

Monitoring der AUTOSAR Timing Extensions mittels TeSSLa

Monitoring of the AUTOSAR Timing Extensions with TeSSLa

Bachelorarbeit

im Rahmen des Studiengangs Informatik der Universität zu Lübeck

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Lübeck, den 1.1. 1970

Erklärung
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(Hendrik Streichhahn) Lübeck, den 1.1. 1970

Kurzfassung Abstract Deutsch

Abstract Kurzfassung Englisch.

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1. Introduction

Timing behavior is one of the most important properties of computer systems. Especially in safety-critical applications, a wrong timed reaction of the system can have disastrous consequences, for example in the Electronic Stability Control of a vehicle. AUTOSAR (AUTomotive Open System ARchitecture) is used by almost all car manufacturers in their software development processes to standardize components and therefore increase the interoperability and exchangeability.

The AUTOSAR Timing Extensions are describing the timing behavior of soft- and hardware components, focusing on cyber-physical systems, like cars. The goal of this thesis is to implement a monitoring tool for the constraints defined in the AUTOSAR Timing Extensions.

A major drawback of this standard is that the definitions are written in an informal way and can be misunderstood. Therefore, the timing constraints defined in TADL2 (Timing Augmented Description Language Version 2) are used as basis for the monitoring tool. The TADL2 timing constraints are comparable and partly compatible to the AUTOSAR Timing Extensions, as most of the constraints defined in the AUTOSAR standard can be described as equivalent combination of TADL2 timing constraints.

The monitoring tool is written in *TeSSLa* (Temporal Stream-based Specification Language), which is made for stream runtime verification and is capable of non-intrusive observation and can be run as Java program or on specialized embedded hardware, like FPGAs.

In the first part of this thesis, an overview over the AUTOSAR Timing Extensions and an example about the informal and ambiguous definitions will be given. Next, the TADL2 timing constraints will be listed and the relations between the these constraints and the AUTOSAR Timing Extensions will be described. In the next chapter, TeSSLa, its fundamental functionality and other prerequisites, which are needed for understanding the theoretical part of this thesis, will be explained. The term of *finite monitorability* is introduced, which insures, that a property on infinite streams can always be monitored with finite resources. Then, each of the TADL2 timing constraint is checked, if it finite monitorable or not. After that, the TeSSLa implementations of these constraints is described and evaluated in a theoretical and practical way.

In the end an overview of the accomplished is given and ideas for further work will be discussed.

2. Timing Constraints

2.1. AUTOSAR Timing Extensions

AUTOSAR is a development partnership in the automotive industry. As stated before, the main goal is to define a standardized interface, to increase interoperability, exchangebility and re-usability of parts and therefore simplify development and production. Three different layers are defined in the specification. Basic Software is an abstraction layer from components, like network or diagnostic protocols, or operating systems. AUTOSAR-Software defines, how application has to be build. For Basic Software and AUTOSAR Software, there are definitions for standardized Interfaces, to enable the communication via the Autosar Runtime Environment. It works as middleware, in which the virtual function bus is defined [AUT17]. The AUTOSAR Timing Extension are describing timing constraints for actions and reactions of components, that are communicating via the Virtual Function Bus. They are defined via events, which consists of a time and a data value, the type of the time and data value is arbitrary, the only restriction is, that the time values are strictly increasing. To describe the logical relationship between groups of events, event chains are defined, which consist of a stimulus and response event. The response event is understood as the answer to the stimulus event.

The AUTOSAR Release 4.4.0 ([AUT18]) is used for this thesis, there are 12 timing constraints defined in this version of the AUTOSAR Timing Extensions

- 1. The subset of 5 **EventTriggeringConstraints** are describing, at which points in time specific events may occur.
 - 1 The **PeriodicEventTriggering** defines repetitions of event with the same time distance and offers the possibility to define an allowed deviation from this pattern and the minimal distance between two subsequent events.
 - 2 The **SporadicEventTriggering** specifies sporadic event occurrences by defining the minimal and maximal distance between subsequent events. Additionally, periodic repetitions and allowed deviations can optionally be described.
 - 3 With the **ConcreteEventTriggering**, offsets between a set of n subsequent events can be described. A periodic behavior may also be defined, where the time distance between each i * n and (i + 1) * n events is specified by the attribute patternPeriod.

- 4 The **BurstPatternEventTriggering** describes event clusters with a minimal and maximal number of events and optionally periodic repetitions of these clusters.
- 5 The **ArbitraryEventTriggering** defines the distance between subsequent event by defining *ConfidenceIntervals*, which describe the probability, in which time interval the following event will occur.
- 2. The **LatencyTimingConstraint** specifies the minimal, nominal and maximal time distance between the stimulus and response events of an event chain.
- 3. The **AgeConstraint** is a simpler form of the *LatencyTimingConstraint* by defining minimal and maximal age a event may have at the point of time, when the event processed.
- 4. The **SynchronizationTimingConstraint** is used for describing events of different kinds, that occur synchronized in a time interval of a specific length.
- 5. The **SynchronizationPointConstraint** defines two sets of executables and events. Every element of the first set must have finished or occurred, before the first element of the second set may start or occur.
- 6. The **OffsetTimingConstraint** specifies the minimal and maximal time distance between corresponding *source* and *target* events.
- 7. The **ExecutionOrderConstraint** offers the possibility to define a list of executables, which must start and finish in the order given in the list.
- 8. The **ExecutionTimeConstraint** defines the minimal and maximal runtime of an executable, including or excluding the runtime of external functions and interruptions.

Problematic with the AUTOSAR Timing Extensions is, that the definitions are not very formal and have room left for interpretation. Let's take a look at the *BurstPatternEventTriggering*. The BurstPatternEventTriggerings describe events clusters, with events that occur with short time distances, with large time distances between the clusters. The following attributes are needed:

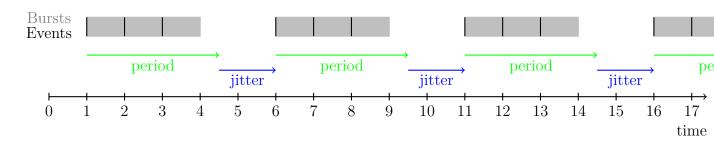


Figure 2.1.: BurstPatternEventTriggering Period-Jitter accumulating

Attribute	Type	Explanation
maxNumberOfOccurrences	PositiveInteger	maximum number of events per burst
minNumberOfOccurrences	PositiveInteger	(optional) minimum number of
		events per burst
minimumInterArrivalTime	TimeValue	minimum time distance between any
		two events
patternLength	TimeValue	length of each burst
pattern Period	TimeValue	(optional) Time distance between the
		start points of two subsequent bursts
pattern Jitter	TimeValue	(optional) maximum of allowed
		deviation from periodic pattern

As example, we set:

- maxNumberOfOccurrences = 3
- minNumberOfOccurrences = 1
- minimumInterArrivalTime = 1
- patternLength = 3
- patternPeriod = 3.5
- patternJitter = 1.5

The combination of *patternPeriod* and *patternJitter* can be interpreted in an accumulating as seen in 2.1 or non-accumulating way as seen in 2.2 way. In the accumulating interpretation, the reference for the periodic occurrences is only the start point of the previous

With the definition of patternLength ("time distance between the beginnings of subsequent repetitions of the given burst pattern") you would think, that the accumulating variant is meant. Against that, the period attribute in PeriodicEventTriggering-Constraint is also defined as "distance between subsequent occurrences of the event"in

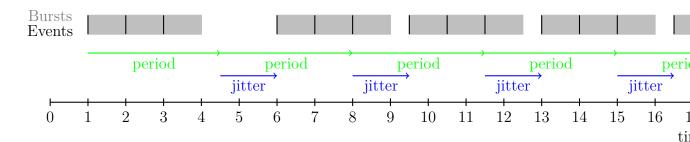


Figure 2.2.: BurstPatternEventTriggering Period-Jitter non-accumulating

the text, hence it is understandable the accumulating way, but there is also the formal definition

$$\exists t_{reference} \forall t_n : t_{reference} + (n+1) * period \leq t_n \leq t_{reference} + (n-1) * period + jitter,$$

where t_n is the time of the *n*-th Event and $t_{reference}$ is a reference point, from which the periodic pattern starts, so the PeriodicEventTriggering-Constraint is meant to be understood in the non-accumulating way. It remains unclear, in which way the BurstPatternEventTriggering is meant to be understood.

Another problem of the AUTOSAR Timing Extensions is, that they were made for design purposes, monitoring them can be difficult, as they may need continuously growing time and memory resources, which makes online monitoring impossible (more on monitorability in 4). As example, we will use the burst pattern again, this time using the attributes as

- $maxNumberOfOccurrences = INT_MAX$
- minNumberOfOccurrences = 1
- minimumInterArrivalTime = 0
- patternLength = 3
- patternPeriod unused
- patternJitter unused

In 2.3 you see the application of the BurstPatternEventTriggering Constraint with the given parameters on a stream with events at the timestamps 3, 3.5, 4, 4.5. You can see the development of possible the burst cluster with ongoing time. The gray lines show, where the burst can lay, the black lines show, where they definitely are. In timestamp 3 with only one event so far, only one burst has to be considered and it can lay between timestamp 0 and 6, the only limitation is, that it must include timestamp 3 with the event in that point. In Timestamp 3.5, there are two events (at 3 and 3.5) so far and there are two possibilities for burst placements. The first

possibility with only one burst with both events in it, and the second possibility, where the events are in different bursts. The third graphic shows the trace in timestamp 4 with three different events so far (3, 3.5, 4) and there are three different possibilities for burst placements to consider. One possible burst contains all three events, the second possibility has one burst with the event at timestamp 3 and one burst with the events at 3.5 and 4 and the third possibility has one Burst with the events at 3 and 3.5 and one burst with the event at 4. The possible bursts in graphic 4 are analog to the third graphic, one possibility with one burst containing all 4 events and 3 possibilities with the first burst containing the first event, the first and second event or the first, the second and the third event and the second burst containing the remaining events.

