

TUT

Tutorial 1 ER Modeling

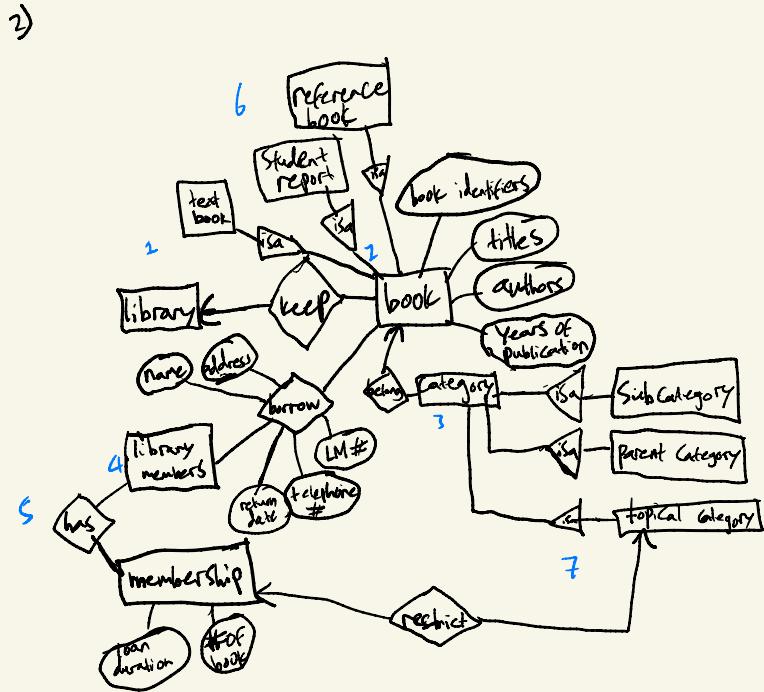
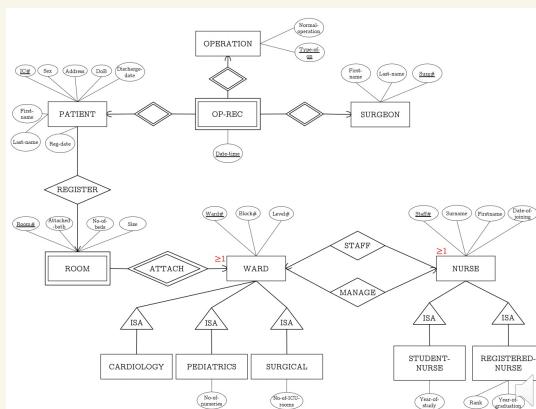
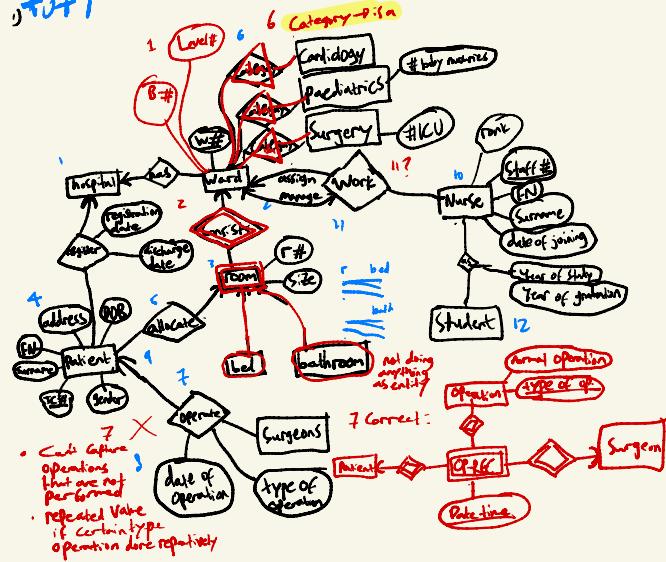
Classroom Exercise

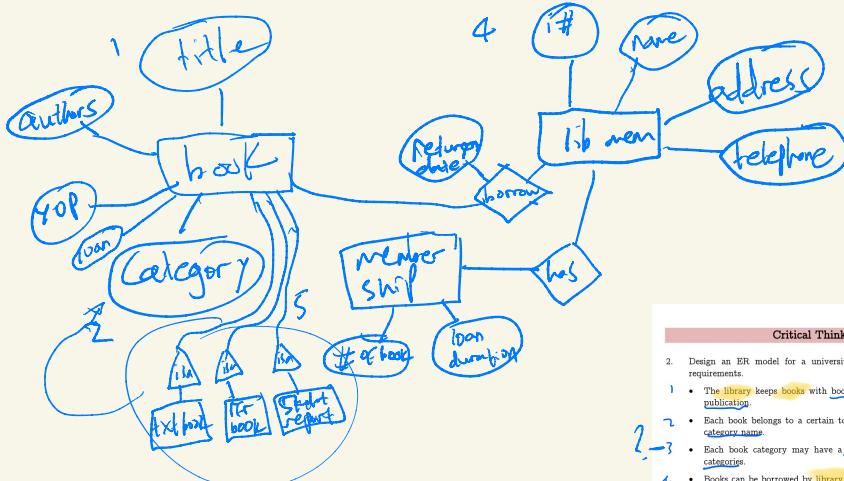
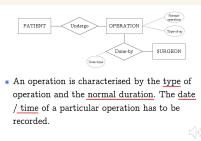
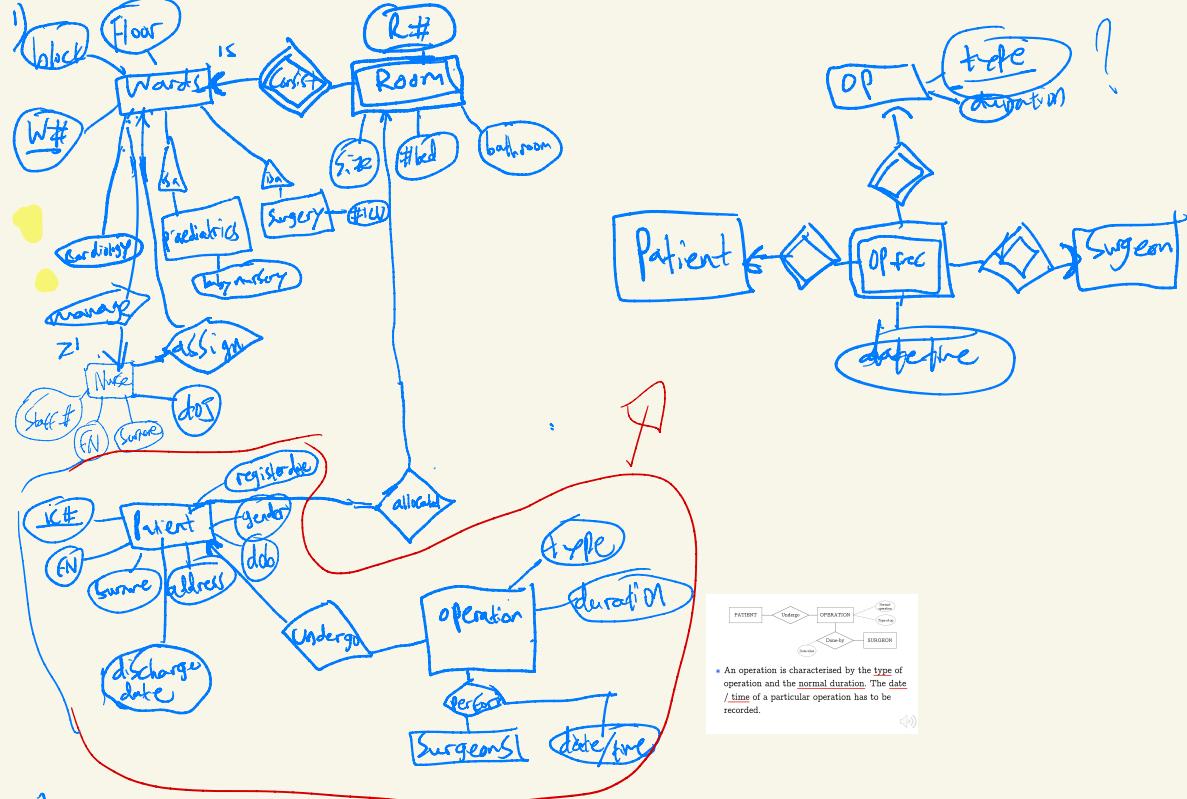
1. Construct an ER diagram for a hospital with the following user requirements:
 - 1 • The hospital has wards identified by a ward number. A ward is located in a particular block and on a particular floor.
 - 2 • Each ward consists of different rooms. All rooms have room numbers unique only to the ward but not unique between different wards. Each ward has at least one room.
 - 3 • Rooms may be of different sizes, with different number of beds and possibly with attached bathrooms. Rooms with the same number of beds need not be of the same size nor have similar bath facilities.
 - 4 • When a patient registers, information about his IC#, first name, surname, address, date of birth, registration date and gender are recorded. Upon discharge, the discharge date is also recorded.
 - 5 • If a patient is allocated to a room, no bed allocation details are recorded.
 - 6 • There are three categories of wards: cardiology, paediatrics and surgery. Each paediatric ward has a number of baby nurseries, while each surgical ward has a number of intensive care units (ICU).
 - 7 • During his/her hospitalisation, a patient may undergo surgical treatment, whereby multiple operations are possible. Complex procedures might require multiple surgeons.
 - 8 • An operation is characterised by the type of operation and the normal duration. The date / time of a particular operation has to be recorded.
 - 9 • Every surgeon has been involved in at least one operation but not every operation type has been carried out in this hospital.
 - 10 • Information about nurses includes staff#, first name, surname, and date of joining.
 - 11 • Every nurse is assigned to a ward. A ward is staffed by many nurses. However, a ward is managed by only one nurse. Not every nurse manages a ward.
 - 12 • Nurses are designated as student nurses or registered nurses. The particular year of study for student nurses and the year of graduation and rank for registered nurses are also stored.

Critical Thinking Exercise

2. Design an ER model for a university library's database with the following requirements.
- 1 • The library keeps books with book identifiers, titles, authors and years of publication.
 - 2 • Each book belongs to a certain topical category which is identified by the category name.
 - 3 • Each book category may have a parent category and / or multiple sub-categories.
 - 4 • Books can be borrowed by library members. Library members are identified by their identification numbers. The other member information including name, address and telephone numbers are also stored.
 - 5 • There are differently named types of memberships. Each membership type has a different cap on the number of books that can be borrowed and the loan duration. It is assumed that a member can borrow a book several times on different dates. Each book loan also comes with a return date determined by the loan duration of the membership type.
 - 6 • The library restricts its textbooks, reference books and student reports to be used within the library; i.e. these types of books cannot be loaned. For textbooks, reference books and student reports, the course name, subject topic and school are required, respectively.
 - 7 • Finally, the topical categories of books that can be borrowed are restricted by the membership type.

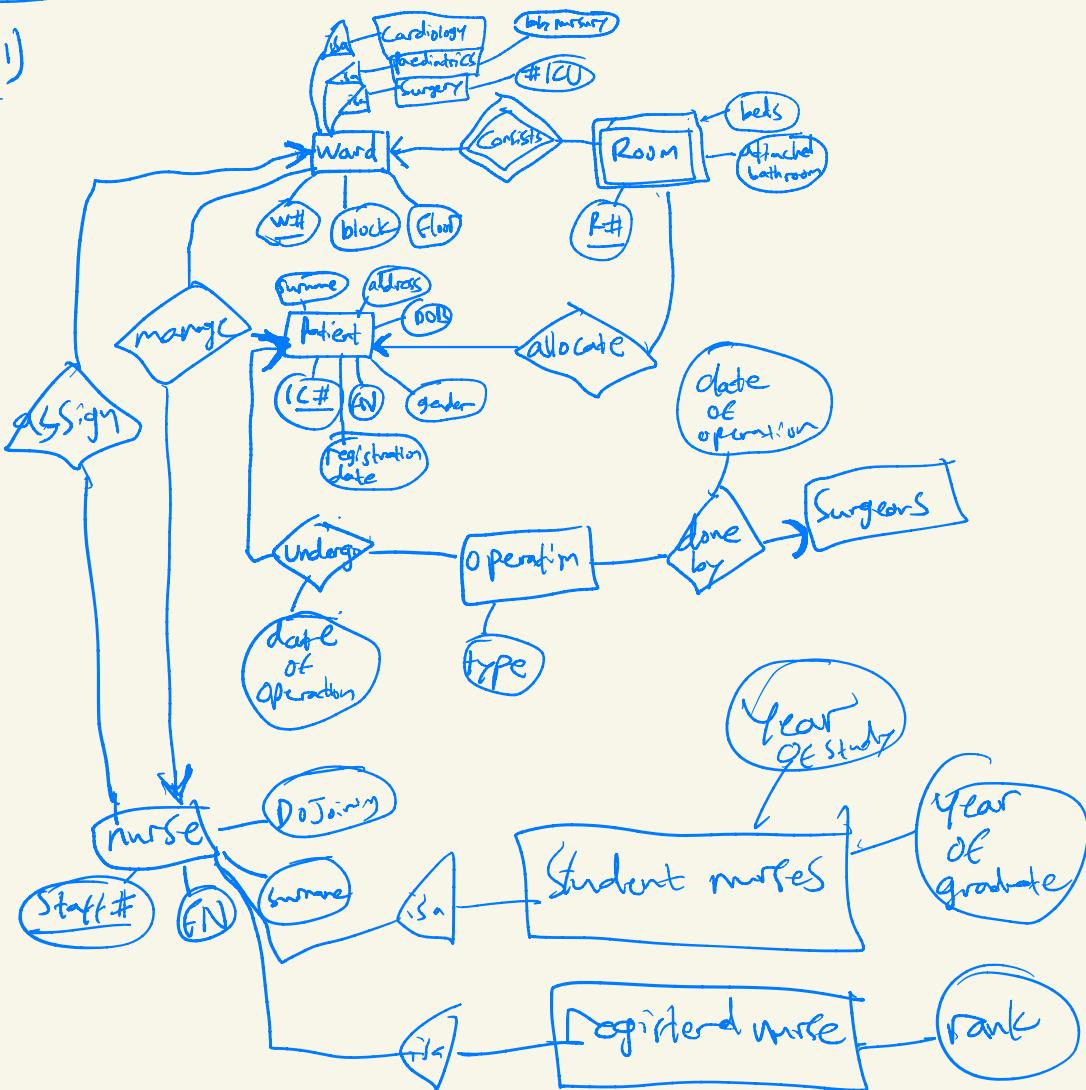
State all assumptions clearly.



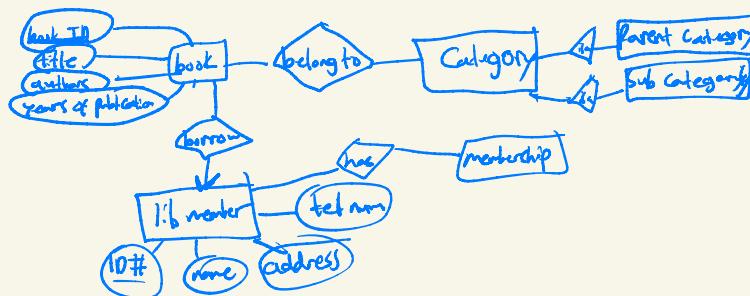


- Critical Thinking Exercise**
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1)

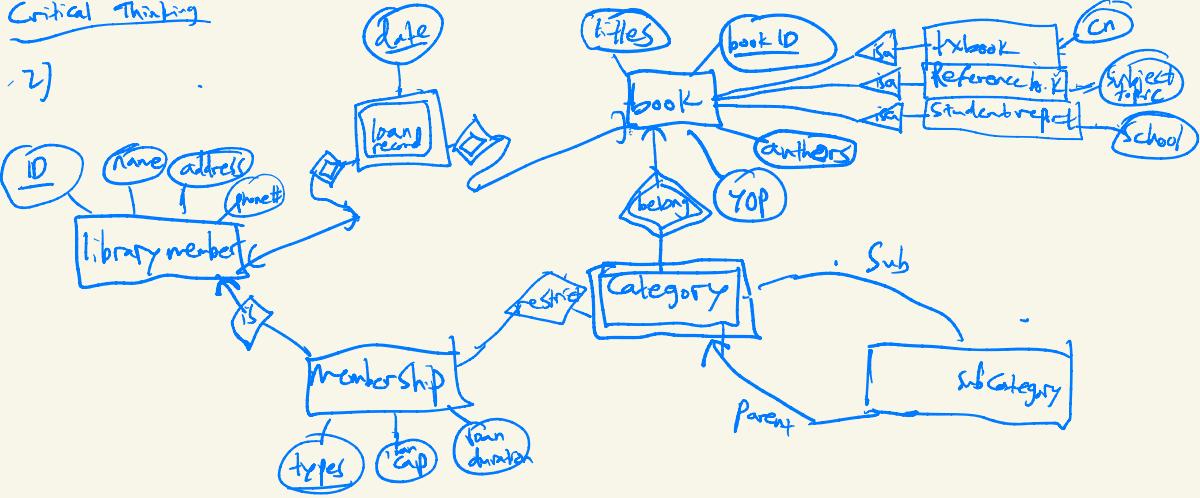


2)



Critical Thinking

2)

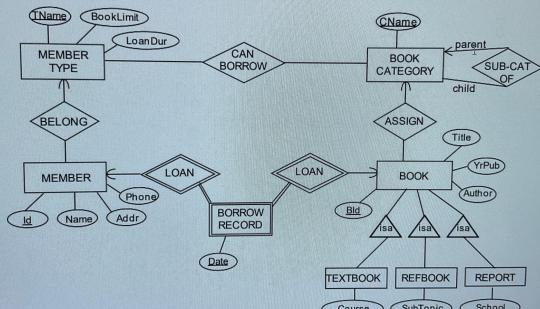


Critical Thinking Exercise

CZ2007

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Question 2



CZ2007 Tutorial 1: ER Modeling

Week 3

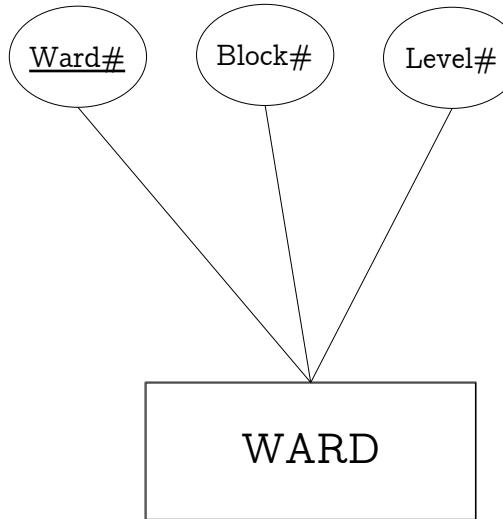


Question 1

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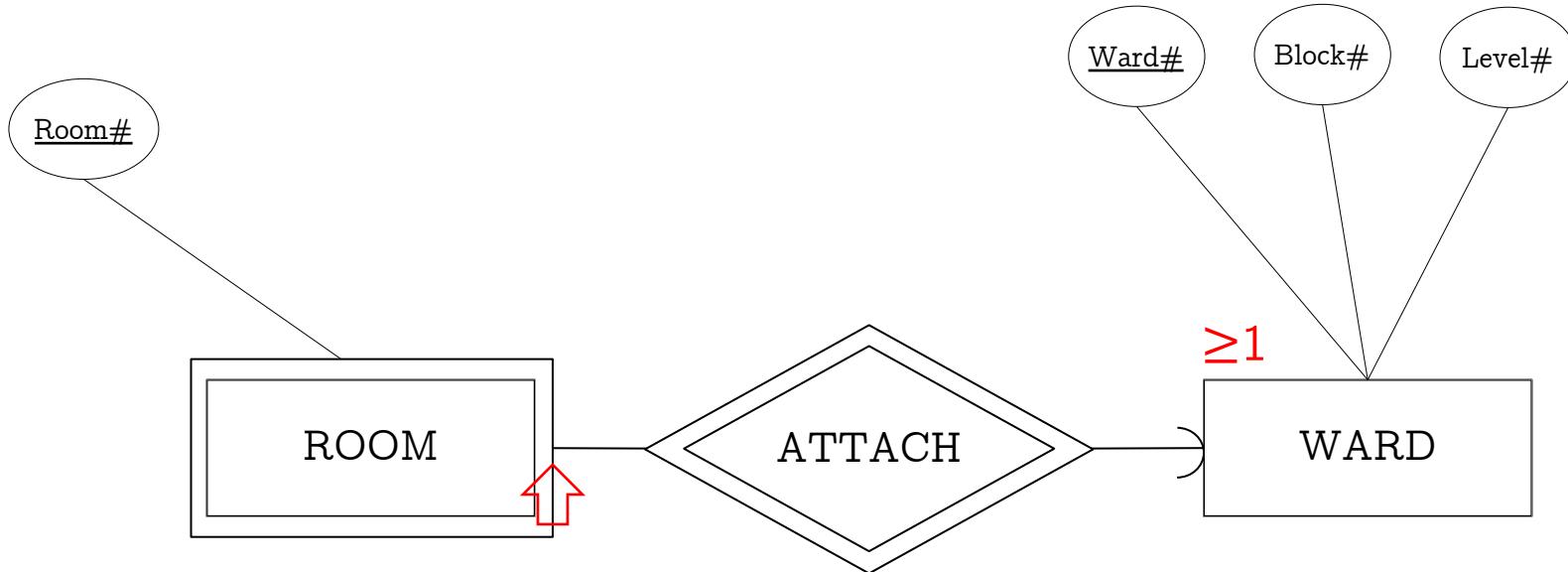
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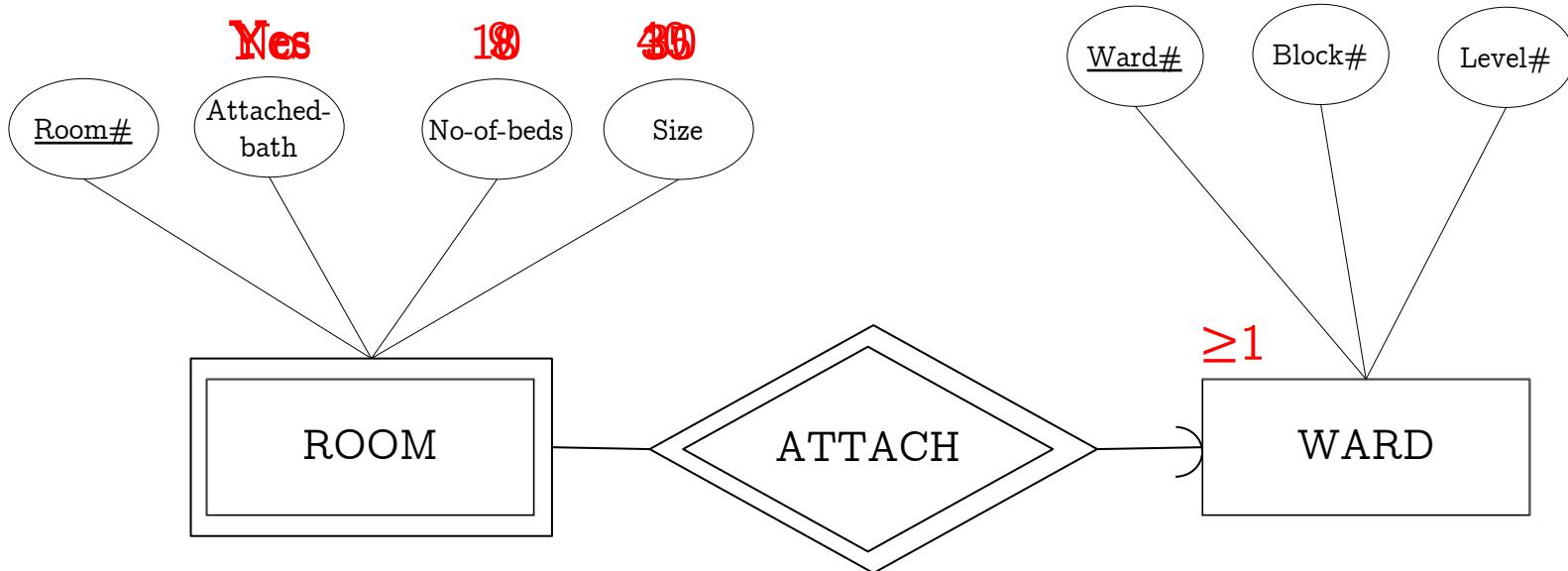
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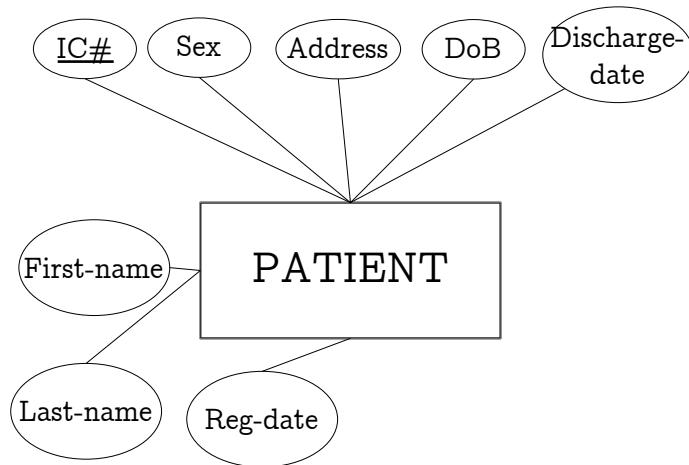


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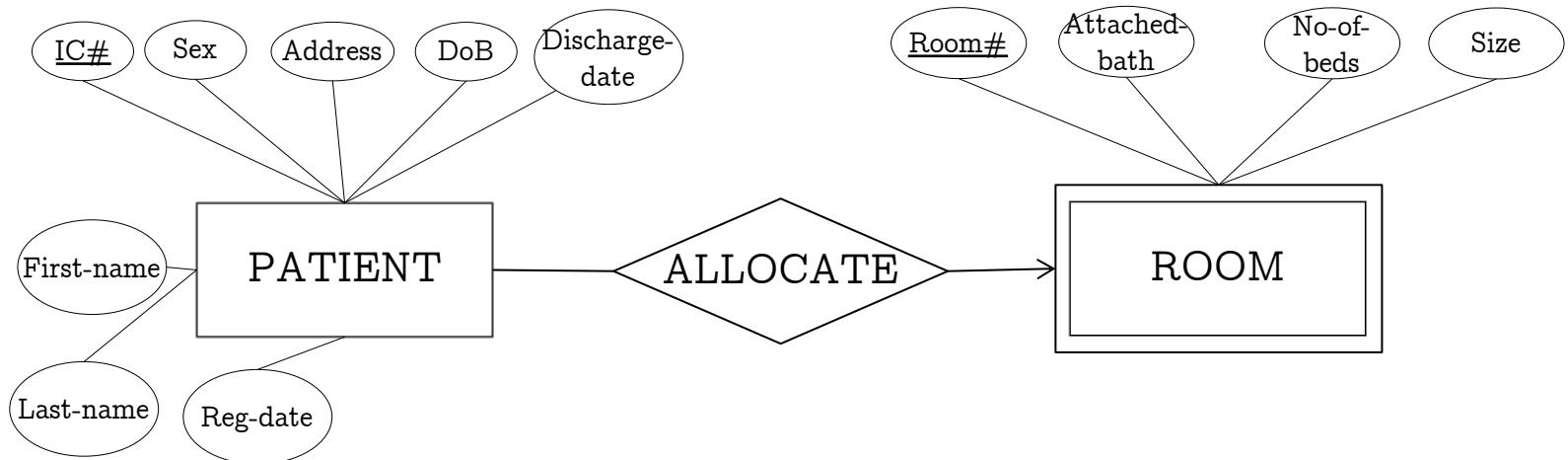
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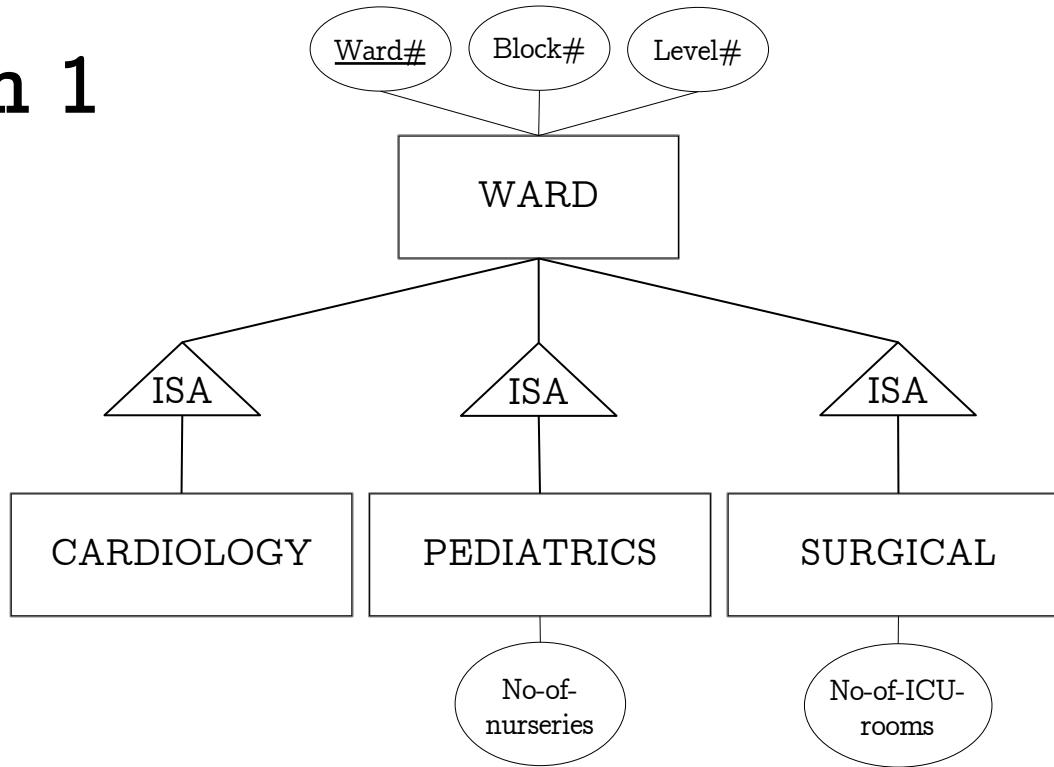
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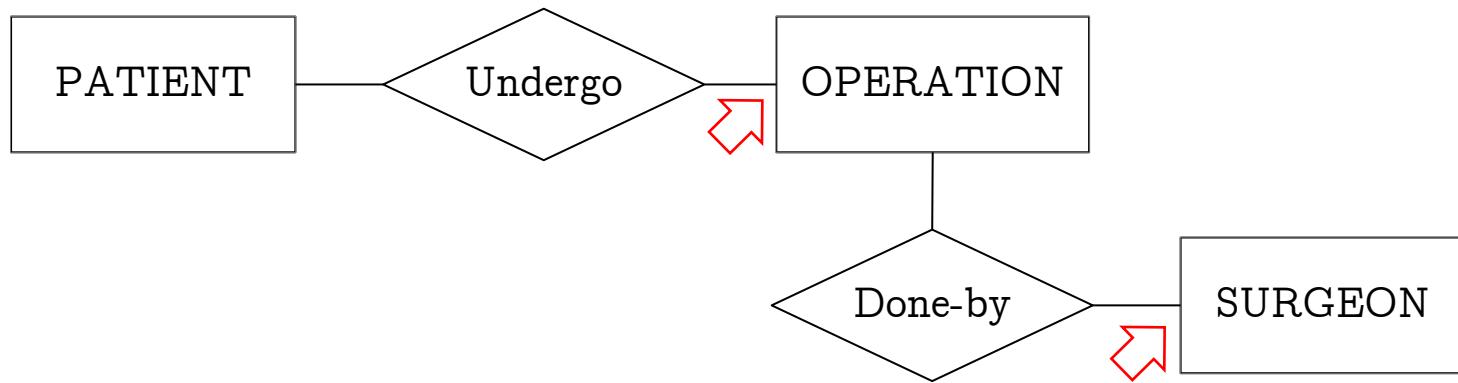


