

Monitoring der AUTOSAR Timing Extensions mittels TeSSLa

Monitoring of the AUTOSAR Timing Extensions with TeSSLa

Bachelorarbeit

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Lübeck, den 1.1. 1970

Erklärung
Ich erkläre hiermit an Eides statt, dass ich diese Arbeit selbständig verfasst und keine anderen als die angegebenen Quellen und Hilfsmittel benutzt habe.
(Hendrik Streichhahn) Lübeck, den 1.1. 1970

Kurzfassung Abstract Deutsch

Abstract Kurzfassung Englisch.

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1. Introduction

Timing behavior is one of the most important properties of computer systems. Especially in safety-critical applications, a wrong timed reaction of the system can have disastrous consequences, for example in the Electronic Stability Control of a vehicle. The AUTOSAR (AUTomotive Open System ARchitecture) standards are used by almost all car manufacturers in their software development processes to standardize components and therefore increase the interoperability and exchangeability.

To describe the timing behavior of soft- and hardware components of cars, the AU- $TOSAR\ Timing\ Extensions$ were developed. The goal of this thesis is to implement a monitoring tool for the timing constraints defined in this standard.

A major drawback of this standard is that the definitions are written in an informal way and can be misunderstood. Therefore, the timing constraints defined in TADL2 (Timing Augmented Description Language Version 2) are used as basis for the monitoring tool. The TADL2 timing constraints are comparable and partly compatible to the AUTOSAR Timing Extensions, as most of the constraints defined in the AUTOSAR standard can be described as equivalent combination of TADL2 timing constraints.

The monitoring tool is written in *TeSSLa* (Temporal Stream-based Specification Language), which is made for stream runtime verification and is capable of non-intrusive observation and can be run as Java program or on specialized embedded hardware, like FPGAs.

In the first part of this thesis, an overview over the AUTOSAR Timing Extensions and an example about the informal and ambiguous definitions will be given. Next, the TADL2 timing constraints will be listed and the relations between the these constraints and the AUTOSAR Timing Extensions will be described. In the next chapter, TeSSLa, its fundamental functionality and other prerequisites, which are needed for understanding the theoretical part of this thesis, will be explained. The term of *finite monitorability* is introduced, which insures, that a property on infinite streams can always be monitored with finite resources. Then, each of the TADL2 timing constraint is checked, if it finite monitorable or not. After that, the TeSSLa implementations of these constraints is described and evaluated in a theoretical and practical way.

In the end an overview of the accomplished is given and ideas for further work will be discussed.

2. Timing Constraints

2.1. AUTOSAR Timing Extensions

AUTOSAR is a development partnership in the automotive industry. As stated before, the main goal is to define a standardized interface and increasing interoperability, exchangebility and re-usability of parts and therefore simplifying development and production. Three different layers are defined in the specification. Basic Software is an abstraction layer from components, like network or diagnostic protocols, or operating systems. AUTOSAR-Software defines the methods, how applications have to be build. For Basic Software and AUTOSAR Software, there are definitions for standardized Interfaces to enable the communication via the AUTOSAR Runtime Environment. It works as middleware, in which the virtual function bus is defined [AUT17]. The AUTOSAR Timing Extension are describing timing constraints for actions and reactions of components, that are communicating via the Virtual Function Bus. They are defined via *events*, which consists of a time and a data value, the type of the time and data value is arbitrary, the only restriction is, that the time values are strictly increasing. To describe the logical relationship between groups of events, event chains are defined, which consist of a stimulus and response event. The response event is understood as the answer to the stimulus event.

The AUTOSAR Release 4.4.0 ([AUT18]) is used for this thesis, there are 12 timing constraints defined in this version of the AUTOSAR Timing Extensions

- 1. The subset of 5 **EventTriggeringConstraints** are describing, at which points in time specific events may occur.
 - 1 The **PeriodicEventTriggering** defines repetitions of event with the same time distance and offers the possibility to set an allowed deviation from this pattern. Also the minimal distance between two subsequent events can be defined.
 - 2 The SporadicEventTriggering specifies sporadic event occurrences by defining the minimal and maximal distance between subsequent events. Optionally, periodic repetitions and allowed deviations from the period can be described.

- 3 With the **ConcreteEventTriggering**, offsets between a set of subsequent events in a time interval can be described. These intervals may not overlap, and periodic repetitions of them can be defined optionally.
- 4 The **BurstPatternEventTriggering** describes not overlapping event clusters with a minimal and maximal number of events and optionally periodic repetitions of these clusters.
- 5 The **ArbitraryEventTriggering** defines the distance between subsequent event by defining *ConfidenceIntervals*, which describe the probability, in which time interval the following event will occur.
- 2. The LatencyTimingConstraint specifies the minimal, nominal and maximal time distance between the stimulus and response events of an event chain.
- 3. The **AgeConstraint** is a simpler form of the *LatencyTimingConstraint* by defining minimal and maximal age a event may have at the point of time, when it is processed.
- 4. The **SynchronizationTimingConstraint** is used for describing events of different kinds, that occur synchronized in a time interval of a specific length.
- 5. The **SynchronizationPointConstraint** defines two sets of executables and events. Every element of the first set must have finished or occurred, before the first element of the second set may start or occur.
- 6. The **OffsetTimingConstraint** specifies the minimal and maximal time distance between corresponding *source* and *target* events.
- 7. The **ExecutionOrderConstraint** offers the possibility to define a list of executables, which must start and finish in the order given in the list.
- 8. The **ExecutionTimeConstraint** defines the minimal and maximal runtime of an executable, including or excluding the runtime of external functions and interruptions.

In this simplified form, some constraints are redundant. The semantic differences will be shown in section 2.2.3.

Problematic with the AUTOSAR Timing Extensions is, that the definitions are not very formal and have room left for interpretation. As example, the *BurstPattern-EventTriggering* will be analyzed in the following. This constraint describes events clusters, with events that occur with short time distances, with larger time distances between the clusters. The following attributes are needed:

• maxNumberOfOccurrences (positive integer)
Maximal number of events per burst

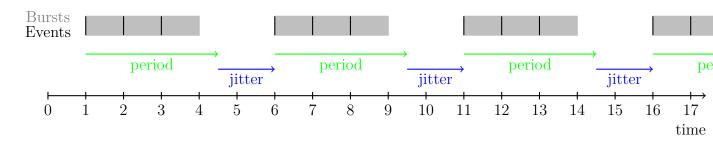


Figure 2.1.: BurstPatternEventTriggering Period-Jitter accumulating

- *minNumberOfOccurrences* (positive integer) Minimal number of events per burst (optional)
- *minimumInterArrivalTime* (time value) Minimal distance between subsequent events
- patternLength (time value)

 Length of each burst
- patternPeriod (time value)

 Time distance between the starting points of subsequent burst(optional)
- patternJitter (time value)
 Maximal allowed deviation from the periodic pattern (optional)

As example, we set:

- maxNumberOfOccurrences = 3
- minNumberOfOccurrences = 1
- minimumInterArrivalTime = 1
- patternLength = 3
- patternPeriod = 3.5
- patternJitter = 1.5

The combination of patternPeriod and patternJitter can be interpreted in an accumulating as seen in 2.1 or non-accumulating way as seen in 2.2 way. In the accumulating interpretation, the reference for the periodic occurrences is only the start point of the previous burst. In the non-accumulating way, there is an global reference point for the periodic repetitions.

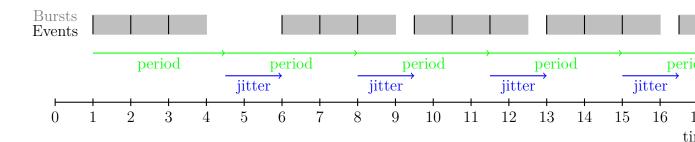


Figure 2.2.: BurstPatternEventTriggering Period-Jitter non-accumulating

With the definition of patternLength ("time distance between the beginnings of subsequent repetitions of the given burst pattern") you would think, that the accumulating variant is meant. Against that, the period attribute in PeriodicEventTriggering-Constraint is defined as "distance between subsequent occurrences of the event" in the text, hence it is also understandable the accumulating way, but there is the formal definition

$$\exists t_{reference} \forall t_n : t_{reference} + (n+1) * period \leq t_n \leq t_{reference} + (n-1) * period + jitter,$$

where t_n is the time of the *n*-th Event and $t_{reference}$ is a reference point, from which the periodic pattern starts, so the PeriodicEventTriggering-Constraint is meant to be understood in the non-accumulating way. It remains unclear, in which way the BurstPatternEventTriggering is meant to be understood.

Another problem of the AUTOSAR Timing Extensions is, that they were made for design purposes, monitoring them can be difficult, as they may need continuously growing time and memory resources, which makes online monitoring unsuitable in nearly all scenarios (more on monitorability in 4). As example, we will use the burst pattern again, this time using the attributes

- maxNumberOfOccurrences = INT MAX
- minNumberOfOccurrences = 1
- minimumInterArrivalTime = 0
- patternLength = 3
- patternPeriod unused
- patternJitter unused

Figure 2.3 shows the application of the *BurstPatternEventTriggering* constraint with the given parameters on a stream with events at the timestamps 3, 3.5, 4, 4.5. The development of possible the burst cluster with ongoing time is visualized. The gray

bars show, where the burst cluster can lay, the black lines show, where they definitely are. In timestamp 3 with only one event so far, only one burst has to be considered and it can lay between timestamp 0 and 6, the only limitation is, that it must include timestamp 3 with the event in that point. In Timestamp 3.5, there are two events (at 3 and 3.5) so far and there are two possibilities for burst placements. The first possibility with only one burst with both events in it, and the second possibility, where the events are in different bursts. The third graphic shows the trace in timestamp 4 with three different events so far (3, 3.5, 4) and three different possibilities for burst placements to consider. One possible burst contains all three events, the second possibility has one burst with the event at timestamp 3 and one burst with the events at 3.5 and 4 and the third possibility has one Burst with the events at 3 and 3.5 and one burst with the event at 4. The possible bursts in graphic 4 are analog to the third graphic, one possibility with one burst containing all 4 events and 3 possibilities with the first burst containing the first event, the first and second event or the first, the second and the third event and the second burst containing the remaining events.

In this Example, we see, that it is possible to create an unlimited number of possibilities for burst placements within one burst length, when the *minimumInter-ArrivalTime*-attribute is 0, which results in an infeasible resource consumption, as unlimited memory and time is needed to check the constraint in following events. Therefore, online monitoring this constraint is unsuitable in most cases.



Figure 2.3.: BurstPatternEventTriggering Possible bursts, ↑ shows the current time

2.2. TADL2

As timing extension to EAST-ADL(Electronics Architecture and Software Technology-Architecture Description Language), the TIMMO (Timing Model) project, and its successor TIMMO2USE, were initiated. EAST-ADL has similar goals as AU-TOSAR, but the definitions are written in a more formalized fashion. The definitions of the AUTOSAR Timing Extensions are only textually described often, the TADL2-Definitions are defined in a more formal way, as they offer a formal definition of each constraint in a timing constraint logic [BFL+12]. EAST-ADL is much less used in the automotive industry, but the EAST-ADL Timing Constraints are partly compatible to the AUTOSAR Timing Extensions, as they are sub- or supersets of each other. Many of the AUTOSAR Timing Extensions can be defined via a combination of TADL2 Constraints, as explained in section 2.2.3.

The timing constraints are defined on events or event chains, similar to the AU-TOSAR Timing Extensions. In TADL2, all events of an event chain have a color attribute, which shows the logical connection of these events. This attribute is defined as abstract and possibly infinite datatype. The only restriction is, that an equality test on these color values must exist. TADL2 offers 18 timing constraints, which will briefly explained in the following:

- The **StrongDelayConstraint** defines the minimal and maximal time distance of the events from two event sets (*source* and *target*).
- The **DelayConstraint** is a less strict variant of the **StrongDelayConstraint**, because it allows additional events in *target*.
- The RepeatConstraint, RepetitionConstraint, PeriodicConstraint, SporadicConstraint and ArbitraryConstraint are describing the time distance between subsequent events, whereby they are having small semantic differences. An exact distinction between these constraints will be given in section 2.2.2.
- The SynchronizationConstraint and StrongSynchronizationConstraint define groups of event sets, whose events occur in common time intervals. The SynchronizationConstraint allows more than one event of each group per interval, the StrongSynchronizationConstraint does not.
- The **ExecutionTimeConstraint** is used to set a minimum and a maximum for the runtime of a task, not considering interruptions in the execution.
- The **OrderConstraint** defines that the n^{th} event of one event set must occur before or at the n^{th} event of a second event set.
- The ComparisonConstraint is used to describe ordering relations of timestamps.

