Variable Selection

```
library(tidyverse)
```

```
-- Attaching core tidyverse packages ----- tidyverse 2.0.0 --
           1.1.4
v dplyr
                   v readr
                                2.1.5
v forcats 1.0.0
                               1.5.1
                   v stringr
v ggplot2 3.5.1
                    v tibble 3.2.1
v lubridate 1.9.3
                               1.3.1
                    v tidyr
v purrr
           1.0.2
-- Conflicts ----- tidyverse_conflicts() --
x dplyr::filter() masks stats::filter()
x dplyr::lag()
                masks stats::lag()
i Use the conflicted package (<a href="http://conflicted.r-lib.org/">http://conflicted.r-lib.org/</a>) to force all conflicts to become
```

```
library(BAS)  # spike-and-slab
library(rstanarm)  # horseshoe
```

Loading required package: Rcpp This is rstanarm version 2.32.1

- See https://mc-stan.org/rstanarm/articles/priors for changes to default priors!
- Default priors may change, so it's safest to specify priors, even if equivalent to the default
- For execution on a local, multicore CPU with excess RAM we recommend calling
 options(mc.cores = parallel::detectCores())

library(loo)

This is loo version 2.8.0

- Online documentation and vignettes at mc-stan.org/loo
- As of v2.0.0 loo defaults to 1 core but we recommend using as many as possible. Use the 'co

