Hellenic Complex Systems Laboratory

A Software Tool for Calculating the Uncertainty of Diagnostic Accuracy Measures

Technical Report XXVIII

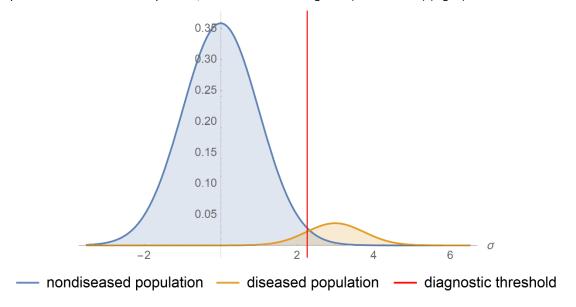
# Abstract

Screening and diagnostic tests are applied for the classification of people into diseased and non-diseased populations. Although diagnostic accuracy measures are used to evaluate the correctness of a classification in clinical research and practice, there has been limited research on their uncertainty. The objective for this work was to develop a tool for calculating the uncertainty of diagnostic accuracy measures, as diagnostic accuracy is fundamental to clinical decision-making. For this reason, the freely available interactive program Diagnostic Uncertainty has been developed in the Wolfram Language. The program provides six modules with nine submodules for calculating and plotting the standard combined, measurement and sampling uncertainty and the resultant confidence intervals of various diagnostic accuracy measures of screening or diagnostic tests, which measure a normally distributed measurand, applied at a single point in time to samples of non-diseased and diseased populations. This is done for differing sample sizes, mean and standard deviation of the measurand, diagnostic threshold and standard measurement uncertainty of the test. The application of the program is demonstrated with an illustrative example of glucose measurements in samples of diabetic and non-diabetic populations, that shows the calculation of the uncertainty of diagnostic accuracy measures. The presented interactive program is user-friendly and can be used as a flexible educational and research tool in medical decision-making, to calculate and explore the uncertainty of diagnostic accuracy measures.

Keywords: diagnostic accuracy measures; uncertainty; measurement uncertainty; sampling uncertainty; diagnostic tests; screening tests;

## Introduction

An increasing number of in vitro screening and diagnostic tests are extensively used as binary classifiers in medicine, to classify people in the non-overlapping classes of populations with and without a disease, which are categorized as quantitative and qualitative. The quantitative and many qualitative screening or diagnostic tests are based on measurements. There is a joint probability distribution of the measurements in the diseased and non-diseased populations. To classify the patients with and without a disease using a test based on a measurement, a diagnostic threshold or cutoff point is defined. If the measurement is above the threshold the patient is classified as test-positive, otherwise as test-negative (or vice versa) (Fig. 1).



**Figure 1. Probability density function plots.** The probability density functions plots of a measurand in a non-diseased and diseased population.

The possible test results are summarized in Table 1.

Table 1: A2x2 Contingency Table

		populations			
		nondiseased	diseased		
test result s	negative	true negative (TN)	false negative (FN)		
	positive	false positive (FP)	true positive (TP)		

# Diagnostic accuracy measures

From the large number of diagnostic accuracy measures (DAM) appearing in literature, only a few are used for evaluating the diagnostic accuracy in clinical research and practice (1). These include:

- 1. Sensitivity (Se), specificity (Sp), overall diagnostic accuracy (ODA), diagnostic odds ratio (DOR), likelihood ratios for positive or negative result (LR + and LR respectively), that are defined conditionally on the true disease status (2) and are prevalence invariant.
- 2. Overall diagnostic accuracy (*ODA*), that is defined conditionally on the true disease status and is prevalence dependent.
- 3. Positive predictive and negative predictive values (*PPV* and *NPV*), that are defined conditionally on the test outcome and are prevalence dependent.

The natural frequency and the equivalent probability definitions of the diagnostic accuracy measures derived from Table 1 and analyzed by the program, are presented in Table 2. The symbols are explained in the Notation Section.

**Table 1:** Natural frequency and probability definitions of diagnostic accuracy measures

measure	natural frequency definition	probability definition		
Se	$\frac{TP}{FN+TP}$	Pr(T D)		
Sp	$\frac{TN}{TN + FP}$	$Prig(\overline{T} \overline{D}ig)$		
PPV	$\frac{TP}{FP+TP}$	Pr(D T)		
NPV	$\frac{TN}{TN+FN}$	$Pr(\overline{D} \overline{T})$		
ODA	$\frac{TN + TP}{TN + FN + TP + FP}$	$Pr(D) Pr(T D) + Pr(\overline{D}) Pr(\overline{T} \overline{D})$		
DOR	$\frac{TNTP}{FNFP}$	$rac{Pr(T D)}{Pr(\overline{T} D)} \ rac{Pr(T \overline{D})}{Pr(\overline{T} \overline{D})}$		
LR+	$\frac{TP(FP+TN)}{FP(FN+TP)}$	$\frac{Pr(T D)}{Pr(T \overline{D})}$		
LR-	$\frac{FN(FP+TN)}{TN(FN+TP)}$	$rac{Prig(\overline{T} Dig)}{Prig(\overline{T} \overline{D}ig)}$		
J	$\frac{TNTP - FNFP}{(TN + FP)(FN + TP)}$	$Pr(T D) + Pr(\overline{T} \overline{D}) - 1$		
ED	$\sqrt{\left(\frac{FN}{FN+TP}\right)^2 + \left(\frac{FP}{TN+FP}\right)^2}$	$\sqrt{Pr(\overline{T} D)^2 + Pr(T \overline{D})^2}$		
CZ	$\frac{TN TP}{(TN + FP)(FN + TP)}$	$Pr(T D) \ Pr(\overline{T} \overline{D})$		

# Uncertainty of diagnostic accuracy measures

Uncertainty is an expression of imperfect or deficient information. When quantifiable it can be represented with probability (3). The following components of the combined uncertainty of the diagnostic accuracy measures will be considered:

### Measurement uncertainty

As there is inherent variability in any measurement process, there is measurement uncertainty, which is defined as a "parameter, associated with the result of a measurement, that characterizes the dispersion of the values that could reasonably be attributed to the measurand" (4).

The measurement uncertainty is gradually replacing the total analytical error concept (5).

### Sampling uncertainty

Diagnostic accuracy measures are estimated by applying a diagnostic method upon samples of populations. Therefore, sampling variability contributes to their uncertainty (6).

# **Implementation**

# Computational methods

For the calculation of the uncertainty of the diagnostic accuracy measures of a screening or diagnostic test based on a measurand, it is assumed that:

- 1. There is a reference ("gold standard") diagnostic method classifying correctly a subject as diseased or non-diseased (7).
- 2. Either the values of the measurand or their transforms (8, 9) are normally distributed in each of the diseased and non-diseased populations.
- 3. Measurement uncertainty is normally distributed and homoscedastic in the diagnostic threshold's range.

Thereafter, we use the term measurand to describe either the normally distributed value of a measurand or its normally distributed applicable transform.

# Diagnostic accuracy measures

The definitions of the diagnostic accuracy measures can be expressed in terms of sensitivity (Se), specificity (Sp), and rate of prevalence (r). These definitions are derived from Table 2 and presented in Table 3.

Table 3: Definitions of diagnostic accuracy measures versus sensitivity and specificity

measure	definition		
PPV	Se v		
PPV	$\overline{Se\ r + (1 - Sp)(1 - r)}$		
NPV	Sp(1-r)		
INFV	$\overline{Sp(1-r) + (1-Se)r}$		
ODA	$Se \ v + Sp \ (1-r)$		
	Se		
DOR	$\frac{\overline{1-Se}}{1-Sp}$		
Don			
	Sp		
LR+	Se		
LIN	$\overline{1-Sp}$		
4.0	1 – <i>Se</i>		
LR-	$\overline{Sp}$		
J	Se + Sp - 1		
ED	$\sqrt{(1-Se)^2+(1-Sp)^2}$		
CZ Se Sp			

The functions of sensitivity (Se) and specificity (Sp), hence the functions of all the above diagnostic accuracy measures, can be expressed in terms of the cumulative distribution function of the normal distribution, therefore of the error function and the complementary error function.

