

160

A. Transfer Function of the Main Circuit $G(s)$

When the frequency of the input voltage is less than the switching frequency, the transfer function of the main circuit $G(s)$ can be expressed as follow:

$$G(s) = \frac{V_{OUT}(s)}{V_s(s)} = \frac{I_O R_{LOAD}}{I_{in} R_s} = \frac{R_{LOAD}}{R_s} \cdot \frac{I_O}{I_{in}} = \frac{R_{LOAD}}{R_s} \cdot D_{off}$$

B. Transfer Function of the Current Part $G_i(s)$

Fig.2 shows the equivalent big-signal continuous-time model of $\frac{\hat{v}_{Rs}}{\hat{v}_{CA}}$. The equivalent inductance is L_e . In order to deduce the transfer function of the big-signal continuous-time model $\frac{\hat{v}_{Rs}}{\hat{v}_{CA}}$, two assumptions are supposed for the CCM DC-DC converter:

(1) The disturbance of the output voltage $\hat{v} = 0$;

(2) The value of resistance R_s is small, i.e. $|\omega L_e| \gg R_s$, so $\omega L_e + R_s \approx \omega L_e$.

In order to deduce the transfer function of the big-signal continuous-time model $\frac{\hat{v}_{Rs}}{\hat{v}_{CA}}$, two assumptions are supposed for the CCM DC-DC converter:

(1) The disturbance of the output voltage $\hat{v} = 0$;

(2) The value of resistance R_s is small, i.e. $|\omega L_e| \gg R_s$, so $\omega L_e + R_s \approx \omega L_e$.

From Fig.2,

$$\frac{V_s}{V_{CA}} = \frac{1}{V_M} \times e(s) \times M(D) \times \frac{R_s}{R_s + sL_e} \approx \frac{1}{V_M} \times e(s) \times M(D) \times \frac{R_s}{sL_e}$$

(1)

As to the boost converter, we have

$$M(D) = \frac{1}{D'}, L_e = \frac{L}{D'^2}, \text{ and } e(s) = V(1 - \frac{sL_e}{R}).$$

So equation (1) can be expressed as

$$\frac{V_s}{V_{CA}} = \frac{VD'R_s}{sLV_M} (1 - \frac{sL}{RD'^2})$$

(2)

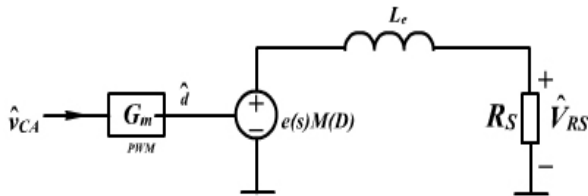


Fig.2 Equivalent Small-Signal Model of $\frac{\hat{v}_{Rs}}{\hat{v}_{CA}}$

From equation (2), it can be seen that the transfer function of the Boost converter contains a zero-point in right half-plane.

In order to consider the worst situation, set $\frac{sL}{RD'^2} \rightarrow 0$, and $D'=1$.

Then equation (2) can be simplified to

$$\frac{V_s}{V_{CA}} \approx \frac{VR_s}{sLV_M}$$

The transfer function of PWM regulation $G_{PWM}(s)$ is

$$G_{PWM}(s) = \frac{1}{V_M}$$

where V_M is the peak-peak value of the sawtooth waveform.

So we get

$$\frac{V_s}{D_{ON}(s)} \approx \frac{V_O R_s}{sL}$$

C. Continuous-Time Transfer Function of Current Controller $G_{ii}(s)$

The controller used for the current program is PI controller. Its transfer function is

$$G_{ii}(s) = K_{ip} + \frac{K_{ii}}{s}$$

where K_{ip} is the proportional factor, K_{ii} is the integral factor.

With respect to the voltage loop, control object is the equivalent power stage which contains the main circuit and the current control program. Its transfer function is as follow:

$$G'(s) = G(s) \times \frac{G_{ii}(s)}{1 + G_{ii}(s) \times G_i(s) \times \frac{1}{R_s}} \times G_{PWM} = \frac{R_{LOAD} \cdot D_{off}}{R_s} \times \frac{K_{ip}s^2 + K_{ii}s}{s^2 + \frac{K_{ip}V_o}{L}s + \frac{K_{ii}V_o}{L}}$$

D. Transfer Function of Voltage Loop $G_V(s)$

PI controller is applied in the voltage loop as well, with a transfer function presented below:

$$G_V(s) = K_{vp} + \frac{K_{vi}}{s}$$

where K_{vp} is the proportional factor and K_{vi} is the integral factor.

