

Monitoring of the AUTOSAR Timing Extensions with TeSSLa

Überwachung der AUTOSAR Timing Extensions mittels TeSSLa

Bachelor Thesis

im Rahmen des Studiengangs Informatik der Universität zu Lübeck

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tatement in Lieu of an Oath
hereby confirm that I have written this thesis on my own and that I have not used by other media or materials than the ones referred to in this thesis.
Hendrik Streichhahn) libeck, den 1.1. 1970

Abstract Satisfying given timing requirements is essential for the correct behavior of embedded real-time systems. In the automotive domain, the AUTOSAR timing extensions are a recent and widely accepted standard for specifying timing requirements. Previous work, such as the TIMMO-2-USE project, has focused on formalizing the AUTOSAR timing model and timing extensions in a mathematically rigorous way, in order to make them amenable for off-line system analysis tools such as automated model-checking and verification.

Because of computational problems, model-checking and offline verification is limited to relatively small-scale systems. Furthermore, not all types of specification violations can be detected at system development time, and sporadic, rare events typically require a capability for long-term observations. Run-time verification is a more lightweight method that lies at the boundary between formal verification and testing. Run-time verification checks properties, expressed in temporal logic, on-the-fly during the operation of the system using finite-state monitors generated from the logical specifications. In this thesis, an analysis of the 18 TADL2 timing constraints defined in the TIMMO-2-USE project is made to decide, whether they can be expressed as finite-state monitors, thus making them monitorable by run-time verification. Further, a monitor for each of the TADL2 timing constraint is implemented in the temporal stream-based specification language TeSSLa.

Kurzfassung Die Einhaltung von Zeitschranken ist essentiell wichtig für das korrekte Verhalten von eingebetteten Echtzeitsystemen. In der Automobilindustrie werden in breiter Masse die AUTOSAR Timing Extensions (etwa AUTOSAR Zeiterweiterungen) verwendet, mit denen das das Zeitverhalten von Hard- und Softwarekomponenten beschrieben werden kann. Andere Arbeiten, etwa das TIMMO-2-USE Projekt, haben daran gearbeitet, die AUTOSAR Timing Extensions zu formalisieren und somit einen Grundbaustein dafür zu legen, die Definitionen vom Zeitverhalten automatisiert zu kontrollieren, etwa durch Model Checking. Ein Problem von Model Checking und ähnlichen Ansätzen ist, dass diese aufgrund der extrem großen Laufzeit auf kleinere Systeme beschränkt sind. Runtime Verification ist eine leichtgewichtigere Methode der Analyse von Systemkomponenten, die einen Mittelweg zwischen formaler Analyse und Testen geht, wobei formal definierte Eigenschaften des Systems während der Laufzeit geprüft werden.

Im Rahmen dieser Arbeit werden die 18 TADL2 Timing Constraints, welche im Rahmen des TIMMO-2-USE Projekt erarbeitet wurden, dahingehend überprüft, ob sie in mittels Runtime Verification überwacht werden können. Darauf aufbauend wird für jeden dieser Constraints ein Monitor in der Sprache TeSSLa, welche für die Überwachung von Zeiteigenschaften auf Strömen entwickelt wurde, implementiert.

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1 Introduction

Timing behavior is one of the most important properties of computer systems. Especially in safety-critical applications, a wrong timed reaction of the system can have disastrous consequences, for example in the Electronic Stability Control of a vehicle. The *AUTOSAR* (**AUT**omotive **O**pen **S**ystem **AR**chitecture) standards are used by almost all car manufacturers [AUT]. With AUTOSAR, development processes and components are standardized, which increases productivity, interoperability and exchangeability.

To describe the timing behavior of soft- and hardware components of cars, the AU- $TOSAR\ Timing\ Extensions$ were developed. The goal of this thesis is to implement
a monitoring tool for the timing constraints defined in this standard.

Some of the constraints defined in the AUTOSAR standard are written in an informal way and can be misunderstood, which will be described as part of this thesis. This is problematic for monitoring, because the implementation of a monitor must not be based on unambiguous definitions. To solve this problem, the timing constraints defined in the Timing Augmented Description Language Version 2 (TADL2) are used as basis for the monitoring tool. TADL2 was created as part of the TIMMO project, which had similar goals to AUTOSAR, but the definitions are written in a more formal way. The AUTOSAR Timing Extensions are comparable and partly compatible to the TADL2 timing constraints. Most of the constraints defined in the AUTOSAR standard can be described as equivalent combination of TADL2 timing constraints and vice versa.

The monitoring tool is written in *TeSSLa* (Temporal Stream-based Specification Language), which is made for stream runtime verification and is capable of non-intrusive observation and can be run as Java program or on specialized embedded hardware, like FPGAs.

In the first part of this thesis, an overview over the AUTOSAR Timing Extensions and an example about the informal and ambiguous definitions will be given. Next, the TADL2 timing constraints will be listed and the relations between the these constraints and the AUTOSAR Timing Extensions will be described. In the next chapter, TeSSLa, its fundamental functionality and other prerequisites, which are needed for understanding the theoretical part of this thesis, will be explained. The term of *simple monitorability* is introduced, which insures, that a property on infinite streams can always be monitored with finite time and memory resources. Then, each of the TADL2 timing constraint is checked, if it *simple monitorable* or not. After

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that, the TeSSLa implementations of these constraints are described and evaluated in a theoretical and practical way.

In the end an overview of the accomplished is given and ideas for further work will be discussed.

2 Timing Constraints

2.1 AUTOSAR Timing Extensions

AUTOSAR is a development partnership in the automotive industry. As stated before, the main goal is to define a standardized interface and to increase the inter-operability, exchangebility and re-usability of parts and therefore simplifying development and production.

The AUTOSAR Timing Extension are describing timing constraints for actions and reactions of components. The constraints are defined via *events*, which consists of a time value and, if needed, a data value of an arbitrary type. To describe the logical relationship between groups of events, *event chains* are defined, which consists of *stimulus* and *response* events, in which the *response* event is understood as the answer to the *stimulus* event.

The AUTOSAR Release 4.4.0 ([AUT18]) is used for this thesis, there are 12 timing constraints defined in this version of the AUTOSAR Timing Extensions

- 1. The subset of 5 **EventTriggeringConstraints** are describing, at which points in time specific events may occur.
 - 1 The **PeriodicEventTriggering** defines repetitions of event with the same time distance and offers the possibility to set an allowed deviation from this pattern. Additionally the minimal distance between two subsequent events can be defined.
 - 2 The **SporadicEventTriggering** specifies sporadic event occurrences by defining the minimal and maximal distance between subsequent events. Optionally, periodic repetitions and allowed deviations from the period can be described.
 - 3 With the **ConcreteEventTriggering**, offsets between a set of subsequent events in a time interval can be described. These intervals may not overlap, and periodic repetitions of them can be defined optionally.
 - 4 The **BurstPatternEventTriggering** describes non overlapping event clusters with a minimal and maximal number of events. Optionally periodic repetitions of these clusters can also be described.

- 5 The **ArbitraryEventTriggering** defines the distance between subsequent event by defining *ConfidenceIntervals*, which describe the probability, in which time interval the following event will occur.
- 2. The **LatencyTimingConstraint** specifies the minimal, nominal and maximal time distance between the stimulus and response events of an event chain.
- 3. The **AgeConstraint** is a simpler form of the *LatencyTimingConstraint* by defining minimal and maximal age a event may have at the point of time, when it is processed.
- 4. The **SynchronizationTimingConstraint** is used for describing events of different kind, that occur synchronized in a time interval of a specific length.
- 5. The **SynchronizationPointConstraint** defines two sets of executables and events. Every element of the first set must have finished or occurred, before the first element of the second set may start or occur.
- 6. The **OffsetTimingConstraint** specifies the minimal and maximal time distance between corresponding *source* and *target* events.
- 7. The **ExecutionOrderConstraint** defines the order, in which a list of executables must start and finish.
- 8. The **ExecutionTimeConstraint** defines the minimal and maximal runtime of an executable, including or excluding the runtime of external functions and interruptions.

In this simplified form, some constraints are redundant. The semantic differences will be shown in section 2.2.3.

Problematic with the AUTOSAR Timing Extensions is, that the constraints are not formally defined and have room left for interpretation. As example, the *Burst-PatternEventTriggering* will be analyzed in the following. This constraint describes events clusters, with events that occur with short time distances, with larger time distances between the clusters. These following attributes define, how the events may occur:

- maxNumberOfOccurrences (positive integer)
 Maximal number of events per burst
- minNumberOfOccurrences (positive integer)
 Minimal number of events per burst (optional)
- minimumInterArrivalTime (time value)
 Minimal distance between subsequent events

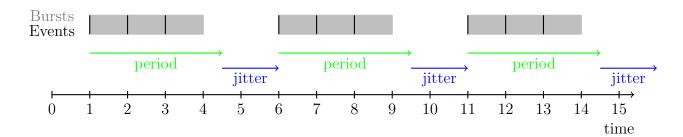


Figure 2.1: BurstPatternEventTriggering Period-Jitter accumulating

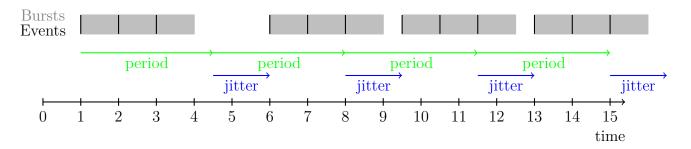


Figure 2.2: BurstPatternEventTriggering Period-Jitter non-accumulating

- patternLength (time value) Length of each burst
- patternPeriod (time value)

 Time distance between the starting points of subsequent burst(optional)
- patternJitter (time value)
 Maximal allowed deviation from the periodic pattern (optional)

As example, we set:

- maxNumberOfOccurrences = 3
- minNumberOfOccurrences = 1
- $\bullet minimumInterArrivalTime = 1$
- patternLength = 3
- patternPeriod = 3.5
- patternJitter = 1.5

The combination of patternPeriod and patternJitter can be interpreted in an accumulating way, as seen in 2.1, or in a non-accumulating way, as seen in 2.2. In the accumulating interpretation, the reference for the periodic occurrences is only the

start point of the previous burst. In the non-accumulating way, there is an global reference point for the periodic repetitions.

With the definition of patternPeriod ("time distance between the beginnings of subsequent repetitions of the given burst pattern" [AUT18]) you would think, that the accumulating variant is meant. Against that, the period attribute in PeriodicEvent-Triggering-Constraint is defined as "distance between subsequent occurrences of the event" [AUT18] in the text, hence it is also understandable the accumulating way, but there is the formal definition

```
\exists t_{reference} \forall t_n : t_{reference} + (n+1) * period \leq t_n \leq t_{reference} + (n-1) * period + jitter,
```

where t_n is the time of the *n*-th Event and $t_{reference}$ is a reference point, from which the periodic pattern starts, so the PeriodicEventTriggering-Constraint is meant to be understood in the non-accumulating way. It remains unclear, in which way the BurstPatternEventTriggering is meant to be understood.

Another problem of the AUTOSAR Timing Extensions is, that they were made for design purposes, monitoring them can be difficult, as a monitor may need time and memory resources, which continuously grow with every input event. This makes online monitoring unsuitable in nearly all scenarios (more on monitorability in 3). As example, we will use the *BurstPatternEventTriggering* again. This time we use the attributes

- $maxNumberOfOccurrences = INT_MAX$ or any significant large number
- minNumberOfOccurrences = 1
- minimumInterArrivalTime = 0
- patternLength = 3
- patternPeriod unused
- patternJitter unused

Figure 2.3 shows the application of the BurstPatternEventTriggering constraint with the given parameters on a stream with events at the timestamps 3, 3.5, 4, 4.5. The development of possible the burst cluster with ongoing time is visualized. The gray bars show the range, in which the burst cluster can lay, the black lines show, where they definitely are. In timestamp 3 with only one event so far, only one burst has to be considered and it can lay between timestamp 0 and 6, the only limitation is, that it must include timestamp 3 with the event in that point. In Timestamp 3.5, there are two events (at 3 and 3.5) so far and there are two possibilities for burst placements. The first possibility with only one burst with both events in it, and the second possibility, where the events are in different bursts. The third graphic shows

the trace in timestamp 4 with three different events so far (3, 3.5, 4) and three different possibilities for burst placements to consider. One possible burst contains all three events, the second possibility has one burst with the event at timestamp 3 and one burst with the events at 3.5 and 4 and the third possibility has one Burst with the events at 3 and 3.5 and one burst with the event at 4. The possible bursts in graphic 4 are analog to the third graphic, one possibility with one burst containing all 4 events and 3 possibilities with the first burst containing the first event, the first and second event or the first, the second and the third event and the second burst containing the remaining events. Because the distance between event is not specified, we can place an arbitrary large number of events in any interval with the length patternLenth.

In this example we see, that it is possible to create an unlimited number of possibilities for burst placements within one burst length, when the *minimumInter-ArrivalTime*-attribute is 0, which results in an infeasible resource consumption, as unlimited memory and time is needed to check the constraint in following events. Therefore, online monitoring this constraint is unsuitable in most cases.



Figure 2.3: BurstPatternEventTriggering Possible bursts, ↑ shows the current time

2.2 Timing Augmented Description Language

As timing extension to EAST-ADL(Electronics Architecture and Software Technology-Architecture Description Language), the TIMMO (Timing Model) project, and its successor TIMMO2USE, were initiated. A part of this project was the Timing Augmented Description Language V2 (TADL2), were created. TADL2 has similar goals as the AUTOSAR timing extensions, but the definitions are written in a more formalized fashion. The definitions of the AUTOSAR Timing Extensions are only textually described often, the TADL2-Definitions are defined in a more formal way, as they offer a formal definition of each constraint in a timing constraint logic [BFL+12]. EAST-ADL is much less used in the automotive industry, but the EAST-ADL Timing Constraints are partly compatible to the AUTOSAR Timing Extensions, as they are sub- or supersets of each other. Many of the AUTOSAR Timing Extensions can be defined via a combination of TADL2 Constraints, as explained in section 2.2.3.

The timing constraints are defined on events or event chains, similar to the AU-TOSAR Timing Extensions. In TADL2, all events of an event chain have a color attribute, which shows the logical connection of these events. This attribute is defined as abstract and possibly infinite datatype. The only restriction is, that an equality test on these color values must be defined. TADL2 offers 18 timing constraints, which will briefly explained in the following.

- The **StrongDelayConstraint** defines the minimal and maximal time distance of the events from two event sets (*source* and *target*).
- The **DelayConstraint** is a less strict variant of the **StrongDelayConstraint**, because it allows additional events in *target*.
- The RepeatConstraint, RepetitionConstraint, PeriodicConstraint, SporadicConstraint and ArbitraryConstraint are describing the time distance between subsequent events, whereby they are having small semantic differences. An exact distinction between these constraints will be given in section 2.2.2.
- The SynchronizationConstraint and StrongSynchronizationConstraint define groups of event sets, whose events occur in common time intervals. The SynchronizationConstraint allows more than one event of each group per interval, the StrongSynchronizationConstraint does not.
- The **ExecutionTimeConstraint** is used to set a minimum and a maximum for the runtime of a task, not counting interruptions in the execution.
- The **OrderConstraint** defines that the n^{th} event of one event set must occur before or at the n^{th} event of a second event set.

- The **ComparisonConstraint** is used to describe ordering relations of timestamps.
- The **PatternConstraint** defines the time distance between periodic points in time and several events.
- The **BurstConstraint** regulates the maximum number of events in time intervals of a specific length.
- The **ReactionConstraint** describes the minimal and maximal time a response event must occur after the associated stimulus event. Additional response events are allowed, additional stimulus events not.
- The **AgeConstraint** is similar to the ReactionConstraint, but it is defined the other way around. Therefore, it describes the minimal and maximal time a stimulus event must occur before the associated response event. Additional stimulus events are allowed, additional response events not.
- The OutputSynchronizationConstraint is used to describe groups of event chains, which all have the same response events. The response events of the event chain must occur in common time intervals, like in the SynchronizationConstraint. In the InputSynchronizationConstraint, the roles of the stimulus and response events are swapped.

2.2.1 Parenthesis - Simple and Flexible Timing Constraint Logic

The formal definition of the TADL2 timing constraint are written in *Timing Constraint Logic* (short: *TiCL*), which was developed as part of the TIMMO-2-USE project. TiCL was formally introduced in [LN12], for better understanding the key aspects of this paper will be explained in the following.

The main goal of TiCL is to be formal and expandable and offering the possibility of defining finite and infinite behaviors of events. In TiCL, only points in time, when events occur, are considered, therefore an events only consists of a real number as timestamp, without the possibility of adding a data value. There are 7 syntactic categories in TiCL

```
\mathbb{R}(arithmetic constants)

Avar(arithmetic variables)

AExp(arithmetic expressions)

Svar(set variables)

SExp(set expressions)
```



Figure 2.4: Graphical example of $\lambda(E)$, $\lambda(F)$ and $\lambda(E \setminus F)$

TVar(time variables)CExp(constraint expressions)

Arithmetic expressions can be defined as arithmetic constants, as arithmetic variables, as application of +,-,*,/ on arithmetic expressions, as application of the cardinality operator on a set $(|E|, E \in SExp)$ or as measure $\lambda(E)$ $(E \in SExp)$. $\lambda(E)$ is defined as Lebesgue measure, which is figuratively speaking, the length of all continuous intervals of E. In figure 2.4 an example of the measure operator λ is visualized. The set E contains all Events between the timestamps 1 and 9, the set E contains the events at the timestamps between 2 and 4 and 6 and 7, therefore $E \setminus F$ contains the events at the timestamps $\{1,1.5,4.5,5,5.5,7.5,8,8.5,9\}$. E consists of one continuous interval from timestamp 1 to 9 with the length of 8, E consists of two continuous intervals from 2 to 4 with the length of 2 and from 6 to 7 with the length of 1, therefore $\lambda(E) = 3$. $E \setminus F$ consists of three continuous intervals, the first from 1 to 1.5 (length = 0.5), the second from 4.5 to 5.5 (length = 1) and the last from 7.5 to 9 (length = 1.5). Consequently the total length of the continuous intervals of $E \setminus F$ is 3.

Set expressions can be defined as set variables, or as set of time variables that fulfill a given constraint expression.

Constraint expressions can be defined as application of the \leq operator on time or arithmetic expressions, the \in operator on time variables and set expressions, the logical conjunction (\wedge) on constraint expressions, the negation of constraint expressions and the \forall -Quantifier on arithmetic, set and time variables over an constraint expression.

As extension to this definition, well known syntactic abbreviations like $true \equiv 0 \leq 1$ or the \exists -quantifier will be used, but there are also some TiCL-specific syntactic

abbreviations, like interval constructors, which will be defined and explained in the following.

Let $x, y \in Tvar$ and $E, F \in SExp$.

The interval constructor $[x <]([x \le])$ is defined as $\{y : x < y\}(\{y : x \le y\})$, therefore the interval contains all points in time laying behind of x (including x).

 $[\leq x]([< x])$ is defined as complement of $[x <]([x \leq])$ and contains all timestamps laying before x.

[x..y] is defined as $[x \le] \cap [< y]$, so all points of time after x and before y, including x but not y, are part of this interval.

 $[E \leq]$ is defined as $\{y: \exists x \in E: x \leq y\}$, this interval contains all point of time at and after the first timestamp in E.

[E <] is equal to $\{y : \forall x \in E : x < y\}$, therefore it defines the interval containing all timestamps after the latest point of time in E. Please note the use of \forall instead \exists in the definition.

 $[\leq E]$ ([< E]) is defined as $[E <]^C$ ($[E \leq]^C$), analogous to the operators on time variables.

[E] is equal to $[E \leq] \cap [\leq E]$. It defines the time interval between the first and last element of E, including these points in time.