- The **PatternConstraint** defines the time distance between periodic points in time to several events.
- The **BurstConstraint** regulates the maximum number of events in time intervals of a specific length.
- The **ReactionConstraint** describes the minimal and maximal time a response event must occur after the associated stimulus event. Additional response events are allowed, additional stimulus events not.
- The **AgeConstraint** is similar to the ReactionConstraint, but it is defined the other way around. Therefore, it describes the minimal and maximal time a stimulus event must occur before the associated response event. Additional stimulus events are allowed, additional response events not.
- The OutputSynchronizationConstraint is used to describe groups of event chains, which all have the same response events. The response events of the event chain must occur in common time intervals, like in the SynchronizationConstraint. In the InputSynchronizationConstraint, the roles of the stimulus and response events are swapped.

2.2.1. Parenthesis - Simple and Flexible Timing Constraint Logic

The formal definition of the TADL2 timing constraint are written in $Timing\ Constraint\ Logic\ (short:\ TiCL)$, which was developed as part of the TIMMO-2-USE project. TiCL was formally introduced in [LN12], for better understanding the key aspects of this article will be explained in the following.

The main goal of TiCL is to be formal and expandable and offering the possibility of defining finite and infinite behaviors of events. In TiCL, only points in time, when events occur, are considered, therefore an events only consists of a real number as timestamp, without the possibility of adding a data value. There are 7 syntactic categories in TiCL

```
\mathbb{R}(arithmetic constants)

Avar(arithmetic variables)

AExp(arithmetic expressions)

Svar(set variables)

SExp(set expressions)

TVar(time variables)

CExp(constraint expressions)
```

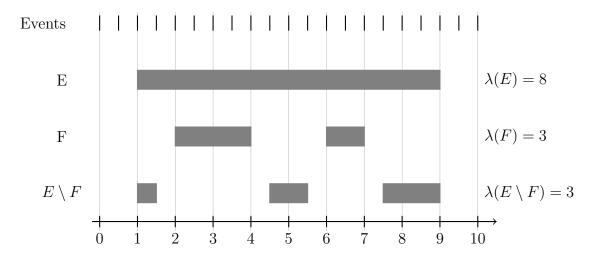


Figure 2.4.: Graphical example of $\lambda(E)$, $\lambda(F)$ and $\lambda(E \setminus F)$

Arithmetic expressions can be defined as arithmetic constants, arithmetic variables, application of +,-,*,/ on arithmetic expressions, application of the cardinality operator on a set $(|E|, E \in SExp)$ or as measure $\lambda(E)$ $(E \in SExp)$. $\lambda(E)$ is defined as Lebesgue measure, which is figuratively speaking, the length of all continuous intervals of E. In figure 2.4 an example of the measure operator λ is visualized. The set E contains all Events between the timestamps 1 and 9, the set E contains the events at the timestamps between 2 and 4 and 6 and 7, therefore $E \setminus F$ contains the events at the timestamps $\{1, 1.5, 4.5, 5, 5.5, 7.5, 8, 8.5, 9\}$. E consists of one continuous interval from timestamp 1 to 9 with the length of 8, E consists of two continuous intervals from 2 to 4 with the length of 2 and from 6 to 7 with the length of 1, therefore $\lambda(F) = 3$. $E \setminus F$ consists of three continuous intervals, the first from 1 to 1.5 (length E 0.5), the second from 4.5 to 5.5 (length E 1) and the last from 7.5 to 9 (length E 1.5), so the total length of the continuous intervals of $E \setminus F$ is 3.

Set expressions can be defined as set variables, or as set of time variables that fulfill a given constraint expression.

Constraint expressions can be defined as application of the \leq -operator on time or arithmetic expressions, the \in operator on time variables and set expressions, the logical conjunction on constraint expressions, the negation of constraint expressions and the \forall -Quantifier on arithmetic, set and time variables over an constraint expression.

As extension to this definition, well known syntactic abbreviations like $true \equiv 0 \leq 1$ or the \exists -quantifier will be used, but there are also some TiCL-specific syntactic abbreviations, like interval constructors, which will be defined and explained in the following.

Interval Constructors

Let $x, y \in Tvar$ and $E, F \in SExp$.

The constructor $[x \le]([x <])$ is defined as $\{y : x \le y\}(\{y : x < y\})$, therefore the interval contains all points in time laying behind of x, possibly containing x.

 $[\leq x]([< x])$ is defined as complement of $[x <]([x \leq])$ and contains all timestamps laying before x.

[x..y] is defined as $[x \le] \cap [< y]$, so all points of time after x and before y, including x but not y, are part of this interval.

 $[E \leq]$ is defined as $\{y : \exists x \in E : x \leq y\}$, this interval contains all point of time at and after the first timestamp in E. [E <] is equal to $\{y : \forall x \in E : x < y\}$, therefore it defines the interval containing all timestamps after the latest point of time in E. $[\leq E]$ ([< E]) is defined as $[E <]^C$ ($[E \leq]^C$), analogous to the operators on time variables.

[E] is equal to $[E \leq] \cap [\leq E]$. It defines the time interval between the first and last element of E, including these points in time.

 $E_{x<}(E_{<x})$ is defined as $E \cap [x <](E \cap [< x])$. This operators filters the timestamps in E so that only the points in time before (after) remain.

[x..E] equals $[x \leq] \cap [\langle (E_{x \leq})]$. The interval begins at x and ends right before the first element of E after x.

[E..F] is defined as $\{x : \exists y \in E : x \in [y..F]\}$ and describes the intervals, where the previous operator is applied on every element of E.

2.2.2. TADL2-Timing Constraints

For better understanding of the following chapters, the TADL Constraints will be presented next. As abbreviation and unification, all timing expressions are defined as set \mathbb{T} , which are understood as real numbers but expanded with ∞ and $-\infty$ in this chapter, but other value ranges for time expressions are possible and will be used in other parts of this thesis.

We define an event as a time value, possibly combined with an data value. The range of the data values are arbitrary, infinite data types are possible, also as empty data types, when only the point in time is relevant for the event. All TADL constraints are defined with attributes, which can be events, timing or arithmetic expressions or sets of them. Also, *EventChains* can be used as attributes. An *EventChain* consists of two sets of events (*stimulus* and *response*), which are causally related. All events in an *EventChain* must have a color value in their data field. This color possibly has an infinite type and an equality check on this must be defined. It is used to check, which events of an *EventChain* are directly related.



Figure 2.5.: Example DelayConstraint - lower = 2, upper = 3

DelayConstraint

The DelayConstraint has 4 attributes

```
source event set target event set lower \mathbb{T} (time expression) upper \mathbb{T}
```

and is defined as

```
\forall x \in source : \exists y \in target : lower \leq y - x \leq upper.
```

For all events x in source, there must be an y event in target, so that y lays between lower and upper after x. Note, that lower and upper can have negative values and that additional events in target, without an associated source event are allowed. Figure 2.5 shows a visualized example of the DelayConstraint with the attributes lower = 2, upper = 3, $source = \{1, 5, 6\}$ and $target = \{2, 3.5, 5, 7, 8.2, 9\}$. The first element of source at timestamp 1 results in a required event in target between the timestamp 3 and 4 that is fulfilled by the event at 3.5. The second event of source requires an target event between 7 and 8, fulfilled by the event at 7. The last event of source is satisfied by the target event at 8.2 and 9.

StrongDelayConstraint

The StrongDelayConstraint has 4 attributes

```
\begin{array}{ccc} source & \text{event set} \\ target & \text{event set} \\ lower & \mathbb{T} \end{array}
```

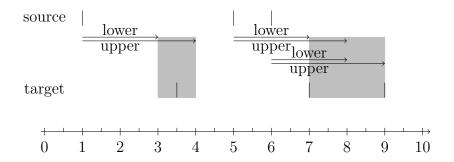


Figure 2.6.: Example StrongDelayConstraint - lower = 2, upper = 3

upper \mathbb{T}

and is defined as

```
|source| = |target| \land 
\forall i : \forall x : x = source(i) \Rightarrow \exists y : y = target(i) \land lower \leq y - x \leq upper.
```

The StrongDelayConstraint is a stricter version of the DelayConstraint, as it requires a bijective assignment between the source and target events, therefore additional events in target without matching source event are not allowed. Figure 2.6 shows an example of the StrongDelayConstraint. The example is the same as in the previous constraint, but without the additional target events at 2, 5 and 8.2.

RepeatConstraint

The RepeatConstraint also has 4 attributes

```
\begin{array}{ccc} event & \text{event set} \\ lower & \mathbb{T} \\ upper & \mathbb{T} \\ span & integer \end{array}
```

and is defined as

$$\forall X \leq event : |X| = span + 1 \Rightarrow lower \leq \lambda([X]) \leq upper.$$

As reminder, the $A \leq B$ -operator over two sets of events A, B describes, that A is a sub-sequence of B, the $\lambda(A)$ -function calculates the total length of all continuous intervals in A and the [A] returns the time interval between the oldest and newest event in A.

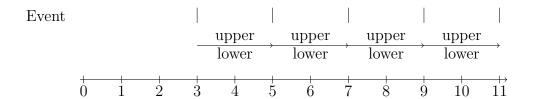


Figure 2.7.: Example RepeatConstraint - lower = 2, upper = 2, span = 1

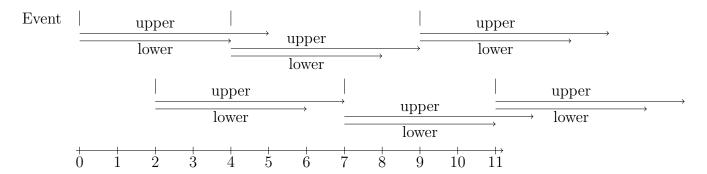


Figure 2.8.: Example RepeatConstraint - lower = 4, upper = 5, span = 2

The definition specifies that the length of each time interval containing span + 1 consecutively events must be between upper and lower.

The idea behind this constraint is to define repeated occurrences of events, with the possibility of overlapping, specified by the span attribute. After any event x, there are span-1 events and than the next event must be between lower and upper after x.

Figure 2.7 shows an example of the RepeatConstraint with the attributes $event = \{3, 5, 8, ...\}$, lower = upper = 2 and span = 1. Because lower is equal upper and span is 1, the events are following a strictly periodic pattern after the first event. Figure 2.8 shows a more complex example with events at $\{0, 2, 4, 7, 9, 11, ...\}$, lower = 4, upper = 5 and span = 2. The span-attribute is 2, so the time distance between all subsequent events with an even index are considered, just like the subsequent events with an uneven index.

RepetitionConstraint

The Repetition Constraint has 5 attributes

event event set

lower \mathbb{T}

upper \mathbb{T}

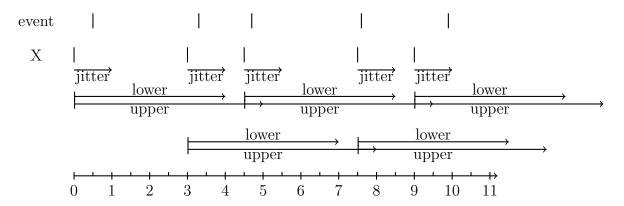


Figure 2.9.: Example Repetition Constraint - lower = 4, upper = 5, span = 2, jitter = 1

```
\begin{array}{ccc} span & integer \\ jitter & \mathbb{T} \end{array}
```

and is defined via the RepeatConstraint and the StrongDelayConstraint as

```
\exists X : RepeatConstraint(X, lower, upper, span) \land StrongDelayConstraint(X, event, 0, jitter)
```

where X is a set of arbitrary time stamps, that follow the structure of the RepeatConstraint(various(span)) loose periodic repetitions). The actual points in time of event lay between the timestamps of X and jitter after that. For each point of time there is one, and only one, corresponding timestamp in X. Figure 2.9 shows an example of the RepetitionConstraint with the attributes $event = \{0.5, 3.3, 4.7, 7.6, 9.9, ...\}$, lower = 4, upper = 5, span = 2 and jitter = 1. The shown timestamps of X are only one possibility and may change due to later elements of event.