The error function erf(x) is defined as:

$$erf(x) = \frac{2}{\sqrt{\pi}} \int_0^x e^{-t^2} dt, x \ge 0$$

while the complementary error function erfc(x) is defined as:

$$erfc(x) = 1 - erf(x) = \frac{2}{\sqrt{\pi}} \int_{x}^{\infty} e^{-t^2} dt, x \ge 0$$

Following the definition of the sensitivity and specificity of a test (Table 2), the respective functions versus diagnostic threshold d are calculated as:

$$se(d, \mu_D, \sigma_D) = 1 - \Psi(d, \mu_D, \sigma_D) = \frac{1}{2} \left( 1 + erf\left(\frac{-d + \mu_D}{\sqrt{2}\sigma_D}\right) \right)$$

$$sp(d,\mu_{\overline{D}},\sigma_{\overline{D}}) = \Psi(d,\mu_{\overline{D}},\sigma_{\overline{D}}) = \frac{1}{2}erfc\left(\frac{-d+\mu_{\overline{D}}}{\sqrt{2}\sigma_{\overline{D}}}\right)$$

### Uncertainty

The uncertainty of an input parameter or a diagnostic accuracy measure x, can be expressed in the forms of standard and expanded uncertainty. The former, denoted as u(x), equals the standard deviation of x. The later, denoted as U(x), is defined as an interval around x including x with probability p (10).

### Measurement uncertainty of means and standard deviations

The standard measurement uncertainty is estimated as described in "Expression of Measurement Uncertainty in Laboratory Medicine" (11). Bias may be considered as a component of the standard measurement uncertainty (12).

# Sampling uncertainty of means and standard deviations

If  $m_P$  and  $s_P$  the mean and standard deviation of a measurand in a population sample of size  $n_P$ , then the standard sampling standard uncertainties of  $m_P$  and  $s_P$  are:

$$u_s(m_P) = \frac{s_P}{\sqrt{n_P}}$$

$$u_s(s_P) = \frac{s_P}{\sqrt{2(n_P - 1)}}$$

$$6$$

### Combined uncertainty of means and standard deviations

If  $u_m$  the standard measurement uncertainty of a screening or diagnostic test measuring a measurand, then the standard combined uncertainties of the mean  $m_p$  and standard deviation  $s_p$  are:

$$u_c(m_P) = \sqrt{\frac{s^2}{n} + u_m^2}$$

$$u_{cs}(s_P) = \sqrt{\frac{s^2}{2(n-1)} + u_m^2}$$
8

### Sampling uncertainty of prevalence

If  $n_{\overline{D}}$  and  $n_{\overline{D}}$  the respective numbers of nondiseased and diseased in a population sample, then the standard uncertainty  $u_r$  of the prevalence rate  $r=\frac{n_{\overline{D}}}{n_{\overline{D}}+n_{\overline{D}}}$  of the disease can be approximated as:

$$u_{s}(r) = \sqrt{\frac{(2+n_{\bar{D}})(2+n_{\bar{D}})}{(n_{\bar{D}}+n_{\bar{D}})(4+n_{\bar{D}}+n_{\bar{D}})^{2}}}$$

according to the Agresti-Coull adjustment of Waldo interval (13).

### Combined uncertainty of diagnostic accuracy measures

The standard combined uncertainty  $u_c$  of each diagnostic accuracy measure is calculated by applying the rules of uncertainty propagation from the input values to the calculated diagnostic accuracy measure, using first order Taylor series expansion (14).

When there are I components of uncertainty, with standard uncertainties  $u_i$  respectively, then:

$$u_c(x) = \sqrt{\sum_{i=1}^{l} u_i(x)^2}$$

### Expanded uncertainty of diagnostic accuracy measures

The effective degrees of freedom  $v_{eff}$  of the combined uncertainty  $u_c$  are calculated using the The effective degrees of freedom  $v_{eff}$  of the combined uncertainty  $u_c$  are calculated using the Welch–Satterthwaite formula (15, 16):

$$v_{eff} = \frac{u_c^4}{\left(\sum_{i=1}^l \frac{u_i^2}{v_i}\right)^2}$$
 11

Consequently, if  $v_{min}$  and  $v_{max}$  the minimum and maximum of  $(v_1, v_2, ..., v_l)$ , it can be shown that:

$$v_{min} \le v_{eff} \le v_{max}$$

If  $F_{\nu}(z)$  the cumulative distribution function of the Student's t-distribution with  $\nu$  degrees of freedom and  $u_c$  the standard combined uncertainty of a diagnostic accuracy measure, its expanded combined uncertainty  $U_c$ , at a confidence level p, is calculated as:

$$U_c(x) = \left(F_v^{-1}\left(\frac{1-p}{2}\right)u_c(x), F_v^{-1}\left(\frac{1+p}{2}\right)u_c(x)\right)$$
 13

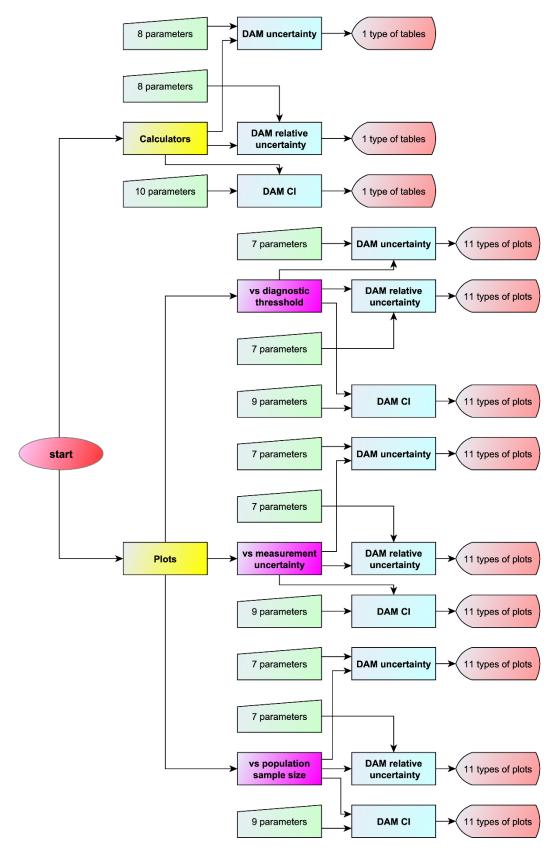
The resultant confidence interval of x, at the same confidence level p, is:

$$CI_p(x) = \left(x + F_v^{-1}\left(\frac{1-p}{2}\right)u_c(x), x + F_v^{-1}\left(\frac{1+p}{2}\right)u_c(x)\right)$$
 14

# The program

To calculate the uncertainty of the diagnostic accuracy measures, an interactive program written in Wolfram Language (17) was developed using Wolfram Mathematica® (18). This program was designed to provide six modules with nine submodules, for calculating and plotting the standard uncertainty and the resultant confidence intervals of various diagnostic accuracy measures of a screening or diagnostic test, applied at a single point in time in non-diseased and diseased population samples (Fig. 2). The test measures a measurand in the population samples, for varying values of their sizes, mean and standard deviation, and standard measurement uncertainty of the measurand. It is assumed that the measurands and measurement uncertainty are normally distributed and that measurement uncertainty is homoscedastic.

The program is freely available as a Wolfram Mathematica Notebook (.nb) (Supplementary file Uncertainty.nb). It can be run on Wolfram Player® or Wolfram Mathematica® (see Section 6).



**Figure 2. Program flowchart.** A simplified flowchart of the program with the number of the input parameters and of the output types for each module.

# Results

# Interface of the program

The modules of the program include panels with controls which allow the interactive manipulation of various parameters, as described in detail in the Appendix. These are the following:

### **Plots**

### Plots vs diagnostic threshold module

Diagnostic accuracy measures standard uncertainties plots submodule
The values of the standard combined, measurement, and sampling uncertainties of the diagnostic accuracy
measures of a screening or diagnostic test are plotted versus the diagnostic threshold of the test (Fig. 3).

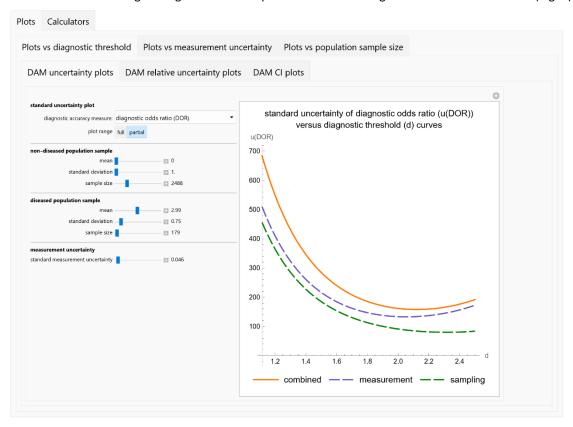


Figure 3. Plots vs diagnostic threshold module, DAM uncertainty submodule screenshot. Standard combined, sampling, and measurement uncertainty of diagnostic odds ratio (u(DOR)) versus diagnostic threshold (d) curve plot, with the settings shown at the left.

Diagnostic accuracy measures relative standard uncertainties plots submodule
The values of the relative standard combined, measurement, and sampling uncertainties of the diagnostic
accuracy measures of a screening or diagnostic test are plotted versus the diagnostic threshold of the test (Fig. 4).

