# PHASE 2 PROJECT

#### **GROUP MEMBERS**

- 1. SHARON KALIKU
- 2. PAUL KAMAU
- 3. KIPKOSGEI KIPTUI
- 4. EZRA KIPCHIRCHIR
- 5. HERI KIMOTHO

#### **BUSINESS STAKEHOLDER**

The real estate agency

#### **BUSINESS PROBLEM**

A real estate agency wants to analyze the factors that influence the prices of houses in order to provide accurate pricing estimates to their clients. The agency aims to understand the relationship between various features of a house, such as the number of rooms, living area, basement area, overall quality, and other relevant factors, and how they affect the sale price.

The clients being, homeowners and potential house buyers have difficulty in making informed decisions regarding property investments, to make this decision, understanding the factors influencing housing prices in a specific area is necessary.

## **OBJECTIVES**

#### **REAL ESTATE AGENCY**

- To identify the locations with the highest sales prices.
- To identify how seasonal trends affect sales.
- To predict prices of houses depending on the features.

Importing the necessary libraries that will be used to perform analysis on our data

```
import pandas as pd
import matplotlib.pyplot as plt
import seaborn as sns
import statsmodels.api as sm
from scipy import stats
import numpy as np
from sklearn.model_selection import train_test_split
from sklearn.linear_model import LinearRegression
from sklearn.metrics import mean_squared_error, r2_score
```

```
from sklearn.preprocessing import PolynomialFeatures
from sklearn.preprocessing import StandardScaler
data = pd.read_csv('kc_house_data.csv')
areas = pd.read_csv('deliverylocations.csv')
```

Defining functions to load and view the data

```
# loading data
def desription data(data):
   data = pd.read csv(data)
   print("\n....")
   print(data.info())
   print("\n....")
   print(data.describe())
   print("\n....")
   print(data.head())
desription data('kc house data.csv')
...........Info:...........
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 21597 entries, 0 to 21596
Data columns (total 21 columns):
#
    Column
                  Non-Null Count
                                 Dtype
0
    id
                  21597 non-null
                                 int64
1
    date
                  21597 non-null
                                 object
2
                                 float64
    price
                  21597 non-null
3
                  21597 non-null
    bedrooms
                                 int64
4
    bathrooms
                  21597 non-null
                                 float64
5
    sqft living
                  21597 non-null
                                 int64
6
    sqft lot
                  21597 non-null
                                 int64
7
    floors
                  21597 non-null
                                 float64
8
                  19221 non-null
    waterfront
                                 object
9
                  21534 non-null
    view
                                 object
10
    condition
                  21597 non-null
                                 object
11
    grade
                  21597 non-null
                                 object
12
    sqft above
                  21597 non-null
                                 int64
13
    sqft basement 21597 non-null
                                 object
14 yr built
                  21597 non-null
                                 int64
    yr_renovated
15
                  17755 non-null
                                 float64
                                 int64
16
   zipcode
                  21597 non-null
17
                  21597 non-null
    lat
                                 float64
18
    lona
                  21597 non-null
                                 float64
    sqft living15 21597 non-null
19
                                 int64
    sqft lot15
                  21597 non-null int64
20
dtypes: float64(6), int64(9), object(6)
memory usage: 3.5+ MB
```

None			
Describ	e:		
id	price		bathrooms
<pre>sqft_living \</pre>	•		
count 2.159700e+04	2.159700e+04	21597.000000	21597.000000
21597.000000	F 402066 0F	2 272200	2 115026
mean 4.580474e+09 2080.321850	5.402966e+05	3.373200	2.115826
std 2.876736e+09	3.673681e+05	0.926299	0.768984
918.106125		0.02020	01700001
min 1.000102e+06	7.800000e+04	1.000000	0.500000
370.000000	2 220000 05	2 000000	1 750000
25% 2.123049e+09 1430.000000	3.220000e+05	3.000000	1.750000
50% 3.904930e+09	4.500000e+05	3.000000	2.250000
1910.000000	113000000103	3.00000	21230000
75% 7.308900e+09	6.450000e+05	4.000000	2.500000
2550.000000			
max 9.900000e+09 13540.000000	7.700000e+06	33.000000	8.000000
13340.000000			
sqft_lot	floors	sqft_above	yr_built
<pre>yr_renovated \</pre>		_	_
count 2.159700e+04	21597.000000	21597.000000	21597.000000
17755.000000 mean 1.509941e+04	1.494096	1788.596842	1970.999676
83.636778	1.454050	1700.550042	1370.333070
std 4.141264e+04	0.539683	827.759761	29.375234
399.946414			
min 5.200000e+02	1.000000	370.000000	1900.000000
0.000000 25% 5.040000e+03	1.000000	1190.000000	1951.000000
0.000000	1.000000	1130.000000	1331.000000
50% 7.618000e+03	1.500000	1560.000000	1975.000000
0.000000	2 00000	2210 00000	1007 00000
75% 1.068500e+04 0.000000	2.000000	2210.000000	1997.000000
max 1.651359e+06	3.500000	9410.000000	2015.000000
2015.000000	0.00000	0.20.000000	
	1	1	
zipcode	lat	long	sqft_living15
sqft_lot15 count 21597.000000	21597.000000	21597.000000	21597.000000
21597.000000			223371000000
mean 98077.951845	47.560093	-122.213982	1986.620318
12758.283512	0 100550	0 140704	COE 220472
std 53.513072 27274.441950	0.138552	0.140724	685.230472
min 98001.000000	47.155900	-122.519000	399.000000
30001100000	171133300	1221313000	333100000

```
651.000000
      98033.000000
                      47.471100 -122.328000
                                               1490.000000
25%
5100.000000
50%
      98065.000000
                      47.571800
                                 -122.231000
                                                1840.000000
7620,000000
75%
      98118.000000
                      47.678000
                                  -122.125000
                                                2360.000000
10083.000000
      98199.000000
                      47.777600
                                 -121.315000
                                                6210.000000
max
871200.000000
date price bedrooms bathrooms sqft living
     id
0 7129300520 10/13/2014 221900.0
                                                 1.00
                                                             1180
                                         3
1 6414100192 12/9/2014 538000.0
                                         3
                                                 2.25
                                                             2570
2 5631500400 2/25/2015 180000.0
                                         2
                                                 1.00
                                                              770
3 2487200875 12/9/2014 604000.0
                                                 3.00
                                                             1960
4 1954400510 2/18/2015 510000.0
                                         3
                                                 2.00
                                                             1680
  sqft lot floors waterfront
                                                grade sqft above \
                              view
                                    . . .
0
      5650
                                            7 Average
               1.0
                         NaN
                              NONE
                                                           1180
                                    . . .
1
      7242
               2.0
                             NONE
                                                           2170
                         NO
                                            7 Average
                                    . . .
2
     10000
               1.0
                          NO
                              NONE
                                        6 Low Average
                                                           770
3
      5000
               1.0
                          NO
                              NONE
                                            7 Average
                                                           1050
4
      8080
               1.0
                          NO NONE
                                               8 Good
                                                           1680
  sqft_basement yr_built yr_renovated zipcode lat long \
0
            0.0
                   1955
                                  0.0
                                        98178 47.5112 -122.257
1
                                              47.7210 -122.319
          400.0
                   1951
                               1991.0
                                        98125
2
                                        98028 47.7379 -122.233
            0.0
                   1933
                                  NaN
3
                                  0.0
                                        98136
                                               47.5208 -122.393
          910.0
                   1965
4
            0.0
                   1987
                                  0.0
                                        98074 47.6168 -122.045
  sqft_living15 sqft_lot15
0
           1340
                      5650
1
           1690
                      7639
2
           2720
                      8062
3
                      5000
           1360
4
           1800
                      7503
[5 rows x 21 columns]
```

#### **Null values**

Looking at the information above we can see only three columns have missing values, that is; "waterfront", "view" and "yr\_renovated". Every house has its own unique features and not all are the same. Some houses contain certain features while others lack them. Since this is real world data, we can account for missing values in "waterfront" and "view" columns by saying not all houses are build the same and those lacking the two features have caused our data on the two columns to be inconsitent with the rest of the other columns. The "yr\_renovated" column can also be accounted for by saying not all houses undergo renovation. Houses build earlier might need renovation but recent houses do not require renovation hence the missing values in the column

```
# Using mode to impute missing values
# Python function to impute missing values

def replace_missing_with_mode(data, column_name):
    mode_value = data[column_name].mode().iloc[0]
    data[column_name].fillna(mode_value, inplace =True)

# columns to be imputed
replace_missing_with_mode(data,'view')
replace_missing_with_mode(data, 'waterfront')

# Changing our date from object to datetime data type
data['date'] = pd.to_datetime(data['date'])
```

