

### Factor Común

- a)  $3(a+z) - 77(a+z) - 8axy(a+z) = -74(a+z) - 8axy(a+z) = -2(a+z) \cdot (7+4ax)$
- b)  $48m^4n^3x + 72m^2n^3x^2 - 36m^2y^3 = 12m^2x(4n^3x + 6n^3x^2 - 3y^3)$
- c)  $25x^7 - 70x^5 + 75x^3 - 5x^2 = 5x^2(5x^5 - 2x^3 + 3x - 1)$
- d)  $(x+1)(x+2) + 5y(x-2) = (x-2)(x+1+5y)$

### Factorización por agrupación

- a)  $ax + bx + ay + by = x(a+b) + y(a+b) = (a+b)(x+y)$
- b)  $2x^2 - 3xy - 4x + 6y = x(2x - 3y) - 2(2x - 3y) = (2x - 3y)(x - 2)$
- c)  $a^2x - ax^2 - 2ay + 2axy + y^2 - 2x^2y = x(a^2 - ax + x^2) - 2y(a^2 - ax + x^2) = (a^2 - ax + x^2)(x - 2y)$
- d)  $a^2 + ab + ax + bx = a(a+b) + x(a+b) = (a+b)(a+x)$

### Trinomio Cuadrado Perfecto

- a)  $9 - 6x + x^2 = \sqrt{9} \sqrt{x^2} = 2x - 3 = \boxed{6x} = (x-3)^2$
- b)  $16 + 40x^2 + 25x^4$   
 $\sqrt{16} = 4$ ,  $\sqrt{25x^4} = 5x^2$   
 $2 \cdot 4 \cdot 5x^2 = 40x^2$   
 $\boxed{40x^2} = (4 + 5x^2)^2$
- c)  $4x^2 - 12xy + 9y^2$   
 $\sqrt{4x^2} = 2x$ ,  $\sqrt{9y^2} = 3y$   
 $2 \cdot 2x \cdot 3y = 12xy$   
 $\boxed{-12xy} = (2x - 3y)^2$
- d)  $\frac{1}{25} + \frac{23x^4}{36} - \frac{x^2}{3}$   
 $\sqrt{\frac{1}{25}} = \frac{1}{5}$ ,  $\sqrt{\frac{x^2}{3}} = \frac{\sqrt{3}x}{3}$   
 $2 \cdot \frac{1}{5} \cdot \frac{\sqrt{3}x}{3} = \frac{2\sqrt{3}x}{15}$
- e)  $16 - 704x^2 + 169x^4$   
 $\sqrt{16} = 4$ ,  $\sqrt{169x^4} = 13x^2$   
 $2 \cdot 4 \cdot 13x^2 = 104x^2$   
 $\boxed{-104x^2} = (4 - 13x^2)^2$

### Trinomio de la forma: $x^2 + bx + c$

- a)  $x^2 - 13x + 42 = (x-6)(x-7)$  b)  $x^2 + 8x + 15 = (x+3)(x+5)$
- c)  $x^2 - 12x - 64 = (x+4)(x-16)$  d)  $x^2 + 4x + 32 = (x+8)(x-4)$
- e)  $x^2 - 7x - 60 = (x-5)(x+12)$  f)  $x^2 - 79x + 48 = (x-3)(x-16)$

Trinomio de la forma  $ax^2+bx+c$

$$a) 7x^2 - 44x - 35 = 7x^2 + 5x - 49x - 35 = x(7x+5) - 7(7x+5) = (7x+5)(x-7)$$

$$b) 4a^2 + 15a + 9 = 4a^2 + 12a + 3a + 9 = 4a(a+3) + 3(a+3) = (a+3)(4a+3)$$

$$c) 76m + 15m^2 - 75 = 75m^2 + 16m - 75 = 75m^2 + 25m - 9m - 75 = 5m(3m+5) - 3(3m+5) = (3m+5)(5m-3)$$

$$d) ~~m~~ m - 6 + 15m^2 - 75m^2 + m - 6 = 75m^2 + 10m - 9m - 6 = 5m(3m+2) - 3(3m+2) = (3m+2)(5m-3)$$

Diferencia de cuadrados perfectos

$$a) 4a^2 - 9 = (2a-3)(2a+3)$$

$$d) 100 - x^2y^6 = (10 - xy^3)(10 + xy^3)$$

$$b) \frac{1}{16} - \frac{4x^2}{49}$$

$$e) 25 - 36x^4 = (5 - 6x^2)(5 + 6x^2)$$

$$c) 100m^2n^4 - 169y^6 = (10mn^2 - 13y^3)(10mn^2 + 13y^3)$$

Diferencia de cubos

$$a) a^3 - 8 = (a-2)(a^2+2a+4)$$

$$b) 8x^3 - 27 = (2x-3)(4x^2+6x+9)$$

$$c) -64n^6 + 1 = (1-2n)(1+2n+4n^2)(1+2n)(1-2n+4n^2)$$

$$d) 276q^3 - \frac{1}{276q^3} =$$

$$e) a^3 - b^3 = (a-b^3)(a^2+ab^3+b^6)$$

Suma de cubos

$$a) x^3 + 1 = (x+1)(x^2-x+1)$$

$$b) 27x^3 + b^6 = (3x+b^2)(9x^2-3b^2x+b^4)$$

$$c) 27m^6 + 64n^9 = (3m^2+4n^3)(9m^4-12m^2n^3+16n^6)$$

$$d) 27 + 343m^{12} = (3+7m^4)(9-27m^4+49m^8)$$