

$id$	$::=$	
$v$	$::=$	Values
	<b>b</b>	Boolean
	<b>n</b>	Number
	<b>str</b>	String
	<b>undefined</b>	Undefined
	<b>null</b>	null
	$get(s, id)$ <b>M</b>	GetStore
$s$	$::=$	Store
	$put(s, id, v)$ <b>M</b>	PutStore
$vd$	$::=$	VariableDeclaration
	$id$	Declaration
	$id = e$	Definition
	$vd, vd'$	Multiple
$e$	$::=$	Expression
	$v$	Value
	$id$	Deref
	$id = e$	Ref
$m$	$::=$	Statement
	$e$	Expression
	$\epsilon$	Skip
	$m; m'$	Seq
	<b>var</b> $vd$	VarDeclaration
$Tv$	$::=$	Value Type
	<b>number</b>	Number
	<b>boolean</b>	Boolean
	<b>string</b>	String
	<b>undefined</b>	undefined
	<b>null</b>	null
$T$	$::=$	Expression Type
	$Tv$	ValueType
	$ref\langle Tv \rangle$	Location Type
$X$	$::=$	
	$S$	
$C$	$::=$	Constraints
	$S$	
$S$	$::=$	Set

		$\emptyset$	EmptySet
		$\{T\}$	Singleton
		$X \cup X'$	Union
		$X \cap X'$	Intersect
<i>terminals</i>	$::=$		
		$\rightarrow$	
		$\Gamma$	
		$\vdash$	
		$;$	
		<b>var</b>	
		$\emptyset$	
<i>formula</i>	$::=$		
		<i>judgement</i>	
<i>Jop</i>	$::=$		
		$\langle m, s \rangle \rightarrow \langle m', s' \rangle$	
		$\Gamma(id) = T$	M
		$\Gamma \vdash e : T \mid_X C$	
		$\Gamma \vdash m \mid_X C$	
<i>judgement</i>	$::=$		
		<i>Jop</i>	
<i>user_syntax</i>	$::=$		
		<i>id</i>	
		<i>v</i>	
		<i>s</i>	
		<i>vd</i>	
		<i>e</i>	
		<i>m</i>	
		<i>Tv</i>	
		<i>T</i>	
		<i>X</i>	
		<i>C</i>	
		<i>S</i>	
		<i>terminals</i>	

$$\boxed{\langle m, s \rangle \rightarrow \langle m', s' \rangle}$$

$$\begin{array}{c}
\frac{}{\langle v; e, s \rangle \rightarrow \langle e, s \rangle} \text{ SEQ1} \\
\frac{\langle e_1, s \rangle \rightarrow \langle e'_1, s' \rangle}{\langle e_1; e_2, s \rangle \rightarrow \langle e'_1; e_2, s' \rangle} \text{ SEQ2} \\
\frac{\langle e, s \rangle \rightarrow \langle e', s' \rangle}{\langle id = e, s \rangle \rightarrow \langle id = e', s' \rangle} \text{ ASSIGN1} \\
\frac{}{\langle id = v, s \rangle \rightarrow \langle v, put(s, id, v) \rangle} \text{ ASSIGN2} \\
\frac{}{\langle id, s \rangle \rightarrow \langle get(s, id), s \rangle} \text{ Deref}
\end{array}$$

$$\frac{}{\langle \mathbf{var} \ id = e, s \rangle \rightarrow \langle id = e, s \rangle} \text{VAR1}$$

$$\frac{}{\langle \mathbf{var} \ id, s \rangle \rightarrow \langle \mathbf{undefined}, s \rangle} \text{VAR2}$$

$$\frac{}{\langle \mathbf{var} \ vd, vd', s \rangle \rightarrow \langle \mathbf{var} \ vd; \mathbf{var} \ vd', s \rangle} \text{VAR3}$$

$$\boxed{\Gamma(id) = T}$$

$$\boxed{\Gamma \vdash e : T \mid_X C}$$

$$\frac{}{\Gamma \vdash \mathbf{n} : \mathbf{number} \mid_{\emptyset} \emptyset} \text{V\_NUM}$$