 $E_{x<}(E_{<x})$ is defined as $E \cap [x <](E \cap [< x])$. This operators filters the timestamps in E so that only the points in time before (after) x remain.

[x..E] equals $[x \leq] \cap [< (E_{x<})]$. The interval begins at x and ends right before the first element of E after x.

[E..F] is defined as $\{x : \exists y \in E : x \in [y..F]\}$ and describes the intervals, where the previous operator is applied on every element of E.

E(i) is $i^t h$ timestamp in E, starting by zero.

 $X \leq Y$ describes, that X is a sub sequence of Y.

2.2.2 TADL2-Timing Constraints

For better understanding of the following chapters, the TADL Constraints will be presented next. As abbreviation and unification, all timing expressions are defined as set \mathbb{T} , which are understood as real numbers but expanded with ∞ and $-\infty$ in this chapter, but other value ranges for time expressions are possible and will be used in other parts of this thesis.

We define an event as a time value, possibly combined with an data value. The range of the data values are arbitrary, infinite data types are possible as well as empty data types, when only the point in time is relevant for the constraint. All TADL constraints are defined with attributes, which can be events, timing or arithmetic expressions or sets of them. Also, *EventChains* can be used as attributes. An *EventChain* consists of two sets of events (*stimulus* and *response*), which are causally related. All events in an *EventChain* must have a color value in their data field. This color possibly has an infinite type and an equality check on the datatype of the color must be defined. It is used to check, which events of an *EventChain* are directly related.

DelayConstraint

The DelayConstraint has 4 attributes

```
\begin{array}{ccc} source & \text{event set} \\ target & \text{event set} \\ lower & \mathbb{T} \text{ (time expression)} \\ upper & \mathbb{T} \end{array}
```

and is defined as

```
\forall x \in source : \exists y \in target : lower \leq y - x \leq upper.
```

For all events x in *source*, there must be a y event in *target*, so that the time distance between x and y is between *lower* and *upper*. Note, that *lower* and *upper* can have negative values and that additional events in *target*, without an associated *source* event are allowed.

Figure 2.5 shows a visualized example of the DelayConstraint with the attributes lower = 2, upper = 3, $source = \{1, 5, 6\}$ and $target = \{2, 3.5, 5, 7, 8.2, 9\}$. The first element of source at timestamp 1 results in a required event in target between the timestamp 3 and 4 that is fulfilled by the event at 3.5. The second event of source requires an target event between 7 and 8, fulfilled by the event at 7. The last event of source is satisfied by the target event at 8.2 and 9.

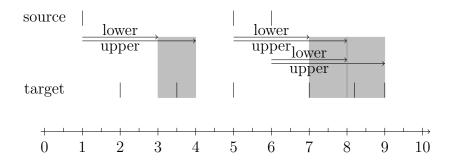


Figure 2.5: Example DelayConstraint - lower = 2, upper = 3

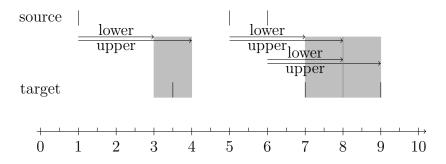


Figure 2.6: Example StrongDelayConstraint - lower = 2, upper = 3

StrongDelayConstraint

The StrongDelayConstraint has 4 attributes

```
\begin{array}{ccc} source & \text{event set} \\ target & \text{event set} \\ lower & \mathbb{T} \\ upper & \mathbb{T} \end{array}
```

and is defined as

```
|source| = |target| \land \\ \forall i : \forall x : x = source(i) \Rightarrow \exists y : y = target(i) \land lower \leq y - x \leq upper.
```

The StrongDelayConstraint is a stricter version of the DelayConstraint, as it requires a bijective assignment between the source and target events, therefore additional events in target without matching source event are not allowed. Figure 2.6 shows an example of the StrongDelayConstraint. The example is the same as in the previous constraint, but without the additional target events at 2, 5 and 8.2.

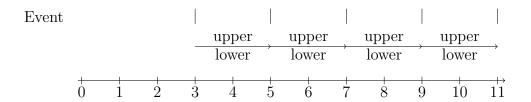


Figure 2.7: Example RepeatConstraint - lower = 2, upper = 2, span = 1

RepeatConstraint

The RepeatConstraint also has 4 attributes

event event set lower \mathbb{T} upper \mathbb{T} span integer

and is defined as

$$\forall X \leq event : |X| = span + 1 \Rightarrow lower \leq \lambda([X]) \leq upper.$$

As reminder, the \leq -operator over two sets of events A, B describes, that A is a sub-sequence of B, the $\lambda(A)$ -function calculates the total length of all continuous intervals in A and [A] is the time interval between the oldest and newest event in A.

The definition of the RepeatConstraint specifies that the length of each time interval containing span + 1 subsequent events must be between upper and lower. The idea behind this constraint is to define repeated occurrences of events, with the possibility of overlapping, specified by the span attribute. After any event x, there are span - 1 events and than the next event must be between lower and upper after x.

Figure 2.7 shows an example of the RepeatConstraint with the attributes $event = \{3, 5, 8, ...\}$, lower = upper = 2 and span = 1. Because lower is equal upper and span is 1, the events are following a strictly periodic pattern after the first event. Figure 2.8 shows a more complex example with events at $\{0, 2, 4, 7, 9, 11, ...\}$, lower = 4, upper = 5 and span = 2. The span-attribute is 2, so the time distances between all subsequent events with an even index are considered, as well as the distances between subsequent events with an uneven index.

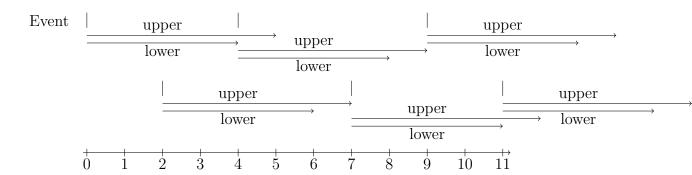


Figure 2.8: Example RepeatConstraint - lower = 4, upper = 5, span = 2

RepetitionConstraint

The RepetitionConstraint has 5 attributes

```
event event set lower \mathbb{T} upper \mathbb{T} span integer jitter \mathbb{T}
```

and is defined via the RepeatConstraint and the StrongDelayConstraint as

```
\exists X : RepeatConstraint(X, lower, upper, span) \land StrongDelayConstraint(X, event, 0, jitter)
```

where X is a set of arbitrary time stamps, that follow the structure of the Repeat-Constraint(various(span)) loose periodic repetitions). The actual points in time of event lay between the timestamps of X and jitter after that. For each point of time there is exactly one, corresponding timestamp in X. Figure 2.9 shows an example of the RepetitionConstraint with the attributes $event = \{0.5, 3.3, 4.7, 7.6, 9.9, ...\}$, lower = 4, upper = 5, span = 2 and jitter = 1. The shown timestamps of X are only one possibility and may change due to later elements of event.

SynchronizationConstraint

The Synchronization Constraint has 2 attributes

```
\begin{array}{ll} event & \text{set of event sets, } |event| \geq 2 \\ tolerance & \mathbb{T} \end{array}
```

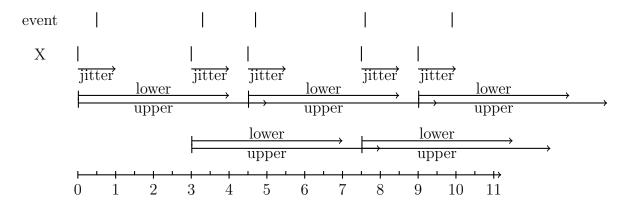


Figure 2.9: Example RepetitionConstraint - lower = 4, upper = 5, span = 2, jitter = 1

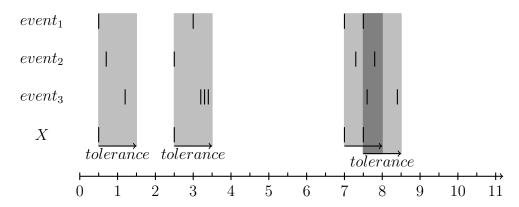


Figure 2.10: Example SynchronizationConstraint - tolerance = 1

and is defined via the *DelayConstraint* as

 $\exists X : \forall i : DelayConstraint(X, event_i, 0, tolerance) \land DelayConstraint(event_i, X, -tolerance, 0)$

X is a set of timestamps and there must be at least one timestamp in each set of event, that is between an element of X and tolerance after that. Also, for each element in any set of event, there must be a matching element of X.

In figure 2.10 is an example of the SynchronizationConstraint with the attributes $event = \{\{0.5, 3, 7, 7.5\}, \{0.7, 2.5, 7.3, 7.8\}, \{1.2, 3.2, 3.3, 3.4, 7.6, 8.4\}\}$ and tolerance = 1. The first points in time of each element of event form the first cluster, the corresponding element of X can be between 0.2 and 0.5. For simplification, only the latest possible value for the element of X are shown, which is the first event of the synchronization cluster. In the second cluster of events it can be seen that multiple timestamps from one element of event can be associated with a single element of event and fourth cluster show, that overlapping is also possible.

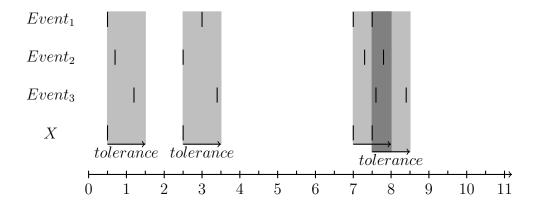


Figure 2.11: Example StrongSynchronizationConstraint - tolerance = 1

StrongSynchronizationConstraint

The StrongSynchronizationConstraint has the same two attributes as the SynchronizationConstraint

```
\begin{array}{ll} event & \text{set of event sets, } |event| \geq 2 \\ tolerance & \mathbb{T} \end{array}
```

and is defined as

 $\exists X : \forall i : StrongDelayConstraint(X, event_i, 0, tolerance)$

This constraint is a stricter variant of the SynchronizationConstraint, as it requires a bijective assignment between the elements of X to one element of each set of event. For every $x \in X$, only one corresponding timestamp per set in event is allowed, like seen in figure 2.11, which shows the same example as the one for the SynchronizationConstraint, but the excess time stamps at 3.2 and 3.3 have been removed.

ExecutionTimeConstraint

The Execution Time Constraints takes 6 attributes

```
\begin{array}{ccc} start & \text{set of events} \\ stop & \text{set of events} \\ preempt & \text{set of events} \\ resume & \text{set of events} \\ lower & \mathbb{T} \end{array}
```

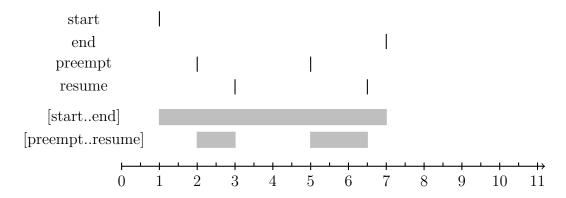


Figure 2.12: Example ExecutionTimeConstraint

upper \mathbb{T}

and is defined as

 $\forall x \in start : lower \leq \lambda([x..stop] \setminus [preempt..resume]) \leq upper$

The interval constructor $\forall x \in start : [x..stop]$ defines the time interval between each point in time of start until the next element of stop, excluding the stop timestamp. [preempt..resume], which is removed from the considered interval length, defines the intervals between each element of preempt until the next timestamp of resume. The Idea behind this constraint is to test the run time of a task, without counting interruptions.

Figure 2.12 shows an example of the ExecutionTimeConstraints with $start = \{1\}$, $end = \{7\}$, $preempt = \{2,5\}$ and $resume = \{3,6.5\}$. Therefore, [start..end] spans the interval from time 1 to 7 with the length of 6 and [preempt..resume] spans two intervals, 2 to 3 and 5 to 6.5 with the length 1 and 1.5. As result, $\lambda([x..stop] \setminus [preempt..resume])$ for x = 1 is 3.5 and the constraint is fulfilled, if, and only if, lower is equal or lower than 3.5 and upper is greater than that.

OrderConstraint

The OrderConstraint takes two attributes

source set of events
target set of events

and is defined as

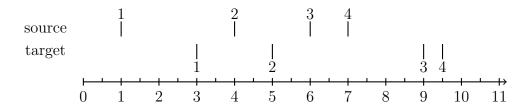


Figure 2.13: Example OrderConstraint

```
|source| = |target| \land \forall i : \exists x : x = source(i) \Rightarrow \exists y : y = target(i) \land < x \le y
```

This constraints ensures the order of events, so that the *i*-th event of *target* occurs after the *i*-th event of *source*. Also, the number of events in *source* and *target* must be equal.

Figure 2.13 visualizes an example of the OrderConstraint with $source = \{1, 4, 6, 7\}$ and $target = \{3, 5, 9, 9.5\}$. The constraint is fulfilled, because the number of elements is equal and each i-th timestamp in target is later that the i-th timestamp of source.

ComparisonConstraint

The ComparisonConstraint is significant different to all previous and following constraints, as it does not describe the behavior of events and only compares two time expressions. It takes 3 attributes

The definition is pretty straight forward as it only applies the given operator to the operands:

```
Comparison Constraint (left Operand, right Operand, Less Than Or Equal) \\ \Leftrightarrow left Operand \leq right Operand \\ Comparison Constraint (left Operand, right Operand, Less Than) \\ \Leftrightarrow left Operand < right Operand \\ Comparison Constraint (left Operand, right Operand, Greater Than Or Equal) \\ \Leftrightarrow left Operand \geq right Operand \\ Comparison Constraint (left Operand, right Operand, Greater Than) \\ \Leftrightarrow left Operand > right Operand
```

```
ComparisonConstraint(leftOperand, rightOperand, Equal)
\Leftrightarrow leftOperand = rightOperand
```

Due to the simplicity of this constraint, no explicit example is given.

SporadicConstraint

The SporadicConstraint takes 5 attributes

```
\begin{array}{ccc} event & \text{set of events} \\ lower & \mathbb{T} \\ upper & \mathbb{T} \\ jitter & \mathbb{T} \\ minimum & \mathbb{T} \end{array}
```

and is defined as combination of the Repetition Constraint and the Repeat Constraint as

```
RepetitionConstraint(event, lower, upper, 1, jitter) \land RepeatConstraint(event, minimum, \infty, 1)
```

The second part of the definition, using the RepeatConstraint, ensures that all events in event lay at least minimum apart. The application of the RepetitionConstraint generates a set of events X, that lay between lower and upper apart from each other. For each point in time in X, there must be exactly one timestamp in event, that is not before the corresponding element of X and not later than jitter after that. Figure 2.14 shows a application of the SporadicConstraint with the attributes lower = 2, upper = 2.5, jitter = 1, minimum = 2 and $event = \{1, 3.5, 6, 8.2, 10.5, ...\}$. Like in the RepetitionConstraint, the exact position of the timestamps in X is variable and may need to be changed due to later entries in event.

PeriodicConstraint

The PeriodicConstraint takes 4 attribute

```
\begin{array}{ccc} event & \text{set of events} \\ period & \mathbb{T} \\ jitter & \mathbb{T} \\ minimum & \mathbb{T} \end{array}
```

and defines a specialized form of the Sporadic Constraint

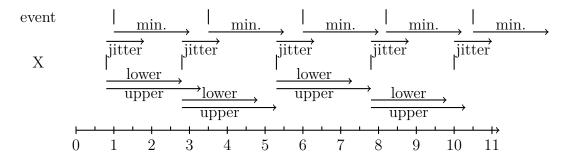


Figure 2.14: Example Sporadic Constraint - $lower=2,\, upper=2.5,\, jitter=1,\, minimum=2$

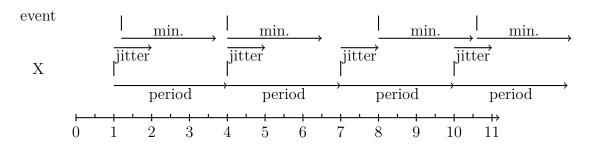


Figure 2.15: Example PeriodicConstraint - period = 3, jitter = 1, minimum = 2.5

SporadicConstraint(event, period, period, jitter, minimum)

The variable timestamps in the set X are now following a strictly periodic pattern, where subsequent elements of this set lay exactly period apart. Each element of event lays between one element of X and jitter after that. Again, there must be bijective mapping between the elements of event and X.

In figure 2.15, the PeriodicConstraint with the attributes period = 3, jitter = 1, minimum = 2.5 and $event = \{1.2, 4.0, 8, 10.6, ...\}$ is visualized. The timestamps of X lay exactly period apart and the events behind that in the previously described way. Also, the minimum time distance between all points of time in event is minimum.

PatternConstraint

The PatternConstraint takes 5 attributes

 $\begin{array}{ll} \textit{event} & \textit{set of events} \\ \textit{period} & \mathbb{T} \\ \textit{offset} & \textit{set of } \mathbb{T} \end{array}$

```
\begin{array}{cc} jitter & \mathbb{T} \\ minimum & \mathbb{T} \end{array}
```

and is defined as

```
\exists X: PeriodicConstraint(X, period, 0, 0) \\ \land \forall i: DelayContraint(X, event, offset_i, offset_i + jitter) \\ \land RepeatConstraint(event, minimum, \infty, 1)
```

This constraint can be understood as a modification of the PeriodicConstraint, as it describes periodic behavior, but not from single events, but from groups of $|offset_i|$ subsequent events, that follow specific time distances (specified by offset) after the strictly periodic timestamps of X.

There is a major weak spot in the definition of this constraint, because the set X can be set to the empty set. In this case, the part of the definition, which uses the PeriodicConstraint and the DelayContraint, are always satisfied, irrespective of the events in event. Therefore, the PatternConstraint only ensures the minimal distance between two events, what should not the purpose of this constraint. The obvious countermeasure to this problem would be to restrict X in a way that ensures that it is not empty and the first element of X must lay before the first event occurrence. The textual description of the constraint, which says literally the "PatternConstraint requires the constrained event occurrences to appear at a predetermined series of offsets from a sequence of reference points" contradicts this countermeasure, because the DelayConstraint allows additional events in the target events with no matching source event. Therefore, any event occurrences additionally to the events following the offset scheme, would be allowed, which conflicts with the citation. Because of this problem, the PatternConstraint is redefined as

```
\exists X: PeriodicConstraint(X, period, 0, 0) \\ \land \forall i: \textbf{Strong} DelayContraint(X, event, offset_i, offset_i + jitter) \\ \land RepeatConstraint(event, minimum, \infty, 1)
```

for the scope of this thesis. The use of the *StrongDelayConstraint*, instead of the *DelayConstraint*, ensures that each event occurrence is following the time distances defined by the offsets. This notion of the *PatternConstraint* is also carried by the described relations between the TADL2 timing constraints and the AUTOSAR Timing Extensions, which were done as part of the development of TADL2[BFL+12]. These descriptions equate the *PatternConstraint* and AUTOSARs *ConcretePattern-EventTriggering*, which is clearly defined in the way of this redefinition.

Figure 2.16 shows an application of the PeriodicConstraint with attributes period = 5, $offset = \{1, 2, 2.5\}$, jitter = 0.5, minimum = 0.5 and $event = \{1.2, 2.2, 2.8, 6, 7, 8, 11.5, 12, 12.5, ...\}$. Like in the previous describes con-

 $event = \{1.2, 2.2, 2.8, 6, 7, 8, 11.5, 12, 12.5, ...\}$. Like in the previous describes constraint, the exact position of all points in time of X may change due to later times-

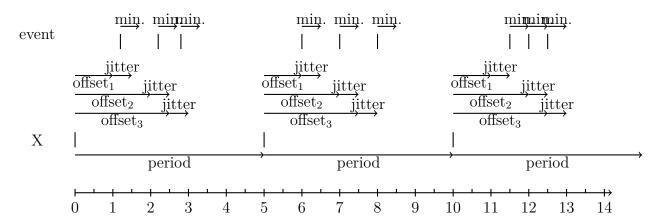


Figure 2.16: Example PatternConstraint - period = 5, $offset = \{1, 2, 2.5\}$, jitter = 0.5, minimum = 0.5

tamps of event.

