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**A rhombohedral ferroelectric phase in epitaxially strained Hf0.5Zr0.5O2 thin films**

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**Hafnia-based thin films are a favoured candidate for the integration of robust ferroelectricity at the nanoscale into next- generation memory and logic devices. This is because their ferroelectric polarization becomes more robust as the size is reduced, exposing a type of ferroelectricity whose mechanism still remains to be understood. Thin films with increased crystal quality are therefore needed. We report the epitaxial growth of Hf0.5Zr0.5O2 thin films on (001)-oriented La0.7Sr0.3MnO3/SrTiO3 substrates. The films, which are under epitaxial compressive strain and predominantly (111)-oriented, display large ferroelec-tric polarization values up to 34 μ C cm−2 and do not need wake-up cycling. Structural characterization reveals a rhombohedral phase, different from the commonly reported polar orthorhombic phase. This finding, in conjunction with density functional theory calculations, allows us to propose a compelling model for the formation of the ferroelectric phase. In addition, these results point towards thin films of simple oxides as a vastly unexplored class of nanoscale ferroelectrics.**

F micro/nano-electromechanical systems3. However, miniaturizing ization, and are of great technological interest for a myriad of applications, notably in microelectronics1, spintronics2 and erroelectric materials exhibit switchable spontaneous polar-

ferroelectrics is not an easy task, since depolarization fields become increasingly important at reduced sizes4,5. Searching for robust fer-roelectric properties at the nanoscale has therefore been a recurrent challenge. Thus, the recent discovery of ferroelectricity in ultrathin layers of HfO2-based materials6 represents a real breakthrough in the field, and seems to expose a new type of ferroelectricity: one that appears only at the nanoscale and becomes stronger at smaller dimensions. In addition, silicon compatibility, the simplicity of their chemistry and low toxicity make them very attractive compared to the other commonly used ferroelectric layers.

In bulk, the stable form of HfO2 (ZrO2)-based compounds is a monoclinic phase (*P*21/*c*, m-phase) at room temperature7,8. Other common high-temperature and high-pressure phases, namely, tetragonal (*P*42/*nmc*, t-phase) and cubic ( *Fm m* , c-phase) phases7,8, can be stabilized at room temperature via doping9 or nanostructur-ing10,11. In addition, rhombohedral phases (r-phase) have also been obtained by doping and applying mechanical stress12–15. The t- and r-phases are distortions from the fluorite structure (c-phase) and have a significantly lower volume than the m-phase. None of the above-mentioned phases is reported to be polar.

A polar orthorhombic phase (*Pca*21, o-phase) was first reported for Mg-doped ZrO2 when cooled to cryogenic temperatures16. This polar phase is believed to be the structural origin for the recently reported ferroelectricity in HfO2-based thin films6. Recent litera-ture has gathered examples of these ferroelectric films with dif-ferent dopants17–19, on different substrates (Si (ref. 6) and Y-ZrO2 (ref. 20)), with different electrodes (that is, TiN (ref. 21), Pt (ref. 22), Ir (ref. 23), TaN (ref. 24) and Si (ref. 25)) and by different growth methods (for example, atomic layer deposition (ALD)26, chemical solution

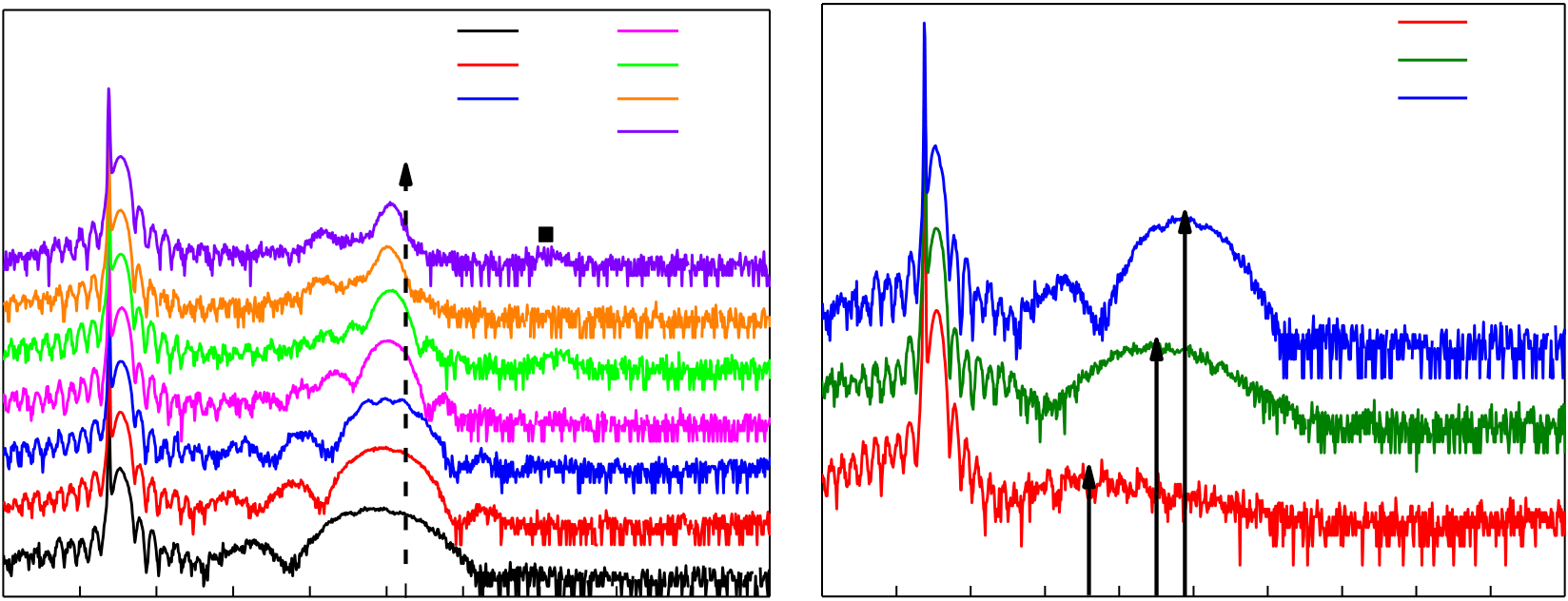
deposition27, pulsed laser deposition (PLD)20 and chemical vapour deposition)28. Various possible mechanisms, such as stress29,30, dop-ing24, confinement by the top electrode21 or surface energy31–33, were put forward as stabilizing factors for the ferroelectric phase.

Initially, the best ferroelectric properties were reported only in ultrathin films (usually around 10 nm thick)26,34,35. The polarization declined significantly with increasing thickness as a result of the nonpolar m-phase appearing35. More recently, ferroelectricity has been found in thicker films (50 to 390 nm)27,36 where the average grain size is below 10 nm. Thus, all reported ferroelectric hafnia-based films have in common that they are formed by small crystal-lites, emphasizing the crucial role played by size effects in stabilizing the ferroelectric phase33. Indeed, it is known that in nanoparticles of radius *r*, the surface energy (*σ*) can produce large internal pres-sures (*P=2σ*/*r*) of the order of gigapascals37,38. Thus, small crystals will prefer the room-temperature stability of lower-volume c- or t- phases to the m-phase39–41. For thicker films, usually above 10 nm (where the crystals have the possibility to grow further), the m-phase (bulk) is always present. The polar o-phase has been postulated as the transformation phase between the t- and m-phases16,24,42.