library(kableExtra)

```
Attaching package: 'kableExtra'
The following object is masked from 'package:dplyr':
    group_rows
df <- read.csv("Data/student-scores-clean.csv") |>
  select(-id, -first_name, -last_name, -email) |>
  mutate(
                           = factor(gender, labels = c("Female", "Male")),
   gender
   part_time_job = factor(part_time_job),
   extracurricular_activities = factor(extracurricular_activities),
   career_aspiration = factor(career_aspiration)
  )
# keep only non-collinear behavioral/demographic predictors
vars_behavioral <- c("gender", "part_time_job",</pre>
                     "absence_days", "extracurricular_activities",
                     "weekly_self_study_hours", "career_aspiration")
df_sub <- df %>% select(average_score, all_of(vars_behavioral))
bas_fit <- bas.lm(</pre>
 average_score ~ .,
 data = df_sub,
 prior = "ZS-null",
 modelprior = uniform(),
 n.models = 2^length(vars_behavioral)
# posterior inclusion probabilities (PIP)
pip <- summary(bas_fit)</pre>
hs_fit <- stan_glm(</pre>
  average_score ~ .,
                 = df_sub,
 data
 family = gaussian(),
 prior_intercept = normal(0, 10),
```

```
SAMPLING FOR MODEL 'continuous' NOW (CHAIN 1).
Chain 1:
Chain 1: Gradient evaluation took 3.9e-05 seconds
Chain 1: 1000 transitions using 10 leapfrog steps per transition would take 0.39 seconds.
Chain 1: Adjust your expectations accordingly!
Chain 1:
Chain 1:
Chain 1: Iteration: 1 / 2000 [ 0%]
                                        (Warmup)
Chain 1: Iteration: 200 / 2000 [ 10%]
                                        (Warmup)
Chain 1: Iteration: 400 / 2000 [ 20%]
                                        (Warmup)
Chain 1: Iteration: 600 / 2000 [ 30%]
                                        (Warmup)
Chain 1: Iteration: 800 / 2000 [ 40%]
                                        (Warmup)
Chain 1: Iteration: 1000 / 2000 [ 50%]
                                        (Warmup)
Chain 1: Iteration: 1001 / 2000 [ 50%]
                                        (Sampling)
Chain 1: Iteration: 1200 / 2000 [ 60%]
                                        (Sampling)
Chain 1: Iteration: 1400 / 2000 [ 70%]
                                        (Sampling)
Chain 1: Iteration: 1600 / 2000 [ 80%]
                                        (Sampling)
Chain 1: Iteration: 1800 / 2000 [ 90%]
                                         (Sampling)
Chain 1: Iteration: 2000 / 2000 [100%]
                                         (Sampling)
Chain 1:
Chain 1: Elapsed Time: 6.643 seconds (Warm-up)
Chain 1:
                        3.818 seconds (Sampling)
Chain 1:
                        10.461 seconds (Total)
Chain 1:
SAMPLING FOR MODEL 'continuous' NOW (CHAIN 2).
Chain 2:
Chain 2: Gradient evaluation took 1.1e-05 seconds
Chain 2: 1000 transitions using 10 leapfrog steps per transition would take 0.11 seconds.
Chain 2: Adjust your expectations accordingly!
Chain 2:
Chain 2:
Chain 2: Iteration:
                       1 / 2000 [ 0%]
                                        (Warmup)
Chain 2: Iteration: 200 / 2000 [ 10%]
                                         (Warmup)
Chain 2: Iteration: 400 / 2000 [ 20%]
                                         (Warmup)
```

```
Chain 2: Iteration: 600 / 2000 [ 30%]
                                         (Warmup)
Chain 2: Iteration: 800 / 2000 [ 40%]
                                         (Warmup)
Chain 2: Iteration: 1000 / 2000 [ 50%]
                                         (Warmup)
Chain 2: Iteration: 1001 / 2000 [ 50%]
                                         (Sampling)
Chain 2: Iteration: 1200 / 2000 [ 60%]
                                         (Sampling)
Chain 2: Iteration: 1400 / 2000 [ 70%]
                                         (Sampling)
Chain 2: Iteration: 1600 / 2000 [ 80%]
                                         (Sampling)
Chain 2: Iteration: 1800 / 2000 [ 90%]
                                         (Sampling)
Chain 2: Iteration: 2000 / 2000 [100%]
                                         (Sampling)
Chain 2:
Chain 2: Elapsed Time: 7.671 seconds (Warm-up)
Chain 2:
                        3.594 seconds (Sampling)
Chain 2:
                        11.265 seconds (Total)
Chain 2:
SAMPLING FOR MODEL 'continuous' NOW (CHAIN 3).
Chain 3:
Chain 3: Gradient evaluation took 1.1e-05 seconds
Chain 3: 1000 transitions using 10 leapfrog steps per transition would take 0.11 seconds.
Chain 3: Adjust your expectations accordingly!
Chain 3:
Chain 3:
Chain 3: Iteration:
                       1 / 2000 [ 0%]
                                         (Warmup)
Chain 3: Iteration: 200 / 2000 [ 10%]
                                         (Warmup)
Chain 3: Iteration: 400 / 2000 [ 20%]
                                         (Warmup)
Chain 3: Iteration: 600 / 2000 [ 30%]
                                         (Warmup)
Chain 3: Iteration: 800 / 2000 [ 40%]
                                         (Warmup)
Chain 3: Iteration: 1000 / 2000 [ 50%]
                                         (Warmup)
Chain 3: Iteration: 1001 / 2000 [ 50%]
                                         (Sampling)
Chain 3: Iteration: 1200 / 2000 [ 60%]
                                         (Sampling)
Chain 3: Iteration: 1400 / 2000 [ 70%]
