SC4024/CZ4124 Data Visualization

Assistant Professor WANG Yong yong-wang@ntu.edu.sg CCDS, Nanyang Technological University

1

Chapter 9.1 Exploratory Data Analysis

Outline

- · What is Exploratory Data Analysis?
- · Correlation Analysis
 - Measurement of Correlation
 - Univariate Analysis
 - o Bivariate Analysis
 - o Confirmatory Analysis
 - Multivariate Analysis

3

3

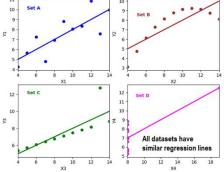
Statistical Analysis Alone is Not Enough

A Review

- Basic statistical analysis alone may not provide useful insights into how datasets can have **differing characteristics** despite having **similar statistical** parameters.
- Francis Anscombe^[1] used the **Anscombe's Quartet**^[1] of four datasets to show why **visualisation** is a **crucial part of data analysis**.







[1] Anscombe, F. J. (1973). "Graphs in Statistical Analysis". American Statistician. 27 (1): 17-21

4

What is Exploratory Data Analysis?

- Exploratory Data Analysis (EDA) is a process of examining (mostly graphically) a
 dataset to discover patterns and relationships, spot anomalies, formulate and test
 initial assumptions using statistical measures^[2].
- The primary aim of EDA is to **examine what data can tell us** before actually going through formal modelling and hypothesis formulation^[2].
- EDA is usually an iterative process that involves:
 - Asking questions about the available data.
 - 2. Construct appropriate data visualisations to answer the questions.
 - **3. Evaluate** and **inspect** the answers, then derive further questions.

Repeat



[2] S.M. Mukhiya & U. Ahmed, Hands-on Exploratory Data Analysis with Python. Packt Publishing (2020)

5

5

Correlation Analysis

Are There Relationships in the Dataset?

- Datasets often have **different categories** (i.e. columns) containing many **measured values** describing a particular phenomena, event or situation.
- Since these values are collected from the **same event**, there is a possibility that they are **related** to one another^[2].
- Correlation is the statistical technique that examines these relationships and describes how strongly different categories of measures or values are related.
- · Correlation answers questions such as:
 - How does one variable change with respect to another?
 - If it does change, to what degree or strength is this change related?



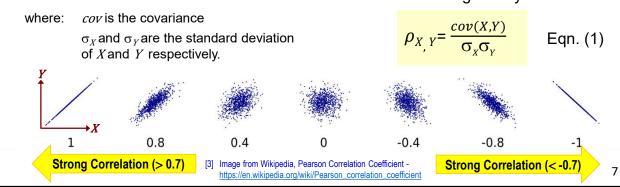
[2] S.M. Mukhiya & U. Ahmed, Hands-on Exploratory Data Analysis with Python. Packt Publishing (2020)

6

Measure Of Correlation

Pearson Correlation Coefficient

- Correlation measures how variables **change in tandem**, either in the same or in opposite directions, and also the magnitude or **strength** of these related changes between the variables.
- The **Pearson correlation coefficient** (ρ_{xy}) , with a value between -1 and +1, measures the correlation between two variables X and Y. It is given by:



7

Univariate Analysis

One Variable At A Time

- Univariate analysis involve the analysis of **one variable at a time** in the dataset. As such, it is not meant to find relationships between variables.
- The main purpose of univariate analysis is to:

Property[Price] Mean = 37.98 Median = 38.45

mean() and

- find patterns in the variable such as its **central tendency** (e.g mean, median, mode)
- understand its dispersion (e.g range, variance, maximum & minimum quartile, etc)

- detect presence of outliers.

