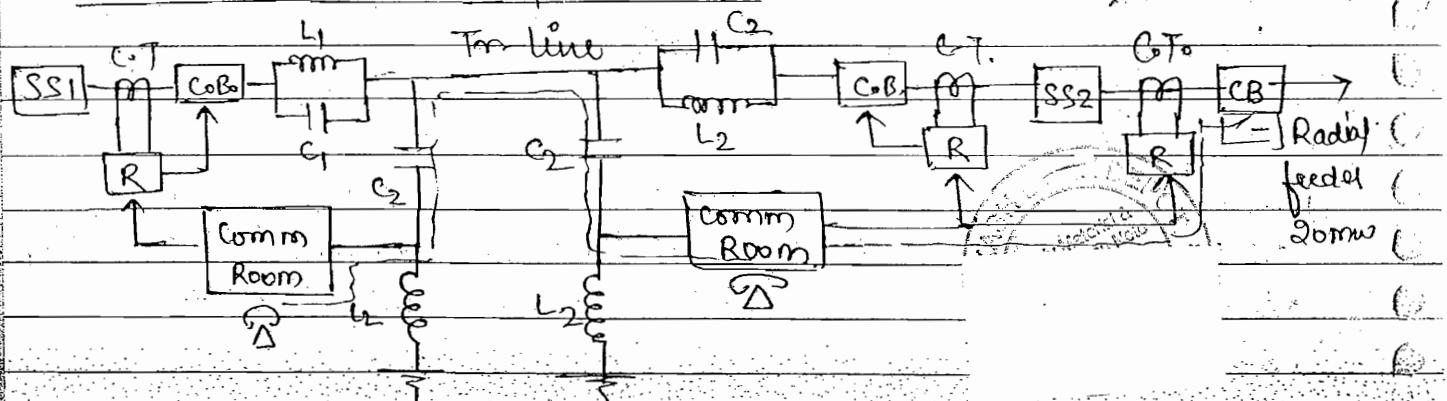
$$Z_f = \frac{|V|}{|I| \angle \theta}$$

$$= Z_f \angle \theta$$

Offset Mho Relay

- Under Normal condition syn. gen. delivers active and reactive pow. to the load If the turbine is present, excitation is failed. Then it will deliver leading VAR's and absorb lagging VAR's. And also deliver the active power. This change of Reactive power flow with in the gen. produces unbalanced causes damage to the gen. wdg. To protect the gen. from the offset MHO relay is used. which is basically a mho relay for which an offset is added for identification of loss of excitation.

• Current Carrier Protection :-

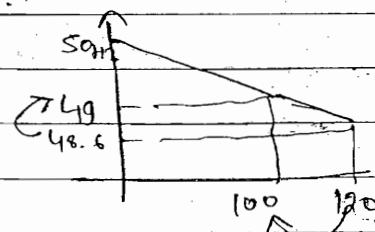


• Fine traps $f_1 = \frac{1}{2\pi\sqrt{L_1 C_1}}$ $\Rightarrow 50\text{Hz}$.

• Wave trap $f_2 = \frac{1}{2\pi\sqrt{L_2 C_2}}$ \Rightarrow Audio freq.

- Current Carrier protection is used:-

- power line carrier protection
- SCADA
- load frequency control

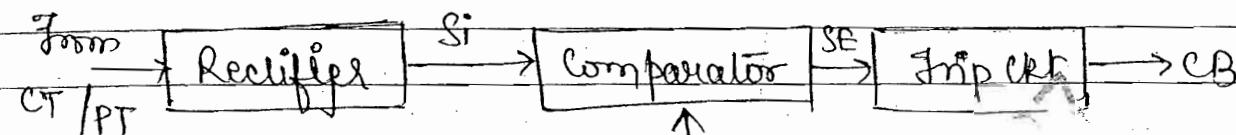


- It consisting of fine trap and wave trap LC tuned circuit: fine trap unit offers low impedance for

power freq. and high fmp. for the communication freq.

the wave trap unit is used low impedance for audio freq. and high fmp for power freq.