                                         (Sampling)
Chain 3: Iteration: 1600 / 2000 [ 80%]
                                         (Sampling)
Chain 3: Iteration: 1800 / 2000 [ 90%]
                                         (Sampling)
Chain 3: Iteration: 2000 / 2000 [100%]
                                         (Sampling)
Chain 3:
Chain 3: Elapsed Time: 8.759 seconds (Warm-up)
Chain 3:
                        6.778 seconds (Sampling)
Chain 3:
                        15.537 seconds (Total)
Chain 3:
SAMPLING FOR MODEL 'continuous' NOW (CHAIN 4).
Chain 4:
Chain 4: Gradient evaluation took 1.2e-05 seconds
```

```
Chain 4: 1000 transitions using 10 leapfrog steps per transition would take 0.12 seconds.
Chain 4: Adjust your expectations accordingly!
Chain 4:
Chain 4:
Chain 4: Iteration:
                       1 / 2000 [ 0%]
                                         (Warmup)
Chain 4: Iteration: 200 / 2000 [ 10%]
                                         (Warmup)
Chain 4: Iteration: 400 / 2000 [ 20%]
                                         (Warmup)
Chain 4: Iteration: 600 / 2000 [ 30%]
                                         (Warmup)
Chain 4: Iteration: 800 / 2000 [ 40%]
                                         (Warmup)
Chain 4: Iteration: 1000 / 2000 [ 50%]
                                         (Warmup)
Chain 4: Iteration: 1001 / 2000 [ 50%]
                                         (Sampling)
Chain 4: Iteration: 1200 / 2000 [ 60%]
                                         (Sampling)
Chain 4: Iteration: 1400 / 2000 [ 70%]
                                         (Sampling)
Chain 4: Iteration: 1600 / 2000 [ 80%]
                                         (Sampling)
Chain 4: Iteration: 1800 / 2000 [ 90%]
                                         (Sampling)
Chain 4: Iteration: 2000 / 2000 [100%]
                                         (Sampling)
Chain 4:
Chain 4: Elapsed Time: 9.657 seconds (Warm-up)
Chain 4:
                        6.807 seconds (Sampling)
Chain 4:
                        16.464 seconds (Total)
Chain 4:
Warning: There were 21 divergent transitions after warmup. See
https://mc-stan.org/misc/warnings.html#divergent-transitions-after-warmup
to find out why this is a problem and how to eliminate them.
Warning: Examine the pairs() plot to diagnose sampling problems
print(hs_fit, digits = 2)
stan_glm
               gaussian [identity]
 family:
               average_score ~ .
 formula:
 observations: 2000
               22
 predictors:
                                       Median MAD SD
(Intercept)
                                               0.68
                                       77.59
genderMale
                                       -0.28
                                               0.24
part_time_job1
                                       -0.08
                                               0.25
absence_days
                                        0.03
                                               0.05
```

```
extracurricular_activities1
                                       -0.05
                                               0.21
weekly_self_study_hours
                                        0.13
                                               0.02
career_aspirationArtist
                                               0.87
                                        2.62
career_aspirationBanker
                                        1.42
                                               0.64
career_aspirationBusiness Owner
                                               0.69
                                       -3.44
career_aspirationConstruction Engineer 3.04
                                               0.78
career_aspirationDesigner
                                        2.57
                                               0.84
career_aspirationDoctor
                                        7.39
                                               0.70
career_aspirationGame Developer
                                        3.67
                                               0.85
career_aspirationGovernment Officer
                                               0.88
                                        2.00
career_aspirationLawyer
                                        2.69
                                               0.66
career_aspirationReal Estate Developer
                                        0.99
                                               0.87
career_aspirationScientist
                                               0.93
                                        4.40
career_aspirationSoftware Engineer
                                        1.50
                                               0.59
career_aspirationStock Investor
                                               0.80
                                        1.13
career_aspirationTeacher
                                        1.04
                                               0.88
career_aspirationUnknown
                                       -0.03
                                               0.47
                                               0.97
career_aspirationWriter
                                        3.00
```