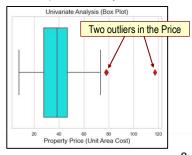


38.450000
75% 46.600000
max 117.590000
Name: Price, dtype: float64

Apply describe() On category Price in Property.csv



Histogram and Kernel Density Curve



Box Plot (Observing Outliers)

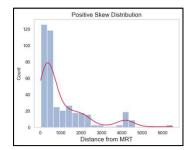
Univariate Analysis

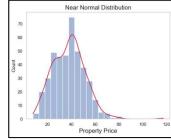
Is My Distribution Normal Enough?

- In order to use **parametric statistical methods** (e.g. Student's t-test), our data must have a **normal distribution**, otherwise nonparametric statistical methods must be used.
- The **normality** of the data or how close they conform to a Gaussian distribution can

be tested using visual methods (e.g. statsmodels's qqplot())^[4].

- Numerical evaluations can be done using statistical methods^[5] such as:
 - Shapiro-Wilk test
 - D'Agostino's K^2 test
 - Anderson-Darling test





Positive Skew - Property['MRT']

Near Normal – Property['Price']

9



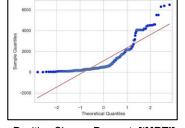
- [4] Statsmodels Q-Q plot function https://www.statsmodels.org/stable/generated/statsmodels.graphics.gofplots.qqplot.html
- [5] Jason Brownlee, A Gentle Introduction to Normality Tests in Python (2018) https://machinelearningmastery.com/a-gentle-introduction-to-normality-tests-in-python/

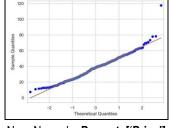
9

Univariate Analysis

Visualising Normality

- A popular plot for checking normality is the quantile-quantile plot or Q-Q plot^[6].
- The plot generates its own sample of the ideal Gaussian distribution and divides these samples into groups (e.g. 5) called **quantiles**. Each data point in our sample is **paired** with a similar member in the idealised distribution and plotted on the same cumulative distribution [5].
- Perfect normality will see all the data points fall along the 45° red line (i.e. matching ideal distribution).
- Dots seen deviating from the line shows deviation from the expected normal distribution.





Positive Skew – Property['MRT']

Near Normal – Property['Price']

NANYANG TECHNOLOGICAL UNIVERSITY SINGAPORE

- [6] Paras Varshney, Q-Q Plots Explained (2020) https://towardsdatascience.com/q-q-plots-explained-5aa8495426c0
- [5] Jason Brownlee, A Gentle Introduction to Normality Tests in Python (2018) https://machinelearningmastery.com/a-gentle-introduction-to-normality-tests-in-python/

Bivariate Analysis

How Are These Two Variables Related?

Bivariate analysis is used to find out if there is a relationship between two
different variables in the dataset.

Relationship between Math & Writing Scores

- A common plot used for bivariate analysis is the two-axes **scatter plot**.
- A relationship exist if the data points seem to fit around a line or a curve. The tighter the clustering, the stronger the relationship.

Did students getting high Math scores also got high Writing scores? Yes, there is a reasonably strong positive correlation between Math and Writing scores Writing vs Math Scores in Student performance.csv

NANVANG

11

11

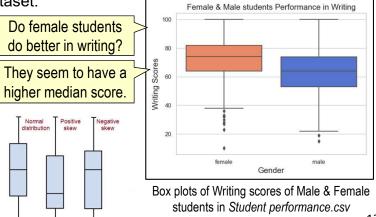
Bivariate Analysis

What If One Variable is Categorical?

• Bivariate analysis using a **box plot** allows us to examine the **statistical measures** of one quantitative variable along with the relationship between multiple values of a **categorical variable** in the dataset.

 The central lines in the box plot allow us to compare the median values within the categories (e.g. female & male).

 The nature of the data distribution (i.e. normal or skewed) can be inferred from the relative position of the central line within the box.



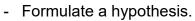
12

Bivariate Analysis

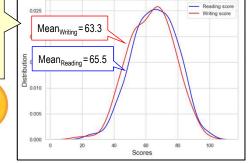
Confirmatory Analysis

- Visual analysis is useful for spotting relationships or patterns in data. However, we should check our assumption using appropriate statistical measures and confirm if an observation is statistically significant.
- The following confirmatory analysis steps could be taken:

Are the differences between the reading & writing scores of the boys significant?