Most works report on ALD-grown films, which are polycrystal-line and contain multiple phases (m-, t- and o-phases). In addition, the similarity of these structures and the small size of crystallites make a complete structural characterization even more challenging. Therefore, well-oriented samples, preferably in a single phase, are desired to study the factors responsible for ferroelectricity. Single-crystal, epitaxial Y-doped HfO2 films have been achieved by PLD on yttrium oxide-stabilized zirconium oxide substrates with the polar o-phase20, reaching a polarization of 16 μ C cm−2. Here, we also uti-lize PLD to grow highly oriented ferroelectric Hf0.5Zr0.5O2 (HZO) films on a perovskite SrTiO3 (STO) substrate with La0.7Sr0.3MnO3 (LSMO) as a back electrode to gain insights into the role of strain on the ferroelectricity in hafnia-based systems.

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| Articles | | | |  |  |  |  |  | 13 nm | |  |  | STO (001) | | HZO (111) | |  | **Nature Materials** | | | |
| **a** | | | | m (-111) | 30 | o (111) | 4 nm | 36 | **b** | 22 | 32 | 1.5 nm | | | |
| STO (001) | | | |
| 7 nm | 18 nm | | 3 nm | | | |
| 9 nm | 22 nm | | LSMO (001) | | 4 nm | | | |
| LSMO (001) | | | |
| 27 nm | |
| m/t (002) |
| \* |
| Intensity | | | | 28 | 32 | 34 | 38 | 40 | 20 | 24 | 26 | 28 | 30 | 34 | 36 | 38 | 40 |
| 20 | 22 | 24 | 26 |

2*θ*(°) 2*θ*(°)

**Fig. 1 |XRD structural characterization of HZO films on LSMO-buffered 001-oriented StO.a**, Specular XRD pattern of HZO films with thicknesses ranging from 4 nm to 27 nm. **b**, Specular XRD patterns of HZO films with thicknesses ranging from 1.5 nm to 4 nm.

**A rhombohedral phase of HZO**   
X-ray diffraction (XRD) *θ–*2*θ* patterns along the crystal trunca-tion rod of HZO films with different thicknesses are shown in Fig. 1a. The highest peaks mark the (001) specular Bragg reflection of the STO substrate and the epitaxially grown LSMO bottom elec-trode with thickness of ~30 nm; the third largest feature is the main Bragg peak of the HZO films appearing at around 30°. The crys-tal truncation rods are visible in the form of thickness oscillations, which demonstrates the good crystalline quality and interfaces of the films. This *2θ* value is slightly lower than that corresponding to the (111) reflection in the commonly reported polar o-phase in HZO, which appears at around 30.5° as shown by the black dashed line35. This indicates an expanded (111)-spacing (*d*111) in the out-of-plane direction. In particular, extremely thin films below 4 nm (Fig. 1b) display highly elongated unit cells with the (111) reflec-tion appearing at *2θ* well below 30°. As the thickness decreases, the HZO (111) peaks shift rapidly to smaller angles (larger *d*-spacing), which indicates a huge compressive in-plane strain for the thin-nest layers. For films thicker than 9 nm, new peaks appear (at 28.3° and 34°), which can be assigned to the m-phase, consistent with the stabilization of the m-phase with increasing crystal size (while increasing thickness)35.