Auxiliary parameter(s):

Median MAD_SD

sigma 4.75 0.08

```
plot(hs_fit, pars = c("beta"), prob = 0.9)
```

⁻⁻⁻⁻⁻

^{*} For help interpreting the printed output see ?print.stanreg

^{*} For info on the priors used see ?prior_summary.stanreg

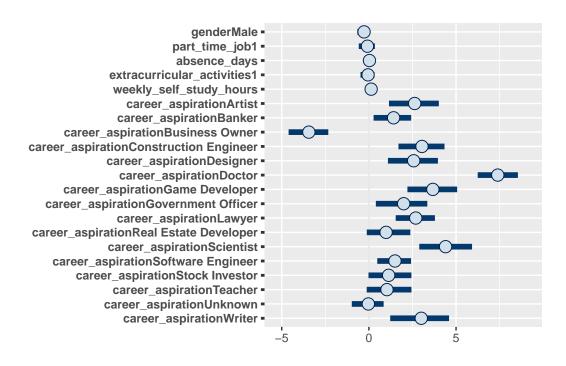


Table 1: LOO Cross-Validation Metrics

Metric	Estimate
elpd_loo	-5965.97
se_elpd_loo	31.85

Metric	Estimate
p_loo	22.22

```
df_sub <- df %>%
  select(
   average_score,
   -starts_with("career_aspiration")
)
```

```
SAMPLING FOR MODEL 'continuous' NOW (CHAIN 1).
Chain 1:
Chain 1: Gradient evaluation took 7.3e-05 seconds
Chain 1: 1000 transitions using 10 leapfrog steps per transition would take 0.73 seconds.
Chain 1: Adjust your expectations accordingly!
Chain 1:
Chain 1:
Chain 1: Iteration: 1 / 2000 [ 0%]
                                        (Warmup)
Chain 1: Iteration: 200 / 2000 [ 10%]
                                        (Warmup)
Chain 1: Iteration: 400 / 2000 [ 20%]
                                        (Warmup)
Chain 1: Iteration: 600 / 2000 [ 30%]
                                        (Warmup)
Chain 1: Iteration: 800 / 2000 [ 40%]
                                        (Warmup)
Chain 1: Iteration: 1000 / 2000 [ 50%]
                                        (Warmup)
Chain 1: Iteration: 1001 / 2000 [ 50%]
                                        (Sampling)
Chain 1: Iteration: 1200 / 2000 [ 60%]
                                        (Sampling)
Chain 1: Iteration: 1400 / 2000 [ 70%]
                                        (Sampling)
Chain 1: Iteration: 1600 / 2000 [ 80%]
                                         (Sampling)
Chain 1: Iteration: 1800 / 2000 [ 90%]
                                         (Sampling)
```

```
Chain 1: Iteration: 2000 / 2000 [100%]
                                        (Sampling)
Chain 1:
Chain 1: Elapsed Time: 5.246 seconds (Warm-up)
Chain 1:
                        1.873 seconds (Sampling)
Chain 1:
                        7.119 seconds (Total)
Chain 1:
SAMPLING FOR MODEL 'continuous' NOW (CHAIN 2).
Chain 2:
Chain 2: Gradient evaluation took 4.9e-05 seconds
Chain 2: 1000 transitions using 10 leapfrog steps per transition would take 0.49 seconds.
Chain 2: Adjust your expectations accordingly!
Chain 2:
Chain 2:
Chain 2: Iteration:
                       1 / 2000 [ 0%]
                                         (Warmup)
Chain 2: Iteration: 200 / 2000 [ 10%]
                                         (Warmup)
Chain 2: Iteration: 400 / 2000 [ 20%]
                                         (Warmup)
Chain 2: Iteration: 600 / 2000 [ 30%]
                                         (Warmup)
Chain 2: Iteration: 800 / 2000 [ 40%]
                                         (Warmup)
Chain 2: Iteration: 1000 / 2000 [ 50%]
                                         (Warmup)
Chain 2: Iteration: 1001 / 2000 [ 50%]
                                         (Sampling)
Chain 2: Iteration: 1200 / 2000 [ 60%]
                                         (Sampling)
Chain 2: Iteration: 1400 / 2000 [ 70%]
                                         (Sampling)
Chain 2: Iteration: 1600 / 2000 [ 80%]
                                         (Sampling)
Chain 2: Iteration: 1800 / 2000 [ 90%]
                                         (Sampling)
Chain 2: Iteration: 2000 / 2000 [100%]
                                         (Sampling)