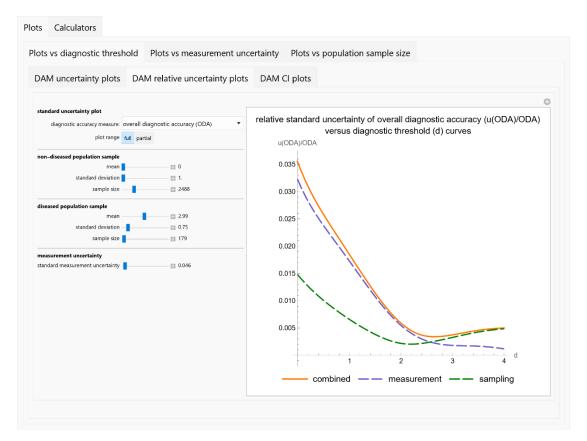
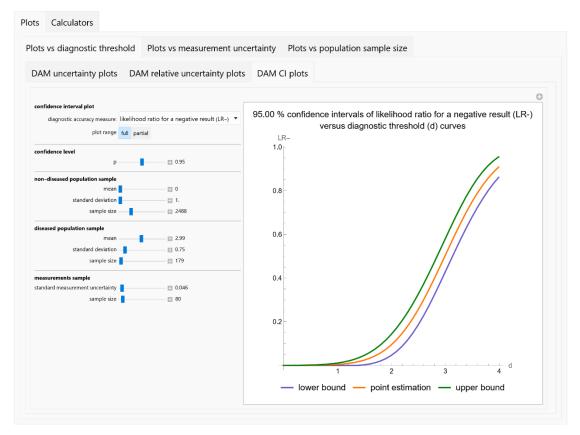


Figure 4. Plots vs diagnostic threshold module, DAM relative uncertainty submodule screenshot. Relative standard combined, sampling, and measurement uncertainty of overall diagnostic accuracy (u(ODA)) versus diagnostic threshold (a) curve plot, with the settings shown at the left.

Confidence intervals of diagnostic accuracy measures plots submodule

The values of the lower and upper bounds of the confidence intervals of a diagnostic accuracy measure of a screening or diagnostic test, at a selected confidence level, are plotted versus the diagnostic threshold of the test (Fig. 5).



**Figure 5. Plots vs diagnostic threshold module, DAM CI submodule screenshot.** Confidence intervals of likelihood ratio for a negative test result (u(LR-)) versus diagnostic threshold (d) curves plot, with the settings shown at the left.

Plots vs measurement uncertainty module

Diagnostic accuracy measures standard uncertainties plots submodule
The values of the standard combined, measurement, and sampling uncertainties of the diagnostic accuracy
measures of a screening or diagnostic test are plotted versus the measurement uncertainty of the test (Fig. 6).

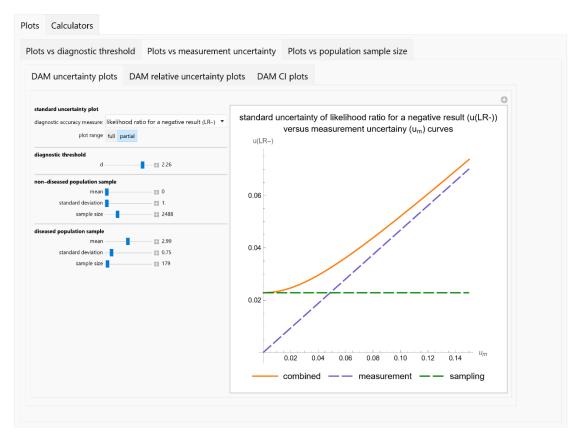


Figure 6. Plots vs measurement uncertainty module, DAM uncertainty submodule screenshot. Standard combined, sampling, and measurement uncertainty of likelihood ratio for a negative test result (u(LR-)) versus standard measurement uncertainty  $(u_m)$  curve plot, with the settings shown at the left.

Diagnostic accuracy measures relative standard uncertainties plots submodule The values of the relative standard combined, measurement, and sampling uncertainties of the diagnostic accuracy measures of a screening or diagnostic test are plotted versus the measurement uncertainty of the test (Fig. 7).

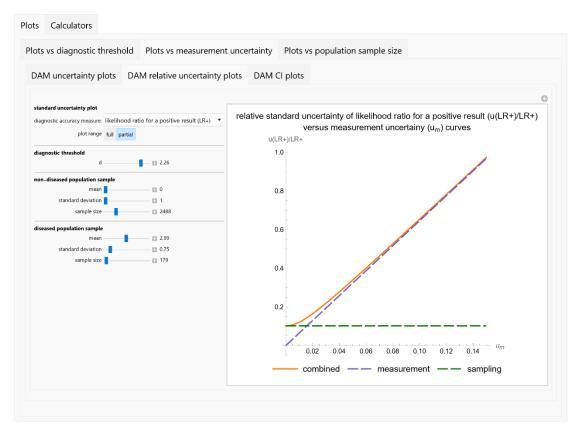


Figure 7. Plots vs measurement uncertainty module, DAM relative uncertainty submodule screenshot. Relative standard combined, sampling, and measurement uncertainty of likelihood ratio for a positive test result (u(LR+)) vs measurement uncertainty  $(u_m)$  curves plot, with the settings shown at the left.

Confidence intervals of diagnostic accuracy measures plots submodule

The values of the lower and upper bounds of the confidence intervals of a diagnostic accuracy measure of a screening or diagnostic test, at a selected confidence level, are plotted versus the measurement uncertainty of the test (Fig. 8).

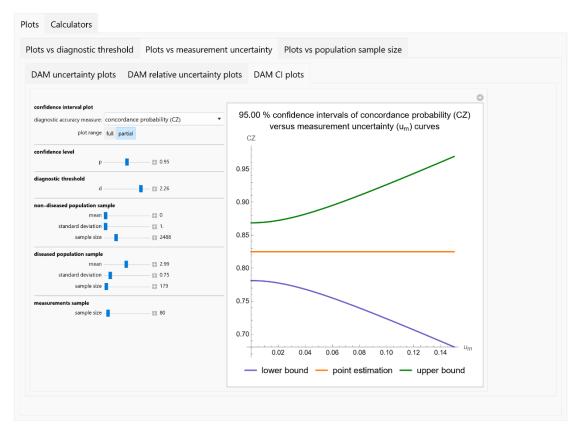


Figure 8. Plots vs measurement uncertainty module, DAM CI submodule screenshot. Confidence intervals of concordance probability (CZ) versus standard measurement uncertainty ( $u_m$ ) curves plot, with the settings shown at the left.

### Plots vs population sample size

Diagnostic accuracy measures standard uncertainties plots submodule

The values of the standard combined, measurement, and sampling uncertainties of the diagnostic accuracy measures of a screening or diagnostic test are plotted versus the total population sample size (Fig. 9).

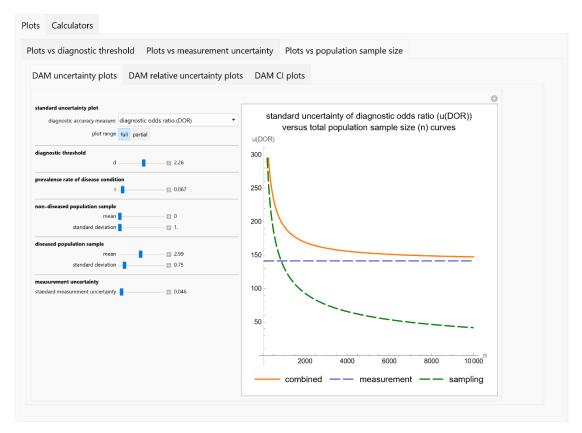


Figure 9. Plots vs total population sample size module, DAM uncertainty submodule screenshot. Standard combined, sampling, and measurement uncertainty of diagnostic odds ratio (u(DOR)) versus total population sample size (n) curves plot, with the settings shown at the left.

Diagnostic accuracy measures relative standard uncertainties plots submodule
The values of the relative standard combined, measurement, and sampling uncertainties of the diagnostic
accuracy measures of a screening or diagnostic test are plotted versus the total population sample size (Fig.
10).

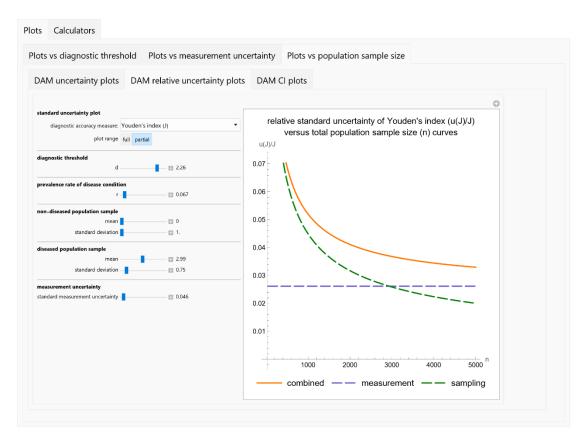


Figure 10. Plots vs population sample size module, DAM relative uncertainty submodule screenshot. Relative standard combined, sampling, and measurement uncertainty of Youden's index (u(f)) versus total population sample size (n) curves plot, with the settings shown at the left.

