
ImpedanceFitter Documentation

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CONTENTS:

1	Main module	1
1.1	How it works	1
1.2	constants.yaml (or alternatively as input dict)	1
1.3	cole_cole_input.yaml	2
1.4	single_shell_input.yaml	2
1.5	double_shell_input.yaml	3
1.6	possible values	3
2	Utilitites	7
3	Cole-cole model	9
4	Single Shell model	11
5	Double Shell model	13
6	Post processing	15
7	Indices and tables	17
	Python Module Index	19
	Index	21

MAIN MODULE

1.1 How it works

The script will cycle through all .TXT and .xlsx files in a selected directory and fit those files to a selected model. You can exclude certain files by using the excludeEnding flag.

The first possible step is to compensate the electrode polarization of the experiment by fitting the data to a cole-cole-model. After this fit it will fit the data to a selected model, this can either be the Double Shell model or the Single Shell model. If there is no electrode polarization to compensate for, you can also skip this. See *impedancefitter.main.Fitter.main()*

After the fit to one of the models has finished, the calculated values get written into the 'outfile.yaml' in the data-directory.

The following parameters need to be provided in yaml-files:

1.2 constants.yaml (or alternatively as input dict)

Parameter	Name in Script	Description
c_0	c0	air capacitance
c_f	cf	stray capacitance
p	p	volume fraction of cells
ε_{cp}	ecp	permittivity of cytoplasm
d_m	dm	membrane thickness
R_c	Rc	outer cell radius
only double shell model		
R_n	Rn	outer Radius of the nucleus
d_n	dn	thickness of the nuclear envelope
ε_{np}	enp	permittivity of nucleoplasm

Exemplary file:

```
c0 : 3.9e-13      # air capacitance
cf : 2.42532194241202e-13  # stray capacitance

Rc : 5.8e-6      # unit(m). cell radius in buffer, this should be changed according to_
↳the chosed cell line
dm : 7.e-9      # thickness of cell membrane m
ecp : 60        # permittivity for cytoplasm
p : 0.075
```

```
Rn : 0.8 * constants['Rc'] # radius of nucleus
dn : 40.e-9 # thickness of nuclear membrane
enp : 120 # Permittivity for nucleoplasm
```

1.3 cole_cole_input.yaml

Parameter	Name in Script	Description	Physical Boundaries
k	k	constant phase element parameter	has to be non 0, otherwise the function wil throw NAN or quit(1/k in the formula)
α	alpha	constant phase element exponent	$0 < \alpha < 1$
ε_l	epsi_l	low frequency permittivity	$el \geq 1$
ε_h	eh	high frequency permittivity	$eh \geq 1$
τ	tau	relaxation time	$\tau > 0$
a	a	exponent in formula for ε^*	$0 < a < 1$
σ	conductivity	low frequency conductivity	$\sigma > 0$

Exemplary file:

```
k: {value: 1.5e-7, min: 1.e-7, max: 1.e-2, vary: True}
epsi_l: {value: 1000, min: 200, max: 3000, vary: True}
tau: {value: 5.e-7, min: 1.e-8, max: 1.e-3, vary: True}
a: {value: 0.9, min: 0.8, max: 1.0, vary: True}
alpha : {value: 0.3, min: 0., max: .5, vary: True}
conductivity : {value: 0.05, min: 0.05, max: 0.2, vary: True}
eh : {value: 78., min: 60., max: 85., vary: True}
```

With the *vary* flag, one can choose whether a variable should be included in the fitting procedure or fixed.