After checking for null values, we check for any duplicated values in the data.

```
# Checking for duplicated values in our data
data.duplicated().sum()

# drop the rows in sqft_basement with a '?'
data= data.drop(data[data.sqft_basement == '?'].index)
```

Creating a new column 'Grade\_1' that stores our new 'grade' column after getting rid of the string 'grade' and converting it to a numeric datatype

```
data["Grade_1"] = data["grade"].str.split().apply(lambda x: x[0])
# Convert the Grade1 column to an integer.
data["Grade_1"] = pd.to_numeric(data["Grade_1"])
```

## Converting the categorical columns to numerical data types

We are converting the following categorical data "Waterfront", "View" and "grade" into numerical data types.

```
data['view_1'] = data['view'].replace({'NONE': 0, 'FAIR':1, 'AVERAGE':
2,'GOOD':3, 'EXCELLENT':4})
data['waterfront_1'] = data['waterfront'].replace({'YES': 0, 'NO':1})
data['condition1'] = data['condition'].replace({'Poor': 0,
'Fair':1,'Average':2,'Good':3,'Very Good':4})
```

Since we have already replaced the strings in our categorical data with numeric values we can drop the original columns

```
data.drop(columns = ['waterfront', 'view', 'grade', 'condition', ],
inplace= True)
data.dtypes
id
                           int64
date
                 datetime64[ns]
                         float64
price
bedrooms
                           int64
                         float64
bathrooms
sqft_living
                           int64
saft lot
                           int64
floors
                         float64
sqft above
                           int64
sqft basement
                          object
yr built
                           int64
                         float64
yr renovated
zipcode
                           int64
                         float64
lat
                         float64
lona
sqft living15
                           int64
sqft lot15
                           int64
Grade 1
                           int64
view 1
                           int64
waterfront 1
                           int64
condition1
                           int64
dtype: object
```

Delivery locations (zip codes) data

```
# Create a new dataframe with two columns for zip codes and cities
new_areas = pd.DataFrame(columns=['Zip Code', 'City'])

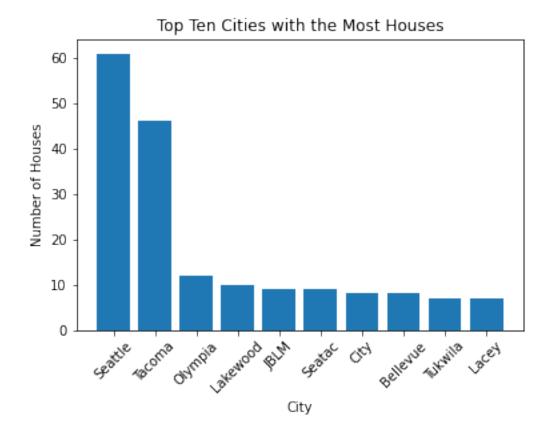
# Iterate over the original dataframe and extract zip codes and cities
for i in range(len(areas.columns)):
    # Skip the columns that are not zip codes
    if i % 2 != 0:
        continue
    # Extract the zip codes and cities from each pair of columns
```

```
zip codes = areas.iloc[:, i]
    cities = areas.iloc[:, i + 1]
    # Append the zip codes and cities to the new dataframe
    new areas = new areas.append(pd.DataFrame({'Zip Code': zip_codes,
'City': cities}), ignore_index=True)
# Print the new dataframe
print(new areas)
    Zip Code
                      City
0
       98001
                    Algona
1
       98001
                   Auburn
2
              Federal Way
       98001
3
                   Auburn
       98002
4
       98003
              Federal Way
447
         NaN
                       NaN
448
         NaN
                       NaN
449
         NaN
                       NaN
450
                       NaN
         NaN
451
         NaN
                       NaN
[452 rows x 2 columns]
new areas.isnull().sum()
new areas.dropna()
    Zip Code
                      City
0
       98001
                    Algona
1
       98001
                    Auburn
2
       98001
              Federal Way
3
       98002
                    Auburn
4
       98003
              Federal Way
404
       98593
                     Vader
405
       98595
                 Westport
406
       98596
                 Chehalis
407
       98596
                  Winlock
408
       98597
                      Yelm
[409 rows x 2 columns]
#renaming to match our first data set
new areas = new areas.rename(columns={"Zip Code": "zipcode"})
new areas
    zipcode
                     City
0
      98001
                  Algona
1
      98001
                  Auburn
2
      98001
            Federal Way
3
      98002
                  Auburn
```

```
4
      98003
            Federal Way
447
        NaN
                     NaN
448
        NaN
                     NaN
449
        NaN
                     NaN
450
        NaN
                     NaN
451
        NaN
                     NaN
[452 rows x 2 columns]
#merging our data sets
new areas['zipcode'] = new areas['zipcode'].astype(str)
data['zipcode'] = new areas['zipcode'].astype(str)
merged data = pd.merge(new areas, data , on='zipcode')
merged data
                               id
                                                           bedrooms
     zipcode
             City
                                         date
                                                   price
bathrooms
       98001
              Algona
                      7129300520
                                   10/13/2014
                                                221900.0
                                                                  3
1.00
1
       98001 Algona 6414100192
                                    12/9/2014
                                                538000.0
                                                                  3
2.25
       98001 Algona 5631500400
                                    2/25/2015
                                                180000.0
                                                                  2
2
1.00
       98001 Auburn
                     7129300520
                                   10/13/2014
                                                                  3
3
                                                221900.0
1.00
       98001 Auburn
                      6414100192
                                    12/9/2014
                                                538000.0
                                                                  3
4
2.25
. . .
2405
                 NaN
                      1049010390
                                    3/19/2015
                                                505000.0
                                                                  3
         nan
2.00
2406
         nan
                 NaN
                      7905370390
                                    10/9/2014
                                                475000.0
                                                                  5
2.50
                      4140090240
                                    11/5/2014
                                                520000.0
                                                                  3
2407
         nan
                 NaN
2.25
                                                                  3
2408
                 NaN
                      4055700030
                                     5/2/2015
                                               1450000.0
         nan
4.50
2409
                                                                  3
                 NaN
                      3775300030
                                   12/31/2014
                                                333500.0
         nan
1.75
      sqft living
                   sqft lot floors ... yr built yr renovated
lat \
             1180
                                               1955
                                                              0.0
                       5650
                                 1.0
47.5112
                                                           1991.0
             2570
                       7242
                                 2.0
                                               1951
47.7210
2
              770
                       10000
                                 1.0
                                               1933
                                                              NaN
```

47.7379						
3	1180	5650	1.0	1955	0.0	
47.5112						
4	2570	7242	2.0	1951	1991.0	
47.7210						
	1000					
2405	1260	5460	1.0	1972	0.0	
47.7355	22.42					
2406	2340	7200	1.0	1975	0.0	
47.7206	2500	0262	1 0	1077	0.0	
2407	2590	9263	1.0	1977	0.0	
47.7691	2070	24020	2.0	1077	N - N	
2408	3970	24920	2.0	1977	NaN	
47.7183 2409	1220	0722	1.0	1065	0.0	
	1220	9732	1.0	1965	0.0	
47.7736						
1	ong sqft	living15	sqft lot15	Grade 1	view 1	
waterfront		_crvriig15	3411_10113	orauc_1	VICW_I	
0 -122.		1340	5650	7	0.0	
NaN	237	13.10	3030	,	0.10	
1 -122.	319	1690	7639	7	0.0	
1.0						
2 -122.	233	2720	8062	6	0.0	
1.0						
3 -122.	257	1340	5650	7	0.0	
NaN						
4 -122.	319	1690	7639	7	0.0	
1.0						
				_		
2405 - 122.	180	1510	5460	7	0.0	
1.0	011	1000	7001	_	0.0	
2406 - 122.	211	1930	7221	7	0.0	
1.0	262	2500	0.450	0	0 0	
2407 -122.	262	2580	9450	8	0.0	
1.0	250	2610	12020	10	2.0	
2408 -122. 1.0	230	2610	13838	10	2.0	
2409 -122.	21/	1630	10007	7	0.0	
1.0	Z1 <del>4</del>	1030	10007	,	0.0	
1.0						
conc	dition1					
	2					
1	2					
0 1 2 3	2					
3	2					
4	2					

```
2
2405
               2
2406
2407
               4
               2
2408
               2
2409
[2410 rows x 22 columns]
merged data.isnull().sum()
#dropping the rows with null values
new data = merged data.dropna()
def create_bar_graph(data):
    # Count the occurrences of each city
    city_counts = data['City'].value_counts()
    # Select the top ten cities
    top_cities = city_counts.head(10)
    # Create a bar graph
    plt.bar(top cities.index, top cities.values)
    plt.xlabel('City')
    plt.ylabel('Number of Houses')
    plt.title('Top Ten Cities with the Most Houses')
    plt.xticks(rotation=45)
    plt.show()
# Example usage:
create bar graph(new data)
```