SynchronizationConstraint

The SynchronizationConstraint has 2 attributes

```
event sets set of event sets, |event| \ge 2
tolerance \mathbb{T}
```

and is defined via the *DelayConstraint* as

```
\exists X: \forall i: DelayConstraint(X, event_i, 0, tolerance) \land \\ DelayConstraint(event_i, X, -tolerance, 0)
```

X is a set of arbitrary point in time and there must be at least one timestamp in

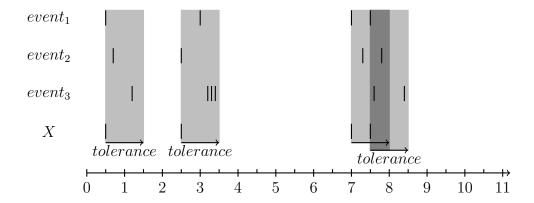


Figure 2.10.: Example SynchronizationConstraint - tolerance = 1

each set of event, that is between an element of X and tolerance after that. Also, for each element in any set of event, there must be a matching element of X. In figure 2.10 is an example of the SynchronizationConstraint with the attributes $event = \{\{0.5, 3, 7, 7.5\}, \{0.7, 2.5, 7.3, 7.8\}, \{1.2, 3.2, 3.3, 3.4, 7.6, 8.4\}\}$ and tolerance = 1. The first points in time of each element of event form the first cluster, the corresponding element of X can be between 0.2 and 0.5. For simplification, only the latest possible value for the element of X are shown, which is the first event of the synchronization cluster. In the second cluster of events it can be seen that multiple timestamps from one element of event can be associated with a single element of event and fourth cluster show, that overlapping is also possible.

StrongSynchronizationConstraint

The StrongSynchronizationConstraint has the same two attributes as the SynchronizationConstraint

```
\begin{array}{ll} event & \text{set of event sets, } |event| \geq 2 \\ tolerance & \mathbb{T} \end{array}
```

and is defined as

 $\exists X : \forall i : StrongDelayConstraint(X, event_i, 0, tolerance)$

The StrongSynchronizationConstraint is a stricter variant of the Synchronization-Constraint, as it requires a bijective assignment between the elements of X to one element of each set of event. For every $x \in X$, only one corresponding timestamp per set in event is allowed, like seen in figure 2.11, which shows the same example as the one for the SynchronizationConstraint, but the excess time stamps at 3.2 and 3.3 have been removed.



 $\textbf{Figure 2.11.:} \ \textbf{Example StrongSynchronizationConstraint} \ \textbf{-} \ tolerance = 1$

ExecutionTimeConstraint

The Execution Time Constraints takes 6 attributes

```
\begin{array}{ccc} start & \text{set of events} \\ stop & \text{set of events} \\ preempt & \text{set of events} \\ resume & \text{set of events} \\ lower & \mathbb{T} \\ upper & \mathbb{T} \end{array}
```

and is defined as

$$\forall x \in start : lower \leq \lambda([x..stop] \setminus [preempt..resume]) \leq upper$$

The interval constructor $\forall x \in start : [x..stop]$ defines the time interval between each point in time of start until the next element of stop, excluding the stop timestamp. [preempt..resume], which is removed from the considered interval length, defines the intervals between each element of preempt until the next timestamp of resume. The Idea behind this constraint is to test the run time of a task, without counting interruptions.

Figure 2.12 shows an example of the ExecutionTimeConstraints with $start = \{1\}$, $end = \{7\}$, $preempt = \{2,5\}$ and $resume = \{3,6.5\}$. Therefore, [start..end] spans the interval from time 1 to 7 with the length of 6 and [preempt..resume] spans two intervals, 2 to 3 and 5 to 6.5 with the length 1 and 1.5. As result, $\lambda([x..stop] \setminus [preempt..resume])$ for x = 1 is 3.5 and the constraint is fulfilled, if, and only if, lower is equal or lower than 3.5 and upper is greater than that.

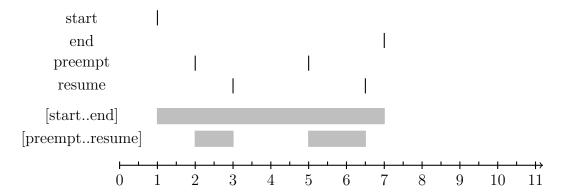


Figure 2.12.: Example ExecutionTimeConstraint



Figure 2.13.: Example OrderConstraint

OrderConstraint

The OrderConstraint takes two attributes

```
source set of events
target set of events
```

and is defined as

$$|source| = |target| \land \forall i : \exists x : x = source(i) \Rightarrow \exists y : y = target(i) \land \langle x \leq y \rangle$$

This constraints ensures the order of events, so that the *i*-th event of *target* is after the *i*-th event of *source*. Also, the number of events in *source* and *target* must be equal.

Figure 2.13 visualizes an example of the OrderConstraint with $source = \{1, 4, 6, 7\}$ and $target = \{3, 5, 9, 9.5\}$. The constraint is fulfilled, because the number of elements is equal and each i-th timestamp in target is later that the i-th timestamp of source.

ComparisonConstraint

The ComparisonConstraint is significant different to all previous and following constraints, as it does not describe the behavior of events and only compares two time expressions. It takes 3 attributes

The definition is pretty straight forward as it only applies the given operator to the operands:

```
ComparisonConstraint(leftOperand, rightOperand, LessThanOrEqual) \\ \Leftrightarrow leftOperand \leq rightOperand \\ ComparisonConstraint(leftOperand, rightOperand, LessThan) \\ \Leftrightarrow leftOperand < rightOperand \\ ComparisonConstraint(leftOperand, rightOperand, GreaterThanOrEqual) \\ \Leftrightarrow leftOperand \geq rightOperand \\ ComparisonConstraint(leftOperand, rightOperand, GreaterThan) \\ \Leftrightarrow leftOperand > rightOperand \\ ComparisonConstraint(leftOperand, rightOperand, Equal) \\ \Leftrightarrow leftOperand = rightOperand \\
```

Due to the simplicity of this constraint, no explicit example is given.

SporadicConstraint

The SporadicConstraint takes 5 attributes

```
\begin{array}{ccc} event & \text{set of events} \\ lower & \mathbb{T} \\ upper & \mathbb{T} \\ jitter & \mathbb{T} \\ minimum & \mathbb{T} \end{array}
```

and is defined as combination of the Repetition Constraint and the Repeat Constraint as

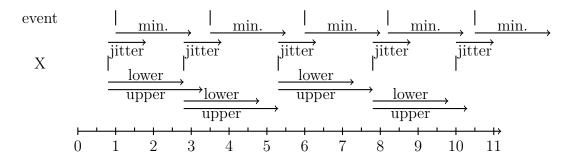


Figure 2.14.: Example SporadicConstraint - lower = 2, upper = 2.5, jitter = 1, minimum = 2

RepetitionConstraint(event, lower, upper, 1, jitter) \land RepeatConstraint(event, minimum, ∞ , 1)

The second part of the definition, using the RepeatConstraint, ensures that all events in event lay at least minimum apart. The application of the RepetitionConstraint generates a set of events X, that lay between lower and upper apart from each other. For each point in time in X, there must be exactly one timestamp in event, that is not before the corresponding element of X and not later than jitter after that.

Figure 2.14 shows a possible application of the SporadicConstraint with the attributes lower = 2, upper = 2.5, jitter = 1, minimum = 2 and $event = \{1, 3.5, 6, 8.2, 10.5, ...\}$. Like in the RepetitionConstraint, the exact position of the timestamps in X is variable and may need to be changed due to later entries in event.

PeriodicConstraint

The PeriodicConstraint takes 4 attribute

```
\begin{array}{ccc} event & \text{set of events} \\ period & \mathbb{T} \\ jitter & \mathbb{T} \\ minimum & \mathbb{T} \end{array}
```

and defines a specialized form of the Sporadic Constraint

SporadicConstraint(event, period, period, jitter, minimum)

The variable timestamps in the set X are now following a strictly periodic pattern, where subsequent elements of this set lay exactly period apart. Each element of event lays between one element of X and iitter after that. Again, there must be

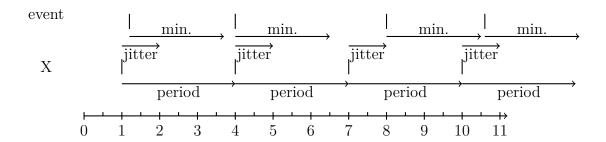


Figure 2.15.: Example PeriodicConstraint - period = 3, jitter = 1, minimum = 2.5

bijective mapping between the elements of *event* and X.

In figure 2.15, the PeriodicConstraint with the attributes period = 3, jitter = 1, minimum = 2.5 and $event = \{1.2, 4.0, 8, 10.6, ...\}$ is visualized. The timestamps of X lay exactly period apart and the events behind that in the previously described way. Also, the minimum time distance between all points of time in event is minimum.

PatternConstraint

The PatternConstraint takes 5 attributes

```
\begin{array}{ccc} event & \text{set of events} \\ period & \mathbb{T} \\ offset & \text{set of } \mathbb{T} \\ jitter & \mathbb{T} \\ minimum & \mathbb{T} \end{array}
```

and is defined as

```
\exists X: PeriodicConstraint(X, period, 0, 0) \\ \land \forall i: DelayContraint(X, event, offset_i, offset_i + jitter) \\ \land RepeatConstraint(event, minimum, \infty, 1)
```

This constraint can be understood as a modification of the PeriodicConstraint, as it describes periodic behavior, but not from single events, but from groups of |offset| subsequent events, that follow specific time distances (specified by offset) after the strictly periodic timestamps of X.

There is a major weak spot in the definition of this constraint, because the set X can be set to the empty set. In this case, the part of the definition, which uses the PeriodicConstraint and the DelayContraint, are always satisfied, irrespective of the event in event. Therefore, the PatternConstraint only ensures the minimal distance

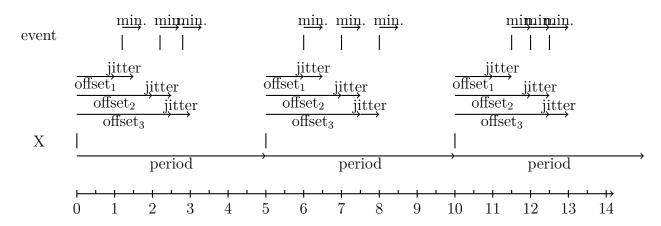


Figure 2.16.: Example PatternConstraint - period = 5, $offset = \{1, 2, 2.5\}$, jitter = 0.5, minimum = 0.5

between two events, what should not the purpose of this constraint. The obvious countermeasure to this problem would be to restrict X in a way that ensures that it is not empty and the first element of X must lay before the first event occurrence. The textual description of the constraint, which says literally the "PatternConstraint requires the constrained event occurrences to appear at a predetermined series of offsets from a sequence of reference points" contradicts this countermeasure, because the DelayConstraint allows additional events in the target events with no matching source event. Therefore, any event occurrences additionally to the events following the offset scheme, would be allowed, which conflicts with the citation. Because of this problem, the PatternConstraint is redefined as

```
 \exists X: PeriodicConstraint(X, period, 0, 0) \\ \land \forall i: \textbf{Strong}DelayContraint(X, event, offset_i, offset_i + jitter) \\ \land RepeatConstraint(event, minimum, \infty, 1)
```

for the scope of this thesis. The use of the *StrongDelayConstraint*, instead of the *DelayConstraint*, ensures that each event occurrence is following the time distances defined by the offsets. This notion of the *PatternConstraint* is also carried by the described relations between the TADL2 timing constraints and the AUTOSAR Timing Extensions, which were done as part of the development of TADL2. These descriptions equate the *PatternConstraint* and AUTOSARs *ConcretePatternEventTriggering*, which is clearly defined in the way of this redefinition.

Figure 2.16 shows an application of the PeriodicConstraint with attributes period = 5, $offset = \{1, 2, 2.5\}$, jitter = 0.5, minimum = 0.5 and $event = \{1.2, 2.2, 2.8, 6, 7, 8, 11.5, 12, 12.5, ...\}$. Like in the previous describes constraint, the exact position of all points in time of X may change due to later timestamps of event.