Confidence intervals of diagnostic accuracy measures plots submodule

The values of the lower and upper bounds of the confidence intervals of a diagnostic accuracy measure of a screening or diagnostic test, at a selected confidence level, are plotted versus the total population sample size (Fig. 11).

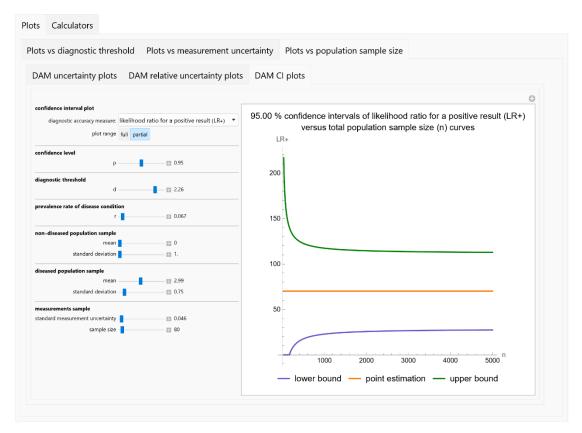
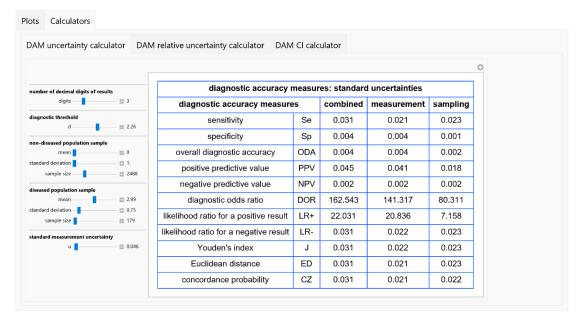


Figure 11. Plots vs population sample size module, DAM CI submodule screenshot. Confidence intervals of likelihood ratio for a positive test result (LR+) versus total population sample size (n) curves plot, with the settings shown at the left.

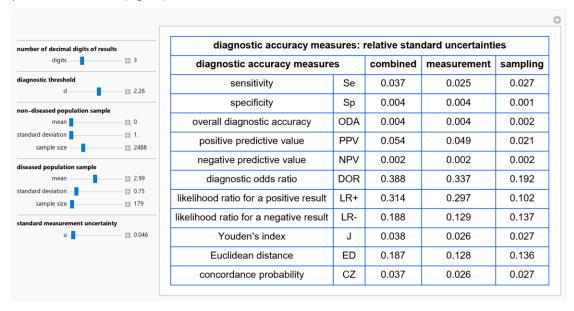
#### Calculators

Diagnostic accuracy measures standard uncertainties calculator module
The values of the standard combined, measurement, and sampling uncertainties of the diagnostic accuracy
measures of a screening or diagnostic test, at a selected diagnostic threshold, are calculated and presented in
a table (Fig. 12).



**Figure 12.** *Calculators module, DAM uncertainty calculator submodule screenshot.* Calculated standard combined, measurement, and sampling uncertainty of diagnostic accuracy measures, with the settings shown at the left.

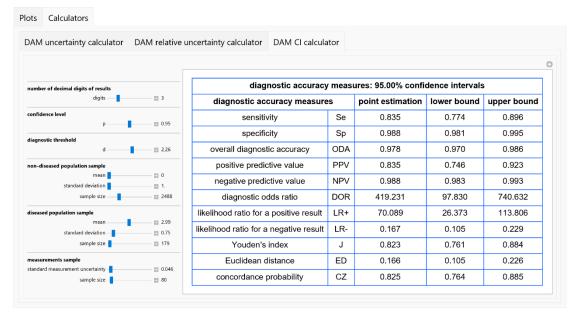
Diagnostic accuracy measures relative standard uncertainties calculator module The values of the relative standard combined, measurement, and sampling uncertainties of the diagnostic accuracy measures of a screening or diagnostic test, at a selected diagnostic threshold, are calculated and presented in a table (Fig. 13).



**Figure 13.** *Calculators module, DAM relative uncertainty calculator submodule screenshot.* Calculated relative standard combined, measurement, and sampling uncertainty of diagnostic accuracy measures, with the settings shown at the left.

Diagnostic accuracy measures confidence intervals calculator module

The values of the lower and upper bounds of the confidence intervals of various diagnostic accuracy measures
of a screening or diagnostic, at a selected confidence level and diagnostic threshold, are calculated and
presented in a table (Error! Reference source not found. 14).



**Figure 14. Calculators** *module, DAM CI calculator module screenshot.* Calculated confidence intervals of diagnostic accuracy measures, with the settings shown at the left.

# Illustrative case study

The program was applied to a bimodal joint distribution of log-transformed blood glucose measurements in non-diabetic and diabetic Malay populations, during an oral glucose tolerance test (OGTT) (19). Briefly, after the ingestion of 75 g glucose monohydrate, the 2-h postprandial blood glucose of 2667 Malay adults, aged 40 -49 years, was measured with reflectance photometry. The estimated prevalence of diabetes was 0.067, therefore the respective numbers of diseased and nondiseased were 179 and 2488. To estimate the distribution of the measurand in the diabetic and non-diabetic populations it was assumed that the measurement coefficient of variation and bias were equal to 4% and 2% respectively. The log-transformed measurands of each population were normally distributed, as shown in Fig. 1. In this case study, the normalized log-transformed measurand means and standard deviations in the diseased and non-diseased populations, the standard measurement uncertainty and the diagnostic threshold were expressed in units equal to the standard deviation of the log-transformed measurand in the non-diseased population. The normalized log-transformed diagnostic threshold 2.26 corresponds to the American Diabetes Association (ADA) diagnostic threshold for diabetes of the 2-h postprandial glucose during OGTT, that is equal to 11.1 mmol/I (20). The normalized log-transformed standard measurement uncertainty 0.046 of the test corresponds to standard measurement uncertainty equal to 2% of the mean of the measurand in the nondiabetic population, or equivalently to coefficient of variation equal to 2%.

The results of the illustrative case study are presented:

- 1. In the plots of Fig. 3-11 and 15-21.
- 2. In the chart of Fig. 22
- 3. In the tables of Fig. 12-14.

The parameter settings of Fig. 15-22 are presented in Table 4.

Table 4. The parameter settings of Fig. 15 - 22

settings	Fig. 15, 16	Fig. 17	Fig. 18	Fig. 19	Fig. 20	Fig. 21	Fig. 22
р	-	0.95	-	0.95	1	0.95	-
d	0.0-4.0	0.0 - 4.0	2.26	1	2.26	ı	2.26
r	ı	ı	-	1	0.067	0.067	•
$\mu_D$	2.99	2.99	2.99	2.99	2.99	2.99	2.99
$\sigma_D$	0.75	0.75	0.75	0.75	0.75	0.75	0.75
$n_D$	179	179	179	179	•	•	179
$\mu_{\overline{D}}$	0.0	0.0	0.0	0.0	0.0	0.0	0.0
$\sigma_{\overline{D}}$	1.0	1.0	1.0	1.0	1.0	1.0	1.0
$n_{\overline{D}}$	2488	2488	2488	2488	-	-	2488
n	-	-	-	-	30-5000	30-5000	-
$U_{m}$	0.046	0.046	0-0.15	0-0.15	0.046	0.046	0.046
$n_U$	-	80	-	80	-	80	-

The symbols of the settings column are explained in the Notation Section.

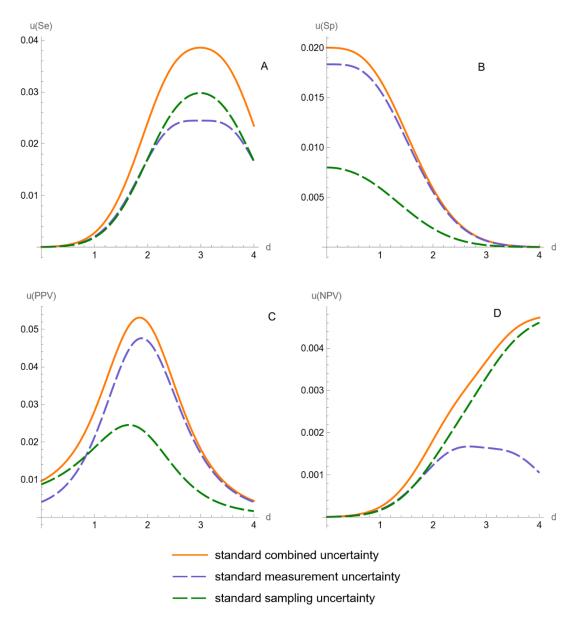


Figure 15. DAM standard uncertainties versus diagnostic threshold plots. Plots of standard combined, sampling, and measurement uncertainties of (A) sensitivity (Se), (B) specificity (Sp), (C) positive predictive

value (PPV) and (D) negative predictive value (NPV) versus diagnostic threshold (d) curves, with the respective parameters in Table 4.

