

# Chapter 1

## Functions and Graphs

### Checkpoint Solutions

#### Checkpoint 1.1: Evaluating Functions

##### Instruction

For the function  $f(x) = x^2 - 3x + 5$  evaluate

- (a)  $f(1)$
- (b)  $f(a + h)$

##### Solution

- (a)  $f(1) = 1^2 - 3 \cdot 1 + 5 = 1 - 3 + 5 = 3.$
- (b)  $f(a + h) = (a + h)^2 - 3(a + h) + 5 = a^2 + 2ah + h^2 - 3a - 3h + 5.$

##### Answer

- (a)  $f(1) = 3.$
- (b)  $f(a + h) = a^2 + 2ah + h^2 - 3a - 3h + 5.$

#### Checkpoint 1.2: Finding Domain and Range

##### Instruction

Find the domain and range for  $f(x) = \sqrt{4 - 2x} + 5.$

##### Solution

- i To find the domain of  $f$ , we need the expression  $4 - 2x \geq 0$ , due to that real negative numbers do not have a square root. Solving this inequality, we conclude that the domain is  $\{x \mid x \leq 2\}.$

ii To find the range of  $f$ , we note that since  $\sqrt{4-2x} \geq 0$ , it follows that  $f(x) = \sqrt{4-2x} + 5 \geq 5$ . Therefore, the range of  $f$  must be a subset of the set  $\{y \mid y \geq 5\}$ .

To show that every element in this set is in the range of  $f$ , we need to show that for all  $y$  in this set, there exists a real number  $x$  in the domain such that  $f(x) = y$ . Let  $y \geq 5$ . Then,  $f(x) = y$  if and only if

$$\sqrt{4-2x} + 5 = y.$$

Solving this equation for  $x$ , we see that  $x$  must solve the equation

$$\sqrt{4-2x} = y - 5.$$

Since  $y \geq 5$ , such an  $x$  could exist. Squaring both sides of the above equation we have

$$4 - 2x = (y - 5)^2.$$

Therefore we need

$$-2x = (y - 5)^2 - 4,$$

which implies

$$x = 2 - \frac{(y - 5)^2}{2}.$$

We just need to verify that  $x$  is in the domain of  $f$ . Since the domain of  $f$  consists of all real numbers less or equal to 2, and

$$2 - \frac{(y - 5)^2}{2} \leq 2,$$

there does exist an  $x$  in the domain of  $f$ . We conclude that the range of  $f$  is  $\{y \mid y \geq 5\}$ .

### Answer

Domain =  $\{x \mid x \leq 2\}$ , range =  $\{y \mid y \geq 5\}$ .

### Checkpoint 1.3: Finding Zeroes

#### Instruction

Find the zeroes of  $f(x) = x^3 - 5x^2 + 6x$ .

#### Solution

The zeroes of a function are the values of  $x$  where  $f(x) = 0$ . To find the zeroes, we need to solve

$$f(x) = x^3 - 5x^2 + 6x = 0.$$

Factor out  $x$

$$f(x) = x(x^2 - 5x + 6) = 0.$$

We can continue factoring by pure inspection, with the goal of finding a pair of numbers that add up to  $-5$  and whose product is  $6$ . This pair of numbers turns out to be  $-2$  and  $-3$ , leading to the factoring

$$f(x) = x(x - 2)(x - 3) = 0.$$

From the above complete factoring of  $f$ , we conclude that there are three zeroes when  $x$  is  $0$ ,  $2$ , and  $3$ .

**Answer**

$$x = 0, 2, 3.$$

### Checkpoint 1.9: Finding the Slope and Equations of Lines

#### Instruction

Consider the line passing through points  $(-3, 2)$  and  $(1, 4)$ .

- (a) Find the slope of the line.
- (b) Find an equation of that line in point-slope form.
- (c) Find an equation of that line in slope-intercept form.