1.4 single_shell_input.yaml

Parameter	Name in Script	Description	Physical Boundaries
σ_m	km	conductivity of the membrane	$\sigma_m > 0$
ε_m	em	pemitivity of the membrane	$\varepsilon_m \geq 1$
σ_{cp}	kcp	conductivity of the cytoplasm	$\sigma_{cp} > 0$
σ_{med}	kmed	conductivity of the supernatant($\varepsilon_{med} = \varepsilon_h$ from cole cole fit)	$\sigma_{med} > 0$

Exemplary file:

```
km: {value: 1.e-8, min: 1.e-12, max: 1e-2, vary: True}
em: {value: 11, min: 1., max: 50., vary: True}
kcp: {value: 0.4, min: 0.1, max: 2., vary: True}
kmed: {value: 0.15, min: 0.0001, max: 1.0, vary: True}
```

With the *vary* flag, one can choose whether a variable should be included in the fitting procedure or fixed.

Note:

If you run without electrode polarization, you must include a line for emed as here:

```
emed: {value: 78, min: 70, max: 80, vary: True}
```

1.5 double_shell_input.yaml

Parameter	Name in Script	Description	Physical Boundaries
σ_m	km	conductivity of the membrane	$\sigma_m > 0$
ε_m	em	permittivity of the membrane	$\varepsilon_m \geq 1$
σ_{cp}	kcp	conductivity of the cytoplasm	$\sigma_{cp} > 0$
ε_{ne}	ene	permittivity of the nuclear envelope	$\varepsilon_{ne} \geq 1$
σ_{ne}	kne	conductivity of the nuclear envelope	$\sigma_{ne} > 0$
σ_{np}	knp	conductivity of the nucleoplasm	$\sigma_{np} > 0$
σ_{med}	kmed	conductivity of the supernatant($\varepsilon_{med} = \varepsilon_h$ from cole cole fit)	$\sigma_{med} > 0$

Exemplary file:

```
km: {value: 300.e-6, min: 1.e-8, max: 5.e-4, vary: True}
em: {value: 11., min: 1., max: 20., vary: True}
kcp: {value: 0.4, min: 0.1, max: 2., vary: True}
ene: {value: 50, min: 1., max: 50., vary: True}
kne: {value: 2.e-3, min: 1.e-8, max: 1.e-1, vary: True}
knp: {value: .8, min: 0.1, max: 1., vary: True}
kmed: {value: 0.05, min: 0.04, max: 0.3, vary: True}
```

With the *vary* flag, one can choose whether a variable should be included in the fitting procedure or fixed.

Note:

If you run without electrode polarization, you must include a line for emed as here:

```
emed: {value: 78, min: 70, max: 80, vary: True}
```

1.6 possible values

In Ermolina, I., Plevaya, Y., & Feldman, Y. (2000). Analysis of dielectric spectra of eukaryotic cells by computer modeling. European Biophysics Journal, 29(2), 141–145. <https://doi.org/10.1007/s002490050259>, there have been

reported upper/lower limits for certain parameters. They could act as a first guess for the bounds of the optimization method.

Parameter	lower limit	upper limit
ε_m	1.4	16.8
σ_m	8e-8	5.6e-5
ε_{cp}	60	77
σ_{cp}	0.033	1.1
ε_{ne}	6.8	100
σ_{ne}	8.3e-5	7e-3
ε_{np}	32	300
σ_{np}	0.25	2.2
R	3.5e-6	10.5e-6
R_n	2.95e-6	8.85e-6
d	3.5e-9	10.5e-9
d_n	2e-8	6e-8

class `impedancefitter.main.Fitter` (*directory=None, constants=None, **kwargs*)

The main fitting object class. The chosen fitting routine is applied to all files in the chosen directory.

directory: {string, optional, path to data directory} provide directory if you run code from directory different to data directory

constants: {dict, optional, needed constants} provide constants if you do not want to use a yaml file (for instance in parallel UQ runs).

model: {string, 'SingleShell' OR 'DoubleShell'} currently, you can choose between SingleShell and DoubleShell.

solvername [{string, name of solver}] choose among global solvers from lmfit: basinhopping, differential_evolution, ...; local solvers: levenberg-marquardt, nelder-mead, least-squares. See also lmfit documentation.

inputformat: {string, 'TXT' OR 'XLSX'} currently only TXT and Excel files with a certain formatting (impedance in two columns, first is real part, second imaginary part, is accepted).