Fig.3 below shows the elementary diagram of PFC circuit. The H in it describes the feedback loop, which is decided by sample rate. The transfer function of H is $H(s) = \frac{V_{ref}}{V_o}$. The

system displayed in Fig.3 is a continuous-time system. The corresponding discrete system can be obtained by the discrimination based on it.

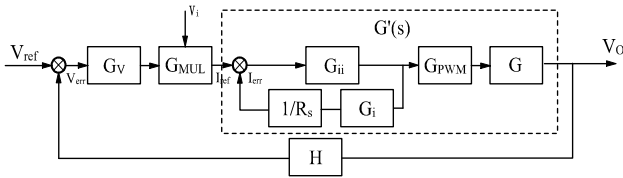


Fig.3 Elementary Diagram of PFC Circuit

For the application of the digital control method, some anti-saturating measures should be taken in order to guarantee the stability of the system. Therefore, an amplitude-limited circuit, such as the two-way zener, should be added to the regulator in order to prevent the system saturation. Fig.4 shows the PI regulator with the anti-saturation circuit.

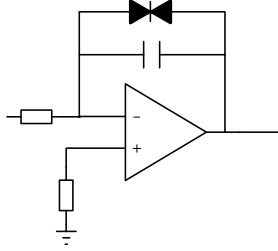


Figure.4 PI Regulator with Anti-Saturation

It can be seen that the PI controller is used in both the voltage loop and the current loop in PFC circuit. As 'I' in 'PI' represents integral, that is to say, without the anti-saturation circuit, the output of the PI regulator will be boundless if the

input is boundless. This means that the system is instable. Therefore, the amplitude-limited circuit is of great necessity to the regulator that will be used in the digital control system of PFC for obtaining a boundary output and ensuring the system stability.

III. MATLAB SIMULATION

The system mentioned above has been verified using SIMULINK. The elementary diagram is shown in Fig.5. Part A in the figure describes the RMS of the input voltage, which is achieved with a second order low pass filter. Its transfer function $G_A(s)$ is:

$$G_A(s) = \frac{0.011z^7 + 0.067z^6 + 0.167z^5 - 0.222z^4 + 0.165z^3 - 0.66z^2 + 0.01z}{z^8 - 8z^7 + 27.7z^6 - 55.00z^5 + 68.55z^4 - 54.5z^3 + 27.12z^2 - 7.7z + 0.9582}$$

Part B describes the main circuit with the transfer function $G(s) = 3.3 \times 10^9 \times \frac{z^2}{z^2 - 2z + 1}$; Part C is the current loop, whose transfer function is $G_{ii}(s) = \frac{12.43z - 3.73}{z - 1}$; Part D describes the voltage loop, its $G_V(s) = \frac{2.1z - 2}{z - 1}$.

Corresponding simulation results are shown in Fig.6. The value of anti-saturation in the voltage loop is between 2.2 to 2.76 and this value in the current loop is between -0.2 to 0.2

