- This lab will cover recursion.
- It is assumed that you have reviewed chapters 4 of the textbook. You may want to refer to the text and your lecture notes during lab as you solve the problems.
- When approaching the problems, <u>think before you code</u>. Doing so is good practice and can help you lay out possible solutions.
- Think of any possible test cases that can potentially cause your solution to fail!
- You must stay for the duration of the lab. If you finish early, you may help other students. If you don't finish by the end of the lab, we recommend you complete it on your own time.
- Your TAs are available to answer questions in lab, during office hours, and on Piazza.

Vitamins (maximum 30 minutes)

- 1. For each of the following code snippets:
 - a. Given the following inputs, trace the execution of each code snippet. Write down all outputs in order and what the functions returns.
 - b. Analyze the running time of each. For each snippet:
 - i. Draw the recursion tree that represents the execution process of the function, and the cost of each call
 - ii. Conclude the total (asymptotic) run-time of the function.

```
#n = 16
a.
     def func1(n):
          if (n \le 1):
               return 0
          else:
               return 10 + func1(n-2)
b.
                         #n = 16
     def func2(n):
          if (n \le 1):
               return 1
          else:
               return 1 + func2(n//2)
\#1st = [1, 2, 3, 4, 5, 6, 7, 8]
c. def func3(lst):
          if (len(lst) == 1):
               return lst[0]
          else:
               return lst[0] + func3(lst[1:])
```

Coding

In this section, it is strongly recommended that you solve the problem on paper before writing code.

1. Write a **recursive** function that returns the **sum** of all numbers from 0 to n.

```
def sum_to(n):
    """
    : n type: int
    : return type: int
"""
```

- 2. Write a **recursive** function that returns the product of all even numbers from 0 to n.
 - ex) if $n = 8 \rightarrow 2 * 4 * 6 * 8 = 384$, so the function returns 384.

```
def product_evens(n):
    """
    : n type: int
    : return type: int
    """
```

- 3. Write a **recursive** function to find the maximum element in a non-empty, **non-sorted** list of numbers. The function parameters, low and high, are int values that are used to determine the range of indices to consider. <u>Aim for a linear run-time</u>.
 - ex) if the input list is [13, 9, 16, 3, 4, 2], the function should return 16.

```
def find_max(lst, low, high):
    """
    : lst type: list[int]
    : low, high type: int
    : return type: int
    """
```

4. In lab 3, you wrote an iterative implementation that determines whether a string is a palindrome (characters are read the same backward and forward). This time, you will do this **recursively**. The function parameters, low and high, are int values that are used to determine the range of indices to consider. Aim for a linear run-time.

```
ex) is_palindrome("racecar", 0, 6) returns True #racecar
is_palindrome("racecar", 1, 5) returns True #aceca
is_palindrome("racecar", 1, 3) returns False #ace

def is_palindrome(input_str, low, high):
    """
    : input_str type: str
    : low, high type: int
    : return type: bool
    """
```

5. Give a **recursive** implementation for the binary search algorithm. The function is given a **sorted** list, lst, a value, val, to search for, and two indices, low and high, representing the lower and upper bounds to consider.

If the value is on the list (between low and high), return the index at which the value is located. If val is not found, the function should return None.

```
def binary_search(lst, val, low, high):
    """
    : lst type: list[int]
    : val type: int
    : low type, high type: int
    : return type: int (found), None
    """
```

6. Write a **recursive** function that takes in a list of integers and **mutates** it so that all even numbers are at the front and all odd numbers are in the back. You do not have to maintain the relative order; just focus on separating them. You are also given low and high, the range of indices to consider. <u>Aim for a linear run-time</u>.

7. Given a string of letters representing a word(s), write a **recursive** function that returns a **tuple** of 2 integers: the number of vowels, and the number of consonants in the word.

Remember that <u>tuples are not mutable</u> so you'll have to create a new one to return each time when you're updating the counts. Since we are always creating a tuple of 2 integers each time, the cost is constant.

```
ex) word = "NYUTandonEngineering"
vc_count(word, 0, len(word)-1) → (8, 12) # 8 vowels, 12 consonants

def vc_count(word, low, high):
    """
    : word type: str
    : low, high type: int
    : return type: tuple (int, int)
```

8. A nested list of integers is a list that stores integers in some hierarchy. The list can contain integers and other nested lists of integers. An example of a nested list of integers is [[1, 2], 3, [4, [5, 6, [7], 8]]]. To check the type of an object, use the isinstance function.

```
ex) lst = [1, 2, 3, 4]

if isinstance(lst, list): #returns True

if isinstance(lst, int): #returns False
```

Write a **recursive** function to find the total sum of a nested list of integers.

ex) If lst = [[1, 2], 3, [4, [5, 6, [7], 8]]], the function should return 36.

```
def nested_sum(lst):
    """
    : lst type: list
    : output type: int
    """
```