Q.P. Code: 15123

## First Semester B.C.A. Degree Examination, November/December 2019

(CBCS - (Freshers & Repeaters)

## **Computer Science**

# Paper 105 T - DISCRETE MATHEMATICS

Time: 3 Hours]

[Max. Marks: 100

Instructions to Candidates : Answer all Sections.

### SECTION - A

- I. Answer any **TEN** of the following. Each question carries **2** marks :  $(10 \times 2 = 20)$
- 1. If  $A = \{2, 3, 4, 5\}$  and  $B = \{0, 1, 2, 3\}$  find  $A \cap B$ .
- 2. If  $A = \{1, 2, 3\}$ ,  $B = \{3, 4, 5\}$  and  $C = \{0, 2, 3\}$ , find  $(A \cap B) \times C$ .
- 3. Define Tautology.
- 4. Define Scalar matrix with example.
- 5. If  $A = \begin{bmatrix} 3 & 2 \\ -1 & 4 \end{bmatrix}$  and  $B = \begin{bmatrix} 3 & 5 \\ -2 & 4 \end{bmatrix}$ , find 2A + 3B.
- 6. Find the characteristic roots of the matrix  $A = \begin{bmatrix} 1 & 2 \\ 3 & 2 \end{bmatrix}$ .
- 7. If  $\log_7^x + \log x_7^2 + \log x_7^3 = 6$ , find x.
- 8. Define permutation and combination.
- 9. Define an abelian group.
- 10. If  $\vec{a} = 2\hat{i} + 3\hat{j} 4\hat{k}$ ,  $\vec{b} = 3\vec{i} 4\vec{j} 5\hat{k}$ , find  $|\vec{a} + \vec{b}|$ .
- 11. Find the distance between the point A = (-7, 4) and B = (-5, -1).
- 12. Find the equation of the line whose y-intercept is -2 and slope is  $\frac{3}{2}$ .

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- II. Answer any SIX of the following. Each question carries 5 marks:  $(6 \times 5 = 30)$
- 13. If  $A = \{1, 4\}$ ,  $B = \{2, 3, 6\}$ ,  $C = \{2, 3, 7\}$  then verify that  $A \times (B C) = (A \times B) (A \times C)$ .
- 14. Show that the function  $f: Q \to Q$  defined by f(x) = 2x + 3 is both one-one and onto. Here Q is the set of all rational numbers.
- 15. Prove that  $p \lor (q \land r) \leftrightarrow [(p \lor q) \land (p \lor r)]$  is a Tautology.
- 16. Write the converse, inverse and contra-positive of the conditional. "If two integers are equal then their squares are equal".
- 17. Prove that  $(p \leftrightarrow q) \equiv (p \rightarrow q) \land (q \rightarrow p)$ .
- 18. Find the inverse of the matrix

$$A = \begin{bmatrix} 3 & -3 & 4 \\ 2 & -3 & 4 \\ 0 & -1 & 1 \end{bmatrix}$$

19. Using Cramer's rule solve:

$$5x - y - 4z = 5$$
,  $2x + 3y + 5z = 2$ ,  $7x - 2y + 6z = 5$ .

20. Verify the Cayley-Hamilton theorem for the matrix  $A = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$ .

#### SECTION - C

- III. Answer any SIX of the following. Each question carries 5 marks: (6 × 5 = 30)
- 21. If  $\log\left(\frac{a+b}{3}\right) = \frac{1}{2}(\log a + \log b)$ , show that  $a^2 + b^2 = 7ab$ .
- 22. How many three digit even numbers can be made using the digits 1, 2, 3, 4, 6, 7, if no digit is repeated?
- 23. If  $2nc_3 : nc_3 = 11:1$  find n.
- 24. Prove that the set  $G = \{1, -1, i, -i\}$  form an abelian group under multiplication.

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- 25. Show that  $H = \{0, 2, 4\}$  is subgroup of the group  $(G, +_6)$ , where  $G = \{0, 1, 2, 3, 4, 5\}$
- 26. If  $\vec{a} = 2\hat{i} 3\hat{j} + \hat{k}$ ,  $\vec{b} = \hat{i} + \hat{j} \hat{k}$ ,  $\vec{c} = 3\hat{i} \hat{j} + 2\hat{k}$ , verify that  $\vec{a} \cdot (\vec{b} + \vec{c}) = \vec{a} \cdot \vec{b} + \vec{a} \cdot \vec{c}$
- 27. Find the area of the triangle whose vertices are A(3, 2, 1), B(4, -1, 2) and C(-1, 3, 2) using vector method.
- 28. Find the value of 'm', if  $\vec{a} = m\hat{i} 3\hat{j} + 4\hat{k}$ ,  $\vec{b} = \hat{i} + 3\hat{j} + \hat{k}$  and  $\vec{c} = 2\hat{i} + \hat{j} + \hat{k}$  are co-planar.

#### SECTION - D

- IV. Answer any FOUR of the following. Each question carries 5 marks: (4 × 5 = 20)
- 29. Prove that the points (6, 4), (7, -2), (5, 1) and (4, 7) form the vertices of a parallelogram.
- 30. Find the ratio in which the points p(2,7) divides the line joining the points A(8,9) and B(-7,4).
- 31. Find the equation of the perpendicular bisector of the line joining the points A(3, -2) and B(4, 1).
- 32. Find the value of k such that the line (k-2)x + (k+3)y 5 = 0 is perpendicular to the line 2x y + 7 = 0.
- 33. If the acute angle between the lines 4x y + 7 = 0 and  $k_x 5y 9 = 0$  is  $45^{\circ}$ . Find the value of k.
- 34. Find the equation of the line passing through the point of intersection of the lines 2x + 3y 7 = 0 and 5x 6y + 8 = 0 and the point (4, 3).