ArbitraryConstraint

The Arbitrary Constraint takes 3 attributes

 $\begin{array}{ll} \textit{event} & \text{set of events} \\ \textit{minimum} & \text{set of } \mathbb{T} \\ \textit{maximum} & \text{set of } \mathbb{T} \end{array}$

where |minimum| = |maximum|. It is defined as

 $\forall i : RepeatConstraint(event, minimum_i, maximum_i, i)$

The Idea behind the *ArbitraryConstraint* is to describe the time distance between each event and several following events. The first entry of *minimum* and *maximum* define the distance between every event and it direct successor. The second entries, where the *span* attribute of the *RepeatConstraint* is 2, defines the distance between one event and its next but one successor and so on.

Figure 2.17 shows an example of the ArbitraryConstraint with the attributes $minimum = \{1, 2, 3\}$, $maximum = \{5, 6, 7\}$ and $event = \{1, 2, 3, 5, 8, 10, ...\}$. The time distances between subsequent events with 0, 1, 2 and more skipped events are shown in table 2.1, the relevant distances are written in **bold** font. Apparently, the time distances are matching the ranges, given by the minimum- and maximum attribute.

	1	2	3	5	8	10
1	0	1	2	4	7	9
2		0	1	3	6	8
3			0	2	5	7
5				0	3	5
8					0	2
10						0

Table 2.1: Time distances as seen in figure 2.17

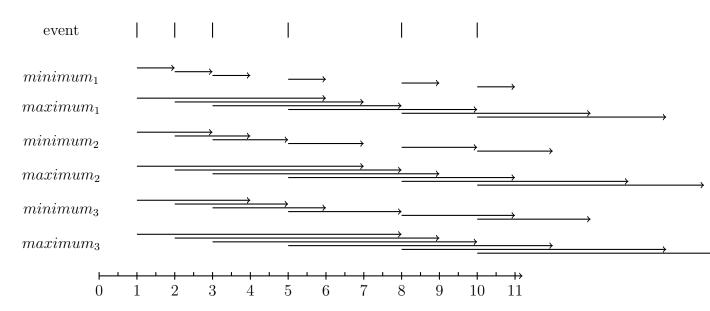


Figure 2.17: Example Arbitrary Constraint - $minimum = \{1,2,3\}$ and $minimum = \{4,5,6\}$

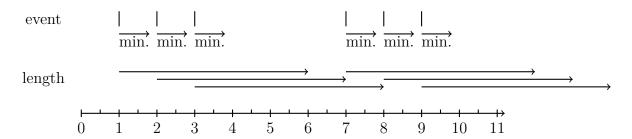


Figure 2.18: Example BurstConstraint - length = 5, maxOccurences = 3 minimum = 0.8

BurstConstraint

The BurstConstraint takes 4 attributes

```
\begin{array}{ccc} & event & \text{set of events} \\ & length & \mathbb{T} \\ \\ maxOccurrences & integer \\ & minimum & \mathbb{T} \end{array}
```

and is defined as

 $RepeatConstraint(event, length, \infty, maxOccurrences) \land RepeatConstraint(event, minimum, \infty, 1)$

The idea of this constraint is to describe the maximum number of events that may occur in a time interval of the given *length*. Additionally all subsequent event must be at least *minimum* apart. Therefore, the intuition is different to the AUTOSAR *BurstPatternEventTriggering*, where clusters of events are described. A complete comparison of these constraints will be done in section 2.2.3.

In figure 2.18, an application of the BurstConstraint with the attributes length = 5, maxOccurrences = 3, minimum = 0.8 and $event = \{1, 2, 3, 7, 8, 9\}$ is visualized. In every interval of the length 5, there are three or less events, also all subsequent events lay at least 0.8 apart. Therefore, the constraint is fulfilled.

ReactionConstraint

The ReactionConstraint takes 3 attributes

 $scope \quad EventChain$ $minimum \quad \mathbb{T}$ $maximum \quad \mathbb{T}$

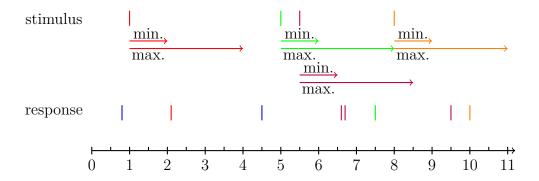


Figure 2.19: Example ReactionConstraint - minimum = 1, maximum = 3

and is defined as

```
\forall x \in scope.stimulus : \exists y \in scope.response : \\ x.color = y.color \\ \land (\forall y' \in scope.response : y'.color = y.color \Rightarrow y \leq y') \\ \land minimum \leq y - x \leq maximum
```

The definition says, that after every event x of scope.stimulus, there is an event y in scope.response with the same color. The time distance between these events must be at least minimum and at most maximum. Additional events with the same color as y in scope.response are allowed, if they lay behind y. The definition implies, that additional events with other colors are allowed in scope.response, but not in scope.stimulus and every color is only allowed once in scope.stimulus. A visualized example with the attributes minimum = 1, maximum = 3, $scope.stimulus = \{(1, red), (5, green), (5.5, purple), (8, orange)\}$ and $scope.response = \{(0.8, blue), (2.1, red), (4.5, blue), (6.6, purple), (6.7, purple), (9.5, purple), (7.5, green), (10, orange)\}$ can be seen in figure 2.19. The red stimulus-event is followed by the red response-event at 2.1, the green stimulus event at 5 by the response event at 7.5 and so on. The blue response events at 1 and 4.5 are additional events without an associated stimulus event. The purple events at 6.7 and 9.5 are the second and third event of this color in scope.response and therefore, their time distance to the stimulus event with the same color is irrelevant.

AgeConstraint

The AgeConstraint takes 3 attributes

```
scope EventChain minimum \mathbb{T} maximum \mathbb{T}
```

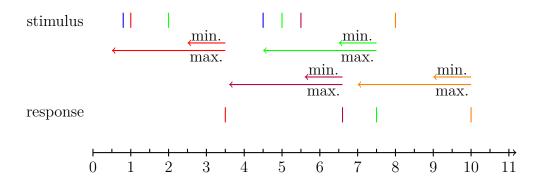


Figure 2.20: Example AgeConstraint - minimum = 1, maximum = 3

and is defined as

```
\forall y \in scope.response : \exists x \in scope.stimulus : \\ x.color = y.color \\ \land (\forall x' \in scope.stimulus : x'.color = x.color \Rightarrow x' \leq x) \\ \land minimum \leq y - x \leq maximum
```

The AgeConstraint is a turned around counterpart to the ReactionConstraint. For every event of scope.response, there must be an event with the same color in scope.stimulus, that is between minimum and maximum older than the response event. Additional events are only allowed in scope.stimulus, and only before the event that matches with a response event.

Figure 2.20 shows an application of the AgeConstraint with the attributes minimum = 1, maximum = 3, $scope.stimulus = \{(0.8, blue), (1, red), (2, green), (4.5, green), (5.5, purple), (8, orange)\}$ and $scope.response = \{(3.5, red), (7.5, green), (6.6, purple), (10, orange)\}$. The blue timestamps are additional events without matching events in scope.response.

OutputSynchronizationConstraint

The OutputSynchronizationConstraint takes 2 attributes

```
scope Set of EventChain tolerance \mathbb{T}
```

where all elements of *scope* have the same *stimulus*. It is defined as

```
\forall x \in scope_1.stimulus : \exists t : \forall i : \exists y \in scope_i.response : x.color = y.color 
  \land (\forall y' \in scope_i.response : y'.color = y.color \Rightarrow y \leq y')
```

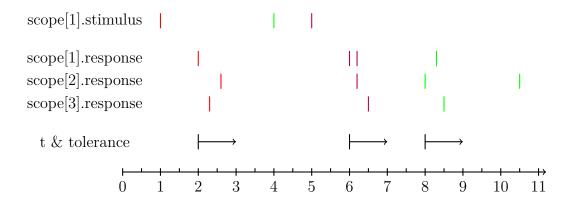


Figure 2.21: Example OutputSynchronizationConstraint - tolerance = 1

```
\land 0 \le y - t \le tolerance
```

The definition says, that after each event x in $scope_1.stimulus$, there must be a interval with the length of tolerance, in which every $scope_i.response$ must have an event y with the same color as x. Additional response events with this color are only allowed after y. Figure 2.21 shows an example of the OutputSynchronization-Constraint with the attributes tolerance = 1,

```
scope[1].stimulus = scope[2].stimulus = scope[3].stimulus = \{(1, red), (4, green), (5, purple)\},\\ scope[1].response = \{(2, red), (6, purple), (6.2, purple), (8.2, green)\},\\ scope[2].response = \{(2.6, red), (6.2, purple), (8, green), (10.5, green)\},\\ scope[3].response = \{(2.3, red), (6.5, purple), (8.5, green)\}.
```

InputSynchronizationConstraint

The InputSynchronizationConstraint takes 2 attributes

```
\begin{array}{ccc} scope & \text{Set of } EventChain \\ tolerance & \mathbb{T} \end{array}
```

where all elements of *scope* have the same *response*. It is defined as

The InputSynchronizationConstraint is a counterpart of the OutputSynchronization-Constraint, as the stimulus events must be synchronized, not the response events.

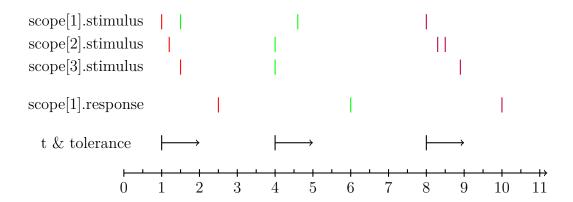


Figure 2.22: Example InputSynchronizationConstraint - tolerance = 1

```
Figure 2.22 contains an example of the InputSynchronizationConstraint with the attributes tolerance = 1 scope[1].stimulus = \{(1, red), (1.5, green), (4.6, green), (8, purple)\} scope[2].stimulus = \{(1.2, red), (4, green), (8.3, purple), (8.5, purple)\} scope[3].stimulus = \{(1.5, red), (4, green), (8.9, purple)\} scope[3].response = scope[2].response = scope[3].response = \{(2.5, red), (6, green), (10, purple)\}
```

2.2.3 Comparison TADL2 - AUTOSAR Timing Extension

As said before, the TADL2 Timing Constraints and the AUTOSAR Timing Extension are compatible in parts and many of the AUTOSAR Timing Extension can be expressed as equivalent combinations of the TADL2 Timing Constraints. In [BFL+12], the relation between these constraints is shown, but this comparison is based on an outdated version of the AUTOSAR Timing Extensions and some of the constraints have been updated, therefore each of the AUTOSAR Timing Extensions will be listed in this chapter and it will be explained, if and how they can be expressed using TADL2 Timing Constraints.

The types used in the AUTOSAR Timing Extension are similar to the ones in TADL2. TADL2 Events are called TimingDescriptionEvent in AUTOSAR, the same goes for EventChains, which are called TimingDescriptionEventChains. A larger difference can be seen in the definition of time. While TADL2 defines time as real numbers, the time definition used in the AUTOSAR Timing Extension can also be multidimensional, for example when the real time and the angle of the crankshaft is regarded. For simplification, all timestamps are considered as real numbers in the following, but an extension to multidimensional time stamps is possible, as AUTOSAR requires a strict order between all time stamps. Some of the AUTOSAR Timing Extensions are defined on Executable Entities, describe things, that can be

executed, for example a function. In the analysis of their timing, only striking point in times of these entities are relevant, for example the start or end points, therefore *Executable Entities* are transformed into event if needed.

It should be noted, that the set of TADL2 timing constraints are not equal to the AUTOSAR Timing Extension and that there are constraints, that cannot be expressed using the corresponding counterpart.

PeriodicEventTriggering

The PeriodicEventTriggering defined in AUTOSAR with the attributes (event, period, jitter, minimumInterArrivalTime) is equivalent to the TADL2 PeriodicConstraint with the same attributes.

SporadicEventTriggering

AUTOSARs SporadicEventTriggering with the attributes (event, jitter, maximumInterArrivalTime, minimumInterArrivalTime, period) is equivalent to the TADL2 SporadicConstraint, but the names of the attributes are different:

```
lower = period

upper = maximumInterArrivalTime

jitter = jitter

minimum = minimumInterArrivalTime
```

ConcretePatternEventTriggering

The idea behind the *ConcretePatternEventTriggering* from AUTOSAR is the same as behind TADL2s *PatternConstraint*, but some details are different. Both define a periodic behavior and offsets, that describe time distances between the periods and the actual events. The main difference is the *jitter* attribute. In AUTOSARs *ConcretePatternEventTriggering*, the *patternJitter* attribute defines the allowed deviation of the start points from the periodic repetitions, but in TADL2 the *jitter* value describes the deviation between the offsets and the actual event.

The ConcretePatternEventTriggering from AUTOSAR additionally defines an patternLength attribute, which describes the length of the intervals, in which the clusters of events will occur. It is constrained by

```
0 \leq max(offset) \leq patternLength \\ \land patternLength + patternJitter < patternPeriod
```

The *patternLength* attribute can not be described with TADL2 timing constraints, as it would require to determine the distance of filtered events, which is not possible with the TADL2 constraints.

TADL2 defines the minimum attribute for the PatternConstraint that describes the minimal time distance between subsequent events. In AUTOSAR, this must be described by using the ArbitraryEventTriggering, where $minimumDistance_1$ is minimum and $maximumDistance_1$ is ∞ .

BurstPatternEventTriggering

The BurstPatternEventTriggering as defined in AUTOSAR and TADL2s BurstConstraint share the same target, as they define a maximum number of events that may occur in a specific time interval, but the BurstPatternEventTriggering is way more complex. Additionally to the attributes of TADL2s BurstConstraint, that define the length of the time interval, the maxOccurrences of the event in this interval and the minimal time between subsequent events, the BurstPatternEventTriggering allows to define the minimal number of events in the interval and periodic repetitions of the burst interval.

Every set of attributes fulfilling the TADL2 BurstConstraint fulfill the AUTOSAR BurstPatternEventTriggering, when the attributes are renamed to the AUTOSAR equivalents ($length \rightarrow patternLength$, $maxOccurences \rightarrow maxNumberOfOccurences$, $minimum \rightarrow minimumInterArrivalTime$). This does not work the other way around, even if the attributes, that exist in the BurstPatternEventTriggering and not in the BurstConstraint are unused. The reason for this is, that the observed interval must start at an event in the TADL2 BurstConstraint, in the BurstPattern-EventTriggering those can start in any point of time.

ArbitraryEventTriggering

AUTOSARs ArbitraryEventTriggering is similar to the ArbitraryConstraint as defined in TADL2, but ArbitraryEventTriggering allows to set a list of ConfidenceIntervals, to describe the probability, how far the events may lay apart. These probabilities can not be expressed in TADL2.

LatencyTimingConstraint

The LatencyTimingConstraint of AUTOSAR takes 5 attributes, a latency type $latencyConstraintType \in \{age, reaction\}$, three time values maximum, minimum and nominal and an event chain scope, consisting of the stimulus and response

events. The nominal-value is not defined in the TADL2 constraint, if this attribute is not required for the specification, the LatencyTimingConstraint can be expressed with the AgeConstraint defined in TADL2 if the latencyConstraintType is age. If the latencyConstraintType is reaction, it can be expressed by the reactionConstraint.

AgeConstraint

The goal of the AgeConstraint in AUTOSAR is to define a minimal and maximal age of an event at the point in time, when it is processed. There is no counterpart to this in the TADL2 constraints, because the point in time, when the event is processed, is unknown. If this point in time is known, AUTOSARs AgeConstraint can be expressed using TADL2s AgeConstraint, but in that case, it could also be expressed using AUTOSARs LatencyTimingConstraint.

SynchronizationTimingConstraint

The Synchronization Timing Constraint is similar to TADL2s Synchronization Constraint, Strong Synchronization Constraint, Output Synchronization Constraint, Input-Synchronization Constraint or combinations of them, depending on the attributes. Table 2.2 shows, with which attributes the Synchronization Timing Constraint is equivalent to which TADL2 Constraint(s).

SynchronizationPointConstraint

The *SynchronizationPointConstraint* describes, that a list of executables and a set of events or executable entities, defined in *sourceEec* and *sourceEvent*, must finish and occur, before the executables and events in *targetEec* and *targetEvent* will start or occur. There is no counterpart to this in the TADL2 constraints.

OffsetTimingConstraint

The Offset Timing Constraint, defined in the AUTOSAR Timing Extensions, is semantically the same as the TADL2 Delay Constraint, just some attributes are named differently. The maximum attribute of the Offset Timing Constraint is named upper and the minimum attribute lower in the Delay Constraint.

event Occurrence- Kind	scope/ scopeEvent	synchronization- ConstraintType	tolerance	TADL2 Constraints	
multiple Occurrences	scopeEvent	not set	tolerance	SynchronizationConstraint (scopeEvent, tolerance)	
single Occurrences	scopeEvent	not set	tolerance	Strong- SynchronizationConstraint (scopeEvent, tolerance)	
multiple Occurrences	scope	response Synchronization	tolerance	Output- SynchronizationConstraint (scope, tolerance) ^ SynchronizationConstraint (scope.response, tolerance)	
single Occurrences	scope	response Synchronization	tolerance	Output- SynchronizationConstraint (scope, tolerance) ^ Strong- SynchronizationConstraint (scope.response, tolerance)	
multiple Occurrences	scope	stimulus Synchronization	tolerance	Input- SynchronizationConstraint (scope, tolerance) ∧ SynchronizationConstraint (scope.stimulus, tolerance)	
single Occurrences	scope	stimulus Synchronization	tolerance	Input- SynchronizationConstraint (scope, tolerance) ∧ SynchronizationConstraint (scope.stimulus, tolerance)	

Table 2.2: Synchronization TimingConstraint \Leftrightarrow TADL2 Constraints

ExecutionOrderConstraint

The goal of *ExecutionOrderConstraint* of the AUTOSAR Timing Extensions is used to describe the order of events or the execution order of executable entities, defined as *orderedElement* attribute. There is no constraint in TADL2 that describes exactly this, but if the *ExecutionOrderConstraint* is used to describe only the order of events, it can be described as

```
OrderConstraint(orderedElement_1, orderedElement_2)
\wedge ... \wedge
OrderConstraint(orderedElement_{n-1}, orderedElement_n)
```

If the *ExecutionOrderConstraint* is used for executable entities, each executable entity must be turned into one or more events to be described via TADL2 Constraints, depending on the other attributes. For example, if the attribute *executionOrder-ConstraintType* is set to *ordinaryEOC*, the start and finish points of the entities define the observed events.

ExecutionTimeConstraint

The idea behind the Execution Time Constraint is similar in AUTOSAR and TADL2. Both describe the minimal and maximal allowed run time of an executable entity, not counting interruptions. AUTOSARs Execution Time Constraint is defined directly on an executable entity and the TADL2 constraint on events describing the start, stop, preemption and resume timestamps. Therefore the executable entity must be turned into these events to express the AUTOSAR Execution Time Constraint via TADL2 constraints. The start and stop points of the executable must be turned into these events, the start and stop points of the interruptions must be turned into the events in the preempt and resume event sets. If external calls should be excluded from the run time, they must also be transferred into the preempt and resume event sets.

3 Monitoring Timing Constraints on possibly infinite Streams

The goal of this thesis is to implement online monitors for the TADL2 Timing Constraints on possibly infinite streams. An online monitor checks the current execution of a system, parallel to its execution. Because every computing system has finite memory resources and the online monitor should be able to process at least as many events as occur in the stream in a specific amount time, not every property can be monitored in an online monitoring setting. In this chapter, the term of Simple Monitorability will be introduced, which ensures that monitoring a property on infinite streams is possible with finite memory resources and finite time resources per event. As introduction into the setting, some related work will be described, inter alia TeSSLa, the programming language which is used for the implementation.