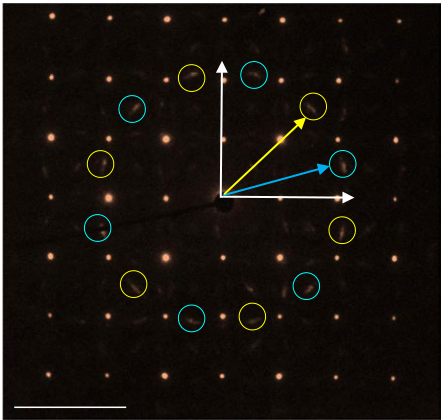
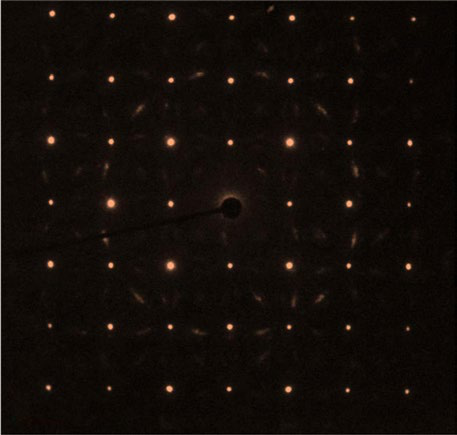
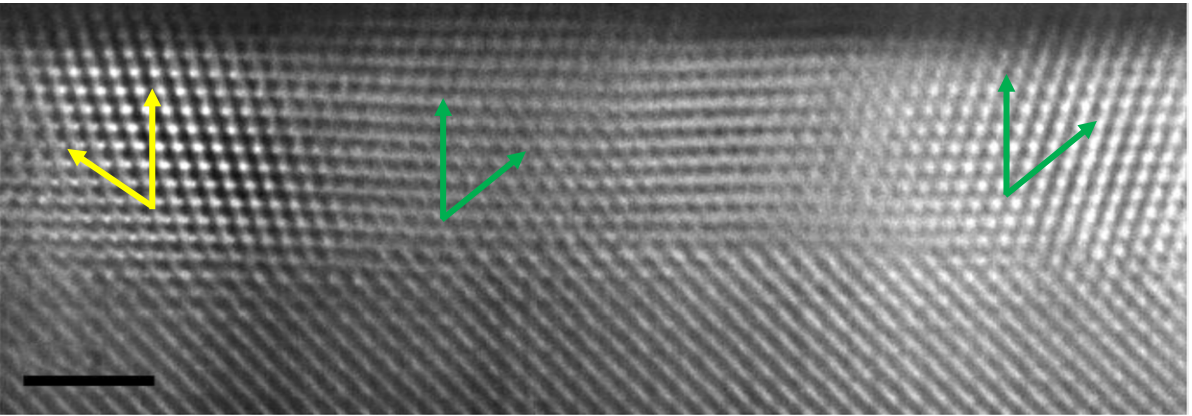
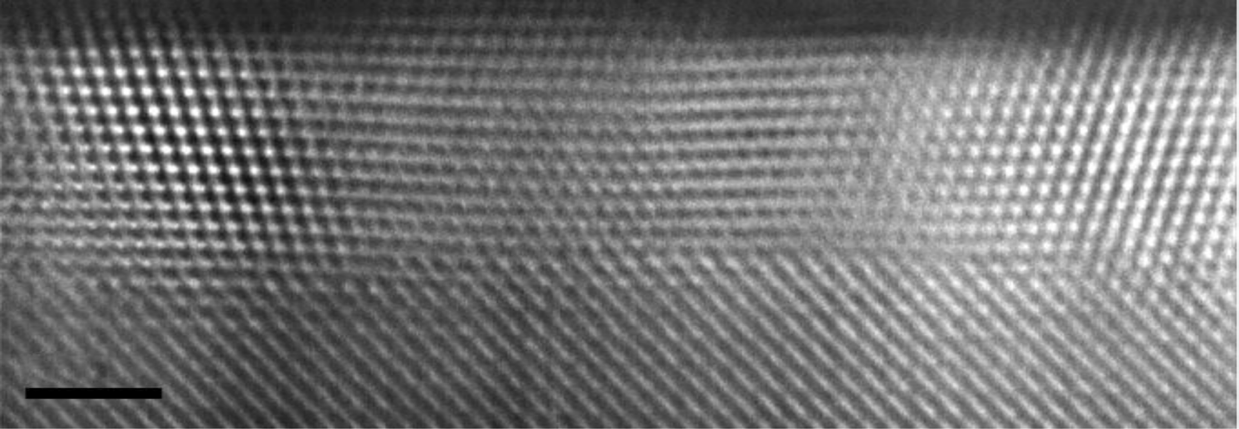
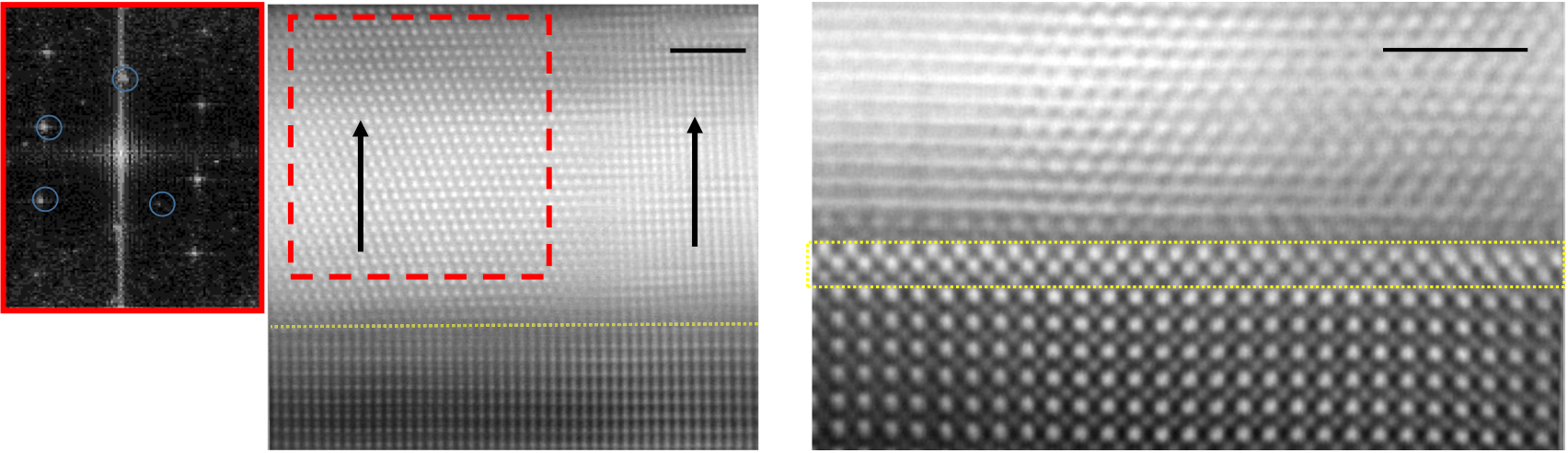
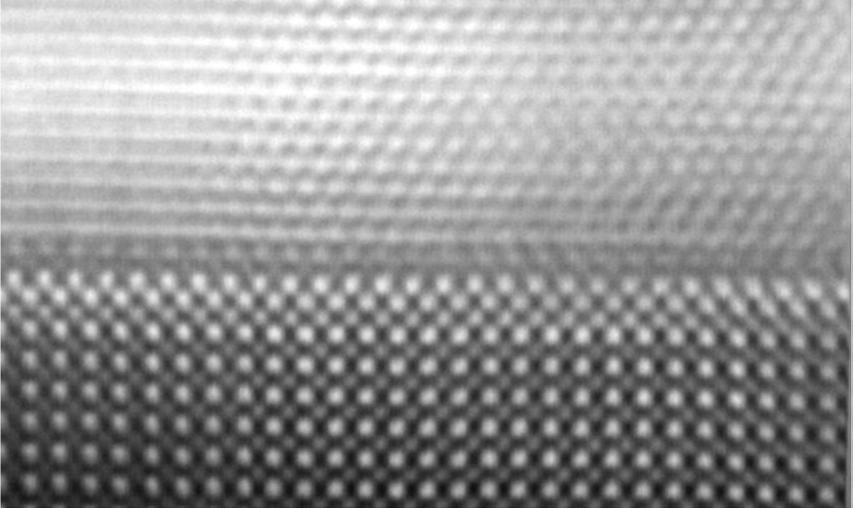
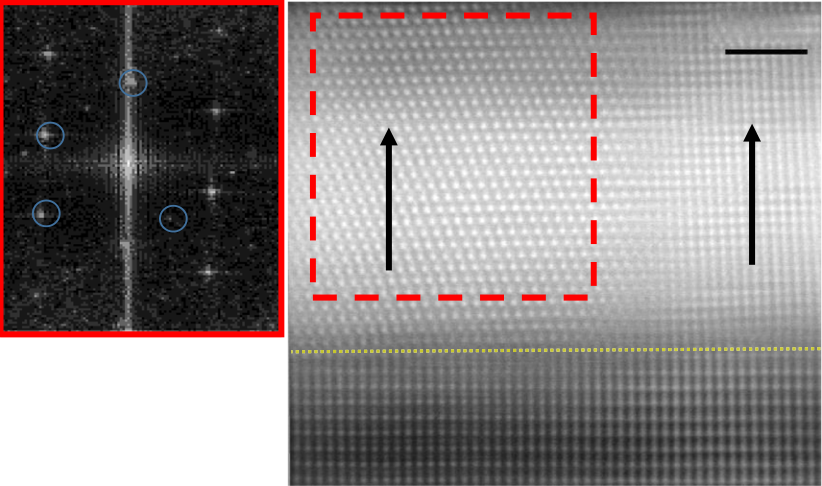
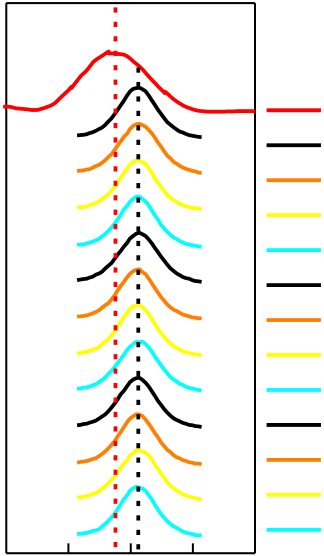
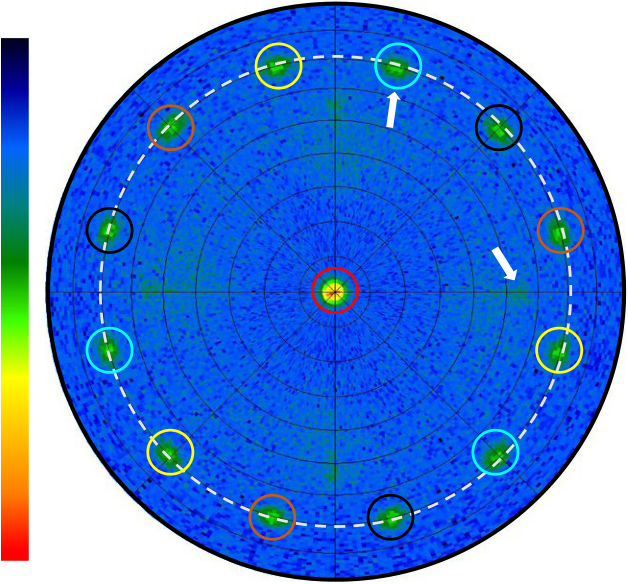
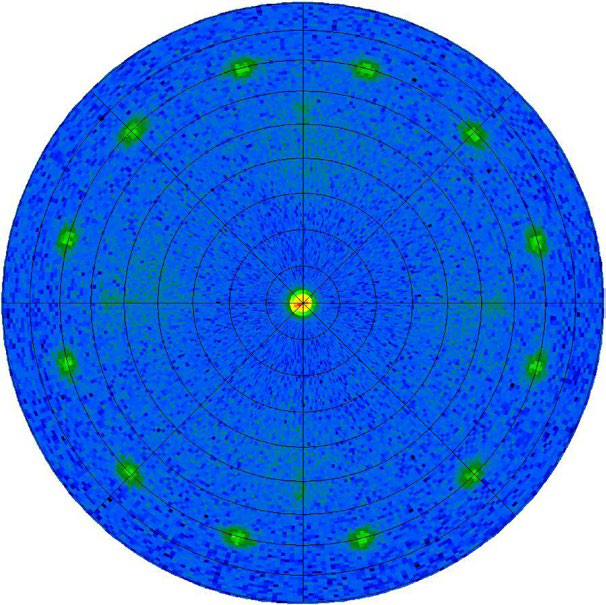
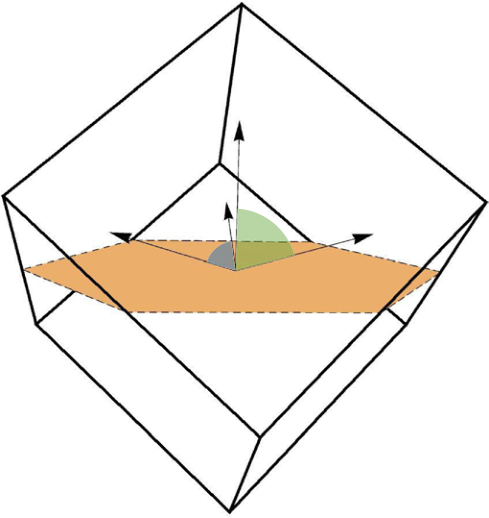
According to the XRD patterns, the films are (111)-oriented (Fig. 1). Pole figure (texture) measurements were performed around the {111} peaks in a 9-nm-thick film. In a (111)-oriented single-domain film, the other three reflections, (-111), (11-1) and (1-11), are expected at an angle (*χ*) of ~71° from the out-of-plane direction, with azimuthal angles (*φ*) differing by 120°. As seen in Fig. 2a, 12 reflections instead of 3 are found at *χ*≈ 71°, revealing four crystal-lographic domains with different but well-defined in-plane orien-tations. The crystal domains are rotated 90° with respect to each other, following the four-fold symmetry of the (001)-oriented cubic substrate. In addition, four weak reflections at *χ*≈ 55° reveal a small amount of (001)-oriented component in the film. Synchrotron XRD was used to scan all 13 reflections in the pole figure, revealing that the 12 peaks with in-plane components of the scattering vector (at *χ*≈ 71°) share the exact same *2θ*= 27.13° (Fig. 2b), giving rise to a *d*-spacing (*d*11–1*=d*1–11*=d*–111*=* 2.94 Å) that is significantly smaller than that of the out-of-plane (111) reflection (*d*111= 2.98 Å). Thus, these measurements reveal a multiplicity that is only consistent with a rhombohedral unit cell (Fig. 2c) and a polar (three-fold) axis out of the plane of the sample.

