

# *Languages: Predictive parsing 2*

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# Learning outcomes

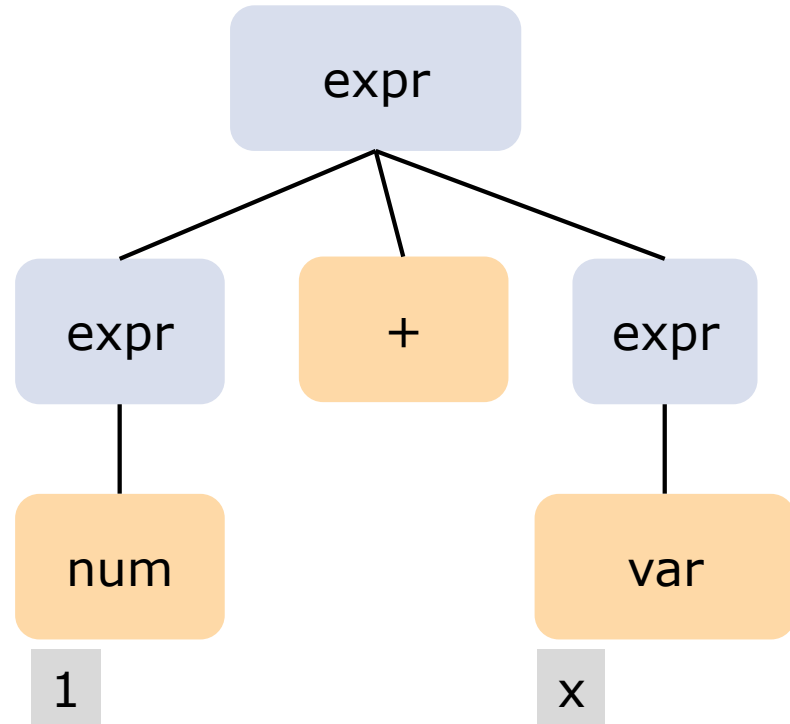
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After this lecture, you should be able to:

- ❑ derive parse trees from a BNF grammar
- ❑ define what it means for a grammar to be "ambiguous"
- ❑ use two additional rules for transforming a grammar

# Parse trees

`expr = num`  
| `var`  
| `expr + expr`



Rules:

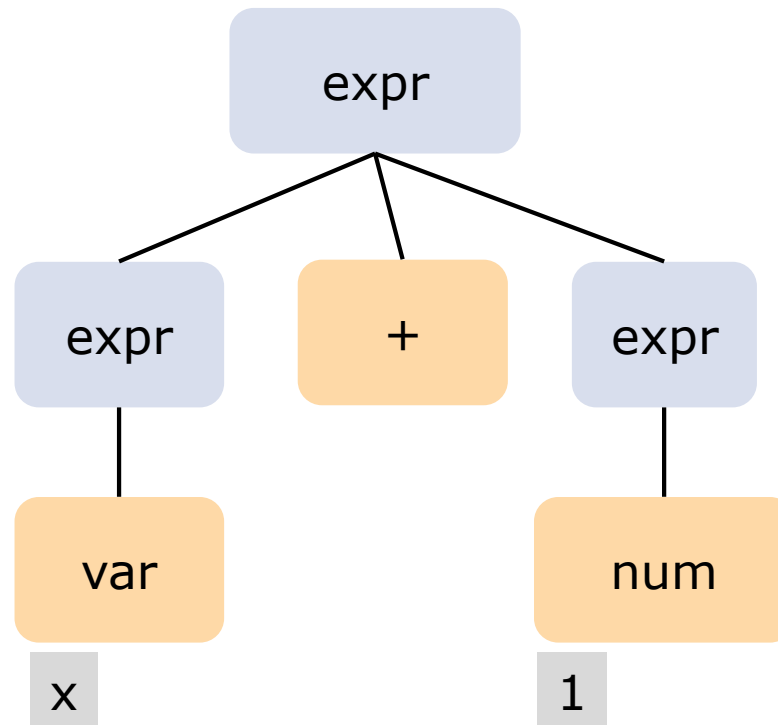
1. root is labeled with the start symbol
2. the symbols in one of its productions become child nodes
3. continue until all leaf nodes are terminal symbols