LogLevel: {string, optional, 'DEBUG' OR 'INFO' OR 'WARNING'} choose level for logger. Case DEBUG: the script will output plots after each fit, case INFO: the script will output results from each fit to the console.

excludeEnding: {string, optional} for ending that should be ignored (if there are files with the same ending as the chosen inputformat)

minimumFrequency: {float, optional} if you want to use another frequency than the minimum frequency in the dataset.

maximumFrequency: {float, optional} if you want to use another frequency than the maximum frequency in the dataset.

solver_kwargs: {dict, optional} Contains infos for the solver. find possible kwargs in the lmfit documentation.

data_sets: {int, optional} Use only a certain number of data sets instead of all in directory.

omega: list Contains frequencies.

Z: list Contains corresponding impedances.

protocol: None or string Choose 'Iterative' for repeated fits with changing parameter sets, customized approach. If not specified, there is always just one fit for each data set.

fit_to_cole_cole (*omega*, *Z*)

Fit data to cole-cole model.

If the `protocol` is specified to be 'Iterative', the data is fitted to the Cole-Cole-Model twice. Then, in the second fit, the parameters 'conductivity' and 'eh' are being fixed.

The initial parameters and boundaries for the variables are read from the .yaml file in the directory of the python script. see also: `impedancefitter.cole_cole.cole_cole_model()`

fit_to_double_shell (*omega*, *Z*, *k_fit*, *alpha_fit*, *emed_fit*)

k_fit, *alpha_fit* and *emed_fit* are the determined values in the cole-cole-fit

If `protocol` is equal to *Iterative*, the following procedure is applied:

1. 1st Fit: the parameters k and α are fixed(coming from cole-cole-fit), and the data is fitted against the double-shell-model. To be determined in this fit: $\sigma_{\text{sup}}/k_{\text{med}}$.
2. 2nd Fit: the parameters k , α and σ_{sup} are fixed and the data is fitted again. To be determined in this fit: σ_{m} , ε_{m} , σ_{cp} .
3. 3rd Fit: the parameters k , α , σ_{sup} , σ_{m} and ε_{m} are fixed and the data is fitted again. To be determined in this fit: σ_{cp} .
4. last Fit: the parameters k , α , σ_{sup} , σ_{ne} , σ_{np} , σ_{m} , ε_{m} are fixed. To be determined in this fit: ε_{ne} , σ_{ne} , ε_{np} , σ_{np} .

See also: `impedancefitter.double_shell.double_shell_model()`

fit_to_single_shell (*omega*, *Z*, *k_fit*, *alpha_fit*, *emed_fit*)

if `protocol` is *Iterative*, the conductivity of the medium is determined in the first run and then fixed. Attention!!! if no electrode_polarization correction is needed, *emed* must be in the input dict!!! See also:

`impedancefitter.single_shell.single_shell_model()`

fit_to_suspension_model (*omega*, *Z*)

fit data to pure suspension model to compare to cole-cole based correction. See also:

`impedancefitter.cole_cole.suspension_model()`

get_max_rows (*filename*)

determines the number of actual data rows in TXT files.

main (*protocol=None*, *electrode_polarization=True*)

Main function that iterates through all data sets provided.

protocol: None or string Choose 'Iterative' for repeated fits with changing parameter sets, customized approach. If not specified, there is always just one fit for each data set.

electrode_polarization: True or False Switch on whether to account for electrode polarization or not. Currently, only a CPE correction is possible.

prepare_txt ()

Function for txt files that are currently supported. The section for "TRACE: A" is used, also the number of skiprows_txt needs to be aligned, if there is a deviating TXT-format.

process_data_from_file (*filename*)

fit the data to the cole_cole_model first (compensation of the electrode polarization) and then to the defined model.

process_fitting_results (*filename*)

function writes output into yaml file to prepare statistical analysis of the result

readin_Data_from_file (*filename*, *max_rows*)

Data from txt files get reads in, returns array with omega and complex-valued impedance *Z*

readin_Data_from_xlsx (*filename*)

read in data that is structured like: frequency, real part of impedance, imaginary part of impedance there may be many different sets of impedance data

select_and_solve (*solvername, residual, params, args*)

selects the needed solver and minimizes the given residual

`impedancefitter.main.logger = <Logger impedancefitter-logger (WARNING)>`

We use an own logger for the impedancefitter module.