- Static Relay: -



S_{REF} [setting value of relay]

$$SE = Si - S_{REF}$$

① If $Si > S_{REF} \Rightarrow SE > 0 \Rightarrow$ Trip

② If $Si < S_{REF} \Rightarrow SE < 0 \Rightarrow$ Block

- Advantages: -

- | | |
|-------------------------------|-----------------------|
| ① Low power consumption. | ② Store data |
| ③ Easily interface with comp. | ④ More reliable |
| ⑤ Less maintenance. | ⑥ Easily programmable |
| ⑦ Low cost | ⑧ Occupies less space |
| ⑨ Stable operation | |

Date _____

$P_t \propto (F+25)$ Corona power loss is more in HVAC compared to HVD C

Disadvantages of Corona

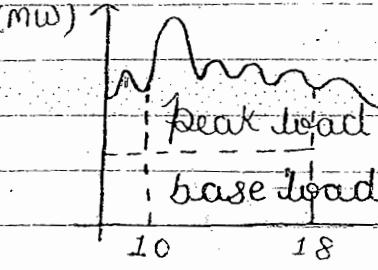
- 1) Power loss occurs.
- 2) Produces interference to other lines.
- 3) Charging current increases.
- 4) Intensity or peak value of the lightning
- 5) Surge is reduced if lightning surge initiates corona.

Economic / Variable load factor

S.S. → Hospitals (24 hrs)
 → Colleges (9 A.M - 5 P.M)

→ Shops (10 A.M - 10 P.M)

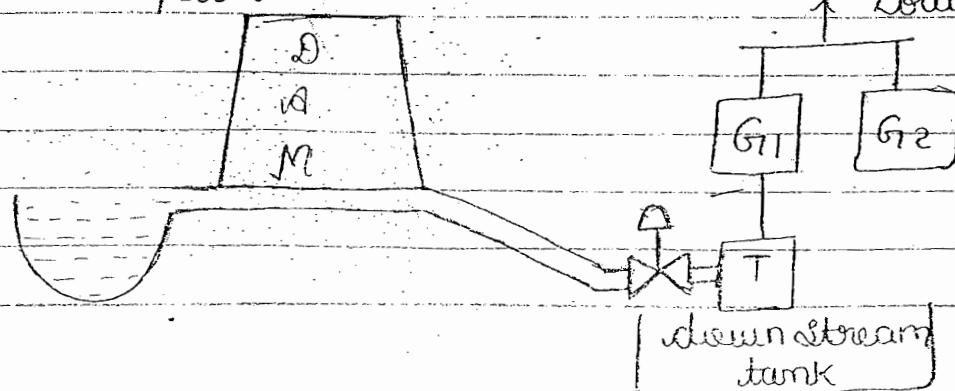
$P(\text{MW})$



Base load plants Peak load plants

- | | |
|------------------|--------------------------|
| 1. Thermal | 1. Pumped storage plant |
| 2. Nuclear | 2. Hydro (Summer) |
| 3. Run off river | 3. Diesel |
| 4. Hydro | 5. Solar |
| 6. Wind | (operating time is less) |

fig pumped storage plant:



Pumped storage plant is also hydro plant.

→ Thermal and nuclear operaⁿ time is more (expansion) so they are used as a base load plant.

→ Depending upon availability hydro is used as base or peak load plant.

1) Plant load factor : (P_{lf})

$$P_{lf} = \frac{P_{avg}}{P_{max}}$$

$$= \frac{P_{avg} \times t}{P_{max} \times t}$$

P_{lf} = area under load curve

(Rectangular area corresponding to P_{max})

2) Plant capacity factor (P_{cf}) →

$$P_{cf} = \frac{P_{avg}}{P_c} \quad P_c = \text{Plant capacity}$$

avg energy Produced in total hours
(energy rate to produce as per P_c in total hours)

$$P_{cf} < 1$$

3) Plant use factor (P_{uf})

$$(P_{uf})$$

~~$P_{uf} = \frac{\text{Energy Produced in used hours}}{\text{energy rate to produce as per } P_c \text{ in used hours}}$~~