#### Solution

- (a) The slope of the line is

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{4 - 2}{1 - (-3)} = \frac{4 - 2}{1 + 3} = \frac{2}{4} = \frac{1}{2}.$$

- (b) To find an equation for the linear function in point-slope form, use the slope  $m = \frac{1}{2}$  and choose any point on the line. If we choose the point  $(1, 4)$ , we get the equation

$$y - 4 = \frac{1}{2}(x - 1).$$

**Answer**

(a)  $m = \frac{1}{2}$

### Checkpoint 1.4: Combining Functions Using Mathematical Operations

#### Instruction

For  $f(x) = x^2 + 3$  and  $g(x) = 2x - 5$ , find  $(f/g)(x)$  and state its domain.

**Solution**

To find  $(f/g)(x)$  we write the function with the quotient operator

$$\frac{f}{g}(x) = \frac{x^2 + 3}{2x - 5}.$$

The domain of this function is  $\{x \mid x \neq \frac{5}{2}\}$ .

**Answer**

$\frac{f}{g}(x) = \frac{x^2+3}{2x-5}$ . The domain is  $\{x \mid x \neq \frac{5}{2}\}$ .

**Checkpoint 1.5: Compositions of Functions****Instruction**

Let  $f(x) = 2 - 5x$ . Let  $g(x) = \sqrt{x}$ . Find  $(f \circ g)(x)$ .

**Solution**

$$(f \circ g)(x) = f(g(x)) = f(\sqrt{x}) = 2 - 5\sqrt{x}.$$

**Answer**

$$(f \circ g)(x) = 2 - 5\sqrt{x}.$$

**Checkpoint 1.6: Application Involving a Composite Function****Instruction**

If items are on sale for 10% off their original price, and a customer has a coupon for an additional 30% off, what will be the final price for an item that is originally  $x$  dollars, after applying the coupon to the sale price?

**Solution**

Since the sale price 10% off the original price, if an item is  $x$  dollars, its sale price is given by

$$f(x) = 0.90x.$$

Since the coupon entitles an individual to 30% off the price of any item, if an item is  $y$  dollars, the price after applying the coupon, is given by

$$g(y) = 0.70y.$$

Therefore, if the price is originally  $x$  dollars, its price after applying the coupon to the sale price will be

$$(g \circ f)(x) = g(f(x)) = (0.70)0.90x = 0.63x..$$

**Answer**

$$(g \circ f)(x) = 0.63x.$$

**Exercise Solutions****Exercise 1.1.1****Instruction**

Assuming the relation in table 1.1.

- (a) Determine the domain and the range of the relation.
- (b) State whether the relation is a function.

$x$	-3	-2	-1	0	1	2	3
$y$	9	4	1	0	1	4	9

Table 1.1: Relation between  $x$  and  $y$  in exercise 1.1.1

**Solution**

- (a) The domain of the relation is the set of unique  $x$  values,

$$\{-3, -2, -1, 0, 1, 2, 3\}.$$

The range of the relation is the set of unique  $y$  values,

$$\{0, 1, 4, 9\}.$$

- (b) This relation is a function, each input is assigned to exactly one output.

**Answer**

- (a) Domain =  $\{-3, -2, -1, 0, 1, 2, 3\}$ , range =  $\{0, 1, 4, 9\}$ .
- (b) Yes, a function.

**Exercise 1.1.2****Instruction**

Assuming the relation in table 1.2.

- (a) Determine the domain and the range of the relation.
- (b) State whether the relation is a function.

$x$	-3	-2	-1	0	1	2	3
$y$	-2	-8	-1	0	1	8	-2

Table 1.2: Relation between  $x$  and  $y$  in exercise 1.1.2

### Solution

- (a) The domain of the relation is the set of unique  $x$  values,

$$\{-3, -2, -1, 0, 1, 2, 3\}.$$

The range of the relation is the set of unique  $y$  values,

$$\{-8, -2, -1, 0, 1, 8\}.$$

- (b) This relation is a function, each input is assigned to exactly one output.

### Answer

- (a) Domain =  $\{-3, -2, -1, 0, 1, 2, 3\}$ , range =  $\{-8, -2, -1, 0, 1, 8\}$ .

- (b) Yes, a function.

### Exercise 1.1.3

#### Instruction

Assuming the relation in table 1.3.