In this Example, we see, that it is possible to create an unlimited number of possibilities for burst placements within one burst length, when the *minimumInter-ArrivalTime*-attribute is 0, which results in an infeasible resource consumption, as unlimited memory and time is needed to check the constraint in following events. Therefore, online monitoring this constraint is impossible in general, because of the strict resource limitations. More on that in 4.



Figure 2.3.: BurstPatternEventTriggering Possible bursts, ↑ shows the current time

2.2. TADL2

As timing extension to EAST-ADL(Electronics Architecture and Software Technology-Architecture Description Language), the TIMMO (Timing Model) project, and its successor TIMMO2USE, were initiated. EAST-ADL has similar goals as AUTOSAR, but the definitions are written in a more formalized fashion. The definitions of the AUTOSAR Timing Extensions are only textually described often, the TADL2-Definitions are defined in a more formal way, as they offer an formalized definition of each constraint in a timing constraint logic [BFL+12]. EAST-ADL is much less used in the automotive industry, but the EAST-ADL Timing Constraints are partly compatible to the AUTOSAR Timing Extensions, as they define sub- or supersets of each other. Many of the AUTOSAR Timing Extensions can be defined via a combination of TADL2 Constraints, as you will see in 2.2.3.

TADL2 offers 18 timing constraints, which are defined on evens or event chains, similar to the AUTOSAR Timing Extensions:

- The **DelayConstraint** defines the minimal and maximal time distance of the events in an event chain. Additional response events are allowed. The **StrongDelayConstraint** prohibits these stray events, but is semantically equal in any other way.
- The RepeatConstraint, RepetitionConstraint, PeriodicConstraint, SporadicConstraint and ArbitraryConstraint are describing the time distance between subsequent events, whereby they are having small semantic differences.
- The SynchronizationConstraint and StrongSynchronizationConstraint define groups of event sets, which events occur in common time intervals. The SynchronizationConstraint allows more than one event of each group per interval, the StrongSynchronizationConstraint does not.
- The **ExecutionTimeConstraint** is used to set a minimum and a maximum for the runtime of a task, not considering interruptions in the execution.
- The **OrderConstraint** defines that the n^th stimulus event of an event chain must occur before or at the n^th response event.
- The **ComparisonConstraint** is used to describe ordering relations of timestamps.
- The **PatternConstraint** defines the time distance between periodic points in time to several events.
- The **BurstConstraint** regulates the maximum number of events in time intervals of a specific length.

- The **ReactionConstraint** describes the minimal and maximal time a response event must occur after the associated stimulus event. The relation between the individual stimulus and response events is done by using the color attribute of each event. Additional response events are allowed, additional stimulus events not.
- The **AgeConstraint** is similar to the ReactionConstraint, but it is defined the other way around. Therefor, it describes the minimal and maximal time a stimulus event must occur before the associated response event. Additional stimulus events are allowed, additional response events not.
- The OutputSynchronizationConstraint is used to describe groups of event chains, which all have the same response events. The response events of the event chain must occur in common time intervals, like in the SynchronizationConstraint. In the InputSynchronizationConstraint, the roles of the stimulus and response events are swapped.

2.2.1. Parenthesis - Simple and Flexible Timing Constraint Logic

The formal definition of the TADL2 timing constraint are written in *Timing Constraint Logic* (short: *TiCL*), which was developed as part of the TIMMO-2-USE project. TiCL was formally introduced in [LN12], for better understanding the key aspects of this article will be explained in the following.

The main goal of TiCL is to be formal and expandable and offering the possibility of defining finite and infinite behaviors of events. In TiCL, only points in time, when events occur, are considered, therefore an events only consists of a real value as timestamp, without the possibility of adding a data value. There are 7 syntactic categories in TiCL

```
\mathbb{R}(arithmetic constants)

Avar(arithmetic variables)

AExp(arithmetic expressions)

Svar(set variables)

SExp(set expressions)

TVar(time variables)

CExp(constraint expressions)
```

Arithmetic expressions can be defined as arithmetic constants, arithmetic variables, application of +, -, *, / on arithmetic expressions, application of the Cardinality operator on a set $(|E|, E \in SExp)$ or as measure $\lambda(E)$ $(E \in SExp)$. $\lambda(E)$ is defined as



Figure 2.4.: Graphical example of $\lambda(E)$, $\lambda(F)$ and $\lambda(E \setminus F)$

Lebesue measure, which is figuratively speaking, the length of all continuous intervals of E. In 2.4 you see a visualized example of the measure operator λ . The set E contains all Events between the timestamps 1 and 9, the set F contains the events at the timestamps between 2 and 4 and 6 and 7, therefore $E \setminus F$ contains the events at the timestamps $\{1, 1.5, 4.5, 5, 5.5, 7.5, 8, 8.5, 9\}$. E consists of one continuous interval from timestamp 1 to 9 with the length of 8, F consists of two continuous intervals from 2 to 4 with the length of 2 and from 6 to 7 with the length of 1, therefore $\lambda(F) = 3$. $E \setminus F$ consists of three continuous intervals, the first from 1 to 1.5 (length = 0.5), the second from 4.5 to 5.5 (length = 1) and the last from 7.5 to 9 (length = 1.5), so the total length of the continuous intervals of $E \setminus F$ is 3.

Set expressions can be defined as set variables, or as set of time variables fulfill a given constraint expression.

Constraint expressions can be defined as application of the \leq -operator on time or arithmetic expressions, the \in operator on time variables and set expressions, the logical conjunction on constraint expressions, the negation of constraint expressions and the \forall -Quantifier on arithmetic, set and time variables over an constraint expression.

As extension to this definition, well known syntactic abbreviations like $true \equiv 0 \leq 1$ or the \exists -quantifier will be used, but there are also some TiCL-specific syntactic abbreviations, which will be defined and explained in the following.

Interval Constructors

Let $x, y \in Tvar$ and $E, F \in SExp$.

The constructor $[x \le]([x <])$ is defined as $y : x \le y(y : x < y)$, therefore the interval contains all points in time laying behind of x, possibly containing x.

 $[\leq x]([< x])$ is defined as complement of $[x <]([x \leq])$ and contains all timestamps laying before x.

[x..y] is defined as $[x \le] \cap [< y]$, so all points of time after x, including x, and before y are part of this interval.

 $[E \leq]$ is defined as $\{y : \exists x \in E : x \leq y\}$, this interval contains all point of time at and after the first timestamp in E. [E <] is equal to $\{y : forall x \in E : x < y\}$, therefore it defines the interval containing all timestamps after the latest point of time in E.

 $[\leq E]$ ([< E]) is defined as $[E <]^C$ ($[E \leq]^C$), analogous to the operators on time variables.

[E] is equal to $[E \leq] \cap [\leq E]$. It defines the time interval between the first and last element of E, including these points in time.

 $E_{x<}(E_{<x})$ is defined as $E \cap [x <](E \cap [< x])$. This operators filters the timestamps in E so that only the points in time before (after) remain.

[x..E] equals $[x \leq] \cap [\langle (E_{x \leq})]$. The interval begins at x and ends right before the first element of E after x.

[E..F] is defined as $\{x : \exists y \in E : x \in [y..F]\}$ and describes the intervals, where the previous operator is applied on every element of E.

2.2.2. TADL2-Timing Constraints

For better understanding of the following chapters, the TADL Constraints will be presented next. As abbreviation and unification, all timing expressions are defined as set \mathbb{T} , which are understood as real numbers but expanded with ∞ and $-\infty$ in this chapter, but other value ranges for time expressions are possible and will be used in other parts of this thesis.

We define an event as a time value combined with an data value. The range of the data values are arbitrary, infinite data types are possible, also as empty data types, when only the point in time is relevant for the event. All TADL constraints are defined with attributes, which can be events, timing or arithmetic expressions or sets of them. Also, *EventChains* can be used as attributes. An *EventChain* consists of two sets of events (*stimulus* and *response*), which are causally related. All events in an *EventChain* must have a color value in their data field. This color possibly has an infinite type and an equality check on this must be defined. It is used to check, which events of an *EventChain* are directly related.



Figure 2.5.: Example DelayConstraint - lower = 2, upper = 3

DelayConstraint

The DelayConstraint has 4 attributes

```
source event set target event set lower \mathbb{T} (time expression) upper \mathbb{T}
```

and is defined as

```
\forall x \in source : \exists y \in target : lower \leq y - x \leq upper.
```

For all events x in *source*, there must be an y event in target, so that y lays between lower and upper 'after' x. Note, that lower and upper can have negative values and that additional events in target, without an associated source are allowed.