$$P_{uf} < 1$$

4. Reserve Capacity R_C :

$$R_C = P_C - P_{max}$$

$$= \frac{P_{avg}}{P_{Cf}} - P_{max}$$

$$R_C = \frac{P_{avg} - P_{max} P_{Cf}}{P_{Cf}}$$

$$= P_{max} \left[\frac{P_{avg} - P_{Cf}}{P_{max}} \right]$$

$$= \frac{P_{Cf}}{P_{max}} (P_{lf} - P_{Cf})$$

5. Demand Factor : (D_f)

$$D_f = \frac{P_{max}}{\text{sum of connected load}}$$

$$D_f < 1$$

6. Diversity factor : (Div_f)

$$(Div_f) = \frac{\text{sum of individual max demand}}{P_{max}}$$

$$Div_f > 1$$

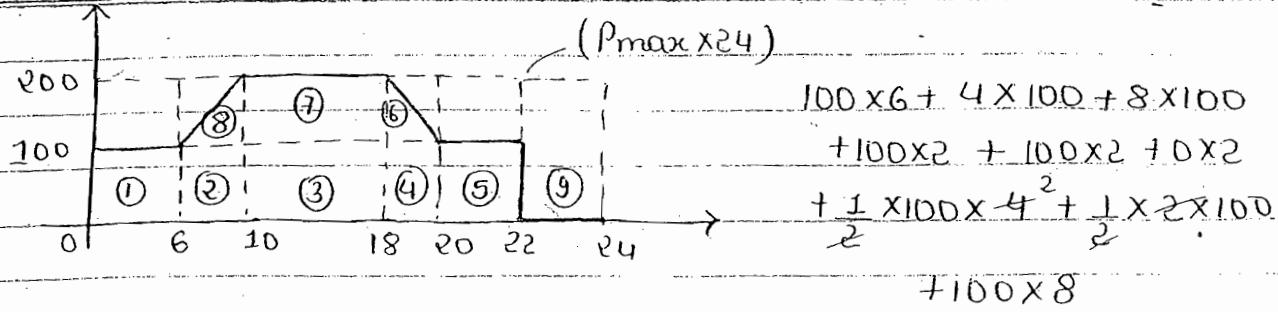
Ques: A Generating Station has a plant installation capacity of 300 MW is delivering the power to the load centre. A load curve is shown in the fig calculate

- (i) P_{max} (ii) Plant capacity (iii) P_{avg} (iv) P_{lf}
- (v) P_{Cf} (vi) P_{uf} (vii) R_C

Given:- $P_{max} = 200 \text{ MW}$

$P_C = 300 \text{ MW}$

$P_{avg} = \text{Total area / Time}$



$$4) P_f = \frac{P_{avg} \times 24}{P_{max}} = \frac{3300}{24} = 137.5 \text{ MW}$$

$$= \frac{137.5}{200} = 0.6875 < 1$$

or $\frac{P_{avg} \times 24}{P_{max} \times 24} = \frac{3300}{200 \times 24} \rightarrow \text{Total hours}$

$$5) P_{cf} = \frac{P_{avg}}{P_c} = \frac{137.5}{300} = 0.4583 < 1$$

or $R_f = \frac{3300}{300 \times 24} = 0.4583 \rightarrow \text{Total hours}$

$$6) P_{uf} = \frac{3300}{300 \times 22} = 0.5 < 1 \quad (\text{area remains same})$$

$$7) R_c = P_c - P_{max} = 300 - 200 = 100 \text{ MW}$$

$$\text{or } R_c = \frac{P_{max} (P_f - P_{cf})}{P_{cf}} = \frac{200 (0.6875 - 0.4583)}{0.4583} = 100 \text{ MW}$$