- (a) Determine the domain and the range of the relation.  
(b) State whether the relation is a function.

$x$	1	2	3	0	1	2	3
$y$	-3	-2	-1	0	1	2	3

Table 1.3: Relation between  $x$  and  $y$  in exercise 1.1.3

### Solution

- (a) The domain of the relation is the set of unique  $x$  values,

$$\{0, 1, 2, 3\}.$$

The range of the relation is the set of unique  $y$  values,

$$\{-3, -2, -1, 0, 1, 2, 3\}.$$

- (b) This relation is not a function, each input is not assigned to exactly one output.  
Take for example  $x = 1$  that can cause both  $y = -3$  and  $y = 1$ .

**Answer**

- (a) Domain =  $\{0, 1, 2, 3\}$ , range =  $\{-3, -2, -1, 0, 1, 2, 3\}$ .  
(b) No, not a function.

**Exercise 1.1.4****Instruction**

Assuming the relation in table 1.4.

- (a) Determine the domain and the range of the relation.  
(b) State whether the relation is a function.

$x$	1	2	3	4	5	6	7
$y$	1	1	1	1	1	1	1

Table 1.4: Relation between  $x$  and  $y$  in exercise 1.1.4

**Solution**

- (a) The domain of the relation is the set of unique  $x$  values,  
 $\{1, 2, 3, 4, 5, 6, 7\}$ .

The range of the relation is the set of unique  $y$  values,  
 $\{1\}$ .

- (b) This relation is a function, each input is assigned to exactly one output.

**Answer**

- (a) Domain =  $\{1, 2, 3, 4, 5, 6, 7\}$ , range =  $\{1\}$ .  
(b) Yes, a function.

**Exercise 1.1.5****Instruction**

Assuming the relation in table 1.5.

- (a) Determine the domain and the range of the relation.  
(b) State whether the relation is a function.

$x$	3	5	8	10	15	21	33
$y$	3	2	1	0	1	2	3

Table 1.5: Relation between  $x$  and  $y$  in exercise 1.1.5

### Solution

- (a) The domain of the relation is the set of unique  $x$  values,

$$\{3, 5, 8, 10, 15, 21, 33\}.$$

The range of the relation is the set of unique  $y$  values,

$$\{0, 1, 2, 3\}.$$

- (b) This relation is a function, each input is assigned to exactly one output.

### Answer

- (a) Domain =  $\{3, 5, 8, 10, 15, 21, 33\}$ , range =  $\{0, 1, 2, 3\}$ .

- (b) Yes, a function.

### Exercise 1.1.6

#### Instruction

Assuming the relation in table 1.6.

- (a) Determine the domain and the range of the relation.  
(b) State whether the relation is a function.

$x$	-7	-2	-2	0	1	3	6
$y$	11	5	1	-1	-2	4	11

Table 1.6: Relation between  $x$  and  $y$  in exercise 1.1.6

### Solution

- (a) The domain of the relation is the set of unique  $x$  values,

$$\{-7, -2, 0, 1, 3, 6\}.$$

The range of the relation is the set of unique  $y$  values,

$$\{-2, -1, 1, 4, 5, 11\}.$$

- (b) This relation is not a function, each input is not assigned to exactly one output.  
See  $x = -2$ , that can cause both  $y = 1$  and  $y = 5$ .



**Answer**

- (a) Domain =  $\{-7, -2, 0, 1, 3, 6\}$ , range =  $\{-2, -1, 1, 4, 5, 11\}$ .  
(b) No, not a function.

**Exercise 1.1.7****Instruction**

Find the below values for the function  $f(x) = 5x - 2$ , if they exist, then simplify.

- (a)  $f(0)$   
(b)  $f(1)$   
(c)  $f(3)$   
(d)  $f(-x)$   
(e)  $f(a)$   
(f)  $f(a + h)$

**Solution**

- (a)  $f(0) = 5 \cdot 0 - 2 = 0 - 2 = -2$ .  
(b)  $f(1) = 5 \cdot 1 - 2 = 5 - 2 = 3$ .  
(c)  $f(2) = 5 \cdot 3 - 2 = 15 - 2 = 13$ .  
(d)  $f(-x) = 5(-x) - 2 = -5x - 2$ .  
(e)  $f(a) = 5a - 2$ .  
(f)  $f(a + h) = 5(a + h) - 2 = 5a + 5h - 2$ .