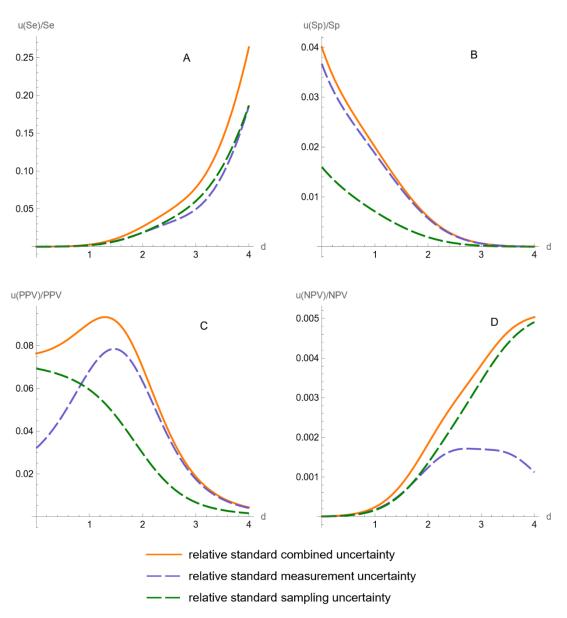
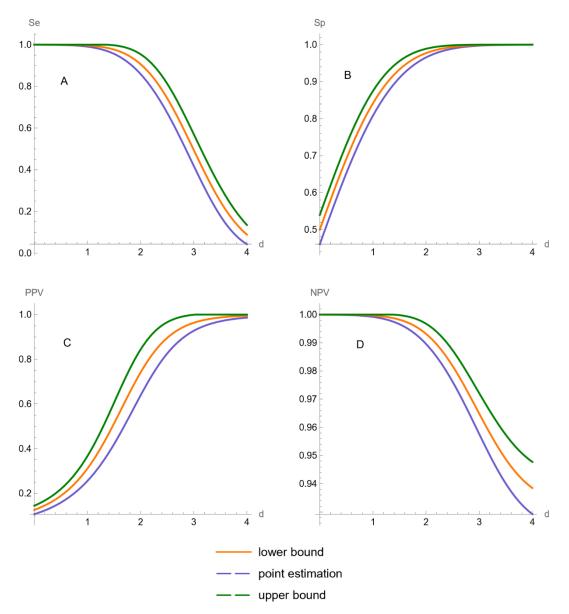


Figure 16. DAM relative standard uncertainties versus diagnostic threshold plots. Plots of relative standard combined, sampling, and measurement uncertainties of (A) sensitivity (Se), (B) specificity (Sp), (C) positive predictive value (PPV) and (D) negative predictive value (NPV) versus diagnostic threshold (d) curves, with the respective parameters in Table 4.



**Figure 17. DAM confidence intervals versus diagnostic threshold plots.** Plots of confidence intervals of (A) sensitivity (Se), (B) specificity (Sp), (C) positive predictive value (PPV) and (D) negative predictive value (NPV) versus diagnostic threshold (d) curves, with the respective parameters in Table 4.

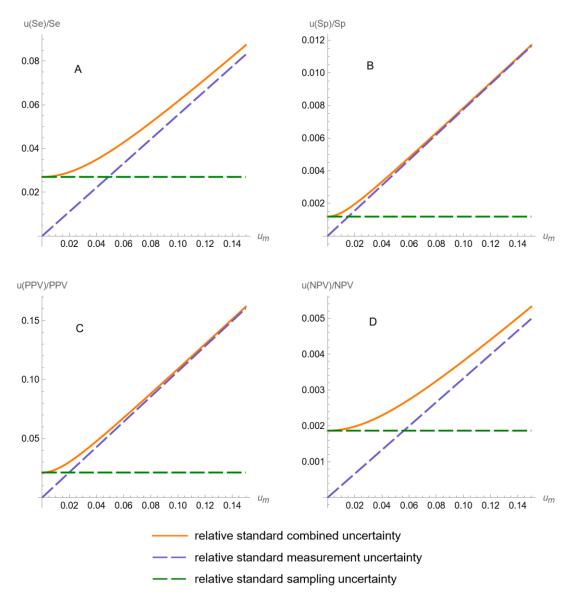


Figure 18. DAM standard uncertainties versus measurement uncertainty plots. Plots of relative standard combined, sampling, and measurement uncertainties of (A) sensitivity (Se), (B) specificity (Sp), (C) positive predictive value (PPV) and (D) negative predictive value (NPV) versus standard measurement uncertainty ( $u_m$ ) curves, with the respective parameters in Table 4.

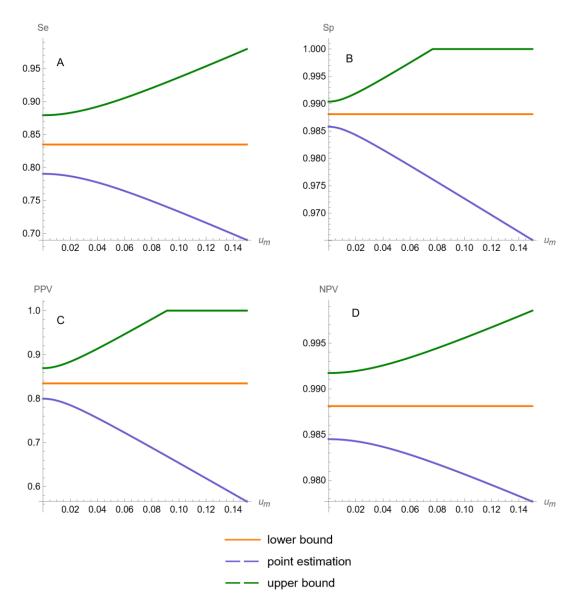


Figure 19. DAM confidence intervals versus measurement uncertainty plots. Plots of confidence intervals of (A) sensitivity (Se), (B) specificity (Sp), (C) positive predictive value (PPV) and (D) negative predictive value (NPV) versus standard measurement uncertainty ( $u_m$ ) curves, with the respective parameters in Table 4.

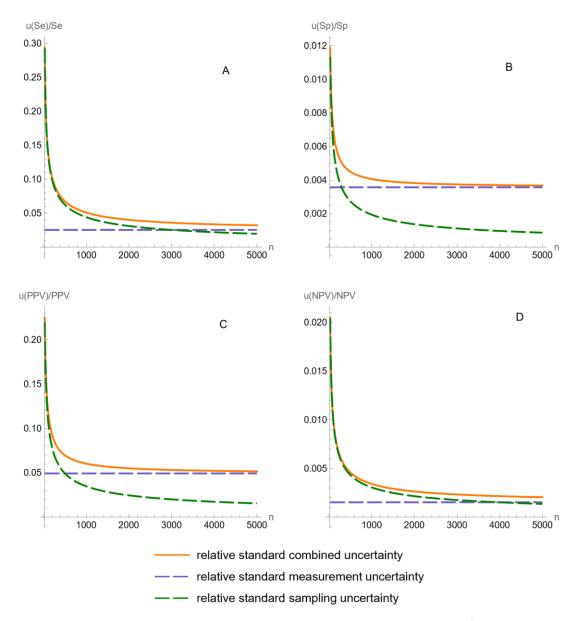


Figure 20. DAM standard uncertainties versus population sample size plots. Plots of relative standard combined, sampling, and measurement uncertainties of (A) sensitivity (Se), (B) specificity (Sp), (C) positive predictive value (PPV) and (D) negative predictive value (NPV) versus total population sample size (n) curves, with the respective parameters in Table 4.