UTILITIES

`impedancefitter.utils.Z_CPE(omega, k, alpha)`

CPE impedance

`impedancefitter.utils.Z_sus(omega, es, kdc, c0, cf)`

Accounts for air capacitance and stray capacitance.

`impedancefitter.utils.compare_to_data(omega, Z, Z_fit, filename, subplot=None)`

plots the relative difference of the fitted function to the data

`impedancefitter.utils.e_sus(omega, eh, el, tau, a)`

complex permittivity of suspension

`impedancefitter.utils.plot_dielectric_properties(omega, cole_cole_output, suspen-
sion_output)`

eps is the complex valued permittivity from which we extract relative permittivity and conductivity compares the dielectric properties before and after the compensation

`impedancefitter.utils.return_diel_properties(omega, epsc)`

return real permittivity and conductivity

`impedancefitter.utils.set_parameters_from_yaml(params, modelName)`

for suspension model: if wanted one could create an own file

COLE-COLE MODEL

`impedancefitter.cole_cole.cole_cole_model` (*omega*, *c0*, *cf*, *k*, *el*, *tau*, *a*, *alpha*, *kdc*, *eh*)
function holding the cole_cole_model equations, returning the calculated impedance Equations for calculations:

$$Z_{ep} = k^{-1}j\omega^{-\alpha}$$

$$\varepsilon_s = \varepsilon_h + \frac{\varepsilon_l - \varepsilon_h}{1 + (j\omega\tau)^a}$$

$$Z_s = \frac{1}{j\varepsilon_s\omega c_0 + \frac{\sigma_{dc}c_0}{\varepsilon_0} + j\omega c_f}$$

$$Z_{fit} = Z_s + Z_{ep}$$

find more details in formula 6 and 7 of <https://ieeexplore.ieee.org/document/6191683>

`impedancefitter.cole_cole.cole_cole_residual` (*params*, *omega*, *data*, *c0*, *cf*)
compute difference between data and model.

`impedancefitter.cole_cole.plot_cole_cole` (*omega*, *Z*, *result*, *filename*, *c0*, *cf*)
plot results of cole-cole model and compare fit to data.

`impedancefitter.cole_cole.suspension_model` (*omega*, *c0*, *cf*, *el*, *tau*, *a*, *kdc*, *eh*)
Simple suspension model using `impedancefitter.utils.Z_sus()`

`impedancefitter.cole_cole.suspension_residual` (*params*, *omega*, *data*, *c0*, *cf*)
use the plain suspension model and calculate the residual (the difference between data and fitted values)

SINGLE SHELL MODEL

`impedancefitter.single_shell.plot_single_shell` (*omega*, *Z*, *result*, *filename*, *constants*)

plot the real part, imaginary part vs frequency and real vs. imaginary part

`impedancefitter.single_shell.single_shell_model` (*omega*, *constants*, *em*, *km*, *kcp*, *kmed*,
emed)

Equations for the single-shell-model(ν_1 is calculated like in the double-shell-model):

$$\varepsilon_{\text{cell}}^* = \varepsilon_{\text{m}}^* * \frac{(2 * (1 - \nu_1) + (1 + 2 * \nu_1) * E_1}{((2 + \nu_1) + (1 - \nu_1) * E_1}$$

$$E_1 = \frac{\varepsilon_{\text{cp}}^*}{\varepsilon_{\text{m}}^*}$$

$$\varepsilon_{\text{sus}}^* = \varepsilon_{\text{med}}^* * \frac{2 * (1 - p) + (1 + 2 * p) * E_0}{(2 + p) + (1 - p) * E_0}$$

$$E_0 = \frac{\varepsilon_{\text{cell}}^*}{\varepsilon_{\text{med}}^*}$$

`impedancefitter.single_shell.single_shell_residual` (*params*, *omega*, *data*, *constants*)

calculates the residual for the single-shell model, using the `single_shell_model`.