**Answer**

- (a)  $-2$ .  
(b)  $3$ .  
(c)  $13$ .  
(d)  $-5x - 2$ .  
(e)  $5a - 2$ .  
(f)  $5a + 5h - 2$ .

### Exercise 1.1.8

#### Instruction

Find the below values for the function  $f(x) = 4x^2 - 3x + 1$ , if they exist, then simplify.

- (a)  $f(0)$
- (b)  $f(1)$
- (c)  $f(3)$
- (d)  $f(-x)$
- (e)  $f(a)$
- (f)  $f(a + h)$

#### Solution

- (a)  $f(0) = 4 \cdot 0^2 - 3 \cdot 0 + 1 = 4 \cdot 0 - 0 + 1 = 0 - 0 + 1 = 1.$
- (b)  $f(1) = 4 \cdot 1^2 - 3 \cdot 1 + 1 = 4 \cdot 1 - 3 + 1 = 4 - 3 + 1 = 2.$
- (c)  $f(3) = 4 \cdot 3^2 - 3 \cdot 3 + 1 = 4 \cdot 9 - 9 + 1 = 36 - 9 + 1 = 28.$
- (d)  $f(-x) = 4(-x)^2 - 3(-x) + 1 = 4x^2 + 3x + 1.$
- (e)  $f(a) = 4a^2 - 3a + 1.$
- (f) 
$$\begin{aligned} f(a + h) &= 4(a + h)^2 - 3(a + h) + 1 \\ &= 4(a^2 + 2ah + h^2) - 3a - 3h + 1 \\ &= 4a^2 + 4h^2 + 8ah - 3a - 3h + 1. \end{aligned}$$

#### Answer

- (a) 1.
- (b) 2.
- (c) 28.
- (d)  $4x^2 + 3x + 1.$
- (e)  $4a^2 - 3a + 1.$
- (f)  $4a^2 + 4h^2 + 8ah - 3a - 3h + 1.$

### Exercise 1.1.15

Find the domain, range, and all zeros/intercepts, if any, of the function  $g(x) = \sqrt{8x - 1}.$

### Solution

- i The domain of the square root function is  $[0, \infty)$ , which implies  $8x - 1 \geq 0$ . Solving for  $x$  gives  $x \geq \frac{1}{8}$ .
- ii To find the range of  $g$ , we note that  $\sqrt{8x - 1} \geq 0$ . Therefore, the range of  $g$  must be a subset of the set  $\{y \mid y \geq 0\}$ . To show that every element in this set is in the range of  $g$ , we need to show that for a given  $y$  in this set, there exists a real number  $x$  in the domain such that  $g(x) = y$ .

Let  $y \geq 0$ . Then  $g(x) = y$  if and only if

$$\sqrt{8x - 1} = y.$$

We are interested in  $x$ , and will solve this equation for  $x$ . Since  $y \geq 0$  such an  $x$  could exist. Squaring both sides of this equation, we have

$$8x - 1 = y^2.$$

Therefore, we need

$$8x = y^2 + 1,$$

which implies

$$x = \frac{y^2 + 1}{8}.$$

We just need to verify that  $x$  is in the domain of  $g$ . Since the domain of  $g$  consists of all real numbers greater than or equal to  $1/8$ , and

$$\frac{y^2 + 1}{8} \geq \frac{1}{8},$$

there does exist an  $x$  in the domain of  $g$ . We conclude that the range of  $g$  is  $\{y \mid y \geq 0\}$ .

- iii To find the zeroes, solve  $g(x) = \sqrt{8x - 10}$ . We discover that  $g$  have one zero at  $x = -1/8$ .
- iv The  $y$ -intercept is given by  $(0, g(0))$ . Since  $x = 0$  isn't in the domain of  $g$ , it follows that that there aren't any intercepts.