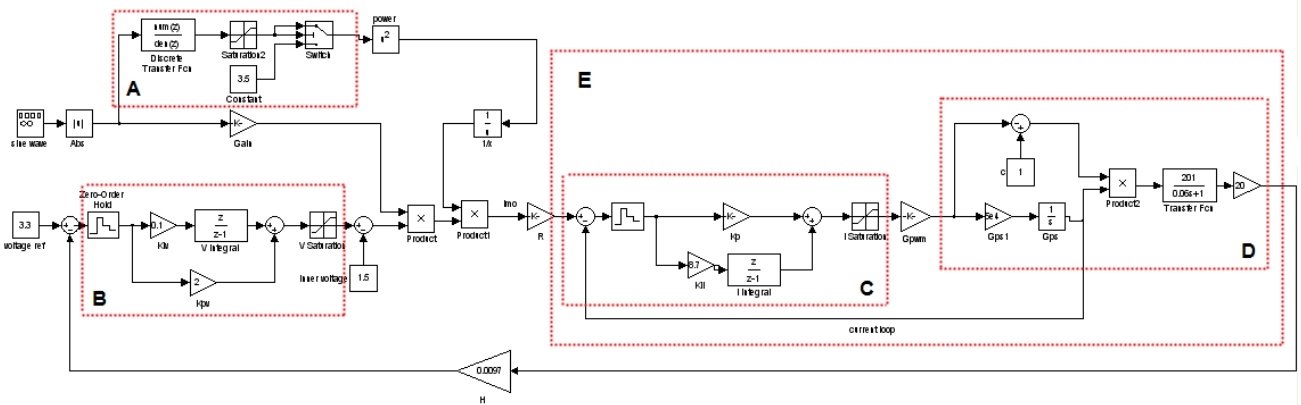
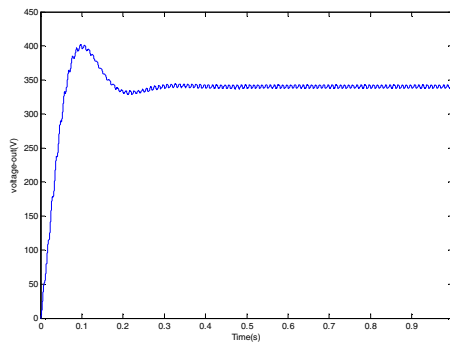
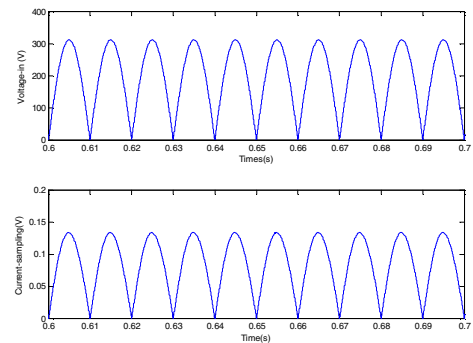


Fig.5 Elementary Diagram in MATLAB



Output Voltage



Input Voltage and Current sampling

Fig.6 Simulation Results

IV. EXPERIMENTAL VERIFICATION

Experiments are executed to verify the circuit designed above. Fig.7 shows the experimental results. It can be seen from the figure that the turn-on angle of the input current in channel 2 is widened in contrast with the current in channel 1. The power factor of the circuit is 96.7%, which indicates the validity of the PFC circuit designed above.

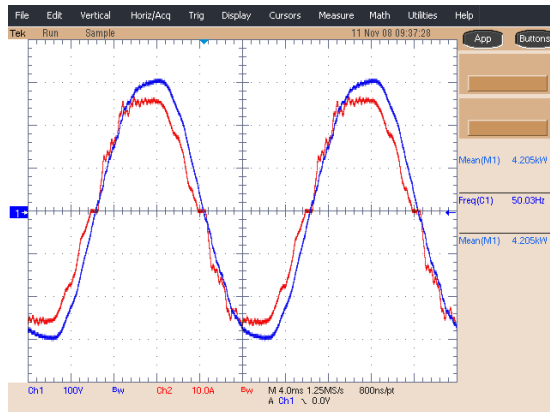


Fig.7 Experimental Result

V. CONCLUSION

In this paper, the mathematical model of PFC is built based on analyzing the controller UC3854. This model describes the object by virtue of the transfer function, which is different from the traditional way that uses switch to build the main circuit. Its advantage lies in that the causality of variables is more explicit. The corresponding simulation and experiment are implemented and the circuit power factor obtained is 96.7%, which demonstrates the model's usefulness for designing the controller of the PFC circuit.

REFERENCES

- [1] Weiping zhang "the modeling and controlling of switching converter" 2006
- [2] Abraham I. Pressman, and Zhiqiang Wang , "Switching Power Supply Design (Second Edition)"
- [3] Naigang Hong, "MATLAB simulation of power electric and power diver",2007.
- [4] Yujie Shi, Yi Bo, "double-cycle control of PFC", journal of Information Engineering Institute, Vol.18 No.3 Sep 1999
- [5] Zhimin Zhou, Jihai Zhou, Aihua Ji, "The design and application of PFC" 2004