- Check normality of data distributions.
- Select appropriate statistical test (e.g parametric or non-parametric).
- Compute the test statistics to determine the
 p value (typically p < 0.05 is considered significant)



KDE plots of Reading & Writing scores of Male students in *Student performance.csv*

13

13

Confirmatory Analysis

Formulating a Hypothesis

- A hypothesis is a statement about the value of a population parameter. In order to test a hypothesis, we formulate a **null** hypothesis and the **alternate** hypothesis.
- Null hypothesis (H₀) a default position statement that there is no relationship between two measured phenomena or no association among groups^[7].
- Alternate hypothesis (H_a) a statement that is contrary to the null hypothesis. It is usually the hypothesis being tested since we see a pattern, think it is true and want to find evidence to reject the null hypothesis and replace it with the alternate.

 $\begin{array}{ll} \mbox{Null hypothesis $(\textbf{H_0})$} & \mu_{\mbox{Reading}} = \mu_{\mbox{Writing}} & \mbox{(No difference in performance)} \\ \mbox{Alternate hypothesis $(\textbf{H_a})$} & \mu_{\mbox{Reading}} > \mu_{\mbox{Writing}} & \mbox{(Reading scores better than writing)} \end{array}$

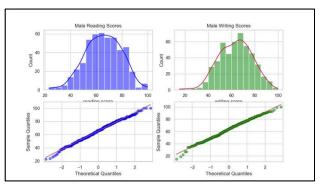


[7] Yogesh Agrawal, Hypothesis testing in Machine learning using Python (2019) https://towardsdatascience.com/hypothesis-testing-in-machine-learning-using-python-a0dc89e169ce

Confirmatory Analysis

Check For Normality

- In order to decide if we should use a parametric or non-parametric statistical test, we should check the **normality** of the two distributions we are comparing.
- We can do a normality check using an appropriate statistical tests^[5] or use the Q-Q plot^[4].
- Visually, both the Reading & Writing score distributions of male students seem to conform to a Gaussian distribution.
- We can do further numerical statistical test to verify this.



Histogram/KDE plots of Reading & Writing scores and their Q-Q plots



- [4] Statsmodels Q-Q plot function https://www.statsmodels.org/stable/generated/statsmodels.graphics.gofplots.qqplot.html
- [5] Jason Brownlee, A Gentle Introduction to Normality Tests in Python (2018) https://machinelearningmastery.com/a-gentle-introduction-to-normality-tests-in-python/

15

Confirmatory Analysis

Statistical Test for Normality

• The **Shapiro-Wilk** test evaluates a sample of data and quantifies how likely the data sample is drawn from a Gaussian distribution^[5]. Python **scipy.stats** library provides several functions for normality statistical tests, including the Shapiro-Wilks.

```
from scipy.stats import shapiro
S,p = shapiro(Dist)
if (p > 0.05):
   print('Distribution is normal')
```

- Both Reading & Writing distributions meet the normality confidence level of 0.05.
- We can thus look at using a parametric test (e.g. the t-test or Z-test)

- # import the Shapiro-Wilks test
- # run the Shapiro-Wilks test
- # check p value
- # distribution is normal if p > 0.05

```
Distribution ( male , reading score ) mean = 65.47

Shapiro-Wilk test = ( Stats= 0.99 , p = 0.08968 )

Distribution ( male , reading score ) is normal

Distribution ( male , writing score ) mean = 63.31

Shapiro-Wilk test = ( Stats= 0.99 , p = 0.10408 )

Distribution ( male , writing score ) is normal
```



Jason Brownlee, A Gentle Introduction to Normality Tests in Python (2018) https://machinelearningmastery.com/a-gentle-introduction-to-normality-tests-in-python/

16

Confirmatory Analysis

Z-test or Student's t-test?