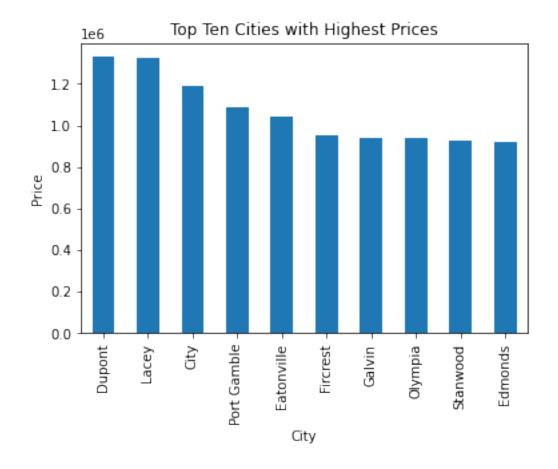


```
city_prices = new_data.groupby('City')['price'].mean()

# Select the top ten cities with the highest mean prices
top_ten_cities = city_prices.nlargest(10)

# Create a bar graph
top_ten_cities.plot(kind='bar', xlabel='City', ylabel='Price',
title='Top Ten Cities with Highest Prices')

# Show the plot
plt.show()
```



# Data visualization

Now we have checked for abnormalities in the data, we can go ahead and plot the data to explore the distribution, relationships and patterns in the data. This will also help us in identifying outliers and trends.

```
y = data["price"]
X = data.drop("price", axis = 1)

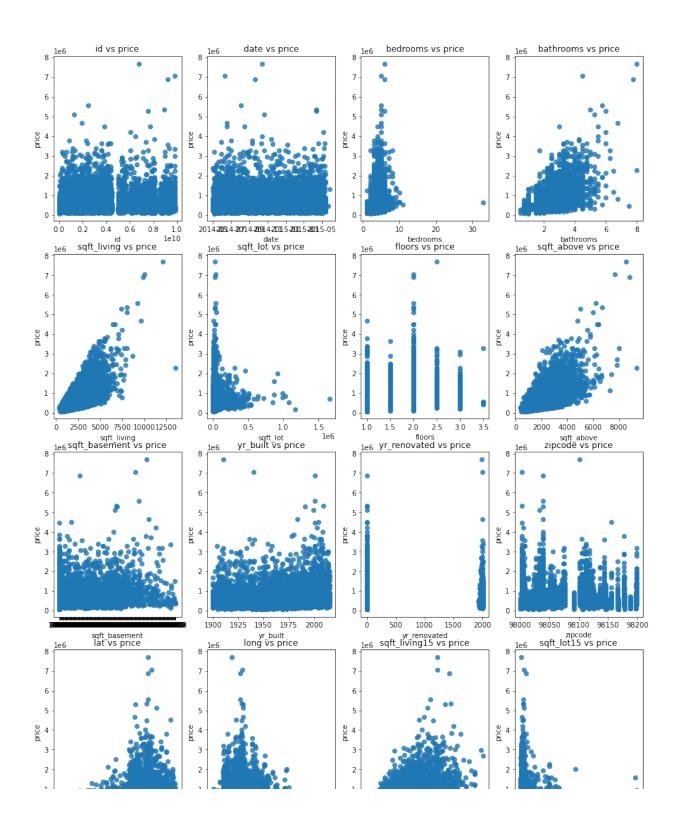
def scatter_plots(y, X):
    plots = X.shape[1]
    cols = 4
    rows = (plots + cols - 1) // cols

fig, axes = plt.subplots(rows, cols, figsize=(15, 5 * rows))
    fig.suptitle(f"Scatter plot of Independent variables vs {y.name}")

for i, ax in enumerate(axes.flat):
    if i < plots:
        x_col_name = X.columns[i]
        ax.scatter(X.iloc[:, i], y, alpha=0.8)</pre>
```

```
ax.set_xlabel(x_col_name)
ax.set_ylabel(y.name)
ax.set_title(f"{x_col_name} vs {y.name}")

# Run the function
scatter_plots(y, X)
```

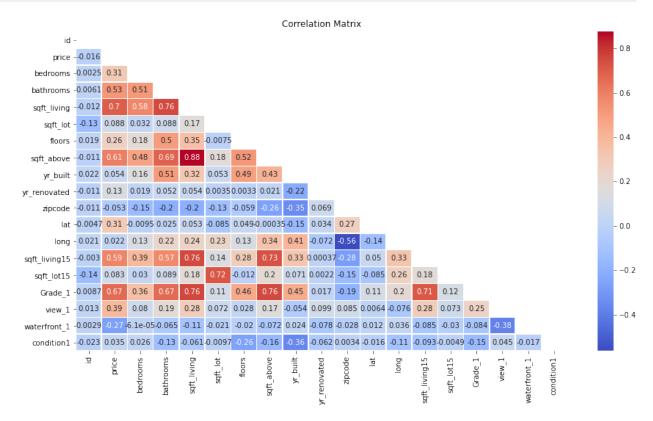


# ## Relationship between our independent variables and the dependent variable("price")

```
#correlation
columns_to_test = data.columns

# computing the correlation matrix
correlation_matrix = data[columns_to_test].corr()
matrix = np.triu(np.ones_like(correlation_matrix, dtype = bool))
one_sided_correlation = correlation_matrix.mask(matrix)

# using heatmap to visualize the correlation
plt.figure(figsize=(15, 8))
sns.heatmap(correlation_matrix, annot=True, cmap='coolwarm',
linewidths=0.5, mask = matrix)
plt.title(f'Correlation Matrix')
plt.show()
```



# Correlation of our columns against the target("price)

```
def correlation(df):
    return data.corr()['price'].sort_values()
correlation(data)
```

```
waterfront 1
                -0.265969
zipcode
                -0.053166
id
                -0.015796
long
                 0.022101
condition1
                 0.035290
yr built
                 0.054459
sqft lot15
                 0.083192
saft lot
                 0.087937
yr renovated
                 0.128227
floors
                 0.256355
lat
                 0.306507
bedrooms
                 0.309204
                 0.394885
view 1
bathrooms
                 0.525889
sqft_living15
sqft_above
                 0.586415
                 0.605143
Grade 1
                 0.667738
sqft living
                 0.702328
price
                 1.000000
Name: price, dtype: float64
```

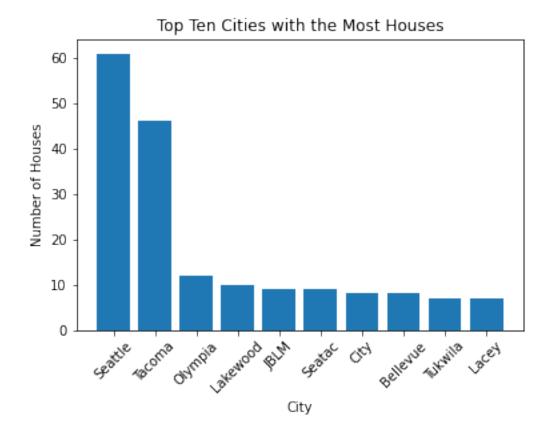
# Analyzing price and location

```
def create_bar_graph(data):
    # Count the occurrences of each city
    city_counts = data['City'].value_counts()

# Select the top ten cities
    top_cities = city_counts.head(10)

# Create a bar graph
    plt.bar(top_cities.index, top_cities.values)
    plt.xlabel('City')
    plt.ylabel('Number of Houses')
    plt.title('Top Ten Cities with the Most Houses')
    plt.xticks(rotation=45)
    plt.show()

# Example usage:
create_bar_graph(new_data)
```