To gain further understanding of the structure, we performed transmission electron microscopy (TEM) and local spectroscopy studies. Plane-view selected-area electron diffraction (SAED), shown in Fig. 3a for a 9-nm-thick film, displays a superposition of diffraction patterns from at least two domains of HZO. The {220} spots from both domains occur at *φ*= 45° + 60*n* (yellow circles in Fig. 3a) and at *φ*= 15° + 60*n* (blue circles), with *n* being an integer from 0 to 5 (the *φ*= 0° direction is defined as the [100]STO direction). HZO domains rotated 180° about the [111]HZO (// [001]STO) direc-tion give identical plane-view diffraction patterns ({220} spots with *d*220= 1.79 Å in Fig. 3a). Thus, the SAED results are consistent with the existence of four domains rotated by 90° from each other around [111]HZO as is independently revealed by X-ray pole figure analysis in Fig. 2a. Furthermore, an epitaxial relation between the substrate and the film with [1-10]HZO//[1-10]STO, and [11-2]HZO//[110]STO, can be clearly identified.

Next, we performed cross-sectional high-angle annular dark-field scanning TEM (HAADF-STEM) analyses on 4-nm- and 9-nm-thick films, along zone axes defined by *φ*= 0° ([100]STO), *φ*= 15° and *φ*= 45° ([110]STO). Figure 3b displays a HAADF-STEM image from a 9-nm-thick sample (zone axis, *φ*= 45°), clearly show-ing the coexistence of majority and minority HZO domains with the [111]HZO and [001]HZO out-of-plane, respectively, in agree-ment with the XRD data. From the fast Fourier transform (inset, Fig. 3b) across many images, we deduce that *d*111= 2.95–3.01 Å and *d*11–1= 2.92–2.96 Å. These values (*d*111≠*d*11–1) provide a clear confirmation of the non-orthorhombic nature of this phase (see Supplementary Fig. 1 for analysis based on forbidden spots) and support the rhombohedral phase revealed by the synchrotron XRD measurements (Fig. 2b). Figure 3c displays a HAADF-STEM image from a 4-nm-thick sample (zone axis, *φ*= 15°), where we observe the coexistence of different (111)-oriented domains. Notably, (001)-oriented areas are only rarely found at these low thicknesses (see Supplementary Fig. 2).

