SOUTH AFRICAN MATHEMATICS OLYMPIAD

Junior Grade 8 Round 1 2011 Solutions

1. **B**
$$2 + 3 \times 10 = 2 + 30 = 32$$

2. **D**
$$0.014 \times 0.4 = 0.0056$$

3. **C** $4 \times 365 = 1460$ and $5 \times 365 = 1825$; since 1500 lies between these, the child has lived between 4 and 5 years: at the next birthday he will turn 5.

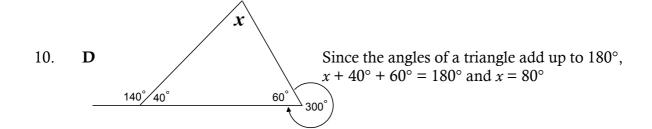
4. **A**
$$4\frac{1}{4} - 3.25 = 4.25 - 3.25 = 1.00$$
.

5. **D** $1^2 = 1$ ends in 1; $2^2 = 4$ ends in 4; $3^2 = 9$ ends in 9; $4^2 = 16$ ends in 6; $5^2 = 25$ ends in 5. Only answer D remains.

6. **C**
$$2030 \div 7 = 290$$

7. **A 7 4 2** equals
$$7 + 4 \div 2 = 7 + 2 = 9$$

- 8. **E** The fractions are $1 \frac{1}{10}$; $1 + \frac{1}{13}$; $1 \frac{1}{20}$; $1 + \frac{1}{120}$; $1 \frac{1}{212}$ so the last one differs from 1 by least
- 9. **B** 2011 201.1 is 1809.9



- 11. **D** The LCM of 3, 4 and 6 is 12; therefore the medication will be taken by all of them again at the same time after 12 hours, which will be at 18:00.
- 12. **C** Debbie is the tallest, so she must have height 150 cm. Amy is the shortest, with height 75 cm. Dawn is taller than Sarah, so has the larger remaining height.
- 13. **B** The shaded triangle CPQ is half of rectangle BCPQ. CP has length one-third of the length of CD, so BCPQ has area one-third of ABCD. Thus triangle CPQ has area 1/6 of ABCD.

- 14. **B** 8 km is 5 miles, and $120 = 8 \times 15$, so 120 km is $5 \times 15 = 75$ miles.
- 15. \mathbf{E} Continuing the pattern a bit further \mathbf{C} A В D \mathbf{E} shows clearly that the last digits in the 4 7 13 1 10 columns simply alternate, with all the 28 25 22 19 16 numbers ending in 3 in the last column 31 34 37 40 43 49 46 . . .
- 16. **B** The eleven numbers have a sum of $11 \times 18 = 198$. When 42 is added we have twelve numbers with a total of 240, so their average must be $240 \div 12 = 20$.
- 17. **C** Pairing the terms shows the sum is (1-2) + (3-4) + ... + (2009 2010) + 2011, which is -1 1 1 ... + 2011, with the -1 appearing 2010/2 = 1005 times. So the sum is 2011 1005 = 1006.

 Alternatively, pair the numbers thus: 1 + (-2 + 3) + (-4 + 5) + ... + (-2010 + 2011), obtaining 1 + 1 + ... with $1 + \frac{1}{2}(2010)$ 1s, totalling 1006.
- 18. **E** The last digits of the numbers given are 1–1, 9–4 etc. All end in 0 or 5 except for the last one which ends in 3.
- 19. **B** The number of polygons in the stages is 1; 4; 7; ..., adding 3 each time. By stage 100 a total of $99 \times 3 = 297$ squares have been added to the original hexagon, giving 298 polygons.
- 20. **C** The pentagons have a total of $12 \times 5 = 60$ edges, and the hexagons have a total of $20 \times 6 = 120$ edges. All these 180 edges must be joined in pairs at the seams, so 90 pairings, i.e. seams, are needed.