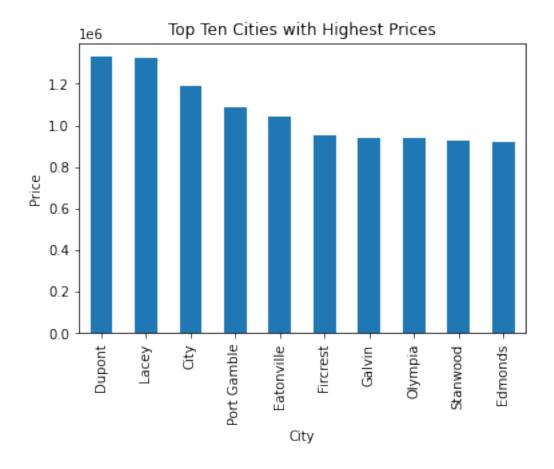


```
city_prices = new_data.groupby('City')['price'].mean()

# Select the top ten cities with the highest mean prices
top_ten_cities = city_prices.nlargest(10)

# Create a bar graph
top_ten_cities.plot(kind='bar', xlabel='City', ylabel='Price',
title='Top Ten Cities with Highest Prices')

# Show the plot
plt.show()
```



# Analyzing seasonal trends in prices

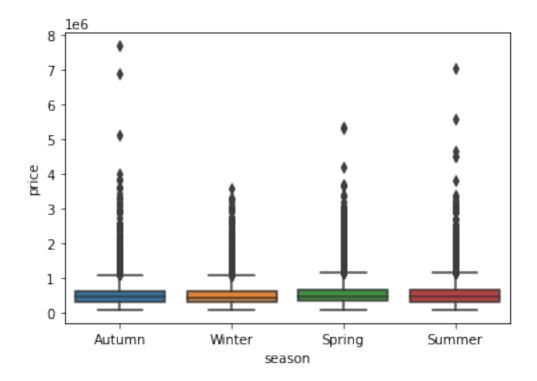
```
# Creating a function to map months to seasons
def get season(date):
    if date.month in [3,4,5]:
        return 'Spring'
    elif date.month in [6,7,8]:
        return 'Summer'
    elif date.month in [9,10,11]:
        return 'Autumn'
    else:
        return 'Winter'
# Applying the function to the 'date' column to create a 'season'
column
data['season'] = data['date'].apply(get_season)
data[['date', 'season']]
            date season
0
      2014-10-13 Autumn
1
      2014-12-09 Winter
2
      2015-02-25 Winter
3
      2014-12-09 Winter
```

```
4 2015-02-18 Winter
... 21592 2014-05-21 Spring
21593 2015-02-23 Winter
21594 2014-06-23 Summer
21595 2015-01-16 Winter
21596 2014-10-15 Autumn

[21597 rows x 2 columns]
```

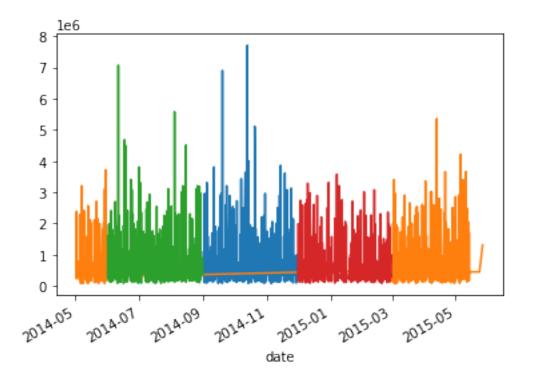
Creating a boxplot of price segmented by season to view differences in price distribution by season.

```
sns.boxplot(x='season', y='price', data=data);
```



Making a timeseries plot of price over time, colored by season to see seasonal patterns.

```
data.set_index('date').groupby('season')['price'].plot();
```



Calculating summary statistics (mean, median, std dev) for price grouped by season to quantify differences.

```
data.groupby('season')['price'].agg([np.mean, np.median, np.std])
                         median
                                            std
                 mean
season
        531276.474881 443725.0
                                 378513.665722
Autumn
Spring 552782.763271
                       465000.0
                                 367075.050556
                                 368925,606702
Summer
        546719.464286
                       455000.0
Winter 519613.645467
                       430000.0 348171.543129
# Extract price by season into separate dataframes
spring = data[data['season'] == 'Spring']['price']
summer = data[data['season'] == 'Summer']['price']
fall = data[data['season'] == 'Autumn']['price']
winter = data[data['season'] == 'Winter']['price']
# Perform ANOVA test
f_val, p_val = stats.f_oneway(spring, summer, fall, winter)
print(f val, p val)
# Interpret results
alpha = 0.05
if p_val < alpha:</pre>
  print("We reject the null hypothesis")
  print("There is a statistically significant difference in price by
```

```
season")
else:
    print("We fail to reject the null hypothesis")
    print("There is no statistically significant difference in price by season")

8.082642416374668 2.2312373653979034e-05
We reject the null hypothesis
There is a statistically significant difference in price by season
```

In this case; these are the hypotheses.

Null hypothesis:

There is no difference in the mean price across the seasons. The season has no effect on price.

H0:  $\mu$ spring =  $\mu$ summer =  $\mu$ fall =  $\mu$ winter

Alternative hypothesis:

There is a difference in mean price for at least one season compared to the others. The season has an effect on price.

H1: At least one  $\mu$  season  $\neq \mu$  other seasons

Where µseason is the population mean price for that season.

So in summary: Null hypothesis (H0): The seasons all have an equal effect on mean price (no difference). Alternative hypothesis (H1): At least two seasons have a statistically significant difference in their effect on mean price. If we reject H0 based on a small ANOVA p-value, we would conclude there is a significant difference in price by season. Failing to reject H0 means we cannot say there is a seasonal effect.

# **Linear Regression**

Since we now have a better understanding of the correlation between our target("price") and our features("independent variables"), we proceed to building regression models to further understand the magnitude our features have on price and predict whether this model can give us accurate house prices when fitted with the said features. We will explore a few features from our data set which we have investigated and come to a conclusion that they have a significance on our target. Steps involved here are as follows;

- 1. Feature Selection
- Model Selection
- 3. Model training
- 4. Model evaluation
- 5. Model interpretation
- 6. Model validation and testing
- 7. \*\*feature engineering

#### 1. Feature selection

Here we just choose the endogenous and exogenous variables. First we will select for the baseline model then after we shall add features to see if it improves and evaluate it.

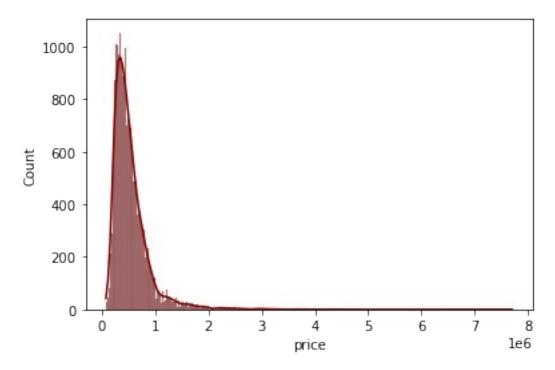
```
y= data["price"]
X = data["sqft_living"]
```

# 2. Building a baseline model

Creating a baseline model for our regression model

First we visualize the target(price) column in order to understand the distribution

```
sns.histplot(data["price"], color="maroon", kde=True)
plt.show();
```



The distribution of our data seems to a have a longer right tail than the left tail. This indicates a positive skewness in our target meaning the mean is greater than the median. This may have impact on our model since linear regression, assume that the target variable follows a normal distribution, so significant skewness can be problematic.

# Splitting our data into train and test sets

First we split the data into test set and training set. We will use the "train\_test\_split" function from scikit-learn library to split our data.

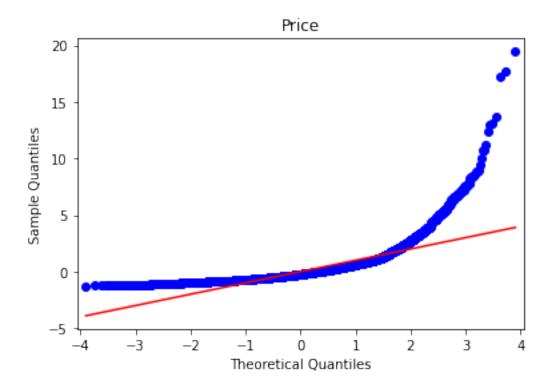
```
#importing scikit-learn library
from sklearn.model_selection import train_test_split
#defining a function for splitting data into train and test sets
def split(X, y):
    X_train, X_test, y_train, y_test = train_test_split(X, y,
test_size=0.2, random_state=0)
    return X_train, X_test, y_train, y_test
#splitting the data by calling the function
X_train, X_test, y_train, y_test = split(X,y)
```

In the train\_test\_split function we have is used above, we have split 80% of the data into training set and 20% of the data into test set.