DOUBLE SHELL MODEL

`impedancefitter.double_shell.double_shell_model` (*omega, constants, km, em, kcp, ene, kne, knp, kmed, emed*)

Equations for the double-shell-model:

$$\begin{aligned}\epsilon_{\text{mix}}^* &= \epsilon_{\text{sup}}^* \frac{(2\epsilon_{\text{sup}}^* + \epsilon_c^*) - 2p(\epsilon_{\text{sup}}^* - \epsilon_c^*)}{(2\epsilon_{\text{sup}}^* + \epsilon_c^*) + p(\epsilon_{\text{sup}}^* - \epsilon_c^*)} \\ \epsilon_c^* &= \epsilon_m^* \frac{2(1 - \nu_1) + (1 + 2\nu_1)E_1}{(2 + \nu_1) + (1 - \nu_1)E_1} \\ E_1 &= \frac{\epsilon_{\text{cp}}^*}{\epsilon_m^*} \frac{2(1 - \nu_2) + (1 + 2\nu_2)E_2}{(2 + \nu_2) + (1 - \nu_2)E_2} \\ E_2 &= \frac{\epsilon_{\text{ne}}^*}{\epsilon_{\text{cp}}^*} \frac{2(1 - \nu_3) + (1 + 2\nu_3)E_3}{(2 + \nu_3) + (1 - \nu_3)E_3} \\ E_3 &= \frac{\epsilon_{\text{np}}^*}{\epsilon_{\text{ne}}^*}\end{aligned}$$

with $R \hat{=}$ outer cell Radius; $R_n \hat{=}$ outer Radius of the nucleus; $d \hat{=}$ thickness of the membrane

$$\begin{aligned}\nu_1 &= \left(1 - \frac{d}{R}\right)^3 \\ \nu_2 &= \left(\frac{R_n}{R - d}\right)^3 \\ \nu_3 &= \left(1 - \frac{d_n}{R_n}\right)^3\end{aligned}$$

`impedancefitter.double_shell.double_shell_residual` (*params, omega, data, constants*)
data is Z

`impedancefitter.double_shell.plot_double_shell` (*omega, Z, result, filename, constants*)
plot the real and imaginary part of the impedance vs. the frequency and real vs. imaginary part

POST PROCESSING

class `impedancefitter.postprocess.PostProcess` (*model*, *electrode_polarization=True*,
yamlfile=None)

This class provides the possibility, to analyse the statistics of the fitted data. The fitting results are read in from the outfile.

model: {string, DoubleShell OR SingleShell} define, which model has been used

electrode_polarization: {bool, default True} set to false if not used

yamlfile: {string, default None} define path to yamlfile or use current working directory

best_model_bic (*parameter*, *distributions*)

Test, which distribution models your data best based on the Bayesian information criterion (see https://openturns.github.io/openturns/master/user_manual/_generated/openturns.FittingTest_BestModelBIC.html#openturns.FittingTest_BestModelBIC). suitable for small samples

Parameters distributions – list of strings like: ['Normal', 'Uniform']

best_model_chisquared (*parameter*, *distributions*)

Test, which distribution models your data best based on the chisquared test (see https://openturns.github.io/openturns/master/user_manual/_generated/openturns.FittingTest_BestModelChiSquared.html).

Parameters distributions – list of strings like: ['Normal', 'Uniform']

best_model_kolmogorov (*parameter*, *distributions*)

Test, which distribution models your data best based on the kolmogorov test (see https://openturns.github.io/openturns/master/user_manual/_generated/openturns.FittingTest_BestModelKolmogorov.html#openturns.FittingTest_BestModelKolmogorov). suitable for small samples

Parameters distributions – list of strings like: ['Normal', 'Uniform']

fit_to_histogram_distribution (*parameter*)

Generate histogram from results.