Question 1

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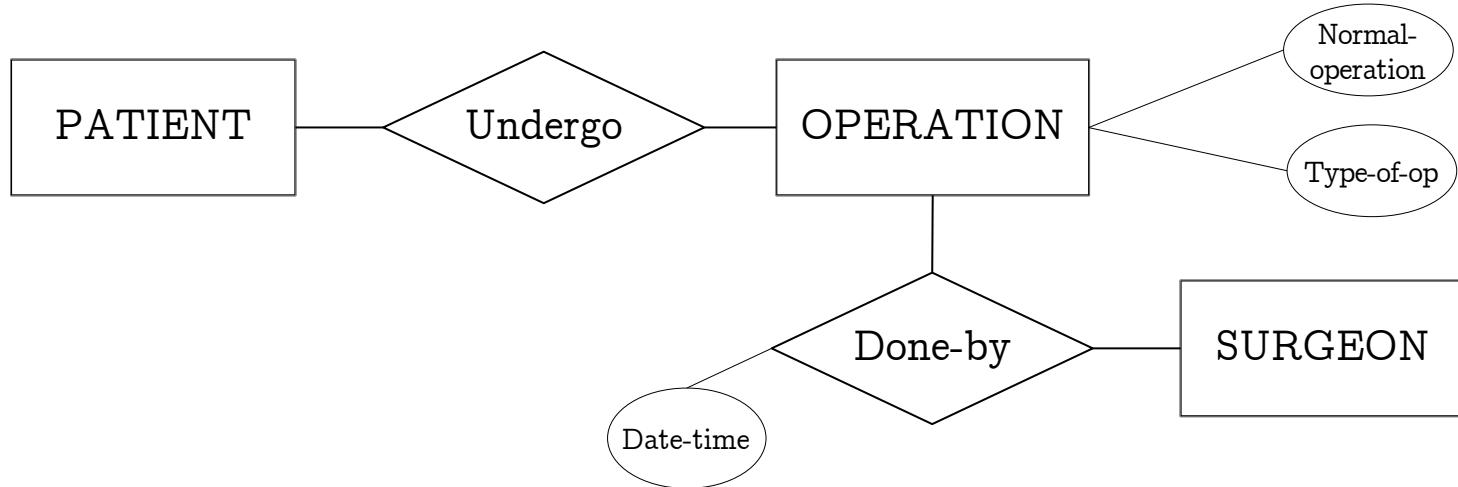
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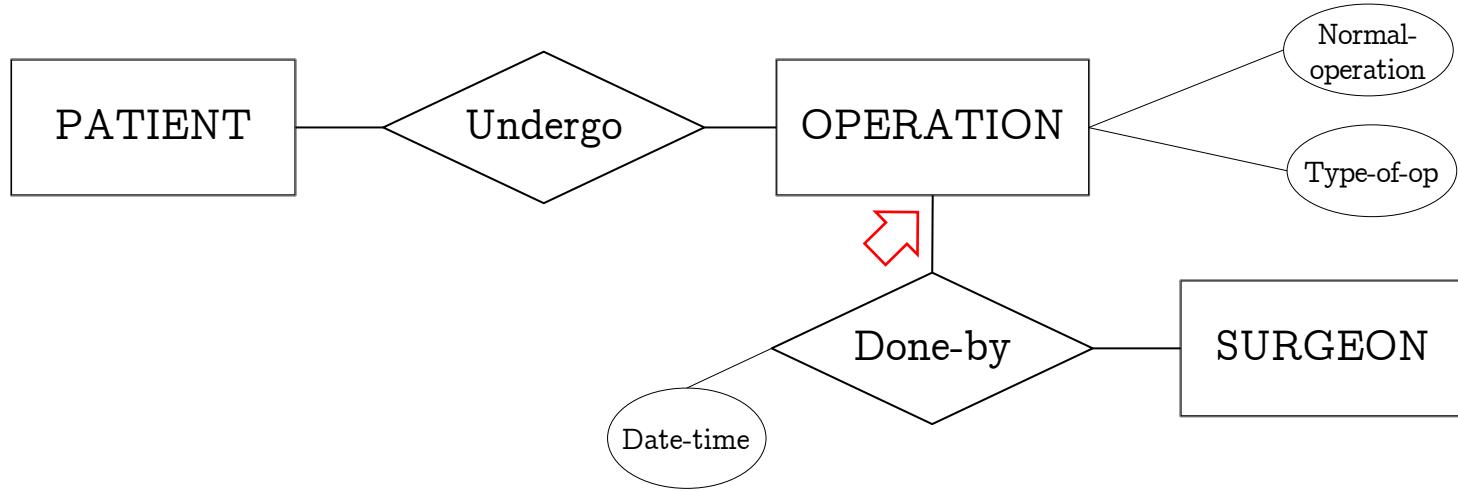
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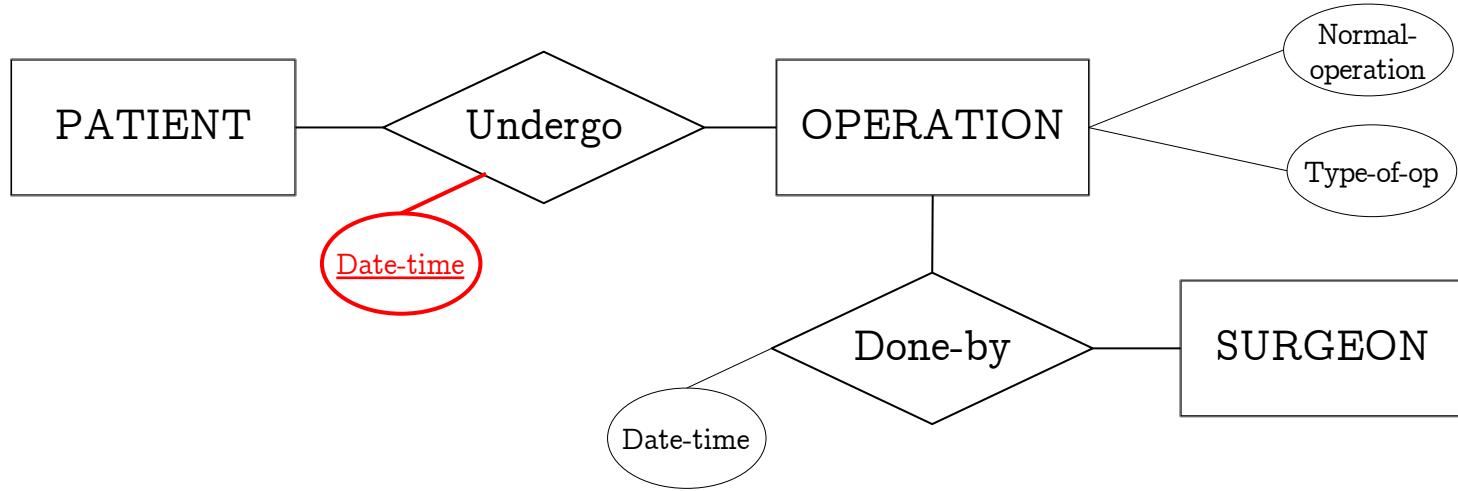
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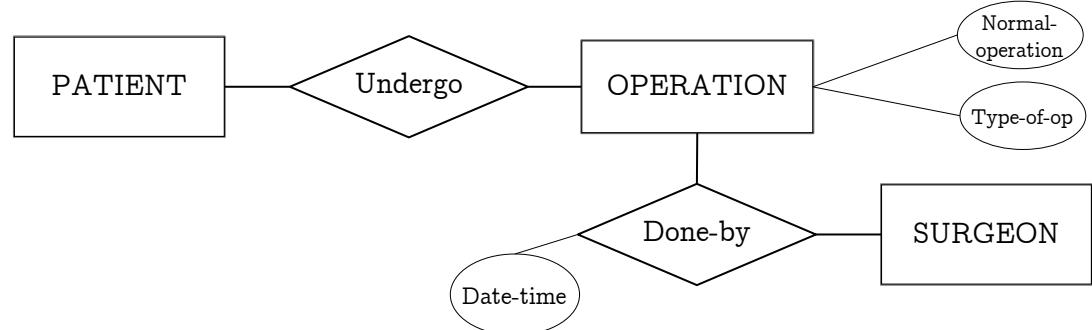
Question 1



- Problem 1:
- When a patient undergoes an operation, there is date/time when it is performed.
- If this is included as attribute of Undergo, then there are two Date-time's.
- Repetition of information in ER diagram is not good.



Question 1



Undergo

Patient	Operation
John	Heart-op
Mary	Heart-op
Steve	Heart-op

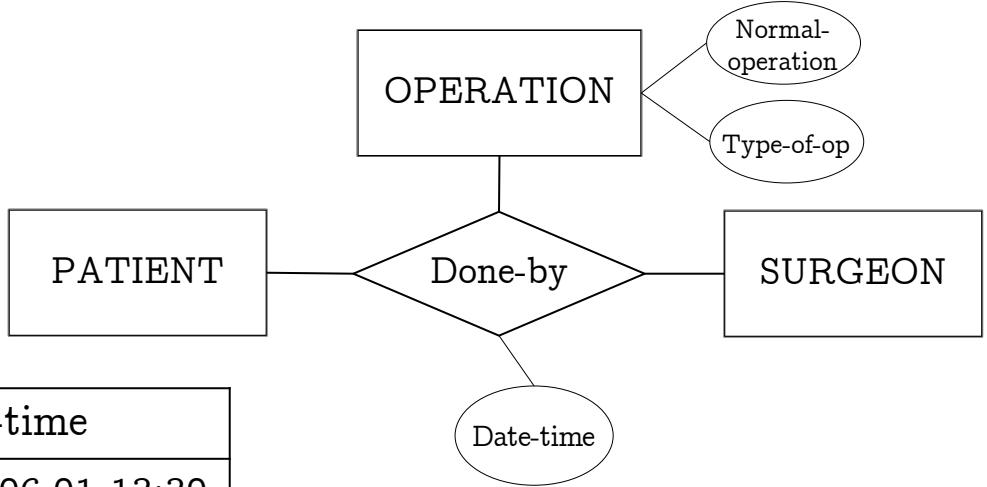
Done-by

Operation	Surgeon	Date-time
Heart-op	Wang	2020.06.01 13:30
Heart-op	Chan	2020.06.01 13:30
Heart-op	Lee	2020.06.01 13:30

- Problem 2:
- Consider the Undergo and Done-by tables of records.
- How do we know which surgeon operate on which patients?



Question 1



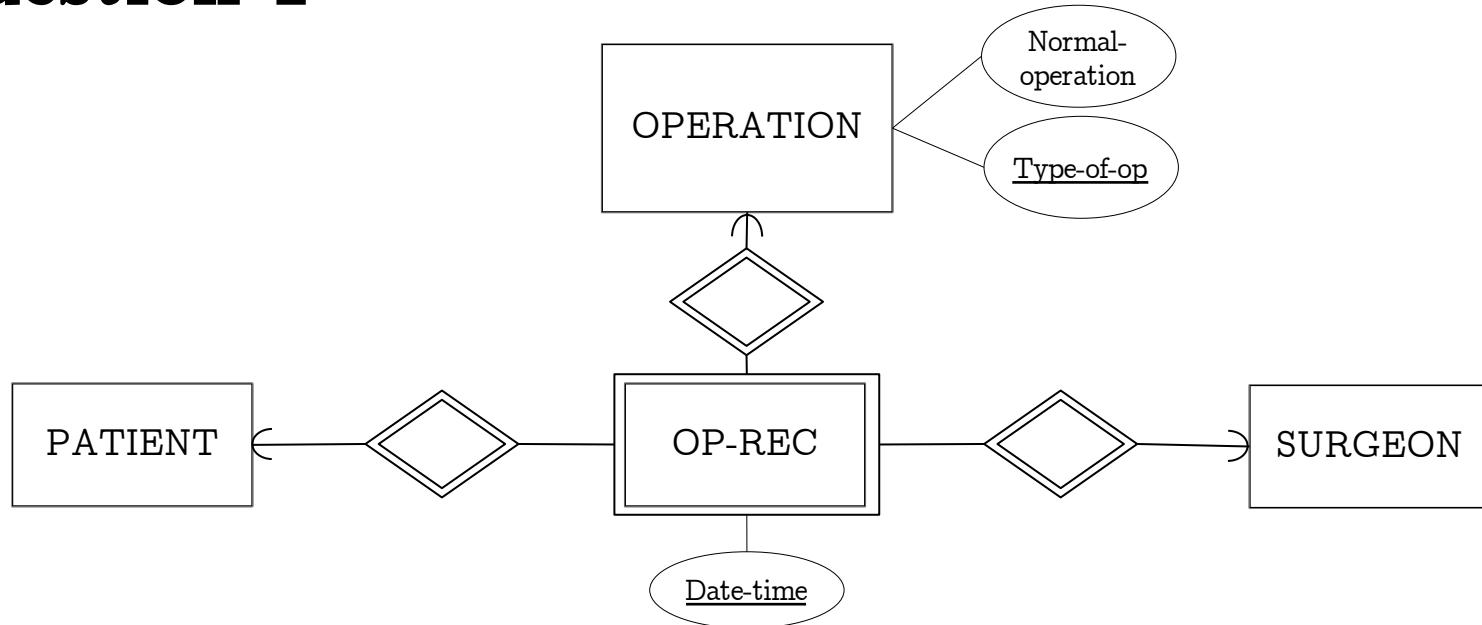
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- Problem 2:
- To resolve Problem 2, we can use a 3-way relationship.



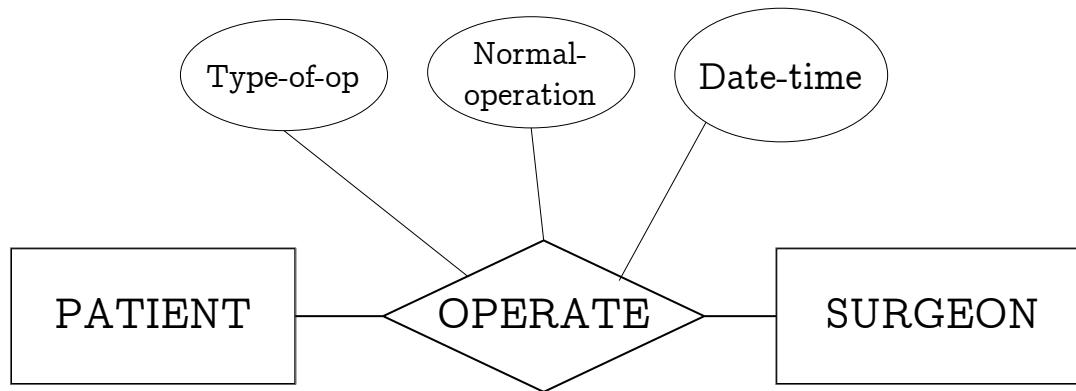
Question 1



- Always convert 3-way relationship to 3 binary relationships
- These relationships are weak relationships



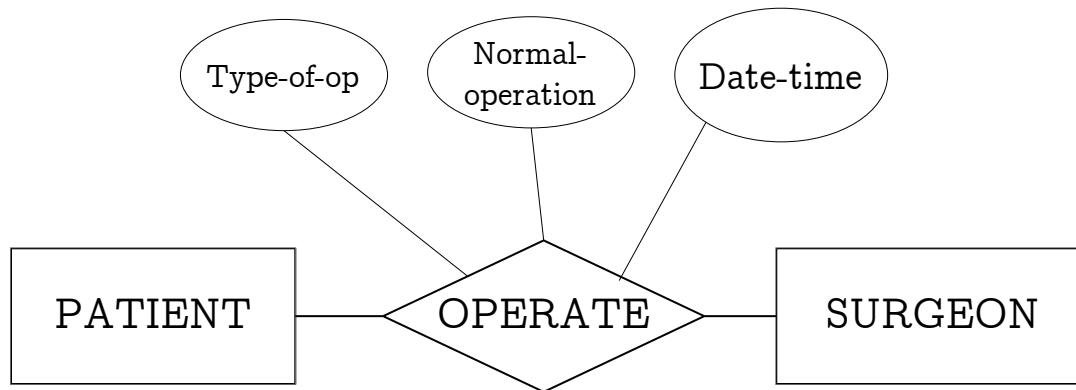
Question 1



- Problem 3:
- Can't capture operations that are not performed (as given in text).



Question 1



- Problem 4:
- If “heart surgery” is performed many times, “type” and “duration” will have the same values and repeated many times.

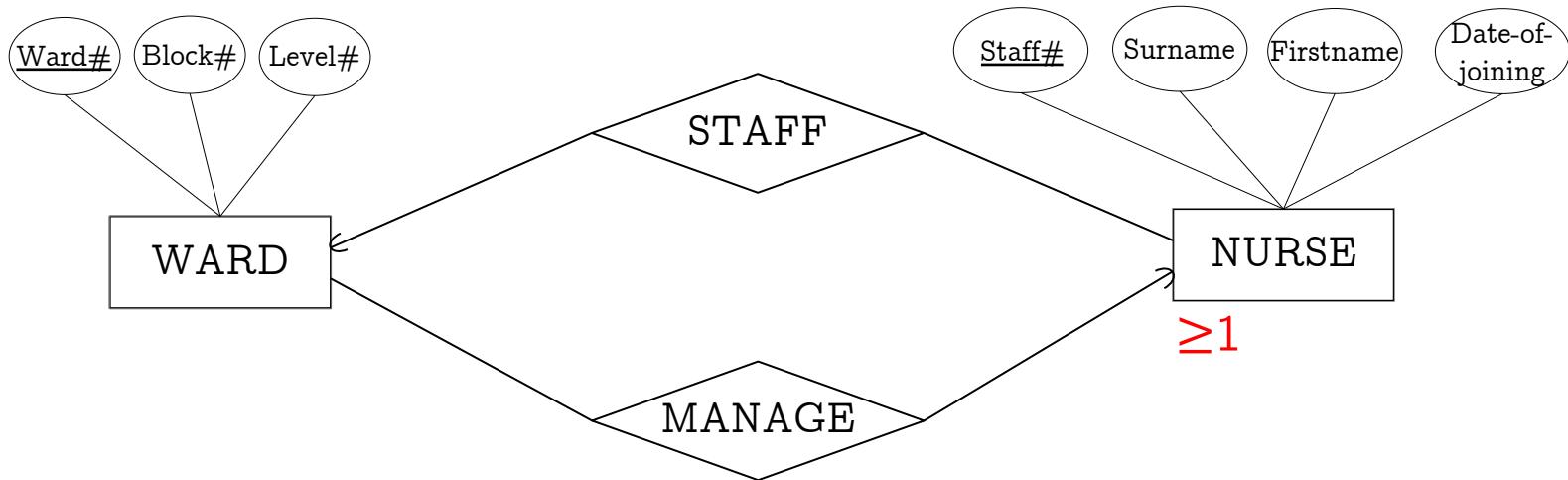


Question 1

- Information about nurses includes staff#, first name, surname, and date of joining.
- Every nurse is assigned to a ward. A ward is staffed by many nurses. However, a ward is managed by only one nurse. Not every nurse manages a ward.
- Nurses are designated as student nurses or registered nurses. The particular year of study for student nurses and the year of graduation and rank for registered nurses are also stored.



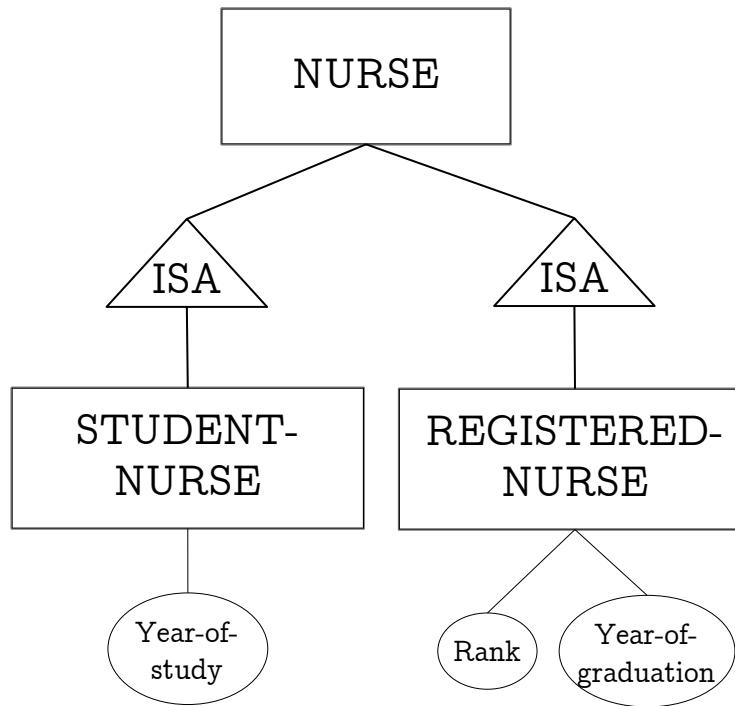
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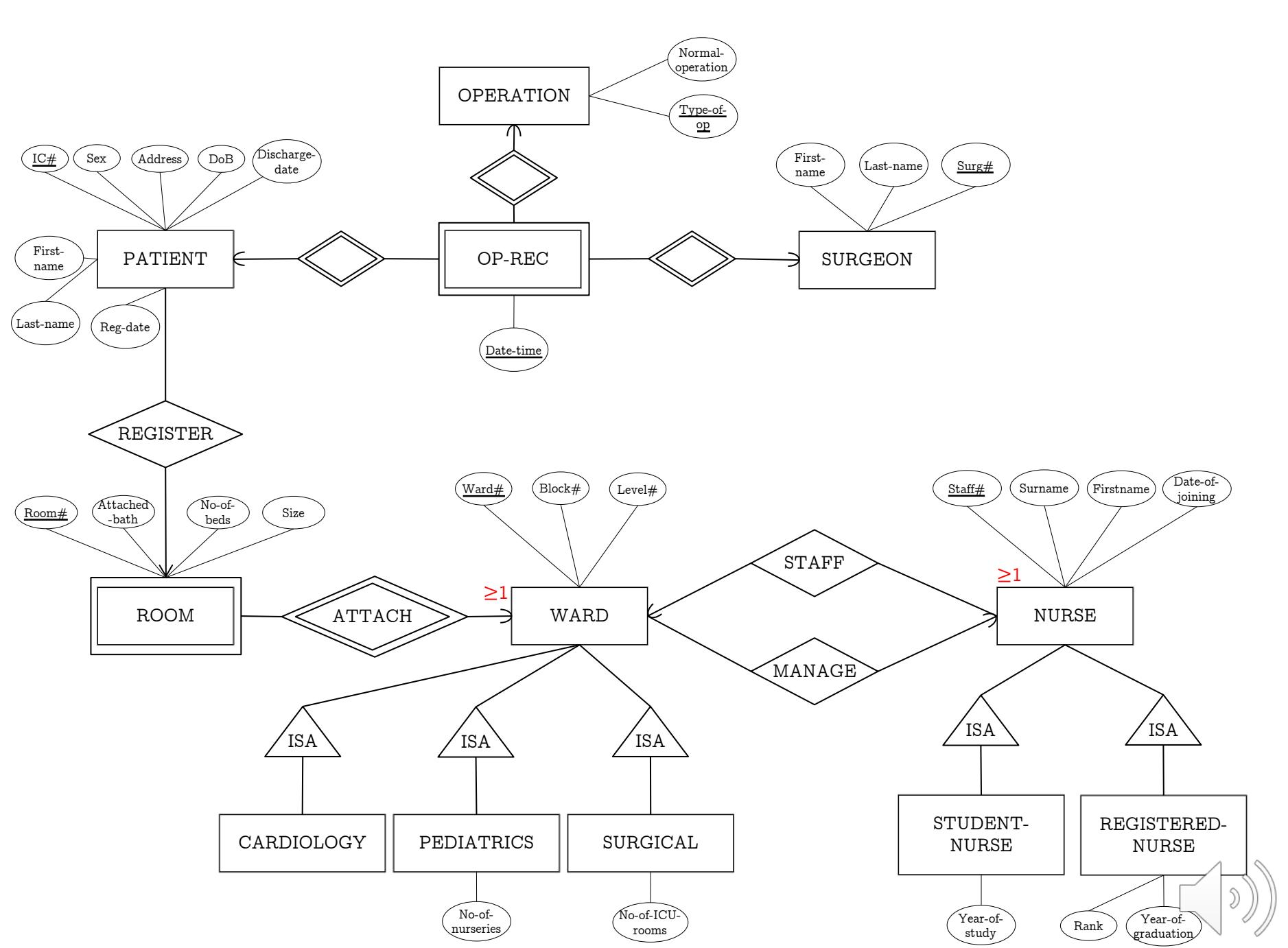


Question 1



- Nurses are designated as student nurses or registered nurses. The particular year of study for student nurses and the year of graduation and rank for registered nurses are also stored.







Do the best
you can until you know better.
Then when you know better, do better.