	1	2	3	5	8	10
1	0	1	2	4	7	9
2		0	1	3	6	8
3			0	2	5	7
5				0	3	5
8					0	2
10						0

Table 2.1.: Time distances as seen in figure 2.17

ArbitraryConstraint

The Arbitrary Constraint takes 3 attributes

```
\begin{array}{ll} \textit{event} & \text{set of events} \\ \textit{minimum} & \text{set of } \mathbb{T} \\ \textit{maximum} & \text{set of } \mathbb{T} \end{array}
```

where |minimum| = |maximum|. It is defined as

 $\forall i : RepeatConstraint(event, minimum_i, maximum_i, i)$

The Idea behind the *ArbitraryConstraint* is to describe the time distance between each event and several following events. The first entry of *minimum* and *maximum* define the distance between every event and it direct successor. The second entries, where the *span* attribute of the *RepeatConstraint* is 2, set the distance between one event and its next but one successor and so on.

Figure 2.17 shows an example of the Arbitrary Constraint with the attributes $minimum = \{1, 2, 3\}$, $maximum = \{5, 6, 7\}$ and $event = \{1, 2, 3, 5, 8, 10, ...\}$. The time distances between subsequent events with 0, 1 and 2 skipped events are shown in table 2.1, the relevant distances are written in **bold** font. Apparently, the time distances are matching the ranges, given by the minimum- and maximum attribute.

BurstConstraint

The BurstConstraint takes 4 attributes

```
\begin{array}{cc} \textit{event} & \text{set of events} \\ \textit{length} & \mathbb{T} \\ \textit{maxOccurrences} & \textit{integer} \end{array}
```

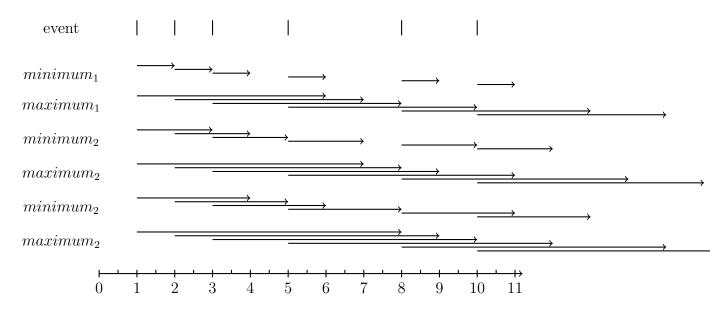


Figure 2.17.: Example ArbitraryConstraint - period = 5, $offset = \{1, 2, 2.5\}$, jitter = 0.5, minimum = 0.5

minimum \mathbb{T}

and is defined as

 $RepeatConstraint(event, length, \infty, maxOccurrences) \land RepeatConstraint(event, minimum, \infty, 1)$

The idea of this constraint is to describe the maximum number of events that may occur in a time interval of the given *length*. Additionally all subsequent event must be at least *minimum* apart. Therefore, the intuition is different to the AUTOSAR *BurstPatternEventTriggering*, where clusters of events are described. A complete comparison of these constraints will be done in section 2.2.3.

In figure 2.18 the BurstConstraint with the attributes length = 5, maxOccurrences = 3, minimum = 0.8 and $event = \{1, 2, 3, 7, 8, 9\}$ is visualized. In every interval of the length 5, there are three or less events, also all subsequent events lay at least 0.8 apart. Therefore, the constraint is fulfilled.

ReactionConstraint

The ReactionConstraint takes 3 attributes

 $\begin{array}{cc} scope & EventChain \\ minimum & \mathbb{T} \end{array}$

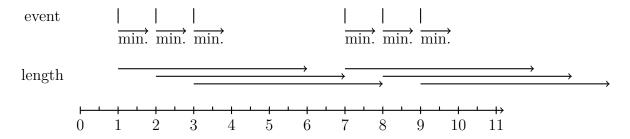


Figure 2.18.: Example BurstConstraint - length = 5, maxOccurences = 3 minimum = 0.8

maximum \mathbb{T}

and is defined as

```
\forall x \in scope.stimulus : \exists y \in scope.response : \\ x.color = y.color \\ \land (\forall y' \in scope.response : y'.color = y.color \Rightarrow y \leq y') \\ \land minimum < y - x < maximum
```

The definition says, that after every event x of scope.stimulus, there is an event y in scope.response with the same color. The time distance between these events must be at least minimum and at most maximum. Additional events with the same color as y in scope.response are allowed, if they lay behind y. The definition implies, that additional events with other colors are allowed in scope.response, but not in scope.stimulus and every color is only allowed once in scope.stimulus. A visualized example with the attributes minimum = 1, maximum = 3, $scope.stimulus = \{(1, red), (5, green), (5.5, purple), (8, orange)\}$ and $scope.response = \{(0.8, blue), (2.1, red), (4.5, blue), (6.6, purple), (6.7, purple), (9.5, purple), (7.5, green), (10, orange)\}$ can be seen in figure 2.19. The red stimulus-event is followed by the red response-event at 2.1, the green stimulus event at 5 by the response event at 7.5 and so on. The blue response events at 1 and 4.5 are additional events without an associated stimulus event. The purple events at 6.7 and 9.5 are the second and third event of this color in scope.response and therefore, their time distance to the stimulus event with the same color is irrelevant.

AgeConstraint

The AgeConstraint takes 3 attributes

 $\begin{array}{cc} scope & EventChain \\ minimum & \mathbb{T} \end{array}$

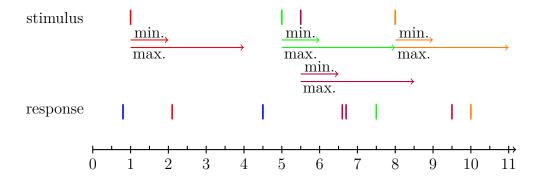


Figure 2.19.: Example ReactionConstraint - minimum = 1, maximum = 3

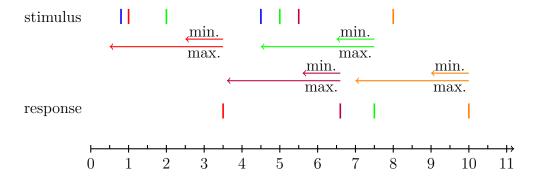


Figure 2.20.: Example AgeConstraint - minimum = 1, maximum = 3

maximum \mathbb{T}

and is defined as

```
\forall y \in scope.response : \exists x \in scope.stimulus : \\ x.color = y.color \\ \land (\forall x' \in scope.stimulus : x'.color = x.color \Rightarrow x' \leq x) \\ \land minimum \leq y - x \leq maximum
```

The AgeConstraint is a turned around counterpart to the ReactionConstraint. For every event of scope.response, there must be an event with the same color in scope.stimulus, that is between minimum and maximum older than the response event. Additional events are only allowed in scope.stimulus, and only before the event that matches with a response event.

Figure 2.20 shows an application of the AgeConstraint with the attributes minimum = 1, maximum = 3, $scope.stimulus = \{(0.8, blue), (1, red), (2, green), (4.5, green), (5.5, purple), (8, orange)\}$ and $scope.response = \{(3.5, red), (7.5, green), (6.6, purple), (10, orange)\}$. The blue timestamps are additional events without matching events in scope.response.

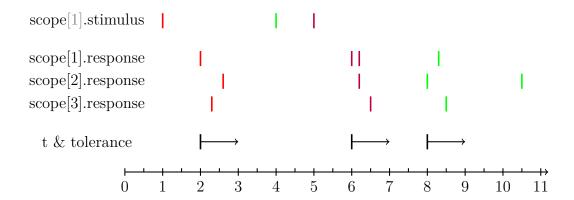


Figure 2.21.: Example OutputSynchronizationConstraint - tolerance = 1

OutputSynchronizationConstraint

The OutputSynchronizationConstraint takes 2 attributes

```
\begin{array}{ccc} scope & \text{Set of } EventChain \\ tolerance & \mathbb{T} \end{array}
```

where all elements of *scope* have the same *stimulus*. It is defined as

The definition says, that after each event x in $scope_1.stimulus$, there must be a interval with the length of tolerance, in which every $scope_i.response$ must have an event y with the same color as x. Additional response events with this color are only allowed after y. Figure 2.21 shows an example of the OutputSynchronization-Constraint with the attributes tolerance = 1,

```
scope[1].stimulus = scope[2].stimulus = scope[3].stimulus = \{(1, red), (4, green), (5, purple)\},\\ scope[1].response = \{(2, red), (6, purple), (6.2, purple), (8.2, green)\},\\ scope[2].response = \{(2.6, red), (6.2, purple), (8, green), (10.5, green)\},\\ scope[3].response = \{(2.3, red), (6.5, purple), (8.5, green)\}.
```

InputSynchronizationConstraint

The InputSynchronizationConstraint takes 2 attributes

```
scope Set of EventChain
```

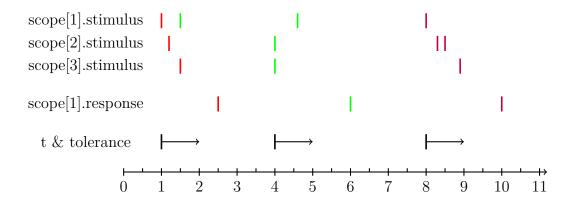


Figure 2.22.: Example InputSynchronizationConstraint - tolerance = 1

tolerance \mathbb{T}

where all elements of *scope* have the same *response*. It is defined as

```
\forall y \in scope_1.response : \exists t : \forall i : \exists x \in scope_i.stimulus : x.color = y.color 
 \land (\forall x' \in scope_i.stimulus : x'.color = x.color \Rightarrow x \leq x') 
 \land 0 \leq x - t \leq tolerance
```

The InputSynchronizationConstraint is a counterpart of the OutputSynchronization-Constraint, as the stimulus events must be synchronized, not the response events. Figure 2.22 contains an example of the InputSynchronizationConstraint with the attributes tolerance = 1

```
scope[1].stimulus = \{(1, red), (1.5, green), (4.6, green), (8, purple)\} \\ scope[2].stimulus = \{(1.2, red), (4, green), (8.3, purple), (8.5, purple)\} \\ scope[3].stimulus = \{(1.5, red), (4, green), (8.9, purple)\} \\ scope[1].response = scope[2].response = scope[3].response = \{(2.5, red), (6, green), (10, purple)\} \\ scope[1].response = scope[2].response = scope[3].response = \{(2.5, red), (6, green), (10, purple)\} \\ scope[3].response = scope[3].
```

2.2.3. Comparison TADL2 - AUTOSAR Timing Extension

As said before, the TADL2 Timing Constraints and the AUTOSAR Timing Extension are compatible in parts and many of the AUTOSAR Timing Extension can be expressed as equivalent combinations of the TADL2 Timing Constraints. In [BFL+12], the relation between these constraints is shown, but this comparison is based on an outdated version of the AUTOSAR Timing Extensions and some of the constraints have been updated, therefore each of the AUTOSAR Timing Extensions will be listed in this chapter and it will be explained, if and how they can be expressed using TADL2 Timing Constraints.

The types used in the AUTOSAR Timing Extension are similar to the ones in TADL2. TADL2 Events are called TimingDescriptionEvent in AUTOSAR, the same goes for EventChains, which are called TimingDescriptionEventChains. A larger difference can be seen in the definition of time. While TADL2 defines time as real numbers, the time definition used in the AUTOSAR Timing Extension can also be multidimensional, for example when the real time and the angle of the crankshaft is regarded. For simplification, all timestamps are considered as real numbers in the following, but an extension to multidimensional time stamps is possible, as AUTOSAR requires a strict order between all time stamps. Executable entities as defined in the AUTOSAR Timing Extension describe things, that can be executed, for example a function. For the timing constraints, only striking point in times of these entities are relevant, for example the start or end points. It should be noted, that the set of TADL2 timing constraints are not equal to the AUTOSAR Timing Extension and that there are constraint, that cannot be expressed using the corresponding counterpart.

PeriodicEventTriggering

The PeriodicEventTriggering defined in AUTOSAR with the attributes (event, period, jitter, minimumInterArrivalTime) is equivalent to the TADL2 PeriodicConstraint with the same attributes.

