

# Variance

$$\text{sd}(x) \\ = \sqrt{\text{Var}(x)}$$

1. Variance:  $\text{Var}(x) = E[(x - \mu_x)^2] = E[x^2] - (\mu_x)^2 = E[x^2] - [E(x)]^2$ .

1)  $x \sim \text{Bernulli}(\theta)$ ,  $\text{Var}(x) = \theta(1-\theta)$ .

2)  $x \sim \text{Binomial}(n, \theta)$ ,  $\text{Var}(x) = n \cdot \theta \cdot (1-\theta)$ .

3)  $x \sim \text{Geometric}(\theta)$ ,  $\text{Var}(x) = \frac{1-\theta}{\theta^2}$ .

4)  $x \sim \text{Poisson}(\lambda)$ ,  $\text{Var}(x) = \lambda$ .

5)  $x \sim \text{Uniform}[L, R]$ ,  $\text{Var}(x) = \frac{(R-L)^2}{12}$ .

6)  $x \sim \text{Exponential}(\lambda)$ ,  $\text{Var}(x) = \frac{1}{\lambda^2}$ .

7)  $x \sim \text{Normal}(\mu, \sigma^2)$ ,  $\text{Var}(x) = \sigma^2$ .

8)  $\text{Var}(ax+b) = a^2 \text{Var}(x)$ .

2. Suppose  $x, y$  are independent.

1)  $\text{Var}(x+y) = \text{Var}(x) + \text{Var}(y)$

2)  $\text{sd}(x+y) = \sqrt{\text{sd}(x)^2 + \text{sd}(y)^2}$