~ Maya Angelou

ALL THE BEST



Tutorial 2

Functional Dependencies

Classroom Exercise

1. Translate the ER Diagram of Q1 in Tutorial 1 into a set of relations.
2. Consider the following relational schema:

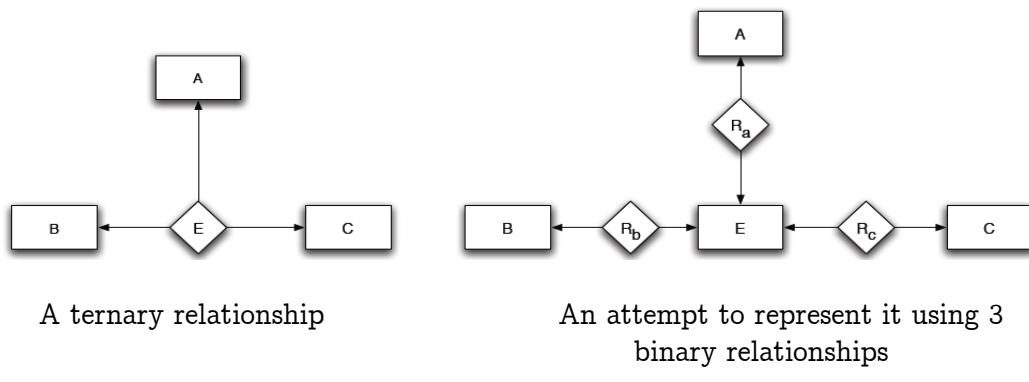
```

USER(uid, name)
SINGER(id, name)
ALBUM(id, title, singerid)
SONG(id, title, albumid)
SING(singerid, songid)
FOLLOW_USER(followeruid, followeeuid)
RATE_SONG(uid, songid, rating)
RATE_SINGER(uid, singerid, rating)
PLAY_SONG(uid, songid, datetime)

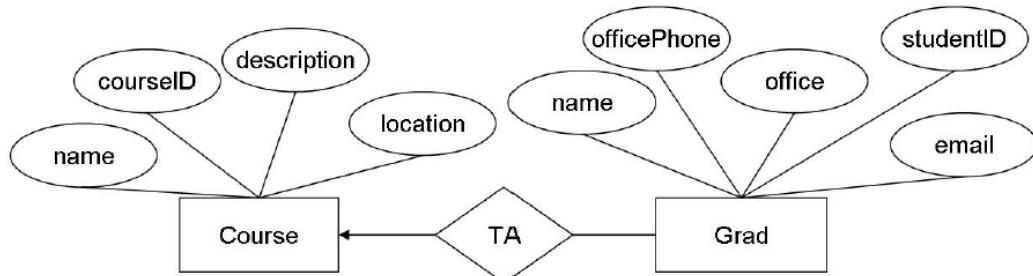
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Construct an ER diagram that leads to the above schema.

3. The figure shows an attempt to represent a ternary relationship between three entities using 3 binary relationships (and one made-up entity). Show through an example why the 3 binary relationship representation is more general than the one ternary relationship representation.



4. Consider the following ER diagram that describes graduate students (Grad) and courses (Course) they serve as Teaching Assistants (TA).



(a) For each of the following statements, write a functional dependency (FD) that best captures the statement.

- The studentID of each graduate student uniquely identifies the student.
- No two offices have the same phone number (officePhone).
- No two courses have the same courseID.
- If two courses have the same course name, their course descriptions are the same.

(b) From the ER diagram and the set of FDs you listed above, can you derive new FDs? If no, explain why not. If yes, derive two non-trivial FDs.

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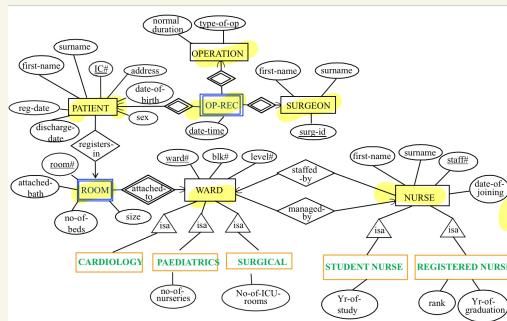
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(b) From the ER diagram and the set of FDs you listed above, can you derive new FDs? If no, explain why not. If yes, derive two non-trivial FDs.

Critical Thinking Exercise

5. Translate the ER Diagram of Q2 in Tutorial 1 into a set of relations.

TUTZ
1)



We = weak entity
M2O = many 2 one

Question 1: Relational Tables

- Surgeon (surgeon-id, first-name, surname)
- Operation (type-of-op, normal-duration)
- Patient (IC#, first-name, surname, address, date-of-birth, sex, reg-date, discharge-date, room#, ward#) - m2o
- Ward (ward#, blk#, level#, no-of-nurseries, no-of-ICU-rooms, manager) - m2o
- Nurse (staff#, first-name, surname, date-of-joining, wardStaff#) - m2o
- Op-Rec (IC#, surg-id, type-of-op, date-time) - w.e./m2o
- Room (room#, ward#, attached-bath, no-of-beds) - w.e./m2o

Surgeon (surgeon-id, fn, surname)
Operation (type-of-op, duration)
Patient ()

Subclass relationships:

- Student_Nurse(staff#, Yr-of-study)
- Registered_Nurse(staff#, rank, yr-of-graduation)
- Surgical_Ward(ward#, No_of_ICU_rooms)
- Pediatrics_Ward(ward#, No_of_nurseries)
- Cardiology_Ward(ward#, no_of_heart_equipment)

* Ward (ward#, blk#, level#, manager) - m2o

* Nurse (staff#, first-name, surname, date-of-joining, ward#) - m2o

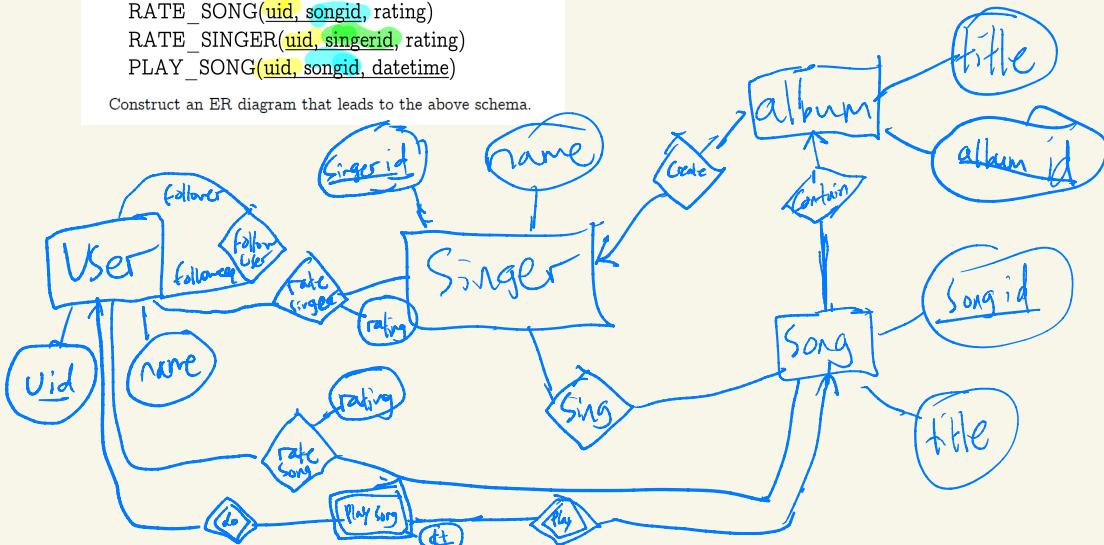
2)

Question 2

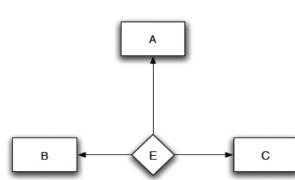
2. Consider the following relational schema:

USER(uid, name)
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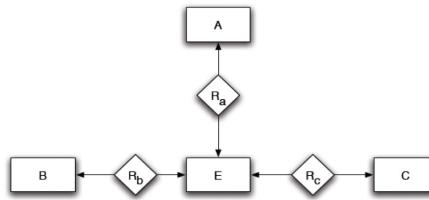
Construct an ER diagram that leads to the above schema.



3. The figure shows an attempt to represent a ternary relationship between three entities using 3 binary relationships (and one made-up entity). Show through an example why the 3 binary relationship representation is more general than the one ternary relationship representation.



A ternary relationship



An attempt to represent it using 3
binary relationships

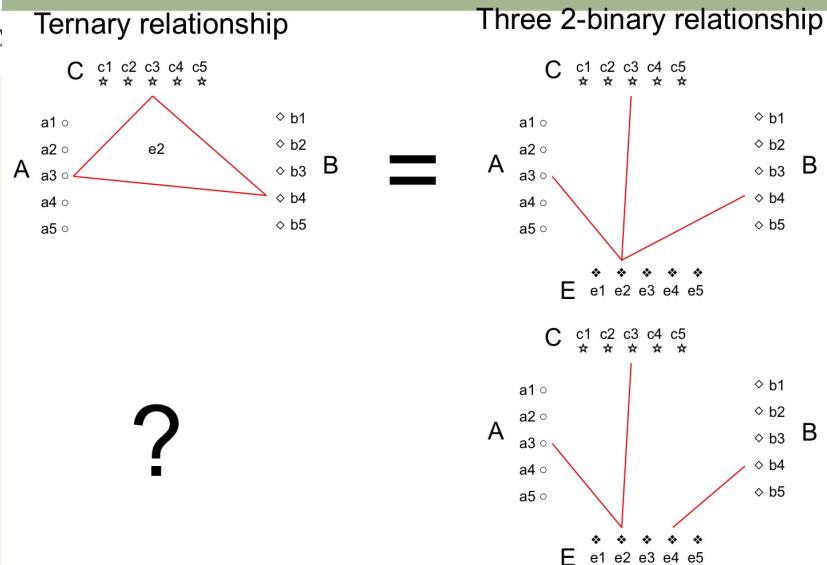
Why is a **3 binary relationship relationship representation** more general than **one ternary relationship representation**?

(<https://stackoverflow.com/questions/39254141/ternary-relationship-or-3-binary-relationship>)

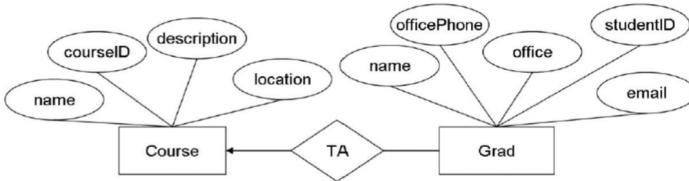
Because with 3 binary relationships each involved entity is related **separately** with each one of the others two.

Assumed that ternary relationship is essential only when you have a many-to-many relationship (otherwise you can rewrite it adding a relational entity linked with binary relationships to the others three), let's take an example:

- Suppose that you have the entities A, B and C, and three relationships that link the entities "like a triangle". Now, suppose that set of tuples a3 is related to the sets b4 and c3.
- Using 3 binary relationships, it's not requested that b4 and c3 are related. for example, b4 can be related to c2, that can partially overlap c3 or be completely disjoined.
- With a ternary relationship, instead it's requested that b4 and c3 are related.
- So you can see that with 3 binary combinations.



4. Consider the following ER diagram that describes graduate students (Grad) and courses (Course) they serve as Teaching Assistants (TA).



- (a) For each of the following statements, write a functional dependency (FD) that best captures the statement.

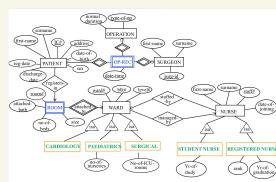
- The studentID of each graduate student uniquely identifies the student.
- No two offices have the same phone number (officePhone).
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- (b) From the ER diagram and the set of FDs you listed above, can you derive new FDs? If no, explain why not. If yes, derive two non-trivial FDs.



a) $\text{studentID} \rightarrow \text{Grad} (\text{name}, \text{OfficePhone}, \text{Office}, \text{email})$
 $\text{OfficePhone} \rightarrow \text{Office}$
 $\text{courseID} \rightarrow \text{Courses} (\text{name}, \text{desc}, \text{loc})$
 $\text{name(Course)} \rightarrow \text{Course description}$

b) $\text{Student ID} \rightarrow \text{Course ID}$ (from m20 TA)
 $\text{Student ID} \rightarrow \text{Courses} (\text{name}, \text{desc}, \text{loc})$



operation (type-of-op, duration)

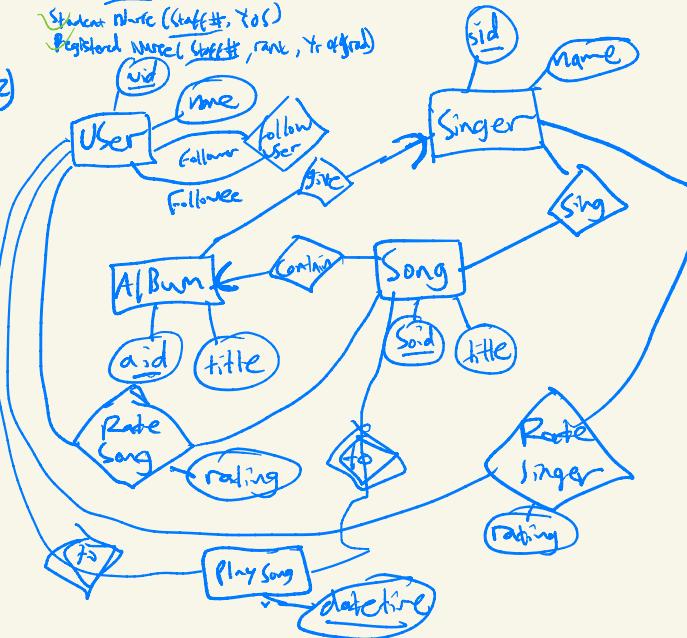
✓person (sid, FN, surname)
✓patient (sid, surname, FOB, age, date, sex, DB, address, room#, word, ICF#)
✓oprec (date, code, type-of-op, ICF#)
✓word (word, attached_label, no_of_hots, type, word_id#)
word (word, type, NatType)

✓cardiologist (word#)
✓neurologist (no-of-inpatients, word#)
✓surgical (no-of-ICU, word#)

✓nurse (staff#, month, FN, surname, DOB)

✓student_nurse (staff#, YOB)
✓registered_nurse (staff#, rank, Yr_of_grad)

2)



4) b)

StudentID → name, description, location

StudentID → coursesID

a) StudentID → Grad

OfficePhone → Offices

CoursesID → Course

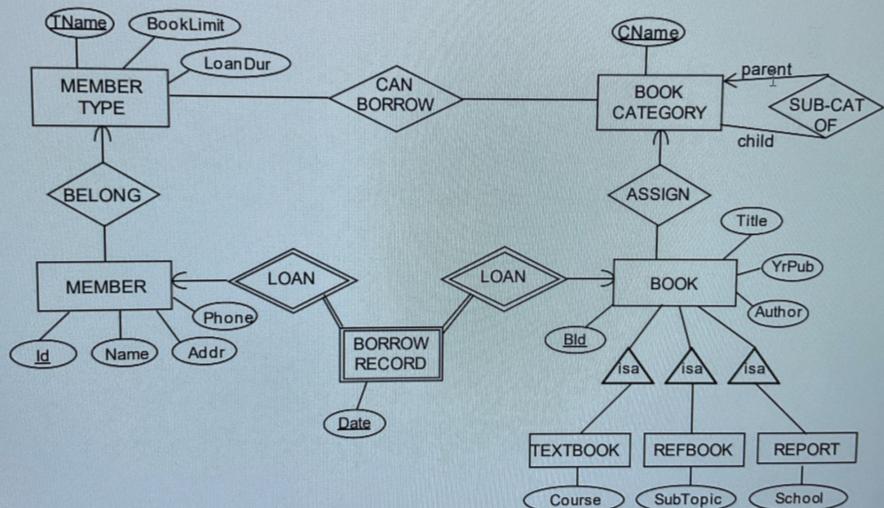
CourseName → Course description

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Critical Thinking Exercise

5. Translate the ER Diagram of Q2 in Tutorial 1 into a set of relations.

Question 2



- memberType (TName, BookLimit, LoanDur)
- Can Borrow (TName, CName)
- Book Category (CName)
- Sub-Cat Of (Child-CName)
- Member (id, Name, Addr, Phone, TName)
- Borrow Record (Date, id, Bid)
- Book (Bid, Title, YrPub, Author, CName)
- Textbook (Course, Bid) . Report (School, Bid)
• Refbook (SubTopic, Bid)

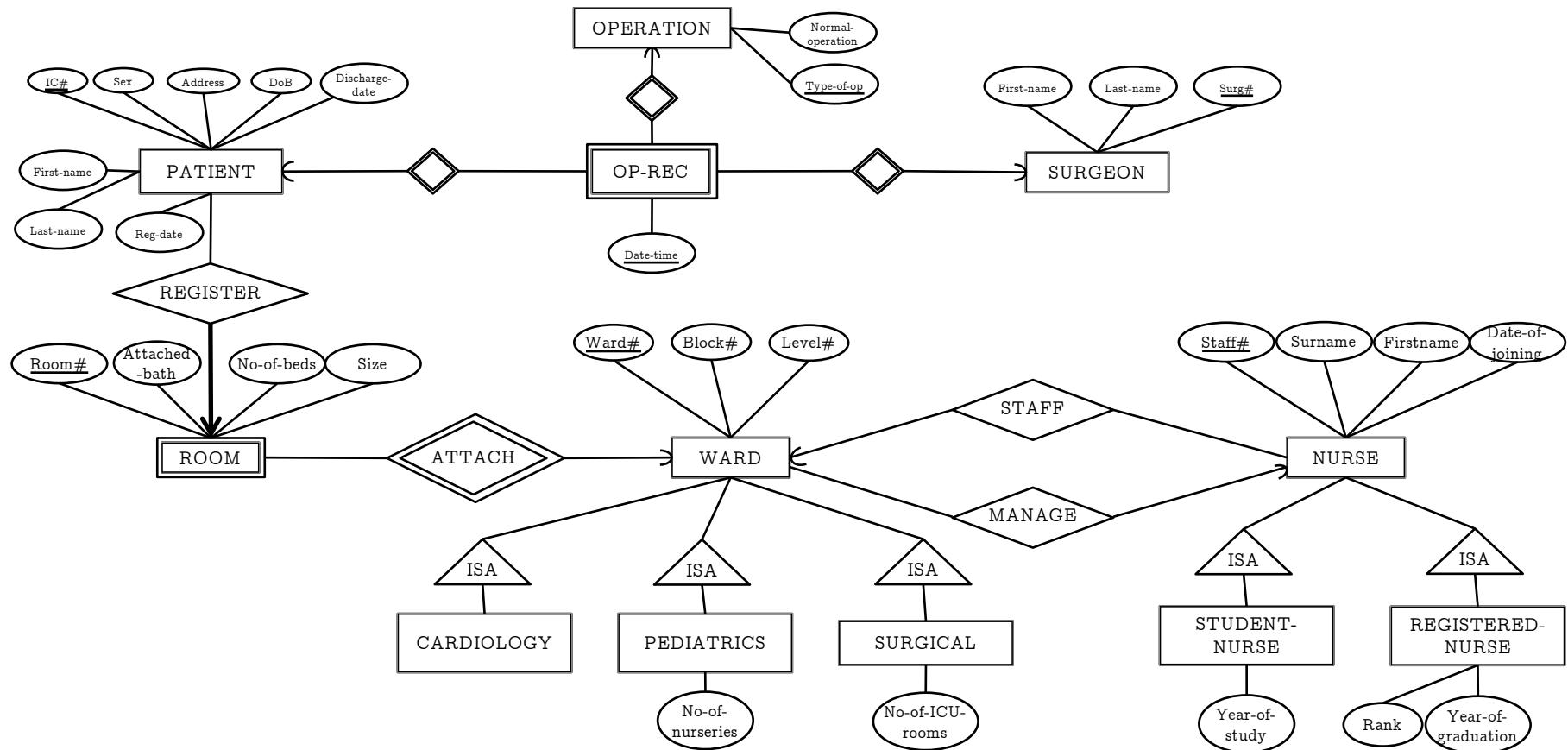
CZ2007 Tutorial 2: ER Diagram + FDs

Week 4

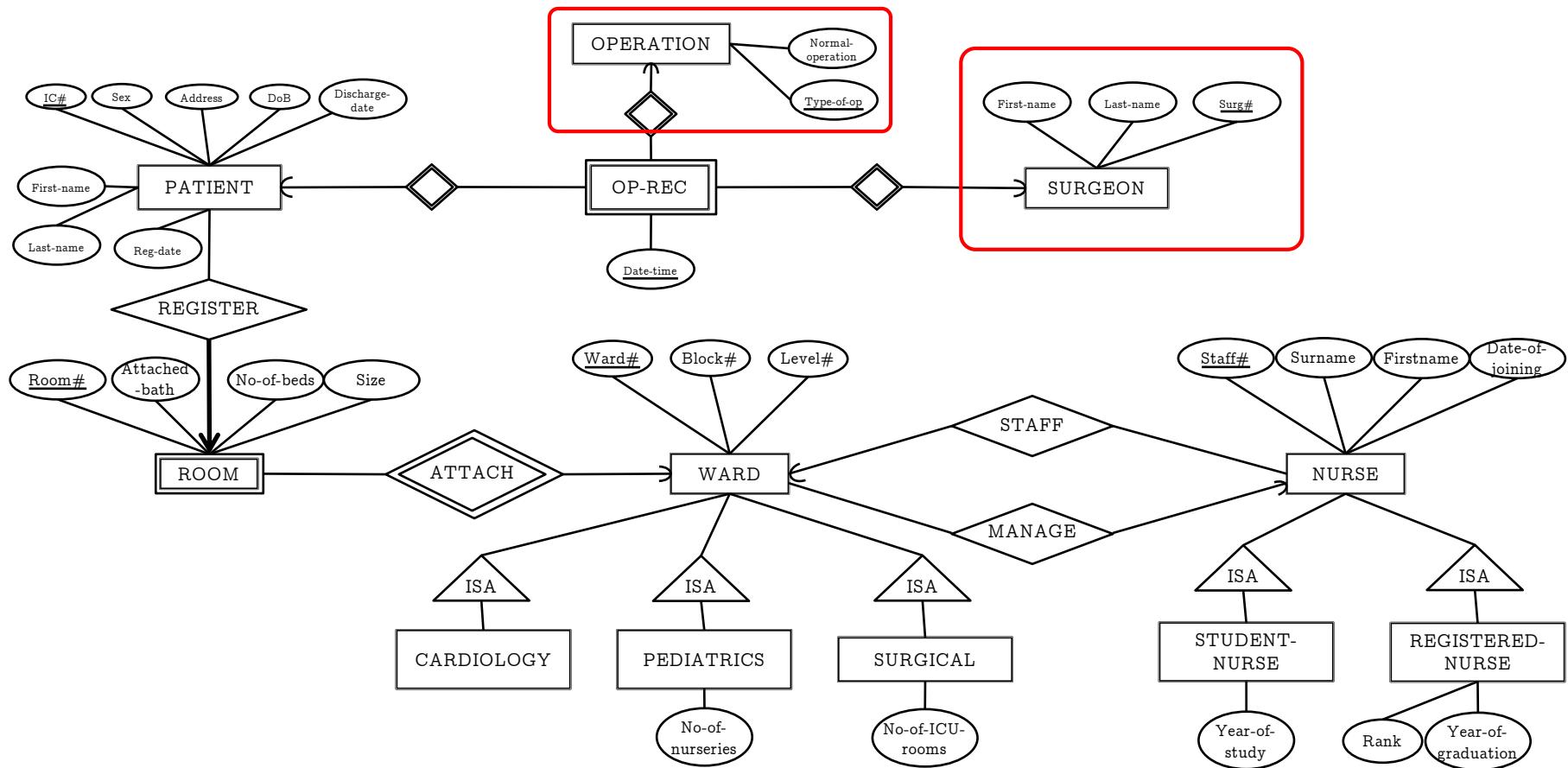


Question 1

1. Translate the ER Diagram of Q1 in Tutorial 1 into a set of relations.



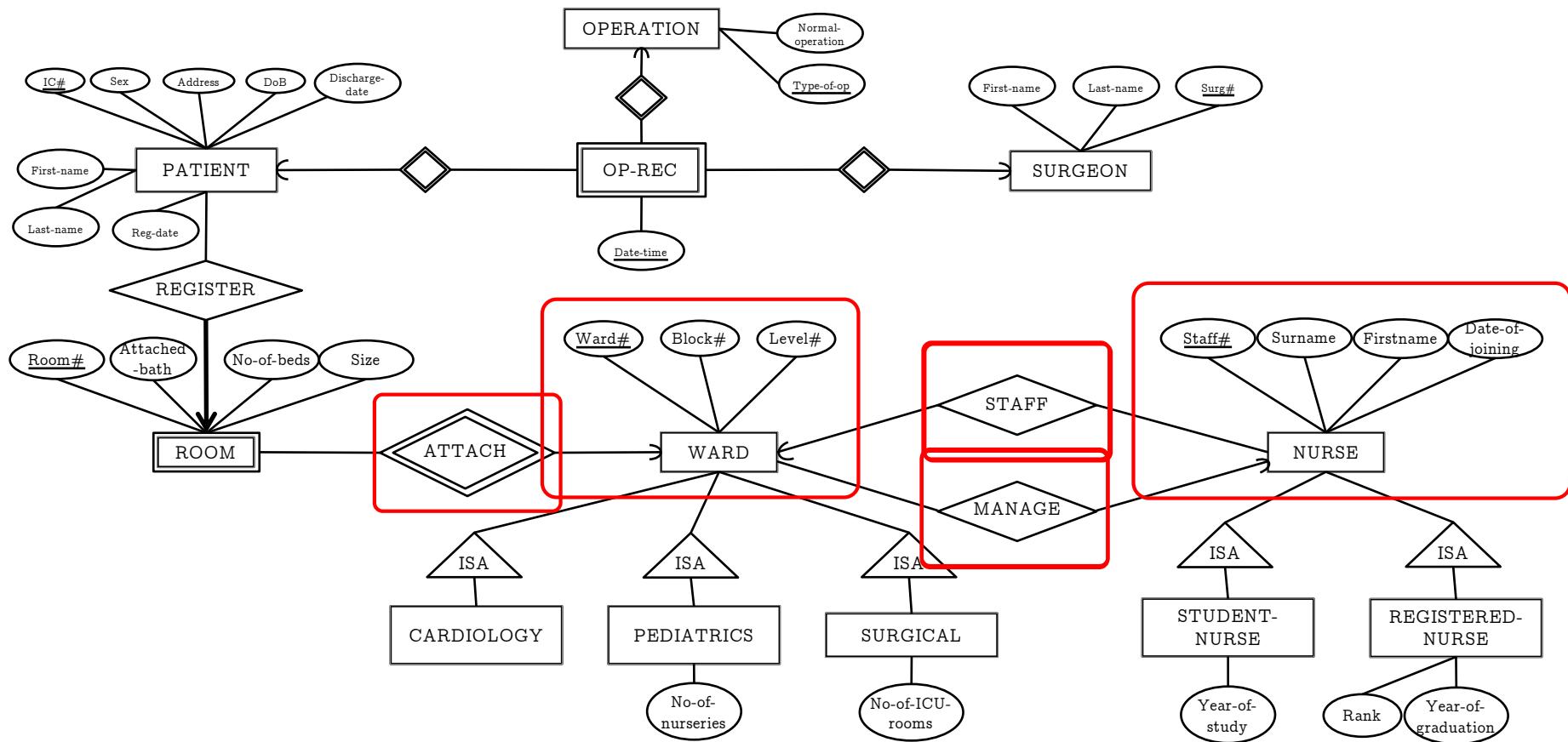
Question 1



- Surgeon (surg#, first-name, surname)
- Operation (type-of-op, normal-duration)



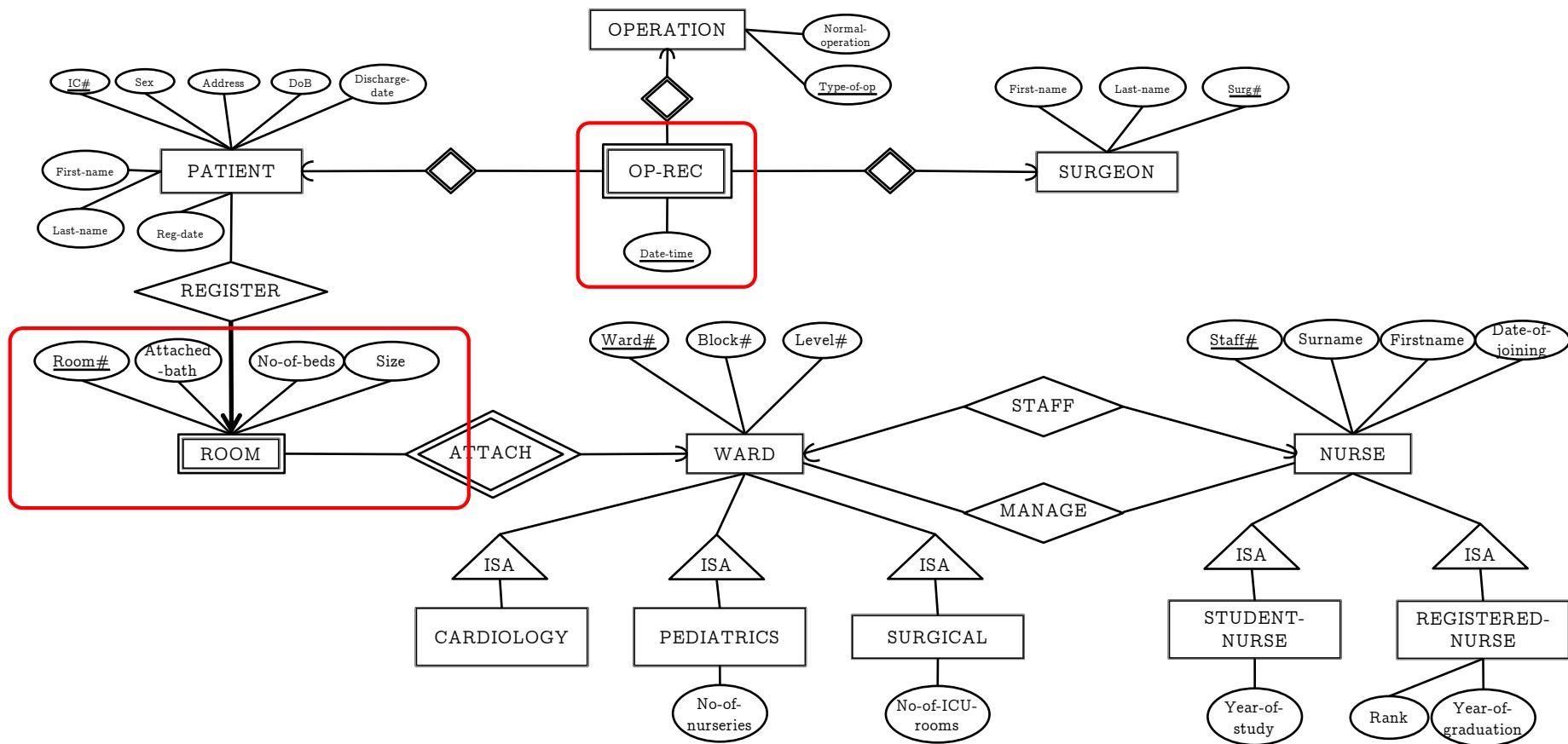
Question 1



- Ward (ward#, blk#, level#, manager) – m2o
- Nurse (staff#, first-name, surname, date-of-joining, ward#) – m2o



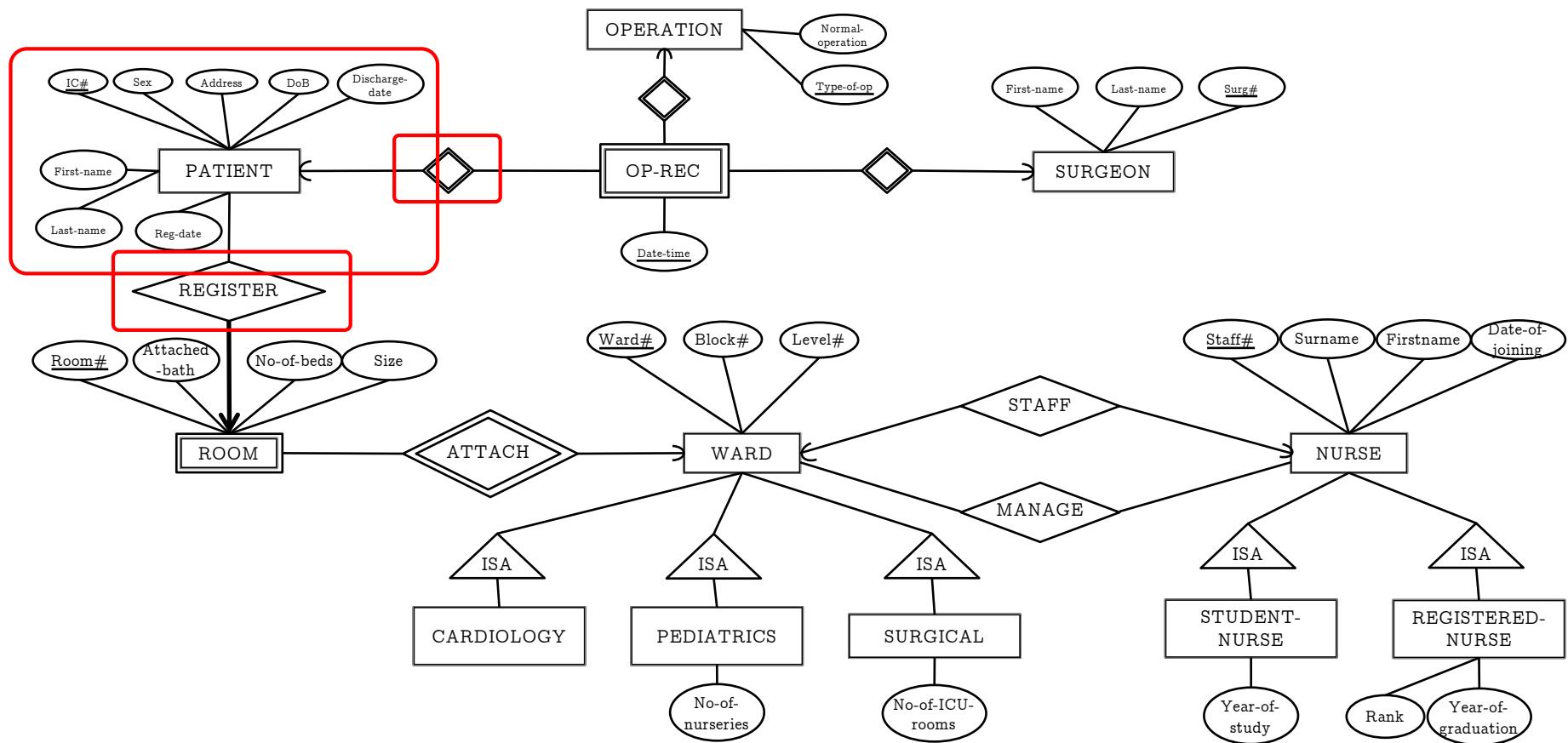
Question 1



- Operate (IC#, surg-id, type-of-op, date-time) – 3 w.e./m2o
- Room (room#, ward#, attached-bath, no-of-beds) – w.e./m2o



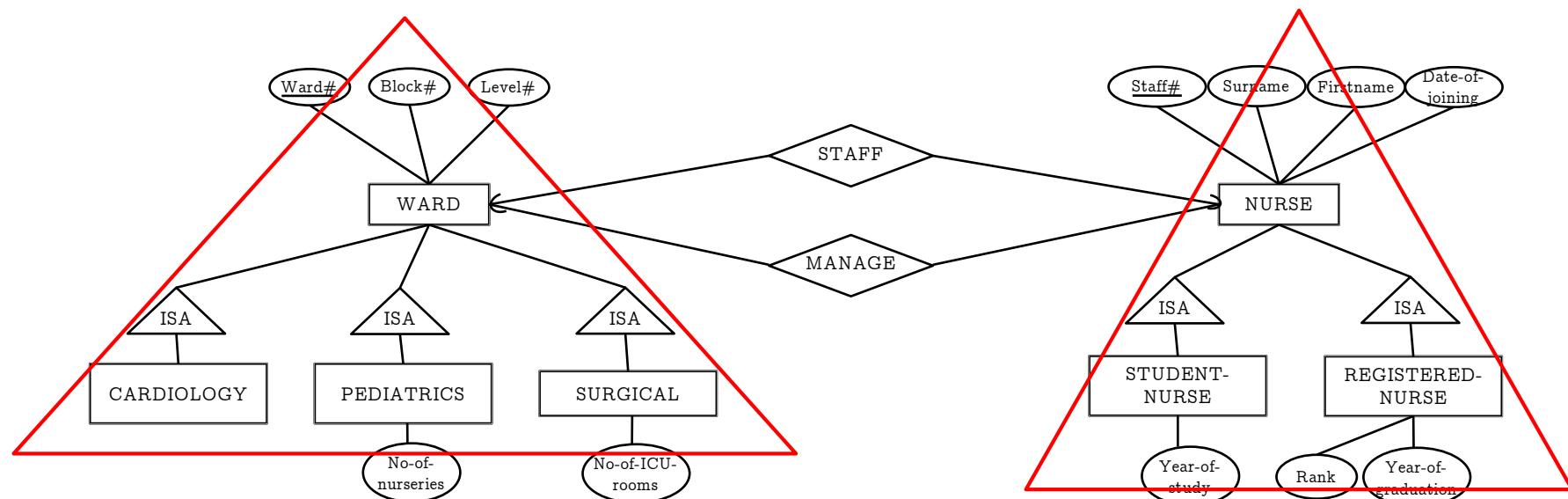
Question 1



- Patient (IC#, first-name, surname, address, date-of-birth, sex, reg-date, discharge-date, **room#**, **ward#**) – m2o



Question 1



- Student_Nurse(staff#, year-of-study)
- Registered_Nurse(staff#, rank, year-of-graduation)
- Surgical_Ward(ward#, no-of-ICU-rooms)
- Pediatrics_Ward(ward#, no-of-nurseries)
- Cardiology_Ward(ward#, no-of-heart-equipment)



Question 2

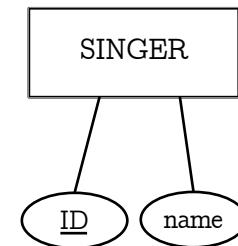
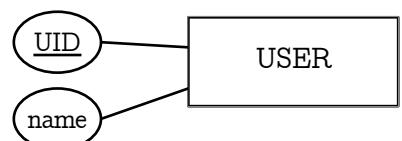
2. Consider the following relational schema:

USER(uid, name)
SINGER(id, name)
ALBUM(id, title, singerid)
SONG(id, title, albumid)
SING(singerid, songid)
FOLLOW_USER(followeruid, followeeuid)
RATE_SONG(uid, songid, rating)
RATE_SINGER(uid, singerid, rating)
PLAY_SONG(uid, songid, datetime)

Construct an ER diagram that leads to the above schema.



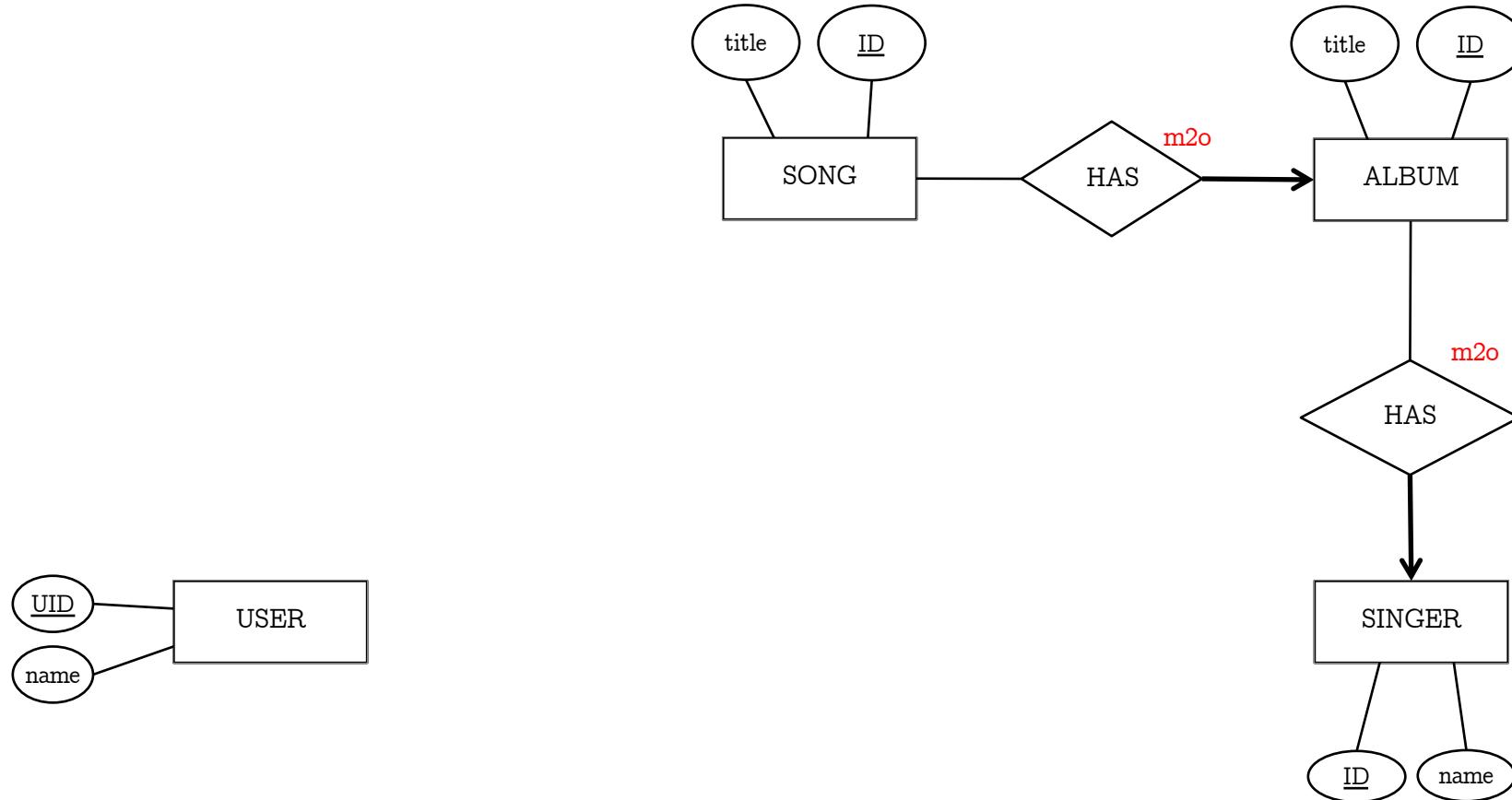
Question 2



- **USER(uid, name)**
- **SINGER(id, name)**



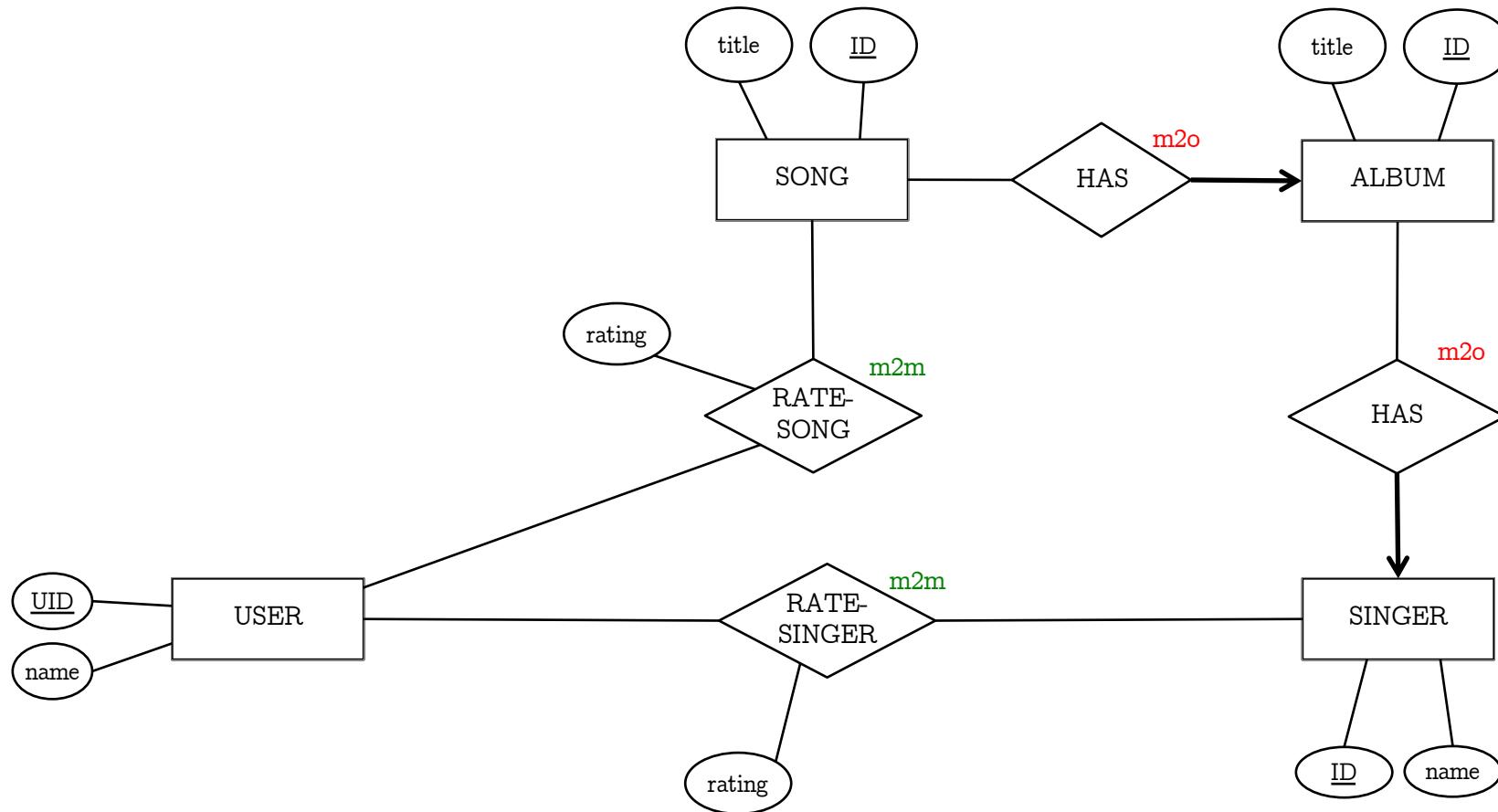
Question 2



- ALBUM(**id**, title, **singerid**)
- SONG(**id**, title, **albumid**)



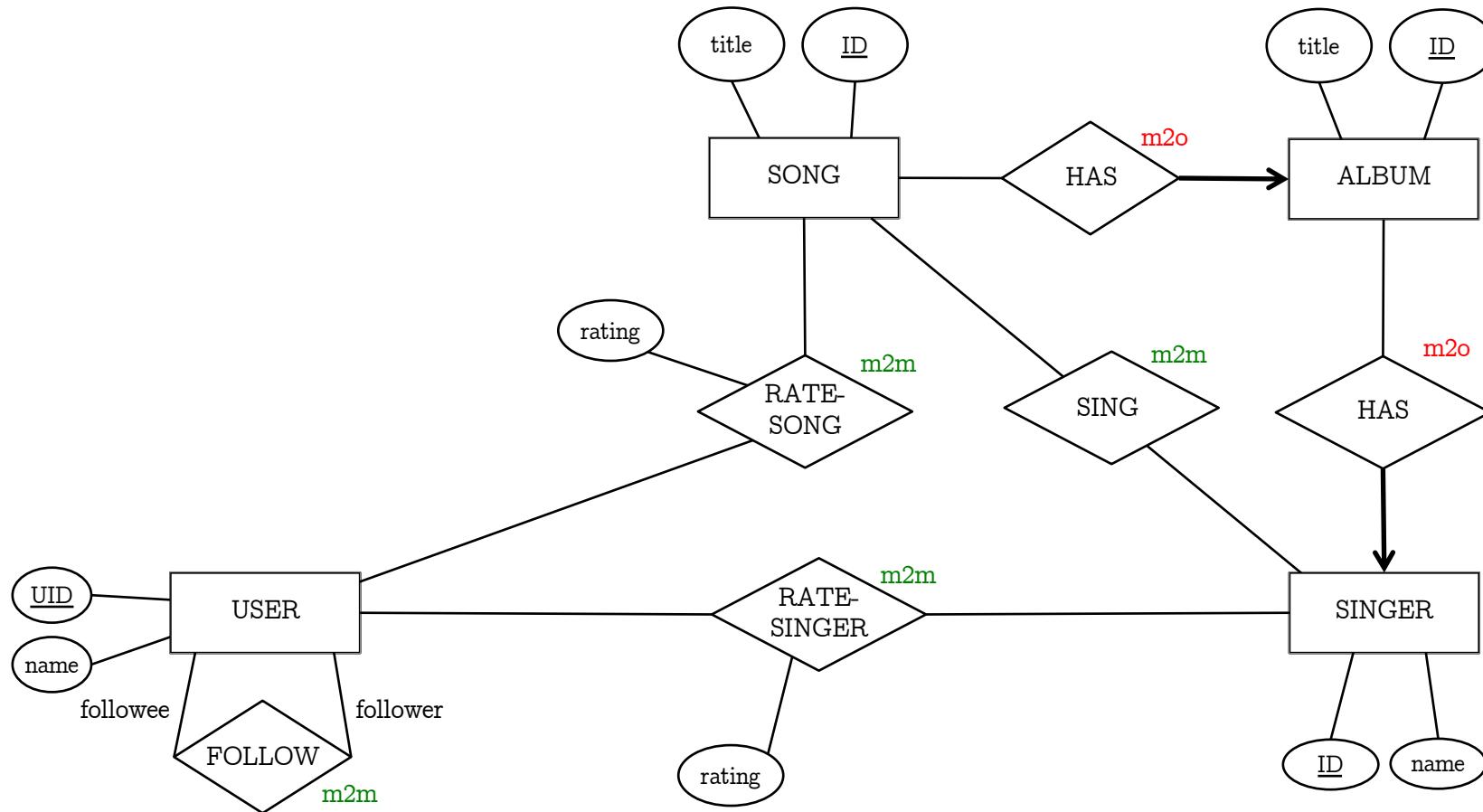
Question 2



- RATE _ SONG(uid, songid, rating)
- RATE _ SINGER(uid, singerid, rating)



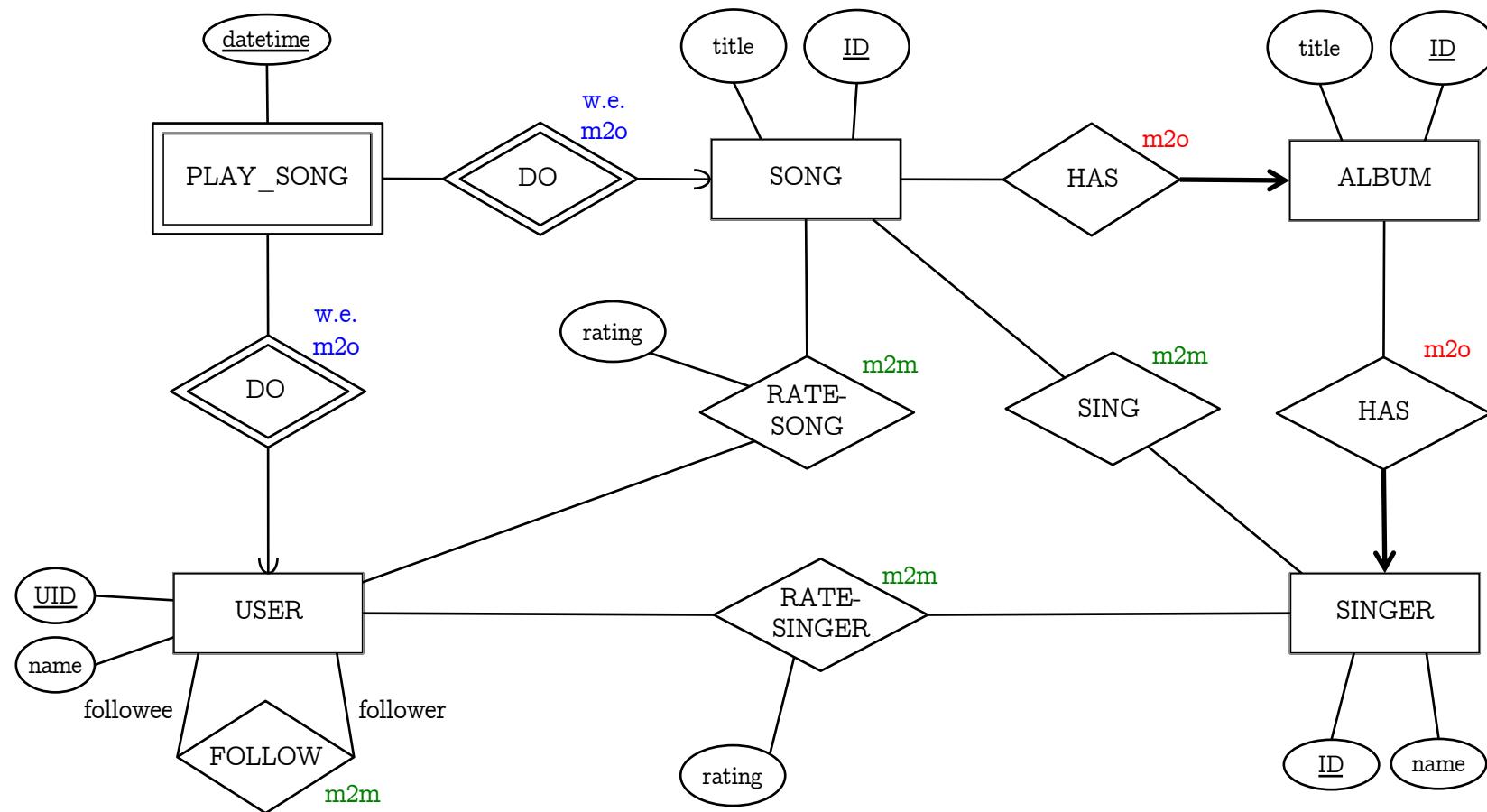
Question 2



- **SING(singerid, songid)**
- **FOLLOW(followeruid, followeeuid)**

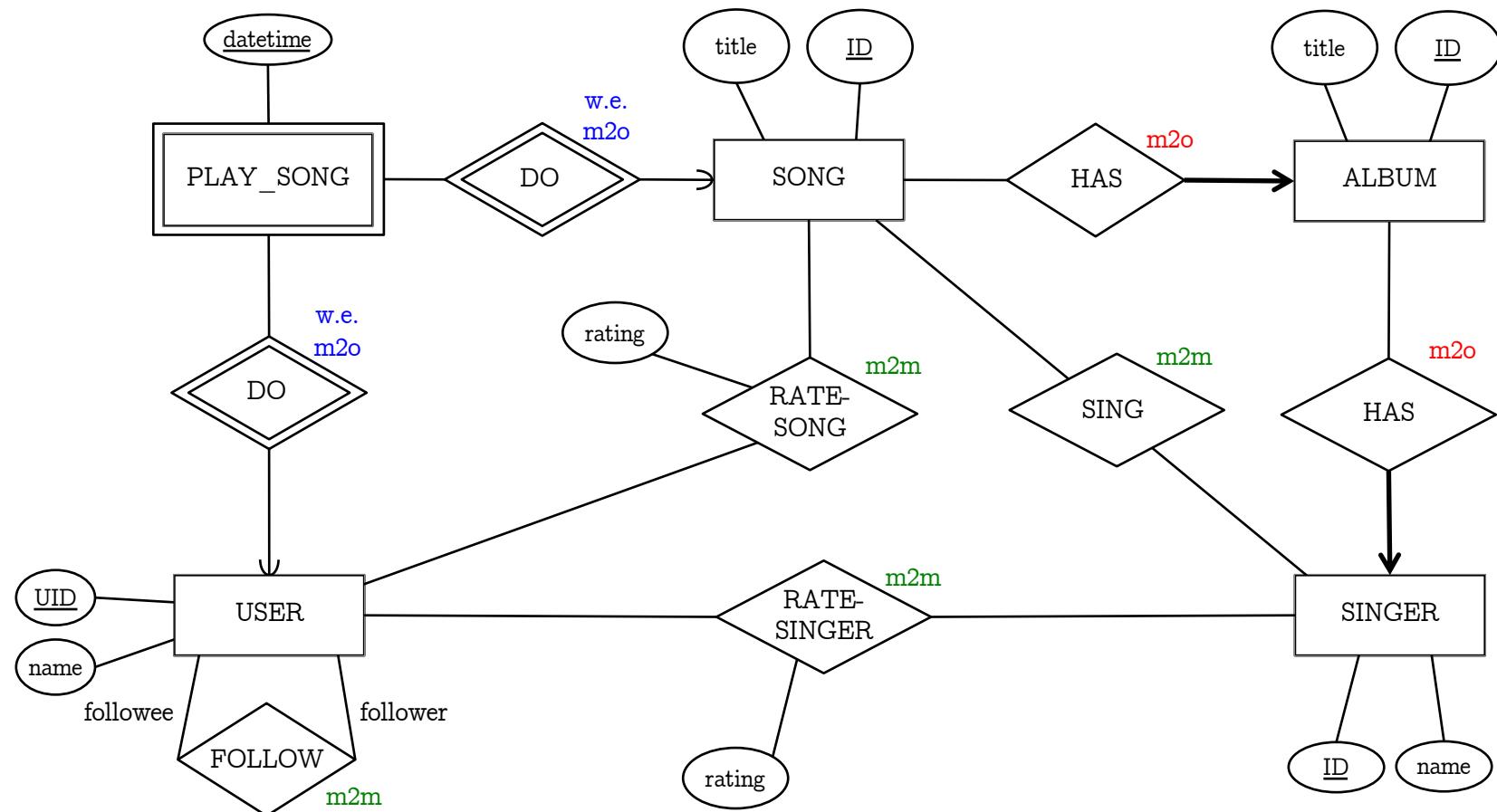


Question 2



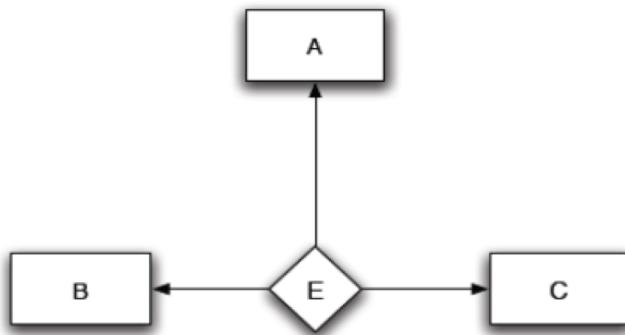
- PLAY_SONG(uid, songid, datetime)



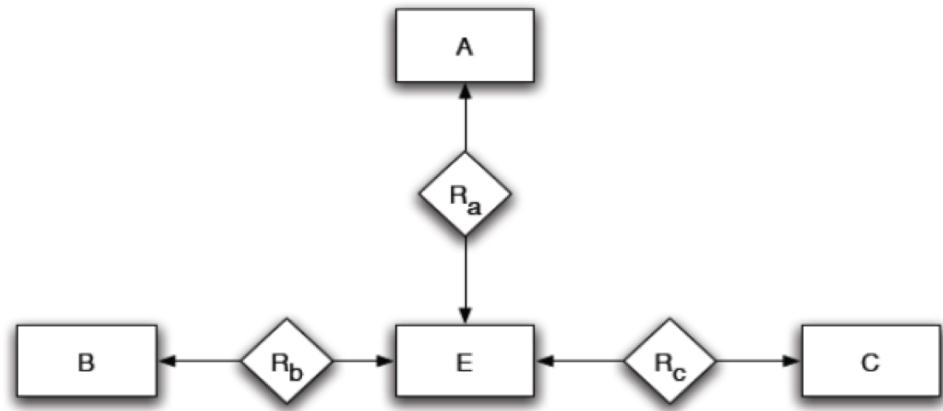


Question 3

3. The figure shows an attempt to represent a ternary relationship between three entities using 3 binary relationships (and one made-up entity). Show through an example why the 3 binary relationship representation is more general than the one ternary relationship representation.



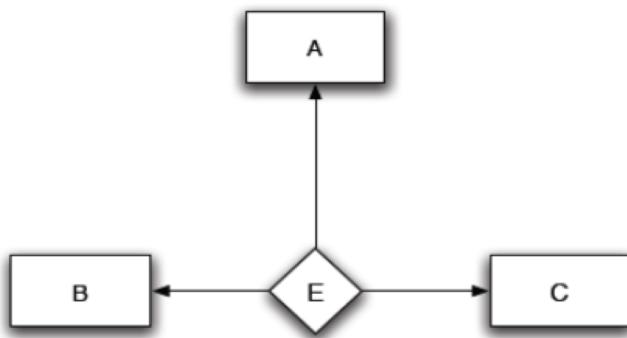
A ternary relationship



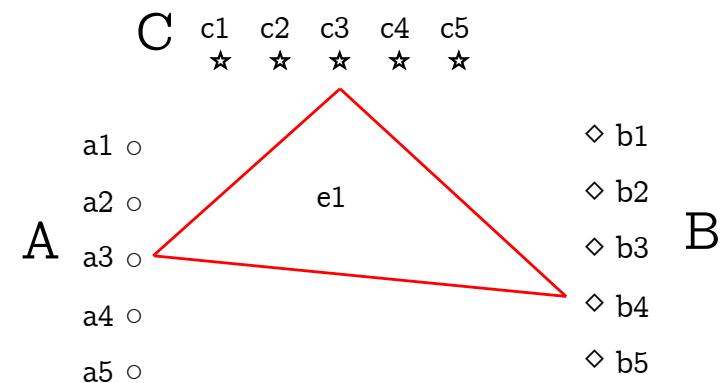
An attempt to represent it using 3
binary relationships



Question 3



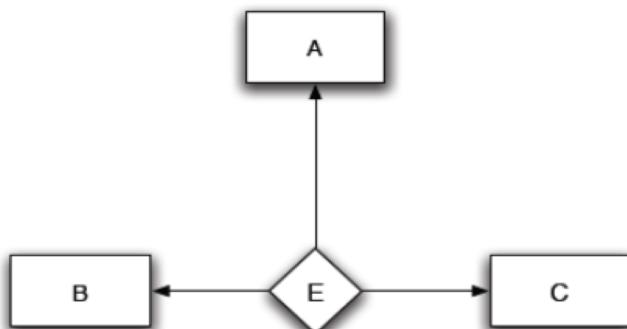
A ternary relationship



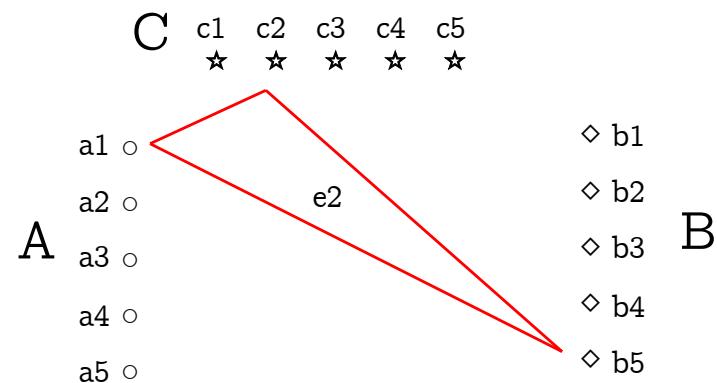
e1 is relationship instance
involving a3, b4, c3



Question 3



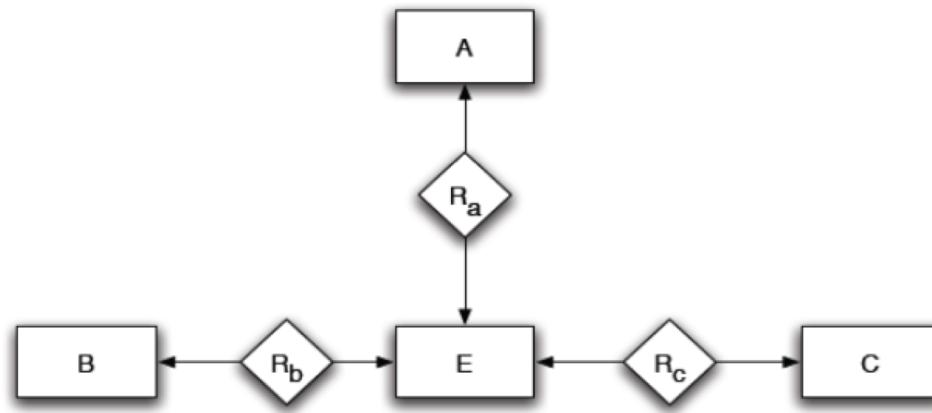
A ternary relationship



$e2$ is relationship instance
involving $a1, b5, c2$



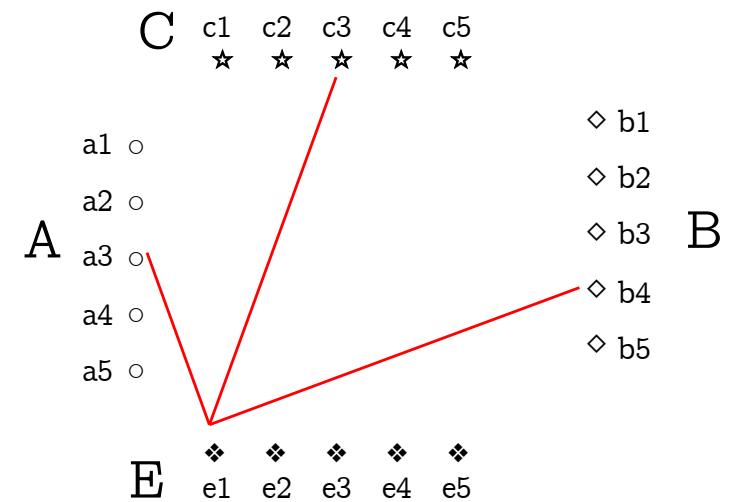
Question 3



e1 related to a3,

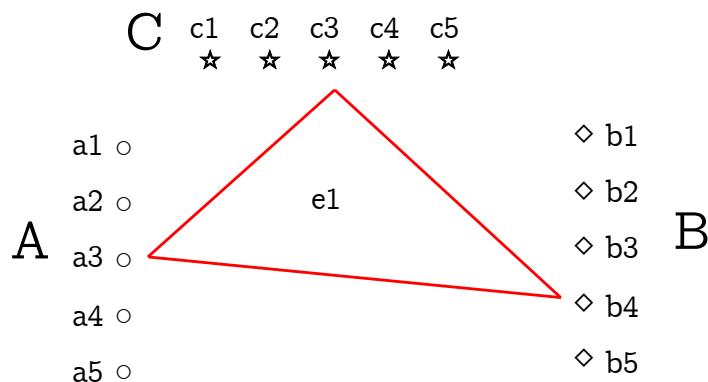
e1 related to b4,

e1 related to c3



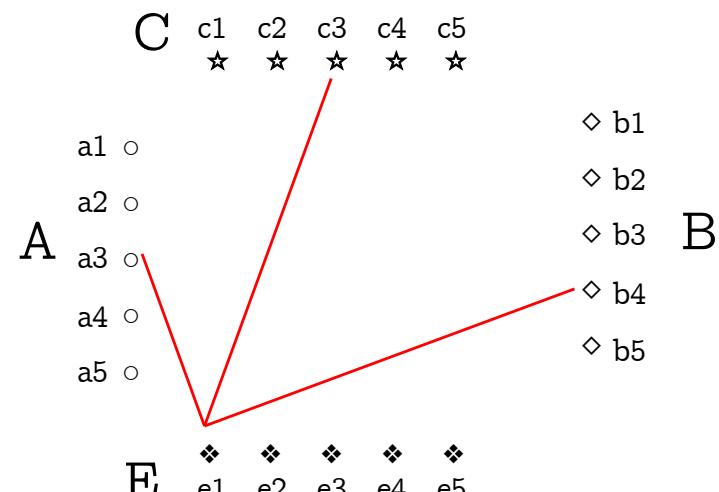
Question 3

e1 is relationship instance
involving a3, b4, c3

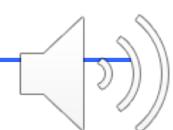


Single ternary relationship

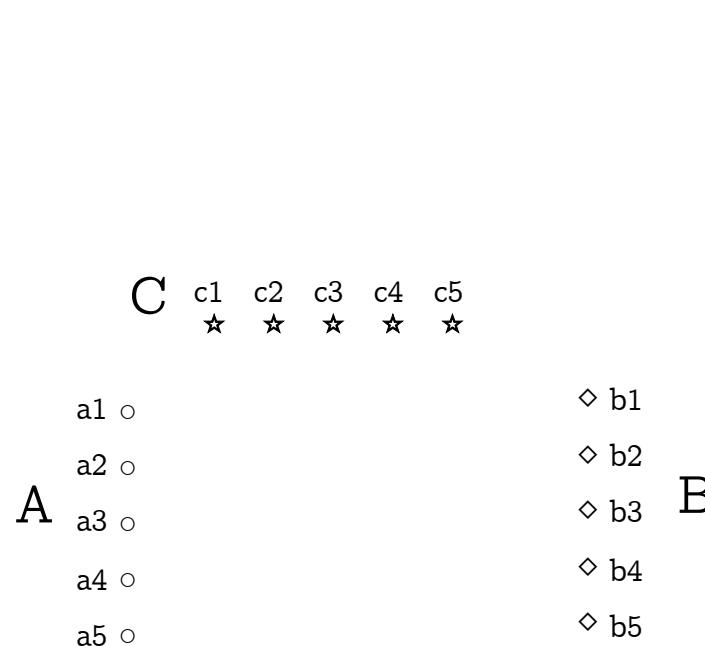
e1 related to a3,
e1 related to b4,
e1 related to c3



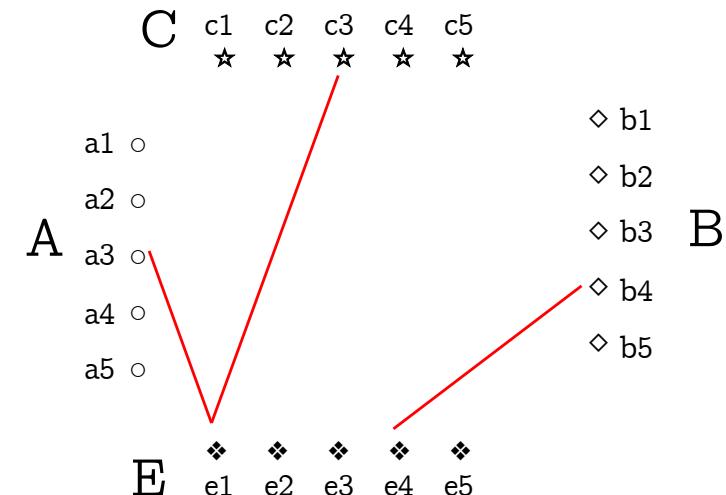
3 binary relationship + 1 entity set



Question 3



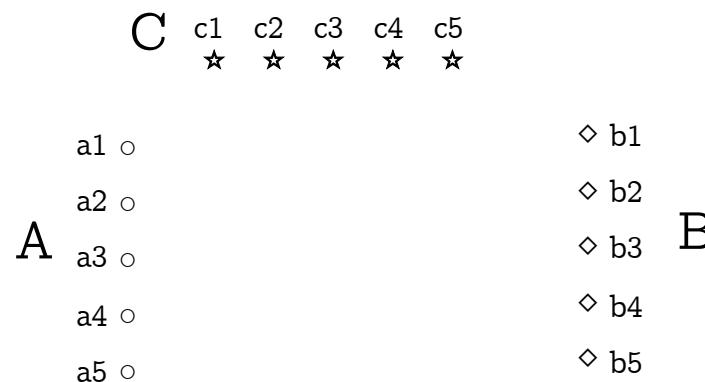
Single ternary relationship



3 binary relationship + 1 entity set

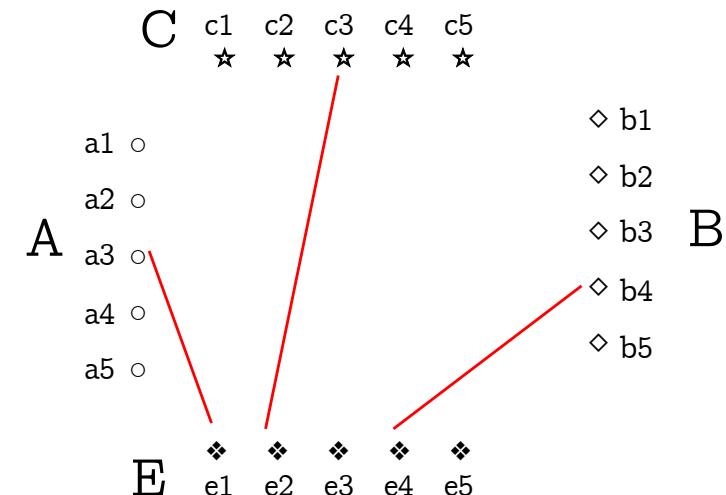


Question 3



Single ternary relationship

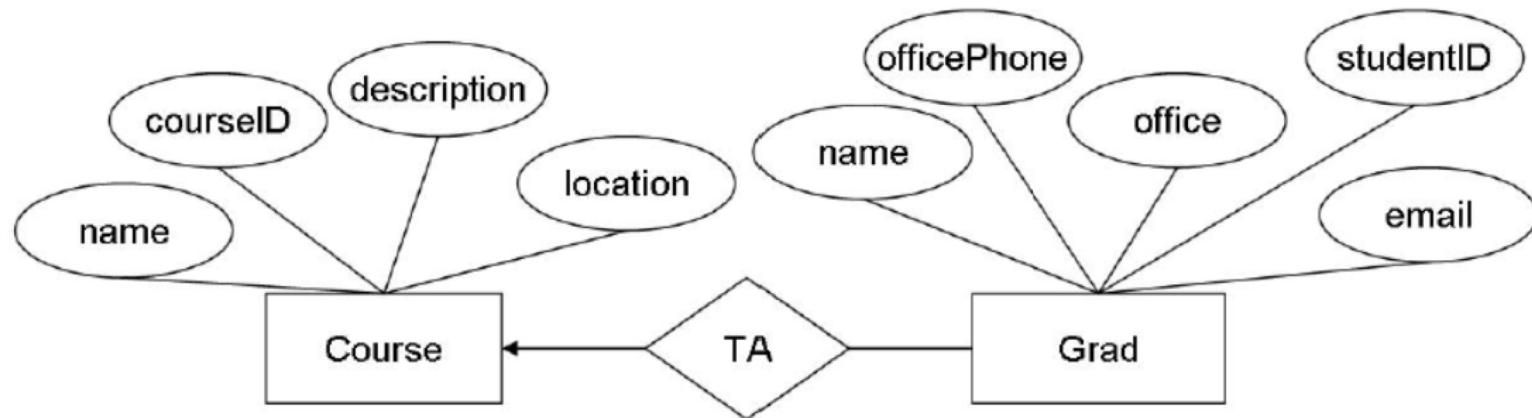
e₁ related to a₃,
e₄ related to b₄,
e₂ related to c₃



3 binary relationship + 1 entity set



4. Consider the following ER diagram that describes graduate students (Grad) and courses (Course) they serve as Teaching Assistants (TA).



- (a) For each of the following statements, write a functional dependency (FD) that best captures the statement.

- The studentID of each graduate student uniquely identifies the student.
- No two offices have the same phone number (officePhone).
- No two courses have the same courseID.
- If two courses have the same course name, their course descriptions are the same.

- (b) From the ER diagram and the set of FDs you listed above, can you derive new FDs? If no, explain why not. If yes, derive two non-trivial FDs.



Question 4(a)

(a) For each of the following statements, write a functional dependency (FD) that best captures the statement.

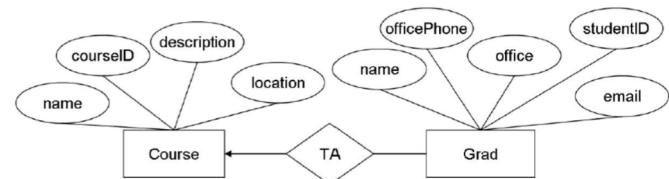
- The studentID of each graduate student uniquely identifies the student.
- No two offices have the same phone number (officePhone).
- No two courses have the same courseID.
- If two courses have the same course name, their course descriptions are the same.

- F1: $\text{studentID} \rightarrow \text{officePhone}, \text{office}, \text{email}, \text{name}$
- F2: $\text{officePhone} \rightarrow \text{Office}$
- F3: $\text{courseID} \rightarrow \text{name}, \text{description}, \text{location}$
- F4: $\text{name} \rightarrow \text{description}$



Question 4(b)

- (b) From the ER diagram and the set of FDs you listed above, can you derive new FDs? If no, explain why not. If yes, derive two non-trivial FDs.
- F1: studentID → officePhone, office, email, name
 - F2: officePhone → Office
 - F3: courseID → name, description, location
 - F4: name → description
 - F5: studentID → courseID. This is derived from m2o TA relationship.
 - F6: studentID → name, description, location. This is derived from F3 and F5.





Winners are not people who never fail
but people who never quit.

Best of Luck



Tutorial 2

Functional Dependencies

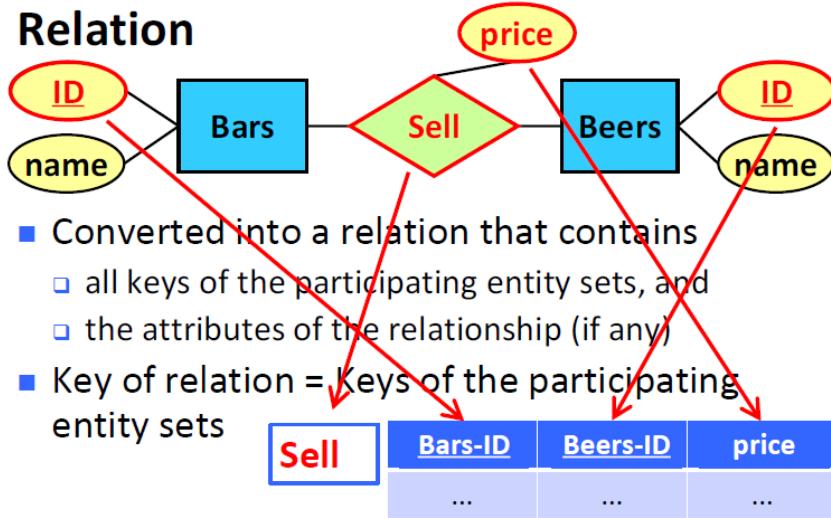
CZ2007
Introduction to Databases

Tutorial 2

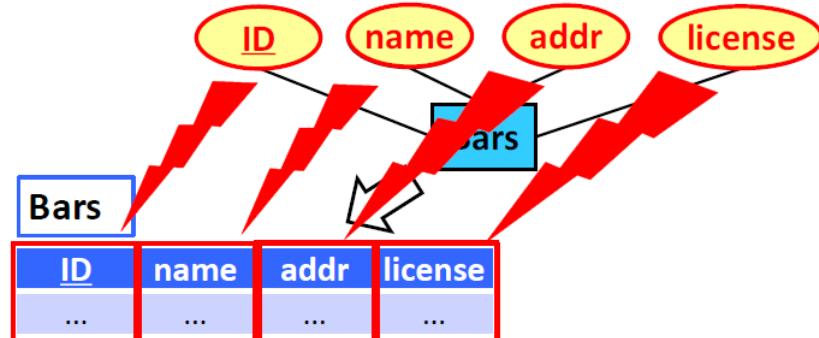
ER Diagram → Relational Schema

- General rules:
 - Each entity set  becomes a relation 
 - Each many-to-many relationship  becomes a relation 
- Special treatment needed for:
 - Weak entity sets   
 - Subclasses   
 - Many-to-one and one-to-one relationships   

Many-to-Many Relationship → Relation

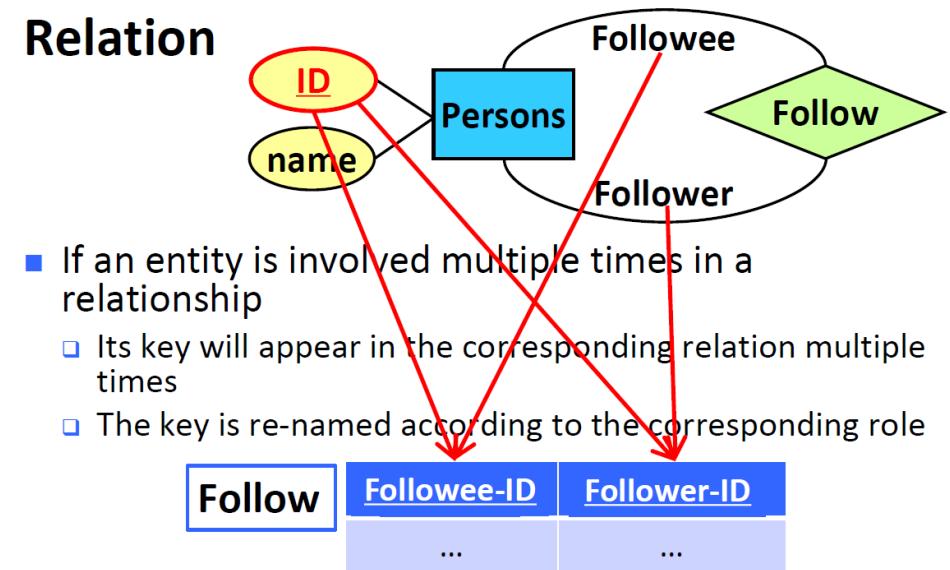


Entity Set → Relation



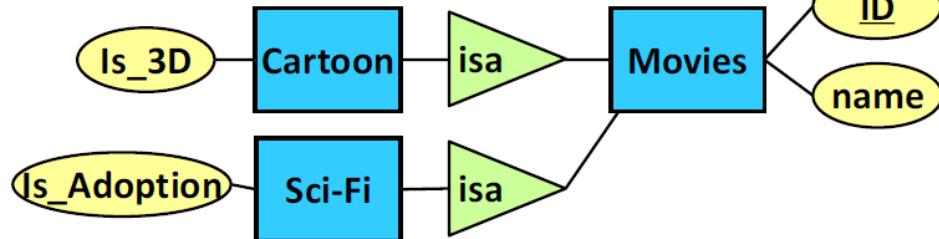
- Each entity set is converted into a relation that contains all its attributes
- Key of the relation = key of the entity set

Many-to-Many Relationship → Relation



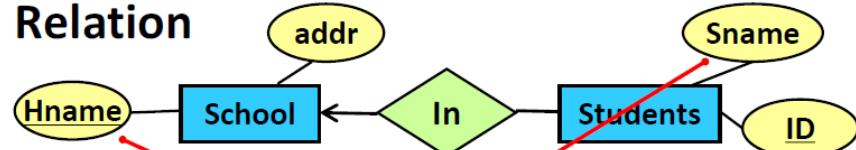
Tutorial 2

Subclass → Relation



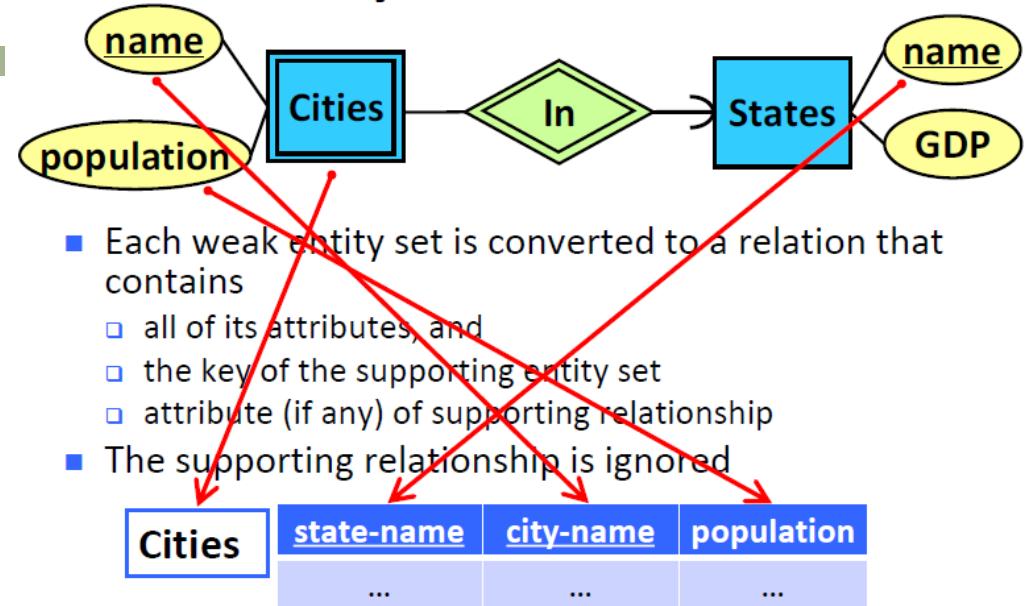
- One relation for each entity set
 - Movies(ID, name)
 - Cartoon(ID, Is_3D)
 - Sci-Fi(ID, Is_Adoption)

Many-to-One Relationship → Relation

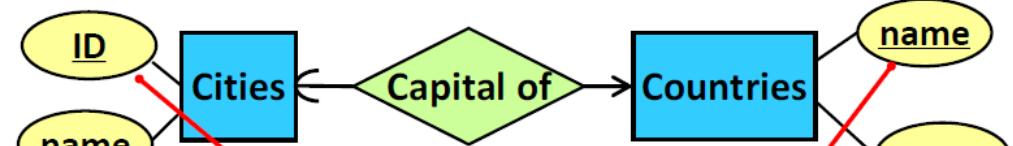


- Translation:
 - School(Hname, addr)
 - Students(ID, Sname, Hname)
 - Only need to put the key of the “one” side into the relation of the “many” side

Weak Entity Set → Relation



One-to-One Relationship → Relation



Tutorial 2

Functional Dependencies:

- In general, how do we know whether a combination of attributes is bad?
- We need to check the **correlations** among those attributes

Formal Definition of FD

- Attributes A_1, A_2, \dots, A_m , B_1, B_2, \dots, B_n
- $A_1 A_2 \dots A_m \rightarrow B_1 B_2 \dots B_n$
- Meaning: There do not exist two objects that
 - Have the same values on A_1, A_2, \dots, A_m
 - but different values on B_1, B_2, \dots, B_n

Reasoning with FDs

- Given $A \rightarrow B$, $BC \rightarrow D$
- Can you prove that $AC \rightarrow D$?
- Proof
 - Given $A \rightarrow B$, we have $AC \rightarrow BC$ (Augmentation)
 - Given $AC \rightarrow BC$ and $BC \rightarrow D$, we have $AC \rightarrow D$ (Transitivity)

Reasoning with FDs

- Armstrong's Axioms
 - Three axioms for FD reasoning
 - Easy to understand, but not easy to apply
- Axiom of Reflexivity
 - A set of attributes \rightarrow A **subset** of the attributes
- Axiom of Augmentation
 - Given $A \rightarrow B$
 - We always have $AC \rightarrow BC$, for any C
- Axiom of Transitivity
 - Given $A \rightarrow B$ and $B \rightarrow C$
 - We always have $A \rightarrow C$

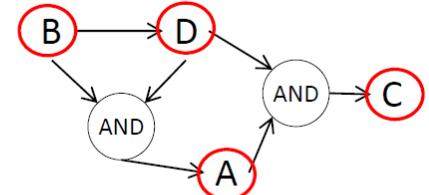
Tutorial 2

Reasoning with FDs

- Given $A \rightarrow B$, $BC \rightarrow D$
- Can you prove that $AC \rightarrow D$?
- Proof
 - Given $A \rightarrow B$, we have $AC \rightarrow BC$ (Augmentation)
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Steps of the Intuitive Solution

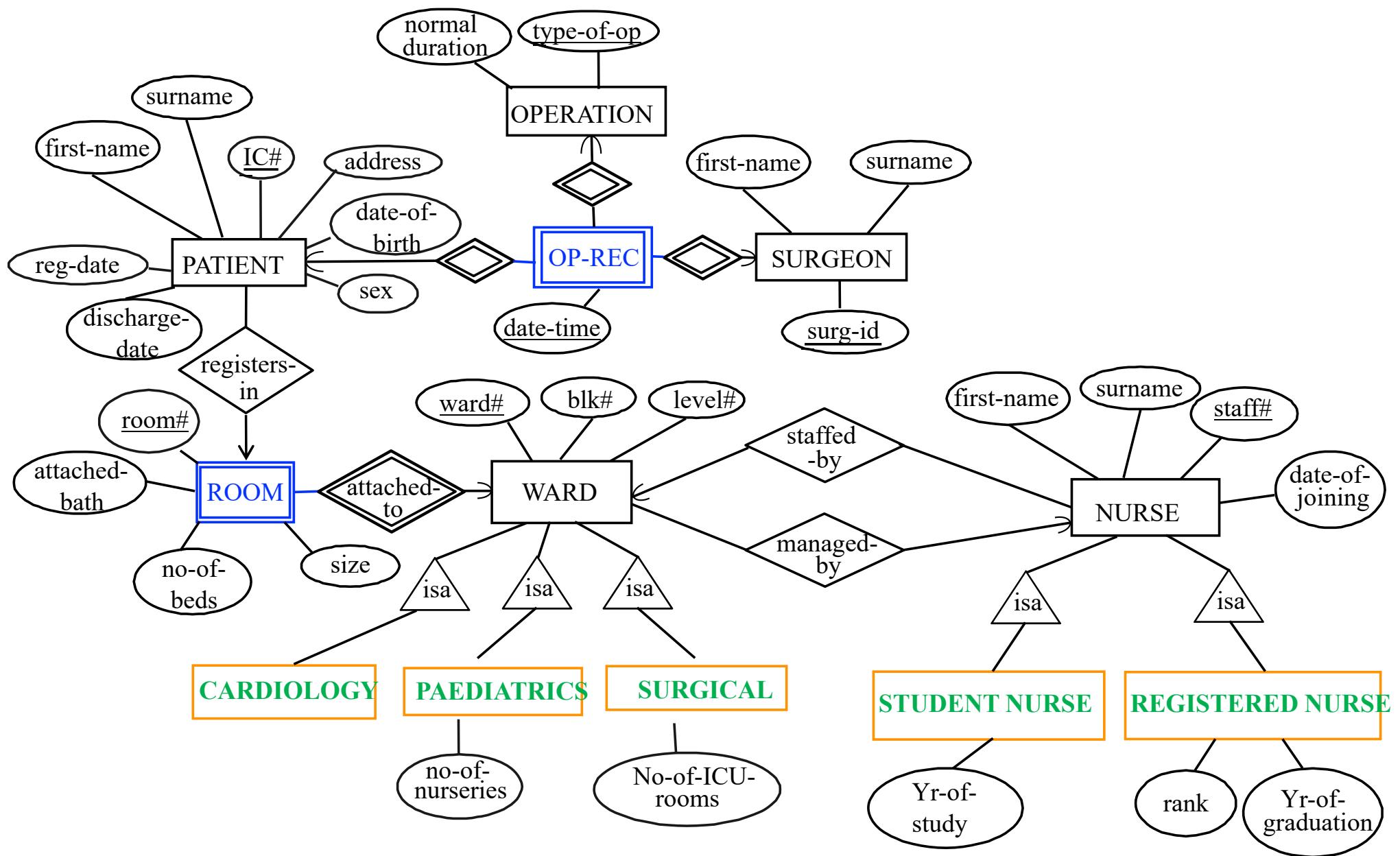
- Four attributes: A, B, C, D
- Given: $B \rightarrow D$, $DB \rightarrow A$, $AD \rightarrow C$
- Can you prove $B \rightarrow C$?



- First, activate B
 - Activated set = { B }
- Second, activate whatever B can activate
 - Activated set = { B, D }, since $B \rightarrow D$
- Third, use all activated elements to activate more
 - Activated set = { B, D, A }, since $DB \rightarrow A$
- Repeat the third step, until no more activation is possible
 - Activated set = { B, D, A, C }, since $AD \rightarrow C$; done

Question 1

1. Translate the ER Diagram of Q1 in Tutorial 1 into a set of relations.



Question 1: Relational Tables

- Surgeon (surg-id, first-name, surname)
- Operation (type-of-op, normal-duration)
- Patient (IC#, first-name, surname, address, date-of-birth, sex, reg-date, discharge-date, **room#**, **ward#**) – m2o
- Ward (ward#, blk#, level#, no-of-nurseries, no-of-ICU-rooms, **manager**)
 - m2o
- Nurse (staff#, first-name, surname, date-of-joining, **wardStaff#**) – m2o
- Op-Rec (IC#, surg-id, type-of-op, date-time) – w.e./m2o
- Room (room#, ward#, attached-bath, no-of-beds) – w.e./m2o

Question 1: Relational Tables

- Subclass relationships:
- Student_Nurse(staff#, Yr-of-study)
- Registered_Nurse(staff#, rank, yr-of-graduation)
- Surgical_Ward(ward#, No_of_ICU_rooms)
- Pediatrics_Ward(ward#, No_of_nurseries)
- Cardiology_Ward(ward#, no_of_heart_equipment)

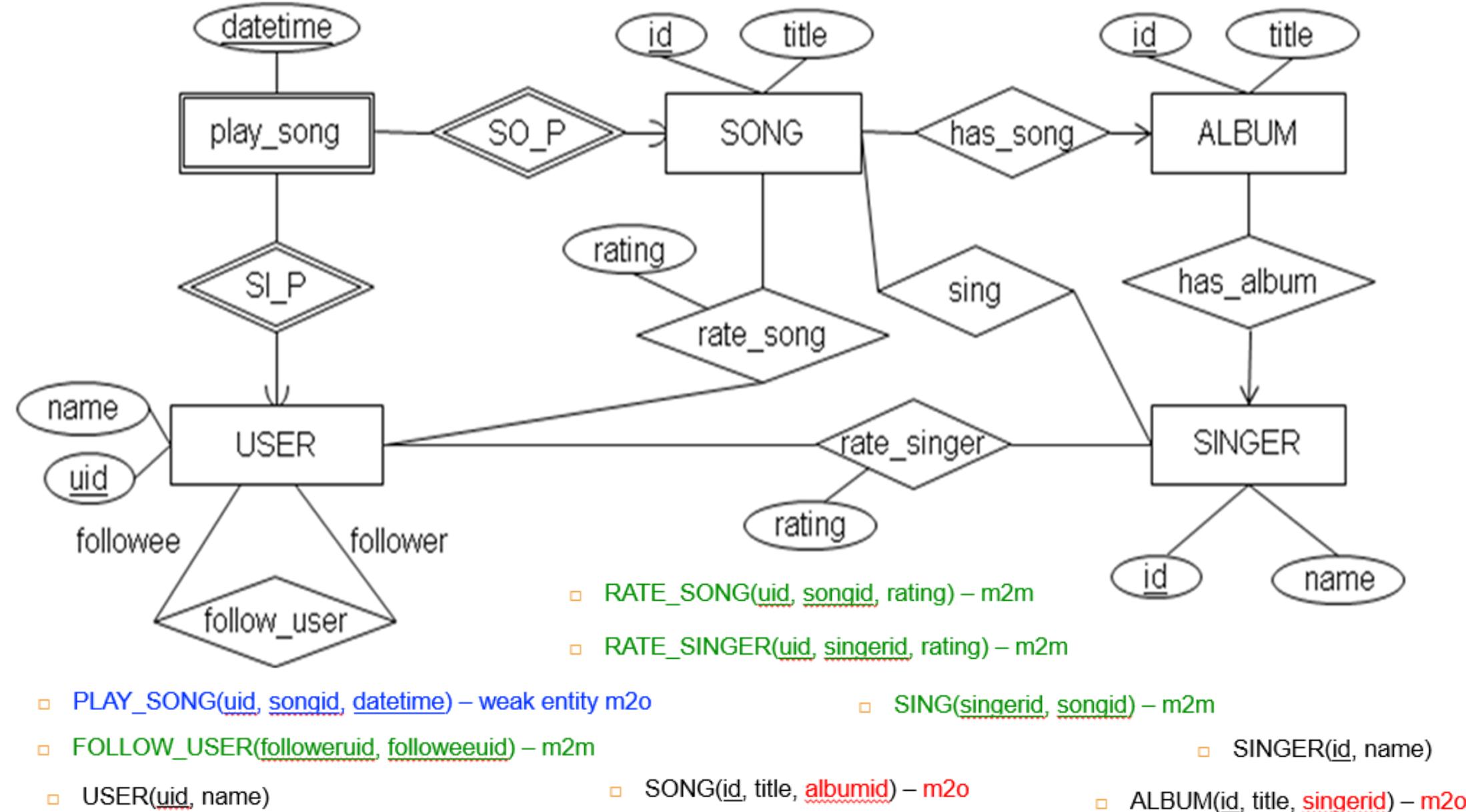
Question 2

2. Consider the following relational schema:

- **USER**(uid, name)
- **SINGER**(id, name)
- **ALBUM**(id, title, **singerid**) – m2o
- **SONG**(id, title, **albumid**) – m2o
- **SING**(singerid, songid) – **m2m**
- **FOLLOW_USER**(followeruid, followeeuid) – **m2m**
- **RATE_SONG**(uid, songid, rating) – **m2m**
- **RATE_SINGER**(uid, singerid, rating) – **m2m**
- **PLAY_SONG**(uid, songid, datetime) – weak entity m2o

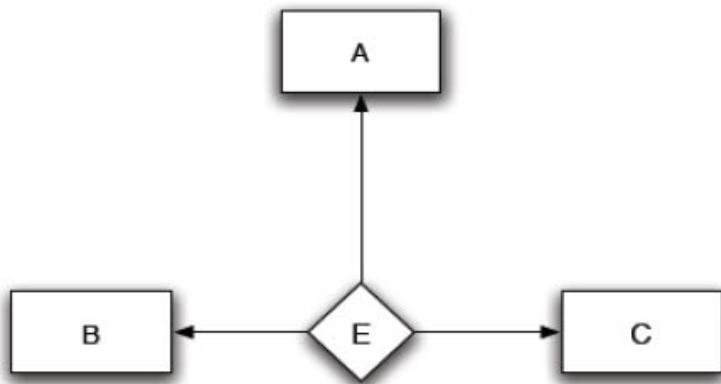
Construct an ER diagram that leads to the above schema.

Question 2

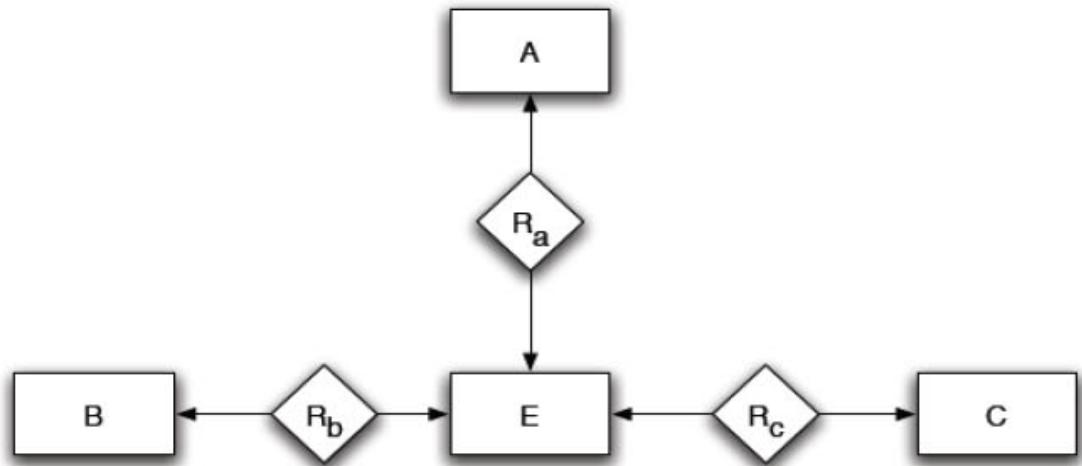


Question 3

3. The figure shows an attempt to represent a ternary relationship between three entities using 3 binary relationships (and one made-up entity). Show through an example why the 3 binary relationship representation is more general than the one ternary relationship representation.



A ternary relationship



An attempt to represent it using 3
binary relationships

Question 3

Why is a **3 binary relationship relationship representation** more general than **one ternary relationship representation**?

(<https://stackoverflow.com/questions/39254141/ternary-relationship-or-3-binary-relationship>)

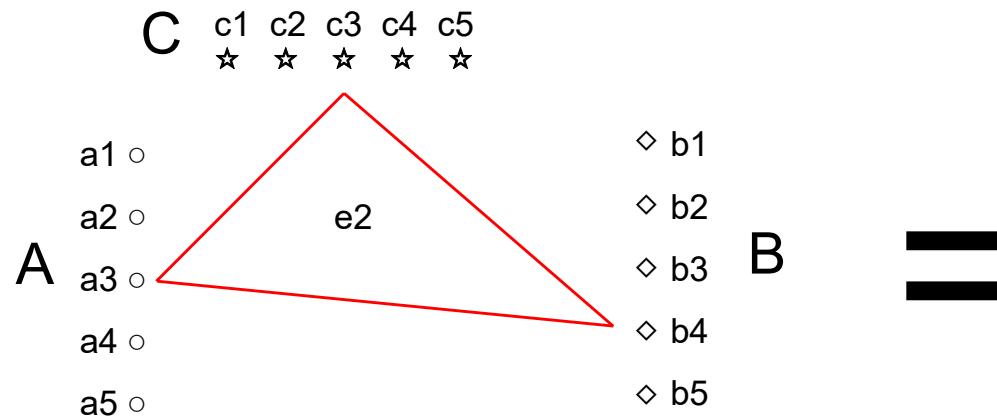
Because with 3 binary relationships each involved entity is related separately with each one of the others two.

Assumed that ternary relationship is essential only when you have a many-to-many-to-many relationship (otherwise you can rewrite it adding a relational entity linked with binary relationships to the others three), let's take an example:

- Suppose that you have the entities A, B and C, and three relationships that link the entities "like a triangle". Now, suppose that set of tuples a3 is related to the sets b4 and c3.
- Using 3 binary relationships, it's not requested that b4 and c3 are related. for example, b4 can be related to c2, that can partially overlap c3 or be completely disjoined.
- With a ternary relationship, instead, b4 must be related to c3.
- So you can see that with 3 binary relationships you can have much more combinations.

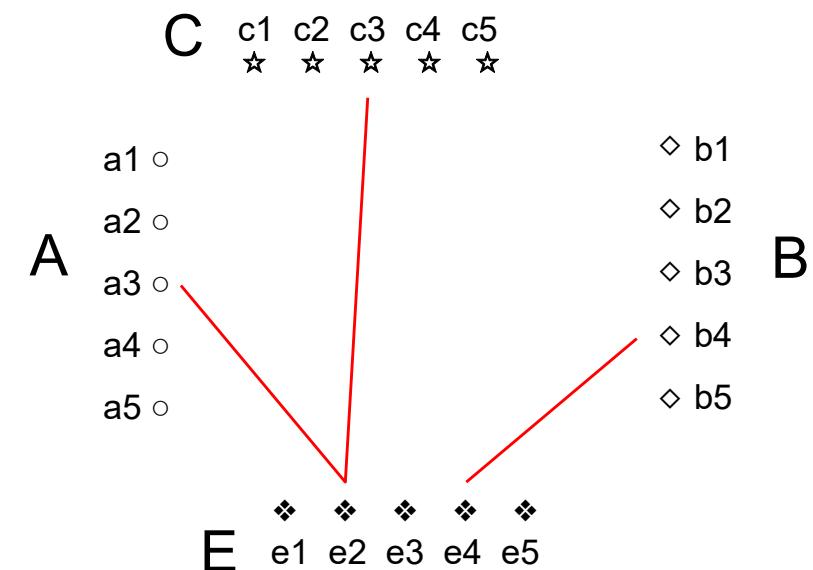
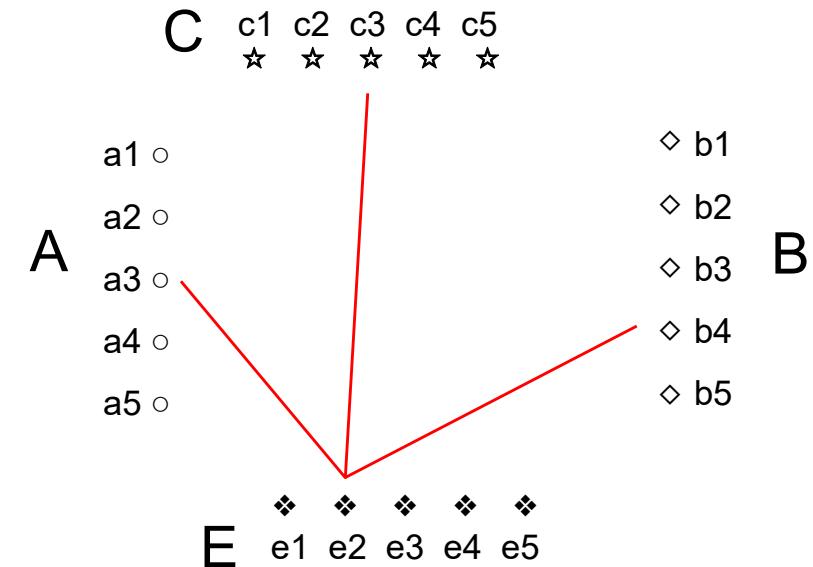
Question 3

Ternary relationship



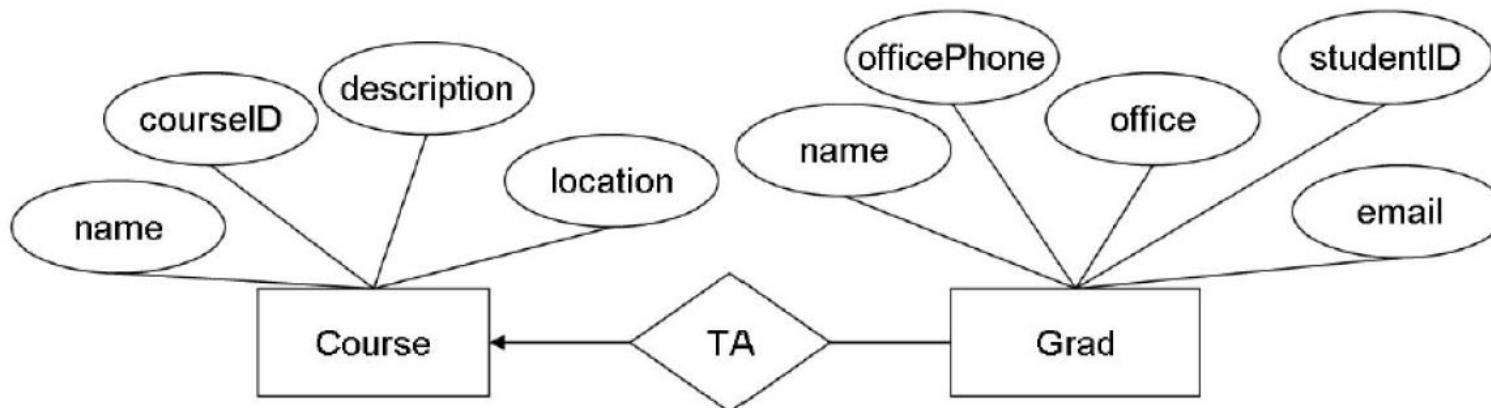
?

Three 2-binary relationships



Question 4

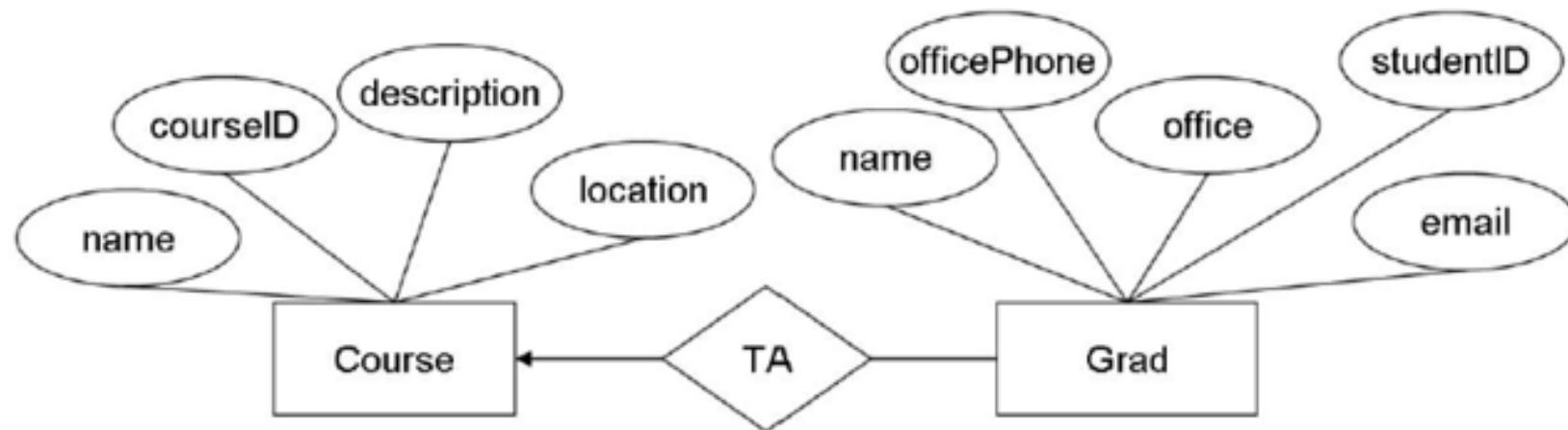
4. Consider the following ER diagram that describes graduate students (Grad) and courses (Course) they serve as Teaching Assistants (TA).



- (a) For each of the following statements, write a functional dependency (FD) that best captures the statement.
- The studentID of each graduate student uniquely identifies the student.
 - No two offices have the same phone number (officePhone).
 - No two courses have the same courseID.
 - If two courses have the same course name, their course descriptions are the same.
- (b) From the ER diagram and the set of FDs you listed above, can you derive new FDs? If no, explain why not. If yes, derive two non-trivial FDs.