In the next cell we are going to build a baseline model using the y\_train and x\_train variables. To do that we import statsmodels library which is a powerful library for statistical modelling and is similar to the sci-kit learn module

```
#importing statsmodels
import statsmodels.api as sm
#function to create models and print the summary
model = sm.OLS(y_train, sm.add_constant(X_train))
results = model.fit()
results.summary()
<class 'statsmodels.iolib.summary.Summary'>
                            OLS Regression Results
Dep. Variable:
                                price R-squared:
0.495
Model:
                                  0LS
                                        Adj. R-squared:
0.495
                        Least Squares F-statistic:
Method:
1.655e+04
Date:
                     Thu, 26 Oct 2023 Prob (F-statistic):
0.00
Time:
                             01:44:37 Log-Likelihood:
2.3497e+05
                                16914
No. Observations:
                                        AIC:
4.700e+05
                                        BIC:
Df Residuals:
                                16912
4.700e+05
Df Model:
                                    1
Covariance Type:
                            nonrobust
```

```
_____
               coef std err t P>|t| [0.025]
0.9751
       -4.448e+04 4960.688 -8.966 0.000 -5.42e+04
const
-3.48e+04
sqft living 280.1781
                        2.178 128.639
                                           0.000
                                                   275,909
284.447
Omnibus:
                        11863.674
                                  Durbin-Watson:
2.008
Prob(Omnibus):
                           0.000
                                  Jarque-Bera (JB):
453836.272
Skew:
                           2.904 Prob(JB):
0.00
Kurtosis:
                          27.703 Cond. No.
5.62e+03
______
_____
Notes:
[1] Standard Errors assume that the covariance matrix of the errors is
correctly specified.
[2] The condition number is large, 5.62e+03. This might indicate that
there are
strong multicollinearity or other numerical problems.
import scipy.stats as stats
# Generate a Q-Q plot
sm.qqplot(data["price"], line='s', fit=True, dist=stats.norm, loc=0,
scale=1)
plt.title('Price')
plt.show()
```



Wonderful! We now have our baseline model and from it we can interpret its metrics

#### Interpretation

Looking at the summary above, we can see that the regression line we found was

```
price = sqft_living285.8630 - 43,990
```

The model is statistically significant overall, with an F-statistic p-value well below 0.05. The model explains about 50% of the variance in price. The model const and sqft\_living coefficients are both statistically significant, with t-statistic p-values well below 0.05. If a house had 0 sqft of living, we would expect price to be about -43,990 dollars. For each increase of 1 sqft in the living, we see an associated increase in price of about 280 dollars.

We now have our baseline model which we created using the train sets obtained from splitting our data. To analyze our model further we will predict our target("price") using the trained model then compare metrics to determine if our model is efficient or we need to adjust it. We also check if our model is under fitted or over fitted. To perform comparisson we will import another module from sci-kit learn

```
#predicting the dependent varible
X_test = sm.add_constant(X_test)
y_pred = results.predict(X_test)

#defining a function to calculate metrics for our prediction model
def calculate_regression_metrics(y_test, y_pred):
    metrics = {}
```

```
# Calculate Mean Absolute Error (MAE)
metrics['MAE'] = mean_absolute_error(y_test, y_pred)

# Calculate Mean Squared Error (MSE)
metrics['MSE'] = mean_squared_error(y_test, y_pred)

# Calculate R-squared (coefficient of determination)
metrics['R-squared'] = r2_score(y_test, y_pred)

return metrics

metrics = calculate_regression_metrics(y_test, y_pred)
print(metrics)

{'MAE': 177033.87791345723, 'MSE': 70202650031.35713, 'R-squared': 0.48779757847019767}
```

# Comparison of our baseline model against the prediction model

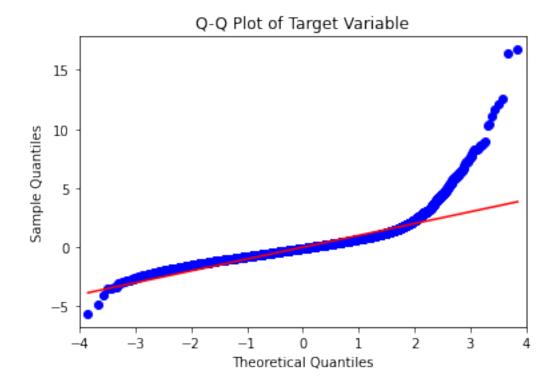
#### R-squared

Comparing the r-squared values from the test model and and the prediction model we can note a difference. Our train model has a R-squared value of almost 50% while our test model has a value of almost 48%. This means our baseline model is good ...

#### Residuals

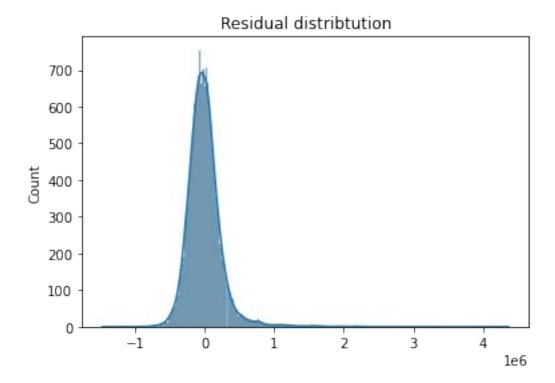
Residuals are the difference between the true values and the values predicted by our model. We visualize to understand the distribution and also check if it meets the assumption of linearity; that is normal distribution

```
# Generate a Q-Q plot
sm.qqplot(results.resid, line='s', fit=True, dist=stats.norm, loc=0,
scale=1)
plt.title('Q-Q Plot of baseline residuals')
plt.show()
```



Quantile-quantile plots are used to asses whether a dataset follows a specific theoretical normal distribution. The visual above shows our model residuals almost follow a straight line but then curves at some point. The skewness or outliers in our target might be the cause of this.

```
#ploting histogram to show residuals distribution
sns.histplot(results.resid, bins = "auto", kde = True)
plt.title("Residual distribution")
plt.show();
```

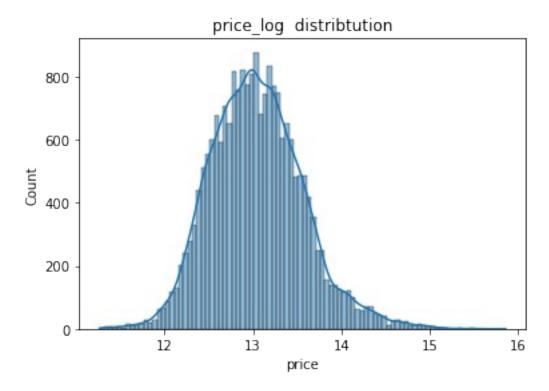


From the above plot we can see that our baseline model residuals have a normal distribution. This meets one of the linearity assumptions of linear regression. Linear models make key assumptions one of which is that the errors or residuals follow a normal distribution. The normality assumption is essential for valid statistical inferences and hypothesis testing. Nonnormal residuals can lead to biased parameter estimates, incorrect p-values, and unreliable confidence intervals.

# Target transformation

The non-normal distribution shown by the residuals (where it curves above) can be accounted for by the skewness of our target. Transforming the target variable can be an effective approach to make the data more closely approximate a normal distribution. By transforming the target variable, you aim to reduce skewness and make the data more symmetric, thus bringing it closer to a normal distribution. This, in turn, helps the residuals conform more closely to the normality assumption, which is crucial for the validity of the model. We shall log transform our target and see if our residuals will follow a normal distribution.

```
#log transforming the target
y_log = np.log(data["price"])
# visualizing to see its distribution
sns.histplot(y_log, bins = "auto", kde = True)
plt.title("price_log distribtution")
plt.show();
```



Wonderful! Our target after transformation seems to follow an almost normal distribution. Next we create a model for the transformed target, then we shall visualize the residuals once again to see their distribution. We will also check if it improves our model or not.