3.1 Related Work

Runtime Verification

As monitoring plays a major role in runtime verification, a short overview of this will be given. The definitions of [LS09] are used, in which *Runtime Verification* is a technique that can detect deviations between the run of a system and its formal specification by checking correctness properties. A *run*, which might also be called *trace*, is sequence of the system states, which might be infinite and an *execution* is an finite prefix of this run. A *monitor* reads the trace and decides, whether it fulfills the correctness properties or violates them.

A distinction is made between offline and online monitoring. Offline monitoring is using a stored trace, that has been recorded before. Therefore, the complete trace (or the complete part of the trace, that should be analyzed) is known in the analysis. Online monitoring checks the properties, while the system is running, which means that the analysis must be done incrementally on a growing prefix of the trace. Because of memory and time limitations, not all previous states can be read again in online monitoring, more detailed contemplations on the limitations of online monitors will be given in in this chapter.

TeSSLa

TeSSLa (Temporal Stream-based Specification Language) [LSS+18] is a specification language build for stream Stream Runtime Verification. In TeSSLa, all streams in one specification must have a common global clock, but events or changes in a signal may occur in streams irregularly, independent of events in other streams. The verified streams are either considered as signal, which remain unchanged for certain amount of time (called *piece wise constant signals*), or they are *event streams*, in which each event consists of a timestamp and a data value. Both variants can be transferred into each other, like described in [LSS+18]. A formal definition of the TeSSLa language core can be found in [CHL+18], a short overview of the formal definition of event streams will be given next.

An event stream is defined over a time domain \mathbb{T} and a data domain \mathbb{D} and is an possibly infinite sequence $s = a_0 a_1 \dots \in \mathcal{S}_D = (\mathbb{T} \cdot \mathbb{D})^\omega \cup (\mathbb{T} \cdot \mathbb{D})^+ \cup (\mathbb{T} \cdot \mathbb{D})^* \cdot (\mathbb{T}_\infty \cup \mathbb{T} \cdot \{\bot\})$ where $a_{2i} < a_{2(i+1)}$ for all i with 0 < 2(i+1) < |s| $(0 < 2(i+1) < \infty$ if the sequence is infinite). While the data domain \mathbb{D} can be bounded (e.g. boolean or integer) or unbounded (e.g. maps or lists), the time domain \mathbb{T} is a totally ordered semi-ring $(\mathbb{T}, 0, 1, +, *, \leq)$, that is not negative.

In TeSSLa, computations are done, when new events are arriving. Based on the specification, output streams are generated with events on the same timestamps as the used input streams, but filtering is possible, where not all input events produce output events. With the *delay*-operator, it is possible to create new timestamps. If the *delay*-operator is not used in a specification, the output streams only contains events in timestamps, which also had events in the input streams. These specifications are called *timestamp conservative*. In a memory perspective, streams may be understood as *piece wise constant signals*. Only the timestamp and the data value of the youngest event of one stream can be directly accessed. This event is available until the next event of this stream occurs. With the use of the *last*-operator, which can be used recursively, the data value of the previous event can be accessed. Another important operator is the *lift*-operator, which applies a function on data values (for example the + operator) on the data value of every event of one or more streams and creates a new stream with events at the same timestamps and the results of the function as data values.

LOLA

[DSS⁺05] introduces *LOLA*, a specification language for the observation of synchronous event streams, comparable to TeSSLa. The main difference between these languages is, that TeSSLa is designed to monitor input streams, which are not synchronized, which means their events may occur independently and do not follow a global clock. Because the events of the timing constraints defined in TADL2 and

AUTOSAR are also not synchronized, TeSSLa is more suitable for monitoring them. [DSS+05] also defines the term of *Efficiently Monitorable Specifications*, which describes that the worst case memory requirement of a LOLA Specification is independent of the length of the observed trace.

3.1.1 Transducer Models

In section 3.2, some transducer models are used, which will be introduced next.

Definition 1 (Deterministic Finite State Transducer[Ber79]). A Deterministic Finite State Transducer(DFST) is a 5-Tuple $(\Sigma, \Gamma, Q, q_0, \delta)$, where

- Σ is an input alphabet
- Γ is an output alphabet
- Q is a finite set of states, with initial state q_0
- $\delta: Q \times \Sigma \to Q \times \Gamma$ is a state transition function

The run of a DFST for an input word $w = w_0 w_1 w_2 ... \in \Sigma^{\infty}$ is a sequence $s_0 \xrightarrow{w_0/o_0} s_1 \xrightarrow{w_1/o_1} s_2 ...,$ where $s_0 = q_0$, $\delta(s_i, w_i) = (s_{i+1}, o_i), i \geq 0$ and the output word $o = o_0 o_1 o_2 ... \in \Gamma^{\infty}$.

DFSTs are similar to deterministic finite automata, with two major differences. First, the transition function outputs a symbol of Γ at every transition and second, the DFST is not accepting, it only transduces an input word.

Timed Deterministic Finite State Transducer(TDFST) are an extension of DFST. The extension from DFST to TDFST is done analogous to the extension of automata to timed automata in [AD94].

Definition 2 (Timed Deterministic Finite State Transducer). Timed Deterministic Finite State Transducer(TDFST) are a 6-Tuple $(\Sigma, \Gamma, Q, q_0, C, \delta)$, where

- Σ is an input alphabet
- Γ is an output alphabet
- Q is a finite set of states, with initial state q_0
- C is a set of clocks
- $\delta: Q \times \Sigma \times \Theta(C) \to Q \times 2^C \times \Gamma$ is a state transition function, where for all $(q_a, \sigma_a, \vartheta_a, q'_a, R_a, \gamma_a), (q_b, \sigma_b, \vartheta_b, q'_b, R_b, \gamma_b) \in \delta$ the conjunction $\vartheta_a \wedge \vartheta_b$ is unsatisfiable.

Let $v_i: C \to R$ be functions that map each clock to its current value.

The run of a TDFST for an input word $w = (w_0, t_0)(w_1, t_1)(w_2, t_2)... \in \Sigma^{\infty}$ is a sequence $s_0, v_0 \xrightarrow[o_0]{(w_0, t_0), \vartheta_0, r_0} s_1, v_1 \xrightarrow[o_1]{(w_1, t_1), \vartheta_1, r_1} s_2, ...$ with output $o = o_0 o_1 o_2... \in \Gamma^{\infty}$, if, and only if,

- $s_0 = q_0$
- $\forall c \in C : v_0(c) = 0$
- $\forall i > 0$:

$$-\delta(s_i, w_i, \vartheta_i) = (s_{i+1}, r_i, o_i)$$

$$- \ \forall c \in r_i : v_{i+1} = v_i[c \leftarrow t_i]$$

$$-t_i, v_i \models \vartheta_i$$

In addition to DFSTs, the state transition function of TDFSTs takes a set of clock constraints into account when defining the next state of the transducer.

3.2 Monitorability

In this section, the term *Simple Monitorability* is introduced. It represents a stricter alternative to *Efficiently Monitorable Specifications* mentioned above, by also restricting the allowed run time per timestamp with events. *Simple Monitorability* ensures, that the worst case memory consumption and the worst case run time per input event of a monitor is independent of the input streams.

Preliminary - Timestamps

As we consider possibly infinite streams, the time value of events can also grow into infinity. This is problematic, because it leads to infinite memory and runtime requirements, which cannot be met, especially not in the context of online monitoring. Therefore, the time domain \mathbb{T} is restricted by the following constraints:

- 1. The first used timestamp has the value $t_0 = 0$
- 2. All used timestamps must be smaller than t_{max} . t_{max} must be big enough, so it is not reached in practical use ¹.

¹ for example, a 64-bit unsigned integer variable is enough, to cover nanoseconds for 584.55 years

- 3. The distance between two subsequent time values is predetermined, but arbitrary small.
- 4. The number of possible timestamps is significantly larger than the number of events

Because of the 2., 3. and 4., a limitation of the number of events in a specific time interval through these restrictions is invalid.

3.2.1 Simple Monitorability

The concept behind the definition of *Simple monitorability* is, that a monitor for event streams is defined by three parts, first the state transition function, a state defining the memory of the monitor and an output function. At each timestamp containing input events, the new state is created by applying the state transition function to the previous state and the input events of the current timestamp. The output function is applied to the new state and the previous output and evaluates, whether the specification is met until this timestamp.

All following definitions of streams and functions follow the syntax and semantic from [CHL⁺18]. The left half of figure 3.1 visualizes the definitions, which will be done now.

Definition 3 (Simple Monitorability). A property is called Simple Monitorable, if a monitor, which outputs $true_{until}$, as long as the property is fulfilled and false after that, can be constructed in the following way:

```
Input Streams Let S_1, S_2, ..., S_n be the input streams with \forall i: S_i = (\mathbb{T} \cdot \mathbb{D}_i)^{\omega} \cup (\mathbb{T} \cdot \mathbb{D}_i)^+ \cup (\mathbb{T} \cdot \mathbb{D}_i)^* \cdot (\mathbb{T}_{\infty} \cup \mathbb{T} \cdot \{\bot\})
```

State Let S_{state} with $S_{state} = (\mathbb{T} \cdot \mathbb{D}_{state})^+ \cup (\mathbb{T} \cdot \mathbb{D}_{state})^*$ be the state stream of the monitor. The cardinality of \mathbb{D}_{state} is finite and the worst case memory requirement is bounded independently of the input streams.

Further let $f: S_1 \times S_2 \times ... \times S_n \times S_{state} \to S_{state}$ be a state transition function, which defines the state stream in an incremental fashion: $\forall t \in \mathbb{T} \exists i \in \{1, 2, ..., n\} : S_i(t) \in \mathbb{D}_i$:

```
S_{state}(t) = f(S_1(t), S_2(t), ..., S_n(t), last(S_{state}, merge(S_1, S_2, ..., S_n))(t))
The worst case run time of f is bounded independently of the input streams.
```

```
Output Stream Let S_{output} = (\mathbb{T} \cdot \{true_{until}, false\})^+ \cup (\mathbb{T} \cdot \{true_{until}, false\})^* be the output stream of the monitor, which is defined via a function g: S_{state} \times S_{output} \rightarrow S_{output} which defines the output stream in an incremental fashion: \forall t \in \mathbb{T} \exists S_{state}(t) \in \mathbb{D}_i:
```

 $S_{output}(t) = g(S_{state}(t), last(S_{output}, S_{state})(t))$ The worst case run time of g is bounded independently of the input streams.

In every timestamp with input events, the state transition function f is applied to the current youngest input events and the previous event of the state stream S_{state} . The output of f, combined of the timestamp of the latest input event, defines the new event in S_{state} . The output of function g is applied to the current state and the previous output and produces the new output. It should be noted that a monitor, which follows this scheme is $timestamp\ conservative$.

For any monitor, which is created in the way described above, a Deterministic Finite State Transducer(DFST) can be constructed, which is equivalent the the combination of a finite state and the state transition function. For that, let

- $Q = \mathbb{D}_{state}$ be the finite set of possible states with initial state q_0
- $\Sigma = ((\mathbb{D}_1 \times \mathbb{T}), ..., (\mathbb{D}_n \times \mathbb{T}))$ be the input alphabet
- $\Gamma = \mathbb{D}_{state}$ be the output alphabet and
- $\delta: Q \times \Sigma \to Q \times \Gamma$ be the transition function.

For the output stream in combination with the output function, an equivalent DFST can be constructed too. For that, let

- $Q' = \{true_{until}, false\}$ be the states with initial state $true_{until}$
- $\Sigma' = \mathbb{D}_{state} \times \mathbb{T}$ be the input alphabet
- $\Gamma' = \{true_{until}, false\}$ be the output alphabet and
- $\delta': Q' \times \Sigma' \to Q' \times \Gamma'$ be the transition function.

It should be noted, that both transducers could be combined into one transducer without changing the expressiveness. This is not done to keep analogies to the following definition.

3.2.2 Simple Monitorability With Delay

Most of the TADL2 constraints can not be monitored correctly in a timestamp conservative way. For example, the RepeatConstraint with the attributes lower = upper = 4 and span = 1 expects subsequent events to have a time distance of 4. If one event is missing, the output of a timestamp conservative monitor would remain $true_{until}$, until the next input event arrives. Therefore, the monitor cannot not check the constraint correctly. Because of this problem, the definition of Simple Monitorability is expanded by the ability of introducing exactly one new timestamps. The following definitions are visualized in the right half of figure 3.1.

Definition 4 (Simple Monitorability With Delay). A property is called Simple Monitorable With Delay, if a monitor, which outputs true_{until}, as long as the property is fulfilled and false after that, can be constructed in the following way:

```
Input Streams Let S_1, S_2, ..., S_n be the input streams with \forall i: S_i = (\mathbb{T} \cdot \mathbb{D}_i)^{\omega} \cup (\mathbb{T} \cdot \mathbb{D}_i)^+ \cup (\mathbb{T} \cdot \mathbb{D}_i)^* \cdot (\mathbb{T}_{\infty} \cup \mathbb{T} \cdot \{\bot\})
```

State Let S_{state} with $S_{state} = (\mathbb{T} \cdot \mathbb{D}_{state})^+ \cup (\mathbb{T} \cdot \mathbb{D}_{state})^*$ be the state stream of the monitor. The number cardinality of \mathbb{D}_{state} is finite and the worst case memory requirement of the state is bounded independently of the input streams. Further let $f: S_1 \times S_2 \times ... \times S_n \times S_{state} \to S_{state}$ be a state transition function, which defines the state stream in an incremental fashion: $\forall t \in \mathbb{T} \exists i \in \{1, 2, ..., n\} : S_i(t) \in \mathbb{D}_i : S_{state}(t) = f(S_1(t), S_2(t), ..., S_n(t), last(S_{state}, merge(S_1, S_2, ..., S_n))(t))$ The worst case run time of f is bounded independently of the input streams.

State_{timeout} Let $S_{state_{timeout}}$ with $S_{state_{timeout}} = (\mathbb{T} \cdot (\mathbb{D}_{state} \cup \{timeout\}))^+ \cup (\mathbb{T} \cdot (\mathbb{D}_{state} \cup \{timeout\}))^*$ be the a second state stream, which is defined via a delay generator DelayGen: $S_{state} \rightarrow S_{state_{timeout}}$. DelayGen has two tasks. First, it copies each input event to the output. Second, a timer is started at every input timestamp. The duration of this timer is dependent of the input. If the next input comes before the timer runs out, the timer is resetted and started again. If the timer runs out once, the Delay Generator outputs the timeout signal, which is repeated at every following input and the timer is not started again. The worst case run time for the calculation of the required delay must be independent of the input streams.

```
Output Stream Let S_{output} = (\mathbb{T} \cdot \{true_{until}, false\})^+ \cup (\mathbb{T} \cdot \{true_{until}, false\})^*
be the output stream of the monitor, which is defined via a function
g: S_{state} \times S_{output} \to S_{output}
which defines the output stream in an incremental fashion:
\forall t \in \mathbb{T} \exists S_{state}(t) \in \mathbb{D}_i:
S_{output}(t) = g(S_{state_{timeout}}(t), last(S_{output}, S_{state_{timeout}})(t)) The worst case run time of g is bounded independently of the input streams.
```

A monitor, which is Simple Monitorability With Delay, is not timestamp conservative anymore, because one new timestamp can be created. Because of this characteristic, the monitor cannot be described via (Timed) Deterministic Finite State Transducers. To solve this problem, a modification to TDFST, which allows ε -transitions, which are guarded by a clock constraint, but do not consume an input symbol to perform a state transition.

Definition 5 (Delay Generator). A Delay Generator is a 6-Tuple $(\Sigma, \Gamma, Q, q_0, C, \delta)$, where

- $Q = \{q_0, q_{timeout}\} \cup \{q_{wait,i} | \forall i \in \mathbb{D}_0\}$ is a finite set of states with initial state q_{start}
- $\Sigma = \mathbb{D}_{state}$ is an input alphabet
- $\Gamma = \mathbb{D}_{state} \cup \{timeout\}$ is an output alphabet
- $C = \{c\}$ is a set of exactly one clock and
- $\delta: Q \times (\Sigma \cup \{\varepsilon\}) \times \Theta(C) \to Q \times 2^C \times \Gamma$ a state transition function. δ is defined as:

```
\forall i \in \mathbb{D}_{state} : \delta(q_{start}, i, \emptyset) = (q_{wait,i}, \{c\}, i)
\forall i, i' \in \mathbb{D}_{state} : \delta(q_{wait,i'}, i, \{c < tmr(i')\}) = (q_{wait,i}, \{c\}, i)
\forall i \in \mathbb{D}_{state} : \delta(q_{wait,i}, \varepsilon, \{c < tmr(i)\}) = (q_{timeout}, \emptyset, timeout)
\forall i \in \mathbb{D}_{state} : \delta(q_{timeout}, i, \emptyset) = (q_{timeout}, \emptyset, timeout)
```

The definition of the *Delay Generator* is visualized in figure 3.2.2. On the left side is the initial state q_0 . The first input leads to a transition to the wait state of the corresponding input state. The clock c is resetted in this transition.

In the middle column of the figure are the wait states, one for each possible state of the monitor. $|\mathbb{D}_I| + 1$ transitions leave each wait state, one is the ε -transition introduced above, which is constrained in a way, that the value of clock c must be equal or greater than the corresponding delay time. This ε -transition leads to $q_{timeout}$ and outputs the timeout symbol. Every other transition leaving the waiting states are done at input symbols, while the value of clock c is less than the corresponding delay time. In these transitions, the input symbol d_i is used as output and clock c is resetted. In the output state, each input symbol leads to a repetition of the timeout symbol.

A monitor, which monitors a property that is *Simple Monitorability With Delay*, is equivalent to a combination of two DFSTs and a *Delay Generator*. The first DFST depicts, like before, the combination of state and state transition function. For this transducer, let

- $Q = \mathbb{D}_{state}$ be the finite set of possible states with initial state q_0
- $\Sigma = ((\mathbb{D}_1 \times \mathbb{T}), ..., (\mathbb{D}_n \times \mathbb{T}))$ be the input alphabet
- $\Gamma = \mathbb{D}_{state}$ be the output alphabet and
- $\delta: Q \times \Sigma \to Q \times \Gamma$ be the transition function.

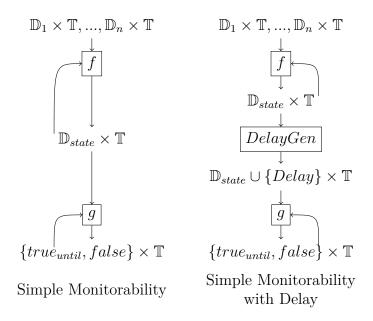


Figure 3.1: Overview Simple Monitorability - with or without delay

The output of this DFST is the input of the *Delay Generator* introduced above. The output of the *Delay Generator* is the input of the second DFST, which represents the output stream in combination with the output function, which is defined in the following way:

- $Q' = \{true_{until}, false\}$ are the states with initial state $true_{until}$
- $\Sigma' = (D_{state} \cup \{timeout\}) \times \mathbb{T}$ is the input alphabet
- $\Gamma' = \{true_{until}, false\}$ is the output alphabet and
- $\delta': Q' \times \Sigma' \to Q' \times \Gamma'$ is the transition function, where delta(q, (timeout, t)) = false for each possible q and t.

The output transducer is nearly the same as before, the difference is, that it additionally takes the timeout symbol as input and then returns false.