Question 4(a)

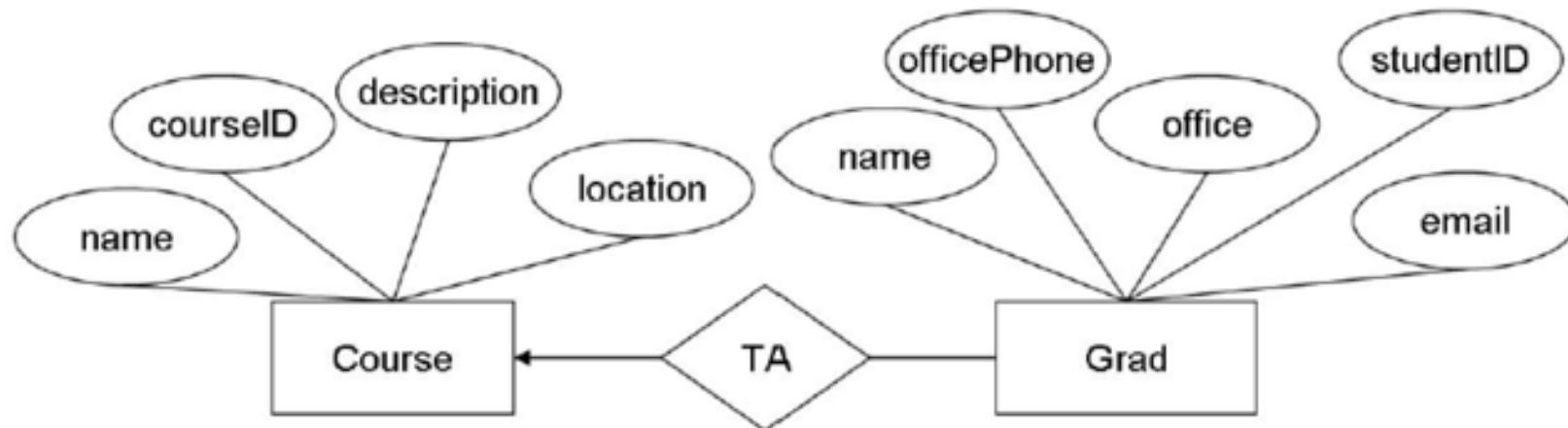
- (a) For each of the following statements, write a functional dependency (FD) that best captures the statement.



- The studentID of each graduate student uniquely identifies the student.
 - F1: $\text{studentID} \rightarrow \text{officePhone}, \text{office}, \text{email}, \text{name}$
- No two offices have the same phone number (officePhone).
 - F2: $\text{officePhone} \rightarrow \text{Office}$

Question 4(a)

- (a) For each of the following statements, write a functional dependency (FD) that best captures the statement.



- No two courses have the same courseID.
- F3: $\text{courseID} \rightarrow \text{name, description, location}$
- If two courses have the same course name, their course descriptions are the same.
- F4: $\text{name} \rightarrow \text{description}$

Question 4(b)

(b) From the ER diagram and the set of FDs you listed above, can you derive new FDs? If no, explain why not. If yes, derive two non-trivial FDs.

- F5: studentID → courseID.

This is derived from the TA relationship, F1, and F3.

- F6: studentID → name, description, location.

This is derived from F3 and F5.

Tutorial 3

Functional Dependencies & Normalisation

Classroom Exercise

1. A medical clinic database schema contains the following:

APPOINTMENT (patient-id, patient-name, doctor-id, doctor-name, appointment-date, appointment-time, clinic-room-no)

Show, with suitable examples, the insertion anomalies that the schema is liable to encounter.

2. Consider the relation ADDRESS having attributes Street, City, State and Zip. Assume that for any given zipcode, there is just one city and state. Also, for any given street, city, and state, there is just one zipcode.
- (a) Infer all possible functional dependencies (FDs) for this relation.
 (b) Which are possible minimal keys?
3. Prove the following properties using Armstrong's axioms or reject it by counterexample relations.
- a) $A \rightarrow B$ $\begin{matrix} AC \rightarrow BC \\ BC \rightarrow C \end{matrix}$ Aug
 Reflexivity Transitivity
- (a) $A \rightarrow B \Rightarrow AC \rightarrow B$
 (b) $A \rightarrow C$ and $AB \rightarrow C \Rightarrow B \rightarrow C$
4. Consider a relation R(A, B, C, D) with the following FDs: $B \rightarrow C$, $D \rightarrow B$
- (a) Find the key(s) of R. $\{AD\}^* = \{A, B, C, D\}$
 (b) Is this relation in BCNF? Why or why not? If it is not, decompose R into a collection of relations that are in BCNF.
5. Prove that every two-attribute relation is in BCNF.

Critical Thinking Exercise

6. Consider a relation R(A,B,C,D,E) and FD's $AB \rightarrow C$, $DE \rightarrow C$, and $B \rightarrow D$. Is this relation in BCNF? Why or why not? If it's not, decompose the relation into collections of relations that are in BCNF.
7. Consider a relation R(A,B,C,D,E) and FD's $A \rightarrow B$, $A \rightarrow C$, $BC \rightarrow A$, and $D \rightarrow E$. Is this relation in BCNF or 3NF or neither? If it's not in BCNF, decompose the relation into collections of relations that are in BCNF. Show each step of the decomposition process.

1. A medical clinic database schema contains the following:

APPOINTMENT (patient-id, patient-name, doctor-id, doctor-name, appointment-date, appointment-time, clinic-room-no)

Show, with suitable examples, the insertion anomalies that the schema is liable to encounter.

key = patient-id

Patient-id \rightarrow Appointment (n)

(same patient-id being input with different doctor-id it's anomalies)

Clearly doctor-id \rightarrow doctor-name is an FD and LHS is not superkey

- ① We must ensure that the doctor attributes are consistent with other patients under this doctor; potential update anomalies
- ② In order to insert a new patient, all the attributes of the doctor who is treating the patient must be also included; if no doctor, then use NULL, which is not good.
- ③ If a new doctor joins and has not seen any patients, we cannot enter the doctor's details. We cannot fill patient information with NULLs since this violates the primary key condition.
- ④ If the same patient has more than one appointment, its ID will be repeated, which violates the unique property of a key.

APPOINTMENT (patient-id, patient-name, doctor-id, doctor-name, appointment-date, appointment-time, clinic-room-no)

patient-id	patient-name	doctor-id	doctor-name	apt-date	apt-time	room-no
p001	john	d100	james	20.01.01	0930	r01
p002	steve	d100	james	20.01.02	1030	r09
p003	william	d100	james	20.01.03	0930	r08
p004	charles	d100	james	20.01.04	1030	r07
2 p005	bob	null	null	null	null	null
null	null	3 d102	lee	null	null	null
4 p003	william	d100	james	20.01.10	1030	r10
p003	william	d110	michael	20.01.11	1130	r10

2. Consider the relation ADDRESS having attributes Street, City, State and Zip. Assume that for any given zipcode, there is just one city and state. Also, for any given street, city, and state, there is just one zipcode.

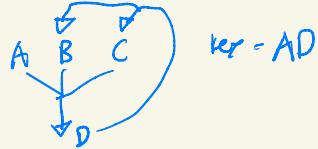
(a) Infer all possible functional dependencies (FDs) for this relation.

(b) Which are possible minimal keys?

a) $ABC \rightarrow D$

$D \rightarrow BC$

A	A
B	B
C	C
D	BCD



① make sure right only 1 attr

$ABC \rightarrow D$

$D \rightarrow B$

$D \rightarrow C$

② make sure there is no redundant

$\checkmark ABC \rightarrow D ?$ $\{AB\}^+ = \{ABC\}$ no D not redundant

$\checkmark D \rightarrow B ?$ $\{D\}^+ = \{D\}$ no B not redundant

$\checkmark D \rightarrow C ?$ $\{D\}^+ = \{D, BC\}$ no C not redundant

③ check if we can remove any left hand side (LHS)

b) ABC, AD

$ABC \rightarrow D ?$

$A \rightarrow D ?$ $A^+ = \{A\}$

$B \rightarrow D ?$ $B^+ = \{B\}$

$C \rightarrow D ?$ $C^+ = \{C\}$

minimal basis:

$ABC \rightarrow D$

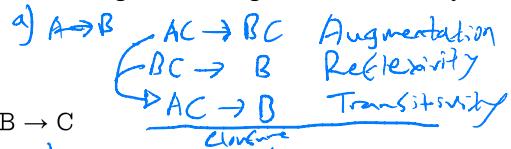
$D \rightarrow B$

$D \rightarrow C$

3. Prove the following properties using Armstrong's axioms or reject it by counterexample relations.

(a) $A \rightarrow B \Rightarrow AC \rightarrow B$

(b) $A \rightarrow C$ and $AB \rightarrow C \Rightarrow B \rightarrow C$



b) $A \rightarrow C$
 $AB \rightarrow C$
 $B \rightarrow C$

then $A^+ = \{A, C\}$
 $B^+ = \{B\}$ C is not in B
 $C^- = \{\}$

given (a_1, b_1, c_1)
 (a_2, b_1, c_2)

4. Consider a relation $R(A, B, C, D)$ with the following FDs: $B \rightarrow C$, $D \rightarrow B$

(a) Find the key(s) of R.

(b) Is this relation in BCNF? Why or why not? If it is not, decompose R

into a collection of relations that are in BCNF.

$$a) \begin{array}{ccc} B & \xrightarrow{\quad} & C \\ \uparrow & & \\ D & & A \end{array} \quad \begin{array}{l} A^+ = \{A\} \\ B^+ = \{B, C\} \\ C^+ = \{C\} \\ D^+ = \{D, B, C\} \\ AD = \{A, D, B, C\} \end{array}$$

b) no, because non-trivial
 $B \rightarrow C$ LHS has no AD attr
 $C \rightarrow B$

$R(A, B, C, D)$
 $B \rightarrow C$ $B^+ = \{B, C\}$
 $R_1 = \{B, C\}$ BCNF ✓

$$\begin{aligned}
 & D^+ - \Sigma B/C \bar{S} \\
 \text{key } D & \quad L_1 = P, Q, C \quad B \rightarrow C \text{ via} \\
 & \quad L_2 = AP \\
 & \quad B^+ = \Sigma B, C \bar{S} \\
 & \quad L_3 = B, S \\
 & \quad L_4 = B, D
 \end{aligned}$$

- Prove that every two-attribute relation is in BCNF.

- Case 1: $A \rightarrow B$ holds, but $B \rightarrow A$ does not. A is the key.
The only nontrivial FD is $A \rightarrow B$; no BCNF violation.
 - Case 2: $B \rightarrow A$ holds, but $A \rightarrow B$ does not. B is the key.
The only nontrivial FD is $B \rightarrow A$; no BCNF violation.
 - Case 3: Both $A \rightarrow B$ and $B \rightarrow A$ hold. A and B are both keys; no BCNF violation.
 - Case 4: AB is key; so we have $AB \rightarrow AB$, which is trivial.

TUT 3

2) $D \rightarrow BC$ b) AD, ABC
 $ABC \rightarrow D$

$D \rightarrow B$

$D \rightarrow C$

3) a) $A \rightarrow B \Rightarrow AC \rightarrow B$ b) $A \rightarrow C$ $B \rightarrow C$
 $AC \rightarrow BC$ $AC \rightarrow B$ given A B C
 $BC \rightarrow B$ 1 1 1
 1 0 1

4) a) AD
b) Not BCNF as FD LHS doesn't contain key
 $R(ABCD)$ $B \rightarrow C$ $D \rightarrow B$
Violate $D \rightarrow B$ $\{D\}^+ = \{D, B, C\}$
 $R_1(B, CD)$ $R_2(A, D) \checkmark$
 $\hookrightarrow B \rightarrow C$ $\{B\}^+ = \{B, C\}$
 $R_3(B, C) \checkmark$ $R_4(B, D) \checkmark$

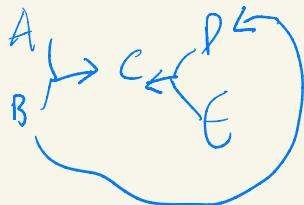
Critical Thinking Exercise

6. Consider a relation $R(A,B,C,D,E)$ and FD's $AB \rightarrow C$, $DE \rightarrow C$, and $B \rightarrow D$. Is this relation in BCNF? Why or why not? If it's not, decompose the relation into collections of relations that are in BCNF.
7. Consider a relation $R(A,B,C,D,E)$ and FD's $A \rightarrow B$, $A \rightarrow C$, $BC \rightarrow A$, and $D \rightarrow E$. Is this relation in BCNF or 3NF or neither? If it's not in BCNF, decompose the relation into collections of relations that are in BCNF. Show each step of the decomposition process.

b) key : ABE

$AB \rightarrow C$ violate

$$\{AB\}^+ = \{ABCDE\}$$



$R_1(A, B, C, D)$ key AB Not BCNF $B \rightarrow D$

$R_2(A, B, E)$ key ABE BCNF ✓

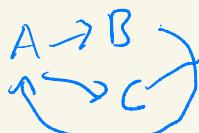
$R_1(A, B, C, D)$

$$B \rightarrow D \quad \{B^+\} = \{B, D\}$$

$R_3(B, D)$ BCNF ✓

$R_4(AB, C)$ key AB BCNF ✓

7) $R(A, B, C, D, E)$



$$D \rightarrow E$$

$$A \rightarrow B \quad \{A, B, C\}$$

$R_1(A, B, C)$ BCNF

$R_2(A, D, E)$

key AD, BCD

CZ2007 Tutorial 3: FDs + BCNF

Week 5



Question 1

- A medical clinic database schema contains the following:
- APPOINTMENT (patient-id, patient-name, doctor-id, doctor-name, appointment-date, appointment-time, clinic-room-no)
- Show, with suitable examples, the anomalies that the schema is liable to encounter.
- Key is patient-id.
- So FD is patient-id → patient-name, doctor-id, doctor-name, appointment-date, appointment-time, clinic-room-no

Question 1

APPOINTMENT (patient-id, patient-name, doctor-id, doctor-name, appointment-date, appointment-time, clinic-room-no)

patient-id	patient-name	doctor-id	doctor-name	appt-date	appt-time	room-no
p001	john	d100	james	20.01.01	0930	r01
p002	steve	d100	james	20.01.02	1030	r09
p003	william	d100	james	20.01.03	0930	r08
p004	charles	d100	james	20.01.04	1030	r07

Question 1

APPOINTMENT (patient-id, patient-name, doctor-id, doctor-name, appointment-date, appointment-time, clinic-room-no)

patient-id	patient-name	doctor-id	doctor-name	appt-date	appt-time	room-no
p001	john	d100	james	20.01.01	0930	r01
p002	steve	d100	james	20.01.02	1030	r09
p003	william	d100	james	20.01.03	0930	r08
p004	charles	d100	james	20.01.04	1030	r07
2 p005	bob	null	null	null	null	null

Question 1

APPOINTMENT (patient-id, patient-name, doctor-id, doctor-name, appointment-date, appointment-time, clinic-room-no)

patient-id	patient-name	doctor-id	doctor-name	appt-date	appt-time	room-no
p001	john	d100	james	20.01.01	0930	r01
p002	steve	d100	james	20.01.02	1030	r09
p003	william	d100	james	20.01.03	0930	r08
p004	charles	d100	james	20.01.04	1030	r07
2 p005	bob	null	null	null	null	null
null	null	3 d102	lee	null	null	null

Question 1

APPOINTMENT (patient-id, patient-name, doctor-id, doctor-name, appointment-date, appointment-time, clinic-room-no)

patient-id	patient-name	doctor-id	doctor-name	appt-date	appt-time	room-no
p001	john	d100	james	20.01.01	0930	r01
p002	steve	d100	james	20.01.02	1030	r09
p003	william	d100	james	20.01.03	0930	r08
p004	charles	d100	james	20.01.04	1030	r07
2 p005	bob	null	null	null	null	null
null	null	3 d102	lee	null	null	null
4						
p003	william	d100	james	20.01.10	1030	r10
p003	william	d110	michael	20.01.11	1130	r10

Question 1

Clearly $\text{doctor-id} \rightarrow \text{doctor-name}$ is an FD and LHS is not superkey

- 1 We must ensure that the **doctor** attributes are consistent with other **patients** under this **doctor**; potential update anomalies
- 2 In order to insert a new patient, all the attributes of the **doctor** who is treating the **patient** must be also included; if no doctor, then use NULL, which is not good.
- 3 If a new **doctor** joins and has not seen any **patients**, we cannot enter the **doctor's** details. We cannot fill **patient** information with NULLs since this violates the primary key condition.
- 4 If the same **patient** has more than one appointment, its ID will be repeated, which violates the unique property of a key.

Question 1

- APPOINTMENT (patient-id, patient-name, doctor-id, doctor-name, appointment-date, appointment-time, clinic-room-no)
- Can we infer all FDs in this relation?
 - patient-id → patient-name
 - doctor-id → doctor-name
 - patient-id, doctor-id → appointment-date, appointment-time, clinic-room-no ?
 - appointment-date, appointment-time, clinic-room-no → patient-id, doctor-id ?

Question 2

- Consider the relation ADDRESS having attributes Street, City, State and Zip.
- Assume that for any given zipcode, there is just one city and state. Also, for any given street, city, and state, there is just one zipcode.
- (a) Infer all possible functional dependencies (FDs) for this relation.
- (b) Which are possible minimal keys?

Question 2

- Let us denote attributes STREET, CITY, STATE, ZIP as A, B, C and D respectively. Then we have $D \rightarrow BC$ and $ABC \rightarrow D$.
- Use closure to find FDs:
 - $A^+ = \{A\}$; $B^+ = \{B\}$; $C^+ = \{C\}$; $D^+ = \{D\}$
 - $AB^+ = \{AB\}$; $AC^+ = \{AC\}$; $AD^+ = \{A\}$ BCD ; $BC^+ = \{BC\}$;
 $BD^+ = \{BD\}$ C; $CD^+ = \{CD\}$ B;
 - $ABC^+ = \{ABC\}$ D; $ABD^+ = \{AB\}$ CD; $ACD^+ = \{A\}$ BCD;
 $BCD^+ = \{BCD\}$

Question 2

- FD's:
 - $D \rightarrow BC$ because $D^+ = \{DBC\}$
 - $AD \rightarrow BC$ because $AD^+ = \{A\underline{BCD}\}$
 - $BD \rightarrow C$ because $BD^+ = \{BDC\}$
 - $CD \rightarrow B$ because $CD^+ = \{CDB\}$
 - $ABC \rightarrow D$ because $ABC^+ = \{ABCD\}$
 - $ABD \rightarrow C$ because $ABD^+ = \{ABCD\}$
 - $ACD \rightarrow B$ because $ACD^+ = \{ABCD\}$
- Minimal keys: ABC, AD

Question 3

- Prove the following properties using Armstrong's axioms or reject it by counterexample relations.
- (a) $A \rightarrow B \Rightarrow AC \rightarrow B$
- (b) $A \rightarrow C$ and $AB \rightarrow C \Rightarrow B \rightarrow C$

Question 3a

- (a) $A \rightarrow B \Rightarrow AC \rightarrow B$
- $A \rightarrow B \Rightarrow AC \rightarrow BC$ (Augmentation Rule)
- $BC \rightarrow B$ (Reflexivity Rule)
- $AC \rightarrow BC$ and $BC \rightarrow B \Rightarrow AC \rightarrow B$
(Transitivity Rule)

Question 3b

- (b) $A \rightarrow C$ and $AB \rightarrow C \Rightarrow B \rightarrow C$
- Consider the records:
- (a1, b1, c1)
- (a2, b1, c2)
- Both $A \rightarrow C$ and $AB \rightarrow C$ are true but $B \rightarrow C$ does not hold

Question 4

4. Consider a relation $R(A, B, C, D)$ with the following FDs: $B \rightarrow C$, $D \rightarrow B$
- Find the key(s) of R .
 - Is this relation in BCNF? Why or why not? If it is not, decompose R into a collection of relations that are in BCNF.

Question 4

- Use closure to find FDs:
 - $A^+ = \{A\}$; $B^+ = \{BC\}$; $C^+ = \{C\}$; $D^+ = \{D\}$
 - $AB^+ = \{ABC\}$; $AC^+ = \{AC\}$; $AD^+ = \{ABCD\}$; $BC^+ = \{BC\}$;
 $BD^+ = \{BCD\}$; $CD^+ = \{BCD\}$;
 - $ABC^+ = \{ABC\}$; $ABD^+ = \{ABCD\}$; $ACD^+ = \{ABCD\}$;
 $BCD^+ = \{BCD\}$
 - Key is AD
- Also we note that A and D do not appear on RHS of FDs; so key must contain AD. In fact, key is AD.

Question 4

- Key is AD.
- Both FDs $B \rightarrow C$, $D \rightarrow B$ violate BCNF. Can decompose using either one first.
- By first decomposing on $B \rightarrow C$, we get $R1(B, C)$ and $R2(A, B, D)$.
- $R2$ is not in BCNF due to violating FD $D \rightarrow B$, so we decompose further: $R3(A,D)$ and $R4(B, D)$.
- Both $R3$ and $R4$ are in BCNF (see Q5)

Question 4

- By first decomposing on $D \rightarrow B$, we get $R1(B, C, D)$ and $R2(A, D)$.
- $R1$ is not in BCNF due to violating FD $B \rightarrow C$, so we must decompose further.
- In both cases, we end up with three relations, $Ra(A, D)$, $Rb(B, C)$ and $Rc(B, D)$.

Question 5

- Prove that every two-attribute relation is in BCNF.
- There are 4 cases in a two-attribute relation.

Question 5

- Case 1: $A \rightarrow B$ holds, but $B \rightarrow A$ does not. A is the key.
The only nontrivial FD is $A \rightarrow B$; no BCNF violation.
- Case 2: $B \rightarrow A$ holds, but $A \rightarrow B$ does not. B is the key.
The only nontrivial FD is $B \rightarrow A$; no BCNF violation.
- Case 3: Both $A \rightarrow B$ and $B \rightarrow A$ hold. A and B are both keys; no BCNF violation.
- Case 4: AB is key; so we have $AB \rightarrow AB$, which trivial.



Do the best
you can until you know better.
Then when you know better, do better.

~ Maya Angelou

ALL THE BEST

Tutorial 4

Normalisation

Classroom Exercise

1. A medical clinic database schema contains the following:

$\begin{matrix} a & b & c & d \\ \text{APPOINTMENT} & (\text{patient-id}, \text{patient-name}, \text{doctor-id}, \text{doctor-name}, \\ & \text{appointment-date}, \text{appointment-time}, \text{clinic-room-no}) \\ e & f & g \end{matrix}$

Identify the functional dependencies in the schema, stating any assumptions made. Using these functional dependencies, normalise the schema to Third Normal Form.

2. Consider the relation Courses(C, T, H, R, S, G) whose attributes may be thought informally as course, teacher, hour, room, student, and grade. Let the set of FD's of Courses be:

$C \rightarrow T$, $HR \rightarrow C$, $HT \rightarrow R$, $HS \rightarrow R$, and $CS \rightarrow G$.

- (a) What are all the keys for Courses?
- (b) Verify that the given FDs are their own minimal basis.
- (c) Use the 3NF decomposition algorithm to find a lossless-join, dependency-preserving decomposition.

3. Consider a relation R(W, X, Y, Z) which satisfies the following set of FDs $G = \{Z \rightarrow W, Y \rightarrow X, Y \rightarrow Z, XW \rightarrow Y\}$, where G is a minimal basis.

- (a) Decompose R into a set of relations in 3NF.
- (b) Is the decomposition also in BCNF? Explain your answer.

4. Consider a relation R(A,B,C,D,E) and FD's $A \rightarrow BC$, $CD \rightarrow E$, $E \rightarrow A$, and $B \rightarrow D$.

- (a) Is the decomposition $R1(A,B,C)$ and $R2(A,D,E)$ of R lossless or lossy? Justify your answer. Is this decomposition dependency preserving? If your answer is NO, then what is not preserved?
- (b) Is the decomposition $R3(A,B,C,D)$ and $R4(C,D,E)$ of R lossless or lossy? Justify your answer. Is this decomposition dependency preserving? If your answer is NO, then what is not preserved?

Critical Thinking Exercise

5. We perform decomposition to normalize an original schema to be of certain normal forms. For such a decomposition to be “equivalent” to the original schema, it is desirable to be lossless. To study this concept, let’s consider an original schema $R(A, B, C)$. Suppose we decompose R into $R_1(A, B)$ and $R_2(A, C)$.
 - (a) Is this decomposition always lossless? Answer *yes* or *no* and briefly explain why.
 - (b) Give an example instance of R (*i.e.*, an example table with several tuples) and demonstrate its decomposition, to support your answer in (a).

1. A medical clinic database schema contains the following:

APPOINTMENT (patient-id, patient-name, doctor-id, doctor-name, appointment-date, appointment-time, clinic-room-no)

a b c d
e f g

Identify the functional dependencies in the schema, stating any assumptions made. Using these functional dependencies, normalise the schema to Third Normal Form.

Q:

Patient-id \rightarrow Patient-name, doctor-id, doctor-name, appointment-date, appointment-time, clinic-room-no

doctor-id \rightarrow doctor-name

key : patient-id a

$a \rightarrow bcdefg$
 $c \rightarrow d$
 $bfg \rightarrow a, c$

minimum basis =
① keep right 1 attr
 $\begin{array}{l} a \rightarrow b \\ a \rightarrow c \\ a \rightarrow d \\ a \rightarrow e \\ a \rightarrow f \\ a \rightarrow g \\ a \rightarrow h \\ a \rightarrow i \\ a \rightarrow j \end{array}$
 $\begin{array}{l} b \rightarrow c \\ c \rightarrow d \\ e \rightarrow g \rightarrow a \\ f \rightarrow g \rightarrow c \\ g \rightarrow a \\ h \rightarrow c \\ i \rightarrow c \\ j \rightarrow c \end{array}$

② remove redundant