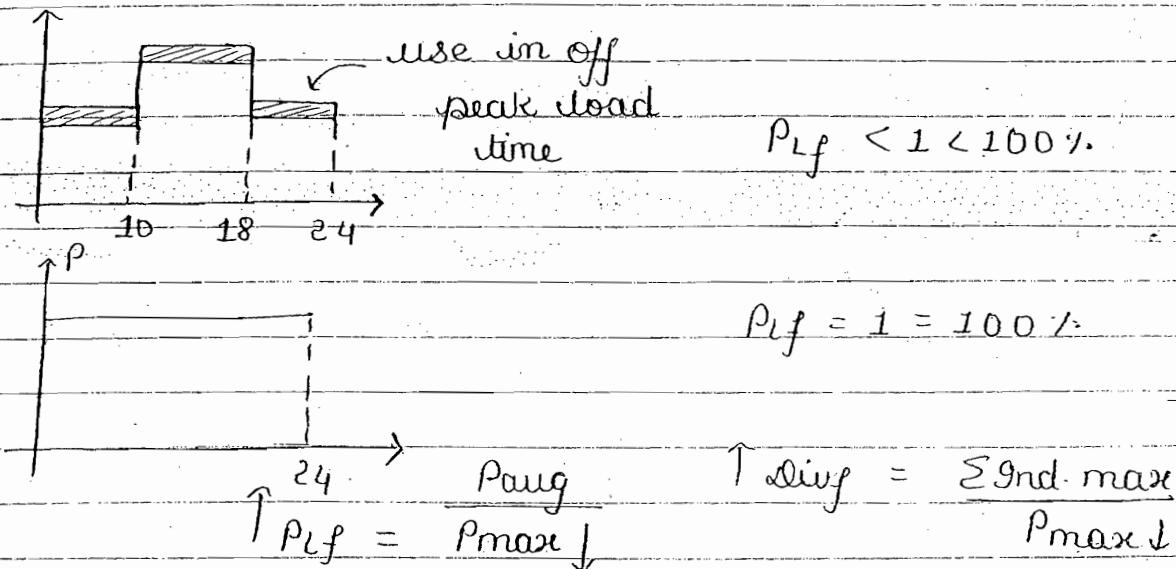
	connected load (kW)	Individual max demand
hospitals	50	40
colleges	40	30
shops	30	25

$$\sum = 120 \text{ P(kW)} - \sum = 95$$

$$D_f = \frac{70}{120} < 1 \quad \text{Div}_f = \frac{95}{70} > 1$$

Connected load (equipments upto their full capacity)

Individual load demand is diverse. (Div_f)



Practically If more than 1 is also possible
Higher P_{lf} is better.

Methods of Improving P_{lf} and diversity factor

If P_{lf} and diversity factor are higher, indicates max demand is lower so that initial investment on the electrical appliances is reduced which reduces cost of electrical energy.

Because of this reason $P_{lf} = 1$ or higher than 1 and diversity factor > 1 is preferred.

Increasing industries for running their offices and industrial during off peak load time

- Agricultural pumpsets are to be run during off peak load period.
- Effective utilisation of Sunlight by maintaining proper ventilation betwⁿ the buildings.
- Increasing the industries for utilising high Pf loads

Power Generation

Thermal Plant

- H/W \rightarrow hot well
- DM \rightarrow Demineralised \rightarrow (to avoid corrosion of boiler)
- CLF P \rightarrow Condensate Extr. pump
- CWP \rightarrow circulating water pump
- BFP \rightarrow Boiler feed pump
- LPH \rightarrow low pr. heater
- HPH \rightarrow High pr. heater
- D \rightarrow Deaerator
- ECO \rightarrow Economiser
- LPT \rightarrow Low pressure turbine
- SPT \rightarrow Inter " "
- HPT \rightarrow High "
- V \rightarrow vacuum pump / steam ejector
- HPCV - High pr. Govt. control valve
- SPCV - Inter pressure " " "
- HTSH - High temp Super Heater
- ITSH - Inter " " "
- PA - Primary air