3.2.3 Not Simple Monitorable

Disproving one of the characteristics of *Simple Monitorability* does not necessarily mean, that a property of infinite streams can not be monitored with finite resources. For example, a property, where all parts of *Simple Monitorability* are fulfilled, except the worst case run time of the state transition function, which is dependent on the input streams, but the average run time of this function over every possible trace

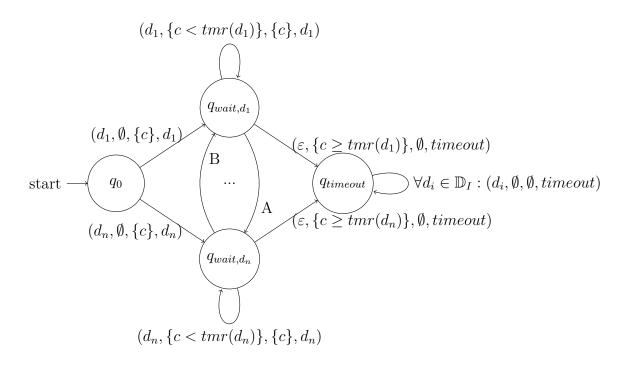


Figure 3.2: Visualization of the Delay Generator. Description A means $(d_n, \{c < tmr(d_1)\}, \{c\}, d_n)$ and description B means $(d_1, \{c < tmr(d_n)\}, \{c\}, d_1)$.

of this function is not². In these cases, a monitor with finite resources can be constructed, which can observe arbitrary long input traces.

If you can prove, that a limitation of the memory consumption, which is required to monitor a property correctly, cannot be given independently of the input streams and their events, it can be safely said, that a property cannot be monitored correctly on arbitrary input traces with finite resources. This is, because the memory of a computation system is always finite. If the required storage space is dependent on the input trace, a set of input streams can always be constructed, which requires an arbitrary large amount of storage space, which is larger than the available memory.

Not all TADL2 constraints are simple monitorable properties, even with delay, because they may require memory resources, which are not independent from the events of the observed trace. Like stated before, correct online monitoring of these constraints is impossible for arbitrary traces, because infinite memory resources may be required. On the other hand, many of these problems are solved by using finite resources, with the hope, that the available resources are enough to cover the inputs of the "real world". In these cases, a distinction is useful, because the memory or time requirements of some properties grow continuously with every input event, and

²In other words, the run time over a trace is linear dependent on the length of the trace

other constraints only require infinite resources in worst case scenarios. The ones with continuous requirement growth will be called *Always Not Simple Monitorable* and the others *Worst Case Not Simple Monitorable* for the rest of this thesis. Obviously, the constraints with continuous resource requirement growth cannot be monitored infinitely, but the constraints, that only need infinite resources in worst cases, can be monitored in many cases.

4 Analysis of the Monitorability of Timing Constraints

4.1 Monitorability of the TADL2 Timing Constraints

In this chapter, each of the TADL2 constraints will classified into the classes Simple Monitorable, Simple Monitorable with Delay and Not Simple Monitorable, like defined in chapter3. For the last class, it will be demonstrated, if the constraint is not simple monitorable in any cases or just in worst case scenarios.

4.1.1 DelayConstraint

The *DelayConstraint* is defined as

 $\forall x \in source : \exists y \in target : lower \leq y - x \leq upper.$

and describes that in the time interval between lower and upper after any source event, there is at least one target event. Therefore, the state that need to be stored to monitor the DelayConstraint is the set of source events, that are younger than upper and did not have a matching target event yet. If this information is not stored, the constraint cannot be monitored correctly. Updates to this state and output of the monitor are done at source and target events and at delay timestamps upper after the oldest stored source event.

The maximal required storage size of the state depends on the number of source events, which can possibly occur in any time interval of the length upper. An example of this worst case situation can be seen in figure 4.1. The attributes in this example are lower = upper = 5, source events occur in the timestamps $\{1, 1.1, ..., 5.9\}$ and target events in the timestamps $\{6, 6.1, ..., 11\}$. At timestamp 6, all 49 source events must be stored, because they are all required to generate the correct output in this and in following timestamps. At this timestamp, the oldest source event can be removed from the storage, because the matching target event occurs in this timestamp. Other timestamps cannot be removed from the storage, because they are younger than lower. With every following target event, the oldest event can be removed from the storage, until every source had its matching target event at

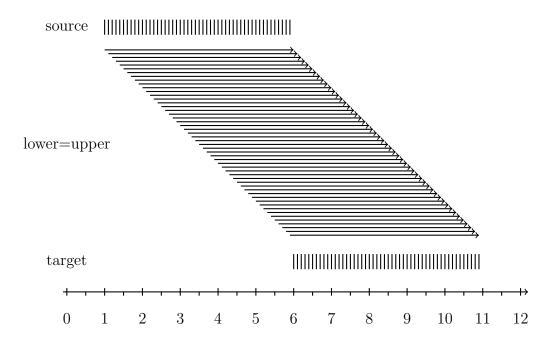


Figure 4.1: DelayConstraint or StrongDelayConstraint with lower = upper = 5

timestamp 11.

Because the time domain is understood as real numbers in TADL2, a possibly infinite number of events can be placed in any interval of the length *upper*. Which means that the required storage space can grow infinitely, therefore, the worst case memory requirement is dependent of the events in the trace. Consecutively, the *DelayConstraint* is not *simple monitorable*.

Because the *source* events are removed from the state, when a matching *target* event occurs, the required storage space does not grow continuously and infinite resources are only required in worst case scenarios. Therefore, the *DelayConstraint* is *worst case not simple monitorable*.

4.1.2 StrongDelayConstraint

The difference between the *DelayConstraint* and the *StrongDelayConstraint* is that for every *source* event, there must be exactly one matching *target* event in the *StrongDelayConstraint*. Therefore, the state of the monitor is nearly the same. Like before, all *source* events, that did not have a matching *target* event yet, must be stored, but at matching *target* events, only one *source* event can be removed from the storage. The worst case memory requirement remains unchanged and is still dependent of the number and the placement of the input events, therefore the *StrongDelayConstraint* is *worst case not simple monitorable*.

4.1.3 RepeatConstraint

The RepeatConstraint defines the time distance between each event and its $span^{th}$ successor. Therefore, the state, that must be stored for monitoring, consists of the timestamps of the span + 1 latest events. The state is updated at every event, the oldest stored event is removed and the timestamp of the current event is placed in the storage. The output function checks, if the time distance between the oldest stored event and the current timestamp is between lower and upper. To monitor this constraint, a single delay is required, because a missing event, or an event that occurs too late, would not be determined in the right timestamp otherwise. The delay offset can be calculated by the time distance between the current timestamp and the timestamp, that lays upper behind the oldest stores event.

As the memory requirements are fix (span + 1 timestamps must be stored) and the state transition and output function can be programmed in a way that they are in $\mathcal{O}(1)$ (e.g. if linked lists are used), the RepeatConstraint is $simple\ monitorable\ with\ delay$.

4.1.4 RepetitionConstraint

The RepetitionConstraint is defined as

```
RepetitionConstraint(s, lower, upper, span, jitter)

\equiv \exists X \subset \mathbb{T} : RepeatConstraint(X, lower, upper, span)

\land StrongDelayConstraint(X, s, 0, jitter)
```

The elements of the set X follow the RepeatConstraint and the events, which should be monitored, are following in an interval of the length jitter after the elements of X. For each element of X, there is exactly one event in s and vice versa.

The monitoring algorithm for this constraint, which will be explained in detail in 5, stores the upper and lower bounds for the next span elements of X. These borders are stored in a list and calculated by

```
lowerBound := List\_append(last(List\_tail(LowerBound), s), lowerBoundNow + lower) \ for the lower bound and \\ upperBound := List\_append(last(List\_tail(UpperBound), s), upperBoundNow + upper).
```

The oldest item in these lists (the head of these lists) are removed and the newly calculated bounds for the span next element of X is inserted at the lists end. lowerBoundNow and upperBoundNow are the describing the limitations of the element of X right before the current event. They are calculated using the list mentioned above and the timestamp of the current event by the following definition:

```
lowerBoundNow := max(List\_head(last(LowerBoundX, s)), time(s) - jitter)
upperBoundNow := min(List\_head(last(UpperBoundX, s)), time(s))
```

If the timestamp of the current event is between lowerBoundNow and upperBoundNow, the output of the monitor is true, in any other case, or when the delay ran out, it is false.

The size of these lists has a fixed upper limit (span) and the state transition and output functions are in $\mathcal{O}(1)$, therefore they are independent from the trace and the RepetitionConstraint is a property, which is simple monitorable with delay.

4.1.5 SynchronizationConstraint

The Synchronization Constraint describe groups of streams, which events occur in common clusters. Each of these streams must have at least one event in each of these intervals. Any events, that lay outside of these intervals are prohibited. Figure 4.2, which is similar to the example for the Delay Constraint, shows an example of this constraint, which is an worst case scenario in terms of monitoring. The tolerance interval is 5 timestamps long, the event set s_1 contains the events $\{1, 1.1, ..., 5.9\}$ and s_2 is containing $\{6, 6.1, ..., 11\}$. Each of the events of s_1 must be stored until the end of the tolerance interval, otherwise it would be impossible to check the constraint correctly. Like described in section 4.1.1, an arbitrary number of events can be placed in this interval and the resource requirements per input timestamp are dependent of the input streams. The required storage space is not growing continuously, because the stored events can be removed at the end of the tolerance interval, the Synchronization Constraint is worst case not simple monitorable.

It should be noted, that the illustration of the constraint in figure 4.2 may be misleading, because the *tolerance* intervals are only shown after the events of s_1 , not after the events of s_2 . Every implementation of a monitor for this constraint must also store the events of s_2 for the length of *tolerance*, as they could be important for events following after them.

4.1.6 StrongSynchronizationConstraint

The difference between the *StrongSynchronizationConstraint* and the *SynchronizationConstraint* is, that in the StrongSynchronizationConstraint, only one event per stream is allowed in each synchronization cluster. Therefore, this constraint can be classified as *worst case not simple monitorable* with the same argumentation as the previous constraint.

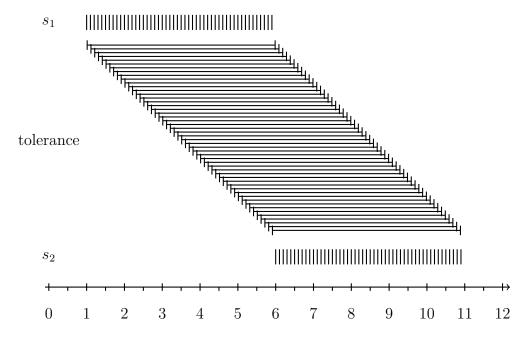


Figure 4.2: SynchronizationConstraint or StrongSynchronizationConstraint with tolerance = 5

4.1.7 ExecutionTimeConstraint

The Execution Time Constraint ensures that the time distance between stop and start events, not counting interruptions (which are specified by preempt and resume events) is between lower and upper.

Under the assumption that the input events are in logical order (every execution is started by an *start* event and finished by an *stop* event, every *preempt* event is followed by an *resume* event with no other event in between and no *preempt* or *resume* events occur outside of the intervals spanned by *start* and *stop* events), three time values must be stored to monitor this constraint. First, the timestamp of the latest *start* event. Second, the timestamp of the latest *preempt* event and third, the sum of the time distances between the *resume* and *preempt* events. This sum is reseted at every *start* event.

These values are updated on events in *start*, *stop* or *preempt*.

For the output function, the run time can be calculated by

runtime = time(now) - time(start) - (sum(time(resume) - time(preempt)).

At any event, this value must smaller or equal to *upper* and at events in *stop*, additionally the runtime must be greater or equal to *lower*.

To monitor this constraint correctly, a delay is required, when a *stop* event is late or missing. The delay duration is the distance between the current timestamp and *upper* minus *runtime* behind the current timestamp.

The required storage space is fixed (remind, that we limited the memory size of timestamps in 3.2), also the runtime of the state transition and output function can be implemented with constant run time, consecutively the *Execution Time Constraint* is *simple monitorable with delay*.

4.1.8 OrderConstraint

The OrderConstraint describes, that an i^{th} target event must exist, if an i^{th} source event exists and that the i^{th} target event occurs after the i^{th} source event. In a finite setting, it must also be checked that the number of source and target events is equal in the end of the observation. Because it is possible that an arbitrary large number of source events occur before the first target occurs, a possibly arbitrary large number must be stored, and the required storage space is dependent on the input streams. Because this is only a worst case scenario and the size of the stored number can be decreased, when a target event occurs, the OrderConstraint is worst case not simple monitorable.

4.1.9 ComparisonConstraint

The Comparison Constraint defines an ordering relation between two single events and does not describe relations of streams or their events. Therefore, the definition of $simple\ monitorability$ is not applicable. But because of the restrictions to timestamps made in 3.2, the maximal required storage space and the run time of the operators \leq , <, >, = have a fixed upper limit.

4.1.10 SporadicConstraint

The *SporadicConstraint* is defined via the *Repetition*- and *RepeatConstraint* without introducing any new timestamps in the definition of the *SporadicConstraint*. These Constraints are *simple monitorable with delay*, therefore the *SporadicConstraint* is also *simple monitorable with delay*.

4.1.11 PeriodicConstraint

The *PeriodicConstraint* is special application of the *SporadicConstraint*, therefore it is also *simple monitorable with delay*.

4.1.12 PatternConstraint

The PatternConstraint was redefined to

```
\exists X: PeriodicConstraint(X, period, 0, 0) \\ \land \forall i: StrongDelayContraint(X, event, offset_i, offset_i + jitter) \\ \land RepeatConstraint(event, minimum, \infty, 1)
```

in section 2.2.2. The input events occur after the strictly periodic timestamps of X. The distances between the elements of X and the following events is defined by offset.

This constraint can be monitored by storing upper and lower limits of the current latest element of X and the number of event occurrences, reset to 0 at every $|offset|^{th}$ event. The limits of the elements of X can be narrowed down at every event occurrence, because the valid distance between the event and the element of X is known by offset and jitter. At every $|offset|^{th}$ event occurrence, the limitations of the current X must be increased by period. The validity of the constraint can be tested by checking, that the current event has the correct distance to the limitations of the current latest element of X. To be able to recognize late or missing events, a delay is required. The timestamp, where the delay must occur, can be calculated by adding jitter and the entry of offset for the next expected event to the current upper limit of latest X.

Because the memory requirements (two timestamps and an integer) are constant and the mentioned state transition, delay calculation and evaluation functions can be implemented in constant time, the *PatternConstraint* is *simple monitorable with delay*.

If the redefinition of the *PatternConstraint* is not done, the constraint can be reduced to

 $RepeatConstraint(event, minimum, \infty, 1)$

like stated before in section 2.2.2. Because the RepeatConstraint is simple monitorable with delay and the upper parameter is ∞ , the constraint is simple monitorable (without delay) in this variant.

4.1.13 ArbitraryConstraint

The Arbitrary Constraint is defined as combination of the Repeat Constraint:

 $ArbitraryConstraint(event, minimum_1, ..., minimum_n, maximum_1, ..., maximum_n)$ $\Leftrightarrow \forall i \in 1, ..., n : RepeatConstraint(event, minimum_i, maximum_i, i).$ The RepeatConstraint is simple monitorable with delay, therefore the ArbitraryConstraint is also simple monitorable with delay.

4.1.14 BurstConstraint

The BurstConstraint is defined as combination of the RepeatConstraint:

```
RepeatConstraint(event, length, \infty, maxOccurrences) \land RepeatConstraint(event, minimum, \infty, 1)
```

The RepeatConstraint is simple monitorable with delay. The upper parameter in both application of the RepeatConstraint is ∞ , therefore the timeout always occurs infinite timestamps after the latest input events, which means, the timeout is dispensable and the BurstConstraint can be monitored without any delay or timeout operator. Consecutively, the BurstConstraint is a simple monitorable property.

4.1.15 EventChains

The ReactionConstraint and the following Constraints are defined on EventChains, which are defined as stimulus and response stream. Each event of these streams has a color attribute, which describes the causal connection of individual events. It is required, that any stimulus event of a specific color must occur before the first response event with the same color. The datatype of this attribute is not specified, except that it may be infinite and an equality test must exist.

Monitoring this property is difficult, because it is required to store every color which has occurred in *response*. The reason for this can be seen in figure 4.3. In the interval between the timestamps 1 and 2, there are 5 events of different colors in *stimulus*. Their counterparts in *response* occur in the interval between 4 and 5. In timestamp 6, there is an event in *response* with of the color black. After that, not black is allowed in *stimulus*. To check this properly for all colors, the color of all events, which occurred in *response* must be stored until the end of the observation.

The memory consumption to monitor this property is growing continuously with any event that introduces a new color in *response*, therefore the correctness of *EventChains* is a *always not simple monitorable* property.

4.1.16 ReactionConstraint

If we assume the correctness of the *EventChains*, a monitor would be similar to a monitor of the *DelayConstraint*. The only difference is that the color attribute of

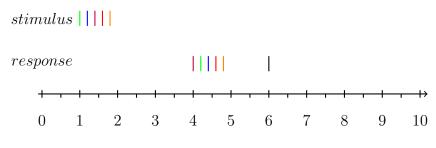


Figure 4.3: Event Chain example

the stored *stimulus* events must also be stored. Removing events from the storage is only allowed, when the time distance and the color between the *stimulus* and *response* events is correct. Like for the *DelayConstraint*, the required worst case storage space is dependent on the input streams, therefore the *ReactionConstraint* is *worst case not simple monitorable*, if the correctness of the *EventChain* is assumed.

4.1.17 AgeConstraint

Similar to the analysis of the *ReactionConstraint*, we assume the correctness of the *EventChain*.

The AgeConstraint is very similar to the ReactionConstraint, the main difference is, that every response event requires a source event in a matching color in the right distance, not the other way around. Because the response events always occur after the source event in the same color, no delay is required, but the number of events in stimulus, that must be stored in worst cases, remains the same as in the ReactionConstraint. Therefore, the AgeConstraint is worst case not simple monitorable, if the correctness of the EventChain is assumed.

4.1.18 OutputSynchronizationConstraint

Again, the correctness of the *EventChain* is assumed in the analysis.

The definition of the OutputSynchronizationConstraint does not limit the time distance between stimulus events and their associated synchronization clusters in the response streams. If we only consider infinite streams, a missing synchronization cluster cannot make the constraint unsatisfied, therefore, only the correctness of these clusters may be false and lead to a negative output. The correctness of these synchronization clusters is not simple monitorable, which is argued the same way as in the simple SynchronizationConstraint. An arbitrary large number of new synchronization clusters can be placed in a time interval with the length tolerance, which has to be stored until the all response streams have fulfilled this cluster. A

key different to the *SynchronizationConstraint* is that only the first occurrences of each color must form a synchronization cluster. After this cluster, events of this color may occur independently. Because of this characteristic, the color of any finished synchronization cluster must be stored for the entire rest of the observation, which means, the *OutputSynchronizationConstraint* is a *always not simple monitorable* property.

If finite streams are considered, the color of all *stimulus* events must be stored, until the matching synchronization cluster occurs. At the end of the observation, it must be checked, if there was a synchronization cluster for all colors, which occurred in *stimulus*.

4.1.19 InputSynchronizationConstraint

Like before, the correctness of the *EventChains* is assumed.

In the *InputSynchronizationConstraint*, synchronization clusters in the *stimulus* streams must only be fulfilled, if the associated events are the last of their color in their streams before an associated *response* event. This means, at least some information for every color, which occurred in the *stimulus* streams, must be stored, until the *response* color with the same color. Because several *response* events of this color may occur, the information about a fulfilled or unfulfilled synchronization cluster may not be removed from the storage. Otherwise it could not be checked, if there was a synchronization cluster with a matching color. Consecutively, the required storage space grows continuously with every new stimulus color and the constraint is *always not simple monitorable*.