Chain 2:
Chain 2: Elapsed Time: 8.151 seconds (Warm-up)
Chain 2:
                        1.663 seconds (Sampling)
Chain 2:
                        9.814 seconds (Total)
Chain 2:
SAMPLING FOR MODEL 'continuous' NOW (CHAIN 3).
Chain 3:
Chain 3: Gradient evaluation took 4.8e-05 seconds
Chain 3: 1000 transitions using 10 leapfrog steps per transition would take 0.48 seconds.
Chain 3: Adjust your expectations accordingly!
Chain 3:
Chain 3:
Chain 3: Iteration:
                       1 / 2000 [ 0%]
                                         (Warmup)
Chain 3: Iteration: 200 / 2000 [ 10%]
                                         (Warmup)
Chain 3: Iteration: 400 / 2000 [ 20%]
                                         (Warmup)
Chain 3: Iteration: 600 / 2000 [ 30%]
                                         (Warmup)
```

```
Chain 3: Iteration: 800 / 2000 [ 40%]
                                         (Warmup)
Chain 3: Iteration: 1000 / 2000 [ 50%]
                                         (Warmup)
Chain 3: Iteration: 1001 / 2000 [ 50%]
                                         (Sampling)
Chain 3: Iteration: 1200 / 2000 [ 60%]
                                         (Sampling)
Chain 3: Iteration: 1400 / 2000 [ 70%]
                                         (Sampling)
Chain 3: Iteration: 1600 / 2000 [ 80%]
                                         (Sampling)
Chain 3: Iteration: 1800 / 2000 [ 90%]
                                          (Sampling)
Chain 3: Iteration: 2000 / 2000 [100%]
                                          (Sampling)
Chain 3:
Chain 3: Elapsed Time: 9.492 seconds (Warm-up)
Chain 3:
                        2.001 seconds (Sampling)
Chain 3:
                        11.493 seconds (Total)
Chain 3:
SAMPLING FOR MODEL 'continuous' NOW (CHAIN 4).
Chain 4:
Chain 4: Gradient evaluation took 5.2e-05 seconds
Chain 4: 1000 transitions using 10 leapfrog steps per transition would take 0.52 seconds.
Chain 4: Adjust your expectations accordingly!
Chain 4:
Chain 4:
Chain 4: Iteration:
                       1 / 2000 [ 0%]
                                         (Warmup)
Chain 4: Iteration: 200 / 2000 [ 10%]
                                         (Warmup)
Chain 4: Iteration: 400 / 2000 [ 20%]
                                         (Warmup)
Chain 4: Iteration: 600 / 2000 [ 30%]
                                         (Warmup)
Chain 4: Iteration: 800 / 2000 [ 40%]
                                         (Warmup)
Chain 4: Iteration: 1000 / 2000 [ 50%]
                                         (Warmup)
Chain 4: Iteration: 1001 / 2000 [ 50%]
                                         (Sampling)
Chain 4: Iteration: 1200 / 2000 [ 60%]
                                         (Sampling)
Chain 4: Iteration: 1400 / 2000 [ 70%]
                                         (Sampling)
Chain 4: Iteration: 1600 / 2000 [ 80%]
                                         (Sampling)
Chain 4: Iteration: 1800 / 2000 [ 90%]
                                          (Sampling)
Chain 4: Iteration: 2000 / 2000 [100%]
                                          (Sampling)
Chain 4:
Chain 4: Elapsed Time: 4.214 seconds (Warm-up)
Chain 4:
                        1.741 seconds (Sampling)
Chain 4:
                        5.955 seconds (Total)
Chain 4:
# random intercept + slope on study hours
model2 <- stan_lmer(</pre>
  average_score ~ weekly_self_study_hours
```