In 2.5 you see a visualized example of the DelayConstraint with the attributes lower = 2, upper = 3, $source = \{1, 5, 6\}$ and $target = \{2, 3.5, 5, 7, 8.2, 9\}$. The first element of source at timestamp 1 results in a required event in target between the timestamp 3 and 4 that is fulfilled by the event at 3.5. The second event of source requires an target event between 7 and 8, fulfilled by the event at 7. The last event of source is satisfied by the target event at 8.2 and 9.

StrongDelayConstraint

The StrongDelayConstraint has 4 attributes

```
source event set target event set lower \mathbb{T} (time expression)
```

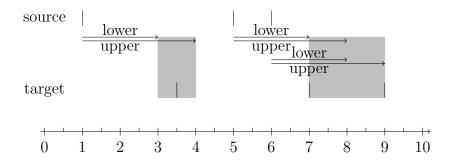


Figure 2.6.: Example StrongDelayConstraint - lower = 2, upper = 3

upper \mathbb{T}

and is defined as

```
|source| = |target| \land 
\forall i : \forall x : x = source(i) \Rightarrow \exists y : y = target(i) \land lower \leq y - x \leq upper.
```

The StrongDelayConstraint is a stricter version of the DelayConstraint, as it requires a bijective assignment between the source and target events, therefore additional events in target without matching source event are not allowed. In 2.6 you see an example of the StrongDelayConstraint. The example is the same as in the previous constraint, but without the additional target events at 2, 5 and 8.2.

RepeatConstraint

The RepeatConstraint also has 4 attributes

```
event event set lower \mathbb{T} (time expression) upper \mathbb{T} span integer
```

and is defined as

$$\forall X \leq event : |X| = span + 1 \Rightarrow lower \leq \lambda([X]) \leq upper.$$

As reminder, the $A \leq B$ -operator over two sets of events A, B describes, that A is a sub-sequence of B, the $\lambda(A)$ -function calculates the total length of all continuous intervals in A and the [A] returns the time interval between the oldest and newest event in A. The definition specifies that the length of each time interval containing

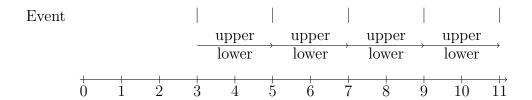


Figure 2.7.: Example RepeatConstraint - lower = 2, upper = 2, span = 1

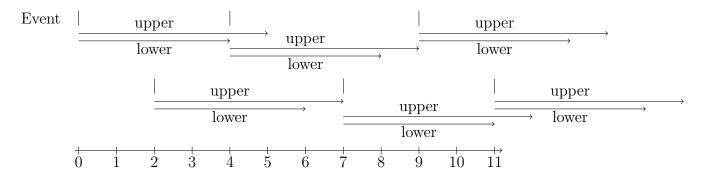


Figure 2.8.: Example RepeatConstraint - lower = 4, upper = 5, span = 2

span + 1 consecutively events must be between upper and lower.

The idea behind this constraint is to define repeated occurrences of events, with the possibility of overlapping, specified by the span attribute. After any event x, there are span-1 events and than the next event must be between lower and upper after x

In 2.7 you see an example of the RepeatConstraint with the attributes $event = \{1, 3, 5, ...\}$, lower = upper = 2 and span = 1. Because lower is equal upper and span is 1, the events are following a strict periodic pattern after the first event. 2.8 shows a more complex example with events at $\{0, 2, 4, 7, 9, 11, ...\}$, lower = 4, upper = 5 and span = 2. The span-attribute is 2, so the time distance between all subsequent events with an even index are considered, just like the subsequent events with an uneven index.

RepetitionConstraint

The RepetitionConstraint has 5 attributes

event event set lower \mathbb{T} (time expression) upper \mathbb{T} span integer

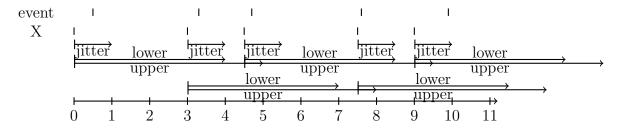


Figure 2.9.: Example Repetition Constraint - lower = 4, upper = 5, span = 2, jitter = 1

jitter \mathbb{T}

and is defined via the RepeatConstraint and the StrongDelayConstraint as

 $\exists X : RepeatConstraint(X, lower, upper, span) \land StrongDelayConstraint(X, event, 0, jitter)$

where X is a set of arbitrary time stamps, that follow the structure of the RepeatConstraint(various(span)) loose periodic repetitions). The actual points in time of event lay between the timestamps of X and jitter after that. For each point of time there is one, and only one, corresponding timestamp in X. In 2.9 you see an example of the RepetitionConstraint with the attributes $event = \{0.5, 3.3, 4.7, 7.6, 9.9, ...\}$, lower = 4, upper = 5, span = 2 and jitter = 1. The shown timestamps of X are only one possibility and may change due to later elements of event.

SynchronizationConstraint

The Synchronization Constraint has 2 attributes

```
\begin{array}{ll} event & \text{set of event sets, } |event| \geq 2 \\ tolerance & \mathbb{T} \end{array}
```

and is defined via the *DelayConstraint* as

```
\exists X : \forall i : DelayConstraint(X, event_i, 0, tolerance) \land DelayConstraint(event_i, X, -tolerance, 0)
```

X is a set of arbitrary point in time an there must be at least one timestamp in each set of event, that is between an element of X and tolerance after that. Also, for each element in any set of event, there must be a matching element of X. In 2.10 is an example of the SynchronizationConstraint with the attributes $event = \{\{0.5, 3, 7, 7.5\}, \{0.7, 2.5, 7.3, 7.8\}, \{1.2, 3.2, 3.3, 3.4, 7.6, 8.4\}\}$ and tolerance = 1. The

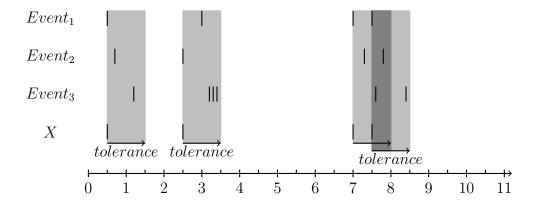


Figure 2.10.: Example SynchronizationConstraint - tolerance = 1

first points in time of each element of event form the first cluster, the corresponding element of X can be between 0.2 and 0.5. For simplification, only the latest possible value for the element of X are shown. In the second cluster of events you see that multiple timestamps from one element of event can be associated with a single element of X. The third and fourth cluster show, that overlapping is also possible.

StrongSynchronizationConstraint

The StrongSynchronizationConstraint has the same two attributes as the SynchronizationConstraint

```
\begin{array}{ll} event & \text{set of event sets, } |event| \geq 2 \\ tolerance & \mathbb{T} \end{array}
```

and is defined as

 $\exists X : \forall i : StrongDelayConstraint(X, event_i, 0, tolerance)$

The StrongSynchronizationConstraint is a stricter variant of the Synchronization-Constraint, as it requires a bijective assignment between the elements of X to one element of each set of event. For every $x \in X$, only one corresponding timestamp per set in event is allowed, like you can see in 2.11, which shows the same example as the one for the SynchronizationConstraint, but the excess time stamps at 3.2 and 3.3 have been removed.

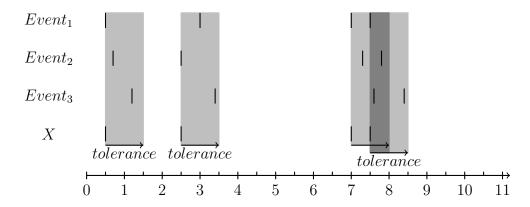


Figure 2.11.: Example StrongSynchronizationConstraint - tolerance = 1

ExecutionTimeConstraint

The Execution Time Constraints takes 4 attributes

```
\begin{array}{ccc} start & \text{set of events} \\ stop & \text{set of events} \\ preempt & \text{set of events} \\ resume & \text{set of events} \\ lower & \mathbb{T} \\ upper & \mathbb{T} \end{array}
```

and is defined as

 $\forall x \in start : lower \leq \lambda([x..stop] \setminus [preempt..resume]) \leq upper$

The interval constructor $\forall x \in start : [x..stop]$ defines the time interval between each point in time of start until the next element of stop, excluding the stop timestamp. [preempt..resume], which is removed from the considered interval length, defines the intervals between each element of preempt until the next timestamp of resume. The Idea behind this constraint is to test the run time of a task, without counting interruptions. 2.12 shows an example of the ExecutionTimeConstraints with $start = \{1\}$, $end = \{7\}$, $preempt = \{2,5\}$ and $resume = \{3,6.5\}$. Therefore, [start..end] spans the interval from time 1 to 7 with the length of 6 and [preempt..resume] spans two intervals, 2 to 3 and 5 to 6.5 with the length 1 and 1.5. As result, $\lambda([x..stop] \setminus [preempt..resume])$ for x = 1 is 3.5 and upper is greater than that.

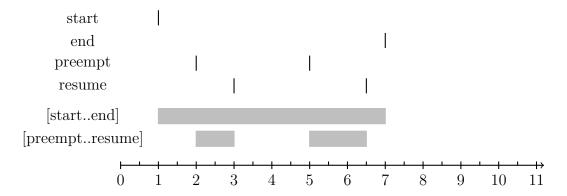


Figure 2.12.: Example ExecutionTimeConstraint



Figure 2.13.: Example OrderConstraint

OrderConstraint

The OrderConstraint takes two attributes

```
source set of events
target set of events
```

and is defined as

$$|source| = |target| \land \forall i : \exists x : x = source(i) \Rightarrow \exists y : y = target(i) \land \langle x \leq y \rangle$$

This constraints ensures the order of events, so that the i-th event of target is after the i-th event of source. Also, the number of events in source and target must be equal.