4.2 Conclusion

Figure 4.4 gives an overview, which TADL2 timing constraints are simple monitorable and which are not. The ComparisonConstraint is not defined on streams, therefore the definition of simple Monitorability is not applicable. All simple monitorable constraints, except the BurstConstraint require the creation of new timestamps. The other constraints are not simple monitorable, of which the Input- and OutputSynchronizationConstraint are always not simple monitorable. If the correct order of the EventChains is assumed, the Reaction- and AgeConstraint are only not simple monitorable in worst cases, like the other not simple monitorable constraints. The arrows show, which constraint is defined via other constraints, for example the RepetitionConstraint is defined via the StrongDelay- and RepeatConstraint. It should be noted that constraints, which are defined via not simple monitorable constraints,

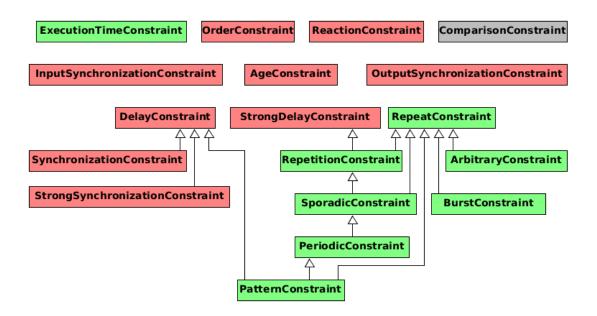


Figure 4.4: Overview over constraints - Simple Monitorable - Not Simple Monitorable

can be simple monitorable, because of further restrictions, which limit the required storage space or runtime.

5 Implementation

5.1 Implementation Of The TADL2 Constraints

In this chapter, the implementation of the monitor of each constraint will be explained. This is done by giving a short documentation of each monitor is given. Additionally, the worst case memory usage and the worst case and average run time per event is determined. In section 5.1.21, each monitor is run on traces, which were generated to match the constraints with specific parameters, to evaluate which performance can be expected in a practical usage of the implementation.

All implementations have in common that they consist of 2 or 3 sections, similar to the state transition, delay (if needed) and output as defined in chapter 3. These sections are the basis for the analysis of the computational complexity, because the generated state defines the required memory capacity and the state transition function, the output function and the calculation of the required delay define the required time per timestamp with input events.

The implementations are programmed and tested for version 1.0.12 of the TeSSLa JAR archive.

5.1.1 DelayConstraint

The implementation of the *DelayConstraint* monitor stores a list of *source* events, which did not have a matching *target* event yet as state. This list is expanded by every *source* event, which is appended at the end of the list. If a *target* event occurs, all matching *source* events (possibly none) are removed from the list. Like stated in section 4.1.1, this list can grow infinitely in worst cases, when the time domain defined in an uncountable way. In these worst cases, an infinite number of *source* events may occur, before any event can be removed from the list, when a matching *target* event occurs.

The used TeSSLa version is using integer values as time domain, therefore it is countable and the list cannot grow infinitely, because at most $upper\ stimulus$ events need to be stored and the largest possible length of the list is linear dependent of the parameter upper. Because this list is the only growable memory usage, the algorithm is in $\mathcal{O}(upper)$ in terms of memory.

In timestamps with a target event, all events in the list, which are in the right

time distance, are removed from the list. This means that in worst cases, all events in the list must be checked and removed, which means, the worst case run time of the state transition is linear dependent of the length of the list and therefore is $\mathcal{O}(upper)$. The output function checks, if the updated list of unmatched source events is either empty or the event in the head of the updated list is not older than upper. Therefore, it is in $\mathcal{O}(1)$.

The required delay period is calculated by adding *upper* to the timestamp of the head of the list of unmatched *source* events, subtracted by the timestamp of the current event $(\mathcal{O}(1))$.

5.1.2 StrongDelayConstraint

The StrongDelayConstraint is implemented very similarly to the DelayConstraint. The only difference in the state transition is that exactly one event, which is the head of the list of unmatched source events, is removed, when a matching target event occurs. Therefore, the maximal memory usage is the same $(\mathcal{O}(upper))$, but the run time of the state transition is constant per input timestamp. In addition to the DelayConstraint, the output function of this constraint checks, if each target event occurrence has exactly one matching source event (which always is in the head of the list). Therefore, it is still in $\mathcal{O}(1)$. The calculation of the delay period remains unchanged.

5.1.3 RepeatConstraint

The implementation of the RepeatConstraint stores the timestamps of the span previous events as state, using TeSSLa's last operator recursively (a macro called nLastTime was programmed for this). Therefore, span timestamps are stored and the last operator is called span times, which means the state transition function is linear dependent of span in terms of time and the memory usage is likewise.

The required delay is calculated by adding upper to the $span^{th}$ oldest event (or the first event, if there hasn't been span events before) minus the current timestamp, therefore, the time for the calculation is linear dependent on the span parameter, because the entire recursive definition of the state mentioned above must be walked trough.

The output function checks, if the $span^{th}$ oldest event is not older than upper and not younger than lower. If there hasn't been span events before, it is checked, if the first event is not older than upper. Like in the calculation of the required delay, the entire recursive definition of the considered for the evaluation. Therefore, the output function is in $\mathcal{O}(span)$.

5.1.4 RepetitionConstraint

The RepetitionConstraint is defined as

```
RepetitionConstraint(s, lower, upper, span, jitter)

\equiv \exists X \subset \mathbb{T} : RepeatConstraint(X, lower, upper, span)

\land StrongDelayConstraint(X, s, 0, jitter)
```

The implementations of the Repeat- and the StrongDelayConstraint cannot be used for the implementation of this constraint, because the timestamps of X are unknown. Relevant for the monitoring are the upper and lower bounds of the elements of X, which precede the actual events in the event stream s. The bounds are stored as two lists with the length of span. One list is containing the lower bounds for the next span X, the other list is containing the upper bounds. At every input event, the new boundaries for the $span^{th}$ next X are calculated, the lower bound by $max(List_head(last(LowerBoundX, e)), time(e) - jitter)$ and the upper bound by $min(List_head(last(UpperBoundX, e)), time(e))$. These new boundaries are appended to the end of the lists, while the oldest entries in the head of the lists are removed. These two lists with the size of span are the only storage, which size is dependent on the input, therefore the algorithm is in $\mathcal{O}(span)$ in terms of memory. The run time of the state transition function is constant (removing the lists head and appending an entry to the lists).

The output function checks, if the current timestamp is between the lower bound for the current timestamp of X and jitter behind the upper bound for that value. If this is the case, the output is true, in any other case, it is false. Because the upper and lower bound for the current X value can be directly accessed (they are the head of the lists), the output function is in $\mathcal{O}(1)$.

5.1.5 SynchronizationConstraint

The Synchronization Constraint is defined via an application of the Delay Constraint, but the application uses a set of unknown timestamps ($\exists X:...$), therefore the Delay Constraint cannot be used for the implementation of this constraint. Because TeSSLa does not allow to define macros or functions with a variable number of input streams, events of each input timestamp must be placed into an integer list, which contains the index (starting at 1) of all streams, which have an event in this timestamp. This is list then used as a parameter to the implementation. The creation of this list is already implemented for up to 10 streams.

The implementation of the *SynchronizationConstraint* stores all events that occurred not longer than *tolerance* ago in a list. In each entry, this list contains the stream, in which the event occurred, the timestamp of the event occurrence and a boolean

variable, that expresses if a fulfilled synchronization cluster for this event has already been found.

This list is updated in every input timestamp in three steps. First, each event occurrences in this timestamp is appended to this list. Second, the list is separated into two parts, one with events older and one with events younger than tolerance. The part of old events is still stored in this timestamp, but removed after it. The younger events form the state that is stored for the next event occurrences. Third it is checked, if at least one event of every stream is part of the list of younger events. In this case, a fulfilled synchronization cluster has been found and the boolean variable, that states if a synchronization cluster is found for this event, is set to true for all events in this list.

Similar to the DelayConstraint, this list can grow infinitely, when the time domain is uncountable, which is not the case in the used TeSSLa version. Because the TeSSLa uses integers as time domain, at most $|event|^1 * tolerance$ events can occur in the tolerance interval. Therefore, the algorithm is in $\mathcal{O}(|event| * tolerance)$ in terms of memory. The first step of the state transition is in $\mathcal{O}(|event| * tolerance)$, because at most |event| events must be appended to the list and the list has the maximum length tolerance. In worst cases, every event in the list(which is in ascending order) is older than tolerance, therefore the worst case runtime of the separation in the second step of the state transition is in $\mathcal{O}(|event| * tolerance)$ in terms of time. In the third step, the complete stored list of young events must be examined, to check if the cluster is fulfilled and, if needed, every event in the list must be set to fulfilled. Therefore the third step is in $\mathcal{O}(|event| * tolerance)$ in terms of time.

The output function checks, if the boolean variable of each event in the list of events, which are older than tolerance, is set to true. If not, the constraint is not fulfilled. Because this list can have the size |event| * tolerance, the output function also is in $\mathcal{O}(|event| * tolerance)$ in terms of time.

The required delay is calculated by adding tolerance to the timestamp of the oldest stored unsatisfied event, subtracted by the timestamp of the current timestamp. The list is in ascending order, but the only unsatisfied events are relevant for the delay, which means, the entire list must be checked in worst cases. Therefore, the calculation of the required delay is in $\mathcal{O}(|event| * tolerance)$.

5.1.6 StrongSynchronizationConstraint

The StrongSynchronizationConstraint is defined as application of the StrongDelay-Constraint, but this application cannot be used for the implementation, like in the previous constraint. Similar to the SynchronizationConstraint, the events of the input streams must be merged into list.

¹|event| is the number of streams, not the number of events.

The difference between the *Synchronization*- and the *StrongSynchronizationConstraint* is, that each event can only be part of one synchronization cluster in the *StrongSynchronizationConstraint*. Therefore, the implementation is different to the implementation of the previous constraint. Not every event is stored separately, only information about synchronization clusters, containing their start time and in which stream an event occurred in this cluster, are stored.

The information about synchronization clusters are stored in a list, which contains a time expression, which marks the starting point and a map, containing a boolean variable for every input stream, which shows, if there already was an event in this stream for this cluster. At event occurrences, the event is either added to one existing synchronization cluster, or a new cluster with the start time of the event is added to the list. For the search of a matching cluster, each event of the list is considered in worst cases, therefore the run time of this part of the state transition is linear to the number of active clusters. In worst cases this number is tolerance, when one event occurs in every timestamp in always the same stream. In a second step, every stored cluster is checked, if it is fulfilled. If so, it is removed from the list. To check, if a cluster is fulfilled, one boolean check must be done for every input stream, therefore at most boolean tolerance * |event| checks must be done and the worst case run time of the state transition is in $\mathcal{O}(tolerance * |event|)$. When the events occur in separated synchronization clusters, the list is significantly shorter than tolerance and the run time may be expected to be linear to the number of input streams.

The list storing the clusters is at most *tolerance* long and the size of individual entries of the list is linear dependent on the number of streams, because they store a boolean variable for every stream. Because of these length restrictions of the list, the algorithm is in $\mathcal{O}(|event| * tolerance)$ in terms of memory.

The output function checks, if the oldest stored (therefore unfulfilled) cluster is older than tolerance. This cluster is in the head of the list, therefore the output function is in $\mathcal{O}(1)$ in terms of time. The required delay is calculated by adding tolerance to the timestamp of the oldest stored unsatisfied cluster, subtracted by the timestamp of the current timestamp ($\mathcal{O}(1)$).

5.1.7 ExecutionTimeConstraint

The implementation of the *ExecutionTimeConstraint* is using TeSSLa's *runtime* operator on the *start* and *stop* events, which calculates the absolute runtime without any interruptions. The time of interruptions is also calculated by the calculated by this operator and then summed up. The sum of these interruptions is reseted by every *start* event. The calculation of this sum with resets, a macro called *resetSum* was programmed, which is a modified version of TeSSLas *ResetCount* function.

TeSSLa's runtime operator subtracts the timestamps of the events of the second

parameter (in this case *stop* and *resume*) from the timestamps of the events of the first parameter(*start* and *preempt*), therefore it stores the timestamps of the *start* and *preempt* events are stored, additionally to the sum the preemptions. For the output, the runtime can be calculated by subtracting the second application (with *preempt* and *resumse* as parameters) of TeSSLa's *runtime* operator from the sum of the first applications (with *start* and *stop* as parameters) of this operator. If the runtime should be checked in timestamps without a *stop* event, the second parameter of the first application of the *runtime* operator must be replaced by a current event. In the implementation this is done by merging all include streams and the delay stream.

The resulting runtime must be smaller or equal to *upper* in any point of time and greater or equal to *lower* at *stop* events. The required delay is calculated subtracting the runtime so far from upper. All of these operations are simple arithmetic functions on timestamps, therefore the algorithm is in $\mathcal{O}(1)$ in terms of time. The required storage space is fixed, therefore it is also in $\mathcal{O}(1)$ in terms of memory.

5.1.8 OrderConstraint

The OrderConstraint is defined in a way, so that the number of events on the source stream is equal to the number of events on the target stream and that the i^{th} source event occurs before the i^{th} target event. The first described property can only be checked, when it is known that no further events will occur. In TeSSLa, this is generally unknown, therefore the implementation has a third input stream, which requires to have exactly one event at the end of the observation.

The implementation counts the number of events on the source and target stream and checks, if the number of source events is larger or equal to the number of target events. In the end of the streams, the number of events on both streams must be equal. Therefore, the stored state consists of two integers and the algorithm is in $\mathcal{O}(1)$ in terms of memory. The incrementations of these counters and the comparison between them are simple arithmetic operations, therefore the state transition and the output function are both in $\mathcal{O}(1)$ in terms of time. The introduction of new timestamps is not required for this constraint, except the one defining the end of the observation, therefore no delay period must be calculated.

5.1.9 ComparisonConstraint

The ComparisonConstraint defines comparisons between timestamps. These functionalities are already defined in TeSSLa, therefore no implementation is given as part of this thesis.

5.1.10 SporadicConstraint

The SporadicConstraint is defined as simple application of the Repetition- and the RepeatConstraint, therefore the SporadicConstraint is also implemented as application of them. The implementations of the Repetition- and the RepeatConstraint are both in $\mathcal{O}(span)$ in terms of time and memory. Because span is fixed to 1 in the SporadicConstraint, the implementation is in $\mathcal{O}(1)$ in terms of memory and time.

5.1.11 PeriodicConstraint

The PeriodicConstraint is defined as application of the SporadicConstraint and is also implemented like this. Because the SporadicConstraint is in $\mathcal{O}(1)$ in terms of memory and time, the PeriodicConstraint is also.

5.1.12 PatternConstraint

The PatternConstraint is defined as application of the Periodic-, Delay- and Re-peatConstraint. Because of the set of unknown timestamps X, the Periodic- and DelayConstraint cannot be used for the implementation. The set X is not used in the application of the RepeatConstraint, therefore its implementation is used as part of the output function.

The implementation of the RepeatConstraint is in $\mathcal{O}(span)$ in terms of time memory. The span attribute is set to 1 in the application, therefore the run time and memory usage is constant in this part.

In the implementation of the PatternConstraint, the lower and upper bound for the current timestamp of X is stored. At every event, these bounds are further enclosed, taking the previous known bounds and the bounds implied by the current event

$$x \in X : time(event) - offset_{count(event) \mod |offset|} - jitter \le x$$

 $\le time(event) - offset_{count(event) \mod |offset|}$

into account. The new lower bound is set by using the maximum of the previous lower bound and the lower bound implied by the current event, the new upper bound by using the minimum of the previous upper bound and the upper bound implied by the current event. At every $|offset|^{th}$ event, period is added to the current bounds. The output function checks, if the timestamp of the current event is between the lower bound $+ offset_{count(event) \mod |offset|}$ and the upper bound plus $offset_{count(event) \mod |offset|}$ plus jitter. The access of the map entries is done in constant time, therefore the calculation of these new borders is done in constant time, and the state transition function in $\mathcal{O}(1)$ in terms of time.

The required delay is defined by the time distance between the current timestamp and the upper bound for X, plus the allowed offset of the following event, plus the allows deviation (*jitter*).

The only state stored in the implementation are the upper and lower bound for the current x-value, therefore the implementation itself is in $\mathcal{O}(1)$ in terms of memory, but the size of the *offset*-parameter, which is a map, is not limited in size and the complete algorithm, including the parameters, is $\mathcal{O}(|offset|)$ in terms of memory.

5.1.13 ArbitraryConstraint

The Arbitrary Constraint is defined as multiple applications of the Repeat Constraint and is also implemented this way. The number of applications of the Repeat Constraint is dependent on the number of elements in the minimum and maximum parameters. The runtime of the Repeat Constraint is in $\mathcal{O}(1)$ per application and event, therefore it the Arbitrary Constraint is in $\mathcal{O}(|minimum|)$ in terms of time. The memory usage of the Repeat Constraint is in $\mathcal{O}(span)$. In the application of the Repeat-Constraint, the span parameter increases for each of the |minimum| = |maximum| applications. Therefore, the implementation is in $\mathcal{O}(\sum_{i=1}^{|minimum|} i) = \mathcal{O}(|minimum|^2 + |minimum|)$ in terms of time.

5.1.14 BurstConstraint

The BurstConstraint is defined as twofold application of the RepeatConstraint and is also implemented this way. The RepeatConstraint is in $\mathcal{O}(span)$ in terms of time and memory. Because the span attribute is set to 1 and maxOccurrences in the applications of the RepeatConstraint, the implementation of the BurstConstraint is in $\mathcal{O}(maxOccurrences)$ in terms of memory and time.

5.1.15 ReactionConstraint

The correctness of the *EventChain* is assumed in the implementation. If this property is unknown, it must be checked individually.

The implementation of the Reaction Costraint stores a map, which maps the color of stimulus events, which did not have a matching response event yet, to their timestamp. This state is updated at every input event. Stimulus events are inserted into the map, response events remove, if possible, a event from the map called above. Similar to the Delay Constraint (the Reaction Costraint is an extension of the Delay Constraint, that additionally considers the color of events), the maximal number of entries in the map is the maximal number of stimulus events, that could possibly

occur in an interval of the length maximum, which is maximum. Therefore, the algorithm is in $\mathcal{O}(maximum)$ in terms of memory. The state transition (insertion, lookup and possibly remove in map) is effectively in $\mathcal{O}(1)$ in terms of time.

The required delay is calculated by adding maximum to the timestamp of the oldest entry in the map mentioned above, and subtracting the current timestamp. Because the map is unsorted, every entry of the map must be considered for this. Therefore, the calculation of the required delay is in the time complexity class $\mathcal{O}(maximum)$. The output function checks, if the oldest entry in the map is not older than maximum. The run time of this operation is linear in the size of the map, which is at most maximum. Like the calculation of the required delay, the evaluation function is in $\mathcal{O}(maximum)$ in terms of time.

5.1.16 AgeConstraint

Like before, the correctness of the *EventChain* is assumed in the implementation. If this property is unknown, it must be checked individually.

Similar to the implementation of the Reaction Costraint, the Age Constraint monitor stores a map containing the latest stimulus event, which are younger than maximum. The color value is used as key and the timestamp is used as map value. This map has the maximal size maximum and is updated at every input event. Stimulus events are inserted or updated, and entries, that are older than maximum are removed. To make this update faster, a list containing the colors of the events in the map is stored additionally. The maximal size of this list is also maximum and the colors are stored in chronological order, so that the color, that occurred the longest time ago, is in the head of the list. The update is done by looking at the head of the list and removing this entry from the list and the corresponding entry with the same color from the map, if the entry is older than maximum. These operations are done in constant time, but has to be repeated, as long as the color in the head of the map is too old, so at most maximum times. Inserting or updating the stimulus event to the map is done in effectively constant time, but inserting or updating the list requires to remove any previous entry with the color of the current event. For this, every entry in the map has to be processed, which means this operation takes maximum steps in worst cases. Consecutively, the state and the state transition is in $\mathcal{O}(maximum)$ in terms of memory and time. The creation of new timestamps is not needed in this constraint, because only previous events need to be considered, upcoming events not.