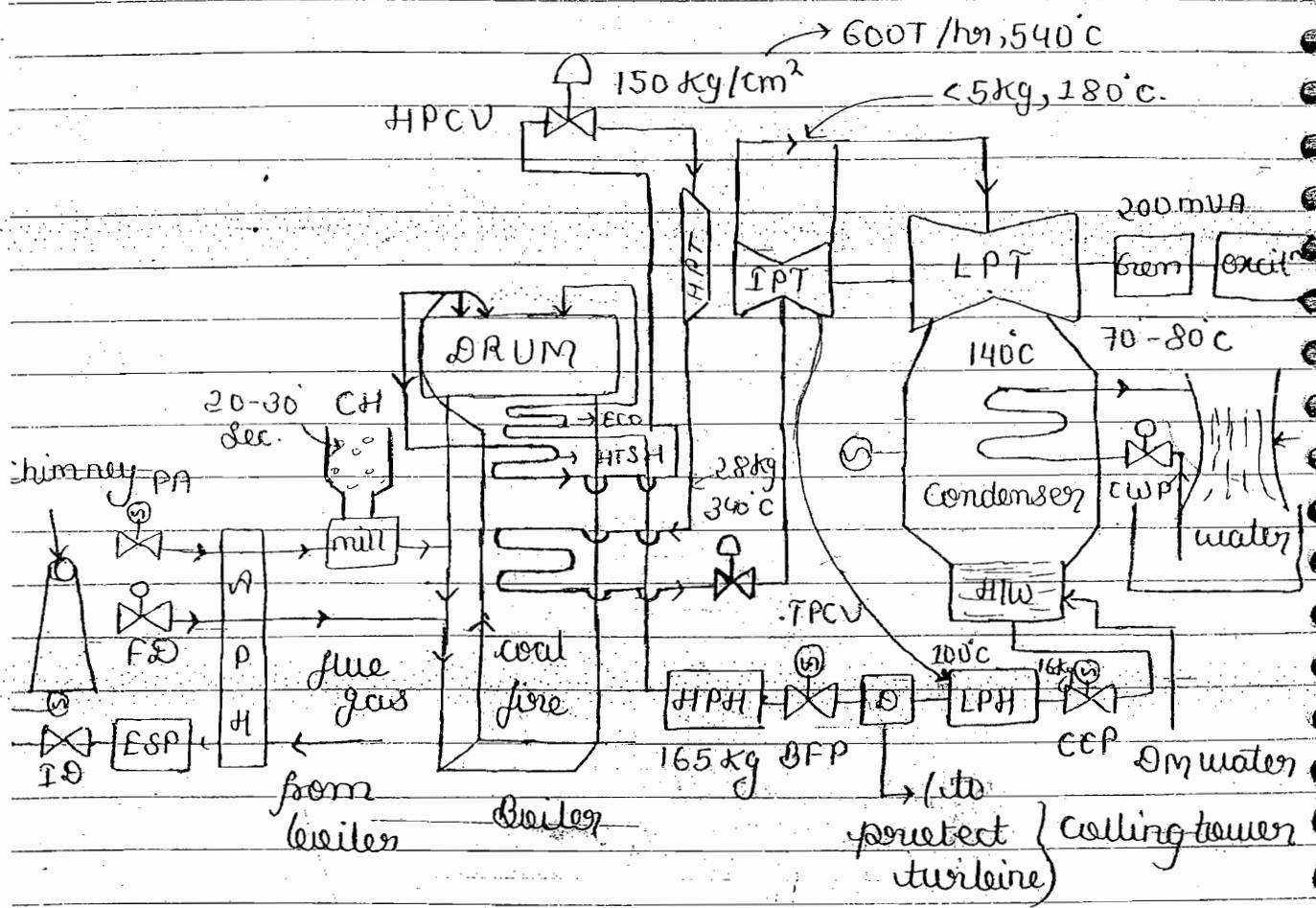
• F.D - forced draft

I.D. - Induced draught

ESP - Electrostatic Precipitator

APH - air pre heater

CH - Coal hoppers



Thermal Plant is working on the principle of Rankine Cycle. That is the process of reheatting steam for improving efficiency. Thermal eff. is betwⁿ 35-40%.

Anthracite - < 10%.

Bituminous - 20-30%

dignite 30-50%

Peat > 50%

Energy of coal \rightarrow kcal/kg

1 unit = 1 kWh = 860 kcal heat energy.

Ex.

Bituminous : |

Energy \rightarrow $2 \text{ kW hr/kg} = 1720 \text{ kcal/kg}$

$\eta = 40\% = 2 \times 0.4 = 0.8 \text{ kW hr/kg}$

$1 \text{ kg} = 0.8 \text{ kW hr} \rightarrow 1 \text{ kWh} = 1/0.8 = 1.25 \text{ kg coal.}$

$P = 200 \text{ MW}, 1 \text{ day} = 24 \text{ hr}$

energy $= 200 \times 24 = 4800 \text{ MWhr} = 4800 \times 10^3 \text{ kW hr}$

coal $= 4800 \times 10^3 \times 1.25 \text{ kg} = 6000 \text{ T/day}$
(tonnes/day)

ash $= 6000 \times 200 = 1200 \text{ T/day}$

(huge amount of ash produced)

235

$U_{92} - 1 \text{ kg} = 270000 \text{ kg coal}$ (less requirement of coal so transportation cost is more)

$$\eta_0 = \eta_{th} \times \eta_e$$

$$\eta_0 = \eta_B \times \eta_{turbine} \times \eta_g$$

η_0 = over all η

η_B = Boiler η , η_g = Generator η

η_{th} = Heat η = Boiler & thermal η

- For protecting boiler tubes from corrosion
O₂ in water is used.