We analysed the chemistry and structure of the interface between HZO and LSMO through energy-dispersive spectroscopy (EDS) performed in conjunction with HAADF-STEM. Comparison of the EDS chemical maps with the HAADF-STEM image (zone axis, *φ*= 0°) reveals the presence, at the interface with LSMO, of 2–3 monolayers of HZO that are in a different phase to the rest of the HZO film (Supplementary Fig. 3). This interfacial HZO phase is completely strained to the substrate (*a*= 3.91 Å), which corresponds

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| **a** | *φ* = 90° | 45° | **b** | 26.75° | 27.13° | **c** |  |

Out-of-plane

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| 10 | *χ* ∼ 71° | *χ* ∼ 55° | 0° | 25 | 26 | 27 | 28 | 29 | *φ* = –165°*φ* = –135°*φ* = –105°*φ* = –75° *φ* = –45° *φ* = –15° *φ* = 15° *φ* = 45° *φ* = 75° *φ* = 105° *φ* = 135° *φ* = 165° | [11-1] | [-111] | [111] | [1-11] |
| 102 | ∼71° |
| 120° |
| 103 |

2*θ* (°)

**Fig. 2 |Domain configuration and symmetry.a**, Pole figure around the (111) peak of a 9 nm HZO film at 2*θ*= 29.98°. The radial direction represents *χ*, which ranges between 0° and 90°, while the azimuthal direction represents *φ*, with a (0°–360°) range. Colour represents intensity in log scale (left).

**b**, 2*θ* scans of the 13 peaks in the pole figure measured at the P08 High-Resolution Diffraction Beamline in PETRA III (DESY) with a wavelength of *λ*= 1.378 Å. **c**, Sketch of the proposed rhombohedral structure of the HZO film with polarization along the [111] direction.

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| **a** | STO[010] | *φ* = 45° | **c** | [11-1] | [111] | [111] | [11-1] | [111] | [11-1] |
| *φ* = 15° |

[100]

*φ* = 0°

|  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- |
| **b** | 5 nm–1 | 111 | HZO {220} | 2 nm | 2 nm | **d** | LSMO (*φ*= 15°) | 2 nm |
| 11-1 | [111] | [001] |
| 002 | 110 |

LSMO (*φ*= 0°)

LSMO (*φ*= 45°)

**Fig. 3 |Electron microscopy characterization.a**, Plane-view SAED pattern from a 9-nm-thick HZO sample. The out-of-plane direction is [111] (zone axis).

The {220} spots (*d*220= 1.79 Å), corresponding to at least two different domains (yellow and blue circles, respectively) rotated by 90° with respect to each other, can be clearly identified. **b**, Cross-sectional HAADF-STEM image (corrected for sample drift) of the 9-nm-thick HZO film, observed along the [110]

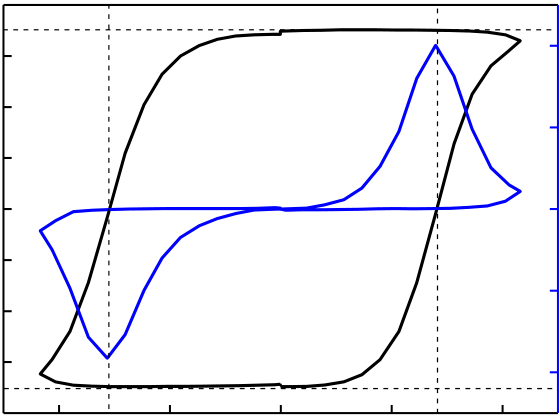
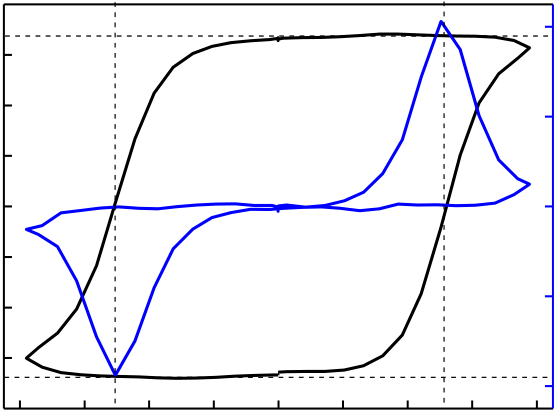
zone of the substrate (*φ*= 45°). Inset (left): Fourier transform of the [111] domain. **c**, Representative cross-sectional HAADF-STEM image (drift-corrected) of a 4-nm-thick film, observed along the zone axis defined by *φ*= 15°. **d**, HAADF-STEM image observed along STO [100], revealing a clear interfacial t-phase of HZO (see EDX in Supplementary Fig. 3).

to a huge (~8%) in-plane tensile-strained t-phase (*a*= 3.60 Å in the unstrained t-phase), as shown in Fig. 3d (see also Supplementary Fig. 3c for HAADF simulations). This in-plane tensile strain results in a much lower out-of-plane parameter measured as *c*/2 = 2.31–2.44 Å (across several images), compared to the unstrained t-phase (*c*= 5.12 Å). An interfacial t-phase has previously been observed in ALD-synthesized doped-HfO2 samples with TiN electrodes43, and also on epitaxially strained Y-doped ZrO2 films grown on STO44. After the above-mentioned two atomic layers at the interface, the r-phase grows under compressive strain. With increasing thickness,

the m-phase in the [001]-orientation appears (Supplementary Fig. 4), also in agreement with the XRD data.

**Ferroelectricity of rhombohedral HZO**   
To test the ferroelectric behaviour of the films, we obtained polariza-tion versus voltage (*P*–*V*) loops through positive up negative down (PUND) measurements (Supplementary Fig. 5). Bistable switch-ing and hysteresis loops can be observed in Fig. 4 for 5-nm- and 9-nm-thick films. After subtracting the non-ferroelectric switching contribution, the blue lines show only the ferroelectric switching

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| Articles |  |  |  | *d* = 5 nm | | | | |  |  |  |  |  |  | *d* = 9 nm | | | **Nature Materials** |
| Polarization (µC cm–2) | 40 | –8 | –6 | 6 | 8 | 0.8 | Polarization (µC cm–2) | 20 | –4 | 10 |
| 30 | 15 |
| 20 | *A* = 10 × 10 µm2 *P*r = 34 µC cm–2 | | | | | 0.4 | 10 | *A* = 50 × 50 µm2 *P*r = 18 µC cm–2 | | | 5 |
| 10 | 5 |
| 0 | –4 | –2 | 0 | 2 | 4 | 0.0 | 0 | –2 | 0 | 2 | 0 |
| –10 | –5 |
| –0.4 | –5 |
| –20 | –10 |
| –30 | –0.8 | –15 | –10 |
| –40 | –20 |
| 4 |
| Electrical field (MV cm–1) | | | | | Electrical field (MV cm–1) | | |

**Fig. 4 |Ferroelectric characterization.** PUND measurements (see Supplementary Information) of 5-nm-thick (left) and 9-nm-thick (right) films under an electric field of frequency 1 kHz are shown. The blue lines are the current (*I*) versus voltage (*V*) curves after extracting the non-ferroelectric switching response; the black lines are the integrated signal giving rise to the corresponding *P*–*V* hysteresis loops.

current with coercive field, *E*c, around 5 MV cm−1 and 3 MV cm−1, respectively, consistent with the expected dependence of *E*c on thickness (*d*) as *E*c∝*d*−2/3. The coercive fields are larger than the 1 MV cm−1 reported in ALD-grown films21. This could be due to the dead layers at the interface with the LSMO electrodes, as discussed previously, and/or the clamping effect from the strained epitaxial film. However, the coercive field itself does not increase on cycling (see Supplementary Fig. 6).