SporadicEventTriggering

AUTOSARs SporadicEventTriggering with the attributes (event, jitter, maximumInterArrivalTime, minimumInterArrivalTime, period) is equivalent to the TADL2 SporadicConstraint, but the names of the attributes are different:

```
lower = period

upper = maximumInterArrivalTime

jitter = jitter

minimum = minimumInterArrivalTime
```

ConcretePatternEventTriggering

The idea behind the *ConcretePatternEventTriggering* from AUTOSAR is the same as behind TADL2s *PatternConstraint*, but subtleties are different. Both define a periodic behavior and offsets, that describe time distances between the periods and

the actual events. The main difference is the *jitter* attribute. In AUTOSARs ConcretePatternEventTriggering, the patternJitter attribute defines the allowed deviation of the start points of the periodic repetitions, as in TADL2 the *jitter* value describes the deviation between the offsets and the actual event.

The ConcretePatternEventTriggering from AUTOSAR additionally defines an patternLength attribute, which describes the length of the intervals, in which the clusters of events will occur. It is constrained by

```
0 \le max(offset) \le patternLength
 \land patternLength + patternJitter < patternPeriod
```

The *patternLength* attribute can not be described with TADL2 timing constraints, as it would require to determine the distance of filtered events, which is not possible with the TADL2 constraints.

TADL2 defines the *minimum* attribute for the *PatternConstraint* that describes the minimal time distance between subsequent events. In AUTOSAR, this must be described by using the *ArbitraryEventTriggering*, where $minimumDistance_1$ is minimum and $maximumDistance_1$ is ∞ .

BurstPatternEventTriggering

The BurstPatternEventTriggering as defined in AUTOSAR and TADL2s BurstConstraint share the same target, as they define a maximum number of events that may occur in a specific time interval, but the BurstPatternEventTriggering is way more complex. Additionally to the attributes of TADL2s BurstConstraint, that define the length of the time interval, the maxOccurrences of the event in this interval and the minimal time between subsequent events, the BurstPatternEventTriggering allows to define the minimal number of events in the interval and periodic repetitions of the burst interval.

Every set of attributes fulfilling the TADL2 BurstConstraint fulfill the AUTOSAR BurstPatternEventTriggering, when the attributes are renamed to the AUTOSAR equivalents ($length \rightarrow patternLength$, $maxOccurences \rightarrow maxNumberOfOccurences$, $minimum \rightarrow minimumInterArrivalTime$). This does not work the other way around, even if the attributes, that exist in the BurstPatternEventTriggering and not in the BurstConstraint are unused. The reason for this is, that the observed interval must start at an event in the TADL2 BurstConstraint, in the BurstPattern-EventTriggering those can start in any point of time.

ArbitraryEventTriggering

AUTOSARs ArbitraryEventTriggering is similar to the ArbitraryConstraint as defined in TADL2, but ArbitraryEventTriggering allows to set a list of ConfidenceIntervals, to describe the probability, how far the events may lay apart. These probabilities can not be expressed in TADL2.

LatencyTimingConstraint

The LatencyTimingConstraint of AUTOSAR takes 5 attributes, a latency type $latencyConstraintType \in \{age, reaction\}$, three time values maximum, minimum and nominal and an event chain scope, consisting of the stimulus and response events. The nominal-value is not relevant for a formal definition of the Constraint, therefore there is no counterpart to this in the TADL2 Constraints. If the latencyConstraintType of the LatencyTimingConstraint is age, it can be expressed with AgeConstraint defined in TADL2. The LatencyTimingConstraint with the latencyConstraintType reaction is equivalent to the reactionConstraint.

AgeConstraint

The goal of the AgeConstraint in AUTOSAR is to define a minimal and maximal age of an event at the point in time, when it is processed. There is no counterpart to this in the TADL2 constraints, because the point in time, when the event is processed, is unknown. If this point in time is known, AUTOSARs AgeConstraint can be expressed using TADL2s AgeConstraint, but in that case, it could also be expressed using AUTOSARs LatencyTimingConstraint.

SynchronizationTimingConstraint

The Synchronization Timing Constraint is similar to the Synchronization Constraint, the Strong Synchronization Constraint, the Output Synchronization Constraint, the Input Synchronization Constraint or combinations of them, depending on the attributes. Table 2.2 shows, with which attributes the Synchronization Timing Constraint is equivalent to which TADL2 Constraint(s).

event Occurrence- Kind	scope/ scopeEvent	synchronization- ConstraintType	tolerance	TADL2 Constraints	
multiple Occurrences	scopeEvent	not set	tolerance	SynchronizationConstraint (scopeEvent, tolerance)	
single Occurrences	scopeEvent	not set	tolerance	StrongSynchronizationConstraint (scopeEvent, tolerance)	
multiple Occurrences	scope	response Synchronization	tolerance	OutputSynchronizationConstraint (scope, tolerance) ^ SynchronizationConstraint (scope.response, tolerance)	
single Occurrences	scope	response Synchronization	tolerance	OutputSynchronizationConstraint (scope, tolerance) ^ StrongSynchronizationConstraint (scope.response, tolerance)	
multiple Occurrences	scope	stimulus Synchronization	tolerance	InputSynchronizationConstraint (scope, tolerance) ∧ SynchronizationConstraint (scope.stimulus, tolerance)	
single Occurrences	scope	stimulus Synchronization	tolerance	InputSynchronizationConstraint (scope, tolerance) ^ SynchronizationConstraint (scope.stimulus, tolerance)	

 Table 2.2.:
 SynchronizationTimingConstraint
 \Leftrightarrow TADL2 Constraints

SynchronizationPointConstraint

The SynchronizationPointConstraint describes, that a list of executables and a set of events or executable entities, defined in sourceEec and sourceEvent, must finish and occur, before the executables and events in targetEec and targetEvent will start or occur. There is no counterpart to this in the TADL2 constraints.

OffsetTimingConstraint

The Offset Timing Constraint, defined in AUTOSAR Timing Extensions, is semantically the same as the TADL2 Delay Constraint, just some attributes are named differently. The maximum attribute of the Offset Timing Constraint is named upper and the minimum attribute lower in the Delay Constraint.

ExecutionOrderConstraint

The goal of *ExecutionOrderConstraint* of the AUTOSAR Timing Extensions is used to describe the order of events or the execution order of executable entities, defined as *orderedElement* attribute. There is no constraint in TADL2 that describes exactly this, but if the *ExecutionOrderConstraint* is used to describe only the order of events, it can be described as

```
OrderConstraint(orderedElement_1, orderedElement_2)
\land ... \land
OrderConstraint(orderedElement_{n-1}, orderedElement_n)
```

If the *ExecutionOrderConstraint* is used for executable entities, each executable entity must be turned into one or more events to be described via TADL2 Constraints, depending on the other attributes. For example, if the attribute *executionOrder-ConstraintType* is set to *ordinaryEOC*, the start and finish points of the entities define the observed events.

ExecutionTimeConstraint

The idea behind the *Execution Time Constraint* is similar in AUTOSAR and TADL2. Both describe the minimal and maximal allowed run time of an executable entity, not counting interruptions. AUTOSARs *Execution Time Constraint* is defined directly on an executable entity and the TADL2 constraint on events describing the *start*, *stop*, *preemption* and *resume* timestamps. Therefore the executable entity must be turned into these events to express the AUTOSAR *Execution Time Constraint* via TADL2

constraints. The start and stop points of the executable must be turned into these events, the start and stop points of the interruptions must be turned into the events in the *preempt* and *resume* event sets. If external calls should be excluded from the run time, they must also be transferred into the *preempt* and *resume* event sets.

3. Related work and basics

3.1. Runtime Verification

Monitoring the AUTOSAR Timing Extensions is the goal of this thesis. As monitoring plays a major role in runtime verification, a short overview of this will be given. The definitions of [LS09] are used, in which Runtime Verification is a technique that can detect deviations between the run of a system and its formal specification by checking correctness properties. A run, which might also be called trace, is sequence of the system states, which might be infinite and an execution is an finite prefix of this run. A monitor reads the trace and decides, whether it fulfills the correctness properties or violates them.

A distinction is made between *offline* and *online* monitoring. Offline monitoring is using a stored trace, that has been recorded before. Therefore, the complete trace (or the complete part of the trace, that should be analyzed) is known in the analysis. Online monitoring checks the properties, while the system is running, which means that the analysis must be done incrementally. Because of memory and time limitations, not all previous states can be read again in online monitoring, more detailed contemplations on the limitations of online monitors will be given in chapter 4.

3.2. TeSSLa

TeSSLa (**Te**mporal **S**tream-based **S**pecification **La**nguage) is a functional programming language, build for runtime verification of streams. In TeSSLa, **streams** are defined as traces of events, each event consists of one data value from a data set \mathbb{D} and a time value from a time domain \mathbb{T} , which is a *totally ordered semi-ring* ($\mathbb{T}, 0, 1, +, *, \leq$), that is not negative.

This time domain needs a total order and subsequent timestamps must have increasing time values. A TeSSLa Specification can have several streams with different data sets, but each of these streams must use the same time domain \mathbb{T} , which timestamps are increasing over all streams. Each stream can have only one event per timestamp, but it is possible to have events on different streams at the same timestamp.

A distinction between synchronous and asynchronous streams is made. A set of synchronous streams have events in the exact same time stamps, events in asynchronous streams do not have this restriction. It is easy to see, that synchronous streams are a subset of the asynchronous ones, therefore we will only use asynchronous streams from now on.

In TeSSLa, calculations are done, when new events are arriving. Based on the specification, output streams are generated with events on the same timestamps as the used input streams, but filtering is possible, where not all input events produce output events. With the *delay*-operator, it is possible to create new timestamps. This possibility will take a large role in this thesis, more on that later.

At the timestamps, in which events arrived and calculations are done, you only have direct access to the youngest event of each stream, but with the use of the *last*-operator, which can be used recursively, the event before that can be accessed. The *lift*-operator applies a function, which is defined on data values \mathbb{D} , on each event of one or more streams. Similar to this, the *slift*-operator (signal lift) first applies the given function, when there was at least one event of each input stream. The time-operator returns the time value of an event.

3.3. Finite Transducers

4. Monitorability of properties on infinite Streams

The goal of this paper is to implement an online monitor for TADL2 Timing Constraint on possibly infinite streams using embedded hardware, like FPGAs or small ARM based computers. Because of finite resources, several constraints must be fulfilled, to get correct results in a reasonable time in every case. Therefore, the term of *Finite Monitorability* will be introduced, which ensures that monitoring is possible using the mentioned setting.

4.1. Finite Monitorability

4.1.1. Timestamps

As we consider streams that can be infinite, the time value of events can also grow into infinity. This is problematic, because it leads to infinite memory and runtime requirements, which cannot be meet, especially not in the context of online monitoring. Therefore, the time domain T must be restricted by the following constraints:

- T must be discrete.
- The first used timestamp has the value $t_0 = 0$
- All used timestamps must be smaller than t_{max} . t_{max} must be big enough, so it is not reached in practical use ¹.
- The distance between two subsequent time values is small enough to observe the wanted constraints.

4.1.2. Finite Monitorability

For the definitions of streams and functions defined on them, TeSSLa-like syntax is used. Also, some standard TeSSLa functions are used in the definitions.

¹ for example, a 64-bit unsigned integer variable is enough, to cover nanoseconds for 584.55 years

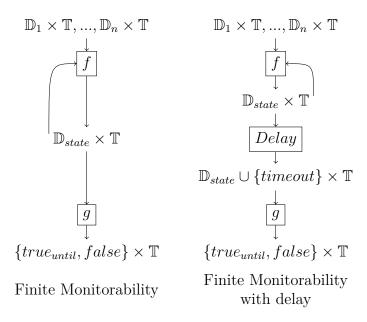


Figure 4.1.: Overview Finite Monitorability - with or without delay

Input Streams

Let $S_1, S_2, ..., S_n$ be input streams with $\forall i : S_i = (\mathbb{T} \cdot \mathbb{D}_i)^{\omega} \cup (\mathbb{T} \cdot \mathbb{D}_i)^+ \cup (\mathbb{T} \cdot \mathbb{D}_i)^* \cdot (\mathbb{T}_{\infty} \cup \mathbb{T} \cdot \{\bot\})$ and All types D_i have a finite size.