$\begin{array}{ll} a \rightarrow b & a^+ = abcdefg \text{ NR} \\ a \rightarrow c & a^+ = abdefg \text{ NR} \\ a \rightarrow d & a^+ = abcdef \text{ R} \\ a \rightarrow e & a^+ = abcdefg \text{ NR} \\ a \rightarrow f & a^+ = abcdefg \text{ NR} \\ a \rightarrow g & a^+ = abcdefg \text{ NR} \\ c \rightarrow d & c = c \text{ NR} \\ e \rightarrow g \rightarrow a & e \rightarrow a \text{ NR} \\ f \rightarrow g \rightarrow c & f \rightarrow c \text{ R} \end{array}$

2. Consider the relation Courses(C, T, H, R, S, G) whose attributes may be thought informally as course, teacher, hour, room, student, and grade. Let the set of FD's of Courses be:

$C \rightarrow T$, $HR \rightarrow C$, $HT \rightarrow R$, $HS \rightarrow R$, and $CS \rightarrow G$.

(a) What are all the keys for Courses? SH

(b) Verify that the given FDs are their own minimal basis.

(c) Use the 3NF decomposition algorithm to find a lossless-join, dependency-preserving decomposition.



$\{SH\}^+ = \{S, H, R, C, L, G\}$

b) ① make right only 1 attr ② remove redundant FDs

$C \rightarrow T$
 $HR \rightarrow C$
 $HT \rightarrow R$
 $HS \rightarrow R$
 $CS \rightarrow G$

$C \rightarrow T$ NR
 $HR \rightarrow C$ NR
 $HT \rightarrow R$ NR
 $HS \rightarrow R$ NR
 $CS \rightarrow G$ NR
③ LHS attr redundancy

③ see if left can be 1
 $a \rightarrow b$ LHS X
 $a \rightarrow c$ C. e
 $a \rightarrow e$
 $a \rightarrow f$ e F-
 $a \rightarrow g$ f+R X
 $b \rightarrow g$ f+R
+ minimal basis

- Suppose other than $A \rightarrow BCDFG$, we derive other FDs using common sense:
a: doctor-id \rightarrow doctor-name, i.e., C-D
a: appointment-date, appointment-time, clinic-room-no \rightarrow patient-id, doctor-id, i.e., EFG \rightarrow AC
- So altogether we have $A \rightarrow BCDFG$, C-D, EFG \rightarrow AC
- Let's check MB conditions: Condition 1 says RHS must be single attribute, so we have $A \rightarrow B$, $A \rightarrow C$, $A \rightarrow D$, $A \rightarrow R$, $A \rightarrow G$, $C \rightarrow D$, EFG \rightarrow A
- Condition 2 says no redundant FDs. EFG \rightarrow C and A \rightarrow D are redundant and removed. Condition 3 says no redundant LHS attributes. None of LHS attribute of EFG \rightarrow A is redundant.
- So MB = $\{A \rightarrow B$, $A \rightarrow C$, $A \rightarrow D$, $A \rightarrow R$, $A \rightarrow G$, $C \rightarrow D$, EFG \rightarrow A $\}$ and we form relations AB, AC, AB, AP, AG, CD, ABFG.
- Do these relations make sense? Any other way to do this?

→ ① step1: RHS contains 1 attr
 $C \rightarrow D$ $EFG \rightarrow AC$
 $EFG \rightarrow AC$ step2: remove redundant FDs
 $\begin{array}{l} a \rightarrow b \\ a \rightarrow c \\ a \rightarrow d \\ a \rightarrow R \\ a \rightarrow G \\ a \rightarrow H \\ a \rightarrow I \\ a \rightarrow J \end{array}$
not redundant
 $\begin{array}{l} c \rightarrow D \\ e \rightarrow G \\ f \rightarrow G \\ f \rightarrow C \\ f \rightarrow R \\ g \rightarrow C \\ g \rightarrow R \\ g \rightarrow H \\ g \rightarrow I \\ g \rightarrow J \end{array}$
not redundant
 $\begin{array}{l} e \rightarrow G \\ f \rightarrow G \\ f \rightarrow C \\ f \rightarrow R \\ g \rightarrow C \\ g \rightarrow R \\ g \rightarrow H \\ g \rightarrow I \\ g \rightarrow J \end{array}$
not redundant
step3: remove any LHS attr that is not redundant
 $\begin{array}{l} a \rightarrow b \\ a \rightarrow c \\ a \rightarrow d \\ a \rightarrow R \\ a \rightarrow G \\ a \rightarrow H \\ a \rightarrow I \\ a \rightarrow J \end{array}$
not redundant
② step1: add $C \rightarrow D$ choice
 $\begin{array}{l} a \rightarrow b \\ a \rightarrow c \\ a \rightarrow d \\ a \rightarrow R \\ a \rightarrow G \\ a \rightarrow H \\ a \rightarrow I \\ a \rightarrow J \end{array}$
 $\begin{array}{l} C \rightarrow D \\ EFG \rightarrow AC \end{array}$
 $\begin{array}{l} a \rightarrow b \\ a \rightarrow c \\ a \rightarrow d \\ a \rightarrow R \\ a \rightarrow G \\ a \rightarrow H \\ a \rightarrow I \\ a \rightarrow J \end{array}$
 $\begin{array}{l} C \rightarrow D \\ EFG \rightarrow AC \end{array}$
 $\begin{array}{l} a \rightarrow b \\ a \rightarrow c \\ a \rightarrow d \\ a \rightarrow R \\ a \rightarrow G \\ a \rightarrow H \\ a \rightarrow I \\ a \rightarrow J \end{array}$
 $\begin{array}{l} C \rightarrow D \\ EFG \rightarrow AC \end{array}$
 $\begin{array}{l} a \rightarrow b \\ a \rightarrow c \\ a \rightarrow d \\ a \rightarrow R \\ a \rightarrow G \\ a \rightarrow H \\ a \rightarrow I \\ a \rightarrow J \end{array}$
 $\begin{array}{l} C \rightarrow D \\ EFG \rightarrow AC \end{array}$

- Suppose we have the following FDs using common sense:
a: patient-id \rightarrow patient-name, i.e., A-B
a: doctor-id \rightarrow doctor-name, i.e., C-D
a: appointment-date, appointment-time, clinic-room-no \rightarrow patient-id, doctor-id, i.e., EFG \rightarrow AC
- So altogether we have $A \rightarrow B$, $C \rightarrow D$, EFG \rightarrow AC
- Let's check MB conditions: Condition 1 says RHS must be single attribute, so we have $A \rightarrow B$, $C \rightarrow D$, EFG \rightarrow A
- Condition 2 says no redundant FDs. There are none. Condition 3 says no redundant LHS attributes. There are none.
- So MB = $\{A \rightarrow B$, $C \rightarrow D$, EFG \rightarrow A $\}$ and we form relations AB, CD, ABFG.
- Do these relations make sense? Yes. This last approach seems the best.

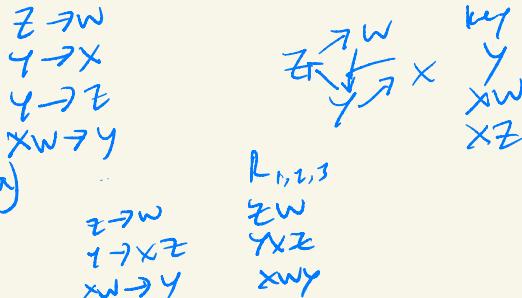
c) CT
CHTR
TCHR
SHR
CSG

CHRTS

3. Consider a relation R(W, X, Y, Z) which satisfies the following set of FDs G = {Z → W, Y → X, Y → Z, XW → Y}, where G is a minimal basis.

(a) Decompose R into a set of relations in 3NF.

(b) Is the decomposition also in BCNF? Explain your answer.



b) Non-trivial FD must contain key

key = Y

$Z \rightarrow W$

$Y \rightarrow X$

$Y \rightarrow Z$

4. Consider a relation R(A,B,C,D,E) and FD's A → BC, CD → E, E → A, and B → D.

(a) Is the decomposition R1(A,B,C) and R2(A,D,E) of R lossless or lossy? Justify your answer. Is this decomposition dependency preserving? If your answer is NO, then what is not preserved?

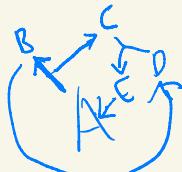
(b) Is the decomposition R3(A,B,C,D) and R4(C,D,E) of R lossless or lossy? Justify your answer. Is this decomposition dependency preserving? If your answer is NO, then what is not preserved?

$$A \rightarrow BC$$

$$CD \rightarrow E$$

$$E \rightarrow A$$

$$B \rightarrow D$$



key: A

dependency
preserving

$$\begin{array}{l} CD \rightarrow E \\ B \rightarrow D \end{array}$$

$$\begin{array}{l} R_1(A, B, C) \\ A \rightarrow BC \\ BC \rightarrow A \end{array}$$

$$\begin{array}{l} R_2(ADE) \\ E \rightarrow A \\ A \rightarrow E \end{array}$$

$$b) R_3(A, B, C, D)$$

$$R_4(CD, E)$$

CD

$$R_3(A, B, C, D)$$

$$\begin{array}{l} A \rightarrow BC \\ BC \rightarrow A \\ B \rightarrow D \\ D \rightarrow E \end{array}$$

$$R_4(CD, E)$$

$$CD \rightarrow E, E \rightarrow D$$

C → A true

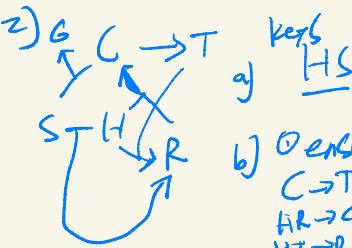
5. We perform decomposition to normalize an original schema to be of certain normal forms. For such a decomposition to be “equivalent” to the original schema, it is desirable to be lossless. To study this concept, let’s consider an original schema $R(A, B, C)$. Suppose we decompose R into $R_1(A, B)$ and $R_2(A, C)$.

- (a) Is this decomposition always lossless? Answer *yes* or *no* and briefly explain why.
- (b) Give an example instance of R (*i.e.*, an example table with several tuples) and demonstrate its decomposition, to support your answer in (a).

a)

TUT 4

- 1) $\begin{array}{l} a \rightarrow b \\ c \rightarrow d \\ e,f,g \rightarrow a,c \end{array}$ a) derive minimal basis
 ① ensure R.H.S has only 1 attr
 $\begin{array}{l} a \rightarrow b \\ c \rightarrow d \\ e,f,g \rightarrow a \\ e,f,g \rightarrow c \end{array}$
 - check if L.H.S
 no
- Check redundancy
 $\begin{array}{l} a \rightarrow b \text{ redundant} \\ e,f,g \rightarrow a \text{ not} \\ e,f,g \rightarrow c \text{ not} \\ e,f,g \rightarrow a,c \text{ not} \\ e,f,g \rightarrow a,c \text{ not} \end{array}$



- b) ensure R.H.S of FD has only 1 attr

$$\begin{array}{l} C \rightarrow T \\ HR \rightarrow C \\ HT \rightarrow R \\ HS \rightarrow R \\ CS \rightarrow G \end{array}$$

- ② Check redundancy of all FDs

$$\begin{array}{ll} C \rightarrow T & \{C\}^+ = \{C\} \\ HR \rightarrow C & \{HR\}^+ = \{HR\} \\ HT \rightarrow R & \{HT\}^+ = \{H, T\} \\ HS \rightarrow R & \{HS\}^+ = \{H, S\} \\ CS \rightarrow G & \{CS\}^+ = \{C, S\} \end{array}$$

-1 minimal basis

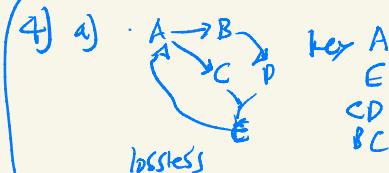
-2 combine FD that has the same L.H.S \cup

-3 CT, HRC HTR HSR CSG

- 3) ensure L.H.S multi attr is not redundant

$$\begin{array}{lll} HR \rightarrow C & H \rightarrow C \times & R \rightarrow C \times \\ HT \rightarrow R & H \rightarrow R \times & T \rightarrow R \times \\ HS \rightarrow R & H \rightarrow R \times & S \rightarrow R \times \\ CS \rightarrow G & C \rightarrow G \times & S \rightarrow G \times \end{array}$$

$$\begin{array}{l} C \rightarrow T \\ HR \rightarrow C \\ HT \rightarrow R \\ HS \rightarrow R \\ CS \rightarrow G \end{array}$$



lossless

R(A,B,C)	A \rightarrow BC ✓
R(A,D,E)	A \rightarrow E \leftarrow D ✓
CD \rightarrow E	CD \rightarrow E ✓
B \rightarrow D	B \rightarrow D ✓

b) lossless

R(A,B,C,D)	A \rightarrow BC ✓	B \rightarrow D ✓
R(C,D,E)	CD \rightarrow E ✓	
E \rightarrow A	E ✓	

- 3) minimal basis?

- 2) combine FD with same L.H.S

$$\begin{array}{ll} Z \rightarrow W & XZ \\ Y \rightarrow XZ & Y \\ XW \rightarrow Y & XW \end{array}$$

- 3) table

$$\begin{array}{ccc} ZW & XYZ & WXY \\ \downarrow & \downarrow & \downarrow \\ BCNF & BCNF & BCNF \end{array}$$

CZ2007 Tutorial 4: BCNF + 3NF

Week 6



Question 1

- A medical clinic database schema contains the following:
- APPOINTMENT (patient-id, patient-name, doctor-id, doctor-name, appointment-date, appointment-time, clinic-room-no)
- Identify the functional dependencies in the schema, stating any assumptions made.
 - There could be different sets of FDs depending on how you interpret them.
- Using these functional dependencies, normalise the schema to Third Normal Form.
 - We may get different sets of normalized relations.

Question 1

- Let's map the attribute names to simpler letters:
 - **patient-id** to A
 - **patient-name** to B
 - **doctor-id** to C
 - **doctor-name** to D
 - **appointment-date** to E
 - **appointment-time** to F
 - **clinic-room-no** to G
- Since A is a key, we have default functional dependency:
 $A \rightarrow BCDEFG$, assuming no other FDs.
- Does this FD form a minimal basis (MB)?

Question 1

- Since A is a key, we have default functional dependency: $A \rightarrow BCDEFG$, assuming no other FDs.
- Does this FD form a minimal basis (MB)?
- Condition 1 of MB: RHS is single attribute. So we break the FD into:
 $A \rightarrow B$, $A \rightarrow C$, $A \rightarrow D$, $A \rightarrow E$, $A \rightarrow F$, $A \rightarrow G$
- Conditions 2 and 3 are satisfied since there are no other FDs to reason.
- So $MB = \{A \rightarrow B, A \rightarrow C, A \rightarrow D, A \rightarrow E, A \rightarrow F, A \rightarrow G\}$ and we can form relations AB, AC, AD, AE, AF, AG from it.
- Do these relations make sense? Any other way to do this?

Question 1

- Suppose other than $A \rightarrow BCDEFG$, we derive other FDs using common sense:
 - $\text{doctor-id} \rightarrow \text{doctor-name}$; i.e., $C \rightarrow D$
 - $\text{appointment-date}, \text{appointment-time}, \text{clinic-room-no} \rightarrow \text{patient-id}, \text{doctor-id}$; i.e., $EFG \rightarrow AC$
- So altogether we have: $A \rightarrow BCDEFG$, $C \rightarrow D$, $EFG \rightarrow AC$
- Let's check MB conditions: Condition 1 says RHS must be single attribute, so we have: $A \rightarrow B$, $A \rightarrow C$, $A \rightarrow D$, $A \rightarrow E$, $A \rightarrow F$, $A \rightarrow G$, $C \rightarrow D$, $EFG \rightarrow A$, $EFG \rightarrow C$
- Condition 2 says no redundant FDs. $EFG \rightarrow C$ and $A \rightarrow D$ are redundant and removed. Condition 3 says no redundant LHS attributes. None of LHS attribute of $EFG \rightarrow A$ is redundant.
- So $MB = \{A \rightarrow B, A \rightarrow C, A \rightarrow E, A \rightarrow F, A \rightarrow G, C \rightarrow D, EFG \rightarrow A\}$ and we form relations $AB, AC, AE, AF, AG, CD, AEEFG$.
- Do these relations make sense? Any other way to do this?

Question 1

- Suppose we have the following FDs using common sense:
 - $\text{patient-id} \rightarrow \text{patient-name}$; i.e., $A \rightarrow B$
 - $\text{doctor-id} \rightarrow \text{doctor-name}$; i.e., $C \rightarrow D$
 - $\text{appointment-date}, \text{appointment-time}, \text{clinic-room-no} \rightarrow \text{patient-id}, \text{doctor-id}$; i.e., $EFG \rightarrow AC$
- So altogether we have: $A \rightarrow B$, $C \rightarrow D$, $EFG \rightarrow AC$
- Let's check MB conditions: Condition 1 says RHS must be single attribute, so we have: $A \rightarrow B$, $C \rightarrow D$, $EFG \rightarrow A$, $EFG \rightarrow C$
- Condition 2 says no redundant FDs. There are none. Condition 3 says no redundant LHS attributes. There are none.
- So $MB = \{A \rightarrow B, C \rightarrow D, EFG \rightarrow A, EFG \rightarrow C\}$ and we form relations AB , CD , $ACEFG$.
- Do these relations make sense? Yes. This last approach seems the best.

Question 1

- Using common sense, we derive functional dependencies:
 - FD1: $\text{patient-id} \rightarrow \text{patient-name}$
 - FD2: $\text{doctor-id} \rightarrow \text{doctor-name}$
 - FD3: $\text{appointment-date}, \text{appointment-time}, \text{clinic-room-no} \rightarrow \text{patient-id}, \text{doctor-id}$
- Using 3NF normalization, we have decomposed relations:
 - PATIENT(patient-id, patient-name)
 - DOCTOR(doctor-id, doctor-name)
 - APPOINTMENT(appointment-date, appointment-time, clinic-room-no ,
patient-id, doctor-id)

Question 2

Consider the relation Courses(C, T, H, R, S, G) whose attributes may be thought informally as course, teacher, hour, room, student, and grade. Let the set of FD's of Courses be:

$C \rightarrow T$, $HR \rightarrow C$, $HT \rightarrow R$, $HS \rightarrow R$, and $CS \rightarrow G$.

- (a) What are all the keys for Courses?
- (b) Verify that the given FDs are their own minimal basis.
- (c) Use the 3NF decomposition algorithm to find a lossless-join, dependency-preserving decomposition.

Question 2(a)

- The usual procedure to find keys is to take the closure of all 63 nonempty subsets.
- However, we notice that none of the right sides of the FDs contains attributes H and S; we may conclude that **H** and **S** must be part of any key.
- Given FDs $C \rightarrow T$, $HR \rightarrow C$, $HT \rightarrow R$, $HS \rightarrow R$, $CS \rightarrow G$, let's start with HS.
 - $HS \rightarrow R \Rightarrow HS \rightarrow HR$ and $HR \rightarrow C \Rightarrow HS \rightarrow C$; $HS^+ = \{CHRS\}$
 - $CS \rightarrow G$ and $C \rightarrow T \Rightarrow HS^+ = \{CGHRST\}$
- Using the closure method, we eventually find out that **HS** is the only key in the Courses relation.

Question 2(b)

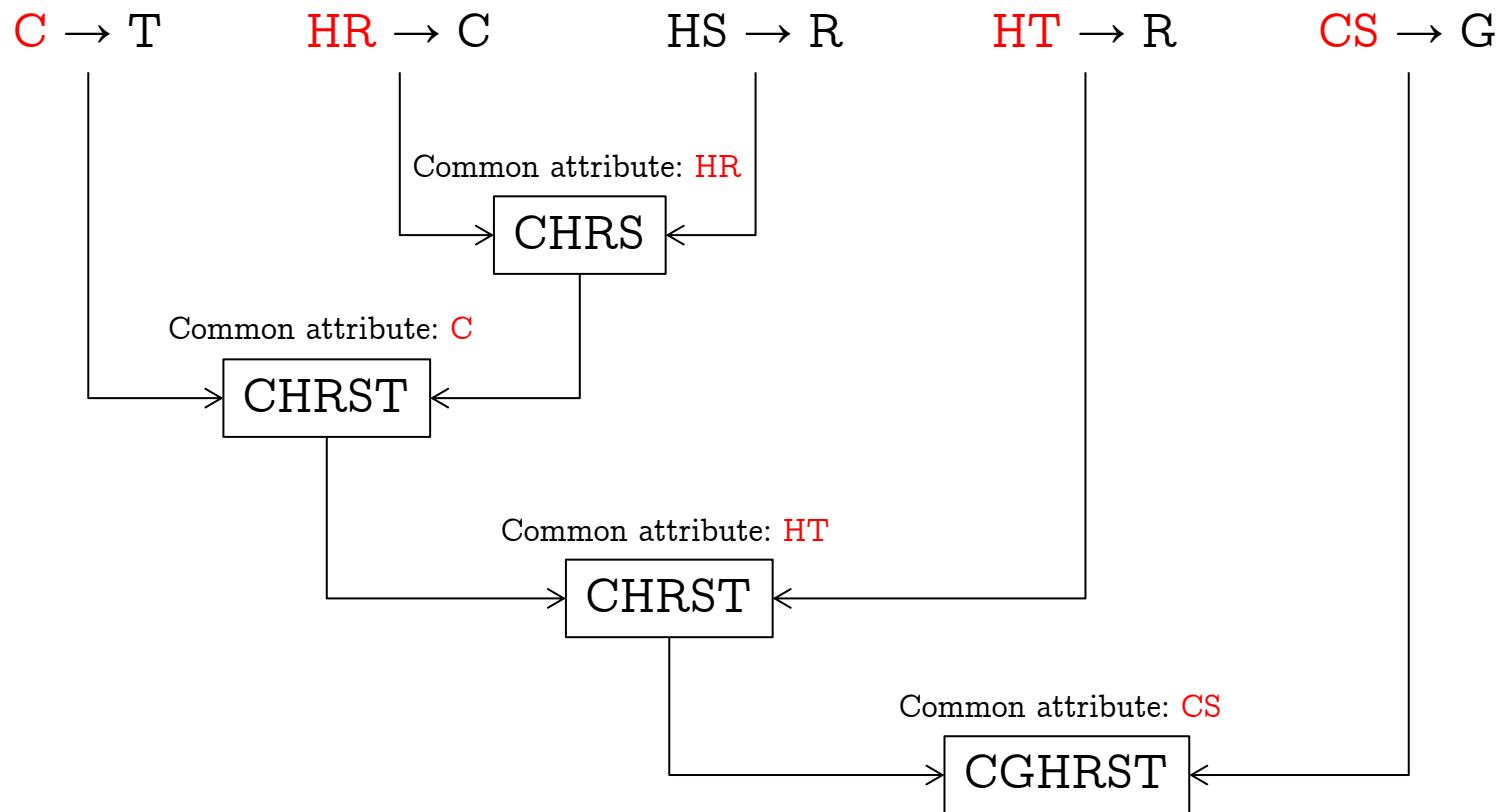
- Given FDs: $C \rightarrow T$, $HR \rightarrow C$, $HT \rightarrow R$, $HS \rightarrow R$, $CS \rightarrow G$
- Check if any of the FDs is redundant.
 - None. If we remove any one of the five FDs, the remaining four FDs do not imply the removed FD.
- Check if any of the LHS attribute of an FD can be removed without losing the dependencies.
 - None. The attributes on the left side of the four FDs are not redundant.
- Thus, the given set of FDs is a minimal basis.

Question 2(c)

- Since the only key is HS, the given set of FDs has some dependencies that violate 3NF.
 - Violating FDs: $C \rightarrow T$, $HR \rightarrow C$, $HT \rightarrow R$, $CS \rightarrow G$
- We also know that the given set of FDs is a minimal basis. Thus, the decomposed relations are (CT), (HRC), (HTR), (HSR) and (CSG).
- Since the relation HSR contains a key, we do not need to add an additional relation. The final set of decomposed relations is (CT), (HRC), (HTR), (HSR) and (CSG).
- Since each decomposed relation came from a FD, the decomposition is FD preserving.

Question 2(c)

The following sequence of joins shows that the decomposition is lossless:



Question 3

Consider a relation $R(W, X, Y, Z)$ which satisfies the following set of FDs $G = \{Z \rightarrow W, Y \rightarrow X, Y \rightarrow Z, XW \rightarrow Y\}$, where G is a minimal basis.

- (a) Decompose R into a set of relations in 3NF.
- (b) Is the decomposition also in BCNF? Explain your answer.

Question 3(a)

- Given $G = \{Z \rightarrow W, Y \rightarrow X, Y \rightarrow Z, XW \rightarrow Y\}$, where G is a minimal basis
 - Decomposed relations: $R1(Z, W)$, $R2(X, Y, Z)$, $R3(X, Y, W)$
- To determine whether BCNF satisfied, find keys using reasoning:
 - $Y \rightarrow X$, $Y \rightarrow Z$, $Z \rightarrow W$ yield $Y \rightarrow WXYZ$; so **Y is a key**
 - $XW \rightarrow Y$ and Y is a key means **XW is a key**.
 - XW is a key and $Z \rightarrow W$ yields $XZ \rightarrow XW$; so **XZ is a key**.
 - Keys: **Y, WX, XZ**

Question 3(b)

- Keys: Y, WX, XZ; check FDs in R1(Z,W), R2(X,Y,Z), R3(X,Y,W):
 - FDs in R1: 2-attribute relation is in BCNF
 - FDs in R2: $Y \rightarrow X$, $Y \rightarrow Z$; LHS are keys
 - FDs in R3: $Y \rightarrow X$, $XW \rightarrow Y$; LHS are keys
- Since all LHS of FDs are keys; relations are in BCNF

Question 4

Consider a relation $R(A,B,C,D,E)$ and FD's $A \rightarrow BC$, $CD \rightarrow E$, $E \rightarrow A$, and $B \rightarrow D$.

- (a) Is the decomposition $R_1(A,B,C)$ and $R_2(A,D,E)$ of R lossless or lossy? Justify your answer. Is this decomposition dependency preserving? If your answer is NO, then what is not preserved?
- (b) Is the decomposition $R_3(A,B,C,D)$ and $R_4(C,D,E)$ of R lossless or lossy? Justify your answer. Is this decomposition dependency preserving? If your answer is NO, then what is not preserved?

Question 4

- FDs: $A \rightarrow BC$, $E \rightarrow A$, $CD \rightarrow E$, $B \rightarrow D$
- (a) Decomposition: $R1(A,B,C)$ and $R2(A,D,E)$
- (b) Decomposition: $R3(A,B,C,D)$ and $R4(C,D,E)$
- Is decomposition lossless (can be joined back)?
- Is decomposition dependency preserving (no FDs lost)?
- Keys: A , E , CD , BC

Question 4(a)

- Decomposition: $R_1(A,B,C)$ and $R_2(A,D,E)$; FDs: $A \rightarrow BC$, $E \rightarrow A$, $CD \rightarrow E$, $B \rightarrow D$; Keys: A , E , CD , BC
- Decomposition $R_1(A,B,C)$ and $R_2(A,D,E)$ is lossless because
 - R_1 and R_2 have a common attribute A , and
 - A is a superkey for $R_1(A,B,C)$
- FDs that hold on $R_1(A,B,C)$
 - $A \rightarrow BC$, $BC \rightarrow A$ since R_1 contains A , B , and C
- FDs that hold on $R_2(A,D,E)$
 - $E \rightarrow A$, $A \rightarrow E$ since R_2 contains A and E
- Two other FDs need to be checked: $CD \rightarrow E$, $B \rightarrow D$
 - From $A \rightarrow BC$, $BC \rightarrow A$, $E \rightarrow A$, $A \rightarrow E$, we have:
 - $\{B\}^+ = \{B\}$, so $B \rightarrow D$ is not preserved
 - $\{CD\}^+ = \{CD\}$, so $CD \rightarrow E$ is not preserved
- Decomposition is NOT dependency-preserving

Question 4(b)

- Decomposition: R3(A,B,C,D) and R4(C,D,E); FDs: $A \rightarrow BC$, $E \rightarrow A$, $CD \rightarrow E$, $B \rightarrow D$; Keys: A , E , CD , BC
- Decomposition R3(A,B,C,D) and R4(C,D,E) is lossless because
 - R3 and R4 have common attributes CD, and
 - CD is a superkey for R4(C,D,E)
- FDs that hold on R3(A,B,C,D)
 - $A \rightarrow BC$, $BC \rightarrow A$, ~~$CD \rightarrow E$~~ , $CD \rightarrow A$, and $B \rightarrow D$ since R1 contains A, B, C, and D
- FDs that hold on R4(C,D,E)
 - $CD \rightarrow E$, $E \rightarrow CD$
- One other FD needs to be checked: $E \rightarrow A$
 - From $A \rightarrow BC$, $BC \rightarrow A$, $CD \rightarrow A$, $B \rightarrow D$, $CD \rightarrow E$, $E \rightarrow CD$ and, we have:
 - $\{E\}^+ = \{A, B, C, D, E\}$, $E \rightarrow CD$ holds in R4, $CD \rightarrow A$ holds in R3, $E \rightarrow A$ is preserved
- Decomposition is dependency-preserving



Do the best
you can until you know better.
Then when you know better, do better.

~ Maya Angelou

ALL THE BEST

Tutorial 5

Relational Algebra

Classroom Exercise

Consider a database with three tables as follows:

Shopper(**shopperName**, street, ageGroup)
