Discussion ! Floatily point representation; (an-aza, bibz-) = = = ak pk + = bk pk decimal: \$=10 Shang: B=2 octal: B=8 hexadecimal: \$=16 a flooting point number X as In Sinory, define $\chi = \pm q \cdot 2^m$ ge: mantissa, g=(1.t), for normal numbers for subnormal numbers 9=10.+)2 m: exponent 16-6-754 single precision: 1 bit 8 bit 23 bit sign exponent traction IEEE-754 donble precision
1 bit 11 bit 52 bit sign exponent traction

Special cases: Zero: when all exponent and traction bits are 0.00 restriction on the sign bit, so we have to. -0 Infinity: all exponent bits are I, all traction bits are 0, + so and - so are distinguished from sign bit NaN: "not a number" (1 Int Int) - all exponent bits are 1, non-zero traction bits Subnormal numbers; all exponent sits are O. non-zero paction sits. How do we define the exponent? for float precision, what's the range can be presented by 8 bit? smellest: (00000000) = 0 logest: (1111111)2 = 2°+2'+2'+--+27=28-1=255 the exponent is shifted by 127 to avoid storing sign for exponent, as we saw above, (00000000) and (1111111) 2 are reserved for special cases. So the actual range is (1,254), after shifting by 127, the exponent range is (-126, 127)

the largest normal number ~ 2127 ~ 1038 -- Smallest normal -- 2-126 ~/0 for double precision, similar story: Smellest: (00--0)2 = 0 $(c-sest; (11--1)_2 = 2^{(1)}-1 = 2047$ the actual useful range: (1, 2046), shift by 1023 gives exponent range: (-1022, 1023) lagest normal number ~ 2/023 ~ 10307 Smallest normal number ~ 2 -1022 ~ 10-308 Machine epsilon: the distance between I and the next largest floating point number. Single precision: 23th Sit $1 = (+1) \times 2^{\circ} \times (1,0000 - -0)_{2}$ | + Em = (+1) x 2° x (1,0000 --- 1)2 So Em = 2 -25 ~ 10-7 double precision:

$$1 = (+1) \times 2^{\circ} \times (1,0000 - 0)_{2}$$

$$1 = (+1) \times 2^{\circ} \times (1,0000 - 1)_{2}$$

$$50 \quad E_{m} = 2^{-52} - 10^{-16}$$