State Stream

```
Let S_{state} with S_{state} = (\mathbb{T} \cdot \mathbb{D}_{state})^+ \cup (\mathbb{T} \cdot \mathbb{D}_{state})^* be a state stream, where \mathbb{D}_{state} has a finite size. Further let f: S_1 \times S_2 \times ... \times S_n \times S_{state} \to S_{state} \times \mathbb{T} a state transition function, which defines the state stream in an incremental fashion: \forall t \in \mathbb{T} \exists i \in \{1, 2, ..., n\}: S_i(t) \in \mathbb{D}_i \to S_{state}(t) = f(S_1(t), S_2(t), ..., S_n(t), last(S_{state}, merge(S_1, S_2, ..., S_n))(t)) The runtime of f is in \mathcal{O}(1).
```

Output Stream

Let $S_{output} = (\mathbb{T} \cdot \{true_{until}, false\})^+ \cup (\mathbb{T} \cdot \{true_{until}, false\})^*$ be the output stream, which is defined via a function

 $g: \mathbb{D}_{state} \times \mathbb{T} \to \{true_{until}, false\} \times \mathbb{T}$ The runtime of g is in $\mathcal{O}(1)$.

Evaluation

A property of a set of streams is called *Finite Monitorable*, if a function f with type \mathbb{D}_{state} and a function g exist, which fulfill the characteristics called above, and which outputs $true_{until}$, as long as the property is fulfilled and false, in any other case. It should be noted that these definitions are $timestamp\ conservative$, because the streams S_{state} and S_{output} can only change their data value at the timestamps of input events.

Equivalences

4.1.3. Finite Monitorability with Delay

Not all of the TADL2 constraints can be monitored in a timestamp conservative. For example, the RepeatConstraint with the attributes lower = upper = 4 and span = 1 expects subsequent events to have a time distance of 4. If one event is missing, the output of a timestamp conservative monitor would still be $true_{until}$, until the next input event arrives. Therefore, the monitor cannot not check the constraint correctly. Because of this problem, the definition of $Finite\ Monitorability$ is expanded by the ability of introducing new timestamps. To ensure the finiteness of the monitor, only one new timestamp can be introduced, more on that in 4.1.3.

Input Streams

The definition of the input streams are unchanged.

State Stream

The function f remains unchanged, but the state stream S_{state} is expanded by an timeout value, which is inserted after a specific period of time, in which no input event has arrived.

Delay

A $Delay\ Generator$ is inserted into the definition. It has two tasks, first it copies each input it gets from the state transition function f to its output. At the timestamp where an input is copied, a timer, which length depends on the state of the monitor, is started. If the next input comes before the timer runs out, the timer is resetted and started again. If the timer runs out, the Delay Generator outputs the timeout signal, which is repeated at every following input. After the timer has run out once, it is not started again.

Output Stream

The output function g is expanded by the timeout value: $g: (\mathbb{D}_{state} \cup \{timeout\}) \times \mathbb{T} \to \{true_{until}, false\} \times \mathbb{T}$ The definition of the output stream S_{output} remains unchanged.

Evaluation

A property of a set of streams is called *Finite Monitorable with Delay*, if a function f with type \mathbb{D}_{state} , a delay generator and a function g exist, which fulfill the characteristics called above, and which outputs $true_{until}$, as long as the property is fulfilled and false, in any other case.

4.1.4. Non-Finite Monitorability

Not all TADL2 constraints are finite monitorable, because a monitor would require infinite memory and/or time resources. In a theoretical view, this makes online monitoring on infinite traces impossible, because a machine with infinite resources does not exist in the real world. In a practical view, many of these problems are solved by using a system with finite memory, with the hope that this finite resources would be enough, to cover the inputs of the "real world". In these cases, a distinction is useful, as some constraints have resource requirements, that grow continuously with every input event. These constraints will be called always Non-Finite Monitorable. Others constraints only require infinite resources in worst case scenarios, therefore these will be called worst case Non-Finite Monitorable. Obviously, the constraints with continuous resource requirement growth cannot be monitored infinitely, but the constraints, that only need infinite resources, can be monitored in many cases.

5. Analysis of the Monitorability of the TADL2 Timing Constraints

In this chapter, each of the TADL2 constraints will classified into the classes *Finite Monitorable*, *Finite Monitorable with Delay* and *Non-Finite Monitorability*, like defined in chapter4. For the last class, it will be demonstrated, if the constraint is non-finite monitorable in any cases or just in worst case scenarios.

DelayConstraint

The *DelayConstraint* is defined as

 $\forall x \in source : \exists y \in target : lower \leq y - x \leq upper.$

and describes that in the time interval between lower and upper after any source event, there is an target event. Therefore, the state that need to be stored to monitor the DelayConstraint is the set of source events, that did not have a matching target event. Updates to this state and outputs of the monitor are done at source and target events and at delay timestamps upper after source events, if there hasn't been a matching target event.

The maximal required storage size of the state depends on the number of source events, which can possibly occur in any time interval of the length upper. An example of this worst case situation can be seen in figure 5.1. The attributes in this example are lower = upper = 5, $source = \{1, 1.1, ..., 5.9\}$ and $target = \{6, 6.1, ..., 11\}$. At timestamp 6, all 49 source events must be stored, as they are all required to generate the correct output in this and the following timestamps. At this timestamp, the oldest source event can be removed from the storage, as the matching target event occurs in this timestamp. With every following target, the oldest event can be removed from the storage, until every source had its matching target event at timestamp 11.

Because the time domain is understood as real numbers in TADL2, a possibly infinite number of events can be placed in any interval of the length *upper*, therefore the required storage space can grow infinitely. Because the *source* events are removed from the state, when a matching *target* event occurs, the required storage space does not grow continuously and infinite resources are only required in worst case scenarios. Therefore, the *DelayConstraint* is *worst case Non-Finite monitorable*.

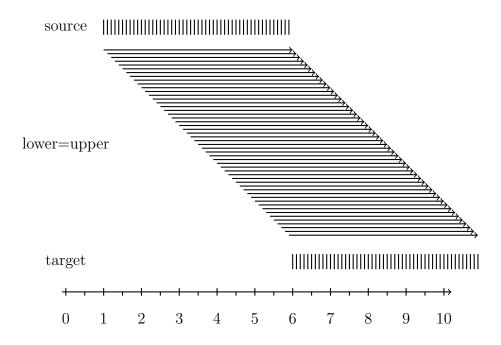


Figure 5.1.: DelayConstraint or StrongDelayConstraint with lower = upper = 5

StrongDelayConstraint

The difference between the *DelayConstraint* and the *StrongDelayConstraint* is, that for every *source* event, there must be exactly one matching *target* event in the *StrongDelayConstraint*. Therefore, the state of the monitor is nearly the same, as every *source* event, that did not have a matching *target* event yet, must be stored. Therefore, the only difference is, when these *source* events can removed from state and the *StrongDelayConstraint* is *worst case Non-Finite monitorable*, like the *DelayConstraint*.

RepeatConstraint

The RepeatConstraint defines the time distance between each event and its $span^{th}$ successor. Therefore, the state, that must be stored, consists of the timestamps of the span + 1 latest events. The state is updated at every event, the oldest stored event is removed and the timestamp of the current event is placed in the storage. The output function checks, if the time distance between the oldest stored event and the current timestamp is between lower and upper. To monitor this constraint, a single delay is required, because a missing event, or an event that occurs too late, would not be determined in the right timestamp.

As the memory requirements are fix (span + 1 timestamps must be stored) and the

state transition and output function can be programmed in a way that they are in $\mathcal{O}(1)$, the RepeatConstraint is finite monitorable with delay.

RepetitionConstraint

The RepetitionConstraint is defined as

```
RepetitionConstraint(s, lower, upper, span, jitter)

\equiv \exists X \subset \mathbb{T} : RepeatConstraint(X, lower, upper, span)

\land StrongDelayConstraint(X, s, 0, jitter)
```

The elements of set X follow the RepeatConstraint and the events, which should be monitored, are following in an interval of the length jitter after the elements of X. For each element of X, there is exactly one event and vice versa.

The monitoring algorithm for this constraint, which will be explained in detail in 6, stores the upper and lower bounds for the next span elements of X. These borders are stored in a list and calculated by

```
lowerBound := List\_append(last(List\_tail(LowerBound), s), lowerBoundNow + lower) \ for the lower bound and \\ upperBound := List\_append(last(List\_tail(UpperBound), s), upperBoundNow + upper).
```

The oldest item in these lists (the head of these lists) are removed and the newly calculated bounds for the span next element of X is inserted. lowerBoundNow and upperBoundNow are the describing the limitations of the element of X right before the current event. They are calculated using the list mentioned above and the timestamp of the current event by the following definition:

```
lowerBoundNow := max(List\_head(last(LowerBoundX, s)), time(s) - jitter) \\ upperBoundNow := min(List\_head(last(UpperBoundX, s)), time(s))
```

If the timestamp of the current event is between lowerBoundNow and upperBoundNow, the output of the monitor is true, in any other case, or when the delay ran out, it is false.

The size of these lists has a fixed upper limit (span) and the state transition and output functions are in $\mathcal{O}(1)$, therefore the RepetitionConstraint is finite monitorable with delay.

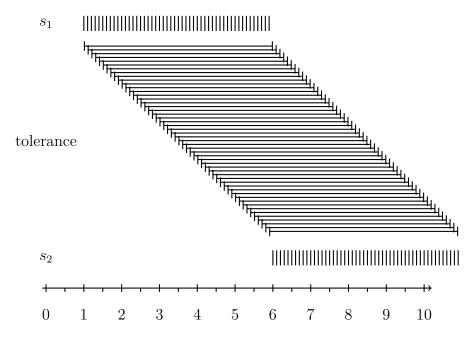


Figure 5.2.: SynchronizationConstraint or StrongSynchronizationConstraint with tolerance = 5

SynchronizationConstraint

The SynchronizationConstraint describe groups of event sets, which events occur in common clusters. Each of these sets must have at least one event in each of these intervals. Any events, that lay outside of these intervals are prohibited.

Figure 5.2, which is similar to the example for the DelayConstraint, shows an example of this constraint, which is an worst case scenario in terms of monitoring. The tolerance interval is 5 timestamps long, the event set s_1 contains the events $\{1, 1.1, ..., 5.9\}$ and s_2 is containing $\{6, 6.1, ..., 11\}$. Each of the events of s_1 must be stored until the end of the tolerance interval, otherwise it would be impossible to check the constraint correctly. Like described in chapter 5, an infinite number of events can be placed in this interval, therefore infinite memory resources are needed. Because the required storage space is not growing continuously, as the stored events can be removed at the end of the tolerance interval, the SynchronizationConstraint is worst case Non-Finite monitorable.

It should be noted, that the illustration of the constraint in figure 5.2 may be misleading, because the *tolerance* intervals are only shown after the events of s_1 , not after the events of s_2 . Every implementation of a monitor for this constraint must also store the events of s_2 for the length of *tolerance*, as they could be important for events following after them.

StrongSynchronizationConstraint

The difference between the *StrongSynchronizationConstraint* and the *SynchronizationConstraint* is, that in the StrongSynchronizationConstraint, only one event per event set is allowed in each synchronization cluster. Therefore, this constraint can be classified as worst case Non-Finite monitorable with the same argumentation as the previous constraint.

ExecutionTimeConstraint

The *ExecutionTimeConstraint* ensures that the time distance between *stop* and *start* events, not counting interruptions (which are specified by *preempt* and *resume* events).

Under the assumption that the input events are in logical order (every execution is started by an *start* event and finished by an *stop* event, every *preempt* event is directly followed by an *resume* event and no *preempt* or *resume* events occur outside of the intervals spanned by *start* and *stop* events), three time values must be stored to monitor this constraint. First, the timestamp of the latest *start* event. Second, the timestamp of the latest *preempt* event and third, the sum of each timestamp of *resume*, minus the respectively latest timestamp of *preempt*. The sum is reseted at every *start* event. These values are updated on events in *start*, *stop* and *preempt*. For the output function, the run time can be calculated by

runtime = time(now) - time(start) - (sum(time(resume) - time(preempt)).

At any event, this value must smaller or equal to *upper* and at *stop* events, additionally the runtime must be greater or equal to *upper*.

To monitor this constraint correctly, a delay is required, when an stop event is late or missing. The required storage space is fixed, also the runtime of the state transition and output function is in $\mathcal{O}(1)$, therefore the ExecutionTimeConstraint is finite monitorable with delay.