In timestamps containing a *response* event, the output function checks, if a *stimulus* event with the same color is in the map and if the time distance between them is greater or equal to *minimum* and smaller or equal to *maximum*. The lookup in the map and the comparisons are done in effectively constant time.

5.1.17 OutputSynchronizationConstraint

Similar to the Synchronization Constraint and Strong Synchronization Constraint, the input streams cannot be directly used as parameter. For the Output Synchronization Constraint, a stream of maps must be created, which represents the events of each timestamp. The key of the entries is the index of the stream (0 for the stimulus stream, 1, 2, ... for the response streams) and the value the color of the event. Again, the creation of this map is already implemented for up to 10 response streams.

In the OutputSynchronizationConstraint, for each stimulus event, there must be one synchronization cluster of the length tolerance, in which each response stream must have at least one event of the same color as the stimulus event. There is no time distance between the cluster and the stimulus event defined, it just has to be before the end of the streams. Therefore, a additional event, which shows the end of the observation, is needed, similar to the OrderConstraint.

The implementation of the OutputSynchronizationConstraint is storing four different informations as state. First, a list of every color that occurred in stimulus. This is updated at every stimulus event by appending its color to the list(run time: $\mathcal{O}(1)$, memory: $\mathcal{O}(count(stimulus))$).

Second, a map containing information about all synchronization clusters, that were not finished until this point in time is stored. This map is using the color attribute as key and the start time stamp and a map as value. This inner map contains a boolean variable for each response stream, which shows, whether there was an event for this synchronization cluster in this stream or not. This map is updated at every response event. For each of these response events, it is checked, if a synchronization cluster with a matching color exists, if not a new synchronization cluster with the color of the event is created. The check per event (two lookups in maps) is done in constant time, therefore this update is in $\mathcal{O}(|response|)$ in terms of time per input timestamp. In worst cases, each event results in the creation of a new synchronization cluster, which must be stored at least for the length of tolerance. The size of each information about one synchronization cluster is linear dependent on the number of response streams and in each interval of the length tolerance, tolerance * |response| events can occur and create a new synchronization cluster, therefore this information is in $\mathcal{O}(tolerance * |response|^2)$ in terms of memory. The third stored information is similar to the second, but the clusters, that either older than tolerance or fulfilled are removed from the map. Therefore, the worst case memory consumption is the also $\mathcal{O}(tolerance * |response|^2)$. To remove fulfilled clusters, it is checked for each cluster in the map, if there was at least one event in each response stream of the color of the cluster. Therefore, this update is in $\mathcal{O}(tolerance * |response|^2)$ in terms of time. The fourth stored information is a set of all colors that had a fulfilled synchronization cluster in the response streams until this point in time. Inserting items into the set is done in constant time. The number of fulfilled synchronization clusters is at most the number events in all response streams, divided by the number of the response streams. Therefore, the required memory of this information is in $\mathcal{O}\left(\frac{\sum_{i} count(response_{i})}{|response|}\right)$, the runtime for updating this information is likewise.

The combined time complexity class is $\mathcal{O}(tolerance * |response|^2)$. The maximum of the memory complexity classes, which defines the memory complexity of the algorithm, is $\mathcal{O}\left(count(stimulus) + \frac{\sum_{i} count(response_i)}{|response|} + tolerance * |response|^2\right)$.

The required delay is calculated by adding tolerance to the start time of the oldest unfinished cluster and subtracting the current timestamp ($\mathcal{O}(tolerance*|response|^2)$). The output function checks that all stored synchronization clusters are either younger than tolerance or fulfilled. Because the entries of the map, that stores the synchronization clusters, cannot be accessed in way, that is sorted by age, every entry of the map must be checked for its age (at most tolerance*|response| checks). For every synchronization cluster that is older than tolerance, it must be checked, if this cluster is fulfilled. The check of a single cluster requires to check the boolean variables of each stream. Per timestamp, at most |response| synchronization cluster can be started, therefore at most response clusters grow older than tolerance per timestamp. Therefore, the output function is in $\mathcal{O}(tolerance*|response|^2)$ in terms of time per input timestamp.

At the end of the observation, it must be checked, if each stimulus event had a matching synchronization cluster. For each of the at most count(stimulus) stimulus colors, a lookup in a set must be done, therefore this check is in $\mathcal{O}(count(stimulus))$ and the complete output function, including the check at the end of observation, is in $\mathcal{O}(tolerance * |response|^2 + count(stimulus))$ in terms of time.

5.1.18 InputSynchronizationConstraint

The input streams must be transformed into a map[Int, Int] stream, similar to the previous constraint, but this time the index 0 indicate the response stream and the indices 1, 2, ... indicate the stimulus streams.

The InputSynchronizationConstraint is defined very similar to the OutputSynchronizationConstraint. The difference is, that the synchronization occurs in a set of stimulus events, not in response events.

Despite the similarities, monitoring the *InputSynchronizationConstraint* is simpler. As state, a map that uses the numbers 1 to |stimulus| as keys and as values a second map that uses colors (integer) as key and the timestamp of the latest occurrence of this color in the stream (the stream is defined by the key of the outer map). This map is updated at every stimulus event, at which either the timestamp of the latest occurrence of this color in this stream is updated, or a new inner map entry is created for this color. The update of an existing entry is done in constant time, but

the time for initializing a new entry is linear dependent on the number of stimulus streams. Because stimulus events may occur and introduce a new color in each timestamp, the state transition is in $\mathcal{O}(|stimulus|^2)$ in terms of time. The memory size of this information is in $\mathcal{O}(|stimulus|*count(stimulus))$, because the map described above possibly stores every input event of the stimulus streams, when they introduce a new color and therefore a new entry in the inner map of the stream must be created. Response events are not considered for the state of the monitor. The creation of new timestamps is not needed in this constraint, because only previous events need to be considered. Therefore, the calculation of a delay span is not required.

For the output function, in timestamps containing a response event, it must be checked, if the last occurrences of the corresponding color in the stimulus stream form a valid synchronization cluster. This is done by searching the youngest and oldest event with this color in the map of latest stimulus events. If a event of this color is missing, the age is interpreted as infty and $-\infty$. Because the color value is the key of the inner map, the time for searching the oldest and youngest event of this color is linear to the number of stimulus streams. Therefore, the output function is in $\mathcal{O}(|stimulus|)$ in terms of time.

5.1.19 EventChain

Additionally to the 18 TADL2 timing constraints, a monitor, which checks the correctness of *EventChain* was implemented. A *EventChain* is defined on a *stimulus* and a *response* stream as:

```
\forall x \in stimulus : \forall y \in response : x.color = y.color \Rightarrow x < y
```

As a state, a set, which contains all colors that previously occurred in *reponse* is stored. This set is updated at each *response* event by a an insertion into a set $(\mathcal{O}(1))$. The maximal size of this map is the number of events in *response*, therefore the state is in $\mathcal{O}(count(response))$ in terms of memory.

The output function checks, if any occurring *stimulus* event is not in the set of *response* events, which is checked in constant time.

5.1.20 Conclusion

Table 5.1.20 gives an overview of the worst case memory consumption and the worst case run time per input timestamp. The worst case memory requirement and the runtime per input timestamp of the *Repeat-*, *Repetition-*, *Execution Time-*,

Sporadic-, Periodic-, Pattern-, Arbitrary- and Burst Constraint, which are the simple monitorable constraints, are either constant, or they are only limited by the parameters of the constraint, not by the input traces. The implementations of the Delay-, Strong Delay-, Synchronization-, Strong Synchronization-, Reaction- and Age Constraint are limited by the events, which may occur in time intervals of a specific length. Monitoring the correctness of Event Chains, the Output Synchronization- or the Input Synchronization Constraint with these implementations require continuously growing memory resources and in the Output Synchronization Constraint, the run time per input timestamp is continuously growing too. The implementation of the Order Constraint is in $\mathcal{O}(1)$ in terms of memory and time per event, although it is classified as Not simple monitorable. This is, because integers of a fixed length are used for the implementation of the constraint and only a finite subset of all streams that fulfill the constraint can be monitored correctly.

 $^{^{2}\}mathcal{O}(tolerance * |response|^{2} + count(stimulus))$ at the end of the observation

		Run Time per Input	
	Memory	Timestamp	
DelayConstraint	$\mathcal{O}(upper)$	$\mathcal{O}(upper)$	
StrongDelayConstraint	$\mathcal{O}(upper)$	$\mathcal{O}(1)$	
RepeatConstraint	$\mathcal{O}(span)$	$\mathcal{O}(span)$	
RepetitionConstraint	$\mathcal{O}(span)$	$\mathcal{O}(1)$	
SynchronizationConstraint	$\mathcal{O}(event * tolerance)$	O(event * tolerance)	
StrongSynchronizationConstraint	$\mathcal{O}(event * tolerance)$	O(event * tolerance)	
ExecutionTimeConstraint	$\mathcal{O}(1)$	$\mathcal{O}(1)$	
OrderConstraint	$\mathcal{O}(1)$	$\mathcal{O}(1)$	
SporadicConstraint	$\mathcal{O}(1)$	$\mathcal{O}(1)$	
PeriodicConstraint	$\mathcal{O}(1)$	$\mathcal{O}(1)$	
PatternConstraint	$\mathcal{O}(1)$	$\mathcal{O}(1)$	
A whiteness Constraint	$\mathcal{O}(minimum)$	$\mathcal{O}(minimum ^2$	
ArbitraryConstraint	O(minimumi)	+ minimum)	
BurstConstraint	$\mathcal{O}(maxOccurrences)$	$\mathcal{O}(maxOccurrences)$	
ReactionConstraint	$\mathcal{O}(maximum)$	$\mathcal{O}(maximum)$	
AgeConstraint	$\mathcal{O}(maximum)$	$\mathcal{O}(maximum)$	
OutputSynchronizationConstraint	$\mathcal{O}(count(stimulus) \\ + \frac{\sum_{i} count(response_{i})}{ response } \\ + tolerance \\ * response ^{2})$	$\mathcal{O}(tolerance \ * response ^2)^2$	
InputSynchronizationConstraint	$\mathcal{O}(stimulus \\ *count(stimulus))$	$\mathcal{O}(stimulus ^2)$	
EventChain	$\mathcal{O}(count(response))$	$\mathcal{O}(1)$	

Table 5.1: Worst Case Run Times of the Implementations

5.1.21 Performance Analysis

To get an overview of the capabilities of the monitor implementations, each of them were run on at least 100 traces with 10.000 events, which were generated by following specific parameters to show, which of these parameters result in faster or slower run times. For this evaluation, the TeSSLa interpreter version 1.0.12 were used and it was run on a computer with a i5-6600k processor running on 4.3 GHz. The operating system was Windows 10.0.19041.0.

The run times were measured as time between the input of all events of all timestamps and the output of the TeSSLa interpreter. For that, a program³ was written, which generates traces for each constraint and then measures the time between the input of the events of one timestamp and the output of the TeSSLa interpreter. The communication between the test program and the TeSSLa interpreter is done via the standard input and standard output stream of the interpreter. The time is measured by the java function System.nanoTime() immediately before the events of one timestamps are written into the input stream and immediately after an reaction was received on the output stream. It must be noted that this time measurement is not completely accurate, because neither the used java runtime environment nor the operating system were build to fulfill real time requirements. Therefore, unpredictable delays may occur in the test program, in the java interpreter or between them, but the averages of the results show, what the monitors are capable of and on which input parameters the run time significantly rises.

A shortened version of the results will be shown here, the complete results of the runtime measurement can be seen at⁴

DelayConstraint

The DelayConstraint was evaluated with 100 Traces of 10.000 events. The traces fulfilled the constraint with the parameters $lower \in \{100, 200, 300, 400, 500, 600, 700, 800, 900, 1000\}$ and upper = lower. The distance of subsequent source event were 2^i , with $i \in \{0, 1, ..., 10\}$, while the distance in each trace was smaller than 2 * lower. The shorter the distances between the source event are, the more (at most upper, when the distance is upper) events are stored as state.

Figure 5.1 shows the average run time of the monitor in dependency of *lower* and *upper* for traces with event distances of 1, which means that *upper* events are stored as state of the monitor. The run time is nearly constant, because the trace generator does not create worst case scenarios and only one event is removed must from the

³This program can be found at https://github.com/HendrikStreichhahn/TeSSLa-Autosar-Timing-Extensions/tree/master/traceGenerator

 $^{^4}$ The complete results can be found at https://github.com/HendrikStreichhahn/TeSSLa-Autosar-Timing-Extensions/tree/master/traceGenerator/results

list at every *target* event.

Figure 5.2 shows the average run times for this constraint with the parameters lower = upper = 800 in dependency of the distance of subsequent source events. Two clusters can be observed. The average run times of traces with event distances of $2^0, 2^1, 2^2, 2^3, 2^4, 2^5$ are higher than the run times of the other traces. This is, because in the first six traces, there are timestamps with two events, and in the traces, each timestamp has at most one event. This can be shown by a simple equation

Proof. Let lower = upper be the distance between source events and their associated target event.

Let $s \in \mathbb{N}_0$ be the first timestamp with an *source* event in the trace.

Let $dist \in \mathbb{N}$ be the distance between subsequent source events.

The placement of all source events is given by: s + x * dist with $x \in \mathbb{N}$

The placement of all target events is given by: s + y * dist + upper with $y \in \mathbb{N}, y < x$ All placements of source and target events, which occur in common timestamps, fulfilled the equation:

$$s + x * dist = s + y * dist + upper$$

 $x * dist = y * dist + upper$
 $x = y + \frac{upper}{dist}$

When upper = 800, there is no integer solution for x and y for $dist \in 64, 128, 256, 512, 1024$, all events occur in individual timestamps for these distance between source events. When $dist \in \{1, 2, 4, 8, 16, 32\}$, there is an integer solution for x and y, so there multiple events in individual timestamps.

Strong Delay Constraint

The traces for the evaluation of the StrongDelayConstraint were generated with the same parameters as for the previous constraint. In figure 5.3 the average run times with fixed source event distances is shown. The results are nearly constant. Figure 5.4 shows the average run times for traces, where lower and upper is fixed to 700 and the distance between subsequent source is varying. It can be seen, that the run times for the traces is separated into two areas, one cluster containing the traces with a source event distance of $2^0, 2^1$ and 2^2 and one containing the other traces. This clustering has the same reason as in the DelayConstraint, it occurs, because in some traces, there are many timestamps with multiple events and in some are not.

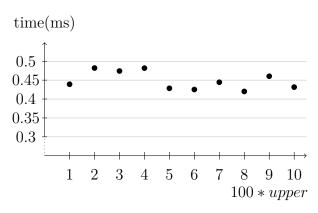
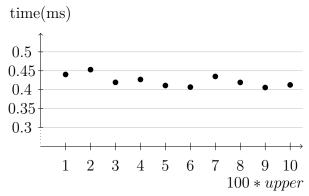


Figure 5.1: Average run times of the *Delay-Constraint* with event distances of $2^0 = 1$

Figure 5.2: Average run times of the *Delay-Constraint* with the parameters lower = upper = 800



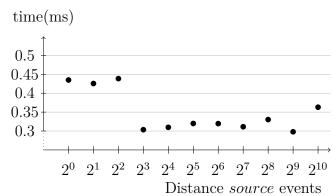
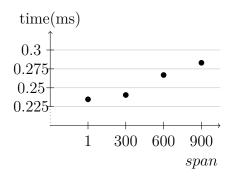


Figure 5.3: Average run times of the *Strong-DelayConstraint* with event distances of $2^0 = 1$

Figure 5.4: Average run times of the StrongDelay-Constraint with the parameters lower = upper = 700



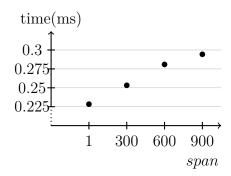


Figure 5.5: Average run times of the RepeatConstraint with the parameters lower = 5000, upper = 6000

Figure 5.6: Average run times of the RepeatConstraint with the parameters lower = 8000, upper = 9000

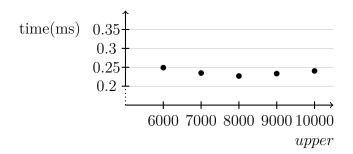
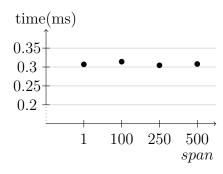


Figure 5.7: Average run times of the RepeatConstraint with the parameters span = 250, lower = 500

RepeatConstraint

The RepeatConstraint was evaluated with 100 Traces of 10.000 events. The traces were created with the attributes $span \in \{1, 300, 600, 900\}$, $lower = \{5000, 6000, 7000, 8000, 9000\}$ and $upper = lower + x, x \in 1000, 2000, 3000, 4000$. Figure 5.7 shows the average run time with a fixed span and lower parameter and a variable value for upper. It can be seen, that the run times are nearly constant, which matches with the analysis of the implementation.

Figure 5.5 and 5.6 show the average run time of the RepeatConstraint monitor with the parameters lower = 5000(8000), upper = 7000(90000). By the analysis of the implementation, a runtime that is linear dependent on span was expected, which can be slightly seen in the results. The increase is not much larger than the deviations between individual measures, but can be seen by nearly all runs with different values for lower and upper.



time(ms)
0.35
0.3
0.25
0.2
1 100 250 500 span

Figure 5.8: Average run times of the Repetition Constraint with the parameters lower = 500, upper = 900

Figure 5.9: Average run times of the Repetition Constraint with the parameters lower = 700, upper = 1100

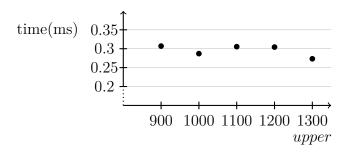


Figure 5.10: Average run times of the RepetitionConstraint with the parameters span = 1, lower = 500

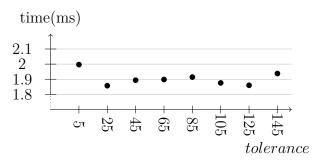
RepetitionConstraint

The traces for this constraint was created with the parameters $span \in \{1, 100, 250, 500\}$, $lower = \{500, 600, 700, 800, 900\}$ $upper = lower + x, x \in 400, 500, 600, 700, 800$ and $jitter = \frac{lower}{2}$.

Figure 5.8 and 5.9 are showing the average run times of the monitor with the parameters lower = 500(700) and upper = 900(1100) with different values of the span parameter. Figure 5.10 shows the average run time in dependency of the upper parameter. Like expected in the analysis, the parameters did not an influence to the run times and the run times are nearly constant.

SynchronizationConstraint

Figure 5.11 shows the average run times of the *SynchronizationConstraint* monitor, which was checking traces with three event streams with two events per synchronization cluster in each stream. The synchronization clusters were 200 timestamps



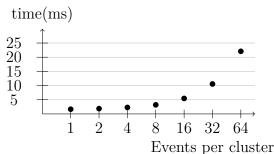


Figure 5.11: Average run times of the *SynchronizationConstraint* with three event streams and two events per cluster and stream and a cluster distance of 200

Figure 5.12: Average run times of the SynchronizationConstraint with three event streams, tolerance = 91 and a cluster distance of 182

apart, so they do not overlap. The run times were nearly constant, which was expected for these parameters, because at most 3 (the number of input streams) events were stored and considered in each input time stamp.

Figure 5.12 shows the average run times of the monitor with traces of three streams, a *tolerance* value of 91 and a distance between clusters of 182. So again, the clusters were not overlapping. It can be seen, that the run times grow linear when increasing the number of events in each cluster. This matches with the expectation, because the more events occur in an interval of the length *tolerance*, the more events need to be stored and considered in each input timestamp.

