Elements of Design for Containers and Solutions in the LinBox library

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Abstract. We develop in this paper design techniques used in the C++ exact linear algebra library LinBox. They are intended to make the library safer and easier to use, while keeping it generic and efficient.

First, we review the new simplified structure of the containers, based on our *founding scope allocation* model (cf. [7]). Namely, vectors and matrix containers are all templated by a field and a storage type. Matrix interfaces all agree with the same minimal blackbox interface. This allows e.g. for a unification of our dense and sparse matrices, as well as a clearer model for matrices and submatrices. We explain the design choices and their impact on coding. We will describe serveral of the new containers, especially our sparse and dense matrices storages as well as their apply (blackbox) method and compare to previous implementations.

Then we present a variation of the *strategy* design pattern that is comprised of a controller–plugin system: the controller (solution) chooses among plug-ins (algorithms) and the plug-ins always call back the solution so a new choice can be made by the controller. We give examples using the solution mul, and generalise this design pattern to the library. We also show performance comparisons with former LinBox versions.

Finally we present a benchmark architecture that serves two purposes. The first one consists in providing the user with an easy way to produces graphs using C++. The second goal is to create a framework for automatically tuning the library (determine thresholds, choose algorithms) and provide a regression testing scheme.

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1 Introduction

The LinBox library is under constant evolution, driven by new problems and algorithms, new compilers, new computing paradigms. This poses new challenges. We are incrementally updating the design of the library towards a 2.0 release.

We show in the next table 1 the increase in the size⁶ of LinBox.

Table 1: Evolution of the number of lines of code (loc, in thousands) in LinBox, FFLAS and Givaro (†contains Givaro, ‡contains FFLAS).

LinBox								
loc	77.3	85.8	93.5	103	108	109	112	135
FFLAS	N/A	N/A	N/A	1.3.3	1.4.0	1.4.3	1.5.0	1.8.0
loc	_		_	11.6	23.9	25.2	25.5	32.1
		N/A						
loc	_		30.8	33.6	39.4	41.1	41.4	42.8
total	77.3	85.8	124	137	171	175	179	210

The increase in the library size demands a stricter developpement model. For instance, we have put FFLAS files into a new stand-alone FFLAS header library, reduced compile times, enforced stricter warnings and checks, support for more compilers and architectures, simplified and automatised version number changes, automatised memory leak checks,...This demand on the developper side is also driven by the fact that code introduced by various one-timers needs to be maintained.

But this increase also forces the library to be more user friendly. For instance, we have: Developped an auto-install.sh script that installs automatically the lastest stable or developpement versions of the trio; Facilitated the discovery of the Blas/Lapack libraries; Simplified and sped up the checking process; Added comprehensive benchmarking tools,...

This article follows several papers and memoirs on $\mathsf{LinBox}\ ([9,13,2,6,7])$ and builds upon them.

Developping generic and high-performance libraries is difficult. We can find a large litterature on coding standards and software desin references in ([1,8,12,11,10]), and many internet sources and a lot of experience acquired by free software projects.

We are going to describe the advancement in the design of LinBox in the next three sections. We will first describe the new container framework in section 2, then improve the $matrix\ multiplication$ algorithms in section 3 by contributing special purpose matrix multiplication plugings, and finally present the new benchmark/optimisation architecture (section 4).

⁶ Using sloccount, available at http://sourceforge.net/projects/sloccount/.

2 Containers

LinBox is mainly conceived around the RAII concept with re-entrant function (Resource Acquisition Is Initialisation), introduced by [11], or the *mother model* ([7]) in the sense that the memory used by objects is allocated in the constructor and freed only at its destruction. The gestion of the memory allocated by an object is exlusively reserved to it.

LinBox essentially uses matrix and vectors over fields as data objects. The fragmentation of the containers into various matrices and blackboxes needed to be addressed and simplified. The many different matrix and vector types with different interfaces needed to be simplified into only two (possibly essentially one in the future) containers: Matrix and Vector.

