Homework #6 Due by Friday 4/19, 11:55pm

Submission instructions:

- 1. You should write 5 '.py' files: one for each question. Name your files: 'YourNetID_hw6_q1.py', 'YourNetID_hw6_q2.py', etc. Note: your netID follows an abc123 pattern, not N12345678.
- 2. In this assignment, we provided 'DoublyLinkedList.py' file (with the implementation of a doubly linked list).

In questions where you need to use <code>DoublyLinkedList</code>, make the definition in a separate file, and use an <code>import</code> <code>DoublyLinkedList</code> statement to import the <code>DoublyLinkedList</code> class.

You should use the linked lists as a black box. You are not allowed to put any changes in 'DoublyLinkedList.py'. Such a change is considered a break of an abstraction barrier.

- 3. You should submit your homework via Gradescope. For Gradescope's autograding feature to work:
 - a. Name all functions and methods exactly as they are in the assignment specifications.
 - b. Make sure there are no print statements in your code. If you have tester code, please put it in a "main" function and do not call it.
 - c. You don't need to submit the 'DoublyLinkedList.py' file

Question 1:

Define a LinkedQueue class that implements the Queue ADT.

Implementation Requirement: All queue operations should run in $\theta(1)$ worst-case.

<u>Hint</u>: You would want to use a doubly linked list as a data member.

Question 2:

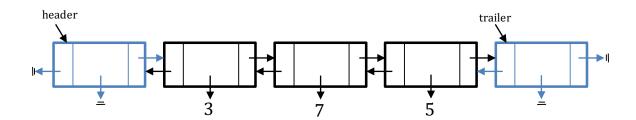
Many programming languages represent integers in a **fixed** number of bytes (a common size for an integer is 4 bytes). This, on one hand, bounds the range of integers that can be represented as an int data (in 4 bytes, only 2^{32} different values could be represented), but, on the other hand, it allows fast execution for basic arithmetic expressions (such as +, -, * and /) typically done in hardware.

Python and some other programming languages, do not follow that kind of representation for integers, and allows to represent arbitrary large integers as int variables (as a result the performance of basic arithmetic is slower).

In this question, we will suggest a data structure for positive integer numbers, that can be arbitrary large.

We will represent an integer value, as a linked list of its digits.

For example, the number 375 will be represented by a 3-length list, with 3, 7 and 5 as its elements.



<u>Note</u>: this is not the representation Python uses. Complete the definition of the following Integer class:

```
class Integer:
    def __init__(self, num_str):
        ''' Initializes an Integer object representing
        the value given in the string num_str'''

def __add__(self, other):
        ''' Creates and returns an Integer object that
        represent the sum of self and other, also of
        type Integer'''

def __repr__(self):
        ''' Creates and returns the string representation
        of self'''
```

For example, after implementing the Integer class, you should expect the following behavior:

```
>>> n1 = Integer('375')
>>> n2 = Integer('4029')
>>> n3 = n1 + n2
>>> n3
4404
```

<u>Note</u>: When adding two Integer objects, implement the "Elementary School" addition technique. DO NOT convert the Integer objects to ints, add these ints by using Python + operator, and then convert the result back to an Integer object. This approach misses the point of this question.

Extra Credit:

Support also the multiplication of two Integer objects (by implementing the "Elementary School" multiplication technique):

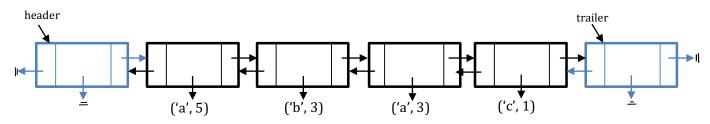
```
def __mul__(self, other):
    ''' Creates and returns an Integer object that
    represent the multiplication of self and other,
    also of type Integer'''
```

Question 3:

In this question, we will suggest a data structure for storing strings with a lot of repetitions of successive characters.

We will represent such strings as a linked list, where each maximal sequence of the same character in consecutive positions, will be stored as a single tuple containing the character and its count.