In 2.13 you see an example of the OrderConstraint with $source = \{1, 4, 6, 7\}$ and $target = \{3, 5, 9, 9.5\}$. The constraint is fulfilled, because the number of elements is equal for both sets and each i-th timestamp in target is later that the i-th timestamp of source.

ComparisonConstraint

The ComparisonConstraint is significant different to all previous and following constraints, as it does not describe the behavior of events, and only compares two timing expressions. It takes 3 attributes

The definition is pretty straight forward as it only applies the given operator to the operands:

```
ComparisonConstraint(leftOperand, rightOperand, LessThanOrEqual) \\ \Leftrightarrow leftOperand \leq rightOperand \\ ComparisonConstraint(leftOperand, rightOperand, LessThan) \\ \Leftrightarrow leftOperand < rightOperand \\ ComparisonConstraint(leftOperand, rightOperand, GreaterThanOrEqual) \\ \Leftrightarrow leftOperand \geq rightOperand \\ ComparisonConstraint(leftOperand, rightOperand, GreaterThan) \\ \Leftrightarrow leftOperand > rightOperand \\ ComparisonConstraint(leftOperand, rightOperand, Equal) \\ \Leftrightarrow leftOperand = rightOperand \\
```

Due to the simplicity of this constraint, no explicit example is given.

SporadicConstraint

The SporadicConstraint takes 5 attributes

```
\begin{array}{ccc} event & \text{set of events} \\ lower & \mathbb{T} \\ upper & \mathbb{T} \\ jitter & \mathbb{T} \\ minimum & \mathbb{T} \end{array}
```

and is defined via the Repetition- and the RepeatConstraint as

RepetitionConstraint(event, lower, upper, 1, jitter)

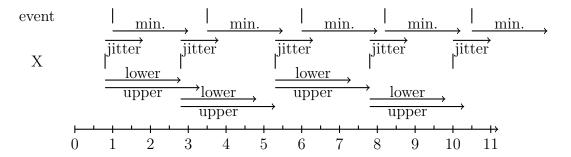


Figure 2.14.: Example SporadicConstraint - lower = 2, upper = 2.5, jitter = 1, minimum = 2

 $\land RepeatConstraint(event, minimum, \infty, 1)$

The second part of the definition, using the RepeatConstraint, ensures that all events in event lay at least minimum apart. The application of the RepetitionConstraint generates a set of events X, that lay between lower and upper apart. For each point of time in X, there must be exactly one timestamp in event, that is not before the corresponding entry of X and not later than jitter after that.

2.14 shows a possible utilization of the SporadicConstraint with the attributes lower = 2, upper = 2.5, jitter = 1, minimum = 2 and $event = \{1, 3.5, 6, 8.2, 10.5, ...\}$. As in the RepetitionConstraint, the exact position of the timestamps in X is variable and may need to be changed due to later entries in event.

PeriodicConstraint

The PeriodicConstraint takes 4 attribute

 $\begin{array}{ccc} event & \text{set of events} \\ period & \mathbb{T} \\ jitter & \mathbb{T} \\ minimum & \mathbb{T} \end{array}$

and defines a specialized form of the Sporadic Constraint

SporadicConstraint(event, period, period, jitter, minimum)

The variable timestamps in the set X are now following a strictly periodic pattern, where subsequent elements of this set lay exactly period apart. Each element of event lays between one element of X and jitter after that. Again, there must be bijective mapping between the elements of event and X.

In 2.15, the PeriodicConstraint with the attributes period = 3, jitter = 1, minimum = 1

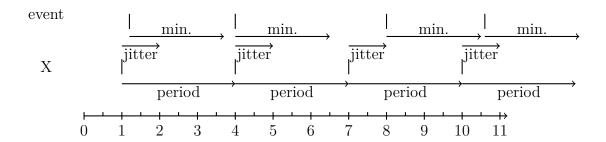


Figure 2.15.: Example PeriodicConstraint - period = 3, jitter = 1, minimum = 2.5

2.5 and $event = \{1.2, 4.0, 8, 10.6, ...\}$ is visualized. The timestamps of X lay exactly period apart and the events behind that in the previously described way. Also, the minimum time distance between all points of time in event is minimum.

PatternConstraint

The PatternConstraint takes 5 attributes

```
\begin{array}{ccc} event & \text{set of events} \\ period & \mathbb{T} \\ of\!fset & set of\! \mathbb{T} \\ jitter & \mathbb{T} \\ minimum & \mathbb{T} \end{array}
```

and is defined as

```
\exists X : PeriodicConstraint(X, period, 0, 0) \\ \land \forall i : DelayContraint(X, event, offset_i, offset_i + jitter) \\ \land RepeatConstraint(event, minimum, \infty, 1)
```

It can be understood as a modification of the PeriodicConstraint, as it describes periodic behavior, but not from single events, but from groups of |offset| events, that follow specific time distances (specified by offset) after the strictly periodic timestamps of X.

2.16 shows an application of the PeriodicConstraint with attributes period = 5, $offset = \{1, 2, 2.5\}$, jitter = 0.5, minimum = 0.5 and $event = \{1.2, 2.2, 2.8, 6, 7, 8, 11.5, 12, 12.5, ...$ Like in the previous describes constraint, the exact position of all points in time of X may change due to later timestamps of event.

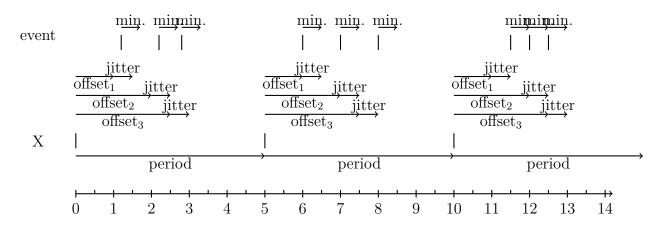


Figure 2.16.: Example PatternConstraint - period = 5, $offset = \{1, 2, 2.5\}$, jitter = 0.5, minimum = 0.5

ArbitraryConstraint

The Arbitrary Constraint takes 3 attributes

 $\begin{array}{ll} & event & \text{set of events} \\ & minimum & set of \mathbb{T} \\ & maximum & set of \mathbb{T} \end{array}$

where |minimum| = |maximum|. It is defined as

 $\forall i : RepeatConstraint(event, minimum_i, maximum_i, i)$

The Idea behind the *ArbitraryConstraint* is to describe the time distance between several subsequent events. The first entries of *minimum* and *maximum* define the distance between each event and it direct successor. The second entries, where the *span* attribute of the *RepeatConstraint* is 2, set the distance between the one event and its next but one successor and so on.

2.17 show an example of the Arbitrary Constraint with the attributes $minimum = \{1, 2, 3\}$, $maximum = \{5, 6, 7\}$ and $event = \{1, 2, 3, 5, 8, 10, ...\}$. The time distances between subsequent events with 0, 1 and 2 skipped events are shown in 2.1, the relevant distances are written in **bold** font. Apparently, the time distances math the ranges, given by the minimum- and maximum attribute.

	1	2	3	5	8	10
1	0	1	2	4	7	9
2		0	1	3	6	8
3			0	2	5	7
5				0	3	5
8					0	2
10						0

Table 2.1.: Time distances as seen in 2.17

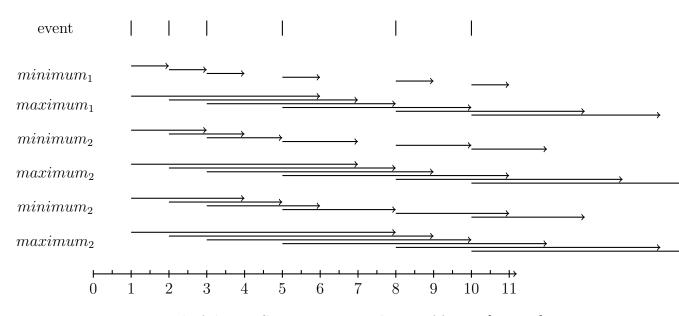


Figure 2.17.: Example Arbitrary Constraint - $period = 5, offset = \{1, 2, 2.5\}, jitter = 0.5, minimum = 0.5$

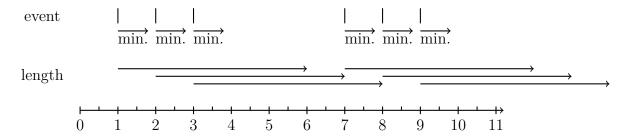


Figure 2.18.: Example BurstConstraint - length = 5, maxOccurences = 3 minimum = 0.8

BurstConstraint

The BurstConstraint takes 4 attributes

$$\begin{array}{ccc} & event & \text{set of events} \\ & length & \mathbb{T} \\ \\ maxOccurrences & integer \\ & minimum & \mathbb{T} \end{array}$$

and is defined as

 $RepeatConstraint(event, length, \infty, maxOccurrences) \\ \land RepeatConstraint(event, minimum, \infty, 1)$

The idea of this constraint is to describe the maximum number of events, that may occur in an time interval of the given *length* and all subsequent event must be at least *minimum* apart. Therefore, the intuition is different to the AUTOSAR *BurstPatternEventTriggering*, where clusters of events are described. A complete comparison of these constraints will be done in 2.2.3.