 Mall(**mallName**, street)
 ShopAt(**shopperName**, **mallName**, **date**, **time**, dayOfWeek)

The three tables record information about shoppers, shopping malls, as well as “which shoppers shop at which malls”. Primary Keys are in **bold**.

Write the following queries in relational algebra. When answering relational algebra queries, breakdown your answers into intermediate steps. When answering relational algebra queries, each answer should be in the form of one single table containing only relevant output attributes. If you think a question’s solution cannot be expressed in relational algebra, explain why.

1. Find those shopper(s) who shopped at all the malls on “Nanyang Ave” every Thursday between 10am to 5pm, and find the streets that these shoppers live in.
2. Find the age groups of those shoppers(s) who only shop at malls that are located on the street where he/she lives.
3. Consider Jurong Point Mall, the shopping mall that is 3.5km south of NTU. Find those shoppers who have shopped there more times than anyone else does. Also find out these shoppers’ age groups.
4. Consider Jurong Point Mall, the shopping mall that is 3.5km south of NTU. Find those shoppers in the 20s-30s age group who have never shopped at Jurong Point Mall on Friday evenings between 7pm to 10pm. Also find out which streets these shoppers live in.
5. Find shopping malls that have never been visited by shoppers in the 40s-50s age group on Wednesday mornings between 9am to 11am. Also find out which streets these malls are located.
6. For each shopper, find how many other shoppers shopped at the same malls as him/her on the same date.
7. Find the mall(s) that is/are shopped by the largest number of repeat shoppers in the 20s-30s age group. Repeat shoppers of a mall are shoppers who have shopped at least once in the mall.

Additional Exercises (Optional)

1. A library database schema contains the following tables:

LIB-MEMBER(ID, name, age)
BOOK(serial#, title, author, year-of-publication)
LOAN(ID, serial#, date-due)

State what each of the following relational algebra queries is looking for:

- (a) $\pi_{\text{name}}((\sigma_{\text{year-of-publication} < 1960} \text{ BOOK} \bowtie \text{LOAN}) \bowtie \text{LIB-MEMBER})$
- (b) $\pi_{\text{ID}}(\sigma_{\text{age} < 21} \text{ LIB-MEMBER}) - \pi_{\text{ID}}(\sigma_{\text{author} = \text{"J.K.Rowling"}} \text{ BOOK} \bowtie \text{LOAN})$
- (c) $\pi_{\text{name}}((\pi_{\text{ID}, \text{serial}\#} \text{ LOAN} \div \pi_{\text{serial}\#}(\sigma_{\text{title} \text{ like} \text{'C Programming'}} \text{ BOOK})) \bowtie \text{LIB-MEMBER})$

2. The schema of a database containing university-type data is given below. Primary key is underlined for each relation.

STUDENT(Sid, Sname, Sex, Age, Year, GPA)
DEPT(Dname, NumPhds)
PROF(Pname, Dname)
MAJOR(Dname, Sid)
COURSE(Dname, C#, Cname)
SECTION(Dname, C#, Sect#, Pname)
ENROLL(Sid, Dname, C#, Sect#, Grade)

Write the following queries in relational algebra.

- (a) Find the names of professors who work in departments that have fewer than 50 PhD students.
 - (b) Find the name(s) of student(s) with the lowest GPA.
 - (c) Find the names and majors of students who have taken the 'Database System' course.
 - (d) Find the ids, names, and GPAs of the students who have taken all courses from the 'Civil Engineering' department.
3. Consider the following relational schema (primary keys are underlined). eventtype can take values: SWI (swimming), ATH (athletics), GYM (gymnastics), etc. medal can take values: gold, silver, bronze. You may assume player names are unique.

PLAYERS(player-id, name, countryname, age)
EVENTS(event-id, name, eventtype)
RESULTS(player-id, event-id, medal)

Write relational algebra expression for the following queries.

- (a) Find the names of the players who won at least one gold and one silver.

(b) Find the players who did not win a medal.

NTU S

Shopper(shopperName, street, ageGroup)

Mall(mallName, street)

ShopAt(shopperName, mallName, date, time, dayOfWeek)

1. Find those shopper(s) who shopped at all the malls on "Nanyang Ave" every Thursday between 10am to 5pm, and find the streets that these shoppers live in.
2. Find the age groups of those shoppers(s) who only shop at malls that are located on the street where he/she lives.
3. Consider Jurong Point Mall, the shopping mall that is 3.5km south of NTU. Find those shoppers who have shopped there more times than anyone else does. Also find out these shoppers' age groups.
4. Consider Jurong Point Mall, the shopping mall that is 3.5km south of NTU. Find those shoppers in the 20s-30s age group who have never shopped at Jurong Point Mall on Friday evenings between 7pm to 10pm. Also find out which streets these shoppers live in.
5. Find shopping malls that have never been visited by shoppers in the 40s-50s age group on Wednesday mornings between 9am to 11am. Also find out which streets these malls are located.
6. For each shopper, find how many other shoppers shopped at the same malls as him/her on the same date.
7. Find the mall(s) that is/are shopped by the largest number of repeat shoppers in the 20s-30s age group. Repeat shoppers of a mall are shoppers who have shopped at least once in the mall.

- 1) $\Pi \text{ Shopper} \left(\left(\sigma_{\text{street} = \text{'Nanyang Ave'}} \right) \bowtie \left(\sigma_{\text{time} \geq 10 \text{ AND } \text{time} \leq 5} \right) \right)$ *ShopAt*
- 2) $\Pi \text{AgeGroup} \left(\text{Shopper} \bowtie (\text{shopper}. \text{street} = \text{Mall}. \text{street} \text{ Mall}) \right)$
- 3) $\Pi \text{ Shopper, ageGroup} \left(\text{Shopper} \bowtie \left(\sigma_{\text{mallname} = \text{'Jurong point mall'}} \right) \right)$ *Shoppername, Count(date)*
- 4) $\sigma_{\text{mallname} = \text{'Jurong point mall'}}$
- 5) $\Pi \text{mallname}$

Shopper(shopperName, street, ageGroup)

Mall(mallName, street)

ShopAt(shopperName, mallName, date, time, dayOfWeek)

1. Find those shopper(s) who shopped at all the malls on "Nanyang Ave" every Thursday between 10am to 5pm, and find the streets that these shoppers live in.

2. Find the age groups of those shoppers(s) who only shop at malls that are located on the street where he/she lives.

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5. Find shopping malls that have never been visited by shoppers in the 40s-50s age group on Wednesday mornings between 9am to 11am. Also find out which streets these malls are located.

6. For each shopper, find how many other shoppers shopped at the same malls as him/her on the same date.

7. Find the mall(s) that is/are shopped by the largest number of repeat shoppers in the 20s-30s age group. Repeat shoppers of a mall are shoppers who have shopped at least once in the mall.

1) $R_1 := \sigma_{street = 'Nanyang Ave'} \text{Mall}$

$R_2 := R_1 \bowtie R_1.\text{mallName} = \text{ShopAt}.\text{mallName}$

$R_3 := \sigma_{dayOfWeek = 'Thursday'} \text{AND } (\text{time} > 18:00)$

$R_4 := \pi_{ShopperName, street} (\text{Shopper})$

2) $R_0 := \rho_{\text{mall1}}(\text{mallName}, \text{mallStreet}) \text{Mall}$

$R_1 := \text{ShopAt} \bowtie R_0$

$R_2 := \text{Shopper} \bowtie R_1$

$R_3 := \sigma_{R2.\text{street} = R2.\text{mallStreet}}$

R_4

3) $R_1 :=$

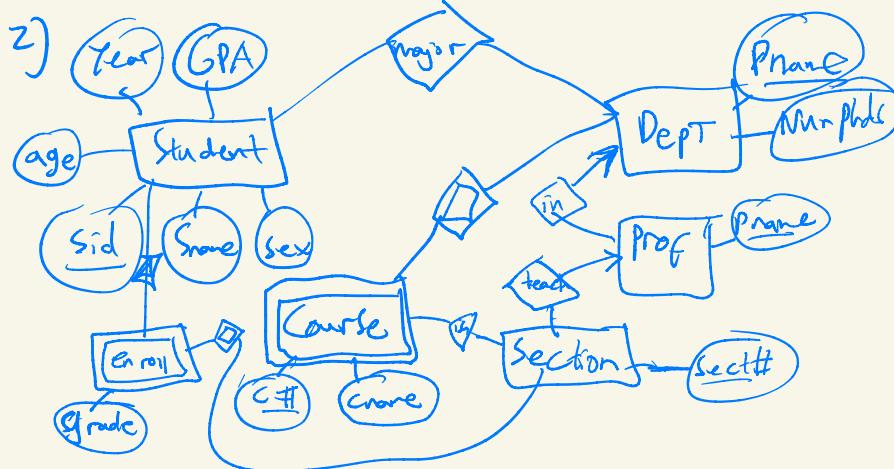
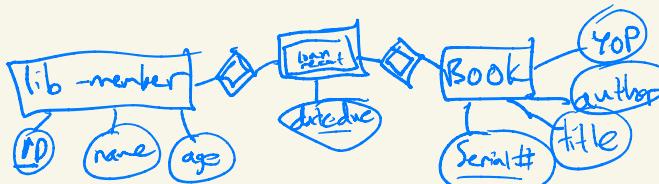
- 1)**
- $$R_1 := \sigma_{mallName='Jingang Ave' \wedge time >= 10am \wedge time <= 12pm} R_1$$
- $$R_2 := P_{R_1(mallName, street, mall)} R_1$$
- $$R_3 := ShopAt \bowtie R_2$$
- $$R_4 := \sigma_{dayOfWeek='Monday' \text{ AND } (ageGroup = '20-30' \text{ AND } ageGroup = '30-40')} R_3$$
- $$R_5 := R_4 \Delta R_1$$
- $$R_6 := \Pi_{shopperName, street} (R_5)$$
-
- 2)**
- $$R_1 := P_{R_1(mallName, street, mall)} Mall$$
- $$R_2 := ShopAt \bowtie R_1$$
- $$R_3 := Shopper \bowtie \{shopper.street = R_2.street \text{ and } Shopper.ShopperName} = R_2.ShopperName\} R_2$$
- $$R_4 := \Pi_{shopper, ageGroup} (R_3)$$
- 3)**
- $$R_1 := \sigma_{mallName = 'Jingang Point Mall'} Shopper$$
- $$R_2 := \gamma_{shopperName, count(date)} \rightarrow Date R_1$$
- $$R_3 := R_2 \bowtie Shopper$$
- $$R_4 := \Pi_{shopperName, ageGroup, cDate} R_3$$
- $$R_5 := \gamma_{Max(cDate) \rightarrow CMax} R_4$$
- $$R_6 := R_4 \Delta_{cDate = CMax} R_5$$
- 4)**
- $$R_1 := (\sigma_{ageGroup >= 20 \text{ AND } ageGroup} <= 30) Shopper \bowtie ShopAt$$
- $$R_2 := \sigma_{mallName = 'Jingang Point Mall' \text{ AND } dayOfWeek = 'Friday' \text{ AND } time >= 10am \text{ AND } time <= 12pm} R_1$$
- $$R_3 := R_1 - R_2$$
- $$R_4 := \Pi_{shopperName, street} R_3$$
- 5)**
- $$R_1 := (\sigma_{ageGroup = '40-50s'} Shopper) \bowtie ShopAt$$
- $$R_2 := \sigma_{dayOfWeek = 'Wednesday' \text{ AND } time >= 9am \text{ AND } time <= 11am} R_1$$
- $$R_3 := R_1 - R_2$$
- $$R_4 := \Pi_{mallName} R_3$$
- $$R_5 := R_4 \Delta Mall$$
- 6)**
- $$R_1 := \Pi_{shopperName, mallName, date} ShopAt$$
- $$PR_2(S, mallName, date) R_1$$
- $$R_3 := R_1 \bowtie R_1.mallName = R_2.mallName \text{ AND } R_1.date = R_2.date \text{ AND } R_1.shopperName = S(R_2)$$
- $$R_4 := \gamma_{shopperName, count(shopperName)} \rightarrow CS(S(R_3))$$
- 7)**
- $$R_1 := \sigma_{ageGroup = '20-30'} Shopper$$
- $$R_2 := R_1 \bowtie ShopAt$$
- $$R_3 := \gamma_{shopperName, count(date)} \rightarrow Date$$
- $$R_4 := \gamma_{mallName, max(cDate) \rightarrow mallName} R_3$$
- $$R_5 := \gamma_{mallName, count(shopperName) \rightarrow Shopper}$$

Additional

a) find Library member who loan book publish before 1960

b) find ID of Lib member who is less than 21 and has never borrow book from author name J.K. Rowling

c) find name of lib member who loan⁴⁾ book with title containing cprogramming



a) $R_1 := \sigma_{\text{Name} < \text{so}} \text{ DEPT}$

$R_2 := \pi_{\text{Name}} (R_1 \bowtie \text{PROF})$

b) $R_1 := \gamma_{\text{Sname}, \text{Min}(\text{GPA}) \rightarrow \text{lowest}}$

c) $R_1 := \sigma_{\text{Crone} = \text{'Database System'}} \text{ COURSE}$

$R_2 := (R_1 \bowtie \text{MAJOR}) \bowtie \text{STUDENT}$

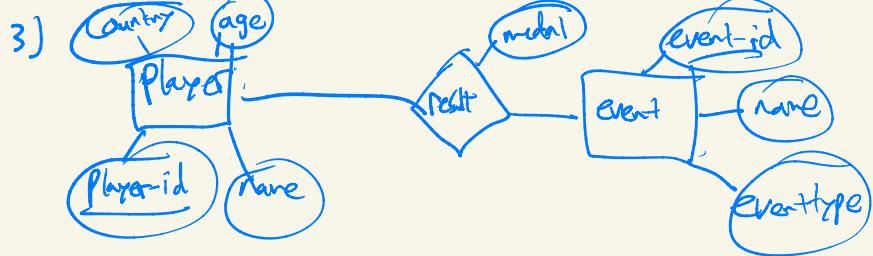
$R_3 := \pi_{\text{Sname}, \text{Crone}} (R_2)$

d) $R_1 := \pi_{\text{Crone}} \text{Course} \bowtie (\sigma_{\text{Dname} = \text{'Civil Engineering'}} \text{ DEPT})$

$R_2 := \pi_{\text{Sname}} ((\text{Student} \bowtie \text{MAJOR}) \bowtie \text{Course})$

$R_3 := R_1 \div R_2$

$R_4 := \text{STUDENT} \bowtie (\text{student.Sname} = R_3.\text{Sname}) \quad R_3$



a) $R_1 := \pi_{name, medal} (PLAYER \bowtie RESULTS)$

$R_2 := \gamma_{name, medal, \text{Count}(medal)} \rightarrow \text{TotalMedal } R_1$

$R_3 := \pi_{name} (\delta_{(medal = 'gold' \text{ AND } \text{Count}(medal) > 1)} R_2)$

$R_4 := \pi_{name} (\delta_{(medal = 'Silver' \text{ AND } \text{Count}(medal) > 1)} R_2)$

$R_5 := R_3 \bowtie R_4$

b) $R_1 := \pi_{player-id} (PLAYERS \bowtie RESULTS)$

$R_2 := \pi_{player-id} (PLAYERS)$

$R_3 := R_1 - R_2$

$R_4 := \pi_{name} (R_3 \bowtie PLAYERS)$

CZ2007 Tutorial 5: Relational Algebra

Week 7



Question 1

Shopper(shopperName, street, ageGroup)

Mall(mallName, street)

ShopAt(shopperName, mallName, date, time, dayOfWeek)

Question 1

Find those **shopper**(s) who shopped at all the **malls** on “Nanyang Ave” every **Thursday** between **10am to 5pm**, and find the **streets** that these shoppers live in.

Select **malls** on Nanyang Ave

$R1 := \Pi_{\text{mallName}} (\sigma_{\text{street} = \text{'Nanyang Ave'}} \text{Mall})$

Select **shoppers** who shopped on Nanyang Ave malls on Thursday between 10am to 5pm

$R2 := \sigma_{\text{street} = \text{'Nanyang Ave'} \text{ and } \text{dayOfWeek} = \text{'Thursday'} \text{ and } \text{time} \geq 10\text{am} \text{ and } \text{time} \leq 5\text{pm}} (\text{ShopAt} \bowtie \text{Mall})$

Select **shoppers** and **malls**

$R3 := \Pi_{\text{shopperName}, \text{mallName}} (R2)$

Find **shoppers** who shopped at ALL **malls** on Nanyang Ave

$R4 := R3 \div R1$

Find **shoppers'** streets

$R5 := R4 \bowtie \text{Shopper}$

Answer: $\Pi_{\text{shopperName}, \text{street}} (R5)$

Question 2

Find the **age** groups of those **shoppers**(s) who **only** shop at malls that are located on the **street** where he/she lives.

Find **shoppers** who shopped, take note of the **streets** the shoppers lived

$R1 := \Pi_{\text{shopperName}, \text{mallName}, \text{street}} (\text{Shopper} \bowtie \text{ShopAt} \text{shopperName} = \text{ShopAt.shopperName})$

Find **malls** shopped by shoppers, take note of the **streets** where malls are located

$R2 := \Pi_{\text{shopperName}, \text{mallName}, \text{street}} (\text{Mall} \bowtie \text{ShopAt} \text{mallName} = \text{ShopAt.mallName})$

Do relation renaming for easier manipulation later

$\rho_{R3(sName, mName, sStreet)} (R1)$

$\rho_{R4(sName, mName, mStreet)} (R2)$

Question 2

Find **shoppers** who ever before shopped at **malls** on the same **street** they live

$R5 := \Pi_{shopperName} (R3 \bowtie_{R1.sName=R2.sName \text{ and } R1.mName=R2.mName \text{ and } sStreet <> mStreet} R4)$

Find **shoppers** who only shopped at **malls** on the same **streets** they live

$R6: \Pi_{shopperName} (\text{Shopper}) - R5$

Find **shoppers'** age group

$R7 := R6 \bowtie \text{Shopper}$

Answer: $\Pi_{shopperName, \text{ageGroup}} (R7)$

Question 3

Consider **Jurong Point Mall**, the shopping mall that is 3.5km south of NTU. Find those shoppers who have shopped there **more times** than anyone else does. Also find out these shoppers' **age** groups.

Find shopping activities at Jurong Point Mall

$R1 := \sigma_{mallName = 'Jurong Point'} \text{ShopAt}$

Count how many times each shopper shopped at JPM

$R2 := \gamma_{shopperName, COUNT(date)} \rightarrow VisitCount R1$

Find out maximum count

$R3 := \gamma_{MAX(VisitCount)} \rightarrow MaxVisitCount R2$

Find out which shopper has this max count

$R4 := \Pi_{shopperName} (R2 \bowtie_{VisitCount = MaxVisitCount} R3)$

Find out shoppers' age group

$\text{Result} := \Pi_{shopperName, ageGroup} (\text{Shopper} \bowtie R4)$

Question 4

Consider Jurong Point Mall, the shopping mall that is 3.5km south of NTU. Find those shoppers in the 20s-30s age group who have **never shopped** at Jurong Point Mall on Friday evenings between 7pm to 10pm. Also find out which streets these shoppers live in.

Find shopping activities at JPM on Friday between 7-10pm

$R1 := \sigma_{mallName = 'Jurong Point' \text{ and } dayOfWeek = 'Friday' \text{ and } time >= 7pm \text{ and } time <= 10pm} (\text{ShopAt})$

Extract shoppers' names from these activities

$R2 := \Pi_{shopperName} (R1)$

Find shoppers in 20s-30s

$R3 := \sigma_{ageGroup = '20s-30s'} (\text{Shopper})$

Find shoppers in 20s-30s who shopped at JPM on Friday 7-10pm

$R4 := \Pi_{shopperName} (R2 \bowtie R3)$

Find all other shoppers

$R5 := (\Pi_{shopperName} R3) - R4$

Find shoppers' streets

$\text{Result} := \Pi_{shopperName, street} (\text{Shopper} \bowtie R5)$

Question 5

Find shopping **malls** that have never been visited by **shoppers** in the 40s-50s age group on Wednesday mornings between 9am to 11am. Also find out which **streets** these malls are located.

Find **shopping activities** on Wednesday between 9 to 11am.

$R1 := \sigma_{\text{dayOfWeek} = \text{'Wednesday'} \text{ and } \text{time} \geq 9\text{am} \text{ and } \text{time} \leq 11\text{am}} (\text{ShopAt})$

Find shoppers in the **40-50s** age group.

$R2 := \sigma_{\text{ageGroup} = \text{'40s-50s'}} (\text{Shopper})$

Find those **malls** shopped by shoppers in the 40-50s age group who shopped on Wednesday mornings between 9am to 11am.

$R3 := \Pi_{\text{mallName}} (R1 \bowtie R2)$

Find out all **other malls**.

$R4 := (\Pi_{\text{mallName}} \text{Mall}) - R3$

Find the **streets** of these **other malls**.

$\text{Result} := \Pi_{\text{mallName}, \text{street}} (\text{Mall} \bowtie R4)$

Question 6

For each shopper, find **how many other shoppers** shopped at the **same malls** as him/her on the **same date**.

Extract relevant attributes.

$\rho_{R1(s1, \text{mall}, \text{date})} (\Pi_{\text{shopperName}, \text{mallName}, \text{date}} \text{ShopAt})$

$\rho_{R2(s2, \text{mall}, \text{date})} (\Pi_{\text{shopperName}, \text{mallName}, \text{date}} \text{ShopAt})$

Find shoppers who shopped at the **same malls** on the **same date**.

$R3 := R1 \bowtie_{s1 <> s2 \text{ and } R1.\text{mall}=R2.\text{mall} \text{ and } R1.\text{date}=R2.\text{date}} R2$

Extract just shoppers' **names**.

$R4 := \Pi_{s1, s2} (R3)$

For each shopper, count **how many other shoppers** shopped at the same malls on the same date.

$\text{Result} := \gamma_{s1, \text{COUNT}(s2) \rightarrow \text{numS2}} R4$

Question 7

Find the mall(s) that is/are shopped by the **largest number** of **repeat shoppers** in the 20s-30s age group. Repeat shoppers of a mall are shoppers who have shopped **more than once** in the mall.

For each mall, find **how many times** shoppers shopped there.

$R1 := \gamma_{mallName, shopperName, COUNT(date) \rightarrow numTimes}(ShopAt)$

Find those **malls** being shopped by the **same shoppers** more than once.

$R2 := \sigma_{numTimes > 1}(R1)$

These are the **repeat shoppers**.

$\rho_{RepeatShoppers(shopperName, mallName, numTimes)} R2$

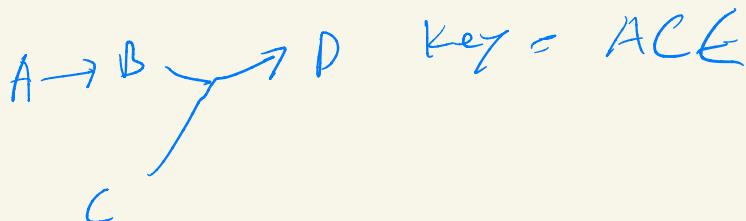
From these repeat shoppers, select those in the **20-30s** age group.

$R3 := \sigma_{ageGroup = "20s-30s"}(Shopper \bowtie RepeatShopper)$

$R(A, B, C, D, E)$

$A \rightarrow B$

$BC \rightarrow D$



$$A \rightarrow B \quad \sum A\Sigma^+ = \{A, B\}$$

$R_1(A, B)$

$R_2(A, C, D, E) \quad ACE$

$$A \rightarrow B \quad \sum A C \Sigma^+ = \{A, C, D\}$$

$$AC \rightarrow D$$

$R_3 = ACD \quad \Sigma$

$R_4 = ACE \quad \Sigma$

$A \rightarrow BD$

① Functional basis

1. ensure all RHS has only 1 attr

$AB \rightarrow C$

$A \rightarrow B$

$C \rightarrow D$

$A \rightarrow D$

$BC \rightarrow D$

$AB \rightarrow C$

$C \rightarrow D$

$BC \rightarrow D$

2. ensure no FDs are redundant

$A \rightarrow B ? \quad \Sigma A\Sigma^+ = \{A\}$
with other FDs $\quad NO$

$A \rightarrow D ? \quad Yes \quad \Sigma A\Sigma^+ = \{A\}$

$AB \rightarrow C ? \quad NO \quad \Sigma A\Sigma^+ = \{A\}$

$C \rightarrow D ? \quad NO \quad \Sigma C\Sigma^+ = \{C\}$

$BC \rightarrow D ? \quad Yes \quad \Sigma B\Sigma^+ = \{B\}$

$\Sigma = \{A \rightarrow B$

$AB \rightarrow C$

$C \rightarrow D$

3. check if we can remove multiple attr from LHS

$AB \rightarrow C$ is the only one FD

3) make tables out of FD
 $R_1(A, B)$ $R_2(C, D)$ $R_3(A, C)$

is A redundant?

$B \rightarrow C \quad \Sigma B\Sigma^+ = \{B\}$

is B redundant? \checkmark

$A \rightarrow C \quad \Sigma A\Sigma^+ = \{A, B, C, D\}$

$A \rightarrow B$

$A \rightarrow C$

$C \rightarrow D$

② see if any FDs can be combined

$A \rightarrow BC$

$C \rightarrow D$

4) remove redundant table

1) i) Select distinct Pname

From PROF, DEPT

Where PROF.Pname = DEPT.Dname
And DEPT.Numphds < 50

2) Select distinct S.Sname, M.Dname

From Student as S

JOIN Major as M on S.Sid = M.Sid

JOIN ENROLL as E on S.Sid = E.Sid

JOIN COURSE as C on C.Cno = E.Cno
And C.Cname = 'Database System'

3) Select distinct S.Sid, S.Sname, S.GPA

From Student as S

Join

(Select distinct Sid, Count(Cno)).

From ENROLL as E

Where E.Dname = 'Civil Engineering'

Group by Sid

Having Count(Cno) =

{Select Count(Cname)

From Course

Where Course.Dname = 'Civil Engineering' }) as G

On G.Sid = S.Sid

3) i) Select Distinct A.ArticleID, I.IssueID

From Article as A

JOIN Issue AS I On A.IssueID = I.IssueID

JOIN WordAppears WA on WA.IssueID = I.IssueID
And WA.ArticleID = A.ArticleID

JOIN words As W on W.WordID = WA.WordID

Where (W.WordText Like '%Politician%') Or
W.WordText Like '%Corruption%')

3)

Select distinct
E1.Employee-name as employee
E2.Employee-name as manager

From Employee as E1
Join Managers as M on M.EmployeeName = E1.Employee-name
Join Employee as E2 on M.Manager-name = E2.Employee-name
And E1.Street = E2.Street And
E1.City = E2.City

1. Write SQL statements for the following queries.

The schema of a database containing university-type data is given below. Primary key is underlined for each relation.