### Answer

Domain =  $x \geq \frac{1}{8}$ , range =  $\{y \mid y \geq 0\}$ , zeroes  $x = -1/8$ , no intercepts.

### Exercise 1.1.23

Sketch the graph for the function  $f(x) = 3x - 6$  with the aid of table 1.7.

$x$	-3	-2	-1	0	1	2	3
$y$	-15	-12	-9	-6	-3	0	3

Table 1.7: Relation between  $x$  and  $y$  in exercise 1.1.23

### Solution

Begin by sketching the axes. We choose the same scale on both axes to not distort the graph. We choose the range for both axes to be -15 to 15, allowing us to plot all the points from table 1.7, see figure 1.1.

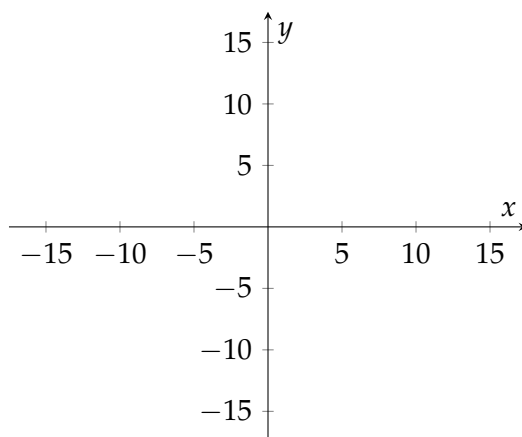


Figure 1.1: Empty graph with just the axes

After having sketched the axes we add markers based on the data in table 1.7, see figure 1.2.

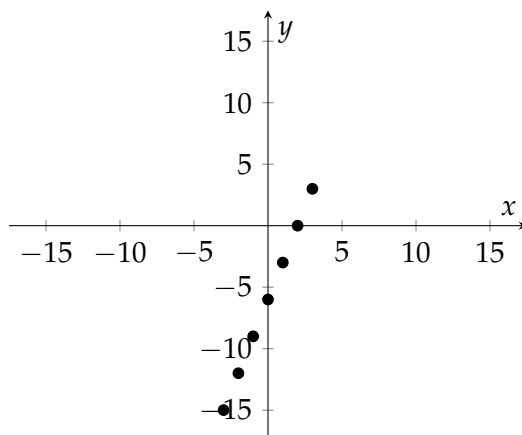


Figure 1.2: Graph with added markers

We then connect the markers with line segments. In this particular case the result will be a single straight line so we can use a ruler when sketching, see figure 1.3.

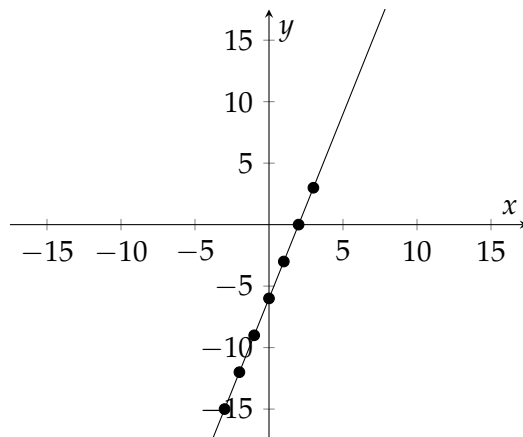


Figure 1.3: Graph with connected markers

**Answer**

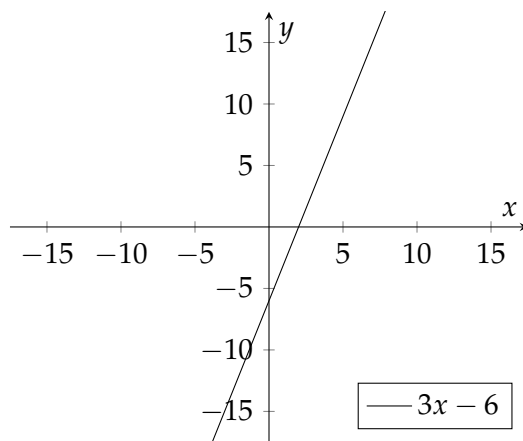


Figure 1.4: Answer to exercise 1.1.23

### Exercise 1.1.29

Use the vertical line test to determine whether the graph in figure 1.5 represent a function. Assume that the graph continues at both ends beyond the given grid. If the graph represents a function, then determine the following for the graph:

- Domain and range
- $x$ -intercept, if any (estimate where necessary)

- (c)  $y$ -intercept, if any (estimate where necessary)
- (d) The intervals for which the function is increasing
- (e) The intervals for which the function is decreasing
- (f) The intervals for which the function is constant
- (g) Symmetry about any axis and/or the origin
- (h) Whether the function is even, odd, or neither

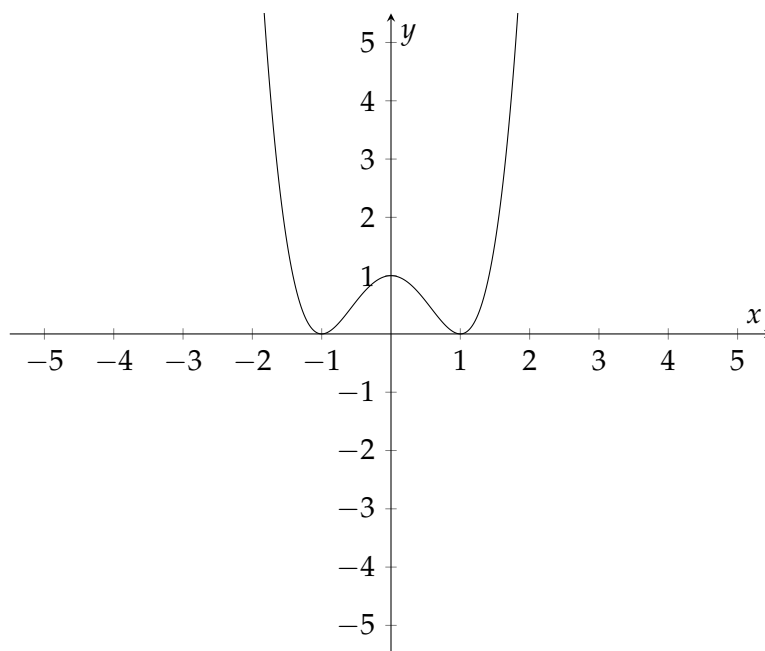


Figure 1.5: Graph for exercise 1.1.29

### Solution

The graph in figure 1.5 do represent a function because every vertical line that may be drawn intersects the graph no more than once. See figure 1.6 for an example of a vertical line with one intersection of the graph. We could slide this line over the entire graph and there would always only be at most one intersection.