- If there is **more than 30 data samples**, the Z-test can be used, otherwise the t-test should be used with small sample sizes^[7].
- Both the Z-test and t-test requires the data to be **normally distributed** and data points are **independent** from each other (i.e. one data point does not affect another data point). Strict normality requirements can be relaxed if the sample size is large.
- The Python **statsmodels** library provides both these statistical tests.

```
from statsmodels.stats.weightstats import ttest_ind # t-test function
from statsmodels.stats.weightstats import ztest # Z-test function
```

• Given that the sample size of male students is 482, the Z-test can be used here.



 Yogesh Agrawal, Hypothesis testing in Machine learning using Python (2019) https://towardsdatascience.com/hypothesis-testing-in-machine-learning-using-python-a0dc89e169ce

17

17

Confirmatory Analysis

One or Two-Tailed Test?

• **Two-tailed test** – use it if you want to determine if there is a difference between two groups and have no concern about the direction of this difference. Example:

```
Null hypothesis (\mathbf{H_0}) \mu_{\text{Reading}} = \mu_{\text{Writing}} (No difference in performance)

Alternate hypothesis (\mathbf{H_a}) \mu_{\text{Reading}} \neq \mu_{\text{Writing}} (There is a difference in performance)
```

 One-tailed test – use it if you want to determine if there is a difference between groups in a specific direction. In our case, the Reading distribution seems to be visually higher than Writing one. We should therefore use:

```
 \text{Alternate hypothesis } (\textbf{H}_{\textbf{a}}) \hspace{1cm} \mu_{\text{Reading}} > \mu_{\text{Writing}} \hspace{1cm} \text{(Reading performance better than Writing)}
```

Note: One-tailed test has more statistical power than a two-tailed test at the same significance level.
 Results are more likely to be significant for a one-tailed test if there is indeed a difference between the groups in the direction predicted^[8].



[8] Should you use a one-tailed test or a two-tailed test for your data analysis? https://www.statisticssolutions.com/should-you-use-a-one-tailed-test-or-a-two-tailed-test-for-your-data-analysis.

Confirmatory Analysis

Statistical Significance

• **Z-test results** – Applying one-tailed ('larger') Z-test^[9] on the **Reading & Writing** data:

- **Rejecting null hypothesis** the threshold at which is generally considered safe to reject the null hypothesis is a **p** value of (**p** < 0.05). This means there is a less than 5% chance that the observed data is due to chance.
- Statistically Significant since the p value computed by the Z-test is way smaller than 0.05, we can safely say that the observed mean Reading score being higher than the mean Writing score for Male students is statistically significant.



 $[9] \quad \textbf{Statsmodels ztest fucntion -} \\ \underline{\textbf{https://www.statsmodels.org/dev/generated/statsmodels.stats.weightstats.ztest.html} \\ \\ \textbf{and betates the properties of the prop$