In 2.18 the BurstConstraint with the attributes length = 5, maxOccurrences = 3, minimum = 0.8 and $event = \{1, 2, 3, 7, 8, 9\}$ is visualized. In every interval of the length 5, there are three or less events, also all subsequent events lay at least 0.8 apart. Therefore, the constraint is fulfilled.

ReactionConstraint

The ReactionConstraint takes 3 attributes

 $scope \quad EventChain$ $minimum \quad \mathbb{T}$ $maximum \quad \mathbb{T}$

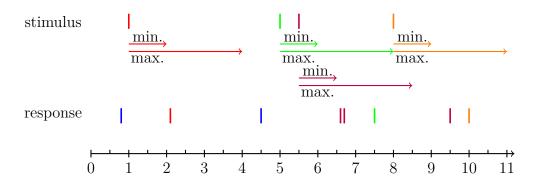


Figure 2.19.: Example ReactionConstraint - minimum = 1, maximum = 3

and is defined as

```
\forall x \in scope.stimulus : \exists y \in scope.response : \\ x.color = y.color \\ \land (\forall y' \in scope.response : y'.color = y.color \Rightarrow y \leq y') \\ \land minimum \leq y - x \leq maximum
```

The definition says, that after all events x of scope.stimulus, there is an event y in scope.response with the same color. The time distance between these events must be at least minimum and at most maximum. Additional events with the same color as y in scope.response are allowed, if they lay behind y. The definition implies, that additional events with other colors are allowed in scope.response, but not in scope.stimulus and each color is only allowed once in scope.stimulus. A visualized example with the attributes minimum = 1, maximum = 3, $scope.stimulus = \{(1, red), (5, green), (5.5, purple), (8, orange)\}$ and $scope.response = \{(0.8, blue), (2.1, red), (4.5, blue), (6.6, purple), (6.7, purple), (9.5, purple), (7.5, green), (10, orange)\}$ can be seen in 2.19. The red stimulus-event is followed by the red response-event at 2.1, the green stimulus-event at 5 by the response-event at 7.5 and so on. The blue response-events at 1 and 4.5 are additional events without an associated stimulus event. The purple events at 6.7 and 9.5 are the second and third event of this color in scope.response and therefore, their time distance to the stimulus event with the same color is irrelevant.

AgeConstraint

The AgeConstraint takes 3 attributes

```
scope \quad EventChain
minimum \quad \mathbb{T}
maximum \quad \mathbb{T}
```

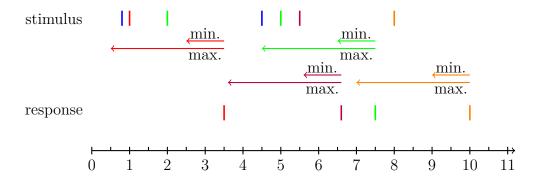


Figure 2.20.: Example AgeConstraint - minimum = 1, maximum = 3

and is defined as

```
\forall y \in scope.response : \exists x \in scope.stimulus : \\ x.color = y.color \\ \land (\forall x' \in scope.stimulus : x'.color = x.color \Rightarrow x' \leq x) \\ \land minimum \leq y - x \leq maximum
```

The AgeConstraint is a turned around alternative to the ReactionConstraint. For every event of scope.response, there must be an event with the same color in scope.stimulus, that is between minimum and maximum older than the response event. Additional events are only allowed in scope.stimulus, and only before the event, that matches with a response event. 2.20 shows an application of the AgeConstraint with the attributes minimum = 1, maximum = 3, $scope.stimulus = \{(0.8, blue), (1, red), (2, green), (4.5, green), (5, green), (5.5, purple), (8, orange)\}$ and $scope.response = \{(3.5, red), (7.5, green), (6.6, purple), (10, orange)\}$. The blue timestamps are additional events without matching events in scope.response.

OutputSynchronizationConstraint

The OutputSynchronizationConstraint takes 2 attributes

```
scope Set of Event Chain
tolerance T
```

where all elements of *scope* have the same *stimulus*. It is defined as

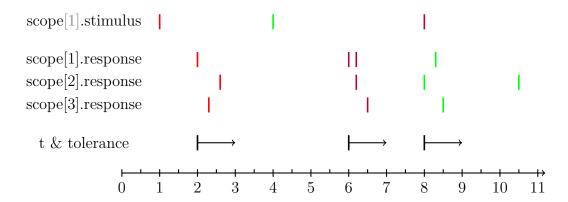


Figure 2.21.: Example OutputSynchronizationConstraint - tolerance = 1

The definition says, that after each event x in $scope_1.stimulus$, there must be a interval with the length of tolerance, in which every $scope_i.response$ must have an event y with the same color as x. Additional response events with this color are only allowed after y. 2.21 shows an example of the OutputSynchronizationConstraint with the attributes tolerance = 1,

```
scope[1].stimulus = scope[2].stimulus = scope[3].stimulus = \{(1,red), (4,green), (8,purple)\},\\ scope[1].response = \{(2,red), (6,purple), (6.2,purple), (8.2,green)\},\\ scope[2].response = \{(2.6,red), (6.2,purple), (8,green), (10.5,green)\},\\ scope[3].response = \{(2.3,red), (6.5,purple), (8.5,green)\}.\\ As you can see, only time distance between the response events are relevant, the distance between stimulus and response is not observed and may also be negative, as you can see in the purple events.
```

InputSynchronizationConstraint

The InputSynchronizationConstraint takes 2 attributes

```
scope Set of Event Chain
tolerance \mathbb{T}
```

where all elements of *scope* have the same *response*. It is defined as

```
\forall y \in scope_1.response : \exists t : \forall i : \exists x \in scope_i.stimulus : x.color = y.color 
 \land (\forall x' \in scope_i.stimulus : x'.color = x.color \Rightarrow x \leq < x') 
 \land 0 \leq x - t \leq tolerance
```

The InputSynchronizationConstraint is a counterpart of the OutputSynchronization-Constraint, as the stimulus events must be synchronized, not the response events.

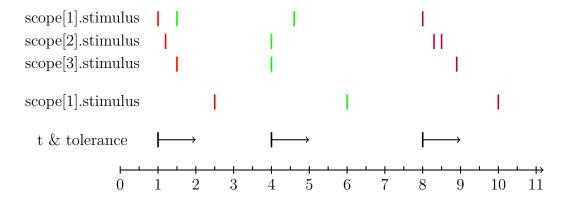


Figure 2.22.: Example InputSynchronizationConstraint - tolerance = 1

2.22 contains an example of the InputSynchronizationConstraint with the attributes tolerance = 1

```
scope[1].stimulus = \{(1, red), (1.5, green), (4.6, green), (8, purple)\}
scope[2].stimulus = \{(1.2, red), (4, green), (8.3, purple), (8.5, purple)\}
scope[3].stimulus = \{(1.5, red), (4, green), (8.9, purple)\}
scope[1].response = scope[2].response = scope[3].response = \{(2.5, red), (6, green), (10, purple)\}
```

2.2.3. Comparison TADL2 - AUTOSAR Timing Extension

As said before, the TADL2 Timing Constraints and the AUTOSAR Timing Extension are compatible in parts and many of the AUTOSAR Timing Extension can be expressed as equivalent combinations of the TADL2 Timing Constraints. In [BFL+12], the relation between these constraints is shown, but this comparison is based on an outdated version of the AUTOSAR Timing Extensions and some of the constraints have been updated, therefore each of the AUTOSAR Timing Extensions will be listed in this chapter and it will be explained, if and how they can be expressed using TADL2 Timing Constraints.

The types used in the AUTOSAR Timing Extension are similar to the ones in TADL2. TADL2 Events are called TimingDescriptionEvent in AUTOSAR, the same goes for EventChains, which are called TimingDescriptionEventChains. A larger difference can be seen in the definition of time. While TADL2 defines time as real numbers, the time definition used in the AUTOSAR Timing Extension can also be multidimensional, for example when the real time and the angle of the crankshaft is regarded. For simplification, all timestamps are considered as real numbers in the following, but an extension to multidimensional time stamps is possible, as AUTOSAR requires a strict order between all time stamps. Executable entities as defined in the AUTOSAR Timing Extension describe things, that can be

executed, for example a function. For the timing constraints, only striking point in times of these entities are relevant, for example the start or end points. It should be noted, that the set of TADL2 timing constraints are not equal to the AUTOSAR Timing Extension and that there are constraint, that cannot be expressed using the corresponding counterpart.

PeriodicEventTriggering

The PeriodicEventTriggering defined in AUTOSAR with the attributes (event, period, jitter, minimumInterArrivalTime) is equivalent to the TADL2 PeriodicConstraint with the same attributes.