StrongSynchronizationConstraint

Figure 5.13 shows the average run time of the monitor with the parameters tolerance = 37 and a cluster distance of 2, so that 19 clusters are overlapping. It can be seen, that the run time increases, when more input streams are used. In Figure 5.14, a fixed number of input streams was used and the cluster distance was 2, like before. Again, an increase in the run times can be seen. This matches with the expectations of the analysis, in which the run time was said to be in $\mathcal{O}(|event| * tolerance)$.

ExecutionTimeConstraint

The run time evaluation of the ExecutionTimeConstraint monitor was done by traces, which fulfill the constraint the parameters $lower \in \{100, 300, 500, 700, 900\}$ and upper = lower + x, $x \in \{100, 600, 1100, 1600, 2100\}$. For each of combination of these parameters, one trace with 1, 11, 21 and 31 preemptions between the each start and end event were created. In figure 5.15 the average run time with fixed

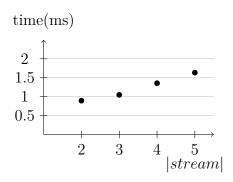


Figure 5.13: Average run times of the StrongSynchronizationConstraint with tolerance = 37 and a cluster distance of 2

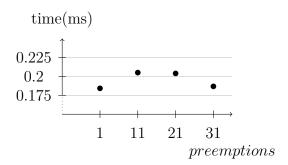


Figure 5.15: Average run times of the ExecutionTimeConstraint with the parameters lower = 100, upper = 200

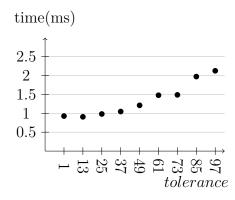


Figure 5.14: Average run times of the *StrongSynchronizationConstraint* with three event streams and a cluster distance of 2

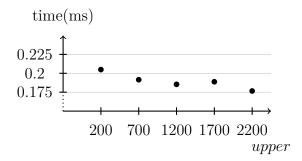


Figure 5.16: Average run times of the Execution Time Constraint with the parameters lower = 100, preemptions = 11

lower and upper can be seen. In figure 5.16, lower and the number of preemptions is fixed. A correlation between the input parameters and the run times can not be observed, which was expected, because the run time is independent from the parameters or the placement of events, like stated in chapter 5.

OrderConstraint

The OrderConstraint monitor was evaluated on traces with distances between subsequent source events between 1 and 91 in steps of 10 and maximal distances between the i^th source and target event between 0 and 45 in steps of 5. In traces, where the distance between the source events and their associated target events were 0 or the distance between subsequent source events were 1, the run time is ca. double as large as in the other traces. The reason for this is that the smaller the distance between the source and target events are, the more often two events occur in the same time

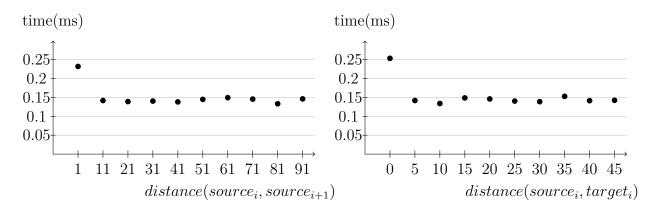


Figure 5.17: Average run times of the Order-Constraint with a distance between source events and their associated target events of 5 in dependency of the distance between subsequent source events

Figure 5.18: Average run times of the *Order-Constraint* with a distance between subsequent source events of 11 in dependency of the distance source events and their associated target event

stamp, which means, that two events must be processed in one timestamp, instead of one, which requires more time.

SporadicConstraint

The traces, that were used for the fulfill the constraint with the parameters $jitter \in \{1, 11, 21, 31\}$, $lower \in \{500, 600, ..., 900\}$ and $upper = lower + x, x \in \{100, 200, ..., 500\}$. The average run time per timestamps of the monitor with the parameters lower = 500 and upper = 600 with different values for the jitter parameter can be seen in Figure 5.19. Similar to the run times with varying upper values (figure 5.20), the run times are nearly constant. Like expected by the analysis of the implementation in the previous section, the parameters had no influence on the run time.

PeriodicConstraint

The run time evaluation was done on traces, which fulfill the PeriodicConstraint with the parameters $period \in \{10, 20, 30, ..., 100\}$ and $jitter \in \{0, 1, ..., 9\}$. In figure 5.21 the average run times of the monitor with a constant period and a variable jitter can be seen, in figure 5.22, jitter is fixed and period is variable. Despite some fluctuations, the run time is constant and independent of the input parameters. This behaviour was expected by the complexity analysis.

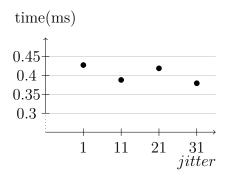


Figure 5.19: Average run times of the Sporadic Constraint with the parameters lower = 500, upper = 900

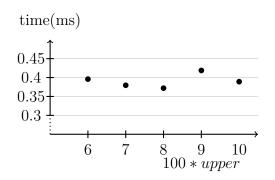


Figure 5.20: Average run times of the Sporadic Constraint with the parameters lower = 500, jitter = 21

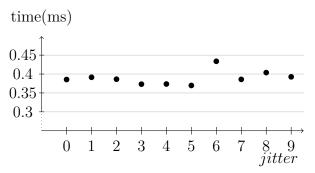
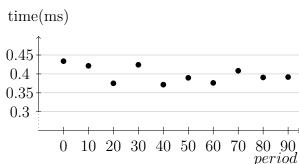
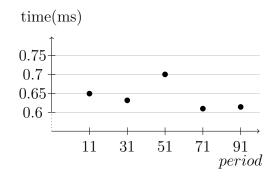


Figure 5.21: Average run times of the *Periodic*-Figure 5.22: Average run times of the *Periodic*-Constraint with a period of 10 and variable jitter



Constraint with a period of 6 and variable period



time(ms) $0.75 \rightarrow 0.65 \rightarrow 0.05 \rightarrow 0.05$

Figure 5.23: Average run times of the PatternConstraint with the parameters offset = [0, 1] and jitter = 0

Figure 5.24: Average run times of the PatternConstraint with the parameters offset = [1, 3, 5] and jitter = 1

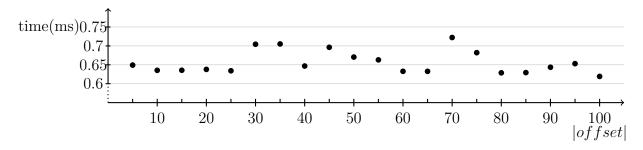


Figure 5.25: Average run times of the PatternConstraint with the parameters period = 200 and jitter = 0

PatternConstraint

The monitor of the PatternConstraint was first evaluated on traces with lengths of the |offset| parameter of 1, 2 and 3 and varying values for the parameters period and jitter. Figure 5.23 and 5.24 are showing some of these results, which where nearly constant at around 0.65ms per input timestamp. After these run time measurements, the run time was measured on traces with the parameters jitter = 0 and period = 200. The offset parameter had an increasing length from 1 to 100 and was filled with offset = [0, 1, 2, 3, ...] and the period parameter was set to 200. The results of this measurement can be seen in figure 5.25 .It can be seen, that the average run times was nearly constant, beside some measurement deviations. This behaviour was expected by the analysis in the previous section.

ArbitraryConstraint

Similar to the previous constraint, multiple runs were done for the run time measurement. First with small lengths of the *minimum* and *maximum* parameter and

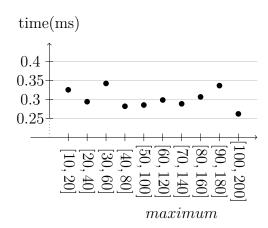


Figure 5.26: Average run times of the Arbitrary Constraint with the parameter minimum = [10, 20]

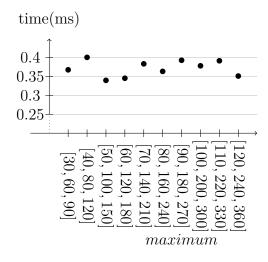


Figure 5.27: Average run times of the Arbitrary Constraint with the parameter minimum = [30, 60, 90]

changing values for the values inside of these parameters, and then with a length of the minimum and maximum parameter of 1 to 100. Figure 5.26 and 5.27 are showing some of the results with short minimum and maximum parameters. It can be seen, that the results with the same length of these parameters are nearly constant, but the traces with a minimum length of 3 took slightly slightly more time. Figure 5.28 shows the average run times in dependency of the length of the minimum parameter. The graphic shows a nearly linear growth of the run time, but based on the analysis a growth by $|maximum|^2$ was expected. The ArbitraryConstraint is defined as

 $ArbitraryConstraint(events, minimum, maximum) \Leftrightarrow \\ \forall i: RepeatConstraint(events, lower = minimum_i, upper = maximum_i, span = i)$

The runtime of the RepeatConstraint is linear dependent on the span parameter, so the run time of the RepeatConstraint is expected to grow by $\sum_{i=1}^{|maximum|} i = \frac{|maximum|^2 + |maximum|}{2}$.

Earlier in this section, we've shown that the run time of the RepeatConstraint is continuously growing, but fairly slow. This explains the nearly linear run time, because the rise in the runtime of the RepeatConstraint is so small that the linear part of $\frac{|maximum|^2 + |maximum|}{2}$ is predominating.

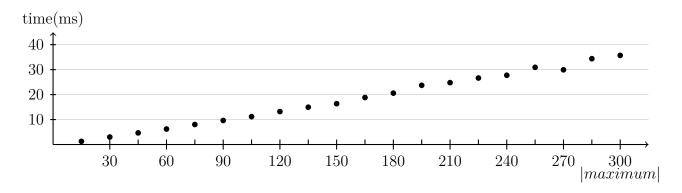


Figure 5.28: Average run times of the Arbitrary Constraint with |minimum| = 1..100

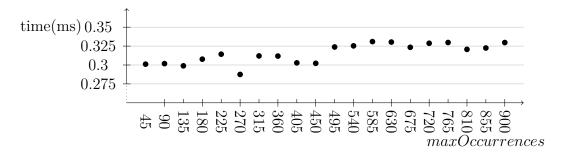


Figure 5.29: Average run times of the *BurstConstraint* with increasing occurrences per burst and a length of 2000

BurstConstraint

Figure 5.29 shows the average run time per input timestamp in with increasing a number of occurrences per burst. Similar to the *RepeatConstraint*, over which the *BurstConstraint* is defined and implemented, are small increase in the run times can be seen by increasing the number of occurrences. This increase is smaller than the fluctuations between the individual measurements, but the trend can be seen in all of the results. The linear growth was expected by the analysis in the previous section.

ReactionConstraint

The runtime evaluation of the ReactionConstraint was done on traces with the parameters $minimum \in \{100, 200, ..., 1000\}$ and maximum = minimum, while the distances between subsequent stimulus event were in $\{1, 2, 4, 8, ..., 1024\}$, so that minimum, $\lceil \frac{minimum}{2} \rceil$, $\lceil \frac{minimum}{4} \rceil$, ..., $\lceil \frac{minimum}{1024} \rceil$ events must be stored and considered at every event in the monitor.

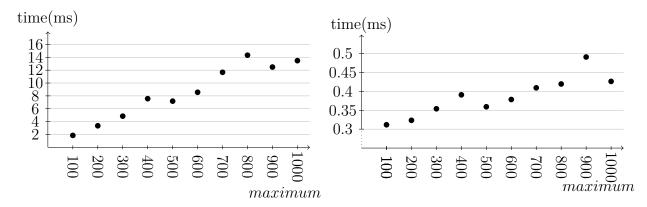


Figure 5.30: Average run times of the *Reaction-Constraint* with a distance between subsequent *stimulus* events of 1 (worst case) and variable *maximum*

Figure 5.31: Average run times of the Reaction-Constraint with a distance between subsequent stimulus events of 128 and variable maximum

Figure 5.30 and 5.31 are showing the average run times of the monitor with increasing minimum and maximum parameters, but fixed distance between subsequent stimulus events. The first figure shows the run times with stimulus distances of 1, which is the worst case, because maximum events must be stored and considered for the correctness decision of the monitor. Like expected by the analysis, the run time is increasing linear with larger maximum values. This behaviour can also be seen in the second figure, where the distance between the events is 128, but the run times are much smaller here. This is, because between $1 \left(\left\lceil \frac{100}{128} \right\rceil \right)$ and $8 \left(\left\lceil \frac{1000}{128} \right\rceil \right)$ were considered in each timestamp with events, not between 100 and 1000 in the previous case.

AgeConstraint

The run time of the AgeConstraint monitor were measured on traces with the same parameters as the previous constraint. Figure 5.32 shows the run times with event distances of 1, which is the worst case in terms of monitoring, in dependency of the maximum parameter. With increasing maximum values, the average run time grew linear, like expected in the analysis. The average run times with the same maximum values and a distance between subsequent stimulus events is shown in figure 5.33. The run time is growing nearly linear again. Deviations can be seen at maximum = 500 and maximum = 1000. Because $\lceil \frac{400}{128} \rceil = \lceil \frac{500}{128} \rceil$ and $\lceil \frac{900}{128} \rceil = \lceil \frac{1000}{128} \rceil$, the number of events, which must be stored, and considered in each input timestamp. Therefore, the run time is not increasing at these parameter values.

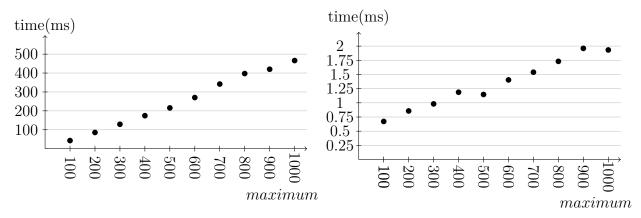


Figure 5.32: Average run times of the *AgeConstraint* with a distance between subsequent *stimulus* events of 1 (worst case) and variable *maximum*

Figure 5.33: Average run times of the *AgeConstraint* with a distance between subsequent *stimulus* events of 128 and variable *maximum*

OutputSynchronizationConstraint

The traces for the evaluation of the InputSynchronizationConstraint were generated with 2,3, 4 and 5 stimulus streams, tolerance values of 10 to 25 in steps of 3 and a distance between synchronization clusters of 2, 4, 8, 16 or 32. In a second run, the run times for traces with 2, 22, 42, ..., 202 response streams were measured. Figure 5.34 shows the run time with a cluster distance of 2 and 4 response streams. Like expected, the growth of the run time is linear. Figure 5.35 the average run times with a fixed cluster distance of 2 and tolerance = 2. As expected, the run times are growing by the square of |response|.

InputSynchronizationConstraint

The traces for the evaluation of the InputSynchronizationConstraint were generated with 2,3, 4 and 5 stimulus streams, tolerance values of 10 to 25 in steps of 3 and a distance between synchronization clusters of 2, 4, 8, 16 or 32. Similar to the previous constraint, traces with up to 202 stimulus streams were tested in a second run. Figure 5.36 shows the run time of the monitor with the traces with three stimulus streams and a fix cluster distance of 2. The run times are nearly constant, which was expected by the analysis of the source code. Figure 5.37 shows the average run time with a fixed cluster distance and tolerance. It can be see that the run time per input timestamp is larger than in the monitor for the previous constraint, but it also increases squarely, which matches with the analysis.

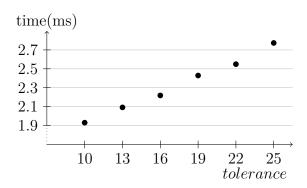


Figure 5.34: Average run times of the *OutputSynchronizationConstraint* with 4 *response* streams and a cluster distance of 2

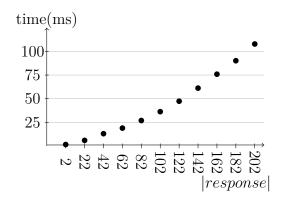


Figure 5.35: Average run times of the OutputSynchronizationConstraint with a cluster distance of 2 and tolerance = 10

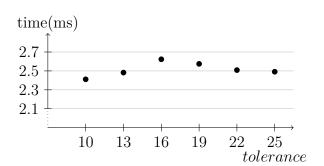


Figure 5.36: Average run times of the *InputSynchronizationConstraint* with 3 stimulus streams and a cluster distance of 2

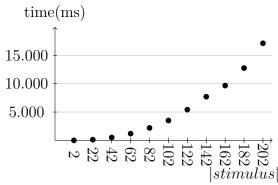


Figure 5.37: Average run times of the InputSynchronizationConstraint with a cluster distance of 2 and tolerance = 10

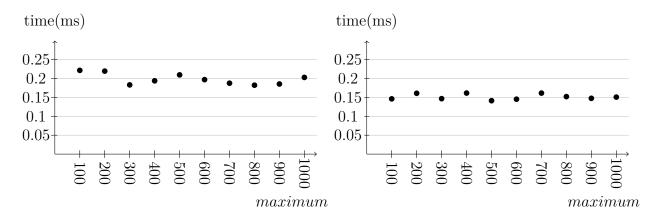


Figure 5.38: Average run times of the *EventChain* check with a distance between subsequent *stimulus* events of 1 and variable maximum(ReactionConstraint parameter)

Figure 5.39: Average run times of the EventChain check with a distance between subsequent stimulus events of 128 and variable maximum(ReactionConstraint parameter)

EventChain

The run time of monitor for the correctness of event chains were also measured. The traces were generated with the same parameters as for the ReactionConstraint. Figure 5.38 and 5.38 are showing the results of this measurement, with fixed distances between subsequent stimulus events of 1 and 128 timestamps and distances between stimulus events and their associated response event of 100, 200, ..., 1000. The run times in both cases are nearly constant, but the run times are slightly larger in figure 5.38. The reason for this is, that the stimulus and response events occur in the same timestamps here, but not in figure 5.39.

6 Summary and Outlook

In this chapter, a summary of the presented work is given. Additionally, some ideas of future work will be presented.

6.1 Summary

In this thesis it has been shown that implementing a monitor for the AUTOSAR Timing Constraint is problematic due to informal definitions. Because of this, the timing constraints defined in the Timing Augmented Description Language v2 (TADL2) were considered for the implementation of a monitoring tool.

After the relations between the AUTOSAR Timing Extensions and the timing constraints defined in TADL2 were explained, the term *simple monitorable*, which ensures that a property on an possibly infinite trace can be monitored with finite resourcesm were introduced and extended by the possibility of inserting new timestamps. This term was applied to the TADL2 timing constraints, with the result, that eight of the constraints are simple monitorable with or without delay, five constraints require infinite memory resources on infinite traces in worst case scenarios and 4 constraints require infinite memory resources on nearly all infinite traces. On one constraint the term *simple monitorable* is not applicable, because it is not defined on event streams.

After the theoretical part, an implementation for all of the TADL2 timing constraints in TeSSLa were given, except for the *ComparionConstraints*, which functionality already was implemented in TeSSLa. The worst case runtime per timestamp with input events and the memory usage were analyzed. At the end, the run time of the implementations were measured on large generated traces.

6.2 Future Work

For a real world use of the monitors, more work on this topic is required. It is possible to map TeSSLa-specifications reconfigurable hardware like FPGAs [DDG⁺18]. Because of memory and recursion restrictions, this is not possible for all specifications. The possibility to map the implementations on reconfigurable hardware

would increase the performance and opens the gate for real world usage in embedded systems in the automotive industry.

Some constraints were classified as not simple monitorable, but could be restricted, so that they are simple monitorable. For example the Reaction- and AgeConstraint are classified as always not simple monitorable, because they need to store every occurring color and therefore have a continuously growing memory usage. If all events have a minimal distance and the color attribute is defined as integers, which occur strictly ordered, a monitor with a fixed upper limit in memory resources could be build. Restrictions of this kind are possible to many of the timing constraints which are classified as not simple monitorable, but it must be ensured that the monitored system also fulfills the restrictions.

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Abbreviations

DFST Deterministic Finite State Transducer

TDFST Timed Deterministic Finite State Transducer

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