

- Van der Pol equation:

$$y'' = y'(1 - y^2) - y$$

Let $q_1 = y'$ and $q_2 = y$, then we have

$$\begin{cases} q'_1 = q_1(1 - q_2^2) - q_2 \\ q'_2 = q_1 \end{cases}$$

- Blasius equation:

$$y''' = -yy''$$

Let $q_1 = y''$ and $q_2 = y'$, $q_3 = y$, then we have

$$\begin{cases} q'_1 = -q_3q_1 \\ q'_2 = q_1 \\ q'_3 = q_2 \end{cases}$$

- Newton's Second Law of Motion for two-body problem:

$$\begin{cases} y''_1 = -GM y_1 (y_1^2 + y_2^2)^{3/2} \\ y''_2 = -GM y_2 (y_1^2 + y_2^2)^{3/2} \end{cases}$$

Let $q_1 = y'_1$ and $q_2 = y_1$, $q_3 = y'_2$, $q_4 = y_2$, then we have

$$\begin{cases} q'_1 = -GM q_2 / (q_2^2 + q_4^2)^{3/2} \\ q'_2 = q_1 \\ q'_3 = -GM q_4 / (q_2^2 + q_4^2)^{3/2} \\ q'_4 = q_2 \end{cases}$$