SporadicEventTriggering

AUTOSARs SporadicEventTriggering with the attributes

(event, jitter, maximumInterArrivalTime, minimumInterArrivalTime, period) is equivalent to the TADL2 SporadicConstraint, but the names of the attributes are different:

```
lower = period

upper = maximumInterArrivalTime

jitter = jitter

minimum = minimumInterArrivalTime
```

ConcretePatternEventTriggering

The idea behind the *ConcretePatternEventTriggering* from AUTOSAR is the same as behind TADL2s *PatternConstraint*, but subtleties are different. Both define a periodic behavior and offsets, that describe time distances between the periods and the actual events. The main difference is the *jitter* attribute. In AUTOSARs *ConcretePatternEventTriggering*, the *patternJitter* attribute defines the allowed deviation of the start points of the periodic repetitions, as in TADL2 the *jitter*-value describes the deviation between the offsets and the actual event.

The ConcretePatternEventTriggering from AUTOSAR additionally defines an patternLength attribute, which describes the length of the intervals, in which the clusters of events will occur. It is constrained by

```
0 \leq max(offset) \leq patternLength \\ \wedge patternLength + patternJitter < patternPeriod
```

The patternLength attribute can not be described with TADL2 timing constraints,

as it would require to determine the distance of filtered events, which is not possible with the TADL2 constraints.

TADL2 defines the *minimum* attribute for the *PatternConstraint* that describes the minimal time distance between subsequent events. In AUTOSAR, this must be described by using the *ArbitraryEventTriggering*, where $minimumDistance_1$ is minimum and $maximumDistance_1$ is ∞ .

BurstPatternEventTriggering

The BurstPatternEventTriggering as defined in AUTOSAR and TADL2s BurstConstraint share the same target, as they define a maximum number of events that may occur in a specific time interval, but the BurstPatternEventTriggering is way more complex. Additionally to the attributes of TADL2s BurstConstraint, that define the length of the time interval, the maxOccurrences of the event in this interval and the minimal time between subsequent events, the BurstPatternEventTriggering allows to define the minimal number of events in the interval and periodic repetitions of the burst interval.

Every set of attributes fulfilling the TADL2 BurstConstraint fulfill the BurstPatternEventTriggering, when the attributes are renamed to the AUTOSAR equivalents ($length \rightarrow patternLength$, $maxOccurences \rightarrow maxNumberOfOccurences$, $minimum \rightarrow minimumInterArrivalTime$). This does not work the other way around, even if the attributes, that are in BurstPatternEventTriggering and not in BurstConstraint are unused. The reason for this is, that the observed interval must start at an event in the TADL2 BurstConstraint, in the BurstPatternEventTriggering those can start in any point of time.

ArbitraryEventTriggering

AUTOSARs ArbitraryEventTriggering is similar to the ArbitraryConstraint as defined in TADL2, but ArbitraryEventTriggering allows to set a list of ConfidenceIntervals, to describe the probability, how far the events may lay apart. These probabilities can not be expressed in TADL2.

LatencyTimingConstraint

The LatencyTimingConstraint of AUTOSAR takes 5 attributes, a latency type $latencyConstraintType \in \{age, reaction\}$, three time values maximum, minimum and nominal and an event chain scope, consisting of the stimulus and response events. The nominal-value is not relevant for a formal definition of the Constraint, therefore there is no counterpart to this in the TADL2 Constraints. If the

latencyConstraintType of the LatencyTimingConstraint is age, it can be expressed with AgeConstraint defined in TADL2. The LatencyTimingConstraint with the latencyConstraintType reaction is equivalent to the reactionConstraint.

AgeConstraint

The goal of the AgeConstraint is the same for the LatencyTimingConstraint with the latencyConstraintType age, but scope is defined with the type TimingDescriptionEvent, not as TimingDescriptionEventChain. The reason for this is, that it can be used in earlier development phases, as it is an abstract type. There is no differentiation like this in TADL2 and the AgeConstraint is semantically the same in AUTOSAR and TADL2.

SynchronizationTimingConstraint

The Synchronization Timing Constraint is similar to the Synchronization Constraint, the Strong Synchronization Constraint, the Output Synchronization Constraint, the Input Synchronization Constraint or combinations of them, depending on the attributes. 2.2 shows, with which attributes the Synchronization Timing Constraint is equivalent to which TADL2 Constraint(s).

SynchronizationPointConstraint

The SynchronizationPointConstraint describes, that a list of executables and a list of events or executable entities, defined in sourceEec and sourceEvent, must finish and occur, before the executables and events in targetEec and targetEvent will start or occur. There is no counterpart to this in the TADL2 constraints.

OffsetTimingConstraint

The Offset Timing Constraint, defined in AUTOSAR Timing Extensions, is semantically the same as the TADL2 Delay Constraint, just some attributes are named differently. The maximum attribute of the Offset Timing Constraint is named upper and the minimum attribute lower in the Delay Constraint.

event Occurrence- Kind	scope/ scopeEvent	synchronization- ConstraintType	tolerance	TADL2 Constraints
multiple Occurrences	scopeEvent	not set	tolerance	SynchronizationConstraint (scopeEvent, tolerance)
single Occurrences	scopeEvent	not set	tolerance	StrongSynchronizationConstraint (scopeEvent, tolerance)
multiple Occurrences	scope	response Synchronization	tolerance	OutputSynchronizationConstraint (scope, tolerance) ^ SynchronizationConstraint (scope.response, tolerance)
single Occurrences	scope	response Synchronization	tolerance	OutputSynchronizationConstraint (scope, tolerance) ^ StrongSynchronizationConstraint (scope.response, tolerance)
multiple Occurrences	scope	stimulus Synchronization	tolerance	InputSynchronizationConstraint (scope, tolerance) ∧ SynchronizationConstraint (scope.stimulus, tolerance)
single Occurrences	scope	stimulus Synchronization	tolerance	InputSynchronizationConstraint (scope, tolerance) ^ SynchronizationConstraint (scope.stimulus, tolerance)

 Table 2.2.:
 SynchronizationTimingConstraint
 \Leftrightarrow TADL2 Constraints

ExecutionOrderConstraint

The goal of ExecutionOrderConstraint of the AUTOSAR Timing Extensions is to describe the order of events or the execution order of executable entities, defined as orderedElement attribute. There is no constraint in TADL2 that describes exactly this, but if the ExecutionOrderConstraint is used to describe only the order of events, it can be described as

```
OrderConstraint(orderedElement_1, orderedElement_2)
 \land ... \land
 OrderConstraint(orderedElement_{n-1}, orderedElement_n)
```

If the *ExecutionOrderConstraint* is used for executable entities, each executable entity must be turned into one or more events to be described via TADL2 Constraints, depending on the other attributes. For example, if the attribute *executionOrder-ConstraintType* is set to *ordinaryEOC*, the start and finish points of the entities define the observed events.

ExecutionTimeConstraint

The idea behind the Execution Time Constraint is similar in AUTOSAR and TADL2. Both describe the minimal and maximal allowed run time of an executable entity, but the TADL2 constraint is capable of not counting interruptions in the execution. On the other hand, the AUTOSAR constraint offers the possibility, to determine if external calls should be included in the run time or not. Also, AUTOSARs Execution Time Constraint is defined directly on an executable entity and the TADL2 constraint on events describing the start, stop, preemption and resume timestamps. Therefore the executable entity must be turned into these events to express the AUTOSAR Execution Time Constraint via TADL2 constraints. The start and stop times need to be turned into their obvious counterparts. If the run time of external calls should not be counted (the execution Time Type attribute is set to net), the start and stop points of these external calls must be moved into the preempt and resume event sets. If the execution Time Type attribute is set to gross, external calls are ignored and the complete time from the start to the end of the execution is counted, therefore the preempt and resume event remain empty.

3. Related work and basics

3.1. Runtime Verification

Monitoring the AUTOSAR Timing Extensions is the goal of this thesis. As monitoring plays a major role in runtime verification, a short overview of this will be given. The definitions of [Run] are used, in which Runtime Verification is a technique that can detect deviations between the run of a system and its formal specification by checking correctness properties. A run, which might also be called trace, is sequence of the system states, which might be infinite and an execution is an finite prefix of this run. A monitor reads the trace and decides, whether it fulfills the correctness properties or violates them.

A distinction is made between *offline* and *online* monitoring. Offline monitoring is using a stored trace, that has been recorded before. Therefore, the complete trace (or the complete part of the trace, that should be analyzed) is known in the analysis. Online monitoring checks the properties, while the system is running, which means that the analysis must be done incrementally. Because of memory and time limitations, not all previous states can be read again in online monitoring, more detailed contemplations on the limitations of online monitors will be given in 4.

3.2. TeSSLa

TeSSLa (Temporal Stream-based Specification Language) is a functional programming language, build for runtime verification of streams. In TeSSLa, streams are defined as traces of events, each event consists of one data value from a data set \mathbb{D} and a time value from a discrete time domain \mathbb{T} . This time domain needs a total order and subsequent timestamps must have increasing time values. A TeSSLa Specification can have several streams with different data sets, but each of these streams must use the same time domain \mathbb{T} , which timestamps are increasing over all streams. Each stream can have only one event per timestamp, but it is possible to have events on different streams at the same timestamp.

A distinction between synchronous and asynchronous streams is made. A set of synchronous streams have events in the exact same time stamps, events in asynchronous streams do not have this restriction. It is easy to see, that synchronous streams are

a subset of the asynchronous ones, therefore we will only use asynchronous streams from now on.

In TeSSLa, calculations are done, when new events are arriving. Based on the specification, output streams are generated with events on the same timestamps as the used input streams, but filtering is possible, where not all input events produce output events. With the *delay*-operator, it is possible to create new timestamps. This possibility will take a large role in this thesis, more on that later.

