Homework 4

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Problem 1)

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16 17 -

18 -

```
a)
                                           Input-Output Data
   0.4
   0.2
 Amplitude
    0
   -0.5
                                             Time (seconds)
 1
         %% Homework 4
 2
         % Henrik Lucander 724140
 3 -
         clear all
 4 -
         close all
         % Problem 1
 5
  6
 7
         %making the transfer function:
 8 -
         num = 1;
 9 -
         den = [1 \ 3 \ 2];
 10 -
         H = tf(num,den);
11
12 -
         Ts = 1/10; %sample rate of 10Hz
```

t = 0:Ts:200; %200s time with sampling time as interval

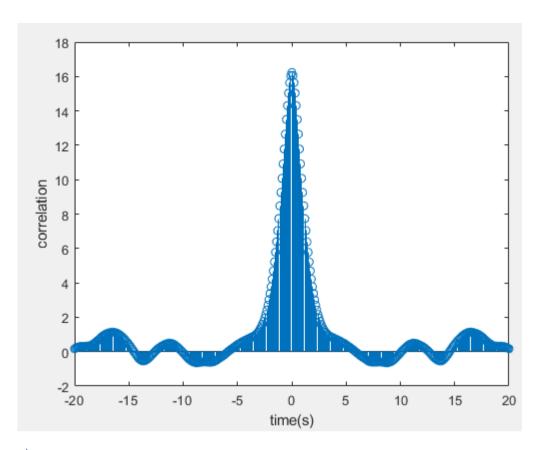
u = idinput(length(t), 'prbs'); %pseudorandom binary signal input

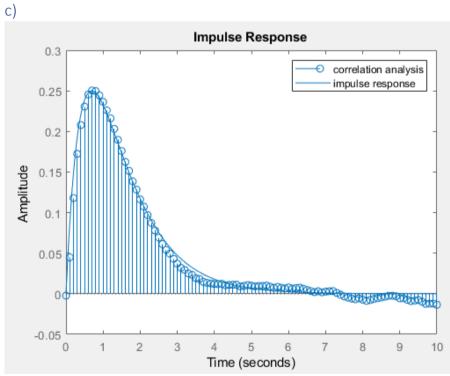
data = iddata(y,u,Ts); %creating an iddata object from the generated signal

y = lsim(H,u,t); %simulating time response of dynamic system

```
b)
21
22 -
         tcorr = -20:Ts:20;
23 -
        autocorr = xcorr(y,200);
24 -
         figure(2);
25 -
         stem(tcorr, autocorr);
26 -
        ylabel('correlation');
 27 -
        xlabel('time(s)');
```

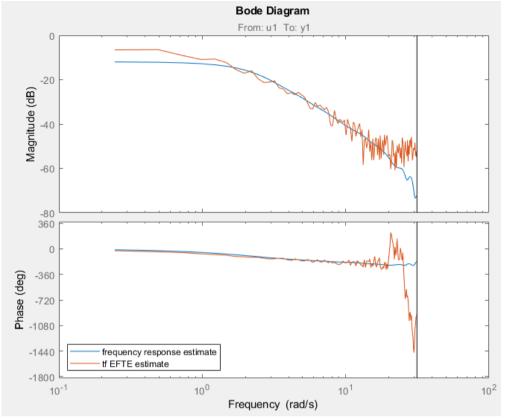
plot(data)





```
28
        % C)
29 -
        figure(3)
30 -
        imp = cra(data, 100);
31 -
        t2 = 0:Ts:10;
        stem(t2,imp*10);
32 -
33 -
        hold on
34 -
        impulse(H, 10);
35 -
        legend('correlation analysis','impulse response');
```

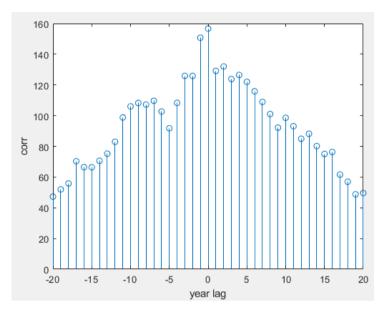




Problem 2)

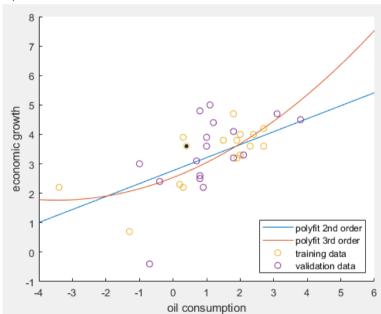
a)

We can analyze the relationship between oil consumption and economic growth by cross correlation.



The variables are correlated, but not very highly. We can see from the plot that the highest correlation is at 0. Therefore, we can say that there is no delay(lag) in the correlation (from year to year).



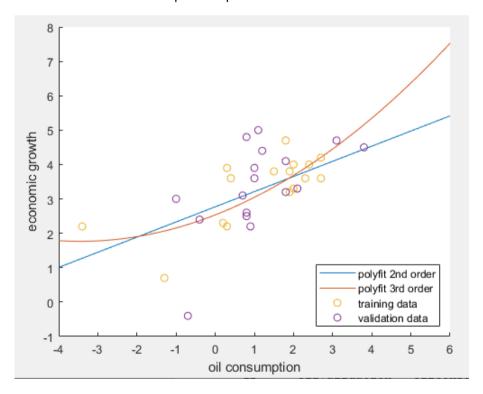


In the plot we can see the estimations for the polynomial model with 2^{nd} order and 3^{rd} order. We can see that the second order fits better.

The m-code used for estimating the polynomial model:

```
19
        % b)
20
        %splitting the data to training and validation sets:
21 -
       oilTraining = oilConsumption(1:end/2);
22 -
       oilValidation = oilConsumption(end/2+1:end);
23 -
       ecoTraining = economicGrowth(1:end/2);
24 -
       ecoValidation = economicGrowth(end/2+1:end);
25 -
       pfitl = polyfit(oilTraining,ecoTraining,1); %second order
       pfit2 = polyfit(oilTraining,ecoTraining,2); %third order
26 -
27
28
        % C)
29 -
       figure(2);
30 -
       hold on;
31 -
       xaxis = linspace(-4,6,100); %x-axis
       pvall = polyval(pfitl,xaxis); %second order
32 -
33 -
       pval2 = polyval(pfit2,xaxis); %third order
34 -
       plot(xaxis, pvall);
35 -
       plot(xaxis, pval2);
```

c)
The estimation function in part "b" plotted as the blue line.



The prediction for the economic growth in year 2015 if the oil consumption percentage change was -0.5% is: **2.5505%**

```
45 - oilChange = -0.5;
46 - ecoGrowthIn2015 = pfit1(1)*oilChange+pfit1(2)
```