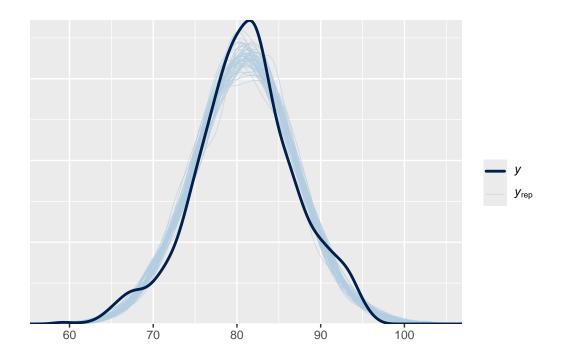
```
SAMPLING FOR MODEL 'continuous' NOW (CHAIN 1).
Chain 1:
Chain 1: Gradient evaluation took 0.000104 seconds
Chain 1: 1000 transitions using 10 leapfrog steps per transition would take 1.04 seconds.
Chain 1: Adjust your expectations accordingly!
Chain 1:
Chain 1:
Chain 1: Iteration: 1 / 2000 [ 0%]
                                         (Warmup)
Chain 1: Iteration: 200 / 2000 [ 10%]
                                         (Warmup)
Chain 1: Iteration: 400 / 2000 [ 20%]
                                         (Warmup)
Chain 1: Iteration: 600 / 2000 [ 30%]
                                         (Warmup)
Chain 1: Iteration: 800 / 2000 [ 40%]
                                         (Warmup)
Chain 1: Iteration: 1000 / 2000 [ 50%]
                                         (Warmup)
Chain 1: Iteration: 1001 / 2000 [ 50%]
                                         (Sampling)
Chain 1: Iteration: 1200 / 2000 [ 60%]
                                         (Sampling)
Chain 1: Iteration: 1400 / 2000 [ 70%]
                                         (Sampling)
Chain 1: Iteration: 1600 / 2000 [ 80%]
                                         (Sampling)
Chain 1: Iteration: 1800 / 2000 [ 90%]
                                         (Sampling)
Chain 1: Iteration: 2000 / 2000 [100%]
                                         (Sampling)
Chain 1:
Chain 1: Elapsed Time: 23.954 seconds (Warm-up)
Chain 1:
                        5.913 seconds (Sampling)
Chain 1:
                        29.867 seconds (Total)
Chain 1:
SAMPLING FOR MODEL 'continuous' NOW (CHAIN 2).
Chain 2:
Chain 2: Gradient evaluation took 6.9e-05 seconds
Chain 2: 1000 transitions using 10 leapfrog steps per transition would take 0.69 seconds.
Chain 2: Adjust your expectations accordingly!
Chain 2:
```

```
Chain 2:
Chain 2: Iteration:
                       1 / 2000 [ 0%]
                                         (Warmup)
Chain 2: Iteration: 200 / 2000 [ 10%]
                                         (Warmup)
Chain 2: Iteration: 400 / 2000 [ 20%]
                                         (Warmup)
Chain 2: Iteration: 600 / 2000 [ 30%]
                                         (Warmup)
Chain 2: Iteration: 800 / 2000 [ 40%]
                                         (Warmup)
Chain 2: Iteration: 1000 / 2000 [ 50%]
                                         (Warmup)
Chain 2: Iteration: 1001 / 2000 [ 50%]
                                         (Sampling)
Chain 2: Iteration: 1200 / 2000 [ 60%]
                                         (Sampling)
Chain 2: Iteration: 1400 / 2000 [ 70%]
                                         (Sampling)
Chain 2: Iteration: 1600 / 2000 [ 80%]
                                         (Sampling)
Chain 2: Iteration: 1800 / 2000 [ 90%]
                                         (Sampling)
Chain 2: Iteration: 2000 / 2000 [100%]
                                         (Sampling)
Chain 2:
Chain 2: Elapsed Time: 21.928 seconds (Warm-up)
Chain 2:
                        7.9 seconds (Sampling)
Chain 2:
                        29.828 seconds (Total)
Chain 2:
SAMPLING FOR MODEL 'continuous' NOW (CHAIN 3).
Chain 3:
Chain 3: Gradient evaluation took 6.8e-05 seconds
Chain 3: 1000 transitions using 10 leapfrog steps per transition would take 0.68 seconds.
Chain 3: Adjust your expectations accordingly!
Chain 3:
Chain 3:
Chain 3: Iteration:
                       1 / 2000 [ 0%]
                                         (Warmup)
Chain 3: Iteration: 200 / 2000 [ 10%]
                                         (Warmup)
Chain 3: Iteration: 400 / 2000 [ 20%]
                                         (Warmup)
Chain 3: Iteration: 600 / 2000 [ 30%]
                                         (Warmup)
Chain 3: Iteration: 800 / 2000 [ 40%]
                                         (Warmup)
Chain 3: Iteration: 1000 / 2000 [ 50%]
                                         (Warmup)
Chain 3: Iteration: 1001 / 2000 [ 50%]
                                         (Sampling)
Chain 3: Iteration: 1200 / 2000 [ 60%]
                                         (Sampling)
Chain 3: Iteration: 1400 / 2000 [ 70%]
                                         (Sampling)
Chain 3: Iteration: 1600 / 2000 [ 80%]
                                         (Sampling)
Chain 3: Iteration: 1800 / 2000 [ 90%]
                                         (Sampling)
Chain 3: Iteration: 2000 / 2000 [100%]
                                         (Sampling)
Chain 3:
Chain 3: Elapsed Time: 22.113 seconds (Warm-up)
Chain 3:
                        6.755 seconds (Sampling)
Chain 3:
                        28.868 seconds (Total)
Chain 3:
```

