

$$Q = \sigma^2 = 0.35^2 = 0.1225$$

$$M = \begin{bmatrix} \alpha_1 \delta_{rot1}^2 + \alpha_2 \delta_{trans}^2 & 0 & 0 \\ 0 & \alpha_3 \delta_{trans}^2 + \alpha_4 (\delta_{rot1}^2 + \delta_{rot2}^2) & 0 \\ 0 & 0 & \alpha_1 \delta_{rot2}^2 + \alpha_2 \delta_{trans}^2 \end{bmatrix}$$

Where:

- \* $\alpha_1 = 0.05$ (turning noise)
- \*  $\alpha_2 = 0.001$ (movement noise, quadratic dependence)
- \*  $\alpha_3 = 0.05$ (translation noise)
- \*  $\alpha_4 = 0.01$ (noise from errors in turning)

Substituting:  $u = [0, 10, 0]^T$  :

$$M = \begin{bmatrix} 0.05^2 \cdot 0^2 + 0.001^2 \cdot 10^2 & 0 & 0 \\ 0 & 0.05^2 \cdot 10^2 + 0.01^2 (0^2 + 0^2) & 0 \\ 0 & 0 & 0.05^2 \cdot 0^2 + 0.001^2 \cdot 10^2 \end{bmatrix}$$

$$M = \begin{bmatrix} 0.05^2 & 0 & 0 \\ 0 & 0.05^2 & 0 \\ 0 & 0 & 0.05^2 \end{bmatrix}$$

$$G_t = \frac{\partial g(x_{t-1}, u_t, \epsilon_t)}{\partial x_{t-1}} \bigg|_{\mu_{t-1}, \epsilon_t = 0} = \begin{bmatrix} 1 & 0 & -\delta_{trans} \sin(\theta + \delta_{rot1}) \\ 0 & 1 & \delta_{trans} \cos(\theta + \delta_{rot1}) \\ 0 & 0 & 1 \end{bmatrix}$$

$$V_t = \frac{\partial g(x_{t-1}, u_t, \epsilon_t)}{\partial u_t} \bigg|_{\mu_{t-1}, \epsilon_t = 0} = \begin{bmatrix} -\delta_{trans} \sin(\theta + \delta_{rot1}) & \cos(\theta + \delta_{rot1}) & 0 \\ \delta_{trans} \cos(\theta + \delta_{rot1}) & \sin(\theta + \delta_{rot1}) & 0 \\ 1 & 0 & 1 \end{bmatrix}$$

$$H_t = \frac{\partial h(x_t)}{\partial x_t}$$

$$z = h(x_t) = \text{atan2}(m_y - y, m_x - x) - \theta$$

Where:

- \*  $(x, y, \theta)$ —current state of the robot,
- \*  $(m_x, m_y)$ —coordinates of the landmark,
- \*  $z$ —measured angle to the landmark.

$$H_t = \begin{bmatrix} \frac{-(m_y - y)}{(m_x - x)^2 + (m_y - y)^2} & \frac{(m_x - x)}{(m_x - x)^2 + (m_y - y)^2} & -1 \end{bmatrix}$$