# Exercise

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```
expr = num  
      | var  
      | expr + expr
```

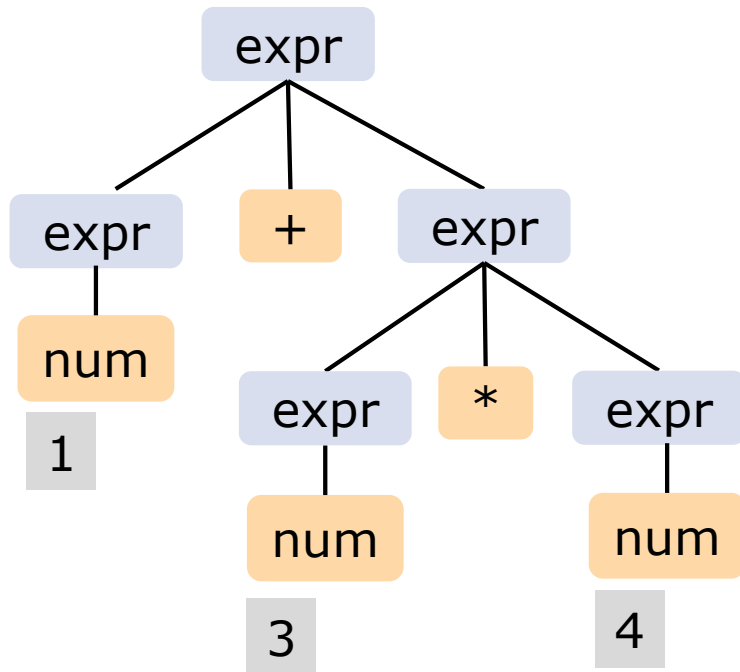
derive "x + 1" using a parse tree



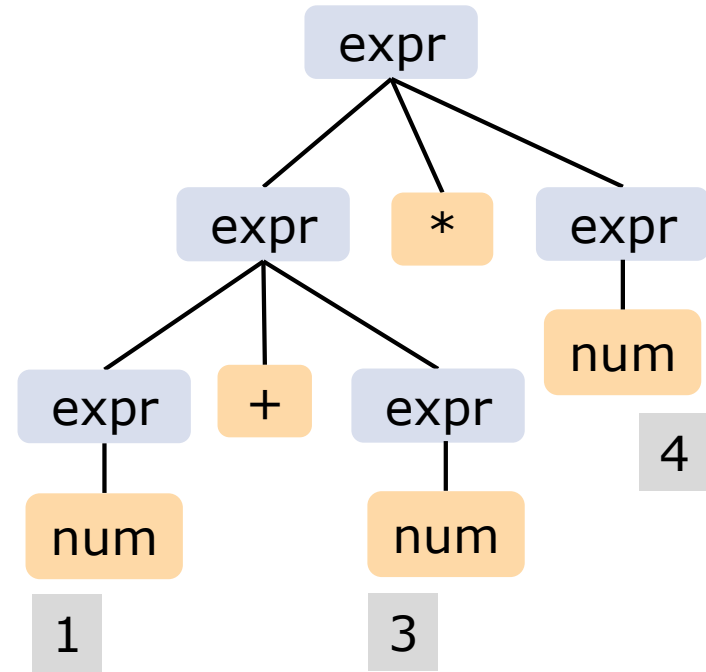
# Ambiguous grammar

$\text{expr} = \text{num} \mid \text{expr} + \text{expr} \mid \text{expr} * \text{expr}$

Create a parse tree for "1 + 3 \* 4"



$1 + (3 * 4)$



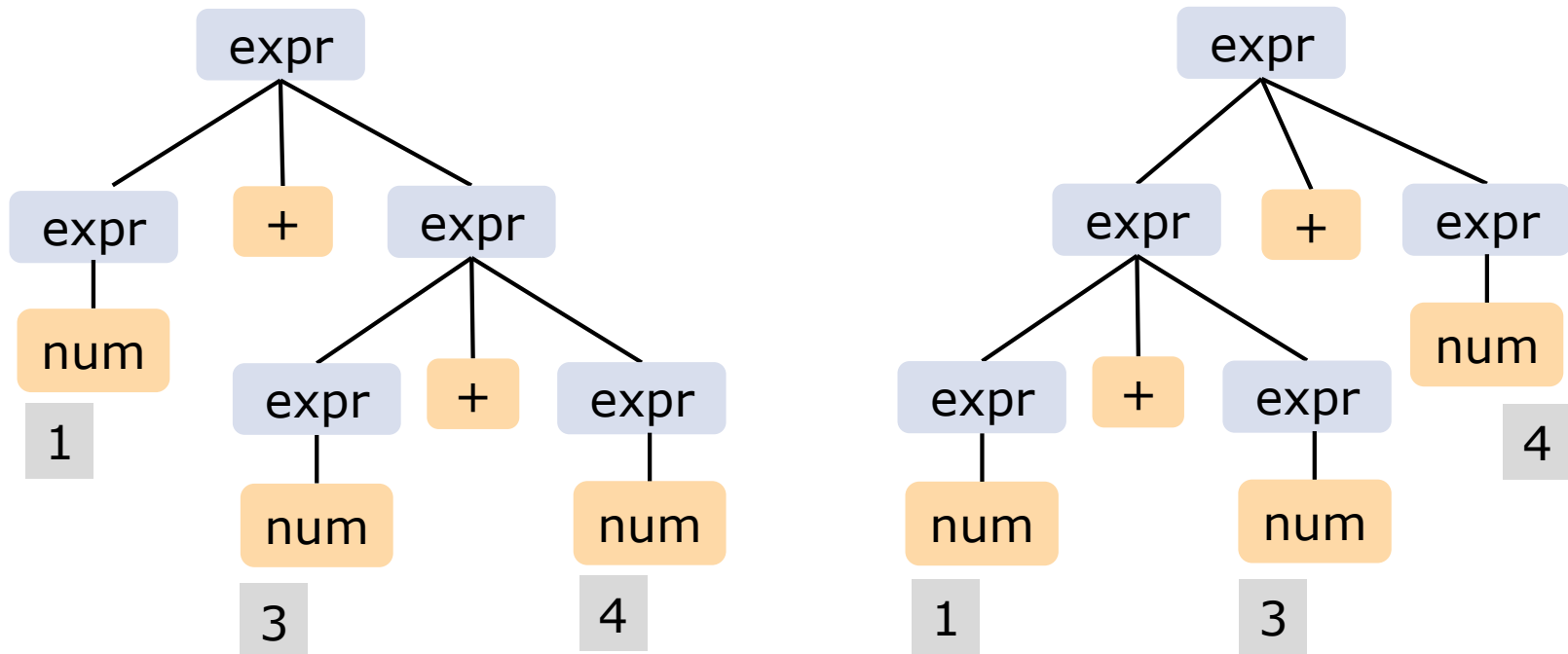
$(1 + 3) * 4$

# Ambiguous grammar

A grammar is **ambiguous** is, for some string that can be derived from the grammar, there is more than one parse tree.

Different parse trees usually suggest different meanings.

So: we usually want unambiguous grammars.



# Review: predictive parsing

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```
stmt ::= print ( expr )  
      | id = expr  
expr ::= id | num
```

```
void stmt() {  
  switch (lookahead) {  
    case PRINT:  
      match(PRINT); match("("); expr(); match(")");  
      break;  
    case ID:  
      match(ID); match("="); expr()  
      break;  
    default:  
      error("syntax error");  
  }  
}
```