OrderConstraint

The OrderConstraint describes, that an i^{th} target event must exist, if an i^{th} source event exists and that the i^{th} target event occurs after the i^{th} source event. Because it is possible that an arbitrary large number of source events occur before the first target occurs, a possibly infinite large number must be stored, which requires infinite memory resources. As this is only a worst case scenario and the size of the stored number can be decreased, when a target event occurs, the OrderConstraint is worst case non-finite monitorable.

ComparisonConstraint

The Comparison Constraint defines an ordering relation between two single timestamps. Therefore, no additional storage is needed and as the relations $(\leq, <, \geq, >, =)$ can be decided in constant time for discrete timestamps, this Constraint is finite monitorable.

SporadicConstraint

The *SporadicConstraint* is defined via the *Repetition*- and *RepeatConstraint* without introducing any new timestamps in the definition of the *SporadicConstraint*. These Constraints are finite monitorable with delay, therefore the *SporadicConstraint* is also finite monitorable with delay.

PeriodicConstraint

The *PeriodicConstraint* is special application of the *SporadicConstraint*, therefore it is also finite monitorable with delay.

PatternConstraint

The PatternConstraint was redefined to

```
\exists X: PeriodicConstraint(X, period, 0, 0) \\ \land \forall i: StrongDelayContraint(X, event, offset_i, offset_i + jitter) \\ \land RepeatConstraint(event, minimum, \infty, 1)
```

in section 2.2.2. The events (event), which are given as attribute, occur after strictly periodic timestamps (X). The distances between the elements of X and the following events is defined by offset.

This constraint can be monitored by storing upper and lower limits of the current latest element of X and the number of event occurrences, reseted by every |offset| event $(count(event) \bmod |offset|)$. The limits of the elements of X can be narrows down by every event occurrence, because the valid distance between the event and the element of X is known by offset and jitter. At every $|offset|^{th}$ event occurrence, the limitations of the current X must be increased by period. The validity of the constraint can be tested by checking, that the current event has the right distance to the limitations of the current element of X. To be able to recognize late or missing events, a delay is required.

Because the memory requirements (two timestamps and a finite integer) are finite

and the mentioned state transition and evaluation functions can be implemented in constant time, the *PatternConstraint* is finite monitorable with delay.

If the redefinition of the *PatternConstraint* is not done, the constraint can be reduced to

 $RepeatConstraint(event, minimum, \infty, 1)$

like stated before in section 2.2.2. In this variant, the constraint is finite monitorable (without delay), because only the minimal distance between two events must be checked.

ArbitraryConstraint

The Arbitrary Constraint is defined as combination of the Repeat Constraint:

 $ArbitraryConstraint(event, minimum_1, ..., minimum_n, maximum_1, ..., maximum_n)$ $\Leftrightarrow \forall i \in 1, ..., n : RepeatConstraint(event, minimum_i, maximum_i, i).$

The *RepeatConstraint* is finite monitorable with delay, therefore the *ArbitraryConstraint* is also finite monitorable with delay.

BurstConstraint

The BurstConstraint is defined as combination of the RepeatConstraint:

```
RepeatConstraint(event, length, \infty, maxOccurrences) \\ \wedge RepeatConstraint(event, minimum, \infty, 1)
```

The RepeatConstraint is finite monitorable with delay, therefore the BurstConstraint is also finite monitorable with delay.

EventChain

EventChains, which are required for the following constraints, are defined as sets of stimulus and response events. The events have an color attribute, which describes the causal connection individual events of stimulus and response. It is required, that any stimulus event with a specific color must occur before the first response event with the same color. The datatype of this attribute is not specified, except that it may be infinite and an equality test exist.

Monitoring this property is difficult, because it is required to store every color which

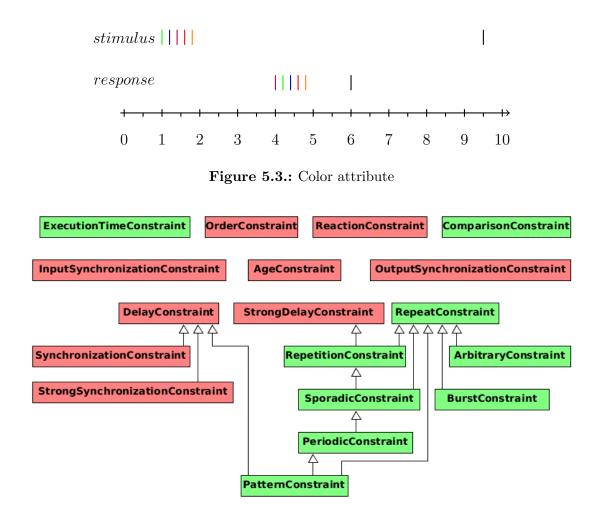


Figure 5.4.: Overview over constraints - Finite Monitorable - Non-Finite Monitorable

has occurred in response. The reason for this can be seen in figure 5.3. In the interval between the timestamps 1 and 2, there are 5 events of different colors in stimulus. Their counterparts in response occur in the interval between 4 and 5. In timestamp 6, there is an event in response with a color, that hasn't been used in stimulus before, therefore this color may not be used in stimulus anymore. To check this for further events in stimulus, it is required to know any color that previously occurred in response.

The memory consumption to monitor this is growing continuously with any event that introduces a new color in *response*, therefore any constraint, that requires the color attribute (*ReactionConstraint*, *AgeConstraint*, *OutputSynchronizationConstraint*, *InputSynchronizationConstraint*) is always non-finite monitorable.

Figure 5.4 gives an overview, which TADL2 timing constraints are finite monitorable

and which are not. All of the 9 finite monitorable constraints require the possibility to create new timestamps (delays), except the ComparisonConstraint, which only compares timestamps. The other half of the constraint is not finite monitorable, but they also split up into two categories, worst case and always non finite monitorable. All constraints that are using the color attribute of the events (Reaction-, Age-, InputSynchronization- and OutputSynchronization) are always non finite monitorable. The other 5 red colored constraints are worst case non finite monitorable. The arrows show, which constraint is defined via other constraints, for example the RepetitionConstraint is defined via the StrongDelay- and RepeatConstraint. It should be noted, that constraints, which are defined via non finite monitorable constraints, can still be finite monitorable, because of further restrictions, which limit the required storage space or runtime.

6. Implementierungen

In this chapter, the implementation of the monitor of each constraint will be explained. Three major aspects will be considered for every constraint

- 1. A short **documentation** of the implementation
- 2. An analysis of the **computational complexity** in terms of time consumption per event and overall memory
- 3. A **performance analysis** of the implementation analyzing large, randomly generated traces

All implementations have in common that they consist of 2 or 3 sections, similar to the state transition, delay (if needed) and output as defined in chapter 4. These sections are the basis for the analysis of the **computational complexity**, because the generated state defines the required memory capacity and the function connecting these sections define the required time per event.

The performance analysis is done by monitoring large traces, which were randomly generated. The implementations are run on the TeSSLa interpreter. To increase reproducibility and minimize disruptive influences on the timing behavior, the interpreter is run on a *Raspberry Pi 2 Model B*, using Raspberry Pi OS lite and openJDK version 11.0.8.

DelayConstraint

The implementation of the monitor of the *DelayConstraint* stores a linked list of source events, which did not have a matching target event yet. This list is expanded by every source event, which is appended at the end of the list. If a target event occurs, all matching source events (possibly none) are removed from the list. Like stated in section 5, this list can grow infinitely in worst cases, when the time domain defined in an uncountable way. In these worst cases, an infinite number of source events may, before any event can be removed from the list, because a matching target event occurs.

TeSSLa is using integer values as time domain, therefore it is countable and the list cannot grow infinitely. The largest possible size of this list is equal to the parameter upper, therefore, and because this list is the only growable memory usage, the algorithm is in $\mathcal{O}(upper)$ in terms of memory.

The state transition as described above is in $\mathcal{O}(upper)$ in terms of time. Appending an *source* event to the list is done in constant time. Removing all events that matched with a *target* event may require to check every event in this list in worst cases, because possibly, all of them must be removed.

The output function checks, if the updated list of unmatched *source* events is either empty, or the event in the head of the updated list is not older than *upper*. Therefore, it is in $\mathcal{O}(1)$.

The required delay period is calculated by adding *upper* to the timestamp of the head of the list of unmatched *source* event, subtracted by the timestamp of the current event $(\mathcal{O}(1))$.

StrongDelayConstraint

The StrongDelayConstraint is implemented very similarly to the DelayConstraint. The only difference is, that only the head of the list of unmatched source events is removed, when a matching target event occurs. Therefore, the state transition is in $\mathcal{O}(1)$ in terms of time per event, while the memory consumption is still in $\mathcal{O}(upper)$. Additionally, the output function checks, if target event occurrences have exactly one matching source event (which always is in the head of the list). Therefore, it is still in $\mathcal{O}(1)$. The calculation of the delay period remains unchanged.

RepeatConstraint

The implementation of the RepeatConstraint stores the timestamps of the span previous events as state, using TeSSLa's last operator recursively (a macro called nLastTime was programmed for this). Therefore, span timestamps are stored and the last operator is called span times, which means the state transition function is in $\mathcal{O}(span)$ in terms of time and the implementation is in $\mathcal{O}(span)$ in terms of memory. The time of the $span^{th}$ oldest event is stored directly as integer, therefore it can be accessed in constant time.

The required delay is calculated by adding upper to the $span^{th}$ oldest event or the first event, if there hasn't been span events before minus the current timestamp, therefore it is in $\mathcal{O}(1)$ in terms of time, because the relevant timestamps can be directly accessed, like stated before.

The output function checks, if the $span^{th}$ oldest event is not older than upper and not younger than lower. If there hasn't been span events before, it is checked, if the first event is not older than upper. Because the timestamps of the $span^{th}$ oldest and the first event and lower and upper can be directly accessed, the output function is in $\mathcal{O}(1)$ in terms of time.

RepetitionConstraint

The RepetitionConstraint is defined as

```
RepetitionConstraint(s, lower, upper, span, jitter)

\equiv \exists X \subset \mathbb{T} : RepeatConstraint(X, lower, upper, span)

\land StrongDelayConstraint(X, s, 0, jitter)
```

The implementations of the Repeat- and the StrongDelayConstraint cannot be used for this implementation, because the timestamps of X are unknown and need to be narrowed down.

Relevant for the monitoring are the boundaries of the elements of X, which precede the actual events in s. Two lists containing span timestamps is stored in the implementation, one for the latest and one for the earliest occurrences of the next span X timestamps. At every input event, the new boundaries for the $span^{th}$ next X are calculated, the lower bound by $max(List_head(last(LowerBoundX, e)), time(e) - jitter)$ and the upper bound by $min(List_head(last(UpperBoundX, e)), time(e))$. These new boundaries are appended to the end of the lists, while the oldest entries in the head of the lists are removed. These two lists with the size of span are the only storage, which size is dependent on the input, therefore the algorithm is in $\mathcal{O}(span)$ in terms of memory. The run time of the state transition function is in $\mathcal{O}(1)$, because the described operations are done in constant time.

The output function checks, if the current time is between the lower bound for the current timestamp of X and jitter behind the upper bound for that value. In any other case, the output is false. Because the upper and lower bound for the current X value can be directly accessed, the output function is in $\mathcal{O}(1)$.

The required delay period is calculated by adding *jitter* to the timestamp of the head of the list of the upper limits for the next X timestamps, subtracted by the timestamp of the current event $(\mathcal{O}(1))$.

SynchronizationConstraint

The Synchronization Constraint is defined via an application of the Delay Constraint, but the application uses a set of unknown timestamps $(\exists X : ...)$, therefore the Delay Constraint cannot be used for the implementation of this Constraint.

In the implementation of the *SynchronizationConstraint*, a set of information for every event, that occurred not longer than *tolerance* ago, is stored in a linked list. This information contains the stream, in which the event occurred, the timestamp of the event occurrence and a boolean variable, that expresses if a fulfilled synchronization cluster for this event has already been found.