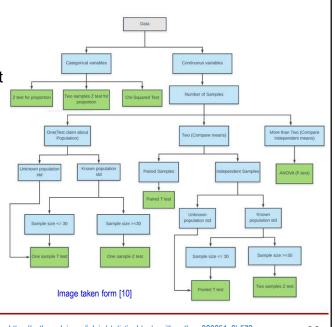
19

19

Confirmatory Analysis

Selecting The Statistical Test

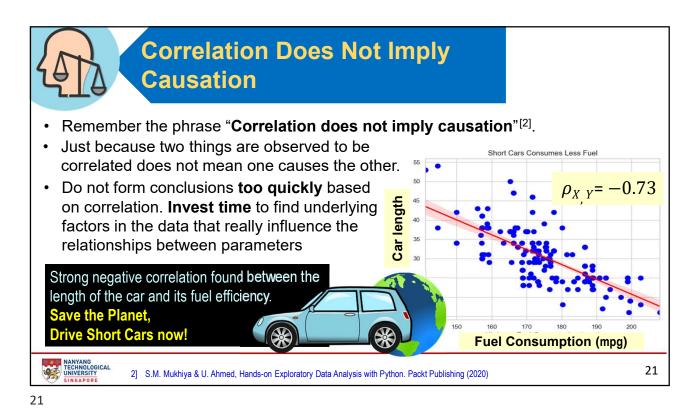
- Selecting an appropriate statistical test for your confirmatory analysis requires consideration of various factors such:
 - Continuous or discrete data.
 - Number of samples to compare.
 - Sample size.
 - Parametric or non-parametric test.
- A helpful flowchart in^[10] shows some statistical tests that can be use based on the nature of the data and test requirements.



NANYANG TECHNOLOGICAL UNIVERSITY SINGAPORE

 $[10] \ \ Jagandeep \ Singh, \ Statistical \ Tests \ with \ Python \ (2020) - \ \underline{https://python.plainenglish.io/statistical-tests-with-python-880251e9b572}$

20



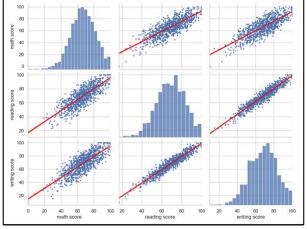
Multivariate Analysis

Analysis of Three or More Variables

• Multivariate analysis allows us to look at the **correlation of three** or **more** variables at a time.

- A common way of visualising multivariate data is to use a matrix of multiple scatter plots.
- The convenient and powerful Seaborn pairplot() function provides this feature^[11].
- Setting the kind parameter to kind='reg' will show the linear regression lines.





Analysing Math, Reading & Writing scores in Student performance.csv

2

Multivariate Analysis Adding In Categorical Variables • An additional categorical variable can be visualised in colours by employing the hue parameter in pairplot()[11]. · By assigning the hue parameter to a specific categorical variable (e.g. hue='gender'), each type in the category is assign a different colour from a default or specified palette. Such multivariate analysis allows interesting relationships and patterns to be observed in the different categorical types. Boys do better in

math than writing

23

Multivariate Analysis

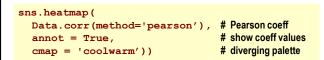
[11] Seaborn pairplot() documentation -

Getting the Correlation Values

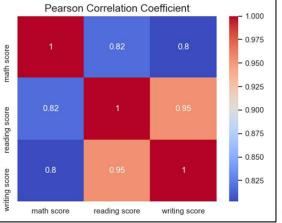
https://seaborn.pydata.org/generated/seaborn.pairplot.html

• Instead of just visualising the correlation, it is often useful to compute a numerical measure for each correlation pair.

• Pandas corr () function and Seaborn's heatmap() can compute and display the pairwise linear (Pearson) correlation coefficients for all the columns in the dataframe with **numerical** values^[12].



[12] Pandas dataframe.corr documentation https://pandas.pydata.org/docs/reference/api/pandas.DataFrame.corr.html



Math, Reading & Writing scores of Female & Male students

Correlation coefficients of Math, Reading & Writing scores 24

Multivariate Analysis

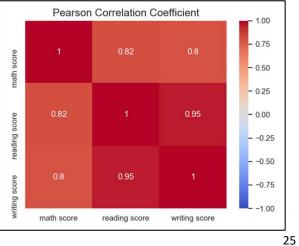
Getting the Correlation Values

• Instead of just visualising the correlation, it is often useful to compute a numerical measure for each correlation pair.