2.1 Dense Vectors and Matrix

First, all matrices and vectors now depend on the field and not its element, so that operation can always be performed on a matrix or vector. The storage is given by another template parameter that can be defauted to *e.g.* dense BLAS type matrices, *cf.* listing 1.1.

```
template < class _Field, class _Storage = denseDefault >
  class Matrix ;

template < class _Field, class _Storage = denseDefault >
  class Vector ;
```

Listing 1.1: Matrix classes in LinBox.

Interface The empty constructors are forbidden (no field). In the mother model ([7]), we need types that Own/Share memory. The SubMatrix and SubVector types share the memory while Matrix and Vector own it. The common interface to all matrices is the BlackBox interface listing 1.2.

```
_out& apply(_out &y, const _in &x) const;
             template < class _in, class _out>
             _out& applyTranspose(_out &y, const _in &x) const;
15
             /* operator rebind */
             template<typename _Tp1>
             struct rebind;
20
             /* dimensions */
             size_t rowdim() const;
             size_t coldim() const;
             /* field */
25
             const Field& field() const;
             /* conversions ?*/
             // resize
             // export/import to default types
30
             // read from MM/stdout/...
             // write to MM/stdout/...
             // setEntry/init()/finalise()/optimize()
    protected:
             /* internals */
35
    };
```

Listing 1.2: Interface of an BlackBox

Notes on xxxEntry: Some handy functions are missing from the BlackBox interface. For instance, refEntry(...) may be difficult to impelement (compressed fields, sparse matrices). The function getEntry(...) may be specialised because potentially costly (it is however a solution). setEntry(...) can be used to populate/grow the matrix (from some init() until a finish() is emitted). setEntry can be (very) costly (ELL format) so set entry should always build some COO or CSR and then convert to the format. clearEntry(...) can be used to zero out an entry if this is allowed (possibly not for structured matrices). Aneeds trait system for algos to adapt. How to check at compile time (static assert)?

Sparse Matrix Sparse Matrix are tricky to handle and must be well implemented to offer best BlackBox performance (*cf.* [3]). There is a huge litterature on sparse matrix formats, some of which are becoming standard. Numerical analysis brings various shapes for sparse matrices and numerous algorithms and routines. Just like the BLAS numerical routines, we would like to take advantage of existing high performance libraries.

Asparse blas, metis, sparse suite, zero-one matrices

Matrix market matrices must be supported (we have a convertor in ffsp-mygpu, I should commit it)

SparseMatrix are Matrix with specified storage: COO, CSR, CSC, ELL, ELL_R,..., and more to come. (including 0-1 based)

```
namespace matrixStorage {
    struct sparse {};
    struct COO : public sparse {};
    struct CSR : public sparse {};
    struct ELL : public sparse {};
    struct ELLR: public sparse {};
    struct HYB : public sparse {};
    ...
  };

template < class _Field >
    class Matrix < _Field, matrixStorage :: COO > {
        //specialisation for COO
  };
```

Listing 1.3: Standard sparse matrix formats.

HYB format is a specialisation for ELL(_R)+COO/CSR. no easy setEntry (in the COO/CSR) part? a function optimize(). Could use Metis too. litterature for other HYB.

We use MM reader.

Added to the interface is a convert method to/from CSR (default).

We can adapt the hearder to suit our needs. In particular write matrix in CSR fashion (saving roughly 1/3 space over COO)

XXX timing new matrices, example rank.

Other Matrices All other matrices (including the special case of Permutations): the same Structured matrices, add, sub, stacked,...

2.2 The apply method

The apply method (left or right) is arguably the most important feature in the matrix interface and the LinBox library. It performs what a linear application is defined for: apply to a vector (and by extension a block of vectors, *i.e.* a matrix).

Proposed interface:

```
// y = A.x
template< class _In, class _Out >
_Out& apply(_Out &y, const _In& x, enum Side) ;

// y = alpha y + beta A.x
template< class _In, class _Out >
_Out& applyAcc(_Out &y, const Element& alpha, const _In& x, const
```

```
Element& beta, enum Side) ;
```

Listing 1.4: Proposed apply.

The apply method should be using a mul solution as in the listing 1.5.

Listing 1.5: Implantation d'apply sur un vecteur par solution mul.

3 Improving LinBox matrix multiplication

Efficient matrix multiplication is key to LinBox library.