This list is updated by every event occurrence in three steps. First, each event occurrences in this timestamp is appended to this list. Second, the list is separated into two parts, one with events older and one with events younger than tolerance. The list of old events is still stored in this timestamp, but removed after it. The younger events form the state that is stored for the next event occurrence. Third, it is checked, if at least one event of every stream is part of the list of the younger events. In this case, a fulfilled synchronization cluster has been found and the boolean variable, that states if a synchronization cluster is found for this event, is set to true for all events in this list.

Similar to the DelayConstraint, this list can grow infinitely, when the time domain is uncountable, which is not the case in TeSSLa. Because the TeSSLa uses integers as time domain, at most $|event|^1*tolerance$ events can occur in the tolerance interval. Therefore, the algorithm is in $\mathcal{O}(|event|*tolerance)$ in terms of memory. The first step of the state transition is in $\mathcal{O}(|event|)$, because at most |event| events have to be appended to the list. In worst cases, every event in the list (which is in ascending order) is older than tolerance, therefore the separation in the second step of the state transition is in $\mathcal{O}(|event|*tolerance)$ in terms of time. In the third step, the complete stored list of young events must be examined, to check if the cluster is fulfilled and, if needed, every event in the list must be set to fulfilled. Therefore the third step is in $\mathcal{O}(|event|*tolerance)$ in terms of time.

The output function checks, if the boolean variable of each event in the list of events, which are older than tolerance, is set to true. If not, the constraint is not fulfilled. Because this list can have the size |event|*tolerance, the output function also is in $\mathcal{O}(|event|*tolerance)$ in terms of time.

The required delay is calculated by adding *tolerance* to the timestamp of the oldest stored unsatisfied event, subtracted by the timestamp of the current timestamp $(\mathcal{O}(|event|*tolerance))$.

StrongSynchronizationConstraint

The StrongSynchronizationConstraint is defined as application of the StrongDelay-Constraint, but this application cannot be used in the implementation, like in the previous constraint.

The difference between the *Synchronization*- and the *StrongSynchronizationConstraint* is, that each event can only be part of one synchronization cluster in the *StrongSynchronizationConstraint*. Therefore, the implementation is different to the implementation of the previous constraint, because not every event stored separately, only information about synchronization clusters, containing their start time and in which stream an event occurred in this cluster, are stored.

¹|event| is the number of streams, not the number of events.

At event occurrences, the event is either added to one synchronization cluster, or a new cluster with the start time of the event is added to the list. In a second step, every fulfilled cluster is removed from the list.

This list is at most tolerance long (events in all timestamps in one stream, no events in other streams). The size of individual entries of the list is dependent on the number of streams, because they store a boolean variable for every stream. Because of the length restriction of the list, the stated state transition is on $\mathcal{O}(|event|*tolerance)$ in terms of time and the $\mathcal{O}(|event|*tolerance)$ in terms of memory.

The output function checks, if the oldest stored (therefore unfulfilled) cluster is older that tolerance. This cluster is in the head of the list, therefore the output function $\mathcal{O}(1)$ in terms of time. The required delay is calculated by adding tolerance to the timestamp of the oldest stored unsatisfied cluster, subtracted by the timestamp of the current timestamp ($\mathcal{O}(1)$).

ExecutionTimeConstraint

The implementation of the *ExecutionTimeConstraint* is using TeSSLa's *runtime* operator on the *start* and *stop* events, which calculates the absolute runtime without any interruptions. The time of interruptions is also calculated by the calculated by this operator and then summed up. The sum of these interruptions is reseted by every *start* event.

TeSSLa's runtime operator subtracts the timestamps of the events of the second parameter (in this case stop and resume) from the timestamps of the events of the first parameter(start and preempt), therefore it stores the timestamps of the start and preempt events are stored, additionally to the sum the preemptions. For the output, the runtime can be calculated by subtracting the first application of TeSSLa's runtime operator from the sum of the second applications of this operator. If the runtime should be checked in timestamps without a stop event, the second parameter of the first application of the runtime operator must be replaced by a current event. In the implementation this is done by merging all include streams and the delay stream. This runtime must be smaller or equal to upper in any timestamp with events and greater or equal to lower at stop events. The required delay is calculated subtracting the runtime so far from upper. These operations are simple arithmetic functions, therefore the algorithm is in $\mathcal{O}(1)$ in terms of time. The required storage space is fixed, therefore it is also in $\mathcal{O}(1)$ in terms of memory.

OrderConstraint

The OrderConstraint is defined, so that the number of events on the source stream is equal to the number of events on the target stream and that the i^{th} source

event occurs before the i^{th} target event. The first described property can only be checked, when it is known that no further events will occur. In TeSSLa, it is generally unknown, if further events will occur, therefore the implementation has a third input stream, which requires to have exactly one event at the end of the observation.

The implementation counts the number of events on the source and target stream and checks, if the number of source events is larger or equal to the number of target events. In the end of the streams, the number of events on both streams must be equal. Therefore, the stored state consists of two integers and the algorithm is in $\mathcal{O}(1)$ in terms of memory. The incrementations of these counters and the comparison between them are simple arithmetic operations, therefore the state transition and the output function are both in $\mathcal{O}(1)$ in terms. The introduction of new timestamps is not required for this constraint, except the one defining the end of the observation.

ComparisonConstraint

The ComparisonConstraint defines comparisons between timestamps. These functionalities are already defined in TeSSLa, therefore no implementation is given as part of this thesis.

SporadicConstraint

The Sporadic Constraint is defined as simple application of the Repetition- and the Repeat Constraint, therefore the Sporadic Constraint is also implemented as application of them. The implementations of the Repetition- and the Repeat Constraint are both in $\mathcal{O}(1)$ per event in terms of time, therefore the implementation of the Sporadic Constraint is also in $\mathcal{O}(1)$ in terms of time. The implementations of the Repetition- and the Repeat Constraint are both in $\mathcal{O}(span)$ in terms of memory. The span parameters of both constraints are unused in the Sporadic Constraint and therefore set to 1. Because of this, the implementation of the Sporadic Constraint is $\mathcal{O}(1)$ in terms of memory.

PeriodicConstraint

The PeriodicConstraint is defined as application of the SporadicConstraint and is also implemented like this. Because the SporadicConstraint is in $\mathcal{O}(1)$ in terms of memory and time, the PeriodicConstraint is also.

PatternConstraint

The PatternConstraint is defined as application of the Periodic-, Delay- and Re-peatConstraint. Because of the set of unknown timestamps (X), the Periodic- and DelayConstraint cannot be used for the implementation.

In the implementation of the PatternConstraint, the lower and upper bound for the current timestamp of X is stored. At every event, these bounds are further enclosed, taking the previous known bounds and the bounds implied by the current event:

$$x \in X : time(event) - offset_{count(event) \mod |offset|} - jitter \le x$$

 $\le time(event) - offset_{count(event) \mod |offset|}$

into account. The new lower bound is set by using the maximum of the previous lower bound and the lower bound implied by the current event, the new upper bound by using the minimum previous upper bound and the upper bound implied by the current event. At every $|offset|^{th}$ event, period is added to the current bounds. The output function checks, if the timestamp of the current event is in the interval $offset_{count(event) \mod |offset|}$ after the bounds. The required delay is defined by the time distance between the current timestamp and the upper bound for X, plus the allowed offset of the following event, plus the allows deviation (jitter).

The only state stored in the implementation are the upper and lower bound for the current x-value, therefore the implementation itself is in $\mathcal{O}(1)$ in terms of memory, but the size of the of fset-parameter, which is a hash map, is not limited and the complete algorithm, including the parameters, is $\mathcal{O}(|offset|)$ in terms of memory.

ArbitraryConstraint

The Arbitrary Constraint is defined as multiple applications of the Repeat Constraint and is also implemented this way. The number of applications of the Repeat Constraint is dependent on the number of elements in the minimum and maximum parameters. The runtime of the Repeat Constraint is in $\mathcal{O}(1)$ per application and event, therefore it the Arbitrary Constraint is in $\mathcal{O}(|minimum|) = \mathcal{O}(|maximum|)$ in terms of time. The memory usage of the Repeat Constraint is in $\mathcal{O}(span)$. In the application of the Repeat Constraint, the span parameter increases for each of the |minimum| = |maximum| applications. Therefore, implementation is in $\mathcal{O}(\sum_{i=1}^{|minimum|} i) = \mathcal{O}(\frac{|minimum|^2 + |minimum|}{2})$.

BurstConstraint

The BurstConstraint is defined as twofold application of the RepeatConstraint and is also implemented this way. The RepeatConstraint is in $\mathcal{O}(1)$ in terms of time and

because the BurstConstraint aplies it in a fixed number (2), the BurstConstraint is also in $\mathcal{O}(1)$ in terms of time. The memory usage of the RepeatConstraint is in $\mathcal{O}(span)$. This parameter is maxOccurrences in the first and 1 in the second application, therefore the BurstConstraint is in $\mathcal{O}(maxOccurrences)$ in terms of memory.

ReactionConstraint

The implementation of the ReactionCostraint stores two informations as state. First, a map containing the color and the timestamp of each stimulus event, which did not have a matching response event yet and second, a set that contains all colors, that previously occurred in response. The state is updated at every input event. Stimulus events are inserted into the map, response events are inserted into the set. Additionally, Stimulus events are removed from the map, if a matching response is occurring. Similar to the DelayConstraint (the ReactionCostraint is an extension of the DelayConstraint, that additionally considers the color of events), the maximal number of entries in the map is the maximal number of stimulus events, that could possibly occur in an interval of the length maximum, which is maximum. The maximal possible size of the set that containing all previous response colors is the number of event, which previously occurred in response. Therefore, the algorithm is in O(maximum + count(response)) in terms of memory. The state transition (insertion in map and in set, lookup and possibly remove in map) is in O(1) in terms of time.

The required delay is calculated by adding maximum to the timestamp of the oldest entry in the map mentioned above, and subtracting the current timestamp. Because the map is an unsorted hash map, every entry in the map has to be checked. Therefore, the calculation of the required delay is in $\mathcal{O}(maximum)$.

The output function checks, if the oldest entry in the map is not older than maximum and, at timestamps containing stimulus events, if the set of previous response colors contains the color of the current stimulus event. The lookup in the set is done in constant time, the search for the oldest entry in the map requires to check every entry, therefore the output function is in $\mathcal{O}(|maximum|)$.

AgeConstraint

The implementation of the AgeConstraint is similar to the implementation of the ReactionCostraint. The only difference between the stored states is, that in the implementation of the AgeConstraint, stimulus events are removed from the map, when they are older than maximum, not when a matching response event is found. Therefore, the algorithm also is in $\mathcal{O}(maximum + count(response))$ in terms of

memory and the state transition function is in $\mathcal{O}(1)$.

The creation of new timestamps is not needed in this constraint, because only previous events need to be considered, upcoming events not.

The output function checks in timestamps, which contain a *stimulus* event it is checked, if the color is in the set of colors, that previously occurred in *response*. In timestamps, which contain a *response* event, it is checked, if a *stimulus* event with the same color is in the map and if the time distance between them is larger than *minimum* and smaller than *maximum*. These operation are in $\mathcal{O}(1)$.

OutputSynchronizationConstraint

InputSynchronizationConstraint

7. Zusammenfassung und Ausblick

Die Zusammenfassung greift die in der Einleitung angerissenen Bereiche wieder auf und erläutert, zu welchen Ergebnissen diese Arbeit kommt. Dabei wird insbesondere auf die neuen Erkenntnisse und den Nutzen der Arbeit eingegangen.

Im anschließenden Ausblick werden mögliche nächste Schritte aufgezählt, um die Forschung an diesem Thema weiter voranzubringen. Hier darf man sich nicht scheuen, klar zu benennen, was im Rahmen dieser Arbeit nicht bearbeitet werden konnte und wo noch weitere Arbeit notwendig ist.

A. Anhang

Dieser Anhang enthält tiefergehende Informationen, die nicht zur eigentlichen Arbeit gehören.

A.1. Abschnitt des Anhangs

In den meisten Fällen wird kein Anhang benötigt, da sich selten Informationen ansammeln, die nicht zum eigentlichen Inhalt der Arbeit gehören. Vollständige Quelltextlisting haben in ausgedruckter Form keinen Wort und gehören daher weder in die Arbeit noch in den Anhang. Darüber hinaus gehören Abbildungen bzw. Diagramme, auf die im Text der Arbeit verwiesen wird, auf keinen Fall in den Anhang.

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TDO zu erledigen $To\ Do$

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