

# Relational Database Design

Chapter 15 in 6<sup>th</sup> Edition

# 10 Relational Database Design

Anomalies can be removed from relation designs by decomposing them until they are in a normal form.

Several problems should be investigated regarding a decomposition.

A decomposition of a relation scheme,  $R$ , is a set of relation schemes  $\{R_1, \dots, R_n\}$  such that  $R_i \subseteq R$  for each  $i$ , and  $\bigcup_{i=1}^n R_i = R$

Note that in a decomposition  $\{R_1, \dots, R_n\}$ , the intersect of each pair of  $R_i$  and  $R_j$  does not have to be empty.

Example:  $R = \{A, B, C, D, E\}$ ,  $R_1 = \{A, B\}$ ,  $R_2 = \{A, C\}$ ,  $R_3 = \{C, D, E\}$

A naïve decomposition: each relation has only attribute.

A good decomposition should have the following two properties.

# Dependency Preserving

- Definition: Two sets  $F$  and  $G$  of FD's are equivalent if  $F^+ = G^+$ .
- Given a decomposition  $\{R_1, \dots, R_n\}$  of  $R$ :

$$F_i = \{X \rightarrow Y : X \rightarrow Y \in F \& X \in R_i, Y \in R_i\}.$$

- The decomposition  $\{R_1, \dots, R_n\}$  of  $R$  is dependency preserving with respect to  $F$  if

$$F^+ = \left( \bigcup_{i=1}^n F_i \right)^+.$$

# Examples

$F = \{ A \rightarrow BC, D \rightarrow EG, M \rightarrow A \}, R = (A, B, C, D, E, G, M, A)$

1) Given  $R_1 = (A, B, C, M)$  and  $R_2 = (C, D, E, G)$ ,

$F_1 = \{ A \rightarrow BC, M \rightarrow A \}, F_2 = \{ D \rightarrow EG \}$

$F = F_1 \cup F_2$ . thus, dependency preserving

2) Suppose that  $F' = F \cup \{ M \rightarrow D \}$ .  $R_1$  and  $R_2$  remain the same.

Thus,  $F_1$  and  $F_2$  remain the same.

We need to verify if  $M \rightarrow D$  is inferred by  $F_1 \cup F_2$ .

Since  $M^+ \mid_{F_1 \cup F_2} = \{M, A, B, C\}$ ,  $M \rightarrow D$  is not inferred by  $F_1 \cup F_2$ .

Thus,  $R_1$  and  $R_2$  are not dependency preserving regarding  $F'$ .

3)  $F'' = \{ A \rightarrow BC, D \rightarrow EG, M \rightarrow A, M \rightarrow C, C \rightarrow D, M \rightarrow D \}$

$F_1 = \{ A \rightarrow BC, M \rightarrow A, M \rightarrow C \}, F_2 = \{ D \rightarrow EG, C \rightarrow D \}$

It can be verified that  $M \rightarrow D$  is inferred by  $F_1$  and  $F_2$ .

Thus,  $F''^+ = (F_1 \cup F_2)^+$

Hence,  $R_1$  and  $R_2$  are dependency preserving regarding  $F''$ .

# Lossless Join Decomposition

- A second necessary property for decomposition:
- A decomposition  $\{R_1, \dots, R_n\}$  of  $R$  is a *lossless join* decomposition with respect to a set  $F$  of FD's if for every relation instance  $r$  that satisfies  $F$ :

$$r = \pi R_1(r) \bowtie \dots \bowtie \pi R_n(r).$$

If  $r \subset \pi R_1(r) \bowtie \dots \bowtie \pi R_n(r)$ , the decomposition is *lossy*.