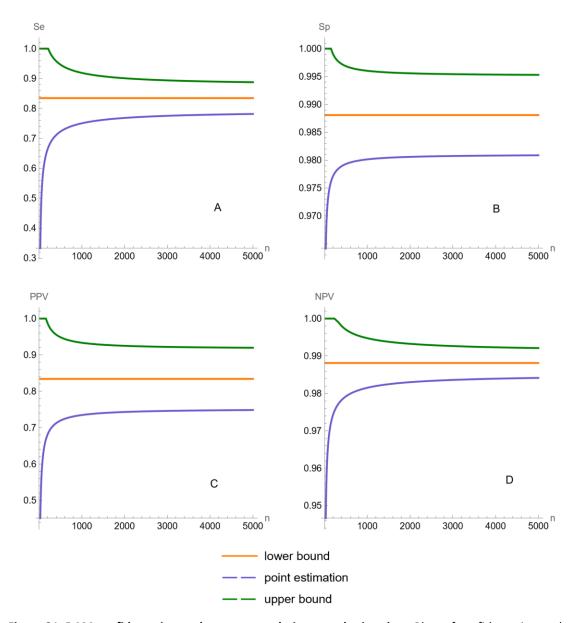


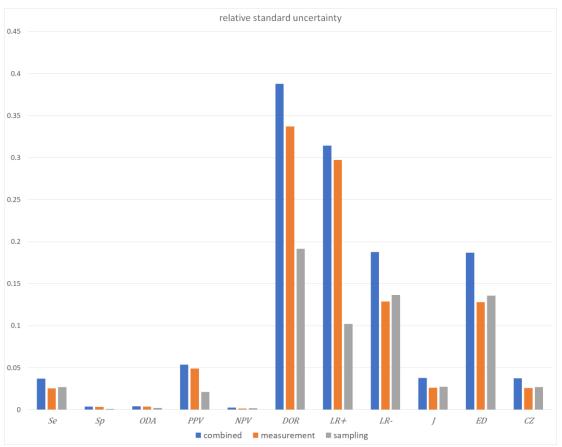
Figure 21. DAM confidence intervals versus population sample size plots. Plots of confidence intervals of (A) sensitivity (Se), (B) specificity (Sp), (C) positive predictive value (PPV) and (D) negative predictive value (NPV) versus total population sample size (n) curves, with the respective parameters in Table 4.

The combined uncertainty and the resultant confidence interval increase with measurement uncertainty (Fig. 6-8, 18, and 19) and decrease with total population sample size (Fig. 9-11, 20, and 21).

In the illustrative case study, combined uncertainty has (see Fig. 13 and Fig. 22):

- 1. Little effect ( $(u_c(x)/x)$ <0.5%) on specificity, overall diagnostic accuracy, and negative predictive value,
- 2. Intermediate effect  $(3.5\% < (u_c(x)/x) < 5.5\%)$  on sensitivity, positive predictive value, Youden's index, and concordance probability,
- 3. Greater effect  $(18\% < u_c(x)/x) < 39\%)$  on diagnostic odds ratio, on likelihood ratio for a positive or negative result, and Euclidean distance,

in accordance with previous findings (21-23).



**Figure 22. DAM relative standard uncertainties of diagnostic accuracy measures.** Histogram of standard combined, sampling, and measurement uncertainties of diagnostic accuracy measures, with the respective parameters in Table 4.

In addition, measurement uncertainty is the main component of the combined uncertainty of specificity, overall diagnostic accuracy, positive predictive value, diagnostic odds ratio, and likelihood ratio for a positive result.

### Discussion

There is a persistent need of estimating the uncertainty of diagnostic accuracy measures, especially regarding screening and diagnostic tests of life-threatening diseases. The current pandemic of novel corona virus disease 2019 (COVID-19) has exposed this convincingly (24-29).

This program has been developed to explore the combined measurement and sampling uncertainty of diagnostic accuracy measures as:

- 1. Diagnostic accuracy is fundamental to clinical decision-making (30),
- 2. Defining the permissible measurement uncertainty is critical to quality and risk management in laboratory medicine (31)
- 3. Sampling uncertainty is decisive for clinical study design to evaluate a screening or diagnostic test (32).

There has been extensive research on either diagnostic accuracy or uncertainty, however, very limited research has been done on both subjects (23, 33-35).

This program explores the combined uncertainty of diagnostic accuracy measures of a screening or diagnostic test (Fig. 3, 4, 6, 7, 9, 10, and 11-13) and the resultant confidence limits (Fig. 5, 8, 11 and 14). Combined uncertainty and the resultant confidence limits depend on the diagnostic threshold (Fig. 3-5, and 15-17), on

measurement uncertainty (Fig. 6-8, 18 and 19), and on population parameters, including total population sample size (Fig. 9-11, 20 and 21).

In antithesis to the complexity of the calculations, the program simplifies its exploration with a user-friendly interface. Furthermore, it provides calculators for the calculation of the components of uncertainty on the diagnostic accuracy measures and the resultant confidence intervals (Fig. 12-14).

As demonstrated by the illustrative case study described above (Section 3.2), in this instance the uncertainty has relatively little effect on specificity, overall diagnostic accuracy, and negative predictive value. However, it affects more sensitivity, positive predictive value, Youden's index, and concordance probability, while it has a considerable impact on diagnostic odds ratio, likelihood ratio for a positive or negative result, and Euclidean distance (Fig. 22). However, further research is needed to explore the uncertainty of diagnostic accuracy measures with different clinically and laboratory relevant parameter settings.

Shortcomings of this program, that could be improved by further research, are the following:

- 1. The assumptions used for the calculations:
  - 1.1. The existence of a "gold standard" diagnostic method. If a "gold standard" does not exist, there are alternative approaches for the estimation of diagnostic accuracy measures (36).
  - 1.2. The normality of either the measurements or their applicable transforms (8, 9, 37, 38), however, this is usually valid. There is related literature on the distribution of measurements of diagnostic tests, in the context of reference intervals and diagnostic thresholds or clinical decision limits (39-43).
  - 1.3. The bimodality of the measurands, that is generally accepted, although unimodal distributions could be considered (44, 45).
  - 1.4. The measurement uncertainty homoscedasticity in the diagnostic thresholds range. If measurement uncertainty is heteroscedastic, thus skewing the measurements distribution, appropriate transformations may restore homoscedasticity (46).

If the above assumptions are not valid, there are other components of uncertainty which are not calculated by this program.

- 2. The first order Taylor series expansion approximation used for the uncertainty propagation calculations (14).
- 3. The uncertainty of prevalence rate approximation by the Agresti-Coull adjusted Waldo interval (13), although there are more exact methods (47).

Nevertheless, addressing these shortcomings, increases exponentially the computational complexity.

The program complements the previously published tool for exploring the relation between diagnostic accuracy and measurement uncertainty (23).

All major general or medical statistical software packages (Matlab®, NCSS®, R, SAS®, SPSS®, Stata® and MedCalc®) include routines for the calculation and plotting of various diagnostic accuracy measures and their confidence intervals. The program presented in this work provides 99 different types of plots and 3 different types of comprehensive tables of the uncertainty of diagnostic accuracy measures and the resultant confidence intervals (Fig. 2), many of which are novel. To the best of our knowledge, no one of the above-mentioned programs or any other software provides this range of plots and tables without advanced statistical programming.

# Conclusion

This program calculates the uncertainty of diagnostic accuracy measures, their components, and the resultant confidence intervals and can be used as a flexible, user-friendly, interactive educational or research tool in medical decision-making.

# Availability and requirements

Project name: Diagnostic Uncertainty

Version: 2.0.0.1

Project home page: <a href="https://www.hcsl.com/Tools/Uncertainty/">https://www.hcsl.com/Tools/Uncertainty/</a>

Operating systems: Microsoft Windows, Linux, Apple iOS

Programming language: Wolfram Language

Other software requirements: Wolfram Player®, freely available at: https://www.wolfram.com/player/ or

Wolfram Mathematica®

System requirements: Intel Core i9 or equivalent CPU and 32GB+ of RAM

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# List of abbreviations

DAM: diagnostic accuracy measure

OGTT: oral glucose tolerance test

ADA: American Diabetes Association

COVID-19: novel corona virus disease 2019

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# Supplemental Material

The following supplemental files are available at <a href="https://www.hcsl.com/Supplements/SUDAM.zip">https://www.hcsl.com/Supplements/SUDAM.zip</a> (accessed on October 4, 2024):

- a) Supplemental File I:
  - Uncertainty.nb: The program *Diagnostic Uncertainty* as a Wolfram Notebook.
- b) Supplemental File II:
  - DiagnosticUncertaintyCalculations.nb: The calculations for estimating diagnostic accuracy measures and their standard uncertainty in a Wolfram Notebook
- Supplemental File III:
   DiagnosticUncertaintyCalculations.pdf: A brief interface documentation of the program.