Pandas corr () function and Seaborn's
 heatmap () can compute and display
 the pairwise linear (Pearson) correlation
 coefficients for all the columns in the
 dataframe with numerical values^[12].

```
sns.heatmap(
  Data.corr(method='pearson'),  # Pearson coeff
annot=True,  # show coeff values
vmin=-1, vmax=1,  # min-max scale
cmap='coolwarm'))  # diverging palette
```

[12] Pandas dataframe.corr documentation https://pandas.pydata.org/docs/reference/api/pandas.DataFrame.corr.html



25

Multivariate Analysis

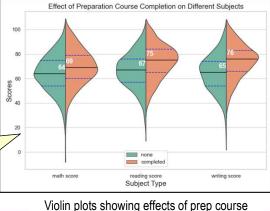
Playing With Many Violins

Multivariate analysis using violin plots allows us to compare the probability

density curve of multiple quantitative variables for a **categorical variable pair**.

 The central lines in the violin plot allow us to compare the median values within the categories (e.g. those who completes test preparation course & those who did not).

 In Seaborn's violinplot(), the hue parameter can be assigned to a categorical variable with two values.
 Setting split=True, then compares them side-by-side. Students do better in all subject when completing test preparation.



Violin plots showing effects of prep course completion on Math, Reading & Writing scores

26

Summary

Exploratory Data Analysis

- · Correlation analysis allows us to visualise relationships within the dataset.
- Data visualisation techniques for this purpose include histogram & kernel density
 plots (univariate), scatter plot (bivariate), box & violin plots (bivariate & multivariate), paired
 plot & heatmap (multivariate).
- Correlation between variable pairs can be quantified using the Pearson correlation coefficient and this values can be effectively visualised using appropriate colour palettes in heatmaps and paired plots.
- Visual observation of relationships and patterns should be confirmed with appropriate statistical analysis based on the nature and number of data distributions being compared.



27

27

References for Correlation Analysis

- [1] Anscombe, F. J. (1973). "Graphs in Statistical Analysis". American Statistician. 27 (1): 17–21
- [2] S.M. Mukhiya & U. Ahmed, Hands-on Exploratory Data Analysis with Python. Packt Publishing (2020)
- [3] Image from Wikipedia, Pearson Correlation Coefficient https://en.wikipedia.org/wiki/Pearson_correlation_coefficient
- [4] Statsmodels Q-Q plot function https://www.statsmodels.org/stable/generated/statsmodels.graphics.gofplots.ggplot.html
- Jason Brownlee, A Gentle Introduction to Normality Tests in Python (2018) https://machinelearningmastery.com/a-gentle-introduction-to-normality-tests-in-python/
- [6] Paras Varshney, Q-Q Plots Explained (2020) https://towardsdatascience.com/q-q-plots-explained-5aa8495426c0
- Yogesh Agrawal, Hypothesis testing in Machine learning using Python (2019) https://towardsdatascience.com/hypothesis-testing-in-machine-learning-using-python-a0dc89e169ce
- [8] Should you use a one-tailed test or a two-tailed test for your data analysis? https://www.statisticssolutions.com/should-you-use-a-one-tailed-test-or-a-two-tailed-test-for-your-data-analysis/
- $[9] \hspace{0.3cm} \textbf{Statsmodels ztest fucntion -} \\ \underline{\textbf{https://www.statsmodels.org/dev/generated/statsmodels.stats.weightstats.ztest.html} \\ \\$
- [10] Jagandeep Singh, Statistical Tests with Python (2020) https://python.plainenglish.io/statistical-tests-with-python-880251e9b572
- [11] Seaborn pairplot() documentation https://seaborn.pydata.org/generated/seaborn.pairplot.html
- [12] Pandas dataframe.corr.documentation https://pandas.pydata.org/docs/reference/api/pandas.DataFrame.corr.html
- [13] Bibor Szabo, How to Create a Seaborn Correlation Heatmap in Python? (2020) https://medium.com/@szabo.bibor/how-to-create-a-seaborn-correlation-heatmap-in-python-834c0686b88e



Note: All online articles were accessed between June to July 2021

28

Acknowledgement

The slides of this lecture is adapted from the course material by Prof. Goh Wooi Boon, NTU.