# Lossless Join Decomposition<sub>(cont)</sub>

*Example 2:*

Suppose that we decompose the following relation:

STUDENT_ADVISOR		
Name	Department	Advisor
Jones	Comp Sci	Smith
Ng	Chemistry	Turner
Martin	Physics	Bosky
Dulles	Decision Sci	Hall
Duke	Mathematics	James
James	Comp Sci	Clark
Evan	Comp Sci	Smith
Baxter	English	Bronte

With dependencies  $\{Name \rightarrow Department, Name \rightarrow Advisor, Advisor \rightarrow Department\}$ , into two relations:

# Lossless Join Decomposition<sub>(cont)</sub>

STUDENT\_DEPARTMENT

Name	Department
Jones	Comp Sci
Ng	Chemistry
Martin	Physics
Duke	Mathematics
Dulles	Decision Sci
James	Comp Sci
Evan	Comp Sci
Baxter	English

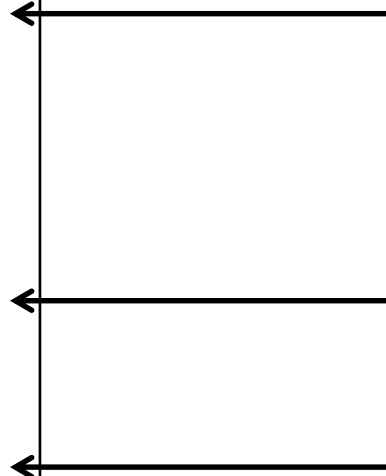
DEPARTMENT\_ADVISOR

Department	Advisor
Comp Sci	Smith
Chemistry	Turner
Physics	Bosky
Decision Sci	Hall
Mathematics	James
Comp Sci	Clark
English	Bronte

If we join these decomposed relations we get:

# Lossless Join Decomposition<sub>(cont)</sub>

Name	Department	Advisor
Jones	Comp Sci	Smith
Jones	Comp Sci	Clark*
Ng	Chemistry	Turner
Martin	Physics	Bosky
Dulles	Decision Sci	Hall
Duke	Mathematics	James
James	Comp Sci	Smith*
James	Comp Sci	Clark
Evan	Comp Sci	Smith
Evan	Comp Sci	Clark*
Baxter	English	Bronte



- This is not the same as the original relation (the tuples marked with \* have been added). Thus the decomposition is lossy.
- Useful theorem: The decomposition  $\{R_1, R_2\}$  of  $R$  is lossless iff the common attributes  $R_1 \cap R_2$  form a superkey for either  $R_1$  or  $R_2$ .



# Lossless Join Decomposition<sub>(cont)</sub>

- *Example 3:* Given  $R(A,B,C)$  and  $F = \{A \rightarrow B\}$ . The decomposition into  $R_1(A,B)$  and  $R_2(A,C)$  is lossless because  $A \rightarrow B$  is an FD over  $R_1$ , so the common attribute  $A$  is a key of  $R_1$ .

# 10.1 Testing for the lossless join property

- Algorithm TEST LJ

Step 1: Create a matrix  $S$ , each element  $s_{i,j} \in S$  corresponds the relation  $R_i$  and the attribute  $A_j$ , such that:

$$s_{j,i} = a \text{ if } A_i \in R_j, \text{ otherwise } s_{j,i} = b.$$

Step 2: Repeat the following process till  $S$  has no change or one row is made up entirely of “a” symbols.

Step 2.1: For each  $X \rightarrow Y$ , choose the rows where the elements corresponding to  $X$  take the value a.

Step 2.2: In those chosen rows (must be at least two rows), the elements corresponding to  $Y$  also take the value a if one of the chosen rows take the value a on  $Y$ .

# 10.1 Testing for the lossless join property<sub>(cont)</sub>

- The decomposition is *lossless* if one row is entirely made up by “a” values.
- The algorithm can be found as the Algorithm 15.2 in E/N book.
- Note: The correctness of the algorithm is based on the assumption that no null values are allowed for the join attributes.