3.1 Plugin

We propose the following design pattern (the closest design pattner to our knowledge is the *strategy* one, see also [5, Fig 2.]. The main advantage of this design pattern is that the modules always call back the controller so that the best choice is always chosen. Besides modules can be easily added as *plug-ins*. An analogy can be drawn with dynamic systems—once the controller sends a correction to the system, it receives back a new measure that allows for a new correction.

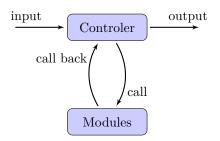


Fig. 1: Controller-Modules design pattern

For instance, we can write the standard cascade algorithms in that model:

This method allows for the reuse of modules and ensures efficiency. It is then possible to adapt to the architecture, the available modules, the resources. The only limitation is that the choice of the module should be done fast. Atiming old fgemm/plugin fgemm with no noticeable change?

```
Algorithm
               1:
                   AlgoThresh:
controler
                                       Algorithm 2: RecursiveCase:
Input: A and B, denses, with
                                      recursive module
        resp. dimensions n \times k
                                       Input: A, B, C and t as in
        and k \times n.
                                               controller.
Output: C = A \times B
                                       Output: C = A \times B
if min(m, k, n) < t then
                                       Cuts A,B,C in S_i,T_i\cdots
    BaseCase(C,A,B) /* fast
                                       P_i = AlgoThresh(S_i, T_i, t)
else
    RecursiveCase(C,A,B,t)
                                       return C
end
return C;
```

Fig. 2: Conception of a recursive controlled algorithm

3.2 New algorithms/infrastructure

We introduce now several new algorithms that improve on matrix multiplication in various ways: reducing memory consumption, introducing new efficient algorithms, using graphics capabilities, generalizing the BLAS to integer routines.

New algorithms: low memory ffgem in FFLAS uses the classic schedules for the multiplication and the product with accumulation (*cf.* [4]), but we also implement the lower memory routines therein.

The difficulty consists in using the part of the memory contained in a submatrix of the original matrix. It is two-fold. – First we use some part of a memory that has already been allocated to the input matrices, therefore we cannot free and reallocate part of it. – Second, several of these algorithms are meant for square matrices and rectangular sub-matrices will just not be enough. For instance.

∧table comparing speeds

New algorithms: Bini

integer blas Apascal

OpenCL Adave

Using conversions - using flint for integer matmul is faster, even with conversion. Need better CRA implementation.

- implementation of Toom-Cook for GF(q)
- when does spmv choose to optimise?

4 Benchmarking

Benchmarking was introduced in LinBox for several reasons. It would give the user a user-friendly way for producing nice graph with no necessary knowledge of the graphing library gnuplot⁷ or provide LinBox website with automatic new tables/graphs. It would be used for regression testing. It can be used for selecting default method, threshold. (cite atlas and?)

XXX needs introductory bench references XXX BTL 8 /eigen \triangle dave benchmark formats

4.1 Graph/Table creation

XXX data/plot structure of abstraction (update code 6.1 with new plot structure)

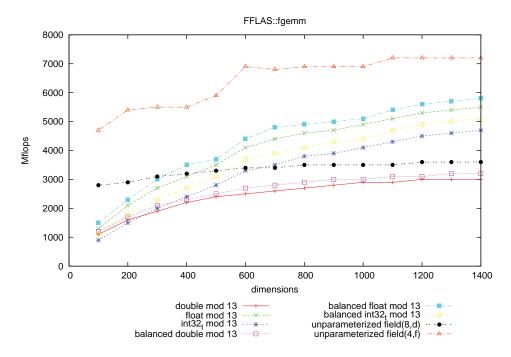


Fig. 3: Example of benchmark: fgemm.

XXX Time spent on each data is limited (will not start execution if fit (linear least squares) forecasts 'too long'.

XXX Adapts to the environment.

⁷ http://www.gnuplot.info/

⁸ http://projects.opencascade.org/btl/

4.2 Regression Testing

XXX Tests are supposed to be comparable: regression testing. XXX howto.

4.3 Method Selecting

XXX Default are provided, method can be selected via a benchmark (cf wino_threshold)

XXX howto

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