### **Notation**

# **Populations**

 $\overline{D}$ : nondiseased population

D: diseased population

### Test outcomes

 $\overline{T}$ : negative test result

T: positive test result

TN: true negative test result

TP: true positive test result

FN: false negative test result

*FP*: false positive test result

# Diagnostic accuracy measures

Se: sensitivity
Sp: specificity

PPV: positive predictive valueNPV: negative predictive valueODA: overall diagnostic accuracy

DOR: diagnostic odds ratio

LR+: likelihood ratio for a positive test result

*LR*—: likelihood ratio for a negative test result

J: Youden's index

ED: Euclidean distance of a ROC curve point from the point (0,1)

CZ: concordance probability

### **Parameters**

 $\mu_P$ : mean of the measurand of a test in the population P

 $\sigma_P$ : standard deviation of the measurand of a test in the population P

 $n_P$ : size of a sample of the population P

r: prevalence of the disease

*d*: diagnostic threshold of a test

*p* : confidence level

 $u_s(x)$ : standard sampling uncertainty of x

 $u_m(x)$ : standard measurement uncertainty of x

 $u_c(x)$ : standard combined uncertainty of x

 $u_i(x)$ : the  $i^{th}$  component of the standard combined uncertainty of x

### Functions and relations

 $se\left(d_{m}\right)$ : sensitivity function of a single test versus its diagnostic threshold d

sp(d,...): specificity function of a single test versus its diagnostic threshold d

 $\Psi(x,\mu,\sigma)$ : cumulative distribution function of a normal distribution with mean  $\mu$  and standard deviation  $\sigma$ , evaluated at x

erf(x): error function, evaluated at x

erfc(x): complementary error function, evaluated at x

Pr(a): probability of an event a

 $Pr(a \mid b)$ : probability of an event a given the event b

 $CI_p(x)$ : confidence interval of x at confidence level p

 $F^{-1}(\dots)$ : the inverse function F

# **Appendix**

# About the program controls

The numerical settings are defined by the user with menus or sliders. Sliders can be finely manipulated by holding down the *alt* key or *opt* key while dragging the mouse. They be even more finely manipulated by also holding the *shift* and/or *ctrl* keys.

Dragging with the mouse rotates the three-dimensional plots, while dragging with the mouse while pressing the *ctrl*, *alt*, or *opt* keys zooms in or out.

# Range of parameters

```
Input parameters
```

*p*: 0.90 – 0.999

$$d: \max \{ \mu_D - 4, \mu_{\overline{D}} - 4\sigma_{\overline{D}} \} - \min \{ \mu_D + 4\sigma_D, \mu_{\overline{D}} + 4\sigma_{\overline{D}} \}$$

 $\mu_{\overline{D}}$ : 0 – 6

 $\sigma_{\overline{D}}$ : 1 – 6

 $n_{\overline{D}}$ : 2 – 10000

 $\mu_D$ : 0.1 – 6

 $\sigma_D$ : 0.1 – 6

 $n_D: 2 - 10000$ 

r. 0.001 - 0.999

 $u_m : 0 - 6$ 

 $n_u: 20 - 1000$ 

# Range of the coordinates of the plots

There are two options for the range of coordinates to be included in each plot:

- 1) Full: All the calculated coordinate points are plotted.
- 2) Partial: The distribution of coordinate values is found and any points sufficiently far out in the distribution are not considered.

#### **Abscissas**

# Full range

$$d$$
:  $(\max \{ \mu_D - 4\sigma_{\overline{D}}, \mu_{\overline{D}} - 4\sigma_{\overline{D}} \} - \min \{ \mu_D + 4\sigma_D, \mu_{\overline{D}} + 4\sigma_{\overline{D}} \})$ 

$$u_m$$
:  $(0 - 0.5 \sigma_{\overline{D}})$ 

$$n: (\max{\{\begin{bmatrix} \frac{2}{r} \end{bmatrix}, \begin{bmatrix} \frac{2}{1-r} \end{bmatrix}, 20\} - \max{\{10, \begin{bmatrix} \frac{2}{r} \end{bmatrix}, 10, \begin{bmatrix} \frac{2}{1-r} \end{bmatrix}, 10000\})}$$

### Partial range

$$d: (\max \{ \mu_D - 2.5\sigma_{\overline{D}}, \mu_{\overline{D}} - 2.5\sigma_{\overline{D}} \} - \min \{ \mu_D + 2.5\sigma_D, \mu_{\overline{D}} + 2.5\sigma_{\overline{D}} \})$$

$$u_m$$
:  $(0 - 0.15 \sigma_{\overline{D}})$ 

$$n \colon \left(\max\left\{\left[\frac{2}{r}\right], \left[\left[\frac{2}{1-r}\right], 20\right\} - \max\left\{5, \left[\left[\frac{2}{r}\right]\right], 5\left[\left[\frac{2}{1-r}\right]\right], 5000\right\}\right)$$

## Input and output

The program provides in six modules and nine submodules plots and tables of the uncertainty and the resultant confidence intervals of diagnostic accuracy measures of a screening or diagnostic test for a measurand, applied at a single point in time in samples of diseased and a non-diseased population.

Singularity points are excluded from the plots.

Indeterminate results of the calculation modules represent numerical quantities whose magnitudes cannot be determined, because they are either too small or too large.

#### **Plots**

Plots vs diagnostic threshold module

Diagnostic accuracy measures uncertainty plots submodule

#### Input

The user defines:

- 1) The diseased and nondiseased population samples parameters:
  - a) The measurand means,
  - b) The measurand standard deviations,
  - c) The sizes of the samples,
- 2) The diagnostic accuracy measure:
  - a) Sensitivity (Se),
  - b) Specificity (Sp),
  - c) Overall diagnostic accuracy (ODA),
  - d) Positive predictive value (PPV),
  - e) Negative predictive value (NPV),
  - f) Diagnostic odds ratio (DOR),
  - g) Likelihood ratio for a positive test result (LR+),
  - h) Likelihood ratio for a negative test result (LR -),
  - i) Youden's index (/),
  - j) Euclidean distance (ED),
  - k) Concordance probability (CZ),
- 3) The standard measurement uncertainty of the test.

### Output

Plots of the values of the:

- 1) Standard combined uncertainty,
- 2) Standard measurement uncertainty,
- 3) Standard sampling uncertainty

of the measure versus diagnostic threshold (d).

Diagnostic accuracy measures relative uncertainty plots submodule

#### Input

The user defines:

- 1) The diseased and nondiseased population samples parameters:
  - a) The measurand means,
  - b) The measurand standard deviations,
  - c) The sizes of the samples,
- 2) The diagnostic accuracy measure:
  - a) Sensitivity (Se),
  - b) Specificity (Sp),

- c) Overall diagnostic accuracy (ODA),
- d) Positive predictive value (PPV),
- e) Negative predictive value (NPV),
- f) Diagnostic odds ratio (DOR),
- g) Likelihood ratio for a positive test result (LR+),
- h) Likelihood ratio for a negative test result (LR-),
- i) Youden's index (/),
- j) Euclidean distance (ED),
- k) Concordance probability (CZ),
- 3) The standard measurement uncertainty of the test.

Plots of the values of the:

- 1) Relative standard combined uncertainty,
- 2) Relative standard measurement uncertainty,
- 3) Relative standard sampling uncertainty

of the measure versus diagnostic threshold (d).

Diagnostic accuracy measures confidence intervals plots submodule

### Input

The user defines:

- 1) The confidence level (p),
- 2) The diseased and nondiseased population samples parameters:
  - a) The measurand means,
  - b) The measurand standard deviations,
  - c) The sizes of the samples,
- 3) The diagnostic accuracy measure:
  - a) Sensitivity (Se),
  - b) Specificity (Sp),
  - c) Overall diagnostic accuracy (ODA),
  - d) Positive predictive value (PPV),
  - e) Negative predictive value (NPV),
  - f) Diagnostic odds ratio (DOR),
  - g) Likelihood ratio for a positive test result (LR+),
  - h) Likelihood ratio for a negative test result (LR-),
  - i) Youden's index (/),
  - j) Euclidean distance (ED),
  - k) Concordance probability (CZ),
- 4) The standard measurement uncertainty of the test,
- 5) The size of the sample of the measurements for the estimation of the measurement uncertainty.

#### **Output**

Plots of the values of the:

- 1) Lower bound,
- 2) Point estimation,
- 3) Upper bound

of the measure versus diagnostic threshold (d), at the selected confidence level.

### Plots vs measurement uncertainty module

Diagnostic accuracy measures uncertainty plots submodule

### Input

The user defines:

- 1) The diseased and nondiseased population samples parameters:
- 2) The diseased and nondiseased population samples parameters:
  - a) The measurand means,
  - b) The measurand standard deviations,
  - c) The sizes of the samples,
- 3) The diagnostic accuracy measure:
  - a) Sensitivity (Se),
  - b) Specificity (Sp),
  - c) Overall diagnostic accuracy (ODA),
  - d) Positive predictive value (PPV),
  - e) Negative predictive value (NPV),
  - f) Diagnostic odds ratio (DOR),
  - g) Likelihood ratio for a positive test result (LR+),
  - h) Likelihood ratio for a negative test result (LR-),
  - i) Youden's index (/),
  - j) Euclidean distance (ED),
  - k) Concordance probability (CZ).