If and only if exists an order such that  $R_i \cap M_{i-1}$  forms

a superkey of  $R_i$  or  $M_{i-1}$ , where  $M_{i-1}$  is the join on  $R_1, R_2, \dots, R_{i-1}$

# 10.1 Testing for the lossless join property<sub>(cont)</sub>

*Example:*  $R = (A, B, C, D)$ ,  $F = \{A \rightarrow B, A \rightarrow C, C \rightarrow D\}$ .

Let  $R_1 = (A, B, C)$ ,  $R_2 = (C, D)$ .

Initially,  $S$  is

	A	B	C	D
$R_1$	a	a	a	b
$R_2$	b	b	a	a

Note: rows 1 and 2 of  $S$  agree on  $\{C\}$ , which is the left hand side of  $C \rightarrow D$ . Therefore, change the  $D$  value on rows 1 to a, matching the value from row 2.

Now row 1 is entirely  $a$ 's, so the decomposition is lossless.

(Check it.)

# 10.1 Testing for the lossless join property<sub>(cont)</sub>

*Example 4:*  $R = (A, B, C, D, E)$ ,

$F = \{AB \rightarrow CD, A \rightarrow E, C \rightarrow D\}$ . Let  $R_1 = (A, B, C)$ ,

$R_2 = (B, C, D)$  and  $R_3 = (C, D, E)$ .

*Example 5:*  $R = (A, B, C, D, E, F)$ ,

$F = \{A \rightarrow B, C \rightarrow DE, AB \rightarrow F\}$ . Let  $R_1 = (A, B)$ ,

$R_2 = (C, D, E)$  and  $R_3 = (A, C, F)$ .

# 10.1 Testing for the lossless join property<sub>(cont)</sub>

*Example 5:*  $R = (A, B, C, D, E, G)$ ,

$F = \{AB \rightarrow G, C \rightarrow DE, A \rightarrow B, \}$ .

Let  $R_1 = (A, B,)$ ,  $R_2 = (C, D, E)$  and  $R_3 = (A, C, G)$ .

	A	B	C	D	E	G
$R_1$	a	a	b	b	b	b
$R_2$	b	b	a	a	a	b
$R_3$	a	b	a	b	b	a

	A	B	C	D	E	G	
$R_1$	a	a	b	b	b	b	←
$R_2$	b	b	a	a	a	b	
$R_3$	a	<del>x</del>	a	a	a	a	←

↑  
a

# 10.2 Lossless decomposition into BCNF

## Algorithm TO\_BCNF

$D := \{R_1, R_2, \dots, R_n\}$

**While**  $\exists$  a  $R_i \in D$  and  $R_i$  is not in BCNF **Do**

{ find a  $X \rightarrow Y$  in  $R_i$  that violates BCNF; replace  $R_i$  in  $D$  by  $(R_i - Y)$  and  $(X \cup Y)$ ; }

$F = \{A \rightarrow C, A \rightarrow D, C \rightarrow E, E \rightarrow D, C \rightarrow G\},$

$R1 = (C, D, E, G), R2 = (A, C, D)$

$R11 = (C, E, G), R12 = (E, D)$  due  $E \rightarrow D$

$R21 = (A, C), R22 = (C, D)$  because of  $C \rightarrow D$

# 10.2 Lossless decomposition into BCNF

## Algorithm TO\_BCNF

$D := \{R_1, R_2, \dots, R_n\}$

**While**  $\exists$  a  $R_i \in D$  and  $R_i$  is not in BCNF **Do**

{ find a  $X \rightarrow Y$  in  $R_i$  that violates BCNF; replace  $R_i$  in  $D$  by  $(R_i - Y)$  and  $(X \cup Y)$ ; }

Since a  $X \rightarrow Y$  violating BCNF is not always in  $F$ , the main difficulty is to verify if  $R_i$  is in BCNF; see the approach below:

1. For each subset  $X$  of  $R_i$ , compute  $X^+$ .
2.  $X \rightarrow (X^+|_{R_i} - X)$  violates BCNF, if  $X^+|_{R_i} - X \neq \emptyset$  and  $R_i - X^+ \neq \emptyset$ .

