

(a)

$$\frac{\langle e_1, E, S \rangle \Downarrow \langle v_1, S' \rangle \quad \langle e_2, E, S' \rangle \Downarrow \langle v_2, S'' \rangle}{\langle (\text{before } e_1 \ e_2), E, S \rangle \Downarrow \langle v_1, S'' \rangle} \text{ (Before)}$$

(b)

$$\frac{\langle e, E + \{x_1 \mapsto E(x_2)\}, S \rangle \Downarrow \langle v, S' \rangle}{\langle (\text{alias } x_1 \ x_2 \ e), E, S \rangle \Downarrow \langle v, S' \rangle} \text{ (Alias)}$$

(c) To save space and avoid repetition, we write:

$$\begin{array}{ll} E_x & \text{for } \{x \mapsto L_1\} \\ E_{xy} & \text{for } \{x \mapsto L_1, y \mapsto L_1\} \end{array}$$

Then the tree looks like this:

$$\frac{\frac{\frac{\langle 1, \emptyset, \emptyset \rangle \Downarrow \langle 1, \emptyset \rangle}{\langle 1, \emptyset, \emptyset \rangle \Downarrow \langle 1, \emptyset \rangle} \text{ (Int)} \quad \frac{\frac{\frac{\langle 3, E_{xy}, \{L_1 \mapsto 1\} \rangle \Downarrow \langle 3, \{L_1 \mapsto 1\} \rangle}{\langle 3, E_{xy}, \{L_1 \mapsto 1\} \rangle \Downarrow \langle 3, \{L_1 \mapsto 1\} \rangle} \text{ (Int)} \quad \frac{\frac{\langle 5, E_{xy}, \{L_1 \mapsto 3\} \rangle \Downarrow \langle 5, \{L_1 \mapsto 3\} \rangle}{\langle 5, E_{xy}, \{L_1 \mapsto 3\} \rangle \Downarrow \langle 5, \{L_1 \mapsto 3\} \rangle} \text{ (Int)} \quad \frac{\frac{\langle x, E_{xy}, \{L_1 \mapsto 3\} \rangle \Downarrow \langle 3, \{L_1 \mapsto 3\} \rangle}{\langle x, E_{xy}, \{L_1 \mapsto 3\} \rangle \Downarrow \langle 3, \{L_1 \mapsto 3\} \rangle} \text{ (Var)} \quad \frac{\langle 8, E_{xy}, \{L_1 \mapsto 3\} \rangle \Downarrow \langle 8, \{L_1 \mapsto 3\} \rangle}{\langle 8, E_{xy}, \{L_1 \mapsto 3\} \rangle \Downarrow \langle 8, \{L_1 \mapsto 3\} \rangle} \text{ (Assgn)} \quad \frac{\langle 11, E_{xy}, \{L_1 \mapsto 3\} \rangle \Downarrow \langle 11, \{L_1 \mapsto 3\} \rangle}{\langle 11, E_{xy}, \{L_1 \mapsto 3\} \rangle \Downarrow \langle 11, \{L_1 \mapsto 3\} \rangle} \text{ (Assgn)} \quad \frac{\langle 11, E_{xy}, \{L_1 \mapsto 3\} \rangle \Downarrow \langle 11, \{L_1 \mapsto 3\} \rangle}{\langle 11, E_{xy}, \{L_1 \mapsto 3\} \rangle \Downarrow \langle 11, \{L_1 \mapsto 3\} \rangle} \text{ (Before)} \quad \frac{\langle 11, E_{xy}, \{L_1 \mapsto 3\} \rangle \Downarrow \langle 11, \{L_1 \mapsto 3\} \rangle}{\langle 11, E_{xy}, \{L_1 \mapsto 3\} \rangle \Downarrow \langle 11, \{L_1 \mapsto 3\} \rangle} \text{ (Alias)} \quad \frac{\langle 11, E_{xy}, \{L_1 \mapsto 3\} \rangle \Downarrow \langle 11, \{L_1 \mapsto 3\} \rangle}{\langle 11, E_{xy}, \{L_1 \mapsto 3\} \rangle \Downarrow \langle 11, \{L_1 \mapsto 3\} \rangle} \text{ (Var)} \quad \frac{\langle 11, E_{xy}, \{L_1 \mapsto 3\} \rangle \Downarrow \langle 11, \{L_1 \mapsto 3\} \rangle}{\langle 11, E_{xy}, \{L_1 \mapsto 3\} \rangle \Downarrow \langle 11, \{L_1 \mapsto 3\} \rangle} \text{ (Add)} \quad \frac{\langle 11, E_{xy}, \{L_1 \mapsto 3\} \rangle \Downarrow \langle 11, \{L_1 \mapsto 3\} \rangle}{\langle 11, E_{xy}, \{L_1 \mapsto 3\} \rangle \Downarrow \langle 11, \{L_1 \mapsto 3\} \rangle} \text{ (Let)}$$