The largest remanent polarization (*P*r) values among all doped-hafnia compositions have been obtained in La-doped and Gd-doped HfO2 films17,24. The highest reported *P*r in the HZO is 26 μ C cm−2 (with switching polarization of 45 μ C cm−2), using a TiN capping layer of at least 90 nm21. In our 5-nm-thick HZO films, *P*r also reaches record values of around 34 μ C cm−2 (*P*r= 50 μ C cm−2 before subtracting the non-ferroelectric switching contribution, as seen in Supplementary Fig. 7)20 compared to other epitaxial PLD. These values are large even when compared with very good con-ventional perovskites, such as unstrained BaTiO3 (ref. 45). However, for the thicker 9 nm film, *P*r drops to 18 μ C cm−2. This finding can be rationalized by our TEM observations showing that the minority (001)-oriented domains (Fig. 3b) and m-phase (non-ferroelectric), which are absent or very rarely found in the thinnest sample, gradu-ally appear with increasing thickness (Supplementary Fig. 4). It is interesting to note that the ferroelectric loops are obtained readily after growth (see Supplementary Fig. 6), without the technologically inconvenient wake-up cycling required for other HZO systems46,47, indicating that the ferroelectric rhombohedral phase is stabilized by compressive epitaxial strain.

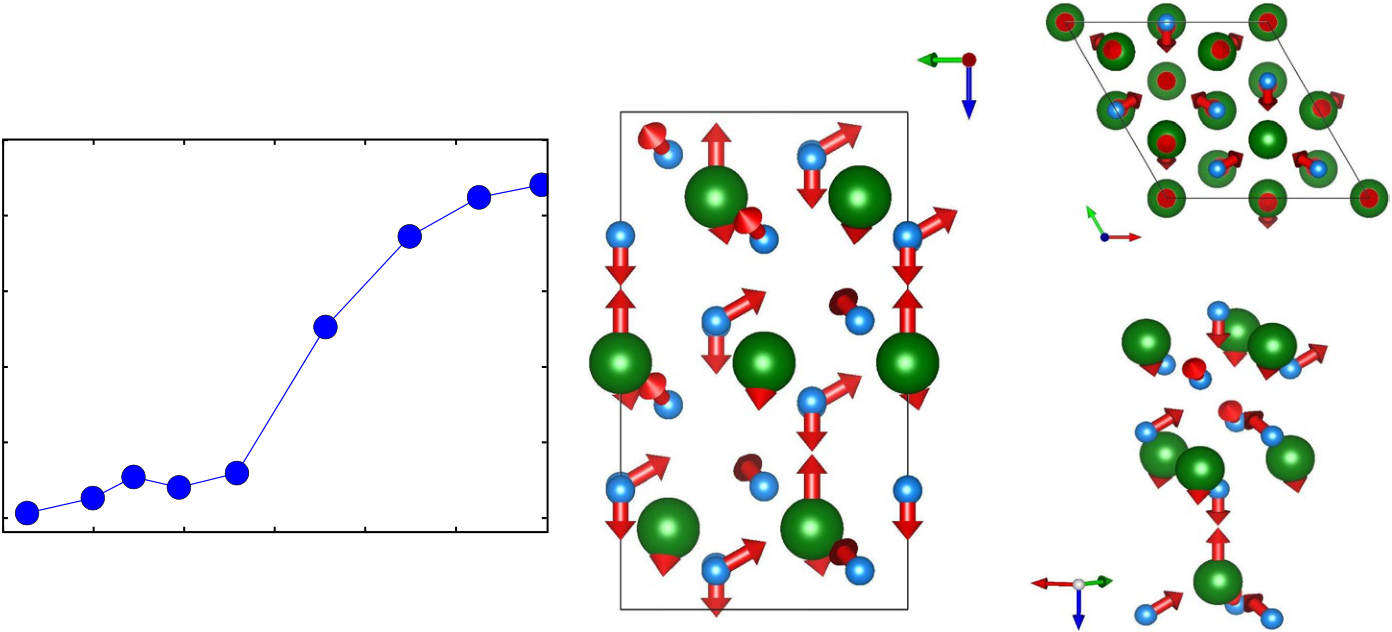
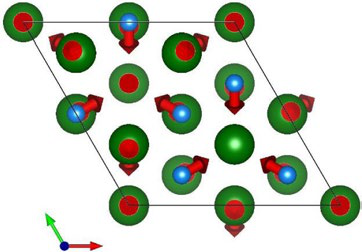
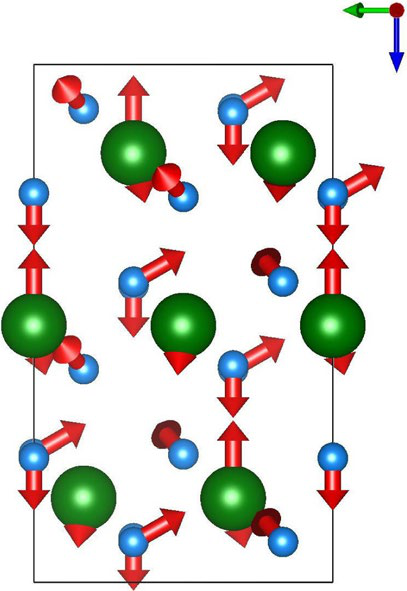
**Density functional theory calculations**   
Finally, we resorted to first-principles simulations to try to identify the rhombohedral HZO phase observed in our films. Since we are not aware of any previous report on a polar rhombohedral poly-morph of HZO, we ran a blind search for (meta)stable structures, using the genetic-algorithm approach implemented in USPEX48–50. For this we employed standard first-principles methods, based on density functional theory, and a simulation supercell of 12 atoms (see Methods for details). We ran our search for pure HfO2 and pure ZrO2 compositions in bulk-like conditions. We obtained in both cases an *R*3*m* structure with a small polarization of the order of 0.1 μ C cm−2. Furthermore, for the HfO2 composition we also found a second polymorph with *R*3 symmetry and a polarization of 41 μ C cm−2. These rhombohedral phases lie above the *P*21/*c* bulk ground state that is usually discussed in the literature on HfO2, which explains why they have not been previously reported or observed. More precisely, from our calculations we obtain *E*(*R*3*m*) −*E*(*P*21/*c*) = 158 meV f.u.−1 and *E*(*R*3) −*E*(*P*21/*c*) = 195 meV f.u.−1 for HfO2. Note that the polar *Pca*21 phase of hafnia discussed in the literature is

also more stable than these rhombohedral polymorphs, as we obtain *E*(*Pca*21) −*E*(*P*21/*c*) = 64 meV f.u.−1 (in agreement with ref. 31, which reports 62 meV f.u.−1 for this energy gap). More details on these structures are provided as Supplementary Information.