Here,  $X^+|_{R_i} - X = \emptyset$  means that each F.D with  $X$  as the left hand side is trivial;

$R_i - X^+ = \emptyset$  means  $X$  is a superkey of  $R_i$



# 10.2 Lossless decomposition into BCNF<sub>(cont)</sub>

*Example 6:*(From Desai 6.35)

Find a BCNF decomposition of the relation scheme below:

*SHIPPING*(*Ship* , *Capacity* , *Date* , *Cargo* , *Value*)

F consists of:

$Ship \rightarrow Capacity$

$\{Ship, Date\} \rightarrow Cargo$

$\{Cargo, Capacity\} \rightarrow Value$

# 10.2 Lossless decomposition into BCNF<sub>(cont)</sub>

From  $Ship \rightarrow Capacity$ , we decompose *SHIPPING* into

$R_1(Ship, Date, Cargo, Value)$

Key:  $\{Ship, Date\}$

A nontrivial FD in  $F^+$  violates BCNF:

$\{Ship, Cargo\} \rightarrow Value$

$Ship \rightarrow Capacity$

$\{Ship, Date\} \rightarrow Cargo$

$\{Cargo, Capacity\} \rightarrow Value$

and

$R_2(Ship, Capacity)$

Key:  $\{Ship\}$

Only one nontrivial FD in  $F^+$ :  $Ship \rightarrow Capacity$

## 10.2 Lossless decomposition into BCNF<sub>(cont)</sub>

$R_1$  is not in BCNF so we must decompose it further into

$R_{11}(Ship, Date, Cargo)$

Key:  $\{Ship, Date\}$

$Ship \rightarrow Capacity$

$\{Ship, Date\} \rightarrow Cargo$

$\{Cargo, Capacity\} \rightarrow Value$

Only one nontrivial FD in  $F^+$  with single attribute on the right side:  $\{Ship, Date\} \rightarrow Cargo$

And

$R_{12}(Ship, Cargo, Value)$

Key:  $\{Ship, Cargo\}$

Only one nontrivial FD in  $F^+$  with single attribute on the right side:  $\{Ship, Cargo\} \rightarrow Value$

This is in BCNF and the decomposition is lossless but not dependency preserving (the FD  $\{Capacity, Cargo\} \rightarrow Value$  has been lost).

# 10.2 Lossless decomposition into BCNF<sub>(cont)</sub>

Or we could have chosen  $\{Cargo, Capacity\} \rightarrow Value$ , which would give us:

$R_1 (Ship, Capacity, Date, Cargo)$

Key:  $\{Ship, Date\}$

A nontrivial FD in  $F^+$  violates BCNF:

$Ship \rightarrow Capacity$

$Ship \rightarrow Capacity$

$\{Ship, Date\} \rightarrow Cargo$

$\{Cargo, Capacity\} \rightarrow Value$

and

$R_2 (Cargo, Capacity, Value)$

Key:  $\{Cargo, Capacity\}$

Only one nontrivial FD in  $F^+$  with single attribute on the right side:  $\{Cargo, Capacity\} \rightarrow$

$Value$

# 10.2 Lossless decomposition into BCNF<sub>(cont)</sub>

and then from  $Ship \rightarrow Capacity$ ,

$R_{11}(Ship, Date, Cargo)$

Key:  $\{Ship, Date\}$

Only one nontrivial FD in  $F^+$  with single attribute

on the right side:  $\{Ship, Date\} \rightarrow Cargo$

And

$R_{12}(Ship, Capacity)$

Key:  $\{Ship\}$

Only one nontrivial FD in  $F^+$ :  $Ship \rightarrow Capacity$

This is in BCNF and the decomposition is both lossless and dependency preserving.

However, there are relation schemes for which there is no lossless, dependency preserving decomposition into BCNF.