#### **Output**

Plots of the values of the:

- 1) Standard combined uncertainty,
- 2) Standard measurement uncertainty,
- 3) Standard sampling uncertainty

of the measure versus standard measurement uncertainty  $(u_m)$ .

Diagnostic accuracy measures relative uncertainty plots submodule

#### Input

The user defines:

- 1) The diseased and nondiseased population samples parameters:
  - a) The prevalence of the disease,
  - b) The measurand means,
  - c) The measurand standard deviations,
- 2) The diagnostic accuracy measure:
  - a) Sensitivity (Se),
  - b) Specificity (Sp),
  - c) Overall diagnostic accuracy (ODA),
  - d) Positive predictive value (PPV),
  - e) Negative predictive value (NPV),
  - f) Diagnostic odds ratio (DOR),
  - g) Likelihood ratio for a positive test result (LR+),
  - h) Likelihood ratio for a negative test result (LR-),
  - i) Youden's index (/),
  - j) Euclidean distance (ED),
  - k) Concordance probability (CZ),
- 3) The standard measurement uncertainty of the test.

#### **Output**

Plots of the values of the:

- 1) Relative standard combined uncertainty,
- 2) Relative standard measurement uncertainty,
- 3) Relative standard sampling uncertainty

of the measure versus standard measurement uncertainty  $(u_m)$ .

Diagnostic accuracy measures confidence intervals plots submodule

#### Input

The user defines:

- 1) The confidence level (p),
- 2) The diseased and nondiseased population samples parameters:
  - a) The measurand means,
  - b) The measurand standard deviations,
  - c) The sizes of the samples,
- 3) The diagnostic accuracy measure:
  - a) Sensitivity (Se),
  - b) Specificity (Sp),
  - c) Overall diagnostic accuracy (ODA),
  - d) Positive predictive value (PPV),
  - e) Negative predictive value (NPV),
  - f) Diagnostic odds ratio (DOR),
  - g) Likelihood ratio for a positive test result (LR+),
  - h) Likelihood ratio for a negative test result (LR -),
  - i) Youden's index (/),
  - j) Euclidean distance (ED),
  - k) Concordance probability (CZ),
- 4) The size of the sample of the measurements for the estimation of the measurement uncertainty.

#### Output

Plots of the values of the:

- 4) Lower bound,
- 5) Point estimation,
- 6) Upper bound

of the measure versus standard measurement uncertainty ( $u_m$ ), at the selected confidence level.

Plots vs population size module

Diagnostic accuracy measures uncertainty plots submodule

#### Input

The user defines:

- 4) The diseased and nondiseased population samples parameters:
  - a) The prevalence of the disease,
  - b) The measurand means,
  - c) The measurand standard deviations,
- 5) The diagnostic accuracy measure:
  - a) Sensitivity (Se),
  - b) Specificity (Sp),
  - c) Overall diagnostic accuracy (ODA),
  - d) Positive predictive value (PPV),
  - e) Negative predictive value (NPV),
  - f) Diagnostic odds ratio (DOR),
  - g) Likelihood ratio for a positive test result (LR+),
  - h) Likelihood ratio for a negative test result (LR-),
  - i) Youden's index (/),

- i) Euclidean distance (ED),
- k) Concordance probability (CZ),
- 6) The standard measurement uncertainty of the test.

Plots of the values of the:

- 4) Standard combined uncertainty,
- 5) Standard measurement uncertainty,
- 6) Standard sampling uncertainty

of the measure versus total population size (n).

Diagnostic accuracy measures relative uncertainty plots submodule

#### Input

The user defines:

- 4) The diseased and nondiseased population samples parameters:
  - a) The prevalence of the disease,
  - b) The measurand means,
  - c) The measurand standard deviations,
- 5) The diagnostic accuracy measure:
  - a) Sensitivity (Se),
  - b) Specificity (Sp),
  - c) Overall diagnostic accuracy (ODA),
  - d) Positive predictive value (PPV),
  - e) Negative predictive value (NPV),
  - f) Diagnostic odds ratio (DOR),
  - g) Likelihood ratio for a positive test result (LR+),
  - h) Likelihood ratio for a negative test result (LR-),
  - i) Youden's index (/),
  - j) Euclidean distance (ED),
  - k) Concordance probability (CZ),
- 6) The standard measurement uncertainty of the test.

#### **Output**

Plots of the values of the:

- 4) Relative standard combined uncertainty,
- 5) Relative standard measurement uncertainty,
- 6) Relative standard sampling uncertainty

of the measure versus total population size (n).

Diagnostic accuracy measures confidence intervals plots submodule

### Input

The user defines:

- 5) The confidence level (p),
- 6) The diseased and nondiseased population samples parameters:
  - a) The prevalence of the disease,
  - b) The measurand means,
  - c) The measurand standard deviations,
- 7) The diagnostic accuracy measure:
  - a) Sensitivity (Se),
  - b) Specificity (Sp),
  - c) Overall diagnostic accuracy (ODA),
  - d) Positive predictive value (PPV),

- e) Negative predictive value (NPV),
- f) Diagnostic odds ratio (DOR),
- g) Likelihood ratio for a positive test result (LR+),
- h) Likelihood ratio for a negative test result (LR-),
- i) Youden's index (/),
- j) Euclidean distance (ED),
- k) Concordance probability (CZ),
- 8) The standard measurement uncertainty of the test,
- 9) The size of the sample of the measurements for the estimation of the measurement uncertainty.

Plots of the values of the:

- 7) Lower bound,
- 8) Point estimation,
- 9) Upper bound

of the measure versus total population size (n) at the selected confidence level.

#### Calculators

Diagnostic accuracy measures uncertainty calculator

#### Input

- 1) The number of the decimal digits of the results
- 2) The diagnostic threshold (d)
- 3) The diseased and nondiseased population samples parameters:
  - a) The measurand means,
  - b) The measurand standard deviations,
  - c) The sizes of the samples,
- 4) The standard measurement uncertainty of the test.

### Output

A table of the values of:

- 1) The standard combined uncertainty,
- 2) The standard measurement uncertainty,
- 3) The standard sampling uncertainty,

of the following diagnostic accuracy measures at the selected diagnostic threshold:

- 1) Sensitivity (Se),
- 2) Specificity (Sp),
- 3) Overall diagnostic accuracy (ODA),
- 4) Positive predictive value (PPV),
- 5) Negative predictive value (NPV),
- 6) Diagnostic odds ratio (DOR),
- 7) Likelihood ratio for a positive test result (LR+),
- 8) Likelihood ratio for a negative test result (LR-),
- 9) Youden's index (J),
- 10) Euclidean distance (ED),
- 11) Concordance probability (CZ).

Diagnostic accuracy measures relative uncertainty calculator

#### Input

- 1) The number of the decimal digits of the results
- 2) The diagnostic threshold (d),

- 3) The diseased and nondiseased population samples parameters:
  - a) The measurand means,
  - b) The measurand standard deviations,
  - c) The sizes of the samples,
- 4) The standard measurement uncertainty of the test.

A table of the values of:

- 1) The relative standard combined uncertainty,
- 2) The relative standard measurement uncertainty, and
- 3) The relative standard sampling uncertainty,

of the following diagnostic accuracy measures at the selected diagnostic threshold:

- 1) Sensitivity (*Se*),
- 2) Specificity (Sp),
- 3) Overall diagnostic accuracy (ODA),
- 4) Positive predictive value (PPV),
- 5) Negative predictive value (NPV),
- 6) Diagnostic odds ratio (DOR),
- 7) Likelihood ratio for a positive test result (LR+),
- 8) Likelihood ratio for a negative test result (LR-),
- 9) Youden's index (/),
- 10) Euclidean distance (ED),
- 11) Concordance probability (CZ).

Diagnostic accuracy measures confidence intervals calculator

#### Input

- 5) The number of the decimal digits of the results
- 1) The confidence level (p),
- 2) The diagnostic threshold (d),
- 3) The diseased and nondiseased population samples parameters:
  - a) The measurand means,
  - b) The measurand standard deviations.
  - c) The sizes of the samples,
- 4) The standard measurement uncertainty of the test,
- 5) The size of the sample of the measurements for the estimation of the measurement uncertainty.

### Output

A table of the values and the confidence intervals of the following diagnostic accuracy measures at the selected confidence level and diagnostic threshold:

- 1) Sensitivity (Se),
- 2) Specificity (Sp),
- 3) Overall diagnostic accuracy (*ODA*),
- 4) Positive predictive value (PPV),
- 5) Negative predictive value (NPV),
- 6) Diagnostic odds ratio (*DOR*),
- 7) Likelihood ratio for a positive test result (LR+),
- 8) Likelihood ratio for a negative test result (LR-),
- 9) Youden's index (/),
- 10) Euclidean distance (ED),
- 11) Concordance probability (CZ).

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