## Log transformed target model

```
#splitting data into test and train test
split(X, y_log)
##creating a model
log_model = sm.OLS(y_train, sm.add constant(X train))
log_results = log_model.fit()
log results.summary()
<class 'statsmodels.iolib.summary.Summary'>
                            OLS Regression Results
Dep. Variable:
                                        R-squared:
                                price
0.484
Model:
                                  0LS
                                        Adj. R-squared:
0.484
Method:
                        Least Squares F-statistic:
1.586e+04
Date:
                     Thu, 26 Oct 2023 Prob (F-statistic):
0.00
```

```
Time:
                              01:45:00
                                          Log-Likelihood:
-7525.5
No. Observations:
                                 16914
                                         AIC:
1.506e+04
Df Residuals:
                                 16912
                                          BIC:
1.507e+04
Df Model:
                                     1
                             nonrobust
Covariance Type:
                                                    P>|t|
                   coef
                           std err
0.9751
               12.2207
                             0.007
                                     1704.768
                                                    0.000
                                                                12.207
const
12.235
sqft living
                0.0004
                          3.15e-06
                                      125.933
                                                    0.000
                                                                 0.000
0.000
_____
Omnibus:
                                 3.650
                                          Durbin-Watson:
1.980
Prob(Omnibus):
                                 0.161
                                         Jarque-Bera (JB):
3.629
Skew:
                                 0.035
                                          Prob(JB):
0.163
Kurtosis:
                                 3.015
                                          Cond. No.
5.62e + 03
Notes:
[1] Standard Errors assume that the covariance matrix of the errors is
correctly specified.
[2] The condition number is large, 5.62e+03. This might indicate that
there are
strong multicollinearity or other numerical problems.
```

# Interpreting the results of the model

From the summary above we can see that the regression line we found was

price = sqft\_living0.0004 - 12.2207

The model is statistically significant overall, with an F-statistic p-value well below 0.05. The model explains about 48% of the variance in price. The model const and sqft\_living coefficients are both statistically significant, with t-statistic p-values well below 0.05. If a house

had 0 sqft of living, we would expect price to be about -12.2207 dollars. For each increase of 1 sqft in the living, we see an associated increase in price of about 0.0004 dollars.

## Prediction of our model

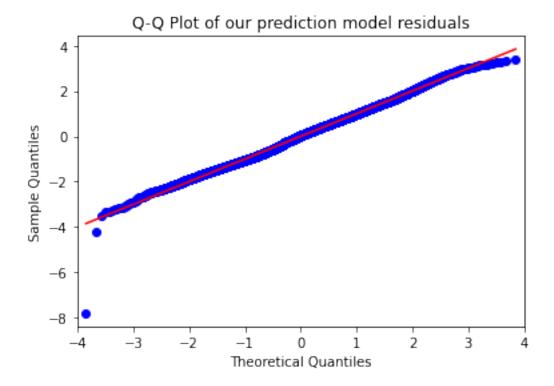
```
X_test = sm.add_constant(X_test)
y_pred = results.predict(X_test)

calculate_regression_metrics(y_test, y_pred)

{'MAE': 536828.527684868,
   'MSE': 352139274884.2067,
   'R-squared': -1250053982156.927}
```

Visualizing the transformed target residuals

```
# Generate a Q-Q plot
sm.qqplot(log_results.resid, line='s', fit=True, dist=stats.norm,
loc=0, scale=1)
plt.title('Q-Q Plot of our prediction model residuals')
plt.show()
```



The residuals of the log transformed target now follow a straight line compared to our first model. This is a good indication since it now meets the assumption of normal distribution.

#### Evaluation between the two baseline models

The first baseline model is much better than the second baseline model since it explains almost 50% in variance of the target variable compared to the second one which explains almost 48%. The second model prediction is also very poor since it has a negative R-squared value which indicates that the regression model's fit to the data is worse the model is not explaining any of the variance in the dependent variable, and it might be a poor fit for the data.

#### 2nd Model

In this model we are going to improve our first baseline model which we did't transform by adding more features and see if our model is going to improve.

Selecting y and X variables for our model

```
#defining variables tu be used in our second model
drop = data.drop(['id', 'price',
'date', 'sqft_lot', 'floors', 'sqft_basement', 'yr_renovated',
'zipcode',
'lat', 'long', 'sqft living15', 'sqft lot15', "sqft above"], axis= 1)
X_{sec} = drop
y sec= data["price"]
X sec
                              sqft living sqft above yr built
       bedrooms
                  bathrooms
                                                                    Grade 1
0
                                                                           7
               3
                        1.00
                                      1180
                                                   1180
                                                              1955
               3
1
                       2.25
                                      2570
                                                   2170
                                                              1951
                                                                           7
2
               2
                       1.00
                                       770
                                                    770
                                                              1933
                                                                           6
3
                                                                           7
                       3.00
                                      1960
                                                   1050
                                                              1965
               3
                       2.00
                                      1680
                                                   1680
                                                              1987
                                                                           8
21592
               3
                       2.50
                                      1530
                                                   1530
                                                              2009
                                                                           8
21593
                       2.50
                                      2310
                                                              2014
                                                                           8
                                                   2310
21594
                       0.75
               2
                                      1020
                                                   1020
                                                              2009
                                                                           7
21595
               3
                        2.50
                                                                           8
                                      1600
                                                   1600
                                                              2004
21596
                                                              2008
                                                                           7
               2
                        0.75
                                      1020
                                                   1020
                waterfront 1
                               condition1
       view 1
0
```

1	Θ	1	2
2	0	1	2
3	0	1	4
4	0	1	2
21592	0	1	2
21593	0	1	2
21594	0	1	2
21595	0	1	2
21596	0	1	2
[21143	rows x 9 c	olumns]	

In this model we have standardized the X variables (features) to have a mean of 0 and a standard deviation of 1 is known as standardization or z-score normalization. Scaling the features to have a standard deviation of 1 ensures that the features have the same variance, which can be important for modelling algorithms. Standardizing the features can help make the data closer to a normal distribution, which can improve the model's performance for such models.

```
ss = StandardScaler()
X1_scaled = ss.fit_transform(X_sec)
```

splitting data into train and test

```
split(X1_scaled, y_sec)
```

Building multiple linear model

```
model = sm.OLS(y train, sm.add constant(X train))
results = model.\overline{fit}()
results.summary()
<class 'statsmodels.iolib.summary.Summary'>
                             OLS Regression Results
Dep. Variable:
                                          R-squared:
                                 price
0.650
Model:
                                    0LS
                                          Adj. R-squared:
0.649
Method:
                         Least Squares F-statistic:
3481.
Date:
                      Thu, 26 Oct 2023 Prob (F-statistic):
0.00
Time:
                              01:45:16
                                          Log-Likelihood:
2.3188e+05
```

		10	014	4.7.0			
No. Observ 4.638e+05	ations:	169	914	AIC:			
Df Residua	ıls:	169	904	BIC:			
4.639e+05							
Df Model:			9				
Covariance	e Type:	nonrob	ust				
	coef	std err		t	P> t	[0.025	
0.975]							
const	5.393e+05	1673.474	322	. 268	0.000	5.36e+05	
5.43e+05				400			
x1 3.06e+04	-3.469e+04	2111.891	-16	. 428	0.000	-3.88e+04	-
x2	4.268e+04	2889.968	14	. 767	0.000	3.7e+04	
4.83e+04	112000101	20031300		., 0,	0.000	3170.01	
x3	1.476e+05	4505.256	32	. 765	0.000	1.39e+05	
1.56e+05	46E2 E416	2026 021	1	216	0.224	2045 050	
x4 1.22e+04	4653.5416	3826.021	Ι.	.216	0.224	-2845.858	
x5	-1.049e+05	2221.989	-47	. 216	0.000	-1.09e+05	-
1.01e+05							
x6	1.491e+05	2882.270	51.	.727	0.000	1.43e+05	
1.55e+05 x7	3.188e+04	1950.901	16	. 339	0.000	2.81e+04	
3.57e+04	311000101	1330.301	10	. 555	0.000	21010101	
x8	-5.399e+04	1872.819	-28	. 826	0.000	-5.77e+04	-
5.03e+04	1 120.04	1012 024	6	221	0.000	7742 202	
x9 1.48e+04	1.13e+04	1812.824	0.	. 231	0.000	7742.283	
=======					=======		===
		12604	CO7	Daniel I.	\		
Omnibus: 2.006		12604.	697	Durbin	-Watson:		
Prob(Omnib	ous):	0.0	000	Jarque	-Bera (JB)	:	
826533.213					,		
Skew:		2.9	997	Prob(J	B):		
0.00 Kurtosis:		36.718		Cond. No.			
6.64		50.	710	cona.	110.		
=======					=======		
======							
Notes:							
	ard Errors ass	sume that the	e cova	ariance	matrix of	the errors	is

```
correctly specified.
```

Our model is good overall with an R-squared value of 65% meaning it explains 65 % ov variance in our target variable. The p-values of our independent variables are below 0.05 meaning our model is statistically significant overall.

```
X_test = sm.add_constant(X_test)
y_pred = results.predict(X_test)

calculate_regression_metrics(y_test, y_pred)

{'MAE': 141592.73032447265,
   'MSE': 46826238256.493065,
   'R-squared': 0.6583531730583653}
```