```
STUDENT(Sid, Sname, Sex, Age, Year, GPA)
DEPT(Dname, Numphds)
PROF(Fname, Dname)
COURSE(Cno, Cname, Dname)
MAJOR(Dname, Sid)
SECTION(Dname, Cno, Sectno, Pname)
SECTIONL(Sid, Grade, Dname, Cno, Sectno)
```

Write the following queries.

(1) Find the names of professors who work in departments that have fewer than 50 PhD students.

(2) Find the names and majors of students who have taken the 'Database System' course.

(3) Find the ids, names, and GPAs of the students who have taken all courses from the 'Civil Engineering' department.

2. Suppose we are maintaining a database of articles published in our newspaper, The Straits Times. We have the following schema (ahlen keys are underlined):

```
Article(issueID, articleID, author, title)
Citation(articleID, issueID, citedArticleID, citedIssueID)
WordAppears(articleID, issueID, articleID, position)
Word(wordID, wordText)
Issue(issueID, date, howManyDistributed)
```

For each of the following queries, write the query in SQL. Assume that dates can be compared using comparison operators (i.e., >, <, =). Assume that position is an integer starting from 1 when the word appears (i.e., first word, 2 = second, etc.).

Q) Find the documents in which the words "politician" and "corruption" appear.

3. For the following relational schema:

```
employee (employee_name, street, city)
works (employee_name, company_name, salary)
company (company_name, city)
manages (employee_name, manager_name)
```

Give an expression in SQL for each of the following queries:

Find the names of all employees in the database who live in the same cities and on the same streets as do their managers. Assume that all people work for at most one company. Each company has at most one manager, who is also an employee of the same company.

Tutorial 6 SQL

Classroom Exercise

Question 1

(i)

```
SELECT Pname
FROM PROF, DEPT
WHERE DEPT.Dname = PROF.Dname AND Numphds < 50;
```

(iii)

```
SELECT Sname, Dname
FROM COURSE C, ENROLL E, MAJOR M, STUDENT S
WHERE C.Cname = 'Database Systems' AND
C.Dname = E.Dname AND C.Cno = E.Cno AND
E.Sid = M.Sid AND E.Sid = S.Sid;
```

(iv)

```
SELECT Sid, Sname, GPA
FROM STUDENT S
WHERE NOT EXISTS
(SELECT C.CID
FROM COURSE C
WHERE Dname = 'Civil Engineering'
EXCEPT
SELECT E.CID
FROM ENROLL E
WHERE Dname = 'Civil Engineering'
AND E.Sid = S.Sid);
```

Question 2

(i)

```
SELECT DISTINCT wa1.issueID, wa1.articleID
FROM WordAppears wa1, WordIDs wi1, WordAppears wa2, WordIDs wi2
WHERE wa1.issueID = wa2.issueID AND wa1.articleID = wa2.articleID
AND wa1.wordID = wi1.wordID AND wa2.wordID = wi2.wordID
AND wi1.wordText = 'politician' AND
wi2.wordText = 'corruption';
```

Question 3

(b) Find the names of all employees in the database who live in the same cities and on the same streets as do their managers. Assume that all people work for at most one company. Each company has at most one manager, who is also an employee of the same company.

Solution:

```
SELECT p.employee-name  
FROM employee p, employee r, manages m  
WHERE p.employee-name = m.employee-name  
AND m.manager-name = r.employee-name  
AND p.street = r.street AND p.city = r.city;
```

TUT 7

1) a) Select S.name, S.GPA
from STUDENT as S
where S.GPA IN (select Min(GPA) from STUDENT);

b) $AC \rightarrow ABCD$ Stupid question
 $D \rightarrow AB \leftarrow D$

2) a) Select CategoryName
from Category AS C
where C NOT IN
(Select distinct BelongsTo From Category)

b) Select B.*
From Book AS B
Join
(Select distinct ISBN, Count(CopyNumber) AS C
From Copy
Where Copy.CopyNumber NOT IN
(Select CopyNumber From LOAN)
(Select CopyNumber From LOAN)
Group by ISBN) AS C
on B.ISBN = C.ISBN
and C.CN > 1

3) a) Select employeeName
from Works W
Join
(Select distinct
Company-name, Avg(Salary) AS AS
from works
Group by Company-name) AS AVGs
On W.Company-name = AVGs.Company-name
and W.Salary > AVGs.AS +
Max(X)

4) ii) Select citedArticleID, citedIssueID, Count(x) as X
From
(Select
CitedArticleID, CitedIssueID, Count(ArticleID) as X
From Citation
Group by CitedArticleID, CitedIssueID)
group by CitedArticleID, CitedIssueID

iii) Select a.author, Count(*)
From Article AS A
Join Citation AS C
on C.articleID = a.articleID
and C.issueID = a.issueID
where a.author in (Select distinct author
from Article Join Issue on Article.issueID = Issue.issueID
where issue.(Year(issueDate)) - Year(issueDate) > 10);

2. Consider the following relational schema:

Reader (RDN, Surname, FirstName, City, Birthdate)
Book (ISBN, Title, Author, NoPages, PubYear, PublisherName)
Publisher (PublisherName, PublisherCity)
Category (CategoryName)
Copy (ISBN, CopyNumber, Shelf, Position)
Loan (ReaderID, ISBN, Copy.ReturnDate)
BookCategory (ISBN, CategoryName)

BelongsTo To which particular categories the current category belongs to. Each book has a specific ISBN. A reader can borrow a book multiple times, and each instance is recorded in its ReturnDate. All the _____ categories that a book belongs to are stored in the table BookCategory.

Formulate the following queries in SQL.

- (a) Which categories do not have any subcategories?
- (b) For which of the books there is at least one copy available?
- (c) Which books have more pages than twice the average of the number of pages of all books?
- (d) What are the surnames of the readers from the city "New York"?

c) Select B.*
From Book AS B
Where B.NoPages >= 2 *
(Select Avg(NoPages)
From Book)

d) Select distinct
Surname
From Reader AS R
Where
R.City = 'New York'
AND R.RDNR IS IN
(Select ReaderID From
Loan);

3. For the following relational schema:

employee (employee-name, street, city)
works (employee-name, company-name, salary)
company (company-name, city)
manages (employee-name, manager-name)

Give an expression in SQL for each of the following queries:

(a) Find the names of all employees who earn more than the average salary of all employees of their company. Assume that all people work for at most one company.

4. Suppose we are maintaining a database of articles published in our newspaper, the Straits Times. We have the following schema (where keys are underlined):

Article (issueID, articleID, author, title)
Citation (articleID, issueID, citedArticleID, citedIssueID)
WordAppears (wordID, issueID, articleID, position)
Words (wordID, wordText)
Issue (issueID, date, howManyPublished)

For each of the following queries, write the query in SQL. Assume that dates can be compared using comparison operators (<, >, =). Assume that position is an index specifying where the word appears (1 = first word, 2 = second, etc.).

(ii) Find the most-cited article(s) in the newspaper's history.

(iii) Find the number of citations per author for "senior" authors (i.e., an author who has at least one article that was published 10 or more years ago).

Tutorial 7 SQL

Classroom Exercise

Question 1

(a)

(i)

```
SELECT      Sname
FROM        STUDENT
WHERE       GPA IN
            (SELECT MIN(GPA) FROM STUDENT);
```

(b)

This query will report error. The reason is the subquery returns a scalar, and therefore cannot be compared against a single data value. You would need to add “ANY” or “ALL” before the subquery for the query to run.

Question2

(a) Which categories do not have any subcategories?

Solution:

```
SELECT C1.CategoryName
FROM Category C1
WHERE NOT EXISTS
(SELECT CategoryName
FROM Category C2
WHERE C2.BelongsTo = C1.CategoryName);
```

(b) For which of the books there is at least one copy available?

Solution:

```
SELECT Title
FROM Book
WHERE ISBN IN
(SELECT ISBN FROM
((SELECT CopyNumber, ISBN FROM Copy)
EXCEPT
(SELECT Copy, ISBN FROM Loan)));
```

An assumption here is that loan table only records books that are on loan; once returned, the record is removed from Loan table.

(c) Which books have more pages than twice the average of the number of pages of all books?

Solution:

```
SELECT ISBN
FROM Book
WHERE NumberOfPages >= 2 * (SELECT AVG(NumberOfPages)
FROM Book);
```

(d) What are the surnames of the readers from the city “New York”?

Solution:

```
SELECT DISTINCT Surname
FROM Reader
WHERE City = 'New York'
```

Question 3

(a) Find the names of all employees who earn more than the average salary of all employees of their company. Assume that all people work for at most one company.

Solution:

```
SELECT employee-name
FROM works t
WHERE salary > (SELECT AVG(salary)
FROM works s
WHERE t.company-name = s.company-name);
```

Question 4

```
SELECT citedIssueID, citedArticleID
FROM Citation
GROUP BY citedIssueID, citedArticleID
HAVING COUNT(*) >= ALL
          (SELECT COUNT(*)
          FROM Citation
          GROUP BY citedArticleID, citedIssueID)
```

(iii) return author and number of references/citations

```
SELECT      a.author, COUNT(*)
FROM        Article a, Citation c
WHERE       a.issueID = c.citedIssueID AND a.articleID = c.citedArticleID
AND EXISTS
    (SELECT      *
     FROM        Article a2, Issue i
     WHERE       a2.issueID = i.issueID AND
                a2.author = a.author AND
                Year(getDate()) - Year(i.date) >= 10)
GROUP BY a.author;
```

QUESTION

- i) update employees
Set street = 'Newstreet',
AND city = 'Newtown'
where personname = 'Mark'
ii) Update works
Set salary = salary + (0.1 * salary)
where companyname = 'TechMatch'
iii) update works
Set salary = salary + (0.1 * salary)

Classroom Exercise

1. The relational database schema for a car-rental company is given below:
person (personid, name, address)
customer (customerid, name, address)
owner (ownerid, license)
participated (reportnumber, driverid, license, damageamount)
employee (empid, name, street, city)
works (personname, companyname, salary)
company (companyname, city)
manages (managername, managername)

(i) Modify the database so that Mark now lives in "Newstreet, Newtown" (i.e. the street changes to Newstreet and the changes to Newtown for Mark).

(ii) Give all employees of "TechMatch" a 10 percent salary raise.

(iii) Give all managers of "TechMatch" a 10 percent salary raise.

- 2) i) Yes same size
ii) No

- 3) i) **CREATE ASSERTION A1 CHECK**

(NOT EXIST
(Select P.color
From Catalog AS C
JOIN Parts AS P on P.pid = C.pid
where P.color IN ('red', 'green')))

- ii) **CREATE ASSERTION A2 CHECK**

(NOT EXIST
(Select P.
From Catalog AS C
where C.Price < (Select Price
From catalog
Where Sid = 1)))

- 4) Create TRIGGER T1
AFTER UPDATE ON R
REFERENCING NEW ROW AS NR
OLD ROW AS OR

FOR EACH ROW
when [(NR.C > OR.C) and ((NR.A = OR.A) AND (NR.B = OR.B))]
DELETE FROM R
WHERE A = OR.A AND
B = OR.B

- 5) CREATE TRIGGER T1
AFTER UPDATE ON FLIGHT
REFERENCING
FOR EACH ROW NEW ROW AS NR
WHEN NR.NUMSEAT < 20
BEGIN
UPDATE FLIGHT
SET PRICE = 4000
WHERE FLIGHTNO = NR.FLIGHTNO
AND DAY = NR.DAY
AND MONTH = NR.MONTH
AND YEAR = NR.YEAR
END

- CREATE TRIGGER T2
AFTER INSERT INTO FLIGHT
REFERENCING
NEW ROW AS NR
FOR EACH ROW
WHEN (NR.NUMSEATS < 20 OR NR.MANAGEF > 2000)
DELETE FROM FLIGHT
WHERE NR.FLIGHTNO = FLIGHTNO

- 6) CREATE TRIGGER S
AFTER INSERT INTO registeredFor
REFERENCING
NEW ROW AS NR

FOR EACH ROW

WHEN C

Exist
(Select S.* , E.examTime
FROM registeredFor AS S
JOIN Exams AS E on S.course = E.course
where S.Student = NR.Student
AND S.ExamDate = NR.ExamDate
AND S.Course = NR.Course
)

begin
INSERT INTO SpecialExams
Values(

NR.Student,
NR.Course,
NR.examDate,

(Select examTime
From Exams AS e
WHERE
C.Course = NR.Course
C.examDate = NR.ExamDate
C.examTime NOT IN

(Select startTime
From registeredFor AS R
WHERE
R.ExamDate = NR.ExamDate
AND R.Course = NR.Course
AND R.ExamTime = NR.ExamTime
AND R.Student = NR.Student
));

8. Consider the relation schema STUDENT (student_id, name, gender, grade).
Suppose the following view is defined on STUDENT and GPA (student_id, grade, semester):

9. It is proposed to insert a tuple (X, 100, 1000) into the view. If yes, what should be the result of X?

10. Then consider the following view:

CREATE VIEW MAJOR_AVG AS
SELECT majorname, avggrade, AVG(gpa)
FROM student
GROUP BY majorname;

Is it possible now to insert a tuple (S1, 80) into this view? If yes, what should be the result of S1?

11. Consider the following schema of product database:

PartNumber (productname, vendor, unit, selling
price, quantity, minStock, maxStock, selling
Category, sellingCategory, priceRate)

The Catalog consists of several hundred parts having four part and a given price. Determine each of the following questions concerning the Catalog:

a) On which supplier has a lowest price for part A and a given price. Determine each of the following questions concerning the Catalog:

b) On which vendor has a lowest price for part A and a given price.

c) On which vendor has a lowest price for part A and a given price. Determine each of the following questions concerning the Catalog:

d) On which vendor has a lowest price for part A and a given price.

e) On which vendor has a lowest price for part A and a given price.

f) On which vendor has a lowest price for part A and a given price.

g) On which vendor has a lowest price for part A and a given price.

h) On which vendor has a lowest price for part A and a given price.

i) On which vendor has a lowest price for part A and a given price.

j) On which vendor has a lowest price for part A and a given price.

k) On which vendor has a lowest price for part A and a given price.

l) On which vendor has a lowest price for part A and a given price.

m) On which vendor has a lowest price for part A and a given price.

n) On which vendor has a lowest price for part A and a given price.

o) On which vendor has a lowest price for part A and a given price.

p) On which vendor has a lowest price for part A and a given price.

q) On which vendor has a lowest price for part A and a given price.

r) On which vendor has a lowest price for part A and a given price.

s) On which vendor has a lowest price for part A and a given price.

t) On which vendor has a lowest price for part A and a given price.

u) On which vendor has a lowest price for part A and a given price.

v) On which vendor has a lowest price for part A and a given price.

w) On which vendor has a lowest price for part A and a given price.

x) On which vendor has a lowest price for part A and a given price.

y) On which vendor has a lowest price for part A and a given price.

z) On which vendor has a lowest price for part A and a given price.

aa) On which vendor has a lowest price for part A and a given price.

bb) On which vendor has a lowest price for part A and a given price.

cc) On which vendor has a lowest price for part A and a given price.

dd) On which vendor has a lowest price for part A and a given price.

ee) On which vendor has a lowest price for part A and a given price.

ff) On which vendor has a lowest price for part A and a given price.

gg) On which vendor has a lowest price for part A and a given price.

hh) On which vendor has a lowest price for part A and a given price.

ii) On which vendor has a lowest price for part A and a given price.

jj) On which vendor has a lowest price for part A and a given price.

kk) On which vendor has a lowest price for part A and a given price.

ll) On which vendor has a lowest price for part A and a given price.

mm) On which vendor has a lowest price for part A and a given price.

nn) On which vendor has a lowest price for part A and a given price.

oo) On which vendor has a lowest price for part A and a given price.

pp) On which vendor has a lowest price for part A and a given price.

qq) On which vendor has a lowest price for part A and a given price.

rr) On which vendor has a lowest price for part A and a given price.

ss) On which vendor has a lowest price for part A and a given price.

tt) On which vendor has a lowest price for part A and a given price.

uu) On which vendor has a lowest price for part A and a given price.

vv) On which vendor has a lowest price for part A and a given price.

ww) On which vendor has a lowest price for part A and a given price.

xx) On which vendor has a lowest price for part A and a given price.

yy) On which vendor has a lowest price for part A and a given price.

zz) On which vendor has a lowest price for part A and a given price.

aa) On which vendor has a lowest price for part A and a given price.

bb) On which vendor has a lowest price for part A and a given price.

cc) On which vendor has a lowest price for part A and a given price.

dd) On which vendor has a lowest price for part A and a given price.

ee) On which vendor has a lowest price for part A and a given price.

ff) On which vendor has a lowest price for part A and a given price.

gg) On which vendor has a lowest price for part A and a given price.

hh) On which vendor has a lowest price for part A and a given price.

ii) On which vendor has a lowest price for part A and a given price.

jj) On which vendor has a lowest price for part A and a given price.

kk) On which vendor has a lowest price for part A and a given price.

TNT9
1)

Classroom Exercise

1. Consider the following relation:

Articles (ID, title, journal, issue, year, startpage, endpage, TR-ID)

It contains information on articles published in scientific journals. Each article has a unique ID, a title, and information on where to find it (name of journal, what issue, and on which pages). Also, if results of an article previously appeared in a "technical report" (TR), the ID of this technical report can be specified. We have the following information on the attributes:

- For each journal, an issue with a given number is published in a single year.
- The endpage of an article is never smaller than the startpage.
- There is never (part of) more than one article on a single page.

Consider the following six queries on Articles:

- a. SELECT title FROM Articles WHERE year>2005;
- b. SELECT title FROM Articles WHERE endpage=100;
- c. SELECT title FROM Articles WHERE year>1995 AND year<2000;
- d. SELECT title FROM Articles WHERE journal='JACM' AND issue=55;
- e. SELECT title FROM Articles WHERE issue=55 AND journal='JACM';
- f. SELECT title FROM Articles WHERE endpage-startpage>50;

Indicate which of the above queries would likely be faster (based on the knowledge you have from the course), if all of the following indexes were created.

- CREATE INDEX idx1 ON Articles (year, startpage);
- CREATE INDEX idx2 ON Articles (startpage, endpage);
- CREATE INDEX idx3 ON Articles (journal, issue, year);

2. Consider the following XML DTD for an employee database.

```
<!DOCTYPE emp |>
<ELEMENT emp (ename, children*, sibl*)>
<ELEMENT children (name, birthday)*>
<ELEMENT sibl (type, example)*>
<ELEMENT ename (#PCDATA)>
<ELEMENT birthday (#PCDATA)>
<ELEMENT type (#PCDATA)>
<ELEMENT example (#PCDATA)>
<ELEMENT day (#PCDATA)>
<ELEMENT month (#PCDATA)>
<ELEMENT year (#PCDATA)>
<ELEMENT sibl (#PCDATA)>
```

Create a valid XML document that follows the rules of the above DTD.
Your document must illustrate all the rules of the DTD.

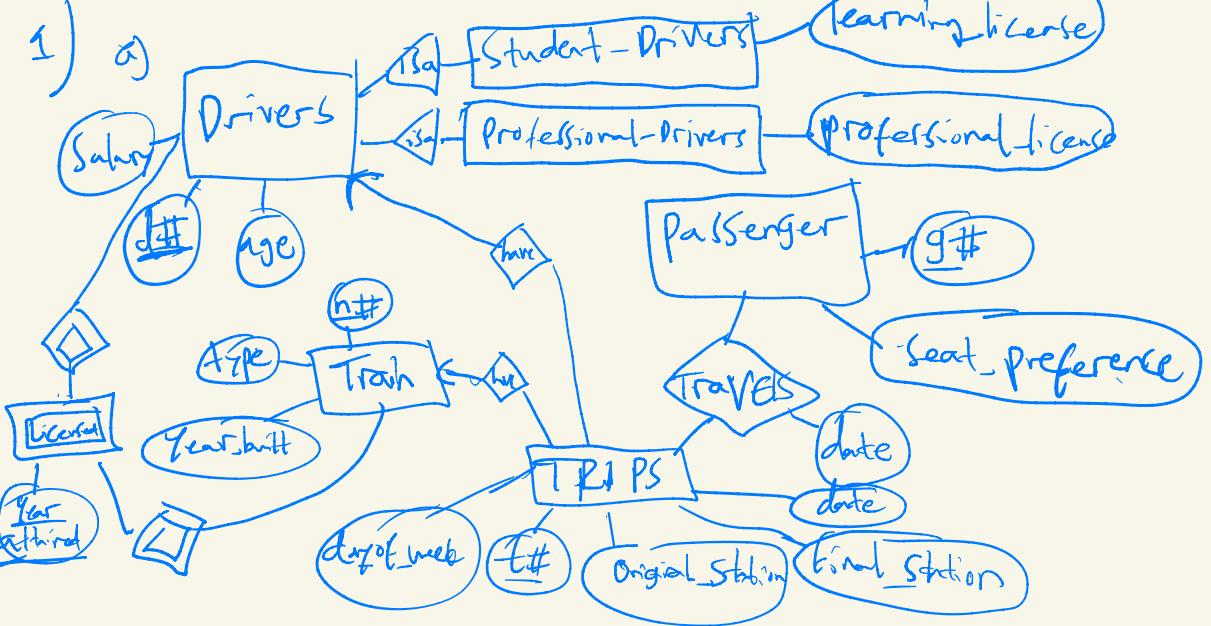
3. Consider the following relational database schema about students and courses (primary keys are underlined).

STUDENT(SID, NAME, EMAIL)
COURSE(CD, NAME, INSTRUCTOR, ROOM)
ENROLLS(SID, CD, GRADE)

In ENROLLS, SID and CD are foreign keys into STUDENT and COURSE, respectively. The following two constraints also hold: (a) each student is enrolled in some course, and (b) each course has at least one student enrolled.

- (i) Design a schema for exposing this data as an XML view to the chair's office. The chair wants to see the data grouped by courses and needs to have access to all the information in the database.
- (ii) Give an example of a database instance for the relational schema and show the resulting document for the XML view according to the DTD that you have designed.

Past year
paper



b) $R_1 := \sigma_{\text{year_built} = 2010} \text{TRAIN}$

$R_2 := (\sigma_{\text{year obtained} < 2018} \text{LICENSED}) \bowtie R_1$

$R_3 := (\text{LICENSED} \bowtie R_1) - R_2$

$R_4 := R_3 \bowtie R_1$

$R_5 := \text{STUDENT-DRIVERS} \bowtie R_4$

c) $R_1 := \sigma_{\text{day of week} = \text{'Monday'}} \text{AND} \text{Original_Station} = \text{Jungnigli}$

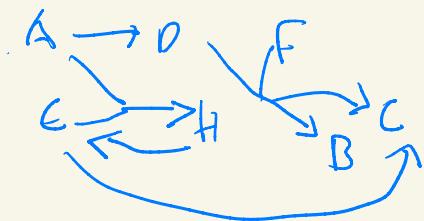
$R_2 := (\sigma_{\text{age} = 50} \text{DRIVERS}) \bowtie R_1$

$R_3 := \pi_{d\#}(R_2)$

$R_4 := R_3$

$R_5 := R_3 \bowtie_{R_3.d\# \neq R_4.d\#} R_4$

2) a)



keys = AFE, AFH

b)

i) $EC \rightarrow AD$

$$\Sigma EC^+ = \{E, C\} \text{ no}$$

ii) $ADF \rightarrow E$

$$\Sigma ADF^+ = \{A, D, F\} \text{ no}$$

iii) $A \rightarrow DH$

$$\Sigma A^+ = \{A\} \text{ no}$$

iv) $AED \rightarrow C$

$$\Sigma AED^+ = \{A, E, D, H, C\} \text{ yes}$$

v) $DH \rightarrow C$

$$\Sigma DH^+ = \{D, H, C\} \text{ yes}$$

c)

 $A \rightarrow D$ $(AE \rightarrow H)$ $DF \rightarrow BC$ $E \rightarrow C$ $H \rightarrow F$ 1NF

R(A, B, C, D, E, F, H) AFE or AFH

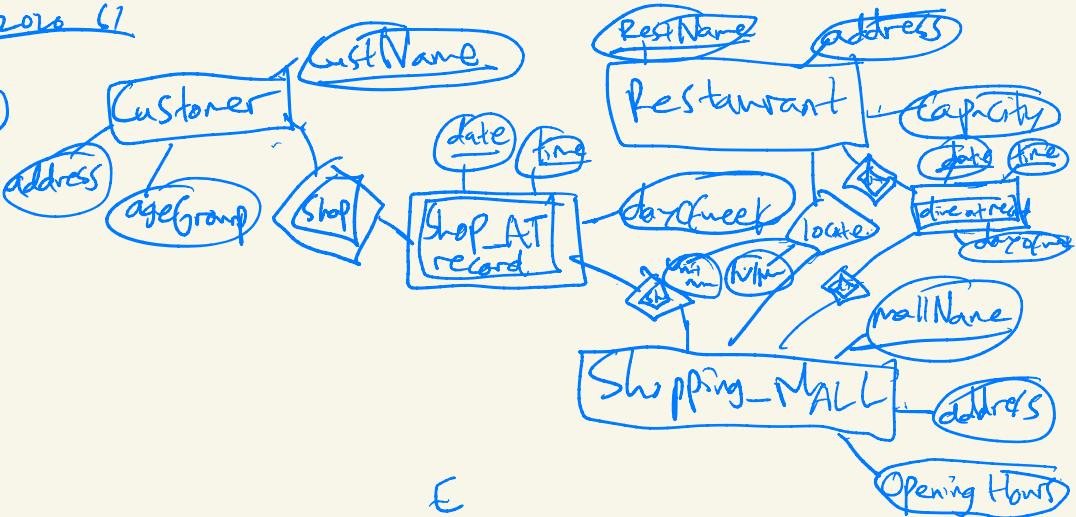
not BCNF due to $H \rightarrow E$,

3NF yes

3)

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1) a)

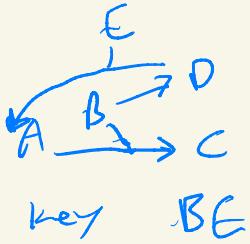


2)

$$AB \rightarrow C$$

$$B \rightarrow D$$

$$D E \rightarrow A$$



a) no as the RHS of FDs given is not in primary keys

b) $AB \rightarrow C$ RHS not in primary key BE

$$\{AB\}^+ = \{A, B, C\}$$

$$R_1 \subseteq \{A, B, C\} \quad R_2 \subseteq \{A, B, D, E\}$$

c) lossless as both table still has B which is part of BE

dependency preserving

$$R_1 \subseteq \{A, B, C\} \quad AB \rightarrow C \quad \checkmark_{R_1} \quad \text{Yes}$$

$$R_2 \subseteq \{A, B, D, E\}$$

$$\begin{array}{l} B \rightarrow D \\ D E \rightarrow A \end{array} \quad \checkmark$$