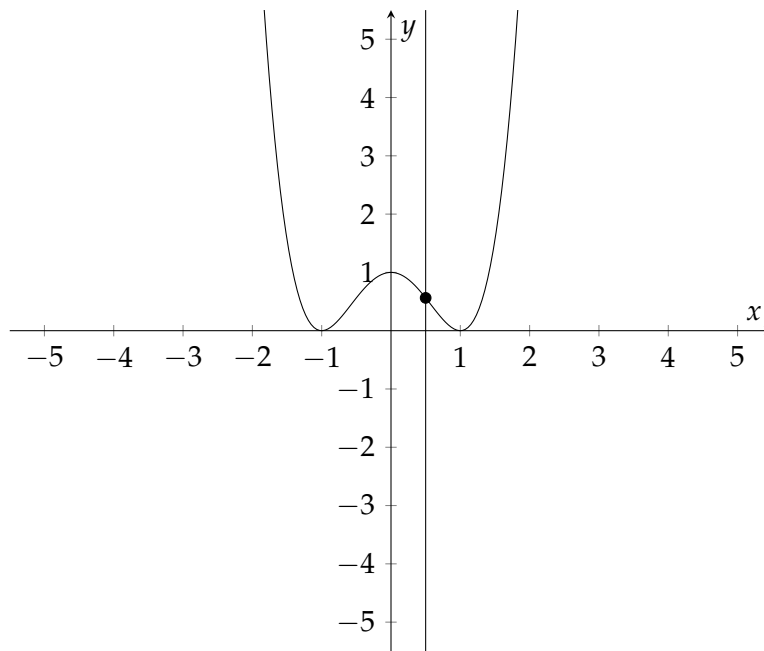


Figure 1.6: Vertical line test illustration

- (a)
  - i The function seems to grow rapidly as  $x$  goes towards  $\pm\infty$ , but there will still always be a  $y$  value. We conclude that the domain is all real numbers.
  - ii  $y$  is always greater or equal to 0, this is the range.
- (b)  $y$  is zero for  $x = -1$ , and  $x = 1$ , these are the  $x$ -intercepts.
- (c) The  $y$ -intercept is  $y = 1$ .
- (d) The function is increasing for the intervals  $-1 < x < 0$  and  $1 < x < \infty$ .
- (e) The function is decreasing for the intervals  $-\infty < x < -1$  and  $0 < x < 1$ .
- (f) The function changes from decreasing/increasing when  $x$  is  $-1$ ,  $0$ , and  $1$ , but there are no intervals for which the function is constant.
- (g)  $(-x, y)$  is on the graph whenever  $(x, y)$  is on the graph, in other words the function is symmetric around the  $y$ -axis.
- (h) The function is not odd because  $f(-x) \neq -f(x)$  for all  $x$  in the domain. Take for example  $x = 0.5$  for which  $f(-x) \approx 0.6$  and  $-f(x) \approx -0.6$ .  
 The function is even because  $f(-x) = f(x)$  for all  $x$ . Take for example  $x = 0.5$  for which  $f(-x) \approx 0.6$  and  $f(x) \approx 0.6$ .

**Answer**

Graph represents a function.

- (a) Domain: all real numbers, range:  $y \geq 0$ .
- (b)  $x = -1$  and  $x = 1$ .
- (c)  $y = 1$ .
- (d)  $-1 < x < 0$  and  $1 < x < \infty$ .
- (e)  $-\infty < x < -1$  and  $0 < x < 1$ .
- (f) Not constant.
- (g)  $y$ -axis.
- (h) Even.

**Exercise 1.1.37****Instruction**

For the pair of functions  $f(x) = x - 8$  and  $g(x) = 5x^2$ , find each of the below new functions. Also determine the domain for each of these new functions.

- (a)  $f + g$
- (b)  $f - g$
- (c)  $f \cdot g$
- (d)  $f/g$

**Solution**

- (a) Add the two given functions to form the requested function,

$$f + g = x - 8 + 5x^2 = 5x^2 + x - 8.$$

The domain of the above new function is all real numbers.

- (b) Subtract the two given functions to form the requested function,

$$f - g = x - 8 - 5x^2 = -5x^2 + x - 8.$$

The domain of the above new function is all real numbers.



(c) Multiply the two given functions to form the requested function,

$$f \cdot g = (x - 8)5x^2 = 5x^3 - 8x^2.$$

The domain of the above new function is all real numbers.

(d) Divide the two given functions to form the requested function,

$$\frac{f}{g} = \frac{x - 8}{5x^2}.$$

The division is defined except for for  $x = 0$ , the domain is hence  $x \neq 0$ .

### Answer

(a)  $5x^2 + x - 8$ , domain: all real numbers.

(b)  $-5x^2 + x - 8$ , domain: all real numbers.

(c)  $5x^3 - 8x^2$ , domain: all real numbers.

(d)  $\frac{x-8}{5x^2}$ , domain:  $x \neq 0$ .

### Exercise 1.1.43

#### Instruction

For the pair of functions  $f(x) = x + 4$  and  $g(x) = 4x - 1$ , find the below listed compositions. Simplify the results. Find the domain of each of the results.

(a)  $(f \circ g)(x)$

(b)  $(g \circ f)(x)$

#### Solution

(a) The composition is given by

$$(f \circ g)(x) = f(g(x)) = (4x - 1) + 4 = 4x - 1 + 4 = 4x + 3.$$

The domain of the above composition is all real numbers.