## Comparing the train and test model of our multiple linear model

The R-squared of our train model is 65% and that of our test model is also 65%. This is can be an indication that our model is performing consistently between the training and test datasets. This can be a positive sign, suggesting that our model has not overfit the training data. This is a good model because the test model has not predicted more than what the train model predicted

metrics

# 3. Polynomial Transformation of features

We will use polynomial transformation to see if our model will improve or not.

```
# Polynomial transforming
y_pol= data["price"]
X_pol = X_sec
X pol
       bedrooms
                  bathrooms
                               sqft living
                                             sqft above yr built
                                                                      Grade 1
/
0
                                                                             7
               3
                        1.00
                                       1180
                                                    1180
                                                               1955
                        2.25
                                       2570
                                                               1951
                                                                             7
                                                    2170
2
               2
                        1.00
                                        770
                                                     770
                                                               1933
                                                                             6
3
                        3.00
                                                                             7
                                       1960
                                                    1050
                                                               1965
                        2.00
                                       1680
                                                    1680
                                                               1987
                                                                             8
                        2.50
                                                               2009
21592
               3
                                       1530
                                                    1530
                                                                             8
```

21593		4	2.50	2310	2310	2014	8
21594		2	0.75	1020	1020	2009	7
21595		3	2.50	1600	1600	2004	8
21596		2	0.75	1020	1020	2008	7
0	view_1	waterf	ront_1	condition1			
0 1	0 0		1	2 2			
2	0		1	2			
3	0		1	4			
4	0		1	2			
21502							
21592 21593	0		1	2 2			
21593	0 0		1	2			
21595	0		1	2			
21596	0		1	2 2			
[21143	rows x	9 colum	ns]				

He we also standardized our data to have a mean of 0 and standard deviation of 1

```
ss = StandardScaler()
X1_scaled = ss.fit_transform(X_pol)
```

splitting the data

```
split(X1_scaled, y_sec)
```

Building the polynomial model

```
def build_polynomial_linear_model(X, y, degree=2):
    # Create polynomial features
    poly = PolynomialFeatures(degree=degree, include_bias=False)
    X_poly = poly.fit_transform(X)

# Add a constant term (intercept)
    X_poly = (X_poly)

# Build and fit a linear regression model using statsmodels
    model = sm.OLS(y, X_poly).fit()
    return model
```

```
# Build the polynomial linear model
model = build_polynomial_linear_model(X_train, y_train, degree=2)
# Print the summary of the model
model.summary()
<class 'statsmodels.iolib.summary.Summary'>
                            OLS Regression Results
_____
Dep. Variable:
                                price
                                        R-squared:
0.719
                                  0LS
Model:
                                        Adj. R-squared:
0.719
Method:
                        Least Squares F-statistic:
815.8
Date:
                     Thu, 26 Oct 2023 Prob (F-statistic):
0.00
Time:
                             01:46:05 Log-Likelihood:
2.3000e+05
No. Observations:
                                16914
                                        AIC:
4.601e+05
Df Residuals:
                                16860
                                        BIC:
4.605e+05
Df Model:
                                   53
Covariance Type:
                            nonrobust
                 coef std err
                                                 P>|t|
                                                             [0.025]
0.9751
           -1.334e+04
                        2241.953
                                     -5.952
                                                 0.000
                                                          -1.77e+04
x1
8949.858
            2.851e+04
                        2972.717
                                      9.591
                                                 0.000
                                                          2.27e+04
x2
3.43e+04
                        5967.287
                                     24,434
            1.458e+05
                                                 0.000
                                                           1.34e + 05
x3
1.57e+05
           -3.598e+04
                        4920.108
                                     -7.312
                                                 0.000
                                                          -4.56e+04
x4
2.63e+04
x5
           -7.013e+04
                        2713.742
                                    -25.844
                                                 0.000
                                                          -7.55e+04
```

6.48e+04 x6
x7       1.559e+04       5007.623       3.114       0.002       5778.958         2.54e+04       x8       5.948e+06       4.21e+04       141.228       0.000       5.87e+06         6.03e+06       x9       1.931e+04       2446.360       7.894       0.000       1.45e+04         2.41e+04       x10       638.3932       252.167       2.532       0.011       144.119         1132.668       x11       3431.9165       2932.150       1.170       0.242       -2315.405         9179.238       x12       -8264.1989       4494.629       -1.839       0.066       -1.71e+04         545.744       x13       6834.6904       4042.086       1.691       0.091       -1088.221         1.48e+04       x14       -3094.1989       2344.446       -1.320       0.187       -7689.558         1501.161       x15       -3005.7492       3100.612       -0.969       0.332       -9083.274         3071.775       x16       702.2192       2066.712       0.340       0.734       -3348.753         4753.192       x17       -2103.9682       1962.403       -1.072       0.284       -5950.483         1742.547       x18       -9.0281       2066.704
2.54e+04 x8
6.03e+06       x9       1.931e+04       2446.360       7.894       0.000       1.45e+04         2.41e+04       x10       638.3932       252.167       2.532       0.011       144.119         1132.668       x11       3431.9165       2932.150       1.170       0.242       -2315.405         9179.238       x12       -8264.1989       4494.629       -1.839       0.066       -1.71e+04         545.744       x13       6834.6904       4042.086       1.691       0.091       -1088.221         1.48e+04       x14       -3094.1989       2344.446       -1.320       0.187       -7689.558         1501.161       x15       -3005.7492       3100.612       -0.969       0.332       -9083.274         3071.775       702.2192       2066.712       0.340       0.734       -3348.753         4753.192       x17       -2103.9682       1962.403       -1.072       0.284       -5950.483         1742.547       x18       -9.0281       2066.704       -0.004       0.997       -4059.984         4041.928       x19       -6142.8575       2645.867       -2.322       0.020       -1.13e+04         -956.682       x20       7820.0516       5934.09
2.41e+04
1132.668 x11 3431.9165 2932.150 1.170 0.242 -2315.405 9179.238 x12 -8264.1989 4494.629 -1.839 0.066 -1.71e+04 545.744 x13 6834.6904 4042.086 1.691 0.091 -1088.221 1.48e+04 x14 -3094.1989 2344.446 -1.320 0.187 -7689.558 1501.161 x15 -3005.7492 3100.612 -0.969 0.332 -9083.274 3071.775 x16 702.2192 2066.712 0.340 0.734 -3348.753 4753.192 x17 -2103.9682 1962.403 -1.072 0.284 -5950.483 1742.547 x18 -9.0281 2066.704 -0.004 0.997 -4059.984 4041.928 x19 -6142.8575 2645.867 -2.322 0.020 -1.13e+04 -956.682 x20 7820.0516 5934.096 1.318 0.188 -3811.398 1.95e+04 x21 3564.2530 5237.666 0.681 0.496 -6702.122 1.38e+04 x22 1.037e+04 3258.857 3.181 0.001 3979.567 1.68e+04 x23 1.484e+04 4213.910 3.521 0.000 6579.119 2.31e+04 x24 -591.2297 2533.067 -0.233 0.815 -5556.306
9179.238 x12
545.744  x13
1.48e+04 x14
1501.161 x15
x15
x16       702.2192       2066.712       0.340       0.734       -3348.753         4753.192       x17       -2103.9682       1962.403       -1.072       0.284       -5950.483         1742.547       x18       -9.0281       2066.704       -0.004       0.997       -4059.984         4041.928       x19       -6142.8575       2645.867       -2.322       0.020       -1.13e+04         -956.682       x20       7820.0516       5934.096       1.318       0.188       -3811.398         1.95e+04       x21       3564.2530       5237.666       0.681       0.496       -6702.122         1.38e+04       x22       1.037e+04       3258.857       3.181       0.001       3979.567         1.68e+04       x23       1.484e+04       4213.910       3.521       0.000       6579.119         2.31e+04       x24       -591.2297       2533.067       -0.233       0.815       -5556.306         4373.847
x17       -2103.9682       1962.403       -1.072       0.284       -5950.483         1742.547         x18       -9.0281       2066.704       -0.004       0.997       -4059.984         4041.928         x19       -6142.8575       2645.867       -2.322       0.020       -1.13e+04         -956.682       x20       7820.0516       5934.096       1.318       0.188       -3811.398         1.95e+04       x21       3564.2530       5237.666       0.681       0.496       -6702.122         1.38e+04       x22       1.037e+04       3258.857       3.181       0.001       3979.567         1.68e+04       x23       1.484e+04       4213.910       3.521       0.000       6579.119         2.31e+04       x24       -591.2297       2533.067       -0.233       0.815       -5556.306         4373.847
x18
x19
x20       7820.0516       5934.096       1.318       0.188       -3811.398         1.95e+04       x21       3564.2530       5237.666       0.681       0.496       -6702.122         1.38e+04       x22       1.037e+04       3258.857       3.181       0.001       3979.567         1.68e+04       x23       1.484e+04       4213.910       3.521       0.000       6579.119         2.31e+04       x24       -591.2297       2533.067       -0.233       0.815       -5556.306         4373.847
x21
x22 1.037e+04 3258.857 3.181 0.001 3979.567 1.68e+04 x23 1.484e+04 4213.910 3.521 0.000 6579.119 2.31e+04 x24 -591.2297 2533.067 -0.233 0.815 -5556.306 4373.847
x23 1.484e+04 4213.910 3.521 0.000 6579.119 2.31e+04 x24 -591.2297 2533.067 -0.233 0.815 -5556.306 4373.847
x24 -591.2297 2533.067 -0.233 0.815 -5556.306 4373.847
x25 -9710.6946 2166.193 -4.483 0.000 -1.4e+04 -
5464.729 x26 -90.7363 2778.952 -0.033 0.974 -5537.773
5356.300 x27 -6.847e+04 6956.386 -9.843 0.000 -8.21e+04 -
5.48e+04 x28 1.324e+05 1.29e+04 10.263 0.000 1.07e+05
1.58e+05 x29 -3.224e+04 5390.309 -5.980 0.000 -4.28e+04 -
2.17e+04