At the timestamps, in which events arrived and calculations are done, you only have direct access to the youngest event of each stream, but with the use of the *last*-operator, which can be used recursively, the event before that can be accessed. The *lift*-operator applies a function, which is defined on data values \mathbb{D} , on each event of one or more streams. Similar to this, the *slift*-operator (signal lift) first applies the given function, when there was at least one event of each input stream. The *time*-operator returns the time value of an event.

3.3. Finite Transducers

4. Monitorability of properties on infinite Streams

The goal of this paper is to implement an online monitor for TADL2 Timing Constraint on possibly infinite streams using embedded hardware, like FPGAs or small ARM based computers. Because of finite resources, several constraints must be fulfilled, to get correct results in a reasonable time in every case. Therefore, the term of *Finite Monitorability* will be introduced, which ensures that monitoring is possible using the mentioned setting.

4.1. Finite Monitorability

4.1.1. Timestamps

As we consider streams that can be infinite, the time value of events can also grow into infinity. This is problematic, because it leads to infinite memory and runtime requirements, which cannot be meet, especially not in the context of online monitoring. Therefore, the time domain T must be restricted by the following constraints:

- T must be discrete.
- The first used timestamp has the value $t_0 = 0$
- All used timestamps must be smaller than t_{max} . t_{max} must be big enough, so it is not reached in practical use ¹.
- The distance between two subsequent time values is small enough to observe the wanted constraints.

4.1.2. Finite Monitorability

For the definitions of streams and functions defined on them, TeSSLa-like syntax is used. Also, some standard TeSSLa functions are used in the definitions.

¹for example, a 64-bit unsigned integer variable is enough, to cover nanoseconds for 584.55 years

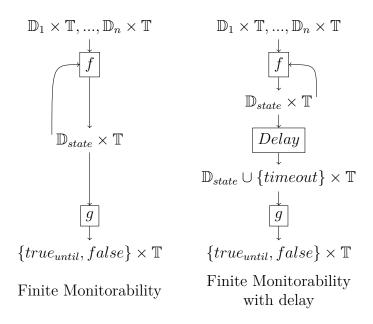


Figure 4.1.: Overview Finite Monitorability - with or without delay

Input Streams

```
Let S_1, S_2, ..., S_n be input streams with \forall i : S_i = (\mathbb{T} \cdot \mathbb{D}_i)^{\omega} \cup (\mathbb{T} \cdot \mathbb{D}_i)^+ \cup (\mathbb{T} \cdot \mathbb{D}_i)^* \cdot (\mathbb{T}_{\infty} \cup \mathbb{T} \cdot \{\bot\}) and All types D_i have a finite size.
```

State Stream

```
Let S_{state} with S_{state} = (\mathbb{T} \cdot \mathbb{D}_{state})^+ \cup (\mathbb{T} \cdot \mathbb{D}_{state})^* be a state stream, where \mathbb{D}_{state} has a finite size. Further let f: S_1 \times S_2 \times ... \times S_n \times S_{state} \to S_{state} \times \mathbb{T} a state transition function, which defines the state stream in an incremental fashion: \forall t \in \mathbb{T} \exists i \in \{1, 2, ..., n\}: S_i(t) \in \mathbb{D}_i \to S_{state}(t) = f(S_1(t), S_2(t), ..., S_n(t), last(S_{state}, merge(S_1, S_2, ..., S_n))(t)) The runtime of f is in \mathcal{O}(1).
```

Output Stream

Let $S_{output} = (\mathbb{T} \cdot \{true_{until}, false\})^+ \cup (\mathbb{T} \cdot \{true_{until}, false\})^*$ be the output stream, which is defined via a function

 $g: \mathbb{D}_{state} \times \mathbb{T} \to \{true_{until}, false\} \times \mathbb{T}$ The runtime of g is in $\mathcal{O}(1)$.

Evaluation

A property of a set of streams is called *Finite Monitorable*, if a function f with type \mathbb{D}_{state} and a function g exist, which fulfill the characteristics called above, and which outputs $true_{until}$, as long as the property is fulfilled and false, in any other case. It should be noted that these definitions are $timestamp\ conservative$, because the streams S_{state} and S_{output} can only change their data value at the timestamps of input events.

Equivalences

4.1.3. Finite Monitorability with Delay

Not all of the TADL2 constraints can be monitored in a timestamp conservative. For example, the RepeatConstraint with the attributes lower = upper = 4 and span = 1 expects subsequent events to have a time distance of 4. If one event is missing, the output of a timestamp conservative monitor would still be $true_{until}$, until the next input event arrives. Therefore, the monitor cannot not check the constraint correctly. Because of this problem, the definition of $Finite\ Monitorability$ is expanded by the ability of introducing new timestamps. To ensure the finiteness of the monitor, only one new timestamp can be introduced, more on that in 4.1.3.

Input Streams

The definition of the input streams are unchanged.

State Stream

The function f remains unchanged, but the state stream S_{state} is expanded by an timeout value, which is inserted after a specific period of time, in which no input event has arrived.

Delay

A $Delay\ Generator$ is inserted into the definition. It has two tasks, first it copies each input it gets from the state transition function f to its output. At the timestamp where an input is copied, a timer, which length depends on the state of the monitor, is started. If the next input comes before the timer runs out, the timer is resetted and started again. If the timer runs out, the Delay Generator outputs the timeout signal, which is repeated at every following input. After the timer has run out once, it is not started again.

Output Stream

The output function g is expanded by the timeout value: $g: (\mathbb{D}_{state} \cup \{timeout\}) \times \mathbb{T} \to \{true_{until}, false\} \times \mathbb{T}$ The definition of the output stream S_{output} remains unchanged.

Evaluation

A property of a set of streams is called *Finite Monitorable with Delay*, if a function f with type \mathbb{D}_{state} , a delay generator and a function g exist, which fulfill the characteristics called above, and which outputs $true_{until}$, as long as the property is fulfilled and false, in any other case.

4.1.4. Non-Finite Monitorability

Not all TADL2 constraints are finite monitorable, because a monitor would require infinite memory and/or time resources. In a theoretical view, this makes online monitoring on infinite traces impossible, because a machine with infinite resources does not exist in the real world. In a practical view, many of these problems are solved by using a system with finite memory, with the hope that this finite resources would be enough, to cover the inputs of the "real world". In these cases, a distinction is useful, as some constraints have resource requirements, that grow continuously with every input event. These constraints will be called always Non-Finite Monitorable. Others constraints only require infinite resources in worst case scenarios, therefore these will be called worst case Non-Finite Monitorable. Obviously, the constraints with continuous resource requirement growth cannot be monitored infinitely, but the constraints, that only need infinite resources, can be monitored in many cases.

In the next chapter, each of the TADL2 constraints will classified into *Finite Monitorable*, *Finite Monitorable with Delay* and *Non-Finite Monitorability*. For the last class, it will be demonstrated, if the constraint is non-finite monitorable in any cases or just in worst case scenarios.

5. Analysis of the Monitorability of the TADL2 Timing Constraints

5.1. DelayConstraint

The *DelayConstraint* describes that in the time interval between *lower* and *upper* after any *source* event, there is an *target* event. Therefore, the state that need to be stored to monitor the *DelayConstraint* is the set of *source* events, that did not have a matching *target* event. Updates to this state and outputs of the monitor are done at *source* and *target* events and at delay timestamps *upper* after *source* events, if there hasn't been a matching *target* event.

The maximal required storage size of the state depends on the number of source events, which can possibly occur in any time interval of the length upper. An example of this worst case situation can be seen in 5.1. The attributes in this example are lower = upper = 5, $source = \{1, 1.1, ..., 5.9\}$ and $target = \{6, 6.1, ..., 11\}$. At timestamp 6, all 49 source events must be stored, as they are all required to generate the correct output in this and the following timestamps. At this timestamp, the oldest source event can be removed from the storage, as the matching target event occurs in this timestamp. With every following target, the oldest event can be removed from the storage, until every source had its matching target event at timestamp 11.

Because the time domain is understood as real numbers in TADL2, a possibly infinite number of events can be placed in any interval of the length *upper*, therefore the required storage space is infinite. Because the *source* events are removed from the state, when a matching *target* event occurs, the required storage space does not grow continuously and infinite resources are only required in worst case scenarios. Therefore, the *DelayConstraint* is *worst case Non-Finite monitorable*.

5.2. Strong Delay Constraint

The difference between the *DelayConstraint* and the *StrongDelayConstraint* is, that for every *source* event, there must be exactly one matching *target* event in the *StrongDelayConstraint*. Therefore, the state of the monitor is nearly the same,

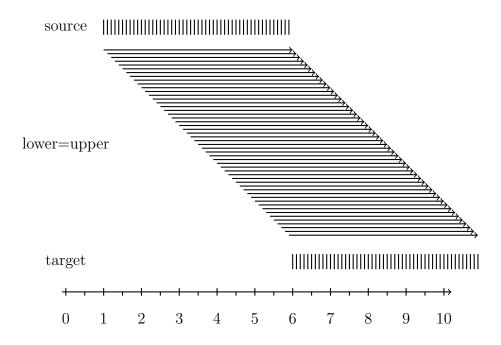


Figure 5.1.: DelayConstraint or StrongDelayConstraint with lower = upper = 5

as every *source* event, that did not have a matching *target* event yet, must be stored. Therefore, the only difference is, when these *source* events are removed from state and the *StrongDelayConstraint* is *worst case Non-Finite monitorable*, like the *DelayConstraint*.