We then considered these two rhombohedral structures with the HZO composition, discovering that on substitution of Hf by Zr, the *R*3 phase loses its stability in favour of the weakly polar *R*3*m* polymorph. We studied several Hf–Zr arrangements compatible with the three-fold symmetry, and observed that the *R*3 destabiliza-tion occurs in all cases. The *R*3*m* phase of bulk-like HZO is char-acterized by *d*111≈ 2.94 Å and *P*≈ 1 μ C cm−2. Then, we examined the effect of epitaxial compression by running simulations for a number of fixed values of the lattice constants in the (111) plane of the HZO *R*3*m* structure, allowing for the relaxation of atoms and the out-of-plane lattice vector. As shown in Fig. 5a, for an epitaxial compres-sion corresponding to an out-of-plane *d*111≈ 3.25 Å, we observe a clear structural transition to a phase that retains the *R*3*m* symmetry but is strongly polar, with *P*≈ 15 μ C cm−2. This *d*111 value is within the range of what we observe in our thinnest HZO films (for our films with thickness between 1.5 nm and 9 nm, we estimate *d*111 val-ues ranging between ~3.27 Å and 2.98 Å, respectively, from the XRD measurements in Fig. 1b). A definitive comparison between theory and experiment is not yet possible because of possible phase coex-istence in our films as they become thicker. Nevertheless, although our computational models do not include effects (crystallite size; surfaces and interfaces; local deviations from the average composi-tion) that could help to stabilize particular phases, our results do suggest that our predicted *R*3*m* phase under epitaxial compression (Fig. 5b–d), and even the *R*3 polymorph predicted in the Hf-rich limit, may be approximate representations of the rhombohedral structure in our actual samples (Supplementary Fig. 8).

**Strain and nanoparticle pressure stabilize ferroelectricity** In general, we can expect epitaxial strain to lower the symmetry of the films. Thus, obtaining a rhombohedral unit cell under isotro-pic epitaxial strain would imply an initially cubic or rhombohedral crystallite. The present results therefore allow us to propose a model for the formation of the as-grown ferroelectric phase reported here, as follows. PLD growth of the thin films at high temperature enables the in situ crystallization of HZO. As previously proposed for hafnia-based ferroelectrics, the small particle sizes induce the formation of low-volume fluorite-like phases (either tetragonal or cubic)39–41. A plane-view bright-field TEM image (Supplementary Fig. 9) from a 9 nm HZO film shows an average grain size of ~10 nm. Our exper-iments strongly suggest that in the initial stages of the growth, after the formation of a fully coherent, atomically thin interfacial layer, the internal pressure due to the small particle size favours the undis-torted cubic phase. As established by Demkov and Navrotsky51, the

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|  |  |
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**c**

*b*

|  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- |
| **a** | 25 | **b** | *c* | **d** | *b* | *a* |
| Polarization (µC cm–2) | 20 |
| 15 |
| 10 |
| 5 |

0

|  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- |
| 2.9 | 3.0 | 3.1 | 3.2 | 3.3 | 3.4 | 3.5 | *a* | *b* |
| *d*111 (Å) |

*c*

**Fig. 5 |theoretical calculations and proposed structure.a**, Computed polarization of the *R*3*m* phase of HZO as a function of *d*111. Note that we simulate epitaxial strain, and thus control *d*111, as described in the text, where larger *d*111 values correspond to smaller in-plane lattice constants. **b**,**c**, Two views of the *R*3*m* phase obtained for epitaxially compressed HZO and HfO2. Green (cyan) spheres represent Hf/Zr (O) atoms. The arrows show the polar distortion with respect to a reference paraelectric structure with *R m* symmetry, which we deduce by appropriately symmetrizing the *R*3*m* state. **d**, Detailed view of the Hf/Zr–O groups that characterize the *R*3*m* structure, allowing the main polar displacements, and how they preserve the three-fold axis, to be more easily appreciated.

(111) crystal face of ZrO2 and HfO2 is energetically favourable, so cubic crystallites growing with that orientation are expected. Due to the favourable epitaxial relationships induced by the STO/LSMO stack (see Fig. 3a), the growing crystallites are subjected to a large epitaxial compressive strain that elongates the cubic unit cell along the out-of-plane [111] direction, inducing rhombohedral symmetry with a polar unit cell (as shown by the synchrotron XRD and fer-roelectric characterization).

Increasing the thickness allows the crystal size to grow, reliev-ing the internal pressure, thus favouring the monoclinic bulk struc-ture. At the same time, the presence of the secondary m-phase also helps to release the elastic energy of the compressively strained structure. Even though XRD shows only traces of the m-phase for thicknesses above ~10 nm, the TEM analysis shows that monoclinic (001)-oriented crystallites are already present in the 9-nm-thick film (Supplementary Fig. 4).

While the stabilization of a high-lying rhombohedral poly-morph of HZO may seem surprising, similar achievements have been accomplished for other ferroelectric thin films (for example, the super-tetragonal phase of perovskite oxide BiFeO3 on compres-sive substrates52). Moreover, the polymorphic character of HfO2 and ZrO2 should facilitate the stabilization of unconventional structures under epitaxial constraints. The evolution of the polarization with the epitaxial constraint reported here (Fig. 5 and Supplementary Fig. 10) mimics the behaviour that is typical among ferroelectric perovskite oxides53,54, suggesting that the connections between these two families should be further explored.

**Outlook**   
We show that strain engineering can be used in very thin films of HZO to induce a ferroelectric rhombohedral phase, with a large *P*r of 34 μ C cm−2. Further work is required to tackle issues associated with the strain requisite, such as larger coercive fields or more com-plex integration in three-dimensional architectures. The insights gained in this work provide the missing clues in the understanding of robust ferroelectricity in thin hafnia-based systems, and also help to overcome one of the main issues for their device utilization: the wake-up cycling. Our theoretical calculations predict an even larger polarization for the rhombohedral phases of Hf-rich compositions, and comparable values for epitaxially compressed HZO struc-tures. In addition, this work suggests a pathway to generate large

ferroelectric polarization in nanocrystallites of simple oxides, whose rich phase diagrams include cubic, tetragonal and rhombohedral phases, and in particular in materials with a clear preference for one specific crystal orientation. These highly oriented cubic phases can be stabilized during growth and deformed into a polar structure via epitaxial strain. Furthermore, the highly epitaxial growth of ultra-thin ferroelectric hafnia-based films on LSMO has great potential for multiferroic tunnel junctions.