- For improving η_{th} , LP and HP heaters are used

so that water temp. is increased.

These heaters are of Steam heaters

Decanter is used for removal of dissolved gases from the water for protection of turbine.

BFP is the highest pressure generating pump in the thermal plant which nearly consumes 4mw electrical power & produces upto 165 kg of pressure.

Economiser used for absorbing heat from flue gases. so that water temp is increased for improvement of thermal efficiency.

Water circulates naturally from drum to boiler and again to the drum due to density difference of water and steam. In high capacity plants extra pumps is used for this purpose HTSH heater improves steam temp upto 540c.

Steam is reheated in the HTSH for improving the thermal efficiency. This is the principle of rankine cycle.

Steam directly sent from IP turbine to LP turbine. vacuum pump is used for absorbing steam from the L.P. turbine to condenser.

- Circulating water is used for conversion of steam into water. This water is sent to the boiler. Circulating water is cooled by using cooling turbine.
- PA fan is used for conveying coal hopper from mill to boiler.
- FB fan is used to supply oxygen for proper combustion of coal.
- FD fan is used to extract flue gas from boiler.
- ESP working on the principle of electrical field used for collection of ash from the flue gas. APH used to increase the PA & FD fan air temp so that moisture from the coal is removed.
- HPCV and FPCV are used for controlling flow rate of steam into the turbine so that speed of freq. are controlled.

Hydro Power Generation

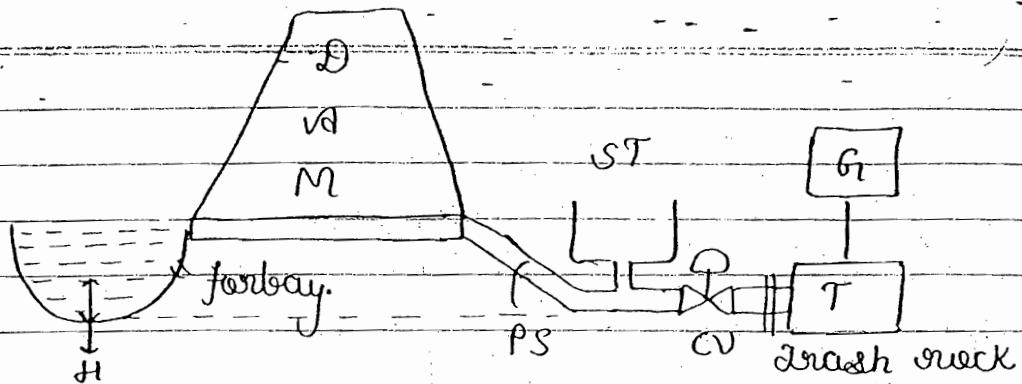
Potential \rightarrow Kinetic \rightarrow Mech \rightarrow Elec.

PS \rightarrow penstock

ST \rightarrow surge tank

CV \rightarrow Control valve

H \rightarrow mean water head



(avoid entering waste material)

Electrical Power Output (P) \rightarrow waste material)

1) Discharge (Q) is given -

$$P = 0.735 \eta QWH$$

$$= 9.81 \times 10^{-3} \eta QWH \text{ kW}$$

$\eta \rightarrow$ plant efficiency

$Q \rightarrow$ discharge of water in m^3/sec .

= capacity of reservoir in m^3

3600 sec.

$w =$ density of water $= 1000 \text{ kg/m}^3$

$H =$ mean water head in m.

2) Rainfall (F) is given -

$$P = 3.14 \times 10^{-3} \eta A F H \text{ kW}$$

$\eta \rightarrow$ plant η

$\times \rightarrow$ yield factor (which we get)

$A \rightarrow$ attachment area sq. km .

$F \rightarrow$ annual rainfall in mm

$H \rightarrow$ mean water head in m

Energy = power $\times t$

$\Delta H \uparrow$ variable

Head (m)	Turbine
2 - 15	propeller or Kaplan
15 - 70	Kaplan or Francis
70 - 500	Francis or Pelton
> 500	Pelton
Pumped Storage	DERIVING

$H < 30 \rightarrow$ low head

$30 < H < 300 \rightarrow$ medium head

$H > 300 \rightarrow$ high head.

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