5.3. RepeatConstraint

The RepeatConstraint defines the time distance between each event and its $span^th$ successor. Therefore, the state, that must be stored, consists of the span + 1 latest events. The state is updated at every event, the oldest stored event is removed and the timestamp of the current event is placed in the storage. The output function checks, if the time distance between the oldest stored event and the current timestamp is between lower and upper. To monitor this constraint, a single delay is required, because a missing event, or an event that occurs too late, would not be determined in the right timestamp.

As the memory requirements are fix (span + 1 timestamps must be stored) and the state transition and output function can be programmed in a way that they are in $\prime(1)$, the RepeatConstraint is finite monitorable with delay.

5.4. RepetitionConstraint

The RepetitionConstraint is defined as

```
RepetitionConstraint(s, lower, upper, span, jitter)

\equiv \exists X \subset \mathbb{T} : RepeatConstraint(X, lower, upper, span)

\land StrongDelayConstraint(X, s, 0, jitter)
```

The elements of set X follow the RepeatConstraint and the events, which should be monitored, are following in an interval of the length jitter after the elements of X. For each element of X, there is exactly one event and vice versa.

The monitoring algorithm for this constraint, which will be explained in detail in 6, stores the upper and lower bounds for the next span elements of X. These borders are stored in a list and calculated by

```
lowerBound := List\_append(last(List\_tail(LowerBound), s), lowerBoundNow + lower) \ for the lower bound and \\ upperBound := List\_append(last(List\_tail(UpperBound), s), upperBoundNow + upper).
```

The oldest item in these lists (the head of these lists) are removed and the newly calculated bounds for the span next element of X is inserted. lowerBoundNow and upperBoundNow are the describing the limitations of the element of X right before the current event. They are calculated using the list mentioned above and the timestamp of the current event by the following definition:

```
lowerBoundNow := max(List\_head(last(LowerBoundX, s)), time(s) - jitter)
upperBoundNow := min(List\_head(last(UpperBoundX, s)), time(s))
```

If the timestamp of the current event is between lowerBoundNow and upperBoundNow, the output of the monitor is true, in any other case, or when the delay ran out, it is false.

The size of these lists has a fixed upper limit (span) and the state transition and output functions are in $\mathcal{O}(1)$, therefore the RepetitionConstraint is finite monitorable with delay.

5.5. SynchronizationConstraint

The *SynchronizationConstraint* describe groups of event sets, which events occur in common clusters. Each of these sets must have at least one event in each of these intervals. Any events, that lay outside of these intervals are prohibited.

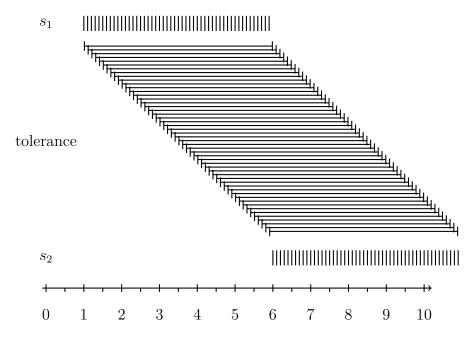


Figure 5.2.: SynchronizationConstraint or StrongSynchronizationConstraint with tolerance = 5

5.2, which is similar to the example for the DelayConstraint, shows an example of this constraint, which is an worst case scenario in terms of monitoring. The tolerance interval is 5 timestamps long, the event set s_1 contains the events $\{1, 1.1, ..., 5.9\}$ and s_2 is containing $\{6, 6.1, ..., 11\}$. Each of the events of s_1 must be stored until the end of the tolerance interval, otherwise it would be impossible to check the constraint correctly. Like described in 5.1, an infinite number of events can be placed in this interval, therefore infinite memory resources are needed. As the required storage space is not growing continuously, as the stored events can be removed at the end of the tolerance interval, the SynchronizationConstraint is worst case Non-Finite monitorable.

It should be noted, that the illustration of the constraint in 5.2 may be misleading, as the *tolerance* intervals are only shown after the events of s_1 , not after the events of s_2 . Every implementation of a monitor for this constraint must also store the events of s_2 for the length of *tolerance*, as they could be important for events following after them.

5.6. StrongSynchronizationConstraint

The difference between the *StrongSynchronizationConstraint* and the *SynchronizationConstraint* is, that in the StrongSynchronizationConstraint, only one event per event set is allowed in each synchronization cluster. Therefore, this constraint can be classified as worst case Non-Finite monitorable with the same argumentation as the previous constraint.

5.7. Execution Time Constraint

The *ExecutionTimeConstraint* ensures that the time distance between *stop* and *start* events, not counting interruptions (which are specified by *preempt* and *resume* events).

Under the assumption that the input events are in logical order (every execution is started by an *start* event and finished by an *stop* event, every *preempt* event is directly followed by an *resume* event and no *preempt* or *resume* events occur outside of the intervals spanned by *start* and *stop* events), three time values must be stored, to monitor this constraint. First, the timestamp of the latest *start* event. Second, the sum of the timestamps of the *preempt* events, reseted by every *start* event and third, the sum of the timestamps of the *resume* events, also reseted by every *start* event.

For the output function, the run time can be calculated by runtime = time(now) - start - (sum(resume) - sum(preempt)).

At any event, this value must smaller or equal to *upper* and at *stop* events, additionally the runtime must be greater or equal to *upper*.

Therefore the required storage space is fixed, also the runtime of the state transition and output function is in $\mathcal{O}(1)$, therefore the ExecutionTimeConstraint is finite monitorable with delay.

5.8. OrderConstraint

The OrderConstraint describes, that an i^{th} target event exists, if an i^{th} source event exists and that the i^{th} target event occurs after the i^{th} source event. Because it is possible that an arbitrary large number of source events occur before the first target occurs, a possibly infinite large number must be stored, which requires infinite memory resources. As this is only a worst case scenario and the size of the stored number can be decreased, when a target event occurs, the OrderConstraint is worst case non-finite monitorable.

- 5.9. ComparisonConstraint
- 5.10. SporadicConstraint
- 5.11. PeriodicConstraint
- 5.12. PatternConstraint
- **5.13.** ArbitraryConstraint
- 5.14. BurstConstraint
- 5.15. ReactionConstraint
- 5.16. AgeConstraint
- 5.17. OutputSynchronizationConstraint
- 5.18. InputSynchronizationConstraint

6. Implementierungen

In der Evaluierung wird das Ergebnis dieser Arbeit bewertet. Eine praktische Evaluation eines neuen Algorithmus kann zum Beispiel durch eine Implementierung geschehen. Je nach Thema der Arbeit kann sich natürlich auch die gesamte Arbeit eher im praktischen Bereich mit einer Implementierung beschäftigen. In diesem Fall gilt es am Ende der Arbeit insbesondere die Implementierung selber zu evaluieren. Wesentliche Fragen dabei können sein:

- Was funktioniert jetzt besser als vor meiner Arbeit?
- Wie kann das praktisch eingesetzt werden?
- Was sagen potenzielle Anwender zu meiner Lösung?

6.1. Implementierungen

Wenn Implementierungen umfangreich beschrieben werden, ist darauf zu achten, den richtigen Mittelweg zwischen einer zu detaillierten und zu oberflächlichen Beschreibung zu finden. Eine Beschreibung aller Details der Implementierung ist in der Regel zu detailliert, da die primäre Zielgruppe einer Abschlussarbeit sich nicht im Detail in den geschriebenen Quelltext einarbeiten will. Die Beschreibung sollte aber durchaus alle wesentlichen Konzepte der Implementierung enthalten. Gerade bei einer Abschlussarbeit am Institut für Softwaretechnik und Programmiersprachen lohnt es sich, auf die eingesetzten Techniken und Programmiersprachen einzugehen. Ich würde in einer solchen Beschreibung auch einige unterstützende Diagramme erwarten.

7. Zusammenfassung und Ausblick

Die Zusammenfassung greift die in der Einleitung angerissenen Bereiche wieder auf und erläutert, zu welchen Ergebnissen diese Arbeit kommt. Dabei wird insbesondere auf die neuen Erkenntnisse und den Nutzen der Arbeit eingegangen.

Im anschließenden Ausblick werden mögliche nächste Schritte aufgezählt, um die Forschung an diesem Thema weiter voranzubringen. Hier darf man sich nicht scheuen, klar zu benennen, was im Rahmen dieser Arbeit nicht bearbeitet werden konnte und wo noch weitere Arbeit notwendig ist.

A. Anhang

Dieser Anhang enthält tiefergehende Informationen, die nicht zur eigentlichen Arbeit gehören.

A.1. Abschnitt des Anhangs

In den meisten Fällen wird kein Anhang benötigt, da sich selten Informationen ansammeln, die nicht zum eigentlichen Inhalt der Arbeit gehören. Vollständige Quelltextlisting haben in ausgedruckter Form keinen Wort und gehören daher weder in die Arbeit noch in den Anhang. Darüber hinaus gehören Abbildungen bzw. Diagramme, auf die im Text der Arbeit verwiesen wird, auf keinen Fall in den Anhang.

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TDO zu erledigen $To\ Do$

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