# Transforming a BNF grammar

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In the last lecture we learned how to deal with:

- left recursion
- empty productions

Two more ways to transform BNF:

- left factoring
- expanding a non-terminal



# Left factoring

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Any problems with a predictive parser here?

$A ::= a B \mid a C \mid b D$

Can we transform the BNF?

$A ::= a E \mid b D$

$E ::= B \mid C$

# Exercise

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Suppose an expression can be a variable or function call.  
Examples:

`tot`                    (a variable)  
`max(y)`                (a function call)

BNF:

```
expr ::= var ( expr )      // a function call
       | var                // a variable
```

Exercise: Apply left factoring

a solution:

```
expr  ::= var expr1
expr1 ::= ( expr ) | ""
```

# Expanding a non-terminal

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Any problems with a predictive parser here?

$A ::= a B \mid E$

$E ::= c C \mid d D$

Can we transform the BNF into a better form?

$A ::= a B \mid c C \mid d D$

For predictive parsers, we want that, for every non-terminal in the grammar:

- ❑ there's only one production for it, or
- ❑ each production starts with a token (maybe "") and each of the tokens are different

# Exercise

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```
prog ::= stmt | stmt ; prog
stmt ::= ID = expr | ID ( expr )
```

Exercise: There are two problems. What are they?

Fix using left factoring and removing left recursion.

```
prog ::= stmt ; prog1
prog1 ::= "" | stmt ; prog1
stmt ::= ID stmt1
stmt1 ::= = expr | ( expr )
```

Exercise: Expand a non-terminal.

```
prog ::= ID stmt1 ; prog1
prog1 ::= "" | ID stmt1 ; prog1
stmt1 ::= = expr | ( expr )
```

Note: there's no longer a 'stmt' non-terminal

# Summary

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- A parse tree shows how a string can be derived from a BNF grammar
- To use predictive parsing, our BNF syntax must be in a certain form. Here are some tools to get BNF in that form:
  - eliminate left recursion
  - left-factoring
  - expanding non-terminals