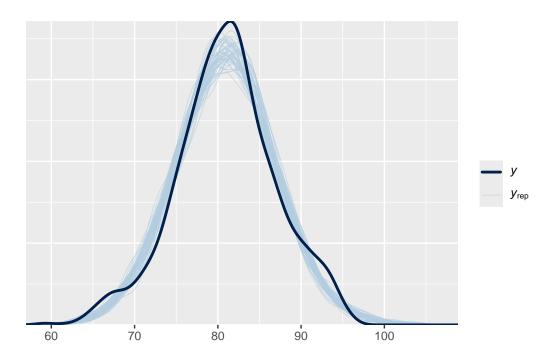
```
SAMPLING FOR MODEL 'continuous' NOW (CHAIN 4).
Chain 4:
Chain 4: Gradient evaluation took 6.9e-05 seconds
Chain 4: 1000 transitions using 10 leapfrog steps per transition would take 0.69 seconds.
Chain 4: Adjust your expectations accordingly!
Chain 4:
Chain 4:
Chain 4: Iteration: 1 / 2000 [ 0%]
                                         (Warmup)
Chain 4: Iteration: 200 / 2000 [ 10%]
                                         (Warmup)
Chain 4: Iteration: 400 / 2000 [ 20%]
                                         (Warmup)
Chain 4: Iteration: 600 / 2000 [ 30%]
                                         (Warmup)
Chain 4: Iteration: 800 / 2000 [ 40%]
                                         (Warmup)
Chain 4: Iteration: 1000 / 2000 [ 50%]
                                         (Warmup)
Chain 4: Iteration: 1001 / 2000 [ 50%]
                                         (Sampling)
Chain 4: Iteration: 1200 / 2000 [ 60%]
                                         (Sampling)
Chain 4: Iteration: 1400 / 2000 [ 70%]
                                         (Sampling)
Chain 4: Iteration: 1600 / 2000 [ 80%]
                                         (Sampling)
Chain 4: Iteration: 1800 / 2000 [ 90%]
                                         (Sampling)
Chain 4: Iteration: 2000 / 2000 [100%]
                                         (Sampling)
Chain 4:
Chain 4: Elapsed Time: 662.01 seconds (Warm-up)
Chain 4:
                        7.682 seconds (Sampling)
Chain 4:
                        669.692 seconds (Total)
Chain 4:
print(model1, digits = 2)
stan_lmer
 family:
               gaussian [identity]
 formula:
               average_score ~ weekly_self_study_hours + absence_days + extracurricular_acti
       (1 | career_aspiration)
 observations: 2000
                            Median MAD_SD
(Intercept)
                            79.18
                                     0.68
weekly_self_study_hours
                             0.14
                                     0.02
absence_days
                                     0.05
                              0.05
extracurricular_activities1 -0.09
                                     0.27
Auxiliary parameter(s):
      Median MAD_SD
```

```
sigma 4.74 0.08
Error terms:
 Groups
                   Name
                               Std.Dev.
 career_aspiration (Intercept) 2.56
                               4.74
 Residual
Num. levels: career_aspiration 17
* For help interpreting the printed output see ?print.stanreg
* For info on the priors used see ?prior_summary.stanreg
print(model2, digits = 2)
stan_lmer
 family:
               gaussian [identity]
               average_score ~ weekly_self_study_hours + absence_days + extracurricular_acti
 formula:
       (1 + weekly_self_study_hours | career_aspiration)
 observations: 2000
-----
                            Median MAD_SD
(Intercept)
                            79.03
                                  0.58
                                    0.03
weekly_self_study_hours
                             0.14
absence_days
                             0.04
                                    0.05
extracurricular_activities1 -0.09
                                    0.27
Auxiliary parameter(s):
      Median MAD_SD
sigma 4.72
             0.07
Error terms:
 Groups
                   Name
                                           Std.Dev. Corr
 career_aspiration (Intercept)
                                           1.9058
                   weekly_self_study_hours 0.0912
                                                    0.11
 Residual
                                           4.7212
Num. levels: career_aspiration 17
```

- ----
- * For help interpreting the printed output see ?print.stanreg
- * For info on the priors used see ?prior_summary.stanreg



pp_check(model2)



```
# Compare with LOO
loo1 <- loo(model1)
loo2 <- loo(model2)
loo_compare(loo1, loo2)
```

elpd_diff se_diff model2 0.0 0.0 model1 -4.9 2.9