x30 7.78e+04	6.559e+04	6218.224	10.548	0.000	5.34e+04	
x31	-9808.4678	3381.602	-2.901	0.004	-1.64e+04	-
3180.173 x32	-1.649e+04	2407.166	-6.848	0.000	-2.12e+04	-
1.18e+04 x33	1.2e+04	4252.296	2.821	0.005	3660.688	
2.03e+04 x34	-6.102e+04	7239.149	-8.430	0.000	-7.52e+04	-
4.68e+04 x35	988.7095	5056.387	0.196	0.845	-8922.338	
1.09e+04 x36	-3.029e+04	5403.455	-5.606	0.000	-4.09e+04	-
1.97e+04 x37	-1.112e+04	3094.758	-3.592	0.000	-1.72e+04	-
5051.385 x38	-9445.1735	2477.159	-3.813	0.000	-1.43e+04	-
4589.683 x39	-1072.1197	3816.331	-0.281	0.779	-8552.529	
6408.289 x40	2.318e+04	1993.588	11.628	0.000	1.93e+04	
2.71e+04 x41	-2.043e+04	3294.082	-6.202	0.000	-2.69e+04	
-1.4e+04 x42	3191.8380	2163.355	1.475	0.140	-1048.563	
7432.239 x43	-7074.8195	2437.320	-2.903	0.140	-1.19e+04	
2297.417						-
×44 -402.971	-4555.7862	2118.670	-2.150	0.032	-8708.602	
x45 1.08e+04	5550.3683	2700.825	2.055	0.040	256.469	
x46 2.13e+04	1.62e+04	2608.060	6.212	0.000	1.11e+04	
x47 1.81e+04	1.406e+04	2078.162	6.766	0.000	9986.589	
x48 1.35e+04	7713.3382	2966.867	2.600	0.009	1897.967	
x49 7023.857	4060.2728	1511.952	2.685	0.007	1096.688	
x50 8643.404	4985.3976	1866.230	2.671	0.008	1327.391	
x51 7499.476	4054.5667	1757.513	2.307	0.021	609.657	
x52 5.03e+05	4.965e+05	3524.436	140.886	0.000	4.9e+05	
x53	859.3544	1587.879	0.541	0.588	-2253.055	
3971.764 x54	-889.9978	1311.948	-0.678	0.498	-3461.554	

```
1681.559
=======
Omnibus:
                              7713.330
                                          Durbin-Watson:
1.997
Prob(Omnibus):
                                 0.000
                                          Jarque-Bera (JB):
171655.002
Skew:
                                 1.678
                                          Prob(JB):
0.00
Kurtosis:
                                18.242
                                          Cond. No.
369.
Notes:
[1] Standard Errors assume that the covariance matrix of the errors is
correctly specified.
```

# Interpreting the polynomial results

Our model is good overall with an R-squared value of 71% meaning it explains 71 % ov variance in our target variable. The p-values of our independent variables are below 0.05 meaning our model is statistically significant overall.

coefficients and p\_values

```
model.params[:5]
x1
      -1.334432e+04
       2.851020e+04
x2
x3
       1.458025e+05
x4
      -3.597659e+04
x5
      -7.013461e+04
x6
       1.373397e+05
x7
       1.559442e+04
8x
       5.947704e+06
x9
       1.931195e+04
x10
       6.383932e+02
x11
       3.431917e+03
x12
      -8.264199e+03
x13
       6.834690e+03
x14
      -3.094199e+03
x15
      -3.005749e+03
       7.022192e+02
x16
x17
      -2.103968e+03
x18
      -9.028054e+00
x19
      -6.142858e+03
x20
       7.820052e+03
```

```
x21
       3.564253e+03
x22
       1.036727e+04
x23
       1.483882e+04
x24
      -5.912297e+02
x25
      -9.710695e+03
x26
      -9.073632e+01
x27
      -6.847166e+04
x28
       1.324299e+05
x29
      -3.223643e+04
x30
       6.558897e+04
x31
      -9.808468e+03
x32
      -1.648529e+04
x33
       1.199563e+04
x34
      -6.102379e+04
x35
       9.887095e+02
x36
      -3.029283e+04
x37
      -1.111744e+04
x38
      -9.445173e+03
x39
      -1.072120e+03
x40
       2.318242e+04
x41
      -2.042966e+04
x42
       3.191838e+03
x43
      -7.074819e+03
x44
      -4.555786e+03
       5.550368e+03
x45
x46
       1.620088e+04
x47
       1.406000e+04
x48
       7.713338e+03
       4.060273e+03
x49
x50
       4.985398e+03
x51
       4.054567e+03
x52
       4.965438e+05
       8.593544e+02
x53
x54
      -8.899978e+02
dtype: float64
model.pvalues[:5]
x1
        2.699746e-09
        9.948197e-22
x2
x3
       1.335751e-129
        2.746822e-13
x4
x5
       1.813546e-144
        0.000000e+00
x6
x7
        1.847929e-03
8x
        0.000000e+00
x9
        3.101291e-15
        1.136250e-02
x10
        2.418390e-01
x11
x12
        6.597936e-02
```

```
x13
        9.087783e-02
x14
        1.869198e-01
x15
        3.323570e-01
x16
        7.340295e-01
x17
        2.836730e-01
        9.965146e-01
x18
x19
        2.026199e-02
x20
        1.875829e-01
x21
        4.961947e-01
x22
        1.469021e-03
x23
        4.304233e-04
x24
        8.154500e-01
x25
        7.414201e-06
        9.739531e-01
x26
x27
        8.466214e-23
x28
        1.224674e-24
x29
        2.270258e-09
x30
        6.258948e-26
x31
        3.730033e-03
x32
        7.724659e-12
x33
        4.793341e-03
x34
        3.742282e-17
x35
        8.449751e-01
x36
        2.100622e-08
x37
        3.286498e-04
x38
        1.378315e-04
x39
        7.787680e-01
x40
        3.882083e-31
x41
        5.707568e-10
x42
        1.401206e-01
x43
        3.704348e-03
x44
        3.154532e-02
        3.988816e-02
x45
        5.359265e-10
x46
        1.371273e-11
x47
x48
        9.335244e-03
x49
        7.250297e-03
x50
        7.561412e-03
x51
        2.106737e-02
x52
        0.000000e+00
x53
        5.883794e-01
        4.975410e-01
x54
dtype: float64
```

#### **Prediction metrics**

```
X_test = sm.add_constant(X_test)
y_pred = results.predict(X_test)
```

```
calculate_regression_metrics(y_test, y_pred)
{'MAE': 141592.73032447265,
  'MSE': 46826238256.493065,
  'R-squared': 0.6583531730583653}
```

# Comparing the polynomial train and test model

On looking on the metrics of the two models we can say that our training data did well in training the model. We can see that the training model has a R-squared value of 65 while our training model has a R-squared of 71%. This shows our test model predicts well since it did not exceed the training model value and it also means that we did not overfit our data.