For example, the string "aaaaabbbaaac" will be represented as the following list:



Complete the definition of the following CompactString class:

```
class CompactString:
   def init (self, orig str):
       ''' Initializes a CompactString object
       representing the string given in orig str'''
   def add (self, other):
       '''' Creates and returns a CompactString object that
       represent the concatenation of self and other,
       also of type CompactString'''
   def lt (self, other):
        returns True if"f self is lexicographically
       less than other, also of type CompactString'''
   def le (self, other):
        ''' returns True if"f self is lexicographically
       less than or equal to other, also of type
       CompactString'''
   def gt (self, other):
       returns True if"f self is lexicographically
       greater than other, also of type CompactString'''
   def ge (self, other):
       ''' returns True if"f self is lexicographically
       greater than or equal to other, also of type
       CompactString'''
   def repr (self):
       ''' Creates and returns the string representation
        (of type str) of self'''
```

For example, after implementing the CompactString class, you should expect the following behavior:

```
>>> s1 = CompactString('aaaaabbbaaac')
>>> s2 = CompactString('aaaaaaacccaaaa')
>>> s3 = s2 + s1 #in s3's linked list there will be 6 'real' nodes
>>> s1 < s2
False</pre>
```

Note: Here too, when adding and comparing two CompactString objects, DO NOT convert the CompactString objects to strs, do the operation on strs (by using Python +, <, >, <=, >= operators), and then convert the result back to a CompactString object. This approach misses the point of this question.

Question 4:

In this question, we will demonstrate the difference between shallow and deep copy. For that, we will work with *nested doubly linked lists of integers*. That is, each element is an integer or a <code>DoublyLinkedList</code>, which in turn can contain integers or <code>DoublyLinkedLists</code>, and so on.

a. Implement the following function:

```
def copy linked list(lnk lst)
```

The function is given a nested doubly linked lists of integers lnk_lst, and returns a **shallow copy** of lnk_lst. That is, a new linked list where its elements reference the same items in lnk lst.

For example, after implementing <code>copy_linked_list</code>, you should expect the following behavior:

```
>>> lnk_lst1 = DoublyLinkedList()
>>> elem1 = DoublyLinkedList()
>>> elem1.add_last(1)
>>> elem1.add_last(2)
>>> lnk_lst1.add_last(elem1)
>>> elem2 = 3
>>> lnk_lst1.add_last(elem2)
>>> lnk_lst2 = copy_linked_list(lnk_lst1)
>>> e1 = lnk_lst1.first_node()
>>> e1_1 = e1.data.first_node()
>>> e1_1.data = 10
>>> e2 = lnk_lst2.first_node()
>>> print(e2_1.data)
10
```

b. Now, implement:

```
def deep copy linked list(lnk lst)
```

The function is given a nested doubly linked lists of integers lnk_lst, and returns a **deep copy** of lnk lst.

For example, after implementing deep_copy_linked_list, you should expect the following behavior:

```
>>> lnk_lst1 = DoublyLinkedList()
>>> elem1 = DoublyLinkedList()
>>> elem1.add_last(1)
>>> elem1.add_last(2)
>>> lnk_lst1.add_last(elem1)
>>> elem2 = 3
>>> lnk_lst1.add_last(elem2)

>>> lnk_lst2 = deep_copy_linked_list(lnk_lst1)
>>> e1 = lnk_lst1.first_node()
>>> e1_1 = e1.data.first_node()
>>> e1_1.data = 10

>>> e2 = lnk_lst2.first_node()
>>> e2_1 = e2.data.first_node()
>>> print(e2_1.data)
```

Note: lnk lst could have **multiple levels** of nesting.

Ouestion 5:

In this question, we will implement a function that merges two sorted linked lists:
def merge_linked_lists(srt_lnk_lst1, srt_lnk_lst2)

This function is given two doubly linked lists of integers srt_lnk_lst1 and srt_lnk_lst2. The elements in srt_lnk_lst1 and srt_lnk_lst2 are sorted. That is, they are ordered in the lists, in an ascending order.

When the function is called, it will **create and return a new** doubly linked list, that contains all the elements that appear in the input lists in a sorted order.

For example:

```
 if \ srt_lnk_lst1 = [1 <--> 3 <--> 5 <--> 6 <--> 8], \\ and \ srt_lnk_lst2 = [2 <--> 3 <--> 5 <--> 10 <--> 15 <--> 18], \\ calling: \ merge_linked_lists (srt_lnk_lst1, srt_lnk_lst2), should \\ create and return a doubly linked list that contains: \\ [1 <--> 2 <--> 3 <--> 3 <--> 5 <--> 6 <--> 8 <--> 10 <--> 15 <--> 18].
```

The merge_linked_lists function is not recursive, but it defines and calls merge sublists - a nested helper recursive function.

Complete the implementation given below for the merge_linked_lists function:

Notes:

- 1. You need to decide on the signature of merge sublists.
- 2. merge sublists has to be recursive.
- 3. An efficient implementation of merge_sublists would allow merge_linked_lists to run in **linear time**. That is, if n_1 and n_2 are the sizes of the input lists, the runtime would be $\theta(n_1 + n_2)$.