**Online content**   
Any methods, additional references, Nature Research reporting summaries, source data, statements of dat[a availability and asso-ciated accession c](https://doi.org/10.1038/s41563-018-0196-0)odes are available at [https://doi.org/10.1038/ s41563-018-0196-0](https://doi.org/10.1038/s41563-018-0196-0).

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**Author contributions**   
B.N. and Y.W. conceived the idea, and the project plan. Y.W. synthesized the films. P.N.

and J.M. prepared samples for TEM, and performed the experiments, and P.N. analysed the data, under the supervision of B.J.K. and B.D. Y.W., M.S. and B.N. performed XRD and analysed the data. Y.W., S.M. and G.A. fabricated devices, tested their ferroelectric properties and analysed the data with help from A.S.E. H.J.Z. and J.Í. performed the first-principles calculations. B.J.K. and G.R.B. extensively helped in understanding the structure and symmetry of the films. P.L. and B.D. provided useful insights all along the project.

Y.W., P.N., B.N. and J.Í. co-wrote the manuscript with feedback from all of the authors.

**Competing interests**   
The authors declare no competing interests.

**Additional information**   
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**Methods**   
**Thin-film synthesis.** Thin films of HZO with thicknesses in the range of 1.5–27 nm were grown by PLD on LSMO-buffered (001)-STO substrates. A KrF excimer laser with a wavelength of 248 nm was used to ablate polycrystalline targets of LSMO (purchased from PI-KEM, as the bottom electrode) and sequentially, HZO (home-made). LSMO was deposited using a laser fluence of 1 J cm−2 and a laser frequency of 1 Hz under a 0.15 mbar oxygen atmosphere and a substrate temperature of 775 °C. A ceramic HZO target (monoclinic *P*21/*c* phase) was synthesized at   
1,400 °C by solid-state reaction, starting from HfO2 (99% purity) and ZrO2   
(99.5% purity) powders. A fluence of 1.1 J cm−2 and repetition rate of 2 Hz was employed to grow the HZO films. The deposition was performed in an oxygen pressure of 0.1 mbar while keeping the substrates at a temperature of 800 °C.

After deposition, the film was cooled down to room temperature at a rate of 5 °C min−1 under an oxygen pressure of 300 mbar.

**X-ray structural characterization.** The structure and orientation of the films was characterized by XRD, using a Panalytical X’pert Pro diffractometer operating in two modes: using the line focus of the incident beam for high-resolution *θ–2θ* specular scans, which provide the lattice parameters; and using the point focus of the incident beam, for high-intensity/medium-resolution measurements of pole figures, which involve scanning *φ* (azimuthal angle) and *χ* (tilt of the sample plane around the incident beam direction) while the detector is fixed at a particular Bragg reflection. Synchrotron diffraction measurements were performed at the P08 High Resolution Diffraction Beamline in PETRA III, with a wavelength of *λ*= 1.378 Å, using a Kohzu six-circle diffractometer and a two-dimensional Pilatus 100k detector.

**Electron microscopy and EDS.** Cross-sectional and plan-view specimens for electron microscopy were prepared via the standard procedure of mechanical grinding and polishing the samples down to 100 μ m, and dimpling (Gatan) followed by ion milling (PIPS II) to electron transparency. Some cross-sections were also prepared via the focused ion beam (Helios 660 ThermoFischer Scientific) technique, and both preparations yielded similar results. Electron microscopy and EDS were performed on a Titan G2, Cs-corrected TEM equipped with an extreme field-emission gun and a Super X EDS system with four solid-state detectors placed symmetrically along the optical axes. Atomic-resolution imaging was performed in the HAADF-STEM mode, where the intensity in the image is ~*Z*2, thus yielding a clear atomic number contrast. Images were analysed using ImageJ, TIA-ES Vision and Digital micrograph. EDS was performed simultaneously with image acquisition in the HAADF-STEM mode. Chemical maps were acquired for 30 min with conditions optimized and collected at thousands of X-ray photons per second, and analysed using Bruker e-spirit software.

**Electrical measurements.** LSMO top electrodes were deposited by PLD with the same growth condition as the bottom LSMO electrodes, as described in the `Thin-film synthesis’ section. LSMO top-electrode pads with different sizes were processed by physical etching (ion milling). Planar LSMO/HZO/LSMO capacitors were measured using a ferroelectric tester (AiXACCT, TF analyser 2000). The ferroelectric response of the films was tested via PUND55 measurements, which are able to separate switching currents from other contributions.

**Simulation methods.** For our structural predictions, we used the USPEX code48–50, which is based on genetic algorithms. We applied this method to search for possible rhombohedral phases of HfO2 and ZrO2 in bulk-like conditions. We considered 12-atom cells for HfO2 and ZrO2. After the blind structural search, we ran additional first-principles simulations for HfO2, ZrO2 and HZO compositions focusing on the discovered *R*3 and *R*3*m* phases. For the HZO composition, we considered several representative Hf/Zr arrangements that preserve the three-fold rotation axis, using a 72-atom cell.

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Our first-principles simulations were carried out using the VASP (Vienna Ab initio Simulation Package) code56,57. We used the PBEsol approximation to density functional theory58. Atomic cores were treated within the projector-augmented wave approach59, and we solved explicitly for the following electrons: 5*p*, 6*s* and 5*d* for Hf; 4*s*, 4*p*, 5*s* and 5*d* electrons for Zr; and 2*s* and 2*p* electrons for O. We represented the electronic wavefunctions in a plane-wave basis, cutoff at 500 eV.

For the ground state of the bulk HfO2 (*P*21/*c*) with lattice parameters (*a*, *b*, *c*) of about (5.1, 5.2, 5.2) Å, a mesh of 8 × 8 × 8 k-points was used for Brillouin zone integrations; similarly dense grids were used in all other simulations in this work.

When doing the structural relaxation, the calculations were stopped for residual forces below 0.005 eV A−1. To simulate the effect of epitaxial strain, we used a hexagonal-like cell with in-plane lattice vectors forming an angle of 120o, and the third lattice vector perpendicular to the plane. The in-plane vectors were fixed at a series of values, smaller ones corresponding to stronger in-plane compression; then the out-of-plane vector, and the atomic positions, were relaxed.

We tested the influence of the density functional in our results by solving selected structures (for the predicted polar rhombohedral phase) using the local-density approximation (LDA). As shown in Supplementary Fig. 10, the comparison between PBEsol and LDA results reflects the well-known LDA over-binding problem (that is, slight underestimation of lattice constants and cell volumes); otherwise, our results and conclusions are the same irrespective of the functional employed.

We made extensive use of crystallographic servers60–62 and the VESTA63   
visualization program. We computed polarizations by comparing the polar   
structures with properly symmetrized, paraelectric states that we use as a reference.

Initially we used the Berry phase formalism to compute the polarization from first principles64, and acquired essentially identical results to those obtained by computing the total dipole based on nominal ionic charges; hence, we used the latter method for most of our later calculations.

**Data availability**   
The data that support the findings of this study are included in the main text and Supplementary Information.

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