$$\frac{}{\Gamma \vdash \mathbf{b} : \mathbf{boolean} \mid_{\emptyset} \emptyset} \text{V\_BOOL}$$

$$\frac{}{\Gamma \vdash \mathbf{str} : \mathbf{string} \mid_{\emptyset} \emptyset} \text{V\_STRING}$$

$$\frac{}{\Gamma \vdash \mathbf{undefined} : \mathbf{undefined} \mid_{\emptyset} \emptyset} \text{V\_UNDEFINED}$$

$$\frac{}{\Gamma \vdash \mathbf{null} : \mathbf{null} \mid_{\emptyset} \emptyset} \text{V\_NULL}$$

$$\frac{\Gamma(id) = T}{\Gamma \vdash id : T \mid_{\{T\}} \emptyset} \text{IDTYPE}$$

$$\Gamma \vdash id : T_1 \mid_{X_1} C_1$$

$$\Gamma \vdash e : T_2 \mid_{X_2} C_2$$

$$\langle \langle \text{no parses (char 2): !*** X1 n X2 = X1 n X(T2) = X2 n X(T1) = \{\}} \rangle \rangle$$

$$\langle \langle \text{no parses (char 2): !*** X' = X1 u X2} \rangle \rangle$$

$$\langle \langle \text{no parses (char 2): !*** C' = C1 u C2 u \{T1 = ref\langle T2 \rangle\}} \rangle \rangle$$

$$\Gamma \vdash id = e : T_2 \mid_{X'} C'$$

ASSIGNTYPE

$$\boxed{\Gamma \vdash m \mid_X C}$$

$$\frac{}{\Gamma \vdash \epsilon \mid_{\emptyset} \emptyset} \text{SKIPTYPABLE}$$

$$\frac{}{\Gamma \vdash \mathbf{var} \ id \mid_{\emptyset} \emptyset} \text{DECTYPABLE}$$

$$\frac{\Gamma \vdash e : T \mid_X C}{\Gamma \vdash e \mid_X C} \text{EXPTYPABLE}$$

$$\Gamma \vdash m_1 \mid_{X_1} C_1$$

$$\Gamma \vdash m_2 \mid_{X_2} C_2$$

$$\langle \langle \text{no parses (char 2): !***X1 n X2 = \{\}} \rangle \rangle$$

$$\langle \langle \text{no parses (char 2): !***C' = C1 u C2} \rangle \rangle$$

$$\langle \langle \text{no parses (char 2): !***X' = X1 u X2} \rangle \rangle$$

$$\Gamma \vdash m_1; m_2 \mid_{X'} C'$$

SEQTYPABLE

$$\Gamma \vdash \mathbf{var} \ id \mid_{X_1} C$$

$$\Gamma \vdash id = e : T \mid_{X_2} C$$

$$\langle \langle \text{no parses (char 2): !***X1 n X2 = \{\}} \rangle \rangle$$

$$\langle \langle \text{no parses (char 2): !***C' = C1 u C2} \rangle \rangle$$

$$\langle \langle \text{no parses (char 2): !***X' = X1 u X2} \rangle \rangle$$

$$\Gamma \vdash \mathbf{var} \ id = e \mid_{X'} C'$$

DEFTYPABLE

$$\begin{array}{c}
\Gamma \vdash \mathbf{var} \, vd \mid_{X_1} C_1 \\
\Gamma \vdash \mathbf{var} \, vd' \mid_{X_1} C_2 \\
\text{<<no parses (char 2): !***X1 n X2 = \{\} >>} \\
\text{<<no parses (char 2): !***C' = C1 u C2 >>} \\
\text{<<no parses (char 2): !***X' = X1 u X2 >>} \\
\hline
\Gamma \vdash \mathbf{var} \, vd, vd' \mid_{X'} C'
\end{array}$$

MULTIDECTypeABLE

Definition rules: 17 good 4 bad  
Definition rule clauses: 33 good 12 bad