(b) The composition is given by

$$(g \circ f)(x) = g(f(x)) = 4(x + 4) - 1 = 4x + 16 - 1 = 4x + 15.$$

The domain of the above composition is all real numbers.

**Answer**

- (a)  $4x + 3$ , domain: all real numbers.
- (b)  $4x + 15$ , domain: all real numbers.

**Exercise 1.1.49****Instruction**

Table 1.8 lists the NBA championship winners for the years 2001 to 2012.

Year	Winner
2001	La Lakers
2002	La Lakers
2003	San Antonio Spurs
2004	Detroit Pistons
2005	San Antonio Spurs
2006	Miami Heat
2007	San Antonio Spurs
2008	Boston Celtics
2009	La Lakers
2010	La Lakers
2011	Dallas Mavericks
2012	Miami Heat

Table 1.8: NBA championship winners for the years 2001 to 2012

- (a) Consider the relation in which the domain values are the years 2001 to 2012 and the range is the corresponding winner. Is this relation a function? Explain why or why not.
- (b) Consider the relation where the domain values are the winners and the range is the corresponding years. Is this relation a function? Explain why or why not.

**Solution**

- (a) The relation in which the domain values are the years and the range is the corresponding winner is a function because a given year have only one winner. This functions set of inputs is the years 2001 to 2012 and the output is a team name. The rule for assigning each input to exactly one output is defined by table 1.8.
- (b) The relation where the domain values are the winners and the range is the corresponding years is not a function because there are teams that have won more than once during the years. A function shall have a rule for assigning each input to exactly one output. In this case we cannot deduce exactly one year from just knowing a team name.

**Answer**

- (a) Yes, a function.
- (b) No, not a function.

**Exercise 1.1.51****Instruction**

The volume of a cube depends on the length of the sides  $s$ .

- (a) Write a function  $V(s)$  for the volume of the cube.
- (b) Find an interpret  $V(11.8)$ .

**Solution**

- (a) A cube will have sides  $s$  of equal length. The volume is found by multiplying  $s$  three times

$$V(s) = s \cdot s \cdot s = s^3.$$

- (b) A cube with the side equal to 11.8 length units will have the volume

$$V(11.8) = 11.8^3 \approx 1643$$

cubic units.

**Answer**

- (a)  $V(s) = s^3$ .
- (b)  $V(11.8) = 11.8^3 \approx 1643$  cubic units.

**Exercise 1.1.57****Instruction**

The manager at a skateboard shop pays his workers a monthly salary  $S$  of \$750 plus a commission of \$8.50 for each skateboard they sell.

- (a) Write a function  $y = S(x)$  that models a worker's monthly salary based on the number of skateboards  $x$  he or she sells.
- (b) Find the monthly salary when a worker sells 25, 40, or 55 skateboards.
- (c) Use the INTERSECT feature on a graphing calculator to determine the number of skateboards that must be sold for a worker to earn a monthly income of \$1400. (Hint: Find the intersection of the function and the line  $y = 1400$ .)

**Solution**

- (a) The workers have a base salary plus a commission based on number of skateboards sales. The function will be the constant base salary plus a product depending  $x$  being number of skateboards sold,

$$y = S(x) = 750 + 8.50 \cdot x.$$

- (b) Having the formula from above we can calculate monthly salary for the different amount of skateboards sold,

$$S(25) = 750 + 8.50 \cdot 25 = 962.5,$$

$$S(40) = 750 + 8.50 \cdot 40 = 1090,$$

$$S(55) = 750 + 8.50 \cdot 55 = 1217.5.$$

- (c) Using a graphing calculator to graph our function and the line  $y = 1400$  we note that there will be two lines that intersect at the point  $(76.47, 1400)$ . We can conclude that a worker will need to sell 77 skateboards to earn \$1400.

**Answer**

- (a)  $y = S(x) = 750 + 8.50 \cdot x$ .  
(b) \$962.5, \$1090, \$1217.50.  
(c) 77 skateboards.