Parameters parameter – string, parameter that is to be fitted.

fit_to_normal_distribution (*parameter*)

Fit results for to normal distribution.

Parameters parameter – string, parameter that is to be fitted.

plot_histograms ()

Plot histograms for all determined parameters. fails if values are too close to each other

INDICES AND TABLES

- `genindex`
- `modindex`
- `search`

PYTHON MODULE INDEX

i

- `impedancefitter.cole cole`, 9
- `impedancefitter.double_shell`, 13
- `impedancefitter.main`, 4
- `impedancefitter.postprocess`, 15
- `impedancefitter.single_shell`, 11
- `impedancefitter.utils`, 7

INDEX

B

best_model_bic() (impedancefitter.postprocess.PostProcess method), 15
best_model_chisquared() (impedancefitter.postprocess.PostProcess method), 15
best_model_kolmogorov() (impedancefitter.postprocess.PostProcess method), 15

C

cole_cole_model() (in module impedancefitter.cole_cole), 9
cole_cole_residual() (in module impedancefitter.cole_cole), 9
compare_to_data() (in module impedancefitter.utils), 7

D

double_shell_model() (in module impedancefitter.double_shell), 13
double_shell_residual() (in module impedancefitter.double_shell), 13

E

e_sus() (in module impedancefitter.utils), 7

F

fit_to_cole_cole() (impedancefitter.main.Fitter method), 5
fit_to_double_shell() (impedancefitter.main.Fitter method), 5
fit_to_histogram_distribution() (impedancefitter.postprocess.PostProcess method), 15
fit_to_normal_distribution() (impedancefitter.postprocess.PostProcess method), 15
fit_to_single_shell() (impedancefitter.main.Fitter method), 5
fit_to_suspension_model() (impedancefitter.main.Fitter method), 5
Fitter (class in impedancefitter.main), 4

G

get_max_rows() (impedancefitter.main.Fitter method), 5

I

impedancefitter.cole_cole (module), 9
impedancefitter.double_shell (module), 13
impedancefitter.main (module), 4
impedancefitter.postprocess (module), 15
impedancefitter.single_shell (module), 11
impedancefitter.utils (module), 7

L

logger (in module impedancefitter.main), 6

M

main() (impedancefitter.main.Fitter method), 5

P

plot_cole_cole() (in module impedancefitter.cole_cole), 9
plot_dielectric_properties() (in module impedancefitter.utils), 7
plot_double_shell() (in module impedancefitter.double_shell), 13
plot_histograms() (impedancefitter.postprocess.PostProcess method), 15
plot_single_shell() (in module impedancefitter.single_shell), 11
PostProcess (class in impedancefitter.postprocess), 15
prepare_txt() (impedancefitter.main.Fitter method), 5
process_data_from_file() (impedancefitter.main.Fitter method), 5
process_fitting_results() (impedancefitter.main.Fitter method), 5

R

readin_Data_from_file() (impedancefitter.main.Fitter method), 5
readin_Data_from_xlsx() (impedancefitter.main.Fitter method), 5
return_diel_properties() (in module impedancefitter.utils), 7

S

select_and_solve() (impedancefitter.main.Fitter method), 6

`set_parameters_from_yaml()` (in module `impedancefitter.utils`), [7](#)
`single_shell_model()` (in module `impedancefitter.single_shell`), [11](#)
`single_shell_residual()` (in module `impedancefitter.single_shell`), [11](#)
`suspension_model()` (in module `impedancefitter.cole_cole`), [9](#)
`suspension_residual()` (in module `impedancefitter.cole_cole`), [9](#)

Z

`Z_CPE()` (in module `impedancefitter.utils`), [7](#)
`Z_sus()` (in module `impedancefitter.utils`), [7](#)